The Configurations $4d^n + 4d^{n-1}$ 5s in Doubly-Ionized Atoms of the Palladium Group*

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Four hundred and eighty-three energy levels belonging to the low even configurations of the third spectra of the palladium group are predicted by the use of interpolation formulas for the interaction parameters.

Key Words: Configurations 4ds + 4ds - 1 5s, energy levels, interaction parameters, palladium group, theoretical, third spectra.

1. Introduction

In the present paper we describe a systematic treatment of the low even configurations of the sequence ' of the third spectra of the palladium group. This treatment is analogous to the treatments of the second spectra of the iron group [1],² the second spectra of the palladium group [2], and the third spectra of the iron group [3] described in three previous papers.

The approximation used in this work is, as in the the previous papers, the Slater approximation with several improvements. We have included the interaction between the configurations $4d^n$, $4d^{n-1}5s$, we have taken different values for the corresponding parameters B, C and α of the two configurations, we have considered the L(L+1) correction as well as the spin-orbit interaction.

The main stages of this treatment are the following: (a) The Slater approximation, improved by the above mentioned corrections, is used to calculate the energy levels of each spectrum. After diagonalizing ("Diag.") the energy matrices, the interactionparameters are considered as free parameters and the best fit to the experimental material is achieved by least-squares calculations ("L.S."). We call this stage "the separate treatment."

(b) The corresponding interaction-parameters of all the spectra of the sequence are expressed as linear functions (in some cases, with a small quadratic correction) of the atomic number. Only the coefficients of these interpolation formulas ("general parameters") retain the role of free parameters. Thus, the whole sequence, containing several hundreds of energy levels, is treated as a single problem ("general treatment") with quite a small number of free parameters.

In the sequence from Y III to Cd III, theory predicts, for the configurations $4d^n + 4d^{n-1}5s$, 209 terms which split into 483 levels. Unfortunately, the experimental material is rather scarce. Only 56 terms splitting into 130 levels were found reliable and could be fitted with the calculated levels. In most spectra the number of known terms does not exceed the number of electrostatic-interaction parameters; thus, a separate treatment of one spectrum loses a great deal of its significance. Such separate treatments were performed only as an introduction to the interpolative treatment, which is rather reliable even in this case, since the number of parameters is reduced by the use of interpolation formulas for them.

In the following, we shall first give an account of the situation and the separate calculations in the various spectra, and then describe the general treatment.

Most of the experimental material used in this paper was taken from Moore's Atomic Energy Levels, [4] later referred to as AEL. Unless other sources are explicitly mentioned, it means that the experimental matter was taken from AEL.

2. Notations

The symbols for the parameters are the usual ones. The parameters A, B, C, ζ refer to the configuration d^n , while A', B', C', ζ' refer to the configuration $d^{n-1}s$. In the actual calculations of the separate treatment A' was replaced by S' = A' - A. In the general treatment A and A' were replaced by the centers of gravity of the configurations, M and M', and the difference D' = M' - M was expressed by an interpolation formula like the interaction parameters.

The parameter $G = G_s(ds)$ measures the exchange interaction between d and s electrons, $H=R^2(dd, ds)/35$ is the parameter of the interaction between the configurations d^n and $d^{n-1}s$, and α is the parameter of the L(L + 1)-correction.

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[&]quot;We call "a sequence" all the stome belonging to the same period with the same degree of ionization. • Figures in brackets indicate the hierstare references at the end of this paper.

"Diag." is an abbreviation for "diagonalization," "L.S." is an abbreviation for "least-squares calculation."

3. The Mean Error

Two kinds of mean-error are used in this paper. The "level-mean-error," Δ , is defined by the formula

$$\Delta = \sqrt{\Sigma \Delta_{\rm I}^2 / (n-m)} \tag{1}$$

where the $\Delta_{\rm L}$ are the differences between the observed levels and the calculated levels fitted to them, *n* is the number of observed levels, and *m* is the number of free parameters. The "term-mean-error," Δ' , (the term, "mean error" as defined in this paper is identical to the concept, "residual standard deviation" used in statistical analysis) is defined by the formula

$$\Delta' = \sqrt{\Sigma \Delta_{\rm T}^2 / (n_{\rm T} - m_{\rm B})} \tag{2}$$

where the $\Delta_{\rm T}$ are the differences between the observed terms and calculated terms fitted to them, $n_{\rm T}$ is the number of observed terms, and $m_{\rm E}$ is the number of the free electrostatic parameters.

The calculation of Δ is easier, since our least-squares program furnishes $\Sigma \Delta_L^2$; the abbreviation "meanerror" means the level-mean-error.

In fact, Δ' is a more serious criterion of the precision of our approximations, as the levels belonging to the same term are strongly correlated, while in the definition of Δ they are considered independent.

4. Survey of the Various Spectra

<u>Y III – (4d + 5s)</u>

This spectrum consists of two terms and needs for its description two electrostatic parameters, so that a separate treatment is meaningless. On the other hand in the general treatment it supplies reliable points for the interpolation formulae of D' and ζ .

The observed and calculated levels are given in table 7.

<u>Zr (11 – (4d² + 4d5s)</u>

These configurations consist of 7 terms which split into 13 levels. In AEL 6 experimental terms, splitting into 12 levels, are reported; only the 'S of d^2 is unknown.

Here, too, a separate treatment is not fully significant, since 6 electrostatic parameters are necessary. Nevertheless, a separate treatment was performed in order to get some preliminary information about the more stable parameters: D', B, G, ζ , ζ' .

Initial values for the parameters were taken from Zr II [2]. In L.S. 1, the parameter H was frozen and the mean error was 4 because the number of free electrostatic parameters is equal to the number of known terms.

The parameters of the various stages of the calculation are given in table 1, the observed and calculated energy levels in table 8.

<u>Nb III – $(4d^3 + 4d^25s)$ </u>

In these configurations theory predicts 15 terms which split into 35 levels. In a paper of L. Iglesias [5] 11 experimental terms, splitting into 28 levels are reported.

Parameters for Diag. 1 were prepared by comparison with the parameters of NB11 and Zr II [2]. It turned out that the level assigned by Iglesias as ${}^{2}D_{3/2}$ is actually the ${}^{2}P_{3/2}$ of d^{3} .

In L.S. 1 we got a mean error of 34.

The estimates of parameters of the various stages of the calculation are given in table 2, the energy levels in table 9.

<u>Mo m – $(4d^4 + 4d^35s)$ </u>

These configurations consist of 27 terms, which split into 72 levels. In AEL only the level ${}^{5}D_{4}$ and the 5 levels belonging to the ${}^{3}F$ of $d^{2}s$ are reported. Since the ground level $d^{4} {}^{5}D_{0}$ is unknown, Rico and Catalan estimated the value of the ${}^{5}D_{4}$ to be 1500 cm⁻¹, and added to all the known levels an unknown additive constant x. (Note, there is no connection between the unknown numerical constant "x", introduced by Rico and Catalan, and the variable x=n-6 defined in eq (5a) in the section on the interpolative treatment.)

Because of these circumstances we did not even include Mo III in the General Least Squares (G.L.S.) calculation, but, using the improved coefficients of the interpolation formulae achieved in the G.L.S., we calculated the interaction parameters of Mo III. Then the matrices of $d^4 + d^3s$ were diagonalized with the use of the interpolated parameters, and thus, we obtained predictions for the levels of Mo III.

Using the calculated values of the (${}^{4}F$) ${}^{5}F$ one gets for x the value 340. For ${}^{5}D_{4}$ we got the value 1807 cm⁻¹ and this gives x=307. We suppose that the uncertainty of x is of the order of magnitude of the term-mean-error of the G.L.S. which is 91 cm⁻¹.

