HANDBOOK FOR SRM USERS

John K. Taylor

*T*he National Bureau of Standards[1] was established by an act of Congress on March 3, 1901. The Bureau's overall goal is to strengthen and advance the nation's science and technology and facilitate their effective application for public benefit. To this end, the Bureau conducts research and provides: (1) a basis for the nation's physical measurement system, (2) scientific and technological services for industry and government, (3) a technical basis for equity in trade, and (4) technical services to promote public safety. The Bureau's technical work is performed by the National Measurement Laboratory, the National Engineering Laboratory, the Institute for Computer Sciences and Technology, and the Institute for Materials Science and Engineering.

The National Measurement Laboratory

Provides the national system of physical and chemical measurement; coordinates the system with measurement systems of other nations and furnishes essential services leading to accurate and uniform physical and chemical measurement throughout the Nation's scientific community, industry, and commerce; provides advisory and research services to other Government agencies; conducts physical and chemical research; develops, produces, and distributes Standard Reference Materials; and provides calibration services. The Laboratory consists of the following centers:

- Basic Standards[2]
- Radiation Research
- Chemical Physics
- Analytical Chemistry

The National Engineering Laboratory

Provides technology and technical services to the public and private sectors to address national needs and to solve national problems; conducts research in engineering and applied science in support of these efforts; builds and maintains competence in the necessary disciplines required to carry out this research and technical service; develops engineering data and measurement capabilities; provides engineering measurement traceability services; develops test methods and proposes engineering standards and code changes; develops and proposes new engineering practices; and develops and improves mechanisms to transfer results of its research to the ultimate user. The Laboratory consists of the following centers:

- Applied Mathematics
- Electronics and Electrical Engineering[2]
- Manufacturing Engineering
- Building Technology
- Fire Research
- Chemical Engineering[2]

The Institute for Computer Sciences and Technology

Conducts research and provides scientific and technical services to aid Federal agencies in the selection, acquisition, application, and use of computer technology to improve effectiveness and economy in Government operations in accordance with Public Law 89-306 (40 U.S.C. 759), relevant Executive Orders, and other directives; carries out this mission by managing the Federal Information Processing Standards Program, developing Federal ADP standards guidelines, and managing Federal participation in ADP voluntary standardization activities; provides scientific and technological advisory services and assistance to Federal agencies; and provides the technical foundation for computer-related policies of the Federal Government. The Institute consists of the following centers:

- Programming Science and Technology
- Computer Systems Engineering

The Institute for Materials Science and Engineering

Conducts research and provides measurements, data, standards, reference materials, quantitative understanding and other technical information fundamental to the processing, structure, properties and performance of materials; addresses the scientific basis for new advanced materials technologies; plans research around cross-country scientific themes such as nondestructive evaluation and phase diagram development; oversees Bureau-wide technical programs in nuclear reactor radiation research and nondestructive evaluation; and broadly disseminates generic technical information resulting from its programs. The Institute consists of the following Divisions:

- Inorganic Materials
- Fracture and Deformation[3]
- Polymers
- Metallurgy
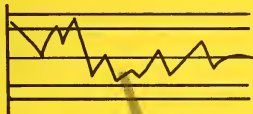- Reactor Radiation

Standard Reference Materials:

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John K. Taylor

Center for Analytical Chemistry
National Bureau of Standards
Gaithersburg, MD 20899

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U.S. DEPARTMENT OF COMMERCE, Malcolm Baldrige, Secretary

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PREFACE

Standard Reference Materials (SRM's) as defined by the National Bureau of Standards (NBS) are well-characterized materials produced in quantity and certified for one or more physical or chemical properties. They are used to assure the accuracy and compatibility of measurements throughout the Nation. SRM's are widely used as primary standards in many diverse fields in science, industry, and technology, both within the United States and throughout the world. They are also used extensively in the fields of environmental and clincial analysis. In many aplications, traceability of quality control and measurement processes to the national measurement system are carried out through the mechanism and use of SRM's. For many of the Nation's scientists and technologists, it is therefore of more than passing interest to known the details of the measurements made at NBS in arriving at the certified values of the SRM's produced. An NBS series of papers, of which this publication is a member, called the NBS Special Publication - 260 Series, is reserved for this purpose.

This 260 Series is dedicated to the dissemination of information on different phases of the preparation, measurement, certification and use of NBS-SRM's. In general, much more detail will be found in these papers than is generally allowed, or desirable, in scientific journal articles. This enables the user to assess the validity and accuracy of the measurement process employed, to judge the statistical analysis, and to learn details of techniques and methods utilized for work entailing the greatest care and accuracy. These papers also should provide sufficient additional information not found on the certificate so that new applications in diverse fields not foreseen at the time the SRM was originally issued to be sought and found.

Inquiries concerning the technical content of this paper should be directed to the author. Other questions concerned with the availability, delivery, price, and so forth of reference materials will receive prompt attention from:

Office of Standard Reference Materials
National Bureau of Standards
Gaithersburg, MD 20899

Stanley D. Rasberry
Chief
Office of Standard Reference
 Materials

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* Send order with remittance to Superintendent of Documents, US Government Printing Office Washington, DC 20402. Remittance from foreign countries should include an additional one-fourth of the purchase price for postage.

** May be ordered from: National Technical Information Services (NTIS). Springfield Virginia 22161.

ABSTRACT

This handbook was prepared to provide guidance for the use of Standard Reference Materials (SRM's) to provide an accuracy base for chemical measurements. The general concepts of precision and accuracy are discussed and their realization by quality assurance of the measurement process. General characteristics of SRM's are described and guidance is given for their selection for specific applications. Ways to effectively use SRM's are recommended, utilizing control charts to evaluate and monitor measurement accuracy. Appendices provide statistical guidance on the evaluation of measurement uncertainty.

Key words: accuracy; calibration; chemical analysis; control charts; measurement uncertainty; precision; quality assurance; standard reference materials; statistical control.

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1. Introduction

Standard Reference Materials (SRM's) have become well established as benchmarks for the quality assurance of measurements. Some analytical chemists find them indispensible for this purpose and use them systematically; others use them sporadically. Yet, there are others and those especially in some areas of analytical chemistry who rarely if ever use reference materials. From casual observation, the frequency of use of reference materials is closely coupled with one or more of the following factors:

- familiarity with the philosophy of their use
- degree of appreciation of the benefits of their use
- availability of directly-applicable SRM's
- understanding of the role of directly and indirectly related SRM's in a measurement system
- degree of full appreciation of measurement as a system.

The National Bureau of Standards has pioneered and continues to be the leader in the development of Standard Reference Materials (SRM's) for quality assurance of measurements. The program to provide such materials, originally known as standard samples, was initiated in 1906, largely in response to needs of the metals industry. It has since grown to a multi-material program of over 1000 items that serves most of the areas of modern analytical chemistry. A large number of materials useful in physical metrology and engineering are also included. Some areas of analysis are covered more completely than others, due to historical reasons, priorities for national issues, and to some extent the degree of industrial awareness of the quality assurance concept. For the early users, SRM's were identical, in most respects, to the materials ordinarily analyzed. Thus the results of measurements of SRM's were easily interpreted. As the program has grown, it has become impossible to provide SRM's with a one-to-one correspondence to every conceivable application; as a result, generic standards are commonly produced which serve multi-purposes. This concept broadens the scope of applications and conserves effort and cost of production.

This handbook was prepared with the objective to improve the understanding and the basis for use of SRM's. While written from the viewpoint of a chemist, the basic concepts described are believed to be applicable to most areas of metrology. The handbook is arranged in a logical progression, starting with the basic concepts of precision and accuracy, followed by discussions of the calibration and quality assurance of the measurement process, the use of Standard Reference Materials to evaluate various kinds of measurements, and the reporting of data with evaluated limits of uncertainty. The statistical considerations most frequently applicable for the evaluation and interpretation of measurement data are reviewed in the Appendix. Each section is written with some degree of independence so that it can be understood without undue reference to the contents of other Sections.

The treatment of each subject is not claimed to be exhaustive but is often an overview. Accordingly, a list of selected references is included which contain both background and other information supplemental to that in the text. A listing of recent research papers from the NBS Center for Analytical Chemistry, related to the preparation, analysis, and certification of specific SRM's is also included.

SOURCES OF INFORMATION
(See page 40 for more details)

- NBS Standard Reference Materials
  Telephone Number: 301-921-2045

- Mailing lists are maintained to keep SRM users updated with catalogs and information on new SRM's. Call the number above to have your name added.

- The free magazine _American Laboratory_ has a monthly column called "Reference Materials" to provide an information forum for SRM users.

2. Precision and Accuracy

2.1 Concepts of Precision and Accuracy

Accuracy is an intuitively understandable and desirable requirement for most measurements. Data which are knowingly inaccurate or whose accuracy is unknown have little appeal to most users. Yet precision is sometimes confused with accuracy and the agreement of successive results can inspire a degree of confidence that the measurements may not merit.

Accuracy, the closeness of a measured value to the true value, includes the concepts of bias and precision (see figure 1 and figure 2) and is judged with respect to the use to be made of the data. A measurement process must be unbiased to be capable of producing accurate values. In such a case, it must be sufficiently precise, as well, or else the individual results will be inaccurate due to unacceptable variability. The following discussion is presented to clarify these concepts. The term uncertainty is used widely in describing the results of measurement and denotes an estimate of the bounds of inaccuracy. Strictly speaking, the actual error of a reported value is usually unknowable. However, limits of error ordinarily can be inferred, with some risk of being incorrect, from the precision and reasonable limits for the possible bias of the measurement process.
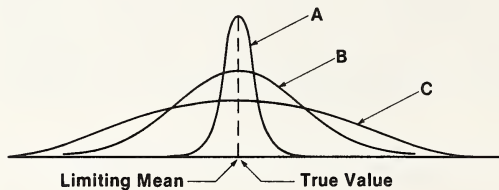
Figure 1.   Unbiased Measurement Processes

The distributions of results from three unbiased processes are shown.
The precision decreases in the order A>B>C. While the limiting
means of all will approach the "true value," process C is relatively
inaccurate (compared with A) due to its imprecision.
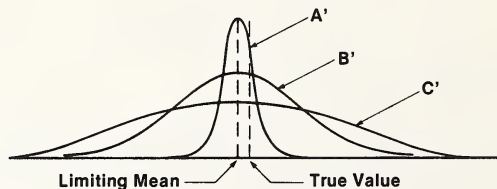
Figure 2.   Biased Measurement Processes

All of the processes are biased and hence inaccurate since the
limiting means do not coincide with the "true value." However, it
will be noted that most of the results for process A' will be more
accurate than those of process C and even B (figure 1), due to
precision considerations.

2

The concept of precision is concerned with the variability of the individual results of replicate measurements. A process which shows a small scatter is said to be precise and vice versa. Obviously such judgments are subjective and based on the intended use of the data. What might be considered as very precise for one purpose could be grossly imprecise for another. Random errors are responsible for the observed scatter of measured values. These may be reduced to the point at which they are negligible with respect to the tolerable error of the measured value, or are limited by inherent characteristics of the instrumentation or the methodology used. The averages of several series of measurements will show a smaller variability than the individual values and the grand average of such is expected to approach a limiting value (limiting mean) as the number of measurements is increased.

The concept of bias is concerned with whether or not the limiting mean differs from the true (or accepted) value of the property measured. Here again, judgment is ordinarily involved since it is impossible to eliminate all error or even to know if this has been achieved. Such decisions are thus based on whether or not bias exists for all practical purposes.

In the case of individual measurements, each will exhibit some degree of inaccuracy, that is to say it will deviate from the true value. This will occur because of random error together with any bias of the measurement system. Indeed, it is highly improbable that any individual measurement made by an unbiased measurement system will be accurate, since the probability of zero random error is zero. Many individual values may appear to have the correct value but this is due to truncation resulting from insensitivity of the measurement process or from rounding of the data.

A measurement process should be sufficiently precise to minimize the number of replicate measurements required for the intended use. A very precise system may need only a few measurements, even one, to provide data that would not be significantly improved by further replication. Also, a measurement system must be sufficiently precise to identify whether or not biases of a comparable magnitude are present in the system. While possible in principle, an unbiased measurement process of low precision may be incapable of providing accurate data, from a practical point of view, because of the large number of measurements required to reduce the uncertainty of the random error to reasonable limits.

Precision may be evaluated by the redundant process of replicate measurement. Results on a single material may be used for this purpose, or the information obtained on a number of samples (even duplicate measurements, see Appendix C.2.2) may be pooled. Accordingly, there is no reason why a laboratory cannot evaluate its own precision without external assistance [1]. While SRM's may be helpful in this regard, they are not necessary for this purpose.

In order to properly estimate precision, a number of measurements over an extended period of time may be required. A small number of measurements tend to underestimate the standard deviation since small random errors are more probable than large ones and less likely to be observed during a limited set of measurements. Also, it is common experience that it is much easier to repeat a measurement than to reproduce it over a period of time. The repeatability, or short-term standard deviation is needed to answer questions about the number of repetitive measurements. that may be required while the long-term standard deviation, or reproducibility is needed to answer such questions as the agreement of data obtained at different times, or the statistical control of a measurement process.

Though precise measurements can serve useful purposes when limited comparisons are required, accuracy is more often an essential requirement. Whenever the true value of the measured quantity is needed, or when data from different laboratories, different methodologies, or that from the same laboratory using the same method over a period of time needs to be interrelated, bias can be a serious problem. The analysis of appropriate reference materials is the best and easiest way to investigate bias. While methods may be compared with reference methods to assess accuracy, this is ordinarily a more difficult and time-consuming process (see Appendix D.4).

2.1.1 Precision and Bias in a Measurement System

The precision of a measurement system may be influenced by a number of factors, each having its own precision. The precision of each factor, quantified in terms of the variance, contributes to the precision of the process. The variance is simply the square of the standard deviation, s. In measurement processes, the variances of the individual steps, s_i^2, add up to define the variance of the process, i.e., $s^2 = s_1^2 + s_2^2 + s_3^2 + .. + s_n^2$. Some of the steps (or factors) can be easily identified and the individual variances estimated. Examples are weighing and extraction. As steps are identifiable, improvements conceiveably can be made when there are "assignable causes" for undesirable imprecision. Because of addition in quadrature, it is evident that one or a few sources of variance can be the major contributors to the total variance. Knowledge of the magnitude of the individual variances can indicate both directions for improvement and possible sources of trouble when "out-of-control" measurements occur.

It is conceivable that variance can be reduced to very low levels, with diligent effort. Laboratories commonly improve their precision as they gain experience with their methodology. Ordinarily, a laboratory will improve its quality control practices to the point where the precision attained is adequate for a particular application or when peer performance has been attained. Because analysis must be pragmatic, cost-benefit decisions will often dictate how far to go. For example, it is a matter of record that laboratories using the same methodology will differ in their precisions. This may be due to difference in levels of skill but also to different levels of tolerance for permissible error.

Bias in measurement systems can result from several sources. The commonly recognized ones are: control of measurement variables; interferences; erroneous calibration; contamination; losses; deteriorations; inefficiencies in extractions or sample dissolution. Variability in some of these can contribute to random error as well, and often to a major degree. Inappropriate calibration techniques can be a serious source of bias. Reliance on spiking which may not simulate matrix-incorporated analyte, or the use of a pure matrix (e.g., pure water) to simulate a natural matrix (waste water) are typical examples. A reference material that closely simulates the analytical samples is needed to identify and evaluate such biases.

Unlike random errors, systematic errors or biases from several sources are not necessarily randomly distributed; hence one must consider that biases can add up algebraically. That is to say, the total bias $B = B_1 + B_2 + \cdots + B_n$. Thus, a large number of small biases can equal or even exceed a large bias from a single source. While the effect of random error decreases as the number of measurements, n, is increased ($s_{\bar{x}} = s_x/\sqrt{n}$), the effect of bias is independent of the number of measurements.

2.2 Dependence on Standards

All measurements depend on standards. Physical measurements depend almost entirely on physical standards with little or no dependence on chemical standards. Chemical measurements on the other hand depend on both with greater dependence on the latter. The early recognition of the need for universally acceptable physical standards, and the chaos that could result from their unavailability led to the development of the now universally accepted physical standards for the primary units of length, mass, time, temperature, and radiant luminosity and the units derived from them such as pressure, force, acceleration, power, and density. No corresponding chemical standards have ever been developed. There are, of course, the useful standards of atomic weights and a variety of physicochemical standards.

The early chemical analytical measurements were largely absolute in nature, which means that they depended almost entirely on physical standards. Thus, classical analysts used gravimetry in which chemical constituents were removed quantitatively or isolated from their matrix, purified, and weighed. Relation of such masses to the chemical information desired was calculated by stoichiometry. The critical sources of error in such measurements were incomplete separations, mechanical losses, and contamination due to coprecipitation and analytical blanks. Physical standards were the primary standards and provided adequate and sufficient means to control the accuracy of such chemical measurements.

While classical methods augmented by such physical-chemical techniques as coulometry, still provide the basis for the most accurate measurement of major constituents or for the assay of pure materials, the bulk of modern chemical measurements are made by comparative techniques in which, in essence, an instrument is used to compare an unknown sample with one of known composition. Some measurements require the removal of the substance of interest prior to analysis, or its isolation from the matrix using physical or chemical techniques. In others, the analytical process may combine the separation and measurement steps. Separation of a group of analytes, followed by selective detection is another approach to analysis.

The trend toward comparative measurements has shifted the need in chemical analysis from heavy dependence on physical standards to heavy dependence on chemical standards. However, there is usually no problem in obtaining chemicals of requisite purity to serve as chemical standards so that essentially no national or international standard chemicals have been developed or exist today, in the same sense as the physical standards. When reference materials exist, they are ordinarily not chemical standards in the hierarchal sense of physical standards of measurement but rather are quality assurance materials as will be discussed later. Of course, some reference materials are high purity chemicals which may be used as primary standards in some areas of chemical analysis.

2.3 Physical and Chemical Standards

Seven basic units for physical measurements have been adopted by international agreement. From these, all other units of measurement may be derived (2). The basic units are defined by appropriate artifacts or measurements. Transfer standards may be calibrated with respect to the basic standards maintained in national laboratories. Such calibrations must be done with a sufficient degree of reliability, traceable to national standards. For most chemical measurements, uncertainties in the physical standards used do not contribute significantly to the analytical uncertainty.

Chemical standards differ from physical standards in several ways. They are chemical elements or compounds, usually identical with or related by stoichiometry, to the analytes measured. It is ordinarily possible to obtain such standards in sufficient purity or to purify them adequately so there is no need to maintain them in a national laboratory. Due to the complexity and variety of chemical measurements it would be infeasible if not impossible to do so.

The problem in the use of chemical standards is the degree to which they can be blended or incorporated into a sample matrix to produce a substance that can reliably calibrate or define the response function of a chemical analyzer. Matrix match between standard and analytical sample is often critical but difficult to achieve. When standards are carried through an entire analytical process, spikes, surrogates, and other artificially introduced constituents may not respond in the same manner as naturally occurring analytes, thus causing calibration problems. On the other hand, standards prepared to simulate the final analytical sample (e.g., an extract or a solution of the original sample) may not calibrate the entire analytical process.

No matter what kind of standards are used, they must be prepared with care from reliable starting materials. The mode of preparation should be such that the uncertainty of the standards does not contribute significantly to the overall analytical uncertainty. Chemists ordinarily assume that standards can be prepared with negligible error. Standards for very low concentration levels may be exceptions. Furthermore, the stability of such standards and the degree of protection required to safeguard them from contamination, deterioration, or losses always needs consideration.

Standards should never be used in an extrapolative mode. They should always bracket the measurement range. No measurement should be reported at a value lower or higher than the lowest or highest standard used to calibrate the measurement process.

2.4 Calibration, Standardization, and Analytical Response Function

Calibration may be defined as the comparison of a measurement standard or instrument with another standard or instrument to identify or eliminate by adjustment any variation (deviation) of the accuracy of the item being compared. Physical standards such as masses, and instruments such as thermometers are calibrated. Physical standards or calibrated instruments, traceable to national standards are required for calibration of other standards or instruments. The uncertainty of the calibrations will depend on the uncertainty of the values of the standards used and the measurement processes used for the intercomparisons.

Chemical measurements require standards consisting of pure chemicals or liquid, solid, or gaseous mixtures prepared from them. For most applications, chemicals of sufficient purity for use as standards or for their preparation, can be obtained from suppliers. For critical applications, chemical standards are sometimes assayed to determine their purity or analyzed for impurities in order to calculate their composition. The latter practice can be erroneous unless it is ascertained that all significant impurities have been determined. The concentrations of solutions used as analytical reagents or as calibrants are sometimes defined on the basis of their preparational data and knowledge or assumptions of purity. When concentrations are determined by comparison with other solutions of known concentrations, the process is called standardization.

In general, the calibration of a chemical analyzer consists in the evaluation of its response function, in terms of chemical composition of the samples to be analyzed. The analyzer responds to some property of the analyte, the value of which needs to be quantified by use of known substances. Then it is tacitly assumed that the instrument will respond analogously to the standard and test samples. The sources of uncertainty in this case are the uncertainty in composition of the known samples and the validity of the analogy.

It is a generally accepted principle of reliable analysis that chemical analyzers should be calibrated over the full range of measurement and that measurement data be restricted to the range calibrated. It is not good measurement practice to report extrapolated data, i.e., data outside of the range calibrated. The range of reliable calibration can be considered as the range of reliable measurement and conversely.

The necessary frequency of re-calibration or re-evaluation of a response function will depend on the stability of the measurement system and the accuracy requirements for the data. To ensure confidence in measured values, such re-evaluations should be made before significant changes are to be expected.

The terms primary and secondary standards are used frequently and need some discussion. Strictly speaking, a primary standard is one whose value may be accepted without further verification by the user. It, in turn, may be used to establish or ascertain a value for a secondary standard. Thus, a secondary standard provided by one laboratory (for example, a mass standard calibrated at NBS) could serve as a primary standard for another laboratory. In any case, the uncertainty of the value of any standard must be known since the adjective designation (primary or secondary) does not define any limits of uncertainty for its value.

Analytical chemists have used the terms primary and secondary to indicate relatively pure materials that may be used to prepare solutions with accurately known compositions (3). The International Union of Pure and Applied Chemistry (4) has set minimum levels of purity for primary and secondary chemicals.

Specifications for certain classes of physical standards, have been established which include design characteristics and permissible departures (tolerances) from nominal values. Thus a 1 gram weight of Class 1 will have a tolerance of 0.034 mg while the tolerance is 2 mg for a Class 6 weight of the same denomination (5). The nominal weight is assumed, when used, but it should be recognized that the true value may lie anywhere within the tolerance range. If such an uncertainty is too large, the standard may be calibrated, but upgrading may be difficult due to design considerations.

2.5 National Measurement System for Analytical Chemistry

What might be called the National Measurement System for Analytical Chemistry is shown in Figure 3. The measurement of any specific sample requires a measurement system, individually designed with consideration of the requirements for the data. This system must be calibrated, using physical and chemical standards. As already discussed, the physical standards may be traceable to national primary standards maintained by the National Bureau of Standards and compatible with those of other nations. The chemical standards, generally, will be prepared by the measurement laboratory. Ordinarily, they serve as quality assurance materials to evaluate measurement accuracy, to intercalibrate laboratories in a measurement program, and to provide compatibility of measurement data. SRM's can serve as calibrants in some cases.
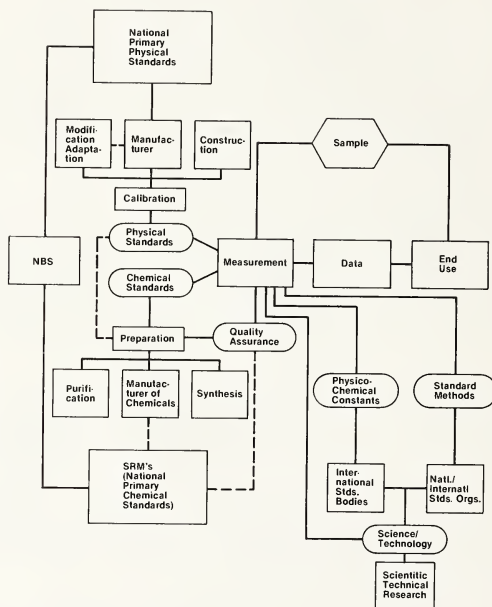
Figure 3. National Measurement System for Analytical Chemistry

The figure illustrates a number of points that have been discussed earlier. The critical dependence of modern analysis on both physical and chemical standards is indicated although the former of requisite reliability usually are available to the analyst from external sources. Ordinarily, the chemist must prepare all chemical standards used, starting with source materials as indicated. Questions about the matrix match of standards and test samples always must be considered. The measurement process is highly dependent on broad areas of science and technology, as well.

Quality assurance of the measurement process is essential for reliable data. The important role of SRM's in controlling the calibration process and in assessing data quality is shown and will be elaborated on throughout this handbook.

3. Quality Assurance

Quality assurance is the name given to the procedures used to ascertain that measurement data are good enough for their intended purpose (1,6). It involves two distinct but related activities:

quality control - those procedures and activities developed and implemented to produce a measurement of requisite quality

quality assessment - those procedures and activities utilized to verify that the quality control system is operating within acceptable limits and to evaluate the quality of the data.

The basic requirements for producing reliable data are appropriate methodology, adequately calibrated, and properly used. These, together with good laboratory and measurement practices, are the basic ingredients of a quality control program. The quality of the data may be assessed by use of reference materials to evaluate bias and the time-consuming process of redundancy to evaluate precision.

3.1 Quality Assurance of a Measurement Process

There is a growing awareness that analytical data for use in any decision process must be technically sound and defensible. Limits of uncertainty are required which need to be supported by suitable documentary evidence. Professional analytical chemists have always espoused this philosophy. Regulatory agencies and contracting parties increasingly are specifying it as a routine requirement. The formal and even informal procedures used to establish the limits of uncertainty of measurement data are generally referred to as quality assurance, in which replicate measurements and independent procedures support claims for the accuracy of the data. When a measurement process can be established and demonstrated to be in a state of statistical control, the accuracy of the process can be imputed to characterize the accuracy of all data produced by it. Hence the requirements for redundancy can be greatly reduced.

A measurement process of the type described above is illustrated in Figure 4. It utilizes methodology appropriate for the measurement program and appropriate quality control practices are followed. Statistical control is demonstrated by the measurement of replicate samples and internal reference materials, using control charts. This also permits the evaluation of the precision of the process.
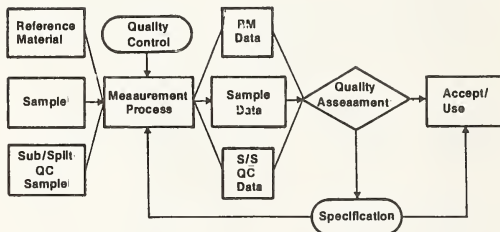
Figure 4. Measurement Process Quality Assurance

When the process is demonstrated to be in a state of statistical control, reference materials such as SRM's may be analyzed to assess measurement accuracy. The resulting judgment of precision and accuracy can be assigned to the sample data output of the process. The figure shows also how data quality assessment is used in a feedback mode to monitor the process, to initiate corrective actions as required, and in a decision mode for the release or use of data.

3.2 Statistical Control

A stable measurement system is expected to produce reproducible data. Statistical control may be defined as the attainment of a state of predictability. Under such a condition, the

mean of a large number of measurements will approach a limiting value (limiting mean) and the individual measurements should have a stable distribution, described by their standard deviation. Under such a condition, the limits within which any new measured value would be expected to lie can be predicted with a specified probability, the confidence limits for a measurement or mean of set of measurements can be calculated, and the number of measurements required to obtain a mean value with a given confidence may be estimated.

It is axiomatic that attainment of statistical control is the first objective of a measurement process. This is just another way of stating that it must achieve stability. Yet, it has the further connotation that the data produced are statistically describable. Eisenhart has stated -- "Until a measurement operation has been 'debugged' to the extent that it has attained a state of statistical control it cannot be regarded in any logical sense as measuring anything at all (7)."

When a measurement system is altered or disturbed, a new or modified measurement system may result with a limiting mean and/or a standard deviation different from the previous values. During normal use of a measurement system, changes can occur as well, unbeknown to the laboratory personnel. A well designed quality assurance program will monitor the system for such changes and indicate when corrective actions are required.

3.3 Control Charts

The philosophy of the use of control charts is based on the premise that analytical measurements may be systematized to provide a process simulating a manufacturing process in many respects. As the result of quality control procedures, a system may be debugged and attain a state of statistical control of its data output. The accuracy of the system can be evaluated for typical test samples and thus can be assigned to all similar measurement data generated by the system.

A control chart is simply a graphical way to interpret test data. In its simplest form, a selected reference sample is measured periodically and the results are plotted sequentially (or time-ordered) on a graph. Limits for acceptable values are defined and the measurement system is assumed to be in control (variability is stable and due to chance alone) as long as the results stay within these limits. A second useful form of control chart is one in which the standard deviation or range (even differences between duplicates) of a series of measurements is plotted in a similar manner. The residence of the values within expected limits is accepted as evidence that the precision of measurement remains in control. The monitored precision of measurement and the accuracy of measurement of the reference sample may be transferred, by inference, to all other appropriate measurements made by the system while it is in a state of control.

Examples of each kind of control chart described above are given in Figure 5. In Figure 5A, the mean, $\bar{x}$, of 2 measurements is plotted sequentially. The central line is the most probable value for $\bar{x}$ (i.e., the grand average, $\bar{\bar{x}}$, of measurements of $\bar{x}$) and the limits LWL to UWL (lower and upper warning limits) define the area in which 95 percent of the plotted points are expected to lie. The limits LCL to UCL (lower and upper control limits) define the area in which almost all (99.7%) of the plotted points are expected to lie when the system is in a state of statistical control. It should be clear that when more than 5 percent of the points lie outside of the warning limits or when values fall outside of the control limits, the system is behaving unexpectedly and corrective actions, and even rejection of data, may be required.

A discussion of the strategy to follow in the use of control charts is beyond the scope of the present presentation but laboratories using them need to develop such. Results are expected to scatter randomly within the limits. Systematic trends or patterns in the data plots may be early warning of incipient problems and are cause for concern, hence techniques to identify such should be practiced.

