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3 Rec	commendation for Block Cipher Modes of Operation
5 Met	hods for Format-Preserving Encryption
6 7 8 9	Morris Dworkin
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94 95

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106

Abstract

107 This Recommendation specifies two methods, called FF1 and FF3-1, for format-preserving 108 encryption. Both of these methods are modes of operation for an underlying, approved symmetric-109 key block cipher algorithm. Compared to the original version of this publication, the tweak size 110 for FF3-1 is smaller than the tweak size for FF3; also, for both FF1 and FF3-1, larger domains are

- 111 required, rather than merely recommended.
- 112

Keywords

Block cipher; confidentiality; encryption; FF1; FF3; FF3-1; format-preserving encryption;

- 114 information security; mode of operation.
- 115

116

117

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contributed to its development, especially Elaine Barker, Nicky Mouha, Lily Chen, John Kelsey,
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133

Conformance Testing

134 Conformance testing for implementations of the functions that are specified in this publication will

be conducted within the framework of the Cryptographic Algorithm Validation Program (CAVP)

136 and the Cryptographic Module Validation Program (CMVP). The requirements on these

implementations are indicated by the word "shall." Some of these requirements may be out-ofscope for CAVP or CMVP validation testing, and thus are the responsibility of entities using,

implementing, installing, or configuring applications that incorporate this Recommendation.

140

141 **Call for Patent Claims** 142 143 This public review includes a call for information on essential patent claims (claims whose use 144 would be required for compliance with the guidance or requirements in this Information 145 Technology Laboratory (ITL) draft publication). Such guidance and/or requirements may be 146 directly stated in this ITL Publication or by reference to another publication. This call also includes 147 disclosure, where known, of the existence of pending U.S. or foreign patent applications relating 148 to this ITL draft publication and of any relevant unexpired U.S. or foreign patents. 149 150 ITL may require from the patent holder, or a party authorized to make assurances on its behalf, in 151 written or electronic form, either: 152 153 a) assurance in the form of a general disclaimer to the effect that such party does not hold and does 154 not currently intend holding any essential patent claim(s); or 155 156 b) assurance that a license to such essential patent claim(s) will be made available to applicants 157 desiring to utilize the license for the purpose of complying with the guidance or requirements in 158 this ITL draft publication either: 159 160 i) under reasonable terms and conditions that are demonstrably free of any unfair 161 discrimination: or 162 163 ii) without compensation and under reasonable terms and conditions that are demonstrably 164 free of any unfair discrimination. 165 166 Such assurance shall indicate that the patent holder (or third party authorized to make assurances 167 on its behalf) will include in any documents transferring ownership of patents subject to the 168 assurance, provisions sufficient to ensure that the commitments in the assurance are binding on 169 the transferee, and that the transferee will similarly include appropriate provisions in the event of 170 future transfers with the goal of binding each successor-in-interest. 171 172 The assurance shall also indicate that it is intended to be binding on successors-in-interest 173 regardless of whether such provisions are included in the relevant transfer documents. 174 175 Such statements should be addressed to: EncryptionModes@nist.gov. 176

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206 **1 Purpose**

This publication is a revision of the seventh part in a series of Recommendations regarding the modes of operation of block cipher algorithms. The purpose of this part is to provide two approved methods for format-preserving encryption (FPE).

Since the original publication of these FPE modes in March of 2016, researchers identified vulnerabilities in [8], building on the work in [1], and in [7]. The present revision includes sets of technical revisions to mitigate the vulnerabilities, as summarized in Appendix F.

213 **2** Introduction

214 A block cipher mode of operation-or simply, mode-is an algorithm for the cryptographic 215 transformation of data that is based on a block cipher. The previously approved modes for 216 encryption are transformations on binary data, i.e., the inputs and outputs of the modes are bit 217 strings-sequences of ones and zeros. For sequences of non-binary symbols, however, there is no 218 natural and general way for the previously approved modes to produce encrypted data that has the 219 same format. For example, a Social Security Number (SSN) consists of nine decimal digits, so it 220 is an integer that is less than one billion. This integer can be converted to a bit string as input to a 221 previously approved mode, but when the output bit string is converted back to an integer, it may 222 be greater than one billion, which would be too long for an SSN.

FPE is designed for data that is not necessarily binary. In particular, given any finite set of symbols, like the decimal numerals, a method for FPE transforms data that is formatted as a sequence of the symbols in such a way that the encrypted form of the data has the same format, including the length, as the original data. Thus, an FPE-encrypted SSN would be a sequence of nine decimal digits.

FPE facilitates the targeting of encryption to sensitive information, as well as the retrofitting of encryption technology to legacy applications, where a conventional encryption mode might not be feasible. For example, database applications may not support changes to the length or format of data fields. FPE has emerged as a useful cryptographic tool, whose applications include financialinformation security, data sanitization, ¹ and the transparent encryption of fields in legacy databases.

234 The two FPE modes specified in this publication are called FF1 and FF3-1. FF3-1 is a revision of 235 the FF3 mode that was specified in the original version of this publication; the revision of FF3, as 236 well as a modified requirement for both FF1 and FF3-1, are described in Appendix F. The 237 acronyms for the modes indicate that they are format-preserving, Feistel-based encryption modes. 238 FF1 was submitted to NIST under the name FFX[Radix] in [3]. FF3 is a component of the FPE 239 method that was submitted to NIST under the name BPS in [4]. In particular, FF3 is essentially 240 equivalent to the BPS-BC component of BPS, instantiated with a 128-bit block cipher. The full 241 BPS mode-in particular, its chaining mechanism for longer input strings-is not approved in this 242 publication.

¹ The sanitization of personally identifiable information in a database—whether by FPE or other methods—does not necessarily provide strong assurance that individuals cannot be re-identified; for example, see [5].

- Each of these FPE modes fits within a larger framework, called FFX, for constructing FPE
- 244 mechanisms; FFX was submitted to NIST in [2]. The "X" indicates the flexibility to instantiate the
- framework with different parameter sets, as well as FFX's evolution from its precursor, the Feistel
- 246 Finite Set Encryption Mode.
- The FFX framework itself is not specified in this publication; in fact, FF1 and FF3-1 are not presented explicitly as instantiations of FFX parameter sets, but rather as separate algorithms, in order to simplify the individual specifications.
- 250 FF1 and FF3-1 each employ the Feistel structure—see Sec. 4.4—which also underlies the Triple
- 251 Data Encryption Algorithm (TDEA) [15]. At the core of FF1 and FF3-1 are somewhat different
- 252 Feistel round functions that are derived from an approved block cipher with 128-bit blocks, i.e.,
- the Advanced Encryption Standard (AES) algorithm [12].
- In addition to the formatted data for which the modes provide confidentiality, each mode also takes an additional input called the "tweak," which is not necessarily secret. The tweak can be regarded as a changeable part of the key, because together they determine the encryption and decryption functions. Tweaks that vary can be especially important for implementations of FPE modes, because the number of possible values for the confidential data is often relatively small, as
- 259 discussed in Appendix A and Appendix C.
- FF1 and FF3-1 offer somewhat different performance advantages. FF1 supports a greater range of lengths for the protected, formatted data, as well as flexibility in the length of the tweak. FF3-1 achieves greater throughput, mainly because it has eight rounds, compared to ten for FF1.

