

Calculated Line Strengths for the Transition Array ($3d^3 + 3d^2 4s$)– $3d^2 4p$ in Ti II

H. Mendlowitz

Department of Physics, Howard University*

and

Institute for Basic Standards, National Bureau of Standards, Washington, D.C. 20234

(August 27, 1968)

The transition array for the transitions between the configurations ($3d^3 + 3d^2 4s$) and $3d^2 4p$ in Ti II are presented here. The relative line strengths have been calculated in the intermediate coupling scheme, taking into account interaction between configurations. The relative phase and magnitude of the radial transition integrals ($s-p$) and ($d-p$) for the jumping electron in the LS coupling have been determined empirically.

Key Words: Calculated line strengths; configuration interaction; intermediate coupling; Ti II; $3d^3$, $3d^2 4s$, $3d^2 4p$ configurations; transition array.

The line strengths for transitions between levels A and B are defined as in Condon and Shortley [1] as

$$S(A, B) = \sum_{a, b} |(a | \mathbf{P} | b)|^2, \quad (1)$$

where the sum is over all the states which are the sublevels of the levels A and B . In this note, we first calculated the square roots of the relative strengths of the transitions between two given configurations in the LS representation and then transformed to the physical representation. It is assumed that the dipole approximation is valid. In this approximation the transition operator \mathbf{P} is given by

$$\mathbf{P} = - \sum_j e \mathbf{r}_j \quad (2)$$

where the sum is taken over all the electrons involved in the transition. The matrix elements for the transition can be readily calculated except for a radial integral factor common to all the matrix elements of the transition array [2, 3].

The radial integral depends upon the quantum numbers of the jumping electron in the upper and lower levels of the transition. In cases where the interaction between configurations is negligible, one

has only one radial integral to consider in the LS representation. Therefore, upon transforming to the intermediate coupling scheme, the relative transition strengths are easily obtained. However, in the case of Ti II, the interaction between the configurations is important, so one has to consider more than one radial integral for the jumping electron. In Ti II, transitions between the following configurations may be important:

$$(1) 3d^3 - 3d^2 4p,$$

$$(2) 3d^2 4s - 3d^2 4p.$$

The state $|a\rangle$ may then be expressed as a superposition of the eigenstates $|K\rangle$ of the various configurations. Thus,

$$|a\rangle = \sum_K |K\rangle (K|a), \quad (3)$$

where we have summed over the configurations K , and $(K|a)$ is the set of expansion coefficients. The matrix element of the transition between states a and b can be written as

$$(b | \mathbf{P} | a) = \sum_K \sum_{K'} (b | K') (K' | \mathbf{P} | K) (K | a), \quad (4)$$

where $(K' | \mathbf{P} | K)$ are the matrix elements of the transition operator \mathbf{P} expressed in the representation where the configurations K' and K are good quantum

*Supported in part by National Science Foundation and Physics Branch of Office of Naval Research.

numbers. In Ti II, this refers to the transition array in the LS representation for each configuration of the lower state separately. The matrix element for the transition can then be expressed as

$$(b|P|a) = \sum_{\alpha} (a|3d^24p, \beta)(3d^24p\beta|P|3d^3, \alpha)(3d^3, \alpha|a) \\ + \sum_{\alpha'} (b|3d^24p\beta')(3d^24p\beta'|P|3d^24s\alpha') \\ (3d^24s, \alpha'|a) \quad (5)$$

where α, α' and β, β' are the sets of relevant quantum numbers in the LS representation. In each of the two sums in eq (5) there is a factorable radial integral factor $(nl||P||n'l')$, where nl and $n'l'$ are the radial and orbital angular momentum quantum numbers of the jumping electron. Each set of configurations has a different set of $n, l; n', l'$. It is the phase and magnitude of the ratio of these radial factors which must be determined to calculate the relative intensities.

The determination of the expansion coefficients $(K|a)$ and the relative phase and magnitude as well

as comparison with experiments are discussed elsewhere [4]. In the table we show the strengths for the transition array for $3d^3 + 3d^24s - 3d^24p$ for Ti II. The composition of the upper and lower level is described in terms of the dominant states in the LS representation. For each position in the array, the upper number is the relative strength of the transition. The next lower number is the wavelength corresponding to the transition obtained from Russell's classifications [5], whenever available. The lowest number gives the wavenumber corresponding to the transition. The relative strengths are given to three significant figures for the stronger transitions and only one significant figure for the weaker lines. The number of significant figures given is consistent with the results of the diagonalization of the energy matrix and the empirical determination of the ratio of the radial integral parameters [4]. The magnitudes of the radial integral parameters have been found to be equal within the approximations that have been used, so in this table, the magnitudes of the radial integral factor have been taken to be unity for simplicity. Those relative strengths listed as zero indicate that, on the scale employed here, these strengths are less than 5×10^{-5} .

TABLE 1. Transition array for $(3d^3 + 3d^24s) - 3d^24p$ in Ti II in intermediate coupling scheme with configuration interaction.

