# NATIONAL BUREAU OF STANDARDS REPORT 8089

PROJECTS and PUBLICATIONS

of the

APPLIED MATHEMATICS DIVISION

A Semiannual Report

January through June 1963



U.S. DEPARTMENT OF COMMERCE NATIONAL BUREAU OF STANDARDS

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# NATIONAL BUREAU OF STANDARDS A. V. Astin, Director



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**NBS PROJECT** 

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8089

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# APPLIED MATHEMATICS DIVISION

January through June 1963

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<sup>°</sup> Only unclassified material is included in this report.



June 30, 1963

### 1. NUMERICAL ANALYSIS

# RESEARCH IN NUMERICAL ANALYSIS AND RELATED FIELDS Task 1101-12-11110/55-55

Origin: NBS Authorized 8/29/54

Manager: Philip J. Davis

Full Task Description: July - September 1954 issue, p. 1

Status: CONTINUED. F. W. J. Olver has completed a paper on error bounds for J. C. P. Miller's algorithm for the computation of functions from recurrence relations. He is now completing an investigation of error bounds for the Hankel asymptotic expansions of Bessel functions of large argument. He has given a series of eight lectures on selected topics in the theory of special functions at the Boulder Laboratories. He has also been advising the mathematics group there on the construction of algorithms for the automatic computation of Bessel functions for complex arguments and complex orders.

A conference on Approximation is being organized by the Society for Industrial and Applied Mathematics to take place for one week during the autumn at Gatlinburg, Tennessee, and F. W. J. Olver is acting as chairman of the Program Committee.

S. Haber continued to work on a survey of the theory of equidistribution mod 1, and on problems of numerical quadrature. He found a new derivation of a family of formulas for numerical integration over  $(-\infty, \infty)$ , which led to a convergence theorem. He proposed a modification of the Monte Carlo method of integration which, it is hoped, will lead to considerably smaller errors in some cases.

Maxine Rockoff has been preparing her work on iterative solutions of certain linear systems for publication.

R. DeMar has strengthened a theorem he had proved earlier concerning the existence of a function in a certain class of entire functions of exponential type which satisfies a set of conditions  $\mathcal{L}_n(f) = a_n$ ;

 $n=0,1,2,\cdots$  for given sequences  $\{f_n\}$  of linear functionals and  $\{a_n\}$  of complex numbers, so that it now applies to more general classes of functions. He also proved a uniqueness theorem for a sequence of linear

functionals whose generating functions are of the form W<sup>n</sup> for some function W regular on a simply connected domain B. The univalence of W on B, which was known to be a necessary condition for the class of entire functions of exponential type whose Borel transforms are regular on the complement of B to be a uniqueness class for these functionals, is shown to be also sufficient. He made some further progress on the problem of determining

conditions on a sequence  $\{a_n\}$  in order that the sequence  $\{\Delta^n f(a_n)\}$ 

of linear functionals have as large a uniqueness class as  $\{\Delta^n f(0)\}$ .

E. C. Johnsen has been investigating the existence of special types of  $v,k,\lambda$  abelian group difference sets (G,D). He has shown that for certain abelian groups G, no difference sets D exist having the inverse multiplier:  $g \to g^{-1}$ ,  $g \in G$ . In particular, when G is cyclic no such difference sets exist. It is known, however, that such difference sets do exist for other abelian groups. Another type which he is investigating consists of those (G,D) where for  $g \in G$ ,  $g \ne D$  if and only if  $g^{-1} \notin D$ . These can only exist for Hadamard design cases, i.e., where v = 4m-1, k = 2m-1,  $\lambda = m-1$ ,  $m \ge 2$  an integer. Some results for this type have been obtained and further results are expected.

#### Publications:

- (1) Packing inequalities for circles. P. Davis. Michigan Journal of Mathematics 10, pp. 25 31, March 1963.
- (2) The invariance of symmetric functions of singular values. M. Marcus and H. Minc (The University of Florida). Pacific Journal of Mathematics 12, No. 1, pp. 327 332, 1962.
- (3) The maximum number of zeros in the powers of an indecomposable matrix.