The predicted levels of Mo III are given in table 10. Te $\underline{\text{III}} = (4d^3 + 4d^45s)$

In these configurations theory predicts 40 terms which split into 100 levels. Unfortunately, no level was observed. Using the results of the G.L.S. the interaction parameters of Tc III were interpolated, and then the energy matrices of these configurations were diagonalized. In this way the energy levels could be calculated.

The predicted levels of Tc III are given in table 11. $\underline{Ru III} - (4a^3 + 4a^55s)$

These configurations consist of 48 terms, which split into 108 levels. In AEL only 7 levels are reported: The ³D of d^8 , and the ⁷S and the ³S of d^8s .

Obviously, no separate treatment was performed, but in the G.L.S. these few data furnished more points for D', G, and ζ . Of course, the main role of the G.L.S. in this case was to calculate all the levels of Ru DI.

The observed and calculated energy levels are given in table 12.

<u>Rh III $-(4d^7 + 4d^85s)$ </u>

In these configurations theory predicts 33 terms, which split into 82 levels. In AEL all these levels are reported. Only the b^2S of d^8s is considered doubtful.

Even at the preliminary stage of estimating parameters for the first diagonalization we had serious doubts as to the reliability of the experimental material. It is well known that the difference between two terms of d^8s having the same parent term of d^6 is determined by the parameter $G = G_2(4d5s)$. This parameter is very stable for all spectra of the transition elements and also does not change considerably for all spectra of the same sequence. In the present spectrum we could get for the parameter G values which were different from each other by about 1000 cm⁻³, depending upon the choice of the parent term. Only the difference between ($^8D)^4D$ and ($^8D)^8D$ was consistent with the interpolated value of G.

Since the experimental levels did not seem reliable we decided to perform Diag. 1 with interpolated parameters and to use its results for a more detailed critique of the observed levels. We got a very bad fit. The deviations between the calculated levels and those reported in AEL were frequently more than 10000 cm⁻¹. In order to check if there exists any set of parameters which will give calculated values close to the observed ones we included in the first leastsquares calculation ("L.S. 1a") 81 levels. Only the b²S which is reported as doubtful was excluded. We got a mean error of 3094 cm⁻¹. In L.S. 1b only 33 levels were included. We did not include 42 levels belonging to 4d⁹⁵s. The terms b²D, a²F, a²H of 4d⁷ were also included. The mean error reduced to 273, but B' and C' assumed nonreasonable values. In L.S. Ic from the configuration $d^{8}s$ only the levels of (⁵D) ⁶D and (⁵D) ⁴D were left. The values of B' and C' were frozen and we got a mean error of 235. It should be noted that in L.S. 1c we used 6 free electrostatic parameters and 2 frozen ones for the description of only 7 observed terms. Thus, the separate treatment lost its physical significance and we could not use it for further critique of the remaining reported levels.

In the G.L.S. calculations, it turned out that also the other doublets of $4d^7$ were doubtful. Finally, only 16 levels were included in the calculation: the **F** and ⁴P of $4d^7$ and the (⁵D) ⁹D and (⁶D) ⁴D of d^8s .

After these calculations had been finished, we had the opprotunity to discuss the results with A. G. Shenstone and he told us that he had reached similar conclusions by comparing the spectrum of Rh III to the isoelectronic spectrum of Ru II, which he analyzed later.

We hope that the predictions of the G.L.S. will help to revise the analysis of this spectrum.

The parameters of the various stages of the calculation are given in table 3, the levels are given in table 13.

<u>Pd III - $(4a^{10} + 4a^{17}5s)$ </u>

In these configurations theory predicts 21 terms which split into 47 levels. In AEL 19 terms, splitting into 45 levels, are reported. Only the ${}^{1}S$ of $4d^{8}$ and the high 'D of $4d^{7}5s$ were not observed. The level assigned as $b {}^{3}D_{1}$ is reported in AEL as doubtful. It also deviates by about 700 cm⁻¹ from its calculated value, thus we did not include this level in the calculations.

In L.S. 1 the mean error was 157 and in L.S. 2 it reduced to 110. Because of the big distance between the configurations $4d^75s$ and $4d^8$ and the weak interaction between them the parameter H is not stable. Pd III is the only spectrum in the sequence in which the number of experimental levels is sufficient to make also the results of the separate treatment quite reliable.

The estimates of parameters of the various stages of the calculation are given in table 4. The observed and calculated levels are given in table 14.

$\underline{\operatorname{Ag\,III}} - (4d^9 + 4d^85s)$

These configurations consist of 8 terms which split into 18 levels. In AEL only the ²S of $d^{e_{s}}$ is not reported, and the ⁴P_{1/2} of $d^{e_{s}}$ is doubtful. Since also the deviation of this level from its calculated value is rather big, we excluded it from the calculations.

After performing Diag. 1 we saw that the level ${}^{z}P_{1/2}$ deviates by more than 1000 cm⁻¹ from its calculated value. In L.S. 1a, where it was included, the mean error was 461. In L.S. 1B, from which it was excluded, the mean error reduced to 112. Hence, we did not include this level in the general least squares.

Not having a sufficient amount of experimental material the parameter H was frozen in L.S. 1a and 1b. After having an interpolation formula for the parameter H we could see that we forced H to assume a value which was much bigger than the correct one. Since in the configuration $a^{B_{5}}$ the parameters H and α can compensate each other, this also caused an unjustified increase of α .

The estimates of parameters of the various stages of the calculation are reported in table 5, the energy levels—in table 15.

 $Cd_{111} - (4d^{10} + 4d^{2}5s)$

These configurations include only three terms which split into 5 levels. All are experimentally known.

There is no sense to perform any separate calculation of this spectrum. By including it in the G.L.S. we got an additional value for each of the parameters D', G, ζ' .

The observed and calculated levels are given in table 16.

5. The Interpolative Treatment of the Whole Sequence

5.1. General Description of the Procedure

In the general (interpolative) treatment the whole sequence is considered as one system, and the coefficients of the interpolation formulas are given the role of free parameters. We call these coefficients "General Parameters."

The parameters B, B', C, C', G, H, and α are represented by linear expressions of the form

$$\mathbf{P}(n) = \mathbf{P} + \Delta \mathbf{P} \cdot \mathbf{x},\tag{3}$$

and the parameters D', ζ , ζ' by quadratic expressions of the form

$$\mathbf{P}(n) = \overline{\mathbf{P}} + \Delta \mathbf{P} \cdot \mathbf{x} + \Delta_2 \mathbf{P} \cdot \mathbf{y}, \tag{4}$$

where

$$x = n - 6$$
 (5a)

and

$$y = x^2 - 10$$
 (5b)

Here *n* is the total number of electrons in the states 4*d* and 5*s*. We consider only the coefficients \overline{P} , ΔP , and $\Delta_z P$ as independent parameters (the "general parameters"). The substitution of *x* and *y* for *n* and n^2 is used in order to get fairly orthogonal parameters.

By fitting the interpolation-formulas to the parameters of the separate treatments we obtain a set of initial general parameters. Using these parameters, we diagonalized the matrices of all spectra of the sequences; this is the "General Diagonalization" ("G. Diag.").

In the "General Least-Squares" ("G.L.S.") the known levels of all the spectra are compared with the results of the General Diagonalization. In this unified least-squares calculation only the general parameters specified in table 6 and the normalization parameters $M(d^n)$ are considered as free parameters.

5.2. The Actual Colculations

As a consequence of the separate treatment which was described in the previous chapter we had for the general treatment only 56 reliable observed terms which split into 130 levels. Because of the relatively small amount of experimental material we were forced to use also the results of Zr III and Ag III (which are not quite reliable) for the calculation of the initial interpolation formulas. For the formulas of D', ζ , and ζ' even the information from Y III or Cd III was used.