The upper and lower levels are described in terms of the dominant states in the LS representation and the energy levels assigned in AEL [6]. For each position in the array, the upper number is the relative strength of the transition with the normalization of the radial integral parameter for the jumping electron in the $d-p$ transition taken as unity. The next lower number is the wavelength corresponding to the transition obtained from Russell's classification when available. The lowest number is the wave number of the transition.

		$(3d^3 + 3d^24s)$				
1/2	1/2	a^2P 9850.90	a^4P 9363.71	a^2S 21338.0	b^2P 16515.79	b^4P 9872.87
$(3d^24p)$	z^2S° 37430.55	0.0004 3624.82 27579.65	0.0000 3561.92 28066.84	0.0000 6212.29 16092.55	0.30 4779.95 20914.76	0.0001 3627.70 27557.68
	$^2P^\circ$ (63210.1)	0.0003 53359.20	0.0000 53846.39	0.66 41872.10	0.003 46694.31	0.0000 53337.23
	γ^2P° 45472.89	0.21 2806.50 35621.99	0.02 36109.18	0.004 24134.89	0.23 3452.47 28957.10	0.003 35600.02
	z^2P° 39674.64	0.06 3352.06 29823.74	0.003 3298.20 30310.93	0.005 5452.02 18336.64	0.02 4316.80 23158.85	0.002 29801.77
	z^4P° 41996.74	0.003 32145.84	0.01 3063.48 32633.03	0.0000 4839.22 20658.74	0.0001 25480.95	0.10 3112.05 32123.87
	γ^4D° 40330.25	0.005 30479.35	0.01 30966.54	0.0000 18992.25	0.0000 23814.46	0.55 3282.33 30457.38
	z^4D° 32532.38	0.007 4407.68 22681.48	0.08 4314.98 23168.67	0.0000 11194.38	0.0000 16016.59	0.008 4411.94 22659.51

TABLE 1. — Continued

 $(3d^3 + 3d^24s)$

$\begin{array}{c} 3/2 \\ \backslash \\ 1/2 \end{array}$	a^2P	a^4P	d_1^2D	b_3^2D	b^4F	b^2P	b^4P	a^2D	a^4F	D^2D
	9975.92	9395.76	(32358.5)	12628.77	907.96	16625.25	9930.74	8710.47	0	24961.34
z^2S° 37430.55	0.26 3641.33 27454.63	0.04 3566.00 28034.79	0.0000 5072.05	0.002 24801.78	0.0000 36522.59	0.18 4805.10 20805.30	0.03 27499.81	0.02 3480.89 28720.08	0.0000 37430.55	0.0001 12469.21
$^2P^\circ$ (63210.1)	0.0008 53234.18	0.0001 53814.34	0.14 30851.60	0.03 50581.33	0.0000 62302.14	0.002 46584.85	0.0001 53279.36	0.0002 54499.63	0.0000 63210.10	0.02 38248.76
y^2P° 45472.89	0.01 35496.97	0.002 36077.13	0.14 13114.39	0.06 3043.85 32844.12	0.0000 44564.93	0.22 3465.58 28847.64	0.002 35542.15	0.001 2719.39 36762.42	0.0000 45472.89	0.04 4873.95 20511.55
z^2P° 39674.64	0.09 3366.17 29698.72	0.02 30278.88	0.0008 7316.14	0.002 3696.38 27045.87	0.0001 38766.68	0.002 4337.32 23049.39	0.01 29743.90	0.69 3228.60 30964.17	0.0003 39674.64	0.008 14713.30
z^4P° 41996.74	0.02 3122.10 32020.82	0.07 3066.52 32600.98	0.0000 9638.24	0.0001 29367.97	0.0000 41088.78	0.0001 25371.49	0.54 3117.67 32066.00	0.0000 33286.27	0.0000 41996.74	0.0000 17035.40
y^4D° 40330.25	0.01 30354.33	0.002 30934.49	0.0000 7971.75	0.0000 27701.48	0.08 2535.87 39422.29	0.0001 23705.00	0.09 3288.58 30399.51	0.0008 31619.78	0.01 2478.77 40330.25	0.0000 15368.91
z^4D° 32532.38	0.0005 4432.10 22556.46	0.02 4320.95 23136.62	0.0000 173.88	0.0000 19903.61	0.16 3161.20 31624.42	0.0000 15907.13	0.002 22601.64	0.0000 23821.91	0.66 3072.97 32532.38	0.0000 7571.04

