NIST Technical Note 1679

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http://dx.doi.org/10.6028/NIST.TN.1679

September 2009



U.S. Department of Commerce Gary Locke, Secretary

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National Institute of Standards and Technology Technical Note 1679 Natl. Inst. Stand. Technol. Technical Note 1679, 40 pages (September 2009) http://dx.doi.org/10.6028/NIST.TN.1679 CODEN: NTNOEF

Abstract

Ten commercial laboratories participated in an interlaboratory study to establish the repeatability and reproducibility of compression strength tests conducted according to ASTM International Standard Test Method E9. The test employed a cylindrical aluminum AA2024-T351 test specimen. Participants measured elastic modulus and 0.2 % offset yield strength, YS(0.2 % offset), using an extensometer attached to the specimen. The repeatability and reproducibility of the yield strength measurement, expressed as coefficient of variations were $cv_r = 0.011$ and $cv_R = 0.020$ The reproducibility of the test across the laboratories was among the best that has been reported for uniaxial tests. The reported data indicated that using diametrally opposed extensometers, instead of a single extensometer, doubled the precision of the test method. Laboratories that did not lubricate the ends of the specimen measured yield stresses and elastic moduli that were smaller than those measured in laboratories that lubricated the specimen ends. A finite element analysis of the test specimen deformation for frictionless and perfect friction could not explain the discrepancy, however. The modulus measured from stress-strain data were reanalyzed using a technique that finds the optimal fit range, and applies several quality checks to the data. The error in modulus measurements from stress-strain curves generally increased as the fit range decreased to less than 40 % of the stress range.

Keywords: compression, testing, ILS, ASTM, E9, yield strength, elastic modulus

1 Introduction

Compression testing is a conceptually simple method to establish the uniaxial stress-strain and mechanical behavior of materials. Because the test specimens can be right circular cylinders, they are easy to fabricate. The short gauge length of the test specimen sometimes makes it the only possible geometry for establishing some uniaxial properties, for example those normal to the plane of a plate. Compression tests can also be used to establish the strength of brittle materials [1, 2] that would be difficult to grip in tension. Kuhn [3] and Chait [4] have reviewed the methods for compression testing, and have demonstrated that although the test is conceptually simple, the user must overcome many experimental difficulties to translate the measured load and displacement curves into accurate stress-strain behavior.

Much of the literature, see Table 1, on implementing the compression test focuses on tests to large strains [5, 7, 8, 10, 12, 13, 17, 18], to establish strain-hardening behavior beyond the strains at which tension test specimens neck. Other studies are devoted to modelling processes such as upsetting [5, 14, 15, 17, 18]. A common theme in these and other studies has been to quantify the effects of friction [18, 7, 12] and barreling [5, 11, 17, 9] on interpreting the stress-strain behavior of the test specimen, or finding the optimal lubricant [4, 6, 12, 13].

ASTM International standard test method E9, [2] first established in 1924, is a consensus standard for conducting compression tests to establish the strength of materials. It contains methods for testing cylindrical test specimens as well as methods for testing sheets with lateral support. The standard contains requirements for calibrating and qualifying the testing machine including extensometers, and aligning the fixtures and test specimen. It recommends, but does not require, specific test specimen geometries and lubricants. In addition, it suggests several fixture designs. It does not require the use of an extensometer in contact with the test specimen to measure strain, and most studies that reference E9 infer the test specimen strain and stress from the displacement of the actuator.

Although the first version of E9 was released eight decades ago, its precision has never been formally evaluated, as required [19]. Such evaluations require a formal interlaboratory study, which can benefit both end user and testing laboratories. Users need the results of interlaboratory tests to determine the uncertainty that should be associated with the value of a material parameter obtained using a test method. Laboratories that employ test methods use interlaboratory studies to identify the deficiencies in their test methods and improve their implementation of them.

This manuscript reports the results of an interlaboratory study to establish the precision of ASTM International standard test method E9 for determining the yield strength and elastic modulus in compression. The results of this study were incorporated into the Precision and Bias statement of E9 in 2009. This report goes beyond the research report [20] that documents the calculation of the precision by comparing the results to other interlaboratory studies of uniaxial test methods, Sec. 4.1, analyzing some of the possi-

Reference	Content	e_{\max}	Materials	Lubricant
Banerjee, 1985[5]	b	1.6	Al	teflon, MoS_2 , oil, none
Carter, 1985[6]	F	0.35	Al	MoS_2 , none
Chait, 1975[4]	r	NA		
Cook, 1945[7]	f	0.7	Cu	none
Gunasekera, 1982[8]	f	1.2	1022 steel	teflon
Hsü, 1969[9]	bfF	NA	Cu	teflon
Kamaluddin, 2007[10]	F	0.8	Al	grease
Kobayashi, 1970[11]	b	1.4	1040 steel	graphite
Lovato, 1992[12]	f	1	Al, Nb, brass, steel	MoS ₂ , teflon, BN, none
Male, 1966[13]	f	0.8	Al, Ti, brass	graphite, lanolin, paraffin
Mescall, 1983[14]	F	NA	4340 steel	
Papirno, 1983[15]	0	NA	steel	teflon
Ray, 1983[16]	f	NA	steel	teflon
Schey, 1982[17]	b	1	1020 steel, 6061 Al	MoS_2 , teflon
Woodward, 1977[18]	f	1.2	steel	teflon
Key			Key to content of	reference
$e_{\max}:$ maximum strain	in test	b: barreling analysis		
NA : not available			f: friction analysi	s
			F: finite element	analysis
			r : review article	

Table 1: Summary of literature that analyzes the compression test.

