

CALORIMETRIC DETERMINATIONS OF THERMAL PROPERTIES OF METHYL ALCOHOL, ETHYL ALCOHOL, AND BENZENE

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ABSTRACT

The method and calorimetric equipment previously used in the determination of thermal properties of saturated water and steam were applied, without essential modification, in an investigation of corresponding properties of methyl alcohol, ethyl alcohol, and benzene. Precautions were taken to obtain these liquids in a very pure state. Determinations were made in the range from 40° to 110° C., yielding values of latent heats of vaporization and changes in heat content. Empirical equations fitted to these properties aid in the interpolation, extrapolation, and application of the data. An estimate is made of the precision of the final results. A skeleton table of the more commonly used thermal properties of the saturated liquids and vapors has been prepared. Comparisons with the values of previous investigators are included.

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I. INTRODUCTION

The calorimetric equipment which was designed and used at the National Bureau of Standards¹ for the measurement of thermal properties of saturated water and steam became available for a limited survey of similar properties of other liquids upon completion of the initial steam program. Reliable thermal data on methyl alcohol, ethyl alcohol, and benzene were needed to supplement calorimetric measurements on heats of combustion which are now in progress at this bureau. On account of the physical and chemical properties of these liquids, the apparatus could be used without essential modification. They can be obtained in comparatively pure form, and their purity can be estimated by rather simple physical measurements.

¹ B. S. Jour. Research, 5, p. 411; 1930.

II. METHOD, APPARATUS, AND PROCEDURE

Each of the three organic liquids already mentioned was subjected to two distinct calorimetric processes. The first of these consisted in heating a known mass of the fluid from one saturation temperature to another, observing the total energy added and the temperature rise. Such measurements yield essentially the change in heat content or enthalpy of the calorimeter and its contents over the observed temperature interval. The second process consisted in removing saturated vapor from the calorimeter at practically constant temperature. These measurements yield essentially the value of the latent heat of vaporization at the temperature of the experiments.

To obtain values of heat content and of latent heat from the measurements as they were performed, a correction is necessary to take into account the change in the ratio of the masses of liquid and vapor in the calorimeter from the beginning to the end of an experiment. This correction has been shown in the published theory of the method² to be the same for both types of experiment, and, where desirable, can be determined by a third type of experiment in the same apparatus. For temperatures near the normal boiling points this correction is small compared to the quantities with which it must be combined, and its value can be calculated from specific volume and vapor pressure data more accurately than it can be measured calorimetrically.

The present series of experiments was undertaken primarily for obtaining values of latent heats, but, since it is not possible to start and finish each latent-heat experiment at identically the same temperature, the heat-capacity experiments were necessary for the evaluation of end corrections. The values of heat content obtained from the present work are probably as precise as any now available, but are not as well established as would have been desirable had more time been available for this work and had there been a specific need for more precise values.

The theory of the method, the apparatus, and the procedure were essentially the same as those developed in the work on steam. The two reports to which reference has already been made are given in considerable detail, and it is deemed unnecessary to include a lengthy repetition here.

The apparatus is built to provide for accurately controlling, observing, and accounting for the amount, change in state, and change in energy of a sample of fluid. A single calorimetric equipment yields results which establish values of latent heat and changes in heat content of the saturated fluids in the range covered by the experiments. A schematic representation of the calorimeter is given in Figure 1.

A quantity of fluid, part liquid and part vapor, is contained in a metal calorimeter shell (*C*). The liquid is circulated rapidly over an electric heater (*H*) and about the interior of the shell by a small centrifugal pump (*P*), to distribute heat and promote close approximation to thermal equilibrium. The sample at some chosen saturation state is heated to some other chosen saturation state, or else is withdrawn as saturated vapor. Energy is added and measured electrically.

Outlets with valves provide for the introduction and withdrawal of both liquid and vapor. The line at the top (*L'*) is for removing vapor, and is provided with a throttle valve (*T*) for controlling the rate of

² B. S. Jour. Research, 4, p. 609; 1930.

vapor flow. Following the throttle valve in this line are three other valves (*S*) for diverting the flow into any one of three receivers. These detachable receivers, suitable for weighing, are connected to the outlets to hold the samples of fluid transferred.

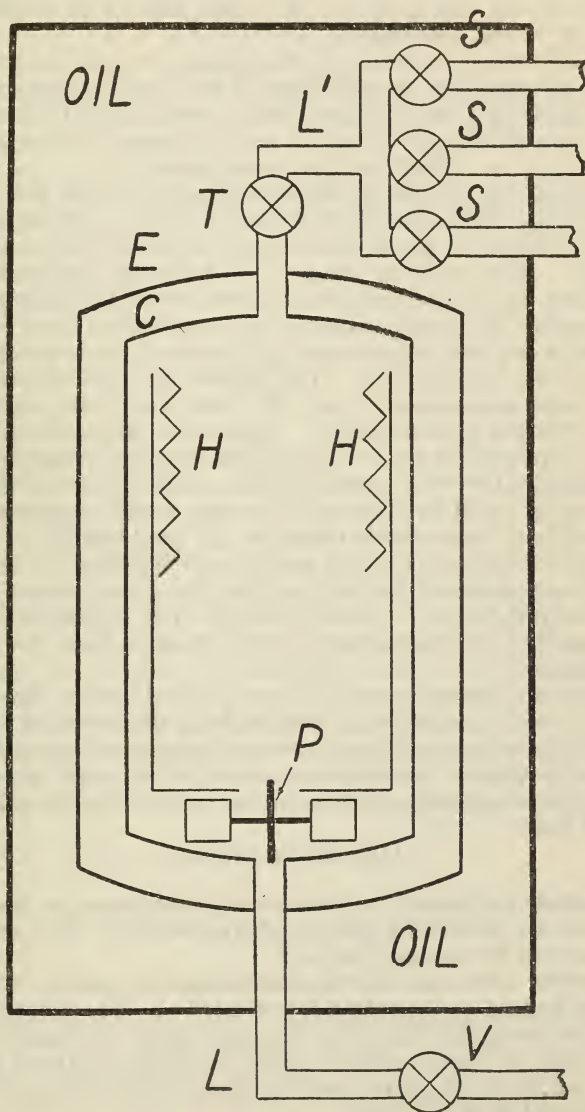


FIGURE 1.—Schematic representation of the calorimeter

The calorimeter is surrounded by an envelope (*E*) and the intervening space is filled with nitrogen. The envelope temperature is controlled and regulated by an oil bath which surrounds the entire apparatus.

Absolute temperatures are measured by means of a platinum resistance thermometer and small temperature differences by means of thermoclements.

In the present series of experiments the operators had the advantage of previous experience with the calorimeter. This proved useful not only in the actual manipulation, but also served as a guide in the simplification of the procedure.

During the steam research it was demonstrated that the pump energy was independent of the height of the liquid in the calorimeter, within the limit of error involved in its experimental determination. For this reason all measurements of pump energy with organic liquids were made with low fillings of the calorimeter.

The experimental values of the latent heat of water were shown to be independent of the rate of withdrawal of vapor. Hence the present series of vaporization experiments was performed at a single convenient rate. The work on steam, it is believed, demonstrates that only saturated vapor is withdrawn under normal operating conditions.

The quantity of energy passing by conduction, convection, and radiation between the calorimeter and its envelope is independent of the fluid in the calorimeter. The values of this thermal-leakage coefficient were determined during the work on steam, and were not remeasured for the present series. Because of the favorable range of temperature covered in these experiments and the greater skill which had been acquired by the operators, the actual values of the thermal leakage were so small in all cases that they could have been entirely neglected without appreciable effect on the final results.

The rate at which mechanical energy was supplied by the circulating pump was measured for each of the three compounds at several different temperatures. Curves through the experimental points made it possible to interpolate at the places where there were no determinations.

