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NBS HANDBOOK 133

U.S. DEPARTMENT OF COMMERCE / National Bureau of Standards

CHECKING THE NET CONTENTS OF PACKAGED GOODS



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Checking the Net Contents of Packaged Goods

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PREFACE

This handbook supersedes National Bureau of Standards (NBS) Handbook 67 "Checking Prepackaged Commodities". Legislative authority for the handbook is the NBS Organic Act (15 U.S.C. 272), which states the NBS functions in part:

> "Cooperation with other Government agencies and with private organizations in the establishment of standard practices, incorporated in codes and specifications."

> "Advisory service to Government agencies on scientific and technical problems."

and

"...cooperation with the States in securing uniformity in weights and measures laws and methods of inspection..."

Although this handbook is intended as a procedural guide for Federal, State, and local regulatory agencies, it will be useful to packagers and manufacturers as well. In order to achieve a body of standard practices in sampling to check compliance with net contents regulations, NBS has met with the U.S. Department of Agriculture, the Food and Drug Administration, and the Federal Trade Commission for several years in the Interagency Committee on Net Weight. Although the objective of this committee has not yet been fully realized, several items of agreement have been reached and are incorporated in the present handbook.

In its advisory capacity, NBS offers the methods contained in this handbook as guidelines. Federal agencies as well as States that have regulatory authority may, if they so desire, adopt these guidelines in codes or specifications.

PURPOSE

The purpose of this handbook is to provide regulatory officials with methods to determine the compliance of packaged goods with net contents labeling regulations.

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Compliance testing of packaged goods is the determination of conformance of the results (that is, the packages produced) of a packaging, distribution, and/or retailing process with specified legal requirements.

This handbook provides procedures to test (by using statistical sampling techniques) individual lots of packages for conformance with legal requirements. Anything that is put into a container, wrapped or banded, and labeled as to quantity may be inspected.

The labeled quantity may be of: weight; volume; linear, square, or cubic measure; count; or combinations thereof. The examination of packaged commodities may be to determine conformance with Federal, State, or local net contents labeling regulations. Most often, compliance testing of packaged goods is carried out to protect the consumer/ purchaser against buying packages with less in them than the labeled quantity and to advise the manufacturer to improve delivered product quantities when necessary.

Inspection for compliance with other labeling requirements (such as size of lettering or units of measurement) may also accompany package quantity compliance testing, but is not covered in this document.

This manual contains information on equipment, test methods, calculations, and test reporting. The handbook is divided into five chapters. The first chapter covers several items of an introductory nature which are directed primarily to the administrator of a package testing program. The remainder of the handbook is intended for use by the field testing official. The second chapter discusses fundamentals and general sampling procedures. The third, fourth, and fifth chapters detail the test methods. Chapter 3 covers packages labeled by weight, Chapter 4 covers packages labeled by volume, and Chapter 5 covers other package quantities. After the general test methods for packages labeled in a particular unit are described, methods for special commodities follow.



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CHAPTER 1. INTRODUCTION

1.1. REGULATORY AGENCIES

1.2. PACKAGE REQUIREMENTS

1.3. THE PACKAGE TESTING PROGRAM

1.4. SAMPLING INSPECTION

1.5. AUDIT TESTING

1.6. 100% TESTING

1.7. SAMPLING PLANS FOR THE AVERAGE REQUIREMENT

1.8. WHY THERE ARE TWO CATEGORIES OF SAMPLING PLANS

1.9. ALLOWANCES FOR VARIATIONS DUE TO MOISTURE LOSS OR GAIN

1.10. DECISIONS PRELIMINARY TO PACKAGE INSPECTION



This chapter provides background information on package regulations and regulatory and enforcement agencies in the United States. The concept of checking packaged goods by sampling is introduced. Other terms which are routine to package inspection are also discussed in the context of this handbook, such as the average requirement, audit testing, and moisture allowance.

1.1. REGULATORY AGENCIES

In the United States, several regulatory agencies have authority in packaged product labeling. At the national level, the U.S. Department of Agriculture promulgates requirements for packaged goods containing meat or poultry, as part of the department's responsibility under the Federal Meat Inspection Act as amended by the Wholesome Meat Act and the Poultry Products Inspection Act as amended by the Wholesome Poultry Products Act. The Food and Drug Administration under the U.S. Department of Health and Human Services promulgates requirements for packages containing all other food products and all drug and cosmetic products and medical devices as part of this agency's responsibility under the Food, Drug, and Cosmetic Act and the Fair Packaging and Labeling Act (FPLA). The Federal Trade Commission promulgates requirements for many nonfood consumersized packaged products as part of the agency's responsibility under the FPLA.

The Environmental Protection Agency promulgates requirements for packaged pesticides as part of the agency's responsibility under the Federal Insecticide, Fungicide and Rodenticide Act. The Bureau of Alcohol, Tobacco, and Firearms in the U.S. Department of the Treasury promulgates regulations for packaged tobacco and alcoholic products as part of its responsibility under the Federal Alcohol Administration Act.

Packaged goods produced for distribution for sale also come under the jurisdiction of State and local weights and measures agencies which have their own legal requirements for packaged goods.

Those parts of the pertinent Federal and State regulations are listed in Appendix B.

Since Federal agencies have legislated authority which may dictate the extent of difference between regulations enforced by individual State agencies and themselves, it will be necessary for State agencies using this handbook to also keep abreast of Federal agency regulations the revisions of which may contain sampling or testing information not in the regulations at the time of publication of this handbook.

1.2. PACKAGE REQUIREMENTS

1.2.1. The Average Requirement

Although the regulations may differ somewhat in wording, the same operational interpretation has traditionally been applied for the purpose of testing packages for compliance with these regulations. This is known in the general terminology of package inspection as the "average requirement." The average requirement is really two requirements which the quantity of contents of packaged goods must meet. The first is a requirement that the average quantity of contents of packages in a lot, shipment, or delivery must at least equal the quantity printed on the label. The second requirement applies to the individual package; that is, the variation of individual package contents from the labeled quantity must not be "unreasonably large." Both requirements apply simultaneously to any given collection of packages. This handbook provides methods to test packages against both requirements. The limits of "reasonable variation" for individual packages are listed in tables of "maximum allowable variation" (Section 2.12.).

1.2.2. An Exception

The National Conference on Weights and Measures (NCWM), an organization of State and local weights and measures officials, has adopted voluntary standards upon which individual jurisdictions may model their laws and regulations. Several States have adopted that portion of the NCWM Model State Regulation for the Method of Sale of Commodities¹ which provides a tolerance for certain package label quantities. In this regulation, such a

¹This regulation is part of National Bureau of Standards (NBS) Handbook 130, 1980, "Model State Laws and Regulations as adopted by the National Conference on Weights and Measures."

tolerance is called an "allowable difference." When packaged product quantities are given tolerances, the average and individual package requirements described above do not apply. This handbook provides procedures for testing these product quantities in Section 5.7.

1.3. THE PACKAGE TESTING PROGRAM

Several items are discussed in this section concerning the establishment of a broad and diversified package testing program.

1.3.1. Where to Test

Packaged commodities may be tested in any location from packaging plant to retail outlet.

From the viewpoint of efficiency, the best location to test any <u>individual</u> packaged product is at the location where the product is packaged. The official can sample from the largest number of packages available at one place, the packager can often recover and repackage the product from the packages that must be opened for testing purposes, and the official can immediately inform the manufacturer of the test results.

The effectiveness of package testing programs conducted by individual State and local agencies would be maximized if these agencies established reciprocity with other State, county. and city jurisdictions to recognize results of tests carried out by other agencies at packaging plants.

Just as checking packages at the point of production has the greatest impact upon packaging processes in terms of the number of packages upon which decisions can be made, checking at wholesale has a greater impact than checking at retail. Therefore, warehouse-outlet package testing is a good alternative, wherever possible, to testing at the production point in terms of efficiency. There is a severe drawback to checking at wholesale, however. This is the problem of getting to the stacks of pallets. breaking down film-wrapped or wired skids, and finally opening sealed cartons. Labor costs, equipment, and time requirements. including the time needed to restack skids and pallets, can be excessive. Because of the importance of wholesale testing to the follow-up of inaccuracies discovered during retail checking, guidelines are given in Appendix C.6. to simplify selection of the package sample at wholesale outlets.

Package testing at retail checks the soundness of the manufacturing, distribution, and retailing processes of the widest variety of goods available at single locations. Package testing at retail locations checks the accuracy of the package label at the locations where consumers purchase the product.

The greatest number of processes impinges on the quality or quantity of the product at the point of sale, such that the greatest number of causes is possible for any inspection lot being out of compliance. A shortage in weight or measure may be the result of mistreatment of the product in the store, of a failure to rotate stock, of mishandling by a middle agent, or of failure of some part of the packaging process. Therefore, locating fault in order to correct defects will be more difficult when retail testing is employed.

Allowances for loss of moisture may have to be applied to packages and commodities when tested at wholesale and retail locations.

Retail package testing does not permit checking very many lots of an individual product or a substantial amount of any single production lot. Thus it is more difficult to detect generally good or bad packaging processes, and the impact of a single inspection on a packager and his/her process is small. Therefore, at the very least, followup inspection of a particular brand or code number at a number of retail and wholesale outlets is extremely important in any retail checking scheme.

Package testing at production point cannot entirely replace that at wholesale or retail outlets. Since only manufacturing practices can be examined at production point, testing of packages at wholesale and retail outlets must also be part of a complete package inspection program. The results of distribution practices, possible tampering with the product, and environmental effects can only be monitored by wholesale and retail checking. Thus inspection resources should be divided, if possible, between testing at the packaging location and testing at wholesale and retail locations.

When the product is packaged at the retail store (the supermarket meat counter being the classic example), package inspection at retail is equivalent to inspection at production point. Many of the disadvantages of retail inspection that are noted above are, of course, avoided in this instance. Allowances for moisture loss are not applied; and any shortage may be immediately corrected.

1.3.2. What to Test

The decision as to what products to test can be made in a number of ways. For a State or local government agency, it can be a decision that is based on surveys and audit testing (see Section 1.5.) to cover as much product ground as possible at food stores; farm stuffs, drugs, hardware, or specialty outlets; and discount and department stores. Follow-up of possible problems detected in audit testing or based on a review of past performance will tend to concentrate inspection resources on particular commodity types, brand names, retail or wholesale locations, or even particular neighborhoods.

The expected benefits for the public must, of course, be balanced against the cost of testing. Expensive products should be tested because of their cost per unit; however, inexpensive items also should be tested because of the sales volume of individually inexpensive goods, the overall cost of which is considerable over an extended period to an individual purchaser. Items on special sale and special products produced for local consumption should not be overlooked.

Certain officials may have a roster of packaging plants (or an individual plant) to inspect for a broad range of items, one of which will include net quantity. In such cases, the official's decision as to what to test is made for him or her.

The testing of food, cosmetic, or drug products will require the inspector to observe all health standards and regulations in the handling of the product. For the safety of the inspector and public, pesticides, herbicides, and other poisonous or hazardous materials should be handled (and, if necessary, disposed of) with extreme caution. observing all health standards and label warnings.

1.4. SAMPLING INSPECTION

This handbook describes package compliance testing methods to be used in conjunction with sampling techniques.

It is possible to test packages for compliance with package requirements without using sampling techniques. In such case, the quantity of contents of all the packages available for test must be measured, averaged, and then compared with the labeled quantity and the variation from the labeled quantity of each individual package compared with the maximum allowable variation for that package type and size. If allowable differences are established, the quantity inside every package is compared against the labeled quantity plus or minus the allowable difference the regulation cites. This is a costly and time-consuming technique for regulatory agencies and, in certain instances, will require opening all of the packages inspected.

On the other hand, the techniques of sampling and of following a sampling plan provide many benefits. The first benefit is that of conservation of the inspector's time needed to test a single lot, thus minimizing the cost of such testing. Naturally, testing entails a certain amount of package destruction. Following a sampling plan, therefore, preserves the integrity of as many packages as possible.

A second benefit is the greater impact an inspector can have on the package production, distribution, and marketing sectors. In order to protect package purchasers who cannot check the quantity of contents themselves and to encourage good manufacturing and distribution processes among packagers and package sellers, the most effective and efficient method of marketplace surveillance is that of sampling according to prescribed sampling plans.

Compliance testing using a sampling plan is a step-by-step method of obtaining evidence, comparing the evidence with package requirements, and making a decision about the disposition of the packages.

Sampling plans are discussed further in Sections 1.7. and 1.8. and in detail in Chapter 2. Sampling plans consist of five steps:

- ^o The inspection lot, upon which action will be taken, is defined and the number of packages comprising the lot is counted. (This is discussed in Section 2.3.).
- A random sample is chosen. (Instructions for taking a random sample are given in Appendix C.)
- ^o Measurements are made on each package in the sample (described in Chapters 3, 4, and 5.)

- Calculations are made using the individual measurements (described in Sections 2.6. and 2.7. and as part of the package checking routine in Chapters 3, 4, and 5.)
- A decision on the disposition of the lot, shipment, or delivery is made based upon the criteria established in the sampling plan (described in Sections 2.6. and 2.7. and as part of the package checking routine in Chapters 3, 4, and 5.).

1.5. AUDIT TESTING

In order to speed the process of detecting possible package net contents violations out of the broad array of packaged commodities available for testing at retail locations, officials often use some kind of audit testing procedure. These audit procedures may entail, for example, very small sample sizes or predetermined and catalogued tare weights.

These audit procedures are not definitive, but they are faster and enable an inspector to cover more products in a single location than he or she would otherwise be able to cover using the more rigorous techniques. This handbook does not dwell on audit methods but does provide audit methods for packaged goods labeled by count (Section 5.1.2.) and for paint, varnish, or lacquers (Sections 4.9.2. and 4.9.3.). It should be noted that Category B plans (Section 2.7.), because of the small sample sizes, can also easily be used in audit testing.

Although not intended strictly for audit testing, when packages are checked at retail, inspection lots may be defined as identically labeled packages that are mixed with respect to code or symbol (this will help indicate a manufacturer's process quality). If testing reveals poor quality, then segregation by lot code before further testing will simplify followup inspection.

If the official finds a possible violation, he or she should then use the more rigorous methods given in this handbook to confirm the condition of the lot, that is, to determine whether or not the packaged product complies with net contents labeling requirements.

1.6. 100% TESTING

Upon occasion, checking every package in a lot may be required.

No matter what the size of the lot, when every package in a lot is tested, no (zero) packages may fall below the limits set by the maximum allowable variation, and, at the same time, the average quantity of contents of the lot must equal or exceed the labeled quantity.

If a packager is using checkweighers, not only should the average of the lot equal (or exceed) the label, but under no circumstances should packages be accepted by the checkweigher that are short measure by more than the maximum allowable variation.

1.7. SAMPLING PLANS FOR THE AVERAGE REQUIREMENT

There are several categories of sampling plans provided in this handbook. There are two categories of sampling plans, Category A and Category B, provided for testing packages subject to the average requirement.

Sampling plans of Category A are made available for use when the severity of the consequences for the packager or retailer of a lot not passing the test is relatively great.

Sampling plans of Category B are provided for use when the consequences of a lot not passing the test are relatively minor for the packager or retailer.

The regulatory agency has the authority to decide the appropriate sampling plan categories according to the agency's operating procedures.

A regulatory agency may require, for example, that its officials must always use only the sampling plans of Category A or only those of Category B. An agency can also require, for another example, that Category B be used as an audit method, which, when it reveals package shortages, must be followed by a Category A sampling plan before any action is taken.

As mentioned in Section 1.2., there are actually two requirements which packages must meet when they are subject to the "average requirement." The first, which applies to the whole inspection lot, is that the average net contents equal or exceed the labeled contents. The descriptions of the sampling plan categories have specific computations as part of each category which provide evidence that this requirement has been met. The second requirement is that individual package variations may not be "unreasonable". The limits of reasonable individual package variations are called maximum allowable variations (MAV) in this handbook. When using sampling techniques for compliance testing of package goods, a very few packages in any given sample will be allowed to exceed the limits defined by the MAV.

1.8. WHY THERE ARE TWO CATEGORIES OF SAMPLING PLANS

Judgments based on less than complete information (samples) cannot be made with complete accuracy. There are risks of making wrong decisions; they are the risk of accepting lots that do not conform to the regulation and the risk of failing lots that do conform. Sampling plans can be designed to have predetermined risks of making the wrong decisions.

It has been traditional in package checking in the U.S. to use sampling plans like Category B. Such plans have a 50-50 risk of acceptance-failure for lots that do average at the labeled weight* (and when individual packages fit well within their allowed limits). This kind of plan in some way splits the risk between packer and consumer. For some possible consequences (called "of relatively great severity"), however, the 50% risk may be excessive for the packer who is indeed producing lots complying with regulation.

Therefore, other sampling plans (those of Category A) are given, which provide a much smaller risk for the packer when the lot average does equal the labeled weight. If small sample sizes were used, this kind of plan would not provide sufficient protection to the consumer. Therefore, Category A plans are given with larger sample sizes that will give better discrimination between conforming lots and underweight lots.

A Category B failure is not as strong an indication of an underweight lot as is a Category A failure; however, a Category B plan gives more consumer protection than a Category A plan of the same sample size.

1.9. ALLOWANCES FOR VARIATIONS DUE TO MOISTURE LOSS OR GAIN

Certain packaged products lose or gain moisture (and, therefore, lose or gain weight) after packaging. Depending upon the nature of the product, its environmental history, and the packaging material and method, moisture loss may occur even when good distribution practices are followed. When the Federal or State laws or regulations governing packaged products allow variations in individual packages for loss or gain of moisture, these allowances will have to be applied to individual packages and, thus, to the average net contents before a decision as to lot conformance can be made.

It is not possible for this handbook, on the basis of technical and regulatory information presently available, to provide definitive moisture allowances for determining compliance with those regulations that allow for quantity variations due to moisture loss or gain. In such cases, the inspection authority responsible for ascertaining package compliance is referred to the agencies responsible for such regulations (Table 1-1.).

Agency	Product type
U.S. Department of Agriculture, Food Safety and Quality Service	meat and poultry
U.S. Department of Health and Human Services, Food and Drug Administration	food, drugs, cosmetics, or medical devices
U.S. Federal Trade Commission	household or consumer commodities which are not food, drugs, medical devices, or cosmetics
U.S. Environmental Protection Agency	pesticides, rodenticides, insecticides
U.S. Department of the Treasury, Bureau of Alcohol, Tobacco, and Firearms	alcohol and tobacco products
State Weights and Measures Offices	all packaged products

Table 1-1. Agencies responsible for package regulations.

*Of course, the producer's risk is reduced when the lot averages greater than the labeled weight.

1.10. DECISIONS PRELIMINARY TO PACKAGE INSPECTION

Prior to conducting package inspections, the package testing official must, at the very least, be given preliminary guidance by his or her supervisor or the program administrator concerning:

- which sampling plan category
- what moisture allowance

is to be used under what circumstance in the jurisdiction.

CHAPTER 2. GENERAL CONSIDERATIONS

- 2.1. THE PACKAGE CHECKING ROUTINE
- 2.2. THE REPORT FORM AND WORKSHEET
- 2.3. DEFINITION OF THE LOT
- 2.4. PACKAGE ERRORS
- 2.5. SELECTING THE SAMPLING PLAN
- 2.6. SAMPLING PLANS IN CATEGORY A
- 2.7. SAMPLING PLANS IN CATEGORY B
- 2.8. INDIVIDUAL PACKAGES
- 2.9. RECORDING PACKAGE ERRORS
- 2.10. THE CRITERIA FOR WEIGHING PACKAGES NOT LABELED BY WEIGHT 2.11. TARE
- 2.12. MAXIMUM ALLOWABLE VARIATIONS
- 2.13. EXCEPTIONS TO THE MAXIMUM ALLOWABLE VARIATION
- 2.14. MOISTURE ALLOWANCE

This chapter introduces several subjects that may require special study by the inspector prior to actual package testing. A thorough study of Appendix C is also recommended before using the methods detailed in Chapters 3, 4, and 5.

2.1. THE PACKAGE CHECKING ROUTINE

The following topics in capital letters are explained in this chapter and in Appendix C, but not in the order in which the official will handle them during field testing. Step-by-step instructions for field testing are given in Chapters 3, 4, and 5.

In package testing, the official will be expected to:

- decide location of test and packaged product to be tested (or this information will be provided to the inspector),
- identify the INSPECTION LOT to be tested,
- ^o begin to fill out a REPORT FORM, including information from the product label and the MAXIMUM ALLOWABLE VARIATION (MAV),
- count the number of packages in the lot and record the LOT SIZE,
- refer to a SAMPLING PLAN, record SAMPLE SIZE, TARE SAMPLE SIZE, and ALLOWABLE NUMBER OF UNREASONABLE ERRORS,
- select a RANDOM SAMPLE and from it, the RANDOM TARE SAMPLE (using WORK-SHEET),
- if label is not in terms of net weight, determine if WEIGHING METHOD may be employed (using the WORKSHEET),
- determine UNIT OF MEASURE and the MAV in DIMENSIONLESS UNITS,
- determine AVERAGE TARE (CORRECTED TARE if foam product aerosols are being checked) and PACKAGE ERRORS (CORRECTED PACKAGE ERRORS if MOISTURE ALLOWANCE is applied), (recording on WORKSHEET, and REPORT FORM),

apply DECISION CRITERIA and determine whether lot does or does not conform to net quantity requirements.

Tables and other material in this chapter are referenced in Chapters 3, 4, and 5 when circumstances require their use.

2.2. THE REPORT FORM AND WORKSHEET

It will be necessary to document the results of package testing on some type of report form. An example of a form is shown on the next page. The report form heading is that portion of the form which is encircled with a dashed line. The official will be referred in the following sections to other locations on the report form indicated by circled numbers.

Two worksheets (Block A and Block B) are also provided on the following pages which will be explained as the items listed are discussed in the text.

The worksheets have several purposes:

- notation of random numbers for selection of sample and tare sample (Appendix C),
- o recording individual tare weights
 (Section 2.11.3. and 2.11.4.),
- recording random package labeled weights (Section 3.6.),
- computations associated with packages labeled in units other than weight (Chapters 4 and 5),
- application of moisture allowance (Section 2.14.), and other corrections to the package weights.

For those reading the handbook for the first time, we suggest a copy of the report form and worksheets be kept at the reader's side at all times so that he or she may refer to them while reading the text. The various boxes on the report form are listed in Table 2-1 together with the sections of the text in which they are explained.

Reference will be made to the boxes on the report form and worksheet in the detailed procedures of Chapters 3, 4, and 5.

1	DEP/ PACKA	ARTMENT HEAD GE CHECKING R	ING EPORT		
REPORT NO			DATE		_
Check Where Sample Obtaine	d				
Packer		Address			יך
Distributor		Address		······· ··· ··· ··· ··· ··· ··· ··· ··	-
Dealer		Address			-
Brand Name	Commod	ty		Labeled Contents	-
Other Identification Includi	ng Code Symbols		Container Descriptio		-
]
1 Lot Size (N)	5 MAV (units of weight)	8 Average Tare (dimensionless units)	1 Weight of Labeled Contents	s
2) Sample Size (n)					
<u> </u>	6 MAV (units of label)	9 Test Allowand	e for Foam Aerosols		
3 Tare Sample Size (n _t)	<u> </u>	(dimensionles		12 Weight of Labeled Content	s
	(7) MAV (dimensionless units)	10 Corrected Tar	10 Corrected Tare		
(4) Unit of Measure	$=\frac{4}{4}$ or $\frac{4}{4}$ =	(dimensionies)	s units)		
		V /1 V /1 V	71 1/1 1/2		Tota
					4
					$\frac{1}{2}$
					4
					Ĺ
					2
					4
					┢
Allowable Number of Unreasonable Errors	(14) Actual Number of Unreasonable Errors	(dir	rage Error nensionless units)	(16) Average Error (same units as label)	
When (15) Is Minus and Car	egory A Sampling Plan is Bein	g Used:			
) Average R ≈ R =	20 (n/N) x 100 =			0/+	
B) Table 2-3, Column 2, =	(21) f (Table 2-4) =	(23) = (22) + (15) =		
	$19 d = (17) \times (18) = (22) T = (19) \times (21) = 10t 0t 10t fails passes 10t 10t $				

Remarks, Instructions, Other Calculations:

Acknowledged Receipt of Report

Inspector

Title

WORKSHEET

Block (A) Cross out column headings which do not apply and fill appropriate headings in blank spaces

	Pkg. No.	MAV (Random Pack)	Labeled	Gross	Tare	Corrected Tare [‡]	Net or Drained	Packag —	e Errors 0/+		
1										1	
2				1							
3				1							
4						1					
5							1				
	0		R _t =		(2) $R_c =$.	/////	////	////	3	$R_c/R_t =$
6										4	(Table 2-7) n _t =
7							1				
8							_				
9											
10				-			1	1		1	
11										1	
12											
13										1	
14											
15											
16										ĺ	
17											
18											
19										1	
20											
21											
22											
23											
24											
25											
26											
27		_									
28										İ .	
29											
30										J	
				SAverage Tare or	-						

Nominal gross wt = labeled wt + average tare corrected nominal gross wt = labeled wt + corrected tare † =_____

* Fill in Applicable Space:	
Foam Aerosol Test Allowance 💷	
Receiving Pan Weight	
(for drained weight)	
MAV for Random Pack	
Flask Weight	
Moisture Allowance	

‡Corrected Tare = Average Tare - Foam Allowance

= Average Tare - Moisture Allowance

or

or

= Average Tare — Average Difference in Gross Weights (vacuum packed coffee)

WORKSHEET (Continued)

Block (B))								
	1	2	3 Weight	4 Weight of	5 Liquid	6	7	8	
	Weight	Quantity	Quantity	Labeled Quantity	Temperature				
1									
2									
3									
4									
5									
6									
/									
9									
10									
10						· · ·	L,,		
3	$\frac{MAV}{6}$ (in units of weight) = column 3 x $\frac{MAV}{6}$ = go on if this value is equal to or larger than 1/2 scale division, if not, measure package quantities directly, opening every package in sample.								
4a	If column 2	quantity is th weigl	e same for pa ht $(1) - we$	ckages (1) and (2)	2) (e.g. fluid v	olume):			
	Table 4-2 value = If Table 4-2 value is equal to or larger than (weight 1) — weight 2)), go on to 53. If not, measure package quantities directly opening every package in sample.								
4 b	If column 2 quantity is not the same for packages (1) and (2) (e.g. length, area, count):								
	for package (1): $\frac{\text{weight (column 1)}}{\text{quantity (column 2)}} = (\text{column 3 line (1)}) = $								
	(column 3 line (1)) x labeled quantity = (column 4 line (1)) =								
	for package (2) : $\frac{\text{volume (column 1)}}{\text{quantity (column 2)}} = (\text{column 3 line (2)}) = $								
	(column 3 line (2)) x labeled quantity = (column 4 line (2)) = $\begin{bmatrix} 1 \\ 1 \end{bmatrix}$								
	(column 4 line (1)) - (column 4 line (2)) =								
	Table 4.2 value = L If Table 4.2 value is equal to or larger than (column 4, line 1 – column 4, line 2) go on to $5b$. If not, measure package quantities directly, opening every package in sample.								
53	If column 2 quantity is the same for packages (1) and (2) :								
	average weight of labeled quantity = column 2 quantity x labeled quantity = column 2 quantity								
50	If column 2	quantity is no	ot the same fo	or packages 🕕 an	d (2) :				
	average weig	ght of labeled	quantity =	column 4; line (1) + line (2) 2	=			
6	Nominal gro	oss weight =	5a) or 56) + average tare =					
7	MAV (in units of weight) = $\frac{MAV \times 6}{Iabeled quantity}$ =								

Box	Subject	Section
1 2 3 4 5 6 7 8 9 9 10 11	Lot Size (N) Sample Size (n) Tare Sample Size (n _t) Unit of Measure MAV (in units of weight) MAV (in same units as labeled contents) MAV (in dimensionless units) Average Tare (dimensionless units) Test Allowance (foams) (dimensionless units) Corrected Tare (dimensionless units) Weight of Labeled Contents	2.3.3. 2.5., 2.6., 2.7. 2.6., 2.7. 2.9.1. 2.12. 2.9.1. 2.11.3., 2.11.4. 3.9.6. 3.9.5., 3.9.6.
12	Weight of Labeled Contents (dimensionless units)	4.4. (volume 5.1.3. (count) 5.3.2. (linear or
13 14 15 16 17 18 19 20 21 22 23	Allowable Number of Unreasonable Errors Actual Number of Unreasonable Errors in Sample Average Error (in dimensionless units) Average Error (in same units as label) Average Range (\bar{R}) Value from Table 2-3, column 2 d (= box 17 x box 18) = column 2, Table 2-3 x \bar{R} (n/N) x 100 f value from Table 2-4 based on box 20 value T (= box 19 x box 21) = Table 2-4 value x column 2, Table 2-3 x \bar{R} T + Average Error (= box 22 + box 15)	2.6.1., 2.7.1. 2.6.1., 2.7.1. 2.6.2. 2.6.2. 2.6.2. 2.6.2. 2.6.2. 2.6.2. 2.6.2. 2.6.2. 2.6.2. 2.6.2. 2.6.2. 2.6.2. 2.6.2. 2.6.2. 2.6.2. 2.6.2.

2.3. DEFINITION OF LOT

The first step in package testing requires the official to define the lot, which is the collection of packages upon which action will be taken as a result of the official's tests. This lot is called the "inspection lot." The best way to define the inspection lot in each case depends on the particular factors that are likely to lead to variations in quantity of the product. The following guidelines form the bases for defining the inspection lot.

(i) The inspection lot should consist only of packages of the same product, with the same label from the same packer.

For example, a lot shall consist of cans of peach halves, 500 grams net weight, Brand X.

This rule should never be violated.

(ii) To the greatest extent possible, the inspection lot should consist only of packages packed at the same place, at the same time, under the same conditions. This guideline is in addition to the provisions of guideline (i). Therefore, a lot should consist of packages of the same product, same label, and also, with the same packager's lot code number if inspection is done at the warehouse, or of packages from the same filling line packed during the same period if inspection is done on-line at the packing plant.

It will not always be possible to take both of these factors into account in forming lots.

Taking both the above factors into account may result, in fact, in making the inspection lot very small, which is undesirable. As large an inspection lot as possible should be formed without violating guideline (i) and taking into account the factors mentioned in guideline (ii).

If the official cannot get to certain packages because of some physical or other constraint, then such packages are not part of the inspection lot to be acted upon. In general, such restricted sampling should be avoided whenever possible.

2.3.1. The Inspection Lot of Standard Pack Packages

Standard pack packages are those packages which are put up with identical labels and only in certain selected quantity sizes. An example of a standard pack meat item would be canned hams labeled "5 pounds."

- ^o When the location of test is a retail store, the inspection lot must consist of packages with identical labels. It is not necessary, but may at times be desirable, to segregate packages according to the same manufacturer's lot symbol or code.
- ^o When the location of test is a warehouse, the inspection lot must consist of packages with identical labels and with the same manufacturer's lot symbol or code.
- ^o When the location of test is on-line at a packing plant, the inspection lot must consist of packages with identical labels and manufacturer's code, and should not exceed one uninterrupted production run. As small as one hour's production may be convenient for sampling purposes.

Note that the inspection lot is not, in general, the same as the "production lot."

2.3.2. The Inspection Lot of Random Pack Packages

Random pack packages are those packages that are put up with identical labels except for the labeled quantity. These packages are usually individually weighed and subsequently marked¹.

An example of a random pack meat item, say, would be whole chickens labeled by their various weights.

^o When the location of inspection is a retail store, an inspection lot must consist of all the packages packaged at that location available for inspection at one time. Since the same production factors apply to all such packages, the entire meat counter, for example, may be considered the lot, except for those packages on the counter put up elsewhere than at the store.

- ^o Upon occasion, the official may wish to define a lot of only one kind of packaged goods (e.g., ground beef) for special reasons, such as the large number of packages of one kind of goods, prior history of product or store, the unit price of the product, or because the results of audit testing indicate the possibility of shortage in a particular item.
- ^o When the location of inspection is either a warehouse or on-line at the packaging plant, the definition of the inspection lot is the same as that for standard pack packages except that "identical labels" is construed to mean identical except for the numerical quantity of contents.

2.3.3. Size of the Inspection Lot

The number of packages in the lot to be tested (defined according to the guidelines given in the previous sections) should be counted. This is the size of the inspection lot, and is entered on the report form in box 1.

2.4. PACKAGE ERRORS

In general, the actual package quantities which the official measures will not equal the labeled quantity. Since it is the deviation from the labeled quantity that is of interest to the official, rather than the actual package quantity, reference will be made to positive or negative deviations from the label (called plus or minus errors or, in general, package error). See Sections 2.6.1. and 2.9.

2.5. SELECTING THE SAMPLING PLAN

Guidance is provided in Sections 1.7. and 1.8. on selecting the appropriate category of sampling plan for packages which must conform with the average requirement.

¹The National Conference on Weights and Measures Model State Packaging and Labeling Regulation (NBS Handbook 130), defines a "random package" as a "package that is one of a lot, shipment, or delivery of packages of the same consumer commodity with varying weights; that is, packages of the same consumer commodity with no fixed pattern of weight." The procedures in this handbook for random packages apply to consumer and non-consumer packages with quantity declarations of weight or of other measure.

Sampling plans for packages given tolerances or allowable differences are presented in Section 5.7.

Special sampling plans must be used for packages labeled by count and containing less than 51 units per package. These plans are given in Section 5.2.

Each set of sampling plans (Table 2-2, 2-5, 5-1, or 5-2) is specified according to lot size. For any given lot size, the tables list that sampling plan with the minimum sample size to be used. The official may use a larger sample size at any time as long as he or she follows the entire sampling plan (all of any horizontal line including the decision criteria corresponding to that sampling plan and that line).

2.6. SAMPLING PLANS IN CATEGORY A

Table 2-2 lists seven sampling plans according to the lot size, indicated in column 1. Each plan indicates in column 2 the number of packages to be chosen at random from the lot; this is the sample size². Appendix C describes several methods of obtaining a random sample. Column 3 indicates the number of packages to be chosen randomly from the sample upon which the determination of tare will be based; this is the tare sample size. Appendix C describes methods for tare sample selection. As mentioned in Section 2.5., Table 2-2 lists the minimum sample size to be used for any given lot size. As long as the official follows the entire sampling plan (all of any given horizontal line including the decision criteria corresponding to that sampling plan and that line) he or she may use a larger sample size at any time. For example, the official may choose to take a sample size of 50 for a lot of 750 packages, rather than a sample of 30. However, he or she must also take 5 packages to determine the tare and cannot declare the lot out of conformance unless 3 or more packages in the sample are short measure by more than the MAV from the labeled quantity (or unless the sample fails the average requirement).

After recording the lot size in box 1 of the report form, the official should select a sampling plan and record the sample size in box 2. The corresponding tare sample size is recorded in box 3 and the allowable number of unreasonable errors (the number from column 4) is recorded in box 13.

After the quantity of contents in each sample package is measured using a method of test presented in Chapter 3, 4 or 5 of this handbook, the decision criteria of the plan are applied. The decision criteria indicate the conformance or nonconformance of the lot with the package requirements.

1 Lot size (number of packages in lot)	2 Sample size (number of packages in sample)	3 Tare sample size ^a (number of packages chosen for tare determination)	4 Allowable number of package errors exceeding the MAV ^b
N	n	n _t	
30 or less	all	2	0
31-800	30	2	1 1
801-2,000	50	5	2
2,001-5,000	80	5	3
5,001-15,000	125	5	5
15,001-50,000	200	10	7
50,001 and greater	315	10	10

Table 2-	2. Samp	lina p	lans c	of (Category	Α.
----------	---------	--------	--------	------	----------	----

^aSpecial rules for tare sampling apply when Section 2.11.4. is followed (glass or aerosol packages).

^bMaximum allowable variation for individual packages (Tables 2-8 through 2-11, Section 2.12.)

 2 Sample sizes of 50 and over are the same as those in Military Standard 105-D, but the sampling plans are <u>not</u> the same as Military Standard 105-D because the decision criteria are different. (In addition to the decision criterion for individual packages (Section 2.6.1.), the lot must also pass the decision criterion for the average (Section 2.6.2.).)

2.6.1. Decision Criterion: Individual Packages

Firstly, conformance with the package requirement that permits individual packages to vary from the labeled quantity by a "reasonable" amount is checked. The package error (see Section 2.4.) for each individual package in the sample is compared against the maximum allowable variation (MAV) for that package type and size (See Section 2.12.). The minus errors that exceed the MAV are called "unreasonable errors." If there are more unreasonable errors than are indicated in column 4 of Table 2-2 (corresponding to the sample size), the lot fails to conform with the package requirements. No further testing of the lot is necessary. The allowable number of unreasonable errors from column 4 of Table 2-2 has been recorded in box 13 and the individual package errors in the checkerboard area of the report form (see Section 2.9.). Each package error that exceeds the MAV is circled on the report form and the number of circled package errors (the number of unreasonable errors) is recorded in box 14 of the report form.

If there are an equal number or fewer unreasonable errors in the sample than the number in column 4 corresponding to the selected sampling plan, (that is, the lot complies with this first requirement) the average error must be computed according to Section 2.6.2. before a final decision can be made as to the compliance of the lot with net quantity regulations.

2.6.2. Decision Criterion: The Average Error

The average error for the sample is equal to the sum of the individual package errors divided by the number of packages in the sample. (The use of the report form to compute the average error is described in Section 2.9.3.). The average error is recorded in boxes 15 and 16 on the report form (dimensionless units are explained in Section 2.9.1.). If the total error (and consequently the average error) is zero or a positive number, a final decision on the lot can be made at this point; that is, the lot conforms with the package net quantity requirements.

When the lot size is 30 or fewer, all packages are tested and the lot is found nonconforming if the total error has a minus value.

For lots of more than 30 packages, if the average error for the sample is a minus value, the "error limit" must be computed before a final decision on the compliance of the lot can be made. The error limit, which we will call "T", is calculated:

- (i) First compute a value which will be called "d".
 - $d = \bar{R} \times (0.8598/\sqrt{n})$

where \overline{R} is the average range of package errors for groups of 5 packages taken in the order of weighing, and n is the number of packages comprising the sample. (Appendix F contains a detailed example of how to calculate \overline{R} .) For the convenience of the official, Table 2-3, column 2 gives values of $0.8598/\sqrt{n}$ for each sample size to use in the calculation of d once \overline{R} is determined³.

 \overline{R} is recorded in box 17 and the value from column 2 of Table 2-3 is recorded in box 18 on the report form.

For example, if the sample size is 30, and R = 2(in dimensionless units),

 $d = (0.1570) \times (2) = 0.3140.$

d (= Table 2-3, column 2 value x \overline{R}) is recorded in box 19 on the report form and, as indicated on the form, is the value in box 17 times the value in box 18.

(ii) Calculate the percentage of the lot which the sample represents. This value is recorded in box 20 on the report form.

