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## OBSERVED PHASE-FRONT DISTORTION IN SIMULATED EARTH-TO-SPACE MICROWAVE TRANSMISSIONS

H. B. JANES AND M. C. THOMPSON, JR.

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## Eechnical Vote 339

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## OBSERVED PHASE-FRONT DISTORTION IN SIMULATED EARTH-TO-SPACE MICROWAVE TRANSMISSIONS

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# Observed Phase-Front Distortion in Simulated 

Earth-to-Space Microwave Transmissions
H. B. Janes and M. C. Thompson, Jr.

An experimental study has been made of the time and space statistics of the phase-front distortion of microwave signals sent from a ground terminal to an elevated terminal. These phase-front characteristics are important in systems involving phase measurements between a ground station and a moving air-borne or space terminal. To isolate atmospheric errors from random motion of the upper terminal, the latter was simulated by a series of mountaintop antenna arrays. Phase-front distortion was analyzed in terms of time variations in radio range on a single path and in first and second range differences from pairs of paths. The cross-correlations of (l) range variations on adjacent paths, and (2) range difference variations on both adjoining and separated pairs of paths are investigated, including the strong dependence of correlation on the portion of the power spectrum included in the data. The effect of the mountaintop terrain on the spatial homogeneity of the phase-front was examined and found to be insignificant. A diurnal pattern in the variance of 15 -minute range difference samples was observed, with minimum variance in the early morning hours. This pattern was not observed in the range variances, nor were the range and range difference variances significantly correlated with refractive index, air temperature, pressure or wind speed data at the lower terminal.

1. Introduction

A microwave signal transmitted through the troposphere is subjected to random retardations because of space and time variations in the atmospheric refractive index along the radio path. These retardations result in random variations of the phase-of-arrival of the signal, and are an important source of error in radio measurements of range and/or angular position.

Several experimental studies of range and range difference (angular position) variations caused by the atmosphere have been conducted over the past several years on slant paths to simulate ground-to-space transmissions [Norton, et al., 1961; and Janes and Thompson, 1964]. To minimize contamination of the data from geometric variations in range, these tests were all made on geometrically-stable paths with the upper terminal on a mountain.

Extension of these fixed-path data to the moving beam case in which the lateral movement of the upper terminal imparts a non-zero angular velocity to the propagation path requires a knowledge of the spatial statistics of the phase-of-arrival along the horizontal path of the moving upper terminal. In effect, the phase-front of a signal originating at the lower terminal will be distorted or "crinkled" by the time it arrives at the line of travel of the upper terminal and the time variability of the observed phase will be a function of the spatial wave-front statistics and the velocity of the upper terminal.

In June and July of 1964, the Central Radio Propagation Laboratory of the National Bureau of Standards ${ }^{* * *}$ performed an experiment under the sponsorship of the United States Air Force Avionics Laboratory ${ }^{* * * *}$ to study the time and space statistics of this elevated phase-front. In particular, the objective was to obtain a detailed statistical description of time and space variations in the phase-front to serve as a basis for predicting atmospheric errors in microwave range and/or angular position measurements involving a moving upper terminal.
*In this discussion, we assume for convenience that the signal is originating at the lower terminal and the phase is being observed at the upper terminal, but the transmitting and receiving roles could, of course, be interchanged without changing the results.
**On October 11, 1965, the CRPL was redesignated the Institute for Telecommunication Sciences and Aeronomy of the Environmental Science Services Administration.
*** Project 4108, Task 4108 02, D. O. AF (33-657) 63-391

The purpose of this report is to describe the experiment, the data obtained, and the results of the statistical analysis.

## 2. General Description of the Experiment <br> 2. 1 Propagation paths, antenna arrangements

In principle, the best experimental arrangement would have included a moving terminal (e.g., an aircraft or satellite) sweeping with a perfectly determined trajectory across the sky to measure the phase-front characteristics of a ground-based signal. However, this possibility was ruled out at the outset for compelling technological reasons. It was decided to substitute an array of fixed mountain-top antennas for the moving terminal, and make phase-of-arrival and phase-difference recordings at several points on the ar ray simultaneously. This arrangement, illustrated in figure 1 , isolates the purely atmospheric effects from the random motion of any practical airborne terminal and permits the collection of statistically large data samples of phase-front behavior.

The site chosen is on the Island of Maui, Hawaii, with propagation paths extending from a point 25 meters above sea level at the abandoned Puunene airport to an array of four antennas approximately 3000 meters above sea level at the summit of Mt. Haleakala. The paths were from 24.5 to 24.9 km in length and were tilted at an angle of 7 degrees from the horizontal. A map and terrain profile are shown in figures 2 and 3.

All phase measurements were made at a radio frequency of 9.4 GHz . Parabolic antennas 122 cm in diameter were used at both upper and lower sites. At the latter site the antenna was mounted 163 cm above ground and the upper antennas were mounted 91 cm above local terrain. In both cases, the antenna beams were sufficiently narrow to avoid ground reflections.

The phase measurement equipment used was a modification of a basic system described previously [Thompson and Vetter, 19587.

The experiment was divided into 9 "runs" or periods of continuous recording activity, each approximately 24 hours long. Each run was characterized by a particular arrangement of the 4 antennas at the upper site. The several arrangements were chosen to give as wide a variety of path separations as possible. Two basic configurations were used, and these are shown in a sketch in figure 4. Configuration A provided two pairs of adjacent paths, the antenna separation of one pair ( $A, C$ and $C, D)$ being twice that of the other ( $A, B$ and $B, C$ ). In addition, path pair A, D provided a separation twice that of $A, C$ and $C, D$. Configuration $B$ provided two path pairs with equal antenna separations, the pairs in turn being separated by various distances up to a maximum of 790 meters.

Table I gives the inclusive times and antenna ar rangement for each run. The "antenna locations" noted in the table refer to the positions of the four upper-site antennas in use in each run as identified by the circled numbers on the topographic map of the Haleakala site in figure 5 .

## 2. 2. Data Output

The principal data consist of continuous recordings of time variations of l) the phase-of-arrival of signals sent over one (and in some cases two) of the four paths in use at any one time, 2) the difference in the phase -of-arrival observed on pairs of paths, and 3) the second difference, or the difference of two phase difference variables observed on two pairs of paths.

Although these data were originally calibrated in terms of phase-of arrival at the radio frequency of 9.4 GHz , the results are discussed here in terms of variations in the apparent or radio path lengths, and their first and second differences, and will be referred to as range (R), range difference $(\Delta R)$, and second range difference ( $\Delta^{2} R$ ), respectively. This permits description of the phase front in terms of spatial deviations or "crinkling" of an imagined surface of constant phase.

The range and first and second range difference data were recorded as continuous variables on magnetic tape and on paper strip charts. The pass-band of the measuring and tape recording system extended from 0 to about 10 Hz . Some typical paper chart recordings of range and range difference are shown in figures 6, 7 , and 8.

