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## Standard Spherical Dipole Source

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G. Koepke
L. D. Driver
K. Cavcey
K. Masterson
R. Johnk
M. Kanda

Electromagnetic Fields Division
Electronics and Electrical Engineering Laboratory National Institute of Standards and Technology Boulder, Colorado 80303-3328

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G. Koepke, L. D. Driver, K. Cavcey K. Masterson, R. Johnk, and M. Kanda<br>National Institute of Standards and Technology Electromagnetic Fields Division Boulder, Colorado 80303


#### Abstract

A spherical dipole was developed to provide a source that can be characterized both by theory and experiment and integrated into modern automated test systems. The frequency and amplitude of the radiated electromagnetic field are established remotely using a signal generator. This signal and all other control features are transmitted to and from the sphere using fiber optic cable. The field measurements show good agreement with predictions over much of the frequency band.


Key words: electromagnetic fields; electronic circuits; fiber optic; remote control; spherical dipole; standard radiator.

## 1. INTRODUCTION

The spherical dipole rf antenna developed at the National Institute of Standards and Technology and documented in this report is designed to be a standard (known and repeatable) electromagnetic (em) source. The ability to predict and monitor the em fields produced by the standard source will provide an effective means to determine the accuracy of emissions measurement systems. These measurement systems must quantify the unintentional emissions of a wide variety of electronic devices. These devices are not designed as em sources yet the internal electronic systems may produce interfering signals with unknown radiation characteristics. A predictable standard source would permit meaningful comparisons of different facilities or techniques and be a useful instrument for further improvements in emissions metrology.

We examined several possible geometries which could be used for a standard source antenna. The short monopole over a box containing a power source has been used successfully as a control standard to monitor the repeatability of various measurements. This geometry is difficult to model accurately due to the variable (usually small) ground plane size which depends on the proximity of a ground reference. The monopole is a good solution when the source is characterized by experiment alone. Another geometry that merits consideration is the fat cylindrical dipole. However, the cylindrical dipole and other more complicated geometries were abandoned in favor of a simple sphere with a small gap on the equator.

The sphere provides a desirable symmetry and avoids sharp edges which complicate the theoretical model. The idea for using a small spherical dipole as a control standard radiator or as a receiving antenna has been explored by several researchers [1 through 9] with good success. The volume provided by a spherical shape allows the antenna to be self-contained. All the necessary circuitry and power sources can be internal, thereby eliminating interconnecting lines which disrupt the radiated field. Previous radiators have employed internal oscillators with rich harmonic content to provide radiating signals; however, there was no remote control over amplitude or frequency. A spherical low frequency probe [7 through 9] and a recent effort by Murakawa, et al., [6] with a spherical radiator have demonstrated the use of a fiber optic transmission line to communicate with the spherical antenna. The use of fiber optic components for microwave frequencies has been made possible due to recent advances in physical size, power consumption, and modulation bandwidth. The spherical radiator described in this report also uses optical fiber to control the frequency and amplitude of the radiated signal. The communication between the operator and the sphere is further enhanced by provisions for monitoring internal functions of the radiator. These functions include the drive rf voltage applied to the equatorial gap, the ambient temperature within the sphere, and a standby mode to maximize battery life.

This report is written to provide the theoretical formulations used to predict electromagnetic fields radiated from a spherical dipole in free space (section 2), to detail the experimental comparison with these predictions (section 3), and to provide complete design and construction details of the standard spherical dipole (sections

4 and 5). Section 6 draws conclusions and section 7 acknowledges contributions by other individuals.

## 2. RADIATED FIELDS FROM A SPHERICAL DIPOLE

2.1 Derivation of the Electric and Magnetic Fields for the Standard Spherical Radiator

In this section, expressions are derived for the electric and magnetic fields of the standard spherical radiator of figure 1. As can be seen in figure 1 , the spherical radiator consists of two perfectly conducting hemispheres that are separated by an infinitesimally small gap at the equator $(\theta=\pi / 2)$. An infinitesimal gap has a width that is immeasurably or incalculably small. Thus, for analysis, the gap width is assumed to be arbitrarily close to 0 . Because of the geometry of this structure, the spherical coordinates ( $r, \theta, \phi$ ) are used to describe the field behavior in the region external to the surface of the sphere. In order to create the electric and magnetic fields, a complex, timeharmonic voltage $V$ is applied across the gap; this, in turn, sets up time-harmonic electric and magnetic fields in the region external to the sphere. The assumption of a time-harmonic source means that a sinusoidal voltage of amplitude $|v|$ is applied between the two hemispheres for an infinitely long time so that field transients are allowed to decay away. As a careful study of figure 1 reveals, the assumed gap does not correspond to the actual gap of the standard radiator because the actual gap has a small but measurable width. However, in all practical situations, the assumption of an infinitesimal gap will have virtually no effect on the values of the computed fields. Because of the spherical symmetry of this antenna, the gap voltage generates an electric field $E$ that is $\theta$-directed and a magnetic field $H$ that is $\phi$ directed.

The spherical symmetry of this structure allows us to obtain a closed-form solution for the electric and magnetic fields. The $\phi-$
directed magnetic field can be expanded in a series of spherical harmonics as follows [10]:

$$
\begin{equation*}
H_{\phi}(r, \theta)=\sum_{n=1}^{\infty} A_{n} r^{-1 / 2} P_{n}^{1}(\cos \theta) H_{n+1 / 2}^{(2)}\left(k_{0} r\right) . \tag{1}
\end{equation*}
$$

The $\theta$-directed electric field can be found by applying eq (1) to the Maxwell curl relation:

$$
\begin{equation*}
\bar{E}=\frac{1}{j \omega \epsilon} \nabla \times \bar{H} . \tag{2}
\end{equation*}
$$

The result of this process is

$$
\begin{equation*}
E_{\theta}(r, \theta)=\sum_{n=1}^{\infty} \frac{j A_{n}}{\omega \epsilon} r^{-3 / 2} P_{n}^{1}(\cos \theta)\left[k_{0} r H_{n-1 / 2}^{(2)}\left(k_{0} r\right)-n H_{n+1 / 2}^{(2)}\left(k_{0} r\right)\right] . \tag{3}
\end{equation*}
$$

In eqs (1) and (3), $A_{n}$ is a yet to be determined coefficient; $P_{n}^{1}(\cos \theta)$ is an associated Legendre function of the first kind of order $n$ and degree 1; and $H_{n+1 / 2}^{(2)}\left(k_{0} r\right)$ are second Hankel functions with the fractional indices $n \pm 1 / 2$. Also, $k_{0}=2 \pi f / c$ ( $f=$ frequency; $c=3.0 \times 10^{8} \mathrm{~m} / \mathrm{s}$ ) is the free-space wave number and $r$ is the distance from the center of the sphere to the point at which the fields are being calculated. This series has been selected since the fractional-order Hankel functions and the associated Legendre functions arise naturally in the solution of electromagnetic structures with a spherical symmetry. Since the terms of the series of eqs (1) and (3) are a function of the spherical coordinates ( $r, \theta, \phi$ ), the application of boundary conditions to this solution is a straightforward process. It should be noted that eqs (1) and (3) are not dependent on $\phi$. This lack of a dependence on $\phi$ is due to the fact that the gap is being excited uniformly with a voltage $v$ around the circumference of the spherical radiator.

From the standpoint of numerically evaluating the series of eq (1), the presence of the Hankel and the Legendre functions seems, at first, intimidating and perhaps puzzling. As it turns out, the special functions can be replaced by much simpler trigonometric and
algebraic functions. In order to illustrate this point, the Hankel and associated Legendre functions are given below for $n=1,2,3$.

The first three Hankel functions are given by [11]:

$$
\begin{equation*}
H_{1 / 2}^{(2)}(x)=\sqrt{\frac{2}{\pi x}}[\sin x+j \cos x], \tag{4}
\end{equation*}
$$

$$
\begin{equation*}
H_{3 / 2}^{(2)}(x)=\sqrt{\frac{2}{\pi x}}\left[\left(\frac{\sin x}{x}-\cos x\right)+j\left(\sin x+\frac{\cos x}{x}\right)\right] \tag{5}
\end{equation*}
$$

and

$$
\begin{equation*}
H_{5 / 2}^{(2)}(x)=\sqrt{\frac{2}{\pi x}}\left[\left(\left\{\frac{3}{x^{2}}-1\right\} \sin x-\frac{3}{x} \cos x\right)+j\left(\frac{3}{x} \sin x+\left\{\frac{3}{x^{2}}-1\right\} \cos x\right)\right] \tag{6}
\end{equation*}
$$

The first four associated Legendre functions are given by [11]:

$$
\begin{gather*}
P_{0}^{1}(\cos \theta)=0, \\
P_{1}^{1}(\cos \theta)=\sin \theta, \\
P_{2}^{1}(\cos \theta)=3 \sin \theta \cos \theta, \tag{9}
\end{gather*}
$$

and

$$
\begin{equation*}
P_{3}^{1}(\cos \theta)=\frac{3}{2} \sin \theta\left(5 \cos ^{2} \theta-1\right) \tag{10}
\end{equation*}
$$

As an inspection of eqs (4) through (10) indicates, the evaluation of the first few spherical Hankel functions and associated Legendre functions is a straightforward process. In order to evaluate functions with higher indices, we could, in principle, utilize expressions similar to those of eqs (4) through (10). However, as the index $n$ becomes larger, the resulting expressions become more and more complex and cumbersome. An alternative approach to
finding the value of these functions for a given argument $x$ and an arbitrary index $\mathrm{n}(\mathrm{n}>3)$ is to use eqs (4) through (10) to evaluate the functions at the first several indices, and then to find the value of the function at a higher index by using a recurrence relation. The recurrence relation for the associated Legendre functions is

$$
\begin{equation*}
(n-1) P_{n}^{1}(x)=x(2 n-1) P_{n-1}^{1}(x)-n P_{n-2}^{1}(x) . \tag{11}
\end{equation*}
$$

The fractional-index Hankel functions can be expressed in terms of the spherical Hankel functions as

$$
\begin{equation*}
h_{n}^{(2)}(x)=\sqrt{\frac{\pi}{2 x}} H_{n+1 / 2}^{(2)}(x) . \tag{12}
\end{equation*}
$$

The recurrence relation for the spherical Hankel function is

$$
\begin{equation*}
h_{n-1}^{(2)}(x)+h_{n+1}^{(2)}(x)=\left(\frac{2 n+1}{x}\right) h_{n}^{(2)}(x) . \tag{13}
\end{equation*}
$$

Equations (12) and (13) constitute the recurrence relation for the fractional-order Hankel functions. As an inspection of eqs (11) through (13) indicates, for a given argument $x$, the value of either of the Legendre function or the Hankel functions can be found for an arbitrary index $n$, provided that two initial starting values are given. For instance, if the values of the functions are known at x for $\mathrm{n}=1,2$ the functions can be evaluated for $\mathrm{n} \geq 3$ for the same argument. Recurrence relations are particularly suitable when the functions are being programmed on a computer. We must be careful, however, when the recurrence relations are used to evaluate either the associated Legendre functions or the Hankel function for a large index $n$. A large index $n$ requires the repeated use of a recurrence relation, which can generate potentially inaccurate results due to numerical instabilities. The existence of numerical instabilities depends on the form of a given recurrence relation. Some recurrence relations are inherently stable and can be used for large indices, while others cannot be used for a large index due to instabilities that can be introduced by a given recurrence relation. For the parameters of this
problem, the recurrence relations of eqs (11) and (13) are stable up to an index of about 40. Fortunately, such a large index is never encountered in this problem since the series of eqs (1) and (3) converge rapidly and require only a few terms (for the case of the 10 cm diameter spherical radiator) in order to generate an accurate result. Thus the recurrence relations will have to be used at most for a few repeated iterations.

Up to this point, the coefficient $A_{n}$ in eqs (1) and (3) has not yet been evaluated. In order to determine this coefficient, boundary conditions must be invoked. For this case the boundary condition of a vanishing electric field at the surface of the sphere (except at the gap) is sufficient to determine uniquely this coefficient. At the surface of the sphere ( $r=a$ ), the expression for the electric field is given by:

$$
\begin{align*}
E_{\theta}(a, \theta) & =V \delta(\theta-\pi / 2) \\
& =\sum_{n=1}^{\infty} \frac{j A_{n}}{\omega \epsilon} a^{-3 / 2} P_{n}^{1}(\cos \theta)\left[k_{0} r H_{n-1 / 2}^{(2)}\left(k_{0} a\right)-n H_{n+1 / 2}^{(2)}\left(k_{0} a\right)\right] \tag{14}
\end{align*}
$$

where the term $\delta(\theta-\pi / 2)$ is the Dirac delta function. This function is 0 for every angle except for $\theta=\pi / 2$ where it becomes infinite. The electric field, therefore, is 0 everywhere on the surface of the sphere except at the gap, where it becomes infinite. The fact that the field becomes infinite at the gap location is due to the assumption of an infinitesimally small gap width. For the actual spherical radiator, the gap is small and has a finite width. Thus the field is finite for the actual radiator, although it is still large in the gap region. In order to evaluate the coefficient $A_{n}$, both sides of eq (14) are multiplied by $P_{m}^{\prime}(\cos \theta)$ $\sin \theta$ and integrated with respect to the angle $\theta$ from 0 to $\pi$. This process is written as

$$
\begin{align*}
& V \int_{0}^{\pi} \sin \theta P_{m}^{1}(\cos \theta) \delta(\theta-\pi / 2) d \theta \\
& =\sum_{n=1}^{\infty} \frac{j A_{n}}{\omega \epsilon} a^{-3 / 2}\left[k_{0} r H_{n-1 / 2}^{(2)}\left(k_{0} a\right)-n H_{n+1 / 2}^{(2)}\left(k_{0} a\right)\right]  \tag{15}\\
& \times\left[\int_{0}^{\pi} P_{m}^{1}(\cos \theta) P_{n}^{1}(\cos \theta) \sin \theta d \theta\right]
\end{align*}
$$

The integrals on both sides of eq (15) can be evaluated readily by using the basic properties of the Dirac delta function and the orthogonal properties of the associated Legendre function. A wellbehaved function that is multiplied by a Dirac delta function and integrated over some range yields

$$
\begin{align*}
\int_{a}^{c} f(x) \delta(x-b) d x & =f(b) \quad(a<b<c)  \tag{16}\\
& =0 \quad(\text { otherwise })
\end{align*}
$$

The orthogonal property of the associated Legendre function is given by

$$
\begin{array}{rlr}
\int_{0}^{\pi} P_{m}^{1}(\cos \theta) P_{n}^{1}(\cos \theta) \sin \theta d \theta & =\frac{2 n(n+1)}{(2 n+1)} \quad(m=n)  \tag{17}\\
& =0 & (m \neq n)
\end{array}
$$

Applying eqs (16) and (17) to eq (15) yields the coefficient $A_{n}$ :

$$
\begin{equation*}
A_{n}=\frac{\omega \in V a^{3 / 2}(2 n+1) P_{n}^{1}(0)}{j 2 n(n+1) a\left[k_{0} a H_{n-1 / 2}^{(2)}\left(k_{0} a\right)-n H_{n+1 / 2}^{(2)}\left(k_{0} a\right)\right]} . \tag{18}
\end{equation*}
$$

Equation (18) in conjunction with eqs (1) and (3) are the final desired expressions for the electric and magnetic fields.
2.2 Expressions for the Radiated Power Density and the Total Radiated Power

The radiated power density of a given antenna structure has the dimension of $\mathrm{W} / \mathrm{m}^{2}$, and it is a measure of power per unit area for any point external to the radiator. The radiated power density is defined in terms of the electric and magnetic fields by taking the vector cross product of the electric field and the complex conjugate of the magnetic field:

$$
\begin{equation*}
\bar{P}_{d}=\frac{1}{2} \operatorname{Re}\left\{\bar{E} \times \bar{H}^{*}\right\} \tag{19}
\end{equation*}
$$

where the symbol (*) denotes the complex conjugate of the timeharmonic magnetic field. In order to find the radiated power density, the solutions of the standard spherical radiator given by eqs (1), (3), and (18) must be applied to eq (19).

$$
\begin{align*}
\bar{P}_{d}= & \frac{1}{2} \operatorname{Re}\left\{\bar{E} \times \bar{H}^{*}\right\} \\
= & \bar{a}_{r} \frac{1}{2} \operatorname{Re}\left\{\sum_{m=1}^{\infty} \sum_{n=1}^{\infty} \frac{j A_{n} A_{m}^{*}}{\omega \in r^{2}} P_{m}^{1}(\cos \theta) P_{n}^{1}(\cos \theta)\right.  \tag{20}\\
& \left.\times\left[k_{0} r H_{m-1 / 2}^{(2)}\left(k_{0} r\right)-m H_{m+1 / 2}^{(2)}\left(k_{0} r\right)\right] H_{n+1 / 2}^{(2)}\left(k_{0} r\right)\right\} .
\end{align*}
$$

Equation (20) is the expression for the radiated power density. The radiated power density is a function of the location of the field observation point ( $r, \theta$ ). The double series form of eq (20) looks formidable and computationally involved; however, in the case of the spherical radiator, relatively few terms are required for the series to converge. This issue is treated in the next section.