Participant	URL
AADFW, Inc, Euless, Tx	http://www.aadfwinc.com
Alcoa, Pittsburgh, Pa	http://www.alcoa.com
Exova, Glendale Hts, IL	http://www.exova.com
Dickson Testing Company Inc., South Gate, Ca	http://www.dicksontesting.com/
Imperial College Mechanical Engr., London, England	http://www.imperial.ac.uk/
MAR-TEST, Inc. (Cincinnati), Cincinnati, Oh	http://www.mar-test.com/
MAR-TEST, Inc. (Stuart), Stuart, Fl	http://www.mar-test.com/
Metcut Research Inc., Cincinnati, Oh	http://www.metcut.com
Stork Climax Research Services, Wixom, MI	http://www.storksmt.com/crs
Westmoreland Mechanical Testing, Youngstown, Pa	http://www.wmtr.com

Table 2: List of participants in this study.

ble sources for the variability, Sec. 4.2, and presenting a method to evaluate the elastic modulus measured in the test, Sec. 4.3.

2 Experimental Procedure

This interlaboratory study followed the methods of ASTM E691 [21], and uses statistical terms in accord with ASTM E177 [22].

2.1 Participants

Using the ASTM International [23] and American Association for Laboratory Accreditation [24] laboratory directories, the organizers contacted and discussed the interlaboratory study with twenty-five possible laboratory participants. From this original list thirteen laboratories agreed and were able to participate, and ten ultimately completed the test program, Table 2.

2.2 Instructions and method

The participants followed ASTM Standard Test Method E9 [2] to establish the elastic modulus, E, and 0.2 % offset yield strength, YS(0.2 % offset). At the time of the study, the version of E9 in use was E9-89a, but the only non-editorial difference between E9-89a and the current version, E9-09 was the addition of the precision statement to the latter,

which was the purpose of the interlaboratory study. The participants also returned electronic traces of the stress-strain curves to the organizers. All compression fixtures were required to be qualified according to ASTM E9 Section 6.6 [2] using at least five of the supplied test specimens, unless the participant had already qualified the test setup according to E9 Section 6.6. The participants conducted the compression tests using at least one extensometer at a nominal strain rate of $de/dt = 0.005 \text{ min}^{-1} = 8.33 \times 10^{-5} \text{ s}^{-1}$. No laboratory reported strain measured from actuator displacement. Each participant reported ten items as required in sections 10.1.1–10.1.9 and 10.1.13 of standard method E9: Material (test specimen ID), configuration description, test specimen dimensions as tested, fixture and lubricant description, testing machine description, speed of testing (required in section 8.7; report actual value), stress-strain diagram, modulus of elasticity, *E*, yield strength, *YS*(0.2 % offset), and any anomalies.

2.3 Test Specimen

The material tested was aluminum alloy AA2024-T351, which is solution heat-treated and stress-relieved by controlled stretching. It was supplied as a plate with thickness, t = 22.2 mm (0.875 in), from which the organizers cut and distributed test specimen blanks, which were distributed throughout the plate. Figure 1 describes the location of the test specimens in the original plate and their numbering scheme. Only test specimens in rows 1 and 2 were used in this study. Test specimens number 1-50 came from row 1; test specimens 51–100 came from row 2. Figure 2 shows the test specimen with dimensions and tolerances. The drawing provided to the participants showed the dimensions in U.S.-Customary units, rather than SI units. Participants machined their own test specimens from sawed blanks that the organizers supplied.

Test specimens were tested with the loading axis transverse to the rolling direction in the plane of the plate, the so-called long-transverse ("LT") orientation, Mil-Handbook-5J [25] Figure 1.4.12.3(a). The test specimen ID takes the form "LT-NN-L-X" where "LT" identifies the orientation relative to the rolling direction, "NN" identifies the test specimen number (1–250), "L" identifies the laboratory that received the test specimen blank (A-K) and "X" identifies the test order of the test specimen at a given laboratory.

2.4 Compression fixtures

The participants used a variety of loading fixtures, some of which involved a sub-press mounted in the testing machine to improve alignment. Others used adjustable platens that were aligned and then locked. Three laboratories used diametrically opposed extensometers instead of a single extensometer. No laboratory reported strain from actuator displacement. Table 3 describes the specimen fixturing, alignment capability, number of extensometers, and the lubricant used in each laboratory.

3 Results

3.1 Stress-strain behavior

Figure 3 plots the engineering stress-strain curves by laboratory. For convenience, com-



Figure 1: Schematic of the location of test specimen blanks in the original plate.

Lab	test setup	Extensometer	Lubricant
А	No sub-press	Two, opposed, class B-1 G = 25.4 mm	Not reported
В	Sub-press	Single, class not reported G = 12.7 mm	Molybdenum disulfide
C	No sub-press, no spherical seat	Single, class not-reported G = 25.4 mm	None
E	sub-press	Single, class B-1 $G = 25.4 \text{ mm}$	Teflon tape
Н	No sub-press	Single class B-2, $G = 12.7 \text{ mm}$	Molybdenum disulfide
Ι	No sub-press	Two opposed, class B-2, G = 25.4 mm	Not reported
J	Precision ground sub-press, aligned to closer tolerance than required for specimen, no spherical seat	Two opposed, class B-1 G = 25.4 mm	None
K	No sub-press. Platens aligned, shimmed and then locked. No spherical seat	Single, class B-2, $G = 12.7 \text{ mm}$	Molybdenum disulfide
L	Sub-press	Single, class B-2 $G = 25.4 \text{ mm}$	WD-40
Μ	Compression platens mounted in aligned hydraulic grips	Single, class B-2, G not reported	None

Table 3: Descriptions of the compression setup, extensioneters and gauge lengths, G, and lubricants for all laboratories.



Figure 2: Dimensions of the test specimen used.

pressive strains and stresses are plotted as positive, rather than negative, values. In each case the stress-strain curve was shifted along the strain axis so that a linear fit to the stress-strain (S - e) data in the range (50 < S < 175) MPa intercepts the origin. Figure 4 presents four views of the same stress-strain curves over different strain ranges.

