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## NBS TECHNICAL NOTE 600

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# Corrections and Calculations on an X-ray Diffraction Line Profile: A Computer Program

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## Corrections and Calculations on an X-ray Diffraction Line Profile: A Computer Program

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#### Corrections and Calculations on an X-ray Diffraction Line Profile: A Computer Program

#### Raymond E. Schramm

This computer program was written to perform corrections and make calculations on an x-ray diffraction profile before Fourier analysis. The corrections are for background and for variations of intensity with the Bragg angle. Also calculated are the separation of the  $K\alpha_1 - K\alpha_2$  doublet and the centroid and position of peak maximum with their standard deviations. There is also an option to smooth the profile.

#### Key Words: Computer programs, Fourier analysis, nickel steels, x-ray analysis, x-ray diffraction, statistics.

#### 1. Introduction

Annealed and heavily strained x-ray diffraction line profiles (fig. 1) can be compared

to provide information on parameters such as particle size, dislocation density, and stacking fault energy. One scheme to do this is Fourier analysis. Gazzara, Stiglich, Meyer, and Hansen<sup>[1]</sup> wrote a computer program "UNFOLD" to perform the mathematical operations; several other programs are also available.<sup>[2,3]</sup> In working with a series of iron-nickel alloys, it became necessary to make corrections and calculations on the x-ray data in addition to those available in the program of Gazzara, et al. The program "PREP" was written to unify the preparation for programs such as "UNFOLD" by making all of the following calculations.

Within subroutines corrections are made for:

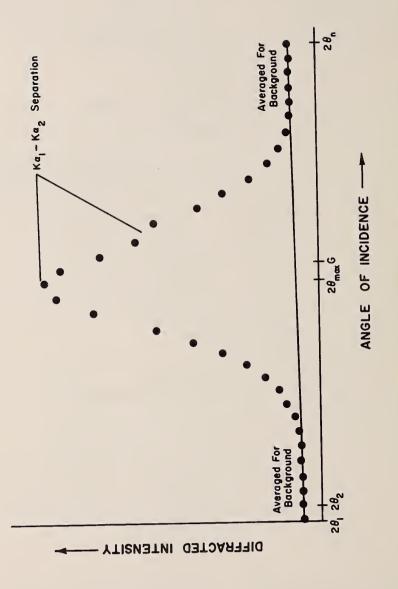
1. Background intensity.

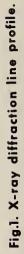
2. Variation of intensity with the Bragg angle due to geometrical factors.

Subroutines are also used to determine:

- 1. Rachinger separation <sup>[4]</sup> of the  $K\alpha_1 K\alpha_2$  doublet.
- 2. Centroids of the K $\alpha$  and K $\alpha_1$  profiles with estimated standard deviations.
- 3. Peak maxima of the K $\alpha$  and K $\alpha_1$  profiles with estimated standard deviations.

<sup>1</sup>Figures in brackets indicate the literature references at the end of this paper.





#### Table 1. List of Symbols Used.

Symbol	Page of	Meaning
🦂 Fi	rst Appearance	
a	4	Background intensity on low angle side of diffraction lines.
b	4	Background intensity at an arbitrary point.
с	7	Composite angular correction factor.
d	8	Angular separation of $K \alpha_1 - K \alpha_2$ doublet.
f	5	Atomic scattering factor.
h	7	Cylindrical specimen height.
m	7	Specimen density.
n	4	Number of experimental points or pairs of $2\theta_i$ and $I(2\theta_i)$ .
r	5	Cylindrical specimen radius.
x	7	Mass fraction of Nickel
z	4	Background intensity on high angle side of diffraction line.
A	5	Sample absorption factor.
B,C,D,	13	Parameters of parabolic fit to peak.
G	2	Profile center of gravity.
I, I <sub>1</sub> , I <sub>2</sub>	4	Reflected intensity (counts/unit time) due to the radiations K $\alpha$ , K $\alpha_1$ , and K $\alpha_2$ respectively.
Κα, Και, Κα	e l	Characteristic radiations of the X-ray tube target.
LP	5	Lorentz-polarization factor.
α	5	Bragg angle of crystal monochromator.
§2θ	14	Increment in 20 between individual measurements.
Δ2 θ	10	Angular span between first and last measurements.
θ	l	Specimen Bragg angle of reflection; $2\theta$ is twice this angle. $2\theta_{max}$ is the position of the peak maximum.
$\lambda$ , $\lambda_1$ , $\lambda_2$	8	Wavelengths of K $\alpha_1$ , K $\alpha_1$ , and K $\alpha_2$ radiations respectively.
μ	5	Linear X-ray absorption coefficients.
ρ	7	Specimen mass density
ρ <sub>s</sub>	7	Mass density of powder sample.
σ	11	Standard deviation of center of gravity and peak maximum.

It has been found advantageous to smooth the profiles of cold-worked samples before Fourier analysis so an option to do this has been provided. It is also possible to have the corrected profile data punched in a format ready to enter "UNFOLD".

Angular positions are entered invalues of 2  $\theta$  (twice the Bragg angle). The diffraction intensities must be in the fixed-time mode (intensity count at each angular increment determined for a fixed length of time) and measured at equal increments of 2  $\theta$  across the entire profile. Several constants are written into the program assuming Debye-Scherrer geometry, the use of a monochromator with Co K  $\alpha$  radiation, and iron-nickel or silver samples. The changes necessary when using other geometries, radiations, or samples are listed in the Appendix.

This program has been written in FORTRAN language and executed on a CDC 3800\* computer.

#### 2. Background Calculation, "BACK"

The background intensity is the measured radiation that is scattered into the detector by means other than primary Bragg reflection of the  $K_{\alpha}$  component by the specimen. It generally arises from a number of sources: fluorescent radiation from the specimen, diffraction of the continuous spectrum, incoherent scattering from the specimen, and diffraction or scatter from something other than the specimen itself (e.g., collimator, air, etc.).

This calculation is made by arbitrarily averaging the intensities of the first five points and the last five points and then drawing a straight line through these two averaged points.

#### Line Profile

Angular Position (2θ)	Intensity (counts/unit time)
2 0 <sub>1</sub>	Ι(2 θ <sub>1</sub> )
•	•
•	•
•	
2θ <sub>n</sub>	I(2θ <sub>n</sub> )

\*The use of trade names in this paper in no way implies endorsement or approval by NBS and is included only to define the procedure. Set:

$$a = \frac{1}{5} \sum_{i=1}^{5} I(2\theta_i) ,$$
$$z = \frac{1}{5} \sum_{i=0}^{4} I(2\theta_{n-i})$$

Then

$$b_{i} = \left(\frac{z - a}{2\theta_{n} - 2\theta_{1}}\right) 2\theta_{i} + \frac{a(2\theta_{n}) - z(2\theta_{1})}{2\theta_{n} - 2\theta_{1}}$$

where  $b_i$  is the background intensity at  $2\theta_i$ .

Background subtraction is an available option in "UNFOLD".

#### 3. Angular Correction, "ANG"

There are several factors affecting the diffracted intensity which are functions of the Bragg angles. This angular correction is divided into three parts.

When a monochromator is used [5],

$$LP = \frac{1 + \cos^2 2\alpha \cos^2 2\theta}{\sin^2 \theta \cos \theta} ,$$

where  $\alpha$  is the Bragg angle of the crystal in the monochromator and  $\theta$  is the Bragg angle of the specimen.

3.2. Atomic Scattering Factor (f)

The atomic scattering factor (f) is a function of  $\frac{\sin\theta}{\lambda}$ ,  $\lambda$  being the wavelength of the radiation being used. Tables of this factor for various values of  $\frac{\sin\theta}{\lambda}$  and for various atomic models are available<sup>[6]</sup>. The values used are given in table 2 in a normalized form (from self-consistent wave functions) for iron, nickel, and silver.

To determine f at intermediate values of  $\frac{\sin\theta}{\lambda}$  a power series polynomial was fitted to the values in table 2. For a better fit  $\frac{\sin\theta}{\lambda}$  was divided into three ranges. The values for this fit are given in table 3.