263 **3 Definitions and Notation**

264 **3.1 Definitions**

alphabet	A finite set of two or more symbols.
approved	FIPS-approved or NIST-recommended: an algorithm or technique that is either 1) specified in a FIPS or a NIST Recommendation, or 2) adopted in a Federal Information Processing Standard (FIPS) or a NIST Recommendation.
base	The number of characters in a given alphabet. The base is denoted by <i>radix</i> .
bit	A binary digit: 0 or 1.
bit string	A finite, ordered sequence of bits.
block	For a given block cipher, a bit string whose length is the block size of the block cipher.
block cipher	A parameterized family of permutations on bit strings of a fixed length; the parameter that determines the permutation is a bit string called the key.

block cipher mode of operation	An algorithm for the cryptographic transformation of data that is based on a block cipher.
block size	For a given block cipher and key, the fixed length of the input (or output) bit strings.
block string	A bit string whose length is a multiple of a given block size, so that it can be represented as the concatenation of a finite sequence of blocks.
byte	A string of eight bits.
byte string	A bit string whose length is a multiple of eight bits, so that it can be represented as the concatenation of a finite sequence of bytes.
character	A symbol in a given alphabet.
character string	A finite, ordered sequence of characters from a given alphabet.
ciphertext	In this publication, the numeral string that is the encrypted form of a plaintext numeral string.
decryption function	For a given block cipher and key, the function of an FPE mode that takes a ciphertext numeral string and a tweak as input and returns the corresponding plaintext numeral string as output.
designated cipher function	For a given block cipher and key, the choice of either the forward transformation or the inverse transformation.
encryption function	For a given block cipher and key, the function of an FPE mode that takes a plaintext numeral string and a tweak as input and returns a ciphertext numeral string as output.
exclusive-OR (XOR)	The bitwise addition, modulo 2, of two bit strings of equal length.
Feistel structure	A framework for constructing an encryption mode. The framework consists of several iterations, called rounds, in which a keyed function, called the round function, is applied to one part of the data in order to modify the other part of the data; the roles of the two parts are swapped for the next round.
forward transformation	For a given block cipher, the permutation of blocks that is determined by the choice of a key.
inverse transformation	For a given block cipher, the inverse of the forward transformation .
key	For a given block cipher, the secret bit string that parameterizes the permutation.

mode	See block cipher mode of operation.
numeral	For a given base, a nonnegative integer less than the base.
numeral string	For a given base, a finite, ordered sequence of numerals for the base.
plaintext	In this publication, a numeral string whose confidentiality is protected by an FPE mode.
prerequisite	A required input to an algorithm that has been established prior to the invocation of the algorithm.
shall	Is required to. Requirements apply to conforming implementations.
should	Is recommended to.
tweak	The input parameter to the encryption and decryption functions whose confidentiality is not necessarily protected by the mode.

265 **3.2 Acronyms**

AES	Advanced Encryption Standard.
CAVP	Cryptographic Algorithm Validation Program.
CCN	credit card number.
CMVP	Cryptographic Module Validation Program.
FIPS	Federal Information Processing Standard.
FISMA	Federal Information Security Management Act.
FPE	format-preserving encryption.
IETF	Internet Engineering Task Force.
ITL	Information Technology Laboratory.
NIST	National Institute of Standards and Technology.
PRF	pseudorandom function.
PRP	pseudorandom permutation.
RFC	Request for Comment.
SSN	Social Security number.

266

267 **3.3 Operations and Functions**

BYTELEN(X)	The number of bytes in a byte string, X , which may be represented as a bit string. For example, BYTELEN(101110011010100)=2.
$\operatorname{CIPH}_{\kappa}(X)$	The output of the designated cipher function of the block cipher under the key K applied to the block X .
LEN(X)	The number of numerals/bits in a numeral/bit string X. For example, $LEN(010)=3$.
LOG(x)	The base 2 logarithm of the real number $x > 0$. For example, $LOG(64) = 6$ and $LOG(10) \approx 3.32$.
NUM(X)	The integer that a bit string X represents when the bits are valued in decreasing order of significance. For example, NUM(10000000)=128. An algorithm for computing NUM(X) is given in Sec. 4.5.
$\operatorname{NUM}_{radix}(X)$	The number that the numeral string X represents in base <i>radix</i> when the numerals are valued in decreasing order of significance. For example, NUM ₅ (00011010)=755. An algorithm for computing NUM _{radix} (X) is given in Sec. 4.5.
PRF(X)	The output of the function PRF applied to the block <i>X</i> ; PRF is defined in terms of a given designated cipher function.
$\operatorname{REV}(X)$	Given a numeral string, X, the numeral string that consists of the numerals of X in reverse order. For example, in base ten, $REV(13579) = 97531$.
$\operatorname{REVB}(X)$	Given a byte string, X, the byte string that consists of the bytes of X in reverse order. For example, $\text{REVB}([1]^1 [2]^1 [3]^1) = [3]^1 [2]^1 [1]^1$.
$\operatorname{STR}_{radix}^{m}(x)$	Given a nonnegative integer x less than <i>radix^m</i> , the representation of x as a string of <i>m</i> numerals in base <i>radix</i> , in decreasing order of significance. For example, $STR_{12}^4(559)$ is the string of four numerals in base 12 that represents 559, namely, 0 3 10 7. An algorithm for computing $STR_{radix}^m(x)$ is given in Sec. 4.5.
[<i>x</i>]	The floor function: given a real number <i>x</i> , the greatest integer that does not exceed <i>x</i> . For example, $\lfloor 2.1 \rfloor = 2$, and $\lfloor 4 \rfloor = 4$.
$\lceil x \rceil$	The ceiling function: given a real number <i>x</i> , the least integer that is not less than <i>x</i> . For example, $\lceil 2.1 \rceil = 3$, and $\lceil 4 \rceil = 4$.
$[x]^s$	Given a nonnegative integer x less than 256^s , the representation of x as a string of s bytes. For example, $[5]^1 = 00000000 00000101$.

[<i>ij</i>]	The set of integers between two integers <i>i</i> and <i>j</i> , including <i>i</i> and <i>j</i> . For example, $[25] = \{2, 3, 4, 5\}$.
$x \mod m$	The nonnegative remainder of the integer x modulo the positive integer m, i.e., $x-m[x/m]$. For example, 13 mod 7 = 6, and -3 mod 7 = 4.
X[i]	Given a numeral/bit string X and an index i such that $1 \le i \le \text{LEN}(X)$, the i th numeral/bit of X. For example, in base ten, if $X = 798137$, then $X[2] = 9$.
X[ij]	The substring of the string X from $X[i]$ to $X[j]$, including $X[i]$ and $X[j]$. For example, in base ten, if $X = 798137$, then $X[35] = 813$.
$X \bigoplus Y$	The bitwise exclusive-OR of bit strings <i>X</i> and <i>Y</i> whose bit lengths are equal. For example, $10011 \bigoplus 10101 = 00110$.
$X \parallel Y$	The concatenation of numeral strings X and Y . For example, $001 \parallel 1011 = 0011011$, and $31 \parallel 31810 = 3131810$.
0 <i>s</i>	The bit string that consists of <i>s</i> consecutive '0' bits. For example, $0^8 = 000000000$.

