UNITED STATES EPARTMENT OF OMMERCE UBLICATION



## NBS TECHNICAL NOTE 615

# WR15 Thermal Noise Standard

U.S. PARTMENT OF COMMERCE National Bureau

QC 100 U5753 no.615 1972 copy 2

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## TECHNICAL NOTE 615

#### **ISSUED MARCH 1972**

Nat. Bur. Stand. (U.S.), Tech Note 615, 154 pages CODEN: NBTNA

## WR15 Thermal Noise Standard

W. C. Daywitt, W. J. Foote, and E. Campbell

Electromagnetics Division Institute for Basic Standards National Bureau of Standards Boulder, Colorado 80302



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#### ERRATA

| Page No. | Line No.             | Erratum                        |
|----------|----------------------|--------------------------------|
| 17       | 15                   | "Silicon" to "Silicon carbide" |
|          | 16                   | "Silicon" to "Silicon carbide" |
|          | last                 | "beryllium" to "beryllia"      |
| 21       | 7                    | "varified" to "verified"       |
| 31       | last                 | "Si" to "SiC"                  |
| 32       | 7,12,25              | "Si" to "SiC"                  |
| 33       | 2,6,9,10<br>12,14,20 | "Si" to "SiC"                  |

2. 3.

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W. C. Daywitt, W. J. Foote, and E. Campbell

#### ABSTRACT

This note describes the design and construction of a WR15 thermal noise power standard. The standard is designed to operate around the Silver Point Temperature (963.19°C) with a noise temperature output accurate to approximately  $\pm 2$  K.

Complete details of the theory, design, construction, and performance tests are given.

Key Words: Noise; Thermal noise standard; Millimeter wave; Error analysis; Nyquist's theorem.

#### 1. INTRODUCTION

This note describes the analysis, design, construction, and performance tests of the NBS WR15 Thermal Noise Power Standard. This standard consists of a 0.148" x 0.074" I.D. rectangular waveguide that is terminated by a well matched load. The load and waveguide are heated to approximately 962°C in a specially designed oven. The noise temperature output of the standard is approximately 1235 K and is known to an accuracy of approximately ± 2 K. A sample of the output temperature T as a function of frequency is shown in figure 1.1.

The description of the standard is divided into three parts: The internal oven components; the external oven

components; and the auxiliary components. The internal components include the high temperature resistive generator or termination, the inconel heat distributor and heating coils, the high temperature platinum 10% rhodium waveguide, and the thermocouples. The external oven components include the oven casing and the cooling coils. The auxiliary components include the control rack containing the oven temperature monitor and controlling circuits, and the recirculating cooling system. Photographs of the total system are shown in figures 1.2, and 1.3.

Before the design and construction were begun, a thorough error analysis of the proposed standard's noise temperature output was performed to determine the necessary design specifications for holding the error to approximately ± 2 K. This error analysis along with the noise output calculation were computerized and used to determine the final error estimate.

The rest of the report is divided into three sections, each with a number of subsections. Where necessary they are liberally augmented by appendices to avoid destroying continuity, and a large amount of cross-referencing to avoid excessive repetition. The figures and drawings are labled alphanumerically, where the number or letter before the decimal point indicates in which section or appendix the principle discussion of the figure is to be found.

The discussion of noise power output and error calculations for the standard are contained in section 2. The discussion of important design specifications resulting from these calculations is found there also. Section 3 contains a description of, and the design and construction details for the standard. Measurement results and observations taken during the course of construction and final testing of the standard are found in section 4, as are the performance tests supporting the output and error calculations.

In many cases detail drawings of an item under discussion are not presented and the reader is hereby referred to the main assembly drawing (drawing #1). However, detail drawings are available upon request.

Most of the fabrication was done in the Shops Division (282) and measurements in the Electromagnetics Division (272) of the Institute for Basic Standards of the National Bureau of Standards, Boulder Laboratories.

Throughout the text SS stands for subsection, ap for appendix, and () for an equation. For example, the equation for  $\Delta T$  is to be found both in SS 2.1 as (2.2), and in ap A as (A.2).

A proposed standard must undergo rigorous NBS internal review before acceptance as a national standard. This review requires complete documentation of all work associated with theory, design, construction, and evaluation of the proposed

standard. Therefore, since this note was drafted for such documentation, and since it is intended for metrologists with interests similar to the authors', a number of items are contained herein which ordinarily would be<sup>h</sup>omitted from a document intended for more general distribution.

#### 2. ANALYSIS

The average thermal noise power output of a standard is described by the noise temperature T [1] which is the thermal noise power P per unit bandwidth available at its output connector divided by Boltzmann's Constant k. That is

$$T \equiv \frac{P}{k}$$

In the standard, T is a calculated quantity [2] against which the noise temperature of another noise source can be compared. This calculated noise temperature depends upon a number of parameters of the physical source, and the corresponding error,  $\delta T$ , in T is the result of uncertainties in these parameters.

This section deals with the calculation of T and  $\delta$ T and the resulting design specifications. In particular, SS 2.1 covers the details of calculating T, and SS 2.2 with those of  $\delta$ T. Subsection 2.3 discusses the design specifications.

#### 2.1. Noise Temperature Output

A schematic drawing of a heated thermal noise source is

shown in figure 2.1. The impedance Z terminates a transmission line used to convey the noise power from the impedance to an accessible output port. The impedance and part of the line is maintained at an elevated temperature by an appropriately designed oven. The available output power P is the sum of two effects; the noise power generated by Z and attenuated by the line, and the noise power generated by the line itself. The calculation of P or T requires the line to be uniform and reflectionless, and is the subject of this subsection.

An equivalent circuit model of figure 2.1 is shown in figure 2.2.  $T_m$  represents the measured temperature of the impedance Z terminating the end of the line at x = 0.  $T_x$ is the measured temperature distribution along the line from x = 0 to the output connector at  $x = \ell$ .  $\alpha_x$  is the available power ratio [1] for the length of line from x to  $x = \ell$ , and  $a_x$  is the attenuation per unit length (dB/length) of the line at x. T is the output noise temperature and is the result of the attenuated noise  $\alpha_0 T_m$  of the impedance and the noise contributed by the line. T can be written as the sum of the impedance temperature  $T_m$  and a correction temperature  $\Delta T$  which accounts for the total effect of the line.

$$T = T_m + \Delta T \tag{2.1}$$

A convenient expression for the correction is given by (ap A)

$$\Delta T = (T_0 - T_m) (1 - \alpha_0) + \int_0^{\chi} T'_x (1 - \alpha_x) dx$$
(2.2)

where  $T_0$  is  $T_{x=0}$ ,  $\alpha_0$  is  $\alpha_{x=0}$ , and  $T'_x$  is the temperature gradient along the waveguide. In terms of the decibel attenuation  $A_x$  of the line from x to  $x = \ell$  (ap A)

$$\alpha_{\rm X} = 10^{-A_{\rm X}/10} - \frac{2|\Gamma_{\rm L}|^2}{1 - |\Gamma_{\rm L}|^2} \operatorname{Sinh}(A_{\rm X}/10 \ \log e)$$
(2.3)

where

$$A_{x} \equiv \int_{x}^{\chi} a_{z} dz. \qquad (2.4)$$

The last term in (2.3) is both a function of the line loss  $A_X$ and the standard's reflection coefficient  $\Gamma_{\ell}$ .  $A_X$  and  $\Gamma_{\ell}$  are usually small, making the last term small and resulting in a noise temperature T that is independent of the reflection coefficient. A rough estimate of the size of the uncertainty in  $\Delta T$  when this last term is neglected is given by

$$2(\overline{T}-T_{m}) |\Gamma_{\varrho}|^{2} (0.23\Delta)$$
 (2.5)

where  $\overline{T}$  is the average temperature of that portion of the  $T_x$  curve from the high temperature fall off to x = l, and  $\Delta$  is the attenuation in dB of that same region.

The attenuation per unit length is given by

$$a_{X} = c \rho_{X}^{\frac{1}{2}}$$
 (2.6)

where c is a constant that is a function of the frequency and the geometry of the line, and  $\rho_{\rm X}$  is the resistivity of the line material. The variation of this resistivity with temperature for an alloy of 90% platinum - 10% rhodium (Pt - 10 Rh) is shown in figure 2.3.

The attenuation per unit length can be treated in either of two ways; it can in general be measured as a function of temperature, or calculated from (2.6) in certain instances. Measurement data for  $a_x$  as a function of temperature is difficult to obtain and generally unavailable. Therefore  $a_x$ is calculated from (2.6). Justification for this decision is to be found in SS 4.1.4.

The WR15 noise standard employs a Pt - 10 Rh waveguide (SS 3.1.2) of inner dimensions 0.148" x 0.074", with a terminating element whose reflection coefficient is not greater than 0.006 (SS 3.1.1). A computer program (ap D) has been written for the calculation of  $\Delta T$  (fig. 1.1) and its associated error (fig. D.1.), neglecting the second term in (2.3) (ap A). In order to perform this calculation, the computer requires the waveguide temperature distribution x versus T (fig. 2.5), the resistivity dependence upon the temperature

 $(\rho^{\frac{1}{2}} = A_0 + A_1 t + A_2 t^2 + A_3 t^3)$ , the operating frequency F in GHz, the transverse waveguide dimensions A and B, and the termination temperature  $T_m$ . For the sample temperature distribution (SS 4.4.2) shown in figure 2.5, where the termination temperature is 962.0°C (1235.2 K), the computed correction temperature  $\Delta T$  and its error are

$$\Delta T = -26.3 \text{ K}$$

and

$$\delta \Delta T = \pm 1.5 \pm 0.9 = \pm 2.4 \text{ K},$$

0.9 K being added due to uncertainties in the temperature distribution (SS 4.4.2). The variation of  $\delta \Delta T$  with frequency for the sample data in figure 2.5 is shown in figure 2.4.  $\Delta T$  as a function of frequency is found in figure 1.1.

#### 2.2. Error Analysis

The total maximum uncertainty, or error,  $\delta T$  in the output noise temperature can be written as (ap C)

$$\delta T = (\delta T)_{T_{m}} + (\delta T)_{T_{0}} + (\delta T)_{\ell} + (\delta T)_{0} + (\delta T)_{\rho} + (\delta T)_{c} + (\delta T)_{g} + (\delta T)_{1} + (\delta T)_{W} + (\delta T)_{A}$$
(2.7)

where

$$(\delta T)_{T_m} \equiv$$
 the uncertainty in T caused by the uncertainty  
 $\delta T_m$  in  $T_m$  (SS 4.4.1).  
 $(\delta T)_{T_0} \equiv$  the uncertainty in T caused by the uncertainty  
in  $T_0$ .

- $(\delta T)_{\ell}$  = the uncertainty in T caused by the uncertainty in the position of the output connector at  $x = \ell$ . Since the reference position is taken at the output connector,  $(\delta T)_{\ell} = 0$ .
- $(\delta T)_0 \equiv$  the uncertainty in T caused by the uncertainty in the position (x=0) of the termination.
- $(\delta T)_{\rho} \equiv$  the uncertainty in T caused by the uncertainty in  $\rho$ .
- (δT)<sub>c</sub> ≡ the uncertainty in T caused by the uncertainty in c.

$$(\delta T)_1 \equiv$$
 the uncertainty in T caused by neglecting the second term in (2.3).

 $(\delta T)_A \equiv$  the uncertainty in T (ap I) caused by air attenuation in the waveguide.

 $(\delta T)_g$  can be estimated in either of two ways as pointed out in ap C. The second method is employed here as explained in SS 4.4.2.

Using the sample temperature distribution in figure 2.5, the results of the error calculation for the WR15 standard (figure D.1.) are tabulated below along with their computer output designations where applicable.

| Parameter Uncertainty<br>(With Computer Designation) | Corresponding<br>Uncertainty in T | Percent of<br>Total Uncertainty |
|--|-----------------------------------|---------------------------------|
| δT <sub>m</sub> (DTM) = 0.4 K                        | 0.342                             | 14.2                            |
| δT <sub>T</sub> (DTO) = 0.5 K                        | 0.0724                            | 3.0                             |
| $\delta T_{\ell}$ (DDB) = 0                          | 0                                 | 0                               |
| $\delta T_{0} (DDO) = 1/4''$                         | 0                                 | 0                               |
| $\delta T_{\rho}$ (DR) = 10%                         | 0.0234                            | 1.0                             |
| $\delta T_{c}$ (DC) = 2.46%                          | 0.637                             | 26.3                            |
| (oT) <sub>g</sub> (See SS 4.4.2)                     | 0.92                              | 38.1                            |
| $(\delta T)_{W}$ (See ap C)                          | 0.36                              | 14.9                            |
| (See ap I) (See ap I)                                | 0.05                              | 2.1                             |
| (See ap A) (See ap A)                                | 0.01                              | 0.4                             |
| Error (Total Uncertainty)                            | ) 2.41 K                          |                                 |

The value for  $(\delta T)_g$  was obtained from the three computer correction calculations  $\Delta T$  shown in figure 2.6, as the difference between the first and second or second and third  $\Delta T$ 's. The curve in figure 2.5 is the curve C in figure 4.7, from which the correction temperature  $\Delta T$  (Delta T in the computer

output) for the standard's output noise temperature is calculated. Thus the noise temperature output is

$$T = T_{m} + \Delta T \pm \delta T$$
  
= 1235.2 - 26.3 ± 2.4  
= 1208.9 + 2.4. (2.8)

The calculations leading to (2.8) were carried out for the operating frequency of 55 GHz. Figure 2.4 shows this error as a function of frequency for the band from 55 GHz to 65 GHz.