The expression for the total radiated power can be readily derived from a Poynting integration in conjunction with the expressions for the electric and magnetic fields that have already been developed. In this case, the Poynting integral corresponds to the following surface integration of the power density:

$$
\begin{equation*}
P_{r a d}=\frac{1}{2} \operatorname{Re}\left\{\oint_{S}\left[\bar{E} \times \bar{H}^{*}\right] \cdot \overline{a_{n}} d S\right\} . \tag{21}
\end{equation*}
$$

Although the surface over which the integration is carried out is arbitrary, it is mathematically convenient to integrate over the surface of a sphere of radius $R(R>a)$ whose center is coincident with the center of the spherical antenna. For a spherical surface, eq (21) becomes

$$
\begin{equation*}
\left.P_{\mathrm{rad}}=\left.\frac{1}{2} \operatorname{Re}\left\{\int_{0}^{2 \pi} \int_{0}^{\pi}\left[\bar{E} \times \bar{H}^{*}\right] \cdot\left[\overline{a_{r}}\right] r^{2} \sin \theta \quad d \theta d \phi\right\}\right|_{r=R}\right\} \tag{22}
\end{equation*}
$$

From eqs (1), (3), and (18), the vector cross product of the electric field and the complex conjugate of the magnetic field is given by

$$
\begin{align*}
\bar{E} \times \bar{H}^{*}= & \bar{a}_{r_{m=1}} \sum_{n=1}^{\infty} \frac{j A_{n} A_{m}{ }^{*}}{\omega \in R^{2}} \\
& \times\left[k_{0} R H_{m-1 / 2}^{(2)}\left(k_{0} R\right)-m H_{m+1 / 2}^{(2)}\left(k_{0} R\right)\right] H_{n+1 / 2}^{(2)}\left(k_{0} R\right)  \tag{23}\\
& \times\left[P_{m}^{1}(\cos \theta) P_{n}^{1}(\cos \theta)\right] .
\end{align*}
$$

Applying eq (23) to (22) and performing the $\phi$ integration yields the following expression for the total radiated power:

$$
\begin{align*}
P_{\text {rad }}= & \pi R e\left\{\sum_{m=1}^{\infty} \sum_{n=1}^{\infty} \frac{j A_{n} A_{m}^{*}}{\omega \epsilon}\right. \\
& \times\left[k_{0} R H_{m-1 / 2}^{(2)}\left(k_{0} R\right)-m H_{m+1 / 2}^{(2)}\left(k_{0} R\right)\right] H_{n+1 / 2}^{(2)}\left(k_{0} R\right)  \tag{24}\\
& \left.\times \int_{0}^{\pi} P_{m}^{1}(\cos \theta) P_{n}^{1}(\cos \theta) \sin \theta \quad d \theta\right\} .
\end{align*}
$$

Applying the orthogonality relation of eq (17) to eq (24) yields the following single-series expression for the total radiated power:

$$
\begin{align*}
P_{\text {rad }}= & \pi \operatorname{Re}\left\{\sum_{n=1}^{\infty} \frac{j\left|A_{n}\right|^{2}}{\omega \in} \frac{2 n(n+1)}{(2 n+1)}\right.  \tag{25}\\
& \left.\times\left[k_{0} R H_{n-1 / 2}^{(2)}\left(k_{0} R\right)-n H_{n+1 / 2}^{(2)}\left(k_{0} R\right)\right] H_{n+1 / 2}^{(2)}\left(k_{0} R\right)\right\} .
\end{align*}
$$

Equation (25) is the final expression for the total amount of radiated power out of a spherical antenna of radius a. The total radiated power is completely independent of the selected radius of integration $R$. This fact is not readily apparent in eq (25) for general values of $R$. Independence from $R$, however, can be demonstrated as $R \rightarrow+\infty$ by utilizing appropriate large argument expansions for the spherical Hankel functions [11]. As is the case with the series expressions for the fields and the radiated power densities, only a few terms of the series of eq (25) are necessary
in order to generate accurate results for the standard spherical radiator. This issue is dealt with in more detail in the next section.

### 2.3 Convergence of the Field and Power Expressions for the Standard Spherical Radiator

Table 1 depicts the complex electric field for the standard spherical radiator with a gap voltage of 1 V . This has been computed from eq (3) as a function of frequency and the number of terms in the series using [12] and the program listed in appendix A. The observation angle has been chosen as $\theta=\pi / 2$ since this corresponds to the electric (and magnetic) field maxima. Also, the rates of series convergence are similar to those obtained at other values of $\theta$. As a careful study of the table indicates, summing five terms in the series is more than sufficient to ensure fourplace accuracy. Up to an operating frequency of 900 MHz three terms are sufficient to yield four-place accuracy. Since only a few terms are required in order to obtain accurate results, the series of eq (3) is convenient to use.

Table 2 depicts the complex magnetic field results as a function of frequency and the number of terms of eq (1). The results are similar to those of the electric field in that five terms ensure four-place accuracy, and three terms are sufficient to obtain fourplace accuracy up to 800 MHz . The ratio of $\mathrm{E}_{\theta}$ in table 1 to $\mathrm{H}_{\phi}$ in table 2 is also close to the free space value of $120 \pi$.

Results for the total radiated power as a function of frequency and the number of series terms computed from eq (25) are depicted in table 3. As an inspection of this table indicates, only three terms of the series need to be summed in order to ensure four-place accuracy up to 1000 MHz . Thus the series for the radiated power converges more rapidly than the corresponding series expressions for the electric and magnetic fields.

Table 1. The magnitude ( $\mathrm{V} / \mathrm{m}$ ) and phase (degrees) of the complex electric field evaluated for a gap voltage $V=1$ at an observation distance of $R=10 \mathrm{~m}$ and $\theta=\pi / 2$ as a function of frequency and the number of series terms $N$.

| freq (MHz) | $\mathrm{N}=1$ | $\mathrm{N}=3$ | $N=5$ | $\mathrm{N}=10$ |
| :---: | :---: | :---: | :---: | :---: |
| 800 | $\begin{aligned} & 8.260 \times 10^{-4} \\ & \text { at } 57.22^{\circ} \end{aligned}$ | $\begin{aligned} & 8.259 \times 10^{-4} \\ & \text { at } 57.22^{\circ} \end{aligned}$ | $\begin{aligned} & 8.258 \times 10^{-4} \\ & \text { at } 57.22^{\circ} \end{aligned}$ | $\begin{aligned} & 8.258 \times 10^{-4} \\ & \text { at } 57.22^{\circ} \end{aligned}$ |
| 200 | $\begin{aligned} & 3.360 \times 10^{-3} \\ & \text { at }-61.72^{\circ} \end{aligned}$ | $\begin{aligned} & 3.357 \times 10^{-3} \\ & \text { at }-61.72^{\circ} \end{aligned}$ | $\begin{aligned} & 3.357 \times 10^{-3} \\ & \text { at }-61.72^{\circ} \end{aligned}$ | $\begin{aligned} & 3.357 \times 10^{-3} \\ & \text { at }-61.72^{\circ} \end{aligned}$ |
| 300 | $\begin{aligned} & 7.754 \times 10^{-3} \\ & \text { at } \quad 177.87^{\circ} \end{aligned}$ | $\begin{aligned} & 7.740 \times 10^{-3} \\ & \text { at } \quad 177.88^{\circ} \end{aligned}$ | $\begin{aligned} & 7.740 \times 10^{-3} \\ & \text { at } \quad 177.88^{\circ} \end{aligned}$ | $\begin{aligned} & 7.740 \times 10^{-3} \\ & \text { at } \quad 177.88^{\circ} \end{aligned}$ |
| 400 | $\begin{aligned} & 1.423 \times 10^{-2} \\ & \text { at } \quad 56.38^{\circ} \end{aligned}$ | $\begin{aligned} & 1.418 \times 10^{-2} \\ & \text { at } \quad 56.39^{\circ} \end{aligned}$ | $\begin{aligned} & 1.418 \times 10^{-2} \\ & \text { at } \quad 56.39^{\circ} \end{aligned}$ | $\begin{aligned} & 1.418 \times 10^{-2} \\ & \text { at } \quad 56.39^{\circ} \end{aligned}$ |
| 900 | $\begin{aligned} & 2.297 \times 10^{-2} \\ & \text { at }-66.35^{\circ} \end{aligned}$ | $\begin{aligned} & 2.286 \times 10^{-2} \\ & \text { at }-66.37^{\circ} \end{aligned}$ | $\begin{aligned} & 2.286 \times 10^{-2} \\ & \text { at }-66.37^{\circ} \end{aligned}$ | $\begin{aligned} & 2.286 \times 10^{-2} \\ & \text { at }-66.37^{\circ} \end{aligned}$ |
| 600 | $\begin{aligned} & 3.394 \times 10^{-2} \\ & \text { at } \quad 169.47^{\circ} \end{aligned}$ | $\begin{aligned} & 3.372 \times 10^{-2} \\ & \text { at } \quad 169.42^{\circ} \end{aligned}$ | $\begin{aligned} & 3.372 \times 10^{-2} \\ & \text { at } \quad 169.42^{\circ} \end{aligned}$ | $\begin{aligned} & 3.372 \times 10^{-2} \\ & \text { at } \quad 169.42^{\circ} \end{aligned}$ |
| 700 | $\begin{aligned} & 4.649 \times 10^{-2} \\ & \text { at } \quad 43.87^{\circ} \end{aligned}$ | $\begin{aligned} & 4.609 \times 10^{-2} \\ & \text { at } \quad 43.75^{\circ} \end{aligned}$ | $\begin{aligned} & 4.609 \times 10^{-2} \\ & \text { at } \quad 43.75^{\circ} \end{aligned}$ | $\begin{aligned} & 4.609 \times 10^{-2} \\ & \text { at } \quad 43.75^{\circ} \end{aligned}$ |
| 800 | $\begin{aligned} & 5.919 \times 10^{-2} \\ & \text { at }-82.75^{\circ} \end{aligned}$ | $\begin{aligned} & 5.854 \times 10^{-2} \\ & \text { at }-82.99^{\circ} \end{aligned}$ | $\begin{aligned} & 5.854 \times 10^{-2} \\ & \text { at }-82.99^{\circ} \end{aligned}$ | $\begin{aligned} & 5.854 \times 10^{-2} \\ & \text { at }-82.99^{\circ} \end{aligned}$ |
| 900 | $\begin{aligned} & 7.019 \times 10^{-2} \\ & \text { at } 150.46^{\circ} \end{aligned}$ | $\begin{aligned} & 6.92 \pi \times 10^{-2} \\ & \text { at } 150.03^{\circ} \end{aligned}$ | $\begin{aligned} & 6.921 \times 10^{-2} \\ & \text { at } 150.03^{\circ} \end{aligned}$ | $\begin{aligned} & 6.921 \times 10^{-2} \\ & \text { at } 150.03^{\circ} \end{aligned}$ |
| 1000 | $\begin{aligned} & 7.821 \times 10^{-2} \\ & \text { at } 24.46^{\circ} \end{aligned}$ | $\begin{aligned} & 7.680 \times 10^{-2} \\ & \text { at } 23.75^{\circ} \end{aligned}$ | $\begin{aligned} & 7.682 \times 10^{-2} \\ & \text { at } 23.76^{\circ} \end{aligned}$ | $\begin{aligned} & 7.682 \times 10^{-2} \\ & \text { at } 23.76^{\circ} \end{aligned}$ |

Table 2. The magnitude $(A / m)$ and phase (degrees) of the complex magnetic field evaluated for a gap voltage $V=1$ at an observation distance of $R=10 \mathrm{~m}$ and $\theta=\pi / 2$ as a function of frequency and the number of series terms $N$.

| freq (MHz) | $\mathrm{N}=1$ | $N=3$ | $\mathrm{N}=5$ | $\mathrm{N}=10$ |
| :---: | :---: | :---: | :---: | :---: |
| 100 | $\begin{aligned} & 2.198 \times 10^{-6} \\ & \text { at } 57.22^{\circ} \end{aligned}$ | $\begin{aligned} & 2.198 \times 10^{-6} \\ & \text { at } 57.22^{\circ} \end{aligned}$ | $\begin{aligned} & 2.198 \times 10^{-6} \\ & \text { at } 57.23^{\circ} \end{aligned}$ | $\begin{aligned} & 2.198 \times 10^{-6} \\ & \text { at } 57.23^{\circ} \end{aligned}$ |
| 200 | $\begin{aligned} & 8.926 \times 10^{-6} \\ & \text { at }-61.72^{\circ} \end{aligned}$ | $\begin{aligned} & 8.919 \times 10^{-6} \\ & \text { at }-61.72^{\circ} \end{aligned}$ | $\begin{aligned} & 8.919 \times 10^{-6} \\ & \text { at }-61.72^{\circ} \end{aligned}$ | $\begin{aligned} & 8.919 \times 10^{-6} \\ & \text { at }-61.72^{\circ} \end{aligned}$ |
| 300 | $\begin{aligned} & 2.059 \times 10^{-5} \\ & \text { at } 177.87^{\circ} \end{aligned}$ | $\begin{aligned} & 2.056 \times 10^{-5} \\ & \text { at } 177.88^{\circ} \end{aligned}$ | $\begin{aligned} & 2.056 \times 10^{-5} \\ & \text { at } 177.88^{\circ} \end{aligned}$ | $\begin{aligned} & 2.056 \times 10^{-5} \\ & \text { at } 177.88^{\circ} \end{aligned}$ |
| 400 | $\begin{aligned} & 3.778 \times 10^{-5} \\ & \text { at } 56.38^{\circ} \end{aligned}$ | $\begin{aligned} & 3.776 \times 10^{-5} \\ & \text { at } 56.39^{\circ} \end{aligned}$ | $\begin{aligned} & 3.776 \times 10^{-5} \\ & \text { at } 56.39^{\circ} \end{aligned}$ | $\begin{aligned} & 3.776 \times 10^{-5} \\ & \text { at } 56.39^{\circ} \end{aligned}$ |
| 500 | $\begin{aligned} & 6.011 \times 10^{-5} \\ & \text { at }-66.35^{\circ} \end{aligned}$ | $\begin{aligned} & 6.071 \times 10^{-5} \\ & \text { at }-66.37^{\circ} \end{aligned}$ | $\begin{aligned} & 6.071 \times 10^{-5} \\ & \text { at }-66.37^{\circ} \end{aligned}$ | $\begin{aligned} & 6.071 \times 10^{-5} \\ & \text { at }-66.37^{\circ} \end{aligned}$ |
| 900 | $\begin{aligned} & 9.011 \times 10^{-5} \\ & \text { at } 169.47^{\circ} \end{aligned}$ | $\begin{aligned} & 8.952 \times 10^{-5} \\ & \text { at } 169.42^{\circ} \end{aligned}$ | $\begin{aligned} & 8.952 \times 10^{-5} \\ & \text { at } 169.42^{\circ} \end{aligned}$ | $\begin{aligned} & 8.952 \times 10^{-5} \\ & \text { at } 169.42^{\circ} \end{aligned}$ |
| 700 | $\begin{aligned} & 1.234 \times 10^{-4} \\ & \text { at } 43.87^{\circ} \end{aligned}$ | $\begin{aligned} & 1.224 \times 10^{-4} \\ & \text { at } 43.75^{\circ} \end{aligned}$ | $\begin{aligned} & 1.224 \times 10^{-4} \\ & \text { at } 43.75^{\circ} \end{aligned}$ | $\begin{aligned} & 1.224 \times 10^{-4} \\ & \text { at } 43.75^{\circ} \end{aligned}$ |
| 800 | $\begin{aligned} & 1.572 \times 10^{-4} \\ & \text { at }-82.75^{\circ} \end{aligned}$ | $\begin{aligned} & 1.554 \times 10^{-4} \\ & \text { at }-82.99^{\circ} \end{aligned}$ | $\begin{aligned} & 1.554 \times 10^{-4} \\ & \text { at }-82.99^{\circ} \end{aligned}$ | $\begin{aligned} & 1.554 \times 10^{-4} \\ & \text { at }-82.99^{\circ} \end{aligned}$ |
| 900 | $\begin{aligned} & 1.864 \times 10^{-4} \\ & \text { at } 150.46^{\circ} \end{aligned}$ | $\begin{aligned} & 1.837 \times 10^{-4} \\ & \text { at } 150.03^{\circ} \end{aligned}$ | $\begin{aligned} & 1.838 \times 10^{-4} \\ & \text { at } 150.03^{\circ} \end{aligned}$ | $\begin{aligned} & 1.838 \times 10^{-4} \\ & \text { at } 150.03^{\circ} \end{aligned}$ |
| 1000 | $\begin{aligned} & 2.076 \times 10^{-4} \\ & \text { at } 24.45^{\circ} \end{aligned}$ | $\begin{aligned} & 2.039 \times 10^{-4} \\ & \text { at } 23.75^{\circ} \end{aligned}$ | $\begin{aligned} & 2.040 \times 10^{-4} \\ & \text { at } 23.76^{\circ} \end{aligned}$ | $\begin{aligned} & 2.040 \times 10^{-4} \\ & \text { at } 23.76^{\circ} \end{aligned}$ |