268 **4 Preliminaries**

269 4.1 Representation of Character Strings

The data inputs and outputs for FF1 and FF3-1 are sequences of numbers that can represent both numeric and non-numeric data, as discussed below.

A finite set of two or more symbols is called an *alphabet*. The symbols in an alphabet are called the *characters* of the alphabet. The number of characters in an alphabet is called the *base*, denoted by *radix*; thus, *radix* \geq 2.

A character string is a finite sequence of characters from an alphabet; individual characters may repeat in the string. In this publication, character strings (and bit strings) are presented in the Courier New font.

- 278 Thus, for the alphabet of lower-case English letters,
- 279 $\{a, b, c, d, e, f, g, h, i, j, k, l, m, n, o, p, q, r, s, t, u, v, w, x, y, z\},\$

hello and cannot are character strings, but Hello and can't are not, because the symbols "H" and "'" are not in the alphabet.

SSNs or Credit Card Numbers (CCNs) can be regarded as character strings in the alphabet of base
ten numerals, namely, {0, 1, 2, 3, 4, 5, 6, 7, 8, 9}. The notion of numerals is generalized to any
given base as follows: the set of base *radix* numerals is

- The data inputs and outputs to the FF1 and FF3-1 encryption and decryption functions must be 286 287 finite sequences of numerals, i.e., numeral strings. If the data to be encrypted is formatted in an
- 288 alphabet that is not already the set of base *radix* numerals, then each character must be represented
- 289 by a distinct numeral in order to apply FF1 or FF3-1.
- 290 For example, the natural representation of lower-case English letters with base 26 numerals is

291
$$a \rightarrow 0, b \rightarrow 1, c \rightarrow 2, \dots x \rightarrow 23, y \rightarrow 24, z \rightarrow 25.$$

292 The character string hello would then be represented by the numeral string 7 4 11 11 14. Other 293 representations are possible.

- 294 The choice and implementation of a one-to-one correspondence between a given alphabet and the 295 set of base *radix* numerals that represents the alphabet is outside the scope of this publication.
- 296 In this publication, individual numerals are themselves represented in base ten. In order to display 297 numeral sequences unambiguously when the base is greater than ten, a delimiter between the 298 numerals is required, such as a space (as in the base 26 example above) or a comma.
- 299 FF1 and FF3-1 use different conventions for interpreting numeral strings as numbers. For FF1,
- 300 numbers are represented by strings of numerals with *decreasing* order of significance; for FF3-1,
- 301 numbers are represented by strings of numerals in the reverse order, i.e., with increasing order of 302
- significance. For example, "0025" is a string of decimal digits that represents the number twenty-
- 303 five for FF1 and the number five thousand two hundred for FF3-1. Algorithms for the functions
- 304 that convert numeral strings to numbers and vice versa are given in Sec. 4.5.

305 4.2 **Underlying Block Cipher and Key**

- 306 The encryption and decryption functions of FF1 and FF3-1 feature a block cipher as the main 307 component; thus, each of these FPE mechanisms is a mode of operation (mode, for short) of the 308 block cipher.
- 309 For any given key, K, the underlying block cipher of the mode is a permutation, i.e., an invertible
- 310 transformation on bit strings of a fixed length; the fixed-length bit strings are called *blocks*, and
- 311 the length of a block is called the *block size*. For an FPE mode, as part of the choice of the
- 312 underlying block cipher with the key, either the forward transformation or the inverse transformation² is specified as the designated cipher function, denoted by $CIPH_{K}$. The inverse of
- 313 314 $CIPH_K$ is not needed for the modes that are specified in this publication.
 - 315 For both modes, the underlying block cipher shall be approved, and the block size shall be 128
 - 316 bits. Currently, the AES block cipher [12], with key lengths of 128, 192, or 256 bits, is the only
 - 317 block cipher that fits this profile.
 - 318 The choice of the key length affects the security of the FPE modes, e.g., against brute-force search,
 - 319 and also affects the details of the implementation of the AES algorithm. Otherwise, the key length
 - 320 does not affect the implementation of FF1 and FF3-1, and the choice of the key length is not

² The forward transformation and the inverse transformations are sometimes referred to as the "encrypt" and "decrypt" functions, respectively, of the block cipher; however, in this publication, "encrypt" and "decrypt" are reserved for functions of the FPE modes.

explicitly indicated in their specifications. Methods for generating cryptographic keys are 321 discussed in [16]; the goal is to select the keys uniformly at random, i.e., for each possible key to

- 322
- 323 occur with equal probability.

324 The key shall be kept secret, i.e., disclosed only to parties that are authorized to know the protected 325 information. Compliance with this requirement is the responsibility of the entities using, 326 implementing, installing, or configuring applications that incorporate the functions that are 327 specified in this publication. The management of cryptographic keys is outside the scope of this 328 publication.

329 4.3 **Encryption and Decryption Functions**

330 For a given key, denoted by K, for the designated block cipher, FF1 and FF3-1 each consist of two 331 related functions: encryption and decryption. The inputs to the encryption function are a numeral 332 string called the plaintext, denoted by X, and a byte string, called the tweak, denoted by T; the function returns a numeral string called the ciphertext, denoted by Y, with the same length as X. 333 334 Similarly, the inputs to the decryption function are a numeral string X and a tweak T; the output is 335 a numeral string *Y* of the same length as *X*.

- 336 For FF1, the encryption function is denoted by FF1. Encrypt(K, T, X), and the decryption function
- 337 is denoted by FF1.Decrypt(K, T, X), with analogous notation for FF3-1.
- 338 For a given tweak, the decryption function is the inverse of the encryption function, so that

339
$$FF1.Decrypt(K, T, FF1.Encrypt(K, T, X)) = X,$$
340 $FF3-1.Decrypt(K, T, FF3-1.Encrypt(K, T, X)) = X.$

341

The tweak does not need to be kept secret; often, it is some readily available data that is associated 342 343 with the plaintext. Although implementations may fix the value of the tweak, variable tweaks 344 should be used as a security enhancement; see Appendix C. In FF1 and FF3-1, tweaks are byte 345 strings. The specifications in Sec. 5 include the lengths that can be supported for the tweak, as well

346 as for the plaintext/ciphertext.

347 The key, K, is indicated in the above notation as an input for the encryption and decryption 348 functions; however, in the specifications in this publication, the key is listed as a prerequisite, i.e., 349 an input that is usually established prior to the invocation of the function.³ Several other 350 prerequisites are omitted from the above notation, such as the underlying block cipher, the 351 designation of CIPH_K, and the base for the numeral strings.

352 4.4 Feistel Structure

353 FFX schemes, including FF1 and FF3-1, are based on the Feistel structure. The Feistel structure 354 consists of several iterations, called *rounds*, of a reversible transformation. The transformation 355 consists of three steps: 1) the data is split into two parts; 2) a keyed function, called the round 356 function, is applied to one part of the data in order to modify the other part of the data; and 3) the 357 roles of the two parts are swapped for the next round. The structure is illustrated in Figure 1 below,

³ The distinction does not affect the execution of the function: all information is required, independent of when they were established or provided to the implementation.

for both encryption and decryption. Four rounds are shown in Figure 1, but ten rounds are actually specified for FF1, and eight rounds for FF3-1.