For example, say the lot to be acted upon consists of 50 packages and a

³Alternatively, a calculator which gives the standard deviation directly may be used to determine d. In this case, $d = 2s/\sqrt{n}$, where s is the standard deviation and n is the number of packages comprising the sample. For convenience, Table 2-3, column 3 gives values of $2/\sqrt{n}$ for each sample size (column 1) to use in this calculation. Slightly different values for d will be obtained using the standard deviation rather than the average range. Since commonly available calculators may not have enough storage capacity to calculate s for large n, the average range method is preferred. If s is used in the calculation, the report form must be modified to indicate the Table 2-3, column 3 value in box 18.

1	2	3				
n	<u>0.8598</u> √n	$\frac{2}{\sqrt{n}}$				
30 50 80 125 200 315	0.1570 0.1216 0.09613 0.07691 0.06080 0.04844	0.3652 0.2828 0.2236 0.1789 0.1414 0.1127	t I			

Table 2-3. Values of 0.8598 and $\frac{2}{\sqrt{5}}$ for sample size n.

Table 2-4. Values of f for percent of lot sampled^a.

Percent of lot sampled	f	Percent of lot sampled	f	Percent of lot sampled	f	
1 2 3 4 5	.99 .99 .98 .98 .98 .97	36 37 38 39 40	. 80 . 79 . 79 . 78 . 77	71 72 73 74 75	.54 .53 .52 .51 .50	
6	. 97	41	.77	76	. 49	
7	. 96	42	.76	77	. 48	
8	. 96	43	.75	78	. 47	
9	. 95	44	.75	79	. 46	
10	. 95	45	.75	80	. 45	
11	. 94	46	.73	81	.44	
12	. 94	47	.73	82	.42	
13	. 93	48	.72	83	.41	
14	. 93	49	.71	84	.40	
15	. 92	50	.71	85	.39	
16	.92	51	. 70	86	. 37	
17	.91	52	. 69	87	. 36	
18	.91	53	. 69	88	. 35	
19	.90	54	. 68	89	. 33	
20	.89	55	. 67	90	. 32	
21	. 89	56	. 66	91	. 30	
22	. 88	57	. 66	92	. 28	
23	. 88	58	. 65	93	. 26	
24	. 87	59	. 64	94	. 24	
25	. 87	60	. 63	95	. 22	
26	.86	61	.62	96	.20	
27	.85	62	.62	97	.17	
28	.85	63	.61	98	.14	
29	.84	64	.60	99	.10	
30	.84	65	.59	100	0	
31 32 33 34 35	.83 .82 .82 .81 .81	66 67 68 69 70	. 58 . 57 . 57 . 56 . 55			

^aPercent of lot sampled = $\frac{\text{sample size}}{\text{lot size}} \times 100.$

sample of 30 packages is to be selected from the lot. The percentage of the lot which the sample represents is equal to $30/50 \times 100 = 60\%$.

(iii) Other values, which will be called "f", are listed in Table 2-4 according to the percentage of the lot which the sample represents (calculated in the previous step), that is, according to the value recorded in box 20. Find the value of f in Table 2-4 corresponding to the percentage figure calculated above. The value of f from Table 2-4 is recorded in box 21 on the report form.

For the above example, the f value is 0.63.

(iv) Calculate the error limit = d x f (which will be called "T"). T is recorded in box 22 on the report form, on which it is indicated that T is the value in box 19 times the value in box 21.

Following the above examples, if d = 0.3140 and f = 0.63; $T = d \times f = 0.20$.

(v) Compare T with the average error to determine lot conformance. When the average error (disregarding its minus sign) is larger than T, the lot does not conform with the package requirements. On the report form, T plus the average error is computed and that value is entered in box 23. Box 23 is indicated to be the sum of the values in box 15 and box 22. If the value in box 23 is zero or positive, the lot conforms with the package requirements; if it is negative, the lot fails.

Following the above examples, if the average error is found to be -0.210, and T = 0.20, the lot in question would fail to comply with the package requirements, that is, T + average error = (0.20) + (-0.210) = (-0.01).

It is important to realize that the calculations in steps (i) through (v) above do not have to be made when the average error is plus, but only when it is minus.

2.7. SAMPLING PLANS IN CATEGORY B

According to the size of the lot, shown in column 1, Table 2-5 indicates in column 2 the number of packages to be chosen at random from the lot (the sample size) and column 3 shows the number of packages that must be opened to determine the average tare (tare sample size). The lot size is recorded in box 1 of the report form, the sample size in box 2, and the tare sample size in box 3.

After the quantity of contents in the sample packages is measured and recorded, it

1 Lot size	2 Sample size	3 Tare sample size ^a	4 Allowable
(number of packages in lot)	(number of packages in sample)	(number of packages chosen for tare determination)	number of package errors exceeding the MAV ^b
N	n	nt	
Up to and including 250	10	2	0
251 and greater	30	2	0

Table 2-5. Sampling plans of Category B.

^aSpecial rules for tare sampling apply when Section 2.11.4. is used (glass or aerosol packages).

^bMaximum allowable variation for individual packages (Tables 2-8 through 2-11, Section 2.12.).

is then necessary to compare these measurements with the package requirements.

> 2.7.1. Decision Criterion: Individual Packages

Those individual package errors that are minus and that exceed the magnitude of the Maximum Allowable Variation (MAV) (Section 2.12.) are called "unreasonable errors." When Category B sampling plans are being used, a zero is entered in box 13 of the report form.

The actual number of unreasonable errors found in the sample is recorded in box 14 on the report form.

If there are any unreasonable errors in the sample (see column 4 of Table 2-5), the lot fails to conform with the package requirement.

If there are no unreasonable errors in the sample, the total error and the average error is calculated before a final decision on the condition of the lot can be made.

2.7.2. Decision Criterion: The Average Error

The average error of the sample is calculated from the values obtained from individual package measurements. The average error is equal to the sum of the individual package errors in the sample divided by the number of packages in the sample. If the total error (and consequently the average error) is zero or a positive number, the lot conforms with the package requirements. If the total error (and consequently the average error) is minus; the lot fails to conform with the package requirements.

The average error is recorded in boxes 15 and 16 on the report form (dimensionless units are explained in Section 2.9.1.).

2.8. INDIVIDUAL PACKAGES

Even if the lot complies with the package requirements using a sampling plan, individual packages in the sample may be short by more than the maximum allowable variation from the labeled quantity. However, any individual package that is short by more than the MAV from the labeled quantity is considered defective and should be repacked, relabeled, or otherwise handled on an individual basis. Disposition of such packages may be recorded on the report form under "Remarks".

2.9. RECORDING PACKAGE ERRORS

Measurement details are described in Chapters 3, 4, and 5. This section summarizes the recording of measurement results on the report form.

2.9.1. The Unit of Measure and Dimensionless Units

It is customary for the official to record package errors in terms of dimensionless integers. This may be done by choosing some increment of measure (called the "unit of measure") as the value by which all the integers must be multiplied in order to arrive at the actual package error. For example, say that an official measures package errors to the nearest 0.002 lb. The scale used to weigh the packages has 0.002 lb divisions on its face. Instead of recording an individual package error of, say, -0.022 lb, the official may record the unit of measure as 0.002 lb, count the number of divisions on the scale face, and then record this number as the individual package error, in this example, -11.

The report form is designed on the assumption that dimensionless units will be used.

It should be noted that any other values the official compares with the package errors recorded in dimensionless integers must also be converted to this integer notation as well (or else the package measurements must be converted back to the units of measure.) Following the previous example, let us say the maximum allowable variation (MAV) for these packages is 0.020 lb. For purposes of comparison with the recorded package errors, the official may convert the MAV to an integer using the same unit of measure used to record the package errors. With a unit of measure of 0.002 lb, the MAV in dimensionless units is (0.020 lb)/ $(0.002 \ 1b) = 10.$

The unit of measure is recorded on the report form in box 4 (e.g. 0.002 lb). The MAV in dimensionless units is recorded in box 7 (e.g. 10).

2.9.2. Choosing the Unit of Measure

The official should record package measurements in units of measure less than or equal to the MAV/6. For example, the MAV for packages labeled 2.50 lb is 1 3/8 oz (Table 2-8 of Section 2.12.). MAV/6 is 0.229 oz. Since a 1/4 oz unit is larger than 0.229 oz, 1/8 oz units would be the largest unit of measure appropriate for recording measurements on these packages.

Table 3-1 in Chapter 3 presents recommended units of measure to be used in recording package weights when the packages are labeled by weight and Table 4-3 in Chapter 4 presents units of measure for common consumer products labeled by liquid volume.

It should be kept in mind that the MAV's for packages labeled in units other than weight (Tables 2-9, 2-10, or 2-11) apply to such packages, even though weighing may be the means of package contents measurement. For example, packages labeled "48 fl oz" have an MAV of 10.0 fl dr (1.25 fl oz). In this example, say, the inspector finds that 32.00 fl oz of the product under test weighs 2.000 lb. Therefore, the MAV of 10 fl dr is equivalent to:

$$\frac{(1.25 \text{ fl oz})(2.000 \text{ lb})}{(32.00 \text{ fl oz})} = 0.0781 \text{ lb}$$

The MAV/6 is 0.013 lb or about 3/16 oz. In this instance, therefore, 1/8 oz units (or 0.008 lb units) are appropriate for testing the packages. If these same 48 fl oz packages had a weight of 1.000 lb for each 32 fl oz, the MAV of 10 fl dr would be equivalent to only 0.0391 lb and MAV/6 = 0.007 lb. Thus, units of 1/16 oz (or 0.004 lb) would be a better choice in measuring these packages.

Equipment used to measure package quantities should be capable of discriminating measurements to 1/6 of the MAV for an individual package. With one exception, this handbook suggests equipment which meets this criterion.

2.9.3. How to Use the Checkerboard Area of the Report Form

Package errors are entered on the report form in the "checkerboard" area⁴. Five values are entered down the first columm, then the next five in the second column, and so on. This area of the form is designed to aid the official to sum the individual package errors as well as determine the range of package errors (computations are explained in Section 2.6. and

Appendix F.). Each package error is associated with a four square block:

A minus package error is entered in the upper left square of the block:

A plus error is entered in the lower right square of the block:

When sample sizes greater than n = 80 are checked, additional report forms must be used to record the package errors.

of +1.

In order to obtain the sum of package errors, add the individual package errors horizontally across the rows in the checkerboard area, recording the sum of each horizontal row in the "total error" column on the extreme right, and then add up the rightmost column. The average error of the sample is obtained by dividing the sum of the total error column by the number of packages in the sample.

2.10. THE CRITERIA FOR WEIGHING PACKAGES NOT LABELED BY WEIGHT

The preferred method of testing packages labeled in units other than weight is to weigh such packages. If the official can determine the weight of the labeled quantity of product, that weight plus the empty container weight can be used to compare with the weights of unopened packages to determine individual package errors. Otherwise, the official must open and measure the contents of every package in the sample -- a time consuming and costly alternative.

However, two criteria must be met before the official can use a weighing technique:

(i) The equipment must be able to discriminate differences in package content weights corresponding to the MAV/6.

> If the recommended equal-arm scales described in Section 3.1. are used, this criterion can be met if 1/2 the smallest scale division is equal to or smaller than MAV/6. If a digitalreadout scale must be used, the

⁴This portion of the report form is based on that of the Division of Measurement Standards, Department of Food and Agriculture, State of California (Report Form 524-003).
smallest increment in the readout must be equal to or smaller than the MAV/6. (Most common liquid commodities will meet this criterion; see step 7 of Section 4.4.)

 (ii) The weight of a known quantity of product must not vary significantly from package to package. (See Section 4.4. for liquid volume, 5.1.3. for count, 5.3.2. for linear measure).

2.11. TARE

In compliance testing of packaged goods, the enforcement agency is interested in utilizing nondestructive tests as far as possible; that is, testing that requires opening as few packages as possible. For example, the net weight of a package can be determined by weighing the unopened package called the gross weight - and subtracting from that weight the average weight of the packaging materials (and sometimes other materials) - called the average tare weight - as long as the actual tare weights of individual packages do not vary too much (see Section 2.11.4.) In more complicated situations, the official first determines whether the labeled unit of measure, if it is not weight, (say, volume) can be converted to a weight value (using the measured weight of a known volume, in the example of volume). If this is possible, the net contents of a package can be found by subtracting the tare weight from the gross weight (and if necessary, converting the resultant value from units of weight to the units on the package label)⁵.

The packages that are used to determine the tare are called the "tare sample." At least two determinations of individual package tare weights should be used to obtain an average tare value (that is, the tare sample size should be at least 2). As the package sample size gets larger, the average tare value should be obtained from more than two determinations. (See Tables 2-2 and 2-5, column 3 for tare sample sizes corresponding to various sample sizes.)

The average tare is recorded in box 8 of the report form in dimensionless units.

Tare weight can vary considerably from package to package as compared with the variability of the package net contents, even for packages in the same production lot. Although this is not the situation for most packaged products, it is a major problem with glass or aerosol containers. Therefore, an alternative tare determination procedure is provided in Section 2.11.4. This procedure must be used for glass or aerosol containers and is optional for any other container. There are several instances in which this procedure will prove useful to the official. For example, relatively heavy containers (e.g., plastic buckets or cans) can vary considerably in tare weight, especially in a retail store inspection lot which may be composed of packages from more than one production facility and in containers made of different materials or made by different manufacturers. The procedure of Section 2.11.4. will indicate if this tare variability is sizeable in comparison with the net weight variability, and indicate if the official should open more packages to obtain the average tare weight.

Two tare definitions are used commonly for the inspection of packaged goods:

- Dry tare is composed of all packaging materials (including glue, labels, ties, etc.) that will contain or enclose the product but before the product is introduced into the container. Prizes, gifts, coupons, or decorations that are not part of the product are defined as part of the tare also.
 - Wet tare is composed of all packaging materials that can be separated from the packaged product after packaging. Washing, scraping, ambient air drying, and other techniques involving more than "normal" household recovery procedures may be used but laboratory procedures such as oven drying the packaging material are not used. As in the dry tare definition, prizes and decorations and such are also part of the wet tare.

0

⁵In actual practice, a "nominal gross weight" value will be determined. The nominal gross weight is the sum of the average tare weight and the labeled weight. This weight value may then be easily compared on an equal-arm scale with the actual gross weight of each unopened package in order to arrive at the individual package errors. For example, see steps 14 and 15 of Section 3.5.

Wet tare should be used wherever possible. In some cases (e.g., canned or glass- or plastic-packed goods) dry tare weights are equivalent to wet tare (within the measurement precision of field test scales). However, the net contents value which is obtained when a dry tare value is subtracted from the package's gross quantity will not always represent the amount of product which can subsequently be obtained from the package. For example, oils or moisture from the product may be absorbed by the packaging material when in contact with the product, increasing the weight of the packaging material and decreasing the weight of the product after packaging. Therefore, caution in the use of dry tare values is advised. (When it is available, the use of a dry tare value can be valuable in audit testing, however, in order to locate possible violations without opening any packages under test).

Direct measurement of net contents is necessary when the product cannot be checked by weighing. (For example, individual units in packages labeled by "count" sometimes differ enough in weight from each other such that the gross weight of a package minus the tare weight cannot be used to adequately indicate the count of units inside the package.)

The direct measurement of net contents will also be necessary when the net content is defined as the "drained weight" of product inside the package. "Drained weight" is prescribed by regulatory agencies in those instances in which it has been concluded that the only usable or consumable material inside the package is the solid portion, whereas the liquid portion is disposed of and therefore "drained away". Common examples are canned or bottled olives and mushrooms. The liquids in which they are packed are not considered part of the net contents. Drained weight procedures are provided in Sections 3.8., 3.11., and 3.12.

2.11.1. Choosing Packages for Tare

The tare sample should be a random sample. Appendix C contains descriptions of random sample and random tare sample selection. The packages to be opened for tare are determined as part of the random number selection that determines the whole sample.

If dry tare is used, Appendix C procedures should be used to select the tare sample from the lot or lots of tare material.

Tare values are determined by weighing the empty packages.

2.11.2. Cleaning Tare Materials

The cleaning of packaging material for tare weight determination will vary with the tare material and the product it contains. In general, a common-sense approach should be followed in cleaning tare materials. A bread bag, for example, may be turned inside out to remove all crumbs. Care should be taken in cleaning tare material such as metal cans with paper labels so that the labels are not wet with water or other solvent used to clean the container. The interior of the containers should be thoroughly dried with a clean, dry cloth or air dried, whichever is the most practicable. Butter or bacon wrappers, for example, should be scraped and wiped clean but no effort should be made to extract product contents absorbed by the tare. Caulking compound tubes should be cut open and scraped and wiped. Solvent may be used if the package is foil-lined, but every effort should be made to avoid wetting the outside of the tube with solvent. Packages containing oil-based products may require several detergent washes to remove the product from the container.

These are just a few of the approaches to be used in cleaning packaging materials prior to determination of the tare weight.

2.11.3. Tare Neither Glass nor Aerosol

Table 2-2 or Table 2-5 indicates in column 3 how many packages to open or how many dry tare units to select at random in order to determine the average tare. The tare sample size is recorded in box 3 of the report form.

The weights of the individual tare units (after cleaning) are recorded in Block A of the worksheet and should be averaged. This average tare weight will be used together with the declared net weight (or other net quantity converted to weight units) to compare with the gross weight of unopened packages in the sample to determine the individual package errors. The average tare weight is entered in box 8 on the report form in dimensionless units.

2.11.4. Alternative Tare Procedure⁶

The following procedure must be followed for packages which are glass or aerosol. The procedure is optional for all other packages. For example, it has been noted that the tare variability is large for the metal cans and plastic overcaps for ground coffee and products in large cans or plastic buckets.

It will often be necessary to follow the tare procedures below for checking random packed meat and poultry using wet tare determinations.

The total number of packages to be opened for tare will be determined by first obtaining the appropriate number of packages according to Table 2-6, determining their tare weights and net contents, obtaining the ratio of the range of net contents to the range of tare weights, and referring to Table 2-7 which shows the total number of containers to be opened. Block A of the worksheet may be used for recording measurements. The detailed procedure is as follows:

- (i) An initial tare sample (see Table 2-6) is selected from the sample (see Appendix C for a description of of random sample selection).
- (ii) The packages chosen for tare are gross weighed, (gross weights are recorded on the worksheet, Block A),

and then emptied⁷. Glass packages may be opened, aerosol packages must not be opened. See Section 3.9.4. for instructions on emptying aerosol packages.

- (iii) The tare weight is determined for each package. Tare weights are recorded on Block A of the worksheet.
- (iv) The individual package errors are determined. Package errors are recorded in Block A of the worksheet.
- (v) The range of tare weights is determined. (The range is the difference between the largest tare value and the smallest. See Appendix F for more complete instructions on determining the range.) This range of tare weights is R_t . R_t is recorded in Block A on the worksheet in box 1.
- (vi) The range of the plus and minus errors (and thus the range of the net weights) is determined for the packages opened for tare determination. This range is R_c . R_c is recorded in Block A of the worksheet in box 2.
- (vii) The ratio R_c/R_t is computed. R_c/R_t is recorded in Block A of the work-sheet in box 3. (R_c and R_t must be

Sampling plan Category	Lot size	Initial tare sample size
A	all	5 packages
В	equal to or less than 250 packages	2 packages
	greater than 250 packages	5 packages

Table 2-6. Initial tare sample size for alternative tare procedures.

⁶Modification of a procedure in "Determining Tare in Net Weight Acceptance Sampling," by Robert S. Elder, <u>Journal of Quality Technology</u>, vol. 4, no. 3, July 1972, pp. 131-133. ⁷For packages labeled in units other than weight, a determination is made of the suitability of using a weight value in place of the labeled measure. This determination is made using the contents of the first two packages chosen for tare determination, and is described in Section 4.4. for packages labeled by volume, in Section 5.1.3. for packages labeled by count, and in Section 5.3.2. for packages labeled by linear or area measure. The alternative tare procedure is then followed for those packages which can be checked by weight. For packages that cannot be checked by weight, net contents must be measured directly for all the sample packages and there is no tare determination. in the same units of measure or both in dimensionless units.)

(viii) The value of n_t is read from Table 2-7 corresponding to the appropriate sample size, n, and the calculated value of R_c/R_t . The number in the table, n_t , indicates the total number of packages to be emptied to determine tare (n_t is recorded on the worksheet in box 4 of Block A).

> For example, if R_c/R_t is 2.90 for n = 30, 10 package tare weights are necessary to determine the average tare. In this example, if five packages have been emptied, five more must be emptied to obtain an average tare value.

> In another example, ten packages are randomly selected from an inspection lot of bottled herring, labeled 4 oz. Their gross weights are:

0.406	1b*	0.400	1b
0.400	1b*	0.394	1b
0.404	1b	0.398	1b
0.398	1b	0.396	1b
0.408	lb	0.398	1b

The starred values are those for the packages that were chosen for tare determination. The tare weights are: 0.146 lb for the first package and 0.150 lb for the second.

The range of tare weights is 0.150 - 0.146 = 0.004 lb = R_+ .

The package net weights for these two packages are:

0.406 lb - 0.146 lb = 0.260 lb 0.400 lb - 0.150 lb = 0.250 lb

The range of net weights is 0.260 - 0.250 = 0.010 lb = R_c .

 $R_c/R_t = 0.010/0.004 = 2.5$. Consulting Table 2-7, for $R_c/R_t = 2.5$ and n = 10, $n_t = 4$; therefore, two more packages must be opened to determine the average tare.

(ix) The number of additional packages equal to (n_t minus the initial tare sample size) is selected.

- (x) Steps (ii), (iii), and (iv) are repeated for these additional packages.
- (xi) The average of all the tare weights is used together with the labeled quantity (in terms of weight) to represent the "nominal gross weight" (unless all the packages in the sample have been opened). The average tare weight in dimensionless units is recorded in box 8 of the report form. The nominal gross weight is used to compare against the actual package gross weights to determine the package errors of the unopened packages in the sample (see Chapters 3, 4, and 5).

If the required number of packages to be opened for tare is more than half the total sample, the official has the option of opening all the packages in the sample. The tare values are not averaged in such instances; instead, each tare weight is subtracted from the corresponding package gross weight to obtain the individual package net weight. There is space on the worksheet to record up to 30 individual package gross, tare, and net weights, and resulting package errors.

Note: For foam product aerosols, a "test allowance" is applied to the tare determination to compensate for differences in product delivery between normal consumer usage and the test procedure (See Section 3.9.6.). This test allowance (provided in Table 3-2) is subtracted from the actual tare weight or the average tare weight. The resultant value is the "corrected tare" to be used in the determination of the individual package errors. The test allowance is recorded in box 9 and the corrected average tare recorded in box 10 of the report form. If all the foam aerosol packages are emptied, there is space on the worksheet to record the actual and corrected tares. In this instance, the official should note on the report form in box 10 to refer to the worksheet.

2.12. MAXIMUM ALLOWABLE VARIATIONS

The limits of reasonable individual package variations are called "Maximum Allowable Variations" (MAV) in this handbook. The MAV applies only to individual packages subject to the average requirement. Package quantities given a tolerence (or an allowable difference - see Section 5.7.) are not compared with the MAV. Table 2-7. Total number of packages $(n_{\rm t})$ to open for tare determination.

	n=315	n t	315 303 289 272 252	232 212 193 175 158	143 130 118 107 97	89 81 81 83 83 83	59 54 47 44	41 38 36 32
	n=200	nt	200 193 184 173 160	148 135 112 111 100	91 82 68 62	55 52 44 40	337 335 332 332 332 332 332 332 332 332 332	25 22 22 22 22 20 22 20 20 20 20 20 20 20
	n=125	nt	125 121 115 108 100	92 77 63 33	557 447 393	2 2 8 0 3 3 8 2 5 8 0 3 3 9 2 6 8 0 9 9 9 9 9 9 9 9 9 9 9 9 9 9 9 9 9 9	24 22 19 18	17 16 15 13
kages in sample	n=80	nt	80 77 74 69 64	5 2 4 4 5 5 0 4 0 2 2 0 4 0 2 0 0 2 0 0 2 0 0 0 0 0	37 33 25 28 28 28 25 8	23 21 18 16	15 14 12 12 12	11 10 8 8
number of pack	n=50	nt	50 46 44	37 34 28 25	23 21 17 16	15 12 11 10	10 8 8 8 7	20017
	n=30	ں ۲	30 28 268 246	23 19 15	14 113 111 10	σαανο	សមាល	444 M
	n=10	nt	10 10 8 9 8	80018	ი ი 4 4 4	~~~~~~	~ ~ ~ ~ ~ ~	~~~~
	···	Rc/Rt	0.2 0R LESS 0.21 - 0.40 0.41 - 0.60 0.61 - 0.80 0.81 - 1.00	$\begin{array}{rrrrr} 1.01 & - & 1.20 \\ 1.21 & - & 1.40 \\ 1.41 & - & 1.60 \\ 1.61 & - & 1.80 \\ 1.81 & - & 2.00 \end{array}$	2.01 - 2.20 2.21 - 2.40 2.41 - 2.60 2.61 - 2.80 2.81 - 3.00	3.01 - 3.20 3.21 - 3.40 3.41 - 3.60 3.61 - 3.80 3.81 - 4.00	4.01 - 4.20 4.21 - 4.40 4.41 - 4.60 4.61 - 4.80 4.81 - 5.00	$\begin{array}{rrrrr} 5.01 & - & 5.20 \\ 5.21 & - & 5.40 \\ 5.41 & - & 5.60 \\ 5.61 & - & 5.80 \\ 5.81 & - & 6.00 \end{array}$

		n=315	nt	30 29 26 4	223 21 190 190	18 17 15 15	15 14 13 13	12 12 11 11	10
termination.		n=200	nt	19 17 16 16	15 13 12 12 12	11 11 10 10	011101		10
oen for tare det		n=125	nt	112 111 100	თ თ თ თ თ	87779	പ പ വ വ വ	ى ى ى ى ى ى	ß
kages (n _t) to o _l	ages in sample	n=80	nt	88777	വവാവ	വ വ വ വ വ	ى ى ى ى ى ى	പറവാനവ	ъ
al number of pac	number of pack	n=50	n t	ى ى ى ى ى ى	പറപാവ	ى ى ى ى ى ى	ى ى ى ى ى	مىمىمى	ъ
ntinued). Tota		n=30	nt	m m m m m	~ ~ ~ ~ ~ ~ ~ ~	~~~~	~~~~	~~~~~	2
Table 2-7 (cc		n=10	n t	~~~~	~~~~	~~~~	~~~~	~~~~	7
		Datio		6.01 - 6.20 6.21 - 6.20 6.41 - 6.40 6.61 - 6.60 6.81 - 7.00	7.01 - 7.20 7.21 - 7.20 7.41 - 7.60 7.61 - 7.80 7.81 - 8.00	8.01 - 8.20 8.21 - 8.20 8.41 - 8.40 8.61 - 8.60 8.81 - 9.00	9.01 - 9.20 9.21 - 9.40 9.41 - 9.60 9.61 - 9.80 9.81 - 10.00	$\begin{array}{rrrrr} 10.01 & - & 10.20 \\ 10.21 & - & 10.20 \\ 10.41 & - & 10.60 \\ 10.61 & - & 10.80 \\ 10.81 & - & 11.00 \end{array}$	11.01 - 11.20

In the past, limits of reasonable variation have been described as values limiting both positive and negative deviations from the label. The present handbook provides MAV's which are used to compare with minus package errors only⁸. Positive deviations will in general be controlled by the competitive marketplace; this handbook, therefore, indicates MAV values which are intended to describe the limits of negative deviations only from the labeled quantity.

Tables 2-8 through 2-11 are separated according to the labeled unit of measure, for example, weight, volume, etc.

The MAV's for packages labeled by weight are the limits to be applied to packages when the principal declaration on the label is in terms of net weight (e.g., soap) or drained weight (e.g., mushrooms). When supplemental statements of drained weight or fill weight accompany the net weight statement on a package, the MAV listed in Table 2-8 applies to the net weight statement only, not to the accompanying drained weight or fill weight statement.

When checking standard pack packages for which the labeled quantity is in units of weight, the official should complete box 5 of the report form using that value from Table 2-8 corresponding to the labeled weight.

When checking standard pack packages labeled in units other than weight, the official should fill in box 6 of the report form using the appropriate value from Table 2-9, 2-10, or 2-11. Block A of the worksheet provides space for recording the MAV for random pack package weights. Block B of the worksheet provides space for calculating the MAV in units of weight for those instances in which weighing will be used to check packages labeled in units other than weight.

The MAV in dimensionless units (box 7) is obtained by dividing the MAV value from Table 2-8, 2-9, 2-10, or 2-11 (and recorded in box 5 or 6) by the unit of measure (box 4). See Section 3.6. for application of the MAV to random pack package lots.

2.13. EXCEPTIONS TO THE MAXIMUM ALLOWABLE VARIATIONS

When packaging practices or the nature of the product demands, MAV's exceeding those

listed in Tables IV through VII are necessary.

Specific Product Exceptions to the MAV:

Any individual thickness measurement of polyethylene sheeting may be -20% of labeled thickness.

The average thickness of a single package of polyethylene sheeting may be -7% of the labeled thickness (see Section 5.4.3.)

The National Conference on Weights and Measures Model State Packaging and Labeling Regulation lists the maximum allowable variation for textiles as the following:

For those packages with no declared dimension less than 24 inches: -3% of the declared dimension +6% of the declared dimension

For the packages with any declared dimension less than 24 inches: -6% of the declared dimension +12% of the declared dimension

2.14. MOISTURE ALLOWANCE

If a moisture allowance is to be applied to the particular packaged product under test, that allowance may be subtracted from the "nominal gross weight" (see Section 2.11. and step 13 of Section 3.5.) to obtain a corrected nominal gross weight. This corrected nominal gross weight is then compared with the gross weight of each unopened package in the sample in order to determine individual package errors. The nominal gross weight and corrected nominal gross weight may be recorded at the bottom of Block A of the worksheet.

Example of how to apply a moisture allow-ance:

Labeled weight = 12.00 oz.

Average tare weight = 0.16 oz.

The moisture allowance is assumed, in this example, to have been assigned by the regulatory agency as 2% of the labeled weight = $0.02 \times 12.00 \text{ oz} = 0.24 \text{ oz}.$

Therefore, the corrected nominal gross weight to use in comparing with the gross weight

⁸Note exception in Section 2.13. for textiles.

0

of unopened packages in the sample =

12.00 oz + 0.16 oz - 0.24 oz = 11.92 oz.

Thus, sample packages weighing more than 11.92 oz will have positive package errors and sample packages weighing less than 11.92 oz will have negative package errors.

Avoirdupo	is units		Metric units	
Labeled weight	M	AV	Labeled weight	MAV
Pounds or ounces	Decimal pounds	Fractional ounces	Grams	Grams
up to and including 0.026 lb up to and including 0.41 oz	0.001		up to and including O to 11.6	0.5
0.026+ ^b to ^C 0.04 lb 0.041+ to 0.64 oz	0.002	1/32	11.6+ to 18	1
0.04+ to 0.08 lb 0.64+ to 1.28 oz	0.004	1/16	18+ to 36	2
0.08+ to 0.12 lb 1.28+ to 1.92 oz	0.008	1/8	36+ to 54	4
0.12+ to 0.18 lb 1.92+ to 2.88 oz	0.012	3/16	54+ to 82	5
0.18+ to 0.26 lb 2.88+ to 4.16 oz	0.016	1/4	82+ to 118	7
0.26+ to 0.34 lb 4.16+ to 5.44 oz	0.020	5/16	118+ to 154	9
0.34+ to 0.46 lb 5.44 + to 7.36 oz	0.024	3/8	154+ to 209	11
0.46+ to 0.58 lb 7.36+ to 9.28 oz	0.028	7/16	209+ to 263	13
0.58+ to 0.70 lb 9.28+ to 11.20 oz	0.032	1/2	263+ to 318	15
0.70+ to 0.84 lb 11.20+ to 13.44 oz	0.036	9/16	318+ to 381	16
0.84+ to 0.94 lb 13.44+ to 15.04 oz	0.040	5/8	381+ to 426	18
0.94+ to 1.08 lb 15.04+ to 17.28 oz	0.044	11/16	426+ to 490	20
1.08+ to 1.26 lb	0.048	3/4	490+ to 572	22
1.26+ to 1.40 lb	0.052	13/16	572+ to 635	24
1.40+ to 1.54 lb	0.056	7/8	635+ to 698	25
1.54+ to 1.70 lb	0.060	15/16	698+ to 771	27

Table 2-8. Maximum allowable variations for an individual package labeled by weight^a.

^aApplies only to shortages in package weight (minus package errors)

 $^{\rm b}$ 0.026+ means "greater than 0.026"

^C"to" means "to and including"

Avoirdu	pois units		Metric units	
Labeled weight	M	AV	Labeled weight	MAV
Pounds	Decimal pounds	Fractional ounces	Kilograms	Grams
1.70+ to 1.88	0.064	1	771+ to 852	29
1.88+ to 2.14	0.070	1 1/8	852+ to 971	32
2.14+ to 2.48	0.078	1.1/4	971+ to 1.125	35
2.48+ to 2.76	0.086	1 3/8	1.125+ to 1.350	40
2.76+ to 3.20	0.094	1 1/2	1.350+ to 1.600	45
3.20+ to 3.90	0.11	1 3/4	1.600+ to 1.800	50
3.90+ to 4.70	0.12	2	1.800+ to 2.100	55
4.70+ to 5.80	0.14	2 1/4	2.100+ to 2.640	65
5.80+ to 6.80	0.15	2 1/2	2.640+ to 3.080	70
6.80+ to 7.90	0.17	2 3/4	3.080+ to 3.800	80
7.90+ to 9.40	0.19	3	3.800+ to 4.400	85
9.40+ to 11.70	0.22	3 1/2	4.400+ to 5.200	100
11.70+ to 14.30	0.25	4	5.200+ to 6.800	115
14.30+ to 17.70	0.28	4 1/2	6.800+ to 8.20	130
17.70+ to 23.20	0.31	5	8.20+ to 10.60	145
23.20+ to 31.60	0.37	6	10.60+ to 14.30	170
31.60+ to 42.40	0.44	7	14.30+ to 19.25	200
42.40+ to 54.40	0.50	8	19.25+ to 24.70	230
54.40+]	%	24.70+	1%

Table 2-8. (continued). Maximum allowable variations for an individual package labeled by weight.

Maximum allowable variations for an individual package labeled by volume - liquid or dry^a. Table 2-9.

	Inch-Pound			Metric	
Labeled quantity	Liquid MAV (dr or fl oz)	Labeled quantity	Dry MAV (cu in)	Labeled quantity	Liquid and dry MAV (mL)
up to and including 0.50 fl oz	٩	up to and including 0.18 cu in	0.03	up to and including 3 mL	0.5 mL ^c
		0.18+ to 0.49 cu in	0.06	3+ to 8 mL	1.0 mL ^c
		0.49+ to 0.92 cu in	0.09	8+ to 15 mL	1.5 mL ^c
0.50+ ^d to ^e 0.75 fl oz	0.5 dr	0.92+ to 1.35 cu in	0.11	15+ to 22 mL	2.0 mL
0.75+ to 2.25 fl oz	1.0 dr	1.35+ to 4.06 cu in	0.23	22+ to 67 mL	3.5 mL
2.25+ to 4.25 fl oz	1.5 dr	4.06+ to 7.67 cu in	0.34	67+ to 126 mL	5.5
4.25+ to 5.75 fl oz	2.0 dr	7.67+ to 10.38 cu in	0.45	126+ to 170 mL	7.5
5.75+ to 7.50 fl oz	2.5 dr	10.38+ to 13.54 cu in	0.56	170+ to 222 mL	6
7.50+ to 11.75 fl oz	3.0 dr	13.54+ to 21.21 cu in	0.68	222+ to 347 mL	11
11.75+ to 17.00 fl oz (1 pt, 1 oz)	4.0 dr	21.21+ to 30.68 cu in	0.90	347+ to 503 mL	15
17.00+ to 21.00 fl oz (1 pt, 1 oz)	5.0 dr	30.68+ to 37.90 cu in	1.13	503+ to 621 mL	18
21.00+ to 27.00 fl oz (1 pt, 1 oz)	6.0 dr	37.90+ to 48.73 cu in	1.35	621+ to 798 mL	22

^aApplies to shortages in package volume (minus package errors).

^bConvert to metric units and use laboratory glassware.

^CUse laboratory volumetric glassware.

d_{0.50+} means "greater than 0.50".

euto" means "to and including".

2-23

Table 2-9. (continued). Maximum allowable variations for an individual package labeled by volume -liquid or dry.

	Inch-Pound			Metric	
Labeled quantity	Liquid MAV (dr or fl oz)	Labeled quantity	Dry MAV (cu in)	Labeled quantity	Liquid and dry MAV (mL)
27.00+ to 31.00 fl oz (1 pt, 1 oz)	7.0 dr	48.73+ to 55.95 cu in	1.58	798+ to 917 mL	26
31.00+ to 39.00 fl oz (1 qt, 7 oz)	8.0 dr	55.95+ to 70.38 cu in	1.80	917+ mL to 1.153 L	30
39.00+ to 55.00 fl oz	10.0 dr	70.38+ to 99.26 cu in	2.26	1.153+ to 1.627 L	37
55.00+ to 69.00 fl oz	12.0 dr	99.26+ to 124.5 cu in	2.71	1.627+ to 2.041 L	44
69.00+ to 85.00 fl oz	14.0 dr	124.5+ to 153.4 cu in	3.2	2.041+ to 2.514 L	52
85.00+ to 103.00 fl oz	2.0 fl oz	153.4+ to 185.9 cu in	3.6	2.514+ to 3.046 L	59
103.00+ fl oz to 1.25 gal	2.5 fl oz	185.9+ to 288.8 cu in	4.5	3.046+ to 4.732 L	74
1.25+ to 1.45 gal	3.0 fl oz	288.8+ to 335.0 cu in	5.4	4.732+ to 5.489 L	89
1.45+ to 1.875 gal	3.5 fl oz	335.0+ to 433.1 cu in	6.3	5.489+ to 7.098 L	104
1.875+ to 2.125 gal	4.0 fl oz	433.1+ to 490.9 cu in	7.2	7.098+ to 8.044 L	118
2.125+ to 2.688 gal	4.5 fl oz	490.9+ to 620.8 cu in	8.1	8.044+ to 10.173 L	133
2.688+ to 3.063 gal	5.0 fl oz	620.8+ to 707.4 cu in	9.0	10.173+ to 11.593 L	148
3.063+ to 4.375 gal	6.0 fl oz	707.4+ to 1011 cu in	10.8	11.593+ to 16.561 L	177
4.375+ to 5.0 gal	7.0 fl oz	1011+ to 1155 cu in	12.6	16.561+ to 18.927 L	207
5.0+ to 6.25 gal	8.0 fl oz	1155+ to 1444 cu in	14.4	18.927+ to 23.659 L	237
6.25+ to 7.063 gal	9.0 fl oz	1444+ to 1631 cu in	16.2	23.659+ to 26.734 L	266
Over 7.063 gal	1%	0ver 1631 cu in	1%	Over 26.734 L	1%
		l Dry Pint = 1 Dry Quart	= 33.6003125 = 67.200625	ure Equivalent cu in 1 Bushel = 21 cu in 1 cu ft = 172	50.42 cu in 3 cu in

Labeled count	MAV
up to and including 17	0 ^b
18-50	lp
51-83	2
84-116	3
117-150	4
151-200	5
201-240	6
241-290	7
291-345	8
346-400	9
401-465	10
466-540	11
541-625	12
626-725	13
726-815	14
816-900	15
901-990	16
991-1075	17
1076-1165	18
1166-1250	19
1251-1333	20
1334 and over	1.5% rounded off to the nearest whole number

Table 2-10. Maximum allowable variation for an individual package labeled by count^a.