Control charts, including the factors for calculating control limits are discussed more thoroughly elsewhere, of which ASTM Special Technical Publication STP 15D is an excellent source of information [8]. Briefly, the central line is either the known value for the test sample (e.g., certified value if an SRM is used), or the mean of at least 15 sets of independent measurements. The standard deviation estimate, s, should be based on at least 15 such measurements. Control limits can then be calculated according to the following table.
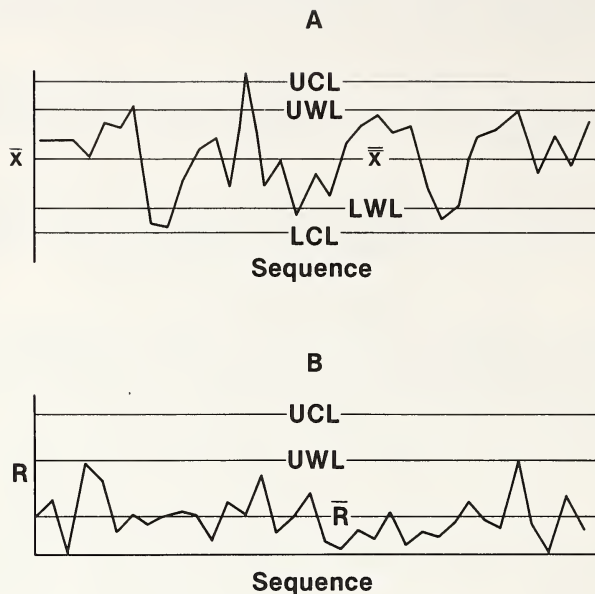
Figure 5. Duplicate measurements made on SRM 122G. A (upper) - $\bar{x}$ chart; B (lower) - R control chart

Control_Limits*

Central Line	$\bar{X}$ (mean of ≈ 15 sets of measurements)
UCL	$\bar{X} + \dfrac{3s}{\sqrt{n}}$
UWL	$\bar{X} + \dfrac{2s}{\sqrt{n}}$
LWL	$\bar{X} - \dfrac{2s}{\sqrt{n}}$
LCL	$\bar{X} - \dfrac{3s}{\sqrt{n}}$

----

*For a more extensive treatment of control limits, see Ref. 8.

For the above limits, n represents the number of repetitive measurements of the reference sample, the mean of which will be plotted on the $\bar{X}$ chart. For an X chart (single measurement of the reference sample) n = 1.

Figure 5B represents a range (R) control chart. In chemical measurements, the difference of duplicates is a good choice to plot on such a chart. The line $\bar{R}$ represents the average range obtained as the result of a reasonably large number (e.g., >15) sets of duplicate measurements. The warning and control limits are appropriate multiples of $\bar{R}$ and have the same significance as discussed in Figure 5A. The range is calculated without regard to sign (absolute value) so the lower limits are zero.

The factors for calculating limits are discussed in the reference [8]. For duplicate measurements, they are

$\bar{R}$ mean of the differences of >15 sets of duplicate measurements

UWL   2.512 $\bar{R}$

UCL   3.267 $\bar{R}$

LWL   0

LCL   0

In use, the differences of duplicate determinations are plotted on the control chart and statistical control is assumed as long as they fall within the expected limits. Again they should not fall disproportionately outside of the warning limits and trends should not be observed.

The R chart is based on the known relation between the range and the standard deviation, hence it is a form of standard deviation or precision chart. When used with an X or $\bar{X}$ chart, it is useful when deciding whether an observed deviation is due to bias or to a change in precision. When used alone, an R chart will monitor precision (but not bias).

The test samples, themselves, when measured in duplicate, may be control charted to monitor precision. The ranges for duplicate measurements of a class of samples can be plotted on the same control chart, as long as they are expected to be measurable with comparable precision.

An s control chart is based on plotting the estimate of the standard deviation obtained from measurments of n replicates of the reference sample. Since a number of measurements are required (at least seven is recommended) to estimate the standard deviation each time it is charted, with any degree of reliability, and since some calculations are required, such charts are seldomly used in chemical measurements. R charts can provide sufficient monitoring of precision with a reasonable amount of effort. They also offer the advantage of using a reasonable number of the actual test samples to monitor precision. The use of an R chart for test samples and an X chart utilizing an SRM may be ideal choices for many laboratories.

An $\bar{X}$ control chart is more robust than an X chart. Since it is based on the mean of two or more measurements, an occasional outlier will have limited influence on the decision process. However, it requires additional work and this should be considered when using such in a quality assessment program. If the assessment strategy calls for confirmatory measurements of reference samples when out-of-control is indicated, the advantage of an $\bar{X}$ chart is lessened. Such a strategy is most effective when control charts are maintained and used in a real-time mode which will also provide the advantage of ability to take immediate corrective actions and thus minimize the uncertainty of data.

The question of how to obtain the statistical information necessary to construct a control chart needs to be considered. Once the decision to develop a control chart is made, one might want to acquire the standard deviation and mean data as quickly as possible, but this could be misleading. It has been mentioned that measurements made over a short period of time show greater consistency than those obtained over a long period of time. Since the control chart will be used over a period of time, the latter is more appropriate for judging performance.

To develop control limits based on long-term behavior, it is recommended that at least 15 data points be accumulated and that no two points be obtained on the same day. This recommendation applies only to obtaining the standard deviation data to establish control limits for an $\bar{X}$ or X chart and for preparing an s or R control chart.

If an SRM is used as the control chart reference sample, the value for the central line is known, namely the certified value. If a laboratory's own internal reference materials are used, much work may be required if the "true value" for the central line is to be used. Some laboratories use an analytical mean value for the central line, and assume that this is essentially the "true value". This may be true only if the measurement process has been demonstrated to have negligible bias. The use of an analytical mean as the value for the central line can be useful in indicating stability of a process but bias can be evaluated only when true values are known.

3.4 Frequency of Use of Reference Materials

The optimum frequency of use of reference samples and also of replicates of actual test samples will depend on the stability of the measurement system and the risk involved when the system departs from statistical control (9). Since all data obtained during the period last-known-in-control to first-known-out-of-control are suspect, such intervals may need to be minimized. The real-time use of control charts and/or reference material data is a further consideration. While the following discussion is directed toward control chart maintenance, the same philosophy applies, whether this is done or whether the results on reference samples are interpreted by other means.

There are several empirical approaches to deciding on the frequency of use of reference samples. The experience of the laboratory may indicate the expected frequency of occurrence of trouble, in which case reference sample measurements, at least three in number, should be equally spaced within such an interval. Another approach is the "length of run" concept. In this, recognizable breaks in the production (of data) process are identified which could cause significant changes in precision or bias. Such breaks could include change of work shift; rest periods; change, modification, or adjustment of apparatus; use of new calibration standards; significantly long down-times; use of a new lot of reagents. At least three reference samples should be measured during any of these periods when the periods are considered to be potentially significant.

In summary, the measurement of reference materials is a risk-reducing procedure. However, if it involves more than 10 percent of a laboratory's measurement effort, either the quality control process may need improvement or too much effort is being exerted in this direction. If less than 5 percent of effort is devoted to such measurements, the laboratory may be taking too high a risk of producing unacceptable data, or may not even know the quality of the data it is producing. The above statements are made with a laboratory making a significant number of high-quality routine measurements in mind. If a laboratory's program involves occasional or one-of-a-kind measurements, the amount of quality assurance effort required, including the number of measurements of reference materials to be made may be significantly more than that indicated above.

Suggested measurement schedules for efficient utilization of reference materials are given in Table 1 and Table 2 (9). The sequence in Table 1 utilizes a combination of an internal reference material (IRM) and a SRM. The sequence in Table 2 utilizes a limited number of duplicate or split samples together with reference materials. In either case, the use of control charts is recommended on a real-time basis. Recommended critical decision points in the measurement sequences are also indicated.

Table 1. Quality Assessment Using RM's

Daily/Event Schedule

Daily/Event Schedule

CALIBRATION - FULL EXPECTED RANGE

* IRM

TEST SAMPLES - GROUP 1

* IRM

TEST SAMPLES - GROUP 2

* IRM
  .
  .

* SRM
  .

TEST SAMPLES - GROUP N-1

* IRM

TEST SAMPLES - GROUP N

* IRM

* CALIBRATION - MIDRANGE POINT

NOTES

* - DECISION POINT

1. MAINTAIN CONTROL CHARTS

X-CONTROL CHART, IRM

R-CONTROL CHART, ΔIRM

2. SYSTEM MUST BE IN CONTROL AT DECISION POINTS

3. AT LEAST 2 GROUPS: MAXIMUM OF 10 SAMPLES IN EACH GROUP

4. AT LEAST ONE SRM MEASUREMENT SHOULD BE MADE DURING

EACH SEQUENCE/DAY

Table 2. Quality Assessment Using Duplicate/Splits

Sequence Schedule

CALIBRATION - FULL EXPECTED RANGE
* CALIBRATION CHECK - MIDRANGE POINT
  SAMPLE 1
* SAMPLE 1 D/S
  SAMPLE 2-9
  SAMPLE 1D
* SAMPLE 1D D/S
* IRM or SRM
  SAMPLE 11-19
  SAMPLE 20
* SAMPLE 2D D/S
* CALIBRATION CHECK - MIDRANGE POINT
* CALIBRATION CHECK - MIDRANGE POINT/DUPLICATE

NOTES

* * = DECISION POINT
1. MAINTAIN CONTROL CHARTS
   a. DUPLICATE MIDRANGE CALIBRATION
   b. DUPLICATE/SPLIT SAMPLE
   c. X-CONTROL CHARTS, SRM AND IRM
2. SYSTEM MUST BE IN CONTROL AT DECISION POINTS
3. IF MORE THAN 20 SAMPLES, REPEAT SEQUENCE
4. IF LESS THAN 20 SAMPLES, DIVIDE INTO TWO GROUPS AND
   FOLLOW SIMILAR PLAN
5. AT LEAST ONE SRM MEASUREMENT SHOULD BE MADE DURING EACH
   SEQUENCE DAY

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4. Reference Materials

4.1 Role of Reference Materials

In the most general terminology, a reference material (RM) is a substance for which one or more properties are established sufficiently well for use to calibrate a chemical analyzer or to validate a measurement process (10,11,12). An internal reference material (IRM) is such a material developed by a laboratory for its own internal use. An external reference material (ERM) is one provided by someone other than the end-user. A certified reference material (CRM) is a RM issued and certified by an organization generally accepted to be technically competent to do so. A Standard Reference Material (SRM) is a certified reference material issued by NBS.

A reference material is for use in a decision process, hence the requirement for reliability of the value of the property measured must be consistent with the risk associated with a wrong decision. The appropriateness of the reference material in the decision process must also be considered. For some purposes, a simple substance, mixture, or solution will be adequate and the value of the property may be calculated from the data for its preparation. However, even this is best verified by suitable check measurements to avoid blunders. Many decision processes require a natural matrix reference material which may necessitate extensive blending and homogenization treatments and complex analytical measurements. In such cases, only a highly competent organization may have the resources and experience to do the necessary work.

The terms certificate and certification merely refer to the documentation that supports the reference material. Guidelines for the content of certificates for reference materials have been prepared by the International Standards Organization (13,14,15). They recommend the kind of information the certificate should contain but do not describe how it should be obtained. Furthermore, there are no guidelines for judging the relative quality of reference materials.

The guiding principle in issuing a SRM is that it will be used for measurement quality assessment, hence the property certified must be accurately known. The uncertainty in the certified values takes into account that due to measurement and any variability (inhomogeneity) between and/or within samples of the material (16). Definitive methods are used for establishing the values of the certified properties or they are measured by two or more independent reliable methods in which case the results must agree to minimize the chance for measurement bias. All certification measurements are described in the certificate or are referenced. The certification measurements are preceeded by stability studies as appropriate to set limits on the life expectancy of the material.

4.2 Concept of Traceability

The concept of traceability to national standards has been advanced in recent years to facilitate intercalibration of laboratories and compatibility of measurements. Traceability as related to a standard may be likened to genealogy in that it may describe the chain of calibrations related to establishing its value, including the intermediate standards that were used and the various measurements involved. In the area of physical measurements, calibrations of standards or artifacts with respect to the national measurement standards can be made at NBS with high precision. These may be made for secondary calibration laboratories who in turn calibrate standards for others, and so forth. Each time this is done, the uncertainty is increased due to uncertainties in a laboratory's own standards and propagation of the uncertainty of measurement. Measurement assurance programs (MAP's) are designed to minimize the latter and thus decrease the accumulation of uncertainty as measurements go lower down the measurement chain. The various measurements must be made with adequate quality assurance if reliable limits of uncertainty are assignable. The responsibility for such is that of the measurement laboratory.

While chemical measurements rely to some degree on physical measurements and require calibrated physical standards, very few chemical standards are disseminated in the same manner as the physical ones are. Hence it is difficult if not impossible to establish the traceability of most chemical standards to other such standards and especially to national standards. An exception to the above is when SRM's are used either as calibrants for a measurement process or as primary standards for chemical analysis. All measurements using such SRM's have the capability of being traceable to a common set of standards and the intercalibration of laboratories is facilitated. Relatedly, certain commercial suppliers are producing reference materials, certified with respect to specific SRM's and protocols for issuing such materials as Certified Reference Materials have been developed (17).

While an SRM ordinarily does not provide traceability in its narrowest interpretation, it may serve a broader and more useful function to provide measurement assurance which ensures both proper calibration and acceptable utilization of methodology. When specific SRM's are commonly used in a systematic manner, as by means of control charts, intercalibration of all laboratories using such and compatibility of data may be achieved as shown by Figure 6. Thus measurement networks can specify the SRM's to be used and the quality assessment procedure to be followed to attain compatibility of monitoring data, for example. While acceptable SRM

data indicate acceptable performance of the measurement system, discrepant results may not be simple to interpret since such could indicate, calibration uncertainties, application problems, or both. One cannot rule out, completely misapplication of methodology or inappropriate methodology as a source of trouble. However, a well-designed quality assurance program should facilitate the identification of the source of the problem.
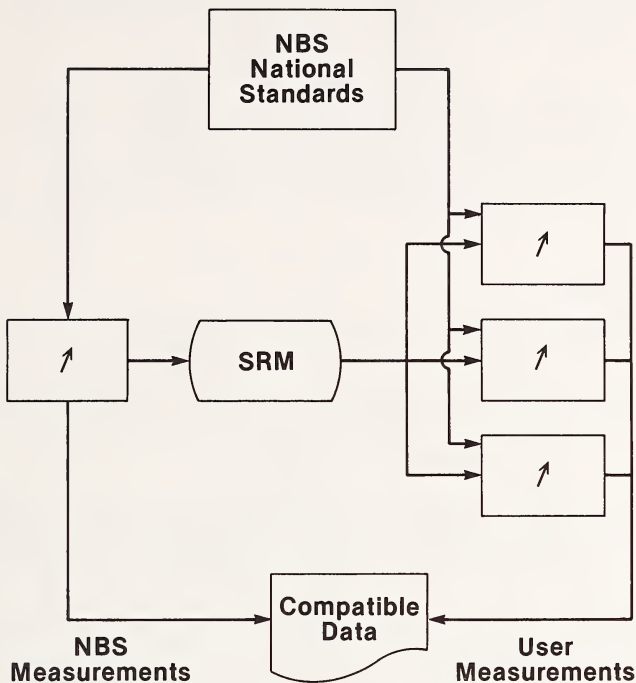
Figure 6. Measurement compatibility by intercalibration, using SRM's

5. Standard Reference Materials

5.1 Philosophy of SRM Production

Standard reference materials are considered to be services to the individual user who must pay the full cost of the service provided. Costs of development, preparation, certification, and marketing are accumulated and pro-rated on the basis of the number of saleable units that are produced. Thus the costs and benefits are prime considerations in authorizing and issuing an SRM. The production of low demand, high-production-cost, and hence high unit-cost SRM's is accordingly difficult, though not impossible.

SRM production is often preceeded by a substantial research effort. Methodology may need to be developed or potential bias problems must be solved if accurate certification is to be done. Materials-related problems such as stability, homogenization techniques, and proper conditions for packaging and storage may need investigation. Often the results of such research are applicable to wider areas of science and technology or at least to broader areas of SRM certification. In such cases, the costs of such work may be supported from general research funds and not charged to production of an SRM. Otherwise all costs, including research and development, must be recovered from sales. This increases the unit-costs of SRM's and impacts on the development of new items for which substantial research and development costs are necessary.

5.2 How an SRM is Produced

Identification of Need

SRM's are developed to meet measurement needs. The need may be specific, as the result of a regulatory issue, or general as the result of a wide-spread measurement problem. The need may come to the attention of NBS in the form of a specific request, or as the result of NBS scientists' interactions with the measurement community. Because the reference material program must be self-supporting, the magnitude of the need, cost of development, and the prospect of cost recovery through sales together with the technological chances of success are important considerations in establishing the feasibility of issuing an SRM.

Determination of characteristics/properties/specifications

The necessary properties of a useful reference material need careful consideration. The kind and level of parameters certified, the matrix and other physical characteristics, homogeneity requirements, and the maximum acceptable uncertainties for the certified values are key considerations. While a reference material is developed for a specific use, it is often possible to extend its usefulness to other areas by certification of additional parameters or by modifying the matrix. In doing the above, it must be considered that modification from a specific to a generic standard could possibly limit its usefulness for the initial purpose while not significantly extending its areas of application. Moreover, the certification of additional parameters can increase costs unless compensated by sufficient additional sales, and users do not ordinarily like to pay for information (in this case certificate values) which is not of direct use to them.

From considering factors such as those discussed above, and from discussions with the user community, minimum specifications for a candidate SRM may be drafted. These may take into consideration materials available on the market or suitable materials may need to be produced to meet the specifications. In some cases, NBS must prepare the material or at least a prototype for initial testing.

Often, preliminary research and development efforts are necessary to evaluate the feasibility of production of SRM's and/or to develop specifications.

Preliminary Studies

After a material has been obtained, measurements are made to evaluate its compliance with the specifications. While the exact level of the analyte is often not a controlling requirement, homogeneity is always an important requirement including both within and between units of issue. Ordinarily, it is desirable to certify the material as a lot rather than as individual items, in which case homogeneity between units of issue must be acceptable.

Homogeneity

Homogeneity evaluation may be done in two phases. Preliminary measurements may need to be made to accept material for conformance with specifications and to decide on such questions as pre-mixing and subdivision into units of issue (e.g., bottling) prior to certification analysis. When a multicomponent/parameter SRM is involved, this can be a major undertaking if homogeneity determinations for each constituent/property are to be undertaken at this time. When possible, a quick and precise method is sought to evaluate homogeneity. In multiparameter materials, this may not be possible for each component in which case initial homogeneity may need to be judged on the basis of that of a limited number of typical constituents.

Final homogeneity evaluation is made from interpretation of certification data on each individual constituent or property. This requires design and execution of the measurement program so that variance of measurement and sample composition can be individually evaluated.

Measurement

The certification measurements are conducted according to a quality assurance plan established before the work is actually begun. This requires development of a statistical plan for sampling and measurement, selection of methodology which has been demonstrated to be reliable, maintenance of statistical control of the measurement process, and quality assessment of the data by concurrent measurement of suitable reference materials as possible.

The methodology is selected on the basis of the following considerations. When possible, the attainable accuracy of measurement should be better than that required for use of the data. The first choice for methodology is a method of known and demonstratable accuracy. The term "definitive method" has been coined for such and is finding considerable usage, especially in relation to reference material analysis. A definitive method is one based on sound theoretical principles and which has been experimentally demonstrated to have negligible systematic errors and a high level of precision. While a technique, that is to say a measurement principle, may be conceptually definitive, a method based on such a technique, must be demonstrated to deserve such a status for each individual application.

An example of a definitive technique is isotope dilution mass spectrometry for trace analysis in which one relates the concentration of unknown samples directly to the actual weights of spikes of isotopes or isotopically labeled compounds. A mass spectrometer is used to measure isotopic ratios, obviating the need for instrumental corrections. The only theoretical uncertainty in such a process is the question of the ability to recover a natural analyte as compared with that of a spike. The accuracy attainable will depend on isotopic and chemical purity of the spike and the care used in preparation and measurement.

Examples of other definitive techniques are gravimetry and coulometry. Both are based on fundamental measurements that can be made with high accuracy. As in the case of any methodology, it must be demonstrated that no significant systematic errors are relatable or present in their use in a specific application. When using such, possible biases of application are minimized by the use of multiple analysts/instruments to the extent possible. Redundancy of measurements in random sequence is another technique to avoid application bias.

Because definitive methods are not always available, the multi-technique approach is one often used in certification of SRM's. Parameters are measured by at least two independent techniques when possible and such measurements must agree within reasonable limits to permit certification. Whenever significant discrepancies occur, additional work is carried out to reconcile them, otherwise the values cannot be certified but may be reported for informational purposes, only.

Another mode of certification, which may be called the multi-laboratory approach, is used for renewal of certain compositional SRM's. A group of laboratories of recognized competence use methods of proven accuracy and the corresponding existing SRM as a control to analyze a renewal SRM. Any significant discrepancies are resolved by careful scrutiny of the data or by reanalysis using the same or independent methodology.

In a few cases, SRM's are certified for the value of a constituent or property that is method dependent, because existing technology requires such. An example of such is the Kjeldahl nitrogen value. In such cases, demonstration of statistical control of the measurement process and agreement of results by independent analysts is a requirement for certification.

Evaluation of Data

All SRM data are given a thorough statistical analysis to establish limits of uncertainty. This will include that due to measurement and to any variability of the units of issue. The advance cooperation of statisticians in planning the experimental programs is essential if the proper measurements are to be made to enable a thorough evaluation of the reported values for the SRM. The interpretation of the certified values is discussed later in this handbook (see 5.4 and 5.5).

Follow-up

SRM production is ordinarily preceeded by studies of the stability of candidate materials. When possible, only materials which have a long shelf life are selected. If there is any limitation on stability, it is indicated on the certificate. In addition, NBS does 'shelf life' analysis on certain SRM's when it is considered that some deterioriation could be possible.

NBS ordinarily prepares a SRM in sufficient quantity so that a several-year supply is available, at the time of issue, based on anticipated demand. Sometimes demand exceeds expectations. A few SRM's are prepared in limited lots due to various considerations, such as shelf life, for example.

NBS aims to keep most SRM's in stock for ready issue and to renew SRM's before the stock is depleted. However, unanticipated demands can cause delays, and changes in technology may cause cancellation of plans for continual stocking because of conflicting priorities of competitive items.

It is the further aim of NBS to make SRM's as useful as possible to purchasers. Customer service can be provided in many cases including advice on use. In the case of questions arising from use, inquiry to the Office of Standard Reference Materials (OSRM) will get quick response and every effort will be made to provide satisfactory solutions to application problems.

A SRM is ordinarily certified using state-of-the-art methodology. This may be the methodology widely used in practical analysis with special care given to calibration, to quality control, and to elimination of sources of bias. In other cases, the methodology may be suitable only for research laboratory use. For example, isotope dilution mass spectrometry is often used-which would be an inappropriate routine technique, due to time and cost considerations. In any case, the certified value is ordinarily independent of the method of measurement. When certified values are method dependent, the methodology used in certification is always named in the certificate together with references where detailed information can be found. For a number of SRM's, a so-called NBS 260 publication describes the measurement process in detail (see front of this publication for current listing).

5.3 Differences Among Measurement Methods

Agreement of measured values by two or more independent measurement methods is one of the approved conditions for certification. Of course, measured values never agree perfectly so the statistical significance of disagreement must be considered. Results may not agree within their respective uncertainty for several reasons.

1. Matrix effects in one or each method may not be fully compensated by the calibration procedure used.

2. Systematic errors may not be fully compensated or unsuspected ones may exist.

3. It is in the nature of things that the more precise one can make a measurement, the smaller the difference that can be detected.

4. A fourth reason for two methods to disagree is perhaps the most common cause - the standard deviation of one method, or both, is underestimated.

In any event, systematic differences in measured values must be examined for their practical significance and values are not certified unless reasonable discrepancies can be resolved.

5.4 Understanding Certificate Information

SRM certificates provide a variety of information about the particular material. Compositional values with uncertainty limits are given for all certified analytes. Ordinarily the latter are for the 95% level of confidence and include allowances for the uncertainties of known sources of systematic error as well as the random error of measurement. Many certificates also will include values for other parameters or analytes which are reported for "informational purposes" only. These values are so reported because they were measured by only one technique, they are the results from discrepant measurements by several techniques, or there are homogeneity problems which detract from their analytical usefulness. Such values may have uncertainty values assigned to them, as well, but they represent the analysts' best judgment of the random error uncertainty.

The certificate sometimes will describe restrictions in the use of the sample which must be adhered to for reliable results. One of these concerns drying. Whenever this is critical, instructions for doing so are included and must be followed. In the case of several SRM's, some elements must be determined on pre-dried samples while others are determined for moist samples with subsequent correction to dry weight, based on a moisture determination.

For heterogeneous materials, the minimum weight of an analytical sample may be specified. This requirement should be followed if certified values are to be realized.

In the case of some SRM's, segregation is a potential or actual problem in that the material, though mixed at the time of certification, may segregate on standing. The certificate may instruct the user to shake, rotate, stir, or otherwise reconstitute the material. Failure to do so will not only invalidate the present measurement but may jeopardize further measurement from the same container, due to disproportionate withdrawal of constituents.

Storage of some SRM's may need to be done under prescribed conditions. Refrigeration and/or freezing may be necessary, and protection from moisture, once opened, or from radiant energy may be necessary. Because of such problems, some SRM's are certified for first use, only.

In some cases certification is valid only for a finite lifetime (e.g., 1 year, 5 years). This is to limit NBS liability to individually notify users in case there is a change in the material. The lifetime is always calculated from the time of shipment -- it is never related to packaging dates marked on the container.

These and other restrictions are necessary to protect the integrity of the sample or to ensure results that will be consistent with the certified values. NBS can accept no responsibility for validity of the material if such instructions are not faithfully followed.

5.5 Uncertainty of Certified Values[1]

For the purpose of this discussion, SRM certification can be divided into two classes:

A. Each unit is measured and carries its own value (e.g., permeation tubes).

B. Samples chosen statistically from the lot of SRM are measured, and one certificate gives the value for all units (most chemical types).

The uncertainty of the certified values for group A SRM's will depend entirely on the uncertainty of measurement. This will be based on the standard deviation and best estimates of uncertainties of the systematic errors which have been corrected for, to the extent possible.

For group B SRM's, any differences in the certified property within the units or between units of the lot poses a problem. A sampling and measurement scheme has to be devised to determine whether inhomogeneity exists and to estimate its magnitude whenever it is important to the use of the SRM.

Homogeneity checks may be made using two different sampling schemes. In one, a batch of material is subsampled, using a statistically developed scheme, and measurements are made to detect significant differences in the compositions of the samples. This has the advantage that grossly heterogeneous material would be rejected, thus saving the time and cost of packaging unacceptable material. It has the disadvantage that further heterogeneity could be introduced in acceptable material by segregation, discrimination, or contamination during packaging. For material believed to be essentially homogeneous, bulk examination may be the method of choice. Once homogeneity is confirmed, the material may be analyzed and packaged as required, which could have advantages in some cases.

Material which is considered to have measurable heterogeneity is best checked after packaging into bottles, vials, or whatever. Not only is it possible to detect original heterogeneity but also any that might result from the packaging process. Three kinds of heterogeneity are generally possible:

a. Between units vs. within units

b. Trend or pattern — along a rod, within a sheet or block of material, in the order of preparation, etc.

c. Between blocks of units — processed on different days, between drums, between lots, etc.

The sampling scheme used for each SRM depends to a large extent on the subject expert's knowledge and experience of what particlar type of heterogeneity is most likely to occur, and the sampling scheme will be designed predominately to check on variability due to that source. A knowledge of the details of the packaging process is also required, such as the sequence of filling bottles or the order in which specimens were cut from a massive material.

If the material is found to be essentially homogeneous, it is accepted; if the material shows large variability, it is rejected. Often the variability is at about the level of what can be detected by a particular analytical method. In that case, the analytical error and the heterogeneity of the material both contribute to the uncertainty in the final product — SRM units.

Let σ_m be the standard deviation of the analytical method, and σ_c be the standard deviation of the value of the individual units about the mean value of the lot. Then the standard deviation σ of a single measurement on a unit, drawn at random from the lot would be

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[1]From a lecture by H. H. Ku, National Bureau of Standards, presented at Precision and Accuracy, Seminar, 27 March 1980. See also Ref. 10, p. 296, and Ref. 12.

$$\sigma = (\sigma_m^2 + \sigma_c^2)^{1/2}$$

Reliable estimates of two of the three sigmas allow an estimate of the third.

When possible, σ_m is evaluated independently of the measurement of the SRM. In this case, the standard deviation, σ, of the measured values of individual samples, together with the value for σ_m, permits an estimation of σ_c.

Often, possible matrix effects considerations preclude or raise questions about the independent estimation of σ_m. And even if σ_m can be assumed to have a certain value, it may be necessary to verify it for the SRM certification measurements.

By duplicate measurements of portions of n randomly selected samples, both σ_m and σ_c may be estimated. Let x_i and y_i be the first and second measurements on portions of the ith unit (bottle, disc, sub-sample, etc.). The results may be tabulated as:

$$x_1 - y_1 = d_1 \qquad\qquad \frac{1}{2}(x_1 + y_1) = z_1$$

$$x_2 - y_2 = d_2 \qquad\qquad \frac{1}{2}(x_2 + y_2) = z_2$$

$$\vdots \qquad\qquad\qquad\qquad \vdots$$

$$x_n - y_n = d_n \qquad\qquad \frac{1}{2}(x_n + y_n) = z_n$$

$$s_1^2 = \frac{1}{2n} \sum (d_i)^2 \qquad\qquad s_2^2 = \frac{1}{n-1} \sum (z_i - \bar{z})^2$$

$$s_1^2 \text{ estimates } \sigma_m^2 ; \qquad\qquad s_2^2 \text{ estimates } \sigma_c^2 + \frac{\sigma_m^2}{2}$$

From these results, the estimates of σ_m^2 and σ_c^2 can be calculated.