The resistance thermometer was recalibrated late in the steam program and showed no significant change from the previous calibration.

The potentiometers and electrical standards have been calibrated at frequent intervals at this bureau, and the thermal quantities are reported in international electrical units referred to the standards as maintained here.

III. NOTATION

The notation employed in this report is the same as that used by Osborne³ in the published theory of the method. For convenience his notation will be repeated in part.

The quantity obtained directly from a heat-capacity experiment is called α and from a vaporization experiment γ . The correction which takes into account the change in the proportion of liquid and vapor masses during an experiment is called β . Each of these quantities, when referred to in this paper, will be used specifically; that is, referring always to 1 g of the fluid.

Other quantities may be defined as follows:

H = heat content or enthalpy per unit mass of saturated liquid ($\epsilon + \pi u$).

H' = heat content or enthalpy per unit mass of saturated vapor ($\epsilon' + \pi u'$).

³ See footnote 2, p. 882.

ϵ = internal energy per unit mass of saturated liquid.

ϵ' = internal energy per unit mass of saturated vapor.

L = latent heat of vaporization per unit mass.

θ = temperature on the international scale.

Θ = temperature on the Kelvin scale.

π = saturation vapor pressure.

u = specific volume of saturated liquid.

u' = specific volume of saturated vapor.

Q = total energy added to the calorimeter in any experiment.

Z = a constant of the calorimeter depending on its temperature and the liquid it contains.

M = total mass of fluid in the calorimeter.

As shown in the published theory, the following thermodynamic relations may be used to reduce the quantities actually observed to those more commonly employed.

$$H = \alpha + \beta \quad (1)$$

$$L = \gamma - \beta \quad (2)$$

$$\gamma = L \frac{u'}{u' - u} = \Theta u' \frac{d\pi}{d\Theta} \quad (3)$$

$$\beta = L \frac{u}{u' - u} = \Theta u \frac{d\pi}{d\Theta} \quad (4)$$

$$H' = H + L \quad (5)$$

$$Q = Z + M\alpha \quad (6)$$

$$\gamma_1 = \frac{1}{\Delta M} \left\{ Q - [Z + M_2\alpha]^2 + \int_1^2 (H - H_1) dM \right\} \quad (7)$$

The values of H and L were obtained from the experimental values of α and γ and the values of β calculated from other data with the aid of the second form of equation (4).

The absolute value of H can not be determined, but any arbitrary datum may be chosen within the temperature range covered by the experiments, and values of H at other temperatures in the range can be established relative to the datum. Adoption of a datum for H simultaneously fixes a reference value for α .

IV. PREPARATION AND PHYSICAL PROPERTIES OF COMPOUNDS

1. METHYL ALCOHOL

Mallinckrodt's methyl alcohol, specially ordered as chloroform free, was distilled by Dr. J. H. Bruun, of the chemistry division of this bureau, in a nonsiphoning, 30-plate, bubbling-cap still ⁴ to remove water and other impurities which can be separated by fractional distillation. The middle fraction of 1,000 cm³ was used from a charge of 2,500 cm³ which was introduced into the still pot. The distillation was performed in an atmosphere of dry carbon dioxide at approximately atmospheric pressure. The distillate was collected in a bottle filled initially with dry air and was stored in a dessicator. Provision was made for transferring the liquid without further contact with the

⁴ Ind. Eng. Chem., Anal. ed., 1, p. 212; October, 1929.

air to a second still, which could be used both for refluxing and distilling. Here the sample was freed from dissolved gases by repeated refluxing, cooling, and evacuation. After thus pumping off the dissolved gas, the sample was distilled under its own vapor pressure at a temperature of about 50° C., and collected in evacuated silver containers. From these it was transferred to the calorimeter.

The specific gravity of the gas-free product, before its use in the calorimeter, was measured by the volumetric section of this bureau. To avoid contact with the atmosphere the alcohol was introduced into an evacuated picnometer through an evacuated line. The volume of the picnometer was about 87 cm³, and the samples used therein were always discarded. The observed specific gravity at 20° C. compared to water at 4° C. was $D_4^{20}=0.79133$. According to the International Critical Tables, vol. 3, p. 27, Klason and Norlin give as their value for absolute methyl alcohol $D_4^{20}=0.79134$.

An accurate combustion analysis of the original material was made by Dr. F. D. Rossini, of the chemistry division of this bureau. This analysis showed that the carbon-hydrogen ratio was that required by the formula CH₃OH, within the limit of error of the analysis, which was ± 0.03 per cent.

After the completion of a vaporization experiment the sample was in four containers, and had to be reassembled before being weighed into the calorimeter again. This was accomplished by transfer under its own vapor pressure through an evacuated line, without any contact with the atmosphere. Such a procedure made possible the performance of the whole series of calorimetric experiments on an original sample of about 350 g.

At one stage in the experiments with methyl alcohol a leak developed in the lower tube leading to the calorimeter. This permitted contact of a portion of the sample with the atmosphere. This portion was again freed from dissolved gas, but contained a small amount of water. For the remainder of the experiments the entire sample of alcohol was reunited, since the amount of water which could have been taken from the air was known to be small.

After the completion of the calorimetric experiments the specific gravity of the assembled sample was again measured and the value obtained was $D_4^{20}=0.79142$.

The increase in specific gravity was thus 0.00009, corresponding, if the impurity was all water, to about 0.026 per cent of water by weight. This fraction of water would produce no measurable effect on the values of α and would correspond to an increase in γ of only about 3 parts in 10,000. Since this is well within the experimental uncertainty involved, it was deemed unnecessary to repeat the experiments with another sample of alcohol.

2. ETHYL ALCOHOL

Through the courtesy of Dr. F. M. Hildebrandt, the United States Industrial Alcohol Co. furnished an especially selected sample of ethyl alcohol (192 volume proof) having a very low aldehyde content.

Most of the water present was removed by refluxing and distilling from an excess of freshly ignited lime at atmospheric pressure. About 2,500 cm³ of alcohol, whose specific gravity indicated a water content of 0.15 per cent by weight, were prepared by this method.

This 2,500 cm³ sample, together with 40 cm³ of Timmermans' benzene, which will be described later, was introduced into a still similar to that used for fractionating the methyl alcohol.

The remainder of the water was removed from this mixture by fractional distillation. The first fraction to distil consists of a constant boiling mixture of benzene, alcohol, and water. When all the water has been removed, a constant boiling binary mixture of benzene and alcohol continues to distil as long as any benzene remains. Since the indices of refraction of benzene and alcohol are so widely different, this property was used as a criterion for the complete removal of the benzene. About 250 cm³ were rejected after the index of the distillate became constant. The next 900 cm³ which distilled were used as the best product of the fractionation.

The method of collecting the sample and of removing dissolved gases from it was the same as that described for methyl alcohol. The specific gravity of the gas-free product was found to be $D_4^{20} = 0.78946$. According to the International Critical Tables, vol. 3, p. 27, Osborne, McKelvy, and Bearce give as their best value for absolute ethyl alcohol $D_4^{20} = 0.78934$. If water was the only impurity the initial sample contained 0.038 per cent by weight. The specific gravity of the alcohol which had been used in the entire series of observations was $D_4^{20} = 0.78949$, indicating 0.047 per cent of water by weight. The effect of this quantity of water on the measured values of latent heat could not have been greater than 0.6 joule per gram, or 1 part in 1,400 of the total.

3. BENZENE

About 1,000 cm³ of benzene prepared by Timmermans and Martin⁵ at the International Bureau of Physico-Chemical Standards at Brussels were refluxed for three hours with about 15 g of a 50-50 mol per cent sodium-potassium alloy. This alloy was furnished by Dr. O. C. Bridgeman, of this bureau, who had prepared it in very pure form for use in determining quantitatively the water content of gasolines.