Table 4 summarizes the reported modulus, E, and yield strength, YS(0.2 % offset), for the laboratories. Figure 5 plots the reported elastic modulus, E, by laboratory. Figure 6 plots the reported 0.2 % offset yield strength, YS(0.2 % offset), by laboratory.

3.2 Testing rates

Figure 7 plots the strain as a function of time for the laboratories that reported time data. The interlaboratory instructions did not specify a control mode for the test. Four laboratories (C,H,K,L) conducted the test in strain control from the extensometer signal, as indicated from the constant slope of the strain-time plot, Figure 7. Three laboratories (A,E,J) conducted the test in position control, as indicated from the changing slope in the strain-time plot. Figure 8 plots the strain rates in the elastic and plastic portions of the



Figure 3: Engineering stress-strain curves.



Figure 4: Engineering stress-strain curves: (a) complete behavior, (b) low-strain behavior, (c) yield behavior, and (d) plastic behavior. Dashed lines show the accepted value for the modulus of 2024-T351, E = 75.2 GPa, the 0.2 % offset yield strength determination, and the e = 0.008 total elongation.



Figure 5: Reported elastic modulus, E. Dashed lines show the average reported modulus and a commonly accepted value of the modulus (E=75.2 GPa) from Mil-HDBK-5J [25] and the average of all the measurements, E = 74.9 GPa.



Figure 6: Reported 0.2 % offset yield strength, YS(0.2 % offset). The dashed line is the average of the results from all laboratories.



Figure 7: Reported strain as a function of time.

 Table 4: Reported data

Lab	Sample	E	YS		Lab	Sample	E	YS	Lab	Sample	E	YS
		GPa	MPa				GPa	MPa			GPa	MPa
Α	LT-85	75.6	339.0	-	Н	LT-10	77.2	345.0	K	LT-24	75.8	343.0
А	LT-1	72.9	340.0		Η	LT-44	73.8	347.0	Κ	LT-42	80.7	348.0
А	LT-40	76.8	341.0		Η	LT-55	73.1	347.0	Κ	LT-51	87.6	351.0
А	LT-26	75.1	342.0		Η	LT-63	77.2	347.0	Κ	LT-56	84.1	351.0
А	LT-66	73.8	342.0		Н	LT-76	75.8	347.0	Κ	LT-5	80.0	352.0
А	LT-78	74.7	342.0		Н	LT-91	77.2	347.0	Κ	LT-13	76.5	354.0
А	LT-82	76.3	343.0		Н	LT-19	78.6	354.0	Κ	LT-83	NA	NA
В	LT-28	73.1	348.0		Ι	LT-43	75.0	348.0	L	LT-79	73.0	348.0
В	LT-39	76.5	349.0		Ι	LT-57	76.0	349.0	L	LT-45	84.2	349.0
В	LT-54	75.0	349.0		Ι	LT-65	75.0	349.0	L	LT-69	78.4	352.0
В	LT-9	75.0	353.0		Ι	LT-21	76.0	350.0	L	LT-12	84.2	355.0
В	LT-80	83.4	356.0		Ι	LT-34	75.0	350.0	L	LT-36	75.7	356.0
С	LT-68	72.0	318.0		Ι	LT-74	75.0	350.0	L	LT-6	77.5	356.0
С	LT-84	72.8	335.0		Ι	LT-70	76.0	351.0	L	LT-92	85.8	363.0
С	LT-90	71.5	336.0		J	LT-4	74.5	340.5	Μ	LT-18	69.0	338.0
С	LT-16	72.4	338.0		J	LT-89	74.2	341.6	Μ	LT-11	72.0	342.0
С	LT-77	71.4	338.0		J	LT-94	74.4	341.6	Μ	LT-59	71.0	342.0
С	LT-27	70.7	339.0		J	LT-73	74.5	342.1	Μ	LT-62	70.0	342.0
С	LT-58	72.9	341.0		J	LT-37	74.8	342.5	Μ	LT-86	72.0	342.0
Е	LT-25	68.3	342.2		J	LT-23	74.8	343.1	Μ	LT-33	72.0	343.0
Е	LT-31	67.0	346.8		J	LT-14	74.1	343.4	Μ	LT-81	68.0	345.0
Е	LT-87	69.3	347.4	-								
Е	LT-71	68.6	349.0									
Е	LT-17	70.5	351.1									
E	LT-8	70.9	351.4									

E LT-41 70.6 355.8 Notes:

YS=*YS*(0.2 % offset)

stress-strain curves calculated by linear regression. The plastic strain rate was calculated for strains greater than the strain at the 0.2% offset yield strength: $e_{\rm YS002} < e < e_{\rm max}$. The elastic strain rate was calculated in the range $0 < e < (e_{\rm YS002} - 0.002)$. Laboratory J conducted the test in position control and set the elastic strain rate close to the specified value.

4 Analysis and discussion

4.1 Expected variability

Table 5 summarizes the mean and standard deviation, sd, and coefficient of variation, cv, of the reported n measurements of the elastic moduli and yield strengths. Table 6 defines the statistical parameters used in this section.



(b) plastic strain rate

Figure 8: Calculated (a) elastic and (b) plastic strain rates for laboratories that reported time data. Symbols differentiate between position-control and strain-control tests. Dashed line indicates the requested rate, $de/dt = 8.33 \times 10^{-5}$ 1/s.