360 361



Figure 1: Feistel Structure

363 For the encryption function example in Figure 1, the rounds are indexed from 0 to 3. The input 364 data (and output data) for each round are two strings of characters—which will be numerals for 365 FF1 and FF3-1. The lengths of the two strings are denoted by u and v, and the total number of characters is denoted by n, so that u+v=n. During Round i, the round function, denoted by F_K, is 366 367 applied to one of the input strings, denoted by B_i , with the length n, the tweak T, and the round number i as additional inputs. (In Figure 1, this triple (n, T, i) of additional inputs is indicated 368 369 within the dotted rectangles, with the appropriate values for *i*). The result is used to modify the other string, denoted by A_i , via modular addition⁴, indicated by +, on the numbers that the strings 370

⁴ For some applications of the Feistel structure—but not FF1 and FF3-1—the "+" operation may be a different reversible operation on strings that preserves their length; for example, the FFX specification in [2] supports an option for character-wise addition.

- 371 represent⁵. The string that represents the resulting number is named with a temporary variable, C_i .
- 372 The names of the two parts are swapped for the next round, so that the modified A_i , i.e., C_i , becomes
- 373 B_{i+1} , and B_i becomes A_{i+1} .

The rectangles containing the two parts of the data have different sizes in order to illustrate that ucannot equal v if n is odd. In such cases, the round function is constructed so that the lengths of its input and output strings depend on whether the round number index, i, is even or odd.

- 377 The Feistel structure for decryption is almost identical to the Feistel structure for encryption. There
- are three differences: 1) the order of the round indices is reversed; 2) the roles of the two parts of
- the data in the round function are swapped as follows: along with *n*, *T*, and *i*, the input to F_K is A_{i+1}
- 380 (not B_i), and the output is combined with B_{i+1} (not A_i) to produce A_i (not B_{i+1}); and 3) modular
- addition (of the output of F_K to A_i) is replaced by modular subtraction (of the output of F_K from B_{i+1}).
- 383 **4.5 Component Functions**

This section gives algorithms for the component functions that are called in the specifications of FF1 and FF3-1. The conversion functions $NUM_{radix}(X)$, NUM(X), and $STR^m_{radix}(x)$ are defined in Sec. 3.3, including examples, and they are specified in Algorithms 1-3 below. These functions support the ordering convention for the numeral/bit strings in FF1, namely, that the first (i.e., leftmost) numeral/bit of the string is the most-significant numeral/bit

In FF3-1, the numeral strings follow the opposite ordering convention, as do the byte strings for the block cipher. In order to adapt $NUM_{radix}(X)$, $STR_{radix}^m(x)$, and $CIPH_K(X)$ for the FF3-1 specifications, the functions REV(X) and REVB(X) are defined in Sec. 3.3 and specified in Algorithms 4 and 5.

The PRF(X) function, specified in Algorithm 6, essentially invokes the Cipher Block Chaining encryption mode [14] on the input bit string and returns the final block of the ciphertext; this function is the pseudorandom core of the Feistel round function for FF1.Encrypt and FF1.Decrypt.

In order to simplify the specifications of NUM(X), REVB(X), and PRF(X), the byte or block strings in Algorithms 2, 5, and 6 are represented as bit strings.

398	Algorithm 1: $NUM_{radix}(X)$
399 400	Prerequisite:
401 402	Base, <i>radix</i> .
403	Input:
404 405	Numeral string, X.
406	Output:
407 408 409	Number, <i>x</i> .

⁵ The ordering convention for interpreting strings as numbers is different for FF3-1 than for FF1.

)	Steps:		
	1. Let $x = 0$.		
2	2. For <i>i</i> from 1 to LEN(<i>X</i>), let $x = x \cdot radix + X[i]$.		
5	3. Return x .		
ŀ			
	Algorithm 2: NUM(X)		
	Input: Dete string V represented in hits		
	Byte string, <i>x</i> , represented in bits.		
	Output:		
	Integer, x.		
	Steps:		
	1. Let $x = 0$. 2. Each i from 1 to LEN(V) let $y = 2y + V[i]$		
	2. FOR <i>t</i> HOLEN(A), let $x = 2x \pm A[t]$. 3. Return <i>r</i>		
	5. Return <i>x</i> .		
	Algorithm 3: $STR_{radix}^{m}(x)$		
	Prerequisites:		
	Base, radix;		
	String length, <i>m</i> .		
	Innut		
	Integer r such that $0 < r < radirm$		
	$\operatorname{Integer}_{\mathcal{A}}$, such that $0 \leq x$ stratage.		
	Output:		
	Numeral string, X.		
	C,		
	Steps: 1 For i from 1 to m		
	1. FOLT HOLE I WILL $V[m+1, i] = r \mod radiv$		
	1. $A[m+1-t] = \lambda$ mod t and λ ; ii. $x = x /a dix $		
	$\frac{1}{2} = \frac{1}{2} \sum_{i=1}^{n} \frac{1}{2} \sum_{i=1$		
	Algorithm 4: $\operatorname{REV}(X)$		
	Input:		
	Numeral string, X.		
	Output:		
	Numeral string, Y.		
	-		
	Steps:		
	1. For <i>i</i> from 1 to LEN(<i>X</i>), let $Y[i] = X[LEN(X)+1-i]$.		
	2. Return $Y[1LEN(X)]$.		

457	Algorithm 5: REVB(X)					
458						
459	Input:					
460	Byte string, X, represented in bits.					
461						
462	Output:					
463 464	Byte string, <i>Y</i> , represented in bits.					
465	Steps:					
466 467	1. For <i>i</i> from 0 to BYTELEN(X) – 1 and <i>j</i> from 1 to 8, let $Y[8i+j] = X[8 \cdot (BYTELEN(X) - 1 - i) + j]$. 2. Return $Y[18 \cdot BYTELEN(X)]$.					
468						
469	Algorithm 6: PRF(<i>X</i>)					
470	Ducucruisitor					
4/1	Prerequisites:					
472	Designated cipner function, CIPH, of an approved 128-bit block cipner; $V_{\text{ext}} = V_{\text{ext}}$ for the block eightr					
474	Key, K, for the block cipher.					
475	Input:					
476	Block string X					
477						
478	Output:					
479	Block, Y.					
480						
481	Steps:					
482	1. Let $m = \text{LEN}(X)/128$.					
483	2. Let X_1, \ldots, X_m be the blocks for which $X = X_1 \parallel \ldots \parallel X_m$.					
484	3. Let $Y_0 = 0^{128}$, and for <i>j</i> from 1 to <i>m</i> let $Y_j = \text{CIPH}_K(Y_{j-1} \oplus X_j)$.					
485	4. Return Y_m .					

486 **5 Mode Specifications**

487 The specifications of the encryption and decryption algorithms for FF1 and FF3-1 are presented in Sections 6.1 and 6.2, organized into prerequisites, inputs, outputs, steps, and descriptions of the 488 489 steps. In addition to the key and designated cipher function, the prerequisites for each mode are 490 the choices of 1) the base, *radix*, and 2) the range of lengths, [*minlen..maxlen*], for the numeral 491 string inputs that the implementation supports. FF1 also has a prerequisite for the choice of the 492 maximum tweak length, maxTlen, that the implementation supports. For each mode, the 493 requirements on the values for the prerequisites are specified prior to the encryption and decryption 494 algorithms.