Another way in which σ_c may be estimated is by the use of an independent method of measurement. Occasionally a highly precise method is available for intercomparison of samples but may not be feasible for use for certification measurement, due to calibration problems. Such a procedure is especially useful for confirmation of the homogeneity status of a candidate SRM.

In any evaluation of homogeneity, it must be remembered that each analyte certified must be individually examined for homogeneity considerations. It is not justifiable to extend conclusions on the homogeneity for one analyte to another even though they may be closely related in other respects.

Homogeneity statements always must be coupled with the size (mass) of sample to be used. Basically, heterogeneous materials such as bulk solids may exhibit gross heterogeneity as the sample size is diminished (see for example Appendix D.2). In crushed material, for example, individual particles could have widely different compositions. Apparent homogeneity is improved as larger sample sizes are considered since individual differences will be averaged out. Accordingly, the minimum sample size necessary to realize the certified values often will be specified in the certificate. The NBS certified values cannot be extended to the composition of subsamples smaller than the recommended size.

Materials of group B which are found to be essentially homogeneous are certified on a lot or bulk basis. All sub-samples are considered to have the same composition which is certified together with a confidence interval based on estimates of uncertainties for both random and systematic errors of measurement.

Materials with significant but usable levels of inhomogeneity may be certified as a batch, in which case the statistical tolerance limits are given. This includes the average value of all samples in the batch and limits within which individual samples are expected to lie, with a stated confidence. Because only a limited number of samples have been analyzed, one cannot say, with certainty, the limits for a given percentage of samples but only a probability that the limits are valid. Thus one could say that there is a 95 percent confidence that 95 percent of the samples in the batch lie within some specified limits (statistical tolerance limits) and this is often what is stated on a certificate for this kind of material.

In the case of most granular SRM's, the within unit-of-issue heterogeneity is essentially the same for all units-of-issue and no significant average difference is to be expected between individual units. In such a case, the average composition of sub-samples within all units would not be expected to differ, significantly. In using such SRM's it should be remembered that the composition of any sub-sample is expected to be within the tolerance limits and the average composition of a number of sub-samples is expected to approach the certified value.

6. Use of SRM's

6.1 Kinds of SRM's

Standard Reference Materials may be described as well-characterized and certified materials, produced in quantity, to improve measurement science and technology. They fall into three general categories (see Table 3): (a) certified chemical composition/purity standards; (b) certified physical property standards; (c) engineering type standards. Categories (a) and (b) may be further subdivided into those materials related to basic measurements and those to applied measurements.

Table 3.   Inventory of SRM's, - 1969 - 1984

SRM Category	Number of SRM's	1969	1979	1984
Chemical Composition/Purity				
Steels and steel-making alloys		141	161	159
Cast, white, ductile, and blast furnace irons		16	23	25
Nonferrous metals and alloys		75	130	120
Gases in metals		9	29	13
High-purity metals		1	8	8
Electron probe microanalytical		0	6	12
High purity chemical/microchemical		16	26	18
Clinical analysis		1	22	28
Biological/botanical		0	9	9
Environmental analysis (gases, liquids, solids)		3	72	109
Forensic analysis		0	3	2
Oil-soluble metallo-organic compounds		24	24	22
Fertilizers		0	3	3
Ores		10	22	21
Cements		5	7	9
Minerals, refractories, carbides, glass		17	22	29
Glass trace elements		0	13	8
Special nuclear materials		18	33	30
Isotopic reference standards		9	15	14
	Subtotals	345	628	639
Physical Properties				
Ion activity		6	17	13
Physical properties of glass		7	13	15
Elasticity		0	1	1
Density		4	3	2
Polymer molecular weight		2	7	10
Polymer rheology		0	1	1
Temperature fixed points		5	12	14
Calorimetry		3	13	8
Thermometers/thermocouples		0	4	4
Vapor pressure		0	4	3
Thermal conductivity/expansion		0	29	16
Thermal resistance		0	1	10
Magnetic properties		0	11	10
Optical properties		4	20	24
Radioactivity		40	156[a]	118[a]
Permittivity		6	7	6
Electrical resistivity		0	14	15
	Subtotals	177	333	270
Special Engineering Properties				
Standard rubbers		20	14	12
Computer tapes		0	3	4
Optical character recognition		0	4	1
Sieve sizing		3	5	4
Cement turbidimetric and fineness		1	1	1
Color		36	2	2
Fading standards		4	4	1
Flammability/smoke density		1	3	3
X-ray and photographic step tablets		1	4	4
Tear resistance-tape adhesion		1	1	1
Metal coating thickness		35	32	10
Octane rating		0	2	0
	Subtotals	102	76	43
	Total	544	1037	952

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[a]Many of the radioactivity SRM's consist of short-lived isotopes and are available only on special order for limited time periods during the year.

Industrial materials that must be analyzed frequently for quality control of production processes constitute a major fraction of all SRM's. Predominant in this group are metals in which essentially all major alloy types are specifically represented. Ores, minerals, cement, glass, and ceramics are also included. Ordinarily, these SRM's are sampled directly from the container and analyzed by the user in the same manner as the day-to-day samples of the laboratory. The results of such SRM analyses are frequently control-charted to monitor the measurement process.

High purity chemicals for use as primary standards in a wide variety of chemical analyses constitute an important group of SRM's. Typically, the user will prepare solutions from these materials that may be used directly in the analytical process or for standardizing other analytical reagents.

Clinical laboratory standards compose a large and growing group of SRM's. Originally, such SRM's consisted largely of pure substances from which spikes or calibration solutions could be prepared. They are now being augmented by natural matrix materials containing analytes of interest that are analyzed directly without preliminary preparation.

The environmental group satisfies most of the routine monitoring requirements and some special situations as well. SRM's related to all of the criteria air pollutant analyses were introduced early into the program. These were followed by SRM's related to the measurement of emissions from mobile and stationary sources, priority pollutants, and hazardous wastes. The SRM's for the gaseous pollutants of the atmosphere are particularly slanted toward the calibration of analyzers and to provide traceability for industrially-produced working standards. Because of the wide variety of sample types and the number of constituents of interest, it is virtually impossible to provide matrix matches for most of the samples encountered by organic analysts. Accordingly, the SRM's in this area represent either high-priority sample types or generic materials that should be widely applicable. Some SRM's useful for spiking or other types of standards preparation are also available.

A number of natural matrix SRM's certified for most of the inorganic constituents of environmental interest and some organic substances have been produced. These include several biological matrix samples (orchard leaves, now replace by citrus leaves was the first SRM in this group) and also urban particulate matter and river and marine sediments. Industrial hygiene analysis materials are a small but important sub-group in the environmental category. This list will be augmented as possible, and as demand is shown for additional items.

The physical property standards reflect many of the kinds of measurements made in testing laboratories. The gamut runs from those useful for the conventional physical measurements of temperature, melting point, vapor pressure, calorimetry, conductivity, and thermal expansion to color, thickness of electrodeposits, and fineness of powders. Radioactivity standards are also classified in this category.

Engineering standards are a small but growing group which is rather diverse. Standard rubbers, SRM's for evaluating the performance of magnetic tapes, and flammability standards are examples.

NBS Special Publication 260, Catalogue of Standard Reference Materials, lists all SRM's, research materials, and special reference materials that are available and those that are in progress at the time it is issued. The catalogue is updated periodically, and supplements are issued in the interim. See page 3 for how to receive a copy.

The SRM program tries to keep abreast of and even anticipate changes in technology, since it may take a period of several years to develop and certify a new SRM. Input from the user community, from contacts with professional colleagues, and NBS's own measurement experience are influential in guiding and establishing priorities for SRM development. SRM sales provide guidance on inventory maintenance and priorities when questions of renewal must be decided. While present contacts are extensive, additional input to the decision process is sought. It is believed that there are areas of technology, and especially new technologies, where SRM's are not significantly utilized and which would benefit from their use. Information about these is especially solicited.

Table 4 lists the major areas into which SRM development is expected to expand in the near future. The list may be revised as technology advances and as new technologies appear. User input is actively sought to confirm the wisdom of the proposed plans, or to provide information on which revisions might be considered.

While SRM's constitute the largest category, two other types of reference materials described below are produced or distributed by NBS.

Research Materials (RM's) are in addition to and distinct from the SRM's issued by NBS. The distinctions between Research Materials and Standard Reference Materials are in the information supplied with them and the purpose for which they should be used. Unlike SRM's, the RM's are not issued with Certificates of Analysis; rather they are accompanied by a "Report of

Table 4. Some Major New SRM Needs Forecast for the Period/1984-1989.

Trace Organic Analysis

    Organic pollutants in natural matrices
    Nutrients and toxic substances in food and agricultural products
    Enzymes, individual proteins, and therapeutic drugs in human serum
    Additives in plastics

Trace Elemental Analysis

    High-performance alloys
    Plastics
    Glass and ceramic materials
    Semiconductor materials
    Fibers

Bulk Compositional Analysis
    Recycled materials
    Uranium and plutonium nuclear fuels (for nuclear safeguards)
    Fibers

Quantification of inorganic chemical species

Density Standards	Nondestructive Evaluation Standards
Dimensional Standards	Radiographic sharpness
	Visual acuity
Electron microscope magnification	Dye penetrant crack plate
Particle sizing	
Photomask linewidth	Nuclear Waste Disposal
Voltage Standards (Josephson Junction)	Leach rate testing
	Thermal expansion and
Optical Properties	conductivity of waste forms
Fluorescence	Polymer Molecular Weight
Reflectance	Star-branched polystryenes
Wavelength	Ethylene-propylene copolymers
Electronic Properties	
Spreading and sheet resistance	
Glass dielectric	

Investigation," the sole authority of which is the author of the report. A Research Material is intended primarily to further scientific or technical research on that particular material. One of the principal considerations in issuing an RM is to provide homogeneous material so that an investigator in one laboratory can be assured that the material he has is the same as that being investigated in a different laboratory. There are presently several materials in this category.

Special Reference Materials called GM's are distributed by NBS to meet industry needs. These materials have been standardized either by some Government agency other than NBS, or by some standards-making body such as the American Society for Testing and Materials (ASTM), the American National Standards Institute (ANSI), and the Organization for International Standardization (ISO). For this class of materials, NBS acts only as a distribution point and does not participate in their standardization.

6.2 Choosing an SRM

The large number of SRM's available may cause some confusion as to which to choose for a given purpose. Obviously, matrix match is a major consideration since there is little or no difficulty in interpreting test results of such materials. Close match is only possible when recurring analysis of well-defined materials is of concern, i.e., large volume industrial products. However, all of the SRM's have been developed as the result of wide-spread needs and much consideration has been given to providing matrices that are either typical or that can satisfy generic purposes.

When a matrix match is possible, analysts are advised to use such SRM's. In consideration of this, many users stock a relatively large number of them, encompassing the variety of materials that they expect to analyze. For many users, a perfect matrix match will not be possible, hence professional judgement will be required to select the ones most useful for

each situation. The Office of Standard Reference Materials, and especially the NBS scientists who certify them, have special experience in most of the measurement areas represented by the SRM inventory. Inquiry to OSRM (see p. 34) will provide access to the scientists who may be able to advise in the selection and use of appropriate SRM's for a given purpose.

6.3 Use of SRM's

Because of the high reliability of the certified values, Standard Reference Materials, find a wide variety of uses ranging from special occasions when a material of known properties is needed to test some aspect of measurement, to the continual quality assurance of measurement systems. Table 5 is a summary of the most common kinds of applications.

Table 5. Uses of SRM's in Measurement Systems
_____

Method Development and Evaluation

       Verification and evaluation of precision and accuracy of test methods
       Development of reference test methods
       Evaluation of field methods
       Validation of methods for a specific use

Establishment of Measurement Traceability

       Development of secondary reference materials
       Development of traceability protocols
       Direct field use

Assurance of Measurement Compatibility

       Direct calibration of methods and instrumentation
       Internal (intralaboratory) quality assurance
       External (interlaboratory) quality assurance
_____

Any use of a reference material depends on the ability to make valid inferences from the measurement results. This involves the tacit assumption or demonstrated evidence that the material is reliable and capable of challenging the measurement process. Furthermore, the measurement process must be known to be in a state of statistical control, since limited measurements of the reference material will be used for predictive or evaluative purposes.

Examples of one-time uses of SRM's as known test materials are numerous. Whenever an analytical method is developed or modified, a well-characterized test material is needed to evaluate its performance characteristics. SRM's, as appropriate, are obvious choices in such cases and numerous examples are cited in the literature. A survey during an 18 month period (10) identified 40 research articles citing the use of SRM's in the development or evaluation of a wide variety of different methods for chemical analysis and in particular for trace analysis. Likewise, performance checks of instrumentation, such as linearity, stability, and sensitivity are highly dependent on reliable test materials. Here again, an SRM is a logical choice for such a purpose.

When new methodology is adopted by a laboratory, familiarization measurements must be made in order to gain proficiency in its use. The use of SRM's will eliminate questions of stability and homogeneity that might complicate the test results when using other materials. Some laboratories use SRM's to confirm a new analyst's capability to perform tests before undertaking measurements in their test programs.

When a contract laboratory is needed to provide analytical services to an individual or in a monitoring program, evidence of the capability to do so is often a requirement. The analysis of test samples provided by the client is one approach to evaluate the competence of candidates. SRM's are virtually unexcelled for this purpose. The only questions in such usage are the selection of an appropriate SRM and the possibility of falsification of data due to recognition of the test sample as an SRM with a known composition.

The use of SRM's for educational purposes should not be overlooked. Understanding of analytical chemistry is best demonstrated by practical laboratory work in which students analyze real samples. No better ones are available than SRM's which provide the opportunity to test both the precision and the accuracy of the analytical results.

SRM's find use as calibrants in certain cases. For example, the practical pH scale is defined by NBS SRM's, and SRM's for fixed temperature points are available. The use of SRM's as primary chemical standards has already been discussed. Some industrial matrix SRM's, and

particularly metals, are used for calibrating chemical analyzers. Many of the standard methods developed by ASTM Committee E-2 on Emission Spectroscopy can be calibrated directly with appropriate SRM's. As an example, ASTM Standard Method E 322 is used when analyzing low alloy steels by X-ray fluorescence and NBS D-800 and 1200 series of low-alloy steel SRM's are recommended as calibrants.

One of the major uses, and the original driving force behind SRM development, is for the quality assurance of measurement processes. When various analysts use different methodologies (and even the same methods), unacceptable discrepancies can arise, usually attributable to calibration or procedural differences. The analysis of commonly available reference materials can identify such problems and lead to their solution.
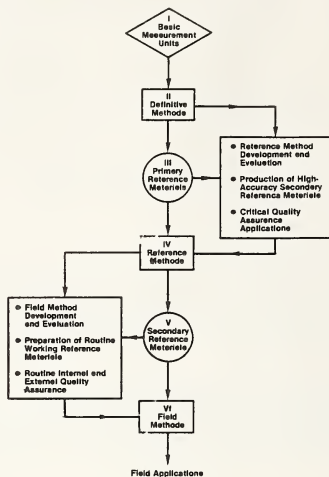
Figure 7. Systems Approach to Measurement Accuracy

This figure depicts a hierarchical system of measurement methods and reference materials. The function of each component (1 to 6) is to transfer accuracy to the level immediately below it and help provide traceability to the level immediately above it, thus helping to assure overall measurement compatibility. Proceeding from the bottom to the top of the measurement hierarchy, accuracy requirements increase at the expense of decreased measurement efficiency. At the top are the so-called definitive methods of analysis or test, which give the most accurate values obtainable. Unfortunately, most definitive methods (for example, gravimetric techniques for preparing analyzed gas SRM's) are usually time consuming and sophisticated. Thus, they are not economically acceptable for widespread and routine use. Definitive methods, however, are used whenever possible to certify NBS SRM's. With these materials, accuracy can be transferred throughout a measurement system.

SRM's are commonly used in developing reference methods and assuring their accuracy. Such methods may be suitable for direct use. Alternatively, they may serve as a basis for developing or evaluating other methods. Reference methods are also commonly used for producing secondary reference materials, which, in turn, are directly used in routine field measurement applications.

In principle, the accuracy of numerous field methods can be traced to a definitive method in a hierarchical accuracy-based measurement system. SRM's and other reference materials are essential in the transfer of accuracy. Also essential are good methods, good laboratory practices, well qualified personnel, and adequate quality assurance procedures.

The complexity of modern chemical analysis provides many sources of error and opportunities for introduction of bias and imprecision. Accordingly, such systems must be operated under a rigid quality assurance system if results are to be meaningful. It is not sufficient to check the calibration of instruments although this is always necessary. Rather, the performance of the entire system needs to be monitored on a regular basis. SRM's are finding increasing use as test materials to monitor system performance.

SRM's are best used on a regular basis. The sporadic use of reference materials when trouble is suspected is a legitimate use but systematic measurement in a control-chart mode of operation will generally be more informative and is highly recommended. SRM's may be used as the sole reference material or they may be used with internal reference materials in a systematic manner, thus conserving the former and adding credence to the latter.

The use of SRM's as quality assurance materials is discussed in more detail in the article contained in Appendix (D.3).

6.4 Interpretation of Reference Material Analyses

Some SRM's have a matrix identity with test samples and can be used directly to establish the response function of chemical analyzers. Others may be used by a laboratory as their primary standards. However, the majority of the SRM's are quality assurance materials and should be analyzed regularly or on occasion to monitor the performance of a measurement system.

The four general cases for use of SRM's as quality assurance materials are illustrated in Figure 8 (a-d). When a matrix match is possible (8a), the uncertainty in the sample measurements can be equatable to that observed in measurement of the SRM. When such a match is not possible but an SRM with a related matrix is available (8b), the test sample uncertainty may be relatable to those observed when measuring the SRM's. Even when the above situations do not apply, the measurement of an appropriate SRM (8c) can monitor the measurement system and its performance when measuring test samlples can be inferred in many cases. When an SRM is unavailable or not used, measurement uncertainty must be inferred from other evidence such as physical calibrations and the experience of others, for example. Obviously it is to the advantage of a laboratory to evaluate its own performance, using SRM's or other reliable reference materials whenever possible.

The results obtained when analyzing reference materials should be interpreted after due consideration. When measured consistently and utilizing control charts, they can effectively monitor a measurement process. When measured in isolation the results could be inconclusive or even misleading.

The inability to correctly analyze a reference material may cast serious doubts on the reliability of a measurement process but provide no diagnostic information. Also, the correct analysis of an SRM may not necessarily indicate the converse. Referral to Figure 9 will clarify this point. In this figure, measured values are plotted with respect to the expected values, certified values, for example. For an unbiased system the data would be represented by line A.

Various kinds of linear measurement bias are illustrated in Figure 9. Line B corresponds to a constant bias (negative in this case but it could be positive, as well) while line C results from bias which is proportional to the concentration level of the sample. The proportionality factor could be less or greater than unity (shown). Line D results from a combination of constant and level-proportional bias. It is obvious that the measurement of one reference sample will not evaluate the performance of a measurement system throughout a concentration range unless supplemented by other information. One could even obtain a result, 2, and conclude that a system was unbiased when the analysis of additional reference materials might indicate performance representable by line D, for example.

Occasionally, situations may occur where linear treatment of biases does not apply, but these are not described in the present paper.

When possible, the analysis of several reference samples, spanning the concentration range of interest, is the most useful way to investigate measurement bias. The three sample approach - analysis of a low, middle, and upper range sample - is practical in most cases, provided that the reference samples are sufficiently homogeneous and that the range of analytical interest is covered. Bias is even identifiable using relatively non-homogeneous samples, provided that a sufficient number are analyzed. It is highly unlikely that n randomly selected samples from a lot would all deviate in a systematic manner from a population mean value, provided n is 5 or more. Thus the measurement of such should indicate the kind of bias, that may be present. Statistical advice may be necessary, in such cases to plan the number of samples and the replicate measurements needed and to evaluate the test results.

When supported by other data, the measurement of even a single reference sample can be meaningful. Thus a knowledge of the standard deviation of measurement, obtained from other data, would answer whether point (1) or point (2) could be considered as represented by line A. Measurement of a series of non-reference-material samples might provide some knowledge about the slope and hence assist in the interpretation of the SRM measurement data. The best diagnostic information would be obtained from the measurement of a series of SRM's containing graduated levels of analyte. When such are available, the use of all of them will maximize the information on the performance characteristics of an analytical system.

SRM ///// **Material**

U_{SRM} U_M

Measurement

$U_{SRM} \equiv U_M$

(A) Matrix-Match

SRM **Material**

U_{SRM} U_M

Measurement

$U_{SRM} = k\ U_M$

(B) Matrix-Related

SRM - - - **Material**

U_{SRM} U_M

Measurement

$U_{SRM} \approx k\ U_M$
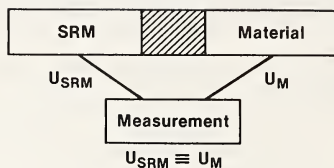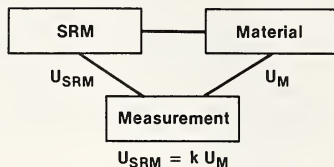
(C) Matrix-Relation Inferred

SRM **Material**

Measurement

Other Evidence **Physical Standards**
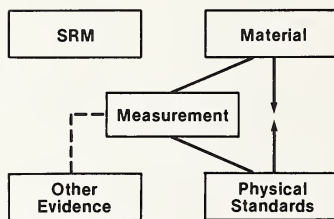
(D) SRM — Not Used

Figure 8. Interpreting SRM measurements
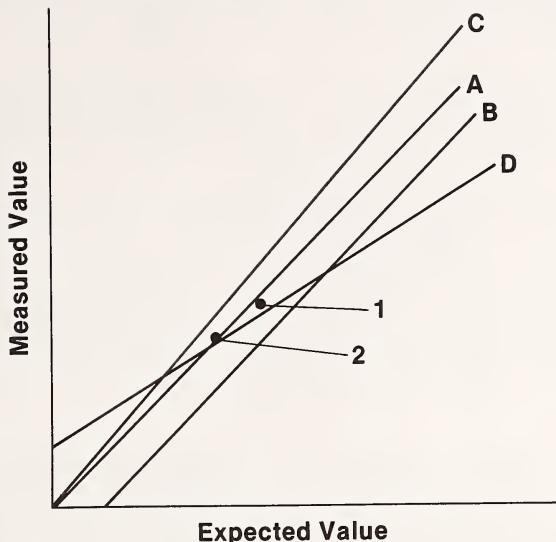
Figure 9. Identifying measurement bias

An SRM may have a reasonable matrix match with test samples but differ from them in level of concentration. If the level of analyte in the SRM is higher than that of the test sample, it may be possible to quantitatively dilute the SRM. The best diluent is the matrix of the SRM but a neutral matrix may be used in some cases. Two SRMs containing different levels of an analyte may be proportionally mixed to obtain a series of materials, ranging from the concentration level of the lower to that of the higher. These techniques are described in ASTM D-3975. - Preparation of Samples for Collaborative Testing of Methods for Analysis of Sediments. The expression used to calculate the composition of a blend of two samples, A and B, is as follows:

$$\alpha_{A+B} = \frac{\alpha_A W_A + \alpha_B W_B}{W_A + W_B}$$

where

α_A = weight percent (or ppm) of constituent α in sample A
α_B = weight percent (or ppm) of constituent α in sample B
α_{A+B} = weight percent (or ppm) of constituent α in mixture
W_A = weight of sample A in mixture
W_B = weight of sample B in mixture

When a material is diluted with a second material containing an insignificant amount of the analyte of interest, the expression to be used is:

$$\alpha_{A+D} = \frac{\alpha_A W_A}{W_A + W_D}$$

where

W_D = weight of diluent sample mixed with W_A.

All dilutions must be made with care. Because uniform mixing may be difficult to achieve, the entire mixture that has been prepared may need to be used, rather than sub-samples of it. Despite such problems, the technique is attractive since it can provide reference materials that simulate the test samples more closely, and to evaluate a measurement process over a range of concentration levels, as discussed in Section 6.4.

When possible, the analysis of several reference samples, spanning the concentration range of interest, is the most useful way to investigate measurement bias. The three sample approach - analysis of a low, middle, and upper range sample - is practical in most cases, provided that the reference samples are sufficiently homogeneous and that the range of analytical interest is covered. Bias is even identifiable using relatively non-homogeneous samples, provided that a sufficient number are analyzed. It is highly unlikely that n randomly selected samples from a lot would all deviate in a systematic manner from a population mean value, provided n is 5 or more. Thus the measurement of such should indicate the kind of bias, that may be present. Statistical advice may be necessary, in such cases to plan the number of samples and the replicate measurements needed and to evaluate the test results.
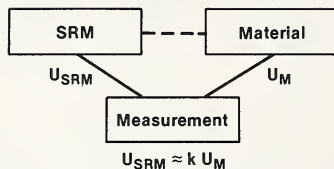
6.5 Evaluation of Measurement Error

The values measured by a user for an analyte or a parameter will rarely agree fully with the certified value due to uncertainties in each. The question naturally arises as to how large a difference is significant. This will depend on the uncertainty of the measurement by the user (see Figure 10) and the certification limits for the SRM. The former can be calculated, using the expression (see also Section C.5):

$$\overline{X} \pm \left(\frac{ts}{\sqrt{n}} + B\right)$$

(where $\overline{X}$ is the mean of n measurements by the user whose estimated standard deviation of measurement is s. Student's t value will depend on the number of degrees of freedom in the estimation of s (n-1 if s is based on the measurement of the moment) for a 95% confidence level which is the usual level for certified values of an SRM. The value, B, is the user's estimate of the magnitude of any uncorrected biases inherent in his measurement and is based on experience and professional judgment.
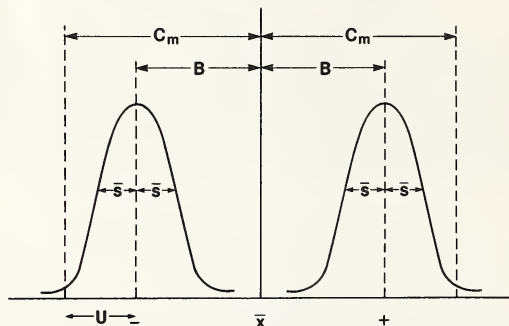
Figure 10. Uncertainty of measured value

C_m = Uncertainty of Measured
B = Biases, Errors Inherent in Measurement
s = Precision of Measurement
$\overline{s}$ = Precision of Mean of n Measurements (really $s_{\overline{X}}$)

$$C_m = \frac{ts}{\sqrt{n}} + B$$

30

If the confidence interval intersects the confidence or tolerance interval of the SRM, there is agreement. If not, then a discrepancy exists which should be investigated. In the case of heterogeneous SRM's, several sub-samples may need to be measured to evaluate measurement bias.

If an apparent discrepancy is found, it is advisable to look close r at the estimates of uncertainty. Rarely will a user's uncertainty ($\frac{ts}{\sqrt{n}}$) be less than that of the NBS measurements which are done with state-of-the-art techniques. Perhaps there are unsuspected biases in the user's laboratory, which the SRM has uncovered. If an explanation cannot be found, the user should communicate with NBS OSRM who will look into the matter and advise as possible. The sample may have deteriorated or become contaminated, so the possibility of such may need to be considered.

It cannot be too strongly emphasized that statistical control must be attained before any data can be believed and any errors identified or corrected. There is no easy way to identify assignable causes for either unacceptable bias or precision, which is the first step for corrective actions. Consultation with experienced users of the methodology employed may be helpful to suggest approaches to follow, if not the specific solutions. The magnitude of the errors encountered may rule out certain sources and indicate likely ones. However, the simultaneous existence of several sources of unacceptable error cannot be discounted.

In diagnosing error, it should be remembered that random errors add up in quadrature, which is to say the variance of random errors is additive, as discussed in 2.1.1. When the measurement system is well-understood, it may be possible to estimate the variance of the individual steps or operations of which it is composed and to compare such with the magnitude of the errors of concern. Obviously, the step or operation with largest variance is the first one to be considered when other information is not available.

On the other hand, there is no reason to believe that biases are randomly distributed but rather they add up, algebraically. According, small systematic errors contribute differently than small random errors.

Whenever excessive bias or imprecision is found to be present, corrective action needs to be taken, otherwise the measurement process will have limited usefulness. The first question that needs to be answered, in this regard, is whether the unsatisfactory situation is inherent to the methodology or is due to its application in a given laboratory or even by specific persons. Collaborative test data and/or the research findings of others may indicate the magnitude of the former. If the experience of a laboratory is not consistent with this, excess application imprecision or bias would be suspected.

Factors to be considered in reducing operational (non-state-of-the-art) bias include:

        better quality of calibrants
        improvement in calibration
        reducing contamination
        reducing mechanical losses
        reducing solution/extraction inefficiences
        removal of interferences.

Factors to be considered in reducing operational random error include:

        improvement of technical skills
        improvement of manipulative skills
        improvement of environmental control
        closer tolerances in operational parameters
        improved instrumentation
        reducing variability of blanks.

7. Reporting Analytical Data

7.1 Limits of Uncertainty for Data

Data are of limited use and even can be useless unless limits of uncertainty can be estimated and assigned to them [1]. The limits should include the limits of uncertainty of any systematic error (bias) and the random errors of measurements. Estimations of limits of systematic error are based on judgment and require a full understanding of the measurement system used. The experience of the analytical community is helpful in this respect. The random error component is based on the skill and experience of the laboratory making the measurements and is evaluated from the standard deviation of the measurement process.

When the measurement process is demonstrated to be in a state of statistical control, the process standard deviation may be used to evaluate the confidence interval for the mean of n measurements (see C.5). The use of control charts is the best way to demonstrate that a process is in a state of statistical control at the time the measurements are made and this can minimize the amount of work needed to establish confidence limits for the data.

In the absence of a control chart, a sufficient number of replicate measurements must be made to demonstrate statistical control and to estimate the standard deviation of measurement with a measurable degree of confidence. The minimum number of replicate measurements required is somewhat arbitrary and depends on the risk concerned with exceeding the limits of confidence that are stated. Metrologists often recommend 7 to 30 determinations as a reasonable number of replicates. The uncertainty of the standard deviation increases rapidly below 7 and little is to be gained by increasing the number above 30.