Table 3. The total radiated power (W) evaluated for a gap voltage $V=1$ at an observation distance of $R=10 \mathrm{~m}$ and $\theta=\pi / 2$ as a function of frequency and the number of series terms N.

| freq (MHz) | $\mathrm{N}=1$ | $\mathrm{~N}=3$ | $\mathrm{~N}=5$ | $\mathrm{~N}=10$ |
| :---: | :---: | :---: | :---: | :---: |
| 100 | $7.606 \times 10^{-7}$ | $7.606 \times 10^{-7}$ | $7.606 \times 10^{-7}$ | $7.606 \times 10^{-7}$ |
| 200 | $1.257 \times 10^{-5}$ | $1.256 \times 10^{-5}$ | $1.256 \times 10^{-5}$ | $1.256 \times 10^{-5}$ |
| 300 | $6.689 \times 10^{-5}$ | $6.689 \times 10^{-5}$ | $6.689 \times 10^{-5}$ | $6.689 \times 10^{-5}$ |
| 400 | $2.252 \times 10^{-4}$ | $2.252 \times 10^{-4}$ | $2.252 \times 10^{-4}$ | $2.252 \times 10^{-4}$ |
| 500 | $5.870 \times 10^{-4}$ | $5.870 \times 10^{-4}$ | $5.870 \times 10^{-4}$ | $5.870 \times 10^{-4}$ |
| 600 | $1.281 \times 10^{-3}$ | $1.281 \times 10^{-3}$ | $1.281 \times 10^{-3}$ | $1.281 \times 10^{-3}$ |
| 800 | $2.403 \times 10^{-3}$ | $2.403 \times 10^{-3}$ | $2.403 \times 10^{-3}$ | $2.404 \times 10^{-3}$ |
| 800 | $3.898 \times 10^{-3}$ | $3.898 \times 10^{-3}$ | $3.898 \times 10^{-3}$ | $3.898 \times 10^{-3}$ |
| 900 | $5.480 \times 10^{-3}$ | $5.481 \times 10^{-3}$ | $5.481 \times 10^{-3}$ | $5.480 \times 10^{-3}$ |
| 1000 | $6.802 \times 10^{-3}$ | $6.806 \times 10^{-3}$ | $6.806 \times 10^{-3}$ | $6.806 \times 10^{-3}$ |

## 3. EXPERIMENTAL EVALUATION OF THE SPHERICAL RADIATOR

The spherical radiator circuits were first tested individually to evaluate the performance of the major components. This evaluation was performed concurrently with the final circuit design to verify that operation and performance specifications were realized. The alignment and setup procedures outlined in section 4 were developed during this time. These preliminary measurements also examined the overall quality and stability of the rf optical link and general system performance. The data shown in figures 2, 3, and 4 demonstrate the signal purity attained by the laser transmitterreciever link. The input signal from a signal generator (left graphs of figures 2 and 3 ) which modulates the laser and the resulting output signal (right graphs) after being demodulated by the optical receiver and amplified by the MMIC amplifier inside the sphere are shown in figures 2 and 3. The data show no spurious signals being generated by the rf optical link even at this maximum signal level. The data clearly show that when the input contains
harmonic signals, these signals will be present in the output. Special care should be exercised when using broadband devices to detect the signal from such a source. The gap voltage detector is such a broadband device and will give an indication of the total contribution from all signals present. There is no correction applied for the simple $50 \Omega$ coax probe used to pick off the signal at the amplifier output and this may account for some of the amplitude variations seen in these figures. Figure 4 shows the frequency response attained by the rf optical link with a constant input to the laser. The frequency is swept from 50 to 1300 MHz . Again there is no correction for the coax probe, but the data clearly indicate a usable bandwidth beyond the 1000 MHz set as a design goal.

The second part of the experimental evaluation examined the spherical radiator transmitting in several environments over a frequency range of 10 MHz to 1000 MHz . The facilities used for radiated field measurements included the TEM cell, anechoic chamber, and open area test site (OATS). The measurements were designed to determine the free-space radiation pattern, power output, and gap voltage indicator transfer function. The radiation pattern and radiated power are necessary to determine how closely the sphere acts as a dipole antenna given all the added material inside the sphere and also the fiber optic control lines which exit the sphere at the equator and connect to the control unit. The closer the measured data follows the predicted data for a perfect spherical dipole, the more accurately radiated fields can be calculated using the theory of section 2. The ability to monitor the rf voltage at the radiating gap around the sphere's equator provides the information necessary to make this calculation and also provides a reference point for repeating a radiating condition. The diode detector, which is described in section 4, has complicated circuitry involved in transmitting the detected voltage to the front panel indicator on the control unit. This circuitry includes an amplifier, voltage-to-frequency converter, optical transmitter/receiver, frequency-to-voltage converter, and additional amplifiers. While the dc components can be aligned and well characterized, the overall rf-to-dc conversion must be calibrated by measurement of the radiated signal. Any direct contact probing of the rf signal in the vicinity of the dipole gap resulted in adverse loading on the final rf amplifier. Direct probing also ignores the actual impedance of the balun and radiating sphere because the hemispheres must be removed to access the rf circuits. The calibration for the gap voltage indicator is
then a comparison between the predicted and measured field strength. This scale factor is shown on each radiation pattern figure. The scale factor is the actual gap voltage, determined by calculations, which would produce the measured field. All measurements were performed with a gap voltage indicator reading of 1.0 V .

The small size of this radiator made it compatible with using a TEM cell as a tool for evaluation at frequencies of 100 MHz and below. The radiator was positioned inside the TEM cell at six unique orientations while maintaining a constant output power and frequency. The sum and difference power and relative phase angle were measured at each position as prescribed by the TEM cell emissions technique $[13,14]$. The source, in this case the spherical radiator, is modeled by orthogonal electric and magnetic dipoles. These equivalent source components are then determined by measurements of power and phase from the two TEM cell ports through a $0^{\circ}-180^{\circ}$ hybrid junction. These measurements provide sufficient data to calculate the radiation pattern and power radiated from the sphere.

Figures 5 through 10 show the results of radiating a signal in a TEM cell with a cross section of $1.2 \times 1.2 \mathrm{~m}$, processing the data as described, and comparing the pattern information with predicted free-space values. The predicted pattern is scaled as noted on each figure to match the maximum values of the measurement based data. The solid lines are calculated using the theory of section 2 and the dotted lines represent two patterns calculated from measurement data at $\phi=0^{\circ}$ and $90^{\circ}$. These data show that the sphere acts very much like the ideal spherical antenna at these frequencies. The scale factor shown on the graphs can be used along with the gap voltage indication and the theory of section 2 to predict the free-space fields from the spherical radiator.

The open area test site (OATS) with a $30 \mathrm{~m} \times 60 \mathrm{~m}$ flat ground screen was used to measure radiated field strength from the spherical radiator. The reflected wave from the ground plane was compensated for by correcting the received signal by the amount contributed by such a reflected signal. The value for the correction was determined by accurately positioning the radiating sphere and the calibrated receiving antenna as in figure 11,
assuming a perfectly conducting ground reflection and then calculating the contribution using [15]

$$
\begin{align*}
\frac{\left|E_{t o t a l}\right|}{\left|E_{d i r}\right|} & =\frac{\left|E_{d i r}+E_{r f 1}\right|}{\left|E_{d i r}\right|} \\
& =\frac{\left|\frac{e^{-j \beta d}}{d}+\Gamma \frac{e^{-j \beta r}}{I}\right|}{\left|\frac{e^{-j \beta d}}{d}\right|}  \tag{26}\\
& =\sqrt{1+\left(\frac{\Gamma d}{r}\right)^{2}+\left(\frac{2 \Gamma d}{r}\right) \cos \phi}
\end{align*}
$$

where

$$
\begin{align*}
& d=\sqrt{D^{2}+\left(h_{T}-h_{R}\right)^{2}} \quad m \\
& r=\sqrt{D^{2}+\left(h_{T}+h_{R}\right)^{2}} \quad m \\
& \Gamma=\left\langle\begin{array}{l}
-1, \text { horizontal } \\
+1, \text { vertical }
\end{array}\right.  \tag{27}\\
& \phi=1.2 F(r-d) \text { degrees } \\
& F=\text { frequency, MHz. }
\end{align*}
$$

The data shown in figures 12 through 23 were taken at a separation distance of $D=10 \mathrm{~m}$, transmitter height of $h_{T}=2 \mathrm{~m}$, and $a$ receiving antenna height adjusted for maximum response.

The radiation pattern begins to show degradation from a perfect dipole at 700 MHz and improves again near 1000 MHz . There is also minor deviation at some lower frequencies ( 400 to 600 MHz ) which are likely to be caused by misalignment and measurement problems. However, the pattern characteristics in the 700 to 900 MHz range show extensive distortion and reduced output level.

The root cause for this distortion in the pattern must lie with the non-uniformity of the feed voltage around the equator (gap). The theory described in section 2 assumes a uniform gap feed voltage and, if that condition is satisfied, a 10 cm sphere does not show an irregular pattern shape at frequencies below 1000 MHz . In fact the dipole pattern is predicted to remain intact well above 3000 mHz . The pattern irregularity must then be caused by internal conditions related to the ability to apply a uniform voltage to the entire gap area. The character of the pattern distortion is
consistent with possible internal resonances which distort the gap feed and absorb power. An analysis of the internal volume of the sphere including all the circuitry, batteries, and the dipole feed system has not yet been attempted. A cursory look at spherical modes and resonances in a perfect spherical volume enclosed within a perfectly conducting surface [16] also indicates that the lowest frequency for this to occur is well above the problem area. Additional work is needed to model the complex internal structure and redesign the feed to reduce the distortion. The pattern irregularities should not diminish the utility of the spherical dipole for its intended use as an intercomparison or transfer standard device, but they make it more difficult to theoretically predict the radiated field strength at these higher frequencies.

Antenna pattern measurements taken in an anechoic chamber from 200 to 1000 MHz show the same character as that seen on the open field site. Figures 24 through 32 compare the electric field calculated using the theory in section 2 and adjusted by the listed scale factor to the measured electric field. These data were taken with a 3 m separation distance between sphere and receiving antenna due to the limited space inside the anechoic chamber. The measured pattern amplitude was then extrapolated to 10 m distance for comparison to the open area test site. There were two patterns measured at each frequency, $\phi=0$ and $\pi / 2$, and both are presented on these graphs. As the overall pattern begins to distort at the higher frequencies these orthogonal measurements show less resemblance to each other.

These measurements have provided a partial picture of the spherical dipole character from 10 to 1000 MHz . Figure 33 is a summary of the scale factors for all the data presented in figures 5 through 10 and 12 through 32. The scale factor must be determined at frequencies not represented in these measurements if field strength predictions are to be made based upon gap voltage indications. The radiator and the gap voltage detector demonstrated good repeatability and would be useful for relative measurements without extensive scale factor calibration.

## 4. DESIGN CONSIDERATIONS

The spherical dipole radiator system was designed to expand the capabilities of earlier devices which used fixed-frequency combtype oscillators to generate the radiating signal. This system was
intended to provide advanced features that will allow it to be incorporated into a modern automated test system and permit the automated test system to control and monitor the frequency and amplitude of the radiated signal. General design goals for the new radiator system were established to take advantage of recent developments in the areas of optical communication, wide bandwidth MMIC amplifiers, and new integrated circuits. The new system was intended to
(1) have continuous frequency coverage from 10 MHz to 1.0 GHz and be suitable for swept frequency, modulated cw , and other automated measurements,
(2) provide at least 40 dB of amplitude dynamic range,
(3) have the rf signal derived from an external signal generator (in keeping with an automated system),
(4) provide a direct indication on the control unit of the gap rf voltage and the ambient temperature inside the sphere,
(5) have all circuitry within the sphere operate on battery supplies and be designed for maximum operating time plus have a provision for remote (at the control unit) on/off,
(6) provide audio and visual alarms for malfunctions or low battery, and
(7) make use of optical cable for all control and signal lines connecting to the sphere.

A block diagram of the complete radiator system is shown in figure 34. The radiator system consists of the spherical radiator with a 10 cm outside diameter and a control unit to interface to the operator and signal source. The two parts are connected by a fully dielectric optical fiber cable. This optical fiber cable is used to carry all the necessary signals between the control unit and sphere. Specific design criteria and rationale for each part of the radiator system are described below.

As was discussed in the introduction, the geometry for the radiator was chosen to be a spherical dipole. This shape allows some flexibility in packaging components within the sphere. Another concern was the diameter. A large sphere would provide much space for components and reduce the effort necessary for packaging plus it would provide more signal strength at lower frequencies. On the other hand, a large sphere would not be as useful in evaluating small enclosures where the smallest possible source is desired. A small sphere will extend the upper usable frequency and provide a compact source which more closely appears as a point source, but with a loss of output at the lower frequency range. Previous spherical radiators were on the order of 10 to 12 cm and these were quite successful. After examining the space requirements, a 10 cm diameter sphere was selected.

The sphere is divided into two hemispheres by a threaded dielectric spacer. This spacer also provides a mounting surface for the circuit board and the optical cable strain relief. The battery packs are then mounted to the circuit board and extend into both hemispheres. Figure 35 is a cross section of the spherical dipole and details this design. Additional details relating to the circuit design can be found in section 5.

### 4.2 Control Unit

The control unit had no specific tradeoff considerations as did the sphere. This unit is basically there to house the laser transmitter, other optical components used to control the sphere, displays and output ports, battery charging circuits, and power supplies. These components fit compactly within a $7.6 \times 48.3 \mathrm{~cm}$ (3 in x 19 in ) rack mountable case. The circuit details can be found in section 5 .

### 4.3 Optical Components and Cable

The use of a fiber optic link to the radiating spherical dipole provides complete electrical isolation of the unit. It also gives freedom from electromagnetic interference and distortion of the radiating field that is normally found with conducting leads. In addition, it allows the radiation of a field at a selectable
frequency and amplitude. This is in contrast to previous radiating spherical dipoles that use comb generators to radiate fields in several narrow frequency bands simultaneously and have amplitudes that vary according to battery charge. The added control that is available by using the optical link allows the unit to be used for accurate swept frequency measurements with programmable spectral profiles. In order for the sphere to perform its primary function in a reliable and well characterized way, there is a need to monitor its output and to minimize battery drain by having some control over its on-off status. These functions are also admirably performed through fiber optic links.

Clearly it would be cumbersome to have four individual optical cables to route every time the sphere was to be relocated. We thus procured custom built composite optical cable which consisted of two single mode fibers for 1300 nm operation and four multimode fibers (one spare of each type). The cable is a ruggedized design intended for field use and incorporates two layers of Kevlar fibers and plastic coatings. Also included between the layers are some stiffening members to help prevent kinking of the fibers.