The parameter choices may affect interoperability. The behavior of an implementation when presented with incorrect inputs is outside the scope of this Recommendation.

497 For each specification, the 128-bit input and output blocks of the designated block cipher, $CIPH_K$, 498 are represented as strings of 16 bytes.

499	5.1 FF1					
500 501	The specifications for the FF1.Encrypt and FF1.Decrypt functions are given in Algorithms 7 and 8 below. The tweak, T , is optional, in that it may be the empty string, with byte length $t=0$.					
502 503	The parameters <i>radix</i> , <i>minlen</i> , and <i>maxlen</i> in FF1.Encrypt and FF1.Decrypt shall meet the following requirements:					
504 505 506 507	 <i>radix</i> ∈ [22¹⁶], <i>radix</i>^{minlen} ≥ 1 000 000, and 2 ≤ minlen ≤ maxlen < 2³². 					
508	Algorithm 7: FF1.Encrypt(<i>K</i> , <i>T</i> , <i>X</i>)					
509 510 511 512 513 514 515	 <i>Prerequisites:</i> Designated cipher function, CIPH, of an approved 128-bit block cipher; Key, <i>K</i>, for the block cipher; Base, <i>radix</i>; Range of supported message lengths, [<i>minlenmaxlen</i>]; Maximum byte length for tweaks, <i>maxTlen</i>. 					
516 517 518 519 520	<i>Inputs</i> : Numeral string, <i>X</i> , in base <i>radix</i> of length <i>n</i> , such that $n \in [minlenmaxlen]$; Tweak <i>T</i> , a byte string of byte length <i>t</i> , such that $t \in [0maxTlen]$.					
521 522 523	<i>Output</i> : Numeral string, <i>Y</i> , such that $LEN(Y) = n$.					
525 524	Steps:					
525	1. Let $u = \lfloor n/2 \rfloor$; $v = n - u$. 2. Let $d = V[1, v]$; $p = V[v + 1, v]$					
520 527	2. Let $A = A[1u], D = A[u + 1u].$ 3. Let $b = \left[\int_{U} LOC(radir) \right]/8$					
528	5. Let $b = v \cdot 100(raax) v $. A Let $d = A \left[b/A \right] + A$					
529	5. Let $P = [1]^1 [2]^1 [1]^1 [radix]^3 [10]^1 [u \mod 256]^1 [n]^4 [t]^4$					
530	6. For <i>i</i> from 0 to 9:					
531	i. Let $Q = T \parallel [0]^{(-t-b-1) \mod 16} \parallel [i]^1 \parallel [\text{NUM}_{radix}(B)]^b$.					
532	ii. Let $R = PRF(P \parallel Q)$.					
533	iii. Let S be the first d bytes of the following string of $\lceil d/16 \rceil$ blocks:					
534	$R \parallel \operatorname{CIPH}_{K}(R \oplus [1]^{16}) \parallel \operatorname{CIPH}_{K}(R \oplus [2]^{16}) \dots \operatorname{CIPH}_{K}(R \oplus [\lceil d/16 \rceil - 1]^{16}).$					
535	iv. Let $y = \text{NUM}(S)$.					
536	v. If <i>i</i> is even, let $m = u$; else, let $m = v$.					
537	v1. Let $c = (\text{NUM}_{radix}(A) + y) \mod radix^m$.					
538	V11. Let $C = \text{STR}_{radix}^m(C)$.					
539 540	VIII. Let $A = B$.					
540 541	1X. Let $D = C$. 7 Return $A \parallel B$					
542						

543 Description

- The "split" of the numeral string X into two substrings, A and B, is performed in Steps 1 and 2. If *n* is even, LEN(A)=LEN(B); otherwise, LEN(A)=LEN(B)-1. The byte lengths b and d, which are used in Steps 6i and 6iii, respectively, are defined in Steps 3 and 4.⁶ A fixed block, P, used as the initial
- 547 block for the invocation of the function PRF in Step 6ii, is defined in Step 5. An iteration loop for
- 548 the ten Feistel rounds of FF1 is initiated in Step 6, executing nine substeps for each round, as
- 549 follows:

550 The tweak T, the substringB, and the round number i, are encoded as a binary string O, in Step 6i. The function PRF is applied to the concatenation of P and Q in Step 6ii, to produce a block, R, 551 which is either truncated or expanded to a byte string, S, with the appropriate number of bytes, d, 552 553 in Step 6iii. (In Figure 1, S corresponds to the output of F_{κ} .) In Steps 6iv to 6vii, S is combined 554 with the substring A to produce a numeral string C in the same base and with the same length. (In Figure 1, the combining of S with A is indicated by the "+" operation.) In particular, in Step 6iv, S 555 556 is converted to a number, y. In Step 6v, the length, m, of A for this Feistel round is determined. In 557 Step 6vi, y is added to the number represented by the substring A, and the result is reduced modulo 558 the *m*th power of *radix*, yielding a number, *c*, which is converted to a numeral string in Step 6vii. 559 In Steps 6viii and 6ix, the roles of A and B are swapped for the next round: the substring B is 560 renamed as the substring A, and the modified A (i.e., C) is renamed as B.

561 This completes one round of the Feistel structure in FF1. After the tenth round, the concatenation

- 562 of A and B is returned as the output in Step 7.
- 563

564 Algorithm 8: FF1.Decrypt(K, T, X)

- 565
- 566 Prerequisites:

567 Designated cipher function, CIPH, of an approved 128-bit block cipher;

- 568 Key, *K*, for the block cipher;
- 569 Base, *radix*;
- 570 Range of supported message lengths, [minlen..maxlen];
- 571 Maximum byte length for tweaks, *maxTlen*.
- 572573 *Inputs*:
- 574 Numeral string, X, in base *radix* of length n, such that $n \in [minlen..maxlen]$;
- 575 Tweak *T*, a byte string of byte length *t*, such that $t \in [0..maxTlen]$.
- 576
- 577 *Output*:
- 578 Numeral string, *Y*, such that LEN(Y) = n.
- 579 *Steps*:
- 580 1. Let $u = \lfloor n/2 \rfloor$; v = n u.
- 581 2. Let A = X[1...u]; B = X[u+1...n].
- 582 3. Let $b = \lceil \lceil v \cdot \text{LOG}(radix) \rceil / 8 \rceil$.
- 583 4. Let $d = 4 \lfloor b/4 \rfloor + 4$
- 584 5. Let $P = [1]^1 || [2]^1 || [1]^1 || [radix]^3 || [10]^1 || [u \mod 256]^1 || [n]^4 || [t]^4$.

⁶ When *B* is encoded as a byte string in Step 6i, *b* is the number of bytes in the encoding. The definition of *d* ensures that the output of the Feistel round function is at least four bytes longer than this encoding of *B*, which minimizes any bias in the modular reduction in Step 6vi.