Secondary data consisted of magnetic tape and paper chart recordings of atmospheric refractivity at 1.5 meters above ground at the lower site, paper chart recordings of wind speed and direction measured at 3.7 meters above ground at the upper site, and 6.4 meters above ground at the lower sites, and paper chart recordings of refractivity at 1.5 meters above ground at from 2 to 4 points on the upper antenna array. In addition, hourly or half-hourly readings of wet and dry bulb temperature and barometric pressure were taken at both sites. To record cloudiness, 35 mm pictures of the path were taken at both sites at hourly or half-hourly intervals.

## 3. Analysis of Results

The objective of the data analysis was to describe as completely as possible the time and space variability of the phase-front after being "crinkled" or distorted in its passage from the lower site to the mountaintop antenna array. In the analysis the time behavior of the phase-front observed at several points was first examined. The resulting time (and frequency) statistics were then used to study 1) the degree of spatial homogeneity of the data gathered along the phase-front, and 2) the spatial covariance of the phase (range) variable, $R$, and of its spatial differential, $\Delta R$. The correlations of these phase-front statistics with time of day and with several meteorological parameters were finally investigated.

The basic input to the analysis consisted of continuous data from 45 fifteen-minute sample periods -- 5 samples from each of the 9 runs. The only criteria used in selecting the samples were that all variables be free of recording defects and that the sample times be distributed as evenly as possible around the clock. Each sample was digitized at the rate of 25 to (in some cases) 30 points per second, giving a total of 22,000 to 27,000 discrete points per sample per variable. The basic output of the analysis consists of variances, power spectra and cross-correlation coefficients arranged to illustrate the statistical characteristics of the phase-front.

## 3. 1 The variance and power spectrum

A few preliminary comments on these statistics may be helpful in interpreting the results.

The power density spectrum (i.e., the Fourier cosine transform of the autocovariance function) is a widely-used statistical tool for analyzing the variability of a given quantity as well as the covariability of two quantities. It indicates the amount of variance (i.e., mean-squared deviation from the sample mean) contributed by the fluctuations lying in a given band of fluctuation frequencies. Its integral over all fluctuation frequencies is the total sample variance. In the case of discrete data, this relationship is given by

$$
s^{2}(X)=\frac{1}{n-1} \sum_{i=1}^{n}\left(X_{i}-\bar{X}\right)^{2}=\left[\frac{1}{2} W\left(f_{o}\right)+\sum_{j=1}^{m-1} W\left(f_{j}\right)+\frac{1}{2} W\left(f_{m}\right)\right] \Delta f,
$$

where $s^{2}(X)=$ sample variance of $X$, determined from $n$ values of $X$, $W\left(f_{j}\right)=$ power density (in units of variance per unit bandwidth) in a frequency band of width $\Delta f$ centered on $f_{j}$, and $m=$ number of non-zero frequencies at which $W(f)$ is estimated in a given computation. (In this analysis $\mathrm{m}=100$, although for graphical clarity, not all values are plotted.)

In the case of two variables, one can obtain the normalized cospectral density, i.e., the coefficient of cross-correlation of fluctuations occurring in the frequency increment $\Delta f$ centered on $f$. If $W_{1}(f), W_{2}(f)$, and $W_{(1-2)}(f)$ are the spectral densities of the two variables and of their difference, respectively, the normalized cospectral density is given by

$$
C(f)=\frac{W_{1}(f)+W_{2}(f)-W_{(1-2)}(f)}{2 \sqrt{W_{1}(f) W_{2}(f)}}
$$

If $W_{1}(f)=W_{2}(f)=W(f)$, a valid assumption in most cases discussed in this report, this simplifies to

$$
C(f)=1-\frac{W_{(l-2)^{(f)}}^{(f)}}{2 W(f)}
$$

In this report, most of the variance and correlation data are represented by two sets of values for each sample. One set of results, computed from the "raw" data, includes the entire pass-band of the input data from zero to 1.5 Hz or (in some cases) 1.25 Hz . (The two upper frequency limits resulted from a change-over to new digitizing equipment. Since it has no significant effect on the results, the upper limit is given simply as "approximately $1.4 \mathrm{~Hz} .{ }^{\prime \prime}$ ) The second set of values, labeled "approximately 0.007 to 1.4 Hz , " was obtained by integrating the power spectra over the specified frequency range, i.e., it consists of only that part of the total variance contributed by the frequency band covered by the computed power spectrum. This computation is analogous to passing the continuous data through an infinitely sharp band-pass filter. These "filtered" data variances are of interest because longer-term trends which often dominate the "raw" data have been, in effect, removed prior to the computation of variances, correlation coefficients, etc.

Examples of time variations in range as seen at one antenna are shown in figures 6, 7, and 8. (The abrupt shifts in level occurring whenever the trace nears either edge of the chart are the result of an automatic scale-shift device used to insure that the level stays within the range of the recorder while at the same time permitting maximum resolution.) The power spectra of all 15 -minute range data samples are plotted in figures 9 to 17 , inclusive. They are shown here to illustrate the wide variability in magnitude of spectral density. For example, the spectral density at 0.1 Hz ranges from about 0.2 to $3 \times 10^{-4} \mathrm{~cm}^{2} / \mathrm{Hz}$. On the other hand, the slope of the spectrum varies only slightly from sample to sample, and is approximately -2.5 , the same value that has been obtained repeatedly in previous experiments [Thompson, Janes and Kirkpatrick, 1960; Thompson and Janes, 1964; Janes, Kirkpatrick, Waters, and Smith, 1965]. (In this context, a slope of -2.5 means that the spectral density is proportional to $f^{-2.5}$.)

In these graphs, a distinction is made between day and night samples to illustrate any persistent diurnal effect. However, with the exception of run 2, no such effect was clearly seen. (The dependence of variance on time of day will be discussed in a later section.)

The curve in each figure joins median values and will serve as representative range spectra for comparison with other spectra.

Having examined the spectral characteristics of range variations at each of several locations, we find the next question to be investigated is whether these characteristics are influenced by the particular location of the upper terminal. The map in figure 5 illustrates the very rugged terrain over which the antennas were distributed on Mt. Haleakala, and it would not be unreasonable to ask if the phase-front structure was distorted by the local terrain. To illustrate the spatial homogeneity of
the phase-front, the range variances observed simultaneously at pairs of points on the array are compared in figure 18 . It can be seen that despite the wide range of variance levels, the variances are highly correlated on paths separated by as much as 790 meters. This suggests that if the mechanisms causing the range variations are influenced by the presence of the mountain, they are at least being influenced uniformly over the 800 -meter segment of the phase-front.

One of the most important characteristics of the phase-front is the so-called spatial correlation of range at an instant of time as a function of separation. In the absence of a continuous record of range versus position along the phase-front, this spatial correlation function can be estimated by the time cross-correlation of range variations observed at pairs of points as a function of separation.