The system uses two lengths of the optical cable. A shorter ( 10 m ) length was specially prepared and one end permanently attached to the sphere. This was due to the fusion splice used on the single mode rf link and the space restrictions of the sphere. The other end was fitted with precision optical connectors. A longer ( 50 m ) length with connectors at both ends is used to provide the bulk of the cable length between the control unit and the sphere. A plastic junction box which houses the optical barrel connectors and protects the ends of the fibers is used to connect the two cables.

### 4.4 Analog rf Link

An analog rf fiber optic link was chosen to give maximum signal fidelity, very low noise, and a high degree of control over the amplitude and frequency of the radiating field. It was desirable to purchase commercial products when available and then design the rest of the system around these components.

Several commercially available analog components and systems were evaluated in-house. The space and power available in the sphere plus the analog signal requirements limited the choices for the optical receiver. The unit chosen proved to be substantially
superior to other units considered because of very low power requirements ( 45 mA at 9 V and 5 mA at -5 V ), a very flat frequency response up to above 1 GHz , excellent dynamic range, and was available in a small 14 pin surface mount package. The receiver itself was marginally capable of providing the desired 0 dBm of power to the dipole gap when driven at maximum power. The bias current requirement is increased and the linearity becomes degraded at maximum power so it is better not to operate in that region. A solution to this involved adding an wideband MMIC amplifier following the receiver and lowering the optical carrier power and modulation depth into the reciever. A nominal value of -12 dBm optical power was found to be a minimum setting which provided sufficient drive to the MMIC amplifier to reach the 0 dBm of rf power desired at the dipole gap. This allowed the receiver to operate well below the maximum signal to insure its linearity and stability. The bias current savings into the receiver are consummed by the additional amplifier circuit and the amplifier must be carefully shielded and isolated from the receiver to prevent oscillations, but the overall analog signal performance improvements are worth the effort.

The analog microwave fiber optic transmitter (laser) used in this system proved to be an excellent low noise companion to the receiver. The unit is designed for direct modulation of the laser with an external analog signal. Since it produces about -3 dBm of optical power out of the fiber pigtail, it was necessary to add about 7 dB of optical attenuation (above connector and fiber losses of about 2 dB ) in the link to bring the carrier to the desired -12 dBm level. The optical attenuator is housed in the control unit. This system used an adjustable attenuator and by using an optical power meter was set to the correct value.

In order to preserve the low noise characteristics of the optical transmitter it is necessary to reduce the reflections from all fiber connections to the lowest reasonably obtainable values. This is because light reflected back into the laser causes instabilities in the mode structures and is also detected in the photodiode monitoring and feedback control circuitry. The best way to reduce reflections is to use fusion splices for all the fiber connections. Although we did use a fusion splice between the fiber on the receiver and the 10 m pigtail attached to the sphere, it was necessary, because of handling and cable routing during use, to be able to disconnect the sphere and optional 50 m cable link. For this reason, high quality connectors which have low reflection
(high return loss) were selected for the cable links. The high return loss is accomplished by polishing the end of the fiber and ferrule at a slight slant, so that reflected light does not couple back into the fiber core.

### 4.5 Voltage and Temperature Monitoring Links

A primary element in the design concept for the spherical dipole radiator was the ability to accurately monitor the voltage across the dipole's gap in order to calibrate the amplitude of the radiation field, and control it by feedback. Also since the required monitoring circuits are expected to show some sensitivity to the large temperature variations anticipated in field use, we thought it was also important to monitor the unit's temperature and characterize the temperature dependence of its output. This would also enable the user to remove or protect the unit if it appears to overheat from solar absorption.

It was also desirable for the monitoring links to be both reliable and relatively inexpensive. In terms of reliability, it is important that the signals from the monitoring circuits should be independent of the optical power in the link. This is important since the optical power varies both with the temperature of the transmitter and with the cleanliness and quality of the optical connections.

To meet these goals we chose a multimode fiber link with 850 nm LED sources in ST style receptacles inside the sphere. The components are readily available from a number of manufacturers and suppliers. The connectors between the fiber sections and at the control unit are a different style. Since we chose special slant polish connectors from one supplier for the singlencided to use multimode connectors on the cables and PIN photodiode receptacles from the same supplier. This was done primarily as a convenience and to save time by getting all the connectors installed on the patch cords by a single supplier. In retrospect, it appears more desirable to use ST style connectors and receptacles throughout the monitoring links.

To free the response of the monitor links from dependence on optical power level, we converted the measured voltages to frequencies for the LEDs and then reconverted from frequency back to voltage in the base electronics unit. To keep power drain low
the voltage-to-frequency converters were operated at 100 kHz and below with a fixed pulse duration set for a 50 percent duty cycle at the highest frequency.

### 4.6 Power Control Link

Power requirements for the electronics in the sphere limit the operation time between battery recharges to about two hours. However, much of the time a unit is in the field or in a test chamber is actually spent in setup and preparation rather than actual measurements. There are three small switches located inside the sphere for turning battery power on and off, but it is not always convenient to disturb the measurement and access these switches. We, therefore, chose to use an additional optical link to switch the sphere electronics on and off remotely from the base control unit. Thus the sphere is fully powered only during relatively brief periods when actual measurements are being made. With this addition, the useful life of a single battery charge can be preserved much beyond the two hour limit for continuous operation. The optical link that is used for this purpose is very similar to those for the voltage and temperature monitors. In this case an 850 nm LED in the base control unit is coupled through a multimode fiber to a photo-Darlington transistor in the sphere.

## 5. CIRCUIT OPERATIONS AND CONSTRUCTION DETAILS

In this section we will present an operation and design overview for each circuit in the radiator system. The schematic diagrams begin with figure 36. The reader is urged to refer to the system block diagram (figure 34) and the base control unit block diagram (figure 43) to reference these individual circuits to their location in the system.

### 5.1 Spherical Radiator Functions

The sphere halves function as the radiating surfaces of the dipole. The volume inside the sphere contains the following system functions:
(1) Battery supplies and related control circuits and voltage or current regulation networks for the various circuits of the sphere.
(2) Fiber optic up and down links that carry rf excitation, rf level, and temperature information.
(3) Fiber optic PINFET receiver (rf excitation mentioned in item 2) and MMIC amplifier that constitutes the rf source which excites the hemispheres.
(4) Individual circuits that realize the functions of 1,2 , and 3 described above.

The base control unit interfaces between the sphere and rf signal source. This unit aids the operator by monitoring several of the system parameters. The following are specific base unit functions:
(1) Charging the sphere batteries through the use of built in constant current sources.
(2) Continuous monitoring of the laser and sphere power status with operator alarms.
(3) Switching sphere battery power off and on by a light carrier on one of the fiber optic links.
(4) Modulating a laser driven fiber optic uplink by the operators' rf signal source.
(5) Monitoring the operating temperature of the sphere and the rf level of the sphere's gap voltage with fiber optic downlink subsystems.
5.2 Sphere Circuitry

A description of the sphere starts with figure 36 . This is a block diagram of the various circuits which distribute dc supply power to the various circuits found inside.

The sphere's batteries are connected to the internal circuits through three miniature switches mounted on the circuit board, one
for each battery pack. Power status is verified by viewing three miniature LEDs (light emitting diodes) adjacent to the switches on the printed circuit board. At the time these three switches are closed and the battery voltages are applied to the circuits, the regulators IC3 and IC4 of figure 37 are latched in the "off" state. Transistors Q100 and Q102 are conducting, but Q101 is off. When the base control unit sphere power switch (S1 of figure 38) is activated, the current through the light emitting diode (D53) immediately increases to 60 mA and D53 illuminates the fiber-optic line which in turn switches the photo-Darlington transistor Q103 of figure 37 to the conductive state. This turns on transistor Q101 and turns off Q100 and Q102. Voltage regulators IC3 and IC4 are activated and supply +9 and +5 V regulated voltages to the sphere circuitry. These regulators are "smart" regulators which regulate the output, monitor the supply battery voltage and disconnect the supply from the load should the battery voltage drop too low. The first supply battery to become discharged under normal conditions is the 12 V battery supplying the regulator IC3 (9 V output). As the 12 V battery discharges, IC3 maintains a regulated output until that output level drops to 5 percent below the set value or 8.55 V . At this point, pin 5 of $I C 3$ is forced to ground ( 0 V ) which turns on Q100 (latching transistor). This activates shutdown pins (pin 3) on IC3 and IC4 which disconnect the supply batteries from their associated loads. In this latched off or shutdown condition the regulators remain off even though the supply voltages rise after the load is removed. Also, when shutdown, IC3 and IC4 will draw less than $100 \mu \mathrm{~A}$. The negative voltage regulator, IC5, is used under low current conditions and does not require special protection.

The temperature of the sphere is determined from an AD590 silicon temperature transducer IC12. The device is biased so that it produces a $1 \mathrm{mV} / \mathrm{K}$ linear voltage output. Figure 39 shows the transducer connected to an AD654JR (IC8) voltage to frequency converter. Resistor R147 is adjusted to provide a 1 mA full scale current with enough trim range to accommodate the AD654JR's 10 percent FS error and components' tolerances. The transfer function of this circuit is a 100 kHz square wave 50 percent duty cycle pulse train at 1.0 V of input. A monostable retriggerable multivibrator (IC7) was used to maintain a fixed pulse width while the repetition rate is decreased to clock frequencies below 100 kHz . This results in a very short duty cycle at lower repetition rates (frequencies) corresponding to input voltages less than 1 V . The duty cycle rises to 50 percent only when the input voltage
reaches 1 V . This scheme was used to greatly reduce battery drain. The pulse train is then converted to optical energy using Q106 which drives the HFBR-1404 LED fiber optic transmitter D108.

Figure 40 shows how the rf gap voltage is detected. A dual matched JFET, Q104, provides a pair of constant current sources for Schottky diodes D105 and D106. The resistors and capacitors in this bridge circuit are used for ac filtering purposes. The reason for using this kind of balanced detector circuit is to minimize the effects of temperature on the sensitive rf detector diode D105. The rectified and filtered voltage from D105 is then amplified by the differential amplifier ICll. This amplified dc voltage drives the AD654JR (IC6) voltage-to-frequency converter shown in figure 41. This circuit functions exactly like that of figure 39 with the same transfer function.

The most important function of the sphere is to radiate electromagnetic energy at the frequency of the modulated laser light sent by the fiber optic uplink. Figure 42 shows a GaAs IC PINFET fiber optic receiver which is used to drive a MMIC phase linear amplifier. This circuitry excites the sphere through the impedance matching transformer TP-103 loaded with R106. This circuit amplifies the $r f$ signal to a maximum 0 dBm over the frequency range of 10 MHz to at least 1 GHz . The PINFET and MMIC circuit appear to be straightforward in design. In reality its function is the most difficult to fabricate due to electromagnetic compatibility considerations. Stray circulating rf fields can and have created problems in other circuitry with prototypes. Most of the problems have been solved by careful parts layout and shielding. The amplifier, balun, and dipole feed structure are contained within a small shielded printed circuit board which is mounted as a unit onto the main board. The output of the receiver is transfered to the amplifier through a short section of miniature coaxial cable.

### 5.3 Base Control Unit Circuitry

Figure 43 shows the various circuits of the base control unit. A circuit in the base control unit monitors the status of the laser temperature, laser output power, and sphere batteries. In figure 38, three comparators sense these functions. In normal operation D109 and D111, which are green LEDs, signal the operator that the
laser is within acceptable operational limits. If the laser should experience difficulty, D110 and or D112 will light red and the audio alarm will sound at one tone.

Control of the sphere's power is invoked by closing switch Sla and exciting D53 of figure 38. Light from this LED is fed by fiber to Q103 of figure 37 and the sphere remains powered up until the regulated +9 V supply circuit drops below 8.55 V . If this occurs, D114 of figure 38 will signal red and the audio alarm will sound with another tone frequency.

The largest demand of current from the sphere battery power supplies is the +12 V system which is regulated at +9 V . It is for this reason that this battery system is monitored. When batteries need recharging, the sphere is opened, the internal power switches are turned off, and the appropriate connector is attached to the base unit's charging circuit which is shown in figure 44. Constant current sources made from JFET devices are used to supply the required charging rates. These current sources can be adjusted to provide the recommended current values by changing the value of the associated feedback resistor in the source to gate loop for each charging line. These resistors are R70, R71, R75, R78, R79, and R80. The JFETs Q54, Q55, and Q56 on the quick charge group may have to be preselected to provide sufficient drain to source current $I_{\text {dss }}$ to reach the recommended levels. The following table shows the applicable parameters.

Table 4. Current limits for the battery charging circuits.

| Battery System | Normal Charge | Quick Charge |
| :---: | :---: | :---: |
| +12.2 V | 10.0 mA | 30.0 mA |
| +7.2 V | 7.0 mA | 21.0 mA |
| -7.2 V | -7.0 mA | -21.0 mA |

Each charging circuit is fused at 0.125 A .

The sphere data downlink receiving circuits shown in figures 45 and 46 are used for both the temperature and rf level. These two downlinks share identical circuit design throughout and while the temperature link (figure 39) and the rf level (figure 41) transmitting circuits in the sphere are shown explicitly, the two
receiving circuits in the control unit are shown with a single set of schematics (figures 45 and 46 ). Due to relatively large tolerances associated with several components in the receiving circuit (e.g., IC1 and IC2), the circuit boards are preselected such that the one which calibrates over the largest range ( 0 to 1.0 $V$ dc) with the best accuracy is used for the rf level. Since the other channel relates to temperature in Kelvin, a unit accurate in the range of 250 to 350 mV is adequate. These are practical guidelines and in actual practice both receiving channels usually operate adequately over the entire range.

The NE5212 in figure 45 is a transimpedance amplifier designed for the recovery of fiber optic signals in applications where very low signals are obtained from high impedance sources such as Dl. The recovered pulse train is amplified by IC14 (OP-37) and converted back to a dc voltage by the frequency-to-voltage converter IC2 (AD650JN). Because the rms (root-mean-square) value of the measurement is desired, an AD637JQ average dc-to-rms convertor is used as shown in figure 46. Further adjustment of the transfer function including offset is accomplished with a final operational amplifier IC15. This amplifier also drives a digital panel meter.

The following alignment procedure for a receiver card should be followed if a card is to be replaced or if measurements indicate a faulty transfer function:
(1) Power up the receiver board while monitoring the currents with suitable meters. The +15 and -15 V lines will draw around 16 mA each and the +5 V line will draw about 24 mA.
(2) Without an input signal applied to the frequency-tovoltage convertor (IC1), adjust R9 of figure 45 to produce 0 V dc at TP17 (test point 17).
(3) Remove J2 of figure 46 and ground pin 3 of IC15. Adjust R32 for 0 V dc at TP19. Replace J2 after this is completed.
(4) Pull Jl of figure 46 and ground pin 13 of the dc-to-rms convertor (IC2). Adjust R17 for 0 V dc at TP18.
(5) Apply 1.0 V dc from an external source between ground and pin 13 of IC2. Adjust R23 for an output of 1.0 V dc at TP18. Also, adjust R25 for 1.0 V dc at TP19.
(6) Adjust R22 fully clockwise for maximum smoothing of any ripple that might appear on the waveform.
(7) Replace jumper J1.
(8) Power up the fiber optic transmitter.
(9) Connect a fiber optic link between the transmitter and the receiver.
(10) At TP8 of figure 41 , set the input to the voltage-tofrequency convertor (IC6) at pin 4 for 1.0 V .
(11) At this voltage adjust the output frequency using R142, as seen at pin 1 , for 100.0 kHz . The duty cycle here will appear to be around 50 percent.
(12) With the 1.0 V setting and the fiber optic line in place, adjust $R 7$ on the receiver card (figure 45) to produce a 1.5 V peak pulse reading at TP15.