The benzene was introduced into an apparatus which could be used both for refluxing and distilling. After it had been frozen and the permanent gas present removed by pumping, the alloy was introduced. After refluxing for a time the benzene was again frozen, and the gas evolved on boiling was pumped off. This process was repeated four times, the amount of noncondensable gas coming off the last time being practically nil.

After three hours of refluxing, during which numerous droplets of liquid alloy were in vigorous circulation within the liquid benzene, the benzene was distilled under its own vapor pressure at a temperature of about 50° C., and collected in evacuated silver containers.

The specific gravity of the air-free product was not measured before the calorimetric experiments because a sufficient quantity could not be spared. After the measurements were completed, specific gravities were measured on two samples which had been distilled from the

⁵ J. chim. phys., 23, p. 18; 1926.

calorimeter, and on the residue left in it after a series of vaporization experiments. The values of $D_{\frac{20}{4}}$ obtained were 0.87906 and 0.87907 for the distillate and 0.87906 for the residue.

The recorded determinations of the specific gravity of benzene at 20° C. vary from 0.8787 to 0.8795, with those which seem more reliable averaging about 0.8790. From specific-gravity measurements alone it is difficult to estimate the purity of benzene for want of a well-established reference value.

The product used in these experiments was prepared from the source which, according to our advices, was the best available. The water content was probably reduced to well below 0.01 per cent. The presence of homologs of benzene in minute quantities would have produced no measurable effects on the thermal properties observed.

V. RESULTS OF MEASUREMENTS

In the following record of these measurements the results have been assembled in the form of tables. An explanation of the mechanism of the reduction of the quantities observed to the properties desired is given in the report on the work on steam.⁶

Three complete sets of α experiments were performed with a large mass and three with a small mass of fluid in the calorimeter. The experiments did not start and stop at exactly the even 10° temperatures so the measured values of Q were corrected to the even intervals for convenience. From curves of $\frac{\Delta Q}{\Delta \theta}$ plotted against temperature, the small corrections to the even 10° points were determined, and these corrections, applied to the measured values of Q , yielded the values of Q_1^2 corrected to the even temperature intervals.

Choosing for example the interval 40° to 50°, the value of the change in α for the liquid was computed for this interval as follows. For each observed value of Q_{40}^{50} there is an observed mass M of fluid in the calorimeter system. To determine the values of the two constants Z and α in the equation.

$$Q_{40}^{50} = Z_{40}^{50} + M\alpha_{40}^{50}$$

the method of least squares was employed. As an indication of the consistency of the results, the value of Z_{40}^{50} so obtained was used for the computation of the value of α indicated by each individual experiment. The tabulated values of α_m are the values obtained by the method of least squares, and the other values of α were computed for the separate determinations as just described. The results of the α experiments are shown in Table 1.

⁶ See footnote 1, p. 881.

TABLE 1.—Results of α experiments

$$\alpha_1^2 = \left[H - L \frac{u}{u' - u} \right]_1^2$$

Temperature interval (°C.)	Methyl alcohol		Ethyl alcohol		Benzene	
	α_1^2	$\alpha_1^2 - \alpha_m$	α_1^2	$\alpha_1^2 - \alpha_m$	α_1^2	$\alpha_1^2 - \alpha_m$
40-50-----	<i>Int. J./g</i>	<i>Int. J./g</i>	<i>Int. J./g</i>	<i>Int. J./g</i>	<i>Int. J./g</i>	<i>Int. J./g</i>
	26.075	—0.005	26.025	—0.012	-----	-----
	26.075	—0.005	26.030	—0.007	-----	-----
	26.089	.009	26.057	.020	-----	-----
	26.087	.007	26.023	—0.014	-----	-----
	26.068	—0.012	26.061	.024	-----	-----
$\alpha_m =$ -----	26.084	.004	26.028	—0.009	-----	-----
50-60-----	26.080	-----	26.037	-----	-----	-----
	26.799	—0.019	26.906	—0.016	18.340	0.037
	26.847	.029	26.918	—0.004	18.290	—0.013
	26.808	—0.010	26.944	.022	18.279	—0.024
	26.807	—0.011	26.908	—0.014	18.280	—0.023
	26.816	—0.002	26.920	—0.002	18.319	.016
$\alpha_m =$ -----	26.829	.011	26.940	.018	18.310	.007
60-70-----	26.818	-----	26.922	-----	18.303	-----
	27.567	.021	27.986	.004	18.546	.010
	27.512	—0.034	27.967	—0.015	18.554	.000
	27.557	.011	27.992	.010	18.546	—0.008
	27.520	—0.026	27.990	.008	18.582	.028
	27.553	.007	27.960	—0.022	18.513	—0.041
$\alpha_m =$ -----	27.564	.018	27.995	.013	18.568	.014
70-80-----	27.546	-----	27.982	-----	18.554	-----
	28.208	—0.004	29.045	.006	18.782	.014
	28.223	.011	29.033	—0.006	18.764	—0.004
	28.204	—0.008	29.026	—0.013	18.757	—0.011
	28.262	.050	29.017	—0.022	18.726	—0.042
	28.176	—0.036	29.073	.034	18.792	.024
$\alpha_m =$ -----	28.197	—0.015	29.041	.002	18.785	.017
80-90-----	28.212	-----	29.039	-----	18.768	-----
	28.866	—0.003	30.026	.005	19.012	.009
	28.874	.005	29.996	—0.025	18.998	—0.005
	28.868	—0.001	30.042	.021	18.999	—0.004
	28.892	.023	29.999	—0.022	18.968	—0.035
	28.854	—0.015	30.058	.037	19.022	.019
$\alpha_m =$ -----	28.862	—0.007	30.007	—0.014	19.019	.016
90-100-----	28.869	-----	30.021	-----	19.003	-----
	29.704	.034	31.316	.021	19.284	.024
	29.651	—0.019	31.309	.014	19.262	.002
	29.656	—0.014	31.259	—0.036	19.235	—0.025
	29.693	.023	31.327	.032	19.295	.035
	29.667	—0.003	31.288	—0.007	19.239	—0.021
$\alpha_m =$ -----	29.650	—0.020	31.269	—0.026	19.247	—0.013
100-110-----	29.670	-----	31.295	-----	19.260	-----
	30.338	.020	32.208	—0.021	19.501	.004
	30.313	—0.005	32.220	—0.009	19.501	.004
	30.302	—0.016	32.258	.029	19.488	—0.009
	30.340	.022	32.209	—0.020	19.504	.007
	30.302	—0.016	32.231	.002	19.490	—0.067
$\alpha_m =$ -----	30.311	—0.007	32.246	.017	19.496	—0.001
	30.318	-----	32.229	-----	19.497	-----

Before continuing further with the reduction of the data from the heat-capacity determinations, the results of the γ experiments will be tabulated. The values of γ were calculated from equation (7), in which γ_1 is the value of γ at the initial temperature and ΔM represents the mass of vapor removed. The quantity $[Z + M_2\alpha]^2$ is that energy quantity involved in a change in calorimeter temperature from the initial to a different final value. The values of Z and α are available

from the results of the α experiments, and that of M_2 , the mass remaining in the calorimeter at the completion of a γ experiment, is known from the weighings. The quantity $\int_1^2 (H - H_1) dM$ represents the energy involved in a change in the temperature of the vapor leaving the calorimeter during an experiment. It is negligibly small under the steady temperature conditions which prevailed during the present work. It is mentioned only for consistency with the exact theory.

The results of the γ experiments are assembled in Table 2. The corrections of the observed values of γ_1 to the desired temperatures involved graphical determinations of $\frac{d\gamma}{d\theta}$. The corrections are very small because the values of θ_1 were so near to the temperatures recorded.

