# ◇ NBS ◇

# *Technical Note* 188

# CALIBRATION OF VOLT-AMPERE CONVERTERS

E. S. WILLIAMS

U. S. DEPARTMENT OF COMMERCE
NATIONAL BUREAU OF STANDARDS

# THE NATIONAL BUREAU OF STANDARDS

## Functions and Activities

The functions of the National Bureau of Standards are set forth in the Act of Congress, March 3, 1901, as amended by Congress in Public Law 619, 1950. These include the development and maintenance of the national standards of measurement and the provision of means and methods for making measurements consistent with these standards; the determination of physical constants and properties of materials; the development of methods and instruments for testing materials, devices, and structures; advisory services to government agencies on scientific and technical problems; invention and development of devices to serve special needs of the Government; and the development of standard practices, codes, and specifications. The work includes basic and applied research, development, engineering, instrumentation, testing, evaluation, calibration services, and various consultation and information services. Research projects are also performed for other government agencies when the work relates to and supplements the basic program of the Bureau or when the Bureau's unique competence is required. The scope of activities is suggested by the listing of divisions and sections on the inside of the back cover.

## Publications

The results of the Bureau's research are published either in the Bureau's own series of publications or in the journals of professional and scientific societies. The Bureau publishes three periodicals available from the Government Printing Office: The Journal of Research, published in four separate sections, presents complete scientific and technical papers; the Technical News Bulletin presents summary and preliminary reports on work in progress; and the Central Radio Propagation Laboratory Ionospheric Predictions provides data for determining the best frequencies to use for radio communications throughout the world. There are also five series of nonperiodical publications: Monographs, Applied Mathematics Series, Handbooks, Miscellaneous Publications, and Technical Notes.

A complete listing of the Bureau's publications can be found in National Bureau of Standards Circular 460, Publications of the National Bureau of Standards, 1901 to June 1947 ($1.25), and the Supplement to National Bureau of Standards Circular 460, July 1947 to June 1957 ($1.50), and Miscellaneous Publication 240, July 1957 to June 1960 (includes Titles of Papers Published in Outside Journals 1950 to 1959) ($2.25); available from the Superintendent of Documents, Government Printing Office, Washington 25, D.C.

# NATIONAL BUREAU OF STANDARDS

## *Technical Note 188*

### ISSUED APRIL 25, 1963

## CALIBRATION OF VOLT-AMPERE CONVERTERS

E. S. Williams

Calibration of Volt-Ampere Converters

E. S. Williams

These notes have been prepared to describe the National
Bureau of Standards calibration services for volt-ampere con-
verters (or transfer volt-ammeters), to suggest procedures
for d-c standardization in the user's laboratory, and to de-
scribe a voltage comparator which can be used to make such
calibrations quickly and easily.

1.  General

A volt-ampere converter, shown schematically in figure 1, incorporates

a thermoelement connected in series with a resistive multiplier for alter-

nating voltage measurements or in parallel with a shunt for alternating

current measurements.  (Multi-range switching is not shown in the figure.)

With alternating current applied to the heater of the thermoelement, the

output emf of the thermocouple is balanced against an adjustable internal

d-c source as indicated by a null on a galvanometer.  (This is usually

called the No. 1 or A-C balance).  The heater is then switched to a second

internal d-c source which is adjusted to give the same thermocouple emf.

(This is the No. 2 or D-C balance).  The direct voltage, $V_t$, is then

measured with a suitable potentiometer.  The alternating input voltage or

current is equal to the output voltage ($V_t$) multiplied by a simple factor,

usually shown directly on the dial of the range switch.  The basic equa-

tions [1 and 2][1] are shown in figure 1.  More complete diagrams and additional

information are given in the references.

A modification of this arrangement uses a decade multiplier or decade

[1]Figures in brackets indicate the literature references on page 14.

shunt, with a two-coil milliammeter as an error indicator, as shown in simplified form for voltage measurements in figure 2.[2] The torques of the two milliammeter coils are in opposition, and the second coil is energized by a zener diode reference-voltage source. When balances of the galvanometer are obtained in the A and then the B positions, by adjusting d-c supplies 1 and 2 respectively, the error indicator shows directly the percent difference between the input voltage or current and the quantity indicated by the setting of the decade multiplier or shunt dials of the converter.

Volt-ampere converters are normally standardized at NBS only to determine their ac-dc differences. These differences depend on the reactances of the measuring circuit and normally increase with frequency. Determinations are therefore usually made only at the highest rated frequency. Because the differences are small and relatively permanent in a well-designed and well-constructed instrument, they ordinarily need to be redetermined only if the instrument is altered or damaged. However, for additional assurance, it is recommended that the ac-dc tests be repeated at intervals of not less than five years, if the converter is to be used in the upper part of its frequency range. The ac-dc differences are not affected appreciably by ordinary changes in laboratory temperature or changes in applied voltage or current on a given range.

---

[2] An instrument of this type has been built by the Sensitive Research Instrument Corporation, 310 Main Street, New Rochelle, New York, and is described in their house organ, "Electrical Measurements," 28, No. 5, May 1961.

For these reasons, only periodic d-c calibrations should be necessary to verify the continued accuracy of a volt-ampere converter in service. These periodic d-c calibrations can, in most cases, be made in the user's own laboratory. This is an important advantage of this type of instrument, because the accuracy of a-c measurements can be maintained with relatively simple d-c calibration techniques. A calibrated potentiometer is a necessary accessory to the instrument and must be at hand; the only additional calibrated equipment needed is a shunt box and a volt box. Normally these would be readily available in an instrument-testing laboratory. Alternatively, the voltage comparator described in these notes will save time and effort.

It is recommended that d-c tests be made at rated voltage or current on each range and at 50 percent of rated value on the highest and lowest ranges, at intervals of 6 to 12 months for normal service. The d-c correction thus determined is practically independent of voltage or current level on a given range if the design of the converter includes compensation ($R_m'$ and $R_s'$) for the resistance of the heater of the thermo-element which does depend on the applied current.