 $(3d^24p)$

TABLE 1. — Continued

 $(3d^3 + 3d^24s)$

$\begin{array}{c} 1/2 \\ \hline 3/2 \end{array}$	a^2P 9850.90	a^4P 9363.71	a^2S 21338.0	b^2P 16515.79	b^4P 9872.87
z^4S° 40027.28	0.03 30176.38	0.09 3260.26 30663.57	0.0005 18689.28	0.0006 23511.49	0.20 3315.32 30154.41
$^2P^\circ$ (63284.3)	0.0006 53433.40	0.0000 53920.59	1.32 41946.30	0.0007 46768.51	0.0000 53411.43
y^2P° 45548.90	0.007 35698.00	0.0006 36185.19	0.007 24210.90	0.14 3443.38 29033.11	0.0000 35676.03
z^2P° 39602.90	0.04 29752.00	0.02 3306.04 30239.19	0.01 5473.52 18264.90	0.002 4330.25 23087.11	0.01 3362.66 29730.03
z^4P° 42068.85	0.0008 3103.00 32217.95	0.07 3056.74 32705.14	0.0001 20730.85	0.0001 25553.06	0.52 3105.08 32195.98
x^2D° 44914.80	0.13 2851.10 35063.90	0.01 2812.05 35551.09	0.0001 23576.80	0.86 3520.25 28399.01	0.001 35041.93
y^2D° 39233.44	0.05 3402.42 29382.54	0.004 29869.73	0.0003 17895.44	0.05 22717.65	0.008 3404.99 29360.57
z^2D° 31756.50	0.18 4563.77 21905.60	0.03 4464.47 22392.79	0.0000 10418.50	0.01 6559.58 15240.71	0.0004 4568.30 21883.63
y^4D° 40425.80	0.02 3269.75 30574.90	0.005 31062.09	0.0000 19087.80	0.001 23910.01	0.56 3272.08 30552.93
z^4D° 32602.51	0.03 4394.06 22751.61	0.06 4301.93 23238.80	0.0000 11264.51	0.0006 16086.72	0.01 4398.31 22729.64
z^4F° 30836.52	0.0003 20985.62	0.0000 21472.81	0.0000 9498.52	0.0000 14320.73	0.0000 20963.65

 $(3d^24p)$

TABLE 1. — Continued

(3d³ + 3d²4s)(3d²4p)

3/2	a ² P	a ⁴ P	d ² D	b ² D	b ⁴ F	b ² P	b ⁴ P	a ² D	a ⁴ F	C ² D
3/2	9975.92	9395.76	(32358.5)	12628.77	907.96	16625.25	9930.74	8710.47	0	24961.34
z ⁴ S°	0.0004	0.18	0.0002	0.005	0.0000	0.007	0.52	0.009	0.0000	0.0000
40027.28	30051.36	3263.68 30631.52	7668.78	27398.51	39119.32	23402.03	3321.70 30096.54	3192.26 31316.81	40027.28	15065.94
z ² P°	0.0003	0.0000	0.03	0.003	0.0000	0.008	0.0000	0.004	0.0000	0.004
(63284.3)	53308.38	53888.54	30925.80	50655.53	62376.34	46659.05	53353.56	54573.83	63284.3	38322.96
y ² P°	0.50	0.06	0.04	0.02	0.0000	0.63	0.08	0.001	0.0000	0.01
45548.90	35572.98	2765.22 36153.14	13190.40	3036.78 32920.13	44640.94	3456.39 28923.65	35618.16	2713.76 36838.43	45548.90	20587.56
z ² P°	0.12	0.05	0.0001	0.07	0.0000	0.06	0.002	0.002	0.0001	0.0000
39602.90	3374.35 29626.98	30207.14	7244.40	3706.23 26974.13	38694.94	4350.83 22977.65	3369.20 29672.16	3236.12 30892.43	39602.90	14641.56
z ⁴ P°	0.04	0.02	0.0000	0.0001	0.0000	0.0002	0.14	0.0000	0.0000	0.0000
42068.85	3115.09 32092.93	3059.74 32673.09	9710.35	29440.08	41160.89	25443.60	3110.67 32138.11	33358.38	42068.85	17107.51
x ² D°	0.03	0.007	0.06	0.0005	0.0000	0.07	0.008	0.16	0.0000	0.02
44914.80	2861.29 34938.88	2814.61 35519.04	12556.30	3096.43 32286.03	44006.84	3533.85 28289.55	34984.06	2761.29 36204.33	44914.80	5010.21 19953.46
y ² D°	0.03	0.02	0.02	0.008	0.0008	0.04	0.01	1.19	0.0000	0.004
39233.44	3416.95 29257.52	3350.53 29837.68	6874.94	3757.69 26604.67	38325.48	4421.95 22608.19	29302.70	3275.38 30522.97	39233.44	14272.10
z ² D°	0.002	0.01	0.01	0.18	0.001	0.04	0.001	0.002	0.03	0.0004
31756.50	4589.95 21780.58	4470.88 22360.74		5226.56 19127.73	3240.72 30848.54	15131.25	4580.46 21825.76	4337.92 23046.03	31756.50	6795.16
y ⁴ D°	0.07	0.009	0.0008	0.0001	0.03	0.001	0.57	0.02	0.004	0.0001
40425.80	30449.88	31030.04	8067.30	3596.55 27797.03	2529.86 39517.84	23800.55	3278.29 30495.06	31715.33	40425.80	15464.46
z ⁴ D°	0.02	0.09	0.0008	0.009	0.07	0.002	0.004	0.0001	0.23	0.0000
32602.51	4418.33 22626.59	4307.90 23206.75	244.01	19973.74	3154.20 31694.55	15977.26	4409.53 22671.77	4184.33 23892.04	32602.51	7641.17
z ⁴ F°	0.0000	0.0000	0.0001	0.0003	0.32	0.0001	0.0000	0.0000	1.07	0.0000
30836.52	20860.60	21440.76		18207.75	3340.34 29928.56	14211.27	20905.78	22126.05	3241.99 30836.52	5875.18