CAUTION: If R7 of figure 45 is set too low, no signal will be present at TP16. If the setting is too high, the frequency output at TP16 will be doubled because the comparator in ICl is double triggering.
(13) Adjust the input voltage to be 200 mV and check to see that R22 is set for minimum ripple at TP18.
(14) Next, vary the input voltage Vin between 20 mV and 1.2 V dc and observe the transfer function by recording vin, Vf/v, Vrms, and Vout.
(15) If the error (Vin - Vout) $x$ 100/Vin (in percent) is greater than 1 percent at $V i n=500 \mathrm{mV}$ or $>4$ percent with Vin $=100 \mathrm{mV}$, change the frequency by four or five percent and repeat the measurements. If the tracking error is within 1 percent proceed to step 19.
(16) If the tolerances in step 15 can not be accomplished, return the frequency to 100 kHz at 1 V and adjust Vin to be 300 mV dc.
(17) Adjust R13 of figure 45 to produce 300 mV dc at TP19 of figure 46.
(18) Vary Vin between 250 and 350 mV dc and check the output tracking. The maximum error over this range should not exceed $\pm 0.5$ percent.
(19) A receiver card that tracks within the tolerance of step 15 is suitable for gap voltage use and a card that can only function as described in step 18 is adequate for temperature measurements. Improvements to the internal circuits within the integrated circuits may be necessary to reduce the tracking errors seen in this system.

This completes the alignment procedure for the receiver circuitry.

The remaining figures (47 through 51) are provided as a guide to locate the parts referenced in the text. These assembly drawings show the physical location on the circuit boards for all components listed in Appendix B (parts list). Figure 47 also details the connections for all components in the base control unit chassis.

## 6. CONCLUSIONS

This effort to design and realize a standard radiator for electromagnetic signals with a wide bandwidth and large dynamic range which could be incorporated into modern automated test systems has been successful. While this paper deals primarily with the design and construction details for this standard radiator, the real value of this device will be determined by the possible insight to be gained from measurements performed with this standard. The use of such a characterized radiator as an intercomparison standard by electromagnetic interference testing laboratories will assist the continuing efforts to improve these measurements.

There is much more work to be done to formalize the standard operating practice related to this radiator. The design allows for a wide range of possiblilies and only experience in the field will
provide the information needed to bring these devices into service as intercomparison or reference standards.

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## Appendix A

## FORTRAN and BASIC Programs

Calculate Electromagnetic Fields from a Spherical Source

## FORTRAN program listing

Calculate the electric and magnetic fields and radiated power from a sphere with small gap excited by a uniform voltage.

```
COMPLEX EFIELD,HFIELD,MAGEFD,MAGHFD,HFCJ,J,SUMPWR1
REAL PI,K,PWR,PWR1
INTEGER N
OPEN(UNIT=6,FILE='SPHDAT',STATUS='UNKNOWN')
PRINT*,'ENTER THE FREQUENCY IN MHZ'
READ (5,*) FREQ
WRITE(6,*) 'THE FREQUENCY IN MHZ'
WRITE (6,*) FREQ
FREQ=FREQ*I. OE+06
PRINT*,'ENTER THE GAP VOLTAGE'
READ(5,*) V
WRITE(6,*) 'THE GAP VOLTAGE'
WRITE(6,*) V
PRINT*,'ENTER THE RADIUS OF THE SPHERE IN METERS'
READ (5,*) A
WRITE(6,*) 'THE RADIUS OF THE SPHERE M'
WRITE(6,*) A
PRINT*,'ENTER THE NUMBER OF SPHERICAL MODES TO BE SUMMED'
READ(5,*) NM
WRITE(6,*) 'THE NUMBER OF MODES'
WRITE(6,*) NM
PRINT*,'ENTER THE FIELD OBSERVATION DISTANCE IN M'
READ(5,*) R
WRITE(6,*) 'THE FIELD OBSERVATION DISTANCE M'
WRITE(6,*) R
PRINT*,'ENTER THE NUMBER OF ANGULAR STEPS'
READ(5,*) NSTEPS
WRITE(6,*) '# OF ANGULAR STEPS'
WRITE(6,*) NSTEPS
NSTEPS1=NSTEPS+1
PI=4.0*ATAN(1.0)
J=(0.0,1.0)
ANG=0.0
DO 100 I=1,NSTEPS1
THETA=PI/180.0*ANG
K=2.0*PI*FREQ/3.0E+08
CALL FIELD(A,R,THETA,FREQ,NM,EFIELD,HFIELD,SUMPWR1)
CALL POLR(EFIELD,MAGEFD)
CALL POLR (HFIELD,MAGHFD)
HFCJ=REAL (HFIELD) -J*AIMAG (HFIELD)
```

```
PWR=0.5*V*V*REAL(EFIELD*HFCJ)
PWRI=V*V*ABS (EFIELD) *ABS (EFIELD) / (2.0*377.0)
SUMPWRI=V*V*SUMPWR1
```

| $\operatorname{WRITE}(5, *)$ | 'ANGLE, E-FIELD MAG \& PHASE (DEG)' |
| :--- | :--- |
| $\operatorname{WRITE}(6, *)$ | 'ANGLE, E-FIELD MAG \& PHASE (DEG)' |
| $\operatorname{WRITE}(5, *)$ | 'H-FIELD MAG \& PHASE' |
| $\operatorname{WRITE}(6, *)$ | 'H-FIELD MAG \& PHASE' |
| $\operatorname{WRITE~}(5, *)$ | 'POWER DENSITY-W/M^2 \& THE COMPLEX POWER' |
| $\operatorname{WRITE~}(6, *)$ | 'POWER DENSITY-W/M^2 \& THE COMPLEX POWER' |
| $\operatorname{WRITE~}(5, *)$ | ANG,MAGEFD |
| $\operatorname{WRITE~}(6, *)$ | ANG,MAGEFD |
| $\operatorname{WRITE~}(5, *)$ | MAGHFD |
| $\operatorname{WRITE~}(6, *)$ | MAGHFD |
| $\operatorname{WRITE~}(5, *)$ | PWR |
| $\operatorname{WRITE~}(6, *)$ | PWR |
| $\operatorname{WRITE~}(5, *)$ | PWR1 |
| $\operatorname{WRITE~}(6, *)$ | PWR1 |
| $\operatorname{WRITE~}(5, *)$ | SUMPWR1 |
| $\operatorname{WRITE~}(6, *)$ | SUMPWR1 |

    FUNCTION PLGNDR(L, M, X)
    INTEGER L,M
    REAL X
    IF (M.LT.O.OR.M.GT.L.OR.ABS (X).GT.1.0) PAUSE
    'IMPROPER ARGUMENTS'
    \(\mathrm{PMM}=1.0\)
    IF (M.GT.0) THEN
    SOMX2=SQRT ( (1.0-X) * (1.0+X))
    \(\mathrm{FACT}=1.0\)
    DO \(11 \mathrm{I}=1, \mathrm{M}\)
    PMM \(=-\) PMM *FACT*SOMX2
    \(\mathrm{FACT}=\mathrm{FACT}+2.0\)
    11 CONTINUE
ENDIF
IF (L.EQ.M) THEN
PLGNDR=PMM
ELSE
PMMP1 $=\mathrm{X} *(2.0 * M+1.0)$ * PMM
IF (L.EQ.M+1) THEN
PLGNDR=PMMP1
ELSE
DO $12 \mathrm{LL}=\mathrm{M}+2, \mathrm{~L}$
PLL= (X* 2 *LL-1) *PMMP1-(LL+M-1) *PMM) /(LL-M)
PMM $=$ PMMP1
PMMP1=PLL
12 CONTINUE
PLGNDR=PLL

ENDIF ENDIF RETURN END

SUBROUTINE SPHRBSF (X,N,H1,H2)
COMPLEX J,H1,H2
REAL PI, X, BSJ (50) , BSY (50)
INTEGER N
$\mathrm{PI}=4.0$ *ATAN $(1.0)$
$J=(0.0,1.0)$
$\operatorname{BSJ}(1)=\operatorname{SIN}(X) / X$
$\operatorname{BSJ}(2)=\operatorname{SIN}(X) /(X * X)-\operatorname{COS}(X) / X$
$\operatorname{BSJ}(3)=(3.0 /(X * X * X)-1.0 / X) * S I N(X)-3.0 /(X * X) * \operatorname{COS}(X)$
$\operatorname{BSY}(1)=-\operatorname{COS}(X) / X$
$\operatorname{BSY}(2)=-\operatorname{COS}(X) /(X * X)-\operatorname{SIN}(X) / X$
$\operatorname{BSY}(3)=(-3.0 /(X * X * X)+1.0 / X) * \operatorname{COS}(X)-3.0 /(X * X) * \operatorname{SIN}(X)$
IF (N.EQ.O) THEN
$\mathrm{H} 1=\mathrm{BSJ}(1)+\mathrm{J} * \mathrm{BSY}$ (1)
$\mathrm{H} 2=\mathrm{BSJ}(1)-\mathrm{J} * \mathrm{BSY}(1)$
$\mathrm{H} 1=\mathrm{H} 1 * \mathrm{SQRT}(\mathrm{X} /(\mathrm{PI} / 2.0))$
$\mathrm{H} 2=\mathrm{H} 2 * \operatorname{SQRT}(\mathrm{X} /(\mathrm{PI} / 2.0))$
RETURN
ENDIF
IF (N.EQ.1) THEN
H1=BSJ (2) +J*BSY (2)
$\mathrm{H} 2=\mathrm{BSJ}(2)-\mathrm{J} * \mathrm{BSY}(2)$
H1=H1*SQRT (X/ (PI/2.0))
H2=H2*SQRT (X/(PI/2.0))
RETURN
ENDIF
IF (N.EQ.2) THEN
H1 $=$ BSJ (3) $+\mathrm{J} * \mathrm{BSY}$ (3)
$\mathrm{H} 2=\mathrm{BSJ}(3)-\mathrm{J} * \mathrm{BSY}(3)$
H1=H1*SQRT (X/ (PI/2.0))
$\mathrm{H} 2=\mathrm{H} 2 * \operatorname{SQRT}(\mathrm{X} /(\mathrm{PI} / 2.0))$
ENDIF
IF (N.GE.3) THEN
DO $11 \mathrm{I}=3, \mathrm{~N}$
$\mathrm{A}=\mathrm{I}$
$\operatorname{BSJ}(I+1)=(2.0 * I-1.0) / \mathrm{X} * \mathrm{BSJ}(\mathrm{I})-\mathrm{BSJ}(\mathrm{I}-1)$
$\operatorname{BSY}(I+1)=(2.0 * I-1.0) / X * B S Y(I)-B S Y(I-1)$
11
CONTINUE
$\mathrm{H} 1=\mathrm{BSJ}(\mathrm{N}+1)+\mathrm{J} * \mathrm{BSY}(\mathrm{N}+1)$
$\mathrm{H} 2=\mathrm{BSJ}(\mathrm{N}+1)-\mathrm{J} * \mathrm{BSY}(\mathrm{N}+1)$
H1=H1*SQRT (X/ (PI/2.0))
$\mathrm{H} 2=\mathrm{H} 2$ *SQRT (X/(PI/2.0))
ENDIF
RETURN
END

SUBROUTINE FIELD(SRAD,DIST,ANGLE,FR,NTERMS,ELFLD,HLFLD, SUMPWR) COMPLEX ELFLD, HF1,HF2,SUM, J, TEMP1,TEMP2,AN,SN,HLFLD
COMPLEX SUM1,SN1,HLFLD, CPWR,SUMPWR,TEMP3,TEMP4
REAL FREQ, SRAD, DIST,ANGLE, OMEGA, EPS, KA, KR, BN
INTEGER NTERMS,I,I1
$J=(0.0,1.0)$
PI=4.0*ATAN (1.0)
$\operatorname{SUM}=(0.0,0.0)$
SUM1 $=(0.0,0.0)$
SUMPWR $=(0.0,0.0)$
OMEGA=2.0*PI*FR
$\mathrm{EPS}=8.85 \mathrm{E}-12$
$\mathrm{KA}=2.0 * \mathrm{PI} * \mathrm{FR} / 3 \cdot 0 \mathrm{E}+08 * \mathrm{SRAD}$
$\mathrm{KR}=2.0 * \mathrm{PI} * \mathrm{FR} / 3.0 \mathrm{E}+08 * \mathrm{DIST}$
DO 100 I=1,NTERMS
C COMPUTE THE COEFFICIENT B(N)
$\operatorname{BN}=(2.0 * I+1.0) *(-\operatorname{PLGNDR}(I, 1,0.0)) /(2.0 * I *(I+1) * \operatorname{SRAD})$
C COMPUTE THE COEFFICIENT A(N)
I1=I-1
CALL SPHRBSF(KA,I1,HF1,HF2)
TEMP1=HF2
CALL SPHRBSF (KA, I, HF1,HF2)
TEMP2=HF2
AN=OMEGA*EPS* ((SRAD) ** (1.5)) *BN/(J* (KA*TEMP1-I*TEMP2))
CALL SPHRBSF(KR,I1,HF1,HF2)
TEMP1=HF2
CALL SPHRBSF (KR, I, HF1, HF2)
TEMP2=HF2
TEMP3 $=$ REAL (AN $)-J *$ AIMAG (AN)
TEMP4 = REAL (TEMP2) -J*AIMAG (TEMP2)
$C P W R=P I *(J * A N /(O M E G A * E P S) *(K R * T E M P 1-I * T E M P 2)) *$
\& TEMP3*TEMP4*2.0*I*(I+1.0)/(2.0*I+1.0)
SUMPWR=SUMPWR+CPWR
$A=C O S$ (ANGLE)
SN=J*AN/(OMEGA*EPS) /((DIST) ** (1.5)) * (-PLGNDR (I, 1, A) *
(KR*TEMP1-I*TEMP2)
SN1=AN/SQRT (DIST) * (-PLGNDR (I, 1, A) ) *TEMP2
SUM=SUM+SN
SUM1=SUM1+SN1
CONTINUE
ELFLD=SUM
HLFLD=SUM1
RETURN
END

SUBROUTINE POLR (ZR,RM)
COMPLEX ZR,RM,J
REAL MAG, PHASE,PI,XR,YR
PI=4.0*ATAN (1.0)
$J=(0.0,1,0)$
MAG=ABS (ZR)
XR=REAL (ZR)

```
YR=AIMAG (ZR)
IF (MAG.EG.O.O) THEN
\(\mathrm{RM}=(0.0,0.0)\)
RETURN
ENDIF
IF (XR.GT.0.0) THEN
PHASE=ATAN (YR/XR)
PHASE=180.0/PI*PHASE
ENDIF
IF (XR.LT.0.0.AND.YR.GE.0.0) THEN
PHASE=PI-ATAN (ABS (YR)/ABS (XR))
PHASE=180.0/PI*PHASE
ENDIF
IF (XR.LT.0.0.AND.YR.LT.0.0) THEN
PHASE \(=-\mathrm{PI}+\mathrm{ATAN}(\mathrm{ABS}(\mathrm{YR}) / \mathrm{ABS}(\mathrm{XR}))\)
PHASE=180.0/PI*PHASE
ENDIF
RM=MAG+J*PHASE
RETURN
END
```


## Rocky Mountain BASIC (HP) Program to Calculate the Radiated Fields from a Spherical Antenna

NOTE: This program will calculate the radiated electric and magnetic fields, the radiated power and the total power radiated. It also will format and save the results of these calculations on a mass storage medium. The source code for this program is available from the authors.

```
    RE-STORE "SPHERE_PWR"
    !
    This routine will calculate the radiated power and total power
    radiated from a spherical dipole source antenna with a uniform
    gap (equator) excitation voltage.
    Original: 03 Jul 1990, g. Koepke translated from FORTRAN program
                                    derived and written by Bob Johnk.
    Revision: 30 Aug 1990: 1400 hours
    OPTION BASE I
    RAD
    GOSUB Declare_vars
    GOSUB Init_values
Repeat_calcs:OFF KEY
    GOSUB Enter_specs
    GOSUB Allocate_arrays
    Timein=TIMEDAT\overline{E}
    GOSUB Calculate_fld
    Timedone=TIMEDATE
    PRINTER IS CRT
    GOSUB Save_results
    GOSUB Deallocate_arys
    DISP "CALCULATIONNS COMPLETE... ";DROUND((Timedone-Timein),4);" second:
    BEEP
    ON KEY O LABEL "Repeat",Local_prty GOTO Repeat_calcs
    ON KEY l LABEL "END",Local_prty GOTO End_prog
Spin:GOTO Spin
End_prog:OFF KEY
    MASS STORAGE IS Msi_id$
    IF Sys_id$[1,4]="S300" THEN ! reset to S300 keys and crt
                CONTROL KBD,15;0
                CONTROL CRT,12;2
    END IF
    LOAD KEY
    DISP "PROGRAM FINISHED ... RUN TO RESTART."
    BEEP
    STOP
    ! ///////////////////////////////////////////////////////////
Declare_vars:!
```

COMPLEX Efield,Hfield,Magefd,Maghfd,Hfcj,J,Sumpwrl
REAL K, Pwr, Pwrl
REAL Ang, Theta
REAL Timein, Timedone
INTEGER N,I,II,Title_print,Local_prty
INTEGER Filesize, Datacount
DIM Id\$[40],Test\$[160]
COM /Setup/ REAL Freq,V,A,R,INTEGER Nm,Nsteps
COM /Sys_msi/ Msi_id\$[20]
COM /Sys/ Sys_id\$[10]
COM /Interrupts/ INTEGER Intr prty
COM /Files/ Diskdrive\$[20],Filename\$[10]
RETURN

```
        //////////////////////////////////////////////////////////
Init_values:!
    Lōcal_prty=5
    Msi_id$=SYSTEM$("MSI")
    Sys_id$=SYSTEM$("SYSTEM ID")
    ! I\overline{F}}\mathrm{ SYs_id$[1,4]="S300" THEN CALL Compat_200
    OUTPUT K\overline{BD USING "K,#";"SCRATCH KEY E"}
    DISP CHR$(129)
    RETURN
```

    !
        ///////////////////////////////////////////////////////
    Enter specs: !
    PRINTER IS CRT
    CLEAR SCREEN
    IF Freq>0 THEN OUTPUT KBD USING "\#,K,K";Freq/1.0E+6,"H"
    INPUT "ENTER the FREQUENCY in MHz. ",Freq
    PRINT "Frequency (MHz) \(=\) "; Freq
    IF Freq<1.0E-10 THEN Enter_specs
    Freq=Freq*1.0E+6
    !
    Gap_v:!
$\overline{\mathrm{I} F} \mathrm{~V}>0$ THEN OUTPUT KBD USING "\#,K,K";V,"H"
INPUT "ENTER the GAP VOLTAGE (volts). ",V
PRINT "GAP volts = ";V
IF V<0 THEN Gap_v
!
Sphere_rad:!
IF $\bar{A}>0$ THEN OUTPUT KBD USING "\#,K,K";A,"H"
INPUT "ENTER the RADIUS of the SPHERE (meters). ", A
PRINT "Sphere RADIUS (m) = ";A
IF A<1.0E-20 THEN Sphere_rad
!