$\frac{\sin\theta}{\lambda}$	Fe	Ni	Ag
0.00	1.000	1.000	1.000
0.05	0.9731	0.9768	0.9817
0.10	0.9108	0.9214	0.9336
0.15	0.8404	0.8568	0.8698
0.20	0.7727	0.7925	0.8017
0.25	0.7077	0.7300	0.7362
0.30	0.6450	0.6689	0.6762
0.35			0.6234
0.40	0.5323	0.5557	0.5781
0.50	0.4412	0.4611	0.5066
0.60	0.3735	0.3875	0.4547
0.70	0.3258	0.3332	0.4151

Table 2. - Normalized atomic scattering factors, f

Table 3. - Power series coefficients for the atomic scattering factors

				cin A
Coefficient	Fe	Ni	Ag	Range of $\frac{\sin \theta}{\lambda}$
				sinθ
a	+1.000	+1.000	+1.000	$0 \leq \frac{\sin \theta}{\lambda} \leq 0.12$
b	-0.184	-0.142	-0.068	<i>R</i>
с	-7.080	-6.644	-5.960	
				sinθ
a	+1.0637002	+1.0645004	+1.0685171	$0.12 < \frac{\sin\theta}{\lambda} \leq 0.35$
b	-1.6056701	-1.4746725	-1.2033810	'n
с	+0.86001593	+0.68002691	-1.2685714	
d	-0.53335684	-0.53337307	+3.0666667	
				sin θ
a	+1.1987014	+1.1781009	+1.2061000	$\frac{\sin\theta}{\lambda} > 0.35$
b	-2,3833411	-2.1006716	-2.4973333	· ·
с	+2.0200144	+4.4750092	+2.8050000	
d	-0.56667538	-0.28333892	-1.2166667	

 $f = a + b \left(\frac{\sin\theta}{\lambda}\right) + c \left(\frac{\sin\theta}{\lambda}\right)^2 + d\left(\frac{\sin\theta}{\lambda}\right)^3$ 

In the case of the iron-nickel alloys it was arbitrarily decided to use the atomic scattering factor for Fe for all bcc alloys and the atomic scattering factor for Ni for all fcc alloys. This gives a reasonable approximation to the electron density distribution in the alloy.

#### 3.3. Sample Absorption (A)

For a flat specimen in a focusing geometry the sample absorption factor is independent of  $2\theta^{[7]}$ . However, for a Debye-Scherrer geometry<sup>[8,9]</sup> a cylindrical sample is used and Bradley<sup>[10]</sup> gives the absorption factor:

$$A = \frac{1}{\pi\mu r} \left\{ 1 - \frac{\ell n(\sec\theta + \tan\theta)}{\sec\theta \tan\theta} \right\} + \frac{\sin 2\theta}{2\pi\mu^2 r^2} + \frac{1}{\pi\mu^3 r^3} \left[ -\frac{1}{4} + \frac{3}{4}\cos^2\theta \left\{ \frac{1}{2} + \frac{1}{2}\frac{\ell n(\sec\theta + \tan\theta)}{\sec\theta \tan\theta} \right\} \right]$$

for  $\mu r > 10$ , where  $\mu$  is the linear absorption coefficient and r is the radius of the cylindrical specimen.

Using trigonometric identities this factor can be restated:

$$A = \frac{1}{\pi \mu r} \left\{ 1 - \frac{\cos^2 \theta \ell n \left( \frac{1 + \sin \theta}{\cos \theta} \right)}{\sin \theta} \right\} + \frac{\sin 2\theta}{2\pi (\mu r)^2} + \frac{1}{\pi (\mu r)^3} \left[ -\frac{1}{4} + \frac{3}{8} \cos^2 \theta \left\{ 1 + \frac{\cos^2 \theta \ell n \left( \frac{1 + \sin \theta}{\cos \theta} \right)}{\sin \theta} \right\} \right].$$

Bradley notes that for a diluted specimen (as in this case, we have used a powder mixed with cement):  $\mu \mathbf{r} = \frac{\mu}{\rho} \frac{\mathbf{m}}{\pi \mathbf{r} \mathbf{h}},$ 

where  $\frac{\mu}{\rho}$  is the mass absorption coefficient, m is the mass of the powder in a specimen of height h and radius r. For a powder with three components (as Fe, Ni, and inactive cement)

$$\mu \mathbf{r} = \left[ \left( \frac{\mu}{\rho} \right)_{\text{Ni}} \times \left( \frac{\mu}{\rho} \right)_{\text{Fe}} (1 - \mathbf{x}) \right] \frac{\mathbf{m}}{\pi \mathbf{r} \mathbf{h}} ,$$

where x is the mass fraction of the Ni. Now:

 $\frac{m}{\pi r h} = r \rho_s$ ,  $\rho_s$  = the mass density of the final sample.

mass absorption coefficients here for Co K $\alpha$  radiation are<sup>[11]</sup>:

$$\left(\frac{\mu}{\rho}\right)_{\rm Ni}$$
 = 75.1,  $\left(\frac{\mu}{\rho}\right)_{\rm Fe}$  = 59.5,  $\left(\frac{\mu}{\rho}\right)_{\rm Ag}$  = 332.

Also: 
$$r = 0.1 \text{ cm}$$
,  $\rho_{c}$  (Fe-Ni alloys) = 3.65 g/cm<sup>3</sup>,  $\rho_{s}$  (Ag) = 3.92 g/cm<sup>3</sup>.

The total angular correction factor used to multiply the intensity is composed of the preceeding three elements.

$$c = \frac{1}{f^2 (LP)A}$$

This is normalized to unity at  $2\theta_1$ .

"UNFOLD" has the option to make this correction taking into account the Lorenzpolarization and atomic scattering factors. This is all that is necessary when using a flat sample but the Debye-Scherrer geometry requires the inclusion of the absorption factor.

#### 4. Rachinger Separation, "RACH"

The Rachinger method <sup>[4]</sup> is a graphical means of separating the  $K\alpha_1 - K\alpha_2$  line doublet.

 $I_{1}(2\theta_{i}) = I(2\theta_{i}) - I_{2}(2\theta_{i}) \text{ where}$   $I = \text{ intensity due to } \alpha_{1} + \alpha_{2} \text{ (recorded intensity),}$   $I_{1} = " " " \alpha_{1},$   $I_{2} = " " " \alpha_{2}.$ 

The usual assumption <sup>[12]</sup> is made that the K  $\alpha_2$  intensity is half that of the K  $\alpha_1$  so that:

$$I_{2}(2\theta_{i}) = \frac{1}{2}I_{1}(2\theta - d),$$

where d is the doublet separation. Now

$$I_{1}(2\theta_{i}) = I(2\theta_{i}) - \frac{1}{2}I_{1}(2\theta_{i}-d).$$

It is important that data be collected sufficiently far out on the low angle side of the profile so that the calculation is started at a diffraction angle sufficiently small that  $I_2 \approx 0$ , or the measured intensity is due mainly to the  $K\alpha_1$  component. Values of  $I_1$  at higher angles can then be determined by successive calculations.

The doublet separation, d, is determined from an approximate peak position of the K $\alpha$ curve and the wavelengths  $\lambda$ ,  $\lambda_1$ , and  $\lambda_2$  of the K $\alpha$ , K $\alpha_1$ , and K $\alpha_2$  radiations respectively. From the Bragg equation:

$$\lambda = 2d'\sin\theta \text{ and } \lambda_1 = 2d'\sin\theta_1$$
  
(d' = interplanar spacing),  
$$\sin\theta_1 = \frac{\lambda_1}{\lambda} \sin\theta.$$

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Similarly for the  $K\alpha_2$  component:

$$\sin \theta_2 = \frac{\lambda_2}{\lambda} \sin \theta_1,$$

and the doublet separation in  $2\theta$  is d =  $2\theta_2 - 2\theta_1$ 

$$d = 2 \left\{ \sin^{-1} \left[ \frac{\lambda_2}{\lambda} \sin \theta \right] - \sin^{-1} \left[ \frac{\lambda_1}{\lambda} \sin \theta \right] \right\}.$$

For cobalt radiation

$$\lambda = 1.79021 \text{ Å}$$
 ,  
 $\lambda_1 = 1.78892 \text{ Å}$  ,  
 $\lambda_2 = 1.79278 \text{ Å}$  .

In general, the angle  $(2\theta_i - d)$  will not coincide with any of the angular values  $2\theta_j$ so it is necessary to interpolate. Assume:

$$2\theta_{j} \leq 2\theta_{i} - d \leq 2\theta_{k}$$
.

A straight line is fitted between  $I_1(2\theta_i)$  and  $I_1(2\theta_k)$  and:

$$I_{1}(2\theta_{i} - d) = \frac{I_{1}(2\theta_{k}) - I_{1}(2\theta_{j})}{2\theta_{k} - 2\theta_{j}} (2\theta_{i} - d) + \frac{[I_{1}(2\theta_{j})](2\theta_{k}) - [I_{1}(2\theta_{k})](2\theta_{j})}{2\theta_{k} - 2\theta_{j}}$$

Although it is not apparent, the Rachinger separation has a tendency to oscillate or become assymmetrical on the high angle side of the profile. This is especially true for a sharp, well separated K $\alpha$ line. For this reason the options for card punching and mathematical smoothing are applied only to the corrected K $\alpha$  profile in this program. This section is still included, however, for those occasions when it might be useful.

