

Bounds on Time Reversal Violation From Polarized Neutron Capture With Unpolarized Targets

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We have analyzed constraints on parity-odd time-reversal noninvariant interactions derived from measurements of the energy dependence of parity-violating polarized neutron capture on *unpolarized* targets. As previous authors found, a perturbation in energy dependence due to a parity (*P*)-odd time (*T*)-odd interaction is present. However, the perturbation competes with *T*-even terms which can obscure the *T*-odd signature. We estimate the magnitudes of these competing terms and suggest strategies for a practicable experiment.

Key words: neutrons; resonances; time-reversal.

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1. Introduction

The enhancement factor of a million observed in the 1980s in compound nucleus parity violating observables stimulated great interest in searching for time reversal violation. The enhancement is expected to be present for all symmetry breaking observables in compound nuclear systems, arising as it does from the close spacing and long lifetimes of the states. The largest enhancements were seen in transmission experiments with epithermal neutrons at resonances in nuclei $A >$

100. Despite considerable effort, however, no epithermal neutron transmission test of time reversal violation (*P*-even or *P*-odd) has been carried out, primarily due to difficulties in preparing a suitable spin polarized or aligned nuclear target. For general background on the proposed experiments and the difficulties see [1,2].

For *P*-even time reversal violation, tests with higher energy neutrons have been performed in holmium ($A = 165$) using a nuclear spin aligned target [3]. The experimental precision is high. However, there are no compound nuclear enhancement mechanisms at work, and a $1/A$ suppression factor arises since only the last valence nucleon contributes to the *T*-violating effect. Further improvement with heavy targets and MeV-beams of neutrons therefore appears unlikely. Use of a

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tensor polarized deuteron target avoids the $1/A$ suppression, and a test using a few hundred MeV polarized proton beam is planned for the COoler SYnchrotron storage ring facility (COSY) at the Institut für Kernphysik (IKP) Juelich, Germany by the Time Reversal Invariance Test at COSY collaboration (TRIC). The experiment is still under development but does have the potential to make an order of magnitude improvement in sensitivity to the underlying T -violating meson exchange coupling constants [4].

Given the difficulties associated with the need for a polarized target in an on-resonance neutron transmission P -odd test, it is appropriate to investigate whether other experiments could investigate time reversal violation, taking advantage also of the intense fluxes of neutrons expected to be available from the next generation of spallation neutron sources in the US, Japan and Europe. In the early 1980s, Bunakov and Gudkov [5] and Flambaum and Sushkov [6] noted that measurements with *unpolarized* targets of the *energy dependence* near p -wave resonances of *parity-violating* correlations in polarized neutron capture could constrain P -odd T -odd interactions. Although parity-violating asymmetries of the order of a few percent had earlier been observed in polarized neutron capture, the idea was not pursued further. Instead, in a separate development, the energy dependence of forward-backward asymmetries in *unpolarized* neutron capture was used [7] to look for evidence of *parity-conserving* time-reversal noninvariance. The study was restricted to a single resonance, but demonstrated that the method could in principle yield a competitive bound on the strength of the P -even T -odd interaction among nucleons if extended to an appropriate sample.

In this paper, we expand on the analysis of P -odd T -violation suggested in [5,6]. The purpose of the work is to establish to what extent T -even contributions may mask the perturbation due to the P -odd T -odd interaction of interest. Despite uncertainties in the precise values of resonance parameters, the theory of how to model neutron resonance reactions is well enough established to allow us to estimate the order of magnitude of these contributions. We follow the Flambaum and Sushkov model for the energy dependence of the relevant asymmetries.

Our results confirm that there is a shift in the zero of the capture correlation asymmetry from the resonance energy E_p , of order $(v_{PT}/v_p)\Gamma$, where v_{PT} is the root-mean-square (rms) value of compound nucleus matrix elements of the unknown P -odd T -odd interaction and v_p is the rms value of compound nucleus matrix elements of the P -odd weak interaction. Our results also

indicate that, in the epithermal regime, electromagnetic and weak interaction effects give rise to two T -even displacements of the zero crossing: one of order $\sqrt{E_p}(\text{in eV})10^{-3}\Gamma$ and the other of order $(\Gamma/D)\Gamma$, where Γ is the average width of resonances and D is the average spacing between them.

A fuller account, also including analysis of the effects of distant resonances, is published elsewhere [8].