^aApplies only to shortages in package count (minus package errors).

 $^{
m b}$ See Section 5.2. for sampling plans to be used with these package sizes.

Length	
	Metric
MAV (expressed as a percentage of the labeled length)	Labeled length meters
1.5%	up to and including 40
2%	40+ to 85
2.5%	85+ to 140
3%	140+ to 300
4%	300+ to 1000
5%	1000+
Area	
ckages labeled by area is 3% of the labeled	area.
5	Length MAV (expressed as a percentage of the labeled length) 1.5% 2% 2.5% 3% 4% 5% 5% 5% 5% 5% 5% 5% 5% 5% 5% 5% 5% 5%

Maximum allowable variations for an individual package labeled by length (width) or by area^a Table 2-11.

.

^aApplies only to shortages in package measure (minus package errors).

b₄8+ means greater than 48

^C"to" means "to and including"

See Section 2.13. for exceptions: textiles, polyethylene sheeting.

CHAPTER 3. METHODS OF TEST FOR PACKAGES LABELED BY WEIGHT

- 3.1. WEIGHING EQUIPMENT
- 3.2. PREPARATION FOR TESTING
- 3.3. RECORDING PACKAGE WEIGHTS
- 3.4. READING THE PACKAGE TESTING SCALE
- 3.5. STANDARD PACK LABELED BY WEIGHT: GENERAL METHOD
- 3.6. RANDOM PACK LABELED BY WEIGHT
- 3.7. LARGE WEIGHTS AND THE SUBSTITUTION METHOD
- 3.8. THE DETERMINATION OF DRAINED WEIGHT
- 3.9. AEROSOL PACKAGES
- 3.10. SPECIAL COMMODITY: FROZEN FOOD AND OTHER FROZEN PRODUCTS
- 3.11. SPECIAL COMMODITY: DRAINED WEIGHT OF FROZEN FOODS
- 3.12. SPECIAL COMMODITY: GLAZED RAW SEAFOOD AND FISH
- 3.13. SPECIAL COMMODITY: CANNED COFFEE

Provided in this chapter are, firstly, descriptions of weighing equipment and conventions in weighing. There follows a stepby-step listing of the general method of test for packages labeled by weight to which reference will be made throughout the rest of the handbook.

Methods of test for special types of commodities labeled by weight (drained weight, random pack, etc.) and then for specific commodities (coffee, seafood) complete the chapter.

3.1. WEIGHING EQUIPMENT

The equipment recommended for use in checking packages labeled by weight is as follows:

Equal-Arm Scale (for small weights in avoirdupois units) (Figure 3-1). - An equal-arm scale with approximately 5 pounds capacity and with center tower and poise beams is recommended. On one face the division size should not be greater than 1/16 ounce and 0.002 pound on the other face. The minimum number of divisions should be 10 divisions on either side of zero on either tower face. The poise beams should have a zero notch in the center and notched divisions each equal to or less than the tower capacity on either side of zero with a span of at least 4 ounces or 0.24 pound. For example, a scale with 20 divisions (of 0.002 lb each) on the tower face should have notched divisions of 0.04 pound intervals on the poise beams. The scale should be fitted with a locking device to hold the lever during transit, with a handle for carrying, and should be provided with a protective cover or box. The sensitivity of this scale must be 1/2 scale division per 0.001 lb. The scale must meet all requirements of NBS Handbook 44 (H-44) for automatic indicating scales (see H-44 Scale Code T.3.1.) except that the accuracy should be 1/2 the acceptance tolerance given in H-44 Scale Code Table 4 with a maximum tolerance of two tower divisions.

Equal-Arm Scale (for small weights in metric units)¹. - Similar in design to the avoirdupois weight scale with the exception that the maximum size of each tower division should be 1 gram and the poise beam should be provided with at least a 200-gram span with notched divisions each equal to or less than the tower capacity. The minimum sensitivity of this scale must be 1/2 scale division per 0.5 gram. The scale must meet H-44 requirements except that the accuracy should be 1/2 the acceptance tolerance given in H-44 Scale Code Table 4 with a maximum tolerance of two tower divisions.

Equal-Arm Scale (for larger weights in avoirdupois units). - For checking packages heavier than the capacity of the scale for small weights, an equal-arm scale with center tower and poise beams and with a capacity of approximately 20 pounds is recommended. One face of the tower should have a maximum division size of 1/8 ounce and the other face of the tower should show divisions not greater than 0.004 pound. There should be at least 10 divisions on either side of zero on either tower face. The poise beams should have a zero notch in the center and notched divisions each equal to or less than the tower capacity on either side of zero. One beam should have at least a 12-ounce span and the other side at least a 0.6-pound span. This scale should also be fitted with a locking device to hold the lever during transit, with a handle for carrying, and should be provided with a protective cover or box. The minimum sensitivity of this scale must be 1/2 scale division per 0.002 pound. The scale must meet H-44 requirements except that the accuracy should be 1/2 the acceptance tolerance given in H-44 Scale Code Table 4 with a maximum tolerance of two tower divisions.

Equal-Arm Scale (for larger weights in metric units)¹. - Similar in design to the 20 pound scale with the exception that the tower should have maximum divisions of 2 grams and the poise beam provided with at least a 400 gram span with notched divisions each equal to or less than the tower capacity. The minimum sensitivity of this scale must be 1/2 scale division per 1.0 gram. The scale must meet H-44 requirements except that the accuracy should be 1/2 the acceptance tolerance given in H-44 Scale Code Table 4 with a maximum tolerance of two tower divisions.

<u>Commercial Scale</u> - Checking of packages heavier than the capacity of the equal-arm

¹The markings specified for the equivalent metric scales may be incorporated into the present avoirdupois weight scales to eliminate the need for two scales.

scale for larger weights, or of those that cannot be accommodated on the platform of the equal-arm scale, may necessitate the use of an on-site device. Care must be exercised to insure that the device meets and is used in accordance with the criteria listed under the "substitution" method as discussed in Section 3.7.



Figure 3-1. Equal-arm package testing scale for small weights (avoirdupois units).

<u>Analytical Balance</u> - In Section 2.9.2., it is noted that only scales that can weigh accurately to 1/6 the maximum allowable variation for an individual package should be used. For example, the MAV for a 10-gram package is 0.5 g; therefore, the accuracy to be used in weighing is 0.08 g, which is beyond the capacity of the small capacity metric package scale. Therefore, in this example, these packages must be weighed on an analytical balance. (This may require signing for packages and transporting to a laboratory, although portable balances are available with the required accuracy.)

Field Standard Weights² (Figure 3-2) - For weighing in avoirdupois units, two kits, one a collection of 31 pounds of standard weights from 2 pounds to 1/16 ounce denominations and another kit of weights varying from 0.3 pound to 0.001 pound are adequate for checking small packages; an additional 25-pound and two 50-pound standard weights will be sufficient for most large packages. For weighing packages labeled in metric units, weights will include a total of 15 kilograms of standard weights with various denominations of weights ranging down to 0.5 gram for checking small packages; two 10-kilogram, and two 20-kilogram standard weights will be sufficient for most large metric packages.



Figure 3-2. Test weight kit.

3.2. PREPARATION FOR TESTING

The principal requirement for a testing location is convenience to both the official and store, warehouse, or plant personnel. If the checking is to be done in the customer area of the store, it should be so located that it does not interfere with normal customer traffic.

Once the test area has been selected, provision should be made for a stable and level table or work area for the test equipment (a bubble level may be used to verify level working surface). The equal-arm scale should be placed on a firm support and leveled. Following Examination Procedure Outline No. 4 from NBS Handbook 112, the inspector should (a) observe the scale at zero-load indication, (b) test the scale with standard weights to capacity with equal loads on each pan, and (c) test the scale with small loads to test the tower indicator and poise beam. The scale should meet the requirements of H-44 except that its accuracy should be 1/2 the acceptance tolerance given in H-44 Scale Code Table 4 with a maximum tolerance of two tower divisions.

 $^{^{2}}$ Tolerances for field standard weights (avoirdupois and metric) are given in Appendix G, Table G-1.

If a commercial scale is to be used, the scale should be checked carefully to determine whether it has met H-44 requirements and used only if it is sufficiently sensitive to indicate changes in weight commensurate with MAV/6 (see Section 2.9.2.). Once the scale has been selected, it should not be released to commercial service until the testing has been completed.

3.3. RECORDING PACKAGE WEIGHTS

Table 3-1 lists the recommended units of measure with which the official should record weights according to the labeled weight of the package. See the discussion of procedures for recording weights in Section 2.9.

3.4. READING THE PACKAGE TESTING SCALE

For the greatest accuracy obtainable with an equal-arm package testing scale, the tower face readings should not be read directly to determine the package errors. Rather, the scale should be used as a "null-indicator" such that the field standard weights are used on the one weigh pan to exactly balance the other weigh pan containing the item to be weighed. The package errors may then be read exactly in terms of reference weights (rather than weight indications on the tower face).

When using the package checking scale as a "null indicator", if an <u>exact</u> balance cannot be achieved, the index of the indicator should point away from the product being weighed to determine the gross or net weights, and towards the material being weighed for tare.

When the package checking scale is being read directly, it will frequently be necessary to round off the indication shown on the tower face to the nearest division (or the nearest division which corresponds to the increments in Table 3-1.). When the index of the package scale indicator is less than one half the distance between two divisions, the official should record the value corresponding to the lower division and correspondingly, when greater than one half the distance, record the value corresponding to the next higher division. When the indicator is one half of the distance between two divisions, the official should record the value corresponding to the next higher division when recording the gross package weight, and should record the value corresponding to the next lower division when recording the tare.

Conventionally, neither packagers nor testing officials make air buoyancy corrections in the determination of package weights. For practicality, air buoyancy corrections are not applied in the procedures given in this handbook.

3.5. STANDARD PACK LABELED BY WEIGHT: GENERAL METHOD

The Decision Charts 1, 2, and 3 on the following pages briefly outline the flow of operations for standard-pack packages labeled by weight.

The steps to be followed, as shown on the charts, are described in greater detail in the remainder of this section. Decision Charts 1 and 2 are identical down through step 16; Chart 1 is appropriate when a sampling plan in Category A is to be used and Chart 2 is for Category B. Chart 3 is a supplement to either Chart 1 or 2 that describes the procedure to be followed when Section 2.11.4. is used for tare determination.

The description below references numbered boxes on the report form and locations on the worksheets (see Section 2.2.). Some of the report form boxes and worksheet spaces are provided for special procedures discussed in later sections of this chapter or in later chapters, and will not be mentioned in the description of the general method.

Steps with (a), (b), and (c) apply to different types of tare weight.

- Fill out the report form heading and also the MAV (refer to Table 2-8) in units of weight (box 5 of the report form), the unit of measure (box 4), and the MAV converted to a dimensionless integer (box 7). (For packages labeled by weight, box 6 is not used.)
- Determine the size of the inspection lot and record it in box 1 of the report form. Record the column 4 value from Table 2-2 or 2-5 (the allowable number of unreasonable errors) in box 13 of the report form.
- Record the sample size, n, from column 2 of Table 2-2 or 2-5 in box 2 of the report form.

Record the tare sample size, n_t, according to the type of tare to be measured:

Avoirdupois u	Inits		Metric ur	nits
Labeled weight	Units of m	leasure	Labeled weight	Units of measure
	(oz avoir)	(ql)		(kg)
Up to and including 1.92 oz (0.12 lb)	IJ	Q	Up to and including 82 g	IJ
Greater than 1.92 oz (0.12 lb) to and including 5.44 oz (0.34 lb)	1/32 ^b	0.002 ^b	Greater than 82 g to and including 250 g	0.001 ^b
Greater than 5.44 oz (0.34 lb) to and including 20 oz (1.25 lb)	1/16	0.004	Greater than 250 g to and including 900 g	0.002
Greater than 1 lb to and including 4 lb	1/8	0.008	Greater than 900 g to and including 2.5 kg	0.005
Greater than 4 lb to and including 8 lb	1/4	0.02	Greater than 2.5 kg to and including 30 kg	0.01
Greater than 8 lb to and including 25 lb	1/2	0.03	Greater than 30 kg to and including 60 kg	0.05
Greater than 25 lb to and including 75 lb	1	0.05	Greater than 60 kg	0.1
Greater than 75 lb to and including 150 lb	2	0.1		
Greater than 150 lb	4	0.2		

Recommended units of measure to be used in recording package weights. Table 3-1.

^aAn analytical or other high accuracy balance will be necessary for weighing packages in this category.

^bThe equal-arm package scale must be used as a null-indicator for packages labeled from 1.92 to 5.44 oz or 82 to 250 g to eliminate effects of possible tower errors.

- For wet tare, record tare sample a. size (from Table 2-2 or 2-5, column 3) in box 3 of the report form.
- b. If the package container is glass or aerosol or for other reasons the alternative tare procedures will be used, record initial tare sample size from Table 2-6 in box 3 of the report form.
- For dry tare, identify the lot с. (or lots) of tare materials (see Appendix C.6.) and record tare sample size (from Table 2-2 or 2-5, column 3) in box 3 of the report form.
- 4 a. For wet tare, select random numbers and from them, the sample packages (see Appendix C for a description of this method.)
 - b. For the alternative tare procedure, identify the sample packages in the order in which their corresponding random numbers were obtained. This is the order in which the packages will be opened for tare. Select the initial tare sample. See Appendix C.6.1. for an example.
 - For dry tare, select the tare samс. ple and include all the materials used in or on the package. Refer to Appendix C.6.1. for a description of how to select the tare sample. Go to step 6.c.
- 5. Determine the gross weight of each a. or b. package in the tare sample (See Figure 3-3). The labeled and gross weights are recorded on the worksheet in Block A. (Fill in the blanks of the column headings with "weight".) Record gross weight in units of weight or dimensionless units.
- 6. а. For wet tare, empty the packages selected for tare and determine the tare weight and resultant package errors³ of these packages.

net weight = gross weight - tare weight



Figure 3-3. The determination of the gross weight of a package.

> Package error = net weight - labeled weight

Record net weights and package errors on the worksheet in Block A in units of weight or dimensionless units. Continue on to step 12.

- h For the alternative tare procedure, empty the tare packages, determine their tare weights and package errors³. Follow steps 7 through 11.
- For dry tare, determine the weights с. of the individual units including all the materials used in or on the package. Record on the worksheet in units of weight or in dimensionless units in Block A filling in the tare heading blank as "dry". Go on to step 12.
- 7. Determine the range of tare weights, R_+ , and record R_+ in box 1 of Block A on the worksheet. (See Appendix F on determining a range.)
- Determine the range of package errors, 8. R_c , and record R_c in box 2 of Block A on the worksheet.
- 9. Compute the ratio R_c/R_t , record it in box 3 of Block A, and use Table 2-7 to

 3 If a moisture allowance is to be applied, convert the moisture allowance, if necessary, to units of weight or dimensionless units and subtract it from each tare weight to obtain a corrected tare weight. Use the corrected tare weight to compute the net weight and package error for the tare sample. (There is space in Block A of the worksheet to record a corrected tare value for each package opened for the tare determination when a moisture allowance is applied.)



determine whether more packages are required to determine tare. From Table 2-7, record the final tare sample size, n_+ , in box 4 on Block A of the worksheet.

If n_t is larger than the initial tare

sample size recorded on the report form in box 3, the initial tare sample size may be crossed out and the n_+ deter-

mined in this step recorded in box 3 in its place. If more packages are required for tare determination than the number of packages already opened, follow the next step. If no more packages are required, go to step 12.

- Select from the sample the additional packages required to determine the tare as described in Appendix C.6.1.
- Empty these additional packages and determine the tare weights and net weights³ for each additional package opened. Record the additional gross weights, tare weights, and package errors in the appropriate spaces on the worksheet in Block A.
- 12. Unless all the packages in the sample have been opened, average the tare weights. Convert the average tare to dimensionless units (if not already converted) and record this in box 8 of the report form.
- 13. Using an appropriate unit of measure, record the package errors for the packages emptied for tare determination in the checkerboard area of the form in dimensionless units. This may be the entire sample if it is necessary to open all the packages in the sample. If all the packages in the sample have been opened for tare, go to step 16.

If a moisture allowance is to be applied, subtract it (in terms of units of weight or dimensionless units) from the average tare weight. This is the corrected tare and is recorded in box 10 of the report form in dimensionless units.

14. The average tare weight (or corrected average tare) plus the labeled weight is the "nominal gross weight" to be used in determining package error. The nominal gross weight may be recorded in the lower part of Block A on the worksheet.

- 15. Place standard weights equal to the "nominal gross weight" on the left pan of the package weighing scale. Place the remaining packages of the sample individually on the right pan (see Figure 3-3) and record the individual package errors (plus, zero, minus differences from the nominal gross weight) in dimensionless units in the checkerboard area of the report form (as described in Section 2.9.3.).
- 16. Circle any minus package errors that exceeds the MAV (these are called "unreasonable errors") and record the number in box 14 of the report form. If the number of unreasonable errors exceeds that number recorded in box 13 the lot fails to conform with requirements. No further testing of the lot is necessary. If box 14 is equal to or less than box 13, go on to step 17.
- 17. Sum the individual package errors for the sample (with due regard for positive and negative package errors) and record the sum for each row in the spaces marked "Total Errors" on the report form. Add up these sums and enter the total at the foot of the Total Errors column. If the total error is zero or positive, the lot conforms with requirements. No further testing of the lot is necessary.

If a Category B plan is being used, and if the total error is negative, the lot fails to conform to the package requirements. No further testing of the lot is necessary.

Divide the total error by the number of packages in the sample to determine the average error and record that value (in dimensionless units) in box 15 of the report form. Record the average error in the same units of measure as the label in box 16.

If a Category A plan is being used and the total (and thus the average) error is negative, go to step 18.

³If a moisture allowance is to be applied, convert the moisture allowance, if necessary, to units of weight or dimensionless units and subtract it from each tare weight to obtain a corrected tare weight. Use the corrected tare weight to compute the net weight and package errors for the tare sample. (There is space in Block A of the worksheet to record a corrected tare value for each package opened for the tare determination when a moisture allowance is applied.)



Circled numbers refer to locations on the report form

18. Determine the error limit T (See Section 2.6.2.): T = (0.8598/√n) x R x f) by the following procedure:

Record the range of package errors in each column of the checkerboard area in the spaces beside the designation "R" on the report form.

Record $\bar{\mathsf{R}}$ in box 17 of the report form.

Record the value of $0.8598/\sqrt{n}$ (from column 2 of Table 2-3) in box 18.

Record d = $(0.8598/\sqrt{n}) \times \overline{R}$ in box 19 (box 17 x box 18).

Record the percent of the lot which is the sample in box 20.

Record the f value from Table 2-4 in box 21.

Record, $T(= box 21 \times box 19)$ in box 22 of the report form.

Add T to the average package error and record this value in box 23.

If the value in box 23 is zero or positive, the lot complies with the package requirements. If the value in box 23 is a minus value, the lot fails to comply with regirements.

3.6. RANDOM PACK LABELED BY WEIGHT

Random pack packages are those whose contents are measured, packaged, and labeled individually. As a group or lot, these packages do not occur, in general, in fixed or patterned quantities. They occur most frequently labeled by weight. Also, they are tested most frequently where they are packaged, usually at the retail store or wholesale warehouse.

See Section 2.3.2. for the definition of a lot for random pack commodities.

The only difference between the checking procedure for random pack packages and standard pack (Section 3.5.) occurs in step 15. Each package in the random pack sample is compared against the weight marked on its label plus the average tare weight for that size and wrap category of packages (small tray, large tray, shrink wrap, etc.). This necessitates changing the weights placed on the left weighpan of the equal-arm scale according to the different labeled weights and tare weights of each package in the sample in order to determine the individual package errors. Record individual labeled weights, gross weights, tare weights, and net weights on the worksheet in Block A and transfer the resulting package errors to the report form. Otherwise, the entire procedure is exactly as in Section 3.5.

When an entire meat counter is audit tested (See Section 1.5.), the MAV to apply to a random pack lot is that MAV corresponding to the average labeled weight of the sample. If official action will be taken on an entire counter two alternatives may be followed. The official should either (1) separate the packages into inspection lots of different labeled weight categories as listed in Table 2-8 (for example, 0.94 to 1.08 lb as one lot, 1.08 to 1.26 lb as a second lot, and so on) or (2) select the sample from the entire counter (defined as the lot) and apply to each sample package the MAV associated with its labeled weight. Block A of the worksheet provides a column headed "MAV (random pack)" for this purpose.

When determining wet tare weights for random pack packages of meat, poultry, fish and similar products, the official may note large variability in the tare weights, stemming from, for example, a varying number of soaker pads in each package, or varying amounts of absorbed liquid in the packaging materials. In such case, the alternative tare procedure of Section 2.11.4. will be useful in the determination of the average tare weight.

3.7. LARGE WEIGHTS AND THE SUBSTITUTION METHOD

Using a commercial scale (rather than the inspector's package checking scale), the substitution method may be used for the checking of large packages (random or standard pack), if the size and/or weight exceed the capacity of the equal-arm packagechecking scales. The commercial scale should be used as a substitution weigher or null indicator only and not as a "direct reading" device because possible scale error and between division interpolation error would contribute to the uncertainty of results.

The following procedure refers to steps in Section 3.5. but does not follow any decision chart.

If the tare can be weighed on one of the testing official's equal-arm scales, follow substeps (a).

If the tare is too heavy or large to use the official's scales, or if product is liquid, follow substeps (b).



Roman numerals in parenthesis refer to steps in Section 2.11.4., letters to Section 3.5. Circled numbers refer to locations on the report form.

Boxed letters and numbers refer to locations on the worksheet.

*If moisture allowance is applied, net weight = gross weight - corrected tare weight. (Corrected tare weight = tare weight - moisture allowance)

- 4. Follow Section 3.5., steps 1 through 4 for instructions in filling out the report form and selecting the random sample and random tare sample.
- a. Empty the first tare sample package and weigh the tare on one of the official's scales. (If packaged product is particulate material, empty package into a container.)
 - b. Place first package to be opened for tare determination on commercial scale and note scale indication. Remove package. (See Example.)
- 6. a. Place on commercial scale standard weights representing tare weight of first tare sample package plus standard weights representing labeled weight plus standard weights of about 3% of the labeled weight such that:
 - If an analogue scale, the index of the indicator is coincident with a scale division.
 - If a digital scale, a "balance" is obtained. Obtain a balance by adding a sufficient amount of small weights (in increments equal to 1/10 the value of the scale's minimum division) to attain the break-point between two consecutive indications⁴. (See Example.)

Record the amount of standard weights and the scale reading in Block B of the worksheet in columns 6 and 8.

- b. Place on commercial scale standard weights equivalent to scale indication in 5b plus a small amount of additional weights (an additional 1%) so that a balance is obtained as described in step 6a for a digital or analogue scale. Record standard weights and scale reading in columns 6 and 8 of Block B on the worksheet.
- a. Remove standard weights representing the tare and labeled weight.

Place the sample package and contents on the commercial scale.

- Remove standard weights from the scale. Place tare sample package on the commercial scale.
- Add or remove weights until the 8. а. scale indication recorded in 6a is duplicated. With an electronic digital scale, if weights must be removed, remove enough weights so the readout of step 6a is duplicated by adding (rather than removing) weights in weight increments of 0.1 division. (That is, always approach the break-point from the minus side of the weight indication.) Record the total amount of weights added or removed in this step as the package error in Block A of the worksheet⁵. If weights are added, this is a minus package error; if weights removed, this is a plus package error.
 - b. Add weights until the scale indication recorded in 6b is duplicated. When using a digital scale, add weights in increments of 0.1 division until the breakpoint is reached. Record the standard weights on the scale in Block B of the worksheet in column 7. The gross weight of the package is equal to the amount of standard weights recorded in step 6b in column 6 of Block B minus the standard weights in column 7. Record the gross weight in Block A of the worksheet.
- a. Repeat steps 5a through 8a for the rest of the tare sample using the tare weight corresponding to each tare sample package in step 6a.
 - b. Repeat steps 5b through 8b to determine the tare weight of the first tare sample package and to determine the gross weights and tare weights of the remaining tare sample packages.
- If the alternative tare procedure is being used, follow steps 7 through 12 of Section 3.5., determining the package errors for all the packages opened for tare.

⁴For a discussion of error weight testing, see pages 120-122 of NBS Handbook 94. ⁵If a moisture loss is to be applied, package error is equal to weights added or removed plus (+) moisture allowance (converted to units of weight). For example if moisture allowance of 2 lb is applied to example, step 8a, a package error of 2.00 lb - 0.32 lb = +1.68 lb results.

	Examples o	f substitution weighing	
Step		standard weights on pans	scale reading
		(avoirdupois - decimal	pounds)
5a.	Scale reading with package on pan		101.1 lb
6a.	After placing standard weights on scale to balance (tare wt + labeled wt + 3% labeled wt (3.11 lb))	104.46 lb	104.5 lb
7a.	After removing standard weights (tare + labeled wt) and adding sample package	3.11 lb	104.2 lb
8a.	After adding or removing standard weights to duplicate step 6a scale indication	3.43 lb	104.5 lb
	Package error = (standard weights, 7	a - 8a) = -0.32 lb	
5b.	After placing sample package on scale		101.1 lb
6b.	After placing standard weights duplicating step 5b scale indication + standard weights to obtain balance	101.94 lb	102.0 lb
7b.	After removing standard weights and adding sample package		101.1 lb
8b.	After adding standard weights to duplicate step 6b scale indication	.93 lb	102.0 lb

Gross weight = (standard weights, 6b-8b) = 101.0 lb



Figure 3-4. Average tare plus labeled weight (nominal gross weight) on scale, substitution method. If the alternative tare procedure is not being used, average the tare weights and follow steps 6a through 8a to find the package errors for the remainder of sample. (In step 6a, use the average tare weight rather than the tare of the tare sample package.) Follow step 16 onward of Section 3.5. to determine lot conformance or nonconformance.

3.8. THE DETERMINATION OF DRAINED WEIGHT

3.8.1. Equipment

<u>Scales and weights</u> recommended in Section 3.1. are suitable for drained weight determinations.

Sieves

- For drained weight of 3 lb (1.36 kg) or less, one 8-in (20 cm) No. 8 mesh U.S. Standard Sieve Series stainless steel sieve, receiving pan, and cover.
- ^o For drained weight greater than 3 lb (1.36 kg), one 12-in (30 cm) sieve, with same specification as above.

<u>Stopwatch</u> - mechanical or electronic, with a maximum error of 2 seconds in a 3 hour period.

3.8.2. Procedure

Since the weight per unit volume of a drained product is often similar to that of the packaging liquid which is drained off, an "estimated gross weight" cannot be used in checking packages of this type. The entire sample must be opened. The following procedure is based upon a test method established by the Food and Drug Administration⁶.

This procedure does not follow the steps outlined in any of the decision charts.

- 4. See Section 3.5., steps 1 through 4 for instructions on filling out the report form and selecting the sample. The tare sample is not needed because all the packages in the sample will be opened.
- Determine the weight of the receiving pan and record it in Block A of the worksheet.
- Determine and record the gross weight of each individual package of the sample (on the worksheet in Block A).
- 7. Pour the contents of the first package into the dry sieve with the receiving pan beneath it, incline sieve to 17-20° angle to facilitate drainage, and allow the product to drain into receiving pan for 2 minutes (do not shake or shift material on the sieve). Remove sieve and product.
- Weigh the receiving pan, liquid, wet container, and any other tare material. (Do not include sieve and product.)
 See Figure 3-5. Record this weight in Block A of the worksheet under "tare."



- Figure 3-5. The determination of tare for packages labeled by drained weight (example: olives).
- Subtract the weight of the receiving pan, step 5, from the weight obtained in step 8 to obtain the tare weight (which includes the weight of the liquid). Record this tare in Block A of the worksheet under "corrected tare".
- 10. Subtract the tare weight, found in step 9, from the appropriate package gross weight, step 6, to obtain the net weight of that package. Record the net weights in Block A of the worksheet under "net or drained".
- Repeat steps 7 through 10 for the remaining packages of the sample, cleaning and drying the sieve and receiving pan between measurements on each package.
- 12. Determine and record the individual package errors on the worksheet and transfer them to the report form (using an appropriate unit of measure in box 4).
- Go to step 16 of Section 3.5. for the determination of lot conformance or nonconformance.

3.9. AEROSOL PACKAGES

The testing of aerosol packaged products is described in the following sections. After

⁶See Method 32.002 of the Official Methods of Analysis of the Association of Official Analytical Chemists.

a list of equipment (Section 3.9.1.) and a description of the assembly of a portable test stand used when emptying the containers, (Section 3.9.2.), the details of the net contents determination are described in Sections 3.9.3. and 3.9.5. Methods for emptying the aerosol containers are given in Section 3.9.4. Test allowances to be applied to the average tare weight or individual tare weights of foam aerosols are given in Section 3.9.6.

3.9.1. Equipment

<u>Scales and weights</u> recommended in Section 3.1. are suitable for weight determinations.

<u>Portable test stand</u> with adjustable valve depressor is assembled by the testing agency from components available from a scientific supply company and hardware store. The components are:

- support stand,
- utility clamp,
- gasoline can,
- two dishpans, and
- ^o <u>1/2-inch carriage bolt</u> (either 2 to 3 inches or 5 to 7 centimeters long) and <u>nut</u>.

3.9.2. Preparation for Test

To assemble the stand for foam and most other aerosol packages, thread the carriage bolt into the nut and use the jaws of the utility clamp to grip the nut tightly. Then mount the clamp on the rod of the support stand. See Figure 3-6.

Adjust the height of the clamp to the height of the container under test and thread the carriage bolt to depress the aerosol valve until maximum flow of product is obtained.

Use the dishpans to collect the expelled product.

Add the support plate and gasoline can to the stand for aerosol products such as paints and coatings (as shown in Figure 3-7). Adjust the support plate so that the orifice of the spray can is lined up with the intake of the gasoline can. Leave the vent on the gasoline can open and clear. The clamp and valve-depression adjustment is made in the same manner as with the other aerosol products.



Figure 3-6. Portable test stand for all aerosol products except paints and coatings.



Figure 3-7. Portable test stand for aerosol paints and coatings.

Unlike conventional standard-pack packages, aerosol packages cannot be opened. Instructions on the container specifically state:

<u>Caution</u>: Contents under pressure--do not puncture.

WARNING: The containers of packaged aerosol products are under pressure and should not be punctured, broken, or subjected to temperatures in excess of 120 °F. The fumes and suspension of finely divided product may be toxic, irritating, and flammable.

Therefore, the exhausting procedure described in Section 3.9.4. should be conducted in a well ventilated area, under an exhaust hood, or outdoors, at least 50 feet from any source of open flame or spark. No smoking should be permitted in the test area.

Use the test stand equipped with the adjustable valve-button depressor for exhausting the container. Place the test stand in a plastic dishpan with another dishpan in an inverted position over the test stand to minimize pollution of the air with the sprayed product during the exhausting procedure. Use the gasoline can as a receiving vessel for paint and coating products. (See Figure 3-7).

3.9.3. The Determination of Net Contents: Part 1

All aerosol packaged products (except refrigerated products) should be checked at a product temperature of 68 °F (20 °C). All refrigerated products should be checked at product temperatures of 40 °F (4 °C). Lower temperatures will require applications of a correction because less product will be expelled at lower temperatures. For practicality, testing at a 68 to 80 °F (20 to 27 °C) range is suggested for nonrefrigerated products and 40 to 45 °F (4 to 7 °C) for refrigerated aerosols. The temperature ranges have been selected as being representative of the temperatures at which the products are normally used.

Since it is not practicable to have a single test procedure covering every product or brand, the products are broken down into two general categories, each category having similar properties. The categories of aerosol packaged products are: (1) foam products and (2) other products. Examples of products in each of the two categories are listed in each section.

The foam products category is the only category with a set of test allowances that are added to the delivered weight⁷. The allowance is made to compensate for differences in delivery between normal consumer usage and the exhausting procedure for compliance testing. Within the foam category, however, there will be some products that will deliver more completely than others. Thus, it is conceivable that a foam aerosol packaged product could deliver the stated quantity within the limits of the test allowance, and yet be short filled on a dry tare basis. It is emphasized that the test allowance should not be used by the packager as justification for packing less than the stated quantity on a dry tare basis.

Regulations under the Fair Packaging and Labeling Act⁸, require that in the case of packages designed to deliver the product under pressure "...the declaration shall state the net quantity of the commodity when the instructions for use as shown on the container are followed. The propellant is included in the net quantity statement."

The procedures presented below may be used for checking aerosol net contents when labeled by weight.

- 4. Follow Section 3.5., steps 1 through 4 for instructions in filling out the report form and selecting the random sample. As explained in Appendix C.6.1., the random sample should be arranged in the order in which the random numbers were selected. This will be the order in which the packages will be opened for tare. Consult Table 2-6 for the size of the initial tare sample.
- Gross weigh each package in the sample and record this weight on the worksheet in Block A under "gross." Follow Section 3.9.4. to empty the initial tare sample aerosol containers.

^{&#}x27;In the testing procedure, the test allowance is subtracted from the tare, the effect of which is the same as adding the test allowance to the delivered weight.

⁸Regulations under the Fair Packaging and Labeling Act (PL 89-755) include 16 CFR §500.22(a), 21 CFR §701.13(g)(1), 21 CFR §201.62(f), 21 CFR §101.105(g). Also see the National Conference on Weights and Measures Model State Packaging and Labeling Regulation (Section 10.3) in NBS Handbook 130. Quotation above from NBS Handbook 130.

After following Section 3.9.4., go on to Section 3.9.5. for instructions on completing the procedure.

3.9.4. Exhausting the Aerosol Container

Follow the procedures below to empty aerosol containers and thereby determine their tare.

Do not shake unless shaking is specified. If shaking is specified, shake according to directions on the container. If no directions as to how the can should be shaken are given, shake the container with a brisk wrist-twisting motion for one minute at the approximate rate of two wrist-twisting cycles per second. If the container has a ball agitator, continue shaking procedure for one minute after the ball has shaken loose.

a. Foam products:⁹ Placing the container in the position specified in the instructions on the package, exhaust the selected containers by holding the valve wide open for 30 minutes. (See Figures 3-8 and 3-9).



Figure 3-9. Portable test stand showing aerosol foam product expelling in inverted position.



Figure 3-8. Portable test stand showing aerosol foam product expelling in upright position.

⁹A foam product is defined as a product that forms a foam at the container valve or on impingement with a surface and the foam volume is not substantially reduced for at least 20 seconds. Examples of foam products: shave creams, hand creams, facial foams, shampoos, oven cleaners, upholstery cleaners, foam degreasers, whipped toppings, frosted whips.

b.

Other products: ¹⁰ If shaking is specified in the instructions, shake at periodic intervals (at least two or three times during expulsion of the product.) With the container in the position specified on the package, exhaust the sample container by depressing the valve-actuator until the visible spray is interrupted. As soon as the spray is interrupted, release the actuator. (A change in sound usually accompanies spray interruption.) Allow the container to warm to 68 to 80 °F (20 to 27 °C) before concluding the evacuation. Agitate the container with a swirling motion for 30 seconds. Hold the container upright at approximately a 45 degree angle, with the valve-actuator depressed, and rotate the container to maintain a visible spray (again, note the sound change) as long as possible. (Rotating will ensure contact of the dip tube with any remaining product in the container.) Continue this procedure until no additional product or gas is expelled. Any undelivered product should be expelled as completely as possible by holding the container in the hand with the valve-actuator depressed and alternately inverting the container and then restoring to the original test position at approximately 10-second intervals until no additional product is delivered.

When exhausting containers with vapor tap valves (in which product continues to be expelled upon inversion of container), stop the exhausting procedure when the container becomes cold to the hand. Allow the container to return to test temperature of 68 to 80 °F (20 to 27 °C) before proceeding with test.

A container with a metered valve cannot be emptied by holding the valve-actuator depressed since such a valve permits only a predetermined amount of product to be expelled each time the valveactuator is depressed. Empty the container by alternately depressing and releasing the valve-actuator until no additional product or gas is expelled.

- 3.9.5. The Determination of Net Contents: Part 2.
- 6. Rinse with a suitable solvent and dry the exteriors of the containers. If the valve-actuators are removable, remove for cleaning and drying, and then replace. Determine the tare weights of the initial tare sample. Record on Block A of the worksheet. For foam product aerosols, an individual package net weight is equal to the package gross weight minus the individual tare weight plus the test allowance (See Section 3.9.6.).

For other aerosols, an individual package net weight is equal to the package gross weight minus the package tare weight. Determine and record the individual package errors for the tare sample. (Package error is equal to package net weight minus the labeled weight.)

- Determine the range of tare weights, R_t, and record in box 1 of Block A on the worksheet.
- Determine and record the range of package errors, R_c, in box 2 of Block A on the worksheet.
- 9. Compute R_c/R_t and from Table 2-7, look up the total number of packages necessary for determining the tare; record n_t in box 4 of Block A of the worksheet and in box 3 of the report form.
- 10. If n_t is larger than the initial tare sample, select additional tare sample packages (those packages arranged in steps 1 through 4 of Section 3.9.3. corresponding to the order in which the random numbers were obtained). It may be necessary to empty all the packages in the sample.
- 11. Gross weigh, empty, and determine the tare¹¹ and package errors for additional packages selected in step 10. Record in Block A of the worksheet.

¹⁰Examples of other products: Frostings, syrups, cheese spread, hair sprays, colognes, window cleaners, starches and material finishes, insecticides, room deodorants, deodorants (personal), waterproofers, mothproofers, antiseptics and medicants, de-icers, ignition sprays, insect repellants, furniture polishes, dog and pet sprays, oil sprays, battery cleaners, shoe polishes and leather conditioners, wall cleaners, suntan lotions, spray-on bandages, runstoppers, pre-shave lotions, nasal relief sprays, external analgesics, charcoal lighters, fire extinguishers, anti-static sprays, carburetor cleaners, plant foods, auto quick start sprays, whitewall tire cleaners, paints, enamels, lacquers, acrylic coatings, varnishes, undercoatings.

12. If all the packages in the sample have been emptied, go to step 16 of Section 3.5. to determine lot conformance. If unopened packages remain in the sample, average the tare weights¹¹, record the average tare or corrected tare in box 5 of Block A on the worksheet, and go to step 14 of Section 3.5. to determine lot conformance.

