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RELATION OF COMPOSITIONS AND HEATS OF SOLU-TION OF PORTLAND CEMENT CLINKER

By Herbert Insley, Einar P. Flint, Edwin S. Newman, and J. Arthur Swenson

ABSTRACT

The results of chemical and microscopic analyses and heat-of-solution measurements on samples of commercial portland cement clinker are reported. Differences between quantitative microscopic analysis and compound composition calculated from chemical analysis have systematic relationships with chemical composition of the clinker. The heats of solution calculated from compound composition by microscopic and by chemical analysis show fair correspondence with the observed heats of solution. Assumptions on which both methods of calculation are based are shown to be somewhat faulty.

CONTENTS

\mathbf{P}	age
I. Introduction	355
II. Materials	356
II. Methods and apparatus	356
1. Preparation of samples	356
2. Chemical analysis	357
3 Microscopic examination	357
4 Heat of solution	358
IV. Results	358
1 Quantitative determinations	358
2. Qualitative microscopic examination	359
(a) $3C_{aO}$ SiO _a	359
(b) $2C_{9}O_{1}SiO_{2}$	360
(c) "Light interstitial" material	360
(d) "Dark interstitial" material	361
(a) Free MgO	361
(f) Free CaO	362
V Discussion	362
VI Summary	364
II References	365
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I. INTRODUCTION

It has long been recognized $[1]^{1}$ that many of the properties of concrete are dependent in part on the relative proportions of the compounds which are present. Determinations of the contributions of individual compounds to the properties of cements and concretes [2, 3] have been based on the assumptions of previous investigators that the cement clinker is completely crystalline and that no more than six phases—3CaO.SiO₂, 2CaO.SiO₂, 3CaO.Al₂O₃, 4CaO.Al₂O₃. Fe₂O₃, free CaO, and free MgO (periclase)—are present.

¹ Figures in brackets indicate the literature references at the end of this paper.

356 Journal of Research of the National Bureau of Standards Vol. 21

The accuracy of such methods depended in large part on the validity of these two assumptions. The recent development of a method for the microscopic examination of polished and etched specimens of portland cement clinker using reflected light [4, 5] permits ready distinction of the constituents and precise determination of the boundaries of individual crystals. The combination of this method with one for measuring the relative amounts of the different constituents makes possible a quantitative and qualitative comparison of the phases actually present in the clinker with those calculated from the chemical analyses.

It is the purpose of the present paper to make such comparisons for a series of commercial cement-clinker samples 2 and to compare the heats of solution obtained by calculation from both microscopic measurement and chemical analysis with the experimentally determined heats of solution.

II. MATERIALS

Twenty-six different samples of clinker were available for this study from five different sources. These included ten samples of "modified low-heat" (type B) clinkers representative of nine brands of cement used in dam construction by the Tennessee Valley Authority (designated by index letter T), three samples of clinker representative of "modified low-heat" cements used in the construction of the Tygart River Dam, West Virginia (designated with index letter W), and two samples of clinker representative of "low-heat" cements used in the construction of Boulder Dam (index letter B). A fourth source was a group of 50 samples of clinker obtained through the generous cooperation of Dalton G. Miller, senior drainage engineer, U. S. Department of Agriculture (index letter M). Ten samples showing wide variations in composition were chosen from this group after a study of the analyses of the corresponding cements. A single sample obtained from the manufacturer (index letter P) is listed because its Al_2O_3 and Fe_2O_3 content is low and its CaO content high.

The pure compounds used for the determination of heat of solution were obtained from several sources. Tricalcium aluminate and $4CaO.Al_2O_3.Fe_2O_3$, which were procured from William Lerch, were examined microscopically and found to be essentially homogeneous. Samples of CaO and MgO were obtained by heating the chemically pure carbonates at about 1,400° C and $\beta 2CaO.SiO_2$ was made by heating CaCO₃ and SiO₂ in the proper proportions together with an amount of H₃BO₃ sufficient to give 0.2 percent of B₂O₃ in the final product.

III. METHODS AND APPARATUS

1. PREPARATION OF SAMPLES

The samples of commercial clinker weighed from 1 to 2 kg. About one-third of each sample was so crushed as to avoid the production of a large amount of fine material and then sieved. The material passing a No. 4 and retained on a No. 14 sieve was used for the experiments, one portion being reserved for chemical analysis, another for microscopic examination and a third for heat-of-solution measurements.

² Some preliminary quantitative results on a small number of clinker samples were given in a paper by Swenson and Flint [6].

2. CHEMICAL ANALYSIS

The usual methods of quantitative analysis were used for all determinations except those of the alkalies, in which case the J. Lawrence Smith method of decomposition was followed by the determination of Na₂O by precipitation as sodium zinc uranyl acetate and of K₂O as potassium chloroplatinate. Free CaO was determined by the ammonium-acetate method [7].

3. MICROSCOPIC EXAMINATION

For examination in polished etched preparations by reflected light the crushed clinker sample was placed in a shell vial of about 1.5 cm inside diameter and immersed in Bakelite BR 0014 liquid resinoid. The preparation was evacuated in a vacuum desiccator by means of a faucet aspirator for 2 or 3 hours and then heated in an oven at about 80° C for about 15 hours. The temperature was then raised to 100° C and the heating continued about 7 hours or until the Bakelite was thoroughly hardened. After breaking the vial away, the lower surface of the preparation was ground down with No. 150 silicon carbide and water on a rotating lap until the clinker grains were exposed. Final grinding was done by hand with emery and alcohol on a slab of plate glass. The specimen was carefully washed with alcohol and polished with rouge and alcohol on a canvas-covered disk rotating at about 1,200 rpm. The polished sections were examined with a vertical illuminator [5].