TABLE 1.—Continued

 $(3d^3 + 3d^24s)$

$\begin{array}{c} 3/2 \\ 5/2 \end{array}$	a^2P	a^4P	d^3D	b^3D	b^4F	b^2P	b^4P	a^2D	a^4F	C^2D
	9975.92	9395.76	(32358.5)	12628.77	907.96	16625.25	9930.74	8710.47	0	24961.34
z^4P°	0.02	0.07	0.0000	0.001	0.0000	0.001	0.55	0.0000	0.0000	0.0000
42208.84	32232.92	3046.69 32813.08	9850.34	29580.07	41300.88	25583.59	3097.19 32278.10	33498.37	42208.84	17247.50
x^2D°	0.19	0.02	0.01	0.02	0.0000	1.39	0.03	0.02	0.0000	0.002
44902.42	2862.32 34926.50	2815.57 35506.66	12543.92	3097.63 32273.65	43994.46	3535.41 28277.17	34971.68	2762.22 36191.95	44902.42	19941.08
y^2D°	0.07	0.04	0.001	0.10	0.0001	0.07	0.10	0.11	0.0000	0.002
39476.87	3388.76 29500.95	30081.11	7118.37	3723.60 26848.10	38568.91	4374.82 22851.62	29546.13	3249.37 30766.40	39476.87	14515.53
z^2D°	0.24	0.13	0.004	0.02	0.0003	0.02	0.02	0.006	0.003	0.0000
32025.50	4533.97 22049.58	4417.72 22629.74		5154.07 19396.73	31117.54	6491.68 15400.25	4524.72 22094.76	4287.88 23315.03	3121.60 32025.50	7064.16
y^4D°	0.28	0.005	0.0000	0.0000	0.002	0.004	1.11	0.0000	0.0003	0.0000
40581.80	3266.41 30605.88	31186.04	8223.30	3576.37 27953.03	2519.79 39673.84	23956.55	3261.59 30651.06	3136.75 31871.33	40581.80	15620.46
z^4D°	0.08	0.12	0.0003	0.002	0.005	0.003	0.06	0.0004	0.01	0.0000
32697.94	4399.77 22722.02	4290.23 23302.18	339.44	20069.17	31789.98	16072.69	4391.02 22767.20	23987.47	3057.40 32697.94	7736.60
y^2F°	0.01	0.005	0.003	0.23	0.0001	0.001	0.001	1.35	0.0000	0.02
39926.83	3337.79 29950.91	30531.07	7568.33	3662.24 27298.06	39018.87	23301.58	29996.09	3202.54 31216.36	39926.83	6680.26 14965.49
z^2F°	0.002	0.0001	0.02	0.02	0.005	0.0005	0.0000	0.21	0.0000	0.0001
31207.44	4708.65 21231.52	4583.44 21811.68		5381.02 18578.67	30299.48	14582.19	21276.70	4443.80 22496.97	3203.44 31207.44	6246.10
x^2F°	0.0003	0.0002	0.20	0.03	0.0000	0.0006	0.0001	0.009	0.0000	0.04
47625.17	2655.30 37649.25	38229.41	15266.67	2856.62 34996.40	46717.21	30999.92	37694.43	2568.98 38914.70	47625.17	4411.08 22663.83
z^4F°	0.0001	0.0000	0.0007	0.001	0.08	0.0000	0.0001	0.007	0.26	0.0000
30958.70	20982.78	4636.34 21562.94		18329.93	3326.76 30050.74	14333.45	21027.96	4493.52 22248.23	3229.19 30958.70	5997.36
z^4G°	0.0000	0.0000	0.0001	0.0000	0.06	0.0000	0.0000	0.001	1.72	0.0000
29544.37	19568.45	20148.61		16915.60	3491.05 28636.41	12919.12	19613.63	4798.52 20833.90	3383.76 29544.37	4583.03