Some caution must be exercised in making this estimation of spatial correlation from time correlation, however. This is because the coefficient of cross-correlation of time variations in range is a function not only of path separation but also of the spectral frequency pass-band over which the data are being examined. For example, figure 19 shows the correlation coefficients of range versus upper terminal separation, using first "raw" data (nominal pass-band 0 to 1.4 Hz ) and then the "filtered" data (using only the pass-band covered by the power spectra, i.e., about 0.007 to 1.4 Hz ). The line segments join median values of correlation at each separation. The necessity for specifying the data pass-band is obvious in this figure. It should also be borne in mind that the finite sample length itself acts as a high-pass filter in that it removes variance contributions from frequencies that are low compared to the reciprocal of the sample length. For example, if one-hour sample periods had been used instead of 15 minutes, the "raw" data correlations ( 0 to 1.4 Hz ) would have, in general, been higher than those shown.

The spectral distribution of correlation can be examined by comparing the power spectra of range ( $R$ ) and range difference ( $\Delta R$ ), as explained in section 3.1. This is done in figures 20,21 , and 22 , using the median spectra from the range spectrum graphs discussed previously, along with the corresponding median spectra of range difference data. (The individual $\Delta R$ spectra from which the latter were obtained are shown in figures 38 to 46 , inclusive.)

Keeping in mind that the extent to which the $\Delta R$ spectrum falls below twice the level of the $R$ spectrum is a measure of correlation of the two $R$ variables (section 3.1), two characteristics of phase-front variations are shown clearly in these figures. Firstly, the correlation of the two $R$ variables at a given separation decreases with increasing spectral frequency until a critical frequency is reached beyond which the $\Delta R$ spectral density is approximately equal to twice that of $R$, indicating a complete lack of correlation. (Because of random sampling errors and the use of median spectra, these spectral density relationships are only approximately fulfilled in these graphs.) Secondly, the minimum frequency above which the ranges are uncorrelated and the degree of correlation at any lower frequency are both inverse functions of path separation. Note, for example, that the range variations on paths separated by 1.25 meters (run 3, figure 20) are well correlated over the entire spectrum frequency range, 0.01 to about 1.5 Hz , while those at separations of 790 meters (run 6, figure 21) show no correlation whatever in the same two-decade band. At a separation of 10 meters (runs 1 and 2, figure 20) the critical frequency dividing correlated and uncorrelated regions appears to be about 0.1 Hz .

### 3.3 Range difference variations

An analysis somewhat analogous to the range analysis can be made of the range difference $(\Delta R)$ data, which represent time variations in the space differential of the phase-front. It was seen in connection with the correlation analysis in the previous section that the spectral density of $\Delta R$ at low frequencies decreases with decreasing path separation. The corresponding dependence of $\Delta R$ variance on path separation is shown in figure 23, where again the "raw" or total variances are compared to the "filtered" variances computed only for the frequency band covered by the spectra. It is not surprising that the latter process, which in effect removes low frequency trends from the data before computing the variance, produces a relatively larger reduction in variance at the large separations, where trends are more evident, than at the small separations. This effect shows up as a reduction in the slope of the points in the right-hand graph in figure 23.

It is interesting to note that if the deviation of the observed phasefront from a non-crinkled (free-space) phase-front could be depicted by a simple wedge-shaped distortion that prevailed over the whole phase-front, the points would fall on a line with slope of +2 . It is clear that the data in both graphs fail to conform to this simple model, and if the data had been filtered further to remove more low-frequency variance (e.g., by using shorter samples) the departure of the data from this model would have been even greater. This again emphasizes the caution that must be exercised in deriving spatial statistics from time data.

Figures 24,25 , and 26 show a comparison of pairs of range differ ence variances obtained simultaneously at different parts of the phasefront. As in the case of the range data, there appears to be good spatial homogeneity in the phase difference data. In other words, these graphs suggest that the $\Delta R$ data were not contaminated in any persistent way by local terrain features along the mountain top.

The question of correlation of range difference variations at different points on the phase-front is complicated by a spectral frequency dependence similar to that already observed in the range data. To illustrate this, a comparison is made in figure 27 of the power spectra of range differences $(\Delta R)$ and of the difference of two $\Delta R$ variables ( $\left.\Delta^{2} R\right)$, using medians of the individual spectra in both cases. Here again, correlation is indicated by the amount by which the $\Delta^{2} R$ spectrum falls below twice the $\Delta R$ spectrum (see section 3.1 ). In this figure all $\Delta R$ data were recorded on adjoining path pairs, i.e., one path was common to both pairs. The 1.25 - and 2.5-meter pairs in run 3 show high correlation at the lower frequencies, but none of the other pairs show definite correlation over this spectral frequency region, with the possible exception of the 10 -meter pair in run 1. Figure 28 shows a similar comparison for separated path pairs, and it is clear that the correlation is negligible over the entire two decades from $10^{-2}$ to 1 cycle per second.

The cross-correlation coefficients computed from the 15 -minute $\Delta R$ samples are plotted in figure 29 for both "raw" and "filtered" data. The abscissa is the separation of the path pairs, measured from their centers. Comparing these spatial correlation functions for $\Delta R$ with the corresponding graphs for the range data (figure 19), it can be seen that the $\Delta R$ correlations decrease more rapidly with increasing separation. It is also interesting to note that "filtering" the data has less effect on the range difference correlation function than on the range correlation functions. This is because the $\Delta R$ variances are not as dominated by low frequency contributions, and hence eliminating the latter before computing the correlation coefficient has relatively less effect on the result.

A significant feature of the range difference correlation functions is that the correlation is negligible for all spacings (between centers of path pairs) greater than about 20 meters, regardless of the antenna separation within each pair. (Note that for all spacings of 20 meters or less, the path pairs adjoin, i.e., one path was common to each pair.) It should be borne in mind that in general, reducing the sample length below the 15 minutes used here would reduce the correlation further. Since any system involving a moving air-borne or space terminal would probably have considerably less than 15 minutes available to make an angle determination from $\Delta R$ data, the correlations shown here are almost certainly higher than could be realized in an operational situation.

## 3. 4 Variances of $R$ and $\Delta R$ versus

## time of day and/or meteorological parameters

It has been evident throughout this investigation that the variances of the 15 -minute samples of range and range difference vary widely from sample to sample. Although this variability is to be expected in any sampling process, it should be determined how much of this variability in sample variances can be traced to a dependence on time of day or on various meteorological data. Any such dependence would be valuable in predicting periods of increased phase-front distortion.

In figure 30, the range variances of all 15 -minute samples are plotted versus time of day. As before, both "raw" and "filtered" data (pass bands: 0 to 1.4 and 0.007 to 1.4 Hz , respectively) are shown. Neither variance shows a clear-cut diurnal pattern, except for a slight reduction in the spread or range of variance values from about 0800 to 1400. In the case of the filtered data, there also appears to be a reduction in the variance level around 0600.

The corresponding range difference variances are plotted versus time of day in figures 31 and 32. Here a slightly more definite diurnal pattern can be seen. In both the raw data of figure 31 and the filtered data in figure 32, there is a tendency for the variances to increase gradually during the daylight hours, reach a maximum in late afternoon, and then subside slowly during the evening. For example, at the smaller separations (l. 25 to 10 meters) the average variance increases by a factor of about 10 from early morning to mid-afternoon.