585 586	6.	For <i>i</i> from 9 to 0: $I = I = I = O = T [O]^{(-t-b-1) \mod 16} [i]^1 [NUM = i (A)]^b$
580		i. Let $\mathcal{Q} = I \parallel [0]$, $\parallel [l] \parallel [NOM_{radix}(A)]$. ii. Let $\mathcal{R} = \text{DDE}(\mathcal{P} \parallel \mathcal{O})$
588		iii Let X be the string of the first d bytes of the following string of $d/16$ blocks:
580		III. Let 5 be the string of the first <i>a</i> bytes of the following string of $a/16$ [000eks. $P \parallel_{\text{CIDII}}$ ($P \oplus [1]^{16} \parallel_{\text{CIDII}}$ ($P \oplus [2]^{16}$) _ CIDII ($P \oplus [\frac{1}{2}/16]$ _ 1]^{16})
500		$ \begin{array}{c} \Lambda \parallel CIPH_K(\Lambda \oplus \lfloor 1 \rfloor^{-1}) \parallel CIPH_K(\Lambda \oplus \lfloor 2 \rfloor^{-1}) \dots CIPH_K(\Lambda \oplus \lfloor u/10 \rfloor - 1 \rfloor^{-1}). \end{array} $
590		IV. Let $y = \text{NOM}(S)$.
502		v. If t is even, let $m = u$, else, let $m = v$.
502		vii. Let $C = (\text{NOM}_{radix}(D) - y) \mod radix$.
595		VII. Let $C = SIR_{radix}(C)$.
505		VIII. Let $B = A$.
393 506	7	1X. Let $A = C$.
590 507	/.	Return $A \parallel D$.
508	Dag	avintion
500	Des The	FE1 Decrypt algorithm is similar to the FE1 Encrypt algorithm; the differences are in Step 6
<i>599</i> 600	who	TT 1. Decrypt algorithm is similar to the TT 1. Encrypt algorithm, the differences are in Step 0, re: 1) the order of the indices is reversed 2) the reles of A and P are swapped and 3) modular
601	add	ition is replaced by modular subtraction, in Step 6vi.
602	5.2	FF3-1
605 606 607 608 609 610	shal	Il meet the following requirements: • $radix \in [22^{16}],$ • $radix^{minlen} \ge 1000000, \text{ and}$ • $2 \le minlen \le maxlen \le 2\lfloor \log_{radix}(2^{96}) \rfloor.$
611	Alg	orithm 9: FF3-1.Encrypt(K, T, X)
612	л	
613	Dee	requisites:
014 615	Vov	Ignated cipiter function, CIPH, of an approved 128-bit block cipiter,
013	Rey Dec	, K, for the block cipher;
010	Bas	e, raaix;
$\frac{01}{10}$	Kan	ge of supported message lengths, [minienmaxien].
018	I	
019	Inpi	$us: \qquad 1 i X i i 1 i 1 i i j j j j j j j j$
620	Nur	neral string, X, in base <i>radix</i> of length n, such that $n \in [minlenmaxlen];$
621	IW	eak bit string, T , such that $Len(T) = 50$.
622		
023 624	Ω_{114}	nut
625	N	μu .
023	INUÍ	nerar sumg, 1, such that LEN(1) - n.
020		

- 627 Steps:
- 628
- 1. Let $u = \lceil n/2 \rceil$; v = n u. 2. Let A = X[1..u]; B = X[u + 1..n]. 629

- 630 3. Let $T_L = T[0..27] \parallel 0^4$ and $T_R = T[32..55] \parallel T[28..31] \parallel 0^4$.
- 631 4. For *i* from 0 to 7:
- 632 i. If *i* is even, let m = u and $W = T_R$, else let m = v and $W = T_L$.
- 633 ii. Let $P = W \bigoplus [i]^4 || [\text{NUM}_{radix}(\text{REV}(B))]^{12}$.
- 634 iii Let $S = \text{REVB}(\text{CIPH}_{\text{REVB}(K)}\text{REVB}(P))$.
- 635 iv. Let y = NUM(S).
- 636 v. Let $c = (\text{NUM}_{radix}(\text{REV}(A)) + y) \mod radix^{m}$.
- 637 vi. Let $C = \text{REV}(\text{STR}_{radix}^{m}(c))$.
- 638 vii. Let A = B.
- 639 viii. Let B = C.
- 640 5. Return $A \parallel B$.
- 641642 *Description*:
- The "split" of the numeral string X into two substrings, A and B, is performed in Steps 1 and 2. If *n* is even, LEN(A)=LEN(B); otherwise, $LEN(A)=LEN(B)+1.^7$ The tweak, T, is partitioned in Step 3 into a 32-bit left tweak, T_L , and a 32-bit right tweak, T_R . An iteration loop for the eight Feistel rounds of FF3-1 is initiated in Step 4, executing eight substeps for each round, as follows:
- 647

648 In Step 4i, the parity of the round number, i, determines the length, m, of the substring A, and 649 whether T_L or T_R will be used as W in Step 4ii, in which a 32-bit encoding of i, XORed with W, is concatenated with a 96-bit encoding of *B* to produce a block, *P*. In Step 4iii, the block cipher under 650 the key, is applied to P using the byte-reversed ordering convention, to produce a block, S. (In 651 652 Figure 1, S corresponds to the output of F_{K} .) In Steps 4iv to 4vi, S is combined with the substring 653 A to produce a numeral string C in the same base and with the same length. (In Figure 1, the combining of S with A is indicated by the "+" operation, although this operation is different than 654 655 for FF1 in that FF3-1 uses the opposite ordering convention for the conversion of strings to 656 numbers and vice versa.) In particular, in Step 4iv, S is converted to a number, y. In Step 4v, the 657 number v is added to the number represented by the substring A, and the result is reduced modulo 658 the *m*th power of *radix*, yielding a number, *c*, which is converted to a numeral string in Step 4vi. 659 In Steps 4vii and 4viii, the roles of A and B are swapped for the next round: the substring B is 660 renamed as the substring A, and the modified A (i.e., C) is renamed as B.

661

662 This completes one round of the Feistel structure in FF3-1. After the eighth round, the 663 concatenation of A and B is returned as the output in Step 5.

664

 $\begin{array}{l} 665 \\ \hline \text{Algorithm 10: FF3-1.Decrypt}(K, T, X) \end{array}$

666

667 *Prerequisites:*

- 668 Designated cipher function, CIPH, of an approved 128-bit block cipher;
- 669 Key, *K*, for the block cipher;
- 670 Base, *radix*;
- 671 Range of supported message lengths, [minlen..maxlen].
- 672
- 673 Inputs:
- Numeral string, *X*, in base *radix* of length *n*, such that $n \in [minlen..maxlen]$;

⁷ If *n* is odd, *A* is one numeral longer than *B*, in contrast to FF1, where *B* is one numeral longer than *A*.