TABLE 1.—Continued

 $(3d^3 + 3d^2 4s)$

$\begin{array}{c} 5/2 \\ \hline 3/2 \end{array}$	a^4P	d^2D	d^3D	b^2F	b^4F	b^4P	a^2D	a^2F	a^4F	C^2D
	9518.05	(32362.7)	12758.15	20951.77	983.80	10024.74	8744.27	4628.61	93.94	25193.04
z^4S°	0.35	0.0000	0.0000	0.0000	0.0001	0.63	0.02	0.0002	0.0000	0.0008
40027.28	3276.76 30509.23	7664.58	27269.13	19075.51	39043.48	3332.11 30002.54	3195.71 31283.01	35398.67	39933.34	14834.24
z^2P°	0.0000	0.24	0.06	0.0000	0.0000	0.0000	0.0001	0.0000	0.0000	0.05
(63284.3)	53766.25	30921.60	50526.15	42332.53	62300.50	53259.56	54540.03	58655.69	63190.36	38091.26
y^2P°	0.0000	0.23	0.08	0.006	0.0000	0.0000	0.004	0.0003	0.0000	0.07
45548.90	36030.85	13186.20	3048.77 32790.75	4064.40 24597.13	44565.10	35524.16	2716.25 36804.63	40920.29	45454.96	4911.19 20355.86
z^2P°	0.004	0.0008	0.008	0.0000	0.0001	0.007	1.41	0.003	0.0003	0.02
39602.90	30084.85	7240.20	3724.08 26844.75	18651.13	38619.10	3379.92 29578.16	3239.66 30858.63	2858.40 34974.29	39508.96	14409.86
z^4P°	0.08	0.0000	0.001	0.0000	0.0000	0.64	0.0002	0.0001	0.0000	0.0001
42068.85	3071.24 32550.80	9706.15	29310.70	21117.08	41085.05	3119.80 32044.11	33324.58	37440.24	41974.91	16875.81
x^2D°	0.0000	0.02	0.02	0.62	0.0000	0.0001	0.009	0.04	0.0000	0.004
44914.80	35396.75	12552.10	3108.93 32156.65	4171.90 23963.03	43931.00	34890.06	36170.53	2481.49 40286.19	44820.86	5069.12 19721.76
y^2D°	0.003	0.0007	0.07	0.0004	0.005	0.0000	0.003	0.08	0.0005	0.0000
39233.44	29715.39	6870.74	3776.06 26475.29	18281.67	38249.64	3422.69 29208.70	3278.92 30489.17	2888.93 34604.83	39139.50	14040.40
z^2D°	0.0004	0.002	0.008	0.01	0.01	0.0003	0.01	1.10	0.05	0.0000
31756.50	22238.45		5262.14 18998.35	10804.73	30772.70	21731.76	4344.29 23012.23	3685.19 27127.89	3157.39 31662.56	6563.46
y^4D°	0.003	0.0000	0.003	0.0000	0.13	0.07	0.001	0.002	0.02	0.0000
40425.80	30907.75	8063.10	27667.65	19474.03	2534.62 39442.00	3288.42 30401.06	31681.53	35797.19	2478.64 40331.86	15232.76
z^4D°	0.01	0.0001	0.0005	0.0005	0.23	0.0007	0.001	0.06	1.01	0.0000
32602.51	4330.71 23084.46	239.81	19844.36	11650.74	3161.77 31618.71	22577.77	4190.29 23858.24	3573.74 27973.90	3075.22 32508.57	7409.47
z^4F°	0.0000	0.0000	0.0001	0.0000	0.08	0.0000	0.0000	0.003	0.26	0.0000
30836.52	21318.47		18078.37	9884.75	3348.82 29852.72	20811.78	22092.25	3814.57 26207.91	3251.91 30742.58	5643.48

 $(3d^2 4p)$

TABLE 1. — Continued

 $(3d^3 + 3d^24s)$ $(3d^24p)$

$\begin{array}{c} 5/2 \\ 5/2 \end{array}$	a^4P	d^2D	b^2D	b^2F	b^4F	b^4P	a^2D	a^2F	a^4F	C^2D
	9518.05	(32362.7)	12758.15	20951.77	983.80	10024.74	8744.27	4628.61	93.94	25193.04
z^4P° 42208.84	0.17 3058.09 32690.79	0.0004 9846.14	0.0006 29450.69	0.0000 21257.07	0.0000 41225.04	1.45 3106.23 32184.10	0.0002 2987.38 33464.57	0.0000 37580.23	0.0000 42114.90	0.0000 17015.80
x^2D° 44902.42	0.0004 35384.37	0.10 12539.72	0.0009 3110.11 32144.27	0.04 23950.65	0.0000 43918.62	0.004 34877.68	0.26 2764.80 36158.15	0.009 40273.81	0.0000 44808.48	0.05 5072.30 19709.38
y^2D° 39476.87	0.001 336.98 29958.82	0.03 7114.17	0.0000 3741.64 26718.72	0.0000 18525.10	0.002 38493.07	0.02 29452.13	1.72 30732.60	0.0001 2868.74 34848.26	0.0001 39382.93	0.006 14283.83
z^2D° 32025.50	0.01 22507.45	0.02	0.22 5188.70 19267.35	0.0005 11073.73	0.007 3220.48 31041.70	0.0001 4544.01 22000.76	0.001 4294.12 23281.23	0.008 27396.89	0.06 3130.80 31931.56	0.0008 6832.46
y^4D° 40581.80	0.01 31063.75	0.002 8219.10	0.001 3593.11 27823.65	0.0006 19630.03	0.04 2524.64 39598.00	0.53 3271.65 30557.06	0.07 31837.53	0.001 2780.55 35953.19	0.005 40487.86	0.0003 15388.76
z^4D° 32697.94	0.08 4312.87 23179.89	0.003 335.24	0.03 5013.69 19939.79	0.0000 11746.17	0.08 3152.25 31714.14	0.01 4409.23 22673.20	0.0002 4173.55 23953.67	0.008 3561.59 28069.33	0.27 3066.22 32604.00	0.0001 7504.90
y^2F° 39926.83	0.0009 30408.78	0.004 7564.13	0.03 27168.68	0.08 5268.63 18975.06	0.0008 38943.03	0.002 29902.09	0.21 3206.00 31182.56	0.12 2832.16 35298.22	0.0001 39832.89	0.0002 14733.79
z^2F° 31207.44	0.0002 21689.39	0.002	0.04 5418.77 18449.29	0.12 10255.67	0.02 3307.72 30223.64	0.0000 4719.51 21182.70	0.0008 4450.49 22463.17	1.70 3761.32 26578.83	0.05 3213.14 31113.50	0.0002 6014.40
x^2F° 47625.17	0.0000 38107.12	0.02 15262.47	0.0001 34867.02	0.26 3748.01 26673.40	0.0000 46641.37	0.0001 37600.43	0.002 38880.90	0.01 42996.56	0.0000 47531.23	0.005 4456.62 22432.13
z^4F° 30958.70	0.0000 21440.65	0.0000	0.0004 18200.55	0.005 10006.93	0.39 3335.20 29974.90	0.0000 20933.96	0.0001 22214.43	0.05 3796.88 26330.09	1.36 3239.04 30864.72	0.0000 5765.66
z^4G° 29544.37	0.0000 20026.32	0.0000	0.0001 16786.22	0.0005 8592.60	0.01 3500.33 28560.57	0.0000 19519.63	0.0000 20800.10	0.008 4012.39 24915.76	0.26 3394.58 29450.43	0.0000 4351.33