#### 5. Center of Gravity Calculation, "CENTROID"

The centroid or center of gravity is one measure of the position of the diffraction line. It is of value in measuring lattice parameters<sup>[13]</sup>, twin fault probabilities<sup>[14]</sup>, etc. According to Pike and Wilson<sup>[13]</sup> the center of gravity is determined by

$$G = \frac{\sum_{i}^{\Sigma} (I_{i} - b_{i}) c_{i}^{*} (2\theta_{i})}{\sum_{i}^{\Sigma} (I_{i} - b_{i}) c_{i}} , \qquad (1)$$

where

G = center of gravity,
2 θ<sub>i</sub> = angular position,
I<sub>i</sub> = measured intensity,
b<sub>i</sub> = background (calculated in sec. 2),
c<sub>i</sub> = angular correction factor (calculated in sec. 3).
The summations are over all points.

Equation (1) is modified from the equation given by Pike and Wilson by the presence of the  $c_i$ 

From the calculation of the background (sec. 2)

setting 
$$\Delta 2\theta = 2\theta_n - 2\theta_1$$
,

$$p_{i} = \left(\frac{z-a}{\Delta 2\theta}\right) 2\theta_{i} + \frac{a(2\theta_{n}) - z(2\theta_{1})}{\Delta 2\theta}$$

or

$$\mathbf{b}_{i} = z \left( \frac{2\theta_{i} - 2\theta_{1}}{\Delta 2\theta} \right) - a \left( \frac{2\theta_{i} - 2\theta_{n}}{\Delta 2\theta} \right)$$
(2)

Substituting eq (2) into eq (1)

$$G = \frac{\sum_{i} \left[ I_{i} - z \left( \frac{2\theta_{i} - 2\theta_{i}}{\Delta 2\theta} \right) + a \left( \frac{2\theta_{i} - 2\theta_{n}}{\Delta 2\theta} \right) \right] c_{i}^{*}(2\theta_{i})}{\sum_{i} \left[ I_{i} - z \left( \frac{2\theta_{i} - 2\theta_{i}}{\Delta 2\theta} \right) + a \left( \frac{2\theta_{i} - 2\theta_{n}}{\Delta 2\theta} \right) \right] c_{i}}$$

or

$$G = \frac{\sum_{i} I_{i} c_{i}^{*}(2\theta_{i}) - z \sum_{i} \left(\frac{2\theta_{i} - 2\theta_{i}}{\Delta 2\theta}\right) c_{i}^{*}(2\theta_{i}) + a \sum_{i} \left(\frac{2\theta_{i} - 2\theta_{i}}{\Delta 2\theta}\right) c_{i}^{*}(2\theta_{i})}{\sum_{i} I_{i} c_{i} - z \sum_{i} \left(\frac{2\theta_{i} - 2\theta_{i}}{\Delta 2\theta}\right) c_{i} + a \sum_{i} \left(\frac{2\theta_{i} - 2\theta_{i}}{\Delta 2\theta}\right) c_{i}}$$
(3)

An estimate of the standard deviation is given by the standard propagation of error.

$$\sigma^{2}(G) = \sum_{i} \left(\frac{\partial G}{\partial I_{i}}\right)^{2} \sigma^{2} \left(I_{i}\right) + \left(\frac{\partial G}{\partial a}\right)^{2} \sigma^{2}(a) + \left(\frac{\partial G}{\partial z}\right)^{2} \sigma^{2}(z) .$$
(4)

Now

$$\frac{\partial G}{\partial I_{i}} = \frac{\binom{(2\theta_{i})}{i}c_{i}}{\sum I_{i}c_{i} - z\sum i} \left(\frac{\frac{2\theta_{i} - 2\theta_{1}}{\Delta 2\theta}}{i}\right)c_{i} + a\sum i} \left(\frac{\frac{2\theta_{i} - 2\theta_{n}}{\Delta 2\theta}}{i}\right)c_{i}}{\frac{c_{i}\left[\sum I_{i}c_{i}(2\theta_{i}) - z\sum i}\left(\frac{\frac{2\theta_{i} - 2\theta_{1}}{\Delta 2\theta}}{i}\right)c_{i}(2\theta_{i}) + a\sum i}\left(\frac{\frac{2\theta_{i} - 2\theta_{n}}{\Delta 2\theta}}{i}\right)c_{i}(2\theta_{i})\right)}{\left[\sum I_{i}c_{i} - z\sum i}\left(\frac{\frac{2\theta_{i} - 2\theta_{1}}{\Delta 2\theta}}{i}\right)c_{i} + a\sum i}c_{i}\left(\frac{\frac{2\theta_{i} - 2\theta_{n}}{\Delta 2\theta}}{i}\right)\right]^{2}}\right]$$

On substituting from eq (3)

$$\frac{\partial G}{\partial I_{i}} = \frac{(2\theta_{i} - G)c_{i}}{\sum_{i} I_{i}c_{i} - z \sum_{i} \left(\frac{2\theta_{i} - 2\theta_{i}}{\Delta 2\theta}\right)c_{i} + a \sum_{i} \left(\frac{2\theta_{i} - 2\theta_{n}}{\Delta 2\theta}\right)c_{i}} \qquad (5)$$

Also

$$\frac{\partial G}{\partial a} = \frac{\sum_{i} \left( \frac{2\theta_{i} - 2\theta_{n}}{\Delta 2\theta} \right) c_{i} \cdot (2\theta_{i})}{\sum_{i} I_{i} c_{i} - z \sum_{i} \left( \frac{2\theta_{i} - 2\theta_{1}}{\Delta 2\theta} \right) c_{i} + a \sum_{i} \left( \frac{2\theta_{i} - 2\theta_{n}}{\Delta 2\theta} \right) c_{i}}$$

$$= \frac{\sum_{i} \left(\frac{2\theta_{i} - 2\theta_{n}}{\Delta 2\theta}\right) c_{i} \left[\sum_{i} I_{i} c_{i}^{*}(2\theta_{i}) - z \sum_{i} \left(\frac{2\theta_{i} - 2\theta_{1}}{\Delta 2\theta}\right) c_{i}^{*}(2\theta_{i}) + a \sum_{i} \left(\frac{2\theta_{i} - 2\theta_{n}}{\Delta 2\theta}\right) c_{i}^{*}(2\theta_{i})\right]}{\left[\sum_{i} I_{i} c_{i} - z \sum_{i} \left(\frac{2\theta_{i} - 2\theta_{1}}{\Delta 2\theta}\right) c_{i} + a \sum_{i} \left(\frac{2\theta_{i} - 2\theta_{n}}{\Delta 2\theta}\right) c_{i}\right]^{2}}$$

On substituting from eq (3)

$$\frac{\partial G}{\partial a} = \frac{\sum\limits_{i}^{\Sigma} \left(\frac{2\theta_{i} - 2\theta_{n}}{\Delta 2\theta}\right) c_{i}^{*}(2\theta_{i}) - G_{\Sigma} \left(\frac{2\theta_{i} - 2\theta_{n}}{\Delta 2\theta}\right) c_{i}}{\sum\limits_{i}^{\Sigma} I_{i} c_{i} - z \sum\limits_{i}^{\Sigma} \left(\frac{2\theta_{i} - 2\theta_{1}}{\Delta 2\theta}\right) c_{i}^{*} + a \sum\limits_{i}^{\Sigma} \left(\frac{2\theta_{i} - 2\theta_{n}}{\Delta 2\theta}\right) c_{i}}$$

Or

$$\frac{\partial G}{\partial a} = \frac{\sum_{i} \left(\frac{2\theta_{i} - 2\theta_{n}}{\Delta 2\theta}\right) c_{i} (2\theta_{i} - G)}{\sum_{i} I_{i} c_{i} - z \sum_{i} \left(\frac{2\theta_{i} - 2\theta_{1}}{\Delta 2\theta}\right) c_{i} + a \sum_{i} \left(\frac{2\theta_{i} - 2\theta_{n}}{\Delta 2\theta}\right) c_{i}}$$
(6)