#### 2.3. Critical Design Specifications

Before a final design for the WR15 standard was chosen, a number of error calculations similar to the calculation in SS 2.2 were performed on different assumed temperature distributions. One important characteristic of the temperature distribution can be seen in figure 4.7. With the separate parameter uncertainties being held constant, the three distributions shown in the figure each produce an error  $\delta \Delta T$  as shown. It is obvious from the figure the farthest right produces the least error. Thus the temperature transition region, that region where the temperature distribution falls from a value near the termination temperature  $T_m$  to a value near the output connector temperature  $T_c$ ,

should be kept as near the output connector as possible if the output error is to be reduced to a minimum. This consideration is given considerable weight in the present design (SS 3.1).

Another uncertainty,  $(\delta T)_{c}$ , which is negligible at lower frequencies (e.g., WR62, 90, and 284), contributes a large portion of the error in WR15. Most of this uncertainty (ap C) comes from dimensional tolerances (SS 3.1.2) and shows that the transverse dimensions of the waveguide must be held to as tight a tolerance as possible.

The next largest uncertainty in T comes from the measurement of the termination temperature  $T_m$ . The uncertainty,  $\delta T_m$  in  $T_m$  (SS 4.4.1) comes from the uncertainty in the temperature gradient across the termination, and the calibration uncertainty of the thermocouple used in the measurement.

The other sources of uncertainty are seen to be insignificant when compared to these first three discussed. The details of their origin may be found in ap C.

#### 3. DESCRIPTION AND DESIGN

A block diagram for the operation of the WR15 noise standard is shown in figure 3.1. The termination and waveguide are placed in an oven that feeds information in the form of thermocouple EMF's to a potentiometer for temperature measurement, and to the heating control circuits. The EMF's

fed to the control circuits can, at will, be measured by the potentiometer. This measurement allows the heating coil temperatures to be adjusted to insure that a predetermined temperature distribution can be repeated (SS 4.4.3). The outputs from the circuit control transformers that supply currents to three heating coils in the oven, allowing the temperature gradient within the oven to be held constant. A separate temperature controlled ( $22^{\circ}C \pm 0.05^{\circ}C$ ) water cooling system keeps the output connector of the standard at room temperature and cools the oven casing.

These components can be located in figures 1.2 and 1.3. The cylindrical object that has been placed on the table is the oven with the output connector at its left end as shown in figure 1.2, and with the thermocouples and ice baths evident in figure 1.3. The clear plastic tubing conducts water to the water cooled output flange, through coils inside the cylindrical casing to the rear oven cooling plate, then back to the recirculating cooler at the bottom right of the photographs. The oven sits on an oven carriage that can ride in the same rail on which the comparison radiometer is mounted. The carriage has four adjustments that allow the output connector of the standard to be precisely mated to the radiometer input connector. The thermocouples which monitor the coil temperatures and those used to measure the termination temperature are inserted through the rear cooling plate (fig. 1.3).

They are connected in the ice baths to thermocouple grade, Teflon\* coated copper wire leads. The ice baths are contained in the silvered vacuum bottles and ride on a platform that is connected to the oven carriage. The copper leads conduct the thermocouple EMF's to the measurement and control rack at the left in the figures. These leads are contained in a small plastic tube that enters the rack just under and to the left of the rack desk. The short looped piece of larger plastic tubing attached to the rack allows the thermocouple leads to be held without kinking. These leads then enter a terminal strip contained in the aluminum shell just under the rack desk. The EMF's from three of the leads, from the thermocouples monitoring the coil temperatures, are balanced against three internally generated EMF's and are then amplified by the three amplifiers located in the lower half of the rack. The amplified outputs are then conducted to the three control circuits at the bottom interior of the rack. The three dials at the bottom of the rack adjust the three internally generated EMF's. The resulting coil currents are conducted through three fused ammeters and out through the cord at the bottom of the rack into the rear of the oven (fig. 1.3) to the oven heating coils. The precision potentiometer

<sup>\*</sup>Certain commercial materials are identified in this paper in order to adequately specify the experimental procedure. In no case does such identification imply recommendation or endorsement by the National Bureau of Standards, nor does it imply that the material identified is necessarily the best available for the purpose.

used to measure the EMF's is located at the top of the rack. The current source for the potentiometer is located inside the rack. The null detector used with the potentiometer, and the switch used to connect the individual leads to the potentiometer, are located just above the rack desk.

The details of the design and construction of these components are contained in the following subsections. SS 3.1 contains the details of the internal oven components, including the waveguide termination, the waveguide, the heat distributor, heating coils, sleeve, and the thermocouples. A description of the thermocouple ice baths is also given in this subsection. SS 3.2 contains the details of the external oven components, including the oven casing, the support spider from which the internal components are suspended, the cooling coils, and the carriage. SS 3.3 contains the details of the auxiliary components consisting of the temperature measurement system, the heating control system, and the water cooling system.

#### 3.1. Internal Oven Components

Drawing #1 shows the oven assembly and carriage. The oven assembly itself (items 25 through 41) shows the internal oven components (items 26, 32, 33, 34, 40, and 41) suspended in the center of the oven casing (items 24, 31, 35) by the supporting spiders (item 36) which are bolted to

the oven end plates (items 29 and 35). The internal components shown include the resistive termination (item 41), the high temperature waveguide (item 26), the inconel heat distributor (item 32) with three sets of bifilar wound heating coils, and the locking rings (item 42) which hold the heat distributor together and support it in the heat distributor sleeve (item 33). Not shown in the drawing is the insulation packed between the coils and the sleeve, at both ends of the heat distributor, and just inside the cooling coils (item 30) leaving an air gap between this insulation and the insulation around the sleeve. Two of the thermocouple grooves in the heat distributor are shown.

When in operation, the front coil (left in the drawing) is used to keep the front end of the heat distributor as near as possible to the termination temperature (SS 2.3); the center coil is used to set the termination temperature; and the back coil is used to compensate for heat loss from the rear of the oven.

#### 3.1.1. High Temperature Resistive Generator

The high temperature termination (resistive generator) from which most of the standard's noise power output originates is designed for high RF loss, high thermal conductivity, and a low reflection coefficient. To insure that the termination material had sufficient loss from 55 to 65 GHz, the losses of

a number of materials were measured (SS 4.1.2) in this band. From this data the length of termination needed could be estimated to be great enough to completely terminate the waveguide, and to provide a low reflection coefficient.

A low reflection coefficient (SS 4.1.3) was achieved by cutting the termination material at an angle to its length resulting in a face length (ap F) of 0.75". The length of material needed turned out to be 0.28" (ap G) resulting in a minimum termination length of approximately 1". It is over this 1" length that the termination temperature  $T_m$  is determined (SS 4.4.1). The final overall length chosen was 2.3" (drawing #2).

To achieve a high thermal conductivity at high temperatures, the material chosen was a homogeneous mixture of beryllium oxide and 40% silicon, the beryllium oxide providing the high thermal conductivity and the silicon the high RF loss. Figure 3.2 shows a table of thermal conductivities for a number of materials.

The final design, shown in drawing #2, has a cutting angle of 23.4° corresponding to vertical and horizontal face angles of 10° and 24° respectively. The cutting angle is used by the manufacture in fabricating the termination, which could not be done "in-house" because of the toxic nature of beryllium [3]. The edges of the termination have a 0.006"

chamfer to allow good thermal contact with the waveguide walls. A 0.5" groove is provided at the end of the termination to allow a hollow ceramic  $(Al_2O_3)$  rod to be attached  $(Al_2O_3$ cement). The rod is used to position the termination longitudinally in the waveguide and to provide a means for inserting a thermocouple into the back of the termination. After cementing, the load and rod are cured at 1100°C in a laboratory furnace.

#### 3.1.2. High Temperature Waveguide

The high temperature (962°C) waveguide provides a low loss transmission path from the high temperature termination to the output connector of the noise source. To allow the use of (2.6) (SS 2.1) in calculating the noise output, the inside waveguide dimensions must be precisely known (to calculate c accurately), and the waveguide resistivity as a function of temperature known to calculate  $\rho_x^{\frac{1}{2}}$ .

The dimensions of the waveguide are 8  $3/8" \ge 0.228"$ (± .001)  $\ge 0.154"$  (± .001) with corner bend radii less than 0.031" outside; by 0.148"  $\ge 0.074"$  (± .001) with corner bend radii less than 0.006" inside. The dimensional tolerances can produce a reflection as large as 0.01 (ap H and SS 4.1.3) from the waveguide when compared to a perfect waveguide.

The length of the waveguide, although not critical, was chosen long enough to protrude out of the heat distributor and into the cooler region of the insulating felt at the rear end of the oven. This was done to avoid contamination of the inside of the waveguide by heat distributor.

An alloy of 90% platinum and 10% rhodium was chosen for the waveguide material because it has proven to follow (2.6) quite well (SS 4.1.4) in the past. Other important reasons for choosing this material were [2]: 1) its nonmagnetic character avoids uncertainties associated with the Curie Point suffered by magnetic materials; 2) it has a high resistance to oxidation and corrosion; 3) it has a high melting point (fig. 3.3); 4) it is not too soft for repeated high temperature use; 5) it is fairly workable; and 6) there is a large amount of resistivity data available for platinum 10% rhodium [4]. Some care must be taken to reduce the free silicon content around the waveguide in the high temperature region of the oven. This silicon can combine with the platinum in the waveguide and the standard thermocouples to form a eutectic that melts around 800°C [5].

For the length of line from the termination to the output connector, atmospheric attenuation (fig. 3.4) in the waveguide produces a completely negligible effect on the output noise temperature (ap I).

#### 3.1.3. Heat Distributor Assembly

The heat distributor assembly consists of the heat distributor (item 32 in drawing #1), the heating coils, the heat distributor sleeve (item 33), the locking rings (item 34), and the insulation surrounding the sleeve and both ends of the heat distributor, and between the coils and the inside of the sleeve.

The heat distributor is approximately 2 1/4" in diameter and is constructed in two halves (fig. 3.5) with four flanges to separate and contain the heating coils. By studying the photograph, six thermocouple grooves and the main waveguide groove can be discerned. A radial bifilar coil is wound into the front end section (right end in the photograph). The distributor is fabricated from inconel "601," a high temperature alloy compound of approximately 76.0% Ni, 0.04% C, 0.20% Mn, 7.20% Fe, 0.007% S, 0.20% Si, 0.10% Cu, and 15.8% Cr [6]. The thermal properties of this material for comparison with other materials can be found in figure 3.2.

Boron nitride [7] is another material that was considered for the heat distributor. This material has a very high thermal conductivity at 1000°C (fig. 3.2) and is very machinable. Figures 3.6 and 3.7 show a finished boron nitrade distributor. The center and back coils are wound directly on the distributor (fig. 3.7). In tests with this material it was found that when heated to 1000°C a sticky substance,

possibly boric oxide [7], was formed that became a "glass" at room temperature. This flaw prevented its use in the noise standard. Some work with the material was done in a nitrogen atmosphere with the same results, but was not conclusive. Experimentation with the material was discontinued as soon as the high stability of the inconel "601" distributor at elevated temperatures was varified.

Drawing #3 shows the dimensions of the heat distributor and the placement of the thermocouple grooves. By referring to the bottom profile the three separate heating coils, which are all bifilar wound, may be located. The back (left hand) coil is wound from left to right and back. The center coil is wound from right to left and back, and the front coil is wound from inside to outside along the radial groove provided. The coils are an #18 gauge (0.040" diameter) resistance wire on which are strung alumina  $(Al_2O_3)$  fish spine beads (0.11" O.D. x 0.056" I.D. x 0.110" length) to prevent shorting. The wire is an alloy of 5.5% Al, 22% Cr, 0.5% Co, and 72% Fe with a resistance to oxidation considerably greater than the nichrome wire used in previous NBS noise standards.

The inconel sleeve which contains the distributor and coils is shown in figure 3.8 on the left of the photograph. Also shown are the inconel locking rings which hold the two halves of the distributor together and support

them in the sleeve. The assembled heat distributor with the waveguide and eight thermocouple grooves are shown at the right. Figure 3.9 shows the whole assembly, including the sleeve, locking rings, and heating distributor from the front. The front and center heating coil leads are brought through two of the front slots while the rear heating coil lead is brought through a slot in the rear of the assembly.

Three forms of zirconium oxide insulation [7] were used in the standard, a 0.15" felt, a cloth, and a yarn. The insulating characteristics of this material are indicated in figure 3.10 and in SS 4.2.1.

#### 3.1.4. Thermocouples

The detailed locations of the thermocouple grooves are given in drawing #3. Figure 3.11 shows a schematic diagram of the location of the tips of the thermocouples. The dots represent the points at which the temperature of the heat distributor is sampled by the thermocouple junction. The three control thermocouples B, C, and F are located in close contact to the back, center, and front heating coils respectively, and are connected to three separate servocontrol circuits that maintain the coils at given temperatures. S<sub>2</sub> and S<sub>3</sub> are calibrated standard thermocouples

in contact with the waveguide and can be positioned anywhere along the dotted line to be just above and below the termination. The thermocouples are used, in conjunction with a third  $(S_1)$  inserted in the rear of the termination, to determine the average termination temperature (SS 3.1.1). The other thermocouple grooves shown in drawing #3 turned out to be unnecessary and are not used.

The thermocouples are constructed by fusing two dissimilar metal leads together and running the two leads through a double bore ceramic tube. The junction resulting from fusing generates the EMF which indicates the temperature. The ends of the leads are soldered to thermocouple grade copper wire leads and are immersed in a non-conducting liquid which is cooled in an ice bath to 0°C. The copper leads then convey the resultant EMF to a suitable measuring instrument.