TABLE 1. – Continued

 $(3d^3 + 3d^24s)$ $(3d^24p)$

$\begin{array}{c} 5/2 \\ \hline 7/2 \end{array}$	a^4P	d^2D	b^2D	b^2F	b^4F	b^4P	a^2D	a^2F	a^4F	C^2D
	9518.05	(32362.7)	12758.15	20951.77	983.80	10024.74	8744.27	4628.61	93.94	25193.04
γ^4D° 40798.37	0.04 3195.99 31280.32	0.0002 8435.67	0.02 3565.33 28040.22	0.0000 19846.60	0.002 2510.90 39814.57	2.59 3248.60 30773.63	0.01 3118.85 32054.10	0.0002 2763.90 36169.76	0.0002 40704.43	0.001 15605.33
z^4D° 32767.02	0.42 4300.05 23248.97	0.0000 404.32	0.0005 20008.87	0.0000 11815.25	0.004 31783.22	0.04 4395.86 22742.28	0.001 4161.54 24022.75	0.0002 28138.41	0.01 3059.73 32673.08	0.0000 7573.98
γ^2F° 40074.71	0.0005 30556.66	0.005 7712.01	0.33 3659.76 27316.56	0.002 19122.94	0.0001 39090.91	0.03 30049.97	2.07 3190.87 31330.44	0.008 35446.10	0.0001 39980.77	0.03 6717.89 14881.67
z^2F° 31490.82	0.0002 21972.77	0.03	0.04 5336.81 18732.67	0.0003 10539.05	0.004 3276.98 30507.02	0.004 4657.20 21466.08	0.33 4395.04 22746.55	0.08 3721.64 26862.21	0.0004 3184.09 31396.88	0.0001 6297.78
x^2F° 47466.80	0.0002 37948.75	0.28 15104.10	0.05 2880.28 34708.65	0.01 3770.40 26515.03	0.0000 46483.00	0.0002 37442.06	0.01 2581.73 38722.53	0.0000 42838.19	0.0000 47372.86	0.06 4488.32 22273.76
z^4F° 31113.61	0.0002 21595.56	0.0007	0.001 18355.46	0.0000 10161.84	0.11 3318.03 30129.81	0.0002 21088.87	0.007 4469.15 22369.34	0.004 26485.00	0.33 3222.84 31019.67	0.0000 5920.57
z^2G° 34543.36	0.0000 25025.31	0.0000 2180.66	0.0001 21785.21	0.03 13591.59	0.0000 33559.56	0.0000 24518.62	0.0000 25799.09	2.45 3341.88 29914.75	0.0001 2901.94 34449.42	0.0000 9350.32
γ^2G° 43740.77	0.0000 34222.72	0.0000 11378.07	0.0002 30982.62	0.20 4386.86 22789.00	0.0000 42756.97	0.0000 33716.03	0.0009 34996.50	0.07 2555.99 39112.16	0.0000 43646.83	0.0000 18547.73
z^4G° 29734.45	0.0000 20216.40	0.0000	0.0000 16976.30	0.0000 8782.68	0.07 3477.18 28750.65	0.0000 19709.71	0.0006 4762.78 20990.18	0.0002 3982.01 25105.84	2.32 3372.80 29640.51	0.0000 4541.41