675	Tweak bit string, T, such that $LEN(T) = 64$.						
676							
677	Out	Output:					
678	Numeral string, Y, such that $LEN(Y) = n$.						
679							
680	Step	Steps:					
681	1.	Let $u = [n/2]; v = n - u$.					
682	2.	Let $A = X[1u]; B = X[u + 1n].$					
683	3.	Let $T_L = T[027] \parallel 0^4$ and $T_R = T[3255] \parallel T[2831] \parallel 0^4$.					
684	4.	For <i>i</i> from 7 to 0:					
685		i. If <i>i</i> is even, let $m = u$ and $W = T_R$, else let $m = v$ and $W = T_L$.					
686		ii. $P = W \bigoplus [i]^4 \parallel [\operatorname{NUM}_{radix}(\operatorname{REV}(A))]^{12}.$					
687		iii Let $S = \text{REVB}(\text{CIPH}_{\text{REVB}(K)}\text{REVB}(P))$.					
688		iv. Let $y = \text{NUM}(S)$.					
689		v. Let $c = (\text{NUM}_{radix}(\text{REV}(B)) - y) \mod radix^{m}$.					
690		vi. Let $C = \text{REV}(\text{STR}^m_{radix}(c))$.					
691		vii. Let $B = A$.					
692		viii. Let $A = C$.					
693	5.	Return $A \parallel B$.					
694							
695	Des	cription:					
(0)							

- The FF3-1.Decrypt algorithm is similar to the FF3-1.Encrypt algorithm; the differences are in Step 4, where: 1) the order of the indices is reversed, 2) the roles of A and B are swapped, and
- 698 3) modular addition is replaced by modular subtraction, in Step 4v.

699 6 Conformance

Implementations of FF1.Encrypt, FF1.Decrypt, FF3-1.Encrypt, or FF3-1.Decrypt may be tested
 for conformance to this Recommendation under the auspices of NIST's Cryptographic Algorithm
 Validation Program [12].

703 Component functions such as PRF are not approved for use independent of these four functions.

In order to claim conformance with this Recommendation, an implementation of FF1 or FF3-1
 may support as few as one value for the base.

Two implementations can only interoperate when they support common values for the base. Moreover, FF1 and FF3-1 have two parameters, *minlen* and *maxlen*, that determine the lengths for the numeral strings that are supported by an implementation of the encryption or decryption function for the mode. FF1 also has a parameter, *maxTlen*, that indicates the maximum supported length of a two length string. The selection of these nerve also affect interpreter bility.

- 710 length of a tweak string. The selection of these parameters may also affect interoperability.
- 711 For every algorithm that is specified in this Recommendation, a conforming implementation may
- replace the given set of steps with any mathematically equivalent set of steps. In other words,
- 713 different procedures that produce the correct output for any input are permitted.

714 Appendix A: Parameter Choices and Security

The values of the parameters, e.g., *radix*, *minlen*, and *maxlen* affect the security that FF1 and FF3-1 can offer, because, as for any FPE method, encrypted data may be vulnerable to guessing attacks when the number of possible inputs is sufficiently small.

In particular, for a base *radix* numeral string *S*, there are *radix* $^{\text{LEN}(S)}$ possible values. For any ciphertext *C*, the corresponding plaintext has the same length; therefore, an attacker can guess the plaintext with probability 1/radix $^{\text{LEN}(C)}$ by selecting a numeral string of LEN(C) at random. Repeated guesses increase the attacker's probability of success proportionately: with *g* distinct guesses, the probability is g/radix $^{\text{LEN}(C)}$.

- For example, SSNs are base 10 numeral strings of length 9, so there are one billion possibilities.
- If an attacker could guess a thousand different values for an SSN, one of the guesses would be correct with probability $1000/10^9$, i.e., one in a million.
- 726 The original specifications of FF1and FF3 only imposed a modest absolute minimum of 100 on
- the number of possible inputs in order to preclude a generic meet-in-the-middle attack on the
- 728 Feistel structure [17]. However, in order to mitigate guessing attacks and the analytic attacks
- described in [1] and [8], the number of possible inputs, namely *radix^{minlen}*, is required to be greater
- than or equal to 1 000 000, for both FF1 and FF3-1. In order to further limit the effectiveness of
- 731 guessing attacks, implementations should also limit the number of guesses that an attacker can
- 732 mount, if possible.
- 733 In order to prevent attacks against one instance of encryption from applying to other instances,
- implementations should enforce the use of different tweaks for different instances, as discussed in
- Appendix C. Usually, tweaks are non-secret information that can be associated with instances of encryption. For FF3-1, the tweak length is fixed, but for FF1 the maximum tweak length parameter,
- 737 *maxTlen*, should be chosen to accommodate the desired tweaks for the implementation.
- 738 Two other potential parameters of the Feistel structure are fixed for FF1 and FF3-1, namely, the
- number of Feistel rounds and the imbalance, i.e., the values of the lengths *u* and *v* in Figure 1. Both
- of these parameters were set with consideration to both performance and security requirements.
- 741 See Appendix H of [2] for a discussion.

742 Appendix B: Security Goal

743 The designers of FFX aimed to achieve strong-pseudorandom permutation (PRP) security for a

- conventional block cipher [10]. In the FFX proposal to NIST [2], the designers of FFX cited the
- history of cryptographic results concerning Feistel networks as underlying their selection of the
- FFX mechanism. They asserted that, under the assumption that the underlying round function is
- a good pseudorandom function (PRF), contemporary cryptographic results and experience
- indicate that FFX achieved several cryptographic goals, including nonadaptive message-recovery
- security, chosen-plaintext security, and even PRP-security against an adaptive chosen-ciphertext
- attack. The quantitative security would depend on the number of rounds used, the imbalance, and
- the adversary's access to plaintext-ciphertext pairs. See [2] for details.

752 Appendix C: Tweaks

753 Tweaks have been supported in stand-alone block ciphers, such as Schroeppel's Hasty Pudding 754 [18], and the notion was later formalized and investigated by Liskov, Rivest, and Wagner [9]. 755 Tweaks are important for FPE modes, because FPE may be used in settings where the number of 756 possible character strings is relatively small. In such settings, the tweak should vary with each 757 instance of the encryption whenever possible.

758 For example, suppose that in an application for CCNs, the leading six digits and the trailing four 759 digits need to be available to the application, so that only the remaining six digits in the middle of 760 the CCNs are encrypted. There are a million different possibilities for these middle-six digits, so, 761 in a database of 100 million CCNs, about a hundred distinct CCNs would be expected to share 762 each possible value for these six digits. If the hundred CCNs that shared a given value for the 763 middle-six digits were encrypted with the same tweak, then their ciphertexts would be the same. 764 If, however, the other ten digits had been the tweak for the encryption of the middle-six digits, 765 then the hundred ciphertexts would almost certainly be different.

Similarly, in the encrypted database, about a hundred CCNs would be expected to share each possible value for the ciphertext, i.e., the middle-six digits. If the hundred CCNs that produce a given ciphertext had been encrypted with the same tweak, then the corresponding plaintexts would also be the same. This outcome would be undesirable because the compromise of the confidentiality of any of the hundred CCNs would reveal the others.

If, however, the leading six digits and the trailing four digits of the CCN had been used as the tweak, then the corresponding plaintexts would almost certainly be different. Therefore, for example, learning that the decryption of 111111-770611-1111 is 111111-123456-1111 would not reveal any information about the decryption of 999999-770611-9999, because the tweak in that case was different.

In general, if there is information that is available and statically associated with a plaintext, it is recommended to use that information as a tweak for the plaintext. Ideally, the non-secret tweak associated with a plaintext is associated only with that plaintext.

779 Extensive tweaking means that fewer plaintexts are encrypted under any given tweak. This

corresponds, in the security model that is described in [2], to fewer queries to the target instance

781 of the encryption.