The search for relationships between range or range difference variance and refractive index or other meteorological variables was considerably less fruitful. Since the radio range is proportional to the average refractive index along the path, the range variance might be expected to be proportional to the refractive index variance observed at a point on the path. To check this possibility, in figure 33, the range variances are compared to the corresponding variances of refractive index (expressed in refractivity (N) units) recorded at the lower site. It is clear from these graphs that no close relationship exists in these sample statistics.

Similarly, in figures 34 to 37 , inclusive, the range variances and the difference variances for three representative path separations are compared with air temperature, refractivity and wind speed observed at the upper and lower sites. The temperature and refractivity values were estimated by interpolation of the meteorological data read at half hour intervals at the upper site and hourly at the lower. The wind speeds were taken from the continuous anemometer recordings by visually estimating the average speed during each of the 15 -minute sample periods. (The data pass-bands noted in the figures refer, of course, only to the radio data.)

The purpose of the se graphs is to illustrate any obviously strong correlations. The number of data points available, especially in the case of the range differences, is too small to justify a sophisticated search for subtle correlations, especially since weak correlations would be of little value operationally. The strongest correlations appear to be between variance and wind speed at the lower site, and even these are not impressive. The correlation coefficients of the logarithm of variance versus wind speed in each case is listed below:

Radio data pass-band
Variable
Range
0 to 1.4 Hz
0.007 to 1.4 Hz $+0.42$
$+0.60$
Range Difference

| $5-$ meter path separation | +0.52 | +0.36 |
| ---: | :--- | :--- |
| $40-$ meter path separation | +0.21 | +0.56 |
| $750-790-$ meter path separation | +0.54 | +0.07 |

$$
40 \text {-meter path separation } \quad+0.21 \quad+0.56
$$

$$
750-790-\text { meter path separation } \quad+0.54 \quad+0.07
$$

## 4. Summary and Conclusions

In this experiment a study has been made of the statistical structure of the elevated phase-front of a ground-based microwave signal that has been distorted by propagation through the lower layers of the troposphere. Time statistics of phase-front variations (in terms of radio slant range and range difference) have been examined with the spacing of the several phase sensors along the phase-front as a parameter.

The principal results can be summarized as follows:

1. Although the antennas for the phase measurements at the upper site were mounted on very uneven terrain on a mountain summit, the results obtained at various points of the array indicated no significant bias as a function of sensor antenna location. Although it is probable that the presence of the mountain did have some effect on the data, it appears that any such effect was uniform over the entire segment of the
phase-front "seen" by the mountain-top array. Although the influence of the mountain is difficult to assess quantitatively, results obtained in a companion experiment at this site sponsored by the U. S. Air Force Electronic Systems Division lend support to a belief that such an influence was small in at least some respects. In the latter experiment a comparison was made of the refractive index profiles measured with an airborne refractometer in vertical ladder flights near the lower terminal as opposed to profiles from slant descent flights directly down the radio path. No systematic difference was found between these two types of profile, indicating that the mountain had no significant effect on long-term (e.g., hour-to-hour) changes in average refractive index along the radio path. Its effect on short-term phase statistics, however, is unknown.
2. The cross-correlation of range variations at separated points on the phase-front was investigated as a function of path separation. Although spatial correlation functions are shown, it is emphasized that the cross-correlation of range variations on two paths is not only a function of their separation but also of the sample length and the fluctuation frequency pass-band of the range data. For this reason, application to a particular system will require careful modification of these results to fit the effective pass-band of the system.
3. Similarly, the cross-correlation of range difference variations on both adjoining and separated pairs of paths was studied. It was found to drop off more rapidly with increasing separation than did the range data, although here again the spectral frequency dependence of the correlation was evident. Using 15-minute samples, the correlation of range difference variables was negligible when the distance between path pairs exceeded about 20 meters regardless of the path separation within each pair. Reducing the sample length further would, in general, have reduced the correlation at a given separation accordingly.
4. An analysis of the range and range difference variances of 15-minute samples revealed little or no significant dependence on several meteorological parameters (i.e., temperature, pressure, refractive index, wind speed at both terminals). The range variance was not found to be correlated with time of day or with the variance of refractive index observed at the lower terminal. On the other hand, the range difference variances (especially for small antenna separations) did show a definite diurnal pattern, with values during the afternoon hours on the order of 10 times larger than night-time values.

## 5. Appendix

In addition to the material discussed in preceding sections of this report, there were other data recorded and processed in the course of the experiment which are not discussed in detail here but which may prove helpful in further interpretation of the results, and are of interest from the standpoint of basic radio propagation research.

Figures 38 through 46 show the power spectra of all range difference samples, plotted to distinguish between day-time and night-time samples. The medians of these sample spectra, represented by the line through the points in each graph, were used in comparing range and range difference spectra in section 3.2 .

Figures 47 through 55 show long-term variations in range observed at one point on the phase-front along with refractivity and relative humidity computed from meteorological data taken at each site. The corresponding air temperature, pressure and wind velocity data are plotted in figures 56 through 64.

To show cloud activity during (or near) each of the day-time sample periods, the appropriate path photographs taken at each path terminal are shown in figures 65 through 73. The locations of upper and lower sites are indicated on figure 69.

Tables II through V list variances of range and first and second range differences computed from all of the 15 -minute sample periods. These tables include "raw" variances (pass-band: approximately 0 to 1.4 Hz ) computed directly from the digitized data, and "filtered" variances (pass-band: approximately 0.007 to 1.4 Hz ) computed by integrating the power spectra over that frequency range.

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Figure 1
location of propagation path used in maui experiment

Figure 2



CONFIGURATION ' $B$ ' (RUNS 4 THRU 9)


TABLEI
Schedule of Recording Periods

| Run | Period (local time) | Configuration | S | D | Antenna Locations |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 1000 June $29-1020$ June 30 | A | $10 . \mathrm{m}$ | - | $7,9,13,14$ |
| 2 | 1355 June 30-1415 July 1 | A | 2.5 | - | 9,11,12,13 |
| 3 | 1749 July 1 - 1645 July 2 | A | 1. 25 | - | 9, 10, 11, 12 |
| 4 | 0855 July 7 - 0811 July 8 | B | 40. | 105.m | 7,14,16,18 |
| 5 | 1302 July 9 - 1300 July 19 | B | 10. | 165. | $7,9,17,18$ |
| 6 | 0800 July 15-0615 July 16 | B | 185. | 605. | 1,5,7,18 |
| 7 | 1300 July 16 - 1630 July 17 | B | 90. | 660. | $1,4,6,15$ |
| 8 | 1528 July 21 - 1400 July 22 | B | 20. | 770. | 1, 3, 7, 13 |
| 9 | 1553 July 22 - 1500 July 23 | B | 5. | 785. | 1, 2, 7, 8 |