TABLE 1. — Continued

 $(3d^3 + 3d^24s)$

$\begin{array}{c} 7/2 \\ 5/2 \end{array}$	b^2F	b^4F	a^2G	a^2F	a^4F	b^2G
	20891.88	1087.21	8997.69	4897.60	225.47	15265.60
z^4P°	0.0000	0.0001	0.0000	0.0007	0.0000	0.0000
42208.84	21316.96	41121.63	33211.15	37311.24	41983.37	26943.24
x^2D°	0.89 4163.65	0.0000	0.0004	0.07 2498.94	0.0000	0.0007
44902.42	24010.54	43815.21	35904.73	40004.82	44676.95	29636.82
y^2D°	0.003	0.01 2604.11	0.009 3279.98	0.11 2891.07	0.001 2546.88	0.002
39476.87	18584.99	38389.66	30479.18	34579.27	39251.40	24211.27
z^2D°	0.01	0.05 3231.32	0.005 4341.39	1.52 3685.20	0.19 3143.76	0.0000
32025.50	11133.62	30938.29	23027.81	27127.90	31800.03	16759.90
y^4D°	0.0000	0.19 2531.25	0.004	0.004	0.02 2477.21	0.0007
40581.80	19689.92	39494.59	31584.11	35684.20	40356.33	25316.20
z^4D°	0.002	0.33 3162.57	0.0001	0.21 3596.05	1.44 3078.64	0.0000
32697.94	11806.06	31610.73	23700.25	27800.34	32472.47	17432.34
y^2F°	0.004	0.003 2573.91	0.57 3232.28	0.001 2853.93	0.0005 2518.06	0.09 4053.84
39926.83	19034.95	38839.62	30929.14	35029.23	39701.36	24661.23
z^2F°	0.001	0.002 3319.08	0.23 4501.27	0.02 3799.78	0.02 3226.76	0.0000
31207.44	10315.56	30120.23	22209.75	26309.84	30981.97	15941.84
x^2F°	0.01 3739.50	0.0000	0.0000	0.0000	0.0000	2.04 3089.40
47625.17	26733.29	46537.96	38627.48	42727.57	47399.70	32359.57
z^4F°	0.0000	0.11 3346.73	0.009	0.004 3836.10	0.32 3252.91	0.0000
30958.70	10066.82	29871.49	21961.01	26061.10	30733.23	15693.10
z^4G°	0.0000	0.0005 3513.08	0.0006 4865.62	0.0002 4056.20	0.009 3409.81	0.0000
29544.37	8652.49	28457.16	20546.68	24646.77	29318.90	14278.77

 $(3d^24p)$

TABLE 1. — Continued

 $(3d^3 + 3d^24s)$

$\begin{array}{c} 7/2 \\ \hline 7/2 \end{array}$	b^2F	b^4F	a^2G	a^2F	a^4F	b^2G
	20891.88	1087.21	8997.69	4897.60	225.47	15265.60
y^4D° 40798.37	0.003 19906.49	0.03 2517.43 39711.16	0.001 31800.68	0.005 2784.67 35900.77	0.004 2464.00 40572.90	0.0001 25532.77
z^4D° 32767.02	0.0004 11875.14	0.07 3155.67 31679.81	0.0000 23769.33	0.006 3587.13 27869.42	0.24 3072.11 32451.55	0.0000 17501.42
y^2F° 40074.71	0.10 5211.58 19182.83	0.002 38987.50	0.03 31077.02	0.17 2841.94 35177.11	0.0002 39849.24	0.002 24809.11
z^2F° 31490.82	0.17 10598.94	0.02 3288.13 30403.61	0.007 4444.56 22493.13	2.21 3759.30 26593.22	0.04 3197.52 31265.35	0.001 16225.22
x^2F° 47466.80	0.36 3761.89 26574.92	0.0000 46379.59	0.01 38469.11	0.01 42569.20	0.0000 47241.33	0.08 3104.60 32201.20
z^4F° 31113.61	0.005 10221.73	0.58 3329.46 30026.40	0.0001 22115.92	0.05 3813.39 26216.01	2.04 3236.57 30888.14	0.0000 15848.01
z^2G° 34543.36	0.0004 13651.48	0.0001 33456.15	0.31 3913.46 25545.67	0.09 3372.21 29645.76	0.0005 2913.08 34317.89	0.18 5185.90 19277.76
y^2G° 43740.77	0.003 22848.89	0.0000 42653.56	0.008 2877.44 34743.08	0.005 2573.72 38843.17	0.0000 43515.30	2.63 3510.84 28475.17
z^4G° 29734.45	0.0002 8842.57	0.02 3489.74 28647.24	0.0001 20736.76	0.003 4025.14 24836.85	0.33 3387.84 29508.98	0.0000 14468.85