The standard thermocouples  $S_1$ ,  $S_2$ , and  $S_3$  employ a reference grade, 0.010" diameter platinum wire and a platinum – 10% rhodium wire for the two leads. The ceramic tube is a high purity (99.8%) alumina ( $Al_2O_3$ ) tube with 0.047" ± 0.003 O.D., and 0.014" bores. The table in figure 3.2 shows some of the properties of the alumina and figure 3.12 shows a graph for the EMF output versus temperature for the platinum 10% rhodium thermocouple. The leads are cut to 36" lengths and sent to NBS-Gaithersburg where they are fused together at

one end, annealed, and calibrated (fig. 3.13) according to Schedule 221.112Z found in the NBS Special Publication 250. After the thermocouple has been calibrated, it is returned with a calibration report (fig. 3.13), inserted into a double bore ceramic rod, and soldered to the copper leads. Extreme care must be exercised in handling the thermocouple [5] after it has been calibrated.

The control thermocouples B, C, and F are constructed from 0.005" diameter Platinel #7674 and #5330 wire leads in a similar fashion to the standard thermocouples. The rod has a 0.031"  $\pm$  0.003 O.D. with 0.007" bores. This thermocouple has a high output as a function of temperature (fig. 3.13) and a longer life, making it more suitable for control purposes.

#### 3.2. External Oven Components

The oven casing (drawing #1) is constructed from a welded aluminum cylinder of 5.75" diameter onto which two brass end plates are bolted. The rear plate supports the rear support spider, the rear guide plate, and waterjacket. The output (front) end plate supports a support spider, and contains a concentric 2.5" diameter hole into which is bolted the water cooled flange of the high temperature waveguide.

The support spiders are constructed so that (ap J) as the heat distributor sleeve expands on heating, the ends of the sleeve in contact with the tapered spiders remain in

contact, keeping the sleeve and heat distributor concentric with the oven casing, thus preventing damage to the waveguide.

A 3/16" helical copper cooling coil is inserted just inside and in contact with the cylindrical oven casing. This coil protrudes through slots at both ends of the casing where it is connected to the lower adaptors of the end plates. When in operation, coolant flows in the front top adaptor, through the coil, and out the back top adaptor of the rear end plate to maintain the oven casing at room temperature. The platinum-rhodium waveguide is soft soldered into the front water cooling flange, protruding enough to allow a WRI5 flange to be attached. The composition of the solder used is 95% Tin - 5% Silver. A cylindrical jacket of insulation is located inside the I.D. of the cooling coil with an air gap between this insulation and the insulation surrounding the heat distributor sleeve.

The oven carriage is designed for single-handed adjustment of the oven position while mating the output waveguide flange to the flange of a radiometer. The plastic wheels of the carriage are designed to run in the same rail to which the radiometer is attached.

#### 3.3. Auxiliary Components

Figure 3.1 shows the three auxiliary systems used in the standard; the temperature measurement system (fig. 3.14), the heating control system (fig. 3.15), and the water cooling system. These systems are described in this section.

#### 3.3.1. Temperature Measurement System

The ice bath, used as a 0°C reference junction where the thermocouple leads are soldered to copper leads, consists of a 440 cc. vacuum insulated bottle filled with distilled water and ice (made from distilled water) in equilibrium at 0°C. Glass test tubes prepared from 1/4" tubing contain the soldered junctions and are immersed in the ice baths. Before the junctions are inserted into the test tubes, each tube is partially filled with a fluorochemical liquid to reduce temperature gradients along the leads and junctions.

The thermocouple grade, teflon coated copper leads conduct the EMF's from the bath to the terminal board. Approximately 13' of this wire is used for each lead (ap L).

The terminal board is housed in a metal shell to encourage a uniform temperature distribution along the junction terminals, thus minimizing the effects of thermal EMF's (SS 4.3.1) generated at the contacts of the copper leads and brass terminals of the terminal board.
The switch is a commercially available, low thermal-EMF switch that connects one switch output lead to any of the thermocouple input leads.

The potentiometer used to measure the EMF's is a commercially available high precision laboratory potentiometer, with a limit of error on the 9.1 mV range equal to 0.1°C when used with a constant current standardizing supply.

The brass lugs used on the leads between the switch and potentiometer, and between the potentiometer and the null detector were gold flashed to resist oxidation and minimize contact EMF's.

# 3.3.2. Heating Control System

A diagram of the heating control system is shown in figure 3.15. Both the oven and rack are gounded to the line ground. The current in the three heating coils are servo controlled to maintain known and small temperature gradients in the oven. The heating control is obtained by sampling the coil temperatures and maintaining them at a desired temperature via control circuits that are mechanically coupled to the current control transformers through drive motors. The maximum current settings of these control transformers are limited by the current limiting transformers to obtain maximum control sensitivity and to prevent the oven from overheating during warmup. The control transformers are commercially available 7.5 amp units,

three of whose shafts have been modified for coupling to servo control drive motors.

A diagram showing how the servo drive voltage is obtained, and how the coil temperatures are measured, is given in figure 3.16. The thermocouple EMF on the upper terminal of the board can be measured by the potentiometer to obtain the coil temperature. For control purposes, this EMF is opposed by an offset voltage set to a value corresponding to the desired coil temperature. The resulting correction voltage is amplified and fed to the control circuits.

A diagram showing the operation of the control circuits (ap M) is given in figure 3.17. A non-zero correction voltage changes the width of a square wave which is then compared to the width of a reference square wave by an "AND" gate. The resulting output signal actuates the transformer drive motors which adjust the transformers to control the coil currents.

The oven is brought up to temperature by the following procedure: 1) the limiting transformers are set to a value that will limit the maximum current available to the control transformers to a value that will not operate the coil fuses or burn out the coils; and 2) as the correction voltage approaches zero, as evidenced by the needle indicators on the amplifiers coming on scale, the limiting transformers are separately adjusted upwards in current to provide just enough

current to maintain the heating coils at temperature with zero correction voltage, or when the needle indicators read zero. Once up to temperature the heating controls need no further adjustment.

#### 3.3.3. Cooling System

The oven casing is cooled by circulating distilled water through the end plates and the cooling coil. The coolant is supplied from a constant temperature (± 0.05°C) bath and recirculated to the bath.

A manifold was constructed that allows the water pressure drop across the oven to be adjusted (fig. 1.2). A thermometer is provided in the manifold to monitor the water temperature entering the front cooling plate of the oven, and two pressure gauges allow the pressure drop across the manifold to be checked.

## 4. MEASUREMENTS AND OBSERVATIONS

This section contains measurement reports and observations made during the course of the design, construction, and testing of the noise standard. In addition, a few brief descriptions of measurement procedures and critical comments are given. For ease in locating specific data the section is subdivided into six subsections. Subsection 4.1 covers the measurements made on the internal oven components.

SS 4.2 and SS 4.3 cover the rest of the oven and auxiliary components.

Subsection 4.4, entitled "System Performance," contains the main measurement documentation supporting the conclusions drawn in previous subsections (SS 2.1 and 2.2) concerning the standard's output and accuracy.

Subsection 4.5 contains a potpourri of measurement data, some more important than others, that was accumulated during work on the standard. Much of the data is only tangentially related to the noise standard, but could be of use for future work and is therefore recorded here for later convenience.

Subsection 4.6 contains critical comments on the standard's construction, which although not incorporated in the present standard, could be put to profitable use later.

The various data appear under brief descriptive headings in a roughly descending order of importance.

## 4.1. Internal Oven Components

## 4.1.1. Thermocouple Accuracy

The thermocouples used to determine the termination temperature  $T_m$  were constructed (SS 3.1.4.) from 0.010" diameter thermocouple wire that was calibrated at NBS-Gaithersburg to an accuracy of  $\pm$  3 microvolts at the fixed points (fig. 3.13), and to an accuracy of  $\pm$  5 microvolts elsewhere in the range from 0°C to 1100°C. The termination temperature is held close to the silver point (961.93°C) to take advantage of the smaller  $\pm$  3 microvolt uncertainty in the calibration data. This amounts to a 0.27°C uncertainty at that temperature.

In measuring the thermocouple EMF with the laboratory potentiometer the measurement uncertainty is estimated to be (SS 3.3.1) 0.1°C. Thus, the total uncertainty in the measurement of a temperature around the silver point with a calibrated thermocouple is 0.37°C.

#### 4.1.2. Lossy Termination Materials

The approximate attenuation per unit length of three materials was measured at 55.8 GHz. These measurements were performed to assure that the load material chosen (60% BeO-40% Si) for the high temperature termination

(SS 3.1.1.) would have adequate loss prior to its being fabricated, and to obtain some feeling for the loss characteristics of other load materials. The results were:

| Silicon Carbide:   | 96 dB/inch  |
|--------------------|-------------|
| Polyiron:          | 69 dB/inch  |
| High Loss Plastic: | 126 dB/inch |

The BeO-Si termination should therefore have a loss of approximately 40% of a similar Silicon Carbide load, or approximately 92 dB/inch.

## 4.1.3. Reflection Coefficient

# of the Termination and Waveguide

Three reflection coefficient measurements of the BeO-Si terminations (SS 3.1.1.) were performed; two swept and one fixed frequency measurement of the termination by itself, and a swept frequency measurement of the termination-hightemperature waveguide combination. The output traces of the three swept measurements are shown in figures 4.1, 4.2, and 4.3. The first figure shows a conventional swept measurement [8] where the labels for the return loss calibration lines appear at the left. The top set of lines contains a calibration line and two lines made by commercial terminations. The second set shows a calibration line and a line made by another commercial termination. The bottom set contains four calibration lines and a line made by the BeO-Si termination.

Figure 4.2 shows a Holloway-Somlo (H-S) swept reflectometer measurement [8] of the BeO-Si terminations using two calibrating reflections whose coefficients are 0.024 and 0.001 (at most) respectively. The top trace is a frequency calibration trace. The next set of traces consists of the 0.024 reflection and the BeO-Si termination which is seen, by comparing the vertical magnitude of the lines, to have a reflection coefficient of 0.006 or less. The third set shows the BeO-Si termination compared to the 0.001 termination. Comparison of these magnitudes shows the BeO-Si reflection coefficient to be about 0.008. The bottom trace is from the BeO-Si termination again, shifted slightly in the H-S reflectometer input waveguide lead.

The two sets of traces in figure 4.3 show the BeO-Si termination-high temperature waveguide combination compared to a 0.024 reflection, and to a 0.048 reflection in the H-S reflectometer. These traces indicate that the combination has a reflection coefficient of approximately 0.012 (c.f. aps G and H).

The reflection coefficient of three BeO-Si terminations were measured in a tuned reflectometer [8] at 59.4 GHz. The results, including measurement uncertainties, show that the reflection coefficients of all three terminations fall in the range from 0.002 to 0.006.

## 4.1.4. High-Temperature Waveguide Loss

The attenuation per unit length of the high-temperature waveguide (SS 3.1.2) was measured [9] at 59.4 GHz and 22°C. The average result of five measurements shows this loss to be 0.023 dB/inch with an uncertainty no greater than 20%.

# 4.1.5. Thermocouple Insertion Distance

The thermocouple used in the temperature distribution measurement of the high-temperature waveguide is inserted by holding the thermocouple stationary and moving the oven along the support rail by rotating the plastic wheels of the oven carriage. If need be, the oven can be positioned to within a few tenths of 0.001" by this technique. A typical measurement setup is shown in figure 4.4. The thermocouple is being inserted into the waveguide from the left. Once the zero distance setting is established by positioning the point of contact between the thermocouple bead and the waveguide at the flange reference plane, the apparent insertion distance of the thermocouple into the waveguide can be measured by the steel scale on the rail or the dial indicator secured to the rail at the right in the picture. By setting the pointer attached to the oven carriage to a given mark on the scale, the apparent insertion distance can be measured to an accuracy approximately 0.005". By using the dial indicator at the right, this distance accuracy is approximately 0.002".

The actual insertion distance is obtained from the apparent distance by adding to the apparent distance a correction accounting for the expansion of the thermocouple rod upon heating as it is inserted into the waveguide. This correction is calculated (ap E) from knowledge of the distribution curve (fig. 2.5) and the expansion characteristics [10] of the  $Al_2O_3$  rod (fig. 4.5). The accuracy of this calculation is estimated to be 0.0005".

# 4.1.6. Inconel Heating Test

Before deciding to use inconel 601 for the heat distributor, a piece with nominal dimensions  $4 \ge 1 \ge 3/16$  inches was maintained at 1100°C for 34 hours. Before heating, one end of the piece was measured to be 0.197" and the other end to be 0.204" in thickness. After heating, the piece was remeasured and found to have the same dimensions to within the measurement accuracy (0.0005"), and was found to have no measurable warp caused by the heating.

Observation of the final heat distributor after many hours of use shows it not to have oxidized further than the initial oxidation acquired upon first heating.

### 4.1.7. Heating Coil Resistances

The heating coil resistances were measured at 22°C (room temperature) and 1000°C. At room temperature the coil resistances, front to back, are 3.3, 22, and 10 ohms respectively. When heated to 1000°C, these same coil resistances increased to 3.8, 24, and 11 ohms respectively.

These resistances appear not to have changed over 3 months intermittent usage (SS 4.1.7).

# 4.2. External Oven Components

# 4.2.1. Zirconium Oxide Insulation

A 3/4" cylinder of boron nitride was heated to  $1000^{\circ}$ C by a heating coil wrapped tightly around it. The combination was insulated by a 0.15" thick zirconium oxide felt wrapping, and suspended in air during heating. The temperature drop from the inside to the outside of the insulation was measured to be  $700^{\circ}$ C.