2. Two Resonance Analysis

The P -odd asymmetry of interest to us measures the strength of the dependence of the differential cross section for the (\bar{n}, γ) reaction on the pseudo-scalar $\boldsymbol{\sigma} \cdot \mathbf{n}_\gamma$, where $\boldsymbol{\sigma}$ is the transverse polarization of the neutron beam and \mathbf{n}_γ is the unit vector in the direction of observed photon's momentum. In the notation of the decomposition of the differential cross section for the (\bar{n}, γ) reaction in Eq. (17) of [6], we study the energy dependence of the combination $A \equiv a_9 - a_{12}/3$, which is precisely the coefficient of $\boldsymbol{\sigma} \cdot \mathbf{n}_\gamma$ when all terms in Eq. (17) of [6] are considered. For the sake of definiteness, we restrict ourselves (as do Flambaum and Sushkov in section 3 of [6]) to radiative neutron capture reactions involving:

- a target nucleus with a $\frac{1}{2}^+$ ground state and a final nucleus with a 0^+ ground state, and;
- gamma-quanta corresponding to transitions from 1^+ or 1^- states of the intermediate compound nucleus to the 0^+ ground state of the final nucleus. Then, the general expressions of Appendix A in [6] imply that $A = A^{(13)} + A^{(24)}$, where $A^{(13)} \equiv 2\text{Re} [V_1 (V_3)^*]$ and

$$A^{(24)} \equiv 2\text{Re} \left[V_2^{(3/2)} (V_4^{(3/2)})^* - V_2^{(1/2)} (V_4^{(1/2)})^* \right] - \frac{1}{\sqrt{2}} \text{Re} \left[V_2^{(1/2)} (V_4^{(3/2)})^* + V_2^{(3/2)} (V_4^{(1/2)})^* \right],$$

V_1 , $V_2^{(j)}$, V_3 and $V_4^{(j)}$ being abbreviations for the invariant amplitudes $V_1(E, 1^+)$, $V_2(E, 1^-, j)$, $V_3(E, 1)$ and $V_4^{(j)}(E, 1, j)$ of Eq. (15) in [6], respectively.

In the two resonance approximation, only the terms corresponding to the p -wave resonance at which the measurement is performed and the nearest 1^+ s -wave resonance (of energy E_s and width Γ_s) are retained in the invariant amplitudes. Thus,

$$V_1 \approx V_1(s) \equiv -\frac{\sqrt{3}}{4k} \frac{g_n^s g_{M1}^s}{E - E_s + i\Gamma_s/2} \quad (2.1)$$

$$V_2^{(j)} \approx V_2^{(j)}(p) \equiv -\frac{\sqrt{3}}{4k} \frac{g_n^p(j) g_{E1}^p}{E - E_p + i\Gamma_p/2} \quad (2.2)$$

$$V_3 \approx V_1(s)W_{sp} \frac{g_{E1}^p / g_{M1}^s}{E - E_p + i\Gamma_p / 2} \quad (2.3)$$

$$V_4^{(j)} \approx V_2^{(j)}(p)W_{sp}^* \frac{g_{M1}^s / g_{E1}^p}{E - E_s + i\Gamma_s / 2}. \quad (2.4)$$

The notation for the partial width amplitudes (g_n^s , g_{M1}^s , etc) differs from that used in [6] (namely, T_s , A_{sf} , etc). More importantly, we take the interaction matrix element W_{sp} to include both a P -odd perturbation U and a P -odd T -odd perturbation \tilde{U} , i.e. $W_{sp} = u_{sp} + i\tilde{u}_{sp}$, where u_{sp} and \tilde{u}_{sp} are real.

Concerning the partial width amplitudes, we assume for the moment that they are all real: $g_n^s[g_n^p(j)]$ is the amplitude for capture by the s -wave [p -wave] resonance of a neutron [of angular momentum j]; $g_{M1}^s[g_{E1}^p]$ is the amplitude for the $M1$ [$E1$] electromagnetic deexcitation of the s -wave [p -wave] resonance to the ground state. In terms of these partial width amplitudes, the neutron partial widths of the s - and p -wave resonances are $\Gamma_s^n = (g_n^s)^2$ and $\Gamma_p^n = (g_n^p(\frac{1}{2}))^2 + (g_n^p(\frac{3}{2}))^2$, respectively, and the partial gamma width for the $M1$ and $E1$ transitions to the ground state are $\Gamma_{M1} = (g_{M1}^s)^2$ and $\Gamma_{E1} = (g_{E1}^p)^2$, respectively. Below, the normalized partial width amplitudes $x_j^p \equiv g_n^p(j) / \sqrt{\Gamma_p^n}$ are used.