Figure 5

SAMPLE CHART RECORDINGS FROM RUN 1

RANGE



TWO RANGE DIFFERENCES - ANTENNA SEPARATION: 20 m


TWO RANGE DIFFERENCES - ANTENNA SEPARATION: 5 m


Figure 6


TWO RANGE DIFFERENCES - ANTENNA SEPARATION: 5 m


Figure 7

RANGE


RANGE DIFFERENCE - ANTENNA SEPARATION: 790 m


RANGE DIFFERENCE - ANTENNA SEPARATION: 185 m


## RANGE POWER SPECTRA <br> PUUNENE-HALEAKALA PATH

FIVE FIFTEEN-MINUTE SAMPLES FROM RUN 1


Figure 9

## RANGE POWER SPECTRA PUUNENE-HALEAKALA PATH

FIVE FIFTEEN - MINUTE SAMPLES FROM RUN 2


CYCLES PER SECOND
Figure 10

## RANGE POWER SPECTRA PUUNENE-HALEAKALA PATH

FIVE FIFTEEN-MINUTE SAMPLES FROM RUN 3


Figure 11

## RANGE POWER SPECTRA PUUNENE-HALEAKALA PATH

TEN FIFTEEN-MINUTE SAMPLES FROM RUN 4


## RANGE POWER SPECTRA PUUNENE-HALEAKALA PATH

TEN FIFTEEN-MINUTE SAMPLES FROM RUN 5


Figure 13

## RANGE POWER SPECTRA PUUNENE-HALEAKALA PATH

TEN FIFTEEN-MINUTE SAMPLES FROM RUN 6


Figure 14

## RANGE POWER SPECTRA PUUNENE-HALEAKALA PATH

## TEN FIFTEEN-MINUTE SAMPLES FROM RUN 7



## RANGE POWER SPECTRA PUUNENE-HALEAKALA PATH

TEN FIFTEEN-MINUTE SAMPLES FROM RUN 8


## RANGE POWER SPECTRA PUUNENE-HALEAKALA PATH

TEN FIFTEEN-MINUTE SAMPLES FROM RUN 9


Figure 17

COMPARISON OF RANGE VARIANCES ON ADJACENT PATHS (COMPUTED FROM 15-MINUTE SAMPLES)



Figure 18

CORRELATION OF RANGE VARIATIONS vs ANTENNA SEPARATION AT UPPER TERMINAL
(COMPUTED FROM 15-MINUTE SAMPLES)



Figure 19
COMPARISON OF RANGE AND RANGE DIFFERENCE SPECTRA PUUNENE - HALEAKALA PATH
$\triangle R$ : RANGE DIFFERENCE POWER SPECTRUM AT SEPARATION b


Figure 20
COMPARISON OF RANGE AND RANGE DIFFERENCE SPECTRA

Figure 21
comparison of range and range difference spectra PUUNENE - HALEAKALA PATH
$\triangle R$ : RANGE DIFFERENCE POWER SPECTRUM AT SEPARATION b
 CYCLES PER SECOND
Figure 22


Figure 23

COMPARISON OF RANGE DIFFERENCE VARIANCES
ON ADJOINING PAIRS OF PATHS
(COMPUTED FROM FIFTEEN-MINUTE SAMPLES)



Figure 24

COMPARISON OF RANGE DIFFERENCE VARIANCES
ON SEPARATED PAIRS OF PATHS
(COMPUTED FROM 15 -MINUTE SAMPLES)



Figure 25


Figure 26

POWER SPECTRA OF FIRST AND SECOND RANGE DIFFERENCES ON ADJOINING PAIRS OF PATHS
$\longrightarrow \Delta R$, SEPARATION b







Figure 27
power spectra of first and second range differences on separated pairs of paths
b = ANTENNA SEPARATION IN EACH PAIR d = DISTANCE BETWEEN PAIRS


CORRELATION OF RANGE DIFFERENCE VARIATIONS VS. SEPARATION OF PATH PAIRS
(COMPUTED FROM 15-MINUTE SAMPLES)



Figure 29



Figure 31

RANGE DIFFERENCE VARIANCE vS TIME OF DAY
(COMPUTED FROM 15 -MINUTE SAMPLES)
DATA PASS-BAND: APPROX. 0.007 TO 1.4 Hz



Figure 32


Figure 33

RANGE VARIANCE vs TEMPERATURE, REFRACTIVITY AND WIND SPEED
DATA PASS-BAND: $\quad 0$ TO APPROX. 1.4 Hz
$\times$ APPROX. 0.007 TO 1.4 Hz







Figure 34
RANGE DIFFERENCE VARIANCE vs
TEMPERATURE, REFRACTIVITY AND WINDSPEED

DATA PASS-BAND: $\begin{cases}0 & 0 \text { TO APPROX. } \\ \times & \text { APPROX. } 0.007 \mathrm{~Hz} \\ \text { TO } & 1.4 \mathrm{~Hz}\end{cases}$

N-UNITS ${ }^{240} \quad 260$

Figure 35
RANGE DIFFERENCE VARIANCE vs
TEMPERATURE, REFRACTIVITY AND WINDSPEED


DATA PASS-BAND:\{ $\left\{\begin{array}{l}0 \\ \times \\ \times \\ \text { APPROX. TO APPROX. } 1.4 \mathrm{~Hz} \\ \text { TO } \\ \hline 1.4 \mathrm{~Hz}\end{array}\right.$
( APPROX. 0.007 TO 1.4 Hz


$$
\underbrace{\circ}
$$



DEGREES, C

Figure 36
RANGE DIFFERENCE VARIANCE vs
TEMPERATURE, REFRACTIVITY AND WINDSPEED











RANGE DIFFERENCE POWER SPECTRA
PUUNENE-HALEAKALA PATHS


CYCLES PER SECOND

## Figure 39


cycles per second

 cycles per second

RANGE DIFFERENCE POWER SPECTRA
PUUNENE - HALEAKALA PATH
fifteen - minute samples from run 4
 PATHS
$\mathrm{a}, \mathrm{c}\left\{\begin{array}{l}\mathrm{x} \\ 0 \\ 0 \\ 0\end{array} 1800-1800-0600\right.$
PATH SEPARATION: 145 m










- 






 $++_{+}^{+}$ CYCLES PER SECOND

HLOIMONVB LINก/z WJ
RANGE DIFFERENCE POWER SPECTRA
PUUNENE - HALEAKALA PATH
fifteen - minute samples from run 5

RANGE DIFFERENCE POWER SPECTRA
PUUNENE - HALEAKALA PATH
fifteen - minute samples from run 6

RANGE DIFFERENCE POWER SPECTRA
PUUNENE - HALEAKALA PATH
FIFTEEN - MINUTE SAMPLES FROM RUN 7

RANGE DIFFERENCE POWER SPECTRA
puunene - haleakala path
FIFTEEN - MINUTE SAMPLES FROM RUN 8

RANGE DIFFERENCE POWER SPECTRA

## FIFTEEN - MINUTE SAMPLES FROM RUN 9



RANGE, REFRACTIVITY AND HUMIDITY DATA FROM RUN 1

|  |  |  |  |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
|  |  |  |  |  |  |  |  |



Figure 47

RANGE, REFRACTIVITY AND HUMIDITY DATA FROM RUN 2



RANGE, REFRACTIVITY AND HUMIDITY DATA FROM RUN 3

RANGE
"NO LONG-TERM RANGE DATA FOR RUN 3"