# 4.3. Auxiliary Components

# 4.3.1. Residual Thermal EMF

The residual EMF generated in the contacts of the terminal board, the thermocouple switch, and the potentiometer

(fig. 3.14) reduce the accuracy of the temperature measurements. This EMF was measured by tying together a pair of the copper leads in the ice bath and measuring the EMF appearing at the potentiometer. This EMF was less than 0.1 microvolt, corresponding to an error of 0.009°C at the Silver Point Temperature (961.93°C) where the high-temperature termination is maintained.

## 4.3.2. Copper Lead Resistance and Resulting Measurement Error

The resistance of the copper leads between the thermocouple leads in the ice junction and the measuring apparatus (fig. 3.14) was measured to be 1.5 ohms, or approximately 0.1 ohms per foot for the total length of 13'. The error in a temperature measurement caused by this resistance and a slight unbalance at the null detector is estimated (ap L) to be no greater than 0.002°C.

#### 4.3.3. Water Temperature Control and Measurement

The temperature of the water coolant entering the oven casing at the waveguide flange is held at approximately  $22^{\circ}$ C to  $\pm 0.05^{\circ}$ C. The estimated error in the measurement of this temperature by the manifold thermometer (SS 3.3.3, fig. 1.2) is  $\pm 2^{\circ}$ C.

# 4.4. System Performance

## 4.4.1. The Termination Temperature

The temperature of the high-temperature termination is determined by measuring the EMF of thermocouple  $S_1$  (SS 3.3.1). The error in this measurement is no greater than 3 microvolts or 0.27°C (SS 4.1.1) when operating near the Silver Point (fig. 3.13). A measurement of the temperature in the waveguide just in front of the termination, and under the waveguide just below the termination, revealed these temperatures to be the same as the termination temperature to within at most 0.1°C. Therefore the determination of the termination temperature by thermocouple  $S_1$  is uncertain to no greater than 0.4°C (0.27°C + 0.1°C).

#### 4.4.2. Determination of the Waveguide Temperature Distribution

The presence of the thermocouple rod inside the waveguide disturbs the waveguide temperature distribution at both ends and in the temperature transition region. Therefore, the normal (unperturbed) distribution cannot be measured directly in these regions. Instead, an area is located between two perturbed distributions in which the normal distribution must lie.

This area is established in the following way. If the high-temperature termination is removed from inside the waveguide, two perturbed temperature distributions can be measured (fig. 4.6); one by inserting the thermocouple into the waveguide from the back end of the oven, and one by inserting the thermocouple from the front. In the first measurement, heat is conducted by the thermocouple rod from the heat distributor region of the waveguide into the temperature transition region as the thermocouple enters this region, giving a higher than normal temperature indication. In the second measurement, as the thermocouple enters the transition region from the front, heat is conducted via the rod away from the transition region giving a lower indication than is normal. It is clear that the normal distribution must lie in an area somewhere between the two perturbed distributions. Since the predominant heat transfer in the transition region is along the waveguide, the distribution in this region should be nearly linear. This is seen to be the case from curves A and B in figure 4.7.

The area in which the normal distribution must lie can be reduced further, as shown by the following argument. The two perturbed distributions from figure 4.6 are expanded in

figure 4.7 in the transition region as curves A and B. In the water cooled region the normal curve is closer to curve B since the distribution is less perturbed in this region when measured from the front than when measured from the back of the oven. Similarly, the normal distribution is closer to curve A in the heat distributor region. Thus the normal distribution lies between the unlabeled curve (which is halfway between curves A and B in the water cooled and heat distributor regions) and curve B in the water cooled region, and between the unlabeled curve A in the heat distributor region. Then if the partial curves in the water cooled and heat distributor regions are joined linearly as shown in figure 4.7, it is clear that the normal curve will lie in the shaded area bordered by the resulting two curves.

The solid curve C which is vertically halfway between the bordering curves is then taken to be the normal distribution, and the correction temperature  $\Delta T$  (SS 2.1) is calculated from it. This correction temperature is -26.34°C in the figure. The uncertainty in this correction (SS 2.2),  $(\delta T)_g$ , is taken to be one-half of the difference between the correction temperatures as calculated from the bordering curves, since the normal curve cannot lie outside these curves. From the figure, this uncertainty is 0.92°C.

The foregoing procedure is valid provided that the curves A and B remain substantially unchanged when the termination is reinserted into the waveguide. This is seen to be the case in figure 4.8 which shows two distribution measurements from the front just before and after the termination was inserted.

The difference between curves A and B is plotted in figure 4.9 for the average coil temperature needed to maintain the termination at 962°C. This curve can be used to predict curve A around the transition region from curve B, obviating the need to remove the termination from the waveguide if it can be shown that the differential curve is relatively independent of the average coil temperature. That this is the case is seen in figure 4.10 which shows the three differential curves for three different average coil temperatures to be closely the same. The dates on which the differential curves were taken indicate the stability and repeatability of the oven characteristics.

#### 4.4.3. Temperature Measurement Repeatability

The ability to repeat a temperature measurement at a specified point in the waveguide is very important if one is to have confidence in the temperature distribution measurements. In order to do this in the temperature transition

region, one must be able to reposition the thermocouple in the waveguide (SS 4.1.5) quite accurately. For example, a 0.001" error in repositioning the thermocouple in the transition region causes a 1°C change in the temperature measurement.

In order to check the repeatability, a set of temperature measurements were performed at three points (0", 0.8", 1.3") in the waveguide. The table in figure 4.11 shows the results of these tests. The time in hours measured from the beginning of the first measurement along with the temperature-distance sensitivity around the various points are also given in the table. The results indicate that the measurement of a temperature at a given point in the waveguide, even in the highest gradient region of the temperature distribution, should be repeatable to 2°C. This result is consistent with the fact that the thermocouple can be repositioned to within 0.002" anywhere along the waveguide interior.

## 4.4.4. Wall Temperature Distributions

The temperature distributions along the four walls inside the waveguide differ from each other in the temperature transition region. Figure 4.12 shows this effect, where the difference between the temperature of each wall and the average temperature of the four walls is plotted as a function of distance into the waveguide from the output

flange. These differences are accurate to 2°C, showing that the wall temperatures are closely the same outside the 0.3" to 1.6" length of waveguide. The error caused by these different temperature distributions is discussed in SS 2.2 and ap C.

## 4.5. Additional Measurements

## 4.5.1. Oven Power Consumption

The power consumed by the oven when operating at 962°C was measured to be

| Front Coil  | 7.2 A x  | 30.7 V = | 221 Watts        |
|-------------|----------|----------|------------------|
| Center Coil | 2.1 A x  | 51.3 V = | 108 Watts        |
| Back Coil   | 3.85 A x | 44.8 V = | <u>172 Watts</u> |
|             |          | Total    | 501 Watts        |

By measuring the temperature rise  $(22^{\circ}C \rightarrow 30^{\circ}C)$  and flowrate (811 mL/min) of the oven casing coolant, the heat removed from the oven is calculated to be 453 Watts.

#### 4.5.2. Laboratory Environment

The temperature and relative humidity of the laboratory in which most of the measurements described in this report were carried out were 69°F and 40%, respectively. A recording of the variation of these quantities over a seven-day period appears in figure 4.13.

# 4.6. Possible Improvements

The following comments are recorded here for future use. They involve both suggestions for improvement of the present WR15 noise standard, and comments that may prove useful in later work.

## 4.6.1. Thermocouple Grooves

The thermocouple grooves in the inconel heat distributor were machined with a milling cutter, leaving a circular runout of the cutter radius at the end of the groove. This circular runout prevents the thermocouple from making repeatable contact when the thermocouple is removed and reinserted. The design of the groove for the front coil thermocouple also prevents this thermocouple from making repeatable contact with the front coil. This nonrepeatability prevents changing the control thermocouples without remeasuring the gradient to be sure it hasn't changed. This problem can be remedied by milling off the radius in grooves B and C (fig. 3.11 and drawing #3), and plugging the hole in groove F leaving a thin wall between the thermocouple bead and the front coil.

#### 4.6.2. Isolation Between Heating Coils

The ability to shape the temperature distribution down the waveguide depends on the amount of thermal isolation between the regions heated by the front, center, and back heating coils. In the present design of the heat distributor this isolation is not great enough to allow much control over the position of the high temperature fall off between the water cooled and heat distributor regions (fig. 2.5). For accuracy reasons (SS 2.3) it is beneficial to push this high-temperature fall-off to as close to the output flange as possible.

One possible means of effecting greater thermal isolation is to cut annular spaces between the front, center, and back coil regions.

# 4.6.3. Diameter of the Heat Distributor

The diameter of the heat distributor was chosen intuitively, the smoothing of heating irregularities along the central heating coil being the main factor in the choice. Time permitting, some experimentation may show that a smaller diameter is quite feasible.

# 4.6.4. Different Wall Temperature Distributions

By examining the wall temperature differential curves in figure 4.12, one is led to the conclusion that the different distributions are caused by varying contact between the waveguide and insulation in the transition region (fig. 2.5), and between the waveguide and heat distributor at the end of the heat distributor. At present this effect is not important, amounting to only 2.9% of the total error in the calculated output temperature (SS 2.2).

#### 5. ACKNOWLEDGMENTS

The success of this project is due in part to the efforts of the following people: R. D. Hunter, M. Kanda, A. C. Newell, M. P. Weidman, and B. C. Yates of the Electromagnetics Division for many V-band measurements and consultations; P. F. Biddle, W. F. Decker, R. J. Fischer, H. H. Garing, P. G. Karas, V. Lecinski, W. E. McNaney, K. C. Nuss, A. Padilla, and to D. L. Smith of the Shops Division; Sharon C. Foote of the Electromagnetics Division for the excellent job of typing; and to D. B. Miner of Audio Visual Aids.

Thanks are also due to Dave Sawyer for making up the conductivity tables.

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Figure 1.1. Output Noise Temperature Versus Operating Frequency.



Figure 1.2. Photograph of the WR15 Noise Standard Showing the Output Flange.



Figure 1.3. Photograph of the WR15 Noise Standard Showing Thermocouples and Ice Junctions.







Figure 2.2. Equivalent Circuit of a Thermal Noise Source.











Figure 2.5. Sample Temperature Distribution for Calculations.



Figure 2.6. The Effect of the Temperature Transition Region on the Output Error.


Figure 3.1. Block Diagram of the Standard's Operation.

|                               | Thermal Conducti  | vity ( $\sim 20^{\circ}$ C) | Coefficient of Linear Thermal Expansion |
|-------------------------------|-------------------|-----------------------------|---|
| Material                      | Cm <sup>o</sup> C | normalized<br>to Silver     | $10^{-0}/^{\circ}$ C nominally)         |
| Air                           | 0.00024           | $5.7 \times 10^{-5}$        |   |
| Aluminum                      | 2.2               | 0.52                        | 24                                      |
| Alumina                       | 0.29              | 0.069                       | 6° 7                                    |
| Beryllium Oxide               | 2.2               | 0.52                        | 6.4                                     |
| Boron Nitride (Parallel)      | 0.61              | 0.14                        | 0                                       |
| Boron Nitride (Perpendicular) | 0.40              | 0.095                       | 0                                       |
| Brass                         | 1.2               | 0.29                        | 20                                      |
| Carbon Steel                  | 0.45              | 0.11                        | 18                                      |
| Copper                        | 3°9               | 0.93                        | 16                                      |
| Glass                         | 0.0079            | 0.0019                      | 9                                       |
| Gold                          | 3. 0              | 0.71                        | 14                                      |
| Inconel                       | 0.15              | 0.036                       | 12                                      |
| Lead                          | 0.35              | 0.083                       | 29                                      |
| Nickel                        | 0.92              | 0.22                        | 13                                      |
| Platinum                      | 0.69              | 0.16                        | 8° 9                                    |
| 403 Stainless Steel           | 0.25              | 0.060                       | 6                                       |
| Silver                        | 4.2               | 1                           | 20                                      |
| Zirconium Oxide Felt          | 0.00079           | 0.00019                     | -                                       |

A Table of Thermal Conductivities and Thermal Expansion Coefficients. Figure 3.2.

| Material  | Melting Temperature<br>in <sup>O</sup> C | Electrical Resistivity (20 $^{\circ}$ C)<br>in $\mu \land - cm$ |
|-----------|--|---|
| Gold      | 1063                                     | 2.4   |
| Iridium   | 2454                                     | 7   |
| Osmium    | 2700                                     | 60  |
| Palladium | 1549                                     | 11  |
| Platinum  | 1773                                     | 10  |
| Rhodium   | 1966                                     | 5   |
| Silver    | 961                                      | 1.6   |

Figure 3.3. Table of Some Properties of Some of the Noble Metals.



Figure 3.4. Atmospheric Attenuation Versus Frequency (Courtesy Microwave Journal).





Figure 3.6. Exploded View of the Boron Nitride Heat Distributor.



Figure 3.7. Photograph of the Assembled Boron Nitride Heat Distributor.







Figure 3.10. Thermal Conductivity Versus Temperature for Zirconium Oxide.







Figure 3.12. Thermal EMF Versus Temperature for Ft-Rh and Platinel Thermocouples.

U.S. DEPARTMENT OF COMMERCE NATIONAL BUREAU OF STANDARDS WASHINGTON 25, D.C.

## REPORT OF CALIBRATION

PLATINUM vs. PLATINUM-RHODIUM THERMOCOUPLE

Submitted by

National Bureau of Standards Division 272, Section 60

The emf of the thermocouple was determined at 1064.43 °C (gold point), 961.93 °C (silver point), 630.74 °C, and 419.58 °C (zinc point) with the reference junctions at 0 °C. The values of emf found are given in Table 1. The uncertainties in these values are estimated not to exceed 3 microvolts.