  M. Marcus and Frank May. Duke Mathematical Journal 29, No. 4,

  pp. 581 588, December 1962.
- (4) Lower bounds to eigenvalues using operator decomposition of the form B\*B. N. W. Bazley and D. W. Fox (Applied Physics Laboratory, Johns Hopkins University). Archive for Rational Mechanics and Analysis 10, 1962.
- (5) Linear operations on matrices. M. Marcus. In manuscript.
- (6) The zeros of infrapolynomials with prescribed values at given points.O. Shisha (with Prof. J. L. Walsh). To appear in the Proceedings of the American Mathematical Society.
- (7) Bounds on ratios of means. O. Shisha (with Dr. G. T. Cargo). Journal of Research NBS, 66B, No. 4, pp. 169 170 (1962).
- (8) Zeros of polynomials and fractional order differences of their coefficients. O. Shisha (with Dr. G. T. Cargo). To appear in the Journal of Mathematical Analysis and Applications.
- (9) The segmental variation of Blaschke products. G. T. Cargo. Duke Mathematical Journal 30, No. 1, pp. 143 150, March 1963.
- (10) Error bounds for first approximations in turning-point problems.

  F. W. J. Olver. To appear in the Journal of the Society for Industrial and Applied Mathematics.
- (11) Error bounds for asymptotic expansions in turning-point problems. F. W. J. Olver. Submitted to a technical journal.
- (12) Error analysis of Miller's recurrence algorithm. F. W. J. Olver. To appear in Mathematics of Computation.
- (13) Uniqueness classes for difference functionals (Abstract). R. F. DeMar. Notices, American Mathematical Society 10, No. 1, p. 91, January 1963.
- (14) On a theorem concerning existence of interpolating functions. R. F. DeMar. Submitted to the Transactions of the American Mathematical Society.

- (15) A uniqueness theorem. R. F. DeMar. To be published in Proceedings of the American Mathematical Society.
- (16) Matrix rational completions satisfying generalized incidence equations. E. C. Johnsen. Submitted to a technical journal.
- (17) The inverse multiplier for Abelian group difference sets. E. C. Johnsen. To appear in the Canadian Journal of Mathematics.

# RESEARCH IN MATHEMATICAL TOPICS APPLICABLE TO NUMERICAL ANALYSIS Task 1101-12-11411/55-56

Origin: NBS Authorized 8/13/54

Sponsor: Office of Naval Research

Manager: Morris Newman

Full Task Description: July - September 1954 issue, p. 5

Status: CONTINUED. M. Newman has continued his investigations of the modular group. He has proved that every normal congruence subgroup of the t x t modular group is a principal congruence subgroup, provided that the level of the group is prime to 6 if t=2 and prime to 2 if t>2. The same result has also been proved for the symplectic modular group.

A complete description of the normal subgroups of genus 1 of the modular group has been given by M. Newman, in terms of certain exponential congruence conditions to be satisfied by certain elements of the group.

M. Newman and J. R. Smart have completed a manuscript entitled "Symplectic modular groups". The principal result of this paper is that if A is symplectic modulo n then there is a B  $\equiv$  A (mod n) such that B is symplectic.

M. Newman and J. Lehner are continuing their study of hyperelliptic subgroups of the modular group.

K. Kloss used the Bendix G-20 computer at Carnegie Institute of Technology to tabulate p(n), the number of partitions of n, modulo  $11^7$  and modulo  $13^7$ , for  $0 < n \le 25,000$ . Auxiliary tables were prepared, listing the numbers  $n \le 25,000$  such that  $13^k \mid p(n)$  or  $11^k \mid p(n)$ , for each positive integer k < 7. It was noted that about 2/11 of the values of p(n) investigated were divisible by 11. Other, shorter, computations of p(n) modulo a power of a prime were made. It was found that there are no primes t with 11 < t < 67 for which a congruence of the form

$$p(mt + k) \equiv 0 \pmod{t}$$

holds for all  $m \ge 0$ .

At the request of M. Newman, K. Kloss investigated the problem: are there any primes  $p \equiv -1 \pmod{12}$  such that  $Q_p = p^2 + p + 1$  is also prime and  $3^p \equiv 1 \pmod{Q_p}$ ? (This is a special case of the well-known conjecture that, if p and q are distinct primes, then  $\frac{p^q-1}{p-1}$  and  $\frac{q^p-1}{q-1}$  have no common factors.)

For each prime p < 500,763, with p  $\equiv$  -1 (mod 12), the Bendix G-20 calculated  $Q_p$  and, if  $Q_p$  was prime, found  $3^p$  (mod  $Q_p$ ). None of the values of p investigated satisfied  $3^p \equiv 1 \pmod{Q_p}$ .