-68-

RANGE, REFRACTIVITY AND HUMIDITY DATA FROM RUN 4



RANGE, REFRACTIVITY AND HUMIDITY DATA FROM RUN 5


RANGE, REFRACTIVITY AND HUMIDITY DATA FROM RUN 6




RANGE, REFRACTIVITY AND HUMIDITY DATA FROM RUN 7

|  | RANGE |  | $1$ |  |
| :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  |
|  |  |  |  |  |
|  | $10 \mathrm{~cm}=4$ | 1 |  |  |
|  |  | \% |  |  |
|  |  |  |  |  |
|  | $V$ |  |  |  |



Figure 53

RANGE, REFRACTIVITY AND HUMIDITY DATA FROM RUN 8



Figure 54
-73-

RANGE, REFRACTIVITY AND HUMIDITY DATA FROM RUN 9




Figure 55

TEMPERATURE, PRESSURE AND WIND DATA FOR RUN I


Figure 56
temperature, pressure and wind data for run 2


Figure 57


Figure 58


Figure 59




Figure 60

TEMPERATURE, PRESSURE AND WIND DATA FOR RUN 6


Figure 61

TEMPERATURE, PRESSURE AND WIND DATA FOR RUN 7





Figure 62

TEMPERATURE, PRESSURE AND WIND DATA FOR RUN 8


Figure 63

TEMPERATURE, PRESSURE AND WIND DATA FOR RUN 9





Figure 64

## PATH PHOTOGRAPHS TAKEN AT TIMES INDICATED RUN I

ASSOCIATED SAMPLE

1-1
(JUNE 29, 1016-1031)
FROM LOWER SITE

FROM UPPER SITE



Figure 65

PATH PHOTOGRAPHS TAKEN AT TIMES INDICATED RUN 2

## ASSOCIATED

SAMPLE

FROM LOWER
SITE


## 2-4

(JULY I, 0531-0546)


Figure 66

PATH PHOTOGRAPHS TAKEN AT TIMES INDICATED RUN 3

## FROM LOWER SITE



3-4
(JULY 2, 0815-0830)
$3-5$
(JULY 2, 1238-1253)


Figure 67

## PATH PHOTOGRAPHS TAKEN AT TIMES INDICATED RUN 4 <br> FROM LOWER <br> SITE

## ASSOCIATED <br> SAMPLE



Figure 68


# PATH PHOTOGRAPHS TAKEN AT TIMES INDICATED 

 RUN 6

Figure 70

# PATH PHOTOGRAPHS TAKEN AT TIMES INDICATED 

 RUN 7

Figure 71

```
PATH PHOTOGRAPHS TAKEN AT TIMES INDICATED
RUN 8
FROM LOWER SITE
```

ASSOCIATED
SAMPLE

8-1
( JULY 21, 1550-1605


Figure 72

## PATH PHOTOGRAPHS TAKEN AT TIMES INDICATED

 RUN 9ASSOCIATED
SAMPLE

9-1
(JULY 22, 1629-164A)


Figure 73
$\Delta^{2} R a b, b c$

$$
1.49(-3)
$$

$$
\begin{aligned}
& 6.92(-4) \\
& 3.38(-4) \\
& 2.29(-4) \\
& 1.22(-4) \\
& 1.94(-4)
\end{aligned}
$$

Variances, in (cm) ${ }^{2}$, of Range and First and Second Range Difference Data
(Computed from 15 -minute samples; pass-band: 0 to approximately 1.4 Hz )

TABLE III
Variances, in $(\mathrm{cm})^{2}$, of Range and First and Second Range Difference Data (Computed from 15 -minute samples; pass-band: 0 to approximately 1.4 Hz )

| Sample No. | Date | Starting Time | R a | $\mathrm{R}_{\mathrm{c}}$ | $\Delta \mathrm{R}_{\text {ac }}$ | $\Delta \mathrm{R}_{\mathrm{ab}}$ | $\Delta \mathrm{R}_{\mathrm{cd}}$ | $\Delta^{2} R_{a b, c d}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 4-1 | 7/7/64 | 0930 | 1. 18 | 1.22 | 1. $16(-1)$ | -- | 8. $38(-3)$ | -- |
| 4-2 | 7/7/64 | 1350 | 6.63(-1) | 7. 29(-1) | 2. $86(-1)$ | 3.49(-2) | 9. $30(-2)$ | 1.07(-1) |
| 4-3 | 7/7/64 | 2015 | 2.88 | 1.67 | 2. $71(-1)$ | 4.73(-2) | 3.79(-2) | 8.77(-2) |
| 4-4 | 7/8/64 | 0000 | 8.01(-1) | 7.13(-1) | 1. $10(-1)$ | 2. $11(-2)$ | 2.63(-2) | 5.62(-2) |
| 4-5 | 7/8/64 | 0615 | 1.99 | 1.94 | 3. $77(-2)$ | $3.81(-2)$ | $5.78(-3)$ | -- |
| 5-1 | 7/9/64 | 1700 | 7.79(-1) | 9.41(-1) | 1. $87(-1)$ | 4.56(-3) | 5.01(-3) | 1.07(-2) |
| 5-2 | 7/9/64 | 2200 | 2. $32(-1)$ | 2.03(-1) | 2.00(-2) | 2. $54(-4)$ | 2.52(-4) | 5. 10(-4) |
| 5-3 | 7/10/64 | 0400 | 3.89(-1) | 3.90(-1) | 2.68(-2) | 2. 18(-4) | 2. $04(-4)$ | 4. $23(-4)$ |
| 5-4 | 7/10/64 | 0700 | 1.09(-1) | 1. $17(-1)$ | 2. $36(-2)$ | 1.18(-3) | 1.09(-3) | 2. $32(-3)$ |
| 5-5 | $7 / 10 / 64$ | 1100 | 2. 91 | 3.66 | 7.09(-1) | 6.55(-3) | 8.41(-3) | 1.31(-2) |
| 6-1 | 7/15/64 | 0830 | 1. 20 | 1.43 | 1.76 | 1.58(-1) | 4.28(-1) | 6.73(-1) |
| 6-2 | 7/15/64 | 1100 | 1.47 | 2.55 | 6.55(-1) | 2.04(-1) | 2.74(-1) | 5.61(-1) |
| 6-3 | 7/15/64 | 1500 | 3.08 | 2.73 | 1.94 | 6. $40(-1)$ | 5.94(-1) | 1. 26 |
| 6-4 | 7/15/64 | 2100 | 1. 54 | 1.83 | 2.99 | 8.88(-1) | 7.96(-1) | 1. 44 |
| 6-5 | $7 / 16 / 64$ | 0130 | 1.71 | 1.81 | 5.75(-1) | 1. $44(-1)$ | $3.23(-1)$ | 3. $30(-1)$ |
| 7-1 | 7/16/64 | 1800 | 1.52 | 1.81 | 2. 26 | 5.58(-1) | 3.64(-1) | 1. 16 |
| 7-2 | 7/17/64 | 0000 | 9.67(-1) | 7.19(-1) | 2.49(-1) | 9.60(-2) | 1. $18(-1)$ | 2.78(-1) |
| 7-3 | $7 / 17 / 64$ | 0500 | 2.04(-1) | 1. $22(-1)$ | 2.85(-1) | 1.33(-2) | 8. $26(-3)$ | 1. $84(-2)$ |
| 7-4 | 7/17/64 | 1130 | 6.02(-1) | 2.42 | 2.72 | 8.23(-1) | 3.91(-1) | 1.61 |
| 7-5 | $7 / 17 / 64$ | 1500 | 2. 50 | 2.63 | 2.73(-1) | 1.07(-1) | 3. $18(-2)$ | 1. $37(-1)$ |
| 8-1 | 7/21/64 | 1550 | 1. $07(+1)$ | 1.05(+1) | 1.86 | 1.70(-2) | 2. $17(-2)$ | 1.68(-1) |
| 8-2 | 7/21/64 | 2015 | 8.03(-1) | 5.25(-1) | 5.15(-1) | 8.26(-3) | 7. 12(-3) | 1.64(-2) |
| 8-3 | $7 / 22 / 64$ | 0100 | 1.09 | 1.39 | 1.57 | 2. $32(-2)$ | 7.84(-3) | 3.07(-2) |
| 8-4 | 7/22/64 | 0530 | 1.23 | 1.25 | 1.04(-1) | 8.83(-4) | -- | 2. $10(-3)$ |
| 8-5 | $7 / 22 / 64$ | 1003 | 6.09 | 7.63 | 2. 14 | 1. $26(-2)$ | 1.55(-2) | 2. $80(-2)$ |
| 9-1 | 7/22/64 | 1629 | 9.25(-1) | 9.49(-1) | 1.98 | 2. $64(-3)$ | 2. $26(-3)$ | 5.63(-3) |
| 9-2 | 7/22/64 | 2100 | 1. 16 | 1.41 | 6.02(-1) | 1.26(-3) | 2. $47(-3)$ | 3.45(-3) |
| 9-3 | 7/23/64 | 0145 | 2.09(-1) | 1.42(-1) | 2. $90(-1)$ | 2. 16(-4) | 4.79(-4) | 6. $16(-4)$ |
| 9-4 | $7 / 23 / 64$ | 0615 | 1.08(-1) | 1.56(-1) | 1. $20(-1)$ | 2.57(-4) | 2. $63(-4)$ | 5.02(-4) |
| 9-5 | $7 / 23 / 64$ | 1120 | 2. 36 | 2. 87 | 3.00(-1) | 6. $43(-4)$ | 4.53(-4) | 1.47(-3) |