Table 2 gives the values of the coefficients A, B, and C in the equation

 $E = A + Bt + Ct^2$ ,

where E is the emf of the thermocouple in absolute microvolts and t is the temperature in degrees Celsius (IPTS-68). The equation may be used for interpolation in the range 630.74° to 1064.43 °C.

Table 3 gives values of emf from 0° to 1450 °C. The uncertainties in the values given are estimated not to exceed 5 microvolts in the range 0° to 1100 °C and then increase to not more than 30 microvolts at 1450 °C. These uncertainties are discussed in National Bureau of Standards Circular 590, Methods of Testing Thermocouples and Thermocouple Materials.

All temperatures in this report are given in degrees Celsius (IPTS-68). The International Practical Temperature Scale of 1968, IPTS-68, was adopted by the International Committee of Weights and Measures at its meeting in October, 1968, and is described in "The International Practical Temperature Scale of 1968," Metrologia, Vol. 5, No. 2, 35 (April 1969).

The calibration of a thermocouple is subject to change during use. The mangitude of the change depends upon such factors as the temperature, the length of time, and the conditions under which it is used. Factors

| Work Order N | No.: | 272-0242     |      |   |    |   |       |  |
|--------------|------|--------------|------|---|----|---|-------|--|
| Test No.     | :    | 3.1d/8432D   |      |   |    |   |       |  |
| Completed    | :    | June 3, 1971 | Page | 1 | of | 2 | pages |  |

Figure 3.13. Sample Page from a Thermocouple Calibration Report.





Figure 3.15. The Heating Control System.



Figure 3.16. The Control Thermocouple Hookup.











Termination Reflection Coefficient.







Figure 4.4. A Typical Temperature Distribution Measurement Set-up.









Figure 4.7. Temperature Distribution, Expanded Scale.



Figure 4.8. Distribution Just Before and After Termination is Inserted.



Figure 4.9. Temperature Differential Between Perturbed Distributions.



INCHES

Figure 4.10. Temperature Differential at Different Coil Temperatures.

| 0''                    | 0.8"                             | <u> </u>                         |
|------------------------|----------------------------------|----------------------------------|
| 22 <sup>°</sup> C/1:29 | 397 <sup>°</sup> C/1:34          | 828 <sup>°</sup> C/1:41          |
| 21 <sup>°</sup> C/1:50 | 395 <sup>°</sup> C/1:57          | 828 <sup>°</sup> C/2:03          |
| 21°C/2:07              | 396 <sup>°</sup> C/2:14          | 828 <sup>°</sup> C/2:19          |
| 21 <sup>°</sup> C/2:25 | 396 <sup>°</sup> C/2:36          | 828 <sup>°</sup> C/2:45          |
| 21 <sup>°</sup> C/3:52 | 396 <sup>°</sup> C/3 <b>:</b> 03 | 828 <sup>0</sup> C/3 <b>:</b> 13 |

## Distance in From Output Flange

## Figure 4.11. Table of Temperature Measurement Repeatability Tests.



Figure 4.12. Temperature Differential Curves Along the Four Inside Waveguide Walls.



Figure 4.13. The Laboratory Environment

| AD= 4.24485+1<br>A1= 3.48204-1<br>A2=-1.33800-1<br>A3= 3.22450-0 | 003<br>003<br>010<br>010    |                      |                            |                      |                                    |                      |                    |                      |            |
|--|-----------------------------|----------------------|----------------------------|----------------------|------------------------------------|----------------------|--------------------|----------------------|------------|
| F= 5.5000+0<br>C= 3.21575-0                                      | 001 A=<br>002 TP            | =1.4600-00           | 1 DA=1.00+<br>+302 L= 2    | 003 B=               | 7.4000-002                         | UB=1.00-0            | 103                |                      |            |
| AK1= 8.868-1   | 006 AF                      | R2= 1.324-           | 009 AR3=                   | 1.00020+00           | 'n                                 |                      |                    |                      |            |
| ×  | 1                           | ×                    | T                          | ×                    | T                                  | ×                    | Т                  | ×                    | I          |
| 0.00 9.621   | 00+002                      | 0.50                 | 9.6200+002                 | 1 • 0 0              | 9.5900+002                         | 1.50                 | 9.5100+U02         | 1.63                 | 9.4800+002 |
| 1.70 9.44  | 00+002                      | 1.60                 | 9.3800+002                 | 1.90                 | 9.3100+002                         | 2.00                 | 9.2200+002         | 2.10                 | 9.0800+002 |
| 2.20 8.901   | 00+002                      | 2.30                 | 8.6300+002                 | 2.40                 | 3.2400+002                         | 2.50                 | 7.6600+002         | 2. ol                | 6.9700+002 |
| 2.70 5.77  | 00+002                      | 2.80                 | 4.5000+002                 | 2.50                 | 3.3600+002                         | 3.00                 | 2.1500+002         | 3.10                 | 9.5000+001 |
| 3.20 6.20  | 00+001                      | 3.30                 |                            | 3.40                 | 4.5008+081                         | 3.50                 | 4.00000+001        | 0.00                 | 000+0000+0 |
| ATTEN= 6.795   | 3-001                       | DELT                 | A T=-2.6343+00             | 1                    |                                    |                      |                    |                      |            |
|  | ытм                         | 010                  | XCU                        | ЫR                   | 001                                | 000                  | DCd                | ŊΓ                   |            |
| INPUT DATA<br>UNCERTAINTY  | 4 • 00-001<br>3 • 4 2 - 001 | 1 5.00-0<br>1 7.24-0 | 01 0.00+000<br>02 0.00+000 | 1.00-001<br>2.34-002 | 0 * 0 0 + 0 0 0<br>0 * 0 0 + 0 0 0 | 2.50-001<br>0.00+000 | 00+00*0<br>00+00*0 | 2.40-002<br>6.37-001 |            |
| TOTAL UNCERT   | AINTY = 1                   | 1.07+000             |                            |                      |                                    |                      |                    |                      |            |

Sample Frintout of the Output & Error Calculations. Figure D. l.

| UVEN)      | 62 • Û    | 456.0     | 824.0       | 922.0   | 943.0   | 962.0    |  |
|------------|-----------|-----------|-------------|---------|---------|----------|--|
| SCALE INTO | U • 3 0 U | U • 7 0 U | 1.103       | 1 + 500 | 1.900   | 5 °5 J J |  |
| IT LON CN  | 52.4      | 336.0     | 766.0       | 908.0   | 944.0   | 362.0    |  |
| RENUE POS  | 0.02.0    | U • 600   | 1.000       | 1 - 400 | 1 • 800 | 5 - 000  |  |
| FROM REFE  | 45.0      | 215.0     | 0.7Eo       | 6.068   | 938.0   | 0.955 .U |  |
| RIBUTIONC  | J . 100   | J.500     | ы. 903<br>С | 1.300   | 1 * 700 | 2.500    |  |
| TURE UIST  | 40.0      | 95.0      | 577.0       | 863.1   | 331.0   | 951.0    |  |
| TEMPERA    | 0.000     | 0.400     | 0.800       | 1.200   | 1.600   | 2.000    |  |
| INPUT      |           |           |             |         |         |          |  |

DISTAN

|              | 1.511   | U.714     | 1.117          | 1.519  | 1.920 | 5.520     |
|--------------|---------|-----------|----------------|--------|-------|-----------|
|              | 0.300   | 0.700     | 1.100          | 1.500  | 1.900 | 3.500     |
|              | 0.207   | 0.013     | 1. <b>J</b> 16 | 1.419  | 1.820 | 3.02U     |
| ~            | 0.200   | 0.600     | 1 - 00 t       | 1.406  | 1.800 | 3 • 00 4  |
| LE LANUE LE  | 0.104   | 8.513     | 0.315          | 1.310  | 1.723 | 2.520     |
| JU UUP LE UJ | 0.100   | U . 5 0 0 | 0.900          | 1.5.10 | 1.700 | 2.500     |
| U. IHTKAC    | 0 0 0 U | 0.412     | 0.015          | 1.217  | 1.619 | 2.020     |
| ANCE IN V    | 0.000   | 0 * 4 0 0 | 0.800          | 1.200  | 1.600 | 2 • 0 0 0 |
| 2            |         |           |                |        |       |           |

Figure E.1. Sample Output from Program "TEX 998."









Figure L. 1. Schematic for Lead Error Calculation,








Figure M. 3. Circuit Diagram for Block IV.



Figure M.4. Circuit Diagram for Block VI.



Figure N.1. Generator attached to a Two-Port Transducer.



Figure N.2. Scattering Parameter Description.



Figure N.3. A Noisy Two-Port.



Figure N.4. Illustration for (N.1).



Figure N.5. A Thermal Noise Source.



Figure N.6. A Uniform, Reflectionless Line.

# 8. DRAWINGS

- 1. Oven Assembly
- 2. High Temperature Resistive Termination
- 3. Oven Details (Iconel Heat Distributor)











## Appendix A -- The Output Equation

The output equation for the noise temperature of a noise power standard is (ap N)

$$T = T_{m} + \Delta T$$
 (A.1)

where  $T_m$  is the termination temperature,

$$\Delta T = (T_0 - T_m) (1 - \alpha_0) + \int_0^k T'_x (1 - \alpha_x) dx$$
 (A.2)

$$\alpha_{\rm X} = 10^{-A_{\rm X}/10} - \frac{2|\Gamma_{\ell}|^2}{1 - |\Gamma_{\ell}|^2} \operatorname{Sinh}(A_{\rm X}/10 \, \log \, e)$$
(A.3)

and

$$A_{x} = \int_{x}^{\ell} a_{z} dz.$$
 (A.4)

Referring to figure 2.2,

 $T_x$  = the temperature at point x on the transmission line (e.g.  $T_0 \equiv T_{x=0}$ )

$$T_x$$
 = the derivative of  $T_x$  with respect to x at point x

- $\alpha_{x}$  = the available power ratio from point x on the line to the end of the line at x =  $\ell$
- $A_{X}$  = the attenuation in decibels of the line from x to  $x = \ell$
- $\Gamma_{l}$  = the reflection coefficient of the termination and transmission-line.

The scattering matrix for the length of line from x to x = l is

$$S_{x} = \begin{pmatrix} 0 & S_{12} \\ S_{21} & 0 \end{pmatrix}$$

giving an attenuation [11] for this length of line equal to (ap N)

$$A_x \equiv -10 \log |S_{21}|^2 = \int_x^{\ell} a_z dz.$$
 (A.5)

For a uniform transmission line with little loss, a<sub>z</sub> can be approximated by

$$a_{z} = c \rho_{z}^{\frac{1}{2}}$$
 (A.6)

where c is a constant dependent upon the frequency, f, and the transmission line geometry.  $\rho_z$  is the line resistivity. For a rectangular waveguide [2]

$$a_{z} = \frac{C_{1}(f^{2} + C_{2})}{f^{\frac{1}{2}}(f^{2} - C_{3})^{\frac{1}{2}}}$$
(A.7)

where

$$C_{1} \equiv \frac{20 \cdot \pi^{\frac{1}{2}} \log e}{bC\mu_{0}^{\frac{1}{2}}},$$

$$C_{2} \equiv \frac{bC^{2}}{2a^{3}},$$

$$C_{3} \equiv \frac{C^{2}}{4a^{2}},$$

$$C \equiv 2.99792 \times 10^8 \text{ meter/sec,}$$
$$\mu_0 \equiv 4\pi \times 10^{-7} \text{ henry/meter,}$$

and

 $\log e = 0.434294.$ 

With the frequency expressed in gigahertz,  $\rho$  in microhm centimeters, a and b in inches, and a in decibel per inch,

$$C_{1} = \frac{1.44865 \times 10^{-4}}{b}$$

$$C_{2} = \frac{69.6533 \ b}{a^{3}}$$

$$C_{3} = \frac{34.8266}{a^{2}}.$$

The second term in (A.3) shows that the noise temperature of the standard is dependent upon the standard's reflection coefficient. The error in  $\Delta T$  caused by dropping this term can be estimated from

$$\delta \Delta T \sim 2 \left( \overline{T} - T_{m} \right) | \Gamma_{\ell} |^{2} 0.23 \Delta \qquad (A.8)$$

where  $\overline{T}$  is the average temperature of the transition region of the waveguide temperature gradient, and  $\Delta$  is the average decibel attenuation over this same region. Using the resistivity curve given in figure 2.3 and temperature curve C in figure 4.7 to calculate  $\Delta$  results in

$$\delta \Delta T < 0.01 \text{ K}.$$

A maximum value of 0.01 (SS 4.1.3) has been chosen for the reflection coefficient of the line and termination. Therefore for the WR15 standard, the second term in (A.3) can be dropped with negligible error.

#### Appendix B -- Quantum Correction

As the ratio hf/kT becomes significant, (A.1) should be replaced by

$$kT = W(T_{m}, f) + [W(T_{0}, f) - W(T_{m}, f)](1 - \alpha_{0})$$
$$+ \int_{0}^{k} W'(T_{x}, f)(1 - \alpha_{x}) dx \qquad (B.1)$$

where

$$W(T,f) \equiv \frac{hf}{e^{2u} - 1}$$

and

$$u \equiv \frac{hf}{2kT}$$
.