Modesum: !
IF Nm>0 THEN OUTPUT KBD USING "\#,K,K";Nm,"H"
INPUT "ENTER the number of SPHERICAL MODES to be summed. ",Nm
PRINT "The number of MODES summed $=$ ";Nm IF Nm<1 THEN Modesum

Observ: !

```
    IF R>0 THEN OUTPUT KBD USING "#,K,K";R,"H"
    INPUT "ENTER the FIELD OBSERVATION DISTANCE (meters). ",R
    PRINT "FIELD OBSERVATION DISTANCE (meters) = ";R
    IF R<A THEN Observ
    !
Num_steps:!
    \overline{IF} Nsteps>0 THEN OUTPUT KBD USING "#,K,K";Nsteps,"H"
    INPUT "ENTER the number of ANGULAR STEPS. ",Nsteps
    PRINT "Angular STEPS = ";Nsteps
    IF Nsteps<1 THEN Num_steps
    !
    RETURN
    !
    ! /////////////////////////////////////////////////////////
Allocate_arrays:! Setup all data files for saving/graphing
    IF Nsteps>0 THEN
        ALLOCATE Pdata(Nsteps*4+1,2),Edata(Nsteps*4+1,2)
        ALLOCATE Hdata(Nsteps*4+1,2)
        Filesize=Nsteps*4+1
    ELSE
        BEEP
        DISP "ILLEGAL number of STEPS. hit RUN ... "
        CALL Pause_key_on
    END IF
    RETURN
    !
    ! ///////////////////////////////////////////////////////////
    !
Deallocate_arys:!
    DEALLOCATTE Pdata(*),Edata(*)
    DEALLOCATE Hdata(*)
    Filesize=0
    RETURN
    !
    ! ////////////////////////////////////////////////////////
    !
Calculate_fld:!
    !
    Title_print=1
    J=CMPLX (0.,1.0)
    FOR I=0 TO Nsteps
        Ang=I*90.0/Nsteps
        DISP "Calculating angle ";Ang;" ... "
        Theta=(PI/180.0)*Ang !convert to radians
        K=2.0*PI*Freq/3.0E+8
        CALL Field(A,R,Theta,Freq,Nm,Efield,Hfield,Sumpwrl)
        DEG
        Magefd=CMPLX(ABS(Efield),ARG(Efield))
        Maghfd=CMPLX(ABS(Hfield),ARG(Hfield))
        RAD
        Hfcj=REAL(Hfield) -J*IMAG(Hfield)
        PWr=.5*V*V*REAL(Efield*Hfcj)
        Pwrl=V*V*ABS (Efield)*ABS(Efield)/(2.0*377.0)
        Sumpwrl=V*V*Sumpwrl
```

```
        GOSUB List_results
        !
        Pdata(I+1,1)=Ang
        Pdata(I+1,2)=Pwr
        !
        Edata(I+1,1)=Ang
        Edata(I+1,2)=REAL(Magefd)
        !
        Hdata (I+1,1)=Ang
        Hdata(I+1,2)=REAL(Maghfd)
        !
    NEXT I
    DISP CHR$(12)
    PRINTER IS 701
    PRINT USING "@"
    PRINTER IS CRT
    RETURN
    /////////////////////////////////////////////////////////
List results:!
    PRINTER IS 701
    IF Title_print THEN
        Title_print=0 ! only once
        PRINT TAB(20);"SPHERICAL DIPOLE FIELDS"
        PRINT RPT$("_",80)
        PRINT
        PRINT "Operating FREQUENCY = ";Freq/1.OE+6;" MHz."
        PRINT "Gap Drive Voltage = ";V;"volts. Sphere radius = ";A;"m."
        PRINT "Spherical MODES = ";Nm;". Observation distance = ";R;"m."
        PRINT "Total Radiated POWER = ";REAL(Sumpwrl);" watts."
        PRINT RPT$("_",80)
        PRINT TAB(48);" Power Density (w/m^2)"
        PRINT "Angle E (mag ---- phase) H (mag ---- phase)";
        PRINT " REAL (EXH) --- E^2/Z"
        PRINT RPT$("-",80)
    END IF
Image1:IMAGE M3D.DD,X,MD.4DE,X,M3D.DD,X,MD.4DE,X,M3D.DD,#
Image2:IMAGE X,MD.4DE,X,MD.4DE,
    PRINT USING Imagel;Ang,Magefd,Maghfd
    PRINT USING Image2;Pwr,Pwr1
    RETURN
    //////////////////////////////////////////////////////////
Save_results:!
    fill in arrays for 0,360 degrees.
    Il=Nsteps+1
    FOR I=Nsteps TO 1 STEP -1
        Ang=180-Pdata(I,1)
        I1=I1+1
        Pdata (I1, 1)=Ang
        Pdata(I1,2) =Pdata(I, 2)
```

```
    Edata (II, 1) =Ang
    Edata (I1, 2) =Edata (I, 2)
    Hdata (II, 1) =Ang
    Hdata (I1, 2) =Hdata (I, 2)
NEXT I
!
I1 \(=2\) *Nsteps +1
FOR I=2 TO 2*Nsteps+1
    Ang \(=180+\) Pdata ( 1,1 )
    I1=I1 +1
    Pdata \((11,1)=\) Ang
    Pdata (I1, 2) =Pdata (I, 2)
    Edata (I1, 1) =Ang
    Edata (I1, 2) =Edata (I, 2)
    Hdata (I1, 1) =Ang
    Hdata(I1, 2)=Hdata (I, 2)
NEXT I
Datacount \(=4\) *Nsteps+1 ! same as Filesize
!
    SAVE THE DATA HERE......
!
Diskdrive\$=""
Filename\$=""
Test \(=\) "Power: "\&VAL\$ (PROUND (Freq/1.0E+6, -1)) \&"gV="\&VAL\$ (V)
Test\$=Test\$\&"a"\&VAL\$(A) \&"Nm"\&VAL\$ (Nm) \&"z'="\&VAL\$(R)
IF LEN(Test\$) \(>40\) THEN
    IdS=Test\$[1,40]
    BEEP
    DISP "ID\$ is too long ... striping to 40 chrs."
    WAIT 3
    DISP CHR\$(12)
ELSE
    Id\$=Test\$[1,LEN(Test\$)]
END IF
IF LEN(Diskdrive\$) \(=0\) THEN
    CLEAR SCREEN
    ! CALL Select_disk
END IF
PRINT TABXY (1,18);" ......... SAVING POWER DATA ............."
! CALL Data_to_disk_r(Pdata(*),Filesize,Datacount,Id\$)
Filename \({ }^{\text {=" " }}\)
Id\$[1,5]="E-fld"
PRINT TABXY (1,18) ;" ......... SAVING E Field DATA ............"
! CALL Data_to_disk_r(Edata(*),Filesize,Datacount,Id\$)
Filename\$=""
\(\operatorname{Id}[1,5]=" H-f l d "\)
PRINT TABXY (1,18);" ......... SAVING H Field DATA ............"
! CALL Data_to_disk_r(Hdata(*),Filesize,Datacount,Id\$)
CLEAR SCREEN
CLEAR LINE
RETURN
```