Substitution of Eqs. (2.1)-(2.4) into $A^{(13)}$ and $A^{(24)}$ yields

$$A = \frac{3}{(4k)^2} \frac{g_{E1}^p \Gamma_p}{(E - E_p)^2 + \Gamma_p^2 / 4} \frac{g_{M1}^s \Gamma_s^n}{(E - E_s)^2 + \Gamma_s^2 / 4} u_{sp} \left[a_p \varepsilon + \tilde{a}_p \frac{\tilde{u}_{sp}}{u_{sp}} + b_p \right], \quad (2.5)$$

where, in terms of $z_p \equiv (x_{3/2}^p)^2 - (x_{1/2}^p)^2 - \frac{1}{\sqrt{2}} x_{1/2}^p x_{3/2}^p$, the coefficients a_p , \tilde{a}_p , and b_p are

$$a_p = 1 + z_p \frac{\Gamma_p^n}{\Gamma_s^n}, \quad \tilde{a}_p = 1 - z_p \frac{\Gamma_p^n}{\Gamma_s^n} \frac{\Gamma_s}{\Gamma_p}$$

$$\text{and } b_p = z_p \frac{\Gamma_p^n}{\Gamma_s^n} \frac{E_p - E_s}{\Gamma_p / 2}.$$

Equation (2.5) demonstrates that a P -odd T -odd interaction does modify, as claimed in [6], the energy dependence of the P -odd asymmetry associated with the pseudoscalar $\boldsymbol{\sigma} \cdot \mathbf{n}_\gamma$.

A signature of this change is its effect on the *location of the zero* in the asymmetry (or, equivalently, A).

According to Eq. (2.5), the zero is offset from the resonance energy E_p by an amount

$$\Delta E_p = - \left(\frac{\tilde{a}_p \tilde{u}_{sp} + b_p}{a_p u_{sp}} \right) \frac{\Gamma_p}{2}. \quad (2.6)$$

If we suppose that $|V_1|$ and the $|V_2^{(j)}|$'s are comparable when $E \approx E_p$ (the parity-mixing essential to the asymmetry under consideration will not be substantial unless this is the case), then

$$\frac{\Gamma_p^n}{\Gamma_s^n} \sim \frac{\Gamma_{M1}}{\Gamma_{E1}} \left(\frac{\Gamma_p / 2}{E_p - E_s} \right)^2 \sim \left(\frac{\Gamma}{D} \right)^2,$$

where Γ is the average width of resonances and D is the typical spacing between $J = 1$ resonances, and the following order of magnitude estimates apply: $a_p - 1 = O(\Gamma^2/D^2)$, $\tilde{a}_p - 1 = O(\Gamma^2/D^2)$, and $b_p = O(\Gamma/D)$. On omitting terms less than of order $(\Gamma/D)^2 \Gamma_p$ by at least one order of magnitude [9], the expression for the offset simplifies to

$$\Delta E_p = - \left(\frac{\tilde{u}_{sp} + b_p}{u_{sp}} \right) \frac{\Gamma_p}{2}. \quad (2.7)$$

Observe that Eq. (2.7) implies that $\Delta E_p \ll \Gamma_p/2$.

We can accommodate hard sphere phase shifts in our analysis by formally replacing g_n^s and $g_n^p(j)$ in Eqs. (2.1)-(2.4) by $g_n^s e^{i\phi_s}$ and $g_n^p(j) e^{i\phi_p(j)}$, respectively. We also have to allow for the fact that the radiative partial width amplitudes are, in principle, complex [10]. To this end, we make the substitutions $g_{M1}^s \rightarrow |g_{M1}^s| e^{i\phi_{M1}^s}$ and $g_{E1}^p \rightarrow |g_{E1}^p| e^{i\phi_{E1}^p}$. In the present two resonance approximation, some of these phases cancel for the combinations of invariant amplitudes appearing in A so that, in fact, A depends only on the phase differences $\delta_p \equiv \phi_p(\frac{1}{2}) - \phi_p(\frac{3}{2})$ and $\delta_\gamma \equiv \phi_{M1}^s - \phi_{E1}^p$. The coefficients a_p , \tilde{a}_p , and b_p become

$$a_p \left(1 + z_p' \frac{\Gamma_p^n}{\Gamma_s^n} \right) \left(\cos \delta_\gamma + \frac{\tilde{u}_{sp}}{u_{sp}} \sin \delta_\gamma \right), \quad (2.8)$$

$$\tilde{a}_p = \cos \delta_\gamma - z_p' \frac{\Gamma_p^n}{\Gamma_s^n} \left(\frac{\Gamma_s}{\Gamma_p} \cos \delta_\gamma - \frac{E_p - E_s}{\Gamma_p / 2} \sin \delta_\gamma \right) \quad (2.9)$$

$$b_p = -\sin \delta_\gamma + z_p' \frac{\Gamma_p^n}{\Gamma_s^n} \left(\frac{E_p - E_s}{\Gamma_p / 2} \cos \delta_\gamma + \frac{\Gamma_s}{\Gamma_p} \sin \delta_\gamma \right) \quad (2.10)$$

where $z'_p \equiv (x_{3/2}^p)^2 - (x_{1/2}^p)^2 - \frac{1}{\sqrt{2}} x_{1/2}^p x_{3/2}^p \cos \delta_p$. The phase difference δ_p , confined as it is to the factor z'_p , which, like z_p , is of order unity, cannot alter the order of magnitude estimates for a_p , \tilde{a}_p , and b_p of the previous paragraph. The dependence on δ_p is less trivial, but some consideration of Eqs. (2.6) and (2.8)-(2.10) shows that they can only be reconciled with a measurement of the offset which finds that $\Delta E_p \ll \Gamma_p$ if $|\sin \delta_p| \ll 1$.