It is not considered good practice to correct for biases without understanding their origin. Biases such as analytical blanks should be measured as accurately as necessary and possible and the results are corrected directly for them [18]. This is proper because analytical chemists believe that blanks are additive errors. Biases such as found when measuring SRM's are investigated to identify their source so that they can be eliminated, minimized, or corrected-for in a proper manner. As already pointed out (see 6.4) the method of correction will be dictated by the nature of the bias. The most reliable approach is to remove the bias rather than to correct for it.

The treatment of bias related to the question of recovery often troubles the trace analyst. Usually corrections are not made but recoveries are reported as one of the qualifications for the data. The recovery, no matter what its value, should be shown to be in a state of statistical control, and this should be a requirement for reporting data of this kind. When a recovery determination is made and the value obtained is variable or does not fall within control limits, corrective action is indicated and control should be re-established before data may be reported.

7.2 Significant Figures

Numerical data are often obtained (or at least calculations can be made) with more digits than are justified by its accuracy or precision. So that it is not misleading, such data when reported should be rounded to the number of figures consistent with the confidence that can be placed on it (see guidelines for Reporting Results 7.3). Accordingly, metrologists have adopted the terminology of significant figures in describing the resulting data. The number of significant figures is said to be the number of digits remaining when the data is so rounded. The last digit, or at most the last two digits are expected to be the only ones that would be subject to change on further experimentation, for example. Thus, for a measured value of 20.5, only the 5 and, at most the 0.5 would be expected to be subject to change. Such data would be described as having three significant figures.

In counting significant figures, any zeros used to locate a decimal point are not considered as significant. Thus 0.0025 contains only two significant figures. Any zeros to the right of the digits are considered as significant, thus only those that have significance should be retained. Thus 2500 and 2501 each have four significant figures. Zeros should not be added to the right of significant digits to define its magnitude, unless they are significant, since this would confuse the significance of the value. For example, it is not good practice to report a value as 2500 ng but rather 2.5 mg if the data is reliable to two significant figures. The use of exponential notation, e.g., 3.5×10^3, is an acceptable way to report data with two significant figures which would otherwise have to be reported as 3500, suggesting 4 significant figures.

In multiplication and division, the operation with the least number of significant figures determines the numbers to be reported in the result. For example, the product 1256 x 12.2 = 15323.2 is reported as 1.53×10^4. In addition and subtraction, the least number of figures to either the right or the left of the decimal point determines the number of significant figures to be reported. Thus the sum of 120.05 + 10.1 + 56.323 = 156.473 is reported as 156.5 because 10.1 defines the reporting level. In complex calculations involving multiplications and additions, for example, the operation is done serially, and the final result is rounded according to the least number of significant figures involved. Thus (1256 x 12.2) + 125 = 1.53×10^4 + 125 = 1.54×10^4.

The following rules should be used in rounding data, consistent with its significance:

1. When the digit next beyond the one to be retained is less than five, the retained figure is kept unchanged. For example: 2.541 becomes 2.5 to two significant figures.

2. When the digit next beyond the one to be retained is greater than five, the retained figure is increased by one. For example: 2.453 becomes 2.5 to two significant figures.

3. When the digit next beyond the one to be retained is exactly five, and the retained digit is even, it is left unchanged and conversely. Thus, 3.450 becomes 3.4 but 3.550 becomes 3.6 to two significant figures.

4. When two or more figures are to the right of the last figure to be retained, they are to be considered as a group in rounding decisions. Thus in 2.4(501), the group (501) is considered to be >5 while for 2.5(499), (499) is considered to be <5.

7.3 Guidelines for Reporting Results of Measurements

The number of significant figures to be used in reporting results is often asked. This will depend on the number of figures in the original data and the confidence limits to support the results. Analysts sometimes feel that observed data have more digits than are meaningful and are tempted to round them to what is felt to be significant. This should be resisted and rounding should be deferred as the last operation. The following guidelines are recommended when deciding what is significant.

The number of figures to retain in experimental data and even in preliminary calculations is unimportant, provided a certain minimum is exceeded. At least the last figure should vary between successive trials and variability of at least the last two figures is preferred. If this is not the case, the data are probably truncated by the operation (e.g., low attenuation), rounded off by the observer, or imprecisely read. Training of observers can often improve the precision of reading. Observers can have preconceived ideas of the attainable precision (or that required for some application) and will round off readings with this in mind. Thus they may be actually throwing away data.

The average of several values should be calculated with at least one more significant figure than that of the data. This will then be rounded for reporting, consistent with the confidence limits estimated.

The standard deviation (necessary for computing confidence intervals) should be computed to three significant figures and rounded to two when reported as data. The confidence interval should be calculated, then rounded to two significant figures (use more than this number in the calculations as available) and the result reported should be consistent with this. While any confidence level may be used, the 95 percent level is commonly used. However, the level used for the calculation must be reported.

As an example of the above, the following data were observed:

15.2, 14.7, 15.1, 15.0, 15.3, 15.2, 14.9

$$\bar{x} = 15.057$$

$$s = 0.207$$

Confidence interval calculation:

$$\frac{ts}{\sqrt{n}} = \frac{2.517 \times 0.207}{\sqrt{7}} = 0.1969$$

The result reported is $\bar{x} = 15.06 \pm 0.20$

where the uncertainty represents the 95 percent confidence interval for the mean of seven measurements.

8. NBS Services Related to SRM's

The NBS Office of Standard Reference Materials and the various scientists that are engaged in their development and certification believe that the use of SRM's in a systematic manner can provide a high level of confidence in analytical measurement data. To the extent possible, assistance will be provided related to their use. While detailed advice on specialized measurement problems cannot be provided, generic advice is available and may be all that is needed in many situations. A list of the kinds of services that can be provided and the telephone number to call to make initial contacts follows.

- SRM General

  o   General catalogues will be sent on request
  o   Special catalogues will be sent to those identifying special interests and updates will be sent as available
  o   Announcement of new SRM's are sent to those on the special interest lists
  o   Replacement of lost certificates will be made on request

- Assistance in Ordering/Customer Services

  o   Call 301 - 921-2045 for special assistance in ordering, quotations on current prices, and availability of specific SRM's.

- Technical Assistance

  o   Questions concerning applications, experimental results when measuring specific SRM's, stability selection of SRM's, details of certification and certified values, and other technical matters are directed to the appropriate project manager (see p. 57) or to Customer Services.

- SRM Workshops

  o   Quality Assurance of Chemical Measurements

      A 2-day seminar, offered semi-annually, ordinarily announced through the SRM mailing list. Call 301 - 921-3497 for current information.

  o   Special SRM Workshops

      Special workshops concerned with development of new SRM's or utilization of SRM's. Call Customer Services

- Calibration Services

      NBS provides a limited amount of calibration services in several areas of physical measurement. The services available and the current test fee may be obtained by inquiry to the NBS Office of Measurement Services, 301 - 921-2805.

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10. Information

Office of Standard Reference Materials
Room B311, Chemistry Bldg.
National Bureau of Standards
Washington, D.C. 20234
(Telephone 301-921-2045)

Chief

Stanley D. Rasberry

Deputy Chief

William P. Reed

Manager, Marketing and Customer Services

Leonara T. Klein

Manager, Production and Certification Programs

Thomas E. Gills

Project Managers

Robert L. Alvarez
Thomas E. Gills
Lee J. Kieffer
Raymond L. McKenzie
Lura J. Powell
William P. Reed
Richard W. Seward

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Absolute Method - A method in which characterization is based entirely on physically (absolute) defined standards.

Accreditiation - A formal process by which a labortory is evaluated, with respect to established criteria, for its competence to perform a specified kind(s) of measurement. Also, the decision based upon such a process. When a certificate is issued, the process is often called certification.

Accuracy - The degree of agreement of a measured value with the true or expected value of the quantity of concern.

Aliquant - A divisor that does not divide a sample into a number of equal parts without leaving a remainder; a sample resulting from such a divisor.

Aliquot - A divisor that divides a sample into a number of equal parts, leaving no remainder; a sample resulting from such a divisor.

Analyte - The specific component measured in a chemical analysis; also called analate.

Assignable cause - A cause believed to be responsible for an identifiable change of precision or accuracy of a measurement process.

Blank - The measured value obtained when a specified component of a sample is not present during the measurement. In such a case, the measured value/signal for the component is believed to be due to artifacts, hence should be deducted from a measured value to give a net value due to the component contained in a sample. The blank measurement must be made so that the correction process is valid.

Blind Sample - A sample submitted for analysis whose composition is known to the submitter but unknown to the analyst. A blind sample thus is one way to test proficiency of a measurement process.

Bias - A systematic error inherent in a method or caused by some artifact or idiosyncrasy of the measurement system. Temperature effects and extraction inefficiencies are examples of this first kind. Blanks, contamination, mechanical losses and calibration errors are examples of the latter kinds. Bias may be both positive and negative and several kinds can exist concurrently, so that net bias is all that can be evaluated, except under special conditions.

Bulk sampling - Sampling of a material that does not consist of discrete, identifiable, constant units, but rather of arbitrary, irregular units.

Calibrant - A substance used to calibrate or to establish the analytical response of a measurement system.

Calibration. - Comparison of a measurement standard or instrument with another standard or instrument to report or eliminate by adjustment any variation (deviation) in the accuracy of the item being compared.

Cause-Effect Diagram - A graphical representation of the causes that can produce a specified kind of error in measurement. A popular one is the so-called fish bone diagram, first described by Ishikawa, given this name because of its suggestive shape.

Central Line - The long-term expected value of a variable displayed on a control chart.

Certification - See accreditation.

Certified Reference Material (CRM) - A reference material one or more of whose property values are certified by a technically valid procedure, accompanied by or traceable to a certificate or other documentation which is issued by a certifying body.

Certified Value - The value that appears in a certificate as the best estimate of the value for a property of a reference material.

Chance Cause - A cause for variability of a measurement process that occurs unpredictably, for unknown reasons, and believed to happen by chance, alone.

Check Standard - In physical calibration, an artifact measured periodically, the results of which typically are plotted on a control chart to evaluate the measurement process.

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*For other definitions, and particularly those related to industrial quality assurance, see: "Quality Systems Terminology", ANSI/ASQC Standard A3-1978, American National Standards Institute, 1430 Broadway, New York, NY 10018.

Coefficient of Variation - The standard deviation divided by the value of the parameter measured.

Common Cause - A cause of variability of a measurement process, inherent in and common to the process itself, as contrasted to a special cause (defined).

Comparative Method - A method which is based on the intercomparison of the sample with a chemical standard.

Confidence Interval - That range of values, calculated from an estimate of the mean and the standard deviation, which is expected to include the population mean with a stated level of confidence. Confidence intervals in the same context also may be calculated for standard deviations, lines, slopes, points.

Control Limit - The limits shown on a control chart beyond which it is highly improbable that a point could lie while the system remains in a state of statistical control.

Control Chart - A graphical plot of test results with respect to time or sequence of measurement together with limits within which they are expected to lie when the system is in a state of statistical control.

Control Sample - A material of known composition that is analyzed concurrently with test samples to evaluate a measurement process (see also Check Standard).

Composite Sample - A sample composed of two or more increments selected to represent a population of interest.

Cross Sensitivity - A quantitative measure of the response obtained for an undesired constituent (interferrent) as compared to that for a constituent of interest.

Detection Limit - The smallest concentration/amount of some component of interest that can be measured by a single measurement with a stated level of confidence.

Double Blind - A sample, known by the submitter but submitted to an analyst in such a way that neither its composition nor its identification as a check sample are known to the latter.

Duplicate Measurement - A second measurement made on the same (or identical) sample of material to assist in the evaluation of measurement variance.

Duplicate Sample - A second sample randomly selected from a population of interest (see also split sample) to assist in the evaluation of sample variance.

Education - Disciplining the mind through instruction or study. Education is general and prepares the mind to react to a variety of situations.

Error - Difference betwen the true or expected value and the measured value of a quantity or parameter.

Figure of Merit - A performance characteristic of a method believed to be useful when deciding its applicability for a specific measurement situation. Typical figures of merit include: selectivity; sensitivity; detection limit; precision; bias.

Good Laboratory Practice (GLP) - An acceptable way to perform some basic operation or activity in a laboratory, that is known or believed to influence the quality of its outputs. GLP's ordinarily are essentially independent of the measurement techniques used.

Good Measurement Practice (GMP) - An acceptable way to perform some operation associated with a specific measurement technique, and which is known or believed to influence the quality of the measurement.

Gross Sample (also called bulk sample, lot sample) - One or more increments of material taken from a larger quantity (lot) of material for assay or record purposes.

Homogeneity - The degree to which a property or substance is randomly distributed throughout a material. Homogeneity depends on the size of the subsample under consideration. Thus a mixture of two minerals may be inhomogeneous at the molecular or atomic level, but homogeneous at the particulate level.

Incrememt - An individual portion of material collected by a single operation of a sampling device, from parts of a lot separated in time or space. Increments may be either tested individually or combined (composited) and tested as a unit.

Individuals - Conceivable constituent parts of a population.

Informational Value - Value of a property, not certified but provided because it is believed to be reliable and to provide information important to the certified material.

Intercalibration - The process, procedures, and activities used to ensure that the several laboratories engaged in a monitoring program can produce compatible data. When compatible data outputs are achieved and this situation is maintained, the laboratories can be said to be intercalibrated.

Laboratory Sample - A sample, intended for testing or analysis, prepared from a gross sample or otherwise obtained. The laboratory sample must retain the composition of the gross sample. Often reduction in particle size is necessary in the course of reducing the quantity.

Limiting Mean - The value approached by the average as the number of measurements, made by a stable measurement process, increases indefinitely.

Limit of Linearity (LOL) - The upper limit of concentration or amount of substance for which incremental additions produce constant increments of response.

Limit of Quantitation (LOQ) - The lower limit of concentration or amount of substance that must be present before a method is considered to provide quantitative results. By convention LOQ = $10s_o$, where s_o is the estimate of the standard deviation at the lowest level of measurement.

Lot - A quantity of bulk material of similar composition whose properties are under study.

Method - An assemblage of measurement techniques and the order in which they are used.

Outlier - A value which appears to deviate markedly from that for other members of the sample in which it occurs.

Pareto Analysis - A statistical approach to ranking assignable causes according to the frequency of occurrence.

Performance Audit - A process to evaluate the proficiency of an analyst/laboratory by evaluation of the results obtained on known test materials.

Population - A generic term denoting any finite or infinite collection of individual things, objects, or events; in the broadest concept, an aggregate determined by some property that distinguishes things that do and do not belong.

Precision - The degree of mutual agreement characteristic of independent measurements as the result of repeated application of the process under specified conditions. It is concerned with the closeness together of results.

Primary Standard - A substance or artifact, the value of which can be accepted (within specific limits) without question when used to establish the value of the same or related property of another material. Note that the primary standard for one user may have been a secondary standard of another.

Probability - The likelihood of the occurrence of any particular form of an event, estimated as the ratio of the number of ways or times that the event may occur in that form to the total number of ways that it could occur in any form.

Procedure - A set of systematic instructions for using a method of measurement or of sampling or of the steps or operations associated with such.

Protocol - A procedure specified to be used when performing a measurement or related operation, as a condition to obtain results that could be acceptable to the specifier.

Protocol for a Specific Purpose (PSP) - Detailed instructions for the performance of all aspects of a measurement program. This is sometimes called a project QA plan.

Quality - An estimation of acceptability or suitability for a given purpose of an object, item, tangible, or intangible thing.

Quality Assessment - The overall system of activities whose purpose is to provide assurance that the quality control activities are being done effectively. It involves a continuing evaluation of performance of the production system and the quality of the products produced.

Quality Assurance - A system of activities whose purpose is to provide to the producer or user of a product or a service the assurance that it meets defined standards of quality. It consists of two separate but related activities, quality control and quality assessment (defined).

Quality Circle - A small group of individuals with related interests that meets at regular intervals to consider problems or other matters related to the quality of outputs of a process and to the correction of problems or to the improvement of quality.

Quality Control - The overall system of activities whose purpose is to control the quality of a product or service so that it meets the needs of users. The aim is to provide quality that is satisfactory, adequate, dependable, and economic.

Random Sample - A sample selected from a population, using a randomization process.

Reduction - The process of preparing one or more subsamples from a sample.

Reference Material (RM) - A material or substance one or more properties of which are sufficiently well established to be used for the calibration of an apparatus, the assessment of a measurement method, or for the assignment of values to materials.

Reference Method - A method which has been specified as capable, by virtue of recognized accuracy, of providing primary reference data.

Relative Standard Deviation - The coefficient of variation, expressed as a percentage.

Replicate - A counterpart of another, usually referring to an analytical sample or a measurement. It is the general case for which duplicate is the special case consisting of two samples or measurements.

Routine Method - A method used in recurring analytical problems.

Sample - A portion of a population or lot. It may consist of an individual or groups of individuals. It may refer to objects, materials, or to measurements, conceivable as part of a larger group that could have been considered.

Secondary Standard - A standard whose value is based upon comparison with some primary standard. Note that a secondary standard, once its value is established, can become a primary standard for some other user.

Segment - A specifically demarked portion of a lot, either actual or hypothetical.

Selectivity - The ability of methodology or instrumentation to respond to a desired substance or constituent and not to others. It is sometimes quantified as cross sensitivity, which see.

Sensitivity - Capability of methodology or instrumentation to discriminate between samples having differing concentrations or containing differing amounts of an analate.

Significant Figure - A figure(s) that remains to a number or decimal after the ciphers to the right or left are cancelled.

Special Cause - A cause of variance or bias that is external (not inherent) to the measurement system.

Split Sample - A replicate portion or sub-sample of a total sample obtained in such a manner that it is not believed to differ significantly from other portions of the same sample.

Standard - A substance or material, the properties of which are believed to be known with sufficient accuracy to permit its use to evaluate the same property of another. In chemical measurements, it often describes a solution or substance, commonly prepared by the analyst, to establish a calibration curve or the analytical response function of an instrument.

Standard Addition - A method in which small increments of a substance under measurement are added to a sample under test to establish a response function or, by extrapolation, to detemine the amount of a constituent orginally present in the test sample.

Standardization - (In analytical chemistry) the assignment of a compositional value to one standard on the basis of another standard.

Standard Method - A method (or procedure) of test developed by a standards-writing organization, based on consensus opinion or other criteria, and often evaluated for its reliability by a collaborative testing procedure.

Standard Operations Procedure (SOP) - A procedure adopted for repetitive use when performing a specific measurement or sampling operation. It may be a standard method or one developed by the user.

Standard Reference Material - A reference material distributed and certified by the National Bureau of Standards.

Strata - Segments of a lot that may vary with respect to the property under study.

Subsample - A portion taken from a sample. A laboratory sample may be a subsample of a gross sample; similarly, a test portion may be a subsample of a laboratory sample.

Technique - A physical or chemical principle utilized separately or in combination with other techniques to determine the composition (analysis) of materials.

Test Portion (also called specimen, test specimen, test unit, aliquot) -   That quantity of a material of proper size for measurement of the property of interest. Test portions may be taken from the gross sample directly, but often preliminary operations, such as mixing or further reduction in particle size, are necessary.

Tolerance Interval - That range of values, calculated from an estimate of the mean and the standard derivation, within which a specified percentage of individual values of population (measurements or sample) are expected to lie with a stated level of confidence

Traceability - The ability to trace the source of uncertainty of a measurement or a measured value.

Training - Formal or informal instruction designed to provide competence of a specific nature.

Uncertainty - The range of values within which the true value is estimated to lie. It is a best estimate of possible inaccuracy due to both random and systematic error.

Validation - The process by which a sample, measurement method, or a piece of data is deemed to be useful for a specified purpose.

Variance - The value approached by the average of the sum of the squares of deviations of individual measurements from the limiting mean. Mathematically, it may be expressed as

$$\frac{\sum (x_i - m)^2}{n} \to \sigma^2 \text{ as } n \to \infty$$

Ordinarily it cannot be known but only its estimate, s^2, which is calculated by the expression

$$s^2 = \frac{\sum (x_i - \bar{x})^2}{n-1}$$

Warning Limits - The limits shown on a control chart within which most of the test results are expected to lie (within a 95% probability) while the system remains in a state of statistical control.

Youden Plot - A graphical presentation of data, recommended first by W. J. Youden, in which the result(s) obtained by a laboratory on one sample is plotted with respect to the result(s) it obtained on a similar sample. It helps in deciding whether discrepant results are due to random or systematic error.

APPENDIX B. CONVERSION FACTORS AND TABLES

B.1 Conversion Factors

In the metric system of weights and measures, designations of multiples and subdivisions of any unit may be arrived at by combining with the name of the unit, the prefixes deka, hecto, and kilo, meaning, respectively, 10, 100, and 1 000, and deci, centi, and milli, meaning, respectively, one-tenth, one-hundredth, and one-thousandth. In some of the following metric tables, some such multiples and subdivisions have not been included for the reason that these have little, if any actual usage.

In certain cases, particularly in scientific usage, it becomes convenient to provide for multiples larger than 1 000 and for subdivisions smaller than one-thousandth. Accordingly, the following prefixes have been introduced and these are new generally recognized:

exa, (E) meaning 10^{18}
peta, (P), meaning 10^{15}
tera, (T), meaning 10^{12}
giga, (G), meaning 10^{9}
mega, (m), meaning 10^{6}
kilo, (k), meaning 10^{3}
hecto, (h), meaning 10^{2}
deka, (da), meaning 10^{1}

deci, (d), meaning 10^{-1}
centi, (c), meanining 10^{-2}
milli, (m), meaning 10^{-3}
micro, (µ), meaning 10^{-6}
nano, (n), meaning 10^{-9}
pico, (p), meaning 10^{-12}
femto, (f), meaning 10^{-15}
atto, (a), meaning 10^{-18}

Thus a kilometer is 1 000 meters and a millimeter is 0.001 meter.

LINEAR MEASURE

10 millimeters (mm)	= 1 centimeter (cm)
10 centimeters	= 1 decimeter (dm) = 100 millimeters
10 decimeters	= 1 meter (m) =1 000 millimeters
10 meters	= 1 dekameter (dam)
10 dekameters	= 1 hectometer (hm) = 100 meters
10 hectometers	= 1 kilometer (km) = 1 000 meters

AREA MEASURE

100 square millimeters (mm^2)	= 1 square centimeter (cm^2)
100 square centimeters	= 1 square decimeter (dm^2)
100 square decimeters	= 1 square meter (m^2)
100 square meters	= 1 square dekameter (dam^2) = 1 are
100 square dekameters	= 1 square hectometer (hm^2) = 1 hectare (ha)
100 square hectometers	= 1 square kilometers (km^2)

FLUID VOLUME MEASURE

10 milliliters (mL)	= 1 centiliter (cL)
10 centiliters	= 1 deciliter (dL) = 100 milliliters
10 deciliters	= 1 liter = 1 000 milliliters
10 liters	= 1 dekaliter (daL)
10 dekaliters	= 1 hectoliter (hL) = 100 liters
10 hectoliters	= 1 kiloliter (kL) = 1 000 liters

SOLID VOLUME MEASURE

1 000 cubic millimeters (mm^3)	= 1 cubic centimeter (cm^3)
1 000 cubic centimeters	= 1 cubic decimeter (dm^3)
	= 1 000 000 cubic millimeters
1 000 cubic decimeters	= 1 cubic meter (m^3)
	= 1 000 000 cubic centimeters
	= 1 000 000 000 cubic millimeters

WEIGHT

10 milligrams (mg)	= 1 centigram (cg)
10 centigrams	= 1 decigram (dg) = 100 milligrams
10 decigrams	= 1 gram (g) = 1 000 milligrams
10 grams	= 1 dekagram (dag)
10 dekagrams	= 1 hectogram (hg) = 100 grams
10 hectograms	= 1 kilogram (kg) = 1 000 grams
1 000 kilograms	= 1 megagram (Mg) or 1 metric ton (t)

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Table B.2. Use of Range to Estimate Variability

Number of Sets, k		Number of Measurements in a Set				
		2	3	4	5	6
3	d_2^*	1.23	1.77	2.12	2.38	2.58
	ν	2.83	5.86	8.44	11.1	13.6
5	d_2^*	1.19	1.74	2.10	2.36	2.56
	ν	4.59	9.31	13.9	18.4	22.6
10	d_2^*	1.16	1.72	2.08	2.34	2.55
	ν	8.99	18.4	27.6	36.5	44.9
20	d_2^*	1.14	1.70	2.07	2.35	2.54
	ν	17.8	36.5	55.0	72.7	89.6
∞	d_2^*	1.13	1.69	2.06	2.33	2.53

$$s = \frac{\overline{R}}{d_2^*}$$

$\overline{R}$ = mean of k sets of replicate measurements

ν = degrees of freedom in estimate of standard deivation

For k > 20, $\nu \approx 0.876$ k

Adapted from Lloyd S. Nelson, J. Qual. Tech. 7(1) January (1975).

Table B.3 Critical Values for the F Test

Critical values for a 2-tailed test of equality of standard deviation estimates at 5% level of significance

$$F_{.975}\,(n_1, n_2)$$

n_1 = degrees of freedom for numerator

n_2 = degrees of freedom for denominator

n_2 \ n_1	1	2	3	4	5	6	7	8	9	10	12	15	20	24	30	40	60	120	∞
1	647.8	799.5	864.2	899.6	921.8	937.1	948.2	956.7	963.3	968.6	976.7	984.9	993.1	997.2	1001	1006	1010	1014	1018
2	38.51	39.00	39.17	39.25	39.30	39.33	39.36	39.37	39.39	39.40	39.41	39.43	39.45	39.46	39.46	39.47	39.48	39.49	39.50
3	17.44	16.04	15.44	15.10	14.88	14.73	14.62	14.54	14.47	14.42	14.34	14.25	14.17	14.12	14.08	14.04	13.99	13.95	13.90
4	12.22	10.65	9.98	9.60	9.36	9.20	9.07	8.98	8.90	8.84	8.75	8.66	8.56	8.51	8.46	8.41	8.36	8.31	8.26
5	10.01	8.43	7.76	7.39	7.15	6.98	6.85	6.76	6.68	6.62	6.52	6.43	6.33	6.28	6.23	6.18	6.12	6.07	6.02
6	8.81	7.26	6.60	6.23	5.99	5.82	5.70	5.60	5.52	5.46	5.37	5.27	5.17	5.12	5.07	5.01	4.96	4.90	4.85
7	8.07	6.54	5.89	5.52	5.29	5.12	4.99	4.90	4.82	4.76	4.67	4.57	4.47	4.42	4.36	4.31	4.25	4.20	4.14
8	7.57	6.06	5.42	5.05	4.82	4.65	4.53	4.43	4.36	4.30	4.20	4.10	4.00	3.95	3.89	3.84	3.78	3.73	3.67
9	7.21	5.71	5.08	4.72	4.48	4.32	4.20	4.10	4.03	3.96	3.87	3.77	3.67	3.61	3.56	3.51	3.45	3.39	3.33
10	6.94	5.46	4.83	4.47	4.24	4.07	3.95	3.85	3.78	3.72	3.62	3.52	3.42	3.37	3.31	3.26	3.20	3.14	3.08
11	6.72	5.26	4.63	4.28	4.04	3.88	3.76	3.66	3.59	3.53	3.43	3.33	3.23	3.17	3.12	3.06	3.00	2.94	2.88
12	6.55	5.10	4.47	4.12	3.89	3.73	3.61	3.51	3.44	3.37	3.28	3.18	3.07	3.02	2.96	2.91	2.85	2.79	2.72
13	6.41	4.97	4.35	4.00	3.77	3.60	3.48	3.39	3.31	3.25	3.15	3.05	2.95	2.89	2.84	2.78	2.72	2.66	2.60
14	6.30	4.86	4.24	3.89	3.66	3.50	3.38	3.29	3.21	3.15	3.05	2.95	2.84	2.79	2.73	2.67	2.61	2.55	2.49
15	6.20	4.77	4.15	3.80	3.58	3.41	3.29	3.20	3.12	3.06	2.96	2.86	2.76	2.70	2.64	2.59	2.52	2.46	2.40
16	6.12	4.69	4.08	3.73	3.50	3.34	3.22	3.12	3.05	2.99	2.89	2.79	2.68	2.63	2.57	2.51	2.45	2.38	2.32
17	6.04	4.62	4.01	3.66	3.44	3.28	3.16	3.06	2.98	2.92	2.82	2.72	2.62	2.56	2.50	2.44	2.38	2.32	2.25
18	5.98	4.56	3.95	3.61	3.38	3.22	3.10	3.01	2.93	2.87	2.77	2.67	2.56	2.50	2.44	2.38	2.32	2.26	2.19
19	5.92	4.51	3.90	3.56	3.33	3.17	3.05	2.96	2.88	2.82	2.72	2.62	2.51	2.45	2.39	2.33	2.27	2.20	2.13
20	5.87	4.46	3.86	3.51	3.29	3.13	3.01	2.91	2.84	2.77	2.68	2.57	2.46	2.41	2.35	2.29	2.22	2.16	2.09
21	5.83	4.42	3.82	3.48	3.25	3.09	2.97	2.87	2.80	2.73	2.64	2.53	2.42	2.37	2.31	2.25	2.18	2.11	2.04
22	5.79	4.38	3.78	3.44	3.22	3.05	2.93	2.84	2.76	2.70	2.60	2.50	2.39	2.33	2.27	2.21	2.14	2.08	2.00
23	5.75	4.35	3.75	3.41	3.18	3.02	2.90	2.81	2.73	2.67	2.57	2.47	2.36	2.30	2.24	2.18	2.11	2.04	1.97
24	5.72	4.32	3.72	3.38	3.15	2.99	2.87	2.78	2.70	2.64	2.54	2.44	2.33	2.27	2.21	2.15	2.08	2.01	1.94
25	5.69	4.29	3.69	3.35	3.13	2.97	2.85	2.75	2.68	2.61	2.51	2.41	2.30	2.24	2.18	2.12	2.05	1.98	1.91
26	5.66	4.27	3.67	3.33	3.10	2.94	2.82	2.73	2.65	2.59	2.49	2.39	2.28	2.22	2.16	2.09	2.03	1.95	1.88
27	5.63	4.24	3.65	3.31	3.08	2.92	2.80	2.71	2.63	2.57	2.47	2.36	2.25	2.19	2.13	2.07	2.00	1.93	1.85
28	5.61	4.22	3.63	3.29	3.06	2.90	2.78	2.69	2.61	2.55	2.45	2.34	2.23	2.17	2.11	2.05	1.98	1.91	1.83
29	5.59	4.20	3.61	3.27	3.04	2.88	2.76	2.67	2.59	2.53	2.43	2.32	2.21	2.15	2.09	2.03	1.96	1.89	1.81
30	5.57	4.18	3.59	3.25	3.03	2.87	2.75	2.65	2.57	2.51	2.41	2.31	2.20	2.14	2.07	2.01	1.94	1.87	1.79
40	5.42	4.05	3.46	3.13	2.90	2.74	2.62	2.53	2.45	2.39	2.29	2.18	2.07	2.01	1.94	1.88	1.80	1.72	1.64
60	5.29	3.93	3.34	3.01	2.79	2.63	2.51	2.41	2.33	2.27	2.17	2.06	1.94	1.88	1.82	1.74	1.67	1.58	1.48
120	5.15	3.80	3.23	2.89	2.67	2.52	2.39	2.30	2.22	2.16	2.05	1.94	1.82	1.76	1.69	1.61	1.53	1.43	1.31
∞	5.02	3.69	3.12	2.79	2.57	2.41	2.29	2.19	2.11	2.05	1.94	1.83	1.71	1.64	1.57	1.48	1.39	1.27	1.00

Excerpted from "Experimental Statistics" (19) Table A.5 which may be consulted for more extensive listings.