A Wentworth recording micrometer [8] was used for quantitative microscopic analysis. This instrument has five micrometer screws. each one of which moves the specimen independently across the field beneath the reference cross hair in the eyepiece. The micrometer screw assigned to a particular constituent (phase) in the clinker is used for traversing grains of that constituent. The readings on the micrometer heads at the end of a complete traverse record the total linear intercepts for the different constituents. A series of traverses were made on each specimen, consecutive traverses being spaced at constant intervals. The specimens were of such a size that 11 traverses, 1 mm apart, could be made. Assuming uniform distribution of constituents of sufficiently small grain size, the ratios of the linear intercepts of the constituents are equal to the volumetric ratios of the constituents in the specimen. The average of the micrometer readings on five different preparations was taken for the analysis of each The average deviations from the mean were less than sample brand. ± 2 percent for most samples. In recalculating volume percentages to weight percentages, the density values were as follows: $\beta 2CaO.SiO_2$, 3.28 [9]; 3CaO.SiO₂, 3.13 [10]; 4CaO.Al₂O₃.Fe₂O₃, 3.77 [10]. Because the composition of the glass phase is variable and indeterminable, a value of 3.00 for the density of 3CaO.Al₂O₃, found by averaging two previously determined values [10, 11] was used for the total "dark interstitial" material.

The preparations were first etched with water for 2 seconds, immediately rinsed with alcohol and dried. This etching served to distinguish free MgO, free CaO, and crystalline "dark interstitial" material [12] from the rest of the clinker constituents. After quantitative microscopic analysis for these three constituents, the preparation was etched for 3 seconds in a 1-percent alcoholic solution of HNO₃ to differentiate 2CaO.SiO₂, 3CaO.SiO₂, 4CaO.Al₂O₃.Fe₂O₃, and total "dark interstitial" material.

As a part of the qualitative examination, all samples were examined petrographically mounted as powders in liquids of known refractive index. Thin sections and polished thin sections [12] were also made of a few samples.

4. HEAT OF SOLUTION

The heats of solution of the clinker samples and of the pure compounds were determined at 25° C with an isothermal calorimeter previously described [13, 14], in a solvent consisting of a mixture of 648.5 g of 2. 500 \pm 0.002 N HNO₃ and 11.5 g of reagent quality HF (48 percent). All experimental heats of solution were calculated on an ignition-loss-free basis. The values of the heats of solution of the pure compounds which were used in the computation of the heats of solution of the clinkers as derived from chemical and microscopic analysis are given in table 1. Differences between these values and those given by Lerch and Brownmiller [15] for the same compounds may be attributed to differences in calorimeters and to volumes and concentrations of the solvents used. In calculating the heat of solution of glass, a value of 700 cal/g was used. This value represents an approximate mean of the values reported by Lerch and Brownmiller [15] for glasses with the same range in Al₂O₃/Fe₂O₃ ratios as the clinker samples in the present paper.

Compound	Heat of so- lution	Ignition loss
3CaO.SiO2	cal/g 639 572	Percent 0.51 .71
4CaO.Al ₂ O ₃ .Fe ₂ O ₃	592 799	. 14
MgO	876 848	(a) (a)

TABLE 1.—Heats of solution of pure compounds

^a MgO and CaO were freshly ignited.

IV. RESULTS

1. QUANTITATIVE DETERMINATIONS

The results of chemical analysis, quantitative microscopic analysis and heat-of-solution determinations are given in table 2. In order to facilitate comparison of results, the values for corresponding constituents as found by calculation of the compound composition according to the Bogue method [16, 17] and by microscopic analysis are given in adjacent columns. The designations C_3S (3CaO.SiO₂) and C_2S (2CaO.SiO₂) are used for both calculated compound composition and microscopic analysis. The constituent designated "light interstitial" by microscopic analysis is considered equivalent to C_4AF (4CaO.Al₂O₃.Fe₂O₃) by calculation, and the constituent designated "total dark interstitial" by microscopic analysis is considered the nearest equivalent to C_3A (3CaO.Al₂O₃) by calculation. The values given in the column headed "crystalline dark interstitial" are for

TABLE 2.—Compositions and heats of solution of commercial clinker samples

[All quantities excepting oxide composition are calculated on an ignition-loss-free basis]