Here, h is Planck's Constant, k is Boltzmann's Constant, f is the frequency, and T is the absolute temperature. The significance of this correction can be determined by expanding (B.1) to second order in u and comparing the result to (A.1).

$$T \doteq T_{m}(1-u_{m}+u_{m}^{2}/3) + (T_{0}-T_{m})(1-\alpha_{0})(1-u_{0}u_{m}/3) + \int_{0}^{\ell} T_{x}'(1-u_{x}^{2}/3)(1-\alpha_{x})dx.$$
(B.2)

For  $T_m$  equal to 1200 K in the 55 to 65 GHz frequency range, the second order terms in (B.2) are found to be quite negligible. The linear term  $T_m u_m$  is found to be 1.6 K at 65 GHz and is independent of the absolute temperature of the thermal noise source. The manner in which this linear term is treated depends on the application to which the standard is put. For example, in the comparison of noise sources this term drops out, but the correction must be considered when making a highly accurate noise factor measurement.

# Appendix C -- Error Calculation

The maximum error  $\delta T$  in the calculated output (SS 2.1) T of the noise standard can be obtained from (A.1) and expressed as

$$\delta T = \delta T_{m} + \delta \Delta T$$
  
=  $(\delta T)_{T_{m}} + (\delta T)_{T_{o}} + (\delta T)_{o} + (\delta T)_{l}$   
+  $(\delta T)_{\rho} + (\delta T)_{c} + (\delta T)_{g} + (\delta T)_{1} + (\delta T)_{w} + (\delta T)_{a}$  (C.1)

where the terms correspond to uncertainties in T caused by uncertainties in  $T_m$ ,  $T_o$ , the location of x = 0, the location of  $x = \ell$ ,  $\rho$ , c,  $T_x^{'}$ , neglecting second term in (A.3) (SS. 2.2), differing wall distributions (SS 4.4.4), and air attenuation (SS 2.2) respectively. These terms are calculated from (see ap A for definitions)

$$(\delta T)_{T_m} = (1 - \alpha_0) \delta T_m$$
(C.2)

$$(\delta T)_{T_o} = (1 - \alpha_o) \delta T_o$$
(C.3)

$$(\delta T)_{o} = |0.23 \ c\alpha_{o}(T_{o} - T_{m})\rho_{o}^{\frac{1}{2}} + (1 - \alpha_{o})T_{o}'| \ \delta(x=0)$$
 (C.4)

$$(\delta T)_{\ell} = 0.23 c \rho_{\ell}^{\frac{1}{2}} |T_{\ell} - T_{m} - \Delta T| \delta (x = \ell)$$
 (C.5)

$$(\delta T)_{\rho} = 0.23 |\alpha_{0}(T_{0} - T_{m})A_{0} + \int_{0}^{k} \alpha_{x}A_{x}dx| \frac{\delta \rho^{\frac{1}{2}}}{\rho^{\frac{1}{2}}}$$
 (C.6)

$$(\delta T)_{c} = 0.23 | (T_{o} - T_{m}) A_{o} \alpha_{o} + \int_{0}^{k} T_{x} A_{x} \alpha_{x} dx | \frac{\delta c}{c}$$
(C.7)

$$\frac{\delta c}{c} = \left| \frac{3C_2}{f^2 + C_2} + \frac{C_3}{f^2 - C_3} \right| \frac{\delta a}{a} + \left| 1 - \frac{C_2}{f^2 + C_2} \right| \frac{\delta b}{b} + \left| \frac{2f^2}{f^2 + C_2} - \frac{f^2}{f^2 - C_3} - \frac{1}{2} \right| \frac{\delta f}{f}$$
(C.8)

and

$$(\delta T)_{g} = \int_{0}^{k} (1 - \alpha_{x}) (\delta T_{x}') dx. \qquad (C.9)$$

In the WR15 standard the output flange is taken as the reference position, making  $\delta(x=\ell)$  and  $(\delta T)_0$  vanish.

The last term, (C.9), can be treated by one of two methods. The gradient uncertainty  $\delta T'_x$  can be broken down into its two separate components  $\Delta t$  and  $\Delta x$  with each handled separately; or it can be estimated by calculating the output T for each of the possible gradients allowed by the temperature measurement uncertainties and taking one-half the resulting range in T as the uncertainty. The first method is the more convenient but places a much larger upper bound on  $\delta T$ than the second method. The second method is used in the present case.

 $(\delta T)_W$  is obtained from the four temperature distributions used to generate figure 4.12 (SS 4.4.4). One-half the range in the four resulting T's calculated from these four distributions is 0.29 K. The distribution giving

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 $T_x$  closest (0.07 K off) to the center of this range was the right-wall distribution (fig. 4.12). Therefore, with the right-wall distribution being used as the waveguide temperature distribution, the uncertainty incurred is no greater than 0.36 K (0.29 + 0.07 K).

Appendix D -- Computer Calculation of  $\Delta T$  and  $\delta \Delta T$ 

The computer program written to calculate  $\Delta T$  and  $\delta \Delta T$ (SS 2.1 and 2.2) is called "Delta T," a printout of which is shown in figure D.1. The input data fed into the computer consists of:

- 1. The coefficients (A0, ..., A3) of the least squares fit to the curve of  $\rho^{\frac{1}{2}}$  as a function of centigrade temperature;
- 2. the frequency F in gigahertz;
- the broad and narrow waveguide dimensions A and B, and their corresponding uncertainties DA and DB;
- 4. the termination temperature T<sub>m</sub> in centigrade;
- 5. the coefficients (AR1, ..., AR3) for the waveguide expansion as a function of centigrade temperature according to the law [4]

 $\ell = \ell_0 (1 + AR1 * t + AR2 * t^2) / AR3;$ 

- 6. the temperature distribution (x,T) along the right wall of the waveguide with x = 0 at the termination;
- 7. the input uncertainties DTM, DTO, DDX, DR, DDT, DDO, DDB, and DC, corresponding to the uncertainties in the termination temperature, the temperature of the waveguide at the termination, the length difference measurements, the square root of the resistivity, the temperature difference measurements, the position of x = 0 and  $x = \ell$ , and the c constant.

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The computer processes this data to an accuracy of 0.1% in the calculation of T.

The output results consist of:

- 1. the c constant;
- 2. the value of L showing how many times the computer must subdivide the temperature distribution data (x,T) to achieve the 0.1% calculational accuracy;
- 3. an approximate value ( $\sim$  10%) for the total decibel attenuation of the waveguide:
- 4.  $\Delta T$  in kelvins;
- the separate uncertainties in ∆T caused by DTM, ..., DC; and
- 6. the error in  $\Delta T$  which is the sum of the separate uncertainties appearing in 5.

The data under the DDX and DDT headings are zero since the uncertainty given by (C.9) is calculated by the second method discussed in ap C.

### Appendix E -- The Thermocouple Rod Expansion Program

As a thermocouple is inserted into the heated waveguide, the apparent distance the thermocouple bead enters the waveguide should be corrected for the expansion of the thermocouple rod. For any given temperature distribution, this correction can be calculated by program "TEX998" for the 99.8% alumina rods used in the thermocouples. Figure E.1 shows a sample output of the program using the distribution shown in figure 2.5. The lengths shown are measured in inches assuming the thermocouple to be inserted into the waveguide from the front of the oven.

# Appendix F -- Termination Formula

Figure F.1 shows a portion of the termination, where a and b are the broad and narrow dimensions. Given a, b, and the angles  $\alpha$  and  $\beta$ , the face angle  $\gamma$ , the cutting angle  $\delta$ , and the longitudinal face length  $\ell$  are given by:

$$\gamma = \cos^{-1}(\cos \alpha \cos \beta)$$
$$\delta = \tan^{-1}\left(\frac{\tan \beta}{\sin \alpha}\right)$$

and

$$\ell = \frac{a}{\tan \alpha} + \frac{b}{\tan \beta}$$

For the WR15 termination with  $\alpha = 24^{\circ}$  and  $\beta = 10^{\circ}$ ,

 $\gamma = 25.9^{\circ}$  $\delta = 23.4^{\circ}$ 

and

& = 0.75''.

#### Appendix G -- The Minimum Termination Length

The minimum length of the termination is determined by two factors: 1) the amount of taper needed to produce a low VSWR; and 2) the amount of material needed to completely terminate the waveguide. Experience has shown that an effective taper geometry that produces a low VSWR and good thermal contact between the termination and the waveguide is achieved by the model shown in figure F.1 for small values of  $\alpha$  and  $\beta$ . The length required to effect the first factor was determined in ap F. The length required for the second factor and the radiation length (the length of material behind the taper from which most of the thermal radiation leaving the termination originates) are determined in this appendix.

### Terminating Length

An estimate of the length of material behind the taper that is required to completely terminate the waveguide can be made in the following way. Consider a length  $\ell$  of material which is characterized by a scattering matrix S, and which is heated to a uniform temperature  $T_m$ . The reflection coefficient of the material is given by

$$\Gamma = S_{11} + \frac{S_{12}S_{21}\Gamma_{L}}{1 - S_{22}\Gamma_{L}}$$

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where  $\Gamma_{\rm L}$  is the reflection coefficient behind the material. If the length is great enough, the power delivered (in units of kB)  $P_{\rm d}$  into a matched load by the material is

$$P_{d} = T_{m}(1 - |\Gamma|^{2}).$$

If  $\Gamma_{\rm L}$  changes to  $\Gamma_{\rm L}'$ , then  $\Gamma$  changes by an amount

$$\delta \Gamma = \frac{S_{12}S_{21}(\Gamma_{L} - \Gamma_{L})}{(1 - S_{22}\Gamma_{L})(1 - S_{22}\Gamma_{L})}$$

and P<sub>d</sub> by an amount

$$\delta P_d = T_m \delta |\Gamma|^2 \leq T_m |\delta \Gamma|^2.$$

The largest change in  $\Gamma$  is obtained from  $\Gamma'_L = 0$  and  $\Gamma_L = e^{i\theta}$ , giving

$$|\delta\Gamma|_{\text{max}}^2 = \frac{|S_{12}S_{21}|^2}{1 - |S_{22}|^2}$$

and

$$\delta T_{\max} \equiv (\delta P_d)_{\max} = \frac{T_m |S_{12}S_{21}|^2}{1 - |S_{22}|^2}.$$

In the present case

$$|S_{12}|^2 = |S_{21}|^2 = 10^{-a\ell/10}$$

where a is the decibel attenuation per unit length of the material. Then

$$\delta T_{\text{max}} = \frac{T_{\text{m}} \ 10^{-2a\ell/10}}{1 - |S_{22}|^2}.$$
 (G.1)

Or to achieve a change of  $\delta T_{max}$  or less

$$\ell \geq \frac{5}{a} \log \left( \frac{T_{\rm m}}{(1 - |S_{22}|^2) \delta T_{\rm max}} \right).$$
 (G.2)

For a = 92 dB/inch (SS 3.1.1),  $|S_{22}| = 0.5$ ,  $T_m = 1200$  K, and  $\delta T_{max} = 0.01$  K;  $\ell \ge 0.28$ ". That is, if the termination (minus taper) is greater than 0.28" in length, then a maximum VSWR change behind the termination can cause no greater than 0.01 K change in the noise power delivered by the termination to the waveguide.

#### Radiation Length

A termination of infinite length with a temperature distribution  $T_x$  has a noise temperature T given by

$$\Gamma = \int_{0}^{\infty} T_{x}(0.23 \ a_{x} dx) 10^{-A_{x}/10}$$
(G.3)

where  $a_x$  is the decibel attenuation per unit length of the termination material, and  $A_x$  is the decibel attenuation of the material from x = 0 to x.

$$A_{X} \equiv \int_{0}^{X} a_{Z} dz$$

Suppose that only the taper and the first  $\ell$  inches of the termination could be maintained at a uniform temperature  $T_m$ . Then

$$T = 0.23 T_{m} \int_{0}^{\ell} a_{x} 10^{-A_{x}/10} + 0.23 \int_{\ell}^{\infty} T_{x} a_{x} 10^{-A_{x}/10} dx.$$
(G.4)

The length l can be increased to the point where the second term in (G.4) is negligible. Taking  $T_x \doteq T_o$ , and  $a_x \doteq a$ , the ratio R of the second to first term in (G.4) becomes

$$R = \frac{T_0 \ 10^{-a\ell/10}}{T_m (1 - 10^{-a\ell/10})}.$$
 (G.5)

This ratio is insignificant if  $\ell$  is greater than some radiation length  $\ell_{\rm R}$  given by

$$\ell \geq \ell_{\rm R} \equiv \frac{10}{a} \log \left( \frac{1 + T_{\rm m} {\rm R}/{\rm T}_{\rm o}}{T_{\rm m} {\rm R}/{\rm T}_{\rm o}} \right). \tag{G.6}$$

For a = 92 dB/inch,  $T_m = 1200$  K,  $T_o = 300$  K, and R = 0.01/1200;  $\lambda_R \doteq 0.2$ ".

## Appendix H -- Waveguide Reflections

#### Broad and Narrow Dimensions

A rectangular waveguide whose broad and narrow dimensions are in error by  $\delta a$  and  $\delta b$  respectively will produce a reflection coefficient (with respect to a perfect waveguide of dimensions a and b) whose magnitude is given by [12]

$$\Delta \Gamma = \left(\frac{\lambda_g}{\lambda_c}\right)^2 \frac{\delta a}{2a} + \frac{2\sigma}{(1+\sigma)^2} \frac{\delta b}{b}$$
(H.1)

where  $\lambda_g$  is the waveguide wavelength,  $\lambda_c$  is the cutoff wavelength, and  $\sigma$  is the VSWR corresponding to  $\Gamma$ . For WR15 ( $\lambda_c = 0.296$ ") at 55 GHz ( $\lambda_g = 0.3115$ ") and a small reflection ( $\sigma \doteq 1$ ),

$$\Delta \Gamma = 3.7 \, \delta a + 6.8 \, \delta b$$
. (H.2)  
For  $\delta a = \delta b = 0.001''$ ,  $\Delta \Gamma = 0.010$ .