2. Potentiometer Method for Volt-Ampere Converter Calibration

For d-c tests of the converter voltage ranges, a potentiometer and volt box are used to measure the voltage across the input terminals of the converter. Then, after the proper balances of the converter are made, the potentiometer is used to measure the output voltage of the converter, as shown in figure 3. The correction to the range factor of the converter is calculated from these two potentiometer readings and the

3

known ratio of the volt box. For tests of the current ranges a shunt is used as shown in figure 4.

## 2.1 Calibration Circuits

Volt-ampere converters generally have a small reversed d-c difference, so that the average for the two directions of the current must be used as a d-c reference. The circuits of figures 3 and 4 show a convenient switching arrangement which provides for reversing the test current and the leads to the potentiometer. It is more convenient if $S_{1a}$ and $S_{1b}$ are ganged together.

Short, low-resistance leads (less than 0.01 percent of the input resistance of the converter) should be used between the volt box and the volt-ampere converter. The common or ground terminal of the instrument and the low-voltage end of the volt box should be grounded as shown in the figure.

It is advantageous (although not necessary) to select shunts and volt-box ranges of such value that their nominal output voltage is the same as that of the converter. Such an arrangement will help to save time by allowing the two measurements to be made without resetting the main potentiometer dials. It will also tend to minimize the effect of potentiometer errors, since it is only the difference between the two readings that is significant.

It is very important that the metal case of a potentiometer which is internally connected to the emf circuit should not be directly grounded, since this would comprise a second ground. If an auxiliary emf dial is provided, it may be connected to the $V_s$ circuit, following the directions

4

given by the manufacturer. This makes it unnecessary to reset the dials when switching to $V_t$. Note that a potentiometer reversing switch may still be required in this circuit.

If the volt-ampere converter has a built-in potentiometer, this potentiometer should first be calibrated. This can often be done conveniently by comparison with a general purpose potentiometer having known corrections. For the calibration of the converter, the built-in potentiometer is then used to measure the output of the volt-ampere converter, and the general purpose potentiometer is connected to the shunt or volt box. Alternatively the internal potentiometer can be used with a suitable switch to measure first the voltage of the standard shunt or volt box and then the volt-ampere converter, as already outlined.

Stable d-c supplies of voltage and current are necessary, and the observer at the potentiometer must have the fine supply controls within his reach. Two observers are required for the test.

## 2.2  Precautions

Because the frequency response of thermoelements such as those used in volt-ampere converters extends to many megacycles, interference from TV stations and other sources of rf fields can sometimes be troublesome unless a filter is incorporated in the leads to the heater of the converter or, in extreme cases, the instrument is used in a shielded room. A quick check of this interference is easily made, however. With the input terminals of the converter connected to the calibrating circuit but with the source disconnected, and with a potentiometer connected to the "potr" terminals, ($V_t$ in figure 1), adjust the No. 1 control on the instrument

5

(with the transfer switch in No. 1 (A-C) position) for minimum deflection of the converter galvanometer. There should be no noticeable change in the deflection when the input terminals are short-circuited. Similarly, after a balance has been obtained (at any settings of the No. 1 and No. 2 controls) with the transfer (selector) switch in the No. 2 (D-C) position, there should be no change in galvanometer deflection when a capacitor (at least 2000 pf) is connected across the "potr" terminals ($V_t$ in figure 1). Such a capacitor will effectively short-circuit any rf current picked up in the potentiometer circuit.

Many bead-type thermoelements (having an electrically-insulating bead between the heater and thermocouple) exhibit a small exponentially-decreasing drift of emf for the first few minutes after a steady heater current is applied. This does not ordinarily cause a significant error, but, for the most accurate results, a wait of a minute after each large change in heater current is desirable.

The sensitivity and stability should be checked after warm-up but before the formal test is begun. For a check of sensitivity, select any convenient range, turn $S_2$ (figure 3 or 4) to the $V_s$ position, and the transfer (selector) switch on the converter to the No. 1 (A-C) position. With the potentiometer set to the corresponding nominal value, adjust the input voltage or current until the potentiometer is balanced. Then balance the converter in the No. 1 position. Change the potentiometer dials by 0.1 percent, readjust the input to rebalance the potentiometer and note the change in deflection of the galvanometer in the converter. An abnormally low sensitivity is usually an indication that the

6

thermoelement is faulty. Then, to check stability, keep the voltage con-
stant and observe the galvanometer deflection for a few minutes. The
drift should be less than 0.01 percent per minute. The error introduced
from this source is mainly dependent upon the time needed by the operator
between setting the No. 1 controls of the converter and balancing the
potentiometer after setting the No. 2 controls. An excessive drift is
usually remedied by replacing the internal batteries.

## 2.3  Procedure

After preliminary settings of the input controls and adjustment of
the No. 1 and No. 2 controls of the converter, an observer at the poten-
tiometer adjusts the voltage or current to balance the potentiometer at
the desired setting, with switch $S_2$ in the $V_s$ position (figure 3 or 4).
The second observer adjusts the No. 1 (A-C) balance controls on the
converter until the galvanometer is set exactly on a scale mark near the
null position. The transfer switch on the converter is then turned to
the No. 2 (D-C) position, and the No. 2 balance controls are adjusted for
the same galvanometer position as was set in the first balance. The
potentiometer observer meanwhile switches to the $V_t$ position and, while
the No. 2 setting is held constant, measures the converter output. The
potentiometer and converter are then switched to their initial positions,
the current or voltage is reversed, and the two-step test is repeated.
For increased reliability, it may be advisable to take an average of four
determinations---two for each direction of current.

NOTE:  If the transfer switch is left in the No. 2 (D-C) position,
the thermoelement will remain energized while the preliminary settings
are made for the next test point.