In the G.L.S. we had 30 free parameters: 22 general parameters and 8 additive parameters $M(d^{n})$. 25 of them are electrostatic interaction parameters and 5 are spin-orbit interaction parameters.

A total of 483 levels, belonging to 209 terms, were calculated. The *level mean error* of the G.L.S. is

$$\Delta_{G.L.S.} = 77 \text{ cm}^{-1}$$

and the term-mean-error is

$$\Delta_{0,\mathbf{LS}}^{\prime} = 91 \text{ cm}^{-1}$$

The general parameters of the G. Diag. and the improved general parameters which were obtained in the G.L.S. are given in table 6.

6. Conclusions

We shall use the results in order to evaluate the relative importance of the various improvements to the Slater approximation used in the present paper. Generally speaking an interaction (or a correctionterm) is important if, relative to other sequences of the transition elements [1-3] the parameter representing it has a large value and a small relative statistical uncertainty.

We see that the spin-orbit interaction is quite important, and it is certainly the most important correction in the right-hand side of the period. This fact can be seen also from the very mixed assignments given to the levels in tables 7 through 16.

The differences (B'-B), (C'-C), and $(\zeta'-\zeta)$ are much bigger than the uncertainties of these parameters. This means that it is important to allow these parameters to assume different values for the configurations $4d^n$ and $4d^{n-1}5s$.

The estimates of the parameter α is considerably smaller than in the iron group, but its standard error is much smaller than its value. This means that it is still necessary in order to improve the fit between the theoretical and experimental levels.

Contrary to the results in the first [6] and second [2] spectra of the palladium group, the interaction between the configurations $4d^n$ and $4d^{n-1}5s$ is rather unimportant in the right hand side of the present sequence. This fact manifests itself in the large standard errors of H and the small values it assumes.

Out of 10 spectra of the sequence there are 8 in which the amount of experimental material is not sufficient for a reliable separate treatment. Thus, in this sequence the interpolative method is not only the more reliable one – practically it is the only method which enables us to predict the energy-levels for all the third spectra of the palladium group. We hope that these predictions will help in their experimental observation.

7. Tables of Results* Part A: Parameters

TABLE 1. Parameters of Zr III - (4d³ + 4d5s)

| | Diag. 1 | L.S. 1* | G.L.S. |
|-----------|---|--|---|
| ASBCGHacu | 4840 16560 530 1600 - 3000 400 25 450 450 | $\begin{array}{c} 4807 \pm 3 \\ 16481 \pm 3 \\ 525 \pm 0.3 \\ 1829 \pm 2 \\ 2350 \pm 3 \\ fixed \\ 23 \pm 0.4 \\ 410 \pm 1.4 \\ 454 \pm 2.4 \end{array}$ | 4741 16593 532 1757 2454 376 34 411 461 |
| Δ | | 4 | |

"In tables 1-6 the number following the \pm sign in the L.S. standard error of the parameter estimate.

TABLE 2. Parameters of Nb 11 - (4d*+4d*5s)

| - | Diag. 1 | L.S. 1 | G.L.S. |
|------------------------------|--|--|--|
| A S'BBC C'GH a Z | 9260 25650 550 2200 2200 2400 400 0 560 560 | $\begin{array}{r} 9308 \pm 26\\ 26330 \pm 52\\ 563 \pm 2\\ 593 \pm 2\\ 2054 \pm 10\\ 2188 \pm 16\\ 2386 \pm 19\\ 388 \pm 7\\ 30 \pm 1\\ 544 \pm 11\\ 589 \pm 11\\ \end{array}$ | 9224 26485 559 592 2018 2210 2424 334 33 535 597 |
| Δ | | 34 | |

TABLE 5. Parameters of Ag III = (4d + 5s)⁶

| | Diag. 1 | L.S.]a | L.S. 16 | C.L.S. |
|--------------------------------------|---|---|--|--|
| A S B C G H a S | 1840 75290 770 3210 2270 400 20 1730 1730 | $1595 \pm 400 \\75465 \pm 480 \\841 \pm 33 \\3063 \pm 319 \\2413 \pm 127 \\fixed \\68 \pm 37 \\1846 \pm 261 \\2031 \pm 162$ | $1689 \pm 93 \\75037 \pm 115 \\804 \pm 8 \\3377 \pm 78 \\2236 \pm 33 \\fixed \\50 \pm 9 \\1846 \pm 61 \\1978 \pm 38$ | 1655 75125 778 3662 2244 82 27 1825 1959 |
| Δ | | 461 | 112 | |

 TABLE 6. Ceneral parameters in the third spectra of the palladium-group

| | G. Diag. | G.L.S. |
|--------------------------------|----------|---------------|
| D' | 48792 | 48746 + 34 |
| ۸D. | 8657 | 8666 ± 10 |
| A D' | 85 | 98±5 |
| Ť | 640 | 640 ± 4 |
| ÅŘ | 28 | 27 ± 1 |
| R | 691 | 685 ± 2 |
| $\overline{AB'}$ | 34 | 31 ± 1 |
| Ē | 2756.9 | 2803 ± 23 |
| ΔČ | 232.4 | 262 ± 8 |
| <u>₹</u> , | 2939.9 | 2939 ± 14 |
| ΔC' | 250.7 | 243 ± 6 |
| Ğ | 2318 | 2334 ± 10 |
| ΔG | - 24 | -31 ± 6 |
| Ĥ | 250 | 208 ± 24 |
| ΔH | - 40 | -42 ± 6 |
| a | 30 | 31 ± 2· |
| Δα | 0 | -0.9 ± 0.7 |
| τ | 1190 | 1193 ± 16 |
| ΔĽ | 221 | 215±6 |
| <u></u> [' | 1293 | 1291 ± 12 |
| Δζ' | 232 | 227 ± 4 |
| $\Delta_2\zeta=\Delta_2\zeta'$ | 15.5 | 13 ± 2 |
| Level mean error | | 77 |
| Term mean error | | 91 |

TABLE 3. Parameters of Rh III-(4d7+4d#5s)

| | Diag, 1 | L.S. la | L.S. 15 | L.S. 1e | G.L.S. |
|-------------|--|---|---|--|---|
| ANDECOCHANS | 11650 56750 669 713 3068 3194 2296 | $\begin{array}{c} 12717 \pm 1790 \\ 62083 \pm 2454 \\ 801 \pm 104 \\ 980 \pm 52 \\ 3616 \pm 547 \\ 3844 \pm 290 \\ 2316 \pm 297 \\ \hline \\ fixed \\ 1110 \pm 677 \\ 1673 \pm 490 \end{array}$ | 11792 ± 1560 70184 ± 1570 651 ± 14 1336 ± 74 3280 ± 57 2926 ± 76 2276 ± 35 fixed 1146 ± 54 1395 ± 78 | $11621 \pm 146 \\ 57185 \pm 222 \\ 647 \pm 21 \\ fixed \\ 3293 \pm 56 \\ fixed \\ 2304 \pm 33 \\ \hline 24 \pm 17 \\ 1141 \pm 60 \\ 1381 \pm 102 \\ \hline $ | 11895 56964 667 716 3062 3178 2304 165 29 1291 1401 |
| л | | 8] | 33 | 22 | 16 |
| 4 | | 3094 | 273 | 235 | |

n = number of levels included in the L. S. calculations.