Oxide composition					Oxide composition								CaO		C ₃ S			C ₂ S		Lig	ht interst	itial	Total	dark inte	erstitial	Dark in	terstitial		Heat	t of soluti	ion •	
Clinker	Source ª	Loss on igni- tion	SiO2	Fe ₂ O ₃	Al ₂ O ₃	CaO	SO3	Na2O	K 20	MgO	Free MgO (micro- scopic)	Chemi- cal	Micro- scopic	Calcu- lated ^b	Micro- scopic	Differ- ence	Calcu- lated b	Micro- scopic	Differ- ence	Calcu- lated C4AF b	Micro- scopic	Differ- ence	Calcu- lated C ₃ A ^b	Micro- scopic	Differ- ence	Crys- tal- line ^f	Glass f	Glass (Lerch method)	Ob- served	Calcu- lated from micro- scopic analy- sis °	Calcu- lated from com- pound compo- sition ^b	Al ₂ O ₃ Fe ₂ O ₃ ratio
1 2	$\begin{array}{c} T \\ T \\ B \\ W \\ B \end{array}$	% 0.25 .22 .97 .50 .97	$\begin{array}{c} 9\% \\ 22.02 \\ 21.98 \\ 23.62 \\ 20.66 \\ 22.16 \end{array}$	9% 4.90 5.99 5.90 6.84 5.81	% 4. 20 5. 35 5. 38 6. 22 5. 38	$\begin{array}{c} \% \\ 63.86 \\ 64.40 \\ 61.74 \\ 62.46 \\ 60.02 \end{array}$	% 0.23 .15 .07 .69 .07	% 0.07 .04 .83 .29 .92	$\% \\ 0.27 \\ .19 \\ .48 \\ .64 \\ .26$	$\% \\ 4.31 \\ 1.61 \\ 0.70 \\ 1.55 \\ 4.52 \end{cases}$	$\begin{matrix} \% \\ 2^{1} 2^{1} 2^{1} 4 \\ <^{1} 4 \\ <^{1} 4 \\ <^{1} 4 \\ 3 \\ \end{matrix}$	% 0.8 .1 0 .5 .05	% 1/2 <1/4 <1/4 <1/4 <1/4	$ \begin{array}{c} 6\% \\ 52.8 \\ 49.8 \\ 27.3 \\ 41.0 \\ 39.0 \end{array} $	% 48 46 30 38 37		% 26.3 25.6 48.1 29.0 32.9	% 29 27 43 27 33	$31 \\ -5 \\ -2 \\ 0$	% 14. 9 18. 2 18. 2 21. 0 18. 0	$\frac{\%}{18}$ 25 20 30 23	3 7 2 9 5	% 3.0 4.1 4.3 5.1 4.3	% 2 2 7 5 4	$ \begin{array}{c} -1 \\ -2 \\ 3 \\ 0 \\ 0 \end{array} $		$\begin{matrix} \% \\ 1\frac{1}{2} \\ 2 \\ 3 \\ 4\frac{1}{2} \\ 2\frac{1}{2} \end{matrix}$	% 3 (d) (d) 5	cal/g 632 625 603 616 615	cal/g 621 610 610 625 618	cal/g 629 620 598 613 618	0. 80 . 80 . 9 . 9 . 9
6 7 8 9 10	$\begin{bmatrix} T \\ T \\ T \\ T \\ T \\ T \end{bmatrix}$	$\begin{array}{c} .83\\ .36\\ 3.11\\ 0.41\\ .12\end{array}$	$\begin{array}{c} 22.16\\ 21.03\\ 22.20\\ 20.31\\ 21.40 \end{array}$	$5.21 \\ 5.01 \\ 3.80 \\ 5.13 \\ 4.90$	$\begin{array}{r} 4.77 \\ 5.08 \\ 4.08 \\ 5.77 \\ 5.50 \end{array}$	$\begin{array}{c} 63.\ 18\\ 63.\ 14\\ 62.\ 52\\ 62.\ 59\\ 62.\ 30\end{array}$	25 . 47 . 12 . 78 . 58	.17 .12 .07 .18 .15	.31 .48 .42 1.16 0.31	3. 08 4. 39 3. 73 3. 73 4. 78	$\begin{array}{c} 1^{1}_{2}\\ 2^{1}_{2}\\ 1^{1}_{2}\\ 2^{1}_{2}\\ 2^{1}_{2}\\ 2^{1}_{2}\\ 2^{1}_{2}\end{array}$.4 1.0 1.6 0.5 .1	$ \begin{array}{c} <^{1}_{4} \\ 1 \\ <^{1}_{4} \\ <^{1}_{4} \\ <^{1}_{4} \\ <^{1}_{4} \end{array} $	$\begin{array}{r} 46.7\\ 48.3\\ 46.7\\ 45.2\\ 43.9\end{array}$	$54 \\ 52 \\ 50 \\ 51 \\ 46$	$ \begin{array}{c} 7 \\ 4 \\ 3 \\ 6 \\ 2 \end{array} $	$\begin{array}{c} 28.9\\ 24.7\\ 30.4\\ 25.7\\ 28.4\end{array}$	23 22 27 21 28.	$ \begin{array}{r} -6 \\ -3 \\ -3 \\ -5 \\ 0 \end{array} $	$15.9 \\ 15.2 \\ 11.9 \\ 15.5 \\ 14.9$	$ \begin{array}{r} 19 \\ 20 \\ 18 \\ 22 \\ 21 \end{array} $	3 5 6 6 6	$\begin{array}{c} 4.1 \\ 5.1 \\ 4.7 \\ 6.7 \\ 6.5 \end{array}$	$\begin{array}{c c} & 2^{1}_{1/2} \\ & 2^{1}_{1/2} \\ & 3 \\ & 3^{1}_{1/2} \\ & 2^{1}_{1/2} \end{array}$	-2 -3 -2 -3 -4	$(1)^{1/2}_{1/4}$ $(1)^{1/2}_{1/2}$ $1^{1/2}_{1/2}$	$\begin{array}{c c} 2 \\ 2^{1/2} \\ 2^{1/2} \\ 2^{1/2} \\ 2^{1/2} \\ 2 \end{array}$	(d) (d) 6 3		$\begin{array}{c} 619 \\ 624 \\ 619 \\ 623 \\ 618 \end{array}$. 99 1. 0 1. 0 1. 1 1. 1 1. 1
11 12 13 14 15	$\begin{bmatrix} T \\ T \\ T \\ W \\ W \end{bmatrix}$	$\begin{array}{c c} .36\\ .35\\ 1.99\\ 0.66\\ .47\end{array}$	$\begin{array}{c} 21.\ 10\\ 23.\ 52\\ 22.\ 50\\ 21.\ 76\\ 22.\ 26\end{array}$	$\begin{array}{r} 4.\ 90\\ 4.\ 31\\ 4.\ 40\\ 5.\ 12\\ 5.\ 05\end{array}$	5.50 4.81 5.38 6.30 6.33	$\begin{array}{c} 65.\ 26\\ 63.\ 94\\ 64.\ 10\\ 64.\ 34\\ 63.\ 24 \end{array}$.07 .10 .06 .32 .73	.13 .17 .07 .08 .11	.46 .23 .23 .44 .66	$\begin{array}{c} 2.\ 27\\ 2.\ 52\\ 1.\ 22\\ 0.\ 96\\ 1.\ 24 \end{array}$	$\begin{array}{c} 1/2 \\ 1/2 \\ 1/1/2 \\ $.9 .5 .8 .8	$\begin{vmatrix} 1/2 \\ < 1/4 \\ < 1/4 \\ 1/2 \\ 1 \end{vmatrix}$	57. 