7

The corrected potentiometer setting in the $V_s$ position of $S_2$ divided by the corrected shunt resistance or multiplied by the corrected volt box ratio is the "true" input current or voltage, $Q_t$. The current or voltage indicated by the converter, $Q_i$, is the corrected average of the potentiometer readings in the $V_t$ position of $S_2$ multiplied by the factor given on the range switch. The percentage d-c correction for the converter is then simply $c = 100 \ (Q_t - Q_i)/Q_n$ where $Q_n$ is the nominal voltage or current.

Example:

| | |
|---|---|
| Range | 5 amps |
| Current (nominal) | 5 amps |
| Shunt, R | 0.09999 ohm |
| Potentiometer setting, $V_s$ | 0.50000 volt |
| Average potentiometer reading, $V_t$ | 0.49996 volt |
| Measured current $= V_s/R = I_m$ | 5.0005 amps |
| Indicated current $= V_t \times F = I_i$ | 4.9996 amps (F=10 for this range) |
| Converter correction $= I_m - I_i$ | +0.0009 amp |
| Percent correction, c | +0.09/5 or +0.02% |

NOTE: Potentiometer correction assumed negligible in the above example.

For an alternative method of making this calculation, see Appendix II.

When the volt-ampere converter is used to measure an a-c quantity, the true alternating voltage or current is $Q = V_t F \ (1 + 0.01c + 0.01d)$ where F is the factor marked on the range switch, c is the d-c correction

8

in percent for the range used and d is the percent ac-dc difference of
the converter at the applied frequency.

Acceptable accuracy in this d-c test can be obtained only if the
corrections to the standard cell, shunt box, volt box, and potentiometer
are known to within ±0.01 percent or better at the working current or
voltages and the corrections applied.

3. Calibration Procedure for Converters Having Double-Coil Indicators

For volt-ampere converters having the double-coil milliammeter as an
error indicator the circuits and procedure are necessarily somewhat
different. As before, two observers are required----one to operate the
converter and one to measure the input with a potentiometer and volt box
or shunt. A reversing switch for the test voltage and current should be
provided, but the switch $S_2$ in figures 3 and 4 is not used.

A procedure paralleling the one described earlier can be used, but
for best precision the following one is recommended.

With the decade multiplier or shunt dials set to the nominal test
value, the transfer switch (SW in fig. 2) should be turned to position B
(equivalent to No. 2 or D-C previously) and the No. 2 supply controls are
adjusted to give a zero indication on the error indicator. The No. 1
supply controls are then adjusted until this internal d-c source balances
the thermocouple output as indicated by a null on the galvanometer. The
transfer switch is then turned to position A and the input voltage or
current is adjusted by the observer at the converter until the galva-
nometer is again balanced. The input is held constant while the second
observer measures the input voltage or current with the potentiometer and

9

volt box or shunt. The difference between the corrected potentiometer reading and the converter indication (dial settings) is then the correction to be applied to the converter with due attention to sign. Again the average of four readings----two for each direction of current----is advised.

Example:

| | |
|---|---|
| Converter setting | 150.0 volts |
| Error indicator | 0.00 |
| Converter indication, $V_i$ | 150.00 volts |
| Volt Box ratio, N | 100 x 1.0002 |
| Average potentiometer readings, $V_s$ | 1.49928 volts |
| Measured voltage = $V_s$ N = $V_m$ | 149.958 volts |
| Converter Correction = $V_m$ - $V_i$ | -0.042 volts |
| Percent correction, c | -4.2/150 =-0.03% |

## 4. Thermoelements

Ordinarily replacement thermoelements can be obtained from the manufacturer with guaranteed ac-dc differences of not more than 0.01 percent. Thus the ac-dc differences of a volt-ampere converter having a rated accuracy of 0.05 percent do not need to be redetermined when a thermoelement is replaced. The d-c calibration may be affected slightly if the new thermoelement has a reversed d-c difference, or (for instrument without compensating resistors) if its heater resistance is not at the nominal value. A d-c measurement on one or two ranges will show the magnitude of the effects.

## 5. A Voltage Comparator

A voltage comparator (figs. 5, 6, and 7) has been constructed at NBS which can be used instead of the external potentiometer for converter calibration. With it, a direct measurement of the percentage difference between $V_s$ and $V_t$ is made. The instrument has five ranges, .25, .5, .75, 1.0, and 1.5 volts, corresponding to the volt-ampere converter outputs obtained in the usual test. If the comparator input voltages ($V_s$ and $V_t$) are nominally equal to any one of these range values, then the comparator indicates percent correction directly with the proper sign. If tests at other output levels are required, the comparator indication can be easily corrected as explained below.

Unlike the requirement of the potentiometer method, the shunt and volt box ranges must be selected so that $V_s$ and $V_t$ are nominally equal. This requirement is rarely difficult, although a wide-range shunt box may be needed.

Very fine controls for voltage and current are not required although good short-time stability is necessary. Again it is necessary to reverse the test current or voltage and take the average of values obtained for the two directions. The switches $S_{1b}$ and $S_2$ shown in figures 3 and 4 are built into the voltage comparator and shown as $S_v$ in figures 5 and 6. The shunt or volt box output and the volt-ampere converter output are connected directly to the $V_s$ and $V_t$ terminals, respectively.

Referring to figure 5, with the test voltage or current set within a few percent of the nominal value, the switch $S_v$ is turned to $V_s+$ or $V_s-$ depending on the polarity of $V_s$, and this input is balanced against the

11

internal Lindeck potentiometer by adjusting $I_s$ until $I_s R_s$ is equal to $V_s$. An internal galvanometer indicates equality. The $I_s$ adjustment and the No. 1 (AC) balance on the VA converter being calibrated should be made simultaneously.