Also:

$$\frac{\partial G}{\partial z} = \frac{-\sum_{i} \left(\frac{2\theta_{i} - 2\theta_{1}}{\Delta 2\theta}\right) c_{i} (2\theta_{i})}{\sum_{i} I_{i} c_{i} - z \sum_{i} \left(\frac{2\theta_{i} - 2\theta_{1}}{\Delta 2\theta}\right) c_{i} + a \sum_{i} \left(\frac{2\theta_{i} - 2\theta_{n}}{\Delta 2\theta}\right) c_{i}}$$

$$+ \frac{\sum_{i} \left(\frac{2\theta_{i} - 2\theta_{1}}{\Delta 2\theta}\right) c_{i} \cdot \left[\sum_{i} I_{i} c_{i} \cdot (2\theta_{i}) - z \sum_{i} \left(\frac{2\theta_{i} - 2\theta_{1}}{\Delta 2\theta}\right) c_{i} \cdot (2\theta_{i}) + a \sum_{i} \left(\frac{2\theta_{i} - 2\theta_{n}}{\Delta 2\theta}\right) c_{i} \cdot (2\theta_{i})\right]}{\left[\sum_{i} I_{i} c_{i} - z \sum_{i} \left(\frac{2\theta_{i} - 2\theta_{1}}{\Delta 2\theta}\right) c_{i} + a \sum_{i} \left(\frac{2\theta_{i} - 2\theta_{n}}{\Delta 2\theta}\right) c_{i}\right]^{2}}\right]$$

,

or

$$\frac{\partial G}{\partial z} = \frac{\sum_{i} \left( \frac{2\theta_{i} - 2\theta_{1}}{\Delta 2\theta} \right) c_{i} \cdot (G - 2\theta_{i})}{\sum_{i} I_{i} c_{i} - z \sum_{i} \left( \frac{2\theta_{i} - 2\theta_{1}}{\Delta 2\theta} \right) c_{i} + a \sum_{i} \left( \frac{2\theta_{i} - 2\theta_{1}}{\Delta 2\theta} \right) c_{i}}$$
(7)

And, since the standard deviation of a random variable is the square root of that variable,

$$\sigma^{2}(I_{i}) = I_{i} , \qquad (8)$$
also  $a = \frac{1}{5} \sum_{i=1}^{5} I_{i} \quad (\text{see sec. 2}) ,$ 

$$\sigma^{2}(a) = \sum_{i} \left(\frac{\partial a}{\partial I_{i}}\right)^{2} \sigma^{2}(I_{i}) \quad \text{where} \quad \frac{\partial a}{\partial I_{i}} = \frac{1}{5} ,$$

$$\sigma^{2}(a) = \frac{1}{25} \sum_{i=1}^{5} I_{i} = \frac{1}{5} a$$
.

In a similar manner for z,

SC

$$\sigma^2(z) = \frac{1}{5} z .$$
 (10)

The center of gravity is calculated from eq (1) and the estimate of its standard deviation is determined from eq (4) using eq (5) through eq (10).

#### 6. Peak Calculation, "PEAK"

The position of peak maximum is another measure of the profile's angular location. It also is used to measure lattice parameter and twin fault probabilities, as well as stacking fault probabilities <sup>[15]</sup>.

A portion of the profile on either side of the maximum (we generally used a total of 7 to 9 points) is fitted to a parabola<sup>[16]</sup> and the maximum of that curve is determined.

$$I_i = B + C \cdot (2\theta_i) + D \cdot (2\theta_i)^2 .$$

Differentiating:

$$\frac{dI_i}{d(2\theta_i)} = C + 2D \cdot (2\theta_i) = 0$$

so that

$$peak = 2\theta_{max} = -\frac{C}{2D} , \qquad (11)$$

where B, C, and D are the parameters of the fitted curve.

The standard propagation of error with correlation between the variables C and D gives:

$$\sigma^{2}(2\theta_{\max}) = \left(\frac{\partial(2\theta_{\max})}{\partial C}\right)^{2} \sigma^{2}(C) + \left(\frac{\partial(2\theta_{\max})}{\partial D}\right)^{2} \sigma^{2}(D) + 2\left(\frac{\partial(2\theta_{\max})}{\partial C}\right) \left(\frac{\partial(2\theta_{\max})}{\partial D}\right) \sigma(C) \sigma(D)$$

(9)

Differentiating eq (11) this becomes

$$\sigma^{2}(2\theta_{\max}) = \left(\frac{1}{4D^{2}}\right)\sigma^{2}(C) + \left(\frac{C^{2}}{4D^{4}}\right)\sigma^{2}(D) + 2\left(\frac{-1}{2D}\right)\left(\frac{C}{2D^{2}}\right)\sigma\left(C\right)\sigma\left(D\right),$$
$$= \frac{\left(2\theta_{\max}\right)^{2}}{C^{2}}\sigma^{2}(C) + \frac{\left(2\theta_{\max}\right)^{2}}{D^{2}}\sigma^{2}(D) - 2\frac{\left(2\theta_{\max}\right)^{2}}{CD}\sigma\left(C\right)\sigma\left(D\right).$$

A modification of a computer program written by W. J. Hall was used here to compute the curve parameters and their standard deviations. This program performs an orthonormal curve fitting using Bjork's modification<sup>[17, 18]</sup> of the Gram-Schmidt technique.

#### 7. Curve Smoothing, "SMOOTH"

In the course of experimenting on several iron-nickel alloys, it was found that the Fourier analyses of the diffraction profiles were far more repeatable if the data from the cold-worked sample were first smoothed. This subroutine affords the option of performing this operation.

The intensity curve is mathematically smoothed by a least-squares fit of a quartic equation to seven points, taking the value at the midpoint and then advancing the group of points by one unit and repeating the process.

$$I_i(smoothed) = (I_{i-3} - 18I_{i-2} + 63I_{i-1} + 164I_i + 63I_{i+1} - 18I_{i+2} + I_{i+3})/256$$

Three points are added before the initial intensity and three after the final intensity and they are all set equal to zero.

This smoothing operation can be performed repeatedly (limited to 99 times by format). It is possible to have up to ten of these smoothed curves printed and to have one of them card punched for input to "UNFOLD".

#### 8. Data Input and Output and a Sample

#### Card Input

Card	Information	Format
1	Identification	50H
	<ul> <li>a. Number of points (intensity with angular positi</li> <li>b. Initial 2θ, i.e., 2θ<sub>1</sub></li> </ul>	on) in profile.
2	<ul> <li>c. 2θ increment, δ 2θ</li> <li>d. 2θ position of peak (must equal 2θ<sub>1</sub> + k × δ 2θ, k an integer).</li> </ul>	I10, 5F10.2, I10
	e. Angular correction added to each $2\theta^*$ .	
	f. Ni fraction in an Fe-Ni alloy.	
	<ul> <li>g. 1 for bcc phase, 2 for fcc phase in an</li> <li>Fe-Ni sample (e, f, and g are necessary only when they are applicable).</li> </ul>	
	Punch options for input to "UNFOLD"	
	<ul> <li>a. 0 for no card punch, 1 for punch of corrected Kα profile, 2 for punch of corrected Kα profile after smoothing.</li> </ul>	•
3	b. Number of smoothings to be printed (max = 10)	315
	<ul> <li>c. Smoothing number to be punched (0 for no punch).</li> <li>(b and c are necessary only if 3a = 2)</li> </ul>	
4	Smoothing numbers to be printed.(This card is omitted if $3a \neq 2$ . The number in 3c must be one of these numbers).	1015
5	Lower and upper angular limits for parabolic fit to determine profile maximum.	2F10.2
6.	Intensities	10F7.0

Output data includes:

- 1. Identification
- 2. Table containing angular positions, recorded intensities, backgrounds, angular corrections, and the corrected K  $\alpha$  and K  $\alpha_1$  profiles.

\* Using the Debye-Scherrer technique, it is possible to calibrate the diffractometer by examining the reflection on both positive and negative sides of the diffraction cone [6,8]. This gives a correction factor to the angle read from the instrument.

- 3. Line maximum and center of gravity with their standard deviations for  $K\alpha$  and  $K\alpha_1$  profiles.
- Peak value used for punching "UNFOLD" input and smoothing number used (if applicable).
- 5. Table containing angular positions and smoothed  $K\alpha$  profile (if applicable).

A sample of input and output follows.