3.9.6. Test Allowances for Foam Product Aerosols

Table 3-2 lists the test allowances to be subtracted from the average tare weight or individual package tare weight for foam product aerosols only. Block A of the worksheet has space for recording this allowance in units of weight. Record the test allowance in dimensionless units in box 9 of the report form. Record the corrected tare or corrected average tare (equal to the tare minus the test allowance) in Block A of the worksheet. If corrected average tare is used, record it in dimensionless units on the report form in box 10. If all the sample packages have been exhausted for tare, note this on the report form and

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refer to the worksheet. When packages in the sample are exhausted for tare determination, the test allowance is applied to each actual tare before determination of the net weight of each package.

3.10. SPECIAL COMMODITY: FROZEN FOOD AND OTHER FROZEN PRODUCTS

The complications of tare determination and, in certain instances, of net weight determination of products which must be maintained at low temperature in order to keep them frozen arise because of the difficulties of separating, while still frozen, the contents from the package, and because of the presence of superfluous ice and frost. The gross weight and tare weight of many products can be determined in a frozen state by simply brushing frost and ice off the exterior of the package. This is often sufficient for most frozen prepared vegetables, fruits, and many convenience items. Although surface defrosting poultry has been used in order to remove the bird from its wrapping, and thus measure the tare, this method should be used with great caution since surface discoloration occurs

Table	3-2	Test	allowances	for	foam	products
IdDIE	J <u></u>	1636	arrowances	101	roam	produces

Avoirdupois:								
Labeled weight of package	Test allowance							
	Ounce	Pound						
0 to less than 1 1/2 oz 1 1/2 oz to less than 5 oz 5 oz to less than 8 oz 8 oz to less than 11 oz 11 oz to less than 14 oz 14 oz to less than 1 lb 1 oz 1 lb 1 oz or more	0 1/16 1/8 3/16 1/4 5/16 3/8	0 0.004 0.008 0.012 0.016 0.020 0.023						
Metric:								
	Test allowance							
Labeled weight of package	Grams							
0 to less than 50 g 50 g to less than 100 g 100 g to less than 200 g 200 g to less than 300 g 300 g to less than 400 g 400 g to less than 500 g 0ver 500 g	0 1 3 5 7 9 10							

¹¹Apply test allowance given in Section 3.9.6. if foam product aerosol is being tested.

upon refreezing. Therefore, such packages chosen for tare determination should be used or disposed of as other than fresh or frozen food. (From the viewpoint of health, the surface defrosting method is acceptable.) However, if a U.S. Department of Agriculture seal is on the label, once the package is opened, the seal must be removed upon repackaging.

Frost found on the interior of frozen food packages should be considered part of the net contents, not part of the tare. In instances such as described above, the procedure to be followed for frozen foods labeled by weight are those given in Section 3.5. or 3.6.

A regulatory agency may define the labeled weight of a particular frozen product as the weight of that solid or semisolid material determined after defrosting; in such case, the procedures in Section 3.11. are followed.

3.11. SPECIAL COMMODITY: DRAINED WEIGHT OF FROZEN FOODS

The following technique is based upon but not identical with Method 22.005 of the Official Methods of Analysis of the Association of Official Analytical Chemists.

It is a "drained weight" procedure, and as such does not infer net weight from the package gross weight minus tare weight. The measurement is of the actual weight of defrosted product. As such, the method requires the defrosting of all packages comprising the sample. Since loss of quality, texture, and moisture will result if the product is refrozen, in general, the packages in the sample should not be refrozen after the test.

3.11.1. Equipment

 $\frac{\text{Scales and weights}}{3.1.}$ recommended in Section

Sieves

- ^o For labeled weight of 3 lb (1.36 kg) or less, one 8-in (20-cm) No. 8 mesh U.S. Standard Sieve Series stainless steel sieve and receiving pan.
- ^o For labeled weight greater than 3 lb (1.36 kg), one 12-in (30-cm) sieve, same specifications as above.

<u>Stopwatch</u> - mechanical or electronic, with a maximum error of 2 seconds in a 3 hour period.

<u>4-gallon or larger container</u> with bottom inlet for a hose attachment and either a screen covered outlet on the upper part of the wall of the container or a wire mesh basket, which extends above the container.

Partial immersion thermometer with -30 to 120 °F (-35 to +50 °C) range, 2 °F (1 °C) graduations, tolerance of ± 2 °F (± 1 °C).

3.11.2. Procedure

The procedure does not follow the steps given in the decision charts.

- 4. See Section 3.5., steps 1 through 4 for instructions on filling out the report form and selecting the sample. A tare sample is not needed.
- Weigh the sieve and receiving pan. The receiving pan and sieve weight is recorded on the lower portion of the worksheet in Block A and under the column headed "tare".
- 6. If the sample packages are not water tight, the packages should each be placed in a plastic bag. While the plastic bag is being tied off, force excess air out of the bag by submerging it in water to a point above the location at which the bag is being tied off.

Completely submerge the bag in a container of water using clamps or weights to keep them submerged. Maintain the water at 68 ± 4 °F (20 ± 2 °C) by introducing water at this temperature at the bottom of the container at a flow rate of 1 to 3 gallons per minute. Avoid agitating the package.

- 7. As soon as the product thaws, as determined by loss of rigidity, remove each bag from the bath and open it with a minimum of agitation. With screen tilted at about 20° from the horizontal and supported for drainage, distribute the package contents over the screen in one sweeping motion. Let the product drain into a waste receptacle or sink.
- 8. Two minutes from the time the product was placed on the sieve, place the

product and sieve on receiving pan and weigh. Record this weight in Block A of the worksheet under "gross."

- 9. The weight determined in step 8 minus the weight of the empty sieve and receiving pan is the drained weight of the product (and may be recorded in Block A of the worksheet under "net or drained"). The package error equals the drained weight minus the labeled weight and may be recorded on the worksheet and transferred to the report form.
- Clean and dry the sieve and receiving pan and repeat steps 6 through 9 for the remaining packages in the sample.
- Go to Step 16 of Section 3.5. for the determination of lot conformance or nonconformance.
 - 3.12. SPECIAL COMMODITY: GLAZED RAW SEAFOOD AND FISH

The National Marine Fisheries Service of the U.S. Department of Commerce recommends that Method 18.001 (a) of the Official Methods of Analysis of the Association of Official Analytical Chemists be used for glazed raw seafood and fish. This method requires removal of the glaze before the product is weighed.

The method may be used for any frozen glazed food product.

3.12.1. Equipment

For equipment requirements, see Section 3.11.1. except:

- 8-in (20-cm) sieve is used for labeled weights of 2 lb (0.9 kg) or less.
- 12-in (30-cm) siève is used for labeled weights greater than 2 lb (0.9 kg).

3.12.2. Procedure

The method does not follow the steps outlined in the decision charts.

- 4. See Section 3.5., steps 1 through 4 for instructions on filling out the report form and selecting the random sample. A tare sample is not needed.
- 5. Weigh sieve and receiving pan. Record this weight in the lower portion of Block A of the worksheet and under the column headed "tare."

- 6. Remove each package from low temperature storage, open it immediately, and place the contents under a gentle spray of cold water. Agitate the product carefully so product is not broken. Continue the spray until all ice glaze that can be seen or felt is removed.
- Transfer the product to the weighed sieve. Without shifting product, incline the sieve to an angle of 17-20° to facilitate drainage and drain exactly 2 minutes (into waste receptacle or sink).
- Place the product and sieve on the receiving pan and weigh. Record this weight in Block A of the worksheet under "gross."
- 9. The drained weight of product is equal to the weight of pan plus sieve plus product (recorded in the gross weight column) minus the weight of pan plus sieve (recorded in tare column). The product drained weight is recorded in the "net or drained" column of Block A on the worksheet. The package error is equal to the drained weight of the product as measured minus the labeled weight. The package error is recorded on the worksheet and transferred (using an appropriate unit of measure) to the report form.
- Repeat steps 6 through 9 for each package in the sample, cleaning and drying the sieve and receiving pan between each package measurement.
- 11. Go to Step 16 of Section 3.5. to determine lot conformance.

3.13. SPECIAL COMMODITY: CANNED COFFEE

It should be noted that the variation in weight of the metal cans used to package ground coffee can often be substantial in comparison with the weight variation of the coffee itself; therefore, the alternative tare procedure of Section 2.11.4. may be necessary.

The gross weight of vacuum packed coffee before breaking the vacuum seal will be lighter than the gross weight after breaking the seal and allowing air to enter the can. This difference in weight will be measurable using the recommended small capacity scale for two and three pound canned coffee. (The gross weight difference for 1 lb coffee is about 1/2 g.)
The checking procedure follows Section 3.5. In step 5 of Section 3.5., the official can correct for the gross weight determined from unopened cans in the following way.

Using the tare sample packages, the official should gross weigh each of the productfilled cans before and after breaking the vacuum seal. Add to the column headed "gross", the heading "sealed" and record the gross weight before breaking the vacuum seal in this column. Cross through the column heading "MAV (Random Pack)", label the heading "gross after breaking seal", and record the gross weight after breaking the vacuum seal in this column. Compute the average weight difference (open weight minus sealed weight). Record the average gross weight difference in the column headed "corrected tare" (cross through heading and fill in "gross weight difference").

The average weight difference is then subtracted from the average tare so that the nominal gross weight to be used in step 14 of Section 3.5. is equal to: the average tare weight minus(-) the average difference in gross weights plus(+) the labeled weight. Record the average tare minus the average difference in gross weights in box 5 of Block A of the worksheet (change heading to "corrected average tare"). For example:

- (i) The gross weight of an unopened 3 lb can of coffee is 3.719 lb.
- (ii) The gross weight of this same opened 3 lb can of coffee is 3.723 lb.

The difference between (i) and (ii) is 0.004 lb.

This difference and the other determination of the gross weight difference are averaged; 0.004 lb is found as the average value.

Therefore, 0.004 lb is, in this example, subtracted from the average tare weight (or individual tare weights in order to determine the package errors of the tare sample packages). This corrected average tare weight plus the labeled weight represents the nominal gross weight which will be compared with the unopened packages in the sample to determine their package errors.

Section 3.5. Step 14 onward is then followed to determine lot conformance.

CHAPTER 4. METHODS OF TEST FOR PACKAGES LABELED BY VOLUME

- 4.1. MEASURING LIQUID VOLUMES
- 4.2. EQUIPMENT FOR LIQUID VOLUME DETERMINATIONS
- 4.3. USING LIQUID VOLUME MEASURES
- 4.4. STANDARD PACK LIQUIDS LABELED BY LIQUID VOLUME: GENERAL METHOD, PART 1, MEASURING THE WEIGHT OF A KNOWN VOLUME
- 4.5. STANDARD PACK LIQUIDS LABELED BY LIQUID VOLUME: GENERAL METHOD, PART 2, USING THE WEIGHT OF THE LABELED VOLUME
- 4.6. OTHER METHODS OF LIQUID VOLUME MEASUREMENT
- 4.7. SPECIAL COMMODITY: MILK
- 4.8. SPECIAL COMMODITY: MAYONNAISE & SALAD DRESSING
- 4.9. SPECIAL COMMODITY: PAINT, VARNISH, AND LACQUERS -NONAEROSOL
- 4.10. SPECIAL COMMODITY: VERY VISCOUS MATERIALS
- 4.11. SPECIAL COMMODITY: PEAT MOSS
- 4.12. SPECIAL COMMODITY: SOLIDS OR SEMISOLIDS
- 4.13. SPECIAL COMMODITY: GOODS LABELED BY CAPACITY

This chapter first presents information on general problems and practices in measuring liquid volumes. The general procedure is broken into two sections. Tests are carried out to check the suitability of weighing the net contents of packages labeled by volume in the first section (4.4.). If weighing is found to be suitable, the second section (4.5.) is followed; this section describes a method which references techniques already covered in Section 3.5. The next section (4.6.) describes methods for use when weighing cannot be employed to check packages labeled by volume. Finally, methods for special types of commodities are described in the remainder of the chapter. Packages labeled by dry volume or cubic measure are included in this category.

Many of the procedures in this chapter are presented as modifications of that given in Section 3.5. Decision Chart 4 is provided as an outline for checking packages labeled by any quantity other than weight; this chart will be followed in parts of Chapter 5 as well.

Steps 1 through 4 in the procedures are not described in any detail in this chapter. The testing official is referred to steps 1 through 4 in Section 3.5. for a more complete description.

It should be noted that certain packages labeled by volume utilize containers which are required by law or regulation to hold certain specified quantities (liquid or dry volume). These quantitative measuring containers include berry baskets and boxes, rigid dry measures, retail and prepackaged measure containers (such as ice cream containers), milk bottles, and lubricating oil bottles, and as such are covered by specific code requirements in NBS Handbook 44. This handbook does not describe the testing of the capacities of these containers. Containers in which such products as cottage cheese, sour cream, and yogurt are packaged may be tested using the techniques of Section 4.13.

4.1. MEASURING LIQUID VOLUMES

The volume which is occupied by a packaged product of any kind varies with the temperature of the product. This fact must be kept in mind when checking products labeled by liquid volume (and can be ignored when checking products labeled by dry volume.) For example, the volume of a certain liquid cosmetic product is 500 mL at 20 °C (68 °F) and 503 mL at 25 °C (77 °F). Therefore, a reference temperature is usually specified in regulations for products sold by liquid volume. The reference temperature at which the volume is required to comply with the regulation.

In general, the reference temperature is that temperature at which the product is customarily sold. For frozen foods labeled by liquid volume (e.g., fruit juices, batters, etc.), packagers routinely recommend a maximum storage temperature of 0 °F $(-17.8 \ ^{\circ}C)^{1}$. For refrigerated foods, the reference temperature is 40 °F $(4.4 \ ^{\circ}C)^{2}$. The reference temperature for all petroleum products is 60 °F $(15 \ ^{\circ}C)^{3}$. For products sold unrefrigerated, the reference temperature is generally accepted as 68 °F $(20 \ ^{\circ}C)^{4}$.

The following discussion applies to packaged products which are liquids at their reference temperature (either 40 °F, 60 °F, or 68 °F).

Whenever the liquid volume of a product is measured, the product temperature must be measured and controlled.

Since many liquid products have a high water content, the following information on water will guide the testing official in a rough manner as to the errors that can

¹Frozen products labeled by liquid volume should be checked at the packaging plant. Those products with a high water content have a minimum volume at about 40 °F (4 °C) and a larger volume at 0 °F (-18 °C) (than their volume at 40 °F (4 °C)).
²21 CFR §101.105(b) (ii).
³16 CFR §500.8(b).
⁴16 CFR §500.8(b); 21 CFR §101.105(b) (iii); 40 CFR §162.10(2); 21 CFR §201.62(b); 21 CFR §701.13(b).

arise with variation in temperature and its effect on volume or on the weight of a known volume. For example,

1 gallon of water at 40 °F (4.4 °C)
occupies:
 1 gal + 0.28 fl dr at 50 °F (10 °C),
 (this corresponds to about 1/4 to
 1/3 of a graduation on the neck of
 a one-gallon glass volumetric con tainer);
 1 gal + 0.9 fl dr at 60 °F (15.6 °C);
 1 gal + 1.25 fl dr at 70 °F (21.1 °C).
In the same way, 1 gallon of water would

weigh about
 8.336 lb⁵ at 40 °F (4.4 °C),
 8.334 lb at 50 °F (10 °C),
 8.328 lb at 60 °F(15.6 °C) and
 8.320 lb at 70 °F (21.1 °C).

These data suggest that the errors, although small, are detectable with the equipment recommended in this handbook. Moreover, if volumes are determined at temperatures higher than the reference, the results will systematically indicate a volume larger than actually existing at the reference temperature.

It is good practice to equilibrate the volumetric glassware to the same temperature as the liquid product. (The normal expansion or contraction of the glassware may be ignored by the testing official; however, he or she must never expose the glassware to a direct source of heat such as a flame.) For example, the official may put the flask to be used for checking milk in the cooler with the milk for about a half hour before checking the packages.

It is also important to maintain the packaged goods which comprise the sample all at the same temperature. As will be described in Section 4.4., the testing official will deliver a certain known volume of product from one package and weigh it. Having repeated this procedure on a second package, the official will compare the weights of the two volumes in order to determine whether he or she can weigh the rest of the packages in the sample and avoid opening these packages. Since the weight of a fixed volume of liquid will vary with the temperature, the official must determine the weights of the two volumes at the same temperature⁶. Again, using the example of water, 1 gallon of water at 68 °C weighs 8.322 lb but at 70 °C weighs 8.320 lb.

As described in Section 4.4., if a difference of more than 0.004 lb is found between the weights of a known volume from two packages (using the equal arm scale for larger weights), weighing cannot be used to check the package net contents. For the example of water given above, the 2 °F difference in product temperature is enough to account for a 0.002 lb difference in the weight of one gallon.

Measurements of product volumes at lower than the reference temperature normally will require the application of a density correction. Unless this correction is known, the official should measure the volumes or weights of a known volume of packaged products at or higher than the reference temperature.

4.2. EQUIPMENT FOR LIQUID VOLUME DETERMINATIONS

<u>Scales and weights</u> recommended in Section 3.1. are suitable for the determination of the weight of a known volume.

Volumetric Measures - Measures specifically designed for package checking purposes may be used in making fluid volumetric determinations (see Figure 4-1). Standard measuring flasks and graduates recommended for use on packages labeled in inch-pound units are the gill, half pint, pint, quart, half gallon, and gallon. In addition, a 2 fluidounce cylindrical graduate, graduated to 1/2 fluid-dram is recommended. When checking packages labeled in metric units. flask sizes of 100 milliliters, 200 milliliters⁷, 500 milliliters, 1000 milliliters, 2000 milliliters, and 5000 milliliters and a 50-milliliter cylindrical graduate, graduated to 1 milliliter should be used.

⁵Weighed in air.

⁶Alternatively, an agency may develop (or obtain from the packager) tables or formulae of volume/temperature variations which could be used to correct individual measurements to volume at the same temperature.

⁷250-milliliter flasks may also be used.

Tolerances for inch-pound and metric field standard flasks and cylinders are given in Appendix G^8 .

If pesticides, herbicides, or similar products are to be tested, a separate set of volumetric measures should be clearly marked and reserved for such purpose. Detergent washing of each set of volumetric measures between tests will then be adequate for field care and use. If contamination of volumetric measures is suspected, they can be cleaned with a potassium dichromate and sulfuric acid solution in a laboratory, not in the field.



Figure 4-1. Standard measuring flask and graduate for testing packages labeled in metric units of volume.

<u>Partial immersion thermometer</u> with a range of -30 to 120 °F (-35 to +50 °C), at least 1 °F (1 °C) graduations, and with a tolerance of ± 2 °F (± 1 °C). <u>Defoaming agents</u> may be necessary when checking liquid commodities that effervesce or are carbonated, such as beer and soft drinks. Three such products are:

- Hexanol
- Octanol, (Capryl Alcohol), purified
- Antifoam B⁹
 Dow-Corning Corporation
 Midland, Michigan

The use of these defoaming agents renders the liquid commodities unfit for human consumption.

Bubble level.

4.3. USING LIQUID VOLUMETRIC MEASURES

There are two ways volumetric flasks will be used in checking liquid products. (i) A certain amount of product (not the entire package contents) will be poured into a flask exactly to a certain mark on the neck of the flask (and weighed). For example, the weight of the labeled volume of a package labeled as 32 fluid ounces may be measured by weighing the contents of a pint flask filled with liquid product. (ii) The entire package contents will be poured into a flask or flasks. The liquid volume is measured by comparing the liquid level with the graduations on the neck.

Because of surface tension, the liquid surface is curved near the junction of glass and liquid. Therefore, the center of the liquid level is compared to the graduation marks with the inspector's eye level at the same level as the liquid surface. For liquids which are clear, the bottom of the liquid surface (which will appear to have some thickness) is matched to or compared with a graduation mark; for liquids which are opaque, the center of the top rim of the liquid surface is the point to be set or to which comparison is made. See Figure 4-2.

⁸It is possible to obtain from the flask manufacturer standard measuring flasks with extended graduations on their necks (rather than those listed in Appendix G, Table G-2). These graduations can extend to the maximum allowable variatons for packages labeled by volume (e.g., for the half pint, graduations down to 3 drams below the half pint mark may be specified for purchase).

⁹The use of trade or brand names does not imply that they are endorsed or recommended by the Department of Commerce over other firms not mentioned.



Figure 4-2. Reading the liquid level on the neck of a flask.

Of course, the flasks should be read on a level surface (a bubble level may be used to verify this).

For fluid volume measurements, the size of the volumetric flask to be used in any determination will depend on the labeled volume of the package. Even though packages may be labeled with a volume identical to the testing official's flask capacity, the actual volume contained in or delivered from any individual package may be less than the minimum mark inscribed on the inspector's flask. Since it is very important to never mix liquids from two different packages, the official should use the flask sized closest to but smaller than the labeled volume for the determination of the weight of a known volume¹⁰. (See Section 4.7. for an exception.)

Immediately prior to use, the volumetric flask(s) or graduate should be filled with water¹¹ to a point slightly below the top graduation on the neck. The flask should be emptied in 30 seconds, by gradually inclining the flask so as to avoid splashing the flask walls as much as possible. When the main flow has ceased, the flask should be nearly vertical. Hold the flask in this position 30 seconds more and touch off the drop of water that adheres to the tip. The flask or graduate is then ready to accept product liquid from a package. This is called the "wet-down" condition. The flask should be washed (with detergent if necessary) and rinsed between deliveries of liquid product from each package. The flask must be wet and drained as described each time it is to be used.

Immerse the thermometer suggested in the equipment section only 76 mm (3 in) into the liquid product. Measure the product temperature immediately after weighing the flask and product.

4.4. STANDARD PACK LIQUIDS LABELED BY LIQUID VOLUME: GENERAL METHOD, PART 1, MEASURING THE WEIGHT OF A KNOWN VOLUME

In order to avoid opening all of the packages comprising the sample and because measurements of volume are generally less precise than measurements of weight, the preferred method (described in this section and in 4.5.) involves a determination of the weight of a known volume that, together with a determination of tare, can be compared against the gross weight of the unopened packages. A decision chart (Chart 4) is provided that lists steps in the procedure for all packages labeled in units other than weight, including those labeled by volume.

The procedure is divided into two sections. In this section a check for the variability of the weight of a known volume is described. This procedure verifies whether a weighing procedure is suitable. If a weighing procedure can be used, the next section (4.5.) describes the use of a weight value for a known volume of product to determine package errors.

Most common consumer products labeled by liquid volume (food, cosmetics, cleaning fluids, and over-the-counter drugs) weigh from about 0.05 lb/fl oz (0.8 g/mL) to greater than 0.07 lb/fl oz (1.1 g/mL). This fact permits the testing official to refer to a list of appropriate weighing devices to use to check these products and thereby skip the step which checks that the scale can detect weights equivalent to MAV/6.

¹⁰The minimum mark on the graduated neck of standard flasks currently in use for package checking does not extend to the MAV limits described in Table 2-9. Therefore, it may be necessary for the official to use smaller flasks in combination with a cylinder to determine a package volume directly, that is, by delivering the contents into volumetric containers (method ii of this section).

¹¹The water should be at the temperature of the product.

Decision Chart 4 Packages Labeled in Units Other than Weight Category A or B

(1) Fill out report form heading, including MAV (6) (Table 2-9, 2-10, or 2-11)

(2) Determine inspection lot size, record lot size, (1) and allowed number of unreasonable errors (13) (Table 2-2 or 2-5) (3) Record sample size, n, (2), and tare sample size, n, (3) (Table 2-2 or 2-5) (Tare sample may be initial tare sample if alternative tare procedure is used - See Tables 2-6 and 2-7.) (4) Choose random sample and from it, the tare sample (5) Gross weigh individual packages in tare sample A (6) Determine the weight of a known quantity of product from the first package of tare sample B1 IS PACKAGE LABEL LIQUID VOLUME AND IS PRODUCT WT/VOL > 0.05 lb/fl oz(0.8 g/ml)? NO YES (7) Calculate or determine weight of quantity corresponding to $\frac{MAV}{6}$ B3 IS WEIGHT OF MAV AS LARGE OR LARGER THAN SCALE USED TO WEIGH CAN DETECT? YES NO (8) Determine the tare of the first package A (11) Open and determine actual quantity inside every package (9) Determine the weight of a known quantity in sample and record package of product from second package of tare sample B2 errors for entire sample. (10) IS RANGE OF WEIGHTS OF KNOWN QUANTITY FROM THE TWO PACKAGES EQUAL TO OR GO TO STEP (16), NO SMALLER THAN TABLE 4-2 VALUE? B4a or b Chart 1 (Category A) or YES Chart 2 (Category B) (11) Calculate the average weight of the labeled quantity B5a or b IS TARE GLASS OR AEROSOL, OR IS ALTERNATIVE TARE PROCEDURE TO BE USED? YES NO (12) Determine tare for the rest of tare sample and average the tare A GO TO Determine and record package errors for tare sample Chart 3, Step (6b) or (13) Calculate the nominal gross weight (= weight of labeled quantity + tare weight)B6 (iii) (14) Convert MAV to units of weight B7 (5) GO TO STEP (15) Chart 1 or 2 converting back to labeled units when completing report form Numerals in parenthesis refer to steps in Sections 4.4. and 4.5. (volume), 5.1.3. (count), 5.3.2. (linear or area measure)

Circled numbers refer to locations on the report form

Boxed letters and numbers refer to locations on the worksheet

The measurement of the weight of a known volume can be combined with the determination of tare and, therefore, will not require more packages to be opened than the number designated in column 3 of Tables 2-2 or 2-5.

If the inspection lot is composed of packages from different manufacturer's lots (they will have different lot symbols or codes on the package), it is extremely important to check the weight of a known volume from each of these different lots. It is possible that the official will find that certain lots of packages labeled by liquid volume must be sorted according to manufacturer's lot code before sampling in order to check such packages by weighing.

Since many products labeled by liquid volume are packaged in glass containers, the official should become familiar with the alternative tare procedures of Section 2.11.4. as applied to liquids. The range of net weights (R_c) is determined straightforwardly: the corresponding tare weights are subtracted from each package gross weight to give net weights for the initial tare sample (see step 11 below).

The general method for checking packages labeled by liquid volume starts with measuring the weight of a known volume of the product.

- 1. 4. See Section 3.5., steps 1 through 4 for instructions on filling out the report form and selecting the random sample and random tare sample. Record the MAV in units of volume (Table 2-9, Section 2.12.) in block 6 of the report form and the labeled volume in the report form heading. (Note that procedures in Section 2.11.4., including Tables 2-6 and 2-7, should be used for fluids packed in glass.)
- 5. Select a flask and weigh the flask in the "wet down" condition described in Section 4.3. Gross weigh individual packages in the tare sample. Record these weights in Block A of the worksheet. (The flask weight is recorded at the bottom of Block A and in column 7, Block B of the worksheet.)

If the liquid product requires mixing for uniformity, this should be done before each package is opened. If the product is of a type that effervesces or foams when opened or poured, such as beer or carbonated beverages, add one drop of a defoaming agent to the product and one drop to the bottom of the wetted flask before pouring. Open the first package selected for tare and fill the flask to the volume indication line.

6. Weigh the flask filled with product (record this weight in column 6 of Block B) and subtract the weight of the flask (step 5) to obtain the weight of the product. (See Figure 4-3). Record the weight, volume, and temperature of the contents from the first package in Block B of the worksheet under columns 1, 2, and 5. Calculate the weight of a unit of volume and record this value in column 3. The units of column 3 are weight per unit volume, as for example lb/fl oz. For another example, if 500 mL weighs 450 g, record 0.900 g/mL in column 3.



- Figure 4-3. Weighing a known volume of liquid.
- If the liquid product is a common consumer item (food, cosmetic, cleaning fluid, or over-the-counter drug), refer to Table 4-1, measure and record the liquid temperature in the flask, and go on to step 8.

If the weight of a given volume of liquid product is outside of the range 0.05 to 0.07 lb/fl oz (0.8 to 1.1 g/mL) (see column 3 in Block B of the worksheet), the following procedure is given.

Determine MAV/6 in terms of weight using either (a), which involves a manipulation of the product, or (b), which involves a calculation, to determine whether the scale is sensitive enough to detect individual package errors.

- a. Add the volume corresponding to MAV/6 (see Table 2-9 for MAV values) to the flask already filled with product and weigh again. Record this weight in column 8 of Block B of the worksheet. The weight corresponding to MAV/6 is equal to the column 8 value minus the column 6 value. This may be recorded in box 3 in Block B of the worksheet.
- b. Calculate the weight of that volume corresponding to MAV/6 from the data obtained in step 6. This calculation may be recorded in the box 3 in Block B of the worksheet.

The weight of MAV/6 as determined in either (a) or (b) must be at least as large as 1/2 the size of the smallest division on the scale used to weigh the product (or at least as large as the smallest increment in the readout if a digital scale is being used.)

If the weight difference is less than 1/2 the smallest scale division, all the packages will have to be opened and volumetric method A employed (see Section 4.6.).

In the instance of (a) above, for example, a package labeled 8 fl oz has a weight of 0.440 lb for a 4 fl oz flask filled with product to the 4 fl oz mark. The MAV for a labeled volume of 8 fl oz is 3 fl dr. After adding 0.5 fl dr more to the flask, the inspector finds the flask now weighs 0.442 lb. The difference in weight is 0.002 lb, which is equal to the smallest scale division of the small capacity equal-arm scale, thus passing the first test of determining the suitability of a gravimetric procedure.

In the instance of (b) above, for example, packages labeled "1 quart" have an MAV of 8 fl dr (1 fl oz). The weight of the liquid is determined to be 0.770 lb for 16 fl oz. Thus, MAV/6 in weight units is:

 $\frac{1 \text{ fl oz}}{6} \times \frac{0.770 \text{ lb}}{16 \text{ fl oz}} = 0.008 \text{ lb}$

In this example, assuming the inspector is using a small-capacity equal-arm scale, MAV/6 is larger than the smallest scale division, so that the next step in the gravimetric procedure may be followed.

Measure and record the temperature of the product from the first package.

- Empty clean and dry the package container. Weigh the package container and record this weight in Block A of the worksheet under the "tare" column.
- 9. Clean the flask and repeat steps 5 and 6 on the second package chosen for tare determination. Determine tare weight for this second package. Only two packages are opened for the determination of the weight of the known volume. Even if more than 2 packages are required for tare, do not determine the weight of a known volume on these other packages. Record the weight of the liquid volume from the second package, the volume, and the temperature in columns 1, 2, and 5 of Block B of the worksheet.
- In order to weigh packages labeled by volume, the two values for the weight

Labeled volume (inch-pound)	Device	Labeled volume (metric)
Up to and including	analytical or other	Up to and including
4.25 fl oz	high accuracy balance	126 mL
Greater than 4.25 fl oz	small capacity	Greater than 126 mL
to and including 32 fl oz	equal-arm scale	to and including 1 L
Greater than 32 fl oz	large capacity	Greater than 1 L
to and including 3 gal	equal-arm scale	to and including 12 L
Greater than 3 gal	commercial scale and substitution weighing	Greater than 12 L

Table 4-1. Weighing devices appropriate to use to check common consumer products labeled by liquid volume.

Type of Scale	Pounds	Grams
Analytical or other high accuracy balance		0.05
Equal arm scale for small weights	0.002	1.0
Equal arm scale for larger weights	0.004	2.0
Commercial scale up to and including 30 lb (14 kg)	0.01	5.0
Commercial scale above 30 lb (14 kg) up to and including 100 lb	0.02	9.0

Table 4-2. Permitted difference in weights of two equal quantities according to the type of scale used to weigh.

of a known volume should not differ by more than the amount given in Table 4-2. Record appropriate Table 4-2 value in box 4a on Block B of the worksheet.

For example, from a sample of ten packages labeled 1/2 gallon two packages are chosen for determination of the tares and for the determination of their weights of a known volume. The weight of a 1-quart flask plus 32 fl oz of the packaged liquid from the first package is 3.050 lb. Therefore, in order to use a weighing procedure (using a package testing scale for small weights), the weight of the 1-quart flask plus 32 fl oz of the liquid from the second package may not differ from 3.050 lb by more than 0.002 lb (that is, it may weigh 3.052 to 3.048 lb).

Record the difference between the weights of the first two packages in Block B of the worksheet in box 4a.

If the difference in weights between the determinations for the two packages meets the above criterion, then the average of the weights of the labeled volume may be used in testing the packages comprising the sample and Section 4.5. may be followed. Go on to step 11. If the difference in weights does not meet the above criterion, then volumetric measurements must be made on all the packages in the sample following one of the procedures given in Section 4.6.

11. Compute the weight of the labeled volume of the product.

The weight of the labeled volume =

average weight of known volume x labeled known volume x volume The weight of the labeled volume may be obtained by multiplying the average of the two values in column 3 of Block B on the worksheet by the labeled volume. For example, if the average of column 3 values is 0.900 g/mL and the labeled volume is 1 L, then the weight of the labeled volume is 0.900 g/mL x 1000 mL = 900 g. Note that the units of the weight of the labeled volume are units of weight only.

To avoid round-off errors as much as possible, carry over at least two extra decimal places in any calculation until the final weight of the labeled volume is obtained.

Determine tare for the rest of the tare sample.

If the alternative tare procedure of Section 2.11.4. is to be used, subtract the corresponding tare weight from each package gross weight to determine the "net weight" (record in Block A of the worksheet). Calculate R_c (which is the range of net weights), R_t (the range of tare weights), R_c/R_t , and compare with Table 2-7 to decide if more packages in the sample must be opened to determine tare. (See steps 7 through 11 of Section 3.5. for more detail.)

Record the weight of the labeled volume in box 5a, Block B, of the worksheet and in box 11 of the report form. Appropriate units of measure for common consumer products (foods, cosmetics, cleaning fluids, over-the-counter drugs) labeled by liquid volume and checked by weight are given in Table 4-3. Record the unit of measure in box 4 of the report form. Go on to Section 4.5.

Inch-Pound	Metric			
Labeled volume	Units of m (oz avoir)	neasure (1b)	Labeled volume	Units of measure (g)
Up to and including 4.25 fl oz	a	a	Up to and including 3 mL	0.01 ^a
			Greater than 3 mL to and including 126 mL	0.1 ^a
Greater than 4.25 fl oz to and including 17.00 fl oz	1/32 ^b	0.002 ^b	Greater than 126 mL to and including 503 mL	1.0 ^b
Greater than 17.00 fl oz to and including 55.00 fl oz	1/16	0.004	Greater than 503 mL to and including 2.041 L	2.0
Greater than 55.00 fl oz to and including 1.25 gal	1/8	0.01	Greater than 2.041 L to and including 5.489 L	5.0
Greater than 1.25 gal to and including 1.875 gal	1/4	0.02	Greater than 5.489 L to and including 37.5 L	10.0
Greater than 1.875 gal to and including 4.375 gal	1/2	0.03		
Greater than 4.375 gal to and including 9 gal	1	0.05		
Greater than 9 gal to and including 18 gal	2	0.1		

Table 4-3. Recommended units of measure to be used for recording the weights of packaged goods labeled by liquid volume.

^ause analytical or other high accuracy balance. ^buse package checking scale as null indicator.

4.5. STANDARD PACK LIQUIDS LABELED BY LIQUID VOLUME: GENERAL METHOD, PART 2, USING THE WEIGHT OF THE LABELED VOLUME

After the official has determined whether packages labeled by volume can be checked by weighing (as described in the previous section), he or she should complete the checking procedure on the sample as described below. The following steps are intended to lead into Section 3.5., the general method for packages labeled by weight.

12. In steps 8 and 11 of Section 4.4. the tare weights of the individual packages in the tare sample were determined. If additional tare sample packages are indicated (using the method of Section 2.11.4.), select, gross weigh, and open them, clean the containers and weigh them. Average the tare weights determined from all opened containers (unless the entire sample has been opened). Record tare weights in Block A of the worksheet under "tare" and "average tare."

13. The average tare plus the weight of the labeled volume of the product (step 11 of Section 4.4.) is equal to the nominal gross weight to be used to compare with the actual gross weights of the remaining unopened packages of the sample. (See step 14 of Section 3.5.). Record nominal gross weight in box 6, Block B of the worksheet.

> In order to determine the net volume for those packages opened for tare, divide the net weight of each package (gross weight (-) tare weight) by the weight of the labeled volume (determined in step 11 of Section 4.4.) and multiply that value by the labeled volume (carry over at least 2 extra decimal places to avoid round off errors.) For example, the net weight of a package labeled 10.5 fl oz is 0.690 lb. The weight of the labeled

volume is found to be 0.6825 lb. The net volume is:

 $\frac{0.690}{0.6825}$ \times 10.5 = 10.615 fl oz.

The package error is therefore equal to net volume minus labeled volume; in this example 10.615 fl oz - 10.5 fl oz = +0.12 fl oz (rounded).

14. Convert the MAV in units of volume (see Table 2-9) to units of weight and record it in box 7, Block B of the worksheet and in box 5 of the report form.

> Convert all measurements and comparison values to weight and to dimensionless units, and follow Section 3.5. step 15 onward, converting back to units of volume when completing the report form (box 16 and under "Remarks" section).

4.6. OTHER METHODS OF LIQUID VOLUME MEASUREMENT

If the packaged product fails either criterion in Section 4.4. (step 7 or 10), it will be necessary for the official to use one of the following methods of liquid volume measurement in this section.

All three methods require opening all of the sample packages. The methods describe how to determine an individual package error. After the package errors for all the packages have been determined, Section 3.5., step 16 onward is followed to determine conformance of the lot with the package requirements.

Method A is used if the scale cannot detect differences in weight equivalent to MAV/6 and may be used as an alternative to any other fluid measurement given here.

Method B is suitable for liquids that are homogeneous.

Method C is suitable for liquids that are not homogeneous but may be used on homogeneous liquids also.

None of the methods in the rest of this chapter follow the decision charts.

4.6.1. Method A: Determining the Volume at the Liquid Level of Fill.

When the test in step 7, Section 4.4., indicates that the scale is not sensitive

enough to detect individual package errors, the following method must be used. It is a laboratory procedure. The step numbers refer to the procedures which would follow step 7 in Section 4.4.

Equipment:

<u>Micrometer depth gage</u> (ends of rods fully rounded)¹² 0-9 in or 0-225 mm.

<u>Bubble level</u> at least 10 in or 25 cm in length.

Laboratory pipets and/or buret: Buret meeting type 1, style 1, class A, Fed Spec NNN-B-782. Pipets meeting type 1, style 1, class A, Fed Spec NNN-P-395, calibrated "to deliver".

Procedure:

- Select another package randomly to replace the package opened in steps 5 and 6 of Section 4.4. Cross out "corrected tare" and insert "depth gage" in blank space heading of column at top of Block A of the worksheet.
- Open the first package in the sample on a level surface, and use the depth gage to determine the level of fill of the package before product is removed.

Record the depth gage reading in Block A of the worksheet.