K. Kloss continued to supervise the PILOT computation of the Wilson remainders, defined for primes p by

$$W_{p} = \frac{(p-1)! + 1}{p}$$
,  $0 \le W_{p} < p$ .

The numbers  $\mathbb{W}_p$  are now known for all p < 450,000. The computations are being continued as machine time permits. An extensive amount of work has been done in punching the PILOT output onto cards and preparing the table for possible publication. A completed table, at least for p < 450,000, should be available by September 1.

K. Kloss programmed Vandiver's criterion for the numerical investigation of Fermat's Last Theorem on the Bendix G-20. (See "An Application of High Speed Computing to Fermat's Last Theorem", by H. S. Vandiver et al., Proc. Nat. Acad. Sci. 40 (1954), pp. 25 - 33.) Because of insufficient time, no new results were obtained. The work will be continued using the PILOT computer.

K. Goldberg has continued his investigation of the coefficients in the iterates and powers of  $f(z) = z + a_1 z^2 + a_2 z^3 + \cdots$ . Let  $\pi$  denote the partition  $1 \cdot k_1 + 2 \cdot k_2 + \cdots + n \cdot k_n = n$ , and define the operator  $\psi_{\pi}$  by

$$\psi_{\pi} h_{\pi} = \sum_{n=0}^{\infty} z^{n} \sum_{\sum i, k_{i}=n} h_{\pi} a_{1}^{k_{1}} a_{2}^{k_{2}} \cdots a_{n}^{k_{n}} / k_{1}! k_{2}! \cdots k_{n}!$$

Then 
$$\psi_{\pi}^{-1}\{f(z)/z\}^{s+1}/f'(z) = \sum_{j=0}^{m} (-1)^{j} j! \sigma_{j}(s-j)^{(m-j)}$$
 and 
$$\psi_{\pi}^{-1}\{f^{-1}(z)/z\}^{s+1}/f^{-1}(z) = (-s-n-\delta)^{(m-2)}(s^{2}+s-n^{2}-n+2\sigma_{2})$$
 where  $m = k_{1} + k_{2} + \cdots + k_{n}$  and  $\prod_{j=1}^{n} (1+jt)^{k_{j}} = \sum_{j=0}^{m} \sigma_{j} t^{j}$ .

J. Reed and K. Goldberg are continuing their work in developing a mathematical model of a certain type of human competitive behavior. They have succeeded in randomizing the input and are now concentrating, on achieving an output which can be correlated with actual records.

### Publications:

- (1) Hadamard matrices of order cube plus one. K. Goldberg. In manuscript.
- (2) A recurrence on integral vectors. K. Goldberg. In manuscript.

- (3) The powers of the iterates of a formal power series. K. Goldberg. In manuscript.
- (4) Incidence spaces and algebras. K. Goldberg and E. C. Dade. In manuscript.
- (5) Group generated incidence spaces and applications. K. Goldberg and E. C. Dade. In manuscript.
- (6) Random notes on combinalysis. K. Goldberg. In manuscript.
- (7) A proposed computer based model. K. Goldberg and J. G. Reed. In manuscript.
- (8) The sum of the elements of the powers of a matrix. M. Marcus and M. Newman. Pacific Journal of Mathematics 12, 627 635 (1962).
- (9) Tables of genera of groups of linear fractional transformations. H. Fell, M. Newman, E. Ordman. Journal of Research NBS, 67B, 61 68 (1963).
- (10) A note on modular groups. M. Newman. Proceedings of the American Mathematical Society 14, 124 125 (1963).
- (11) Note on a subgroup of the modular group. M, Newman and J. R. Smart. Proceedings of the American Mathematical Society 14, 102 104 (1963).
- (12) Copositive and completely positive quadratic forms. M. Hall and M. Newman. Proceedings of the Cambridge Philosophical Society 59, 329 339 (1963).
- (13) Bounds for cofactors and arithmetic minima of quadratic forms.

  M. Newman. Journal of the London Mathematical Society 38, 215 217 (1963).
- (14) Modulary groups of t x t matrices. M. Newman and J. R. Smart. Duke Mathematical Journal 30, 253 257 (1963).
- (15) Symplectic modulary groups. M. Newman and J. R. Smart. To appear in Acta Arithmetica.
- (16) Weierstrass points of  $\Gamma$  (n). J. Lehner and M. Newman. To appear in Annals of Mathematics.