The No. 2 (DC) balance is then made on the converter, the switch $S_v$ is moved to $V_t$ and the converter output is compared with $I_s R_s$. If $V_s$ and $V_t$ are equal (a very special case) the galvanometer will again balance indicating that the volt box (or shunt) and the converter have equal corrections. If they are not equal, the balance can be restored by inserting the difference potential across the resistor $R_c$ by adjusting $I_c$. A milliammeter in this circuit measures $I_c$ and is marked so as to indicate the percent difference between $V_s$ and $V_t$ if the $I_s$ meter is at full scale. When this indication is corrected for any shunt or volt box error, the converter correction is determined.

If $V_t$ is smaller than $V_s$ the switch $S_c$ is reversed. This position of the switch is marked plus to show that the difference is to be added to the indication of the converter.

The correction formula for voltage ranges is shown in Appendix I to be $c = v + \dfrac{D_c}{D_s}$ where c is the percent correction of the volt-ampere con- verter, v is the percent volt box correction, $D_c$ is the indication of the "correction" milliammeter ($I_c$) with its proper sign, and $D_s$ is the indi- cation of the one milliampere (full scale) instrument in the Lindeck potentiometer ($I_s$). It is expected that the comparator will nearly always be used with this instrument at full scale so that $D_s$ is 1 and the formula is $c = v + D_c$. This is also the case for the current ranges. The formula,

derived in Appendix I, is $c = -u + \frac{D_c}{D_s}$ where u is the percent shunt correction and $D_s$ is again one at full scale or rated input.

The NBS voltage comparator is built entirely of commercial parts. The rotary switches $S_v$ and $S_p$ have solid silver contacts and 10-turn, helically wound, 1000 ohm control resistors are used. All other resistors are in the 1/2 percent accuracy class and wire wound. The $I_s$ circuit is supplied by two No. 6 dry cells and the $I_c$ circuit by one. It is important that the current in the $I_s$ circuit be stable to at least 0.01 percent for as long as it takes to make the second balance. The meters are of the panel type in the two percent accuracy class.

It should be noted here that high accuracy in comparator circuits is not necessary. The "correction" meter has a full scale range of 0.1 percent so that a ten percent error is necessary in its associated resistors to cause a 0.01 percent error in the resulting volt-ampere converter correction. Furthermore, as suggested earlier, exact setting of the test voltage or current is not necessary. It can be shown that if the volt-ampere converter input differs from the nominal value by nine percent, the indicated converter correction (c) will not be in error by more than 0.01 percent even if the converter correction is as large as 0.1 percent. Therefore, the $D_s$ term in the equations above may be considered to be unity if it is within a few percent of full scale.

The voltage comparator has the advantage of being low in cost and easily constructed and used. It frees a precision potentiometer for other work, makes very fine control unnecessary and greatly simplifies the calculations.

13

The author acknowledges the assistance of Mr. F. L. Hermach who offered many valuable suggestions and who originally developed the equations given in Appendix II.

## 6.  References

[1]  F. L. Hermach and E. S. Williams, Multirange Audiofrequency Thermocouple Instruments of High Accuracy, J. Research, 52, 227, (1954) RP2494.

[2]  F. L. Hermach and E. S. Williams, A Wide-Range Volt-Ampere Converter for Current and Voltage Measurements, AIEE Transactions (Communications and Electronics), 384, (September 1959).

Appendix I

Derivation of Equations for the Voltage Comparator

The voltage to be measured ($V_p$) by the volt-ampere converter (with a potentiometer connected to the output) is $V_p = V_t F (1 + c)$ where $V_t$ is the converter output, F is the multiplying factor, and c is the proportional correction to F. The same voltage ($V_p$) as measured by the volt box and potentiometer is $V_p = V_s N (1 + v)$ where $V_s$ is the potentiometer reading, N is the volt box ratio, and v is the proportional correction to N. Therefore,

$$V_t F (1 + c) = V_s N (1 + v). \qquad (1)$$

When the two balances are made on the voltage comparator $V_s = I_s R_s$ and $V_t = I_s R_s - I_c R_c$ for the "plus" position of switch $S_c$ so that

$$\frac{N(1 + v)}{F(1 + c)} = 1 - \frac{I_c R_c}{I_s R_s}.$$

In order that $V_s$ and $V_t$ be nominally equal, the volt box range must be chosen so that $F = N$. The one milliampere instrument in the $I_s$ circuit is read directly so that $D_s = I_s$ where its indication is designated as $D_s$. The 0.5 milliampere instrument in the $I_c$ circuit is marked to indicate 0.1 at full scale so that $I_c = 5 D_c$ where $D_c$ is the indication of the "correction" meter. Then with the resistors chosen so that $R_c/R_s = 1/500$, we may write

$$\frac{1 + v}{1 + c} = 1 - \frac{5 D_c}{500 D_s}.$$

If v and c are very much less than unity then, very closely, $c = v + D_c/100 D_s$ and if c and v are in percent this becomes

$$c = v + \frac{D_c}{D_s}. \qquad (2)$$

Similarly, a current measured by the volt-ampere converter is $I_p = V_t F (1 + c)$ where $I_p$ is the measured current and the other terms are

the same as above. The same current measured with the shunt and poten-
tiometer is $I_p = V_s/R(1 + u)$ where $R$ is the nominal resistance of the
shunt, $u$ is the shunt correction and $V_s$ is the potentiometer reading,
therefore,

$$\frac{V_s}{R(1 + u)} = V_t F(1 + c). \tag{3}$$

When the two balances are made on the voltage comparator

$$V_s = I_s R_s \quad \text{and} \quad V_t = I_s R_s - I_c R_c$$

so that

$$\frac{1}{F(1 + c)R(1 + u)} = 1 - \frac{I_c R_c}{I_s R_s}.$$

In order that $V_s$ and $V_t$ be nominally equal, the shunt must be chosen so
that $FR = 1$.