TABLE 2.—Results of γ experiments

$$\gamma = \frac{Lu'}{u' - u}$$

Methyl alcohol			Ethyl alcohol			Benzene							
Temperature (° C.)	γ	$\gamma - \gamma_m$	Temperature, (° C.)	γ	$\gamma - \gamma_m$	Temperature, (° C.)	γ	$\gamma - \gamma_m$					
50	<i>Int. J./g</i>	<i>Int. J./g</i>	50	<i>Int. J./g</i>	<i>Int. J./g</i>	50	<i>Int. J./g</i>	<i>Int. J./g</i>					
	1129.2	—0.1		886.5	—0.4		415.6	—0.3					
	1129.0	—3		885.6	—1.3		415.9	.0					
	1128.8	—5		886.7	—2		415.8	—1					
	1129.4	.1		887.7	.8		416.2	.3					
	1129.2	—1		887.3	.4		416.3	.4					
	1129.6	.3		887.5	.6		415.9	.0					
	1129.7	.4		887.2	.3		$\gamma_m =$	415.9					
	1129.6	.3		887.0	.1								
	1129.6	.3		887.0	.1								
$\gamma_m =$	1129.3	886.9											
64.7	1101.6	—9	70	856.8	.3	80	395.0	—2					
	1102.2	—3		856.0	—5		395.7	.5					
	1102.2	—3		856.5	.0		394.8	—4					
	1101.5	—1.0		856.8	.3		395.1	—1					
	1102.2	—3		856.4	—1		395.7	.5					
	1102.9	.4		856.5	.0		395.1	—1					
	1102.7	.2		856.6	.1		395.2	.0					
	1102.9	.4		856.5	.0		395.4	.2					
	1102.7	.2		856.5	.0		394.9	—3					
	1102.8	.3		$\gamma_m =$	856.5			$\gamma_m =$	395.2				
1103.0	.5	820.9	—4		373.1	—1							
1103.0	.5	820.5	—8		373.0	—2							
1103.0	.5	821.3	.0		373.2	.0							
$\gamma_m =$	1102.5		90	821.8	.5	110	373.6	.4					
	1049.2	—3		821.5	.2		373.3	.1					
	1048.8	—7		821.5	.2		373.4	.2					
	1049.4	—1		821.9	.6		373.0	—2					
	1050.0	.5		821.3	.0		$\gamma_m =$	373.2					
	1049.9	.4		821.3	.0			$\gamma_m =$	373.2				
	1048.6	—9		782.5	—2				$\gamma_m =$	373.2			
	1050.7	1.2		781.7	—1.0					$\gamma_m =$	373.2		
	1049.5			783.2	.5						$\gamma_m =$	373.2	
	1001.7	.1		782.7	.0							$\gamma_m =$	373.2
1000.8	—8	783.1	.4	$\gamma_m =$	373.2								
1001.9	.3	783.2	.5		$\gamma_m =$	373.2							
1001.2	—4	782.7				$\gamma_m =$	373.2						
1002.1	.5	$\gamma_m =$	782.7				$\gamma_m =$	373.2					
1000.8	—8		$\gamma_m =$					782.7	$\gamma_m =$	373.2			
1002.0	.4							$\gamma_m =$		782.7	$\gamma_m =$	373.2	
1002.3	.7			$\gamma_m =$						782.7		$\gamma_m =$	373.2
$\gamma_m =$	1001.6				$\gamma_m =$					782.7			$\gamma_m =$
$\gamma_m =$	1001.6					$\gamma_m =$				782.7			
$\gamma_m =$	1001.6	$\gamma_m =$					782.7			$\gamma_m =$			
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$\gamma_m =$	1001.6						$\gamma_m =$	782.7			$\gamma_m =$		
$\gamma_m =$	1001.6			$\gamma_m =$				782.7				$\gamma_m =$	
$\gamma_m =$	1001.6				$\gamma_m =$			782.7					$\gamma_m =$
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$\gamma_m =$	1001.6				$\gamma_m =$			782.7					$\gamma_m =$
$\gamma_m =$	1001.6					$\gamma_m =$		782.7					
$\gamma_m =$	1001.6	$\gamma_m =$						782.7		$\gamma_m =$			
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$\gamma_m =$	1001.6						$\gamma_m =$	782.7			$\gamma_m =$		
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$\gamma_m =$	1001.6	$\gamma_m =$						782.7		$\gamma_m =$			
$\gamma_m =$	1001.6		$\gamma_m =$					782.7	$\gamma_m =$				
$\gamma_m =$	1001.6						$\gamma_m =$	782.7			$\gamma_m =$		

To reduce the values of α and γ to the desired quantities H and L , it is necessary to evaluate the correction term β throughout the range of the experiments. Since β is small in this range, it is believed that its values can be calculated more accurately from vapor pressure and specific volume data than they could be measured calorimetrically.

All terms in the right-hand member of the equation $\beta = \Theta u \frac{d\pi}{d\Theta}$ were evaluated for each of the substances concerned from the results of measurements made by Young.⁷ Values of $\frac{d\pi}{d\Theta}$ were calculated by differentiation of his vapor pressure equations. Table 3 shows the quantities taken from the work of Young and the values of β computed therefrom at those temperatures where they are needed in the further reduction of the data.

TABLE 3.—Calculation of values of β

$$\beta = \Theta u \frac{d\pi}{d\Theta}$$

[1 liter-atmosphere=101.29 international joules]

Temperature		Methyl alcohol			Ethyl alcohol			Benzene		
θ	Θ	$u \times 10^3$	$\frac{d\pi}{d\Theta}$	β	$u \times 10^3$	$\frac{d\pi}{d\Theta}$	β	$u \times 10^3$	$\frac{d\pi}{d\Theta}$	β
°C.	°K.	Liters/g	Atm./deg.	Int. J./g	Liters/g	Atm./deg.	Int. J./g	Liters/g	Atm./deg.	Int. J./g
0	273.1	1.2345	0.00245	0.08	1.2403	0.00111	0.04	(1.1110)	(0.0020)	(0.06)
10	283.1	1.2489	.00416	.15	1.2534	.00200	.07	1.1243	.00309	.10
20	293.1	1.2637	.00677	.25	1.2669	.00344	.13	1.1380	.00469	.16
25	298.1	1.2713	.00852	.33	1.2738	.00443	.17	1.1449	.00568	.20
30	303.1	1.2790	.01061	.41	1.2808	.00570	.22	1.1520	.00688	.24
40	313.1	1.2948	.01606	.65	1.2953	.00907	.37	1.1664	.00978	.36
50	323.1	1.3111	.02353	1.00	1.3104	.01394	.59	1.1813	.01350	.52
60	333.1	1.3240	.03355	1.48	1.3261	.02073	.92	1.1967	.01814	.72
64.7	337.8	1.3362	.03917	1.77						
70	343.1	1.3405	.04651	2.14	1.3430	.02969	1.38	1.2126	.02383	.99
80	353.1	1.3600	.06302	3.03	1.3609	.04192	2.01	1.2278	.03064	1.33
90	363.1	1.3790	.08359	4.19	1.3791	.05729	2.87	1.2436	.03865	1.75
100	373.1	1.401	.1088	5.69	1.397	.07648	3.99	1.262	.04794	2.26
110	383.1	1.424	.1391	7.59	1.417	.0999	5.42	1.281	.05857	2.87
120	393.1	1.449	.1751	9.97	1.444	.1280	7.27	1.300	.07059	3.61
130	403.1	1.477	.2174	13.11	1.473	.1612	9.69	1.321	.08407	4.53

Table 4 gives the values of L computed from the mean experimental values, γ_m , by the relation $L = \gamma - \beta$.