782 Appendix D: Examples

- 783 Examples for FF1 and FF3-1 are available at the examples page on NIST's Computer Security
- 784 Resource Center website: <u>https://csrc.nist.gov/projects/cryptographic-standards-and-</u>
- 785 guidelines/example-values.

786 Appendix E: References

- M. Bellare, V. T. Hoang, and S. Tessaro, "Message-recovery attacks on Feistel-based
 Format Preserving Encryption," in ACM CCS '16, pages 444–455, ACM Press, 2016, https://doi.org/10.1145/2976749.2978390.
- M. Bellare, P. Rogaway, and T. Spies, *The FFX Mode of Operation for Format- Preserving Encryption*, Draft 1.1, February 20, 2010,
 <u>https://csrc.nist.gov/csrc/media/projects/block-cipher-</u>
 techniques/documents/bcm/proposed-modes/ffx/ffx-spec.pdf.
- M. Bellare, P. Rogaway, and T. Spies, Addendum to "The FFX Mode of Operation for Format-Preserving Encryption": A parameter collection for enciphering strings of arbitrary radix and length, Draft 1.0, September 3, 2010, <u>https://csrc.nist.gov/csrc/media/projects/block-cipher-</u>
 techniques/documents/bcm/proposed-modes/ffx/ffx-spec2.pdf.
- [4] E. Brier, T. Peyrin, and J. Stern, *BPS: a Format-Preserving Encryption Proposal*, [April 2010], <u>https://csrc.nist.gov/csrc/media/projects/block-cipher-</u>
 801 techniques/documents/bcm/proposed-modes/bps/bps-spec.pdf.
- Y-A. de Montjoye, L. Radaelli, V. Kumar Singh, and A. Pentland, "Unique in the shopping mall: On the reidentifiability of credit card metadata," *Science*, vol. 347 no.
 6221 (January 30, 2016), pp. 536-539, <u>https://doi.org/10.1126/science.1256297</u>.
- 805 [6] M. Dworkin and R. Perlner, *Analysis of VAES3 (FF2)*, Report no. 2015/306, IACR
 806 Cryptology ePrint Archive, April 2, 2015, <u>https://eprint.iacr.org/2015/306</u>
- F. B. Durak and S. Vaudenay, "Breaking the FF3 Format-Preserving Encryption Standard Over Small Domains" in *Advances in Cryptology*—*CRYPTO 2017*, Lecture Notes in Computer Science vol. 10402, Springer, pp. 679–707, <u>https://doi.org/10.1007/978-3-319-</u>
 63715-0_23.
- [8] V.T. Hoang, S. Tessaro, N. Trieu, "The Curse of Small Domains: New Attacks on
 Format-Preserving Encryption" in *Advances in Cryptology—CRYPTO 2018*, Lecture
 Notes in Computer Science 10991, Springer, Cham., pp. 221–251,
 https://doi.org/10.1007/978-3-319-96884-1
- 815 [9] M. Liskov, R. Rivest, and D. Wagner, "Tweakable block ciphers," in *Advances in*816 *Cryptology—CRYPTO 2002*, Lecture Notes in Computer Science 2442, Berlin: Springer,
 817 pp. 31–46, September 13, 2002, https://doi.org/10.1007/3-540-45708-9 3.
- 818 [10] M. Luby and C. Rackoff, "How to construct pseudorandom permutations from pseudorandom functions," *SIAM Journal on Computing*, vol. 17 no. 2 (1988), pp. 373– 386, <u>https://doi.org/10.1137/0217022</u>.
- [11] National Institute of Standards and Technology, *Explanation of changes to Draft SP 800-38G*, June 27, 2014, <u>https://csrc.nist.gov/news/2014/explanation-of-changes-to-draft-sp-823</u>
 <u>800-38G</u>.
- [12] National Institute of Standards and Technology, *Cryptographic Algorithm Validation Program (CAVP)*, <u>https://csrc.nist.gov/projects/cryptographic-algorithm-validation-</u>
 program.

- [13] National Institute of Standards and Technology, Federal Information Processing Standard
 (FIPS) 197, *The Advanced Encryption Standard (AES)*, November 2001,
 https://doi.org/10.6028/NIST.FIPS.197.
- [14] National Institute of Standards and Technology. NIST Special Publication (SP) 800-38A,
 Recommendation for Block Cipher Modes of Operation—Methods and Techniques,
 December 2001, https://doi.org/10.6028/NIST.SP.800-38A.
- [15] National Institute of Standards and Technology. NIST Special Publication (SP) 800-67
 Revision 2, *Recommendation for the Triple Data Encryption Algorithm (TDEA) Block Cipher*, January 2012, <u>https://doi.org/10.6028/NIST.SP.800-67r2</u>.
- [16] National Institute of Standards and Technology. NIST Special Publication (SP) 800-133,
 Recommendation for Cryptographic Key Generation, December 2012,
 <u>https://doi.org/10.6028/NIST.SP.800-133</u>.
- 839 [17] J. Patarin, *Generic attacks on Feistel schemes*, Report no. 2008/036, IACR Cryptology
 840 ePrint Archive, January 24, 2008, <u>https://eprint.iacr.org/2008/036</u>.
- R. Schroeppel, *Hasty Pudding Cipher specification* [Web page], June 1998 (revised May 1999), <u>http://richard.schroeppel.name:8015/hpc/hpc-spec</u>.

843 Appendix F: Revision History

A third mode, FF2—submitted to NIST under the name VAES3—was included in the initial draft of this publication. As part of the public review of Draft NIST Special Publication (SP) 800-38G and as part of its routine consultation with other agencies, NIST was advised by the National Security Agency in general terms that the FF2 mode in the draft did not provide the expected 128 bits of security strength. NIST cryptographers confirmed this assessment via the security analysis in [6] and announced the removal of FF2 in [11].

- 850 For both FF1 and FF3-1, the domain size, i.e., the number of possible input strings, is the quantity
- 851 *radix^{minlen}*. In response to the analysis in [8], the lower bound that is required for the domain size
- 852 in the specifications of both FF1 in Sec. 5.1 and FF3-1 in Sec. 5.2 was raised from one hundred in
- the original publication to one million in Rev. 1.
- 854

The name "FF1" is unchanged from the original version of this publication, because the lower bound on the domain size only affects which parameter combinations are approved, not the specification of the encryption and decryption functions. FF3-1 has a different name than FF3 because, in addition to the new lower bound on the domain size, the encryption and decryption

- 859 functions of FF3 were revised.
- 860

In particular, in response to the analysis in [7] on FF3, the size of the tweak specified in Sec. 5.2 was reduced from 64 bits for FF3 to 56 bits for FF3-1, which entailed the modification of the definitions of the strings T_L and T_R in Step 3 of Algorithm 9 and Step 3 of Algorithm 10. The modified definitions of these two strings can equivalently be implemented by taking a 64-bit tweak, reordering some of its bits in a particular manner, and then forcing the bits in eight particular bit positions to be zero. For tweaks with certain properties—for example, if non-zero bits only occur in the leading 28 bit positions—the specification of FF3-1 is backwards compatible with the

867 occur in the leading 28 bit positions—the specification of FF3-1 is backwards compat 868 original specification of FF3.