Table B.4   Factors for Computing Two-Sided Confidence Limits for σ

Degrees of Freedom ν	$\alpha = .05$		$\alpha = .01$		$\alpha = .001$	
	B_U	B_L	B_U	B_L	B_U	B_L
1	17.79	.3576	86.31	.2969	844.4	.2480
2	4.859	.4581	10.70	.3879	33.29	.3291
3	3.183	.5178	5.449	.4453	11.65	.3824
4	2.567	.5590	3.892	.4865	6.938	.4218
5	2.248	.5899	3.175	.5182	5.085	.4529
6	2.052	.6143	2.764	.5437	4.128	.4784
7	1.918	.6344	2.498	.5650	3.551	.5000
8	1.820	.6513	2.311	.5830	3.167	.5186
9	1.746	.6657	2.173	.5987	2.894	.5348
10	1.686	.6784	2.065	.6125	2.689	.5492
11	1.638	.6896	1.980	.6248	2.530	.5621
12	1.598	.6995	1.909	.6358	2.402	.5738
13	1.564	.7084	1.851	.6458	2.298	.5845
14	1.534	.7166	1.801	.6549	2.210	.5942
15	1.509	.7240	1.758	.6632	2.136	.6032
16	1.486	.7308	1.721	.6710	2.073	.6116
17	1.466	.7372	1.688	.6781	2.017	.6193
18	1.448	.7430	1.658	.6848	1.968	.6266
19	1.432	.7484	1.632	.6909	1.925	.6333
20	1.417	.7535	1.609	.6968	1.886	.6397
21	1.404	.7582	1.587	.7022	1.851	.6457
22	1.391	.7627	1.568	.7074	1.820	.6514
23	1.380	.7669	1.550	.7122	1.791	.6568
24	1.370	.7709	1.533	.7169	1.765	.6619
25	1.360	.7747	1.518	.7212	1.741	.6668
26	1.351	.7783	1.504	.7253	1.719	.6713
27	1.343	.7817	1.491	.7293	1.698	.6758
28	1.335	.7849	1.479	.7331	1.679	.6800
29	1.327	.7880	1.467	.7367	1.661	.6841
30	1.321	.7909	1.457	.7401	1.645	.6880
31	1.314	.7937	1.447	.7434	1.629	.6917
32	1.308	.7964	1.437	.7467	1.615	.6953
33	1.302	.7990	1.428	.7497	1.601	.6987
34	1.296	.8015	1.420	.7526	1.588	.7020
35	1.291	.8039	1.412	.7554	1.576	.7052
36	1.286	.8062	1.404	.7582	1.564	.7083
37	1.281	.8085	1.397	.7608	1.553	.7113
38	1.277	.8106	1.390	.7633	1.543	.7141
39	1.272	.8126	1.383	.7658	1.533	.7169
40	1.268	.8146	1.377	.7681	1.523	.7197
41	1.264	.8166	1.371	.7705	1.515	.7223
42	1.260	.8184	1.365	.7727	1.506	.7248
43	1.257	.8202	1.360	.7748	1.498	.7273
44	1.253	.8220	1.355	.7769	1.490	.7297
45	1.249	.8237	1.349	.7789	1.482	.7320
46	1.246	.8253	1.345	.7809	1.475	.7342
47	1.243	.8269	1.340	.7828	1.468	.7364
48	1.240	.8285	1.335	.7847	1.462	.7386
49	1.237	.8600	1.331	.7864	1.455	.7407
50	1.234	.8314	1.327	.7882	1.449	.7427

Excerpted from "Experimental Statistics" (19) Table A.20 which may be consulted for more extensive listings.

Table B.5 Percentiles of the t Distribution

Confidence level of 2-sided interval	20	40	60	80	90	95	98	99
df	$t_{.60}$	$t_{.70}$	$t_{.80}$	$t_{.90}$	$t_{.95}$	$t_{.975}$	$t_{.99}$	$t_{.995}$
1	.325	.727	1.376	3.078	6.314	12.706	31.821	63.657
2	.289	.617	1.061	1.886	2.920	4.303	6.965	9.925
3	.277	.584	.978	1.638	2.353	3.182	4.541	5.841
4	.271	.569	.941	1.533	2.132	2.776	3.747	4.604
5	.267	.559	.920	1.476	2.015	2.571	3.365	4.032
6	.265	.553	.906	1.440	1.943	2.447	3.143	3.707
7	.263	.549	.896	1.415	1.895	2.365	2.998	3.499
8	.262	.546	.889	1.397	1.860	2.306	2.896	3.355
9	.261	.543	.883	1.383	1.833	2.262	2.821	3.250
10	.260	.542	.879	1.372	1.812	2.228	2.764	3.169
11	.260	.540	.876	1.363	1.796	2.201	2.718	3.106
12	.259	.539	.873	1.356	1.782	2.179	2.681	3.055
13	.259	.538	.870	1.350	1.771	2.160	2.650	3.012
14	.258	.537	.868	1.345	1.761	2.145	2.624	2.977
15	.258	.536	.866	1.341	1.753	2.131	2.602	2.947
16	.258	.535	.865	1.337	1.746	2.120	2.583	2.921
17	.257	.534	.863	1.333	1.740	2.110	2.567	2.898
18	.257	.534	.862	1.330	1.734	2.101	2.552	2.878
19	.257	.533	.861	1.328	1.729	2.093	2.539	2.861
20	.257	.533	.860	1.325	1.725	2.086	2.528	2.845
21	.257	.532	.859	1.323	1.721	2.080	2.518	2.831
22	.256	.532	.858	1.321	1.717	2.074	2.508	2.819
23	.256	.532	.858	1.319	1.714	2.069	2.500	2.807
24	.256	.531	.857	1.318	1.711	2.064	2.492	2.797
25	.256	.531	.856	1.316	1.708	2.060	2.485	2.787
26	.256	.531	.856	1.315	1.706	2.056	2.479	2.779
27	.256	.531	.855	1.314	1.703	2.052	2.473	2.771
28	.256	.530	.855	1.313	1.701	2.048	2.467	2.763
29	.256	.530	.854	1.311	1.699	2.045	2.462	2.756
30	.256	.530	.854	1.310	1.697	2.042	2.457	2.750
40	.255	.529	.851	1.303	1.684	2.021	2.423	2.704
60	.254	.527	.848	1.296	1.671	2.000	2.390	2.660
120	.254	.526	.845	1.289	1.658	1.980	2.358	2.617
∞	.253	.524	.842	1.282	1.645	1.960	2.326	2.576

Excerpted from "Experimental Statistics" (19) Table A-4, which may be consulted for more extensive listings.

p n	γ = 0.95					γ = 0.99				
	0.75	0.90	0.95	0.99	0.999	0.75	0.90	0.95	0.99	0.999
2	22.858	32.019	37.674	48.430	60.573	114.363	160.193	188.491	242.300	303.054
3	5.922	8.380	9.916	12.861	16.208	13.378	18.930	22.401	29.055	36.616
4	3.779	5.369	6.370	8.299	10.502	6.614	9.398	11.150	14.527	18.383
5	3.002	4.275	5.079	6.634	8.415	4.643	6.612	7.855	10.260	13.015
6	2.604	3.712	4.414	5.775	7.337	3.743	5.337	6.345	8.301	10.548
7	2.361	3.369	4.007	5.248	6.676	3.233	4.613	5.488	7.187	9.142
8	2.197	3.136	3.732	4.891	6.226	2.905	4.147	4.936	6.468	8.234
9	2.078	2.967	3.532	4.631	5.899	2.677	3.822	4.550	5.966	7.600
10	1.987	2.839	3.379	4.433	5.649	2.508	3.582	4.265	5.594	7.129
11	1.916	2.737	3.259	4.277	5.452	2.378	3.397	4.045	5.308	6.766
12	1.858	2.655	3.162	4.150	5.291	2.274	3.250	3.870	5.079	6.477
13	1.810	2.587	3.081	4.044	5.158	2.190	3.130	3.727	4.893	6.240
14	1.770	2.529	3.012	3.955	5.045	2.120	3.029	3.608	4.737	6.043
15	1.735	2.480	2.954	3.878	4.949	2.060	2.945	3.507	4.605	5.876
16	1.705	2.437	2.903	3.812	4.865	2.009	2.872	3.421	4.492	5.732
17	1.679	2.400	2.858	3.754	4.791	1.965	2.808	3.345	4.393	5.607
18	1.655	2.366	2.819	3.702	4.725	1.926	2.753	3.279	4.307	5.497
19	1.635	2.337	2.784	3.656	4.667	1.891	2.703	3.221	4.230	5.399
20	1.616	2.310	2.752	3.615	4.614	1.860	2.659	3.168	4.161	5.312
21	1.599	2.286	2.723	3.577	4.567	1.833	2.620	3.121	4.100	5.234
22	1.584	2.264	2.697	3.543	4.523	1.808	2.584	3.078	4.044	5.163
23	1.570	2.244	2.673	3.512	4.484	1.785	2.551	3.040	3.993	5.098
24	1.557	2.225	2.651	3.483	4.447	1.764	2.522	3.004	3.947	5.039
25	1.545	2.208	2.631	3.457	4.413	1.745	2.494	2.972	3.904	4.985
26	1.534	2.193	2.612	3.432	4.382	1.727	2.469	2.941	3.865	4.935
27	1.523	2.178	2.595	3.409	4.353	1.711	2.446	2.914	3.828	4.888

p = proportion of population covered

γ = confidence level

n = number of individuals (measurements, samples) used to compute $\bar{x}$ and s

Excerpted from "Experimental Statistics" (19) Table A.6 which may be consulted for more extensive listings.

```
46 96 85 77 27 92 86 26 45 21 89 91 71 42 64 64 58 22 75 81 74 91 48 46 18
44 19 15 32 63 55 87 77 33 29 45 00 31 34 84 05 72 90 44 27 78 22 07 62 17
34 39 80 62 24 33 81 67 28 11 34 79 26 35 34 23 09 94 00 80 55 31 63 27 91
74 97 80 30 65 07 71 30 01 84 47 45 89 70 74 13 04 90 51 27 61 34 63 87 44
22 14 61 60 86 38 33 71 13 33 72 08 16 13 50 56 48 51 29 48 30 93 45 66 29

40 03 96 40 03 47 24 60 09 21 21 18 00 05 86 52 85 40 73 73 57 68 36 33 91
52 33 76 44 56 15 47 75 78 73 78 19 87 06 98 47 48 02 62 03 42 05 32 55 02
37 59 20 40 93 17 82 24 19 90 80 87 32 74 59 84 24 49 79 17 23 75 83 42 00
11 02 55 57 48 84 74 36 22 67 19 20 15 92 53 37 13 75 54 89 56 73 23 39 07
10 33 79 26 34 54 71 33 89 74 68 48 23 17 49 18 81 05 52 85 70 05 73 11 17

67 59 28 25 47 89 11 65 65 20 42 23 96 41 64 20 30 89 87 64 37 93 36 96 35
93 50 75 20 09 18 54 34 68 02 54 87 23 05 43 36 98 29 97 98 87 08 30 92 98
24 43 23 72 80 64 34 27 23 46 15 36 10 63 21 59 69 76 02 62 31 62 47 60 34
39 91 63 18 38 27 10 78 88 84 42 32 00 97 92 00 04 94 50 05 75 82 70 80 35
74 62 19 67 54 18 28 92 33 69 98 96 74 35 72 11 68 25 08 95 31 79 11 79 54

91 03 35 60 81 16 61 97 25 14 78 21 22 05 25 47 26 37 80 39 19 06 41 02 00
42 57 66 76 72 91 03 63 48 46 44 01 33 53 62 28 80 59 55 05 02 16 13 17 54
06 36 63 06 15 03 72 38 01 58 25 37 66 48 56 19 56 41 29 28 76 49 74 39 50
92 70 96 70 89 80 87 14 25 49 25 94 62 78 26 15 41 39 48 75 64 69 61 06 38
91 08 88 53 52 13 04 82 23 00 26 36 47 44 04 08 84 80 07 44 76 51 52 41 59

68 85 97 74 47 53 90 05 90 84 87 48 25 01 11 05 45 11 43 15 60 40 31 84 59
59 54 13 09 13 80 42 29 63 03 24 64 12 43 28 10 01 65 62 07 79 83 05 59 61
39 18 32 69 33 46 58 19 34 03 59 28 97 31 02 65 47 47 70 39 74 17 30 22 65
67 43 31 09 12 60 19 57 63 78 11 80 10 97 15 70 04 89 81 78 54 84 87 83 42
61 75 37 19 56 90 75 39 03 56 49 92 72 95 27 52 87 47 12 52 54 62 43 23 13

78 10 91 11 00 63 19 63 74 58 69 03 51 38 60 36 53 56 77 06 89 03 89 91 24
93 23 71 58 09 78 08 03 07 71 79 32 25 19 61 04 40 33 12 06 78 91 97 88 95
37 55 48 82 63 89 92 59 14 72 19 17 22 51 90 20 03 64 96 60 48 01 95 44 84
62 13 11 71 17 23 29 25 13 85 33 35 07 69 25 68 57 92 57 11 84 44 01 33 66
29 89 97 47 03 13 20 86 22 45 59 98 64 53 89 64 94 81 55 87 73 81 58 46 42

16 94 85 82 89 07 17 30 29 89 89 80 98 36 25 36 53 02 49 14 34 03 52 09 20
04 93 10 59 75 12 98 84 60 93 68 16 87 60 11 50 46 56 58 45 88 72 50 46 11
95 71 43 68 97 18 85 17 13 08 00 50 77 50 46 92 45 26 97 21 48 22 23 08 32
86 05 39 14 35 48 68 18 36 57 09 62 40 28 87 08 74 79 91 08 27 12 43 32 03
59 30 60 10 41 31 00 69 63 77 01 89 94 60 19 02 70 88 72 33 38 88 20 60 86

05 45 35 40 54 03 98 96 76 27 77 84 80 08 64 60 44 34 54 24 85 20 85 77 32
71 85 17 74 66 27 85 19 55 56 51 36 48 92 32 44 40 47 10 38 22 52 42 29 96
80 20 32 80 98 00 40 92 57 51 52 83 14 55 31 99 73 23 40 07 64 54 44 99 21
13 50 78 02 73 39 66 82 01 28 67 51 75 66 33 97 47 58 42 44 88 09 28 58 06
67 92 65 41 45 36 77 96 46 21 14 39 56 36 70 15 74 43 62 69 82 30 77 28 77

72 56 73 44 26 04 62 81 15 35 79 26 99 51 28 22 25 94 80 62 95 46 99 23 86
28 86 85 64 94 11 58 78 45 36 34 45 91 38 51 10 68 36 87 81 16 77 30 19 36
69 57 40 80 44 94 60 82 94 93 98 01 48 50 57 69 60 77 69 60 74 22 05 77 17
71 20 03 30 79 25 74 17 78 34 54 45 04 77 42 59 75 78 64 99 37 03 18 03 36
89 98 55 98 22 45 12 49 82 71 57 33 28 69 50 59 15 09 25 79 39 42 84 18 70

58 74 82 81 14 02 01 05 77 94 65 57 70 39 42 48 56 84 31 59 18 70 41 74 60
50 54 73 81 91 07 81 26 25 45 49 61 22 88 41 20 00 15 59 93 51 60 65 65 63
49 33 72 90 10 20 65 28 44 63 95 86 75 78 69 24 41 65 86 10 34 10 32 00 93
11 85 01 43 65 02 85 69 56 88 34 29 64 35 48 15 70 11 77 83 01 34 82 91 04
34 22 46 41 84 74 27 02 57 77 47 93 72 02 95 63 75 74 69 69 61 34 31 92 13
```

Table B.8   Z-Factors for Two-Sided Confidence Interval

Confidence Level	Z Factor
50%	0.67
67	1.00
75	1.15
90	1.645
95	1.960
95.45	2.000
99.00	2.575
99.74	3
99.9934	4
99.99995	5
$100 - 10^{-9}$	6
$100 - 10^{-12}$	7
$100 - 10^{-15}$	8
$100 - 10^{-18.9}$	9
$100 - 10^{-23}$	10

C.1 Introduction

The following pages contain a brief description, with examples, of statistical calculations related to some of the questions that arise when evaluating chemical measurement data. The reader is referred to the many excellent books that are available which discuss these matters in more detail and the basis for the relationships used. General information on precision measurement is contained in reference [16], and NBS Handbook 91 [19] is especially recommended for a detailed discussion of statistical concepts. It contains many numerical examples as well as extensive tables, from which most of the ones included in Appendix B were taken.

The results of repetitive measurements are usually considered to be normally distributed and representable by a bell-shaped curve. If a series of n measurements were made many times, one would obtain data sets represented by distributions such as those in Figure C.1. The means of each set will differ from each other. If the sample standard deviation, s, is calculated for each set of such measurements, a different result would be expected each time. Figure C.2 shows the two-sided (assymetric) confidence limits for σ based on such estimates, for several probability levels.
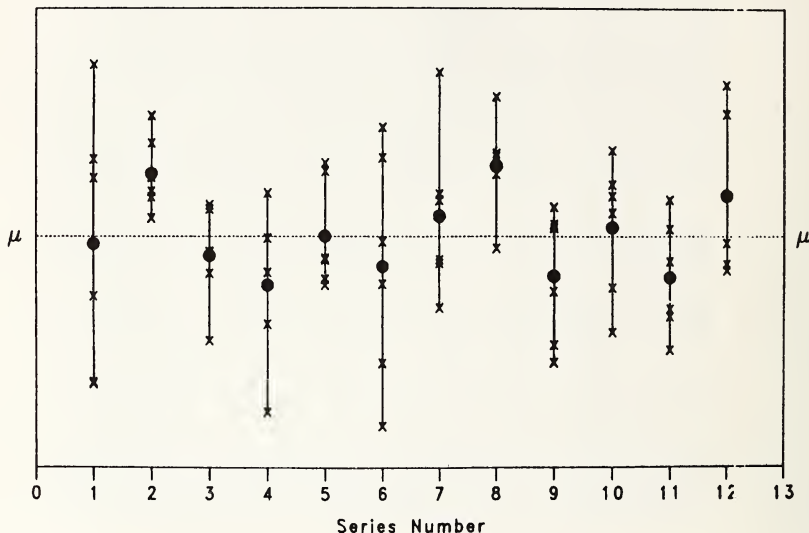

Figure C.1 Expected distribution of the means of random samples/measurements. The individual measurements are indicated by x and the means, $\overline{x}$, by dots

When several series of measurements are made, both the means and the standard deviations will vary from measurement to measurement, as illustrated in Figure C.3. As n increases from 4 to 1000, the variation of the means decreases but never disappears.

On considering the above, it should be obvious that even the best of measurements will differ amongst themselves, whether made by the same or different laboratories or scientists. One often needs to answer questions such as the confidence that can be placed in measurement data and the significance of apparent differences resulting from measurements. The various equations given in this appendix take into account both the expected variability within populations and the uncertainties in the estimates of the population parameters that must be considered when answering such questions.

C.2 Estimation of Standard Deviation

The basic parameters which characterize a population (universe) of samples or measurements on a given sample are the mean, μ, and the standard deviation, σ. Unless the entire population is examined, μ and σ cannot be known but are estimated from sample(s) randomly selected (assumed) from it. The result is a sample mean, $\bar{x}$, and an estimate of the standard deviation,
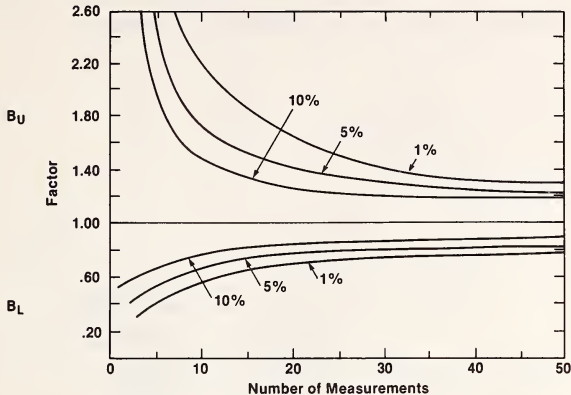

Figure C.2   Confidence Interval for σ

This figure illustrates the expected variability of estimates of standard deviations made on various occasions, as a function of the number of measurements involved. The factor, when multiplied by the estimate of the standard deviation gives the interval that is expected to include the population standard deviation for a given percentage of occasions. The labels, e.g., 10%, indicate the percentage of time that such an interval would not be expected to include σ. See section C.4 for a discussion and Table B.4 for the factors to be used in such calculations.
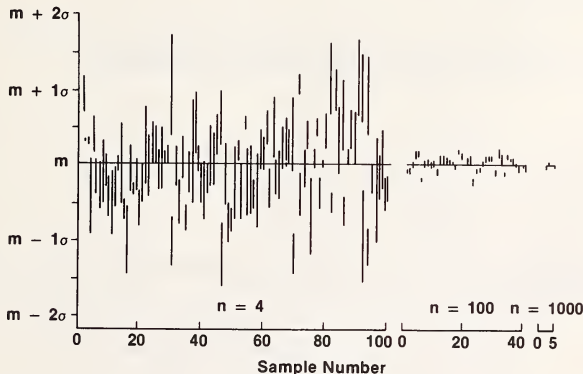

Figure C.3   Computed 50% confidence intervals for the population mean, m, from 100 samples of 4, 40 samples of 100, and 4 samples of 1000 [19].

The vertical lines essentially are error bars. The sample means, located at the center of each, are not indicated. The sample means and standard deviations (proportional to the error bars) vary with each set of measurements. The error bars decrease inversely as the square root of the sample size is increased and the means show correspondingly smaller deviations from the population mean.

s, which must be used if such things as confidence intervals, population characteristics, tolerance intervals, comparison of precision, and the significance of apparent discrepancies in measured values are to be evaluated.

Several ways by which the standard deviation may be estimated are given in the following sections.

C.2.1 Estimation of Standard Deviation from Replicate Measurements

For a series of n measurements

$$x_1, x_2, x_3 \cdot \cdot \cdot \cdot \cdot \cdot x_n$$

$$\overline{x} = \frac{x_1 + x_2 + x_3 + \ldots + x_n}{n}$$

$$s = \sqrt{\frac{\Sigma (x_i - \overline{x})^2}{n-1}}$$

s is estimated with $\nu = n-1$ degrees of freedom.

Example: C.2.1 - Series of Measurements

x	$(x_i - \overline{x})$	$(x_i - \overline{x})^2$
15.2	.143	.0204
14.7	-.357	.1257
15.1	.043	.0018
15.0	-.057	.0033
15.3	.243	.0590
15.2	.143	.0204
14.9	-.157	.0247

$$\overline{x} = 15.057 \qquad \Sigma = .2572$$

n = 7

$$s = \sqrt{\frac{.2572}{6}} = 0.207$$

C.2.2 Estimation of Standard Deviation from Duplicate Measurements

$$s = \sqrt{\frac{\Sigma d^2}{2k}}$$

where   k = number of sets of duplicate measurements

d = difference of a duplicate measurement

ν = k degrees of freedom

Note: It is not necessary that the duplicate measurements be made on the same materials. It is only necessary that the materials measured are expected to have the same standard deviation of measurement.

Example A: C.2.2 - Duplicates, Same Material

x_f	x_s	$|d|$	d^2
14.7	15.0	0.3	0.09
15.1	14.9	0.2	0.04
15.0	15.1	0.1	0.01
14.9	14.9	0.0	0.0
15.3	14.8	0.5	0.25
14.9	15.1	0.2	0.04
14.9	15.0	0.1	0.01
Σ			0.44

$$s = \sqrt{\frac{0.44}{14}} = 0.18$$

ν = 7 degrees of freedom

Example B: C.2.2 - Estimation from Duplicates, Different Materials

x_f	x_s	$|d|$	d^2
14.7	15.0	0.3	0.09
20.1	19.8	0.3	0.09
12.5	13.0	0.5	0.25
23.6	23.3	0.3	0.09
15.1	14.9	0.2	0.04
18.2	18.0	0.2	0.04
20.7	20.9	0.2	0.04
Σ			0.64

$$s = \sqrt{\frac{0.64}{14}} = 0.21$$

ν = 7 degrees of freedom

C.2.3 Estimation of Standard Deviation from the Range

The range, R, of a series of measurements is defined as the difference of the highest and lowest value obtained. The average range, $\overline{R}$, based on several sets (k) of measurements is calculated.

$$\overline{R} = \frac{R_1 + R_2 + R_3 + \ldots + R_k}{k}$$

$$s = \overline{R}/d_2^*$$

The value for d_2^* is obtained from Table B.2 and will depend on the number of sets, k, used to calculate $\overline{R}$ and the number of measurements in a set. The table shows also the number of degrees of freedom for the estimate of the standard deviation. The materials used to estimate $\overline{R}$ may be different, with the same restrictions as noted in C.2.2.

Example C.2.3 - From the Range of Duplicate Measurements

First Result	Second Result	Range, R
14.5	14.2	0.3
14.8	14.9	0.1
14.05	14.3	0.25
14.2	14.8	0.6
14.9	14.9	0.0
14.3	14.4	0.1
14.7	14.1	0.6
14.4	14.7	0.3
14.1	14.25	0.15
14.95	14.65	0.3
14.25	14.95	0.7

$$\overline{R} = \frac{0.3 + 0.1 + 0.25 + 0.6 + 0 + 0.1 + 0.6 + 0.3 + 0.15 + 0.3 + 0.7}{11}$$

$\overline{R}$ = 0.309

$s = \overline{R}/d_2^*$

d_2^* = 1.16 for 11 estimates of R (see Table B.2 by interpolation)

s = 0.27

ν = 10 degrees of freedom for s (from Table B.2, rounded)

C.2.4 Pooling Estimates of Standard Deviations

Several estimates of the standard deviation may be pooled to obtain a better estimate. Given several estimates of the standard deviation obtained on several occasions, with the corresponding measurements:

$$
\begin{array}{llll}
s_1 & n_1 & \nu_1 & = n_1 - 1 \\
s_2 & n_2 & \nu_2 & = n_2 - 1 \\
s_3 & n_3 & \nu_3 & = n_3 - 1 \\
\cdot & \cdot & \cdot & \cdot \\
\cdot & \cdot & \cdot & \cdot \\
s_k & n_k & \nu_k & = n_k - 1
\end{array}
$$

$$
s_{pooled} = \sqrt{\frac{\nu_1 s_1^2 + \nu_2 s_2^2 + \cdots + \nu_k s_k^2}{\nu_1 + \nu_2 + \cdots + \nu_k}}
$$

s_{pooled} will be based on $(\nu_1 + \nu_2 + \cdots + \nu_k)$ degrees of freedom

Note: Ordinarily, $\nu = n-1$

Example C.2.4 - Pooling Standard Deviations

The standard deviation of a measurement process was estimated on five occasions. These are to be pooled to improve the estimate of σ.

Trial	s	n	ν
1	0.171	7	6
2	0.205	5	4
3	0.185	7	6
4	0.222	4	3
5	0.180	5	4

$$
s_p = \sqrt{\frac{6(0.171)^2 + 4(0.205)^2 + 6(0.185)^2 + 3(0.222)^2 + 4(0.180)^2}{6 + 4 + 6 + 3 + 4}}
$$

$$
s_p = \sqrt{\frac{0.1755 + 0.1681 + 0.2054 + 0.1479 + 0.1296}{23}}
$$

$s_p = 0.190$ with 23 degrees of freedom.

C.3 Do Two Estimates of Precision Differ?

Conduct an F test, as follows:

Let s_1 = estimate of standard deviation (larger value) based on n_1 measurements.

Let s_2 = estimate of standard deviation (smaller value) based on n_2 measurements.

In each case, the respective degrees of freedom, $\nu = n-1$.

Calculate $F = s_1^2 / s_2^2$

Look up critical value of F_c in Table B.3, based on the respective degrees of freedom for the estimates of s_1 and s_2.

If $F > F_c$ consider $s_1 > s_2$ at the chosen level of confidence

If $F < F_c$ there is no reason to believe that $s_1 > s_2$ at the chosen level of confidence

Example C.3 - Comparison of Precision Estimates

$$
\begin{array}{llllll}
s_1 & = 2.00 & & n_1 = 6 & \nu_1 = 5 \\
s_2 & = 1.00 & & n_2 = 6 & \nu_2 = 5 \\
F & = 4.00/1.00 = 4.0 \\
F_c & = 7.15 \text{ at } 5\% \text{ level of significance}
\end{array}
$$

Conclusion: There is no reason to believe that $s_1 > s_2$.

C.4 What are the Confidence Limits for an Estimate of a Standard Deviation?

The width of the confidence interval for an estimated standard deviation will depend on the number of degrees of freedom, ν, upon which the estimate is based ($\nu=n-1$). The interval is not symmetrical (see Figure C.2), as in the case for a mean, since a small number of measurements tend to underestimate the standard deviation. To calculate the bounds of the interval, one may use a table such as Table B.4 and find the factors B_U and B_L corresponding to the number of degrees of freedom involved and the confidence level sought. In the table, $\alpha = 0.05$ corresponds to a confidence of 95% for the interval so calculated. The confidence interval is then, sB_L to sB_U.