Lab	n	E	sd(E)	cv(E)	YS	sd(YS)	cv(YS)
		GPa	GPa		MPa	MPa	
А	7	75.0	1.4	0.018	341.3	1.4	0.004
В	5	76.6	4.0	0.052	351.0	3.4	0.010
С	7	72.0	0.8	0.011	335.0	7.7	0.023
Е	7	69.3	1.4	0.021	349.1	4.3	0.012
Н	7	76.1	2.0	0.026	347.7	2.9	0.008
Ι	7	75.4	0.5	0.007	349.6	1.0	0.003
J	7	74.5	0.3	0.004	342.1	1.0	0.003
Κ	7	80.8	4.5	0.056	349.8	3.9	0.011
L	7	79.8	4.9	0.062	354.1	5.1	0.014
Μ	7	70.6	1.6	0.023	342.0	2.1	0.006
NT 4	17		(0.0.01	CC ()			

Table 5: Summary statistics for the modulus and yield strength data.

Note: YS = YS(0.2 % offset)

Parameter	Grand Average	s_r	cv_r	s_R	cv_R
E	$\overline{\bar{E}}$ = 75.0 GPa	2.7 GPa	0.036	4.4 GPa	0.059
<i>YS</i> (0.2 % offset)	$\bar{YS}(0.2 \% \text{ offset}) = 346.2 \text{ MPa}$	3.8 MPa	0.011	6.8 MPa	0.020

Table 6 defines the parameters. Because laboratory B tested only five specimens instead of seven, the mean values shown in Figures 5, 6, 10, and 12 differ from the Grand Average, also known as the average of cell averages, Table 6, Eq. 2.

The results of an interlaboratory study contain variability that arises within a given laboratory and variability that arises between laboratories. The terms repeatability and the reproducibility, denoted by subscripted "r" and "R," are often used to differentiate between these sources [22]. In a general sense, repeatability characterizes the ability of an individual laboratory to repeat measurements, while reproducibility characterizes the ability of an individual laboratory to achieve the global mean or accepted value. For example, if the results from an individual laboratory are tightly grouped, their repeatability is high, but their mean value may still deviate significantly from the accepted value, in which case their reproducibility is low.

Both the variability in the material and the variability of the test method influence the repeatability. The excellent repeatability of the measurements for both E and YS(0.2% offset) in laboratories A, I, and J, Table 5, shows that the material variability in this study is quite low, and therefore the implementation of the test method by the individual laboratories is the major contributor to repeatability.

Figure 9 and Table 7 compare the results for repeatability and reproducibility for this study to the results of other interlaboratory studies of tensile tests at room [26, 27] and

Formula	Description	
n	number of tests in a laboratory, $n \approx 7$	
p	number of laboratories, $p = 10$	
Y_{ij}	individual test result in lab j	
	1 < i < n ; 1 < j < p	
$\bar{Y}_j = \frac{1}{n} \sum_{i=1}^n Y_{ij}$	average test result in lab j (cell average)	(1)
$\bar{\bar{Y}} = \frac{1}{p} \sum_{j=1}^{p} \bar{Y}_j$	average of cell averages (grand average)	(2)
$s_j = \sqrt{\frac{1}{n-1} \sum_{i=1}^n (Y_{ij} - \bar{Y}_j)^2}$	standard deviation measured in lab j	(3)
$s_r = \sqrt{\frac{1}{p} \sum_{j=1}^p (s_j)^2}$	repeatability (within-lab) standard deviation	(4)
$cv_r = \frac{s_r}{\bar{V}}$	coefficient of variation within laboratories	(5)
$s_{\bar{Y}} = \sqrt{\frac{1}{p-1} \sum_{j=1}^{p} (\bar{Y}_j - \bar{\bar{Y}})^2}$	standard deviation of cell averages	(6)
$s_R = \sqrt{s_{\bar{Y}}^2 + s_r^2(\frac{n-1}{n})}$	reproducibility standard deviation ((between-lab)	(7)
$cv_R = \frac{s_R}{\bar{\bar{Y}}}$	coefficient of variation between laboratories	(8)

elevated temperatures [28] to establish the 0.2 % offset yield strength, YS(0.2 % offset). In Figure 9 the within-laboratory and between-laboratory standard deviations, s_r , Eq. 4, and s_R , Eq. 7, see Table 6, are divided by the mean value and expressed as their respective coefficients of variation, cv_r , Eq. 5, and cv_R , Eq. 8.

The repeatability coefficient of variation of the yield strength measurements in this study, derived from the average of the standard deviations of the individual laboratories, is $cv_r = 0.0111$, Eq. 5, while the coefficient of variation of the reproducibility, $cv_R = 0.0197$, Eq. 8, is about twice as large. The repeatability and reproducibility of compression tests established in this study are among the best measurements of all reported uniaxial measurements [26, 27, 28].



(b) Reproducibility

Figure 9: Literature data [26, 28, 27] on (a) repeatability (within-laboratory) and (b) reproducibility (between-laboratory) of yield strength, YS(0.2 % offset). Table 7 summarizes the data.

Source	Material	Т	YS	cv_r	cv_R
		°C	MPa		
[26]	EC-H19 aluminum	20.0	158.4	0.0210	0.0210
[26]	2024-T351 aluminum	20.0	362.9	0.0140	0.0150
[26]	AISI A105 steel	20.0	402.4	0.0140	0.0250
[26]	SS316 stainless steel	20.0	480.1	0.0140	0.0410
[26]	Inconel 600	20.0	268.3	0.0090	0.0220
[26]	SAE 51410 steel	20.0	967.5	0.0090	0.0160
[27]	AA5754 Al	20.0	105.7	NA	0.0160
[27]	AA51802-O	20.0	126.4	NA	0.0100
[27]	AA6016-T4	20.0	127.2	NA	0.0110
[27]	DX56, low-carbon steel	20.0	162.0	NA	0.0230
[27]	HR3 steel plate	20.0	228.6	NA	0.0410
[27]	ZStE 180 steel	20.0	267.1	NA	0.0500
[27]	S355 steel plate	20.0	427.6	NA	0.0310
[27]	SS316L stainless steel	20.0	230.7	NA	0.0350
[27]	X2CrNi18-10 stainless steel	20.0	303.8	NA	0.0330
[27]	X2CrNiMo18-10	20.0	353.3	NA	0.0390
[27]	30NiCrMo16 high strength steel	20.0	1039.9	NA	0.0100
[27]	Nimonic 75 CRM 661	20.0	302.1	NA	0.0180
[27]	Nimonic 75 CRM 661	20.0	298.1	NA	0.0200
[28]	SS304 stainless steel	316.0	127.3	0.0580	0.1040
[28]	Low-carbon steel	316.0	236.4	0.0110	0.0350
[28]	2.25 Cr 1Mo steel	316.0	454.7	0.0230	0.0330
[28]	A286 stainless steel	316.0	699.5	0.0280	0.0300
[28]	SS304 stainless steel	593.0	101.4	0.0770	0.0990
[28]	Low-carbon steel	593.0	133.0	0.0390	0.1040
[28]	2.2.5Cr 1Mo ferritic steel	593.0	337.9	0.0260	0.0670
[28]	A286 stainless steel	593.0	642.2	0.0260	0.0350
This study	Al 2024-T351	20.0	346.2	0.0111	0.0197