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```
!
    !
DEF FNPlgndr(INTEGER L,M,REAL X)
    REAL Pmm,Fact,Somx2,Plgndr,Pmmp1,Pll
    INTEGER I,Ll
    IF (M<0. OR M>L OR ABS (X)>1.0) THEN
            BEEP
            DISP "IMPROPER ARGUMENTS in FN Plgndr ... "
            PAUSE
    END IF
    Pmm=1.0
    IF M>0 THEN
        Somx2=SQRT ((1.0-X) * (1.0+X))
        Fact=1.0
        FOR I=1 TO M
                Pmm=-Pmm*Fact*Somx2
                Fact=Fact+2
            NEXT I
        END IF
        !
        IF L=M THEN
        Plgndr=Pmm
        ELSE
            Pmmp1=X* (2.0*M+1.0)*Pmm
            IF L=M+1 THEN
                Plgndr=Pmmpl
            ELSE
                FOR Ll=M+2 TO L
                    Pll=(X*(2*Ll-1)*Pmmpl-(Ll+M-1)*Pmm)/(Ll-M)
                    Pmm=Pmmp1
                    Pmmpl=Pll
                NEXT Ll
                Plgndr=Pll
            END IF
        END IF
        RETURN Plgndr
FNEND
!
! **************************************************************
!
DEF FNFac(INTEGER N)
    INTEGER I
    REAL Fac
    IF N=0 THEN RETURN (1.0)
    Fac=1.0
    FOR I=1 TO N
        Fac=Fac*I
    NEXT I
    RETURN Fac
FNEND
!
**************************************************************
!
SUB Sphrbsf(REAL X,INTEGER N,COMPLEX H1,H2)
```

! calculate spherical basis functions.
COMPLEX J
REAL Bsj(50), Bsy(50)
$J=\operatorname{CMPLX}(0 ., 1.0)$
!
Bsj (1) $=\operatorname{SIN}(X) / X$
$\operatorname{Bsj}(2)=\operatorname{SIN}(X) /(X * X)-\operatorname{COS}(X) / X$
$\operatorname{Bsj}(3)=(3.0 /(X * X * X)-1.0 / X) * \operatorname{SIN}(X)-3.0 /(X * X) * \operatorname{COS}(X)$ !
$\operatorname{Bsy}(1)=-\cos (X) / X$
$\operatorname{Bsy}(2)=-\operatorname{COS}(X) /(X * X)-S I N(X) / X$
$\operatorname{Bsy}(3)=(-3.0 /(X * X * X)+1.0 / X) * \operatorname{COS}(X)-3.0 /(X * X) * S I N(X)$
!
SELECT N
CASE 0
H1=Bsj (1) +J*Bsy (1)
$\mathrm{H} 2=\mathrm{Bsj}$ (1) $-\mathrm{J} * \mathrm{Bsy}$ (1)
H1=H1*SQRT (X/ (PI/2.0))
$\mathrm{H} 2=\mathrm{H} 2$ *SQRT $(\mathrm{X} /(\mathrm{PI} / 2.0))$
CASE 1
H1=Bsj (2) +J*Bsy (2)
H2=Bsj (2) $-J * B s y(2)$
H1=H1*SQRT (X/ (PI/2.0))
$\mathrm{H} 2=\mathrm{H} 2 * \operatorname{SQRT}(\mathrm{X} /(\mathrm{PI} / 2.0))$
CASE 2
H1=Bsj (3) $+\mathrm{J} * \mathrm{Bsy}$ (3)
$\mathrm{H} 2=\mathrm{Bsj}$ (3) $-\mathrm{J} * \mathrm{Bsy}$ (3)
H1=H1*SQRT (X/ (PI/2.0))
$\mathrm{H} 2=\mathrm{H} 2$ *SQRT (X/(PI/2.0))
CASE >2
FOR I=3 TO N
Bsj $(I+1)=(2.0 * I-1.0) / X * B s j(I)-B s j(I-1)$
$\operatorname{Bsy}(I+1)=(2.0 * I-1.0) / X * B s y(I)-B s y(I-1)$
NEXT I
H1=Bsj $(N+1)+J * B s y(N+1)$
$\mathrm{H} 2=\mathrm{Bsj}(\mathrm{N}+1)-\mathrm{J} * \mathrm{Bsy}(\mathrm{N}+1)$
$\mathrm{H} 1=\mathrm{H} 1 * \mathrm{SQRT}(\mathrm{X} /(\mathrm{PI} / 2.0))$
$\mathrm{H} 2=\mathrm{H} 2 * \operatorname{SQRT}(\mathrm{X} /(\mathrm{PI} / 2.0))$
END SELECT
SUBEXIT
SUBEND
!


SUB Field(REAL Srad,Dist,Angle,Fr,INTEGER Nterms, COMPLEX Elfld, Hlfi

COMPLEX Temp1,Temp2,Temp3,Temp4
REAL Omega,Eps,Ka,Kr,Bn,A
INTEGER I,II
!
$J=\operatorname{CMPLX}(0 ., 1.0)$
Sum=CMPLX (0.,0.)
Sum1 $=\operatorname{CMPLX}(0 ., 0$.
Sumpwr=CMPLX (0., 0.)
Omega=2.0*PI*Fr
$\mathrm{Eps}=8.85 \mathrm{E}-12$
$\mathrm{Ka}=2.0 * \mathrm{PI} * \mathrm{Fr} / 3.0 \mathrm{E}+8$ *Srad
$\mathrm{Kr}=2.0$ *PI*Fr/3.0E+8*Dist
! PRINT RPT\$("?",20);Fr;" MHz, Angle = ";Angle
! PRINT "Omega =";Omega;", Ka =";Ka;", $\mathrm{Kr}=\mathbf{=} ; \mathrm{Kr}$
!
FOR I=1 TO Nterms
! calculate the coefficient $\mathrm{B}(\mathrm{N})$
$B n=(2.0 * I+1.0) *(-F N P l g n d r(I, 1,0)) /.(2.0 * I *(I+1.0) * S r a d)$
! PRINT "****************"
PRINT "Index number $I=" ; I$
PRINT "Bn = ";Bn;", ";
! calculate the coefficient $A(N)$
I1=I-1
CALL Sphrbsf(Ka,I1,Hf1,Hf2)
Templ=Hf2
CALL Sphrbsf(Ka,I,Hf1,Hf2)
Temp2=Hf2
An=Omega*Eps*((Srad)^(1.5))*Bn/(J*(Ka*Temp1-I*Temp2))
PRINT "An = ";An
!
CALL Sphrbsf(Kr,I1,Hf1,Hf2)
Templ=Hf2
PRINT "Templ =";Templ
CALL Sphrbsf(Kr, I, Hf1, Hf2)
Temp2=Hf2
PRINT "Temp2 =";Temp2
Temp3 $=$ REAL (An) $-J *$ IMAG (An)
Temp4 =REAL (Temp2) -J*IMAG (Temp2)
PRINT "Temp3 $=$ "; Temp3
PRINT "Temp4 =";Temp4
Cpwr $=$ PI* (J*An/(Omega*Eps)*(Kr*Temp1-I*Temp2)) *Temp3*Temp4
Cpwr=Cpwr*2.0*I* (I+1.0)/(2.0*I+1.0)
! PRINT "Cpwr ="; Cpwr
Sumpwr=Sumpwr+Cpwr
! PRINT "Sumpwr ="; Sumpwr
$A=\cos$ (Angle)
$\mathrm{Sn}=(\mathrm{J} * \mathrm{An} /(($ Omega*Eps) *(Dist^1.5)))*(-FNPlgndr (I, 1, A))
$\mathrm{Sn}=\mathrm{Sn}$ * (Kr*Temp1-I*Temp2)
! PRINT "Sn = "; Sn
Sn1=An/SQRT (Dist) * (-FNPlgndr (I, 1, A)) *Temp2
Sum=Sum+Sn
! PRINT "Sum (E) =";Sum
Sum1=Sum1+Sn1
NEXT I
Elfld=Sum
Hlfld=Suml
PRINT RPT\$("end-",5);" ANGLE";Angle
SUBEXIT
SUBEND
!


## Appendix B

Parts List

| SYMBOL EQUIVALENT |  |
| :--- | :--- |
| AC | ALARM CIRCUIT |
| BD | BIAS DETECTOR |
| DLR | DOWN-LINK RECEIVER |
| DLT | DOWN LINK TRANSMITTER |
| BCC | BATTERY CHARGING CIRCUIT |
| RFL | R-F LINK |
| SR | SPHERICAL REGULATOR |
| ULS | UP-LINK SWITCH |

PASSIVE COMPONENTS (resistors and capacitors)
All resistance values are in ohms ( $\Omega$ ) and capacitance values are in Farads (F). Tolerances are $\pm 10$ percent unless otherwise marked. POT is a potentiometer or variable resistor.

| RESISTOR | VALUE | LOCATION | CONNECTION | FIGURE |
| :---: | :---: | :---: | :---: | :---: |
| R1 | 1K | DLR | D1, -15VDC | 45 |
| R2 | 10 | DLR | C2, IC 13 PIN 2 | 45 |
| R3 | 511 | DLR | C4, IC 14 PIN 2 | 45 |
| R4 | 511 | DLR | C5, GND | 45 |
| R5 | 511 | DLR | IC 14 PIN 3, GND | 45 |
| R6 | 10 | DLR | +15VDC, IC 14 PIN 7 | 45 |
| R7 | 50K POT | DLR | IC 14 PIN 2 and PIN 6 | 45 |
| R8 | 10 | DLR | IC 14 PIN 4, -15VDC | 45 |
| R9 | 20K POT | DLR | IC 1 PIN 13 and PIN 14 | 45 |
| R10 | 270K, 1\% | DLR | R9, IC 1 PIN 12 | 45 |
| R11 | 10 | DLR | +15VDC, IC 1 PIN 12 | 45 |
| R12 | 511 | DLR | IC 1 PIN 9 and PIN 10 | 45 |
| R13 | 20K | DLR | R14, IC 1 PIN 1 | 45 |
| R14 | 5.1K | DLR | IC 1 PIN 3, R13 | 45 |
| R15 | 10 | DLR | IC 1 PIN 5, -15VDC | 45 |
| R16 | 1K | DLR | +15VDC, R17 | 46 |
| R17 | 50K POT | DLR | R16, R18 | 46 |
| R18 | 1K | DLR | R17, -15VDC | 46 |
| R19 | 1M | DLR | IC 2 PIN 4, R17 | 46 |
| R20 | 100 | DLR | +15VDC, IC 2 PIN 11 | 46 |
| R21 | 1K | DLR | R22, IC 2 PIN 1 | 46 |
| R22 | 100K POT | DLR | R21, IC 2 PIN 6 | 46 |
| R23 | 1 K POT | DLR | IC 2 PIN 6 and PIN 9 | 46 |
| R24 | 100 | DLR | IC 2 PIN 10, -15VDC | 46 |
| R25 | 5K POT | DLR | IC 2 PIN 14, GND | 46 |
| R26 | 10K, 1\% | DLR | IC 15 PIN 2, R27 | 46 |
| R27 | 100, 1\% | DLR | R26, GND | 46 |
| R28 | 10 | DLR | +15VDC, IC 15 PIN 7 | 46 |


| R29 | 10K, 1\% | DLR | IC 15 PIN 2 and PIN 6 | 46 |
| :---: | :---: | :---: | :---: | :---: |
| R30 | 10 | DLR | -15VDC, IC 15 PIN 4 | 46 |
| R31 | 10K, 1\% | DLR | R27, C26 | 46 |
| R32 | 50K POT | DIR | C30, R33 | 46 |
| R33 | 1K | DLR | R32, +15VDC | 46 |
| R34 | 20K, 1\% | DLR | IC 15 PIN 6, GND | 46 |
| R35 | 10K | DLR | -15VDC, R32 | 46 |
| R50 | 1M | AC | IC 16 PIN 2, +15VDC | 38 |
| R51 | 1M | AC | IC 16 PIN 2, GND | 38 |
| R52 | 1. $5 \mathrm{~K}, 1 / 4 \mathrm{~W}$ | AC | IC 16 PIN 3, +15VDC | 38 |
| R53 | 1K, 1/4W | AC | IC 16 PIN 6, D109 | 38 |
| R54 | 1K POT | AC | IC 16 PIN 6, D110 | 38 |
| R55 | 1M | AC | IC 16 PIN 2, +15VDC | 38 |
| R56 | 1M | AC | IC 16 PIN 2, GND | 38 |
| R57 | 1.5K, 1/4W | AC | IC 16 PIN 3, +15VDC | 38 |
| R58 | 1K, 1/4W | AC | IC 16 PIN 6, D111 | 38 |
| R59 | 1K POT | AC | IC 16 PIN 6, D112 | 38 |
| R60 | 1M | AC | IC 16 PIN 3, S16 | 38 |
| R61 | 270 | AC | R62, D113 | 38 |
| R62 | 10M | AC | R61, IC 16 PIN 2 | 38 |
| R63 | 220K | AC | IC 16 PIN 2, GND | 38 |
| R64 | 10K POT | AC | IC 16 PIN 1 and PIN 5 | 38 |
| R65 | 1K POT | AC | IC 16 PIN 6, D114 | 38 |
| R66 | 20K | AC | IC 16 PIN 6, D52 | 38 |
| R67 | 10K POT | $A C$ | +5VDC, Q50 | 38 |
| R68 | 49.9, 1\% | ULS | +5VDC, D53 | 38 |
| R69 | 20K POT | ULS | Q50, GND | 38 |
| R70 | 500 POT | BCC | D115, Q51 | 44 |
| R71 | 500 POT | BCC | D116, Q52 | 44 |
| R72 | 100 | BCC | D117, Q53 | 44 |
| R73 | 200 | BCC | Q51, R76 | 44 |
| R74 | 100 | BCC | Q52, R77 | 44 |
| R75 | 500 POT | BCC | Q53, R78 | 44 |
| R76 | 50 | BCC | R73, Q54 | 44 |
| R77 | 50 | BCC | R74, Q55 | 44 |
| R78 | 100 POT | BCC | R75, Q56 | 44 |
| R79 | 100 POT | BCC | Q54, D119 | 44 |
| R80 | 100 POT | BCC | Q55, D120 | 44 |
| R81 | 50 | BCC | Q56, D121 | 44 |
| R82 | 1K | BCC | +15VDC, D124 | 44 |
| R96 | 560 | RFL | +9VDC, Q57 | 42 |
| R97 | 18 | RFL | IC 9 PIN 15, C138 | 42 |
| R98 | 310 | RFL | R97, GND | 42 |
| R99 | 310 | RFL | R97, GND | 42 |
| R100 | 22 | RFL | IC 9 PIN 1, C100 | 42 |
| R101 | 22 | RFL | +9VDC, Cl01 | 42 |
| R102 | 22 | RFL | IC 9 PIN 4, Cl02 | 42 |
| R103 | 22 | RFL | IC 9 PIN 6, C106 | 42 |
| R104 | 100 | RFL | C103, C104 | 42 |
| R105 | 150 | RFL | +7.2VDC, L100 | 42 |
| R106 | 200 | RFL | across TP-103 | 42 |
| R107 | 499K, 1\% | SR | Q100, R108 | 37 |
| R108 | $499 \mathrm{~K}, ~ 1 \%$ | SR | IC 3 PIN 5, Q100 | 37 |
| R109 | 100K, 1\% | SR | Q100, D101 | 37 |
| R110 | 1M | SR | D104, C108 | 37 |


| R111 | 100K | SR | Q101, Q102 | 37 |
| :---: | :---: | :---: | :---: | :---: |
| R112 | 1K, 1\% | SR | D103, Q102 | 37 |
| R113 | 1M POT | SR | IC 3 PIN 1 and PIN 7 | 37 |
| R114 | 100K, 1\% | SR | IC 3 PIN 7, GND | 37 |
| R115 | 1K, 1\% | SR | IC 3 PIN 3, IC 4 PIN 3 | 37 |
| R116 | 5K POT | SR | IC 4 PIN 8, Q103 | 37 |
| R117 | 10K | SR | Q103, GND | 37 |
| R118 | 470, 1\% | SR | IC 5 PIN OUT, R119 | 37 |
| R119 | 5K POT | SR | R118, GND | 37 |
| R120 | 10K | BD | +12.2VDC, C118 | 40 |
| R121 | 100K POT | BD | Q104 PIN 1, R122 | 40 |
| R122 | 51.1K, 1\% | BD | R121, Q104 PIN 3 | 40 |
| R123 | 82.5K, 1\% | BD | Q104 PIN 5 and PIN 7 | 40 |
| R124 | $681 \mathrm{~K}, 1 \%$ | BD | C119, C121 | 40 |
| R125 | 681K, 1\% | BD | C120, C122 | 40 |
| R126 | 500 | BD | D105, C123 | 40 |
| R127 | 500 | BD | D106, C124 | 40 |
| R128 | 1M, 1\% | BD | IC 11 PIN 10, R129 | 40 |
| R129 | 1M, 1\% | BD | R128, IC 11 PIN 12 | 40 |
| R130 | 20K POT | BD | IC 11 PIN 9 and PIN 13 | 40 |
| R131 | 22.1K, 1\% | BD | IC 11 PIN 8 and PIN 9 | 40 |
| R132 | 22.1K, 1\% | BD | IC 11 PIN 13 and PIN 14 | 40 |
| R133 | 22.1K, 1\% | BD | IC 11 PIN 8 and PIN 2 | 40 |
| R134 | 22.1K, 1\% | BD | IC 11 PIN 14 and PIN 3 | 40 |
| R135 | 22.1K, 1\% | BD | IC 11 PIN 1 and PIN 2 | 40 |
| R136 | 22.1K, 1\% | BD | IC 11 PIN 3, GND | 40 |
| R137 | 100K | BD | IC 11 PIN 1, GND | 40 |
| R138 | 20K | BD | IC 11 PIN 1, C127 | 40 |
| R139 | 100K | BD | IC 11 PIN 7, GND | 40 |
| R140 | 10 | DLT | +5VDC, IC 6 PIN 8 | 41 |
| R141 | 500, 1\% | DLT | IC 6 PIN 3, TP3, R142 | 41 |
| R142 | 1K POT | DLT | R141, GND | 41 |
| R143 | 1K | DLT | IC 6 PIN 1, +5VDC | 41 |
| R14 4 | 10K | DLT | IC 7 PIN 2, +5VDC | 41 |
| R145 | 100, 1\% | DLT | Q105, GND | 41 |
| R146 | 910, 1\% | DLT | IC 8 PIN4, R147 | 39 |
| R147 | 200 POT | DLT | R146, GND | 39 |
| R148 | 100 | DLT | +5VDC, IC 8 PIN 8 | 39 |
| R149 | 500, 1\% | DLT | IC 8 PIN 3, TP3, R150 | 39 |
| R150 | 1K POT | DLT | R149, TP3, GND | 39 |
| R151 | 1K | DLT | +5VDC, IC 8 PIN 1 | 39 |
| R152 | 10K | DLT | +5VDC, IC 7 PIN 14 | 39 |
| R153 | 100, 1\% | DLT | Q106, GND | 39 |
| R154 | 220K | SR | R155, L102 | 39 |
| R155 | 220K | SR | R154, L103 | 39 |
| R156 | 270K | SR | R101, R146 | 39 |


| CAPACITOR | VALUE | LOCATION | CONNECTION | FIGURE |
| :---: | :---: | :---: | :---: | :---: |
| C1 | . $1 \mu \mathrm{~F}$ | DLR | R1, GND | 45 |
| C2 | . $1 \mu \mathrm{~F}$ | DLR | +5VDC, GND | 45 |
| C3 | $1.0 \mu \mathrm{~F}$ | DLR | IC 13 PIN 2, GND | 45 |
| C4 | . $1 \mu \mathrm{~F}$ | DLR | IC 13 PIN 5, R3 | 45 |
| C5 | . $1 \mu \mathrm{~F}$ | DLR | IC 13 PIN 7, R4 | 45 |


| C6 | $.1 \mu \mathrm{~F}$ | DLR | +15VDC, GND | 45 |
| :---: | :---: | :---: | :---: | :---: |
| C7 | 1. $0 \mu \mathrm{~F}$ | DIR | IC 14 PIN 7, GND | 45 |
| C8 | $1.0 \mu \mathrm{~F}$ | DLR | IC 14 PIN 4, GND | 45 |
| C9 | . $1 \mu \mathrm{~F}$ | DLR | R8, GND | 45 |
| C10 | . $1 \mu \mathrm{~F}$ | DIR | R11, GND | 45 |
| C11 | $0.001 \mu \mathrm{~F}$ | DIR | IC 14 PIN 6, IC 1 PIN 9 | 45 |
| C12 | $1 \mu \mathrm{~F}$ | DLR | IC 1 PIN 11 and PIN 12 | 45 |
| C13 | . $001 \mu \mathrm{~F}$ | DLR | IC 1 PIN 1 and PIN 3 | 45 |
| C14 | 150pF | DLR | IC 1 PIN 6, GND | 45 |
| C15 | $1 \mu \mathrm{~F}$ | DLR | IC 1 PIN 5, GND | 45 |
| C16 | $.1 \mu \mathrm{~F}$ | DLR | -15VDC, GND | 45 |
| C17 | . $1 \mu \mathrm{~F}$ | DIR | R16, GND | 46 |
| C18 | $.1 \mu \mathrm{~F}$ | DIR | R18, GND | 46 |
| C19 | $.1 \mu \mathrm{~F}$ | DLR | +15VDC, GND | 46 |
| C20 | $1 \mu \mathrm{~F}$ TANT. | DLR | IC 2 PIN 11, GND | 46 |
| C21 | $\begin{aligned} & .01 \mu \mathrm{~F}, \mathrm{NPO} \\ & \text { CHIP CAP } \end{aligned}$ | DLR | IC 2 PIN 1, GND | 46 |
| C22 | $1 \mu \mathrm{~F}$ TANT | DLR | IC 2 PIN 10, GND | 46 |
| C23 | $.1 \mu \mathrm{~F}$ | DLR | -15VDC, GND | 46 |
| C24 | . $1 \mu \mathrm{~F}$ | DLR | +15VDC, GND | 46 |
| C25 | $1 \mu \mathrm{~F}$ TANT | DLR | IC 15 PIN 7, GND | 46 |
| C26 | . $1 \mu \mathrm{~F}$ | DLR | R27, GND | 46 |
| C27 | $1 \mu \mathrm{~F}$ TANT | DIR | IC 15 PIN 4, GND | 46 |
| C28 | $.1 \mu \mathrm{~F}$ | DIR | R30, GND | 46 |
| C29 | . $1 \mu \mathrm{~F}$ | DLR | R31, GND | 46 |
| C30 | $.1 \mu \mathrm{~F}$ | DLR | R32, GND | 46 |
| C31 | $.1 \mu \mathrm{~F}$ | DIR | R32, GND | 46 |
| C50 | $.1 \mu \mathrm{~F}$ | MLS | Q50, GND | 38 |
| C100 | . $1 \mu \mathrm{~F}$ | RFL | R100, GND | 42 |
| Cl01 | . $1 \mu \mathrm{~F}$ | RFL | R101, IC\#9 PIN 9 | 42 |
| C102 | . $1 \mu \mathrm{~F}$ | RFL | R102, GND | 42 |
| C103 | $.1 \mu \mathrm{~F}$ | RFL | R104, GND | 42 |
| C104 | $.1 \mu \mathrm{~F}$ | RFL | R104, GND | 42 |
| C105 | . $1 \mu \mathrm{~F}$ | RFL | IC 9 PIN 5, GND | 42 |
| C106 | . $1 \mu \mathrm{~F}$ | RFL | R103, GND | 42 |
| C107 | 1000 pF | RFL | IC 10 OUTPUT, D100 | 42 |
| C108 | $1 \mu \mathrm{~F}$ TANT | SR | D104, R110 | 37 |
| C109 | $.1 \mu \mathrm{~F}$ | SR | IC 3 PIN 8, GND | 37 |
| C110 | . $01 \mu \mathrm{~F}$ | SR | IC 3 PIN 1 and PIN 7 | 37 |
| C111 | $4.7 \mu \mathrm{~F}$ TANT | SR | IC 3 PIN 1, R113 | 37 |
| C112 | $1 \mu \mathrm{~F}$ TANT | SR | Q102, GND | 37 |
| C113 | $.1 \mu \mathrm{~F}$ | SR | IC 4 PIN 8, GND | 37 |
| C114 | . $01 \mu \mathrm{~F}$ | SR | IC 4 PIN 2, PIN 6 | 37 |
| C115 | $4.7 \mu \mathrm{~F}$ TANT | SR | IC 4 PIN 1, GND | 37 |
| C116 | $4.7 \mu \mathrm{~F}$ TANT | SR | IC 5 ADJ, GND | 37 |
| C117 | . $1 \mu \mathrm{~F}$ | SR | IC 5 IN, GND | 37 |
| C118 | . $1 \mu \mathrm{~F}$ | BD | R120, GND | 40 |
| C119 | . $01 \mu \mathrm{~F}$ | BD | Q104 PIN 3 and PIN 4 | 40 |
| C120 | . $01 \mu \mathrm{~F}$ | BD | Q104 PIN 4 and PIN 7 | 40 |
| C121 | . $001 \mu \mathrm{~F}$ | BD | D105, GND | 40 |
| C122 | . $001 \mu \mathrm{~F}$ | BD | D106, GND | 40 |
| C123 | $.001 \mu \mathrm{~F}$ | BD | IC 11 PIN 10, GND | 40 |
| C124 | $.001 \mu \mathrm{~F}$ | BD | GND, IC 11 PIN 12 | 40 |
| C125 | . $01 \mu \mathrm{~F}$ | BD | +5VDC, GND | 40 |
| C126 | . $01 \mu \mathrm{~F}$ | BD | -5VDC, GND | 40 |



| SYMBOL | EQUIVALENT |
| :--- | :--- |
| AC | ALARM CIRCUIT |
| BD | BIAS DETECTOR |
| DLR | DOWN-IINK RECEIVER |
| DLT | DOWN LINK TRANSMITTER |
| BCC | BATTERY CHARGING CIRCUIT |
| RFL | R-F LINK |
| SR | SPHERICAL REGULATOR |
| ULS | UP-IINK SWITCH |

## SEMICONDUCTORS (transistors, diodes, ICs and LEDs)

COMPONENT TYPE LOCATION CONNECTION FIGURE MANUFACTURER

| IC 1 | AD 650JN | DLR | PIN 1 TO C13 | 45 | A. D. |
| :---: | :---: | :---: | :---: | :---: | :---: |
| IC 2 | AD 637JQ RMS/DC | DLR | PIN 1 TO C21 | 46 | A. D. |
| IC 3 | LP2951CM | SR | PIN 5 TO R108 | 37 | National |
| IC 4 | LP2951CM | SR | PIN 6 TO Cll4 | 37 | National |
| IC 5 | LM337LZ | SR | ADJ. TO Cll6 | 37 | Harris |
| IC 6 | AD654JR | DLT | PIN 6 TO Cl29 | 41 | A. D. |
| IC 7 | HC4538 | DLT | PIN 2 TO R144 | 39 | Motorola |
| IC 8 | AD654JR | DLT | PIN 6 TO Cl32 | 39 | A. D. |
| IC 9 | PDC 2200-24 | RFL | PIN 5 TO C105 | 42 | B.T.D. |
| IC 10 | MSA-0635 | RFL | OUT TO Cl07 | 42 | Avantek |
| IC 11 | MC34184D | BD | PIN 2 TO R135 | 40 | Motorola |
| IC 12 | AD590 | DLT | R146, +5VDC | 39 | HP |
| IC 13 | NE5212 | DLR | PIN 5 TO C4 | 45 | Signetics |
| IC 14 | OP AMP OP37 | DLR | PIN 2 TO R3 | 45 | PMI |
| IC 15 | OP AMP OP37 | DLR | PIN 2 TO R26 | 46 | PMI |
| IC 16 | LH0042CH | AC | PIN 3 to | 44 | National |
| IC 17 | LH0042CH | AC | Laser pin 9 PIN 3 to | 44 | National |
|  |  |  | Laser pin 7 |  |  |
| IC 18 | LHOO42CH | AC | PIN 3 to | 44 | National |
|  |  |  | IC 5 pin 1 |  |  |
| D1 (P31) | 710-502-000 | DLR | IC 13 PIN 1 | 45 | Radiall |
| D50 | 1N270 | AC | L53, -OF ALARM | 38 | generic |
| D51 | 1N270 | AC | L55, -OF ALARM | 38 | generic |
| D52 | 1N4153 | AC | R66, GND | 38 | Unitrode |
| D53 | MFOE1202 | ULS | Q50,R68 | 38 | Motorola |
| D100 | 1N5235B, 6.8V | RFL | R96, GND | 42 | Motorola |
| D101 | 1N4153 | SR | R109, IC 3 PIN 3 | 37 | Unitrode |
| D102 | 1N4153 | SR | IC 3 PIN 3,Cl08 | 37 | Unitrode |
| D103 | 1N4153 | SR | IC 3 PIN 3,R112 | 37 | Unitrode |
| D104 | 1N4153 | SR | D102, Q101 | 37 | Unitrode |
| D105 | HP5082-2755 | BD | R126,IC 10 out | 40,42 | HP |
| D106 | HP5082-2755 | BD | R127, GND | 40 | HP |
| D107 | HFBR-1404 | DLT | +5VDC, Q105 | 41 | HP |
| D108 | HFBR-1404 | DLT | +5VDC, Q106 | 39 | HP |
|  | NOTE: The backsh | ls a | removed on D107 | and D | 08. |

SEMICONDUCTORS (transistors, diodes, ICs and LEDs)

* Panel mounted \#276-069 (green) or \#276-068(red)

| D109 | GREEN LED* |
| :--- | :--- |
| D110 | RED LED* |
| D111 | GREEN LED* |
| D112 | RED LED* |
| D113 | GREEN LED* |
| D114 | RED LED* |
| D115 | GREEN LED* |
| D116 | GREEN LED* |
| D117 | GREEN LED* |
| D118 | RED LED* |
| D119 | RED LED |
| D120 | RED LED* |
| D121 | RED LED |
| D122 | RED LED* |
| D123 | RED LED |
| D124 | GREEN LED* |
| D125 | LED HLMP-K155 |
| D126 | LED HLMP-K155 |
| D127 | LED HLMP-K155 |


| AC | R53, GND |
| :--- | :--- |
| AC | R54, D50 |
| AC | R58, GND |
| AC | D50, R59 |
| AC | R61, GND |
| AC | D51, R65 |
| BCC | $+12.2 \mathrm{~V}, \mathrm{R} 70$ |
| BCC | $+7.2 \mathrm{~V}, \mathrm{R} 71$ |
| BCC | $-7.2 \mathrm{~V}, \mathrm{R72}$ |
| BCC | R79, +12.2V |
| BCC | See D118 |
| BCC | R80, +7.2V |
| BCC | See D120 |
| BCC | R81, -7.2V |
| BCC | See D122 |
| BCC | R82,GND |
| SR | R156, SWITCH |
| SR | R154, SWITCH |
| SR | R155, SWITCH |
|  |  |
| RFL | R105, C107 |


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| Radio Shack |
| HP |
| HP |
| HP |
| American Precision |
| Industries, Inc. |
| East Aurora, NY |
| Motorola |
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| Motorola |
| Harris |
| Motorola |
| Motorola |

        2N3904
    note $: * *$ is dual matched $N$ channel JFET
41 Motorola
39 Motorola

Connectors and other miscellaneous parts
BUC = BASE UNIT CONTROL

COMPONENT TYPE
LOCATION CONNECTION FIGURE MANUFACTURER



DC Power Supplies:

| P37 | $\begin{aligned} & +/-15 \text { VDC } \\ & \# 84-15-2110 \end{aligned}$ | BUC | Battery Charger | 47 | Sola Solids |
| :---: | :---: | :---: | :---: | :---: | :---: |
| P38 | $\begin{aligned} & +24 \text { VDC } \\ & \# 84-24-050 \end{aligned}$ | BUC | Battery Charger | 47 | Sola Solids |
| P39 | $\begin{aligned} & +/-15 \text { VDC } \\ & \text { DB15-50 } \end{aligned}$ | BUC |  | 47 | Acopian |
| P40 | $\begin{aligned} & +/-5 \text { VDC } \\ & 5 \text { EB200 } \end{aligned}$ | BUC |  | 47 | Acopian |
| P41 | $\begin{aligned} & +/-5 \text { VDC } \\ & \text { 5EB100 } \end{aligned}$ | BUC |  | 47 | Acopian |
| 3-1/2 Digit Front Panel Led Displays: |  |  |  |  |  |
| P42 | DP-3522 | BUC | Gap Voltage | 47 | Acculex |
| P43 | see P42 | BUC | Temperature | 47 | Acculex |
| P44 | Battery Pack Custom made, 10x1. | $\begin{aligned} & \mathrm{SR} \\ & 2 \mathrm{~V} \end{aligned}$ | +12 V Supply ls | 36 | Shelley-Ragon, Inc. |
| P45 | 7.2V Ni-Cad Pack <br> (2) sets | SR | +7.2 V Supply <br> -7.2V Supply | 36 | generic |
| P4 6 | BUC Enclosure $630-001 / R 317-12$ | BUC |  | 47 | Tracewell Enclosures |
| P50 | Optical Connector OFTI-STC 300-4STC-0001 | SR | D107, D108, Q103 | 51 | Optical Fiber Technologies, Inc. |
| P51 | Connector SMA right angle plug 2007-7985-02, 0.08 | SR <br> 5" | IC10 | 51 | Omni-Spectra |

P52 Pin Connectors Not shown, used to connect ACE R/C, Inc.
ACE/DEANS 2 PIN 12 V battery to circuit board
\#19K53 in sphere
Pin Connectors Not shown, used to connect ACE/DEANS 4 PIN \#19K50
7.2 V batteries and charger to sphere circuit board

ACE R/C, Inc. Higgensville, MO.

Interconnect Devices, Ir Kansas City, Kansas

Spring loaded contact
pins connecting the hemispheres
to the balun circuit in the sphere Part \# S-4-A-7-G

Plus miscellaneous bits and pieces of hardware, some purchased (e.g. nuts and bolts) and some fabricated as needed (e.g. brass sphere parts, power supply and circuit board mounts, etc.).


Figure 1. Coordinate system for the spherical dipole. The infinitesimal gap lies in the $\theta=90^{\circ}$ plane.


 Figure 3. Spectrum plot of the analog rf link for generator the left and the corresponding output is on the right.

(wgp) l2n07 lRu6is
  Optical Analog Link Signal Transfer Character
©
(wgp) 10107 12u615





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Figure 9．Sphere electric field radiation pattern determined using TEM cell measurements at 50 MHz ．
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0.12
Figure 10. Sphere electric field radiation pattern determined


Figure 11. Configuration of open area test site (OATS).





（سノへル）○！コ！」コ！」7ココ1ヨ

Figure 17．Sphere electric field radiation pattern determined using OATS measurements at 500 MHz ．
（ひノヘル）○！ə！」コ！」みココ1ヨ


Figure 19. Sphere electric field radiation pattern determined
using OATS measurements at 700 MHz .




Figure 21. Sphere electric field radiation pattern determined using OATS measurements at 850 MHz .


Figure 23. Sphere electric field radiation pattern determined using OATS measurements at 1000 MHz .

（யノへル）○！ə！」コ！」7ココ1ヨ



Figure 27．Sphere electric field radiation pattern determined using Anechoic Chamber measurements at 500 MHz ．
（ルノヘル）p！a！」コ！ヘ7ココ1ヨ



Figure 29. Sphere electric field radiation pattern determined using Anechoic Chamber measurements at 700 MHz .

Figure 30. Sphere electric field radiation pattern determined using Anechoic Chamber measurements at 800 MHz .


Figure 31．Sphere electric field radiation pattern determined using Anechoic Chamber measurements at 900 MHz ．
（ルノへu）plə！」コ！」7コロ1ヨ





Figure 35. Mechanical drawing of the sphere.



Figure 36. Schematic - DC distribution in the sphere.