## **Punched Card Input**

FE-28N		D-WORKE							
. 1	.11	50.60	0.02	25	1.92		0	•28	2
2	4 4	•							_
2	4 6	8							
51.	72	52.02							
270.	260•	260.	270.	260.	290.	240.	290.	310.	310.
290.	290.	310.	300.	270.	260.	320.	280.	330.	330.
300•	330.	360.	340.	370.	330.	350.	360.	340.	350.
390.	400.	400.	370.	420.	450.	490.	470.	510.	510.
530.	600.	620.	710.	740.	740.	830.	910.	950.	940.
1010.	1170.	1260.	1330.	1410.	1550.	1620.	1720.	1840.	1940.
2050.	2130.	2220.	2270.	2350.	2380.	2390.	2390.	2360.	2320.
2280.	2190.	2040.	1940.	1840.	1600.	1330.	1160.	1050.	950.
860.	810.	760.	720.	670.	610.	560.	510.	490.	470.
440•	420.	400.	390.	380.	370.	360.	350.	340.	330.
320.	310.	300.	290.	280.	270.	270.	270.	270.	270.
270.									

## **Printed Output**

FE-28NI COLD-WORKED (111)

2 THETA	REC CNT	BACK	ANG COR	ALPHA	ALPHA 1
50.60	270	264	1.0000	6	0
50.62	260	264	1.0004	-4	0
50.64	260	264	1.0009	-4	0
50.66	270	264	1.0013	6	0
50.68	260	264	1.0017	-4	0
50.70	290	264	1.0022	26	0
50.72	240	264	1.0026	-24	0
50.74	290	264	1.0030	26	0
50.76	310	264	1.0035	46	46
50.78	310	264	1.0039	46	46
50.80	290	265	1.0044	26	26
50.82	290	265	1.0048	26	26
50.84	310	265	1.0052	46	46
50.86	300	265	1.0057	35	35
50.88	270	265	1.0061	5	-17
<b>50 • 9</b> 0	260	265	1.0065	-5	-28
50.92	320	265	1.0070	56	43
50.94	280	265	1.0074	15	2
50.96	330	265	1.0078	66	43
50.98	330	265	1.0083	66	48
51.00	300	265	1.0087	35	43
51.02	330	265	1.0092	65	79
51.04	360	265	1.0096	96	75

51.06	340	265	1.0100	75	74
51.08	370	265	1.0105	106	85
51.10	330	265	1.0109	65	42
51.12	350	265	1.0113	86	64
51.14	360	265	1.0118	96	56
			1.0122	75	
51.16	340	266			38
51.18	350	266	1.0127	85	48
51.20	390	266	1.0131	126	84
51.22	400	266	1.0135	136	115
51.24	400	266	1.0140	136	104
51.26	370	266	1.0144	106	77
51.28	420	266	1.0148	156	137
51.30	450	266	1.0153	187	163
	490		1.0157	228	186
51.32		266			
51.34	470	266	1.0162	207	150
51.36	510	266	1.0166	248	196
51.38	510	266	1.0170	248	209
					200
51.40	530	266	1.0175	268	
51.42	600	266	1.0179	340	259
51.44	620	266	1.0184	360	267
51.46	710	266	1.0188	452	377
51.48	740	266	1.0192	483	385
51.50	740	, 266	1.0197	483	378
51.52	830	267	1.0201	575	475
51.54	910	267	1.0206	657	528
	950				564
51.56		267	1.0210	698	
51.58	940	26 <b>7</b>	1.0214	688	500
51 <b>.6</b> 0	1010	267	1.0219	760	567
51.62	1170	267	1.0223	923	734
	1260	267	1.0228	1016	779
51.64					
51.66	1330	267	1.0232	1088	824
51.68	1410	267	1.0236	1170	888
51.70	1550	267	1.0241	1314	1063
51.72	1620		1.0245	1386	1103
		267			
51.74	1720	267	1 0250	1489	1123
51.76	1840	267	1.0254	1613	1224
51.78	1940	267	1.0258	1716	1304
51.80	2050	267	1.0263	1830	1386
51.82	2130	267	1.0267	1912	1382
51.84	2220	267	1.0272	2006	1454
51.86	2270	267	1.0276	2058	1496
51.88	2350	267	1.0280	2141	1530
51.90	2380	268	1.0285	2173	1521
51.92	2390	268	1.0289	2184	1491
51.94	2390	268	1.0294	2185	1494
51.96	2360	268	1.0298	2155	1428
51.98	2320	268	1.0303	2114	1366
52.00	2280		1.0307	2074	
		268			1309
52.02	2190	268	1.0311	1982	1221
52.04	2040	268	1.0316	1828	1082
52.06	1940	268	1.0320	1726	979
52.08	1840	268	1.0325	1623	908
52.10	1 <b>6</b> 00	268	1.0329	1376	692
52.12	1330	268	1.0334	1097	442
52.14	1160	268	1.0338	922	311
52.16	1050	268	1.0342	809	266
52.18	950	268	1.0347	705	215
52.20	860	268	1.0351	612	158
52.22	810	268	1.0356	561	213
52.24	760	268	1.0360	509	286
52.26	720	269	1.0365	468	312
52.28	670	269	1.0369	416	283
52.30	610	269	1.0374	354	246
52.32	560	269	1.0378	302	223
22022	200	207		202	
			18		

52.34	510	269	1.0382	250	144
52.36	490	269	1.0387	230	87
52.38	470	269	1.0391	209	53
52.40	440	269	1.0396	178	
52.42	420	269	1.0400	157	36
52.44	400	269	1.0405	136	34
52.46	390	269	1.0409		25
52.48	380	269	1.0414	126	53
52.50	370	269	1.0418	115	71
52.52	360	269	1.0422	105	78
52.54	350	269		95	76
52.56	340	269	1.0427	84	67
52.58	330		1.0431	74	61
52.60	320	269	1.0436	63	37
52.62	—	269	1.0440	53	17
	310	270	1.0445	42	3
52.64	300	270	1.0449	32	-6
52.66	290	270	1.0454	21	-12
52.68	280	270	1.0458	11	-20
52.70	270	270	1.0463	0	-18
52.72	270	270	1.0467	0	-9
52.74	270	270	1.0471	0	-2
52.76	270	270	1.0476	Ō	3
52.78	270	270	1.0480	0	6
52.80	270	270	1.0485	Ō	10

ALPHA CURVE PEAK MAX = 51.9298 STD DEV = 0.1335 PEAK FIGURED FROM 51.72 TO 52.02 LINE CG = 51.8653 STD DEV = 0.0045 ALPHA 1 CURVE PEAK MAX = 51.8958 STD DEV = 0.2744 PEAK FIGURED FROM 51.68 TO 51.98 LINE CG = 51.8257 STD DEV = 0.0065

PUNCH PEAK FOR ALPHA = 51.92 SMOOTHING 4

ANGLE	INPUT	SMOOTH	2	SMOOTH	4	SMOOTH	6	SMOOTH	8
50+60	6		2		0		-0		-0
50.62	-4	-	·1		-1		-1		-1
50.64	-4	-	•3		-2		$-1^{-1}$		-1
50.66	6		1		2		2		2
50.68	-4		7		5		4		3
50.70	26		4		2		2		2
50.72	-24	-	·1		3		5		7
50.74	26	1	7		19		20		20
50.76	46	4	3		39		36		35
50.78	46	4	3		41		40		39
50.80	26	2	9		33		35		36
50.82	26	3	0		32		34		35
50.84	46	4	0		37		34		33
50.86	35	3	1		28		26		25

50.88	5	8	12	14	16
50.90	-5	10	12	13 25	14 25
50.92	56 15	29 40	26 42	41	41
50•94 50•96	66	54	53	52	51
50•98	66	57	55	54	54 57
51.00	35	50 64	54 65	56 66	67
51.02 51.04	65 96	85	82	81	80
51.06	75	91	91	89	88
51.08	106	88	87	88 84	88 84
51.10	65 86	80 83	82 83	83	82
51•12 51•14	96	87	84	82	82
51.16	75	81	83	84 9 <b>7</b>	85 98
51•18 51•20	85 126	91 120	94 118	117	116
51.22	136	137	132	129	127
51.24	136	128	128 126	128 130	128 132
51•26 51•28	106 156	122 149	150	152	153
51.30	187	191	187	185	184
51.32	228	215	213	212 226	210 225
51•34 51•36	207 248	224 236	225 235	235	236
51.38	248	251	251	251	251
51.40	268	278	279	280	28 <b>1</b> 326
51.42	340 360	323 380	324 381	325 381	380
51.44 51.46	452	439	435	432	429
51.48	483	474	471	471	471
51.50	483 575	502 5 <b>71</b>	510 574	514 576	517 576
51.52 51.54	657	652	643	637	633
51.56	698	685	680	677	675
51.58	688	700	708 782	714 787	718 790
51.60 51.62	760 923	775 905	899	895	893
51.64	1016	1014	1008	1004	1001
51.66	1088	1090	1095 1187	1097 1189	1097 1190
51.68 51.70	1170 1314	1184 1295	1291	1290	1289
51.72	1386	1394	1394	1393	1392
51.74	1489	1493	1496 1607	1497 1607	1498 1608
51•76 5 <b>1•7</b> 8	1613 1716	1607 1721	1720	1719	1719
51.80	1830	1825	1825	1824	1824
51.82	1912	1918	1917	1917 1999	1917 1999
51.84 51.86	2006 2058	1998 2069	1998 2071	2071	2072
51.88	2141	2133	2132	2131	2131
51.90	2173	2173	2172	2171 2187	2 <b>171</b> 2187
51•92 51•94	2184 2185	2187 218 <b>1</b>	2187 2180	2181	2181
51.96	2155	2156	2157	2159	2160
51.98	2114	2120	2123	2123	2122 2059
52.00	2074 1982	206 <b>9</b> 1971	2064 1969	206 <b>1</b> 1968	1969
52.02 52.04	1828	1844	1852	1858	1861
52.06	1726	1734	1736	1736	1736
52.08	1623 1376	1599 1373	1587 1369	1579 1365	1574 1363
52.10 52.12	1097	1114	1124	1130	1134
52.14	922	924	<b>9</b> 29	933	938
			20		