## Corner Bend Radii

Non-vanishing corner bend radii inside an otherwise perfect rectangular waveguide will cause a reflection whose magnitude is given by [13]

$$\Delta \Gamma = \left(\frac{\lambda_g R}{a}\right)^2 \left(\frac{4 - \pi}{8 ab}\right)$$
(H.3)

where R is the radius of the corner bend.

For WR15 waveguide at 55 GHz with R =  $0.006^{"}$ ,  $\Delta\Gamma$  = 0.002.

### Appendix I -- Atmospheric Attenuation

The maximum change in the output noise temperature of the standard  $\delta T$  due to the attenuation by the column of air in the waveguide between the termination and the output flange can be approximated by

$$\delta T = (T_{a} - T_{m})(1 - \alpha)$$
 (I.1)

where  $T_a$  is the average temperature of the air column,  $T_m$ is the termination temperature, and  $\alpha$  is the average attenuation of the column. With  $T_a$  = 300 K,  $T_m$  = 1200 K, and  $\alpha$  = 0.00025 dB/inch (60 GHz in figure 3.4);  $\Delta T$  = 0.05 K.

# Appendix J -- Support Spider

The inconel sleeve (drawings 1 and 3) is suspended inside the oven by a support spider (which is kept near room temperature by the end plate) on each end plate. The spider is so designed that as the sleeve expands on heating its center line remains fixed. This is accomplished by choosing the angle for the support spider shown in figure J.1 so that as the sleeve length  $\ell$  and diameter D increase, the sleeve ends climb smoothly up the support spider. It is apparent from the figure that the proper angle  $\theta$  is given by

$$\tan \theta = \frac{\delta D/2}{\delta \ell/2}.$$
 (J.1)

Since D and & expand on heating by the same factor, (J.1) reduces to

$$\tan \theta = \frac{D}{l}.$$
 (J.2)

For  $\ell = 7.75''$  and D = 3.25'';  $\theta = 22.75^{\circ}$ .

# Appendix K -- Thermocouple Rod Expansion

The expansion of the thermocouple rod upon heating can be described in terms of a linear coefficient of expansion  $\varepsilon$ ;

$$d\ell = dx + \epsilon \cdot \Delta t \cdot dx$$
 (K.1)

where dx and dl are elemental lengths of the rod before and after heating respectively, and  $\Delta t$  is the corresponding temperature change. The length of the entire rod is the sum of these elemental lengths. Thus,

$$\ell = \int_{0}^{\ell_{0}} d\ell = \ell_{0} + \int_{0}^{\ell_{0}} \epsilon \cdot \Delta t \cdot dx \qquad (K.2)$$

where  $l_{o}$  is the length of the unheated rod.

The following table [10] gives  $\varepsilon$  in 10<sup>-6</sup>/degree C for a 99.8% Al<sub>2</sub>O<sub>3</sub> rod:

| Temperature Change |        | $\epsilon$ in 10 <sup>-6</sup> /degree C |
|--------------------|--------|--|
| -200 to            | 25°C   | 3.4                                      |
| 25 to              | 200°C  | 6.7                                      |
| 25 to              | 500°C  | 7.3                                      |
| 25 to              | 800°C  | 7.8                                      |
| 25 to              | 1000°C | 8.0                                      |
| 25 to              | 1200°C | 8.3                                      |

The coefficients of a least-square curve fitting the product  $\varepsilon$  ·  $\Delta t$  over the 0 to 1000°C temperature range are given in the next table:

| <sup>a</sup> 0 | -1.58 | Х | 10 <sup>4</sup>   |
|----------------|-------|---|-------------------|
| <sup>a</sup> 1 | 6.28  | х | 10 <sup>-6</sup>  |
| <sup>a</sup> 2 | 1.72  | х | 10 <sup>-9</sup>  |
| <sup>a</sup> 3 | 9.27  | х | 10 <sup>-13</sup> |
| a <sub>4</sub> | -9.72 | х | 10 <sup>-16</sup> |

where now

$$\ell = \ell_0 + \int_0^{\ell_0} \alpha_x dx \qquad (K.3)$$

and

$$\alpha_{X} \equiv \alpha(t_{X}) = \sum_{n=0}^{4} a_{n} t_{X}^{n}. \qquad (K.4)$$

## Appendix L -- Lead Resistance Error

The copper leads from the thermocouples (fig. L.1) to the terminal board have a resistance r. In reading the thermocouple emf an error E will be caused by this resistance if an imperfect null (e + 1  $\mu$ V) is obtained on the potentiometer. Neglecting the small resistance of the thermocouple itself, the current caused by this imperfect null is

$$i = \frac{1 \ \mu V}{2r + R} \tag{L.1}$$

where R is the balancing resistance of the potentiometer. The corresponding error is

$$E = 2ri = \frac{2r/R}{1 + 2r/R}$$
 (L.2)

When balancing at the silver point temperature with a platinum-rhodium thermocouple (9.127 mV), R turns out to be 170  $\Omega$ . The lead resistance is (SS 4.3.2) 1.5 ohms. Therefore E is 0.017  $\mu$ V which corresponds to an error of 0.002°C at the silver point temperature.

# Appendix M -- Oven Temperature Control

#### General Description

The operation of the control system can be understood from figure M.1 and the block summaries given below.

- I. The output of the reference voltage source is a variable DC voltage adjustable from zero to 50 mV.
- II. The block II output is the algebraic sum of the reference source and the thermocouple voltage. This sum is zero under normal operating conditions.
- III. The DC amplifier amplifies any deviation from zero of the block II output (a calibrated meter indicates magnitude and polarity).
  - IV. The DC to duty cycle converter changes the fluctuating DC (error signal) to a square wave of fluctuating duty cycle. The converter output is waveform A of figure M.2.
  - V. Waveform A (fig. M.2) together with waveform B, a waveform of fixed duty cycle, is presented to an "and" gate to produce waveform AB (fig. M.2). The width of the positive-going portion of AB determines the position of the current transformer, which in turn, determines the amount of current

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delivered to the heating coil. The temperature control servo loop is closed through the heat conduction path from the heater coil to the thermocouple.

#### DC to Duty Cycle Converter

The output of emitter follower 04 (fig. M.3) is the amplified sum of the DC input of Ol from the DC amplifier. and the sawtooth input of 03. This 04 output is a sawtooth waveform that translates vertically with changes in temperature (changes in the DC amplifier output). Q8 and Q9 form a bistable circuit with the Q8 emitter voltage fixed by zener diode Z. When the output of O4 is greater than the emitter voltage of 08, 08 and 09 switch off. 08 and 09 switch on again when the 04 emitter voltage drops sufficiently below the 08 emitter reference. As seen in figure M.3 the negativegoing transition of the Q9 collector always coincides with the negative-going transition of the free-running sawtooth waveform. The positive-going transition of the Q9 collector occurs when the Q4 output becomes greater than the Q8 fixed emitter voltage. This circuit configuration results in an output square wave which has a duty cycle determined by the DC level from the DC amplifier. This variable-duty-cycle square wave is waveform A of figure M.2. The frequency of this square wave is determined by the free-running sawtooth generator and is not critical.

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### Current Transformer Servo

Q1 of figure M.4 receives a variable-duty-cycle square wave signal from the "and" gate. This signal is inverted at the collector of Ql which is connected via Dl to a "oneshot" formed by Q2 and Q3. The incoming signal triggers the "one-shot," and the collector of Q2 goes positive for a time determined by the RC time constant of R3 Cl, together with the position of pot R4. R4 is mechanically connected to the transformer shaft. Therefore the rotational position of the transformer shaft determines the width of the "one-shot" output pulse. This pulse is compared to the width of the incoming signal, and any difference in width results in an error signal at the base of Q4. The signal at the base of Q4 is a narrow positive or negative-going pulse depending on whether the Ql input is narrower or wider than the "one-shot" output. If the error signal is positive-going, it will cause Q5 to conduct, which in turn energizes the pulse stretcher Q6 together with C2 and R5. The pulse stretcher output signal is sufficient to drive the servomotor in one direction through Q7, Q8, Q9, and Q15. The same thing happens for an error of the opposite sense via Q10 through Q14 driving the motor in the opposite direction. The servomotor will continue to drive until R4 adjusts the

"one-shot" pulse width to equal that of the incoming signal. Q8 and Q13 are "nand" gates (inverting "and" gates) that are coupled so that both drive circuits (clockwise and counterclockwise) cannot be energized simultaneously.

# Appendix N -- Derivation of the Output Equation

## N.1. Introduction

A thermal noise source consists of a termination and a transmission line to convey the noise generated in the termination to an output port. The transmission line is lossy, so it both attenuates the termination noise and adds noise of its own to the output, and the line must be chosen in such a way that the output power can be accurately calculated.

The derivation begins in SS N.2 with a review of some two-port power relationships which are used in SS N.3 to find an expression for the noise output power of a lossy two-port. Finally, this output power equation is applied in SS N.4 to incremental segments of a transmission line to obtain the output noise power equation for the noise standard.

## N.2. Some Basic Two-Port Equations

The work to follow requires the use of some two-port power equations. These equations will be presented in this section in a form that is most useful to SS N.3 and SS N.4. Throughout this appendix a capital 'P' will stand for net or delivered average power and a small 'p' for available average power. It is to be understood that where the

parameters are frequency dependent, the bandwidth is narrow enough to insure that these parameters are essentially constant across it.

A passive, linear, two-port transducer is shown in figure N.1 with a generator attached to its input (first) port, and a load attached to its output (second) port. M and N are the mismatch factors of port one and port two respectively, and are defined in the following equations:

$$M \equiv P_1/P_1, \qquad N \equiv P_2/P_2,$$

where  $p_1$  is the average power available from the generator, and  $p_2$  is that portion of  $p_1$  available at port two of the junction.  $P_1$  is the net average power into port one from the generator and  $P_2$  is the net average power from port two. The ratio  $\alpha$  of available powers is defined by

$$\alpha \equiv p_2/p_1$$
.

The corresponding transducer efficiency n is

$$\eta \equiv P_2/P_1$$
.

The definitions for M, N,  $\alpha$ , and  $\eta$  can be combined to obtain the following relationship between these four quantities:

### $M\eta \equiv N\alpha$

Furthermore, by considering the definitions of  $\alpha$  and  $\eta$ , it can be seen that if the transducer is lossless, then both  $\alpha$  and  $\eta$  are unity.

These definitions are general because they apply to a transducer with any number of propagating modes. However, to have a workable expression for the noise power output calculation, one is restricted to a single propagating mode, in which case the transducer has an equivalent circuit like figure N.1. This circuit is shown in figure N.2 where scattering parameters [11] are used and where, in terms of these parameters, M, N,  $\alpha$ , and  $\eta$  take the following form [11,1]:

$$M = \frac{(1 - |\Gamma_{g}|^{2})(1 - |\Gamma_{1}|^{2})}{|1 - \Gamma_{g}\Gamma_{1}|^{2}}$$

$$N = \frac{(1 - |\Gamma_{L}|^{2})(1 - |\Gamma_{2}|^{2})}{|1 - \Gamma_{L}\Gamma_{2}|^{2}}$$

$$\alpha = \frac{(1 - |\Gamma_{g}|^{2})|S_{21}|^{2}}{(1 - |\Gamma_{2}|^{2})|1 - S_{11}\Gamma_{g}|^{2}}$$

$$\eta = \frac{(1 - |\Gamma_{L}|^{2})|S_{21}|^{2}}{(1 - |\Gamma_{1}|^{2})|1 - S_{22}\Gamma_{L}|^{2}}$$

The two-port scattering matrix is given by

$$S = \begin{pmatrix} S_{11} & S_{12} \\ S_{21} & S_{22} \end{pmatrix}.$$

The reflection coefficients of the generator, the input and output ports of the two-port, and the reflection coefficient of the load are denoted by  $\Gamma_{g}$ ,  $\Gamma_{1}$ ,  $\Gamma_{2}$ , and  $\Gamma_{L}$  respectively.

The input and output port reflection coefficients are related to the scattering matrix parameters and the terminal reflection coefficients through the equations [11]

$$\Gamma_{1} = S_{11} + \frac{S_{12}S_{21}\Gamma_{L}}{1 - S_{22}\Gamma_{L}},$$
  
$$\Gamma_{2} = S_{22} + \frac{S_{12}S_{21}\Gamma_{g}}{1 - S_{11}\Gamma_{g}}.$$

It can be seen from the equations for  $\alpha$ ,  $\eta$ ,  $\Gamma_1$ , and  $\Gamma_2$ , that  $\alpha$  is independent of the load reflection coefficient, and that  $\eta$  is independent of the generator reflection coefficient.

## N.3. Two-Port Noise

An expression for the average thermal noise power of a lossy two-port transducer is derived in this section. The expression to be obtained can be found in at least two other sources [14,15], so the short derivation given here is not intended to be new or unique. It is presented because it is an important logical step between SS N.2 and SS N.4 and because it will help familiarize the reader with the parameters just described.

A linear, passive, two-port transducer is shown in figure N.3, terminated at both ends. Both of these terminations and the two-port are thermally isolated from their

surroundings, and have come to a uniform absolute temperature T.  $P_1$  represents the average net power from the first termination, and  $P_2$  that from the second. The portion of  $P_1$ that emerges from port two is  $P_1\eta$ . P represents the noise power added to  $P_1\eta$  by the two-port itself, and is the quantity to be found. M and N are mismatch factors, and again a capital 'P' refers to delivered or net power while small 'p' refers to the available power. For example, if  $p_1$  and  $p_2$ denote the available powers from port one and port two terminations respectively, then the definitions in SS N.2 lead to

 $P_1 = Mp_1$  and  $P_2 = Np_2$ .