TABLE 4. Parameters of Pd (1)-(4d+5s)*

| _ | Diag. J | L.S. 1 | Diag. 2 | L,Ş. 2 | G.L.S. |
|--------------|--|--|--|--|--|
| ASBBCCGH a Z | *8100 65100 800 2500 3100 2270 385 40 1300 1530 | $\begin{array}{c} 7613 \pm 105 \\ 65836 \pm 159 \\ 699 \pm 13 \\ 747 \pm 5 \\ 3221 \pm 92 \\ 3429 \pm 25 \\ 2277 \pm 24 \\ 146 \pm 56 \\ 31 \pm 4 \\ 1664 \pm 72 \\ 1681 \pm 26 \end{array}$ | 7600 65835 699 747 3221 3429 2277 235 31 1664 1681 | $\begin{array}{c} 7602\pm 90\\ 65827\pm 121\\ 695\pm 9\\ 744\pm 3\\ 3322\pm 67\\ 3445\pm 18\\ 2274\pm 18\\ 30\pm 70\\ 28\pm 3\\ 1519\pm 43\\ 1666\pm 18 \end{array}$ | 7663 65818 694 747 3328 3420 2274 124 28 1545 1667 |
| Δ | | 157 | | 110 | |

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Tables of Results Part B: Energy Levels

TABLE 7. Observed and calculated levels of Y in

| Curr | Term | | Observed | G.I | S. |
|------|--------|------------|--------------|-------------|------|
| | , icim | | Voserveu | Cale, | 0-C |
| 4d | a²D | 3/2 | 0.0 204.0 | 18 | - 18 |
| 5s | a²S | 5/2 1/2 | 7466.2 | 802 7371 | 95 |

| Conf. | Term | J | Observed | Observed G.L Cale. | |
|----------------|------------------|------------------|---|------------------------------|----------------------|
| ď | a ^s F | 23 | 0.00 681.0 | — L 683 | L -2 |
| d^2 d^2 | a'D a'P | 420 | 1486.4 5741.55 8062.07 8325.65 | 1488 5725 8045 8312 | -2 16 17 13 |
| d" ds | aKG (HD)aHD | 241 | 8836.2) 11048.70 18398.87 | 8833 11067 18382 | - 18 17 |
| d² ds | 'S (²D)ئD | 2 3 0 2 | 19533.35 (13832.0?) 25066.25 | 19532 24518 25122 | í 56 |

TABLE 8. Observed and calculated levels of Zr III

TABLE 10. Observed and calculated levels of Mo III

| _ | | _ | | _ | | |
|------------------|-------------------------------|-----------------------|--|---|---|---|
| | | | ~ . | | G.L.S. | Calc. |
| ∠oni. | Jerm | Ĺ | Observed | Cale. | 0-C | E |
| ď | ۶D | 0 1 2 3 4 | (0.00) (243.10) (669.60) (1225.20) (1873.80 | 40 275 688 1224 1847 | (- 40) (- 32) (- 18) (1) (27) | 1.500 1.499 1.498 1.497 |
| ď | яÞ | 0 1 2 | (11271.30) (12509.80) (14357.30) | 11328 12554 14373 | (~ 57) (- 44) (- 16) | 1.493 1.491 |
| ď | ₽Ή | 4 5 6 | (12630.31) (13201.34) (13741.54) | 12634 13201 13701 | (4) (0) (41) | 0.843 1.043 1.167 |
| ď | ዣ∰+≁G ዣ+≁G+≁ዝ | 2 3 4 | (13927.76) (13947.40) (14295.85) | 13923 13924 14233 | (5) (23) (63) | 0.675 1.015 1.185 |
| * | \$ <u>G</u> +\$F ₹G | 3 4 5 | (15672.25) (16143.15) (16763.14) | 15835 16224 16629 | (— 163) (— 81) (134) | 0.822 1.067 1.190 |
| 8 8 8 8 | որ Մ | 321640 | (19390.90) 19783.28 (19995.50) | 19391 19493 19806 19754 20377 | (0) 290 (190) | 1.329 1.160 0.509 1.003 1.008 |
| 6.9.6 | ъ Ф | ¥ 2 3 | | 22555 23221 26903 | Ē | 1.011 1.005 |
| ď | 3F | 2 1 0 | (30992.50) (32292.70) (32887.80) | 310 9 6 32323 32976 | (93) (30) (88) | 1.495 1.493 |
| ď | Ŧ | 4 3 2 | (31932.50) (32142.80) (32126.50) | 31970 32252 32112 | (~ 37) (- 109) (15) | 1.245 1.082 0.672 |
| d®s | (ጥ)ኝዮ | 1 2 3 4 5 | (32419.44) (32844.04) (33453.10) (34226.01) (35130.10) | 32439 32854 33459 34227 35122 | (-20) (-10) (-6) (-1) (8) | 0.010 1.000 1.249 1.349 1.398 |
| d" | νG | 4 | | 36033 | | 1.005 |
| d [₽] s | (ሞ)ነዋ ፤ <u>የ</u> +፣ፑ ፣P | 1 2 3 | (42405.50) (42665.90) (43462.69) | 42389 42652 43420 | (17) (14) (43) | 2.473 1.378 1.596 |
| d ³ s | (<u>4F)*F</u> +*P (4F)*F | 2 3 4 | (42605.84) (43562.61) (44656.23) | 42526 43557 44646 | (80) (6) (10) | 1.112 1.142 1.231 |
| d ^e s | (*G)®G | 3 4 5 | (46557.96) (46581.03) | 46227 46544 46921 | (14) (340) | 0.763).053).185 |
| ď | ۲D | 2 | | 47541 | | 1.007 |
| d ^a s | δ 5 +3D Ωε+3D | 0 1 2 | (48753,45) (49052.05) | 48707 48636 48972 | (117) (80) | 1.159 1.383 |
| d₽s | H4(H*) | 4 5 6 | | 49460 50272 50459 | | 0.835 1.048 1.167 |

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TABLE 9. Observed and calculated levels of Nb III

| | | | | | G.L. | .s. | | |
|----------|------------------|-----------------------------------|-------|---------------|-------|--------|------------|---|
| Iglesias | Conf. | Term | 1 | Ob- served | Calc. | 0-с | Cale. # | |
| | | | | | | | | |
| | æ | a¶* | 3/2 | 0.0 | 63 | -63 | 0.403 | |
| | | | 5/2 | 315.8 | 200 | - 49 | 1.029 | |
| | | | 010 | 1020.0 | 1200 | 1 - 32 | 1.231 | |
| | | | 110 | 0664.0 | 9614 | 1 | 7 420 | |
| | a. | a.r. | 210 | 9607.5 | 9562 | 45 | 1 690 | |
| | | | 512 | 0503.7 | 0.002 | 109 | 1.506 | |
| | ا هر | a%) | 7/2 | 9236 1 | 9215 | 21 | 0.896 | |
| | " | | 9/2 | 9804.5 | 0761 | 44 | 1 808 | |
| | ഷ | ъP | 1/2 | 7004.0 | 10753 | | 0.904 | |
| a²D | 1 | $^{2}P + ^{4}P + ^{2}D$ | 3/2 | 10912.2 | 10959 | - 46 | 1.307 | |
| | æ | | 9/2 | 12916.4 | 12856 | 60 | 0.925 | |
| | - | | 10/2 | 13263.8 | 13163 | 81 | 1.091 | |
| | ഷ | - ው + ጥ | 3/2 | | 12894 | | 0.928 | |
| | ľ | 7 20 | 5/2 | 13094.01 | 13041 | 53 | 1.203 | |
| | da | a ² F | 7/2 | 19861.0 | 19907 | - 46 | 1.142 | |
| | - | | 5/2 | 19975.0 | 20061 | -86 | 0.857 | 1 |
| | d ² s | (FD&F | 3/2 | 25220.2 | 25248 | -28 | 0.403 | |
| | | | 5/2 | 25735.2 | 25759 | - 23 | 1.029 | 1 |
| | | | 7/2 | 26463.7 | 26481 | - 18 | 1.238 | |
| | | | 9/2 | 27373.5 | 27382 | -9 | 1.333 | |
| | ď | ۵D | 5/2 | | 31463 | | 1.197 | |
| • | | | - 3/2 | | 31785 | | 0.800 | |
| | d ² s | (*F)6*F | 5/2 | 33658.0 | 33650 | 8 | 0.894 | ļ |
| | | | 7/2 | 35079.2 | 35060 | 19 | 1.141 | |
| | d ^a s | (*P)&*P | 1/2 | 34514.5 | 34500 | 15 | 2.664 | |
| | | | 3/2 | 34807.2 | 34797 | 10 | 1.704 | |
| | | _¶+²D | 5/2 | 34989.8 | 34983 | 7 | 1.507 | |
| | d ² s | (¹ D)b ^z D | 3/2 | 36535.7 | 36577 | -42 | 0.832 | |
| | | <u>*</u> P + P | 5/2 | 37114.7 | 37105 | 10 | 1.258 | |
| | d ^a s | (°G) b° C | 9/2 | 40875.2 | 40939 | - 64 | 1.112 | |
| | | | 7/2 | 40943.9 | 40959 | -15 | 0.891 | |
| | d ² 5 | (*P)*P | 1/2 | | 43004 | [| 0.672 | 1 |
| | | | 3/2 | | 43729 | | 1.328 | |
| | d^2S | (°S)°S | 1/2 | | 57154 | | 1.997 | 1 |