040. 544. 342. 233. 5	$ \begin{array}{r} 60 \\ 42 \\ 50 \\ 47 \\ 35 \end{array} $	$ \begin{array}{c} 3 \\ 1 \\ 6 \\ 5 \\ 1 \end{array} $	17.737.132.331.139.0	$ \begin{array}{r} 11 \\ 33 \\ 29 \\ 24 \\ 34 \end{array} $	$ \begin{array}{r} -7 \\ -4 \\ -3 \\ -7 \\ -5 \end{array} $	$\begin{array}{c} 14.\ 9\\ 13.\ 1\\ 13.\ 6\\ 15.\ 6\\ 15.\ 4\end{array}$	$23 \\ 20 \\ 18 \\ 24 \\ 25$	8 7 4 8 10	$\begin{array}{c} 6.5 \\ 5.7 \\ 7.2 \\ 8.3 \\ 8.5 \end{array}$	5 3 3 4 5	$ \begin{array}{c c} -2 \\ -3 \\ -4 \\ -4 \\ -4 \end{array} $	$\overset{1/2}{<^{1/4}_{1/4}}_{1/2}^{1/2}$	$\begin{array}{c} 4\frac{1}{2} \\ 3 \\ 1\frac{1}{2} \\ 3\frac{1}{2} \\ 4 \end{array}$	$\begin{smallmatrix} 12\\ 10\\ (^{d})\\ (^{d})\\ 5 \end{smallmatrix}$	$\begin{array}{r} 643 \\ 624 \\ 619 \\ 626 \\ 613 \end{array}$	$\begin{array}{c} 627 \\ 613 \\ 616 \\ 616 \\ 610 \end{array}$		1. 12 1. 12 1. 22 1. 22 1. 22
16 17 18 19 20	$ \begin{array}{c} M \\ P \\ M \\ M \\ M \\ M \end{array} $.88 .38 .14 .87 .29	$\begin{array}{c} 22.48\\ 24.18\\ 21.28\\ 19.62\\ 21.50\end{array}$	$\begin{array}{c} 4.\ 01\\ 2.\ 22\\ 3.\ 90\\ 3.\ 50\\ 3.\ 22 \end{array}$	5.37 3.84 6.94 7.24 6.80	$\begin{array}{c} 64.\ 48\\ 66.\ 84\\ 65.\ 12\\ 66.\ 62\\ 66.\ 78\end{array}$.32 .03 .32 .59 .12	.15 .25 .18 .20 .10	$ \begin{array}{r} .56 \\ .28 \\ .50 \\ .60 \\ .21 \\ \end{array} $	$\begin{array}{c} 1.\ 75\\ 2.\ 15\\ 1.\ 60\\ 0.\ 84\\ 1.\ 00 \end{array}$	$\langle 1/4 \\ < 1/4 \\ 1/4 \\ - 1/2 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 \\ < 1/4 $	$0 \\ .1 \\ .2 \\ .5 \\ .5$	$ \begin{vmatrix} < \frac{1}{4} \\ < \frac{1}{2} \\ < \frac{1}{4} \\ <$	$\begin{array}{c} 48.\ 6\\ 58.\ 6\\ 47.\ 3\\ 64.\ 3\\ 55.\ 1\end{array}$	$51 \\ 65 \\ 51 \\ 69 \\ 57$	$2 \\ 6 \\ 4 \\ 5 \\ 2$	28. 425. 425. 38. 220. 3	$23 \\ 18 \\ 17 \\ 3 \\ 17 \\ 17 \\ 3 \\ 17 \\ 17 \\ 17 \\$	$ \begin{array}{r} -5 \\ -7 \\ -8 \\ -5 \\ -3 \end{array} $	$ \begin{array}{c} 12.3\\ 6.8\\ 11.8\\ 10.7\\ 9.8 \end{array} $	$23 \\ 12 \\ 22 \\ 10 \\ 11$	$ \begin{array}{c} 11 \\ 5 \\ 10 \\ -1 \\ 1 \end{array} $	7.76.412.413.612.8	3 5 9 17 15	$ \begin{array}{c} -5 \\ -1 \\ -3 \\ 2 \end{array} $	$\begin{array}{c}1\\2\\3\\5\\8\\12\end{array}$	$2\frac{1}{2}$ 2 4 9 3	11 8 5 13 (d)	$\begin{array}{c} 629 \\ 638 \\ 632 \\ 647 \\ 638 \end{array}$	$\begin{array}{c} 620 \\ 628 \\ 629 \\ 651 \\ 643 \end{array}$		$ \begin{array}{c} 1. 34 \\ 1. 73 \\ 1. 75 \\ 2. 0' \\ 2. 1' \end{array} $
21	$\begin{array}{c} M\\ M\\ M\\ M\\ M\\ M\\ M\end{array}$.15 .52 .11 .71 .48	$19.74 \\ 22.10 \\ 20.48 \\ 22.50 \\ 21.08$	$\begin{array}{c} 3.\ 11 \\ 1.\ 98 \\ 2.\ 93 \\ 1.\ 99 \\ 2.\ 21 \end{array}$	$\begin{array}{c} 7.89 \\ 5.22 \\ 7.85 \\ 5.55 \\ 6.39 \end{array}$	$\begin{array}{c} 66.\ 48\\ 65.\ 68\\ 66.\ 48\\ 62.\ 63\\ 66.\ 92\\ \end{array}$. 25 . 19 . 39 . 45 . 04	$ \begin{array}{r} .08 \\ .30 \\ .14 \\ .34 \\ .13 \end{array} $.58 .43 .62 1.08 0.14	$\begin{array}{c} 1.\ 60\\ 3.\ 86\\ 1.\ 22\\ 4.\ 72\\ 2.\ 61 \end{array}$	$< \frac{1}{4}$ 2 1 5 1	.8 .9 .8 .5 1.6	$\begin{array}{c c} 11/2 \\ 1 \\ 1 \\ < 1/4 \\ 2 \end{array}$	58.556.753.037.958.5	$63 \\ 67 \\ 54 \\ 47 \\ 71$	$5 \\ 10 \\ 1 \\ 9 \\ 12$	$\begin{array}{c} 12.\ 7\\ 20.\ 8\\ 18.\ 7\\ 36.\ 1\\ 16.\ 7\end{array}$	$7. \\ 11 \\ 14 \\ 26 \\ 3$	$-6 \\ -10 \\ -5 \\ -10 \\ -14$	9.5 6.0 8.9 6.1 6.8	$ \begin{array}{r} 7 \\ 6 \\ 10 \\ 7 \\ 5 \end{array} $	$-3 \\ 0 \\ 1 \\ -2$	$15.9 \\ 10.7 \\ 16.0 \\ 12.4 \\ 13.4$	$ \begin{array}{c} 21 \\ 13 \\ 20 \\ 15 \\ 18 \end{array} $	5 2 4 3 5	$ \begin{array}{c} 11 \\ 6 \\ 14 \\ 6 \\ 8 \end{array} $	$ \begin{array}{c} 10 \\ 7 \\ 6 \\ 9 \\ 10 \end{array} $	$(d) \\ (d) \\ (d) \\ (d) \\ 13$	$\begin{array}{c} 646 \\ 652 \\ 639 \\ 641 \\ 660 \end{array}$	$ \begin{array}{r} 658 \\ 649 \\ 656 \\ 646 \\ 661 \end{array} $		2, 53 2, 64 2, 68 2, 78 2, 89
26	M	. 27	23.10	1.97	7.35	65.44	.08	.19	. 39	1. 29	<1/4	0.6	<1/4	35.2	41	6	39.8	35	-5	6.0	6	0	16.4	18	2	14	4	(d)	631	637	619	3. 78