52.16	809	803	799	797	797
52.18	705	703	701	699	698
52.20	612	618	620	621	621
52.22	561	557	558	559	560
52.24	509	511	511	510	510
52.26	468	466	465	465	464
52.28	416	415	414	413	412
52.30	354	356	356	356	356
52.32	302	300	300	301	302
52.34	250	255	257	258	259
52.36	230	228	228	228	228
52.38	209	206	205	204	203
52.40	178	180	180	180	180
52.42	157	156	156	157	157
52.44	136	138	138	138	139
52.46	126	125	125	125	125
52.48	115	115	115	115	115
52.50	105	105	105	105	105
52.52	95	95	95	95	95
52.54	84	84	84	84	84
52.56	74	74	74	74	74
52.58	63	63	63	63	63
52.60	53	<b>5</b> 3	53	53	53
52.62	42	42	42	42	42
52.64	32	32	32	32	32
52.66	21	21	21	21	21
52.68	11	10	10	10	10
52.70	0	2	2	3	3
52.72	0	-0	-0	-0	-0
52.74	0	-0	-0	-1	-1
52.76	0	0	0	-0	-0
52.78	0	0	0	0	0
52.80	0	0	0	0	0

## Punched Card Output For "UNFOLD"

2187	• 2180.	2157.	2123.	2064.	1969.	1852.	1736.	1587.	1369.
1124	• 929•	799.	701.	620.	558.	511.	465.	414.	356.
300	• 257•	228.	205.	180.	156.	138.	125.	115.	105.
95	• 84•	74.		53.	42.	32.	21.	10.	2.
-0	• -0.	0.	0.	0.					
2187	• 2172•	2132.	2071.	1998.	1917.	1825.	1720.	1607.	1496.
1394	• 1291.	1187.	1095.	1008.	899.	782.	708.	680.	643.
574	• 510.	471.	435.	381.	324.	279.	251.	235.	225.
213	• 187.	150.	126.	128.	132.	118.	94.	83.	84.
83	. 82.	87.	91.	82.	65.	54.	55.	53.	42.
26	• 12•	12.	28.	37.	32.	33.	41.	39.	19.
3	• 2•	5.	2.	-2.	-1.	0.			

#### 9. Program Listing

The listing which follows includes two versions on the subroutine "ANG", one for the two phase Fe-Ni alloys and one for Ag. Of course, only one version should appear in the program deck. The program has been written in FORTRAN. PROGRAM PREP DIMENSION Y(300), Y1(300), YC(300),NS(10) COMMON X(300), B(300), C(300), N DOUBLE PRECISION PK, PK1, CG, CG1, SDPK, SDPK1, SDCG, SDCG1 111 READ 6 IF (EOF,60) 999,100 READ 2, N,AI,AINC,APK,V,FN,IG 100 READ 1, IPUN, NP, NUMP IF (IPUN-2) 121,120,121 READ 1, (NS(I), I=1,NP) 120 DO 101 J=1,N 121 X(J) = AI + (J-1)\*AINC101 READ 3, R1,R2 READ 4, (Y(J), J=1,N) CALL BACK(Y,A,Z,D) CALL ANG(IG, V, FN) CALL RACH(Y,Y1,APK,A1) CALL CENTROID(Y,CG,SDCG,A,Z,D) CALL CENTROID(Y1,CG1,SDCG1,A,Z,D)

CALL PEAK(Y, PK, SDPK, R1, R2) NN = XFIXF((PK - A1\*360./3.1415927)/AINC) R3 = R1 - NN\*AINC R4 = R2 - NN\*AINCCALL PEAK(Y1, PK1, SDPK1, R3, R4) DO 103 J=1,N IF (APK-X(J))103,102,103 NF = J102 GO TO 104 103 CONTINUE DO 105 J=1,N 104  $Y_1(J) = (Y_1(J) - B(J)) * C(J)$ YC(J) = (Y(J)-B(J))\*C(J)105 PRINT 14 PRINT 6 PRINT 7 PRINT 8, (X(J),Y(J),B(J),C(J),YC(J),Y1(J),J=1,N) PRINT 9, PK, SDPK PRINT 10, R1,R2 PRINT 11, CG,SDCG PRINT 12, PK1, SDPK1 PRINT 10, R3,R4 PRINT 11,CG1,SDCG1 IF (IPUN) 107,107,108 IF (IPUN-2) 110,109,109 108 CALL SMOOTH (YC, NUMP, NS, NP, NCEN) 109 GO TO 107 PP = AI + (NF-1)\*AINC 110 PRINT 13, PP DO 106 K=1,NF C(K) = YC(NF+1-K)106 PUNCH 5, (YC(J), J=NF,N) PUNCH 5, (C(J), J=1, NF)

#### GO TO 111 107 FORMAT (1015)

, 1

2	FORMAT (I10,5F10.2,I10)
3	FORMAT (2F10.2)
4	FORMAT (10F7.0)
5	FORMAT (10(F6.0, \$. \$))
6	FORMAT (50H
7	FORMAT (///3X,\$2 THETA\$,3X,\$REC CNT\$,6X,\$BACK\$,3X,\$ANG COR\$,5X,
	1\$ALPHA\$,3X,\$ALPHA 1\$/)
8	FORMAT (F10.2,2F10.0,F10.4,2F10.0)
9	FORMAT (///\$ ALPHA CURVE \$/\$ PEAK MAX = \$,F9.4/\$ STD DEV = \$.
	1F9.4)
10	FORMAT (1X, \$PEAK FIGURED FROM \$, F7.2, 2X, \$TO\$, F7.2)
11	FORMAT (/\$ LINE CG = \$, F9.4, \$ STD DEV = \$, F9.4)
12	
	1F9.4)
13	FORMAT (///1X, \$PUNCH PEAK FOR ALPHA = \$, F7.2)
14	FORMAT (/////)
999	

SUBROUTINE BACK (Y,A,Z,D)

BACKGROUND CALCULATION

C C C

200

```
COMMON X(300), B(300), C(300), N

DIMENSION Y(300)

A = (Y(1)+Y(2)+Y(3)+Y(4)+Y(5))/5.

Z = (Y(N-4)+Y(N-3)+Y(N-2)+Y(N-1)+Y(N))/5.

D = X(N) - X(1)

DO 200 J=1,N

B(J) = (Z-A)*X(J)/D + (A*X(N)-Z*X(1))/D

RETURN

END
```

SUBROUTINE ANG(IG, V, FN)

С		
C C C	ANGULAR CORRECTION - FOR FE-NI ALLOY SAMPLES AND CO RADIATION	
	COMMON X(300), B(300), C(300), N	
	PI = 3.1415927	
	DA = COS(31.2333*PI/180.)**2	
	DO 313 J=1.N	А
	SL = SIN((X(J)+V)*PI/360)/1.79021	
	IF (IG-1) 306,306,301	В
301	IF (SL-0.12) 302,302,303	
302	F = 10.142*SL-6.44*SL**2	_
	GO TO 311	C-FCC
303	IF (SL-0.35) 304,304,305	
304	F=1.0645004-1.4746725*SL+0.68002691*SL**2-0.53337307*SL**3	
		D-FCC
305	F=1.1781009-2.1006716*SL+1.4750092*SL**2-0.28333892*SL**3	E-ECC
	GO TO 311	E-FCC
306	IF (SL-0.12) 307,307,308	
307	$F = 1 \cdot - 0 \cdot 184 \cdot SL - 7 \cdot 08 \cdot SL \cdot 2$	C-BCC
	GO TO 311	
308	IF (SL-0.35) 309,309,310	
309	F=1.0637002-1.6056701*SL+0.86001593*SL**2-0.53335684*SL**3	D-BCC
	GO TO 311	
310	F=1.1987014-2.2833411*SL+2.0200144*SL**2-0.56667538*SL**3	E-BCC
311	A = SIN((X(J)+V)*PI/360)	