```
        +7.2\vee BAT
```



```
SPHERE BATTERY POWER
\& LATCH-OFF REGULATOR

```

and latch-off regulator.

```


Figure 37. Schematic - Sphere battery power and latch-off regulator.


「 MONITOR/ALARM CIRCUITS
? \& DIPOLE BATTERY STATUS
dipole battery status. Power on loff uplink drive.




\section*{E}

LINK

IATE OR POLYSTYRENE.
cal downlink.


NOTE: C132 MUST BE POLYCARBONATE OR POLYSTYRENE.

Figure 39. Schematic - Temperature optical downlink.


WS:


NOTE: 0104 MUST BE CRPRBLE OF PROVIDING CONTROL BIAS CURRENTS AS FOLLOWS:
\[
\begin{aligned}
& \frac{\Delta I d}{V i n}<\frac{10 n A}{V} \\
& \text { FOR 1.) } 9 V<V i n<14 V \\
& \text { 2) } 4 u A<I d<8 u A
\end{aligned}
\]

Figure 40. Schematic - Biased detector \& differential amplifier.


AGE
NK

ITE OR POLYSTYRENE.
ge optical downlink.


NOTE: C129 MUST BE POLYCARBONATE OR POLYSTYRENE.

Figure 41. Schematic - Dipole gap voltage optical downlink.


SPHERE

\section*{PINFET AND MMIC RF AMPLIFIER}


Figure 42. Schematic - PINFET and MMIC rf amplifier.



\section*{BASE UNIT CHARGING CIRCUITS} FOR SPHERICAL DIPOLE BATTERIES

al dipole batteries.


NOTE: FOR J310, Idss IS MATCHED TO REQUIREMENT.

Figure 44. Schematic - Base unit charging circuits for spherical dipole batteries.

OPTICAL DOWN LINK RECEIVER



Figure 45. Schematic - Optical downlink receiver.



Figure 46. Schematic - Downlink signal processing circuitry.



Figure 47. Assembly drawing - Base unit.

\section*{RY CHARGING CIRCUIT BOARD}

cuit board.

BATTERY CHARGING CIRCUIT BOARD


Figure 48. Assembly drawing - Battery charging circuit board.

it board.


Figure 49. Assembly drawing - Downlink reciever circuit board.



Figure 50. Assembly drawing - Switch alarm circuit board.

re circuit board.


Figure 51. Assembly drawing - Sphere circuit board.
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\hline & 3. Devecember 1951 \\
\hline \multicolumn{2}{|l|}{4. title and subtitle Standard Spherical Dipole Source} \\
\hline \multicolumn{2}{|l|}{\({ }^{5 .}\) G. Koepke, L.D. Driver, K. Cavcey, K. Masterson, R. Johnk, M. Kanda} \\
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A spherical dipole was developed to provide a source that can be characterized both by theory and experiment and integrated into modern automated test systems. The frequency and amplitude of the radiated electromagnetic field are established remotely using a signal generator. This signal and all other control features are transmitted to and from the sphere using fiber optic cable. The field measurements show good agreement with predictions over much of the frequency band.
12. KEY WORDS (6 TO 12 ENTRIES; ALPHABETICAL ORDER; CAPITAUZE ONLY PROPER NAMES; AND SEPARATE KEY WORDS BY SEMICOLONS) electromagnetic fields; electronic circuits; fiber optic; remote control; spherical dipole; standard radiator
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