### 2. MATHEMATICAL TABLES AND PROGRAMMING RESEARCH

#### MATHEMATICAL TABLES

The following long-range mathematical table projects are being carried in the Computation Laboratory. Progress continues as dictated by the relative priority in the overall program of the Laboratory and by available funds. All of the table projects were inactive during the past quarter because priority was given to the preparation of the forthcoming "Handbook of Mathematical Functions."

1102-40-11112/47-2 TABLES OF COULOMB WAVE FUNCTIONS

1102-40-11112/51-8 TABLES OF POWER POINTS OF ANALYSIS OF VARIANCE TESTS

1102-40-11112/52-37 TABLES OF SPHEROIDAL WAVE FUNCTIONS

1102-40-11112/52-57 TABLES OF THE SIEVERT INTEGRAL

# HANDBOOK OF MATHEMATICAL FUNCTIONS Task 1102-40-11421/57-216

Origin and Sponsor: National Science Foundation Authorized 12/27/56

Manager: Irene A. Stegun

Full task description: October - December 1956 issue, p. 10

Status: CONTINUED. Of the 29 chapters of the volume, page proofs for seven chapters remain to be checked.

# AUTOMATIC CODING Task 1102-12-11120/55-56

Origin: NBS Authorized 9/29/54

Manager: P. Walsh

Full task description: July - September 1954 issue, p. 11

Status: TERMINATED. The development of a stored-program monitor system for the 7090 was abandoned because IBM developed a monitor system and because a disk memory was not acquired. The IBM monitor system IBSYS was obtained, checked out, and placed on a stand-by status. When its imperfections are sufficiently removed it will probably replace the currently used Bell Monitor System. A Cobol compiler was checked out and placed in a ready-for-use status.

#### 3. PROBABILITY AND MATHEMATICAL STATISTICS

# RESEARCH IN PROBABILITY AND MATHEMATICAL STATISTICS Task 1103-12-11131/63-1259

Origin: NBS Authorized 10/1/62

Manager: Joan Raup Rosenblatt

Full task description: July-December 1962 issue, p. 11

Status: CONTINUED.

- (1) Introductory book for physics students. An introductory book on data analysis for college students of physics is to be written by C. Eisenhart and T. A. Willke for the Momentum Books series, published for the Commission on College Physics of the American Association of Physics Teachers by D. Van Nostrand Co. Plans for the preparation of the manuscript are in an early stage. Together with the projected monograph on precision and accuracy (July-December 1962 issue), this project motivates the Laboratory's work on the properties of estimators based on small samples.
- (2) "Practical properties" of statistical techniques. The Laboratory is making an effort to prepare for publication certain materials from the files of unpublished reports and working papers. The first of a series of such publications has appeared: "Tables describing small-sample properties of the mean, median, standard deviation, and other sample statistics in sampling from various distributions", by Churchill Eisenhart, Lola S. Deming, and Celia S. Martin. This publication will make generally available most of the tables announced in three abstracts in the Annals of Mathematical Statistics, 19, pp. 598-600 (1948).

The second of this series of publications is in preparation. Under the title "Miscellaneous studies in probability and statistics: distribution theory, small-sample problems, and occasional tables", it will include "Distribution of the ratio of two F variates having n-1 and n degrees of freedom" by J. M. Cameron and Cyrus Derman, "Some notes on the Cauchy distribution" by Cyrus Derman, "The better one out of two" by E. P. King, "Variance of medians and pseudo-medians" by Mary G. Natrella, and "Probability points of order statistics in random samples of size n from a uniform distribution over (0,1)".

Janace Speckman has completed the first draft of a note on the properties of a measuring procedure in which observations are made until two identical values have been obtained, this duplicated value serving as an estimate of the mean. The mean squared error of such an estimator is compared with the mean squared error of a fixed sample size estimator, the arithmetic mean, when the fixed sample size is taken to be the expected sample size of the estimation process described above, for rounding lattices with several widths and several locations relative to the population mean.

Bruce Hoadley is investigating the properties of various techniques for linear regression and polynomial curve-fitting, under the assumption that the predictor variable is observed with error.

John Van Dyke completed a working paper entitled "Fitting  $y = \beta x$  when the variance depends on x."