TABLE 10. Observed and calculated levels of Mont-Continued

TABLE 11. Calculated Levels of To III-Continued

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| _ | | _ | | | _ | | | _ | | • | | - |
|--------------------|---|----------------|-------------|-----------------|----------|----------------------|----------------|-----|----------------------|----|----------------------------------|----|
| Conf | Torm | | Ohaan | | | G.1 | S . | | Cala | } | Conf. | |
| 000 | .6111 | | | eu. | 0 | lale. | 0- | С | S S | ļ. | | 1 |
| d ^a s | ₽D+₽P+P | 1 | | | 5 | 0200 | | | 0.946 | | | 1 |
| | *D *D | 23 | | l | 9 5 | 1289 1204 | | | 1.333 | | 44 | Ĺ |
| đ ^a s | (°C)'G | 4 | | | 5 | 2519 | | | 0.985 | | q2 | |
| d^0s | (*P)?P aP+12+ars | ę | | | 5 | 3082 | | | 1 284 | Ι. | ศ ^ร ส ^ร | |
| | -1+1+0 (•₽) [#] ₽ | 2 | | | 5 | 3858 | | | 1.487 | | d ^a s | |
| d^3s | (*H)'H | 5 | | | 54 | 4931 | | | 1.002 | | | i |
| d ^a s | પથ+ <u>વ</u> ા | 1 | | | 5 | 5174 | | | 1.133 | | æ | |
| d ⁹ s | $(a^2 \mathbf{D})^{\dagger} \mathbf{D}$ | 2 | | | 54 | 6633 | | | 1.001 | | d ^a s | İ. |
| d ^o s j | (*F)*F | 43 | | | 51 51 | 8811 8960 | | | 1.249 1.084 | | | |
| | | 2 | | | 5 | 9121 | | | 0.672 | | | |
| d* | 'S | 0 | | | 6 | 1910 | | | | | đ | Ì |
| d ³ 1 | (*F) ¹ F | 3 | | | 6 | 4072 | | | 1.004 | | d ⁴ s | |
| 4°5 | (<i>b</i> *D)*D | 2 | | | 7 | 1390 1793 1040 | | | 1.329 | | d*s | |
| ر م ي | (å²D⊮D | 2 | | | 7 | 6 88 7 | | | 1.000 | | | |
| | Tae | LLE Ì | 11. Cate | ulatee | i lei | vels of 1 | ľe m | | | ' | d*s | |
| Conf. | 1 | Гегп | 1 | , | _ | G.L | .s. | | Cale. | | d ⁶ | |
| | | | | | | | | | E | | d ⁴ s | |
| d ⁵ | | •5 40 | | 5/) 5/ | 2 | - 101 | - 2 70 | ן ו | .997 | | | |
| •• | | ^v | | 7/3 9/3 | 2 | 193 194 | 43 42 | | | | d"s | |
| ď | 4 | >+1 | D | 11/ 5/ | 22 | 193 209 | 98 87 | | .271 .510 | | ct 8 | |
| | - | - | | $\frac{3!}{1!}$ | 2 | 213 217 | 08 59 | | . 564 207 | ╞ | d ⁴ s | |
| ď | 1 | םי ≥+י | P | 7/3 5/3 | 2 | 230 238 | 07 49 | | .422 .430 | | | ļ |
| | ł | | | 3/) | 2 | 238 | 50 02 | | | | d ¹⁴ s | |
| des A | | -1) _ 2 | F | 13/2 | 2 | 281 285 205 | 53 21 26 | | .935 .077 .075 | | 6 ** 3 | |
| | 1 <u>*</u> | ≤')+1 | F | 3/2 | 2 | 302 | 99 | | .681 | | d^{*s} | |
| ď | | - - -+ * | G | 9/: | 2 | 313 | 08 | 1 | .292 | | et*s | ŀ |
| | 1 | (+T | F | 7/3 | 2 | 312 | 91 | 1 | ,182 | | .H. | |
| | 4 | ▲F ` + 의 | D | 5/) 3/) | 2 | 317 324 | 46 63 | 1 | .015 1.534 | | d ⁴ s | |
| æ | | + • | F | 7/3 | 2 | 321 | 62 | 1 | .171 | | d ^a s | 1 |
| | 4 ° | (+ 1 | D | 5/3 | 2 | 337 | 89 | l | .002 | | d ^a s | |
| d ^E | ן י ₽+ | °C - | רי ד | 9/: | 2 | 336 | 12 | I | .028 | | | ł |

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| | | <u></u> | | |
|--------------------------------------|--|--------------------|-------------------------|-------------------------|
| Conf. | Тегт | J | G.L.S. | Cale. S |
| đ | *H *C *C+*H | 11/2 7/2 9/2 | 34954 34555 35662 | 1,083 0.915 1.034 |
| ds | 2F | 7/2 | 36640 | 1.146 |
| ര് | *S. 2D | 5/2 1/2 3/2 | 30000 39605 44478 | 0.872 1.997 0.801 |
| u- d ⁴ s | t ^a D ^a tD | 5/2 1/2 | 44737 | 1.193 |
| | | 3/2 5/2 | 45063 45607 46287 | 1.864 1.656 1.585 |
| æ | °G | 9/2 9/2 | 47069 49288 | 1.553 |
| d's | (*D)*D | 7/2 1/2 | 49405 56604 | 0.891 0.053 |
| | | 372 5/2 7/2 | 57168 57959 58847 | 1.367 1.427 |
| đ | *P | 3/2 | 58686 | 1.317 |
| d ^a s | (<i>a</i> ³P)⁺P | 1/2 1/2 3(2 | 58938 61309 69857 | 0.660 2.613 1.716 |
| d*s | (*H)4H | 5/2 7/2 | 65015 61772 | 1.584 0.670 |
| | | 9/2 11/2 | 62063 62579 | 1.001 1.141 |
| d*s | (03F)4F (118F14F + 4C | 13/2 3/2 5/2 | 63738 63609 | 1.228 0.419 0.928 |
| | | 7/2 9/2 | 63808 64055 | 1.156 1.278 |
| и ^в | °D | 5/2 3/2 | 64334 64525 | 1.195 0.805 |
| ďs | (<u>*G)*G</u> + *P | 5/2 7/2 9/2 | 65388 66037 66416 | 0.692 |
| d"s | $({}^{3}C){}^{4}C$ $(\underline{a}{}^{3}P){}^{2}P + {}^{4}D$ | 11/2 1/2 | 66569 68826 | 1.259 0.564 |
| d's | (<i>a</i> ³P)²P (³H)²H ²H + ²] | 3/2 9/2 11/2 | 71968 69062 69934 | 1.309 0.933 1.071 |
| d"s | (^a D)∔D | 7/2 5/2 | 69731 69916 | 1.420 1.356 |
| | $^{+}\mathbf{D} + ^{2}\mathbf{P}$ | 3/2 1/2 | 69973 70649 | 1.206 0.170 |
| d ^a s d ^a s | (a ³ F) ³ F | 7/2 5/2 | 70791 71320 | 1.066 0.882 |
| | (²[)²[² <u>ĭ</u> +²H | 13/2 11/2 | 72399 72703 | 1.079 0.949 |
| d*s | (*C)*Ġ (*C)*G + (*G)*C | 7/2 9/2 | 72503 7 3239 | 0. 899 1.112 |
| d*s | $({}^{4}\mathbf{G}){}^{2}\mathbf{G} + ({}^{2}\mathbf{G}){}^{2}\mathbf{G}$ ${}^{2}\mathbf{G} + {}^{2}\mathbf{F}$ | 9/2 7/2 | 74267 74648 | 1.098 0.966 |
| d ^a s d ^a s | (a¹S)²S (¹D)²D + (³D)²D | 1/2 3/2 | 76572 76635 | 1.966 0,807 |
| d ^a s | $({}^{a}D){}^{a}D + ({}^{i}D){}^{a}D$ | 5/2 5/2 3/2 | 77879 77018 78766 | 1.197 1.187 0.809 |
| d*s | ('F) ' F | 7/2 5/2 | 81046 81264 | 1.153 |
| 1 | | | | 1 1 |