Example C.4 - Confidence Limits for Estimate of Standard Deviations

$$s = 0.15 \qquad n = 10, \qquad \nu = 9$$

For $\alpha = .05$. $\nu = 9$ (see Table B.4) one finds $B_U = 1.746$; $B_L = 0.6657$

The confidence interval for s is 0.15 x 0.6657 to 0.15 x 1.746 or 0.10 to 0.26.

C.5 Confidence Interval for a Mean

The confidence interval for the mean will depend on the number of measurements, n, the standard deviation, s, and the level of confidence desired. The confidence interval is calculated using the expression

$$\bar{x} \pm \frac{ts}{\sqrt{n}}$$

The value for t (see Table B.5) will depend on the level of confidence desired and the number of degrees of freedom, ν, associated with the estimation of s. If s is based on the set of measurements used to calculate the mean, $\bar{x}$, then $\nu = n-1$. If the measurements are made by a system under statistical control, as demonstrated by a control chart, ν will depend on the number of measurements made to establish the control limits.

Example C.5 - Confidence Interval Based on s Estimated from Data Set of Seven Measurements

$$\begin{aligned}
\bar{x} &= 10.05 \\
s &= 0.11 \\
n &= 7 \\
\nu &= 6
\end{aligned}$$

For a 95 percent level of confidence, t = 2.447, hence

$$10.05 \pm \frac{2.447 \times 0.11}{\sqrt{7}} = 10.05 \pm 0.10, \text{ or } 9.95 \text{ to } 10.15$$

Example C.5 - Confidence Interval Based on s Obtained from Control Chart Limits, One Measurement of x

$$\begin{aligned}
x &= 10.05 \\
s &= 0.11 \\
\nu &= 45 \text{ (control chart)} \\
n &= 1
\end{aligned}$$

For a 95 percent level of confidence, t = 2.016, hence

$$10.05 \pm \frac{2.016 \times 0.11}{\sqrt{1}} = 10.05 \pm 0.22 \text{ or } 9.83 \text{ to } 10.27$$

Values of t in the above were obtained from Table B.5, by interpolation

Note: There is no statistical basis for a confidence level statement for one measurement unless supported by a control chart or other evidence of statistical control.

C.6 Do the Means of Two Measured Values Disagree, significantly?

The decision on disagreement is based on whether the difference, Δ, of the two values exceeds its statistical uncertainty, U. The method used for calculation of the uncertainty depends on whether or not the respective standard deviation estimates may be considered to be significantly different.

Case I No reason to believe that the standard deviations differ (e.g., same method, analyst, experimental conditions, etc.).

Step 1 Chose the significance level of the test.

Step 2 Calculate a pooled standard deviation from the two estimates to obtain a better estimate of the standard deviation.

$$s_p = \sqrt{\frac{\nu_A \, s_A^2 + \nu_B \, s_B^2}{\nu_A + \nu_B}}$$

s_p will be based on $\nu_A + \nu_B$ degrees of freedom

Step 3 Calculate the uncertainty, U, of the difference

$$U = t \, s_p \sqrt{\frac{n_A + n_B}{n_A \, n_B}}$$

Step 4 Compare $\Delta = |\, \overline{x}_A - \overline{x}_B \,|$ with U

If $\Delta \leq U$, there is no reason to believe that the means disagree.

Example

$$\overline{x}_A = 4.25 \qquad \overline{x}_B = 4.39$$

$$s_A = 0.13 \qquad s_B = 0.17$$

$$n_A = 7 \qquad n_B = 10$$

$$\nu_A = 6 \qquad \nu_B = 9$$

$$\Delta = |\, \overline{x}_A - \overline{x}_B \,| = 4.25 - 4.39 \,| = 0.14$$

Step 1 $\alpha = 0.05$ (95% confidence)

Step 2 $$s_p = \sqrt{\frac{6 \, (0.13)^2 + 9 \, (.17)^2}{15}}$$

$$s_p = \sqrt{\frac{.1014 + .2061}{15}}$$

$$s_p = 0.155$$

Step 3 $$U = 2.131 \times 0.155 \sqrt{\frac{7 + 10}{70}}$$

$$U = 0.080$$

Step 4 $.14 > .080$

Conclude that 4.39 differs from 4.25 at the 95% level of confidence.

Case II Reason to believe that the standard deivations differ (e.g., different experimental conditions, different laboratories, etc.)

Step 1 Chose α, the significance level of the list.

Step 2 Compute the estimated variance of each value

$$V_A = \frac{s_A^2}{n_A} \qquad , \qquad V_B = \frac{S_B^2}{n_B}$$

Step 3   Compute the effective number of degrees of freedom, f

$$f = \frac{(V_A + V_B)^2}{\dfrac{V_A^2}{n_A+1} + \dfrac{V_B^2}{n_B+1}} - 2$$

Step 4   Compute the uncertainty, U, of the difference

$$U = t'\sqrt{V_A + V_B} \; ,$$

Step 5   Compute Δ with U

If Δ is $\leq$ U there is no reason to believe that the means disagree

Example

$\overline{x}_A = 4.25$	$\overline{x}_B = 4.39$
$s_A = 0.13$	$s_B = 0.17$
$n_A = 7$	$n_B = 10$

Step 1 $\alpha = 0.05$ (95% confidence)

Step 2 $V_A = \dfrac{(.13)^2}{7} = 2.414 \times 10^{-3}$ $V_B = \dfrac{(.17)^2}{10} = 2.89 \times 10^{-3}$

Step 3 $f = \dfrac{(2.414 \times 10^{-3} + 2.89 \times 10^{-3})^2}{\dfrac{2.414 \times 10^{-3}}{8} + \dfrac{2.89 \times 10^{-3}}{11}} - 2$

$f = 17$

Step 4 $U = 2.11\sqrt{2.414 \times 10^{-3} + 2.89 \times 10^{-3}}$

$U = 0.153$

Step 5 $\Delta = 0.14$; $U = 0.153$

Conclude there is no reason to believe that $\overline{x}_B > \overline{x}_A$ at 95% level of confidence.

C.7 Statistical Tolerance Intervals

A tolerance interval represents the limits within which a specified percentage of the population is expected to lie with a given probability. It is especially useful to specify the variability in composition of samples. If the standard deviation of the population of samples were known, the limits for a given percentage of the population could be calculated with certainty. Because only an estimate of the standard deviation is usually known, based on a limited sampling of the population, a tolerance interval, based on inclusion of a percentage of the population with a specific probability of inclusion, is all that can be calculated.

The calculation is made as follows:

$$\text{Tolerance Interval} = \overline{x} \pm ks$$

where   k = a factor (obtained from Table B.6 for example) based on the percentage of population to be included, the probability of inclusion, and the number of measurements used to calculate $\overline{x}$ and s.

Example C.7 - Statistical Tolerance Interval

For measurements of ten samples of a shipment of coal, the sulfur content was found to be

$$\overline{x} = 1.62\% \qquad s = 0.10\% \qquad n = 10$$

From Table B.6, k = 3.379 for $\gamma = 0.95$, p = 0.95, n = 10.

The tolerance interval is thus 1.62% ± 0.34% or 1.28% to 1.96%.

C.8 Pooling Means to Obtain a Grand Average, $\bar{\bar{x}}$

Case I All means based on same number of measurements of equal precision

$$\bar{\bar{x}} = \frac{\bar{x}_1 + \bar{x}_2 + \bar{x}_3 + \ldots + \bar{x}_n}{n}$$

Case II Means based on different number of measurements, but no reason to believe the precisions differ

$$\bar{\bar{x}} = \frac{n_1\bar{x}_1 + n_2\bar{x}_2 + \ldots + n_n\bar{x}_n}{n_1 + n_2 + \ldots + n_n}$$

Case III Means based on different number of measurements with differing precisions

Step 1 Compute weight to be used for each mean,

$$w_i = \frac{n_i}{s_i^2} \quad e.g., \quad w_1 = \frac{n_1}{s_1^2}$$

Step 2

$$\bar{\bar{x}} = \frac{w_1\bar{x}_1 + w_2\bar{x}_2 + \ldots + w_n\bar{x}_n}{w_1 + w_2 + \ldots + w_n}$$

$$s_{\bar{\bar{x}}}^2 = \frac{1}{w_1 + w_2 + \ldots w_n}$$

Example C.8 Case - Calculation of Grand Average, Case I

To calculate the grand average, $\bar{\bar{x}}$, of the following means, all believed to be equally precise.

$\bar{x}_1 = 10.50$
$\bar{x}_2 = 10.37$
$\bar{x}_3 = 10.49$
$\bar{x}_4 = 10.45$
$\bar{x}_5 = 10.47$

$$\bar{\bar{x}} = \frac{10.50 + 10.37 + 10.49 + 10.45 + 10.47}{5}$$

$\bar{\bar{x}} = 10.456$

Example C.8 - Calculation of Grand Average, Case II

$\bar{x}_1 = 10.50 \qquad n = 10$
$\bar{x}_2 = 10.37 \qquad n = 5$
$\bar{x}_3 = 10.49 \qquad n = 20$
$\bar{x}_4 = 10.45 \qquad n = 5$
$\bar{x}_5 = 10.47 \qquad n = 7$

$$\bar{\bar{x}} = \frac{10.50 \times 10 + 10.37 \times 5 + 10.49 \times 20 + 10.45 \times 5 + 10.47 \times 7}{47}$$

$\bar{\bar{x}} = 10.472$

Example C.8 - Calculation of Grand Average, Case III

i	$\bar{x}_i$	n_i	s_i	w_i
1	10.50	10	.10	1000
2	10.37	5	.15	222
3	10.49	20	.11	1652
4	10.45	5	.10	500
5	10.47	7	.16	273

$$\bar{\bar{x}} = \frac{10.50 \times 1000 + 10.37 \times 222 + 10.49 \times 1652 + 10.45 \times 500 + 10.47 + 273}{1000 + 222 + 1652 + 500 + 273}$$

$\bar{\bar{x}} = 10.478$

$s_{\bar{x}}^2 = 2.74 \times 10^{-4}$

$s_{\bar{\bar{x}}} = 0.0166$

C.9 Outliers

Outliers are data values that do not belong or have a very low probability of belonging to the data set in which they occur. They can result from such causes as blunders or malfunctions of the methodology, or from unusual losses or contamination. If outliers occur too often, there may be deficiencies in the quality control program which can be corrected and thus improve the measurements. One should always look for causes when data are rejected.

Outliers can be identified when data are plotted, when results are ranked, and when control limits are exceeded. Only when a measurement system is well understood and the variance is well established, or when a large body of data are available, is it possible to distinguish between extreme values and true outliers with any degree of confidence.

The following rules for rejection of data should be used with caution since an outlier in a well-behaved measurement system should be a rare occurrence.

A. Rejection for Assignable Cause

   System malfunction, misidentification of a sample, suspected transcription error, known contamination, are examples.

B. Rule of Huge Error

   If the questioned value differs from the mean by some multiple, M, of the standard deviation, it may be considered to be an outlier. The size of the multiple depends on the confidence required for rejection. One evaluates

   $$M = \frac{|x - \bar{x}|}{s}$$

   A practical rule might be to use $M \geq 4$ as a criterion for rejection. This corresponds to a significance level of $< 2\%$ when the standard deviation is well established, such as based on a data set of 15 or larger.

   If s is not well established but depends on the data set in question, the odds for rejection are much larger. For example, if $\bar{x}$ and s are based on 6 measurements, $M > 6$ would be the criterion for rejection for a 2% level of significance.

C. Statistical Tests

   Several statistical tests are available for identifying outliers based on ranking data and testing extreme values for credibility. The Dixon criterion is described on page 17-3 of NBS Handbook 91 (19) and the critical values for decision on rejection using this criterion are given in Table A-14 of the same reference.

   A method for identifying outlier laboratories in a collaborative test or proficiency testing program is described by Youden on page 148 of NBS Special Publication 300 (16) where a table of the test score values necessary to use his criterion also will be found.

Example C.9 - Outliers, Huge Error Concept

x (original order)	x (ranked order)
10.50	10.45
10.47	10.47
10.49	10.47
10.45	10.48
10.47	10.49
10.57	10.50
10.52	10.50
10.50	10.52
10.48	10.53
10.53	10.57

1. 10.57 appears to be an outlier

2. Calculate mean and sample standard deviation, s, ignoring 10.57

    $\bar{x}$ = 10.490   s = 0.0255

3. $\dfrac{10.57 - 10.49}{0.0255}$ = 3.13

4. Since 3.13 < 4 conclude that 10.57 should be retained in the data

5. Calculate mean and sample standard deviation including 10.57

    $\bar{x}$ = 10.498   s = 0.0349

C.10   Use of Random Number Tables

It is often desirable to randomize the sequence in which measurements are made, samples are chosen, and other variables of an analytical program are set. Tables of random numbers, such as Table B.7, are a convenient and simple way to accomplish this. The following procedure may be used.

1. Number the samples (or measurements) serially, say 00 to xy. For example, 00 to 15 for 16 items.

2. Start at any randomly selected place in the table and proceed from that point in any systematic path. The order in which the item numbers are located becomes the random sequence number to be assigned to them.

Example: Start at Row 7, Column 3 (chosen by chance) of Table B.7 and proceed from left to right as in reading. The first number is 76 which is not usable for the above series of items. The first usable number is 15. Proceeding as above, the items are located in the following order: 15, 06, 02, 03, 05, 00, 11, 13, 07, 10, 09, 08, 04, 14, 01, 12. If a number already chosen is encountered, pass over it to the next usable number.

John K. Taylor

Center for Analytical Chemistry
National Bureau of Standards
Washington, D.C. 20234
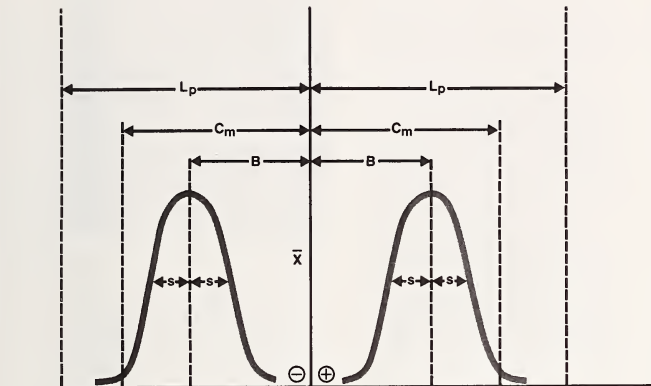
Quality Assurance of

Figure 1. Measurement tolerances and errors

The objective of quality assurance programs for analytical measurements is to reduce measurement errors to tolerable limits and to provide a means of ensuring that the measurements generated have a high probability of being of acceptable quality. Two concepts are involved. *Quality control* is the mechanism established to control errors, while *quality assessment* is the mechanism to verify that the system is operating within acceptable limits. General handbooks that discuss quality assurance in more detail are given in References 1–3.

Quality is a subjective term. What is high quality in one situation may be low or unacceptable quality in another case. Clearly the tolerable limits of error must be established for each. Along with this there must be a clear understanding of the measurement process and its capability to provide the results desired.

The tolerance limits for the property to be measured are the first conditions to be determined. These are based upon the considered judgment of the end user of the data and repre-

sent the best estimate of the limits within which the measured property must be known, to be useful for its intended purpose. The limits must be realistic and defined on the basis of cost–benefit considerations. It is better to err on the side of too-narrow limits. Yet, measurement costs normally increase as tolerances are decreased, so that the number of measurements possible for a fixed budget may be inadequate when coupled with material-variability considerations.

Once one has determined the tolerance limits for the measured property, the permissible tolerances in measurement error may be established. The basis for this is shown in Figure 1. The tolerance limits for the measured property are indicated by L_p. Uncertainties in the measurement, based on the experience and judgment of the analyst, are indicated by C_m. These include estimates of the bounds for the biases (systematic errors), B, and the random errors as indicated by s, the estimate of the standard deviation. Obviously, C_m must be less than L_p if the data are to be useful. The

confidence limits for $\bar{x}$, the mean of n replicate measurements, are:

$$C_m = \pm \left[B + \frac{ts}{\sqrt{n}} \right]$$

in which t is the so-called student factor. While the effect of random error is minimized by replication of measurements, there are practical limitations, and any measurement process that requires a large number of replicates has a serious disadvantage.

Well-designed and well-implemented quality assurance programs provide the means to operate a measurement system in a state of statistical control, thereby providing the basis for establishing reliable confidence limits for the data output.

Until a measurement operation . . . has attained a state of statistical control, it cannot be regarded in any logical sense as measuring anything at all.

C. E. Eisenhart

The Analytical System

Analytical measurements are made because it is believed that compositional information is needed for some end use in problem solving. Explicitly or implicitly, a measurement system such as that depicted in Figure 2 is involved. One must have full understanding of the measurement system for each specific situation in order to generate quality data.

The conceptualization of the problem, including the data requirements and their application, constitutes the model. The plan, based on the model, includes details of sampling, measurement, calibration, and quality assurance. Various constraints such as time, resources, and the availability of samples may necessitate compromises in the plan. Adequate planning will require the collaboration of the analyst, the statistician, and the end user of the data in all but the most routine

Chemical Measurements

cases. In complex situations, planning may be an iterative process in which the actual data output may require reconsideration of the model and revision of the plan.

Sampling has been discussed in a recent paper (4). Obviously, the sample is one of the critical elements of the measurement process. Closely related is the measurement methodology to be used. The method used must be adequate for the intended purpose and it must be properly utilized. The necessary characteristics of a suitable method include: adequate sensitivity, selectivity, accuracy, and precision. It is desirable that it also have the following characteristics: large dynamic measurement range; ease of operation; multiconstituent applicability; low cost; ruggedness; portability. To judge its suitability, the following information must be known about it: type of sample; forms determined; range of applicability; limit of detection; biases; interferences; calibration requirements; operational skills required; precision; and accuracy. Obviously all of the above characteristics must match the measurement requirements. In case of doubt, trial measurements must be made to demonstrate applicability to a given problem. A cost–benefit analysis may be needed to determine which of several candidate methods is to be selected. A method, once adopted, must be used in a reliable and consistent manner, in order to provide reproducible data. This is best accomplished by following detailed written procedures called Standard Operating Procedures (SOPs) in quality assurance terminology. Standard methods developed by voluntary standardization organizations are often good candidates for SOPs, when they are available.

Two kinds of calibrations are required in most cases. Physical calibrations may be needed for the measurement equipment itself and for ancillary measurements such as time, temperature, volume, and mass. The measurement apparatus may include

built-in or auxiliary tests such as voltage checks, which may need periodic verification of their stability if not of their absolute values. But especially, most analytical equipment requires some kind of chemical calibration, often called standardization, to establish the analytical function (i.e., the relation of instrument response to chemical quantification). Obviously, the analyst must thoroughly understand each of the calibrations required for a particular measurement. This includes a knowledge of the standards needed and their relation to the measurement process, the frequency of calibration, the effect on a measurement system due to lack of calibration, and even the shock to the system resulting from recalibration.

Quality Control

Quality control encompasses all of the techniques used to encourage reproducibility of the output of the measurement system. It consists of the use of a series of protocols developed in advance and based on an intimate understanding of the measurement process and the definite requirements of the specific measurement situation. Protocols, i.e., procedures that must be rigorously followed, should be established for sampling, measurement, calibration, and data handling. Some of these, or at least selected portions, may be applicable to most or all of the measurements of a particular laboratory and become the basis of a good laboratory practices manual (GLPM).
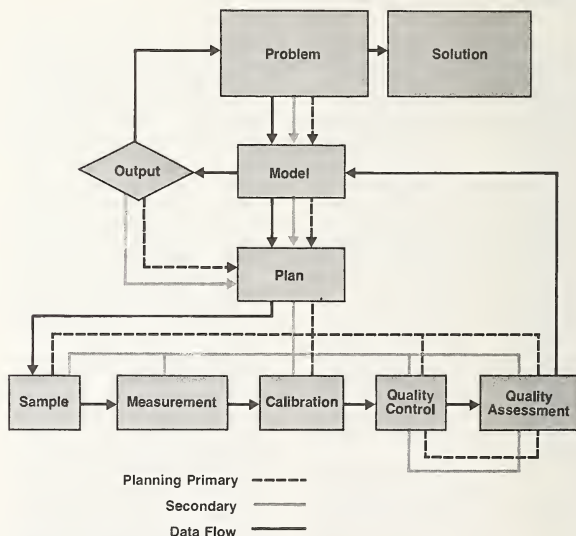

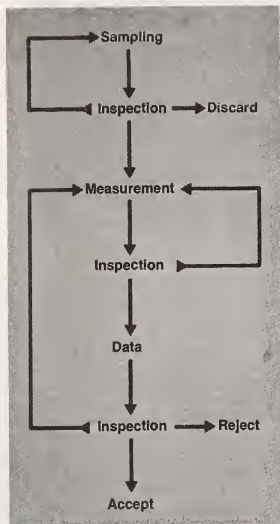**Figure 2.** Analytical measurement system

Figure 3. Quality control by inspection

In fact, the GLPM should cover the generalities, if not the specifics, of all measurement practices of the laboratory. The protocols for a specific measurement process include the GLPs together with any requirements of the specific situation.

The GLPM and protocols should be developed collaboratively by all of those involved in the measurements, and this development process may be the most important aspect of their function. It encourages a keen consideration of the measurement process and creates an awareness of potential problems that GLPs attempt to avert.

Protocols are of little use unless · they are followed rigorously, and the attitudes of laboratory personnel are certainly key factors in this regard. Analysts must aspire to produce high quality data and must be their own most severe critics. Notwithstanding, good quality control systems should include provisions for inspection, both periodically and aperiodically (unannounced) to ascertain how well they are functioning. Large laboratories may have a quality control officer or group, independent of the laboratory management, that oversees the operation of the quality control system.

Quality Control by Inspection

An informal kind of quality control involves the frequent if not constant inspection of certain aspects of the measurement system for real or apparent problems (5). The essential features of such a system are depicted in Figure 3. Based on an intimate knowledge of the measurement process, samples may be casually inspected for their adequacy. The rejection and possible replacement of obviously unsuitable ones can eliminate not only extra work but also erroneous data that might be difficult to identify later. Difficulties in the actual measurement may often be identified as they occur and remedial measures, including remeasurement, may be taken either to save data that might otherwise be lost or at least to provide valid reasons for any rejections. Likewise, data inspection can identify problems and initiate remedial actions, including new measurements, while it is still possible to do so.

Control Charts

The performance of a measurement system can be demonstrated by the measurement of homogeneous and stable control samples in a planned repetitive process. The data so generated may be plotted as a control chart in a manner to indicate whether the measurement system is in a state of statistical control. Either the result of a single measurement on the control sample, the difference between duplicate measurements, or both may be plotted sequentially. The first mode may be an indicator of both precision and bias, while the second monitors precision only.

To effectively use such a chart, the standard deviation of a single measurement of the control sample must be known. This may be obtained by a series of measurements of the control sample, or it may be obtained from the experience of the laboratory on measuring similar samples. Control limits, i.e., the extreme values believed to be credible, are computed from the standard deviation. For example, the 2σ limit represents those within which the values are expected to lie 95% of the time. The 3σ limit represents the 99.7% confidence level. Departures from the former are warnings of possible trouble, while exceeding the latter usually means corrective action is needed. In the event that the standard deviation cannot be estimated with sufficient confidence initially, the control chart may be drawn using the best estimate, and the limits may be modified on the basis of increasing measurement experience.

The development of a control chart must include the rationale for its use. There must be a definite relation between the control measurements and the process they are designed to control. While the control chart only signifies the degree of replication of measurements of the control sample, its purpose is to provide confidence in the measurement process. To do this, the control measurements must simulate the measurements normally made. In chemical measurements, this means simulation of matrix, simulation of concentration levels, and simulation of sampling. The latter objective may be difficult if not impossible to achieve. It must be further emphasized that the control measurements should be random members of the measurement routine, or at least they should not occupy biased positions in any measurement sequence.

To the extent that control samples are representative of the test samples, and to the extent that measurements of them are representative of the measurement process, the existence of statistical control for these samples can imply such control of the measurement process and likewise of the results obtained for the test samples.

No specific statements can be made about the frequency of use of control samples. Until a measurement process is well understood, control samples may need to be measured frequently. As it is demonstrated to be in control, the need may become less and the incentive to do "extra" work may diminish. Along with the decision on how much effort should be devoted to quality control the risks and consequences of undetected loss of control must be weighed. Many laboratories consider that the 5–15% extra effort ordinarily required for all aspects of quality control is a small price to pay for the quality assurance it provides. When measurements are made on a frequently recurring schedule, internal controls, such as duplicate measurements of test samples, can provide evidence of reproducibility so that control samples may be used largely to identify systematic errors, drifts, or other types of problems.

When laboratories are engaged in a variety of measurements, the use of representative control samples may be difficult if not impossible. In such cases, often only the measurement methodology can be tested, and evaluation of the quality of the measurement output requires considerable judgment. In such cases, the experience of the lab becomes a key factor.

In some complex measurement systems, certain steps or subsystems are more critical than others, and hence it may be more important to develop control charts for them than for the entire system. The control of such steps may indeed prevent propagation of error into the end result. An example is the sampling step, which may be very critical with respect to the end result. In such a case, the records of periodic inspections may be adaptable to the control chart technique of quality control.

Quality Assessment

Procedures used to evaluate the effectiveness of the quality control system may be classified according to whether the evidence arises from internal or external sources. Internal procedures, useful largely for estimating precision, include the use of internal reference samples and control charts to monitor the overall performance of the measurement system as described in an earlier section. Replicate measurements on replicate or split samples can provide valuable insight into the reproducibility of both the measurement and sampling processes. Comparison of the results obtained as a consequence of interchange of analysts, equipment, or combinations of these can attest to operational stability as well as identify malfunctions. Measurements made on split samples using a completely independent method can lend confidence to the method normally in use or indicate the presence of measurement bias.

External quality assessment is always needed since it can detect problems of bias that are difficult to identify by internal procedures. Participation in collaborative tests, exchange of samples with other laboratories, and the use of certified reference materials are time-honored assessment devices. NBS Standard Reference Materials (SRMs) (6) are especially useful for quality assessment in cases where they are available and applicable. The information that can be obtained or inferred by their use is described in a later section. Operators of monitoring networks may provide proficiency testing or audit samples to assess laboratory performance. Ordinary practices should be used here, so that normal rather than optimum performance is measured.

A laboratory should diligently use the information obtained in the quality assessment process. Adverse data should not be treated in a defensive manner but the reason for it should be investigated objectively and thoroughly. When laboratory records are reliably and faithfully kept, the task of identifying causes of problems is made easier. This is an important reason for developing data handling protocols and ensuring that all protocols are strictly followed.

Systematic Errors

Systematic errors or biases are of two kinds—concentration-level independent (constant), and concentration-level related. The former are sometimes called additive while the latter are called multiplicative. Both kinds may be present simultaneously in a given measurement system. An example of the first kind is the reagent blank often present in measurements involving chemical processing steps. The second kind can result from, for example, use of an inaccurately certified calibrant.

Systematic errors may arise from such sources as faulty calibrations, the use of erroneous physical constants, incorrect computational procedures, improper units for measurement or reporting data, and matrix effects on the measurement. Some of these can be eliminated or minimized by applying corrections or by modification of the measurement technique. Others may be related to fundamental aspects of the measurement process. The most insidious sources of error are those unknown or unsuspected of being present.

One of the most important sources of error in modern instrumental measurements concerns uncertainties in the calibrants used to define the analytical function of the instrument. The measurement step essentially consists of the comparison of an unknown with a known (calibrant) so that any error in the latter results in a proportional error in the former. The need to use calibrants of the highest reliability is obvious.

The measurement protocol should include a detailed analysis of the sources of error and correction for them to the extent possible. The uncertainties, B, referred to earlier, represent the uncertainties in the corrections for the systematic errors. In making such an estimate, the 95% confidence limits should be assigned to the extent possible. The magnitudes of these uncertainties can be estimated from those assigned by others in the case of such factors as calibration standards and physical constants. Other constant sources of error may be more subtle both to identify and to evaluate, and the judgment and even intuition of the experimenter may be the only sources of information.

The effectiveness of elimination of, or correction for, systematic errors is best evaluated from external quality assessment procedures. Differences found between known and measured values of test samples, such as SRMs, need to be reconciled with the laboratory's own estimates of bounds for its random and systematic errors. When the random error is well established, as by the quality control process, significant discrepancies can be attributed to unsuspected or incorrectly estimated systematic errors.

The Use of SRMs for Quality Assessment

An SRM is a material for which the properties and composition are certified by the National Bureau of Standards (6, 7). To the extent that its compositional properties simulate
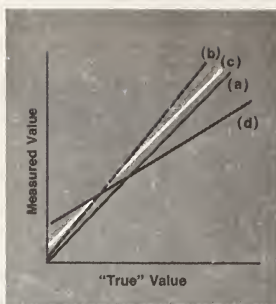

Figure 4. Typical analytical systematic errors (bias). (a) = unbiased; (b) = measurement-level related; (c) = constant error; and (d) = combination of b and c

those of the sample ordinarily measured, its "correct" measurement can imply "correct" measurement of the usual samples. Such a conclusion requires that the protocol of measurement was the same in each case. Hence it is necessary that no special care be exercised in measuring the SRM, other than that ordinarily used.

Analysis of SRMs has been recommended as a means of providing "traceability" to national measurement standards. However, a word of caution is appropriate on this point. Measurement processes are seldom identical, so that traceability is most often based on inference. Also, the fact that an acceptable result is or is not obtained for an SRM provides no unique explanation for such a result.

The use of an SRM should never be attempted until the analytical system has been demonstrated to be in a state of statistical control. An SRM is not needed for such a purpose and such use is discouraged. Ordinarily, the SRM will be available in limited amount so that the statistics of the measurement process should be demonstrated by measurements on other materials. Only under such a situation can the results of an SRM measurement be considered as representative of the measurement system.