Table 7: Literature data [28, 26, 27] for repeatability and reproducibility in mechanical testing.

Notes:

YS = YS(0.2 % offset)

NA = data not available

4.2 Effect of test method implementation

Because the laboratories were free to implement the test method in different ways, while still complying with the standard, their results can be used to learn about the effect of different aspects of test method on the measurement. In particular, the results can be examined to determine the effects of the number of extensioneters and lubrication on the quality of the measurement.

4.2.1 Effect of number of extensometers

Some laboratories used a single extensioneter, while others used two opposed extensioneters to measure the strain. Figure 10 plots the reported modulus and yield strength for the laboratories, grouped by the number of extension sused in the determination. The three laboratories, A, I, J, with the best repeatability and reproducibility of E and YS(0.2 %offset) are the only ones that used a system of two-opposed extensioneters instead of a single extensioneter. In addition, the measured elastic modulus in these three laboratories was the closest to the accepted [25] value E = 75.2 GPa, Figure 10a. Note that the repeatability of the modulus and yield strength from the labs that used a single extensometer is worse (i.e. larger variability), but also that for an individual laboratory, the values usually all lie above or below the grand average. Using two extensometers will tend to average the effect of non-axial loading, since during bending, one side of the test specimen will be displaced more, and the other less. Because the values for an individual, single-extension side of the global mean value points toward the alignment of the compression fixture, rather than machining of the test specimen as the source of the non-axiality. If the ends of the test specimen were not parallel, the measured values would tend to encompass the mean value, because no special relationship exists between the test specimen and the loading fixture. Conversely, the extensometer is usually mounted on the test specimen with a fixed relation to the orientation of loading fixture, so bending induced by a slightly misaligned loading fixture is always in the same geometric relation to the extensioneter, which will tend to always over- or under-estimate the strain.

4.2.2 Effect of Lubricant

The standard allows the laboratory to choose whether to lubricate the ends of the test specimen during the test. Figure 11 shows the engineering stress-strain curves, identified by the use or omission of lubricants. Several laboratories did not report lubricant use. Table 3 identifies the lubricants used. Three laboratories used no lubricant, and their stress-strain curves are the lowest in the collection. Figure 12 plots the reported modulus, E, and yield strength, YS(0.2 % offset), identified by lubricant use. The average yield strength from the three laboratories that did not use lubricant was 10.6 MPa lower (3.1 %) than the average of the laboratories that lubricated the specimen. Similarly the average reported elastic modulus, E, from the three laboratories was 4.1 GPa (5.7 %) smaller. Table 8, an analysis of variance, shows that the reported yield strength, YS(0.2 % offset), and modulus, E, are both significantly different for the lubricated and unlubricated cases.



(b) YS(0.2 % offset)

Figure 10: Reported (a) modulus and (b) 0.2 % offset yield strength, YS(0.2 % offset), identified by number of extensioneters used.



Figure 11: Effect of lubricant on stress-strain behavior.



(a) Modulus, E



(b) Yield strength, YS(0.2 % offset)

Figure 12: Effect of lubricant on (a) modulus E and (b) yield strength YS(0.2 % offset). Dashed lines are the mean values for all data, including "not-reported," not lubricated ("No") and lubricated ("Yes") tests.

Table 8: Analysis of variance tables for assessing the effect of lubrication on modulus and yield strength.

```
% Table generated on 2010-09-22 19:05:27
Analysis of Variance Table
Model 1: E ~ 1
Model 2: E ~ Lubricated
 Res.Df RSS Df Sum of Sq F Pr(>F)
   52 1180.16
1
                     208.85 10.966 0.00171 **
2
     51 971.31 1
Signif. codes: 0 *** 0.001 ** 0.01 * 0.05 . 0.1
                                                 1
Analysis of Variance Table
Model 1: YS02 ~ 1
Model 2: YS02 ~ Lubricated
 Res.Df RSS Df Sum of Sq
                              F
                                     Pr(>F)
    52 2655.5
1
2
     51 1223.9 1
                     1431.6 59.653 3.939e-10 ***
Signif. codes: 0 *** 0.001 ** 0.01 * 0.05 . 0.1
                                                 1
```

Key to parameters in table:

E: E, elastic modulus

YS02: YS(0.2 % offset), 0.2 % offset yield strength

Data from laboratories that did not report the lubrication are omitted. Model 1 is the mean value of of the parameter, and model 2 computes the mean value for the lubricated ("Yes") and unlubricated ("No") cases.