441

Conf. Term J G.L.S. Cale. ø, d's (6³P)*P 83340 5/2 1.585 3/2 1/2 84675 1.697 2.650 1.330 85616 9/2 $d^{\dagger}s$ 84019 (6°F)*F 7/2 84506 1.227 5/2 3/2 84501 1.019 84305 0.442 d⁴s (**δ¹F**)¹F + [±]G 7/2 90827 1.039 (*b**F)*F 0.860 5/2 91454 (bPPP d s 3/2 1/2 91036 1.334 92733 0.678 d"s (b'G)²G 9/2 91658 1.113 ¥G+¥F 7/292142 0.993 d"s (ሪካው)ቸው 3/2104753 0.800 5/2 1/2 104764 1.200 $d^{4}s$ (JPSPS 120665 1.999

TABLE 11. Calculated levels of Tc III - Continued

| d45 | . (5 | 'S)'S | 8 | 1/2 | 1206 | 65 | 1.999 | d®s | (⁴D)⁵D ³D++ >P | 43 | | 55985 57107 | 1 | 1.493 1.542 |
|---------------|--|-------------|----------------------------|-------|----------------------------------|-------------|--------------------------------|--------------------------------------|--|------------------|---|-------------------------|---|-------------------------|
| | TABLE 12. | 0 | bserved and | colcu | lated let | els of Ru t | | | - •D | 2 1 0 | : | 57152 56727 56198 | | 1.600 1.726 |
| Conf. | Term | J | Observed | | G.L Cale. | s. 0C | Calc. | æs | (*C)4G | 3 4 5 | | 60682 60980 60957 | | 0.771 1.054 1.195 |
| | | | | | | ~ | | a | <u>(ዋ/ዋ</u> +³D | 2 | | 62624 63453 | | 1.323 |
| ſ | u°D | 3 | 1158.8 | | - 35 | 35 20 | 1.496 | | P | Ō | | 64541 | | |
| | | 1 0 | 1826.3 2266.3 2476.0 | | 1827 2279 2495 | | 1.498 1.498 | a s | [*([*) | 5 6 7 | | 64001 64093 64422 | | 0.847 1.030 1.143 |
| æ | ³ H+3F+3Ç 3 <u>H</u> +3G 3H | 4 5 6 | | | 15028 15326 15081 | | 0.994 1.065 1.162 | æs | (<u>1D)</u> 3D+3F 3D 3D - 3D | 32 | | 65012 66051 | | 1.294 |
| ď | ۶P | 2 1 0 | | | 15092 18412 19048 | | 1. 486 1 .454 | d ^a s | * <u>P</u> +*P (<u>*F)*F</u> +*P *F *F |) 1 2 3 | | 65273 65406 65724 | | 0.316 1.054 1.275 |
| æ | ୬F+୬H ୬F+୬G | 43 | | | 16824 16857 | | 1.043 1.025 | | 3F 3F+3F+5F | 45 | | 65554 65454 66565 | | 1.336 |
| æ | अ भ्⊆+ग अट+ग्रह | 2 5 4 | | | 17357 18612 19611 | | 0.677 | d ⁷⁵ 5 | *D++*F++D *D++*F++P *F++P | 212 | | 69516 68811 67522 | | 1.006 0.497 0.984 |
| | 3D | 3 | | | 19878 | | 0.814 | | ³F+²C+³D ³ F | 3 4 | | 70165 68919 | | 1,040 1.241 |
| | u. | 23 | | | 22319 22644 | | 1.171 | d ^ь s d ^ъ s | (²1)¹]+²H ° <u>H</u> +²G | 6 4 5 | | 68535 70311 72693 | | 1.002 0.923 1.110 |
| 6 6 1 6 | 'G ('S) <i>a</i> *S 'S | 4 3 0 | 27162.8 | | 23209 24503 27177 27242 | -14 | 1.004 1.006 1.997 | đ | »H+ıI »G+»H | 0 5 4 | | 72408 70511 72228 | | 1.139 1.126 0.965 |
| đ đ | ባ) የF 40 | 23 | | | 28412 31296 34042 | | 1.008 | | ^a G+ ^a F | 3 | | 71472 | | 0.908 |
| u- | -r | 12 | | | 35818 38006 | | 1.498 1.491 | d ^a s | 'S (a²D)'D+²F | 2 | | 73602 | | 0.892 |
| æ | ₽F | 4 3 2 | | | 36927 37559 37008 | | 1.244 1.079 0.671 | ars. | 4 <u>F</u> +₁F 11+1945 | 2 3 4 | | 73625 73412 73715 | | 0.705 1.059 1.227 |

TABLE 12. Observed and calculated levels of Rum-Continued

Observed

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Term

(*S)a*S 'G (*G)*G

(*P?P++D

٩D

J

 $\frac{2}{4}$

3 4

5 6

3

2

ī

2

Conf.

d 5

ď

d⁶s

d s

d^a

G.L.S.

 $\mathbf{0} - \mathbf{C}$

_.g

Calc.

41121

42394

51433

51551

51674

51743

51703

53614

53937

54432

54879

Calc.

6

1.992

1.005 0.345

0.924

1,152

1.266

1.332

1.600

1.701

2.257

1.013

.