* Index letters indicate source as follows: T=Tennessee Valley Authority type B clinker; W=Tygart River Valley modified "low heat" clinker; M=Miller's Series; B=Boulder Dam "low heat"; P=from producer.
b Compound composition calculated by the Bogue method from the chemical analysis.
• Heat of solution of glass-700 cal/g.
d Not determined.

• Heats of solution used in calculations:

	Compound	cal/g
C ₃ A C ₃ S		799
C ₂ S C ₄ AF MgO		572 592 876
CaO		848

f Microscopically determined.

87595-38 (Face p. 358)

material rapidly etched by H₂O and determined microscopically. The difference between that value and the value found under the heading, "total dark interstitial", is recorded in the column under "dark interstitial-glass." Determinations of glass by the heat-ofsolution method [15] were made on several samples by William Lerch. These are recorded in the column designated "Glass-Lerch Method."

2. QUALITATIVE MICROSCOPIC EXAMINATION

No attempt will be made in the following record of the qualitative microscopic examinations to give detailed results on each brand of clinker, because the structural and optical variations of most of the constituents in individual samples do not at present have a recognizable relation to the chemical composition or to the heats of solution.

(a) 3CaO.SiO ;

The samples examined show a wide range in size and perfection of outer form of the tricalcium silicate crystals. The crystals of this compound are on the average larger than those of any other compound, but the variation in size is large, not only from one lot of clinker to another, but from one piece of clinker to another. The crystals in some samples show considerable perfection of form, the individuals in polished section having straight edges and sharp angles. In other samples there is marked corrosion with rounding of angles and deep embayment of edges. A tabulation of the observations made on the whole set of samples indicates that the tricalcium silicate crystals in samples with low Al₂O₃/Fe₂O₃ ratios have greater perfection of form, whereas the crystals in samples with high Al₂O₃/Fe₂O₃ ratios are deeply corroded and embayed. The corroded crystals are generally, although not always, surrounded by a fringe of minute crystals of 2CaO.SiO₂ (see p. 360).