Therefore, with $R_c/R_s = 1/500$, $c = -u + I_c/500\, I_s$ and proceeding as
above, we have

$$c = -u + \frac{D_c}{D_s} \tag{4}$$

neglecting second and higher order terms.

## Appendix II

### Derivation of Equations for the Potentiometer Method

The calculations illustrated earlier for converters used with a
potentiometer can be shortened considerably by using formulas similar to
those above. The equations (1) and (3) are valid whether a potentiometer
or voltage comparator is used.

Considering equations (1) for voltage measurements, we may rewrite
it

$$\frac{V_s N}{V_t F} = \frac{1 + c}{1 + v}.$$

The nominal values of $V_s$ and $V_t$ are not necessarily equal but in any
case the ratio $V_s N/V_t F$ is nominally 1. If $V_s$ is set exactly to its

16

nominal value, and if we substitute for $V_t$ a value $V_{tn}(1 + a)$, where $V_{tn}$ is the nominal value, and a is a fractional correction to the nominal value, i.e., $a = (V_t - V_{tn})/V_{tn}$, then $V_s N/V_{tn} F = 1$ and

$$\frac{V_s N}{F V_{tn}(1 + a)} = \frac{1 + c}{1 + v}$$

for which

$$c = v - a \qquad\qquad (5)$$

neglecting second and higher order terms.

Similarly, we may write equation (3)

$$\frac{V_s}{RFV_t} = (1 + u)(1 + c).$$

In this case the ratio $V_s/RFV_t$ is nominally 1. If $V_s$ is set exactly to its nominal value and $V_t = V_{tn}(1 + a)$ as before, we then have

$$\frac{V_s}{RFV_{tn}(1 + a)} = (1 + u)(1 + c)$$

from which

$$c = -a - u. \qquad\qquad (6)$$

neglecting second and higher order terms.

Example:

| | |
|---|---|
| Range | 5 amps |
| Current | 5 amps |
| Shunt R | 0.09999 ohms ($u = -0.010\%$) |
| Potentiometer setting $V_s$ | 0.50000 volts |
| Average potentiometer reading $V_t$ | 0.49996 volts ($a = -0.008\%$) |
| Converter d-c correction $c = -a - u$ | $+ 0.02\%$ |

IF $R_m = R'_m$ THEN $V_a = \dfrac{R_m}{R_t} V_t$

(INDEPENDENT OF $R_h$)



(a)

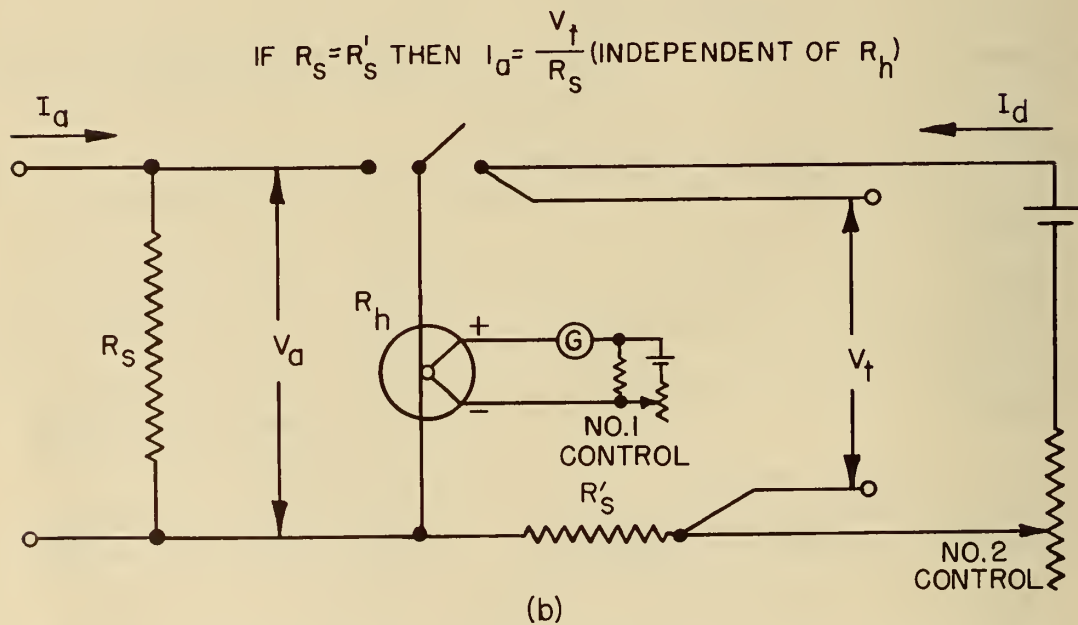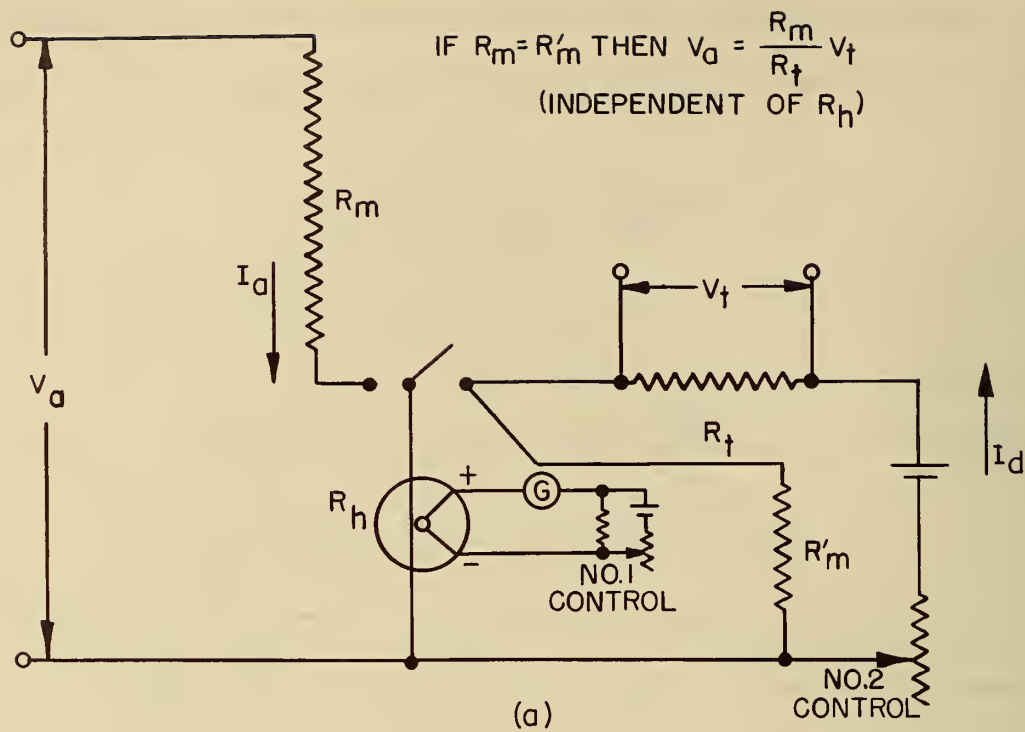IF $R_s = R'_s$ THEN $I_a = \dfrac{V_t}{R_s}$ (INDEPENDENT OF $R_h$)