TABLE 12. Observed and calculated levels of Ru III - Continued

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TABLE 13. Observed and calculated levels of Rh III - Continued

| c | T | | Observed. | Ģ | Cala | | | | | | |
|------------------|-----------------------------------|----------|-----------|--------|------|------------|--|--|--|--|--|
| Cont. | | | Observed | Çalc. | 0-C | Laic. B | | | | | |
| d ^a s | (ዋና) የ | 4 | | 74832 | | 1.184 | | | | | |
| | ³ F+'F | 3 | | 74904 | | 1.063 | | | | | |
| | ³F | 2 | | 76138 | | 0.738 | | | | | |
| æs. | (°F)'F+°F | 3 | | 75145 | | 1.050 | | | | | |
| a™s | H ¹ (H [*]) | 5 | | 76539 | | 1.008 | | | | | |
| d ^e s | (*C)°C-+*F | A | | 77177 | | 1.071 | | | | | |
| de s | (°SPS | 1 | | 77522 | | 1.997 | | | | | |
| d ⁵ s | (*F)'F | 3 | | 78799 | | 1.027 | | | | | |
| <i>a</i> . | (*\$)*5 | Ų. | | 82821 | | 0.000 | | | | | |
| æs. | (9-05-0 | 5 | | 82910 | | 0.502 | | | | | |
| | | 3 | | 83477 | | 1.311 | | | | | |
| æs | ריינסי <i>א</i> ו | 2 | | 87969 | | 0.999 | | | | | |
| d's | Č ² G) ² G | 5 | | 88207 | | 1.200 | | | | | |
| | | 4 | | 88335 | | 1.051 | | | | | |
| | | 3 | | 88434 | | 0.754 | | | | | |
| æs | (°G)'G | 4 | | 92963 | | 1.001 | | | | | |
| d's | (*P)*P | 2 | | 99093 | | 1.490 | | | | | |
| | | | | 99316 | | 1.486 | | | | | |
| | | ° | | 99513 | | | | | | | |
| d ⁶ s | (*P)'P+*D | 1 | | 103479 | | 0.923 | | | | | |
| ds | (cªD)PD | 3 | | 105494 | | 1.333 | | | | | |
| | | 2 | | 105701 | | 1.172 | | | | | |
| | | 1 | | 106119 | | 0.595 | | | | | |
| d ^a s | (c [#] D) ⁱ D | 2 | | 110249 | | 1.003 | | | | | |
| | | | | | | | | | | | |

| TABLE 13. Observed | i and | catea | lated | leveli | s of | R | a II | 1 |
|--------------------|-------|-------|-------|--------|------|---|------|---|
|--------------------|-------|-------|-------|--------|------|---|------|---|

| | - · · | | | | | _ |
|-------|------------------|------|----------|-------|------|---------|
| Conf. | Term | , | Observed | G.L | .s. | Calc. e |
| | | | | Cale. | 0-с | |
| d' | a'F | 9/2 | 0,0 | - 25 | 25 | 1.327 |
| | | 7/2 | 2147.8 | 2124 | 24 | 1.236 |
| | | 5/2 | 3485.7 | 3476 | 9 | 1.031 |
| _ | | 3/2 | 4322.0 | 4328 | -6 | 0.414 |
| d7 | a ⁴ P | 5/2 | 11062.3 | 11060 | 2 | 1.592 |
| | 1 <u>1</u> + 1 | 3/2 | 10997.1 | 11085 | - 88 | 1.642 |
| | | 1/2 | 12469.8 | 12519 | -50 | 2.507 |
| a. | 16 | 9/2 | | 13092 | | 1.093 |
| | 2D 1 2D 1 4D | 112 | | 15229 | | 1 150 |
| a. | 3D + 4D | 3/2 | | 19359 | | 0.827 |
| | 1 - 1 | 1/2 | | 10457 | | 0.027 |
| ď | 41 | 11/2 | | 17317 | | 1.091 |
| | | 9/2 | | 19500 | | 0.931 |
| ď | *D | 5/2 | | 18436 | | 1,203 |
| | l ≇D+åb | 3/2 | ! | 21873 | | 0.960 |
| ď | 2F | 5/2 | 1 | 26708 | | 0.863 |
| _ | - | 7/2 | | 27889 | | 1.140 |
| ď | 4P | 3/2 | | 42251 | | 0.800 |
| | | 5/2 | | 43173 | | 1.196 |
| a"s | (°D)a*D | 9/2 | 43022.0 | 43010 | 12 | 1.552 |
| | | 7/2 | 44394.4 | 44385 | 9 | 1.584 |
| | | 5/2 | 45278.2 | 45274 | 4 | 1.654 |
| | | 3/2 | 45876.6 | 45876 | 1 | 1.862 |
| | | 119 | 46227.1 | 46230 | -3 i | 3 317 |

| Conf. | Conf. Term | | Observed | G.L | Calc. g | |
|--------------------|--|--------------------------|--|----------------------------------|----------------------|----------------------------------|
| | | | | Ćale. | 0-C | |
| d ^{is} s | (⁵D)a⁴D | 7/2 5/2 3/2 1/2 | 54632.2 56125.7 57012.5 57531.3 | 54576 56109 57013 57545 | 56 17 0 -14 | 1.418 1.370 1.200 0.023 |
| a®s. | (³H)⁴H ⁴H + ⁺G | 13/2 11/2 | | 62412 62573 | | 1.227 1.153 |
| d ^a s . | <u>чн</u> +чс+ч (а ^з Р)чР | 9/2 7/2 5/2 | | 62416 62857 62555 | | 1.091 0.796 1.585 |
| đ ^a s | ٩F+٩H | 3/2 1/2 9/2 7/2 | | 65466 67426 64224 64732 | | 1.574 2.523 1.191 1.081 |
| | ⁴F+⁴G | 5/2 | | 64864 | | 0.957 |
| | (PF)¶F | 3/2 | i | 65263 | | 0. 492 |
| d ^a s | <u>€</u> +4H | 11/2 | | 66126 | | 1.236 |
| .#8.e | 4 <u>C</u> +4F ⊛म्राज्य | 9/2 7/2 5/2 | | 67620 68041 67796 69678 | | 1.175 1.020 0.668 |
| 0-3 | ₩ + + | 9/2 | | 69710 | | 0.964 |
| d ^e s . | $\mathbf{F} + \mathbf{C} + \mathbf{D}$ | 7/2 | | 70567 | | 1.123 |
| d"s | (³ F) ³ F *P+*D+*P * <u>P</u> +*S | 5/2 3/2 1/2 | | 72351 70583 73950 | | 0.871 1.345 0.842 |
| దిం | $(^{a}D)^{4}D$ $^{4}D + ^{4}P$ | 1/2 3/2 | | 70819 71264 | | 0.159 1.236 |
| | ۴D | 5/2 7/2 | | 70984 71445 | | 1.361 |
| d ^e s | (°C)°C | 9/2 | | 73708 | | 1.089 |
| d ^a s | P(P) | 13/2 | | 74084 | | 1.080 |
| d"s | $(a^{1}G)^{2}G$ $^{2}G + ^{2}F$ | 9/2 7/2 | | 76094 76404 | | 0.939 1.096 0.945 |
| d [®] s | (3D) *D | 3/2 5/2 | | 77596 | | 0.821 |
| d s | *S+*P+*P | 1/2 | | 79502 | | 1.847 |
| d°1 | (a'D)*D | 5/2 3/2 | | 80313 80439 | | 0.810 |
| d's | ('F)*F | 7/2 5/2 | | 82984 83130 | | 0.886 |
| d ^a s | (<i>b</i> [*] ₽) ⁴ ₽ | 1/2 3/2 | | 85311 86279 | i | 2.601 1.718 |
| de. | (METHE | 5/2 | | 88927 87320 | | 1.579 |
| | | 7/2 | | 88264 89090 | i ľ | 1.221 |
| d ^a s | (d⁰P)⁴P | 3/2 3/2 1/2 3/2 | | 87453 92424 95311 | | 0.412 0.687 1.330 |
| a s | ±π_+∎G | 7/2 | | 94021 | | 1.093 |
| d"s | (<i>b</i> ³F)²F (b³G)²G ²G + ²F | 5/2 9/2 7/2 | | 94542 95741 96104 | | 0.862 1.114 0.940 |
| d ^a s | (<i>b</i> ¹ D) ⁴ D | 5/2 | | 110016 | | 1.200 |
| dēs | (6 ¹ S)*S | $\frac{3/2}{1/2}$ | ļ | 128531 | | 0.801 1.999 |