Since most laboratories used an extensiometer with a gauge length G = 25.4 mm on the test specimen, Fig. 2, with length $l \approx 48$ mm and diameter d = 12.7 mm, the end of the test specimen is approximately one test specimen diameter away from the extensometer contact point. That distance complies with the requirements of E9, and should minimize the effect of the non-uniform stress caused by friction at the specimen ends. No study has examined the sensitivity of the strain measurement to the non-uniform stress at the end of the specimen, but the existence of non-uniform stresses caused by friction is well known [29]. Finite element analysis (FEA), using the commercial finite-element modeling software Abaqus/Standard 6.10 [30], was used to analyze the effect of friction and gauge length on the response of the specimen. By exploiting the axial and radial symmetry of the specimen and platens, it was only necessary to model the upper-right



Figure 13: Finite element mesh and boundary conditions of the upper-right quadrant of the test specimen.

quadrant the specimen with radius r = 6.3 mm and length l = 24.25 mm. The specimen mesh, Figure 13, was constructed with 1542 quadrilateral four-node axi-symmetric (CAX4) elements. The platens were modeled as non-deforming, rigid planes of infinite elastic modulus. Roller boundary conditions were applied on the axial centerline and the specimen midplane. The specimen material was modeled as a homogeneous elastic-plastic time-independent material exhibiting strain hardening. The plastic deformation was modeled by the J_2 (or von Mises) flow plasticity theory with isotropic hardening.[30] The uniaxial stress-strain curve was taken from specimen LT-14 of the experimental results, down-sampled to 58 points, with the Young's modulus set to the accepted value E = 75.2 GPa, and Poisson's ratio $\nu = 0.33$. This material model yields at a true stress $\sigma = 190.4$ MPa at a true strain $\epsilon = 0.0026$, and not at the value of the 0.2 % offset value YS(0.2 % offset)=343.4 MPa. All of the stress-strain curves, Fig. 4a, exhibited this behavior.

Two limiting cases of zero friction and complete friction at the specimen-platen interface were modeled. The simulation was performed by pushing the rigid platen increasingly to displacement of 0.485 mm, which is e = 0.02 deformation for the zero friction case. The effect of extensioneter gauge length was tested by following the axial displacement of two nodes, Figure 13, located l = 6.35 mm and l = 12.7 mm above the center plane of the specimen. These nodes correspond to the contact points of extensiometers with G = 12.7 mm and G = 25.4 mm respectively. To calculate the stress-strain behavior, the force on the platen, the displacement of the platen, the displacement of the two extensiometer contact points and a surface corresponding to the length between the platens, see Figure 13, were recorded. The stresses were calculated from the measured radii at those points.

Figure 14 shows the computed true stress-strain curves for strain measures across three gauge lengths (G = 12.7 mm, G = 25.4 mm, and G = 48.5 mm-across the loading platens) and for the two limiting friction cases: frictionless (f = 0) and perfect friction (f = 1). It also shows the true stress-strain curve used as the input model. In the figure, the true stresses, are calculated from the load P and the instantaneous area, A, by by assuming conservation of volume in deformation:

$$A_0 l_0 = A l \tag{9}$$

where A_0 and l_0 are the original area and gauge length respectively. This calculation mimics what would be done in analysis of an actual experiment, where the instantaneous load-bearing area, A, is calculated from the strain. For the frictionless case, all the strain measures yield the same stress-strain behavior as the input model, as they should. For the case of perfect friction, f = 1, the strains measured across the two extensioneter gauge length, G = 12.7 mm and G = 25.4 mm differ by less than 0.5 MPa from each other and from the frictionless cases. The difference between the average of yield strengths measured by laboratories that lubricated and those that did not was was twenty times this large: Δ YS(0.2 % offset)=10.4 MPa, Figures 11 and 12. The true stress calculated from the displacement of the loading platen, a common method that use the displacement of the actuator, corrected for machine compliance, is about 6 MPa, or 1.4 %, above all the other curves. Note that no laboratory measured strain this way; each laboratory used an extensioneter on the test specimen, with contact points remote from the test specimen end faces. The agreement between the extensioneter methods for the frictionless and complete friction cases eliminates friction as the source of the difference in yield behavior between the laboratories that lubricated and those that did not.

The finite-element analysis also determined the evolution of the stress distributions in the test specimen. Figure 15 shows the von Mises stress evolution for four strains. Stresses less than the yield stress of the material model, $\sigma = 190.4$ MPa, are shown in white. Consistent with other analyses [29, 6], a non-deforming cap forms at the test specimen end. As the specimen deforms, a region of slightly higher stress develops that extends just into the region that the longer, G = 25.4 mm extensometer samples. Figure 16 shows the evolution of the shear stress, σ_{12} for the same four strains. The bulk of the test specimen has zero shear stress. Only at the test specimen ends, where friction constrains the deformation, does shear strain develop.



(b) Expanded section

Figure 14: Computed true stress-strain curves for the cases of frictionless (f = 0) and perfect friction (f = 1) and different gauge lengths, G: (a) full curve, and (b) expanded section that shows the small differences between the results at large strain.



Figure 15: Von Mises stress distribution in the upper-right quadrant of the test specimen for four true strains: (a) $\epsilon = 0.002$, (b) $\epsilon = 0.008$, (c) $\epsilon = 0.015$, and (d) $\epsilon = 0.022$, measured from the G = 12.7 mm extensioneter for the case of perfect friction.

4.3 Elastic Modulus

The elastic modulus measured in the test is very sensitive to the alignment and sensitivity of the test setup. As a result, ASTM E 9 [2] requires that laboratories validate their compression test fixture by measuring the elastic modulus of aluminum alloy 2024-T4 bar, according ASTM E 111 [31] and obtaining measurements on five consecutive specimens to within 5 % of a stated value, E=73.8 GPa. The behavior of the reported elastic modulus should be a good indicator of the quality of the compression test facility.