(b)

Figure 1. Simplified diagram of volt-ampere converter; (a) For voltage measurements; (b) For current measurements
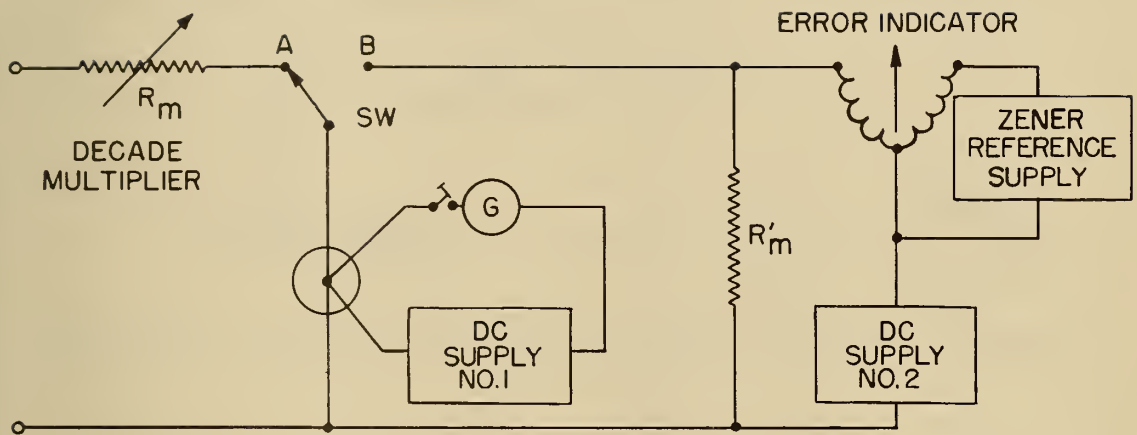
Figure 2. · Simplified diagram of volt-ampere converter with error
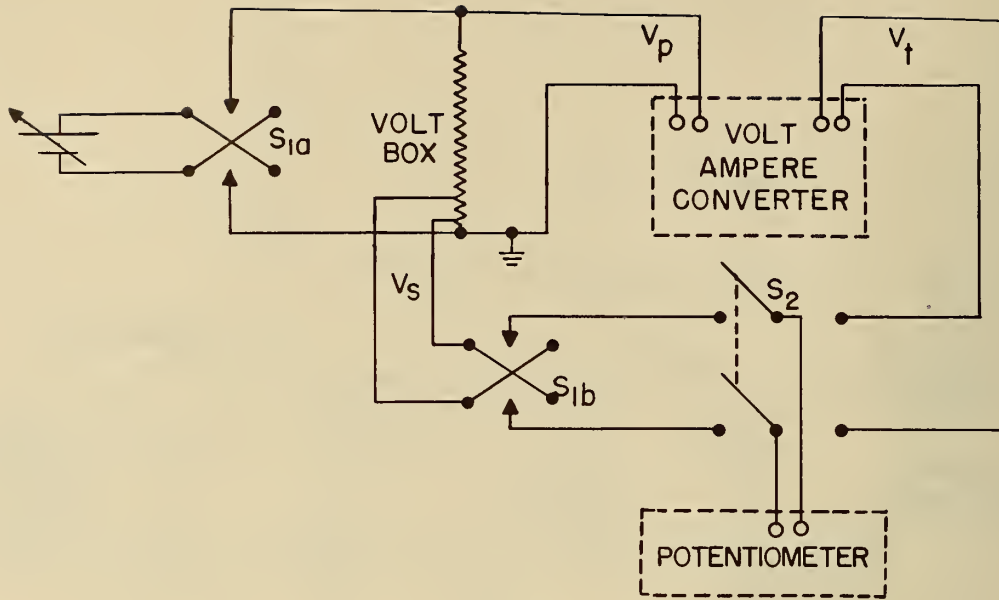indicator (for voltage measurements)