numbers in parentheses indicate powers of 10 , i.e., $3.25(-2)=3.25 \times 10^{-2}$.
TABLE IV
of Range and First and Second Range Difference Data 2

| Sample No. | Date | Starting Time | $R_{a}$ | $\Delta \mathrm{R}_{\mathrm{ad}}$ | $\Delta \mathrm{R}_{\mathrm{ac}}$ | $\Delta R_{c d}$ | $\Delta \mathrm{R}_{\mathrm{ab}}$ | $\Delta R_{b c}$ | $\mathrm{R}_{\mathrm{ac}, \mathrm{~cd}}$ | $\Delta^{2} R_{a b, b c}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1-1 | 6/29/64 | 1016 | 3.25(-2) | 1.29(-2) | ) $4.10(-3)$ | 4.67(-3) | ) $1.40(-3)$ | 1. $54(-3)$ | 7.72(-3) | 1. $52(-3)$ |
| 1-2 | 6/29/64 | 1418 | 2. $36(-2)$ | 2.68(-2) | ) $1.31(-2)$ | 1.02(-2) | ) $4.77(-3)$ | 4.84(-3) | 2. $44(-2)$ | 6.82(-3) |
| 1-3 | 6/29/64 | 1815 | 1.116(-2) | 4.66(-3) | ) $2.54(-3)$ | 2. $27(-3)$ | ) $1.15(-3)$ | 8.38(-4) | 5.02(-3) | 1.70(-3) |
| 1-4 | $6 / 29 / 64$ | 2215 | 9.55(-3) | 1.89(-3) | ) $8.02(-4)$ | 1.23(-3) | ) $3,16(-4)$ | 5. $19(-4)$ | 1.64(-3) | 4.36(-4) |
| 1-5 | $6 / 30 / 64$ | 0215 | 9.33(-3) | 1.64(-3) | ) $5.88(-4)$ | 5. $97(-4)$ | ) 2.06(-4) | 1. $88(-4)$ | 7.80(-4) | 2.02(-4) |
| 2-1 | $6 / 30 / 64$ | 1452 | 7.87(-2) | 1. $44(-2)$ | ) $4.24(-3)$ | 3.89(-3) | ) $1.25(-3)$ | 1.27(-3) | 3.69(-3) | 8.68(-4) |
| 2-2 | 6/30/64 | 1930 | 1.58(-2) | 4.44(-3) | ) $8.39(-4)$ | 8. $14(-4)$ |  | 3.00(-4) | 1.19(-3) | 3.86(-4) |
| 2-3 | $7 / 1 / 64$ | 0000 | 6.95(-3) | 2.02(-3) | ) $2.47(-4)$ | 2. $02(-4)$ | ) 6.05 (-5) |  |  | 2.09(-4) |
| 2-4 | $7 / 1 / 64$ | 0531 | 7.89(-3) | 3.94(-4) | ) $2.50(-4)$ | 1.58(-4) | ) $6.87(-5)$ | 1. 19(-4) |  | 1. $29(-4)$ |
| 2-5 | $7 / 1 / 64$ | 1001 | $3.66(-2)$ | 1. $56(-3)$ | ) $7.92(-4)$ | 4. $10(-4)$ | ) $1.51(-4)$ | 1.69(-4) | 5.08(-4) | 1.70(-4) |
| 3-1 | 7/1/64 | 1800 | 1.74(-1) | 4.08(-3) | ) $4.63(-4)$ | 4.32(-4) | ) $1.53(-4)$ | 1. $05(-4)$ | 2. $37(-4)$ | 5.63(-5) |
| 3-2 | $7 / 1 / 64$ | 2230 | 4.56(-1) | 2. $43(-3)$ | ) $7.09(-4)$ | $6.44(-4)$ | ) 2. $26(-4)$ | 1.69(-4) | 3.12(-4) | 5.84(-5) |
| 3-3 | $7 / 2 / 64$ | 0315 | 6. $14(-2)$ | 2.81(-4) | ) $9.74(-5)$ | 9.06(-5) | ) $3.38(-5)$ | $2.47(-5)$ | $6.87(-5)$ | 1.48(-5) |
| 3-4 | $7 / 2 / 64$ | 0815 | 3. $45(-2)$ | 1.62(-4) | ) $6.03(-5)$ | 4.96(-5) | ) $2.43(-5)$ | 2. $34(-5)$ | 9.37(-5) | 1.85(-5) |
| 3-5 | $7 / 2 / 64$ | 1238 | 5.10(-2) | 2. 19(-3) | ) $6.45(-4)$ | 6. $15(-4)$ | ) 2. $21(-4)$ | 1. 50(-4) | 5. $16(-4)$ | 1.32(-4) |