The interlaboratory study did not require laboratories to revalidate their test setups, but they did report the measurements of elastic modulus, Figure 5, made during the compression tests of this study. Most of the laboratories only used a ASTM E 83 [32] Class B-2 extensometer, see Table 3, rather than the roughly twice-as-accurate class B-1 extensometer required by ASTM E 111 [31] when elastic modulus is the primary parameter to be determined. But because the primary parameter to be determined was the yield strength, E 9 Section 9.2 permits the use of the class B-2 extensometer.

The laboratories had wide latitude in the method to determine the elastic modulus to report. To reduce the variability due to the interpretation of the individual laboratory, and to put each modulus measurement on a consistent basis, we reanalyzed each stress-strain curve to estimate the elastic modulus using a technique [33] based on the method



Figure 16: Shear stress distribution in the upper-right quadrant of the test specimen for four true strains: (a) $\epsilon = 0.002$, (b) $\epsilon = 0.008$, (c) $\epsilon = 0.015$, and (d) $\epsilon = 0.022$, measured from the G = 12.7 mm extensioneter for the case of perfect friction.

of Scibetta and Schuurmans [34]. These reanalyzed moduli are denoted by the symbol E_{GA} , to differentiate them from the moduli that the participants calculated and reported, denoted by E. In addition to estimating the modulus, the method includes some checks on the quality of the data that may be useful for laboratories that seek to improve their modulus measurement.

Many of the following plots evaluate the quality of the measurements by employing the absolute modulus error, ΔE_{GA} , in a measurement, which is defined as the absolute value of the difference between the accepted modulus [25] for 2024-T351 aluminum, $E_{A1}^{acc} = 75.2$ GPa and the calculated modulus, E_{GA} .

$$\Delta E_{GA} = |E_{Al}^{acc} - E_{GA}| \tag{10}$$

Other references [35, 36, 37, 2] recommend different values in the range 73.8 GPa < E < 76.1 GPa, and differentiate [36] between longitudinal and transverse orientation.

Method for analysis The method consists of nine steps.

- 1 Find the knee of the stress-strain (s e) curve by the method of Scibetta and Schuurmans [34].
 - 1. Find the point on the stress-strain curve (e_1, s_1) closest to $s_1 = 0.05 \max(s)$

- 2. Create point (e_o, s_o) where $e_o = e_1$ and $s_o = 0.2 \max(s)$.
- 3. Find the point on the stress-strain curve (e_t, s_t) that is on a line drawn through (e_0, s_0) that is tangent to the stress-strain curve.
- 2 Truncate the stress-strain data at (e_t, s_t) and normalize by these values. Retain the maximum values of the test record: (e_{\max}, s_{\max}) .
- 3 Check digital resolution, δ , of stress and strain. The digital resolution should be $\delta_e < \frac{3}{2^{12}} \frac{x_{\text{max}}}{e_t}$ and $\delta_s < \frac{3}{2^{12}} \frac{x_{\text{max}}}{s_t}$. No more than more than 25 % of points should have zero stress or strain change from the previous point.
- 4 Use the Scibetta-Schuurmans [34] algorithm to determine optimum fit window and calculate the slope, which is the elastic modulus E_{GA} , in normalized form. The Scibetta-Schuurmans algorithm finds the optimal region for determining the modulus by performing a linear regression of stress on strain on every possible subset of data in the region $e_o < e < e_t$ that contains at least 20 % of the data. The regression with the lowest residual standard deviation is the optimum fit. In some cases, more than one million fits were evaluated for each stress-strain curve.
- 5 Check for excessive noise in optimum fit window, defined as the standard error of the regression in step 4: s_j defined in Table 6 where *n* is the number of stress-strain pairs in the optimal region, Y_{ij} is the normalized stress evaluated at point *j*, and \bar{Y}_j is the predicted normalized stress from the fit to the optimal region. Perform the complementary regression of strain upon stress as well. In both cases, the standard error in strain or stress should not be greater than 0.01.
- 6 Extend the range of fit to include all stress points whose deviation from the optimal fit line is less than one times standard error computed in Step 5.
- 7 Refit the extended data set to determine modulus, E_{GA} .
- 8 Examine the shape of the stress and strain residuals as a function of strain in the extended fit. If the slope of the residuals in the first or fourth quartile of the extended range is more than 0.05, the data exhibit excessive curvature. At least five points must exist in each quartile to evaluate this curvature.
- 9 Check that the stress range of the optimal fit is greater than $0.4s_t$.

The method employs four metrics to determine the quality of the modulus:

- Data quality 1: digital stress and strain resolution should be sufficient (Step 2)
- Data quality 2: strain or stress signal should not have excessive noise (Step 5)
- Fit quality 1: the stress and strain residuals in extended data range should not have excessive curvature (Step 8)

• Fit quality 2: the size optimal fit range, R_f , should be greater than or equal to 40 % of the total range used to determine the modulus (Step 9)

The rest of this section will examine the results of the modulus measurement, E_{GA} , using these four quality metrics.

Data Quality 1: sufficient digital resolution Figure 17 summarizes the strain and stress resolution. Estimating the digital resolution of a data set post-test is difficult, and the interested reader should consult the original reference by Graham and Adler [33]. To create the figure, the digital resolution was estimated from the data set by taking the absolute value of the difference of each sequential pair of stress and strain points, for example $|s_i - s_{i+1}|$. Those differences, expressed in units of δ from step 3, were binned to create a histogram. If too many of the points show no change between reading, or if the most frequent change is many times larger than the digital resolution, δ defined in Step 3, the stress-strain curve may have insufficient digital resolution. This condition could arise, for example, if a load cell were used near the very lower limit of its working range, or if the analog-to-digital converter had insufficient precision. Figure 17 plots the index of the bin with the maximum fraction of the data, in units of δ , defined in step 3, against the fraction of the points in the "zeroth" bin, which is the fraction of points where the stress or strain value did not change between readings. The symbols show the fraction of the points in the bin of maximum fraction, broken into two groups: those where the bin of maximum fraction contained less than 25 % of the data ((0, 25]) and those that contained more than 25 % of the data ((25, Inf). The method identifies experiments with insufficient digital resolution as those where the bin of maximum fraction is greater than 3 and either the fraction in the zeroth bin is > 25 % or the fraction in the bin of maximum fraction is > 25 %. The first condition is identified by the dashed lines. The second "or" condition comprise those points identified by green circles with y value greater than 3. No experiment demonstrated insufficient digital resolution.