Since the entire circuit is thermally isolated from its surroundings, the temperature of the two-port and the terminations must remain equal even though there is a continual exchange of electromagnetic energy between them. This fact leads to the important conclusion that the average net powers leaving and entering port two must be equal,

 $P_1\eta + P = P_2$ . In terms of the available powers  $p_1$  and  $p_2$ ,  $P = Np_2 - Mp_1\eta$ .

Since both terminations are at the temperature T,

 $p_1 = p_2,$ 

where both  $p_1$  and  $p_2$  are equal to kTB in the low frequency approximation.

Therefore

$$P = NkTB(1-\alpha)$$

where the relationship

 $M_{\Pi} = N\alpha$ 

has been used to eliminate  $\eta$ . Representing the available power generated in the two-port by p,

$$p = P/N = kTB(1-\alpha)$$
. (N.1)

This equation is still general in the sense of the fourth paragraph of SS N.2, and is assumed to hold for all passive input and output terminations.

To illustrate the use of (N.1), consider figure N.4 and the total noise power available from port two that is generated in the two-port at temperature T, and the termination at temperature  $T_g$ . This total power consists of the attenuated power  $p_g \alpha$  available from the termination and the available two-port power p. By using (N.1) in place of p, the total available power is given by

$$p_g \alpha + p = kT_g B\alpha + kTB(1-\alpha)$$
.

The net amount of this power actually delivered to the right from port two is equal to N times the total available power, or

$$N(p_g \alpha + p) = NkT_g B\alpha + NkTB(1-\alpha).$$

## N.4. The Thermal Noise Source and Standard

In 1958, Sees [16] derived an expression for the average noise power output of a thermal source along the lines presented here, but without the benefit of the expressions found in SS N.3. Therefore, in this section those expressions will be applied to a lossy transmission line to find the contribution of the line to the total noise output of the source.

Figure N.5 shows a thermal noise source consisting of a termination at a temperature  $T_m$  that terminates a transmission line of length  $\ell$ .  $T_x$  is the temperature of the transmission line at point x along its length, and  $\alpha_x$  is the available power ratio of the section of line from <u>x</u> to  $\ell$ . Plots of  $T_x$  and  $\alpha_x$  as a function of position along the line are also shown in the figure.

For analysis the line is divided into many small segments, each of length  $\Delta x$ , where the particular segment at position x is shown in the figure, and (N.1) of the previous section is applied to each segment. Thus, the available power  $\Delta p_x$ 

from the segment at x is equal to the average temperature  $T_{\rm X}$  of the segment times one minus the available power ratio  $\Delta\alpha_{\rm x}$  for the segment,

$$\Delta p_{\mathbf{X}} = k T_{\mathbf{X}} B (1 - \Delta \alpha_{\mathbf{X}}) .$$

Using

$$\alpha_{x-\Delta x/2} = \Delta \alpha_x \cdot \alpha_{x+\Delta x/2}$$

leads to

$$\Delta p_{x} = kT_{x}B\left(\frac{\alpha_{x+\Delta x/2} - \alpha_{x-\Delta x/2}}{\alpha_{x+\Delta x/2}}\right).$$

For small segments

$$\alpha'_{x} \equiv \frac{d\alpha_{x}}{dx} = \frac{\alpha_{x+\Delta x/2} - \alpha_{x-\Delta x/2}}{\Delta x},$$

and  $\alpha_{x+\Delta x/2}$  can be replaced by  $\alpha_x$ . Therefore.

$$\Delta p_{\mathbf{x}} = \frac{\mathbf{k} \mathbf{T}_{\mathbf{x}} \mathbf{B} \alpha_{\mathbf{x}}^{\prime} \Delta \mathbf{x}}{\alpha_{\mathbf{x}}}.$$

The portion of this power that reaches the output port at  $x = \ell$  is

$$\alpha_{\mathbf{x}} \Delta \mathbf{p}_{\mathbf{x}} = \mathbf{k} \mathbf{T}_{\mathbf{x}} \mathbf{B} \alpha_{\mathbf{x}}^{\dagger} \Delta \mathbf{x}.$$

To get the total effect of the line, the effects due to each segment are added together:

$$\Sigma \alpha_{x} \Delta p_{x} = \Sigma k T_{x} B \alpha'_{x} \Delta x = k B \int_{0}^{\ell} T_{x} \alpha'_{x} dx.$$

The amount of termination noise available at the output is

Therefore the total available noise power output,  $kT_{tot}B$ , of the thermal source is given by the sum of these last two expressions and leads to a noise temperature  $T_{tot}$  given by

$$T_{tot} = T_m \alpha_0 + \int_0^{\ell} T_x \alpha'_x dx. \qquad (N.2)$$

Another form for this equation can be obtained from an integration by parts:

$$T_{tot} = T_m + \Delta T, \qquad (N.3)$$

where the correction temperature  $\Delta T$  is

$$\Delta T \equiv (T_o - T_m) (1 - \alpha_o) + \int_0^{\ell} T'_x (1 - \alpha_x) dx. \qquad (N.4)$$

The net power delivered across the output port corresponds to

$$MT_{tot} = M(T_m + \Delta T).$$

Equations (N.3) and (N.4) are valid for any number of simultaneously propagating modes. However, to have a workable expression for  $\alpha_x$  to be used in calculating the output of a noise standard it is necessary to select the transmission line and operating frequency so that only one mode is present. This means using a uniform, reflectionless line at a frequency below cutoff for all but the dominant mode. Figure N.6

illustrates such a condition, where now any portion of the line, for example the section from x to  $\ell$ , can be represented electrically by a two-port. The termination reflection coefficient is represented by  $\Gamma_g$ , the reflection coefficient looking from point x towards the termination by  $\Gamma_x$ , and the entire reflection coefficient of the thermal standard by  $\Gamma_{\ell}$ .  $\alpha_x$  is the available power ratio from x to  $\ell$ , and  $S_x$  is the corresponding scattering matrix.

From Kerns and Beatty [11, p.77],  $S_{\chi}$  for a uniform, reflectionless line is

$$S_{x} = \begin{pmatrix} 0 & e^{-\int_{x}^{\ell} \lambda_{y} dy} \\ e^{-\int_{x}^{\ell} \lambda_{y} dy} & 0 \end{pmatrix}$$

where  $\lambda_{y}$  is the propagation constant

 $\lambda_y = \varepsilon_y + i\beta$ 

and  $\varepsilon_y$  is real positive and determines the wave attenuation. For example, the attenuation in decibels of the line is 8.68  $\int_0^{\ell} \varepsilon_y dy$ . This attenuation constant depends on the resistivity (which in turn is a function of the line temperature) of the material making up the line. It can be measured [17] or, with care, calculated from a perturbation expansion [18,2]. Using these scattering parameters in the expression

for  $\alpha$  of SS N.2 leads to

$$\alpha_{\mathbf{x}} = \frac{\left(1 - |\Gamma_{\mathbf{x}}|^{2}\right) e^{-2\int_{\mathbf{x}}^{\ell} \varepsilon_{\mathbf{y}} d\mathbf{y}}}{1 - |\Gamma_{\ell}|^{2}}$$

where  $|\Gamma_{x}|$ ,  $|\Gamma_{l}|$ , and  $|\Gamma_{g}|$  are related by the equation [11, p. 42, eq. (2.12)]

$$|\Gamma_{\mathbf{x}}| = |\Gamma_{\mathbf{g}}e^{-2\int_{0}^{\mathbf{x}}\lambda_{\mathbf{y}}d\mathbf{y}}| = |\Gamma_{\mathbf{g}}| e^{-2\int_{0}^{\mathbf{x}}\varepsilon_{\mathbf{y}}d\mathbf{y}}$$
$$= |\Gamma_{\mathbf{g}}| e^{2\int_{\mathbf{x}}^{\mathbf{g}}\varepsilon_{\mathbf{y}}d\mathbf{y}}.$$

The  $\alpha_{r}$  ratio can be rewritten in the following form

$$\alpha_{\mathbf{x}} = e^{-2\int_{\mathbf{x}}^{\ell} \varepsilon_{\mathbf{y}} dy} - \frac{2|\Gamma_{\ell}|^{2}}{1 - |\Gamma_{\ell}|^{2}} \sinh\left(2\int_{\mathbf{x}}^{\ell} \varepsilon_{\mathbf{y}} dy\right) \quad (N.5)$$

where the dependence on the reflection coefficient  $\Gamma_{l}$  of the noise generator is more evident. In calculating  $T_{tot}$  this last term can usually be neglected.

# N.5. Summary and Conclusions

The results of SS N.2 and SS N.3 have been applied in SS N.4 to find the noise temperature T<sub>tot</sub> of a thermal noise standard:

$$T_{tot} = T_m + \Delta T$$
 (N.3)

in which

$$\Delta T \equiv (T_o - T_m) (1 - \alpha_o) + \int_0^{\ell} T'_x (1 - \alpha_x) dx \qquad (N.4)$$

and

$$\alpha_{\rm X} = e^{-2\int_{\rm X}^{\ell} \varepsilon_{\rm y} dy} - \frac{2|\Gamma_{\ell}|^2}{1 - |\Gamma_{\ell}|^2} \sinh\left(2\int_{\rm X}^{\ell} \varepsilon_{\rm y} dy\right). \quad (N.5)$$

Most output calculations neglect the second term in (N.5). Little error results, however, since most thermal standards are constructed from low-loss lines (small  $\varepsilon_y$ ) and low reflection coefficient terminations (small  $|\Gamma_{\sigma}|$ ), making

$$|\Gamma_{\ell}| = |\Gamma_{g}| e^{-2\int_{0}^{\ell} \varepsilon_{y} dy}$$

small and the last term in (N.5) small also.

The net power delivered to a load at the output of the standard source is  $MT_{tot}$ , where M is the output mismatch factor. If  $\Gamma_L$  is the load reflection coefficient, then

$$M = \frac{(1 - |\Gamma_{L}|^{2})(1 - |\Gamma_{\ell}|^{2})}{|1 - \Gamma_{L}\Gamma_{\ell}|^{2}}.$$

M and  $\Gamma_{l}$  can also be written in terms of the standard and load impedances,  $Z_{l}$  and  $Z_{L}$ .

$$M = \frac{4 \operatorname{ReZ}_{\ell} \operatorname{ReZ}_{L}}{|Z_{\ell} + Z_{L}|^{2}},$$

and

$$\Gamma_{\ell} = \frac{Z_{\ell} - Z_{o}}{Z_{\ell} + Z_{o}},$$

where  $Z_{0}$  is the characteristic line impedance [11].

| FORM NBS-114A (1-71)   |                              |                           |                                 |                    |
|--|------------------------------|---------------------------|---------------------------------|--------------------|
| U.S. DEPT. OF COMM.<br>BIBLIOGRAPHIC DATA<br>SHEET   | 1. PUBLICATION OR REPORT NO. | 2. Gov't Accession<br>No. | 3. Recipient'                   | s Accession No.    |
| 4. TITLE AND SUBTITLE  |                              |                           | 5. Publication Date             |                    |
| WR15 Thermal Noise Standard  |                              |                           | 1. 2. (                         |                    |
|  |                              |                           | 6. Performing Organization Code |                    |
| 7. AUTHOR(S)<br>W.C. Daywitt, W. J. Foote, and E. Campbell   |                              |                           | 8. Performing Organization      |                    |
| 9. PERFORMING ORGANIZATION NAME AND ADDRESS  |                              |                           | 10. Project/7                   | Task/Work Unit No. |
| NATIONAL BUREAU OF STANDARDS, Boulder Labs.<br>DEPARTMENT OF COMMERCE<br>Boulder, Colorado 80302   |                              |                           | 11. Contract/Grant No.          |                    |
| 12. Sponsoring Organization Name and Address   |                              |                           | 13. Type of I                   | Report & Period    |
| Same as 9.   |                              |                           | 1-71 - 1-72                     |                    |
|  |                              |                           | 14. Sponsorin                   | g Agency Code      |
|  |                              |                           |                                 |                    |
| 13. SUPPLEMENTARY NOTES  |                              |                           |                                 |                    |
| 16. ABSTRACT (A 200-word or less factual summary of most significant information. If document includes a significant bibliography or literature survey, mention it here.)<br>This note describes the design and construction of a WR15 thermal noise power standard. The standard is designed to operate around the Silver Point Temperature (963.19°C) with a noise temperature output accurate to approximately ± 2 K.<br>Complete details of the theory, design, construction, and performance tests are given. |                              |                           |                                 |                    |
|  |                              |                           |                                 |                    |
| Error analysis; millimeter wave; Noise; Nyquist's theorem; Thermal noise standard  |                              |                           |                                 |                    |
| 18. AVAILABILITY STATEME   | NT                           | 19. SECURIT<br>(THIS RE   | Y CLASS<br>PORT)                | 21. NO. OF PAGES   |
| X UNLIMITED.   |                              | UNCL AS                   | SIFIED                          | 154                |
| FOR OFFICIAL I   | DISTRIBUTION. DO NOT RELEASE | 20. SECURIT               | Y CLASS                         | 22. Price          |
| 10 N 11S.  |                              | UNCLASS                   | SIFIED                          | \$1.25             |
|  |                              |                           |                                 |                    |

USCOMM-DC 66244-P71



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