 $(3d^24p)$

TABLE 1.—Continued

 $(3d^3 + 3d^24s)$

$\begin{array}{c} 7/2 \\ 9/2, 11/2 \end{array}$	b^2F	b^4F	a^2G	a^2F	a^4F	b^2G
	20891.88	1087.21	8997.69	4897.60	225.47	15265.60
z^4F°	0.0000	0.09	0.0000	0.002	0.24	0.0000
31300.92	10409.04	3308.81 30213.71	22303.23	26403.32	3217.06 31075.45	16035.32
z^2G°	0.04	0.0000	0.01	3.16	0.0001	0.0007
34748.50	13856.62	33661.29	25750.81	3349.04 29850.90	2895.81 34523.03	19482.90
y^2G°	0.25	0.0000	0.01	0.10	0.0000	0.05
43780.99	4367.66 22889.11	42693.78	2874.08 34783.30	2571.03 38883.39	43555.52	3505.91 28515.39
z^4G°	0.0000	0.10	0.0000	0.0000	3.09	0.0000
29968.08	9076.20	3461.50 28880.87	20970.39	25070.48	3361.21 29742.61	14702.48
z^2H°	0.0001	0.0000	0.02	0.0000	0.0000	3.30
45673.75	24781.87	44586.54	2725.78 36676.06	40776.15	45448.28	3287.66 30408.15

 $(3d^24p)$

TABLE 1. — Continued

 $(3d^3 + 3d^24s)$

<div style="display: inline-block; transform: rotate(-45deg);"> 9/2, 11/2 7/2 </div>	b^4F	a^2G	a^2H	a^4F	b^2G
	1215.58	9118.15	12676.99	393.22	15257.53
γ^4D° 40798.37	0.28 2525.60 39582.79	0.03 31680.22	0.0000 28121.38	0.04 2474.22 40405.15	0.006 25540.84
z^4D° 32767.02	0.56 3168.52 31551.44	0.0007 23648.87	0.0000 20090.03	2.36 3088.02 32373.80	0.0000 17509.49
γ^2F° 40074.71	0.01 38859.13	0.70 3229.42 30956.56	0.002 3648.87 27397.72	0.003 2519.31 39681.49	0.12 4028.34 24817.18
z^2F° 31490.82	0.0001 3302.09 30275.24	0.30 4468.50 22372.67	0.0001 18813.83	0.02 3214.75 31097.60	0.0000 16233.29
x^2F° 47466.80	0.0000 46251.22	0.0000 38348.65	0.0001 34789.81	0.0000 47073.58	2.63 3103.80 32209.27
z^4F° 31113.61	0.09 3343.77 29898.03	0.009 4545.14 21995.46	0.0001 18436.62	0.24 3254.25 30720.39	0.0000 15856.08
z^2G° 34543.36	0.0000 33327.78	0.03 3932.02 25425.21	0.66 4571.98 21866.37	0.0000 34150.14	0.001 5183.73 19285.83
γ^2G° 43740.77	0.0000 42525.19	0.01 2887.46 34622.62	0.90 3218.27 31063.78	0.0000 43347.55	0.06 3509.85 28483.24
z^4G° 29734.45	0.0005 28518.87	0.0002 20616.30	0.0003 17057.46	0.006 3407.20 29341.23	0.0000 14476.92

 $(3d^24p)$

TABLE 1. — Concluded

 $(3d^3 + 3d^24s)$

$\begin{array}{c} 9/2, \\ 11/2 \end{array}$	$\begin{array}{c} 9/2, \\ 11/2 \end{array}$	b^4F	a^2G	a^2H	a^4F	b^2G	a^2H
		1215.58	9118.15	12676.99	393.22	15257.53	12774.81
z^4F°	0.91 3322.94 31300.92	0.0001 30085.34 22182.77	0.0000 18623.93 30907.70	3.10 3234.52 16043.39	0.0004 18526.11		
z^2G°	0.0005 34748.50	0.38 3900.54 33532.92	0.02 4529.46 22071.51	0.003 2909.92 34355.28	0.24 5129.15 19490.97	0.81 4549.63 21973.69	
y^2G°	0.0000 43780.99	0.01 2884.11 34662.84	0.03 3214.12 31104.00	0.0000 43387.77	3.33 3504.89 28523.46	1.09 3224.24 31006.18	
z^4G°	0.01 3476.99 29968.08	0.0000 28752.50 20849.93	0.0000 17291.09	0.35 3380.28 29574.86	0.0000 14710.55	0.30 17193.27	
z^2H°	0.0000 45673.75	0.004 44458.17 36555.60	0.0000 3029.73 32996.76	0.0009 45280.53	0.05 3286.78 30416.22	0.009 3038.71 32898.94	
z^4G°	0.13 3444.31 30240.68	0.0000 21122.53	0.0000 17563.69	4.00 3349.41 29847.46	0.0000 14983.15	0.0000 17465.87	
z^2H°	0.0000 45908.56	0.02 2717.29 36790.41	0.01 3008.33 33231.57	0.0000 45515.34	4.02 3261.60 30651.03	0.47 3017.19 33133.75	

 $(3d^24p)$

References

- [1] Condon, E. U., and Shortley, G. H., The Theory of Atomic Spectra (Cambridge Univ. Press, New York, 1935).
 [2] Mendlowitz, H., Astroph. J. **138**, 1277 (1963).
 [3] Mendlowitz, H., Astroph. J. **141**, 573 (1966).
 [4] Mendlowitz, H., Astroph. J. **154**, 1099 (1968).
 [5] Russell, H. N., Astroph. J. **46**, 283 (1927).
 [6] Moore, C. E., Atomic Energy Levels, NBS Circ. 467 (1949).

(Paper 73A1-534)