The existence of zoning in 3CaO.SiO₂, and its relation to solid solution, have been noted in a previous publication [5]. Some degree of zoning is present in all the samples studied in the present investigation, although in several cases it can be observed only under the most favorable etching conditions.³ The most pronounced zoning was observed in tricalcium silicate crystals in samples 10, 23, and 26, whereas samples 6, 8, 11, 12, and 16 exhibited very little zoning. The zone boundaries generally parallel the crystal edges, although infrequently the boundaries appear to be curved or irregular. Rhythmic zoning is not unusual, weakly etched alternating with strongly etched zones. The degree of etching and the development of the zoning are affected considerably by the orientation of the crystals. Surfaces parallel to basal faces etch weakly and show no zoning, whereas surfaces normal to basal faces etch most strongly and show the greatest development of zoning. No close relation between the zoning of 3CaO.SiO₂ and the composition of the clinker has yet been found.

Solid solution in 3CaO.SiO₂ crystals is shown by other optical evidence as well as zoning. Samples which contain crystals that show strong zonal etching are also found to contain crystals with marked zonal extinction when examined petrographically. A change

 $^{^{\}circ}$ The most satisfactory etching conditions to produce evidence of zoning were 3 seconds at 25° C in a solution of 1 percent of HNO₃ in alcohol.

in index of refraction from interior to exterior of such crystals or from a strongly zoned to an unzoned crystal is, however, not detectable.

(b) 2CaO.SiO2

All dicalcium silicate in industrial clinker is believed to be of the beta form. Three types of $\beta 2\text{CaO.SiO}_2$ differing somewhat in twinning and in habit have been distinguished. These were named types I. II, and III in a previous paper [5]. Another variant has been observed in many clinker specimens in the present investigation. It is called type Ia and is distinguished from type I by the presence of discrete particles along what are apparently traces of twinning planes (figs. 1 and 2). This structure is believed to be caused, according to Tavasci's theory [4], by unmixing during cooling of a material in solid solution in 2CaO.SiO₂.

Examples of all four types have been found in the clinker specimens studied. Type II, containing a single set of parallel twinning lamellae, occurs only in samples 4 and 15. Type III, often containing irregular cracks or veinlets but without distinctive twinning lamellae, occurs sometimes as overgrowths on crystals of types I and Ia and sometimes as individual crystals. Types I and Ia are sometimes found in the same clinker piece. Crystals of type I are more abundant than those of any other type in the majority of the samples. All of the dicalcium silicate crystals studied exhibit rounded or serrated edges with no evidence of regular external form.

In many of the specimens, crystals of $3CaO.SiO_2$ are surrounded by a fringe of minute rounded particles (figs. 3 and 4). Although these particles are generally too small to show the characteristic internal structure with the microscope, their etching behavior indicates that they are $2CaO.SiO_2$. This fringing material generally surrounds $3CaO.SiO_2$ crystals exhibiting considerable corrosion and embayment and, therefore, it has been found in this investigation in samples with the higher Al_2O_3/Fe_2O_3 ratios. The other types of $2CaO.SiO_2$ apparently bear no relation to the chemical composition of the clinker samples.

Crystals of dicalcium silicate show a wide range in size, but are in general smaller than those of the tricalcium silicate.

(c) "LIGHT INTERSTITIAL" MATERIAL

In the investigation of cement clinker by means of the reflecting microscope, two types of interstitial material have been differentiated which have been called, because of their relative reflectivity and reaction to etchants, the "light interstitial" material and the "dark interstitial" material [12]. The evidence previously gathered and supported by the results of the present investigation indicates that the light interstitial material is crystalline with optical properties like those of 4CaO.Al₂O₃.Fe₂O₃. The light interstitial material is intimately associated with the dark interstitial in most of the clinker specimens. Not only the size of the aggregates but the size of the individual crystals appears to bear some relation to the chemical composition, those clinker samples with the lower Al₂O₃.Fe₂O₃. The form of the crystals is also somewhat dependent on chemical composition. When the Al₂O₃/Fe₂O₃ is low, the crystals of 4CaO.Al₂O₃.Fe₂O₃ Journal of Research of the National Bureau of Standards



FIGURE 1.—2CaO.SiO₂ of types Ia and III in clinker sample 17. Etched with 1-percent alcoholic solution of HNO₃. Reflected light. Magnification, $\times 1000$.



 $\label{eq:Figure 2.2} F_{\rm IGURE} \ 2.-2CaO.SiO_2 \ of \ types \ Ia \ and \ III \ in \ clinker \ sample \ 26.$ Etched with 1-percent alcoholic solution of HNO_3. Reflected light. Magnification, \times 500.

Journal of Research of the National Bureau of Standards

Research Paper 1135



FIGURE 3.—Corroded crystals of 3CaO.SiO₂ fringed with unusually large, rounded grains of 2CaO.SiO₂.
From clinker sample 21. Etched with 1-percent alcoholic solution of HNO₃. Reflected light. Magnification, ×500.



have good prismatic development with straight edges, but when the Al₂O₃/Fe₂O₃ ratio is high the faces are poorly developed, probably because they form at a later stage of the crystallization of the clinker.