6

| <u> </u> | | | | | | | |
|----------|------------------|---|----------|-------------|--------|----------|-------|
| 1.51 | C | T | , | 0 | G.L | G.L.S. | |
| AEL | Conf. | Term | | Observed | Cale. | 0-C | Calc. |
| | - | - | | | 1 | | |
| | đ | a³F` | 4 | 0.0 | 2 | -2 | 1.248 |
| 1 | | | 3 | 3229.7 | 3227 | <u>8</u> | 1.083 |
| | | | 1 | 9001.0 | 4:20 | • | 0.714 |
| a۹D | ď | a*P+∙D | 2 | 10230.5 | 10330 | -99 | 1.284 |
| | 1 | 3 ₽ | 1 | 13470.3 | 13394 | 76 | 1.500 |
| | | | 0 | 13699.1 | 13636 | 63 | |
| _a3₽. | <i></i> #8 | ann+ap | 2 | 14634.3 | 14768 | -133 | 1 168 |
| | đ | a'G | 1 a | 17880.4 | 17824 | 56 | 1.002 |
| | d. | is | Ó | | 41196 | | |
| | d"s | (*F)a*F | 5 | 52915.9 | 52885 | 31 | 1.395 |
| | | | 4 | 55088.8 | 55040 | 49 | 1.344 |
| | | l | 2 | 57845.0 | 57806 | 39 | 1.240 |
| | | | Î | 58527.3 | 58492 | 36 | 0.017 |
| | d ^r s | (*F)62F | 4 | 62560.9 | 62397 | 163 | 1.242 |
| | | | 3 | 65255.4 | 65181 | 74 | 1.151 |
| | die. | (4D)-6D | 2 | 67079.4 | 65690 | 94 | 1 605 |
| ' | ** | | ž | 65788.3 | 65817 | -29 | 1.754 |
| | | | ī | 67151.4 | 67195 | -44 | 2.403 |
| | d ⁷ s | (°G)a°G | 5 | 69985.8 | 70034 | -49 | 1.185 |
| | | <u>∗</u> <u>c</u> +∗n | 4 | 71047.2 | 71027 | 20 | 1.022 |
| | л. | *G (2DMD | 3 | 72786.1 | 72791 | -4 | 0,759 |
| | 64-3 | | 1 | 72009.6 | 72006 | -115 | 1.001 |
| | | 12D13D- | | 749911 | 74390 | -30 | 1.239 |
| | | | ľ | 14401.1 | (1020 | -30 | |
| | đ's | (² H)a ³ H | 6 | 74673.3 | 74741 | ~67 | 1.167 |
| 1 | | 1 | 5 | 75967.6 | 75971 | -4 | 1.040 |
| | | <u>а</u> Я+ьС | 4 | 78581.1 | 78525 | 56 | 0.890 |
| | d7. | CASH43C | A | 75403.0 | 75336 | 67 | 0.957 |
| | a's | (P) P | 2 | 75455.0 | 75447 | 8 | 1.430 |
| | | | 1 | 76055.8 | 76193 | -137 | 1.346 |
| | | (<u>'P)</u> ³ P+ (2P) ³ P | 0 | 78732.5 | 78682 | 50 | |
| | d's | (a ² D)a ³ D | 3 | 76231.4 | 76235 | -4 | 1.331 |
| | | aŭ+b+b+b+b | 2 | 78169.8 | 78125 | 45 | 1.176 |
| | | on+-h+ib | I I | 78120.0 | 78210 | -90 | 1.049 |
| | đs | (*H)a'H | 5 | 80805.1 | 80802 | 3 | 1.012 |
| | d's | ' <u>P</u> +³D+³P | ī | 82620.3 | 82809 | -189 | 0.925 |
| | đs | (a²D)c¹D+ ³₽+²D | 2 | 83204.3 | 83113 | 91 | 1.074 |
| | $a^{n}s$ | (°F)c°F | 2 | 85420.7 | 85494 | -74 | 0.678 |
| | | | 3 | 85830.4 | 85940 | -110 | 1.084 |
| | | | •4 | 86795.2 | 86937 | -142 | 1.246 |
| | $d^{T_{S}}$ | (⁷ E)a ¹ E | 3 | 90684.3 | 90857 | -173 | 1.004 |
| ļĮ | $d^{7}s$ | (b *D) b* D | l ï | (103529.4?) | 102858 | | 0.501 |
| | | | 2 | 103549.6 | 103296 | 254 | 1.160 |
| | | | 3 | 104419,1 | 104124 | 295 | 1.327 |
| | đi | (<i>6</i> ⁰D)¹D | 2 | | 108183 | | 1.002 |

TABLE 14. Observed and calculated levels of Pd III

TABLE 15. Observed and calculated levels of Ag in

| C f | T | | 0 | G.L | Cala | |
|------------------|-----------------------|-----|----------|--------|------|------------|
| Loni. | Lerm | J | Observed | Calc. | 0-C | Calc. 6 |
| a ^p | ۵ | 5/2 | 0 | 23 | 23 | 1.200 |
| | | 3/2 | 4607 | 4587 | 20 | 0.800 |
| , 5 . | BEWIE | 0/2 | 63250 | 63283 | -33 | 1.332 |
| | (1/4- | 7/2 | 65764 | 65744 | 20 | 1.226 |
| | | 5/2 | 68145 | 68146 | -1 | 1.031 |
| | | 3/2 | 69351 | 69360 | -9 | 0.440 |
| | መካለም | 719 | 71601 | 71570 | 113 | 1 151 |
| 0-3 | Ψ+*D+*P | 5/2 | 73934 | 73955 | -21 | 1.135 |
| | - | | | | | |
| d ⁸ s | ⁴ <u>₽</u> +⁴F | 5/2 | 76406 | 76415 | -9 | 1.284 |
| | 4 <u>P</u> +2D | 3/2 | 77413 | 77476 | -63 | 1.426 |
| | ዋ | 1/2 | (79326?) | 78938 | | 2.656 |
| đ. | 4D+4P+2P | 3/7 | 80131 | R0213 | | 1 180 |
| D • a | <u>ወ</u> +•P | 5/2 | 82231 | 82363 | -132 | 1.236 |
| | | | | | | |
| d ⁹ 5 | ²₽+²D | 3/2 | 85182 | 85216 | -34 | 1.212 |
| | | 1/2 | (87477) | 85512 | | 0.682 |
| <i>.</i> | (4G)/a ² G | 9/2 | 85599 | 85703 | -104 | 1.113 |
| | | 7/2 | 85727 | 85760 | -33 | 0.893 |
| d ^a s | ("S) ² S | 1/2 | | 111864 | | 1.994 |

TABLE 16. Observed and calculated levels of Cd III

| Cont | T | | Charact | 6.1 | Cala | |
|--------------|-----------------------------|------------------|--------------------------------------|--------------------------------|----------------------------|-------------------------|
| Com. | Jerm | ľ | Observed | Calc. | 0-C | 8 |
| d™ 67°5 | a ¹ S (*D)a*D | 0 3 2 1 | 0.0 80454.3 82354.6 86219.5 | -72 80540 82361 86237 | 72 86 6 18 | 1.332 1.125 0.500 |
| d P s | (²D)a¹D | 2 | 88871,8 | 88834 | 38 | 1.042 |

An Additional Remark. The calculations reported in the present paper had been completed about five years ago and then the results were sent to several spectroscopy groups. Some weeks ago, after the stencils for the preprints of this paper had already been typed, we received from Rico a reprint of his paper [7] on the spectrum of Mo III. In table I of his paper he compares his observed levels with our theoretical calculations and the fit is quite good. Checking these results we found out, that by adding to all the calcu-

lated levels of Mo III 80 cm⁻¹ the fit is very much improved and we get a mean error of 95 cm⁻¹ with $M(d^4)$ being the only free parameter. In table 10 we have added the observed levels of Mo III enclosed in brackets in order to indicate that they were not included in the G.L.S.

The author also was informed by L. Iglesias that now she is making a new analysis of Rh III. Hence, we already know that the calculations reported in the present paper actually help in the further analysis of the third spectra of the Pd group.

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