TABLE 4.—Computation of latent heats

$$L = \gamma - \beta$$

Temperature θ	Methyl alcohol			Ethyl alcohol			Benzene		
	γ	β	L	γ	β	L	γ	β	L
°C.	Int. J./g	Int. J./g	Int. J./g	Int. J./g	Int. J./g	Int. J./g	Int. J./g	Int. J./g	Int. J./g
50	1,129.3	1.0	1,128.3	886.9	0.6	886.3	415.9	0.5	415.4
64.7	1,102.5	1.8	1,100.7						
70				856.5	1.4	855.1			
80							395.2	1.3	393.9
90	1,049.5	4.2	1,045.3	821.3	2.9	818.4			
110	1,001.6	7.6	994.0	782.7	5.4	777.3	373.2	2.9	370.3

⁷ Proc. Roy. Dublin Soc., 12, p. 374; 1910.

To facilitate the interpolation and extrapolation of the values of latent heat, an empirical equation expressing L as a function of θ was fitted to the observed values for each of the substances. The type chosen for these equations was the same as that which proved adequate to represent the experimental values for water. Each equation requires that the latent heat approach zero at the critical temperature θ_c at a negatively infinite rate, and that no real values exist above this temperature. Table 5 gives the values of L calculated from the equations which appear below the columns of figures.

TABLE 5.—Formulation of latent heat values

Temperature θ	Methyl alcohol		Ethyl alcohol		Benzene	
	Latent heat of vaporization					
	Observed	Equation	Observed	Equation	Observed	Equation
$^{\circ}\text{C.}$	<i>Int. J./g</i>	<i>Int. J./g</i>	<i>Int. J./g</i>	<i>Int. J./g</i>	<i>Int. J./g</i>	<i>Int. J./g</i>
0	-----	¹ (1, 200. 1)	-----	(946. 0)	-----	(447. 2)
10	-----	(1, 188. 5)	-----	(936. 2)	-----	(441. 2)
20	-----	(1, 175. 4)	-----	(925. 4)	-----	(435. 0)
25	-----	(1, 168. 4)	-----	(919. 6)	-----	(431. 9)
30	-----	(1, 161. 0)	-----	(913. 5)	-----	(428. 7)
40	-----	(1, 145. 3)	-----	(900. 5)	-----	(422. 1)
50	1, 128. 3	1, 128. 2	886. 3	886. 5	415. 4	415. 4
60	-----	1, 109. 7	-----	871. 3	-----	408. 4
64. 7	1, 100. 7	1, 100. 5	-----	-----	-----	-----
70	-----	1, 089. 8	855. 1	854. 9	-----	401. 3
80	-----	1, 068. 3	-----	837. 3	393. 9	393. 9
90	1, 045. 3	1, 045. 2	818. 4	818. 5	-----	386. 3
100	-----	1, 020. 5	-----	798. 4	-----	378. 4
110	994. 0	994. 1	777. 3	777. 0	370. 3	370. 3
120	-----	(965. 9)	-----	(754. 0)	-----	(361. 9)
130	-----	(935. 7)	-----	(729. 6)	-----	(353. 2)

¹ Values in parentheses are outside the range of the experiments.

For methyl alcohol

$$L = -0.005 (240 - \theta)^2 + 2.60875 (240 - \theta) + 219 (240 - \theta)^{1/4}$$

For ethyl alcohol

$$L = -0.004067 (240 - \theta)^2 + 2.198 (240 - \theta) + 165.83 (240 - \theta)^{1/4}$$

For benzene

$$L = -0.00056185 (290 - \theta)^2 + 0.65028 (290 - \theta) + 74.11 (290 - \theta)^{1/4}$$

The values of the changes in heat content as shown in Table 6 follow directly from the data of Tables 1 and 3, through the equation

$$H \Big]_1^2 = \alpha \Big]_1^2 + \beta \Big]_1^2.$$

TABLE 6.—Computation of changes in heat content

$$H \Big]_1^2 = \alpha \Big]_1^2 + \beta \Big]_1^2$$

Temperature θ	Methyl alcohol			Ethyl alcohol			Benzene		
	$\alpha \Big]_{40}^{\theta}$	$\beta \Big]_{40}^{\theta}$	$II \Big]_{40}^{\theta}$	$\alpha \Big]_{40}^{\theta}$	$\beta \Big]_{40}^{\theta}$	$II \Big]_{40}^{\theta}$	$\alpha \Big]_{50}^{\theta}$	$\beta \Big]_{50}^{\theta}$	$H \Big]_{50}^{\theta}$
$^{\circ}\text{C.}$	<i>Int. J./g</i>	<i>Int. J./g</i>	<i>Int. J./g</i>	<i>Int. J./g</i>	<i>Int. J./g</i>	<i>Int. J./g</i>	<i>Int. J./g</i>	<i>Int. J./g</i>	<i>Int. J./g</i>
40	0.00	0.00	0.00	0.00	0.00	0.00	-----	-----	-----
50	26.08	.35	26.43	26.04	.22	26.26	0.00	0.00	0.00
60	52.90	.83	53.73	52.96	.55	53.51	18.30	.20	18.50
70	80.44	1.49	81.93	80.94	1.01	81.95	36.86	.47	37.33
80	108.66	2.38	111.04	109.98	1.64	111.62	55.62	.81	56.43
90	137.52	3.54	141.06	140.00	2.50	142.50	74.63	1.23	75.86
100	167.20	5.04	172.24	171.30	3.62	174.92	93.89	1.74	95.63
110	197.51	6.94	204.55	203.52	5.05	208.57	113.38	2.35	115.73

Empirical equations in the form of power series have been fitted to these values of $H]_1^2$. These equations are shown in Table 7, together with a comparison of the experimental values with those calculated from the equations.

TABLE 7.—Formulation of heat content values

Temperature θ	Methyl alcohol		Ethyl alcohol		Benzene	
	$H]_{40}^{\theta}$		$H]_{40}^{\theta}$		$H]_{50}^{\theta}$	
	Observed	Equation	Observed	Equation	Observed	Equation
$^{\circ}\text{C.}$	<i>Int. J./g</i>	<i>Int. J./g</i>	<i>Int. J./g</i>	<i>Int. J./g</i>	<i>Int. J./g</i>	<i>Int. J./g</i>
40	0.00	0.00	0.00	0.00	0.00	0.00
50	26.43	26.47	26.26	26.26	0.00	0.00
60	53.73	53.75	53.51	53.57	18.50	18.51
70	81.93	81.91	81.95	81.99	37.33	37.32
80	111.04	111.01	111.62	111.62	56.43	56.43
90	141.06	141.11	142.50	142.55	75.86	75.87
100	172.24	172.26	174.92	174.86	95.63	95.63
110	204.55	204.54	208.57	208.63	115.73	115.75

For methyl alcohol

$$H]_{\theta_1}^{\theta_2} = \left[23.529 \left(\frac{\theta}{10} \right) + 0.2583 \left(\frac{\theta}{10} \right)^2 + 0.010036 \left(\frac{\theta}{10} \right)^3 \right]_{\theta_1}^{\theta_2}$$

For ethyl alcohol

$$H]_{\theta_1}^{\theta_2} = \left[22.648 \left(\frac{\theta}{10} \right) + 0.3053 \left(\frac{\theta}{10} \right)^2 + 0.014233 \left(\frac{\theta}{10} \right)^3 \right]_{\theta_1}^{\theta_2}$$

For benzene

$$H]_{\theta_1}^{\theta_2} = \left[17.184 \left(\frac{\theta}{10} \right) + 0.1008 \left(\frac{\theta}{10} \right)^2 + 0.002462 \left(\frac{\theta}{10} \right)^3 \right]_{\theta_1}^{\theta_2}$$

From the equations for $H]_1^2$ there were obtained values of a quantity $C_{\pi} = \frac{dH}{d\theta}$, defined as the rate of change of the heat content with temperature under saturation conditions. Since the values of $H]_1^2$ as recorded in Table 6 were measured under such conditions, equations for C_{π} were obtained by differentiation of the equations already given for $H]_1^2$. The derived equations and the values of C_{π} calculated at several temperatures are given in Table 8.