## TABLE V

Variances, in $(\mathrm{cm})^{2}$, of Range and First and Second Range Difference Data
(Computed from 15 -minute samples; pass-band: approximately 0.007 to 1.4 Hz )

| Sample <br> No. | Date | Starting Time | R ${ }_{\text {a }}$ | $\mathrm{R}_{\mathrm{c}}$ | $\Delta \mathrm{R}{ }_{\mathrm{ac}}$ | $\Delta \mathrm{R}_{\mathrm{ab}}$ | $\Delta \mathrm{R}_{\mathrm{cd}}$ | $\Delta^{2} R_{a b, c d}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 4-1 | 7/7/64 | 0930 | 2. $04(-2)$ | 1.69(-2) | 9. 26 (-3) | 9.60(-3) | 2. $58(-3)$ |  |
| 4-2 | 7/7/64 | 1350 | 3.72(-2) | 3.15(-2) | 5.09(-2) | 1.52(-2) | 2. $90(-2)$ | 3.78(-2) |
| 4-3 | 7/7/64 | 2015 | 4.41(-2) | 4.02(-2) | 5.87(-2) | 2.96(-2) | 1.87(-2) | 4.83(-2) |
| 4-4 | 7/8/64 | 0000 | 2.02(-2) | 2. $22(-2)$ | 2. 46 (-2) | 1.53(-2) | 1.33(-2) | 3.14(-2) |
| 4-5 | 7/8/64 | 0615 | 6.17(-3) | 6. $57(-3)$ | 4.43(-3) | 3.91(-3) | 1.80(-3) |  |
| 5-1 | 7/9/64 | 1700 | 5. 29(-2) | 4.83(-2) | 6.07(-2) | 3.38(-3) | 4.38(-3) | 7.45(-3) |
| 5-2 | 7/9/64 | 2200 | 3.32(-3) | 2.60(-3) | 4.80(-3) | 2.12(-4) | 2. $28(-4)$ | 4.63(-4) |
| 5-3 | 7/10/64 | 0400 | 4.15(-3) | 2.79(-3) | 3.76(-3) | 1.83(-4) | J. 52(-4) | 3.56(-4) |
| 5-4 | 7/10/64 | 0700 | 8.64(-3) | 7.38(-3) | 1.12(-2) | 1.10(-3) | 1.09(-3) | 2.51(-3) |
| 5-5 | 7/10/64 | 1100 | 4.46(-2) | 3.90(-2) | 3. $20(-2)$ | 2.62(-3) | 5. $30(-3)$ | 8.86(-3) |
| 6-1 | 7/15/64 | 0830 | 6. 23(-2) | 1.02(-1) | 1.30(-1) | 4.38(-2) | 1.05(-1) | 1.62(-1) |
| 6-2 | 7/15/64 | 1100 | 4.69(-2) | 5.90(-2) | 1.23(-1) | 7.87(-2) | 9.49(-2) | 1.95(-1) |
| 6-3 | 7/15/64 | 1500 | 3.44(-1) | 2. 22(-1) | 4.90(-1) | 2.67(-1) | 2.63(-1) | 4.36(-1) |
| 6-4 | 7/15/64 | 2100 | 4.43(-1) | 3.44(-1) | 8.58(-1) | 5.62(-1) | 4.65(-1) | 9.12(-1) |
| 6-5 | 7/16/64 | 0130 | 5.65(-2) | 7.64(-2) | 1.65(-1) | 1.03(-1) | 1.21(-1) | 2. $26(-1)$ |
| 7-1 | 7/16/64 | 1800 | 6.47(-2) | 4.36(-2) | 1.05(-1) | 1.05(-1) | 4.38(-2) | 1.63(-1) |
| 7-2 | 7/17/64 | 0000 | 2. 54(-2) | 2.13(-2) | 3.98(-2) | 2.40(-2) | 2.94(-2) | 5.61(-2) |
| 7-3 | 7/17/64 | 0500 | 3.45(-3) | 1.64(-3) | 4.84(-3) | 1.15(-3) | 1.15(-3) | 2. 19(-3) |
| 7-4 | 7/17/64 | 1130 | 5.41(-2) | 7.02(-2) | 1.50(-1) | 8.40(-2) | 7.92(-2) | 2. 12(-1) |
| 7-5 | 7/17/64 | 1500 | 2. $34(-2)$ | 2.81(-2) | 4.00(-2) | 1.52(-2) | 9. $50(-3)$ | 2. $47(-2)$ |
| 8-1 | 7/21/64 | 1550 | 8.73(-2) | 6. $57(-2)$ | 1.47(-1) | 1.37(-2) | 9. $31(-3)$ | 2.61(-2) |
| 8-2 | 7/21/64 | 2015 | 4.44(-2) | 4.74(-2) | 7.46(-2) | 8.13(-3) | 5.97(-3) | 1.54(-2) |
| 8-3 | 7/22/64 | 0100 | 1.20(-1) | 4.91(-2) | 1.04(-1) | 1.90(-2) | 5. $21(-3)$ | 2. $34(-2)$ |
| 8-4 | 7/22/64 | 0530 | 9. $86(-3)$ | 6.83(-3) | 1.65(-2) | 6.38(-4) | -- | 1.37(-3) |
| 8-5 | 7/22/64 | 1003 | 8.17(-2) | 5.31(-2) | 1. $50(-1)$ | 6. $30(-3)$ | 8.59(-3) | 1.79(-2) |
| 9-1 | 7/22/64 | 1629 | 8.06(-2) | 7. 20(-2) | 1.31(-1) | 2. 17(-3) | 1.70(-3) | 3.89(-3) |
| 9-2 | 7/22/64 | 2100 | 4.45(-2) | 6. $32(-2)$ | 9.74(-2) | 1.17(-3) | 2.65(-3) | 3.58(-3) |
| 9-3 | 7/23/64 | 0145 | 9.43(-3) | 1.29(-2) | 2.00(-2) | 1. $84(-4)$ | 4.75(-4) | 6.35(-4) |
| 9-4 | 7/23/64 | 0615 | 4.80(-3) | 8. $10(-3)$ | 1.18(-2) | 2. $30(-4)$ | 2. $69(-4)$ | 4.85(-4) |
| 9-5 | 7/23/64 | 1120 | 9.52(-3) | 9.75(-3) | 1.61(-2) | 3.70(-4) | 2. $98(-4)$ | 7.60(-4) |

numbers in parentheses indicate powers of 10 , i.e., $3.25(-2)=3.25 \times 10^{-2}$.
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[^0]:    * Located at Boulder, Colorado 80301.
    * Located at 5285 Port Royal Road, Springfield, Virginia 22171.

[^1]:    * Formerly the Central Radio Propagation Laboratories of the National Bureau of standards. CRPL was transferred to ESSA in October, 1965 but will continue to use NBS publications series pending inauguration of their own.

[^2]:    For sale by the Superintendent of Documents, U. S. Government Printing Office
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