A consideration of the nature of analytical errors, shown in Figure 4, will clarify why the measurement of a single SRM may not be fully informative. It will be noted that errors may be constant, measurement-level related, or a combination of these, and a single right or wrong result will not indicate on which of several possible curves it might lie. Measurement of a series of SRMs may clarify the nature of the measurement process and this should be done whenever possible. An intimate understanding of the operation of a particular measurement system may also make it possible to eliminate some of the possible sources of error and to better interpret the data from measurement of SRMs.

Record Keeping

Adequate record keeping in an easily retrievable manner is an essential part of the quality assurance program. Records needed include the description of test samples, experimental procedures, and data on calibration and testing. Quality control charts should be diligently prepared and stored. A chain of custody of test materials should be operative and such materials should be retained and safeguarded until there is no doubt about their future use or need.

Data Control

The evaluation, review, and release of analytical data is an important part of the quality assurance process. No data should be released for external use until it has been carefully evaluated. Guidelines for data evaluation, applicable to almost every analytical situation, have been developed by the ACS Committee on Environmental Improvement (8). A prerequisite for release of any data should be the assignment of uncertainty limits, which requires the operation of some kind of a quality assurance program. Formal release should be made by a professional analytical chemist who certifies that the work was done with reasonable care and that assigned limits of uncertainty are applicable.

Laboratory Accreditation

Laboratory accreditation is one form of quality assurance for the data output of certified laboratories. Accreditation is based on criteria that are considered essential to generate valid data and is a formal recognition that the laboratory is competent to carry out a specific test or specific type of test (9, 10). The certification is as meaningful as the care exercised in developing certification criteria and evaluating laboratory compliance. Generic criteria developed by national and international standardization organizations have been influential in this respect (11). These criteria are well conceived and provide general guidance for the sound operation of analytical laboratories, whether or not certification is involved.

Implementation

Detailed quality assurance plans are ineffective unless there is commitment to quality by all concerned. This commitment must be total, from management to technical staff. The former must provide the resources, training, facilities, equipment, and encouragement required to do quality work. The latter must have the technical ability and motivation to produce quality data. Some may argue that if there is such commitment, there is no need for a formal quality assurance program.

However, the experience of many laboratories has demonstrated that a formal quality assurance program provides constant guidance for the attainment of the quality goals desired.

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John K. Taylor, coordinator for quality assurance and voluntary standardization activities at the National Bureau of Standards Center for Analytical Chemistry, received his BS from George Washington University, and his MS and PhD degrees from the University of Maryland. His research interests include electrochemical analysis, refractometry, isotope separations, standard reference materials, and the application of physical methods to chemical analysis.

Sampling for Chemical Analysis
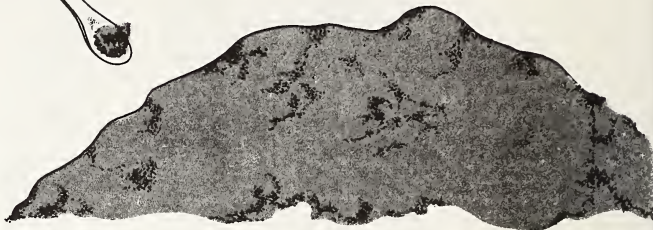
A major consideration in the reliability of any analytical measurement is that of sample quality. Too little attention is directed to this matter. The analyst often can only report results obtained on the particular test specimen at the moment of analysis, which may not provide the information desired or needed. This may be because of uncertainties in the sampling process, or in sample storage, preservation, or pretreatment prior to analysis. The sampling plan itself is often so poorly considered as to make relation of the analytical results to the population from which the sample was drawn uncertain, or even impossible to interpret.

All of the above aspects of sampling merit full consideration and should be addressed in every analytical determination. Because the scope is so broad, we will limit the present discussion to a small segment of the total problem, that of sampling bulk materials. For such materials the major steps in sampling are:
• identification of the population from which the sample is to be obtained,
• selection and withdrawal of valid gross samples of this population, and
• reduction of each gross sample to a laboratory sample suitable for the analytical techniques to be used.

The analysis of bulk materials is one of the major areas of analytical activity. Included are such problems as the analysis of minerals, foodstuffs, environmentally important substances, and many industrial products. We shall discuss the major considerations in designing sampling programs for such materials. While our discussion is specifically directed toward solid materials, extension to other materials will often be obvious.

A brief list of definitions commonly used in bulk sampling is provided in the glossary.

Preliminary Considerations in Sampling

Poor analytical results may be caused in many ways—contaminated reagents, biased methods, operator errors in procedure or data handling, and so on. Most of these sources of error can be controlled by proper use of blanks, standards, and reference samples. The problem of an invalid sample, however, is special; neither control nor blank will avail. Accordingly, sampling uncertainty is often treated separately from other uncertainties in an analysis. For random errors the overall standard deviation, s_o, is related to the standard deviation for the sampling operation, s_s, and to that

for the remaining analytical operations, s_a, by the expression: $s_o^2 = s_a^2 + s_s^2$. Whenever possible, measurements should be conducted in such a way that the components of variance arising from sample variability and measurement variability can be separately evaluated. If the measurement process is demonstrated to be in a state of statistical control so that s_a is already known, s_s can be evaluated from s_o, found by analysis of the samples. Otherwise, an appropriate series of replicate measurements or replicate samples can be devised to permit evaluation of both standard deviations.

Youden has pointed out that once the analytical uncertainty is reduced to a third or less of the sampling uncertainty, further reduction in the analytical uncertainty is of little importance (1). Therefore, if the sampling uncertainty is large and cannot be reduced, a rapid, approximate analytical method may be sufficient, and further refinements in the measurement step may be of negligible aid in improving the overall results. In fact, in such cases a rapid method of low precision that permits more samples to be examined may be the best route to reducing the uncertainty in the average value of the bulk material under test.

An excellent example of the importance of sampling is given in the deter-

Report

Byron Kratochvil

Department of Chemistry
University of Alberta
Edmonton, Alberta, Canada T6G 2G2

John K. Taylor

National Bureau of Standards
Washington, D.C. 20234

Figure 1. Relative standard deviation associated with the sampling and analysis operations in testing peanuts for aflatoxins (after T. B. Whittaker, *Pure and Appl. Chem.*, **49,** 1709 (1977))
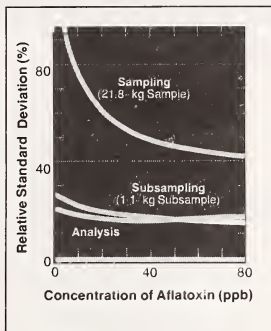
mination of aflatoxins in peanuts (2). The aflatoxins are highly toxic compounds produced by molds that grow best under warm, moist conditions. Such conditions may be localized in a warehouse, resulting in a patchy distribution of highly contaminated kernels. One badly infected peanut can contaminate a relatively large lot with unacceptable levels (above about 25 ppb for human consumption) of aflatoxins after grinding and mixing. The standard deviations of the three operations of sampling, subsampling, and analysis are shown in Figure 1. The analytical procedure consists of solvent extraction followed by thin-layer chromatography and measurement of the fluorescence of the aflatoxin spots. Clearly, sampling is the major source of the analytical uncertainty.

Types of Samples

Random Samples. In common with the statistician, the analytical chemist ordinarily wishes to generalize from a small body of data to a larger body of data. While the specimen/sample actually examined is sometimes the only matter of interest, the characteristics of the population of specimens are frequently desired. Obviously, the samples under examination must not be biased, or any inferences made from them will likewise be biased.

Statisticians carefully define several terms that are applied to statistical inference. The *target population* denotes the population to which we would like our conclusions to be applicable, while the *parent population* designates that from which samples were actually drawn. In practice these two populations are rarely identical, although the difference may be small. This difference may be minimized when the selection of portions for examination is done by a random process. In such a process each part of the population has an equal chance of being selected. Thus, random samples are those obtained by a random sampling process and form a foundation from which generalizations based on mathematical probability can be made.

Random sampling is difficult. A sample selected haphazardly is not a random sample. On the other hand, samples selected by a defined protocol are likely to reflect the biases of the protocol. Even under the most favorable circumstances, unconscious selection and biases can occur. Also, it can be difficult to convince untrained individuals assigned the task of obtaining samples that an apparently unsystematic collection pattern must be followed closely for it to be valid.

Whenever possible, the use of a table of random numbers is recommended as an aid to sample selection. The bulk material is divided into a number of real or imaginary segments. For example, a body of water can be conceptually subdivided into cells, both horizontally and vertically, and the cells to be sampled selected randomly. To do this each segment is assigned a number, and selection of segments from which sample increments are to be taken is made by starting in an arbitrary place in a random number table and choosing numbers according to a predecided pattern. For example, one could choose adjacent, alternate, or nth entries and sample those segments whose numbers occur until all of the samples decided upon have been obtained.

The results obtained for these and other random samples can be analyzed by some model or plan to identify whether systematic relations exist. This is important because of the possible introduction of apparent correlations due to systematic trends or biases in the measurement process. Accordingly, measurement plans should always be designed to identify and minimize such problems.

Despite the disadvantages, sampling at evenly spaced intervals over the bulk is still often used in place of random sampling owing to its simplic-
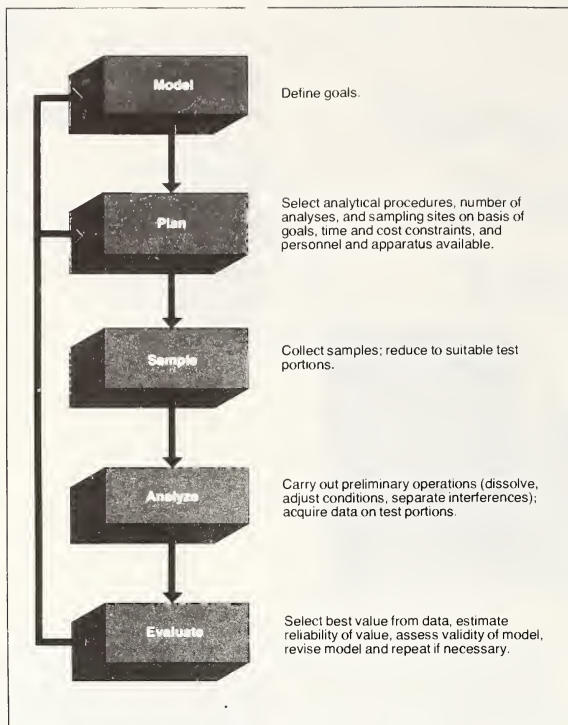
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Figure 2. The place of sampling in the overall analytical process

ity. Because this procedure is more subject to bias than random sampling, it is not recommended. If it is used, the results must be closely monitored to ensure that errors from periodicity in the material are not introduced.

Systematic Samples. Frequently, samples are obtained and analyzed to reflect or test some systematic hypothesis, such as changes in composition with time, temperature, or spatial location. Such samples, if collected in a systematic manner, may each be considered to represent a separate discrete population under the existing conditions. However, the results may still be statistically tested for the significance of any apparent differences.

In a carefully designed sampling plan, consideration should be given to the possible concurrence of unanticipated events or phenomena that could prejudice the information on the sample measured. For example, measurements to be taken at time intervals are sometimes made with a random start or other superimposed random time

element. Needless to say, the less known about a given process, the more randomness is merited. Conversely, as a process is more fully understood, systematic approaches can provide maximum efficiency of data acquisition.

Representative Samples. The term "representative sample" is frequently used in analytical discussions to connote a single sample of a universe or population (e.g., waste pile, lagoon, ground water) that can be expected to exhibit average properties of the population (see glossary). Obviously, such a sample cannot be selected by a random process. And even if it could, to ascertain the validity of its representativeness would require considerable effort.

The concept of a truly representative sample would appear to be valid in only two cases. The first case involves samples defined *a priori* as representative for a specific purpose. For example, the Hazardous Waste Management System prescribes seven pro-

...ocols for sampling wastes—ranging from viscous liquids, solids, or containerized liquids to reservoirs—to provide samples that "will be considered by the Agency (EPA) to be representative of the waste" (*3*). The second case involves the sampling of truly homogeneous materials.

While the measurement of samples defined as representative may reduce analytical costs, the information so obtained ordinarily does not enjoy the status of that obtained from valid random samples of the population. An exception is when effort has been vigorously exerted to homogenize the population prior to sampling. Such processes are difficult and are ordinarily only justified when the objective is to produce a number of subsamples of essentially similar properties.

Because of the difficulties of selecting or producing a "representative sample" it is recommended that this concept be discouraged for general purposes and reserved only for cases where the effort required to prepare such a sample is justified. An appreciation of the compositional information that is lost as a result is a further reason to discourage the practice. With a properly designed and executed random sampling plan, the valuable characteristics of sample mean and variation between members can be ascertained, neither of which can be obtained by measurement of one "representative sample."

Composite Samples. A composite sample (see glossary) may be considered as a special way of attempting to produce a representative sample. Many sampling procedures are based on the assumption that average composition is the only information desired. Such averages may be bulk averages, time-weighted averages, and flow-proportional averages, for example, and may be obtained by measurement of a composite, suitably prepared or collected. Elaborate procedures involving crushing, grinding, mixing, and blending have been developed and even standardized for the preparation of solid composites, while sampling systems for liquids (especially water) have been developed to obtain various composite samples.

Analysis of a number of individual samples permits determination of the average (at the expense of extra analytical effort) and the distribution of samples within the population (between-sample variability). In some cases, it may be of interest to isolate the within-sample variability as well. All this information is necessary for collaborative test samples and in reference material usage, especially when apparent differences in analytical results within and between laboratories need to be evaluated.

Because of the limited information provided by a composite sample, full consideration should be given to the consequences before deciding between this approach and the analysis of individual samples.

Subsampling. Usually, the sample received by the analytical laboratory will be larger than that required for a single measurement, so some subsampling (see glossary) will be required. Often, test portions (see glossary) must be taken for replicate measurements or for measurement of different constituents by several techniques. Obviously, such test portions must be sufficiently alike that the results are compatible. Frequently it is necessary to reduce particle size, mix, or otherwise process the laboratory sample (see glossary) before withdrawing portions (subsamples) for analysis. The effort necessary at this stage depends on the degree of homogeneity of the original sample. In general, the subsampling standard deviation should not exceed one-third of the sampling standard deviation. Although this may sound appreciable, it is wasteful of time and effort to decrease it below this level. But this does not mean care is unnecessary in subsampling. If a sample is already homogeneous, care may be needed to avoid introducing segregation during subsampling. Even though analysts may not be involved with sample collection, they should have sufficient knowledge of sampling theory to subsample properly. They should also be provided with any available information on the homogeneity of the samples received so that they can subsample adequately and efficiently.

Model of the Sampling Operation

Before sampling is begun, a model of the overall operation should be established (Figure 2). The model should consider the population to be studied, the substance(s) to be measured, the extent to which speciation is to be determined, the precision required, and the extent to which the distribution of the substance within the population is to be obtained.

The model should identify all assumptions made about the population under study. Once the model is complete, a sampling plan can be established.

The Sampling Plan

The plan should include the size, number, and location of the sample increments and, if applicable, the extent of compositing to be done. Procedures for reduction of the gross sample (see glossary) to a laboratory sample, and to the test portions, should be specified. All of this should be written as a

detailed protocol before work is begun. The protocol should include procedures for all steps, from sampling through sample treatment, measurement, and data evaluation; it should be revised as necessary during execution as new information is obtained. The guidelines for data acquisition and quality evaluation in environmental chemistry set out by the ACS Subcommittee on Environmental Analytical Chemistry are sufficiently general to be recommended reading for workers in all fields (4).

The sampling protocol should include details of when, where, and how the sample increments are to be taken. On-site criteria for collection of a valid sample should be established beforehand. Frequently, decisions must be made at the time of sampling as to components likely to appear in the sample that may be considered foreign, that is, not part of the population. For example, a portion of dredged sediment in which the mercury content is to be determined might contain cans, discarded shoes, rocks or other extraneous material. For the information sought these items might be considered foreign and therefore legitimately rejected. Decisions as to rejection become less clear with smaller items. Should smaller stones be rejected? How small? And what about bits of metal, glass, leather, and so on? Criteria for such decisions should be made logically and systematically, if possible before sampling is initiated.

The type of container, cleaning procedure, and protection from contamination before and after sampling must be specified. The question of sample preservation, including possible addition of preservatives and refrigeration, should be addressed. Some sampling plans call for field blanks and/or field-spiked samples. The critical nature of the latter and the difficulties possible under field conditions require the utmost care in planning and execution of

the sampling operation if the results are to be meaningful.

Whenever possible, the analyst should perform or directly supervise the sampling operation. If this is not feasible, a written protocol should be provided and the analyst should ensure that those collecting the samples are well-trained in the procedures and in use of the sampling equipment, so that bias and contamination are minimized. No less important is careful labeling and recording of samples. A chain of custody should be established such that the integrity of the samples from source to measurement is ensured. Often auxiliary data must be recorded at the time the sample is taken: temperature, position of the collecting probe in the sample stream, flow velocity of the stream, and so on. Omission or loss of such information may greatly decrease the value of a sample, or even render it worthless.

Sampling Bulk Materials. Once the substances to be determined, together with the precision desired, have been specified, the sampling plan can be designed. In designing the plan, one must consider:

• How many samples should be taken?
• How large should each be?
• From where in the bulk material (population) should they be taken?
• Should individual samples be analyzed, or should a composite be prepared?

These questions cannot be answered accurately without some knowledge of the relative homogeneity of the system. Gross samples should be unbiased with respect to the different sizes and types of particles present in the bulk material. The size of the gross sample is often a compromise based on the heterogeneity of the bulk material on the one hand, and the cost of the sampling operation on the other.
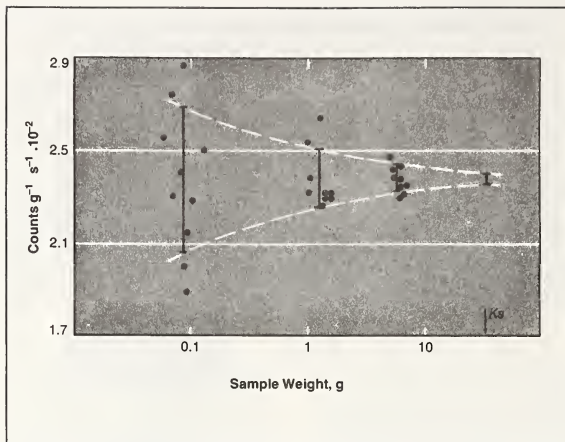
When the properties of a material

Table I. Confidence Intervals and Statistical Tolerance Limits [a]

n	t [b]	$\dfrac{ts}{\sqrt{n}}$ [c]	K [c]	Ks
2	12.70	±18	37.67	±75
4	3.18	±3.2	6.37	±12.9
8	2.36	±1.7	3.73	±7.4
16	2.13	±1.1	2.90	±5.8
32	2.04	±0.7	2.50	±5.0
100	1.98	±0.4	2.23	±4.4
∞	1.96	0	1.96	±4.0

[a] Calculated for s = 2, based on measurement of n samples
[b] 95% confidence limits for the mean of n samples
[c] Based on a 95% confidence that the interval will contain 95% of the samples

Figure 3. Sampling diagram of sodium-24 in human liver homogenate (from Reference 7)

to be sampled are unknown, a good approach is to collect a small number of samples, using experience and intuition as a guide to making them as representative of the population as possible, and analyze for the component of interest. From these preliminary analyses, the standard deviation s_s of the individual samples can be calculated, and confidence limits for the average composition can be established using the relation

$$\mu = \bar{x} \pm ts_s/\sqrt{n} \qquad (1)$$

where μ is the true mean value of the population, $\bar{x}$ is the average of the analytical measurements, and t is obtained from statistical tables for n measurements (often given as $n - 1$ degrees of freedom) at the desired level of confidence, usually 95%. Table I lists some t values; more extensive tables are provided in books on quantitative analysis and statistics (5).

On the basis of this preliminary information, a more refined sampling plan can be devised, as described in the following sections. After one or two cycles the parameters should be known with sufficient confidence that the optimum size and number of the samples can be estimated with a high level of confidence. The savings in sampling and analytical time and costs by optimizing the sampling program can be considerable.

Minimum Size of Individual Increments. Several methods have been developed for estimation of the amount of sample that should be taken in a given increment so as not to exceed a predetermined level of sam-

pling uncertainty. One approach is through use of Ingamells's sampling constant (6). Based on the knowledge that the between-sample standard deviation s_s (Equation 1), decreases as the sample size is increased, Ingamells has shown that the relation

$$WR^2 = K_s \qquad (2)$$

is valid in many situations. In Equation 2, W represents the weight of sample analyzed, R is the relative standard deviation (in percent) of sample composition, and K_s is the sampling constant, corresponding to the weight of sample required to limit the sampling uncertainty to 1% at 68% confidence. The magnitude of K_s may be determined by estimating s_s from a series of measurements of samples of weight W.

Once K_s is evaluated for a given sample, the minimum weight W required for a maximum relative standard deviation of R percent can be readily calculated.

An example of an Ingamells sampling constant diagram is shown in Figure 3 for a human liver sample under study in the National Environmental Specimen Bank Pilot Program at the National Bureau of Standards (NBS) in conjunction with the Environmental Protection Agency (7). A major goal of the program is to evaluate specimen storage under different conditions. This requires analysis of small test portions of individual liver specimens. The material must be sufficiently homogeneous that variability between test portions does not mask small variations in composition owing

to changes during storage. The homogeneity of a liver sample for sodium was assessed by a radiotracer study in which a portion was irradiated, added to the remainder of the specimen, and the material homogenized. Several test portions were then taken and the activity of ^{24}Na measured as an indicator of the distribution of sodium in the samples. From Figure 3 it can be seen that the weight of sample required to yield an inhomogeneity of 1% (± 2.4 counts $g^{-1}s^{-1}$) is about 35 g. For a subsample of one gram, a sampling uncertainty of about 5% can be expected.

Minimum Number of Individual Increments. Unless the population is known to be homogeneous, or unless a representative sample is mandated by some analytical problem, sufficient replicate samples (increments) must be analyzed. To determine the minimum number of sample increments, a sampling variance is first obtained, either from previous information on the bulk material or from measurements made on the samples. The number of samples necessary to achieve a given level of confidence can be estimated from the relation

$$n = \frac{t^2 s_s^2}{R^2 \bar{x}^2} \qquad (3)$$

where t is the student's t-table value for the level of confidence desired, s_s^2 and $\bar{x}$ are estimated from preliminary measurements on or from previous knowledge of the bulk material, and R is the percent relative standard deviation acceptable in the average. Initially t can be set at 1.96 for 95% confidence limits and a preliminary value of n calculated. The t value for this n can then be substituted and the system iterated to constant n. This expression is applicable if the sought-for component is distributed in a positive binomial, or a Gaussian, distribution. Such distributions are characterized by having an average, μ, that is larger than the variance, σ_s^2. Remember that values of σ_s (and s_s) may depend greatly on the size of the individual samples.

Two other distributions that may be encountered, particularly in biological materials, should be mentioned. One is the Poisson distribution, in which the sought-for substance is distributed randomly in the bulk material such that σ_s^2 is approximately equal to μ. In this case

$$n = \frac{t^2}{R^2 \bar{x}} \qquad (4)$$

The other is the negative binomial distribution, in which the sought-for substance occurs in clumps or patches, and σ_s^2 is larger than μ. This pattern often occurs in the spread of contamination or contagion from single

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sources, and is characterized by two factors, the average, $\bar{x}$, and a term, k, called the index of clumping. For this system

$$n = \frac{t^2}{R^2}\left[\frac{1}{\bar{x}} + \frac{1}{k}\right] \qquad (5)$$

Here k must be estimated, along with $\bar{x}$, from preliminary measurements on the system.

Sometimes, what is wanted is not an estimate of the mean but instead the two outer values or limits that contain nearly all of the population values. If we know the mean and standard deviation, then the intervals $\mu \pm 2\sigma$ and $\mu \pm 3\sigma$ contain 95% and 99.7%, respectively, of all samples in the population. Ordinarily, the standard deviation σ is not known but only its estimate s, based on n observations. In this case we may calculate statistical tolerance limits of the form $\bar{x} + Ks$ and $\bar{x} - Ks$, with the factor K chosen so that we may expect the limits to include at least a fraction P of the samples with a stated degree of confidence. Values for the factor K (8) depend upon the probability γ of including the proportion P of the population, and the sample size, n. Some values of K are given in Table I. For example, when $\gamma = 0.95$ and $P = 0.95$, then $K = 3.38$ when $n = 10$, and $K = 37.67$ for duplicates ($n = 2$).

Sampling a Segregated (Stratified) Material. Special care must be taken when assessing the average amount of a substance distributed throughout a bulk material in a nonrandom way. Such materials are said to be segregated. Segregation may be found, for example, in ore bodies, in different production batches in a plant, or in samples where settling is caused by differences in particle size or density.

The procedure for obtaining a valid sample of a stratified material is as follows (9):
• Based on the known or suspected pattern of segregation, divide the material to be sampled into real or imaginary segments (strata).
• Further divide the major strata into real or imaginary subsections and select the required number of samples by chance (preferably with the aid of a table of random numbers).
• If the major strata are not equal in size, the number of samples taken from each stratum should be proportional to the size of the stratum.

In general, it is better to use stratified random sampling rather than unrestricted random sampling, provided the number of strata selected is not so large that only one or two samples can be analyzed from each stratum. By keeping the number of strata sufficiently small that several samples can be taken from each, possible varia-
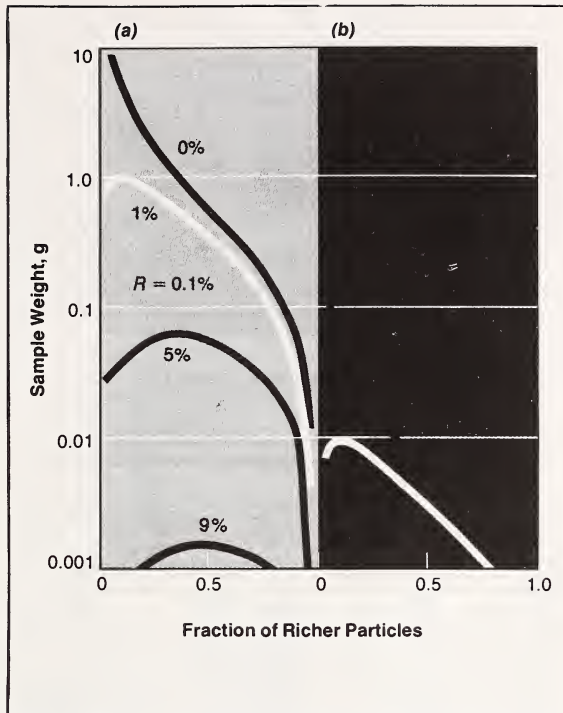
Figure 4. Relation between minimum sample size and fraction of the richer particles in a mixture of two types of spherical particles (diameter 0.1 mm and density 1) for a sampling standard deviation (R) of (a) 0.1% and (b) 1%. Richer particles contain 10% of substance of interest, and leaner ones contain 0, 1, 5, or 9% (after Reference 12, p 554)

tions within the parent population can be detected and assessed without increasing the standard deviation of the sampling step.

Minimum Number of Individual Increments. When a bulk material is highly segregated, a large number of samples must be taken from different segments. A useful guide to estimating the number of samples to be collected is given by Visman (10), who proposed that the variance in sample composition depends on the degree of homogeneity within a given sample increment and the degree of segregation between sample increments according to the relation

$$s_s^2 = A/W + B/n \qquad (6)$$

where s_s^2 is the variance of the average of n samples using a total weight W of sample, and A and B are constants for a given bulk material. A is called a ho-

mogeneity constant, and can be calculated from Ingamells's sampling constant and the average composition by

$$A = 10^4 \bar{x}^2 K_s \qquad (7)$$

Sampling Materials in Discrete Units. If the lot of material under study occurs in discrete units, such as truckloads, drums, bottles, tank cars, or the like, the variance of the analytical result is the sum of three contributions: (1) that from the variance between units in the lot, (2) that from the average variance of sets of samples taken from within one unit, and (3) that from the variance of the analytical operations. The contribution from each depends upon the number of units in the lot and the number of samples taken according to the following relation (9):

$$\sigma_x^2 = \frac{\sigma_b^2}{n_b}\frac{(N - n_b)}{N} + \frac{\sigma_w^2}{n_b n_w} + \frac{\sigma_t^2}{n_t} \qquad (8)$$

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Glossary

Bulk sampling—sampling of a material that does not consist of discrete, identifiable, constant units, but rather of arbitrary, irregular units.

Composite—a sample composed of two or more increments.

Gross sample (also called bulk sample, lot sample)—one or more increments of material taken from a larger quantity (lot) of material for assay or record purposes.

Homogeneity—the degree to which a property or substance is randomly distributed throughout a material. Homogeneity depends on the size of the units under consideration. Thus a mixture of two minerals may be inhomogeneous at the molecular or atomic level, but homogeneous at the particulate level.

Increment—an individual portion of material collected by a single operation of a sampling device, from parts of a lot separated in time or space. Increments may be either tested individually or combined (composited) and tested as a unit.

Individuals—conceivable constituent parts of the population.

Laboratory sample—a sample, intended for testing or analysis, prepared from a gross sample or otherwise obtained. The laboratory sample must retain the composition of the gross sample. Often reduction in particle size is necessary in the course of reducing the quantity.

Lot—a quantity of bulk material of similar composition whose properties are under study.

Population—a generic term denoting any finite or infinite collection of individual things, objects, or events in the broadest concept; an aggregate determined by some property that distinguishes things that do and do not belong.

Reduction—the process of preparing one or more subsamples from a sample.

Sample—a portion of a population or lot. It may consist of an individual or groups of individuals.

Segment—a specifically demarked portion of a lot, either actual or hypothetical.

Strata—segments of a lot that may vary with respect to the property under study.

Subsample—a portion taken from a sample. A laboratory sample may be a subsample of a gross sample; similarly, a test portion may be a subsample of a laboratory sample.

Test portion (also called specimen, test specimen, test unit, aliquot)—That quantity of a material of proper size for measurement of the property of interest. Test portions may be taken from the gross sample directly, but often preliminary operations, such as mixing or further reduction in particle size, are necessary.

where

σ_x^2 = variance of the mean,
σ_b^2 = variance of the units in the lot,
σ_w^2 = average variance of the samples taken from a segment,
σ_t^2 = variance of the analytical operations,
N = number of units in the lot,
n_b = number of randomly selected units sampled,
n_w = number of randomly drawn samples from each unit selected for sampling, and
n_t = total number of analyses, including replicates, run on all samples.