TABLE 8.—Computation of specific heat values

$$C_{\pi} = \frac{dH}{d\theta} = C_p \text{ (approximately)}$$

Temperature θ	Methyl alcohol	Ethyl alcohol	Benzene
	C_{π}	C_{π}	C_{π}
$^{\circ}\text{C.}$	<i>Int. J./g. $^{\circ}\text{C.}$</i>	<i>Int. J./g. $^{\circ}\text{C.}$</i>	<i>Int. J./g. $^{\circ}\text{C.}$</i>
40	2.608	2.577	1.838
50	2.686	2.677	1.866
60	2.771	2.785	1.896
70	2.862	2.901	
80	2.959	3.027	1.927
90	3.062	3.160	1.960
100	3.171	3.302	1.994
110	3.286	3.453	2.030

For methyl alcohol

$$C_{\pi} = 2.3529 + 0.5166 \left(\frac{\theta}{10} \right) + 0.003011 \left(\frac{\theta}{10} \right)^2$$

For ethyl alcohol

$$C_{\pi} = 2.2648 + 0.06106 \left(\frac{\theta}{10} \right) + 0.004270 \left(\frac{\theta}{10} \right)^2$$

For benzene

$$C_{\pi} = 1.7184 + 0.02016 \left(\frac{\theta}{10} \right) + 0.0007386 \left(\frac{\theta}{10} \right)^2$$

From specific volume and thermal expansion data it is possible to transform the values of changes in heat content under saturation conditions to values of the changes under a constant pressure of 1 atmosphere. Such transformations have been made and equations for H_1^2 at $p = 1$ atmosphere have been fitted.

From these it is possible to get derived equations for $C_p = \left(\frac{\partial H}{\partial \theta} \right)_{p=1 \text{ atm.}}$ defined as the rate of change of heat content with temperature under a constant pressure of 1 atmosphere. Values of C_p were calculated for each of the three liquids at temperatures below the normal boiling points. A comparison of these values of C_p with the recorded values of C_π showed that the difference between the two was less than 1 part in 500 at every temperature. Since this difference is believed to be within the error involved in deriving values of specific heat from measured values of α , the recorded values of C_π are not sensibly different from the values of C_p as indicated by these experiments.

The specific volumes of the saturated vapors can be calculated from the relation $\gamma = \theta u' \frac{d\pi}{d\theta}$ to the degree of precision of our knowledge of $\frac{d\pi}{d\theta}$. The values of u' thus computed are shown in Table 9. The values of $\frac{d\pi}{d\theta}$ are calculated from Young's vapor pressure equations and the values of γ result from the present investigation.

TABLE 9.—Computation of specific volumes

$$u' = \frac{\gamma}{\theta \frac{d\pi}{d\theta}}$$

Temperature		Methyl alcohol			Ethyl alcohol			Benzene		
θ	Θ	γ	$\frac{d\pi}{d\theta}$	u'	γ	$\frac{d\pi}{d\theta}$	u'	γ	$\frac{d\pi}{d\theta}$	u'
$^{\circ}\text{C.}$	$^{\circ}\text{K.}$	<i>L.-atm./g</i>	<i>Atm./deg</i>	<i>L./g</i>	<i>L.-atm./g</i>	<i>Atm./deg</i>	<i>L./g</i>	<i>L.-atm./g</i>	<i>Atm./deg.</i>	<i>L./g</i>
0	273.1	11.85	0.00245	17.71	9.340	0.00111	30.81	4.416	(0.0020)	8.085
10	283.1	11.74	.00416	9.97	9.243	.00200	16.32	4.356	.00309	4.980
20	293.1	11.61	.00677	5.851	9.137	.00344	9.062	4.298	.00469	3.127
25	298.1	11.54	.00852	4.544	9.081	.00443	6.877	4.266	.00586	2.442
30	303.1	11.47	.01061	3.567	9.020	.00570	5.221	4.235	.00688	2.031
40	313.1	11.31	.01606	2.249	8.894	.00907	3.132	4.171	.00978	1.362
50	323.1	11.14	.02353	1.465	8.757	.01394	1.944	4.106	.01350	.9413
60	333.1	10.97	.03355	.9816	8.611	.02073	1.247	4.039	.01814	.6684
70	343.1	10.78	.04651	.6755	8.454	.02989	.8244	3.971	.02383	.4857
80	353.1	10.58	.06302	.4755	8.287	.04192	.5599	3.902	.03064	.3607
90	363.1	10.36	.08359	.3413	8.110	.05729	.3899	3.831	.03865	.2730
100	373.1	10.13	.1088	.2495	7.922	.07648	.2776	3.759	.04794	.2102
110	383.1	9.89	.1391	.1856	7.727	.0999	.2019	3.684	.05857	.1642
120	393.1	9.64	.1751	.1401	7.517	.1280	.1494	3.608	.07059	.1300
130	403.1	9.37	.2174	.1069	7.299	.1612	.1123	3.542	.08407	.1045

Table 10 has been prepared to summarize the thermal properties of these three saturated fluids. The values of π are from the data of Young. The values of u at temperatures below the normal boiling points are from density determinations as recorded in the International Critical Tables, volume 3, pages 27 to 30. Values of u above the boiling points are those determined by Young. The values of u' are computed as shown in Table 9. The results of the present

investigation are extrapolated down to 0° C. and up to 130° C. The value of H has been arbitrarily chosen as 0° at 0° C. for each liquid. For the benzene which freezes at about 5° above this temperature the datum $H=0$ is for the undercooled liquid. The heat of fusion is therefore not included in the tabulated values.

It is hoped that this table may prove useful as a working table for those who are concerned with the thermal properties of any one of these saturated fluids.

TABLE 10.—*Thermal properties of methyl alcohol, ethyl alcohol, and benzene at saturation*

METHYL ALCOHOL

Temperature θ	Vapor pressure π	Specific volume		Heat content Liquid H	Latent heat L	Heat content Vapor H'
		Liquid $u \times 10^3$	Vapor u'			
°C.	Atmospheres	Liters/g	Liters/g	Int. J./g	Int. J./g	Int. J./g
0	0.0389	1.234	17.71	0.0	1,200.1	1,200.1
10	.0713	1.249	9.97	23.80	1,188.5	1,212.3
20	.1251	1.264	5.851	48.17	1,175.4	1,223.6
25	.1632	1.271	4.544	60.59	1,168.4	1,229.0
30	.2109	1.279	3.567	73.18	1,161.0	1,234.2
40	.3427	1.295	2.249	98.89	1,145.3	1,244.2
50	.5388	1.311	1.465	125.4	1,128.2	1,253.6
60	.8255	1.324	.9816	152.6	1,109.7	1,262.3
70	1.219	1.340	.6755	180.8	1,089.3	1,270.6
80	1.764	1.360	.4755	209.9	1,068.3	1,278.2
90	2.493	1.379	.3413	240.0	1,045.2	1,285.2
100	3.451	1.401	.2495	271.2	1,020.5	1,291.7
110	4.686	1.424	.1856	303.4	994.1	1,297.5
120	6.252	1.449	.1401	336.9	965.9	1,302.8
130	8.209	1.477	.1069	371.6	935.7	1,307.3