Most of the 4CaO.Al₂O₃.Fe₂O₃ crystals found in commercial cement clinker are pleochroic, but the pleochroism varies widely from one clinker sample to another and even from one crystal to another in the same sample. This variation appears to have no relation to the chemical composition of the sample. In one sample examined (No. 4) the larger crystals were light amber in color with no perceptible pleochroism, whereas the smaller crystals in the same clinker piece were much darker and exhibited strong pleochroism.

(d) "DARK INTERSTITIAL" MATERIAL

The dark interstitial material has been classified into crystalline and glassy types. One method of distinction is the rate of reaction with water when used as an etching reagent, the former type being rapidly etched and the latter slowly etched.⁴ The crystalline dark interstitial material can be subdivided into a rectangular isotropic form and a prismatic anisotropic form, whereas the glassy type has a variable index of refraction and is apparently isotropic when observed in thin section or powdered form.⁵

In the samples investigated the rectangular crystalline form, which has the optical properties of 3CaO.Al₂O₃, is found in only two samples (20 and 21) and there in only very small amounts. The anisotropic prismatic form, which appears to be produced only in the presence of alkali [12], is a much more abundant constituent. It occurs to some extent in all the samples examined; in samples with low Al₂O₃/Fe₂O₃ ratios it is present in small amounts and in localized clusters of crystals as if it were the result of nonuniformity of the mix, whereas in other samples the prismatic crystals are distributed more uniformly.

The dark interstitial material which reacts slowly with water has been found to some extent in all the samples in this series. Although it is impossible to measure the indices of refraction of this phase accurately, those samples having low Al₂O₃/Fe₂O₃ ratios contain glass which is microscopically colorless with an index of refraction less than 1.72, whereas those with high Al_2O_3/Fe_2O_3 ratios contain glass with an index higher than 1.72 and with a green color. In all the samples the glassy phase is intimately mixed with the prismatic crystals of 4CaO.Al₂O₃.Fe₂O₃.

(e) FREE MgO

Free MgO occurs as angular grains with the optical properties of periclase. These have been identified in polished sections of commercial clinker [12]. In the present investigation free MgO has been seen in the majority of the samples. Although the magnesia grains are small, it is observed that, in general, the greater the amount of MgO the larger the grain size of the periclase. The free MgO is associated with the interstitial material in all the samples. In most of the samples the periclase grains are more or less uniformly dis-

⁴ After immersion in water for 1 to 2 seconds, the first type is etched noticeably while the second type

^b there interston in water for *t* to 2 seconds, the first type is excitate holicarby while the second type ^b Continuous homogeneous grains of this glassy form appear perfectly isotropic, although they are so-small that they may actually be slightly birefringent. Therefore, it is impossible to decide whether or not the glassy phase is equivalent to the "metastable phase" of Brownmiller [18].

tributed throughout the specimens examined, but in some (notably No. 5) the grains occur in clusters. This may be the result of improper mixing of raw materials.

(f) FREE CaO

Free CaO occurs as rounded grains which are detected by etching reactions previously described [12]. In most of the samples the free CaO grains are present as clusters associated with concentrations of $3CaO.SiO_2$ crystals and, therefore, are probably the result of some lack of uniformity in the batch.

V. DISCUSSION

A comparison of direct and indirect methods of quantitative determination of the phases present in portland cement clinker shows certain systematic relations (table 2). These are most apparent when the columns headed "difference" are examined. These columns show the differences between the values for equivalent constituents as determined microscopically and chemically. It will be observed that the percentages of 2CaO.SiO₂ determined microscopically exceed those determined chemically only for two samples with the lowest $Al_2O_3/$ Fe₂O₃ ratios, whereas the percentages of 3CaO.SiO₂ obtained microscopically are less than those obtained chemically only for samples with low Al₂O₃/Fe₂O₃ ratios. The microscopic values for "light interstitial" material tend to be greater than those for calculated 4CaO.Al₂O₃,Fe₂O₃ for samples with low Al₂O₃/Fe₂O₃ ratios, but the differences are close to zero for samples with Al₂O₃/Fe₂O₃ ratios of 2.00 or greater. The reverse is true when microscopically determined total "dark interstitial" material is compared with calculated The microscopic values are less than or equal to the 3CaO.Al₂O₃. calculated (with one exception) for low Al₂O₃/Fe₂O₃ ratios and greater than the calculated for ratios more than 2.00.

Several reasons may be given for the differences between the compositions determined microscopically and those obtained by calculation. The fact that tricalcium silicate contains other material in solid solution would tend to make the observed amount greater than that obtained by calculation by the Bogue method [16] as pure $3CaO.SiO_2$. Moreover, Lea and Parker [19] have shown from a consideration of the system $CaO-Al_2O_3$ -Fe₂O₃-SiO₂ that cement clinkers with high Al_2O_3/Fe_2O_3 ratios contain greater amounts of $3CaO.SiO_2$ and lesser amounts of $2CaO.SiO_2$ when crystallization is arrested during cooling than when complete equilibrium is attained.