If stratification is known to be absent, then much measurement time and effort can be saved by combining all the samples and mixing thoroughly to produce a composite sample for analysis. Equation 8 is applicable to this situation also. If the units vary significantly in weight or volume, the results for those units should be weighted accordingly.

For homogeneous materials σ_w^2 is zero, and the second term on the right-hand side of Equation 8 drops out. This is the case with many liquids or gases. Also, if all units are sampled, then $n_b = N$ and the first term on the right-hand side of Equation 8 also drops out.

Particle Size in Sampling Particulate Mixtures

Random sampling error may occur even in well-mixed particulate mixtures if the particles differ appreciably in composition and the test portion contains too few of them. The problem is particularly important in trace analysis, where sampling standard deviations may quickly become unacceptably large. The sampling constant diagram of Ingamells and the Visman expression are useful aids for estimating sample size when preliminary information is available. Another approach that can often provide insight is to consider the bulk material as a two-component particulate mixture, with each component containing a different percentage of the analyte of interest (11). To determine the weight of sample required to hold the sampling standard deviation to a preselected level, the first step is to determine the number of particles n. The value of n may be calculated from the relation

$$ n = \left[\frac{d_1 d_2}{\overline{d}^2}\right]^2 \left[\frac{100(P_1 - P_2)}{R\overline{P}}\right]^2 p(1 - p) \tag{9} $$

where d_1 and d_2 are the densities of the two kinds of particles, $\overline{d}$ is the density of the sample, P_1 and P_2 are the percentage compositions of the component of interest in the two kinds of particles, $\overline{P}$ is the overall average composition in percent of the component of interest in the sample, R is the percent relative standard deviation (sampling error) of the sampling operation, and p and $1 - p$ are the fractions of the two kinds of particles in the bulk material. With knowledge of the density, particle diameter, and n, the weight of sample required for a given level of sampling uncertainty can be obtained through the expression, weight = $(4/3)\pi r^3 \overline{d} n$ (assuming spherical particles).

Figure 4 shows the relation between the minimum weight of sample that should be taken and the composition of mixtures containing two kinds of particles, one containing 10% of the sought-for substance and the other 9, 5, 1, or 0%. A density of 1, applicable in the case of many biological materials, is used, along with a particle diameter of 0.1 mm. If half the particles in a mixture contain 10% and the other half 9% of the substance of interest, then a sample of 0.0015 g is required if the sampling standard deviation is to be held to a part per thousand. If the second half contains 5%, a sample of 0.06 g is necessary; if 1%, 0.35 g would be needed. In such mixtures it is the relative difference in composition that is important. The same sample weights would be required if the compositions were 100% and 90, 50, or 10%, or if they were 0.1% and 0.09, 0.05, or 0.01%. The same curves can be used for any relative composition by substitution of x for 10%, and 0.1 x,

0.5 x, and 0.9 x ... the curves corresponding to 1, 5, and 9% in Figure 4. If a standard deviation of 1% is acceptable, the samples can be 100 times smaller than for 0.1%.

An important point illustrated by the figure is that if the fraction of richer particles is small, and the leaner ones contain little or none of the substance of interest, large test portions are required. If a sample of gold ore containing 0.01% gold when ground to 140 mesh (0.1 mm in diameter) consists, say, of only particles of gangue and of pure gold, test portions of 30 g would be required to hold the sampling standard deviation to 1%. (An ore density of 3 is assumed.)

Concluding Comments

Sampling is not simple. It is most important in the worst situations. If the quantities $\bar{x}$, s, K_s, A, and B are known exactly, then calculation of the statistical sampling uncertainty is easy, and the number and size of the samples that should be collected to provide a given precision can be readily determined. But if, as is more usual, these quantities are known only approximately, or perhaps not at all, then preliminary samples and measurements must be taken and on the basis of the results more precise sampling procedures developed. These procedures will ultimately yield a sampling plan that optimizes the quality of the results while holding down time and costs.

Sampling theory cannot replace experience and common sense. Used in concert with these qualities, however, it can yield the most information about the population being sampled with the least cost and effort. All analytical chemists should know enough sampling theory to be able to ask intelligent questions about the samples provided, to take subsamples without introducing additional uncertainty in the results and, if necessary, to plan and perform uncomplicated sampling operations. It is the capability of understanding and executing all phases of analysis that ultimately characterizes the true analytical chemist, even though he or she may possess special expertise in a particular separation or measurement technique.

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Kratochvil   *Taylor*

Byron Kratochvil, professor of chemistry at the University of Alberta, received his BS, MS, and PhD degrees from Iowa State University. His research interests include solvent effects on solute properties and reactions, applications of nonaqueous systems to chemical analysis, and methods for determining ionic solutes.

John K. Taylor, coordinator for quality assurance and voluntary standardization activities at the National Bureau of Standards Center for Analytical Chemistry, received his BS from George Washington University, and his MS and PhD degrees from the University of Maryland. His research interests include electrochemical analysis, refractometry, isotope separations, standard reference materials, and the application of physical methods to chemical analysis.

SYMPOSIUM ON REFERENCE MATERIALS AND THEIR USE IN NUCLEAR FUEL CYCLE

John K. Taylor[1]

Reference Materials—What They Are and How They Should be Used

ABSTRACT: The role of reference materials in monitoring the chemical measurement process is considered. Requirements for reliable reference materials are reviewed. The use of reference material data in estimating the uncertainties of the results of measurements on test samples is discussed.

KEYWORDS: accuracy, chemical analysis, precision, quality assurance, quality control, reference materials, standard reference materials

The increasing requirements for accuracy in chemical analysis and the necessity to interrelate and combine data sets from several laboratories or from the same laboratory over intervals of time have created a demand for well-characterized reference materials (RMs) for quality assurance purposes. When properly used, such materials can provide a high degree of confidence in analytical data.

On the basis of inquiries received and discussions with various analysts, it is clear that RMs are not fully used in some situations and are poorly used in others. It is the purpose of this paper to clarify the role of RMs in the chemical measurement process and to suggest ways in which they may be used to the best advantage.

Role of Reference Materials

An RM is any substance that may be measured simultaneously or sequentially in a measurement process to provide information about the process or the measurements arising therefrom. RMs may be internally developed to monitor a specific measurement process, or they may be provided by an external source. Externally developed reference materials (ERMs) are usually certified by some organization and frequently called certified reference materials (CRMs) [1]. The National Bureau of Standards (NBS) Standard Reference Materials (SRMs) are a special class of CRMs that have been carefully

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[1] Coordinator for quality assurance and voluntary standardization, Center for Analytical Chemistry, National Bureau of Standards, Washington, DC 20234.

analyzed (sometimes with the aid of cooperators) and certified by NBS [2–4]. While the RMs described above may differ in status, each can provide useful information to the analyst for the assessment of data quality.

The only rational basis for use of a RM is as a monitor of a measurement system that is in a state of statistical control [5]. This means that a valid measurement principle has been identified and put into practice using quality control procedures that assure a requisite degree of reproducibility. Indeed, such a measurement process should, conceptually, be capable of producing an infinite population of measurements, some of which at any moment may be considered as a sample. The measurements of the RM may then be considered as random samplings of the output of the measurement system, which would permit their interpretation for evaluation of the measurement process.

Requirements for RMs

RMs of any type must be appropriate in matrix and composition and of stable composition over the intended period of use. They must be sufficiently uniform in composition when subsampled (homogeneous) and available in sufficient quantity to be useful over a reasonable period of time.

CRMs have the further requirement that they must be issued with a certificate in which their measured parameters and assigned uncertainties are fully documented [6]. Internal reference materials (IRMs) must have an equal degree of reliability with respect to stability and homogeneity. The requirement for accuracy of the assigned values of specified parameters of the latter will depend upon the end use of the materials, but this may be of lesser importance than homogeneity in some cases.

Laboratories are well advised to upgrade the accuracy of their IRMs to the highest extent possible. Intercomparisons with high quality CRMs, such as SRMs, can be used to accomplish this purpose.

Interpretation of RM Data

The primary function of IRMs (often called control samples) is to evaluate the attainment of statistical control of the measurement system. As long as such samples are stable and homogeneous in

composition, the precision observed in the analysis of the IRM may be inferred as the precision of the measurement system for that particular measurement. Accordingly, it is clear that stability and uniformity are the prime requirements of such materials and that accurate knowledge of compositions is only a secondary consideration. While such information is highly desirable, the proof of absence of bias using such samples may be difficult to establish based on internally generated evidence alone.

ERMs and CRMs in particular are best used to demonstrate accuracy, that is, the freedom from bias, of measurement systems that are demonstrated to be in a state of statistical control. Because the CRM may be costly or available in limited amounts or both, this latter demonstration is often best left to the use of IRMs. Because of their high quality and the care used in their certification, SRMs often stand at the top of the RM hierachy and, hence, are especially useful to evaluate the accuracy of a measurement process. Needless to say, SRMs should be used in carefully designed test sequences together with IRMs if maximum information is to be provided.

Figure 1 contains a typical sequence in which IRMs and SRMs may be measured together with the test samples to monitor a measurement process. Figure 1 assumes that control charts are maintained [7], the kinds of which are indicated in the "Notes." The control limits of the charts are determined from the results of previous measurements of the IRM. Points on the control charts are plotted immediately after the data are obtained, and they must fall within the control limits, at the decision points, in order to continue the measurements sequence. Otherwise any measurements obtained since the last time the system was known to be in control are suspect and discarded or held in abeyance. Furthermore, the system must

be demonstrated to have regained control before data may again be accepted.

Figure 2 is similar to Fig. 1 but uses duplicate or split samples to monitor statistical control. Control charts based on the differences between the results obtained for the duplicate/split samples are the basis for monitoring statistical control. Such charts are described in several publications [7]. The rationale to be followed at the decision points is essentially the same as described in the discussion of Fig. 1.

No matter what kinds of RMs are used, their ability to monitor the measurement process and especially the measurements in progress must be demonstrated, and this is often a matter of inference. Though statistical control of the measurement system and freedom from bias may be readily demonstrated for the case of measurement of RMs, the performance of the system on measurements of other test samples is the matter of concern. To the extent that the RMs simulate the test samples, the inference drawn from measurement of the former may be transferred to the latter. Conversely, the confidence may diminish as the degree of simulation is decreased. In every case, the experience and professional judgment of the analyst must be used to infer how well an RM monitors the actual measurement process.

RMs may also be used to evaluate the suitability of a proposed method for a special purpose or to determine the performance characteristics of methods under development. Such use of RMs has much the same limitations as in the evaluation of monitoring a process. As stable test samples, RM analyses can provide data on the

Daily/Event Schedule

```
        CALIBRATION - FULL EXPECTED RANGE
*       IRM      ,
        TEST SAMPLES - GROUP 1
*       IRM
        TEST SAMPLES - GROUP 2
*       IRM
          .
*       SRM
          .
        TEST SAMPLES - GROUP N-1
*       IRM
        TEST SAMPLES - GROUP N
*       IRM
*       CALIBRATION - MIDRANGE POINT
              NOTES
*    -  DECISION POINT
1. MAINTAIN CONTROL CHARTS
     X-CONTROL CHART, IRM
     R-CONTROL CHART, ΔIRM
2. SYSTEM MUST BE IN CONTROL AT DECISION POINTS
3. AT LEAST 2 GROUPS: MAXIMUM OF 10 SAMPLES IN EACH GROUP
4. AT LEAST ONE SRM MEASUREMENT SHOULD BE MADE DURING
.  EACH SEQUENCE/DAY
```

FIG. 1—*Quality assessment using IRM samples.*

Sequence Schedule

```
        CALIBRATION - FULL EXPECTED RANGE
*       CALIBRATION CHECK - MIDRANGE POINT
        SAMPLE 1
*       SAMPLE 1 D/S
        SAMPLE 2-9
        SAMPLE 10
*       SAMPLE 10 D/S
*       IRM or SRM
        SAMPLE 11-19
        SAMPLE 20
*       SAMPLE 20 D/S
*       CALIBRATION CHECK - MIDRANGE POINT
*       CALIBRATION CHECK - MIDRANGE POINT/DUPLICATE
                  NOTES
*    *  DECISION POINT
1. MAINTAIN CONTROL CHARTS
     a.  DUPLICATE MIDRANGE CALIBRATION
     b.  DUPLICATE/SPLIT SAMPLE
     c.  X-CONTROL CHARTS, SRM AND IRM
2. SYSTEM MUST BE IN CONTROL AT DECISION POINTS
3. IF MORE THAN 20 SAMPLES, REPEAT SEQUENCE
4. IF LESS THAN 20 SAMPLES, DIVIDE INTO TWO GROUPS AND
     FOLLOW SIMILAR PLAN
5. AT LEAST ONE SRM MEASUREMENT SHOULD BE MADE DURING EACH
     SEQUENCE DAY
```

FIG. 2—*Quality assessment using duplicates/splits.*

precision of a method of measurement. How well this may be transferred to a practical measurement situation, and how well potential biases are evaluated is again a matter of judgment, which may need to be supported by additional information.

Conclusion

Laboratories should refrain from reporting data unless they are in a position to assign uncertainties to the reported values [8]. Such an assignment requires the attainment of statistical control of the measurement system and estimation of the bounds of systematic error. The analysis of reliable RMs in a planned measurement sequence can provide the basis of estimating both the random and systematic components of the measurement uncertainty. However, the assignment of such uncertainties to the test results must be done with due consideration of any matrix differences between the RMs and the test samples. The analysis of high quality ERMs, such as SRMs, together with the laboratory's IRMs (control samples) is the best approach to monitoring a chemical measurement system for quality assurance of the data output.

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Report

John K. Taylor
Center for Analytical Chemistry
National Bureau of Standards
Washington, D.C. 20234

Validation of Analytical Methods

Validation of analytical methods is a subject of considerable interest. Documents such as the "ACS Guidelines for Data Acquisition and Data Quality Evaluation" (1) recommend the use of validated methods. The promulgation of federal environmental regulations requires the inclusion of validated reference methods. Standards-writing organizations spend considerable time in collaborative testing of methods they prepare, validating them in typical applications and determining their performance characteristics. Nevertheless, questions about the appropriateness of methods and the validity of their use in specific situations often arise. Some of these questions may be due to differences in understanding both what a method really is and what the significance of the validation process is. This paper attempts to clarify the nomenclature of analytical methodology and to define the process of validating methods for use in specific situations.

Hierarchy of Methodology

The hierarchy of methodology, proceeding from the general to the specific, may be considered as follows: *technique → method → procedure → protocol.*

A *technique* is a scientific principle that has been found to be useful for providing compositional information; spectrophotometry is an example. Analytical chemists historically have investigated new measurement techniques for their ability to provide novel measurement capability, or to replace or supplement existing methodology. As a result of innovative applications, analysts can now analyze

for myriad substances in exceedingly complex mixtures at ever lower trace levels, with precision and accuracy undreamed of only a few years ago (2).

A *method* is a distinct adaptation of a technique for a selected measurement purpose. The pararosaniline method for measurement of sulfur dioxide is an example. It involves measuring the intensity of a specific dye, the color of which is "bleached" by the gas. Several procedures for carrying out this method may be found in the literature. Modern methodology is

complex and may incorporate several measurement techniques; a method may thus be interdisciplinary.

A *procedure* consists of the written directions necessary to utilize a method. The "standard methods" developed by ASTM and AOAC are, in reality, standardized procedures. ASTM D2914—Standard Test Method for the Sulfur Dioxide Content of the Atmosphere (West–Gaeke Method)—is an example (3). While a precise description is the aim, it is difficult, if not impossible, to describe every de-

Hierarchy of Analytical Methodology

		Definition	Example
Technique		Scientific principle useful for providing compositional information	Spectrophotometry
Method		Distinct adaptation of a technique for a selected measurement purpose	Pararosaniline method for measurement of sulfur dioxide
Procedure		Written directions necessary to use a method	ASTM D2914—Standard Test Method for the Sulfur Dioxide Content of the Atmosphere (West–Gaeke Method)
Protocol		Set of definitive directions that must be followed, without exception, if the analytical results are to be accepted for a given purpose	EPA Reference Method for the Determination of Sulfur Dioxide in the Atmosphere (Pararosaniline Method)

tail of every operation in a procedure. Accordingly, some level of sophistication is presumed for the user of every published procedure; if very sophisticated users are contemplated, only a minimum of detail will be provided and vice versa. However, it should be noted that any omission in the description of critical steps is a potential source of variance or bias, even in the hands of knowledgeable analysts. Because of the flexibility intentionally or unintentionally provided to the analyst, or because of differences in interpretation, it is fair to say that minor-to-major differences of application occur in the use of even the most precisely defined procedures. Such differences often account for the interlaboratory variability observed in many collaborative tests. Further, at some point of departure from a published procedure, a new method results that may need its own validation.

The term **protocol** is the most specific name for a method. A protocol is a set of definitive directions that must be followed, without exception, if the analytical results are to be accepted for a given purpose. Protocols may consist of existing methods or procedures, modifications of such, or they may be developed especially for specific purposes. Typically, they are prescribed by an official body for use in a given situation such as a regulatory process. The EPA Reference Method for the Determination of Sulfur Dioxide in the Atmosphere (Pararosaniline Method) is an example of a protocol (4). The test method specified as part of a contractual arrangement for the acceptance of data or a product or material is another example of a protocol, although it may not be called that in the contract.

A plethora of methods, procedures,

Figure 1. Basic concept of the validation process

and protocols based on the same measurement principle can arise for a given analytical determination. Usually, they are worded differently, and they may contain subtle or major differences in technical details. The extent to which each needs to be individually validated is a matter of professional judgment. It is evident that some validation tests could be merely a matter of experimentally testing the clarity of the written word.

Goals for Validation

Validation is the process of determining the suitability of methodology for providing useful analytical data. This is a value judgment in which the performance parameters of the method are compared with the requirements for the analytical data, as illus-

trated in Figure 1. Obviously a method that is valid in one situation could be invalid in another. Accordingly, the establishment of firm requirements for the data is a prerequisite for method selection and validation. When data requirements are ill-considered, analytical measurement can be unnecessarily expensive if the method chosen is more accurate than required, inadequate if the method is less accurate than required, or utterly futile if the accuracy of the method is unknown.

Fortunately, typical and even standard measurement problems often exist. Examples include a wide variety of clinical analyses, environmental determinations, and recurring measurements for the characterization of industrial products. The kinds of samples for which methods have been val-
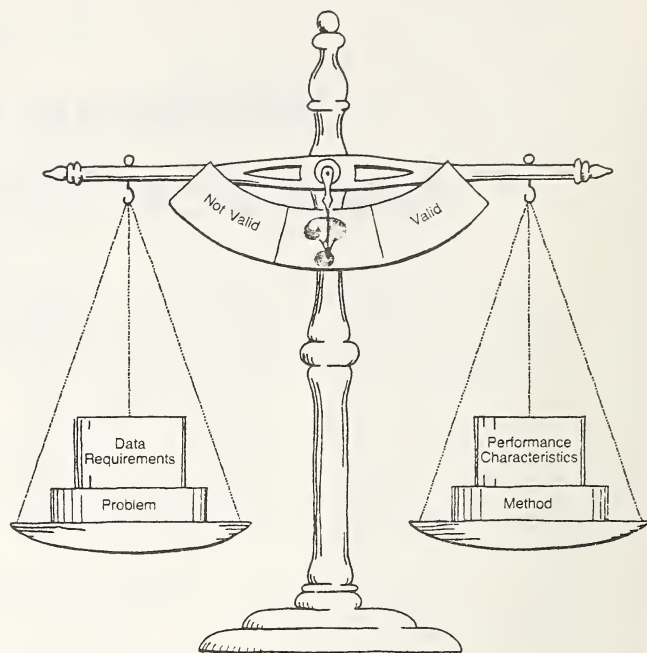
idated should be clearly described, and users should be aware of the need to demonstrate their own abilities to use the method in their own laboratories.

Statements of precision and accuracy are often a result of a validation process, especially in the case of a collaborative test exercise. Such statements are often misinterpreted; they merely describe the results of the exercise and are, at best, estimates of typical performance expectations for the method. They should not be construed to be performance parameters nor should they be used to estimate the uncertainty of any future data obtained by using the method. However, information on precision and accuracy should be obtained to the extent possible since it provides a quantitative basis for judging general performance capability.

Other information useful for characterizing methodology or for judging its suitability for a given use includes: sensitivity to interferences, limits of detection, and useful range of measurement. The specific details for evaluating methodology in these respects are beyond the scope of the present paper. Ordinarily, such information is best obtained as a result of applied research during the method development stage. Because the limit of detection is closely related to the attainable precision at the lower limit of measurement, both the limit of detection and the lowest concentration range measurable (often called limit of quantitation) should be evaluated, as pertinent, in every laboratory (1, 5).

Validation Process

The validation process verifies that the methodology is based on sound technical principles and that it has been reduced to practice for practical measurement purposes. Both the need to validate methodology and the procedure to be followed are matters for professional judgment. The validation can be either general or specific.

General Validation. Validation of measurement techniques depends on the elucidation of the scientific principles upon which they are based. Such validation results from the research of the scientific community, and its soundness is evaluated by peer review. Better understanding of measurement principles can extend their scope and improve the quality of their use. To confirm the above statement, one need only think about the varied research that has contributed to the understanding of the principles of gas chromatography and that has led to development of its status as a prime measurement technique.

Methods arise as the result of applied research, typically by individuals, that often involves both a compre-

hensive understanding of measurement techniques and a high degree of ingenuity and innovation in their application. Testing of the methods in typical practical situations plays a key role in both the development process and in validation. While ordinarily limited in scope, validation at the research stage can be comprehensive and can apply to a wide variety of end uses.

Procedures are developed for the end use of methods in practical analytical situations. The user laboratory ordinarily needs more experimental details than are contained in a published research report of a method to use it in practical measurements. Frequently, as a method gains widespread use, procedures evolve that the users may decide need to be standardized. This is often done by consensus in a standards organization forum. During this process, the resulting standard procedure is examined both technically and editorially. A thorough review process includes collaborative testing in which typical stable test materials are analyzed to verify the procedure's usefulness and to identify both technical and editorial weaknesses. The process is illustrated in Figure 2. If the composition of the reference samples is known, precision and bias, both intra- and interlaboratory, can be evaluated; otherwise, only precision can be evaluated. If a method of known accuracy is available, the collaborative test may consist of its comparison with the candidate method, in which case both precision and bias can be evaluated. The performance parameters of the procedure so evaluated are for the conditions of the collaborative test that are considered typical. Any extension of them to other kinds of samples is by inference only, and may need to be justified. Although it can be time-consuming, the development of a standard method is one of the best ways to validate a procedure because of the breadth of examination that is involved.

A protocol is prescribed by fiat of an organization requiring a specific kind of measurement. Presumably it results from an intelligent decision based on the organization's validation process or that of others. This may consist of an extensive collaborative test or publication of a proposed protocol for public comment. Unfortunately, expediency has overruled sound scientific judgment in some cases, resulting in the promulgation of unvalidated and scientifically defective protocols (6). Protocols that are specified in a contractual arrangement may be selected arbitrarily or through a well-conceived selection process. Verification of their validity for the specific use should be a prime consideration.
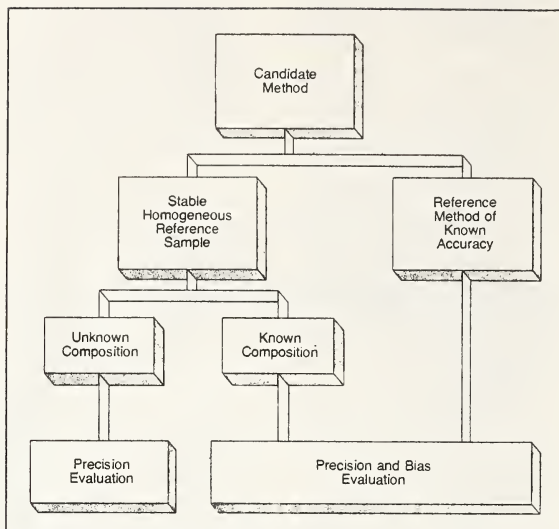
Validation for Specific Use. The

Figure 2. Collaborative test process

ultimate use of analytical methodology is to produce compositional information about specific samples necessary for the solution of particular problems ranging from exotic research investigations to the very mundane. The selection of appropriate measurement methodology is often a major consideration. Methods or procedures, even if previously validated in general terms, cannot unequivocally be assumed to be valid for the situation in hand, because of possible differences in sample matrix and other considerations. Professional analytical chemists traditionally have recognized this and their responsibility to confirm or prove (if necessary) both the validity of the methodology used for specific application (2) and their own ability to reduce it to practice.

The classical validation process is illustrated in Figure 3. When reference samples are available that are similar in all respects to the test samples, the process is very simple: It consists of analyzing a sufficient number of reference samples and comparing the results to the expected or certified values (7). Before or during such an exercise, the analyst must demonstrate the attainment of a state of statistical control of the measurement system (8) so that the results can be relied upon as representative of those expected when using the methodology–measurement system.

When a suitable reference material is not available, several other approaches are possible. One consists of comparing the results of the candidate method with those of another method known to be applicable and reliable, but not useful in the present situation because of cost, unavailability of personnel or equipment, or other reasons. Even the agreement of results with those obtained using any additional independent method can provide some useful information.

Spiked samples and surrogates may be used as reference samples. This approach is less desirable and less satisfactory because of the difficulty in the reliable preparation of such samples and because artificially added materials such as spikes and surrogates may exhibit matrix effects differing from those of natural samples. Split samples of the actual test samples may be used to evaluate the precision of a method or procedure, but they provide no information about the presence or magnitude of any measurement bias.

Another approach is to infer the appropriateness of methodology from measurements on analogous but dissimilar reference materials. The critical professional judgment of the analyst is necessary to decide the validity of the inference.

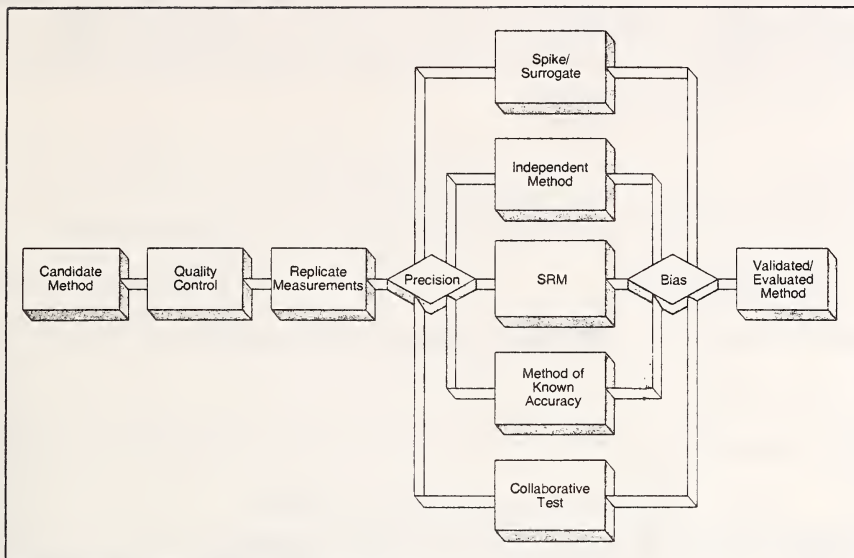In all cases, sufficient tests must be made to evaluate the methodology for

Figure 3. General process for evaluation/validation of methodology

the variety of matrices and ranges of composition expected during the measurement process. Ordinarily, the latter should include three levels of concentration, namely, the extremes and the mid-range of compositions expected. Statistical considerations suggest that at least six degrees of freedom (ordinarily seven measurements) should be involved at each decision point.

Conclusion

A valid method is necessary but not sufficient for the production of valid data. Most methods require a degree of skill on the part of the analyst; this skill constitutes a critical factor in the measurement process. It is common knowledge that data obtained by several laboratories on the same test sample using the same methodology may show a high degree of variability. The alleviation of such a problem is in the area of quality assurance of the measurements (8). Data obtained by a valid method used in a well-designed quality assurance program should allow the assignment of limits of uncertainty that can be used to judge the data's validity.

It should be remembered that the validity of any data will also depend upon the validity of the model and of the sample (8, 9). The model represents the conceptualization of the

problem to be solved, describes the samples that should be analyzed, the data base required, and the way the model will be utilized. Obviously, even flawless measurement data will be of little value if the basic concepts are faulty. Likewise the samples analyzed must be valid if the results obtained for them are to be intelligently interpreted.

The key role of reliable reference materials in the validation of analytical measurements cannot be overemphasized. Their use in validating the methodology has already been discussed. A planned sequential analysis of reference materials in a quality assurance program can assess the quality of the data output and thus validate the overall aspects of the analytical measurement system (7).

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John K. Taylor is coordinator for chemical measurement assurance and voluntary standardization at the National Bureau of Standards' Center for Analytical Chemistry. He received his BS degree from George Washington University and his MS and PhD degrees from the University of Maryland. His research interests include electrochemical analysis, refractometry, isotope separations, standard reference materials, and the application of physical methods to chemical analysis.

4. TITLE AND SUBTITLE

Standard Reference Materials:

Handbook for SRM Users

5. AUTHOR(S)

John K. Taylor

11. ABSTRACT (A 200-word or less factual summary of most significant information. If document includes a significant bibliography or literature survey, mention it here)

This handbook was prepared to provide guidance for the use of Standard Reference Materials (SRM's) to provide an accuracy base for chemical measurements. The general concepts of precision and accuracy are discussed and their realization by quality assurance of the measurement process. General characteristics of SRM's are described and guidance is given for their selection for specific applications. Ways to effectively use SRM's are recommended, utilizing control charts to evaluate and monitor measurement accuracy. Appendices probide statistical guidance on the evaluation of measurement uncertainty.

12. KEY WORDS (Six to twelve entries; alphabetical order; capitalize only proper names; and separate key words by semicolons)

accuracy; calibration; chemical analysis; control charts; measurement uncertainty; precision; quality assurance; Standard Reference Materials; statistical control

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