- 10. Empty, clean, and dry the package container.
- 11. Duplicate the level of fill determined in step 9 above with distilled water delivered from pipets or buret. Record the resulting water volume as the packaged goods volume in Block A of the worksheet under the column heading "net or drained" ("volume" may be added in the blank space).
- 12. Subtract the labeled volume from the package volume (step 11) to arrive at the individual package error. The labeled volume and the package error are recorded in the appropriate columns in Block A of the worksheet, and the package error transferred to the report form using an appropriate unit of measure in box 4 of the report form.
- Repeat steps 9 through 12 for each package in the sample. Follow step 16 onward of Section 3.5. to determine lot conformance.

¹²The rods will have to be custom ground.

4.6.2. Method B: Measuring a Known Volume for Every Package

The following method is suitable for liquids that are homogeneous (or can be mixed until they are homogeneous) and do not separate. Taking advantage of product homogeneity, this method uses the weight of a known volume to calculate the weight of the labeled volume. Since weighing is used to determine errors in volume, the scale must be capable of distinguishing volumes equivalent to MAV/6 (See Section 4.4., step 7.).

Equipment is the same as that listed in Section 4.2.

Section 4.4. describes the determination of the weight of a known volume of product from two packages. When the range of weights from two packages exceeds the Table 4-2 value, the method of Sections 4.4. and 4.5. may still be used as long as the weight of a known volume is determined for each and every package in the sample. The step numbers refer to the procedures which would follow step 10 in Section 4.4.

Block B of the worksheet contains enough space in it to record the individual measurements and calculations for 10 packages. Block A of the worksheet may be used to record gross and tare weights. Cross out "corrected tare" heading in Block A and fill in "weight of labeled quantity". Cross out "net or drained" and insert "pkg errors (wt)".

 Compute the weights of the labeled volume for the first two packages opened from the tare sample. Do not average the weights. Each weight is calculated, for example:

The weight of the labeled volume for package 1 =

weight of known volume x labeled volume known volume

where the weight of the known volume is that weight determined for package 1 only. Record this weight in column 4 of Block B on the worksheet and in Block A.

12. Subtract the sum of the actual tare weight (determined for the first package in step 8 and for the second package in step 9 in Section 4.4.) plus the weight of the labeled volume computed in step 11 (above) from the appropriate gross weight determined in step 5 of Section 4.4. to arrive at the individual package errors in terms of weight for the first two packages opened for tare in Section 4.4.

Package error (in units of weight) =
 (gross weight) (tare weight + weight of
 labeled volume).

The package error in units of weight may be recorded in Block A.

Calculate the package error in units of volume.

Package error (in units of volume) =
 (package error in units of weight) x
 (labeled volume/weight of labeled
 volume for each package)
and is recorded in Block A under the
column headed "package errors".

For example, the tare weight of package 1 is 0.075 lb and the weight of the labeled volume (32 fl oz) for package 1 is 2.156 lb. The gross weight of package 1 is 2.245 lb. The package error in units of weight is therefore: (2.245 lb) - (0.075 lb + 2.156 lb) =+0.014 lb. In units of volume, the package error is (+0.014 lb) x (32 fl oz)/(2.156 lb) = +0.01 fl oz.

- Gross weigh the rest of the packages comprising the sample (only the tare sample packages were weighed in step 5 of Section 4.4.).
- Determine the weight of a known volume for each package in the sample (see steps 5 and 6 of Section 4.4.).
- 15. Clean, air dry, and weigh each package container (see step 8 in section 4.4.).
- 16. Repeat steps 11 and 12 above for the entire sample.
- Record package errors on the report form (using an appropriate unit of measure in terms of volume).

Go to step 16 of Section 3.5. to determine lot conformance.

4.6.3. Method C: Measuring the Volume Delivered from the Package

The product does not have to be homogeneous to use this method, but the product should

be mixed before opening even if its components separate quickly. Oil and vinegar salad dressings are good examples of the type of product for which this method can be used. Unlike Method B, this method uses the weight of a known volume only to calculate the volume remaining in an emptied container so that any inhomogeneity of the product will not greatly affect the calculated net contents.

In steps 6 and 9 of Section 4.4., the weight of a known volume of liquid is determined for each of two packages in the sample. When it is found in step 10 that these weights differ too much from each other, the following method may be followed to determine package errors.

It will be possible to use an average weight of a known volume to determine the amount of liquid remaining in a package after delivery of the main body of liquid to volumetric flask(s) as long as the two weights determined in steps 6 and 9 of Section 4.4. do not differ by more than 5%. For example, if the weights of 8 fl oz of product were determined to be 0.496 lb for the first package and 0.484 lb for the second package, the difference, 0.012 lb, is less than 5% of the average weight, 0.490 lb. Therefore, 0.490 lb for 8 fl oz may be used to calculate the liquid volume remaining in the packages.

If the weights determined in steps 6 and 9 of Section 4.4. differ by more than 5%, the method will require both the determination of the weight of a known volume and a direct measurement of product volume delivered from the package for every package. (The results of steps 6 and 9 of Section 4.4. may be used only for the weights of a known volume for the first two packages opened for tare. The weight of a known volume will have to be determined for each package in the sample).

The volume of product remaining in an emptied container is obtained by determining the weight difference between the wet container and the container after drying (this is attributed to the weight of liquid remaining in the package container) and converting this weight to volume:

(wet tare - dry tare) x known volume weight of known volume

This resultant volume (step 15 below) is then added to the volume of product delivered (step 12 below) from the package to obtain the total product volume (step 16 below). For example, the first package was opened from a sample labeled 40 fl oz, and following Section 4.4., step 6, part of the product was poured into a 1-qt flask to the 1-qt mark.

The remaining product is now poured into a 1/2-pt flask and is found to fill the flask to 1/2 fl dr below the 8-fl oz mark.

Therefore, the volume delivered from the package is

= 32 fl oz + 8 fl oz - 1/16 fl oz = 39.9375 fl oz delivered.

The weight of the wet package container is 1.012 lb (step 12 below) and after air drying, 1.000 lb (step 13). According to procedures followed in steps 6 and 9 of Section 4.4., it was found for this first two tare sample packages that 32 fl oz weighs 2.123 lb (average weight).

Therefore, one fluid ounce weighs
 2.123 lb/32.00 fl oz = 0.06634 lb.
And,
 0.012 lb/(0.06634 lb/fl oz) =
 0.18 fl oz.
This is the volume of product remaining in

the package.

The total product volume is 39.94 fl oz + 0.18 fl oz = 40.12 fl ozThe package error is 40.12 fl oz - 40.00 fl oz = +0.12 fl oz

The step numbers below refer to procedures which follow step 10 in Section 4.4.

The equipment is the same as that listed in Section 4.2.

11. Calculate the average weight of the labeled volume as described in step 11 of Section 4.4. Divide the difference in weights for the first two package volumes (recorded in Block B of the worksheet in box 4a) by the average weight of the labeled volume (recorded in Block B, box 5a). If this ratio is 0.05 or smaller, use the average weight of the labeled volume to compute the amount of liquid remaining in the package in step 15. If this ratio is greater than 0.05, separate values for the weight of a given volume must be determined for each package in the sample to be used in step 15.

 Returning to the first package opened in step 5, Section 4.4., deliver the rest of the package contents into graduated flask(s) and/or a graduate and record the remaining volume delivered in column 2 of Block B of the worksheet (where the first volume was recorded in Section 4.4.).

The volume of product still left in the package is now determined.

- 13. Weigh the empty (but wet) package container.
- 14. Clean, dry, and weigh the package container.
- 15. Record the difference in weight between wet and dry tare in column 6 of Block B on the worksheet, filling in the heading of Column 6 as "wet tare - dry tare".

Calculate the volume of liquid left in the package. If the ratio calculated in step 11 above is 0.05 or smaller, the remaining volume of liquid in the package is calculated from values in Block B of the worksheet, and

> = column 6 x labeled volume value in box 5a

If the ratio is greater than 0.05 in step 11, the remaining volume of liquid (from values in Block B of the worksheet)

 $= \frac{\text{column } 6}{\text{column } 3}$ for each package.

Record remaining volume in the package in column 7, Block B of the worksheet.

16. Add the volume remaining in the package as determined in step 15 to the volume poured from the package determined in step 12 (and recorded in column 2 of Block B of the worksheet) to arrive at the total volume.

Total product volume

= column 2 + column 7

In Block B of the worksheet, record the total volume in column 8 filling in the heading as "total volume".

Record total volume under "net or drained" in Block A.

 Subtract the labeled volume from the total package volume (step 16) to arrive at the individual package error. Package error in units of volume = total product volume - labeled volume.

Record package errors in Block A of the worksheet and in the checkerboard area of the worksheet (identifying an appropriate unit of measure in box 4).

18. Repeat steps 12 through 17 above for the second package opened. If the ratio calculated in step 11 is greater than 0.050, the weight of a known volume of product from this package would already have been determined in Step 9 of Section 4.4. This weight of a known volume can be used in step 15 above for this package only.

> If the ratio calculated in step 11 is 0.050 or smaller, the average weight of the labeled volume may be used (already calculated in step 11.)

19. If the ratio calculated in step 11 above is greater than 0.050, determine a weight of a known volume as described in Section 4.4. for each of the remaining packages in the sample following each determination with steps 12 through 17 above.

> If the ratio calculated in step 11 is 0.050 or smaller, open each package in the sample, deliver its contents into flask(s and a graduate) as described in step 12 above, and repeat steps 13 through 17 using the average weight of the labeled volume already determined in step 11. Repeat for every package in the sample.

After package errors have been determined, go to step 16 of Section 3.5. to determine lot conformance.

4.7. SPECIAL COMMODITY: MILK

Because of the homogeneity of milk within the production lot, as long as the inspector is careful to define the inspection lot as that product from a single production lot (as identified by the packager's lot code or symbol), certain steps in Section 4.4. are eliminated.

Equipment is the same as described in Section 4.2. except that a flask may be selected equal to the volume declared on the milk container.

Sections 4.4. and 4.5. are followed except:

 In step 5 of Section 4.4., if product delivered from a container does not fill the flask to a graduation line, milk from another package may be added to bring the liquid level up to a graduation.

- Steps 7, 9, and 10 of Section 4.4. may be skipped. This means only one package is used to determine the weight of the labeled volume of the product in step 11 of Section 4.4.
 - 4.8. SPECIAL COMMODITY: MAYONNAISE AND SALAD DRESSING

The following method is also suitable for water-immiscible products without a level liquid surface. This method is provided for mayonnaise and salad dressing because the volume of such products is changed by scooping or stirring the product.

4.8.1. Equipment

 $\frac{\text{Volumetric measures}}{4.2.}$ recommended in Section

<u>Plastic disks</u> and the procedure of fill described in Section 4.13.

4.8.2. Procedure

1.- 4. Follow the procedure in Section 3.5., steps 1 through 4, for filling out the report form heading and selecting a random sample. A random tare sample is not needed.

> In Block A of the worksheet, cross out column heading "tare" and insert "headspace". Cross out "gross" and insert "container volume" in space below it.

- 5. Open the first package and place a disk larger than the package container opening over the opening. Deliver water from a graduate onto the top of the product until the container is filled (as described in step 6 of Section 4.13.2. on the use of the plastic disks.) Record the volume of water added in column "headspace" in Block A of the worksheet.
- Empty, clean, and dry the package container.
- With the disk over the opening, fill the package container again with water

from flask(s) and graduate(s). Record this volume of water in column headed "container volume" of Block A on the worksheet.

- Subtract the volume recorded in step 5 from the volume recorded in step 7. This is the volume of product in this individual package. Record this volume in the column headed "net or drained" in Block A of the worksheet.
- 9. Subtract the labeled volume from the package volume determined in step 8 to arrive at the individual package error. Record package error in Block A and in the checkerboard area of the report form using an appropriate unit of measure in box 4.
- Repeat steps 5 through 9 for the remaining packages in the sample.

Go to step 16 of Section 3.5. to determine lot conformance.

4.9. SPECIAL COMMODITY: PAINT, VARNISH, AND LACQUERS - NONAEROSOL

This section describes three different test methods which may be employed depending upon the degree of accuracy necessary and the location at the time of the check. The procedures are: a field auditing method usually conducted on the premises of the vendor, an in-plant auditing method, and a "possible violation" method which is designed for laboratory or in-plant use because of clean-up and product collection requirements.

Although the procedures are suitable for use with products labeled by volume and packaged in cylindrical containers with separate lids which can be resealed, the various steps have been set forth using paint as the example. A worksheet is also included.

4.9.1. Equipment

<u>Scales and weights</u> recommended in Section 3.1.

$\frac{Volumetric measures}{4.2.}$ recommended in Section

Micrometer depth gage (ends of rods fully rounded)¹³, 0 to 9 in (0 to 225 mm).

¹³The rods will need to be custom ground.

WORKSHEET FOR CHECKING PAINT

Audit

1		Can D	iameter		6	7	8	9	10
Can Height	2 Top	3 Middle	4 Bottom	5 Average	Average Liquid Diameter	Average Liquid Level	Average Container Depth	A verage Liquid Depth	Volume

1 cu. in. = 0.004329 gal. 1 cm³ = 0.001 L Volume $(10) = 0.7854 \times (6) \times (6) \times (9)$

If volume in 10 is less than labeled volume, use possible violation procedures (Section 4.9.4.)

Possible Violation

1 Label	2 Gross Weight	3 Lid Weight Wet (-) Dry	4 Liquid Level	5 Tare	6 Water Volume	7 Net Weight = 2 - 5	$ \begin{bmatrix} 8 \\ Weight of \\ Label Volume \\ = \frac{7 \times 1}{6} $	$\begin{array}{c} (3) \\ Package Volume \\ = (6) + \left[\begin{array}{c} (3) \\ (7) \\ (7) \\ \end{array} \right] \times (6) \end{array}$
					_			

Diameter tape measure, 2 to 12 in (5 to 30 cm).

<u>Spanning bar</u>, 1 by 1 by 12 in (2.5 by 2.5 by 30 cm).

Paint solvent or other solvent suitable for the product being tested.

Level.

Rule, 12 in (30 cm).

Cloth, 12 in (25 cm) square.

Wood, 12 in (25 cm) long, 2- by 6-in.

Rubber mallet.

Circular metal disc, ¼ in (0.65 cm) thick and slightly smaller than package container diameter.

Rubber spatula.

Bubble level.

Optional: Micrometer.

4.9.2. Field Auditing Procedure

The following procedure is suitable only for use in checking products put up in cylindrical containers up to 1 gallon (4 L) in capacity. Step 5a can be used with any sized containers and 5b with gallon (4 L) containers only. The method checks the volume of only one can in the sample, after selection of that can likely to have the smallest volume of product inside it.

Because of configuration of the bottom of the can, paint clinging to the lid, and slight variations in the wall and label thicknesses of the paint container, there is an estimated uncertainty of at least ± 0.6 percent to this auditing procedure. Therefore, this method is recommended solely for eliminating from more rigorous testing packaged products that appear to be full measure. Section 4.9.4. is recommended when the volume determined in step 12 of this section is less than the labeled volume or in any case where short measure is suspected.

1.- 4. Following Section 3.5., steps 1 through 4, identify the lot and select a random sample. A tare sample is not needed.

- 5. a.
- Any sized container up to 1 gal (4 L):

Measure the outside diameter of each container near its middle (as shown in Figure 4-4) to the closest 0.001 in (0.02 mm), using a direct reading diameter tape measure. Record readings in column 3 of the Worksheet for Checking Paint in the audit section.

Set the containers on a level surface and record the range in heights on the worksheet under column 1 in the audit section. If the range of outside diameters exceeds 0.005 in (0.125 mm) or the range in heights exceeds 0.0625 in (1.58 mm), this procedure cannot be used. If the ranges are within the specified limits, open all cans in the sample and select the container with the greatest headspace. This may be determined by visual inspection or with the use of the micrometer depth gage. Replace all lids except that of the selected container and reseal the lids by placing a cloth and then the section of wood on lid and hammering on the wood with the rubber mallet. Tip the cans upside down momentarily to complete the resealing operation. Continue with step 6 below.

5. b. Gallon (4 L) cans:

This test is appropriate when the weight of the paint is much greater than the weight of the can, and is, therefore, applicable for gallon (4 L) sizes only.

Gross weigh each package in the sample. Select the package from the sample with the lightest gross weight. Carefully remove the lid of this can.

 Measure the outside diameter of the selected container near its top, middle (already measured if step 5a was used), and bottom, to the closest 0.001 in (0.02 mm), using a direct reading diameter steel tape, and record these measurements in columns 2, 3, and 4 on the paint worksheet in the audit section.





Sum the three diameter values and divide by three to obtain the average diameter. Record the average diameter in column 5 of the paint worksheet.

 If a micrometer is available, measure the wall and the paper label thickness of the container, otherwise assume the wall and label thicknesses given in Table 4-4.

> Subtract twice the wall and paper label (if any) thickness from the average can diameter (step 6) to obtain the average liquid diameter. Record the liquid diameter in column 6 of the paint worksheet.

- 8. Using a level working surface, place the container of paint on the circular metal disc slightly smaller in diameter than the bottom rim of the can so the bottom of the container nests on the disc as shown in Figure 4-5. This eliminates the "sag" in the base of the paint container.
- 9. Place the spanning bar and depth gage across the top of the paint can as shown in Figure 4-5. Mark the location of spanning bar on rim of paint container. Measure the depth of the liquid level to the nearest 0.001 in (0.02 mm) at three points in a straight line, at points approximately 3/8 in from the inner rim for cans 5 in in diameter or less, on either side and at the center of the can as shown in Figure 4-6 (1/2 in from the rim for)can diameters exceeding 5 in). If working in metric units, measure at 1 cm from the rim for cans with diameters of 15 cm or less and 1.5 cm from the rim for can diameters exceeding 15 cm. Sum the three readings and divide by three to obtain the average depth of the liquid level in the container. Record the average liquid level in column 7 of the audit section on the paint worksheet.
- Measure the distance to the bottom of the container (Figure 4-7) at three points in a straight line in the same manner as outlined in step 9. Sum the three readings and divide by three to

Wall thickness						
Inc	h-pound	Metric				
can size	in	can size	mm			
1 gal 1/2-gal 1 qt 1 pt	0.010 0.010 0.009 0.008	4 L 2 L 1 L 500 mL 250 mL	0.25 0.25 0.23 0.23 0.20			
	Label thick (all d	an sizes)				
	Inch-pound	Metric				
	0.004 in	0.10 mm				
2						

Table 4-4. Thickness of paint can walls and labels.

^dThe thickness of labels lithographed directly onto the container may be ignored.

obtain the average depth of the container and record the average depth in column 8 of the paint worksheet in the audit section.



Figure 4-5. Measuring the depth of the liquid level.



Figure 4-6. Top view of paint can showing locations at which depth measurements are made.

11. Subtract the average depth of the liquid level (step 9) from the average depth of the container (step 10) to obtain the average height of the liquid column and record it in column 9 of the paint worksheet. Determine the volume of paint in the container by using the following formula:

> Volume = $0.7854 \text{ D}^2\text{H}$ or $0.7854 \times D \times D \times \text{H}$

Where D = average liquid diameter (step 7) H = average liquid depth (step 11)

Record this volume in column 10 of the paint worksheet.

If this calculated volume is less than the labeled volume, go on to Section 4.9.4.



Figure 4-7. Measuring the distance to the bottom of a container.

4.9.3. In-Plant Auditing Procedure

In this method, a container is selected which is likely to have the smallest volume of product inside it, and the level of fill of a can of the same dimensions as the one under test is duplicated with water. The method is not restricted to gallon cans or smaller (as was Section 4.9.2.) but can be used to check any size package as long as the liquid level is within 9 inches of the top of the container. Follow steps 1 through 8 of Section 4.9.2. If any paint is found clinging to the side walls or lid, carefully scrape the paint into the container with a rubber spatula.

- 9. Place the spanning bar and depth gage across the top of the paint can. Measure the depth of the liquid level at the center of the surface and record the depth in the audit section of the paint worksheet in column 7.
- 10. Select an empty can with the same bottom configuration and with diameter and height within ±0.001 in (±0.025 mm) for l-pt (500 mL) cans, ± 0.002 in (± 0.05 mm) for l-qt (l-L) cans, ± 0.003 in (± 0.075 mm) for l/2-gal (2-L) cans, and ± 0.004 in (±0.1 mm) for 1-gal (4-L) cans, of the container under test. Set up the empty can in the same manner as step 8 of Section 4.9.2. and step 9 above. Fill the container with water from a volumetric measure of the same volume as the labeled volume. Measure the depth of the liquid level at the center of the container and record this level in column 7 below the reading recorded in step 9. If this depth is equal to or greater than the depth determined in step 9, assume the package satisfactory. If the depth is less than the depth determined in step 9, short measure may be suspected. Use the possible violation procedure given in Section 4.9.4. when short measure is suspected.

4.9.4. Possible Violation Procedure

The following method may be used as long as the liquid level is within 9 inches of the top of the container. The steps noted with an (a) are required if paint is found adhering to the lid and it cannot be removed by scraping into the can.

It may be necessary to use the alternative tare procedure of Section 2.11.4., although the following steps do not specifically include that technique.

 - 4. See Section 3.5., steps 1 through 4, for instructions on filling out the report form and selecting the random sample and random tare sample.

- 5. Do not shake or invert the containers selected as the sample. Determine the gross weight of these packages and record in the lower section of the paint worksheet headed "Possible Violation". Set up the first package selected for tare in the same manner as in step 8, Section 4.9.2. Remove the lid. If paint is clinging to the side walls, scrape it down into the can with the spatula.
 - a. If paint is adhering to the lid (and it cannot be removed completely by scraping the paint into the can), determine the weight of the lid plus any paint adhering to the lid. Clean the lid of paint and weigh again. Subtract the clean
 lid weight from the paint-filled lid weight to determine the weight of the paint adhering to the lid. Record this weight in column 3 on the lower portion of the paint worksheet.
- 6. Place the spanning bar and depth gage across the top of the paint can. Mark the location of the spanning bar on the rim of the paint container. Measure the depth of the liquid level at the center of the container to the nearest 0.001 in (0.02 mm). Record the depth in column 4 of the paint worksheet.
- Empty and clean the sample container of paint with a suitable solvent; dry and weigh the container.
- Set up the container in the same manner as in step 5 above.
- 9. Place the spanning bar at the same location on the rim of the paint container as marked in step 6. With the depth gage set as described in step 6, deliver water into the container in known amounts¹⁴ until the water reaches the same level occupied by the paint as indicated by the depth gage. Record this volume of water (in fl oz or mL) in column 6 on the lower portion of the paint worksheet. This is the volume occupied by the paint in the container.

¹⁴One method of measuring water delivered into the container is to use a test measure of the same size as the labeled quantity of paint. Fill the test measure to the mark with water and pour the water into the package container. Add or subtract the water necessary to reach the same level occupied by the paint with the aid of a syringe dropper and small graduate. The volume occupied by the paint is the volume of the test measure plus the additional water added or minus the water removed from the package container.

5.

- Subtract the tare of the container (step 7) from the gross weight (step 5) to arrive at the net weight of paint in the selected container. Record the net weight in column 7 on the lower portion of the paint worksheet.
- 11. Calculate the weight of the labeled volume of paint =

net weight (step 10) x labeled volume volume of paint in can (step 9)

= column 7 value x column 1 value column 6 value.

Record this value in column 8 of the worksheet

11. a. Calculate the package volume =

volume in can (step 9) + lid paint weight (step 5a) x

can volume (step 9)
net weight (step 10)

Record it in column 9 of the worksheet.

12. Calculate package error.

Package error =

column 6 value (-) labeled volume

12. a. Package error =

column 9 value (-) labeled volume

13. Repeat steps 5 through 12a (above) for the second package chosen for tare.

In order to use weighing to check the sample (and assuming the tare is not so variable as to require opening more than two cans¹⁵,) the weights of the labeled volume for the first two packages (recorded in column 8) should not differ from each other by more than the value given in Table 4-2 (See Section 4.4.). If this criterion is met, the rest of the sample may be checked by weighing; the nominal gross weight is equal to the sum of the average weight of the labeled volume plus the average tare. Go to step 15 of Section 3.5. to complete the test.

It should be noted that the weight of a given volume of paint often varies considerably from container to container; therefore, volumetric measurements may prove necessary for the entire sample. In such instances, that is, if the criterion of Table 4-2 is not met, follow steps 5 through 11a and 12a (skip steps 11 and 12) if paint is adhering to the lid or steps 5 through 9 if paint is not adhering to the lid for all the packages in the sample. When package errors have been determined in this manner, go to Step 16 of Section 3.5. to determine lot conformance.

4.10. SPECIAL COMMODITY: VERY VISCOUS MATERIALS¹⁶

The following method can be used for any package labeled by volume but is especially suitable for very viscous materials such as cartridge-packed caulking compounds, glues, pastes, and the like, often packed in tubes. This is most suitable as a laboratory procedure (using a hood to ventilate solvent fumes, if necessary), but if used in the field, a well ventilated area to conduct the test should be chosen if solvents other than soap and water must be used.

4.10.1. Equipment

<u>Small-capacity scale and weights</u> recommended in Section 3.1.

<u>Pycnometer</u>, a vessel of known volume for weighing semifluids. The pycnometer can be purchased or constructed. If constructed, it will be referred to as a "density cup".

Make a 150-mL or 5-fl oz density cup (see Figure 4-8) by cutting off the lip of a 150-mL beaker with an abrasive saw and grinding the lip flat on a lap wheel. The slicker plate can be purchased commercially.

Appropriate solvents (water, Stoddard solvent, kerosene, alcohol, etc.).

<u>Caulking gun</u> (for cartridge packed products).

4.10.2. Preparation for Test

Weigh and calibrate pycnometer or the complete density cup unit (cup and slicker plate) with respect to volume (mL or fl oz)

2

¹⁵See Section 2.11.4., steps (v) through (xi).

¹⁶Derived from a method devised by Mr. James Little, NBS.

prior to use. Calibrate the density cup gravimetrically with respect to the contained volume using the procedure given in NBS IR 74-461, "The Calibration of Small Volumetric Glassware." Special instructions furnished by the pycnometer manufacturer may be necessary in order to calibrate a pycnometer (if it has not already been calibrated). It is not necessary to reweigh or recalibrate for each test; however, the pieces of each unit should be marked to prevent interchange of cups and slicker plates. container with solvent, weigh it (record this weight as tare weight in Block A of the worksheet).

 If pycnometer is used, cover with lid and screw cap down tightly. Excess material will be forced out through hole in lid. Clean exterior surfaces.

> If using density cup, place the slicker plate over 3/4 of the cup mouth (see Figure 4-9), press down, and slowly move the plate across the remainder of the opening. With the slicker plate kept in place, clean all exterior surfaces with solvent and dry them.



Figure 4-8. Empty density cup and slicker plate.

4.10.3. Procedure

The following measurements must be made on each package in the sample.

- 4. See Section 3.5., steps 1 through 4 for instructions on filling out the report form heading and selecting the random sample. A tare sample is not needed.
- Weigh a calibrated pycnometer or density cup and slicker plate and record the weight in column 7 of Block B of the worksheet, filling in the heading as "pycnometer" or "cup and plate weight". The pycnometer or cup volume is recorded in column 2 of Block B.
- 6. Weigh and then open the first package. Record the gross weight in Block A of the worksheet. Transfer the product to the pycnometer or density cup, filling the pycnometer or cup to excess. Use a caulking gun for transferring product from caulking cartridges. Remove the product as completely as possible from the package container, clean package



Figure 4-9. Density cup filled with product.

- 8. If pycnometer is used, weigh filled pycnometer or if using density cup, weigh the filled density cup with slicker plate at least to the nearest 0.002 pound or nearest gram. Record this weight in column 6 of Block B on the worksheet filling in the heading as "filled weight." Subtract the weight of the empty pycnometer or cup and plate (column 7 of Block B) from the filled weight to arrive at the weight of the product contained in the pycnometer or density cup. Record this weight in column 1 of Block B on the worksheet.
- Calculate the weight of product corresponding to the labeled volume of product =

product weight in cup x labeled volume density cup volume

If using pycnometer, substitute product weight in pycnometer and pycnometer volume in above equation.

The weight of product in the pycnometer or density cup is found in column 1 and the pycnometer or density cup volume in column 2 of the worksheet. Carry over at least two extra decimal places in each calculation until the weight of the labeled volume is obtained. Record the weight of the labeled volume in column 4 of Block B of the worksheet.

10. The gross weight of the package minus the weight of the package container (in Block A of the worksheet) is the actual weight of product in the individual package being measured. Record this weight difference in the "net or drained" column of Block A on the worksheet. Subtract the weight of the labeled volume from this actual weight of product to arrive at the individual package error in units of weight.

Convert the package errors to units of volume.

Package error (volume) = Package error (weight) x <u>cup volume</u> weight of product in cup

If using pycnometer, substitute pycnometer volume for cup volume and weight of product in pycnometer for weight of product in cup in above equation. Record the package error on the report form (using an appropriate unit of measure).

 Clean the pycnometer or density cup and slicker plate and repeat steps 6 through 10 for the rest on the packages in the sample. Go to Step 16 of Section 3.5. to determine lot conformance.

4.11. SPECIAL COMMODITY: PEAT MOSS

ASTM D 2978-71, "Standard Method of Test for Volume of Peat Materials", is the reference standard for the following procedure.

Every package in the sample is opened.

This method is suitable for particulate solids (such as soils or other garden materials) labeled in cubic dimensions or dry volume. Some materials may not pass through the sieve specified for peat moss listed below (mulches, etc.); therefore, separate the materials by hand (to compensate for packing and settling of the product after packaging) before filling the test measure (see step 5 below).

4.11.1. Equipment

12.5-mm (1/2-in) sieve.

<u>Wooden or metal container</u>, with inside dimensions of 12 by 12 by 12 in marked off in 1-in horizontal lines on the inside (1-cu ft container) or of 50 by 50 by 40 cm marked off in 5-cm horizontal lines (0.1-m³ container). This container will have to be constructed.

Straight edge, 20 in (75 cm) in length.

Sheet for catching overflow of material.

Bubble level.

4.11.2. Procedure

- 4. See Section 3.5., steps 1 through 4 for instructions on filling out the report form heading and selecting the random sample. No tare sample is needed.
- 5. Open each package in turn, removing the contents and passing the contents through the sieve allowing the package contents to go directly into the measuring container (overfilling it). Shake the measuring container with a rotary motion at one rotation per second for 5 seconds. Do not lift the measuring container when rotating it. If package contents are greater than the measuring container capacity, level the measuring container with a straight edge using a zig-zag motion across the top of the container and empty the container. Repeat the filling operations as many times as necessary, noting the partial fill of the container for the last quantity delivered using the interior horizontal markings as a guide. Record the amount of material in Block A in the column headed "net or drained" on the worksheet¹⁷.
- Compute the package errors (= actual measurement minus the labeled measurement) and record each in Block A of the worksheet. Transfer the package errors to the report form using an

¹⁷Use conversion factors (such as "Factors for High Precision Conversion", NBS Letter Circular 1071, July 1976) to convert from cubic measure to dry volume.

appropriate unit of measure in box 4 of the report form. Go to step 16 of Section 3.5. to determine lot conformance.

4.12. SPECIAL COMMODITY: SOLIDS OR SEMISOLIDS

The following procedure can only be used to test packaged products which are solid or semisolid and which will not dissolve in, mix with, absorb, or be absorbed by the fluid into which the product will be immersed.

Every package must be opened. The product is removed from its package and completely submerged in water or other fluid in a container. The volume of the product may be determined either (a) by noting the difference in volume registered by comparison with graduated markings on the container or (b) by measuring the volume of water or fluid overflowing from a container previously filled to overflow capacity.

4.12.1. Equipment

Either of the following:

- <u>Graduate or volumetric flask</u> of capacity larger than the labeled volume of package being tested;
- Container with overflow spout of physical dimensions large enough to contain commodity, plus graduate or volumetric flask equivalent to labeled volume.

<u>Thin wire</u>.

Water or other fluid which will not dissolve or mix with package contents.

Bubble level.

4.12.2. Procedure

- 1.- 4. Follow Section 3.5., steps 1 through 4 for instructions on filling out the report form heading and selecting the random sample. A tare sample is not needed.
- 5. On a level surface, follow either (a) or (b) below.
 - Select a graduate of a larger capacity than the labeled volume of the package and fill it with

water or other liquid to a volume which will still allow the packaged product to be added to the graduate without exceeding the graduated portion of the graduate. Record this volume in the column labeled "tare" on Block A of the worksheet. Open the first package and submerge the product by pushing the product down with the wire. Record the resulting volume in the column labeled "gross" on Block A of the worksheet. The difference in liquid level before and after adding the product to the graduate is the volume of the product (record in "net or drained" column of Block A on the worksheet.)

- Fill container with an overflow b. spout to overflowing with water or other liquid and allow to sit until dripping stops. Place a graduate or other volumetric container of a capacity large enough to contain the package volume at the spout. Open the first package and carefully submerge the product using the thin wire to push the entire product below the liquid level. The volume of liquid displaced by the product (including the final dripping of liquid into the container or graduate) is the volume of the product. Record this volume in "net or drained" column of Block A on the worksheet.
- 6. The volume of the product (as determined by 5a or 5b above) minus the labeled volume is the individual package error. Record the package error in Block A of the worksheet and transfer to the report form using an appropriate unit of measure. Repeat steps 5 and 6 (as appropriate) with the remainder of the packages in the sample. Go to step 16 of Section 3.5. to determine lot conformance.

4.13. SPECIAL COMMODITY: GOODS LABELED BY CAPACITY

The capacity of packaged products such as bowls, pots, glasses, cups, etc. is labeled in terms of liquid volume and is defined as the brim-full or level-full capacity unless there are markings of capacity on a side wall of the product, or a ridge capable of accepting a lid. (In the former instance, the capacity is defined as the capacity at the designated mark. In the latter instance, the capacity is defined as the capacity at the level of the ridge or "seat.") The procedures presented below are for determining the brim-full, marked or seated capacity of a container.

4.13.1. Equipment

<u>Volumetric Flasks and graduate</u> as described in Section 4.2.

500-milliliter buret meeting Type 1, Style 1, Class A requirements of Federal Specification NNN-B-782.

Rubber bulb syringe.

<u>Plastic Disks</u>. 1/8-in or 3-mm thick disks with diameters to correspond to seat diameter or larger than brim diameter of each container tested. Diameter tolerance is ± 0.002 in or ± 0.05 mm. The outer edge should be beveled at a 30-degree angle with the horizontal to 1/32-in or 0.8 mm thick at the edge. There should be a 3/4-in or 20-mm diameter hole through the center of the disk and a series of 1/16-in or 1.5-mm diameter holes 1 in or 25 mm apart around the periphery of the disk and 1/8 in or 3 mm in from the outer edge. All edges should be smooth. See Figure 4-10.

Bubble level.



Figure 4-10. Plastic disk (beveled edge upward) inserted in the seat of a container to be tested.

4.13.2. Procedure¹⁸

The following procedures are divided into (a) determination of flush fill to brim or

(b) determination of capacity to seat. A level working surface must be used for all test procedures. At the end of the procedure, there is information on testing a container to a marked capacity. This test does not use the plastic disks.

- 4. See Section 3.5., steps 1 through 4 for instructions on filling out the report form heading and selecting the random sample. A tare sample is not needed.
- a. Select a plastic disk with a diameter larger than the outside brim diameter of the container to be tested. Place the disk with the beveled edge upward on the container. Center the disk on the container. See Figure 4-11.



- Figure 4-11. Disk in place for flush fill (or brim-full) capacity determination.
- b. Select a disk with a diameter equal to the seat diameter of the container being tested. Insert the plastic disk on the seat of the container with the beveled edge upward. See Figure 4-10.
- 6. Add water to the container using flask (or flasks), graduate, or buret corresponding to label capacity. (If the flask appears likely to overfill the container, do not deliver that apparent overfill). Add water until all of the air in the container has been displaced and the water begins to rise in the center hole of the disk. Stop the filling procedure when the water fills the center disk hole and domes up slightly due to the surface tension.

¹⁸Plastic disk procedure provided by the American Can Co., Neenah, Wisconsin.

If the water dome breaks on the surface of the disk, the container is overfilled and the test is void; dry the container and start over.

Do not add additional water once the level of the water dome has dropped.

- 7. Record the amount of water used to fill container (in the "gross" column of Block A on the worksheet) and subtract 0.03 fl oz (1 mL) (corresponding to the amount of water in the disk hole) to obtain the container capacity. Record the container capacity in the "net or drained" column of Block A in the worksheet.
- Repeat this procedure on the remaining packages in the sample. Compute the package errors (= package capacity

minus the labeled capacity), record them in Block A of the worksheet, and transfer them to the report form using an appropriate unit of measure. Go to step 16 of Section 3.5. to determine lot conformance.

When testing containers with markings of capacity on the side wall of the container, follow steps 1 through 4 above. Water from a buret, flask, or graduate should be added to each container such that a level of fill is obtained corresponding to the markings. The inspector should record the amount of water used to reach the mark (similar to filling a volumetric flask to a mark if the container walls are transparent) as the container capacity. Then follow step 8 above to complete the test.

CHAPTER 5. METHODS OF TEST FOR PACKAGES LABELED BY COUNT, LENGTH, AREA, THICKNESS, OR COMBINATIONS OF QUANTITIES

- 5.1. PACKAGES LABELED BY COUNT WHEN THE LABELED COUNT IS 51 OR MORE UNITS PER PACKAGE
- 5.2. PACKAGES LABELED BY COUNT WHEN THE LABELED COUNT IS 50 OR FEWER UNITS PER PACKAGE
- 5.3. PACKAGES LABELED BY LINEAR OR SQUARE (AREA) MEASURE
- 5.4. SPECIAL COMMODITY: POLYETHYLENÈ SHEETING
- 5.5. SPECIAL COMMODITY: PAPER PLATES
- 5.6. SPECIAL COMMODITY: SANITARY PAPER PRODUCTS
- 5.7. SPECIAL COMMODITY: PACKAGES GIVEN TOLERANCES

CHAPTER 5. METHODS OF TEST FOR PACKAGES LABELED BY COUNT, LINEAR MEASURE, AREA, THICKNESS, OR COMBINATIONS OF QUANTITIES

Many commodities and manufactured products are sold in units of quantity other than weight or liquid or dry volume. For example, food wrap is sold by its length, width, and area. Polyethylene sheeting is sold by its length, width, area and thickness. Disposable paper plates are sold by the number of plates in the package and by their diameter.

This chapter provides general procedures for packages labeled by count or length and procedures for special commodities such as polyethylene sheeting.

Certain packaged goods are labeled by several units, usually count and some other quantity such as dimension, capacity, etc. In such instances, all labeled quantities must individually meet the average requirements unless other requirements are in force. The National Conference on Weights and Measures (NCWM) Model State Method of Sale of Commodities Regulation (MOS)¹ has provided an exception to this general situation: pressed and blown tumblers and stemware are given tolerances. When tolerances apply to packaged goods, the average requirement does not apply. A special sampling plan and test procedure is provided for pressed and blown tumblers and stemware (Section 5.7.).