ETHYL ALCOHOL

0	0.0162	1.240	30.81	0.0	946.0	946.0
10	.0312	1.253	16.32	22.97	936.2	959.2
20	.0579	1.267	9.062	46.63	925.4	972.0
25	.0771	1.274	6.877	58.75	919.6	978.4
30	.1023	1.281	5.221	71.08	913.5	984.6
40	.1756	1.295	3.132	96.39	900.5	996.9
50	.2892	1.310	1.944	122.7	886.5	1,009.2
60	.4608	1.326	1.247	150.0	871.3	1,021.3
70	.7117	1.343	.8244	178.4	854.9	1,033.3
80	1.068	1.361	.5599	208.0	837.3	1,045.3
90	1.561	1.379	.3899	239.9	818.5	1,058.4
100	2.227	1.397	.2776	271.2	798.4	1,069.6
110	3.105	1.417	.2019	305.0	777.0	1,082.0
120	4.241	1.444	.1494	340.3	754.0	1,094.3
130	5.682	1.473	.1123	377.3	729.6	1,106.9

BENZENE

0	0.0349	1.111	8.805	0.0	447.2	447.2
10	.0598	1.124	4.980	17.29	441.2	458.5
20	.0982	1.138	3.127	34.79	435.0	469.8
25	.1235	1.145	2.442	43.59	431.9	475.5
30	.1556	1.152	2.031	52.52	428.7	481.2
40	.2383	1.168	1.262	70.51	422.1	492.6
50	.3539	1.181	.9413	88.75	415.4	504.2
60	.5113	1.197	.6684	107.3	408.4	508.6
70	.7203	1.213	.4857	126.1	401.3	527.4
80	.9916	1.228	.3607	145.2	393.9	539.1
90	1.337	1.244	.2730	164.6	386.3	550.9
100	1.769	1.262	.2102	184.4	378.4	562.8
110	2.300	1.281	.1642	204.5	370.3	574.8
120	2.945	1.300	.1300	225.0	361.9	586.9
130	3.717	1.321	.1045	245.8	353.2	599.0

VI. DISCUSSION OF ACCURACY

An estimate of the accuracy of the tabulated values of H and L within the range of the experiments has been made on a basis similar to that outlined in the report on the properties of steam. The systematic errors in calorimetry are believed to be essentially the same in both sets of experiments.

By a study of the factors which enter into the measurements, a figure was assigned to each which represents an estimate of the outstanding systematic error, after all known corrections have been applied. In addition to these, corresponding figures were deduced which represent the error in both the α and the γ due to accidental errors in the measurements. An estimate was also made of the probable error in the calculated values of β . The density determinations furnish a basis for estimating the error which may be present on account of impurities in the liquids investigated.

These estimates were combined to obtain a value for the uncertainty in the final tabulated results. On this basis it is believed that more precise determinations on compounds of a higher degree of purity would yield values of H and L differing by less than 1 part per 1,000 from those of the present investigation in the range from 40° to 110° C.

VII. COMPARISON WITH PREVIOUS WORK

1. HEAT CAPACITY

The results of calorimetric determinations of heat capacity have usually been recorded in terms of specific heats. For comparison of the present results with those of other observers the calculated values of specific heats can be compared directly, or, where equations are available, the values of changes in heat content can be calculated from integrated specific heat equations. The latter method would have been followed if the temperature ranges of the various experiments had overlapped sufficiently. However, the earlier work is confined to the range well below the normal boiling points, and hence covers regions in general, below that of the present investigation.

The values of specific heat indicated by the present work have been extrapolated down to 20° C. for purposes of comparison. The extrapolated values of this derived quantity involve considerable uncertainties and should not be given a great deal of weight in the selection of the best values below 40° C. A graphical comparison of previously published values of specific heats with those of the present work is given in Figure 2. This summary includes the experimental results of Bose,⁸ Kelley,⁹ Williams,¹⁰ Daniels,¹⁰ Forch,¹¹ Mills and MacRae,¹² Dejaridin,¹³ Tréhin,¹⁴ and Andrews, Lynn, and Johnston.¹⁵

⁸ Z. phys. Chem., 58, p. 585; 1907.

⁹ J. Am. Chem. Soc., 51, p. 180; 1929; and 51, p. 779; 1929.

¹⁰ J. Am. Chem. Soc., 46, p. 903; 1924.

¹¹ Annalen der Physik, 317, p. 202; 1903.

¹² J. phys. Chem., 14, p. 797; 1910.

¹³ Annales de Physique, 11, p. 253; 1919.

¹⁴ Annales de Physique, 15, p. 240; 1921.

¹⁵ J. Am. Chem. Soc., 48, p. 1274; 1926.

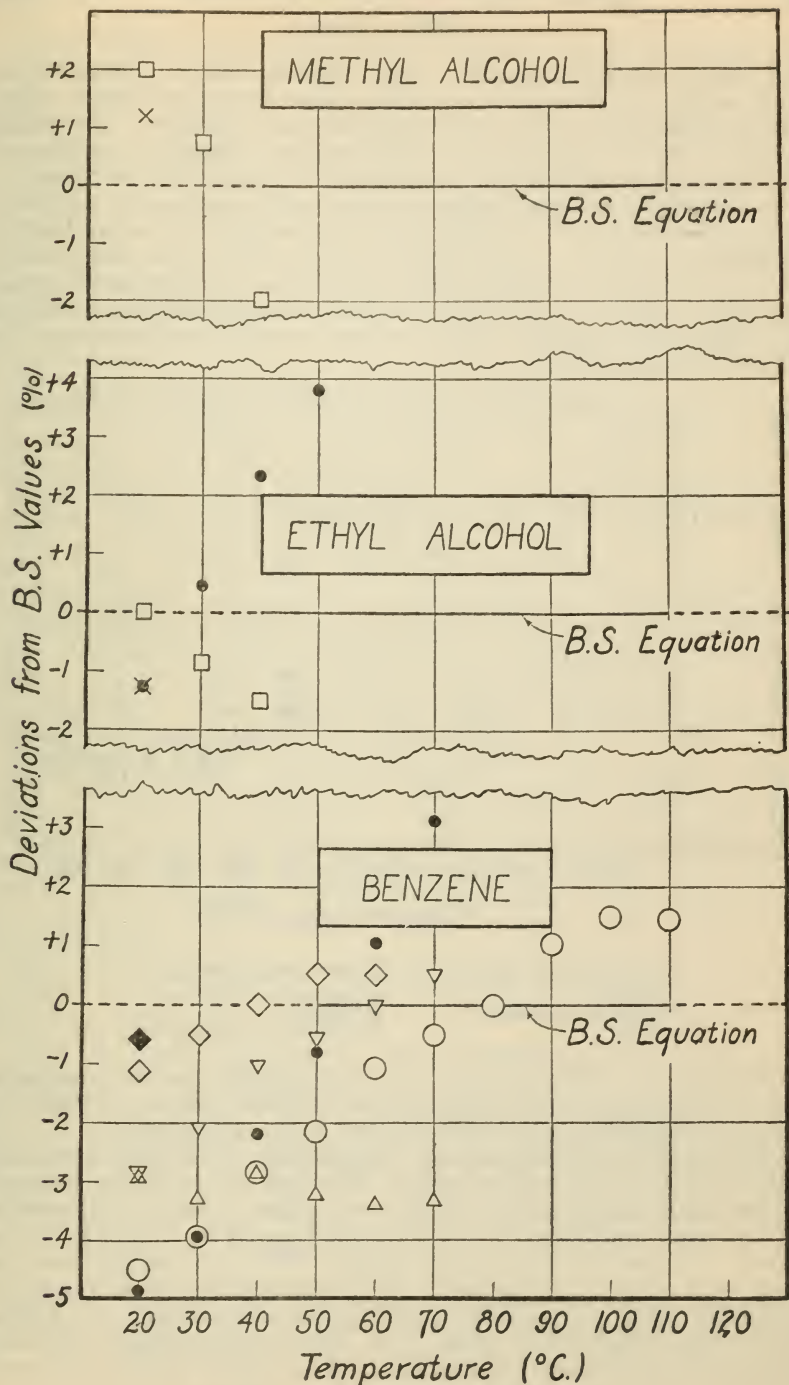


FIGURE 2.—Comparison of specific heats

- | | |
|-------------------------|--------------------------------|
| □ Bose. | △ Mills and MacRea. |
| × Kelley. | ◇ Dejardin. |
| ● Williams and Daniels. | ▽ Tréhin. |
| ◆ Forch. | ○ Andrews, Lynn, and Johnston. |

2. LATENT HEAT

In the following comparison of the various values of latent heats which appear in the literature, those data based on direct calorimetric measurements will be given first consideration. The values which have been calculated from other types of measurements through the Clapeyron relation are not considered of comparable precision.