Data Quality 2: excessive noise Excessive noise in the strain or stress signal will degrade the quality of the measured modulus. The method identifies experiments with excessive noise in these signals as ones in which the standard error of the fit is greater than 0.01. Figure 18 plots the standard error of the fit for both strain and stress by laboratory. The symbols identify three levels of modulus error, Eq. 10. The noise in all the experiments was sufficiently low. No obvious relation exists between the absolute modulus error, ΔE , and either the standard error of stress or strain.

Fit Quality 1: Excessive curvature in extended data set Some metric of the curvature of the optimal fit range is necessary, since the method only selects the best fit over an optimal region. That fit might still be poor. One method for examining the quality of the fit is to examine the deviation from the fit line in the first and fourth quartiles of the optimal range. Curvature of the stress-strain record frequently appears this way. If the slope of the residuals vs. strain in the outer quartiles is greater than 5 % of the slope in the optimal region, the curvature of the fit is deemed excessive.



Figure 17: (a) Strain and (b) stress data resolution. Dashed lines enclose the region of insufficient resolution. Symbols denote the fraction of points in the bin of maximum fraction.





Laboratory

(b) stress noise

Κ

L M

0.0000

В

CEHIJ

А

Figure 19 shows the slope of the residuals in the outer quartiles. Different symbols show the level of absolute error of the elastic modulus, Eq. 10. All but one of the tests fall inside the ± 5 % limits. In addition, linear regression of the absolute modulus error against the absolute value of the residual slope reveals no relationship.

Fit Quality 2: Final fit range The second measure of the quality of the fit to determine the elastic modulus, E_{GA} , is the size of the optimal fit range, R_f . Figure 20 plots the absolute modulus error, Eq. 10, against the fraction of the range of original stress data. The dashed line is the boundary of the minimum acceptable limit $R_f \ge 0.4$. The absolute modulus error, Eq. 10, increases as the size of the fit region decreases, as expected, and the boundary between the two regions lies at the chosen final fit range minimum $R_f =$ 0.4. The mean error for tests with fit region $R_f < 0.4$ is 2.5 times larger (4.88 GPa vs. 1.95 GPa) than that from the acceptable region.

Conclusions from elastic modulus analysis Of the quality metrics, the size of the final fit range is the best predictor of overall quality of the modulus measurement, and the level chosen, $R_f \ge 0.4$, is a good metric for identifying potential problems with modulus measurement.

5 Conclusions

Five conclusions can be drawn from this study.

- The repeatability of yield strength determined from compression tests conducted according to ASTM E9 can be expected to be about 1.1 % of the mean value, $cv_r = 0.011$, Figure 6 and Table 5.
- The reproducibility of yield strength determined from compression tests conducted according to ASTM E9 can be expected to be about 2 % of the mean value, cv_R = 0.020, Figure 6 and Table 5.
- Despite the perceived difficulties with alignment in compression, the repeatability and reproducibility of the compression test was among the best measured for uniaxial tests, Figure 9.
- Using two diametrally opposed extensioneters instead of a single extensioneter can improve the precision of the strain measurement by more than two times, Figure 10.
- If the final fit range for estimating the modulus is less than 40 % of the elastic region, the modulus measurement is frequently in error, Figure 20.

In addition, although the reported data indicated that yield strengths measured on unlubricated conditions were 3.1 % lower than those measured using lubricated specimens, Fig. 12, a finite-element analysis of the deformation that incorporated test-specimen-end friction did not identify any mechanism by which friction could caused the discrepancy.



(b) 4th quartile slope

Figure 19: Slope of residuals in the (a) 1st, and (b) 4th quartile of the extended fit for modulus. Symbols denote three increasing levels of absolute modulus error, Eq. 10. Dashed lines denote the acceptance limit Data have been jittered to prevent over-plotting of points.



Figure 20: Absolute error in modulus, Eq. 10, as a function of the fraction of the final fit range, R_f , used to calculate the modulus. Symbols identify the different laboratories. Points to the left of the dashed line are deemed to have insufficient fit range.

Author contributions

William Luecke supervised the interlaboratory study and analyzed the reported modulus and yield strength data. Stephen Graham and Matthew Adler analyzed the stress-strain curves to recalculate the modulus and the associated data and fit qualities. Li Ma conducted the finite element analysis of the specimen deformation under frictionless and perfect friction.

Acknowledgments

The authors could not have completed this study without the generous donation of the testing services of the participants, including those who volunteered, but ultimately could not complete the testing in the brief time allotted: Ray Schiltz (AADFW, Inc), Rich Brazill (Alcoa), Rick Kapaun (Exova), Bill Swartz (Constellation Technology Corp.), I. Ahmed (Dickson Testing Company Inc.), James Hartman (Honeywell Aerospace), Hugh MacGillivray (Imperial College Mechanical Engr.), Matt Webb (MAR-TEST, Inc. (Cincinnati)), Frank Worpenberg (MAR-TEST, Inc. (Stuart)), Ken Broenner (Metcut Research Inc.), Dennis Galloway (Stork Climax Research Services), and Mike Self (Westmoreland Mechanical Testing).

WEL thanks the other two members of the organizing team, Rich Brazill and James Hartman for their assistance. Rich Brazill supplied the aluminum plate, the test specimen blanks, and the test specimen assignments.

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