Another exception to the average requirement is for packages labeled by low count (less than 51 units per package). For statistical reasons, the count of such packages cannot be held to an average requirement. This chapter provides a set of sampling plans to be used in such instances (Section 5.2.).

5.1. PACKAGES LABELED BY COUNT WHEN THE LABELED COUNT IS 51 OR MORE UNITS PER PACKAGE

Two methods for the determination of count without opening all the packages which comprise the sample are presented here. Both use the weight of a counted number of packaged articles. One of these methods is intended as an auditing procedure only. Of course, when the weight of each discrete unit or number of units is found to be too variable, the official must count packaged units rather than weigh them.

5.1.1. Equipment

<u>Scales and weights</u> recommended in Section 3.1.

5.1.2. Auditing Procedure

The following method does not follow the steps outlined in the decision charts. The accuracy of the method is ±1 percent, therefore any action based on shortages of count must use either actual count or Section 5.1.3. as the basis for determining compliance. This method is, however, useful for auditing packages labeled by high unit counts (in excess of 100).

- 4. See Section 3.5., steps 1 through 4 for instructions on filling out the report form heading and selecting the random sample and random tare sample.
- Gross weigh the first package for tare determination. Record this weight in Block A of the worksheet.
- Select that number of items from the first tare package which weighs the greater, either (a) or (b):
 - a. 10 percent of the labeled count,
 - b. a quantity sufficient to indicate at least 50 minimum divisions on the package checking scale. For example, using the package checking scale with 1/16-oz divisions, the selected count must weigh at least 3 1/8 oz. For the package checking scale with 1-g divisions, the selected count must weigh at least 50 g. Record the count and weight in Block B in columns 1 and 2 of the worksheet.

¹The NCWM MOS is a voluntary standard for State regulatory use which is periodically revised by State agency representatives. Not all 50 States have regulations based on this model.

7. Calculate the weight of the labeled count =

labeled count x weight (col. 1) count (col. 2)

Record the result in column 4 of Block B on the worksheet and in Block A of the worksheet under the column headed "labeled" filling in the space with "count weight".

- Gross weigh the rest of the tare sample and keep contents of opened packages separated in case Section 5.1.3. must be followed. Determine the tare weights of the tare sample and record this in Block A of the worksheet.
- The weight of the labeled count plus the tare weight represents the "nominal gross weight" to be used to compare with the actual gross weights of unopened packages in the sample.

Package error (in units of weight) =
 actual gross weight (-) nominal
 gross weight.

Record the package errors in Block A of the worksheet.

10. Convert the package errors in units of weight to units of count: Package error (count) = Package error (weight) x

> labeled count weight of labeled count

Round up all fractional counts computed in this manner to whole units. Record the package error in units of count in the checkerboard area of the report form. Compute the average error. If the average error is minus, follow Section 5.1.3. to determine lot conformance. If the average error is equal to zero or positive, the lot is presumed to conform to the package requirements.

5.1.3. Possible Violation Procedure

The following method follows the steps outlined in Decision Chart 4.

The measurement of the weight of a number of packaged units is combined with the determination of tare and, therefore, will not require more packages to be opened than that number designated in Table 2-2 or 2-5, column 3.

If Section 5.1.2. has been used, this procedure can be followed without taking a new sample if package contents can still be counted and the contents have been kept separate.

 4. See Section 3.5., steps 1 through 4 for instructions on filling out the report form heading and selecting the random sample and random tare sample.

Record the MAV from Table 2-10 in units of count in box 6 on the report form.

- Gross weigh the packages selected for tare determination and record their gross weights in Block A of the worksheet. Open these packages.
- Determine and record the weight of the exact number of items in the first opened package.

Record the weight in column 1 and the count in column 2 of Block B on the worksheet.

7. In order to determine whether the scale used to weigh the packages is able to discriminate differences in count, add or subtract that number of units corresponding to the MAV/6 (or at least one unit)² to or from the units already on the scale in step 6. The difference between this weight and that determined in step 6 must be at least as large as 1/2 the size of the smallest scale division (or at least as large as the smallest increment in the readout on/a digital scale).

For example, From Table 2-10, the MAV is 7 units for a package labeled with a count of 250 units. The scale should be capable of discriminating differences corresponding to MAV/6 or, in this example, one unit.

If the criterion above is not met, count the package contents in each package in the sample; if met, go on to step 8.

8. Determine and record (in Block A of the worksheet) the tare weight of the first package opened.

²Alternatively, the weight corresponding to MAV/6 may be calculated as described in step 7b of Section 4.4.

- Determine and record the weight and the count of the items in the second package opened for tare.
- 10. Calculate the weights of the labeled counts for the first two packages.

Weight of labeled count =

labeled count x contents weight contents count

Record these weights in the appropriate boxes of 4b and in col. 4 of Block B of the worksheet.

To avoid round-off errors, carry over at least two extra decimal places in the calculation until the weight of the labeled count is obtained.

The difference in weight of the labeled count between the two packages must not exceed that value given in Table 4-2 (see Section 4.4.).

If the difference in weights does not meet this criterion, determine the actual count per package for every package in the sample. If the difference meets this criterion, go on to step 11.

- Average the weights of the labeled count (record in box 5b, Block B of the worksheet).
- Determine the tare for the rest of the tare sample (if any); record the tare values in Block A of the worksheet. Average the tare weights. Record package errors for the tare sample packages.
- 13. The average weight of the exact number of items in the package as labeled (step 11) plus the average tare weight (step 12) equals the "nominal gross weight" to be used to compare against the gross weight of the unopened packages in the sample. Record the nominal gross weight in Block A of the worksheet.
- 14. Calculate the MAV in units of weight; MAV (in units of weight) =

MAV (in units of count) x <u>average weight of labeled count (5b,B)</u> labeled count Record MAV in units of weight in box 7 of Block B of worksheet and in box 5 of the report form. Select an appropriate unit of measure in terms of weight (see Section 2.9.2.), convert the MAV to dimensionless units and record in box 7 of the report form.

With all measurements converted to weight and then to dimensionless units, go to Step 15 of Section 3.5., converting back to count when completing the report form.

5.2. PACKAGES LABELED BY COUNT WHEN THE LABELED COUNT IS 50 OR FEWER UNITS PER PACKAGE

A special sampling plan³ is provided for packages labeled by count when the number of units per package is 50 or fewer. The sampling procedure requires counting the number of units in each package in the sample and noting the number of those packages that contain less than the labeled count. The required number of packages for the sample and the allowable number of undercount packages are given in Table 5-1. No check on the average count is made.

 - 4. Follow the procedures in Section 3.5., steps 1 through 4, except sample size and tare sample size are found in Table 5-1. Record the column 4 value from Table 5-1 (the number of packages which are allowed to contain fewer than the labeled count) in box 13 of the report form.

The MAV in units of count is found in Table 2-10 and recorded in box 6 on the report form.

- 5. 12. Follow steps 5 through 12 of Section 5.1.3.
- 13. If it is possible to weigh to determine count, compare the gross weight of the unopened packages in the sample with the "nominal gross weight" (the average weight of the labeled number of items in the package (step 11) plus the average tare weight (step 12).) Each package error is equal to the actual gross weight minus the nominal gross weight.

 3 No distinction is made as to the severity of consequences of a lot being found out of conformance with the requirements. If the labeled count is 50 or fewer, this is the only sampling plan to be followed.

1	2	3	4
Lot size (number of packages in lot) N	Sample size (number of packages in sample) n	Tare sample size (number of packages chosen for tare determination) ⁿ t	Number of packages allowed to contain fewer than the labeled count.
Up to and includ- ing 500	10	2	1
501-5000	30	2	2
5001 and greater	50	5	3

Table 5-1. Sampling plans for packages labeled by low count^a

^aLabeled count is 50 or fewer units.

If it is necessary to open every package in the sample and count the contents, the package error is equal to the actual count minus the labeled count. Record the package errors.

14. Circle and count the number of minus package errors. If this number is larger than the number in box 13 of the report form, the lot fails to comply with the package requirements. If the number of minus package errors is equal to or less than that number recorded in box 13 of the report form, the lot complies.

For example, an inspector must test a lot of 360 packages of cotton balls labeled "50 cotton balls." A random sample of 10 packages is chosen from the lot. Because his scale cannot discriminate differences in count, the inspector opens every package and counts the balls. The 10 package counts are: 50, 52, 50, 50, 51, 53, 52, 50, 47, 50.

Since only one package contains fewer than 50 balls, the inspector declares the lot to have passed the test.

The MAV's listed in Table 2-10 for packages labeled by count and fewer than 51 units per package define the limits of reasonable variation for an individual package even though the MAV is not used directly in the sampling plan. Individual packages which are undercount by more than the MAV from the labeled count are, however, considered defective (even if the lot as a whole passes inspection) and should be repacked, relabeled, or otherwise handled on an individual basis. Following the previous example, the package containing 47 balls should be individually handled even though the lot complies with the package requirements.

5.3. PACKAGES LABELED BY LINEAR OR SQUARE (AREA) MEASURE

The weight of the labeled linear or area measure may be used together with the tare weight as the nominal weight value against which unopened packages in the sample may be compared as long as the scale used to weigh the packages can discriminate the weight equivalent to MAV/6 and the weight of the labeled measure does not vary outside the ranges permitted in Table 4-2. Decision Chart 4 may be used as a guide.

Products labeled by length or area often require the application of tension to the ends of the product before measurement, in order to straighten the product. Tension must be applied to woven or twisted fiber products such as thread, yarn, rope, cording, twine, etc. Because of the specialized equipment required for these products (and because such equipment is not readily available outside the packaging plant), the inspector is referred to the following standards suitable for in-plant inspection combined with sampling plans described in this handbook. These standards are: "Standard Method of Test for Yarn Number by the Skein Method", ASTM D1907-75, for thread and yarn; "Standard Methods of Testing Twine Made from Bast and Leaf Fibers", ASTM D1233-73; and "Standard Tolerances for and Methods of Testing Single Jute Yarn", ASTM D541-71.
Textiles labeled by length should be inspected using textile measuring devices which have been found to conform with the tolerances of NBS Handbook 44.

5.3.1. Equipment

<u>Scales and weights</u> as recommended in Section 3.1.

T-square.

Steel tapes and rules:

Inch-pound:

- For labeled dimensions 25 in or less, 36 in rule with 1/64 in or 1/100 in divisions, overall length tolerance of of 1/64 in.
- For labeled dimensions greater than 25 in, 100 ft tape with 1/16 in divisions, overall length tolerance of 0.1 in.

Metric:

- For labeled dimensions 40 cm or less, 1 m rule⁴ with 1/2 mm divisions, overall length tolerance of 0.4 mm.
- For labeled dimensions greater than 40 cm, 30 m tape⁴ with 1 mm divisions, overall length tolerance of 2.5 mm.

5.3.2. Procedure

 - 4. See Section 3.5., steps 1 through 4 for instructions on filling out the report form and selecting the random sample and tare sample. Separate report forms and worksheets should be filled out for packages labeled by separate dimensions and/or area.

> Record the MAV in units of length or area measure (given in Table 2-11) in box 6 of the report form.

 Gross weigh and open the packages selected for tare determination. Record in Block A of the worksheet. Determine the measurements (to the nearest division of the appropriate tape or rule being used to measure) of the packaged goods (length, width, area - depending upon which dimensions are declared on the label) and weigh the goods from the first package opened for tare determination.

> Record the weight and measure in columns 1 and 2 of Block B on the worksheet. Calculate the weight of the labeled measurement using boxes in 4b in Block B of the worksheet.

Weight of the labeled measurement =

labeled measurement x

contents weight (col. 1)
contents measurement (col. 2)

Record this weight in column 4 of Block B on the worksheet.

7. Add or subtract the length or area of packaged product corresponding to MAV/6 from the product already on the scale⁵. The difference between this weight and that determined in step 6 must be at least as large as 1/2 of the smallest division on the scale used to weigh the product (or at least as large as the smallest increment in the readout, if a digital scale is being used.)

> For example, for a package labeled 200 sq ft, the MAV of 3% is 6 sq ft and MAV/6 is 1 sq ft. Therefore, adding or subtracting 1 sq ft of product to the scale should change the scale indication by at least 1/2 the minimum scale division (or smallest readout increment if a digital scale.)

If this criterion is met, go on to the next step. If not, all the packages in the sample must be opened in order to measure the contents.

8. The tare weight of the first package opened is determined and recorded in Block A of the worksheet.

⁴The markings specified for the equivalent metric rule and tape may be incorporated in the inch-pound rule and tape.

⁵Alternatively the official may calculate the weight corresponding to MAV/6 (knowing the exact length or area in the package) and compare this value with 1/2 the minimum division on the scale being used. For example, an inspector finds 200 sq ft of product weights 2.000 lb, therefore 1 sq ft must weigh 0.010 lb. If the small capacity scale is being used, this is 5 times the usual minimum division on this scale (0.002 lb); therefore, this first criterion would be met.

- 9. Determine the measurements of the product in the second package chosen for tare determination. Determine the tare weight of this package and record in Block A of the worksheet. Calculate the weight of the labeled measurement for the second package (see formula in step 6). Record this calculation in the appropriate boxes of 4b in Block B of the worksheet and the final weight of the labeled measurement in column 4 of Block B.
- 10. The difference between the weights of the labeled measurement for two packages must not exceed that value given in Table 4-2 (Section 4.4.). If the weights do differ by more than that value in Table 4-2, all the packages in the sample must be opened, measured individually and compared against the labeled measure to determine the package errors. If Table 4-2 criterion is met, go on to step 11.
- Calculate the average weight of the labeled measurement and record in 5b in Block B of the worksheet.
- 12. Determine the tare weights of the rest of the tare sample (if any). Record the tare in Block A of the worksheet. Average the tare weights. Record the package errors for the tare sample packages.
- 13. The average weight of the labeled measurements (step 11) plus the average tare weight (step 12) equals the "nominal gross weight" to be used to check the gross weight of the unopened packages in the sample. Record the nominal gross weight in Block A of the worksheet.
- 14. Convert the MAV to units of weight.

MAV (in units of weight) =

avg. wt of label meas. x MAV (length, area)

Record MAV in units of weight in box 7 of Block B on the worksheet and in box 5 on the report form.

Select an appropriate unit of measure in terms of weight (see Section 2.9.2.). With all measurements converted to weight, go to step 15 of Section 3.5. to determine lot conformance. Convert package errors in weight to length or area when completing the report form.

5.4. SPECIAL COMMODITY: POLYETHYLENE SHEETING

Polyethylene sheeting is sold not only by its linear or area measurement, but also by its thickness. The procedure to check thickness is based on the NBS Voluntary Product Standard PS 17-69, "Polyethylene Sheeting (Construction, Industrial, and Agricultural Applications)."

First the dimensions of the sheeting are checked, as in Section 5.3.2. which follow's Decision Chart 4. If the dimensions conform to the package requirements, the thickness of the sheeting is then checked (this portion of the procedures does not follow a decision chart). All the sample packages are opened for thickness measurements.

A worksheet is provided to record length, width and thickness measurements for polyethylene sheeting.

5.4.1. Equipment

<u>Scales and weights</u> recommended in Section 3.1.

Micrometer:

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A deadweight dial micrometer (see Figure 5-1) equipped with a flat anvil, 1/4-in (6-mm) diameter or larger, and a 3/16-in (4.5-mm) diameter flat surface on the head of the spindle. The anvil and spindle head surfaces should be ground and lapped, parallel to within 0.0001 in (0.002 mm), and should move on an axis perpendicular to themselves. The dial spindle should be vertical and the dial should be at least 2 in (50 mm) in diameter. The dial indicator should be continuously graduated to read directly to 0.0001 in (0.002 mm). If capable of making more than one revolution, it must be equipped with a separate indicator to indicate the number of complete revolutions. The dial indicator mechanism should be fully jeweled. The frame should be of sufficient rigidity that a load of 3 lbf (13 N) applied to the dial housing, exclusive of the weight or spindle presser foot, will not cause a change in indication on the dial of more than 0.001 in (0.02 mm).

WORKSHEET FOR CHECKING POLYETHYLENE SHEETING

Labe	eled Length								
Labe	eled Width								
Labe	eled Thicknes	s	0.8 imes Labeled Thi	ckness	Co	mpare with All Th	ickness Measurem	ents	
			0.93 $ imes$ Labeled TI	nickness	Co	mpare with Averag	e Package Thickno	ess	
Package Length Width			Thickness	Package	Length	Width	Thickness		
Package			l					1	
Average			· · · · · · · · · · · · · · · · · · ·						
Package									
Average					1				
				_				_	
				_					
				_					
,								_	
Package Average									
				-					
Package			I				<u>I</u>		
Average			····						
	_								
Package Average			· · · · · · · · · · · · · · · · · · ·	V////					
Sample					ı <u> </u>				

The indicator reading must be repeatable to 0.00005 in (0.0012 mm) at zero setting.

Weight on probe head (total of anvil, weight, spindle, etc.) must be 4 oz (113.6 g).

 Electronic or motor-driven comparator with same specifications as above.

<u>Steel tape rules</u> recommended in Section 5.3.1.

T-square.

5.4.2. Preparation for Test

Gage blocks covering the range of thicknesses to be tested should be used to check the accuracy of either the micrometer or the comparator and should be maintained without rust, tarnish, or scratches. The micrometer or comparator should be operated in an atmosphere free from drafts and fluctuating temperature and should be allowed to stabilize at ambient room temperature before use.

Place the deadweight dial micrometer or comparator on a solid, level table, free from excessive vibration. Check the weight of the deadweight used with the spindle head. It should have a weight of about 3.6 oz.



Figure 5-1. Deadweight dial micrometer.

If the dial does not read zero with nothing between the anvil and the spindle head, set it at zero. Raise and lower the spindle head or probe several times and check to see if it indicates zero each time. If it does not, find the cause and correct it before proceeding. The accuracy of the micrometer or comparator should be checked with appropriate gage blocks whenever the device is moved to a different location and at the beginning of each day's use of the device.

5.4.3. Procedure

Steps 6a and 8a below apply to rolled product, 6b and 8b to folded product. Steps 10a and b apply to a two-stage MAV and therefore both steps 10a and 10b are followed for any single product test.

- 4. See Section 3.5., steps 1 through 4 for instructions on filling out the report form heading and selecting the random sample and random tare sample. Separate report forms for length (width), area, and thickness should be appended to one another. The MAV for dimensions is found in Table 2-11. The MAV's for thickness are listed in Section 2.13. and in step 10a and b below.
- Gross weigh the packages chosen for tare, open them, and record the gross weights in Block A of the worksheet.
- Weigh the first package net contents and record in column 1 of Block B. Extend the first package to its full dimensions, and remove by hand all creases and folds as far as possible.

Measure the length and width of the product to the closest 1/8 in (3 mm). Make all measurements at intervals uniformly distributed along the length and width of the product. Record the individual measurements in the polyethylene worksheet. Compute the average length and width and record on the special worksheet.

- With rolls of product, make three length measurements along the width of the roll and at least ten width measurements along the length of the product.
- b. In the case of a product that is folded, such as drop cloths or tarpaulins, make three length measurements along the width of the sample and three width measurements along the length of the sample.
- Follow steps 7 through 14 of Section 5.3.2. to determine whether the inspection lot conforms with the package

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requirements on length and width. If the lot fails to conform, thickness need not be checked.

- Measure the thickness of the plastic sheet with a micrometer or comparator at:
 - a. five uniformly distributed locations across the width at each end and 5 locations along each side of each roll in the sample, or;
 - five uniformly distributed locations across the width at one end and along the length at one side of folded product for each package in the sample.

When measuring the thickness, place the sample between the micrometer or comparator surfaces and lower the spindle head or probe near, but outside of the area where the measurement will be made. Raise the spindle head or probe a distance of 0.0003 to 0.0004 in (0.008 to 0.01 mm) and move the sheet to the measurement position. Drop the spindle head onto the test area of the sheet. Read the dial thickness 2 seconds or more after the drop, or when the dial hand or digital readout becomes stationary. This procedure minimizes small errors present when the spindle head or probe is lowered slowly onto the test area.

For succeeding measurements, raise the spindle head or probe 0.0003 to 0.0004 in (0.008 to 0.01 mm) above the rest position on the test surface, move to the next measurement location, and drop the spindle head onto the test area. Care should be taken not to raise the spindle head or probe more than 0.0004 in or 0.01 mm above its rest position on the test area. Any part of the test area in contact with the spindle head or probe during measurement must be at least 1/4 in or 6 mm from the edge of the sheet.

Record all thickness measurements on the polyethylene worksheet. Compute the average thickness for the individual package and record this thickness.

- Repeat step 8 on the remaining packages in the sample.
- In Section 2.13., the MAV for polyethylene was described to apply in two stages. Follow both a and b below.
 - a. No single measurement of thickness should be less than 80% of the labeled thickness.

Circle any value in the thickness columns of the worksheet which is smaller than (0.8 x labeled thickness). If the number of values circled exceeds the number recorded in box 13 of the report form, the lot fails to conform to requirements.

No further testing of the lot is necessary. If this number of circled thickness measurements is equal to or less than the box 13 value, go on to step 10b.

b. The average thickness for any single package should be at least 93% of the labeled thickness.

Circle any package average thickness value which is smaller than $(0.93 \times labeled thickness)$.

If the number of package average thicknesses circled⁶ exceeds the number recorded in box 13 of the report form, the lot fails to conform to requirements. No further testing of the lot is necessary. If this number of circled package average thicknesses is equal to or less than the box 13 value, go to step 17 of Section 3.5. to determine lot conformance with respect to average thickness.

5.5. SPECIAL COMMODITY: PAPER PLATES⁷

The plate count is first checked against requirements for the average, then the plate size is checked. The procedure does not follow a decision chart.

⁶Count circled average thicknesses only; do not include circled individual thicknesses in this count.

⁷Equipment and method derived from those provided by Mr. William Marks, American Can Co., 333 No. Commercial St., Neenah, WI 54956.

5.5.1. Equipment

<u>Scales and weights</u> recommended in Section 3.1.

<u>Measuring base</u> of any flat, sturdy material approximately 15 in (40 cm) square. Two vertical side pieces approximately 1 in (3 cm) high and the same length as the sides of the measuring base are attached along two adjoining edges of the measuring base to form a 90° corner.

Graph paper, 20 divisions per inch (10 divisions per centimeter).

5.5.2. Preparation for Test

Trim all white borders from 2 or more sheets of graph paper. Place one sheet on the measuring base and position it so that one corner of graph paper is snug in the corner of the measuring base and vertical sides; tape the sheet to the measuring base. Overlap other sheets on the first sheet so that the lines of top and bottom sheet coincide, expanding the graph area to a size bigger than plates to be measured; these sheets are also taped to the measuring base. Number each inch (centimeter) line from the top and left size of base plates: 1,2,3, etc.

5.5.3. Procedure

- Follow the procedures in Section 5.1. or 5.2. (depending on the labeled count) to determine lot conformance with respect to count. If the lot • conforms, go on to step 2 below.
- The sample selected for determining lot conformance with respect to count may be used to determine conformance with respect to dimensions; however, the inspector may have to select additional packages for the sample. For example if the lot size is between 251 and 500 packages, and a category B

plan will be used to check dimensions, Table 5-1 permits a sample size of 10 packages for packages labeled by low count but Table 2-5 requires a sample size of 30 packages for this lot size for checking dimensions.

For low count packages, check sample size required according to Table 2-2 or 2-5 and if necessary, select additional packages for the sample. A tare sample is not needed in this part of the procedure.

Select one plate from each package to represent that package⁸.

 Place each plate to be measured eating surface down on the measuring base plate. Locate the plate in the corner of the measuring base so that two sides of the plate are touching the two vertical side pieces (See Figure 5-2).

> Rest the palm of your hand on the plate to ensure that plate is flat and read the plate diameter.



- Figure 5-2. Preparing to measure the dimensions of a paper plate.
- The package error is equal to the plate diameter minus the labeled diameter. Record the package error on Block A of the worksheet and, using an

⁸Certain packages of plates contain a combination of plates of differing sizes. In this instance, a plate of each declared size is taken from the package to represent all the plates of that size in the package. If three sizes are declared, for example, three plates are selected from each package. Upon occasion, packages of plates declared to be of one size may contain plates which can visually be seen to be of different sizes in the same package. In this instance, select the smallest plate, and using the methods above, determine the package error for the smallest. If the smallest plate is not short measure by more than the MAV, all the different sizes of plates in the package will have to be checked and the average dimensions of the package calculated. For example, if 5 plates measure 8 7/16 in and 15 measure 8 9/16 in, the average dimension for this package of 20 plates is 8.53 in.

appropriate unit of measure, transfer to a report form (separate from the form used to record count).

5. Repeat steps 3 and 4 for all the packages in the sample. Go to step 16 of section 3.5. to determine lot conformance.

5.6. SPECIAL COMMODITY: SANITARY PAPER PRODUCTS⁹

The labeled count is first checked and is followed by a check on the linear measurements. The procedure does not follow a decision chart.

These products often declare total area as well as unit count and sheet size declarations. If the actual sheet size measurements and the actual count comply with the average requirements, the total area declaration is assumed to be correct.

5.6.1. Equipment

<u>Scales and weights</u> recommended in Section 3.1.

<u>Plastic sheet</u>, 1/8 to 1/2 in (0.3 to 2 cm) thick, 20 by 20 in (50 by 50 cm).

Rule, 12 in (30 cm) in length, 0.01 in (0.5 mm) divisions.

The measurements are easier to make if two rules are inlaid flush with a working surface, perpendicular to each other.

5.6.2. Procedure

- Follow the procedures in Section 5.1. or 5.2. to determine lot conformance with count requirements.
- If necessary, select additional packages for the sample to be checked for dimensions (as in Section 5.5.3., step 2). A tare sample is not necessary.
- Select one sheet, napkin, etc. from each package, place the product between the working surface and the plastic plate (removing creases if necessary) and measure and record its dimensions.
- 4. The package error is equal to the actual dimension minus the labeled dimension. Record the package errors on Block A of the worksheet, and using an appropriate unit of measure, transfer them to a report form separate from the form used to record count.
- 5. Repeat steps 3 and 4 for all the packages in the sample. Go to step 16 of Section 3.5. to determine lot conformance.

5.7. PACKAGES GIVEN TOLERANCES

The package requirement that the <u>average</u> quantity of a lot (shipment or delivery) meet or exceed the labeled quantity is not applied to that category of products to which a "tolerance" or "allowable difference"¹⁰ has been provided by regulation. When a

Reference to the

⁹Derived from apparatus and method by Mr. William Marks, American Can Co., Neenah, WI 54956. ¹⁰The National Conference on Weights and Measures (NCWM) Model State Method of Sale of Commodities Regulation (MoS) is a voluntary standard for State regulatory use which is periodically updated by State agency representatives. The 1980 edition of NBS Handbook 130 which contains the current NCWM model regulations lists the following "allowable differences". Individual State regulations may permit or not permit the following or other allowable differences.

Product	Allowable difference	NCWM Mos		
pressed and blown tumblers and stemware labeled by count and and capacity	inch-pound: ± 1/4 oz for items less than or equal to 5 oz; ± 5% for items greater than 5 oz.	Section 3.2.1.		
	metric: ± 10 mL for items less than or equal to 200 mL; ± 5% for items greater than 200 mL.			
	F 11			

tolerance is provided in a regulation, a minimum net quantity is defined for the packages in the lot. If any and all packages in a lot are allowed to be less than the declared quantity by a certain amount, then the average net quantity of those packages cannot be expected to meet some higher value.

The sampling plans in Table 5-2 are provided for all such products. and blown products is an allowable difference requirement. The procedure does not follow any of the decision charts. Equipment is the same as recommended in Section 4.13.1.

 Follow the procedures in Section 5.1. or 5.2. (depending on the labeled count) to determine conformance of the lot with respect to count.

1	2	3	4
Lot size N	Sample size n	Tare sample size ⁿ t	Number of package errors which may exceed allowable difference
Up to and including 500 501-5,000 5,001 and over	10 30 50	2 2 5	0 1 2

Table 5-2.	Sampling	plans	for	packages	given	to	lerances
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To use the sampling plans in Table 5-2 the inspection lot is identified and a random sample following Appendix C methods is selected according to the size of the lot.

The packages in the sample are measured following an appropriate procedure (Section 5.7.1. is provided for tumblers and stemware.) Each package error is compared with the applicable allowable difference. The number of packages with package errors greater than the allowable difference is counted and compared with the number given in column 4 of Table 5-2. If the number in column 4 is exceeded, the lot fails to conform with the package requirements. If the number of packages with errors exceeding the allowable difference is less than or equal to the number in column 4 above, the lot conforms. No calculation of the average package error is made. The lot conforms or fails based on the individual package errors only. Individual packages exceeding the allowable difference are acted upon individually even though the requirements for the lot may be met.

5.7.1. Tumblers/Stemware

This section describes how to test tumblers and stemware which are labeled by count and capacity. The package count must meet the requirements for the average; the individual units (tumblers, stemware) must meet the requirements for capacity, which for pressed Keep the packages in the order in which the random numbers were recorded from the random number table.

If the lot conforms to requirements for count, go on to step 2 below.

 The same packages selected for the sample to be tested for count may be used to test for capacity. Since a different sampling plan will be used, a different sample size may be needed.

> For example, an inspection lot of 7 oz, 15 count, plastic glasses is composed of 500 packages. A Category B plan is used to check the count. Referring to Table 2-5, a sample size of 30 is selected to be checked for count. The lot is found to conform to the average requirements for count. Referring to Table 5-2, a sample size of 10 is adequate for checking the labeled capacity. Therefore, the 10 packages which are associated with the first 10 random numbers that were selected from the random number table become the sample to be checked for capacity.

Every package is checked. (No tare sample is needed.)

Unless the tumbler or stemware is glass, one tumbler per package is sufficient to determine capacity of all units in that package. If the tumbler, etc. is glass, the capacity of all the containers in the package is determined.

- Follow Section 4.13.2., steps 5, 6, and 7 on each item to be checked (either one tumbler or piece of stemware from each package in the sample or, if glass, all the tumblers or pieces of stemware from each sample package). Use separate worksheets from those used to record labeled count.
- 4. The package (or tumbler) error is equal to the volume capacity as measured minus the labeled capacity. Record the package error on the report form. If capacity has been measured for every unit in the package, note on the report form to refer to the worksheet(s) for the appropriate individual unit error.
- Compare each package (or if glass, each tumbler/stemware) error with the allowable difference. If any package or tumbler/stemware error exceeds the allowable difference (either positive or negative errors), circle that error.
- Compare the total number of circled errors with Table 5-2 column 4 value corresponding to the sample size.

For example, if the sample size is 30, one package or tumbler/stemware error in the sample can exceed the allowable difference.

If the number of circled errors is more than the column 4 value of Table 5-2, the lot fails to conform to the package requirements. If the number of circled errors is less than or equal to the value in Column 4 of Table 5-2, the lot conforms with the package requirements.

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APPENDIX	A:	GLOSSARY OF TERMS
APPENDIX	B:	PACKAGE NET CONTENTS REGULATIONS
APPENDIX	C:	SELECTION OF A RANDOM SAMPLE
APPENDIX	D:	AUXILIARY TABLE FOR RANDOM STARTING PLACE
APPENDIX	E:	RANDOM NUMBER TABLE
APPENDIX	F:	CALCULATION OF THE AVERAGE RANGE
APPENDIX	G:	CERTAIN EQUIPMENT TOLERANCES



APPENDIX A. GLOSSARY OF TERMS

ACCEPTANCE TOLERANCE.¹ The limit of inaccuracy for new, newly reconditioned, or adjusted equipment. (See Section 3.1.)

ALLOWABLE DIFFERENCE. The amount by which the actual quantity in the package may differ from the declared quantity. Pressed and blown tumblers and stemware labeled by count and capacity are given an allowable difference in capacity. (See Section 5.7.)

ANALOGUE SCALE. A weighing device in which weight values are indicated by means of "a series of graduations in combination with an indicator, or in which the most sensitive element of an indicating system moves continuously during the operation of the device."¹ (See Section 3.7.)

AUDIT TESTING. Preliminary tests designed to quickly seek out a potential case of noncompliance. (See Section 1.5.)

AVERAGE. The sum of a number of individual measurement values divided by the number of values. For example, the sum of the individual weights of 12 packages divided by 12 would be the average weight of those packages.

AVERAGE ERROR. The sum of the individual package errors (defined) (considering their arithmetic sign) divided by the number of packages comprising the sample. (See Section 2.6.2.)

AVERAGE REQUIREMENT. (See Section 1.2.1.)

AVERAGE TARE. The sum of the weights of individual package containers (or wrappers, etc.) divided by the number of containers or wrappers weighed.

AVOIRDUPOIS UNITS. The inch-pound unit (defined) for weight commonly used in the United States of America, based on the pound of 16 ounces and the ounce of 16 drams.

BERRY BASKETS AND BOXES.¹ Disposable containers for berries and small fruits in capacities of 1 dry quart or less.

BREAK POINT. That point at which a digital indicator changes its indication from one value to an adjacent value. (This is determined by adding test weights 0.1 of the value of the smallest indication until the break point is reached.) (See Section 3.7.) CATEGORY A (CATEGORY B). A set of sampling plans provided in this handbook for use in checking packages which must meet the average requirement (defined). (See Section 1.8. See Section 2.6. for Category A, and Section 2.7. for Category B.)

CODE NUMBER. A series of identifying numbers and/or letters on the outside of a package designed to provide information such as the date and location of packaging, the expiration date, and so on.

COMBINATION QUANTITY DECLARATIONS.² A package label that contains the count of items in the package as well as one or more of the following: weight, measure, or size.

COMPLIANCE TESTING. The determination of conformance of packages with specified legal requirements.

CORRECTED AVERAGE TARE. For foam product aerosols (defined), this is the average tare (defined) as measured minus the test allowance (defined). (See Section 3.9.6. and Table 3-2.)

DECISION CRITERIA. The rules for deciding whether a lot is in conformance with package requirements or not based on the results of checking the packages in the sample. (See Sections 2.6.1., 2.6.2., 2.7.1., and 2.7.2.)

DELIVERY. A quantity of identically labeled product received at one time by a buyer.

DIMENSIONLESS UNITS. The integers in terms of which the official records package errors. The dimensionless units must be multiplied by the unit of measure (defined) to obtain package errors in terms of weight, length, etc. (See Section 2.9.1.)

DISPOSABLE CONTAINERS. A package container designed to be used only once.

DIVISION¹ (on a scale). A defining line, or one of the lines defining the subdivisions of a graduated series.

DRAINED WEIGHT. The weight of solid or semisolid product representing the contents of a package obtained after a prescribed method for excluding the liquid has been employed. (See Section 3.8. and 3.11.)

 1 NBS Handbook 44, 1980. 2 NBS Handbook 130, 1980, Model State Method of Sale of Commodities Regulation. DRY MEASURES.³ Rigid containers designed for general and repeated use in the volume measurement of particulate solids.

DRY TARE. All packaging materials (including glue, labels, ties, etc.) that will contain or enclose the product but before the product is introduced into the container. Prizes, gifts, coupons, or decorations which are not part of the product are defined as part of the tare also. (See Section 2.11.)

ERROR. See PACKAGE ERROR.

ERROR LIMIT. In Category A sampling plans, the value that is calculated if the average error of the sample is a minus value. The error limit (denoted as "T") is then added to the sample average error before applying the decision criterion on the average. (See Section 2.6.2.)

FOAM PRODUCT AEROSOL. A product that forms a foam at the container valve or on impingement with a surface, the foam volume not being substantially reduced for at least 20 seconds.

FLUSH FILL CAPACITY. The capacity of a cup or container as defined by the volume contained by it when a flat plate (such as a slicker plate (defined)) rests on its rim.

GROSS WEIGHT. The weight of the package including contents, packing material, labels, etc.

HEADSPACE. The container volume not occupied by product.

INDEX OF AN INDICATOR. That particular portion of an indicator (as, for example, on a weighing scale) that is directly utilized in making a reading (e.g., the tip of a movable pointer on a dial) (See Section 3.4.)

INCH-POUND UNITS. Units based upon the yard, gallon, and the pound commonly used in the United States of America. Some of these units have the same name as similar units in the United Kingdom (British, English, or UK units) but are not necessarily equal to them.

INITIAL TARE SAMPLE. The first packages (either two or five) selected from the sample to be opened for tare determination in the alternative tare procedure. Depending upon the variability of these individual tare weights as compared with the variability of the net contents, this initial tare sample may be sufficient or more packages may be needed to determine the tare. (See Section 2.11.4. and Table 2-6.)

INSPECTION LOT. The collection of identically labeled (except for actual quantity in the case of random pack) packages available for inspection at one time. This collection will pass or fail as a whole based on the results of tests on a sample drawn from this collection. (See Section 2.3.)

LABEL.⁴ "Any written, printed, or graphic matter affixed to, applied to, attached to, blown into, formed, molded into, embossed on, or appearing upon or adjacent to a consumer commodity or a package containing any consumer commodity, for purposes of branding, identifying, or giving any information with respect to the commodity or to the contents of the package, except that an inspector's tag or other nonpromotional matter affixed to or appearing upon a consumer commodity...[is]...not...a label."

LOCATION OF TEST. The place where the official finds the package that he or she will examine. Broadly defined as three general locations: (1) where the commodity was packaged, (2) a warehouse or storage location; or (3) a retail outlet.

LOT. See INSPECTION LOT.

LOT SIZE. The number of packages in the inspection lot (defined). (See Section 2.3.3.)

LUBRICATING OIL BOTTLES.⁵ A rigid (inflexible) measure container (defined) for repeated use in "measurement of lubricating oil for direct delivery to the crankcase of a motor vehicle, whether or not the bottle is sealed with a cap or some other device."

MAV (MAXIMUM ALLOWABLE VARIATION). A deficiency in the weight, measure, or count of an individual package beyond which the deficiency is considered to be an unreasonable error (the number of packages with deficiencies greater than the MAV is controlled by the sampling procedure). (See Section 2.12.)

MEAN OR ARITHMETIC MEAN. See AVERAGE.

³NBS Handbook 44, 1980.
⁴NBS Handbook 130, 1980, Model State Packaging and Labeling Regulation.
⁵NBS Handbook 44, 1980.

MEASURE CONTAINERS.⁶ Measure containers are containers whose capacities are used to determine quantity. They are of two basic types, (a) retail and (b) prepackaged. Retail containers are packaged at the time of retail sale and prepackaged containers are packaged in advance of sale. An example of a prepackaged measure container is an ice cream package.

METERED VALVE. A push-button operated aerosol delivery device that meters a pre-determined quantity of product when depressed and then shuts off automatically. No additional product will be expelled until the push button is released and depressed again to repeat the procedure.

MILK BOTTLES.⁶ A container that is designed as a measure container (defined) for repeated use in the measurement and delivery of milk and other fluid dairy products at retail.