An attempt has been made to reduce the previously published values of latent heats to present international joules for purposes of comparison. Such a reduction involves considerable uncertainty, but this is believed to be within the limit of error involved in the measurements themselves. It is not possible to make reliable estimates of the purity of the liquids used by various investigators because of the lack of published details.

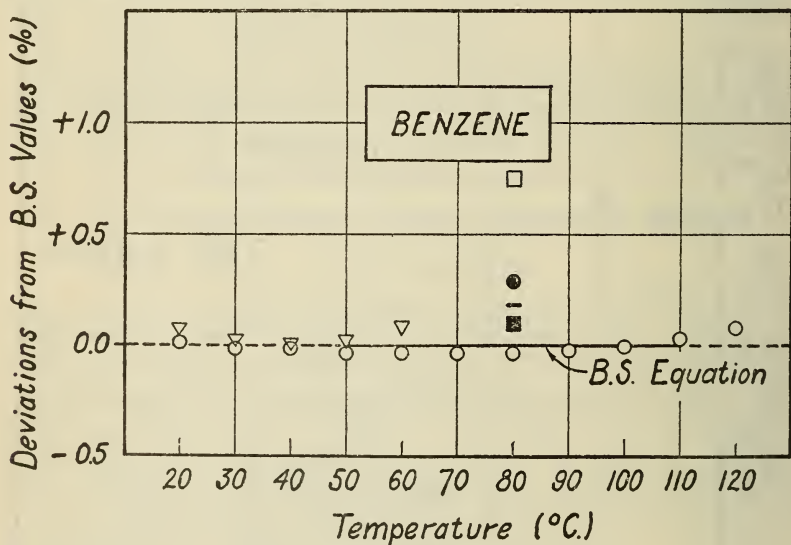


FIGURE 3.—Comparison of latent heats of benzene

- | | |
|---------------------------|--------------------------------|
| □ Brown. | ■ Nagornow and Rotinjanz. |
| ▽ Griffiths and Marshall. | ● Mathews. |
| — Tyrer. | ○ Sutcliffe, Lay and Prichard. |

The data on methyl alcohol and ethyl alcohol are too meager to warrant exhibition on deviation charts. Figure 3 gives a comparison of the experimental values of the latent heat of benzene.

The literature records two determinations of the latent heat of methyl alcohol at its boiling point. The first of these is by Brown¹⁶ and the second by Mathews.¹⁷ Brown's value is reported in calories and has been multiplied by 4.199 and decreased by 1 part in 512 to convert to present international joules. When so transformed, his value for L at 64.7° C. becomes 1,101.6 international joules per gram. Mathews' value for L at the same temperature reduces to 1,100.5 international joules per gram. The latter is identical with that indicated by the present experiments. For methyl alcohol the agreement among the few results is satisfactory.

¹⁶ J. Chem. Soc., 83, p. 987; 1903.

¹⁷ J. Am. Chem. Soc., 48, p. 562; 1926.

Three values for the latent heat of ethyl alcohol at its boiling point are recorded. Marshall and Ramsay¹⁸ determined the ratio of the latent heat of absolute ethyl alcohol at its boiling point to that of benzene at the same temperature. This ratio, 2.293, together with the value of Griffiths and Marshall for the latter, indicates a latent heat for the alcohol of 902.7 international joules per gram at 80° C.

A determination by Brown,¹⁹ when transformed as already described gives a value of L for ethyl alcohol at 80° C. of 903.5 international joules per gram. The work of Mathews²⁰ gives the value 840.3 international joules per gram for L at the same temperature. The density which he records for his sample indicates that it may have contained nearly 0.2 per cent of water. The comparative value indicated by the present experiments is 837.3 international joules per gram. The alcohol samples which gave values of the latent heat of over 900 joules per gram were probably not dry. The agreement with the value of Mathews is moderately good, the difference probably being largely due to the small amount of water in his sample.

Considerable data are available on the heat of vaporization of benzene. These will be discussed in chronological order.

The work of Griffiths and Marshall²¹ at temperatures from 20° to 50° C. gave values which were represented by the equation $L = 107.05 - 0.158 \theta$, in terms of a calorie defined as 4.199 joules. To convert to present international joules, the coefficients of the right-hand member have been multiplied by 4.199 and decreased by 1 part in 512, because of the changes in electrical units since the work was performed. The transformed equation which gives values of L in international joules is $L = 448.6 - 0.66 \theta$.

The work of Tyrer²² gives a value of the latent heat of benzene at its boiling point in terms of a calorie based on indications of a voltmeter and silver voltameter. From the date of this work it is assumed that the units were those established by international agreement in 1910. On this basis the electrical equivalent of the calorie used by Tyrer becomes 4.188 international joules. His value for the latent heat of benzene at 80° C. then becomes 394.8 international joules per gram.

Nagornow and Rotinjanz²³ report a group of determinations which yielded a mean value of 393.4 international joules per gram as the latent heat of benzene at 80° C.

From the work of Mathews²⁴ the value 395.1 international joules per gram at 80° C. is indicated.

Sutcliffe, Lay and Prichard²⁵ determined the latent heat of benzene from its boiling point up to 152° C., and by combining their data with those of Griffiths and Marshall, fitted an equation to the experimental values in the range 20° to 150° C. Transformed to yield values of L in international joules per gram, this equation becomes

$$L = 447.72 - 0.6163\theta - 6.141 \times 10^{-4}\theta^2 - 1.509 \times 10^{-6}\theta^3$$

The agreement among the values of L for benzene in the entire range is very gratifying. The equation of Sutcliffe, Lay, and Prichard, which represents the data of Griffiths and Marshall as well as

¹⁸ Phil. Mag., **41**, p. 38; 1896.

¹⁹ J. Chem. Soc., **87**, p. 265; 1905.

²⁰ See footnote 17, p. 898.

²¹ Phil. Mag. **41**, p. 1; 1896.

²² J. Chem. Soc., **99**, p. 1633; 1911.

²³ Z. phys. Chem., **77**, p. 700; 1911.

²⁴ See footnote 17, p. 898.

²⁵ Proc. Roy. Soc. London, **115**, p. 88; 1927.

their own, yields values which are everywhere in agreement with those calculated from our equation, within the limit of our own experimental error.

For all three of the fluids the values of L derived from the present measurements differ from those calculated from the data of Young with the aid of the Clapeyron relation by approximately 1 part in 50 at the boiling points and 1 part in 100 at 110° C.

VIII. SUMMARY

Thermal properties of methyl alcohol, ethyl alcohol, and benzene were investigated in the temperature range 40° to 110° C. Determinations were made of the latent heats of vaporization and the changes in heat content of the saturated fluids in this range. The results have been assembled in the form of tables and empirical equations have been fitted to the experimental values to aid in the application of the data. A working table of the thermal properties of these three fluids at saturation conditions has been prepared from the present and previously published data.

IX. ACKNOWLEDGMENT

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