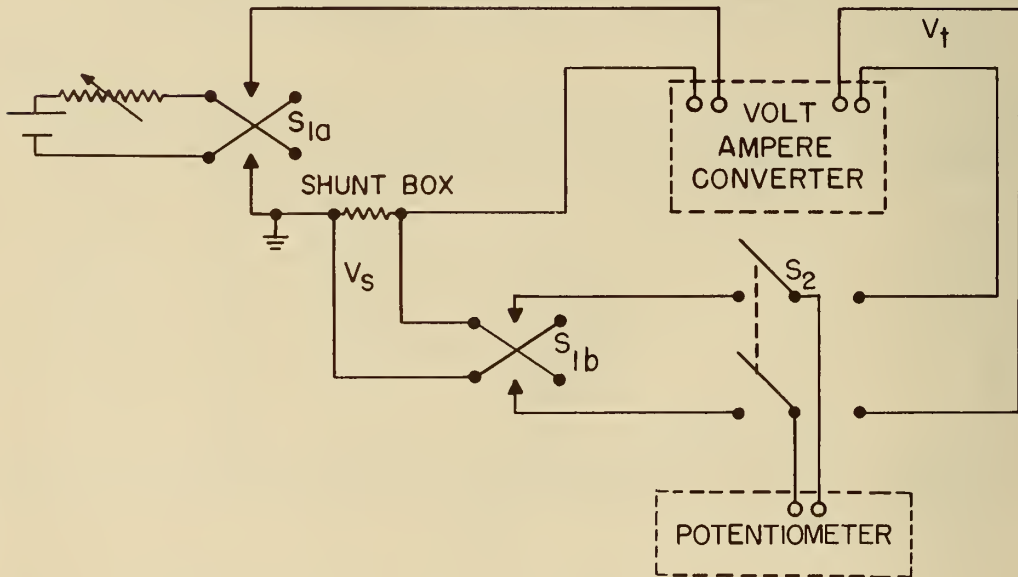Figure 3. Calibration circuit for volt-ampere converter voltage ranges
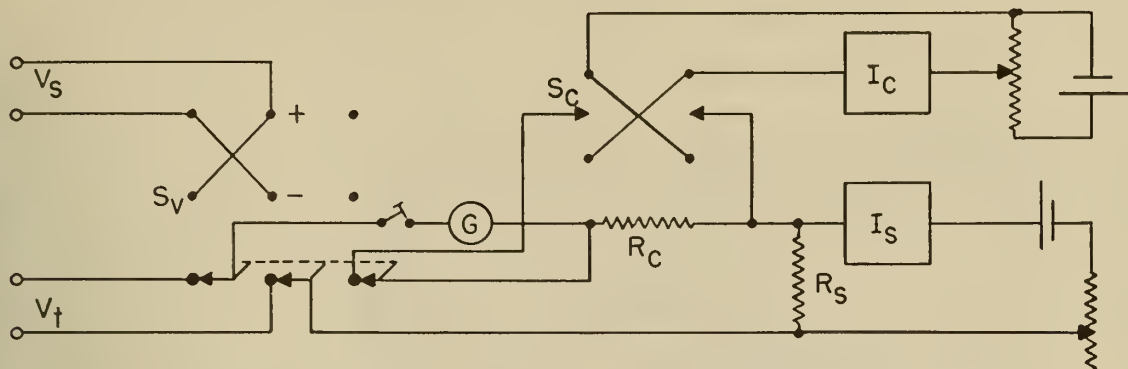


Figure 4. Calibration circuit for volt-ampere converter current ranges

NOTE: VOLTAGES $V_s$ AND $V_t$ ARE IDENTIFIED IN FIGURES 3 AND 4

Figure 5. Simplified diagram of voltage comparator

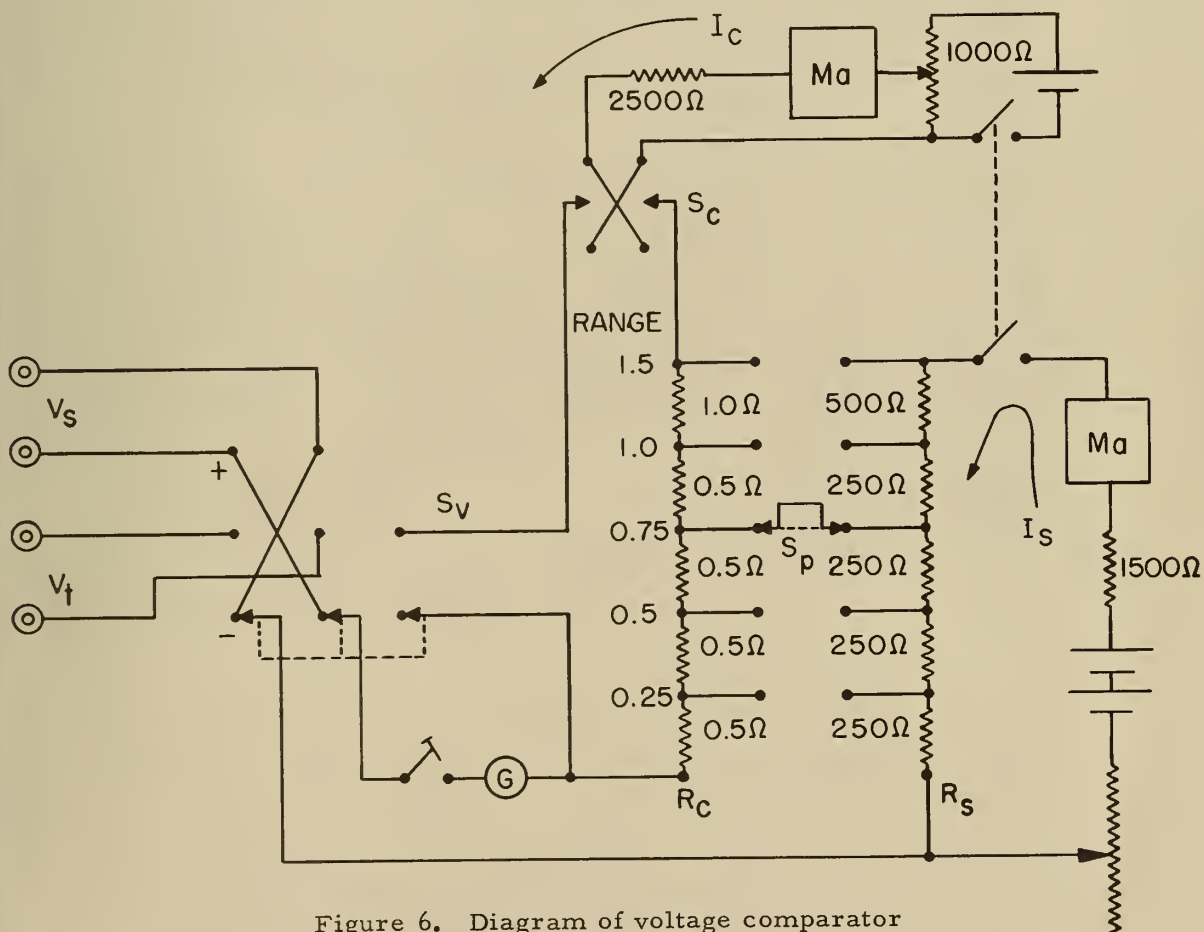NOTE: Voltages $V_s$ and $V_t$ are identified in figures 3 and 4