MINUS OR PLUS ERRORS. Negative or positive deviations from the labeled quantity of the actual package quantities as measured. (See PACKAGE ERRORS.)

MOISTURE ALLOWANCE. That variation in weight of a packaged product permitted in order to account for loss of weight due to loss of moisture during good package distribution practices. (See Sections 1.9., 2.14., Step 13 of Section 3.5.)

NET QUANTITY OR NET CONTENTS. That quantity of packaged product remaining after all necessary deductions for tare (defined) have been made.

NOMINAL.⁶ "Refers to 'intended' ... as opposed to 'actual'."

NOMINAL GROSS WEIGHT. The sum of the nominal tare weight (defined) plus the declared or labeled weight (or other labeled quantity converted to a weight basis). (See Section 2.11. and step 13. of Section 3.5.)

NOMINAL TARE WEIGHT. The quantity designated as tare (defined) and used in the

determination of the nominal gross weight. It may be an average tare value or a corrected average tare value.

NULL INDICATOR. A device or portion of device used to indicate a "zero" or load-balanced condition.

OBSERVED VALUE. A particular quantity determined as the result of an observation, test, or measurement.

PACKAGED GOODS.⁷ "Product or commodity put up in any manner in advance of sale suitable for either wholesale or retail sale."

PACKAGE ERROR. The difference between the actual net contents of an individual package as measured and the declared net contents on the package label; (-) minus for less than the label and (+) plus for more than the label. (See Section 2.9.)

POISE.⁵ "A movable weight mounted upon or suspended from a weighbeam bar and used in combination with graduations, and frequently with notches, on the bar to indicate weight values."

PRINCIPAL DISPLAY PANEL.⁸ "The term 'principal display panel or panels' shall be construed to mean that part, or those parts, of a label that is, or are, so designed as to most likely be displayed, presented, shown, or examined under normal and customary conditions of display and purchase. Wherever a principal display panel appears more than once on a package, all requirements pertaining to the 'principal display panel' shall pertain to all such 'principal display panels'."

PRODUCTION LOT. The total collection of packages defined by the packager and usually defined as those packages produced within a certain unit of time and coded identically.

PYCNOMETER. A container of known volume used to contain material for weighing so that the weight of a known volume may be

⁶NBS Handbook 44, 1980.

⁷16 CFR §500.2(h).

⁸NBS Handbook 130, 1980, Model State Packaging and Labeling Regulation.

determined for the material. (See Section 4.10.)

RANDOM PACK.⁹ That type of package in which a commodity is measured, packaged and then labeled individually in a variety of quantity sizes and with no fixed quantity pattern. In many cases these packages are put up in the retail store or central distribution point. Although commonly labeled by weight (e.g., meat), linear or square measure (e.g., yard goods) is also encountered.

RANDOM SAMPLING. The process of selecting sample packages such that all packages under consideration have the same probability of being selected. An acceptable method of random selection is to use a table of random numbers (see Appendices C, D, and E).

RANGE. The difference between the largest and the smallest of a set of measured values. (See Appendix F.)

REASONABLE VARIATIONS. The amount by which individual package net contents may vary from the labeled net contents. This term is found in most Federal and State laws and regulations governing packaged goods. (See Appendix B.) This handbook defines the limits of reasonable variation only in terms of negative deviations from the label and terms these limits "Maximum Allowable Variations."

ROUNDING. To round a numerical value is the process of omitting certain of the end digits of a number and adjusting the last digit retained so that the resulting number is as near as possible to the original number. (See Section 3.4.)

SAMPLE. A group of packages taken from a larger collection of packages and providing information that can be used as a basis for making a decision concerning the larger collection of packages or of the package production process.

SAMPLE SIZE. The number of packages in a sample.

SAMPLING PLAN. A specific plan that states the number of packages to be checked and the associated decision criteria. (See Section 1.4.) SCALE TOLERANCE. The value fixing the limit of allowable error for commercial weighing equipment as defined in NBS Handbook 44.

SEAT (as in "seat diameter" or "seated capacity"). The projection or shoulder near the upper rim of a cup or container that is designed to serve as the support for a lid or cover.

SEATED CAPACITY. The capacity of a cup, container, or bottle, as defined by the volume contained by them when the lid or a flat disc is inserted in the lid groove located inside and near the upper rim of the cup, container, or bottle. (See Section 4.13.)

SENSITIVITY (of scale). The relative displacement of an index of an indicator with respect to a graduated scale for a given change in weight. (See Section 3.1.)

SHIPMENT. A quantity of identically labeled product sent at one time to a single location.

SLICKER PLATE. A flat plate usually of glass or clear plastic composition used to determine the "level full" condition of a capacity (volumetric) measure. (See Section 4.10.)

STANDARD DEVIATION. A measure of the scatter of the individual package contents around the mean contents. (See Section 2.6.2.)

STANDARD PACK. That type of package in which a commodity is put up with identical labels and only in certain selected quantity sizes. Examples are canned, boxed, bottled and bagged foods, and over-the-counter drugs.

SUBSTITUTION WEIGHING. The use of a commercial scale as a "null indicator" (defined); that is, the weight of the package or product is determined by using the official's test weights (defined) with the commercial scale serving merely as an indicator for a "zero" or load balanced condition and not as an indicating device. (See Section 3.7.)

⁹NBS Handbook 130, 1980 in the Model State Packaging and Labeling Regulation defines random package as the following, "The term 'random package' shall be construed to mean a package that is one of a lot, shipment, or delivery of packages of the same consumer commodity with varying weights; that is, packages of the same consumer commodity with no fixed pattern of weight."

SUPPLEMENTARY QUANTITY DECLARATIONS.¹⁰ "The required quantity declaration may be supplemented by one or more declarations of weight, measure, or count, such declaration appearing other than on a principal display panel. Such supplemental statement of quantity of contents shall not include any terms qualifying a unit of weight, measure, or count that tends to exaggerate the amount of commodity contained in the package (e.g., 'giant' quart, 'full' gallon, 'when packed', 'minimum', or words of similar import)."

SURVEY TESTING. See audit testing.

TAPE RULES.¹¹ Flexible steel linear measures.

TARE. The weight of a container, wrapper, or other material (see discussion in Section 2.11.) that is deducted from the gross quantity to obtain the net quantity.

TARE SAMPLE. The packages or packaging material used to determine the average tare weight. (See Section 2.11.)

TARE SAMPLE SIZE. The number of packages or packaging material units used to determine the average tare weight. (See column 3 of Tables 2-2 or 2-5.)

TEST ALLOWANCE. An allowance made to compensate for differences in delivery of foam aerosol packaged products between normal consumer usage and the test procedure. (See Section 3.9.6.)

TEST WEIGHTS. Weights of known value used to check the accuracy of package quantities and scales (also used in substitution weighing). (See Section 3.1.)

TOLERANCE. A value fixing the limit of allowable departure from the labeled contents; usually presented as a (+) and a (-) value. (See Sections 1.2.2. and 5.7.)

UNIT OF MEASURE. An increment of weight, length, or volume chosen so that an inspector may record package errors in terms of small integers, (whereas the package errors are actually the integers multiplied by the unit of measure). (See Section 2.9.1.)

UNREASONABLE ERRORS. Minus package errors that exceed the MAV. (See step 16 of Section 3.5.)

¹⁰16 CFR §500.20. ¹¹NBS Handbook 44, 1980. VALVE ACTUATOR (VALVE BUTTON). The push button located on the top of the aerosol package that controls the flow of product by means of a valve.

VAPOR TAP VALVE. A push button aerosol delivery device that will expel product whether the container is in the upright or inverted position.

VOLUMETRIC MEASURES. Field standard measuring flasks, graduates, cylinders, etc. for use in the measurement of volumes of liquids. (See Section 4.2.)

WET TARE. All packaging materials that can be separated from the packaged product after packaging. Washing, scraping, ambient air drying, and other techniques involving more than "normal" household recovery procedures may be used but laboratory procedures such as oven drying the packaging material are not used. As in the dry tare definition, prizes, decorations, and such are also part of the wet tare. (See Section 2.11.)

Certain portions of the Federal and State regulations which refer specifically to labeled net contents on packages are listed below.

B.1. FEDERAL REGULATIONS

References are taken from the July, 1980, Code of Federal Regulations.

B.1.1. U.S. Department of Health and Human Services, Food and Drug Administration

Food 21 CFR §101.105

(q) The declaration of net quantity of contents shall express an accurate statement of the quantity of contents of the package. Reasonable variations caused by loss or gain of moisture during the course of good distribution practice or by unavoidable deviations in good manufacturing practice will be recognized. Variations from stated quantity of contents shall not be unreasonably large.

Food, aerosols 21 CFR §101.105

(g) The declaration shall accurately reveal the quantity of food in the package exclusive of wrappers and other material packed therewith: Provided, That in the case of foods packed in containers designed to deliver the food under pressure, the declaration shall state the net quantity of the contents that will be expelled when the instructions for use as shown on the container are followed. The propellant is included in the net quantity declaration.

Prescription drugs 21 CFR §201.51

(g) The declaration of net quantity of contents shall express an accurate statement of the quantity of contents of the package. Reasonable variations caused by loss or gain of moisture during the course of good distribution practice or by unavoidable deviations in good manufacturing practice will be recognized. Variations from stated quantity of contents shall not be unreasonably large. In the case of a liquid drug in ampules or vials, intended for injection, the declaration shall be considered to express the minimum quantity and the variation above the stated measure shall comply with the excess volume prescribed by the National Formulary or the U.S. Pharmacopeia for filling of ampules. In the case of solid drug in ampules or vials, the declaration shall be considered to express the accurate net weight. Variations shall comply with the limitations provided in the U.S. Pharmacopeia or the National Formulary.

Over-the-counter drugs, aerosols 21 CFR §201.62

(f) The declaration shall accurately reveal the quantity of drug or device in the package exclusive of wrappers and other material packed therewith: Provided, That in the case of drugs packed in containers designed to deliver the drug under pressure, the declaration shall state the net quantity of the contents that will be expelled when the instructions for use as shown on the container are followed. The propellant is included in the net quantity declaration.

Over-the-counter drugs 21 CFR §201.62

(q) The declaration of net quantity of contents shall express an accurate statement of the quantity of contents of the package. Reasonable variations caused by loss or gain of moisture during the course of good distribution practice or by unavoidable deviations in good manufacturing practice will be recognized. Variations from stated quantity of contents shall not be unreasonably large.

Cosmetics, aerosols 21 CFR §701.13

(g)(1) In the case of cosmetics packed in containers designed to deliver the cosmetic under pressure, the declaration shall state the net quantity of the contents that will be expelled when the instructions for use as shown on the container are followed. The propellant is included in the net quantity declaration.

Cosmetics 21 CFR §701.13

(s) The declaration of net quantity of contents shall express an accurate statement of the quantity of contents of the package. Reasonable variations caused by loss or gain of moisture during the course of good distribution practice or by unavoidable deviations in good manufacturing practice will be recognized. Variations from stated quantity of contents shall not be unreasonably large.

Medical devices 21 CFR §801.62

(q) The declaration of net quantity of contents shall express an accurate statement of the quantity of contents of the package. Reasonable variations caused by loss or gain of moisture during the course of good distribution practice or by unavoidable deviations in good manufacturing practice will be recognized. Variations from stated quantity of contents shall not be unreasonably large.

B.1.2. U.S. Department of Agriculture, Food Safety and Quality Service

Meat 9 CFR §317.2

(h)(2) The statement as it is shown on a label shall not be false or misleading and shall express an accurate statement of the quantity of contents of the container exclusive of wrappers and packing substances. Reasonable variations caused by loss or gain of moisture during the course of good distribution practices or by unavoidable deviations in good manufacturing practice will be recognized. Variations from stated quantity of contents shall not be unreasonably large.

Poultry

9 CFR §381.121

(c)(6) The statement as it is shown on a label shall not be false or misleading and shall express an accurate statement of the quantity of contents of the container, exclusive of wrappers and packaging substances. Reasonable variations caused by loss or gain of moisture during the course of distribution, notwithstanding good distribution practices or by unavoidable deviations, notwithstanding good manufacturing practice will be recognized. Variations from stated quantity of contents shall not be unreasonably large. The statement shall not include any term qualifying a unit of weight, measure or count such as "jumbo quart," "full gallon," "giant quart," "when packed," "minimum" or words of similar import, except as provided in paragraph (b). of this section.

B.1.3. Federal Trade Commission

Non-food consumer commodities are covered under the Fair Packaging and Labeling Act 16 CFR §500.22.

(a) The statement of net quantity of contents shall accurately reveal the quantity of the commodity in the container exclusive of wrappers and other material packed therewith: Provided, That in the case of a commodity packed in a container designed to deliver the commodity under pressure, the statement shall declare the net quantity of the contents that will be expelled when the instructions for use are followed. The propellant is included in that net quantity statement.

(b) Variations from the stated weight or measure shall be permitted when caused by ordinary and customary exposure, after the commodity is introduced into interstate commerce, to conditions which normally occur in good distribution practice and which unavoidably result in change of weight or measure.

(c) Variations from the stated weight. measure or numerical count shall be permitted when caused by unavoidable deviations in weighing, measuring, or counting the contents of individual packages which occur in good packaging practice: Provided, that such variations. shall not be permitted to such extent that the average of the quantities in the packages comprising a shipment or other delivery of the commodity is below the quantity stated, and no unreasonable shortage in any package will be permitted, even though overages in other packages in the same shipment or delivery compensate for such shortage. Variations from stated quantity of contents shall not be unreasonably large.

B.1.4. Environmental Protection Agency

Pesticides (including aerosols) 40 CFR §162.10

(d) Net weight or measure of contents.
 (1) The net weight or measure of content shall be exclusive of wrappers or other materials and shall be the average content unless explicitly stated as a minimum quantity.

(2) If the pesticide is a liquid, the net content statement shall be in terms of

liquid measure at 68 °F (20 °C) and shall be expressed in conventional American units of fluid ounces, pints, quarts, and gallons.

(3) If the pesticide is solid or semisolid, viscous or pressurized, or is a mixture of liquid and solid, the net content statement shall be in terms of weight expressed as avoirdupois pounds and ounces.

(4) In all cases, net content shall be stated in terms of the largest suitable units, i.e., "1 pound 10 ounces" rather than "26 ounces."

(5) In addition to the required units specified, net content may be expressed in metric units.

(6) Variation above minimum content or around an average is permissable only to the extent that it represents deviation unavoidable in good manufacturing practice. Variation below a stated minimum is not permitted. In no case shall the average content of the packages in a shipment fall below the stated average content.

B.1.5. U.S. Department of the Treasury, Bureau of Alcohol, Tobacco and Firearms

<u>Wine</u> 27 CFR §4.37

(e) Tolerances. Statement of net contents shall indicate exactly the volume of wine within the container, except that the following tolerances shall be allowed:

(1) Discrepancies due exclusively to errors in measuring which occur in filling conducted in compliance with good commercial practice.

(2) Discrepancies due exclusively to differences in the capacity of containers, resulting solely from unavoidable difficulties in manufacturing such containers so as to be of uniform capacity: Provided, That no greater tolerance shall be allowed in case of containers which, because of their design, cannot be made of approximately uniform capacity than is allowed in case of containers which can be manufactured so as to be of approximately uniform capacity.

(3) Discrepancies in measure due to differences in atmospheric conditions in various places and which unavoidably result from the ordinary and customary exposure of alcoholic beverages in containers to evaporation. The reasonableness to discrepancies under this paragraph shall be determined on the facts in each case.

(f) Unreasonable shortages. Unreasonable shortages in certain of the containers in any shipment shall not be compensated by overages in other containers in the same shipment.

27 CFR §240.578

Proprietors of bonded wine cellars will be held strictly responsible for the correct determination of the quantity and alcohol content of wine removed. As required by §240.173, appropriate and accurate measures and instruments for measuring and testing the wine must be provided at each wine cellar. Bottles must be filled as nearly as possible to conform to the amount shown on the label or blown in the bottle to be contained therein, but in no event may the amount of wine contained in any bottle, due to lack of uniformity of the bottles, vary more than two percent from the amount stated to be contained therein; and further in such case there shall be substantially as many bottles overfilled as there are bottles underfilled for each lot of wine bottled.

<u>Distilled spirits</u> 27 CFR §5.47 and 27 CFR §5.47a

(b) Tolerances. The following tolerances shall be allowed:

(1) Discrepancies due to errors in measuring which occur in filling conducted in compliance with good commercial practice.

(2) Discrepancies due to differences in the capacity of bottles, resulting solely from unavoidable difficulties in manufacturing such bottles to a uniform capacity: Provided, That no greater tolerance shall be allowed in case of bottles which, because of their design, cannot be made of approximately uniform capacity than is allowed in case of bottles which can be manufactured so as to be of approximately uniform capacity.

(3) Discrepancies in measure due to differences in atmospheric conditions in various places and which unavoidably result from the ordinary and customary exposure of alcoholic beverages in bottles to evaporation. The reasonableness of discrepancies under this paragraph shall be determined on the facts in each case. 27 CFR §19.397

(b) Variations in proof and fill. If the contents do not agree with the respective data on the label or bottle as to -

(1) Quantity (fill), except for such variations in measuring as may occur in filling conducted in compliance with good commercial practice with the overall objective of maintaining 100 percent fill for all bottled products; and/or

(2) Proof, subject to a normal drop in proof occurring during bottling operations not to exceed three-tenths of a degree the proprietor shall rebottle, recondition, or label the spirits in such manner that the label will correctly describe the contents.

Beer 21 CFR §245.126 (in part)

The statement of net contents shall indicate exactly the volume of beer within the bottle except for such variations in measuring as may occur in filling conducted in compliance with good commercial practice. Short-fill bottles of beer which are sold or otherwise disposed of by a brewery to its own employees for their own use but which are not for resale need not be labeled, but, if labeled, need not show an accurate statement of net contents.

B.2. STATE REGULATIONS

The National Conference on Weights and Meaures, an organization of State and local weights and measures officials, has adopted voluntary guidelines and standards upon which individual States and other jurisdictions may model their laws and regulations. A majority of the States have adopted the following portion of the National Conference on Weights and Measures Model State Packaging and Labeling Requirements¹ quoted below.

SECTION 7. DECLARATION OF QUANTITY: NONCONSUMER PACKAGES

7.6. <u>CHARACTER OF DECLARATION: AVERAGE</u>. --The average quantity of contents in the package of a particular lot, shipment, or delivery shall at least equal the declared quantity, and no unreasonable shortage in any package shall be permitted, even though overages in other packages in the same shipment, delivery, or lot compensate for such shortage.

SECTION 12. VARIATIONS TO BE ALLOWED.

12.1. PACKAGING VARIATIONS. --

12.1.1. VARIATIONS FROM DECLARED NET QUANTITY. -- Variations from the declared net weight, measure, or count shall be permitted when caused by unavoidable deviations in weighing, measuring, or counting the contents of individual packages that occur in good packaging practice, but such variations shall not be permitted to such extent that the average of the quantities in the packages of a particular commodity, or a lot of the commodity that is kept, offered, or exposed for sale, or sold, is below the quantity stated, and no unreasonable shortage in any package shall be permitted, even though overages in other packages in the same shipment, delivery, or lot compensate for such shortage. Variations above the declared quantity shall not be unreasonably large.

12.1.2. VARIATIONS RESULTING FROM EX-POSURE. -- Variations from the declared weight or measure shall be permitted when caused by ordinary and customary exposure to conditions that normally occur in good distribution practice and that unavoidably result in change of weight or measure, but only after the commodity is introduced into intrastate commerce: <u>Provided</u>, that the phrase "introduced into intrastate commerce" as used in this paragraph shall be construed to define the time and the place at which the first sale and delivery of a package is made within the state, the delivery being either

(a) directly to the purchaser to his agent, or

(b) to a common carrier for shipment to the purchaser, and this paragraph shall be construed as requiring that, so long as a shipment, delivery, or lot of packages of a particular commodity remains in the possession or under the control of the packager or the person who introduces the package into intrastate commerce, exposure variations shall not be permitted.

C.1. Introduction

All of the sampling plans presented in this handbook are based on the assumption that the packages constituting the sample are chosen at random from the inspection lot. Randomness in this instance means that every package in the lot has an equal chance of being selected as part of the sample. It does not matter what other packages have already been chosen, what the package net contents are, or where the package is located in the lot.

To select a random sample requires some care. The procedures which follow present several methods of obtaining a random sample, and a randomly selected subsample for tare. However, they are not the only techniques which may be used. (See Section C.5.)

For the discussion which follows, there are N packages in the inspection lot and there are to be n packages in the sample.

To obtain a random sample, two steps are necessary. First it is necessary to identify each package in the lot of N packages with a specific number as they sit on the shelf or in the warehouse or as they come off the packaging line. Then it is necessary to obtain n random numbers from a table of random numbers. These n random numbers indicate exactly which packages in the lot shall be taken for the sample.

C.2. LOT NUMBERING SYSTEMS

A numbering system or scheme for the lot must be decided upon before getting the random numbers for the sample. There are many methods of numbering the lot, two of which are outlined below.

C.2.1. Serial Lot Numbering System

In a simple arrangement, such as packages on a shelf or on a packing line, the packages in the lot can be considered to be numbered from 1 to N. The testing official does not have to mark the packages with numbers; he or she may imagine each package as having a number associated with it. The official may straighten the packages on the shelf before beginning if it helps to clarify the numbering system in his mind. A simple sketch on a piece of cross-section paper may also be helpful. For example, if the packages are in only one layer, the packages could be found (or arranged) in rows and columns on the shelf, like this (standing in front of and looking down at the shelf):



Imagine that the packages are numbered from 1 to 10 in some systematic fashion, perhaps:



If there is more than one layer of packages, the serial numbering system can be extended, layer by layer. In the example above, the second layer would be considered to be packages numbered 11 through 20, the third layer, packages numbered 21 through 30, etc.

The official can use any numbering scheme he or she wishes as long as each of the N packages has a number associated with it, so that he or she knows where to go to find any particular numbered package. In the 3-layer scheme suggested above, for example with N = 30, package number 26 would be in the third layer, second row from the front, first package on the left.

C.2.2. Three-dimensional Numbering System

If a large stack of packages must be numbered, it may be more convenient to use a three-dimensional lot numbering system. For example, the official may choose some convenient lower left corner of the stack as a "zero point" (starting place). He or she can then use three directions to count from this starting place--to the Right, Up, and toward the Back (RUB). If, from the zero point, there are 10 units to the Right, 3 units Up, and 7 units Back, the dimensions of the stack are 10 by 3 by 7. Unit No. 4-1-5, for example, would be located 4 units to the Right of the zero point, 1 unit Up, and 5 units towards the Back. (See Figure C-1).

C.3. THE RANDOM NUMBER TABLE

C.3.1. General

The random number table in Appendix E contains all digits from 0 through 9, with approximately equal frequency of occurrence. The table consists of 31 pages. On each page digits are printed in blocks of five columns and blocks of five rows. The printing of the table in blocks is intended only to make it easier to locate specific columns and rows.

C.3.2. Random Starting Place.

- a. <u>Starting Page</u>. The pages of Appendix E are numbered El through E31. Use the day of the month to determine the starting page. For example, if the inspection is being done on February 11, use page 11 as the first page (then pages 12 through 31, followed by pages 1 through 10 if necessary).
- Starting Column and Row. Use the b. auxiliary table, Appendix D, to get the starting column and row.¹ This table consists of two pages. On each page there are 600 pairs of numbers. Each pair is shown in parenthesis. The first number of a pair indicates the starting column in Appendix E, and the second number the starting row. The first pair at the upper left hand corner of the first page may be used the first time. After a pair is used, it may be crossed out and another pair used the next time, proceeding systematically either across or down the page.

For example, assume that testing takes place on the llth day of the month. Start with page ll of the random number table in Appendix E. Use the auxiliary table in Appendix D to get a starting place on page ll. If the auxiliary table is being used for the first time, use the first pair of numbers (22, 45). Start using the random number table of Appendix E, on page ll, column 22, row 45. That number is 3.

If l-digit random numbers are needed, record them, going down the column to the bottom of the page and then to the top of the next column, and so on. Ignore duplicates and record zero (0) as ten (10). Following on from the last example, these numbers are 3, 5, 7, 10, 4, etc. If twodigit random numbers are needed, rule off the page, and further pages if necessary, in columns of two digits each. If there is a single column left on the page, ignore this column, and rule the next page in columns of two. Again, ignore duplicate numbers and record 00 as 100. For example, using the same starting place as in the last example, (page 11, column 22, row 45) the two-digit numbers recorded would be 31, 58, 72, 2, 46, 71, 43, etc. When threedigit numbers are needed, rule the page in columns of three. Record 000 as 1000. Starting on page 11, column 22, row 45, the numbers recorded would be 316, 585, 722, 24, 461, 715, 376, 244, 921, 289, etc.



Figure C-1. Choosing a starting place for a three-dimensional lot numbering system.

C.4. OBTAINING RANDOM NUMBERS FOR THE SAMPLE

C.4.1. Serial Lot Numbering System

Once the packages in the lot have been assigned numbers (from 1 to N), it is necessary to obtain n random numbers which will correspond to those packages which will become the random sample. If the lot contains 100 packages or less, use twodigit random numbers. If the lot consists of more than 100, but not more than 1000 packages, use three-digit random numbers.

¹Alternatively, the inspector may choose a starting page in the random number table, and closing his or her eyes, drop a pencil anywhere on the page to indicate a starting place in the table.

Using the random number table (Appendix E), rule the table off in columns if desired. Read off each successive number which is less than or equal to N until n different numbers have been recorded in Block A of the worksheet in the column headed "Pkg. No.". These correspond to the packages to be selected for the sample.

The testing official, of course, may rearrange these random numbers in a serial fashion to facilitate actual package selection (or mark through the random numbers on the worksheet as he or she selects the package); in any event, the order in which the numbers come out of the random number table indicate the order in which packages in the sample are used to determine the tare.

For example: The lot consists of 99 packages. A sample of 10 packages is required. Starting on page 11, column 22, row 45, the following random numbers are recorded: 31, 58, 72, 2, 46, 71, 43, 82, 79, 40. (If a duplicate appears in the table, it is ignored--e.g., 72 appears twice.) If 00 had appeared, it would have been ignored in this case (it would usually be recorded as 100). The packages to be taken for the sample are the packages in the serial numbering system corresponding to these 10 random numbers.

Example of package selection using a serial lot number system

Sample package in the sequence to be used for tare determination	Package number in lot ²	Order in which packages will be selected
1	31	2
2	58	6
3	72	8
4	2	1
5	46	5
6	71	7
7	43	4
8	82	10
9	79	9
10	40	3

Note that the tare sample is obtained according to the order in which the random numbers are recorded; that is, for a sample of 10, the tare sample in this instance, would be packages numbered 31 and 58 in the lot.

C.4.2. Three-dimensional Lot Numbering System

The official should choose some convenient lower left corner of the stack as a "zero point" and record the number of packages in the stack in each of the three directions (RUB). For example, the stack might be 10 by 7 by 3, i.e., 10 units to the Right of the starting place, 7 units Up, and 3 units Back.

A work table like the following is useful to record the positions of sample packages in the lot as determined from the random number table:

Package Selection Worksheet for a Three-Dimensional Lot Numbering System								
Sample package in the sequence	Package location							
tare determination	Right	Up	Back					
1 2 3 4 5 6 7 8 9 10 ↓								
(continue if larger s	sample s	ize is	required)					
Dimensions of stack =	= Ř	Ū	Ē					

At the bottom of the table in the spaces labeled "Dimensions of Stack," record the total number of units in each direction in the stack. This will aid in going through the random number table, because numbers larger than this are not usable. Beginning at a random starting place in Appendix E, go down that column of Appendix E filling in the first column of the work table by using every random number less than or equal to the dimension shown at the bottom of the work table. When the first column of the work table is completed, fill in the second column. When the bottom of a column is reached in Appendix E, begin at the top of the next column. If all the dimensions of the stack are 10 or less, use one-digit columns of the random number table; if any

²This is the column headed "Pkg. No." in Block A of the worksheet.

dimension is greater than 10, but not greater than 100, use two-digit columns; if greater than 100, but not greater than 1000, use three-digit columns, and so on.

In the case of a three-dimensional lot numbering system, it is not necessary to ignore duplicates in the table since there is very little chance of duplicating all three numbers required. (Of course, if a set of three numbers is found to have been duplicated, it should be deleted and replaced by three additional random numbers.)

If any maximum dimension happens to be "two", a random selection can be made by tossing a coin rather than by using random numbers; or a selection may be based on identifying the number "one" with even random numbers found in the table and "two" with odd.

For example, suppose that the dimensions of the stack are 10 by 7 by 3. The official wants to select 10 packages at random. He or she needs three one-digit numbers to indicate the location in the stack of each of the 10 samples. Assume that the random starting place is the 22nd column and the 45th row on page 11 of Appendix E.

The first sample package is found 3 packages to the right, 7 packages up, and the third package back from the zero point.

The ninth sample package is 5 packages to the right, 5 packages up, and the second package back. (See completed example.)

C.5. OTHER METHODS OR TABLES TO OBTAIN RANDOM NUMBERS

Random number dice may be used as an alternative to the random number table as a way of obtaining random numbers. These dice are special 20-sided dice sold and used in a set of three. Each die has 20 faces--two faces numbered 0, two faces numbered 1, etc., through the number 9. Two sources for purchasing the dice are:

Lansford Publishing Company³ P. O. Box 8711 San Jose, California 95155

Technovate³ 910 Southwest 12th Avenue Pompano Beach, Florida 33060

The random number dice could be used to get random numbers for the sample for serial lotnumbering systems if the lot contained 1000 packages or less, or for three-dimensional lot-numbering systems if no dimension were larger than 1000.

Other types of random number tables than Appendix E may be helpful in choosing a random sample especially in the instance of lot sizes for which N is the number 5 or smaller in the first digit. For example, consider a lot of 200 packages which is serially numbered 1 to 200. Using the random number table in Appendix E would require searching for three-digit numbers less than 200. Since the numbers 0 to 9 occur with equal frequency, many of the random numbers found by going

Completed example of package selection using a three-dimensional lot numbering system

Sample package in the sequence to be used for tare determination	Package Right	location Up	n Back
1	3	7	3
2	5	3	1
3	7	1	3
4	10(0)	2	1
5	4	2	1
6	7	7	2
7	3	3	2
8	9	6	1
9	5	5	2
10	2	2	2
Dimensions			
of Stack =	10	7	3
	R	U	В

 $^{^{3}}$ The mention of firm names does not imply that they are endorsed or recommended by the Department of Commerce over other firms not mentioned.

through the table must be rejected because they are larger than 200. In such instances the book, <u>Tables of Random Permutations</u>, by Lincoln E. Moses and Robert V. Oakford (published by Stanford U. Press, Stanford, California in 1963) would be quite a time saver. In this book, a number of tables which correspond to N with a small first digit (e.g., N = 10, 25, 50, 100) are provided which reduce the time to search (and reject) many random numbers.

C.6. OTHER CONSIDERATIONS WHEN SELECTING THE SAMPLE

C.6.1. Selecting the Tare Sample

0

The order in which random numbers come out of the random number table indicate those packages in the sample which are the tare sample.

The worksheet provides a column labeled "Pkg. No." in Block A. The random numbers are recorded in this column in the order in which they come from the random number table. The testing official will want to select the packages in the order corresponding to a serial arrangement of the numbers. One way of doing this and not forgetting the order of the packages for the tare sample (which, if glass or aerosol, could amount to a large proportion of the sample) is to associate each random number with the number printed to the left of it on the worksheet in Block A (1 to 30) and to order or mark the packages which are selected with this latter number. This latter number indicates the order in which the packages will be opened for tare. In the example of a package selection using a serial lot numbering system (referring to the example in Section C.4.), the package corresponding to random number 31 is the first package to be opened for tare, that package corresponding to random number 58 is the second and so on. However, in selecting the sample, the package corresponding to random number 2 will be the first removed from the lot. In this case, the official may wish to mark (or lay a piece of paper on) this first package removed from the lot with a "4". The second package removed from the lot in a serial fashion will be the package corresponding to the random number 31 but the inspector will want to note that this package

is the first package he or she should open for tare determination.

It is very important, when testing glass or aerosol packages, to retain the order of packages corresponding to the order in which the random numbers come out of the random number table, since the additional packages (if any) to be opened for tare are selected in this order.

When testing at the packaging location, if dry tare is to be used, the tare sample should be selected from the same lot of tare materials into which the finished product (which is being checked) is being packaged. The official should collect or watch the collection of the dry tare components (empty container) if at all possible, with the major contribution to the tare weight (the can, cardboard box, etc.) selected randomly in the same fashion as the sample packages are selected. As long as they do not comprise a major proportion of the tare weight, supplementary tare materials which will constitute the finished package (solder, ties, glue, labels, caps, etc.) may be selected from the lot without regard to rigorous random selection; but, such materials should be visually identical to and selected from the same batch as other such materials being used on the packaging line.

C.6.2. Selecting the Sample at Different Locations

- When the lot consists of packages on a retail shelf, if, while the official is choosing his sample, a customer should remove packages from the lot, the official should continue to choose the sample as if that missing package were not there in the first place (that is, select the next adjacent package).
- It is permissible to eliminate individual packages from the sample (and from the inspection lot) if they can be seen to be defective from visual examination alone, e.g., cut boxes, empty bottles, torn wrappers, etc. Such packages can be treated individually and should not be part of the sample. However, individual packages must not be eliminated from the sample after quantitative measurements have been made.

0

If a defective package is found while sampling, the official may select a package immediately adjacent to the defective package. If found after selection, but before measurement, and the original package location is not convenient, the official may select another random number in order to determine which package to use to replace the defective one in the sample.

- ^o When the lot is defined as packages on open display plus cartons in a storeroom, the sample should be taken proportionately from the packages on the shelf and from the cartons. That is, if there were 24 packages on display and 220 packages in the storeroom, then 1/10 of the sample should be from packages on display and 9/10 of the sample from packages in the storeroom. If there are to be 30 packages in the sample, 3 should come from the display and 27 from the storeroom.
- ^o When the lot consists of cartons in a storage area or warehouse, the random sample can be obtained by using the three-dimensional lot numbering system. However, it may be extremely difficult to select a random sample from a warehouse since the packages may be aggregated into larger storage units, such as cartons, strapped-together pallets, or shrink-packs.

Therefore, for convenience, the official may randomly select more than one package from each carton, and more than one carton from each pallet. However, choosing the entire sample from a single pallet or a single carton must be strictly avoided.

The testing official may find it convenient to use the three-dimensional numbering system for selection of cartons on a pallet, and the serial numbering system for the selection of pallets and of packages from a carton.

The official should first choose the pallets (if any) from which the sample will be taken, then the cartons from those pallets (or from the entire lot if there are no pallets), and finally choose from the previously selected cartons, the individual packages which will comprise the sample. Each step will usually have a different number of units from which the pallet, carton, or package is chosen.

^o When the lot consists of a portion of production at the packing plant, the packages coming off the packaging line can be considered to be numbered serially from 1 to N (the last package in the lot). Random numbers may be obtained from the random number table as described for serial lot numbering systems. The random numbers should be chosen, then ordered serially before physically choosing the packages corresponding to those numbers from the packing line.

APPENDIX D: AUXILIARY TABLE FOR RANDOM STARTING PLACE

1

Table provided by James F. Filliben, Statistical Engineering Division, National Bureau of Standards. Derived from <u>A Million Random Digits</u> by the Rand Corporation, copyright, 1955, The Free Press.