	BB = COS((X(J)+V)*PI/360)	F
	CC = SIN((X(J)+V)*PI/180)	•
	D = COS((X(J)+V)*PI/180)	
	$C(J) = (A^{**2})^{BB} (F^{*F*(1 + DA^{*}D^{**2})})$	~
	E = BB * BB * LOGF((1 + A)/BB)/A	G
	-5.5 $-5.5$ $-5.5$ $-5.5$ $-5.5$ $-5.5$ $-5.5$	H
	RM = (75.1*FN + 59.5*(1.1*FN/)*0.505 ABS = (1E)/(PI*RM)+CC/(2.*PI*RM*RM)+(25+.375*BB*BB*(1.+E))/	1
		I
	1(PI*RM**3)	
313	C(J) = C(J)/ABS	
	CN = C(1)	
	DO 312 J=1,N	
312	C(J) = C(J)/CN	
226	RETURN	
	END	

SUBROUTINE ANG(IG,V,FN)

C C	ANGULAR CORRECTION - FOR AG SAMPLES AND CO RADIATION	
С	COMMON X(200),B(200),C(200),N	
	$PI = 3 \cdot 1415927$	А
	$DA = COS(31 \cdot 2333 * PI/180 \cdot) * 2$	~
	00 313 J=1•N	в
	SL = SIN((X(J)+V)*PI/360)/1.79021	
306	IF (SL-0.12) 307,307,308	C
307	$F = 1 - 0.068 \times SL - 5.96 \times SL \times 2$	
- •	GO TO 311 IF (SL-0.35) 309,309,310	
308	IF (SL-0.35) 50995099510 F=1.0685171-1.2033810*SL-1.2685714*SL**2+3.06666667*SL**3	D
309	CO TO 211	-
310	F=1•2061-2•4973333*SL+2•805*SL**2-1•21666667*SL**3	E
311	A = SIN((X(J)+V)*PI/360)	
211	BB = COS((X(J)+V)*PI/360)	F
	CC = SIN((X(J)+V)*PI/180)	•
	D = COS((X(J)+V)*PI/180)	
	$C(J) = (A^{**2})^{*BB}/(F^{*}F^{*}(1 + DA^{*}D^{**2}))$	G
	$E = BB*BB*LOGF((1_{\bullet}+A)/BB)/A$	H
	RM = 130•14 ABS = (1•-E)/(PI*RM)+CC/(2•*PI*RM*RM)+(-•25+•375*BB*BB*(1•+E))/	I
		I
	1(PI*RM**3)	
313	C(J) = C(J)/ABS	
	CN = C(1) DO 312 J=1,N	
212	C(J) = C(J)/CN	
312	RETURN	
	END	
	SUBROUTINE RACH(Y,Y1,APK,P1)	
С		
С	RACHINGER SEPARATION - FOR CO RADIATION	
С		
	COMMON X(300), B(300), C(300), N	
	DIMENSION Y(300), Y1(300)	

P1 = 1.78892/1.79021\*SIN(APK\*3.1415927/360.) P2 = 1.79278/1.79021\*SIN(APK\*3.1415927/360.) P1 = ATAN(P1/SQRT(1.-P1\*\*2)) P2 = ATAN(P2/SQRT(1.-P2\*\*2)) D = (P2-P1)\*360./3.1415927

DO 606 I=2.N

24

A B

```
IF (X(I)-X(1)-D) 606,605,605
605
       DO 600 J=1,I
600
       Y1(J) = B(J)
       IA = I + 1
       GO TO 607
606
      CONTINUE
607
       IB = N - 1
      DO 603 J=IA .N
      DO 604 K=1,IB
      IF (X(K)-X(J)+D) 601,601,604
601
      IF (X(K+1)-X(J)+D) 604,604,602
602
      Z = ((Y1(K+1)-B(K+1))*C(K+1)-(Y1(K)-B(K))*C(K))/(X(K+1)-X(K))
     1*(X(J)-D)+((Y1(K)-B(K))*C(K)*X(K+1)-(Y1(K+1)-B(K+1))*C(K+1)*X(K))
     1/(X(K+1)-X(K))
      GO TO 608
604
      CONTINUE
608
      Y1(J) = (Y(J)-B(J))*C(J) - Z/2
      Y1(J) = Y1(J)/C(J) + B(J)
603
      RETURN
      END
      SUBROUTINE CENTROID(Y,CG,SDCG,A,Z,D)
С
```

```
С
      CENTROID CALCULATION
С
```

```
COMMON X(300), B(300), C(300), N
      DIMENSION Y(300)
      DOUBLE PRECISION S(6),P1
      DO 500 J=1,6
      S(J) = 0 \bullet
500
      P1 = 0.
      DO 501 J=1.N
      S(1) = S(1)+Y(J)*X(J)*C(J)
      S(2) = S(2) + (X(J) - X(1)) / D + C(J) + X(J)
      S(3) = S(3)+(X(J)-X(N))/D*C(J)*X(J)
      S(4) = S(4) + Y(J) * C(J)
      S(5) = S(5)+(X(J)-X(1))/D*C(J)
```

```
S(6) = S(6) + (X(J) - X(N)) / D * C(J)
      CG = (S(1)-Z*S(2)+A*S(3))/(S(4)-Z*S(5)+A*S(6))
      DO 502 J=1,N
502
      P1 = P1+Y(J)*(X(J)-CG)*(X(J)-CG)*C(J)*C(J)/(S(4)-Z*S(5)+A*S(6))/
     1(S(4) - Z * S(5) + A * S(6))
      SDCG = P1+A/5.*(S(3)-CG*S(6))*(S(3)-CG*S(6))/(S(4)-Z*S(5)+A*S(6))
     1/(S(4)-Z*S(5)+A*S(6))
      SDCG=SDCG+Z/5.*(CG*S(5)-S(2))*(CG*S(5)-S(2))/(S(4)-Z*S(5)+A*S(6))/
     1(S(4)-Z*S(5)+A*S(6))
      SDCG = DSQRT(SDCG)
      RETURN
```

```
END
```

501

С С

С

SUBROUTINE PEAK(Z, PK, SDPK, R1, R2)

PARABOLIC FIT TO PEAK MAX

```
COMMON X(300), BG(300), COR(300), N
DIMENSION A(99,3),B(99),C(3,3),D(3),R(200),Y(3),Z(300),E(3,3),
1 AA(3)
```

```
TYPE DOUBLE A, B, C, D, R, Y, AA, PK, SDPK
      DO 406 J=1.N
      IF (R1-X(J)) 403,403,406
      IR1 = J
403
      GO TO 411
      CONTINUE
406
       DO 404 J=IR1+N
411
       IF (R2-X(J)) 407,405,404
405
       IR2 = J
       GO TO 412
       IR2 = J-1
407
       GO TO 412
       CONTINUE
404
       NP = IR2 - IR1 + 1
412
       DO 401 I=IR1.IR2
       A(I-IR1+1,1) = 1.0
       A(I-IR1+1,2) = X(I)
       A(I-IR1+1,3) = X(I) * X(I)
       B(I-IR1+1) = (Z(I)-BG(I))*COR(I)
401
       D(1) = 0.0
       Y(1) = 0 \cdot 0
       SS=0.
       DO 1 I=1,NP
       SS=B(I)*B(I)+SS
       D(1) = A(I,1) * A(I,1) + D(1)
     1 Y(1)=A(I,1)*B(I)+Y(1)
       Y(1) = Y(1) / D(1)
       IR=0
       DO 5 K=2+3
DO 3 J=K+3
       IR=IR+1
       R(IR) = 0.0
       DO 2 I=1.NP
     2 R(IR)=A(I,K-1)*A(I,J)+R(IR)
       R(IR) = R(IR) / D(K-1)
       DO 3 I=1,NP
     3 A(I,J)=A(I,J)-A(I,K-1)*R(IR)
       D(K)=0.0
       Y(K) = 0 \cdot 0
       DO 4 I=1.NP
       B(I)=B(I)-A(I,K-1)*Y(K-1)
        Y(K) = A(I,K) * B(I) + Y(K)
     4 D(K)=A(I,K)*A(I,K)+D(K)
     5 Y(K)=Y(K)/D(K)
        DO 55 I=1+3
        AA(I)=Y(I)*D(I)**0.5
        SS=SS-AA(I)*AA(I)
        FN=NP-I
        IF(FN) 51,51,52
        SD = 0.
 51
        GO TO 53
 52
        SD=SQRT(SS/FN)
        DO 55 J=1+I
 53
     55 E(I,J)=SD
        IRS=-3
        DO 8 K=1,3
        IRS=IRS-K+4
        IR=IRS
        DO 8 JJ=1+K
        J=K=JJ+1
        C(K,J)=Y(J)
        IF(JJ-1) 8,8,6
      6 DO 7 I=2,JJ
        C(K,J)=C(K,J)-C(K,K-I+2)*R(IR)
```

```
26
```