Figure 6. Diagram of voltage comparator

Figure 7. Photograph of voltage comparator

U. S. DEPARTMENT OF COMMERCE
Luther H. Hodges, *Secretary*

NATIONAL BUREAU OF STANDARDS
A. V. Astin, *Director*

# THE NATIONAL BUREAU OF STANDARDS

The scope of activities of the National Bureau of Standards at its major laboratories in Washington, D.C., and Boulder, Colorado, is suggested in the following listing of the divisions and sections engaged in technical work. In general, each section carries out specialized research, development, and engineering in the field indicated by its title. A brief description of the activities, and of the resultant publications, appears on the inside of the front cover.

## WASHINGTON, D. C.

**Electricity.** Resistance and Reactance. Electrochemistry. Electrical Instruments. Magnetic Measurements. Dielectrics. High Voltage.
**Metrology.** Photometry and Colorimetry. Refractometry. Photographic Research. Length. Engineering Metrology. Mass and Scale. Volumetry and Densimetry.
**Heat.** Temperature Physics. Heat Measurements. Cryogenic Physics. Equation of State. Statistical Physics.
**Radiation Physics.** X-ray. Radioactivity. Radiation Theory. High Energy Radiation. Radiological Equipment. Nucleonic Instrumentation. Neutron Physics.
**Analytical and Inorganic Chemistry.** Pure Substances. Spectrochemistry. Solution Chemistry. Standard Reference Materials. Applied Analytical Research. Crystal Chemistry.
**Mechanics.** Sound. Pressure and Vacuum. Fluid Mechanics. Engineering Mechanics. Rheology. Combustion Controls.
**Polymers.** Macromolecules: Synthesis and Structure. Polymer Chemistry. Polymer Physics. Polymer Characterization. Polymer Evaluation and Testing. Applied Polymer Standards and Research. Dental Research.
**Metallurgy.** Engineering Metallurgy. Microscopy and Diffraction. Metal Reactions. Metal Physics. Electrolysis and Metal Deposition.
**Inorganic Solids.** Engineering Ceramics. Glass. Solid State Chemistry. Crystal Growth. Physical Properties. Crystallography.
**Building Research.** Structural Engineering. Fire Research. Mechanical Systems. Organic Building Materials. Codes and Safety Standards. Heat Transfer. Inorganic Building Materials. Metallic Building Materials.
**Applied Mathematics.** Numerical Analysis. Computation. Statistical Engineering. Mathematical Physics. Operations Research.
**Data Processing Systems.** Components and Techniques. Computer Technology. Measurements Automation. Engineering Applications. Systems Analysis.
**Atomic Physics.** Spectroscopy. Infrared Spectroscopy. Far Ultraviolet Physics. Solid State Physics. Electron Physics. Atomic Physics. Plasma Spectroscopy.
**Instrumentation.** Engineering Electronics. Electron Devices. Electronic Instrumentation. Mechanical Instruments. Basic Instrumentation.
**Physical Chemistry.** Thermochemistry. Surface Chemistry. Organic Chemistry. Molecular Spectroscopy. Elementary Processes. Mass Spectrometry. Photochemistry and Radiation Chemistry.

**Office of Weights and Measures.**

## BOULDER, COLO.

**Cryogenic Engineering Laboratory.** Cryogenic Equipment. Cryogenic Processes. Properties of Materials. Cryogenic Technical Services.

### CENTRAL RADIO PROPAGATION LABORATORY

**Ionosphere Research and Propagation.** Low Frequency and Very Low Frequency Research. Ionosphere Research. Prediction Services. Sun-Earth Relationships. Field Engineering. Radio Warning Services. Vertical Soundings Research.
**Radio Propagation Engineering.** Data Reduction Instrumentation. Radio Noise. Tropospheric Measurements. Tropospheric Analysis. Propagation-Terrain Effects. Radio-Meteorology. Lower Atmosphere Physics.
**Radio Systems.** Applied Electromagnetic Theory. High Frequency and Very High Frequency Research. Frequency Utilization. Modulation Research. Antenna Research. Radiodetermination.
**Upper Atmosphere and Space Physics.** Upper Atmosphere and Plasma Physics. High Latitude Ionosphere Physics. Ionosphere and Exosphere Scatter. Airglow and Aurora. Ionospheric Radio Astronomy.

### RADIO STANDARDS LABORATORY

**Radio Physics.** Radio Broadcast Service. Radio and Microwave Materials. Atomic Frequency and Time-Interval Standards. Radio Plasma. Millimeter-Wave Research.
**Circuit Standards.** High Frequency Electrical Standards. High Frequency Calibration Services. High Frequency Impedance Standards. Microwave Calibration Services. Microwave Circuit Standards. Low Frequency Calibration Services.