12,35) 9,18) (34,12) (31,27) (31,27) (19,37) (19,33) (6,143) (6,11) 5,16) 20) 6) 6) 3,1) 42,22) 4,26) 28,35) 28,48) 26,42) 46,49) 50,38) 19,35) 32,13) (24,18) (44,42) (4,9) (17,49) (17,49) (35,5) (28,41) (14,7) (2,30) (2,33) 19,40) 28,3) 35,31) 12,11) 32,22) (11,42) (46,3) (46,19) (21,38) (25,6) (14,10) (14,1) (16,18) (31,40) (31,40) (50,2 (50,2 12, 32, 10, (18,42) (12,33) (14,2) (32,48) (35,22) (45,32) (6,31) (7,26) (48,36) (48,36) 24,45) 34,6) 13,23) 41,25) 27,37) 23,42) 7,50) 29,37) 29,37) 16,44) 14,4) (1,36) (15,1) (2,22) (35,23) (23,16) 33,46) 19,41) 20,28) 27,11) 25,19) (25,39) (12,18) (3,18) (24,2) (24,2) (16,26) 111 (11,11,11) (11,11,11,11) (11,11,11,11) (11,11,11,11) (11,11,11,11) (11,11,11,11) (11,11) (149,35) 28, 1,) 29,36) 3,11) 3,25) 2,1) 9,42) 28,32) 38,4) 23,21) 1,13) 13,26) 8,33) 23,20) 23,20) 1,7,43) 6,42) 8,33) 18,21) 29,39) 23,38) 41,47) 25,5) 44,11) 42,41) 17,18) 17, 7) 18,41) 21,50) 23,9) 34,21) (47.12) (47.12) (20.50) (1.35) (32,1) 38,34) 19,11) 44,43) 3,12) 37,31) 15,42) (15,12) 6,8) 14,30) 9,24) 25,33) 47,10) 42,26) 19,39) 32,23) 36,22) 30,2) 14,2) 18,16) 14,22) 26,49) 20,37) 47,26) 19,23) 8,18) 20,31) 36,47) 33,25) 34,8) 29,9) (41,26) (13,30) (35,19) (47,43) 3,4) (24, 5) (24, 5) (28, 8) (22, 37) 24,42) 16,5) 26,4) 37,48) 47,43) 34,42) 10,2) 8,47) 8,20) 6,22) 46,38) 17,12) 27,3) 29,48) 3,16) 13,37) 40,27) 28,6) 47,5) 48,32) 32,28) 46,39) 44,50) 26,16) 26,16) 17,15) 1,27) 50,10) 44,10) 38,23) 9,42) 19,38) 10,40) 19,2) 36,45) (27,26) (8,36) (43,4) (42,10) (11,3) 1,36) 15,27) 27,28) 19,14) 32,3) (18,13) (47,32) (7,42) (37,21) (6,14) 19,12) 35,50) 50,13) 50,16) 24,13) (19,16) (11,12) (25,28) (25,28) (31,45) (44,15) (49,21) (49,34) (43,4) (41,32) (41,32) (2,17) (19,47) (41,47) (17,20) (17,20) (5,44) (28,26) 50,29) 7,9) 50,32) 8,49) 15,35) [10, 6] 27,48) 35,1] 38,19) 29,23) 17, 6) 30,19) 49,19) 31,30) 3,5) 37, 7) 27,24) (32,22) (32,22) (8,19) (27,16) 30,28) 2,48) 1,39) 33,40) 22,48) 10,26) 28,43) 33,34) 15,35) 36,14) (27,42) 9,19) (25,28) (15,46) (19,23) 43,23)
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(11,21) (14,22) (2,11) (50,40) (32,2) (15, 7) (41,37) (22,17) (41,36) (41,36) (31, 7) (43,15) 9,35) (35,16) (49,17) (29,11) (11,23) (3,36) (43,19) (50,27) (34,35) (24,20) (27,49) (27,45) (42,28) (27,36) (18,36) (29,44) (27,19) (35,34) (4,30) (35,24) (26,41) (14,27) (39,17) (23,21) (50,33) (38,37) (38,37) (16,36) (16,31) (48,40) (49,6) (19,6) (19,6) (17,29) (17,29) (17,29) (24,10) (41,37) (48,2) (26,24) (25,27) (13,43) (2,3) (14,47) (22,11) (25,2) (47,41) (37,2) (47,6) (47,6) (37,39) (20,28) (36.26) (33,28) (7,9) (22,50) (14,31) 2,24) (19,17) (11,6) (11,6) (11,6) (32,15) (38,18) (42,10) (17,6) (8,4) (46,41) (34,12) (17,30) (44,41) (50,43) (28,13) (28,13) (44,41) (27,14) (19,40) (41,6,11) (29,43) (21,11,11) (12, 30, 25) (37, 6) (33, 12) (11, 38) (15, 14) (13, 19) (11, 30) (11, 30) (12, 30) (12, 30) (12, 30) (46, 1) (37,49) (7,11) (47,18) (3, 5) (29,28) (49,25) (17,43) (14,3) (3,35) 29,31) 9,11) 7,26) 37,20) 37,20) 9,2) 10,32) (1,6) (1,6) (1,6) (1,6) (1,6) (1,6) (1,10 32, 47) 32, 44) 3, 30) 4, 40) (28, 38) (28, 38) (28, 38) (28, 38) (28, 24) (28, 210) (25, 24) (44, 45) (13,30) (47,5) (31,25) (31,25) (31,25) (31,4) 13, 9) 27,19) 42,31) 46,48) 6,42) 28,40) 44,42) 6,6) 33,16) 9,23) 15,13) 2,41) 10,47) 6,9) 36,15) 27.16) (27.16) (44,36) (22,39) (38,5) (21,38) (49,40) (28,13) (34,40) (30,5) (30,43) (49,14) (19,47) (13,10) (30,32) (44,50) (45,18) (32,49) (46,12) (46,12) (39,24) (39,24) (11,12) (23,2) (23,2) (23,2) (15,17) (15,17) (11,43) (3,25) (10,15) (14,9) (40,46) (38,38) (5,3) (16,9) (28,33) (26,14) (26,14) (24,42) (50,31) (47,48) (4,30) (36,24) (15,14) (23,37) (48,49) (11,32) (11,32) (9,10) 50,46) 9,42) 48,20) 6,45) 38,16) (20,28) (14,27) (46,25) (26,11) (25,5) 7,21) 48,32) 10,10) 33,33) 41,45) 19,24) 30,27) 30,44) 31,2) 17,47) 50,46) 31,45) 47,39) 35,30) 13,3) (43,29) (5,34) (7,15) (28,16 (41,23) (38,16) (20,30) (20,30) (16,45) (11,4) (11,4) (11,49) (12,14) (12,14) (50,27) 7,47) 38,28) 27,31) 40,28) 46,20) (14,21) (38,47) (18,10) (35,42) (40,15) (17,44) (39,14) (19,29) (11,24) (41,24) (25,36) (12,19) (48,35) (49,36) (15,49) (15,49) (19,19) 1¹⁴, 7) 5, 1) 8, 22) 8, 22) 1, 6, 9) 1, 6, 9, 11) 1, 9, 31) 1, 9, 31) 1, 29, 38) 9,1) 6,13) (28,35) (46,34) (44,20) (28,18) (25, 4) (13,29) (15,29) (20, 1) 32,33) 7,33) 26,20) 34,50) 4,16) (38,20) (20,15) (24,42) (14,40) (20,33) (115, 47) (4, 12) (12, 25) (14, 4, 12) (14, 42) (14, 42) (12, 12) (11, 13) (11, 13) (11, 13) (11, 13) (11, 13) (11, 13) (11, 13) (11, 13) (11, 13) (11, 13) (12, 12) (13, 46) (15, 27) 20,30) 44,16) 11,24) 8,45) 39,21) 7,25) (11,36) (14,47) (29,24) (29,24) 149,11) 23,20) 5,3) 35,3) 147,38) (14, 18)(47, 3)(15, 7)(17, 23)(7, 48)(50,19) (31,18) (29,31) (29,31) (49,7) (40,33) [42, 5) [14,33) [45,17] [21,17] [21,17] 34,39) 50,45) 444,48) 10,1) 9,17) 25,29) 36,17) 30,16) 39,48) 11,42) 2,38) 41,26) 6,30) 34,12) 35,36) (1,23) (18,18) (45,18) (40,34) (8,4) (50,36) (49,15) (42,43) (47,37) (17,25) (36,42) (45,32) (45,32) (45,34) (15,32) 11,11) 30,19) 30,31) 30,31) (23,29) (23,21) 16,14) 16,11) 146,11) 147,12) 14,140) 21,47) 44,21) 40,23) 36,32) 27,40) 42,45) 3, 2) (33,36) (20,26) (30,25) (36,41) 19,48) 25,37) 50,20) 1,20) (44,42) (39,48) (15,11) (17,30) (47,48) (42) 12,50) 12,50) 12,21) (7,1) (37,12) (19,34) (18,10) (5,50) 23,19) 36,44) 31,118) 12,10) 12,10) (24,36) (24,36) (24,36) (36,1) (10,8) (47, 11) (47, 9) (37, 6) (37, 50) (37, 27) (13,15) (18,47) (49,49) (47,6) (25,22) (49,39) (20,46) (23,1) (42,23) (45,35) (23,25) (44,19) (38,33) (41,35) (26, 5) (25, 5) (24, 34) (33, 39) (3, 48) 9,42) (12,50) (1,25) (27,19) (21,32) 15,35) 39,20) 32,30) 9,46) 35,32) 17,24) (35,11) (19,28) (46,19) (23,19) (16, 7) (15,25) (29,31) (26,36) (32,38) (12,13) (17,12) (20,2) (36,23) (15,15) (14,29) (14,15) (30,27) (19,40) (34,1) 2,20) (31,20) (2,23) (16,16) (27,12) 16,45) 21,1) 19,36) 9,48) 23,47) 23,20) 24,23) 9,27) 11,24) (11,24) 15, 1) 28,24) (45,25) 38,45) 28,28) 27,33) 4,19) 41,36) 36,16) 1,6) (21,46) (40,49) (47,4) (14,41) (14,41) (14,12) 34, 9) (28,11) (39,43) (21,49) (21,44) (45,32) (35,5) (27,13) (38,3) (40,6) (30,21) (6,35) (29,30) (38,42) (20,7) (34,12) (50,15) (47,7) (24,18) (24,11) (18,50) (29,46) (15,39) (24,20) (24,20) (6,14) (44,37) (28,7) (6,14) (30,34) (13,28) (7,9) (28,42) (9,20) (40,42) (41, 7) (44,22) (16,41) (3,33) (44,48) (43,44) (17,19) (12,30) (12,30) (12,30) (12,49) (443.39) (27,38) 7,41) 10,26) 11,41) 34,41) 5,15) 7,50) (23,40) (32,40) (20,11) (20,49) (9,38) (3,15) (2,23) (43,39) (13,35) (22,34) (26,4) (26,4) (12, 5) (24,15) (17,41) (19,30) (38,38) 31,28) 30,14) 50,39) 20,8) 5,8) 50,33) 31,16) 44,11) 4,46) 7,21) 23,32) 37,2) 5,15) 14,13) 35,44) 29,13) 33,36) 39,17) 17,16) 42,1) (24,16) (34,23) (11,44) (22,6) (28,43) 13,14) 27,11) 35,34) 24,28) 37,27)

APPENDIX E: RANDOM NUMBER TABLE

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31000	63837	17813	08076	19164	95508	17513	29416	61238	25818
87014	83331	56364	32768	85680	08844	59844	68794	32783	60318
47293	97023	35804	69886	47494	94574	45842	67221	77115	43398
33898	89236	06100	68848	08674	87786	42425	92091	86274	82166
26877	95856	65227	25165	01752	99463	15216	28719	04716	80246
53984	87855	70753	80386	78600	39244	76967	83263	57849	85890
97809	03548	00574	21143	11605	30245	87395	80966	28721	11095
85683	79483	74858	87491	57785	61270	51111	50490	40940	02832
07758	57784	22934	17165	37776	33361	79191	97398	40881	98552
13995	74006	90843	85761	89037	13567	67089	47435	75156	70217
89630	94575	64517	80897	04861	50564	15287	94279	69154	75473
20355	08661	11092	19682	84287	23597	48246	74325	66320	90155
13496	74367	32701	87819	29050	90959	99765	59374	45204	87750
68419	49317	30340	62744	45214	79826	34043	73218	72788	26143
61481	09786	08768	93715	43847	68901	51249	35382	67776	06271
71877	53924	09630	62975	64470	46832	40591	23477	21063	31229
99283	86530	86819	38955	91744	89632	64623	84986	85990	47639
09047	83453	12775	32000	60098	98862	93422	66212	86413	82884
83724	89682	53950	41500	16023	83862	88274	68301	99673	40945
56126	46618	87708	91994	38384	27047	91550	18903	45535	45586
13810	51503	55122	22997	82556	22697	54985	64852	58775	66737
85630	22794	81623	10927	52252	27384	03122	17454	03250	23232
93350	28643	39097	00914	69844	06450	32818	88752	28722	94656
05002	71178	15414	99874	58046	35461	56349	81936	14964	83638
70358	57182	45747	30830	70542	25932	16298	23521	72454	11640
98169	51114	18115	40718	46082	75847	15678	22842	44615	97810
28010	95831	94028	57041	75137	55128	99785	33467	33834	04860
05576	47156	09300	11197	97670	20064	98145	84774	07907	10992
80748	66311	79421	00202	68501	40422	07368	26795	24358	78969
39746	23690	67845	83962	09451	21501	75317	09049	69440	16137
39380	72397	88106	07851	67756	58042	44218	52775	49082	54400
55865	70318	58189	35340	91500	80940	39231	54836	18038	03557
34223	72744	83926	40078	80791	42723	68340	47452	17443	69289
91312	44474	09925	41416	96671	11213	60979	04130	72380	73582
51010	08021	53914	37499	40228	92606	07225	18014	71063	50111
48890	58264	18790	91535	04933	56656	76389	37904	98017	07663
24876	93198	77444	53782	48866	65614	11410	90637	63675	43554
49408	42923	28162	09789	15155	66742	66785	79065	93573	19853
56307	90901	18117	36505	01598	68997	96338	40823	96247	55573
48320	09322	13457	84931	54701	14878	05422	65358	85636	31948
51083	00619	05548	25431	15175	82428	00637	41814	68871	31688
43249	71593	85595	59834	01488	06917	32858	80134	01832	25905
00370	17413	75537	79824	24428	28941	58659	66731	99940	27156
55737	45462	12484	64858	43581	06220	07507	39119	38024	99720
39551	38058	10445	18463	80812	51243	22351	63266	94057	06573
02369	11289	99499	32922	88429	90484	42010	53308	33206	36137
92788	62546	26147	83529	10012	77611	78925	86071	66344	35705
98650	95898	74254	45173	17430	73882	03411	88447	43279	35057
95591	85858	51058	26140	00995	16881	87372	72646	18796	58537
67853	23563	41063	63355	72454	16016	72229	54720	09846	81392

32942 07410	95416 99859 68155	42339 83828 45673	59045 21409 76210	26693 29094	49057 65114 45738	87496 36701 29550	20624 25762	14819 12827 09574	48667 45692
46251	25437	69654	99716	11563	08803	86027	51867	12116	38469
65558	51904	93123	27887	53138	21488	09095	78777	71240	87225
99187	19258	86421	16401	19397	83297	40111	49326	81686	40601
35641	00301	16096	34775	21562	97983	45040	19200	16383	68739
14031	00936	81518	48440	02218	04756	19506	60695	88494	58501
60677	15076	92554	26042	23472	69869	62877	19584	39576	18290
66314	05212	6785,9	89356	20056	30648	87349	20389	53805	85243
20416	87410	75646	64176	82752	63606	37011	57346	69512	56464
28701	56992	70423	62415	40807	98086	58850	28968	45297	80419
74579	33844	33426	07570	00728	07079	19322	56325	84819	48754
62615	52342	82968	75540	80045	53069	20665	21282	07768	60375
93945	06293	22879	08161	01442	75071	21427	94842	26210	95002
75689	76131	96837	67450	44511	50424	82848	41975	71663	79656
02921	16919	35424	93209	52133	87327	95897	65171	20376	13475
14295	34969	14216	03191	61647	30296	66667	10101	63203	75144
05303	91109	82403	40312	62191	67023	90073	83205	71344	96216
57071	90357	12901	08899	91039	67251	-28701	03846	94589	88403
78471	57741	13599	84390	32146	00871	09354	22745	65806	78187
89242	79337	59293	47481	07740	43345	25716	70020	54005	23973
14955	59592	97035	80430	87220	06392	79028	57123	52872	94991
42446	41880	37415	47472	04513	49494	08860	08038	43624	46013
18534	22346	54556	17558	73689	14894	05030	19561	56517	96479
39284	33737	42512	86411	23753	29690	26096	81361	93099	33868
33922	37329	89911	55876	28379	81031	22058	21487	54613	81052
78355	54013	50774	30666	61205	42574	47773	36027	27174	44830
08845	99145	94316	88974	29828	97069	90327	61842	29604	47994
01769	71825	55957	98271	02784	66731	40311	88495	18821	12463
17639	38284	59478	90409	21997	56199	30068	82800	69692	45133
05851	58653	99949	63505	40409	85551	90729	64938	52403	56841
42396	40112	11469	03476	03328	84238	26570	51790	42122	40874
13318	14192	98167	75631	74141	22369	36757	89117	54998	87031
60571	54786	26281	01855	30706	66578	32019	65884	58485	10909
09531	81853	59334	70929	03544	18510	89541	13555	21168	81318
72865	16829	86542	00396	20363	13010	69645	49608	54738	17894
56324	31093	77924	28622	83543	28912	15059	80192	83964	61904
78192	21626	91399	07235	07104	73652	64425	85149	75409	67104
64666	34767	97298	92708	01994	53188	78476	07804	62404	34828
82201	75694	02808	65983	74373	66693	13094	74183	73020	31086
15360	73776	40914	85190	54278	99054	62944	47351	89098	26735
68142	67957	70896	37983	20487	95350	16371	03426	13895	42170
19138	31200	30616	14639	44406	44236	57360	81644	94761	92813
28155	03521	36415	78452	92359	81091	56513	88321	97910	22235
87971 58147	29031 68841	51780 53625	27376	81056 75223	86155 16783	55488 19272	50590 61994	74514 71090	58791 78416
18875	52809	70594	41649	32935	26430	82096	01605	65846	65228
75109	56474	74111	31966	29969	70093	98901	84550	25769	82586
35983	03742	76822	12073	59463	84420	15868	99505	11426	62723
12651	61646	11769	75109	86996	97669	25757	32535	07122	76763
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81769	74436	02630	72310	45049	18029	07469	42341	98173	79260
36737	98863	77240	76251	00654	64688	09343	70278	67331	98729
82861	54371	76610	94934	72748	44124	05610	53750	95938	01485
21325	15732	24127	37431	09723	63529	73977	95218	96074	42138
74146	47887	62463	23045	41490	07954	22597	60012	98866	90959
90759	64410	54179	66075	61051	75385	51378	08360	95946	95547
55683	98078	02238	91540	21219	17720	87817	41705	95785	12563
79686	17969	76061	83748	55920	83612	41540	86492	06447	60568
70333	00201	86201	69716	78185	62154	77930	67663	29529	75116
14042	53536	07779	04157	41172	36473	42123	43929	50533	33437
59911	08256	06596	48416	69770	68797	56080	14223	59199	30162
62368	62623	62742	14891	39247	52242	98832	69533	91174	57979
57529	97751	54976	48957	74599	08759	78494	52785	68526	64618
15469	90574	78033	66885	13936	42117	71831	22961	94225	31816
18625	23674	53850	32827	81647	80820	00420	63555	74489	80141
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31893	11224	92074	•54641	53673	54421	18130	60103	69593	49464
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39901	38669	82462	30166	79613	47416	13389	80268	05085	96666
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59723	91330	82433	61427	17239	89160	19666	08814	37841	12847
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82558	71239	10853	42581	08792	13257	61973	24450	52351	16602
80822	66731	20341	27398	72906	63955	17276	10646	74692	48438
41067	39859	54458	90542	77563	51839	52901	53355	83281	19177
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96789	22551	12111	86683	61270	58036	64192	90611	15145	01748
12633	15075	47189	99951	05755	03834	43782	90599	40282	51417
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72872	54109	74626	22111	87286	46772	42243	68046	44250	42439
20724	19944	34450	81974	93723	49023	58432	67083	36876	93391
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25961	70386	74185	77536	84825	09934	99103	09325	67389	45869
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31694	55633	18813	90291	05275	01223	79607	95426	34900	09778
23016	96567	38840	26903	28624	67157	51986	42865	14508	49315
17292	18430	05959	33836	53758	16562	41081	38012	41230	20528
75465	99837	85141	21155	99212	32685	51403	31926	69813	58781
89013	86492	75047	59643	31074	38172	03718	32119	69506	67143
44551	77837	30752	95260	68032	62871	58781	34143	68790	69766
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40789	73539	99439	86692	90348	66036	48399	73451	26698	39437
64086	82765	20389	93029	11881	71685	65452	89047	63669	02656
79143	31528	39249	05173	68256	36359	20250	68686	05947	09335
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76327	50155	04860	32918	10798	50492	52655	33359	94713	28393
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79482	10156	87785	49603	85048	63090	60719	29756	10696	75713
97826	82559	69027	41569	05422	47286	97825	15559	43482	07676
00872	36839	01840	14860	76529	55890	12228	33910	26878	88758
68457	71054	94300	18582	55813	26346	68685	24920	36374	87702
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_				-					
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23561	85971	37362	10657	30353	70564	17859	34684	45661	08168
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38916	03129	90039	33356	62300	57453	13940	45965	61549	36957
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38852	56056	91833	78352	44200	12426	48964	62341	53454	05451
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40131	51356	32702	75474	84559	53684	28758	39890	72112	15426
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05418	98621	75977	52630	27675	96279	13152	44711	46961	45757
37221	69111	23417	17803	11075	66454	95453	60328	68808	98125
23823	99934	93432	05912	93150	84781	99233	03767	24838	94955
84321	03554	23836	64544	27469	23266	57244	28275	82170	07575
02344	23656	61016	09765	19867	21790	46457	25411	03500	46762
70325	88171	23685	97217	76585	88384	51221	31272	17338	80422
22987	01461	15898	25857	74145	84101	90051	36721	45737	65918
83159	50055	54172	05122	07096	55938	95953	33901	54679	64178
68181	68525	53187	92984	58323	41389	66592	56584	14326	07823
65843	69659	40222	34435	50890	24504	70304	43227	29870	44698
54251	76480	23860	30082	69132	08840	98017	54350	66249	75725
42504	70709	53223	89394	66872	79919	06862	25977	42529	78046
56201	69520	52851	03783	60280	27101	07911	12147	97079	52817
25284	80305	76573	14254	56770	83548	44466	06063	04232	62838
00702	10030	47850	44094	84878	51686	39037	19661	73877	24708

57045	08074	88727	91303	10880	90387	03049	44649	41682	07161
92889	33197	04117	79760	15336	25030	73686	24054	08666	24607
06135	40078	34575	82871	86196	69883	71312	99329	34122	63290
27526	09658	27405	99448	02380	71414	48311	18536	45957	52546
32443	44984	94521	49020	45683	50812	57968	56310	97631	88709
34091	84585	92750	72213	03810	84047	17607	87085	12607	62564
68190	21907	52999	14903	80020	49368	63721	86548	80086	51686
05191	64586	50535	20491	87132	18487	34210	66368	58881	83704
78088	71769	13917	08311	88957	91965	22411	52575	44377	32138
34271	03646	95035	67881	17645	34452	47064	84451	57918	48975
76667	51400	93187	10311	92693	97380	61008	83243	01776	05137
80232	15879	47748	03011	38553	29224	76115	36026	01249	61250
53017	39124	84777	80739	87900	74156	54184	24003	45929	23730
28699	18974	35297	40752	31285	02656	34584	71261	28462	33431
35394	84361	77346	21801	39236	24825	77081	88028	12544	07565
84813	25422	08800	36063	94441	88637	50780	79144	71908	51899
39900	30333	13938	22799	30507	56296	43120	47179	26489	54531
99174	36078	79599	06223	38520	31678	97203	14143	17457	41301
53762	31370	73669	10523	08875	22489	69203	49879	77277	81867
72787	78482	19585	45029	31822	85128	29960	54344	44851	75381
82163	23362	09644	74123	06831	83252	16929	33737	19381	21302
62357	13766	93851	27009	42621	13612	18873	76885	78819	55665
62350	73856	33253	02353	42231	21028	27646	23292	94705	70722
84764	94194	97699	27029	32935	51595	04454	91100	67131	09041
78327	42124	56300	93706	75936	67290	59600	20201	83979	73231
39284 73507 77675	08465 00339 53001	61364 10678 74015	37573 66490 20232	18285 22653	64619 10032 50260	20079 68648	85596 79622 57780	81849 98925 02739	81686 99635 55069
55144	58892	57952	65272	56004	41356	00190	17413	64296	60680
69545	93269	67239	96561	07443	72133	62418	17791	02994	02665
24029 44665 13196	31914 26518	39122 13219	68971 61450	26865 13321 97721	01521 52526	49285 22629	71212 78390	00822 30087	25330 17735
66401	50382	14549	66579	77859	30100	79010	32512	29816	07127
61962	67996	12828	22706	72646	79669	72214	52460	89227	49089
06771 56042	43014 94875	92202 92991	23860 24042	29456 92395	38047 30212	44988 52225	15786 50280	03658 12944 81051	25037 79124
85814	29832	59007	57398	01033	52085	17512	32395	98564	82408
99657	30745	72197	03217	11839	73768	49206	96954	94375	70130
61069 61108 25672	54986 30705	13341 46984	89688 74866	70977 65173	32056 80340	81627 43903	56776 66334	12859 27757 03276	44176 95664
11136	98716	28020	28414	92289	22989	45797	16935	49843	98385
88537	12364	87867	50446	37446	35919	69387	82296	37350	25132
83003	85363	97045	18857	67214	15043	05498	97716	85302	70414
82128	04345	08532	69206	36560	04641	64006	28763	89057	22560
21388 29672 65120	13394 42547 17193	26085 77381	15173 48198	44457 72074	13154 08512	98748 43387	31213 27964	87025 86082	16793 57332

14541	36678	54343	94932	25238	84928	30668	34992	69955	06633
88626	98899	01337	48085	83315	33563	78656	99440	55584	54178
31466	87268	62975	19310	28192	06654	06720	64938	67111	55091
52738	52893	51373	43430	95885	93795	20129	54847	68674	21040
17444	35560	35348	75467	26026	89118	51810	06389	02391	96061
62596	56854	76099	38469	26285	86175	65468	32354	02675	24070
38338	83917	50232	29164	07461	25385	84838	07405	38303	55635
29163	61006	98106	47538	99122	36242	90365	15581	89597	03327
59049	95306	31227	75288	10122	92687	99971	97105	37597	91673
67447	52922	58657	67601	96148	97263	39110	95111	04682	64873
57082	55108	26992	19196	08044	57300	75095	84330	92314	11370
00179	04358	95645	91751	56618	73782	38575	17401	38686	98435
65420	87257	44374	54312	94692	81776	24422	99198	51432	63943
52450	75445	40002	69727	29775	32572	79980	67902	97260	21050
82767	26273	02192	88536	08191	91750	46993	02245	38659	28026
17066	64286	35972	32550	82167	53177	32396	34014	20993	03031
86168	32643	23668	92038	03096	51029	09693	45454	89854	70103
33632	69631	70537	06464	83543	48297	67693	63137	626 7 5	56572
77915	56481	43065	24231	43011	40505	903 <u>8</u> 6	13870	84603	73101
90000	92887	92668	93521	44072	01785	27003	01851	40232	25 842
55809	70237	10368	58664	39521	11137	20461	53081	07150	11832
50948	64026	03350	03153	75913	72651	28651	94299	67706	92507
27138	59012	27872	90522	69791	85482	80337	12252	83388	48909
03534	58643	75913	6355 7	25527	47131	72295	55801	44847	48019
48895	34733	58057	00195	79496	93453	07813	66038	55245	43168
57585	23710	77321	70662	82884	80132	42281	17032	96737	93284
95913	24669	42050	92757	68677	75567	99777	49246	93049	79863
12981	37145	95773	92475	43700	85253	33214	87656	13295	09721
62349	64163	57369	65773	86217	00135	33762	72398	16343	02263
68193	37564	56257	50030	53951	84887	34590	22038	40629	29562
56203	82226	83294	60361	29924	09353	87021	08149	11167	81744
31945	23224	08211	02562	20299	85836	94714	50278	99818	62489
68726	52274	59535	80873	35423	05166	06911	25916	90728	20431
79557	25747	55585	93461	44360	18359	20493	54287	43693	88568
05764	29803	01819	51972	91641	03524	18381	65427	11394	37447
30187	66931	01972	48438	90716	21847	35114	91839	26913	68893
30858	43646	96984	80412	91973	81339	05548	49812	40775	14263
85117	38268	18921	29519	33359	80642	95362	22133	40322	37826
59422	12752	56798	31954	19859	32451	04433	62116	14899	38825
73479	91833	91122	45524	73871	77931	67822	95602	23325	37718
83648	66882	15327	89748	76685	76282	98624	71547	49089	33105
19454	91265	09051	94410	06418	34484	37929	61070	62346	79970
49327	97807	61390	08005	71795	49290	52285	82119	59348	55986
54482	51025	12382	35719	66721	84890	38106	44136	95164	92935
30487	19459	25693	09427	10967	36164	33893	07087	16141	12734
42998	68627	66295	59360	44041	76909	56321	12978	31304	97444
03668	61096	26292	79688	05625	52198	74844	69815	76591	35398
45074	91457	28311	56499	60403	13658	81838	54729	12365	24082
58444	99255	14960	02275	37925	03852	81235	91628	72136	53070
82912	91185	89612	02362	93360	20158	24796	38284	55328	96041

44553	29642	20317	69470	57789	27631	68040	73201	51302	66497
01914	36106	71351	69176	53353	57353	42430	68050	47862	61922
00768	37958	69915	17709	31629	49587	07136	42959	56207	03625
29742	67676	62608	54215	97167	07008	77130	15806	53081	14297
07721	20143	56131	56112	23451	48773	38121	74419	11696	42614
99158	07133	04325	43936	83619	77182	55459	28808	38034	01054
97168	13859	78155	55361	04871	78433	58538	78437	14058	79510
07508	63835	83056	74942	70117	91928	10383	93793	31015	60839
68400	66460	67212	28690	66913	90798	71714	07698	31581	31086
88512	62908	65455	64015	00821	23970	58118	93174	02201	16771
94549	31145	62897	91582	94064	14687	47570	83714	45928	32685
02307	86181	44897	60884	68072	77693	83413	61680	55872	12111
28922	89390	66771	39185	04266	55216	91537	36500	48154	04517
73898	85742	97914	74170	10383	16366	37404	73282	20524	85004
66220	81596	18533	84825	43509	16009	00830	13177	54961	31140
64452	91627	21897	31830	62051	00760	43702	22305	79009	15065
26748	19441	87908	06086	62879	99865	50739	98540	54002	98337
61328	52330	17850	53204	29955	48425	84694	11280	70661	27303
89134	85791	73207	93578	62563	37205	97667	61453	01067	31982
91365	23327	81658	56441	01480	09677	86053	11505	30898	82143
54576	02572	60501	98257	40475	81401	31624	27951	60172	21382
39870	60476	02934	39857	06430	59325	84345	62302	98616	13452
82288	29758	35692	21268	35101	77554	35201	22795	84532	29927
57404	93848	87288	30246	34990	50575	49485	60474	17377	46550
22043	17104	49653	79082	45099	24889	04829	49097	58065	23492
61981	00340	43594	22386	41782	94104	08867	68590	61716	36120
96056	16227	74598	28155	23304	66923	07918	15303	44988	79076
64013	74715	31525	62676	75435	93055	37086	52737	89455	83016
59515	37354	55422	79471	23150	79170	74043	49340	61320	50390
38534	33169	40448	21683	82153	23411	53057	26069	86906	49708
41422	50502	40570	59748	59499	70322	62416	71408	06429	70123
38633	80107	10241	30880	13914	09228	68929	06438	17749	81149
48214	75994	31689	25257	28641	14854	72571	78189	35508	26381
54799	37862	06714	55885	07481	16966	04797	57846	69080	49631
25848	27142	63477	33416	60961	19781	65457	23981	90348	24499
27576	47298	47163	69614	29372	24859	62090	81667	50635	08295
52970	93916	81350	81057	16962	56039	27739	59574	79617	45698
69516	87573	13313	69388	32020	66294	99126	50474	04258	03084
94504	41733	55936	77595	55959	90727	61367	83645	80997	62103
67935	14568	27992	09784	81917	79303	08616	83509	64932	34764
63345	09579	40232	51061	09455	36491	04810	06040	78959	41435
87119	21605	86917	97715	91250	79587	80967	39872	52512	78444
02612	97319	10487	68923	58607	38261	67119	36351	48521	69965
69860	16526	41420	01514	46902	03399	12286	52467	80387	10561
27669	67730	53932	38578	25746	00025	98917	18790	51091	24920
59705	91472	01302	33123	35274	88433	55491	27609	02824	05245
36508	74042	44014	36243	12724	06092	23742	90436	33419	12301
13612	24554	73326	61445	77198	43360	62006	31038	54756	88137
82893	11961	19656	71181	63201	44946	14169	72755	47883	24119
97914	61228	42903	71187	54964	14945	20809	33937	13257	66387

E-31

To calculate the average range of package errors for groups of 5 packages:

 Mark off the package errors in successive groups of five packages in the order of weighing.

> For example, the following package errors were recorded on the report form (only the first three columns are shown):

pkg.	pkg.	pkg.	pkg.	pkg.	pkg.
number	error	number	error	number	error
(1)	+2	(6)	-2	(11)	+2
(2)	+4	(7)	-4	(12)	-4
(3)	+5	(8)	-5	(13)	+5
(4)	+10	(9)	-10	(14)	+10
(5)	+3	(10)	-3	(15)	-3

 Calculate the range (R) of package errors for each group of five. <u>R does not have a sign</u>.

The range is obtained as follows:

 If there are only plus errors in a group of five, subtract the smallest plus error from the largest plus error. This is the range (R) for the group.

> For example for the first group of five packages: +2 +4 +5 +10 +3 R = +10 - (+2) = 8

If there are only minus errors in the group, subtract the largest number with a minus sign from the smallest number with a minus sign. This is the range (R) for the group.

For example for the second group of five packages: -2 -4 -5

$$-10$$

-3
R = -2 - (-10) = 8

0

If there are both plus and minus errors in the group of five, add the largest error which has a plus sign to the largest error which has a minus sign (but ignore the minus sign). This is the range (R) of the group. For example for the third group of five packages: +2 -4

- +5+10 -3 R = +10 + 4 = 14
- Calculate the sum of all R and note the number of groups. For example, let us consider the previous three examples as one set of sample data. For these examples the sum of R = 8 + 8 + 14 = 30 and the number of groups is 3.
- 4. Calculate the average R, called $\bar{\mathsf{R}},$ as follows:

 $\bar{R} = \frac{Sum of all R (step 3)}{number of groups}$

In the example above, $\bar{R} = \frac{30}{3} = 10$

APPENDIX G.

Table G-1. Tolerances for field standard weights (avoirdupois and metric).^a

CLASS F STANDARD	TOLERANCES FOR WEIGHTS (Avoir	FIELD dupois)	CLASS F TOLERANCES FOR FIELD STANDARD WEIGHTS (Metric)		
Tolerances for weights 2 lb or larger are 1 part in 10,000; weights between 0.5 lb and 0.02 lb are 1 part in 5,000; weights smaller than 0.02 lb have tolerances determined by the equation in footnote c. For all denomi- nations not shown, but which are intermediate between those listed, the tolerance for the smaller denomination shall apply.			Tolerances for weig 1 part in 10,000; w 10 g are 1 part in than 10 g have tole the equation in foo denominations not s intermediate betwee tolerance for the s apply.	hts 1 kg or larger are eights between 300 g and 5,000; weights smaller rances determined by tnote c. For all hown, but which are n those listed, the maller denomination shall	
Denomination	Tole	rances	Denomination	Tolerances	
Pounds (1b)	Pounds (1b)	Grams (g)	Kilograms (kg)	Grams (g)	
10,000 5,000 3,000 2,500 2,000 1,000 500 100	1.00 0.50 0.30 0.25 0.20 0.10 0.05 0.010	454 227 136 113 90.5 45.5 22.5 4 5	500 300 200 100 50 30 20 10	50.0 30.0 20.0 10.0 5.00 3.00 2.00 1.00	
50 30 20 10	0.005 0.003 0.002 0.001	2.3 1.4 0.91 0.45	5	Milligrams (mg) 500 300	
	Micropounds	Milligrams (mg)	2	200 100	
5 3 2 1 0.5 0.3 0.2 0.1 0.05 0.03 0.02 0.01 0.005 0.003 0.002 0.001 0.002 0.001 0unces (oz)	(μ1b) 500 300 200 154 100 60 40 20 10 6 4 3.20 2.58 2.18 1.92 1.54 Micropounds	227 136 91 70 45 27 18 9.1 4.5 2.7 1.8 1.45 1.17 0.99 0.87 0.70 Milligrams (mg)	Grams (g) 500 300 200 100 50 30 20 10 ^C 5 3 2 1 Milligrams (mg) 500 300 200	70 60 40 20 10 6 4 2 1.50 1.28 1.12 0.90 0.72 0.61 0.54	
$ \begin{array}{c} 8\\ 4\\ 2\\ 1\\ (1/2) 0.5\\ 0.3\\ (1/4) 0.25\\ 0.2\\ (1/8) 0.125 \end{array} $	(μ1b) ^b 100 50 25 12 6.2 3.92 3.70 3.44 2.96	45 23 11 5.4 2.8 1.78 1.68 1.56 1.34	100 50 30 20 10 5 3 2 1	0.43 0.35 0.29 0.26 0.21 0.17 0.14 0.12 0.10	

Denomination	Tole			
Ounces (oz)	Micropounds	Milligrams (m	ng)	
0.1 (1/16) 0.0625 0.05 (1/32) 0.03125 0.03 0.02 0.01	(μ1b) ^b 2.76 2.38 2.20 1.90 1.87 1.65 1.32	1.25 1.08 1.00 0.86 0.85 0.75 0.60		

Table G-1. Tolerances for field standard weights (avoirdupois and metric) (Continued).

^aNBS Handbook 105–1, <u>Specifications and Tolerances for Reference Standards and Field</u> <u>Standard Weights and Measures.</u> 1. <u>Specifications and Tolerances for Field Standard</u> <u>Weights and Measures</u>, in preparation.

^bl μ lb = 0.000001 lb

^CThe following equation for tolerances for weights smaller than 10 g is designed to be used only with metric units. Avoirdupois values must be converted.

 $T(w) = 0.9 w^{0.318}$ where T(w) is the tolerance in milligrams and w is the metric equivalent in <u>grams</u> of the nominal weight for which the tolerance is being determined.

APPENDIX G

Table G-2. Scale units and tolerances for field standard flasks and cylinders (inch-pound and metric fluid measures) a Scale units for flasks in inch-pound fluid measure

Size		Graduated range of each side of nomi	n nal	Minimum graduation
Gill 1/2 Pint Pint Quart 1/2 Gallon Gallon		1/2 fl dr 1 fl dr 2 fl dr 4 fl dr 6 fl dr 8 fl dr		1/4 fl dr 1/4 fl dr 1/2 fl dr 1 fl dr 1 fl dr 1 fl dr 1 fl dr
Tolerances for (with	inch-	pound field stand versions to millil	ard flas iters)	ks and cylinders
Nominal capacity at 68 °F		Tolerances at nominal capac	ity	Tolerances at total or partial capacity (i.e. graduated portion)
1 Gill 1 920 Minims (118.3 m 1/2 Pint 3 840 Minims (236.6 m 1 Pint 7 680 Minims (473.2 m 1 Quart 15 360 Minims (946.3 m 1/2 Gallon 30 720 Minims (1 892.7 1 Gallon 61 440 Minims (3 785.4 2 Fluid 960 Minims (59.1 mL Ounce Cylinder	3 Minims (0.18 4 Minims (0.25 7 Minims (0.43 12 Minims (0.74 16 Minims (0.99 20 Minims (1.23 5 Minims (0.31	mL) mL) mL) mL) mL) mL)	1.0 Minims (0.06 mL) 1.5 Minims (0.09 mL) 3.0 Minims (0.18 mL) 5.0 Minims (0.31 mL) 5.0 Minims (0.31 mL) 5.0 Minims (0.31 mL) 5.0 Minims (0.31 mL)	
Sc	ale u	units for metric f	lasks	
Size		Graduated range o each side of nomi	n nal	Minimum graduation
100 mL 200 mL 250 mL 500 mL 1000 mL 2000 mL		2 mL 4 mL 4 mL 8 mL 15 mL 25 mL		0.5 mL 0.5 mL 0.5 mL 0.5 mL 1.0 mL 1.0 mL
Tolerance	es foi	r metric field sta and cylinders	ndard fl	asks
Capacity	ſ	Tolerance at nominal capacity	Toler or pa (i.e.	ance at total rtial capacity graduated portion)
10 mL ^b 100 mL 200 mL 500 mL 1000 mL 2000 mL 50 mL cylinder	0.2 mL 0.3 mL 0.3 mL 0.5 mL 1.0 mL 0.3 mL		0.08 mL 0.10 mL 0.10 mL 0.20 mL 0.30 mL 0.30 mL	

^aNBS Handbook 105-2, <u>Specifications and Tolerances for Reference Standard and Field</u> <u>Standard Weights and Measures. 2. Specifications and Tolerances for Field Standard</u> <u>Measuring Flask</u>, revision in preparation.

^bTolerance of 10 mL graduate is 0.08 mL calibrated "to contain" and 0.10 mL calibrated "to deliver".

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11. ABSTRACT (A 200-word o	or less factual summary of most s	significant information. If docume	ent includes a significant		
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This handbook pr	ovides procedures for	testing individual lot	s of packaged goods		
for conformance	with legal requirement	ts for the net quantity	y of contents using		
statistical samp	ling techniques. In :	its advisory capacity,	NBS provides these		
methods as guide	lines.				
The handbook is	divided into firm the		free The Circuit		
the handbook is	alvided into rive chap	pters and seven append:	Lees. The first		
chapter covers i	meroductory material (on package inspection.	Ine second chapter		
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