	E(K,J)=E(K,J)+ABSF(R(IR)*E(K,K-I+2)) 7 IR=IR-1 8 IR=IR-3 +K
	PK = -C(3,2)/(2.*C(3,3)) SDPK = DSQRT((PK*E(3,2))/C(3,2))**2 + (PK*E(3,3)/C(3,3))**2 - 1 2*(PK**2)*E(3,2)*E(3,3)/C(3,2)/C(3,3))
	RETURN END
	SUBROUTINE SMOOTH (YC, NUMP, NS, NP, NCEN)
	DIMENSION $S(11,500), D1(500), D2(500), NS(10), YC(300)$ COMMON $X(300), B(300), C(300), NUM$ X1 = X(NCEN)
22	DO 22 N=1,NUM S(1,N+3) = YC(N) NUM = NUM + 3
20	DO 20 N=1,3 D2(N) = 0. D2(NUM+N) = 0.
5	D0 5 N=4,NUM D1(N) = S(1,N) K = 0
8	DO 12 I=1,NP J=NS(I) DO 9 N=4,NUM
9 6	$D_2(N) = D_1(N)$ K = K + 1 $D_0 7 L = 4.0 NUM$
7	D1(L)=(D2(L-3)-18*D2(L-2)+63*D2(L-1)+164*D2(L)+63*D2(L+1) 1-18*D2(L+2)+D2(L+3))/256* IF (K-J) 8,10,8
10 11	M = I + 1DO 11 N=4.0WMS(M.0) = D1(N)
12	CONTINUE IF (NUMP) 13,15,13
	NCEN = NCEN + 3 DO 18 N=1,NP IF (NUMP-NS(N)) 18,17,18
17 18	NUMP = N + 1 GO TO 19 CONTINUE
19	PUNCH $105$ , (S(NUMP,N), N=NCEN, NUM) M = NCEN - 3 DO 14 N=1, M
14	K = NCEN - N + 1 $D_2(N) = S(NUMP * K)$ PUNCH 105 * ( $D_2(N) * N = 1 * M$ )
15	NUMP = NUMP - 1 $PRINT 109, X1,NS(NUMP)$ $PRINT 107, (NS(N),N=1,NP)$
16	M = NP + 1 DO 16 N=4,NUM PRINT 108, X(N-3),(S(J,N),J=1,M)
105 107	FORMAT (10(F6.0,\$.\$)) FORMAT (////1X,\$ANGLE\$,5X,\$INPUT\$,3X,10(\$SMOOTH \$,12,1X))
108 109	FORMAT (1X,F7.2,11F10.0) FORMAT (//1X,\$PUNCH PEAK FOR ALPHA = \$,F7.2/1X,\$SMOOTHING\$,I3) END

 Appendix: Corrections Necessary When Using Other Radiations, Samples and Geometries.
 Specific program steps are referred to by the letter identification which appears

in the identification columns.

- A. Other radiations
  - In "ANG":

The value of the diffraction angle in the monochromator must be inserted into the calculation of DA (step A). In this case, for Co K $\alpha$  radiation and a quartz crystal,  $2\alpha = 31.2333^{\circ}$ . It is also necessary to use the K $\alpha$  wavelength to determine SL (step B); here  $\lambda = 1.79021$ Å.

In "RACH":

The values of the K $\alpha$ , K $\alpha_1$ , and K $\alpha_2$  wavelengths (i.e.,

 $\lambda$ ,  $\lambda_1$ , and  $\lambda_2$ ) are necessary to evaluate Pl and P2 (steps A and B) as follows:

$$P1 = \frac{\lambda}{\lambda} \sin \left[ APK \left( \frac{\pi}{360} \right) \right]$$
$$P2 = \frac{\lambda}{\lambda} \sin \left[ APK \left( \frac{\pi}{360} \right) \right]$$

B. Other samples

In "ANG":

The parameters of the power series fit to the atomic scattering factors must be used in steps C, D, and E. RM in step H is the factor  $\mu$  r in section 3 and must be evaluated as noted there.

C. Other geometries

In "ANG":

When no monochromator is used, DA (step A) should be set equal to one. For a flat sample, eliminate CC, E, and RM (steps F, G, and H respectively) and set ABS (step I) equal to one.

#### References

- C. P. Gazzara, J. J. Stiglich, Jr., F. P. Meyer, and A. M. Hansen, "A General Computer Program for Particle Size and Strain Analysis", in <u>Advances in X-ray Analysis</u>, Vol. 12, C. S. Barrett, J. B. Newkirk, and G. R. Mallett, Editors (Plenum Press, New York, 1969), p. 257.
- [2] R. J. De Angelis, "Evaluation from X-ray Diffraction Profiles of Fourier Coefficients and the Microstrain Distribution Function", in <u>Local Atomic</u> <u>Arrangements by X-ray Diffraction</u>, J. B. Cohen and J. E. Hillard eds. (Gordon and Breach Science Publishers, New York, 1966).
- W. Wallace, Automatic Separation of Strain and Particle Size Effects in Experimentally Observed X-ray Line Shapes, ASTIA Rept. # AD 686 311 (1968).
- [4] W. A. Rachinger, "A Correction for the  $\alpha_1 \alpha_2$  Doublet in the Measurement of Widths of X-ray Diffraction Lines", J. Sci. Instr. 25, 254, (1948).
- [5] B. D. Cullity, <u>Elements of X-ray Diffraction</u> (Addison-Wesley Publishing Co., Inc., Reading, Massachusetts, 1956), p. 172.
- [6] International Tables for X-ray Crystallography, Vol. III (Kynoch Press, Birmingham, England, 1962) pp 202f.
- [7] Cullity, Op. Cit., p. 188.
- [8] H. M. Otte, "Lattice Parameter Determinations with an X-ray Spectrogoniometer by the Debye-Scherrer Method and the Effect of Specimen Condition", J. Appl. Phys. 32, 1536 (1961).
- [9] H. M. Otte and A. L. Esquivel, "Measurement of Applied Stress by X-ray Diffraction", Mater. Sci. Res. 2, 121 (1965).
- [10] A. J. Bradley, "The Absorption Factor for the Powder and Rotating-Crystal Methods of X-ray Crystal Analysis", Proc. Phys. Soc. <u>47</u>, 879 (1935).
- [11] Cullity, Op. Cit., p. 466.
- [12] <u>Ibid.</u>, p 464.

- [13] E. R. Pike and A. J. C. Wilson, "Counter Diffractometer The Theory of the Use of Centroids of Diffraction Profiles for High Accuracy in the Measurement of Diffraction Angles", Brit. J. Appl. Phys. 10, 57 (1959).
- [14] J. B. Cohen and C. N. J. Wagner, "Determination of Twin Fault Probabilities from the Diffraction Patterns of fcc Metals and Alloys", J. Appl. Phys. <u>33</u>, 2073 (1962).
- B. E. Warren and E. P. Warekois, "Stacking Faults in Cold Worked Alpha-Brass", Acta Met. 3, 473 (1955).
- [16] Cullity, Op. Cit., p. 448.
- [17] A. Björk, "Solving Linear Least Squares Problems by Gram-Schmidt Orthogonalization", BIT (Nordisk tidskrift for informations-behandling)
   7, 1 (1967).
- [18] A. Björk, "Iterative Refinement of Linear Least Squares Solutions I", BIT 7, 257 (1967).
- F. M. Clikeman, A. J. Bureau, and M. G. Stewart, "Photoproton Reaction in Be<sup>9</sup>", Phys. Rev. 126, 1822 (1962).

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