If $|\sin \delta_p| \lesssim \Gamma/D (\ll 1)$, then the previous order of magnitude estimates for a_p , \tilde{a}_p , and b_p continue to apply. If, instead, $1 \gg |\sin \delta_p| \gg \Gamma/D$, then $a_p - 1 = O(\sin^2 \delta_p)$, $\tilde{a}_p - 1 = O(\sin^2 \delta_p)$ and $b_p = O(\sin^2 \delta_p)$. In both cases, Eq. (2.7) holds, it being understood that b_p is of order the larger of Γ/D and $\sin \delta_p$. [In the second case, terms of order $\Gamma_p \sin^3 \delta_p$ or smaller have been dropped in Eq. (2.7).]

There is a dearth of information on the order of magnitude of phases like ϕ_{M1}^s and ϕ_{E1}^p for epithermal neutron capture in medium-to-heavy nuclei. It has been recognized that they are very small at these energies and so they have been ignored (see, for example, p. 302 in [10]). By adapting the results of [11], we estimate that $\sin \delta_p$ is of order k/κ_f or, equivalently, $\sqrt{E_p/S_n^f}$, where S_n^f is the neutron separation energy for the ground state of the final nucleus. We also use the fact that the neutron energy E of interest is approximately equal to E_p (k and κ_f are the neutron wavenumbers corresponding to E and S_n^f , respectively).

For nuclei formed in capture on non-fissile spin $\frac{1}{2}^+$ nuclei of mass number $A > 100$, S_n^f ranges from about 6 MeV to about 9 MeV. Our order of magnitude estimate of $\sin \delta_p$ thus evaluates to

$$\sin \delta_p \sim \sqrt{E_p (\text{in eV})} 10^{-3},$$

which suggests that the contribution to ΔE_p due to the phase difference δ_p is dominant except in the somewhat unfavourable circumstance (such as with the ^{113}Cd target used in [7]) that $\Gamma/D \sim 10^{-2}$. Even then, E_p has to be less than about 100 eV or so. We find similar results when the effects of distant states are included [8].

3. Conclusions

To be of interest as a test of P -odd time reversal invariance, data on displacements of zeros in (n, γ) correlations should comprise measurements at several p -wave resonances within a given compound nucleus [12]. For spallation sources, non-fissile nuclei of mass number $A > 100$ emerge as appropriate targets [13]. In

practice, the E_p -dependent shift is likely to be the larger of the displacements due to T -even interactions: E_p would typically be $\gtrsim 100$ eV in any reasonably sized data sample, whereas the choice of target nucleus would almost certainly be such that $\Gamma/D < 10^{-2}$. Taking $\Gamma \sim 100$ meV (appropriate to non-fissile $A > 100$ nuclei in the epithermal regime), we expect this E_p -dependent shift (when dominant) to be of order 1 meV. Consequently, one ought to detect non-zero displacements in measurements which can determine the location of zeros with a precision of order 0.1 meV.

When this level of precision cannot be attained and only bounds on shifts in zeros are set, the corresponding bound on the strength of a P -odd T -odd interaction is not encouraging. One measurement close to threshold ($E_p \sim 1$ eV) will not suffice [12]. Several null measurements, which put limits on shifts of slightly more than the 1 meV or so estimated above for the E_p -dependent shifts, would constrain the ratio v_{PT}/v_P to be less than of order 10^{-2} .

How much better can one do if *non-null* measurements of the displacements of zeros are possible? Individual measurements are, of course, not amenable to quantitative analysis because the precise value of the T -even interaction shift estimated in this paper (and other shifts due to effects not considered in this work like non-resonant direct neutron capture) cannot be calculated with any certainty. What, conceivably, could be done is to model the *statistics* of shifts reliably. Values of this shift are drawn from a Cauchy distribution with scale parameter $\lambda \equiv v_{PT}/v_P$. With a large enough sample of non-null determinations of displacements (of zeros) and a sound model for their statistics, it should be possible to extract some information on λ . For example, if a statistical analysis could fix a bound on the shift due to the P -odd T -odd interaction at ten percent of the T -even interaction shift ($\sim 10^{-2}\Gamma$), the corresponding bound on λ would be of order 10^{-3} . This would be a competitive limit, comparable to the kind of bound it has been suggested could be extracted from the 3-fold transmission test requiring a polarized target [14].

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