Because there is partial solid solution between $4CaO.Al_2O_3.Fe_2O_3$ and $3CaO.Al_2O_3$ in the system $CaO-Al_2O_3$ -Fe $_2O_3$ [20], it seems probable that the excess of observed light interstitial material over calculated $4CaO.Al_2O_3.Fe_2O_3$ in clinker with low Al_2O_3/Fe_2O_3 ratios may be explained by the earlier crystallization of $4CaO.Al_2O_3.Fe_2O_3$ with solid solution of material approximating $3CaO.Al_2O_3$ in composition. In clinkers with high Al_2O_3/Fe_2O_3 ratios, dark interstitial material may be expected to crystallize first and to take some $4CaO.Al_2O_3.Fe_2O_3$ into solid solution. The prismatic doubly refracting constituents [12] presumably produced by alkalies are not accounted for in the Bogue method of calculation. Their presence would tend to increase the amount of dark interstitial material, but what the quantitative effect would be on the discrepancies between calculated and microscopically determined compositions is not known.

To account for the rather large differences between the light interstitial constituent and calculated $4\text{CaO}.\text{Al}_2\text{O}_3.\text{Fe}_2\text{O}_3$ in some samples, it has been suggested that the light interstitial constituent may consist of another phase besides $4\text{CaO}.\text{Al}_2\text{O}_3.\text{Fe}_2\text{O}_3$, for instance, a highly refractive iron-bearing glass which is not distinguished from 4CaO.- $\text{Al}_2\text{O}_3.\text{Fe}_2\text{O}_3$ by the etching reagents used. Attempts to differentiate the light interstitial material into two phases by the use of other etching reagents and illuminating methods have thus far been unsuccessful.

In the Bogue method all the MgO is calculated as free MgO (periclase). In all but one of the samples examined the free MgO as determined by microscopic analysis is less than the total MgO by chemical analysis. Evidently a part of the MgO is dissolved in the glass or in one or more of the crystalline constituents.

The agreement between the microscopic method and the ammonium acetate method in the determination of free CaO is, in general, good. The somewhat lower results by the microscopic method for most samples are to be expected because the chemical method includes both free Ca(OH)₂ and free CaO, whereas the microscopic method distinguishes only crystalline CaO. The large difference for sample 8 is probably to be attributed to a partial hydrolysis of the clinker constituents, as indicated by the high ignition loss.

Although the presence of glass is evidence that commercial clinkers are not the product of crystallization under equilibrium conditions, the simultaneous occurrence of fine-grained crystalline light and dark interstitial material with glass in the same specimen indicates also that the clinkers have not been completely quenched. The commercial product may, therefore, be considered as an intermediate stage between a material quenched from a definite temperature and one crystallized at continuous equilibrium conditions.

In comparing calculated and observed heats of solution (table 2) it is evident that, in general, the heats of solution as computed from calculated compound composition agree somewhat better with the observed than do those calculated from microscopic analysis, the average difference between observed and microscopic analysis being 8.3 cal/g and between observed and calculated compound composition being 5.6 cal/g. In making the heat of solution calculations based upon the Bogue method of determining compound composition, it was assumed that:

1. The compounds calculated to be present had the compositions and the heats of solution of the pure compounds unaffected by solid solution.

2. The oxides present in minor amounts, such as alkalies, did not enter into compounds or affect the heats of solutions.

3. Perfect equilibrium crystallization took place during cooling without the formation of glass.

In making the calculation of heats of solution from microscopic analyses it was not only necessary to use the heats of solution of the pure compounds but also to use the heat of solution of $3CaO.Al_2O_3$ for all the crystalline dark interstitial material, whether rectangular or prismatic. A constant value of 700 cal/g was used for all the glass, although the composition and consequently the heat of solution of the glass vary with the composition and rate of cooling of the clinker specimen.

All the assumptions made with respect to both types of calculation are known to be inexact, but they are felt to be the closest approximations that can be made at the present state of knowledge. Considering the errors in the basic assumptions, the degree of correspondence of either of the methods of calculations with the observed heats of solution has little significance.

The glass content by the Lerch method (table 2) is greater than the glass content by the microscopic method for all samples on which determinations were made. Because the Lerch method is essentially a heat-of-solution method it is open to some of the same errors (already pointed out by Lerch and Brownmiller [15]) that affect the calculation of heat of solution from compound compositions, namely, the assumption that the compounds present are free from solid solution and the assumption that the alkalies and other minor oxides have no effect on the heat of solution. The accuracy of the method will be increased as more knowledge is obtained on the actual composition and properties of these compounds in cement clinker.

VI. SUMMARY

The results of chemical and microscopic analysis and heat-ofsolution measurements on 26 samples of commercial portland cement clinker are reported.

A comparison of compound composition by microscopic analysis and by calculation from chemical analysis shows that:

1. The content of $3CaO.SiO_2$ by microscopic analysis is greater than by calculation, except for very low Al_2O_3/Fe_2O_3 ratios.

2. The content of $2CaO.SiO_2$ is less by microscopic analysis, except for very low Al_2O_3/Fe_2O_3 ratios.

3. Microscopically determined "dark interstitial" material is less than calculated $3CaO.Al_2O_3$ for low Al_2O_3/Fe_2O_3 ratios and greater for high Al_2O_3/Fe_2O_3 ratios.

4. Microscopically determined "light interstitial" material is greater than calculated $4\text{CaO.Al}_2\text{O}_3$.Fe₂O₃ for low Al₂O₃/Fe₂O₃ ratios and approximately equal for high ratios.

Qualitative and quantitative microscopic analyses indicate that the crystalline compounds present are not pure, but contain limited amounts of material in solid solution.

Glass is present in all the samples studied.

A comparison of observed heats of solution with those calculated from chemical analysis and from microscopic analysis shows a fairly close correspondence, but it is pointed out that the assumptions on which the calculations by both methods are based are inexact.

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