John Van Dyke resumed work on the calculation of percentage points for the coverage of tolerance intervals whose expected coverage is specified (Wilks, 1961), for samples from the normal distribution.

Janace Speckman is pursuing the following studies on topics related to the measurement of precision and accuracy for NBS calibration programs.

(i) The robustness of R-charts based on normal distribution theory. With Mary C. Croarkin, she is conducting an empirical-sampling study of the distribution of the range from normal, chi-square, log-normal, and uniform distributions. (ii) The normalizing effect of using various transformations of the sample variance s<sup>2</sup>.

- (3) Design and analysis of experiments. J. M. Cameron prepared a note entitled "Computation of a basis for a vector space and its complement", extending his algorithm for obtaining an orthogonal set of individual degrees of freedom for error.
- (4) Handbook on experimental statistics. The Ordnance Engineering Design Handbook Experimental Statistics, prepared by Mary G. Natrella, has been issued by the Department of the Army. In order to make this handbook available to the public, it is planned that it be published by the NBS. The NBS edition is in press.
- (5) Bibliography. Lola S. Deming has completed the last of a series of bibliographies that deal with various specific subjects in the field of statistics. The preceding six bibliographies of the series gave references for the period 1930 1957. The new one brings up to date, through 1960, each of the subjects: correlation and regression theory; time series; limit theorems; Markov chains and stochastic processes; frequency functions, moments, and graduation; theory of estimation and testing of hypotheses, sampling distributions, and theory of sample surveys.
- Churchill Eisenhart is writing up his historical findings on "The background and evolution of the method of least squares." In this connection he has found that the Principle of the Arithmetic Mean seems to have originated in Western Europe sometime in the latter half of the 16th century A.D., and appears to have evolved from the Method of Reversal for eliminating (or, at least, reducing) the effects of systematic errors, that is, from the technique of taking measurements in pairs such that the two members of a pair are affected by systematic errors of (approximately) equal magnitude but of opposite signs, in which case the arithmetic mean of the pair is (at least, more nearly) free from the effects of these errors.

The earliest implicit instance that he has found of the practice of taking the arithmetic mean of a number of measurements of the same quantity is in William Borough"s A Discourse of the Variation of the Compasse, or Magneticall Needle (1581); the earliest explicit instance is in Henry Gellebrand's A Discourse Mathematical on the Variation of the Magneticall Needle (1635). A very explicit instance is to be found on p. 726 of the Phil. Trans. for 1668. Not until around the middle of the eighteenth century, however, does the practice seem to have become widely (but not universally) followed.

The practice of taking several measurements of a single quantity by the same method under essentially the same circumstances - a necessary precursor to taking the arithmetic mean of such measurements - seems to have originated early in the 16th century A.D. in connection with the efforts of mariners to devise a method for determining the longitude of a ship at sea from observations on the deviation of a compass needle from the true north, termed the variation or declination of the needle, which had been found by Columbus and others to be northeasterly to the east of the Azores, and northwesterly to the west of the Azores.

#### Publications:

- (1) Roger Joseph Boscovich and the combination of observations. Churchill Eisenhart. Actes du Symposium International R. J. Boskovic, 1961, pp. 19 25 (Beograd 1962).
- (2) An algorithm for obtaining an orthogonal set of individual degrees of freedom for error. Joseph M. Cameron. Journal of Research NBS, 67B, 19 22, January March 1963.
- (3) Selected bibliography of statistical literature: supplement, 1958 1960. Lola S. Deming. Journal of Research NBS, 67B, 91 133, April June 1963.
- (4) Tables describing small-sample properties of the mean, median, standard deviation, and other statistics in sampling from various distributions. Churchill Eisenhart, Lola S. Deming, and Celia S. Martin. NBS Technical Note 191, June 1963.
- (5) Ranking laboratories by round-robin tests. W. J. Youden. Materials Research and Standards 3, 9 13, January 1963.
- (6) On the pedestrian queueing problem. George Weiss. Bulletin International Statistical Institute, XXXIX, Part 4, 163 - 168, 1962.
- (7) Realistic evaluation of the precision and accuracy of instrument calibration systems. Churchill Eisenhart. Journal of Research NBS, 67C, 161 187, April June 1963.
- (8) Precision of simultaneous measurement procedures. W. A. Thompson, Jr. Journal of the American Statistical Association, 58, No. 302, 474 479, June 1963.
- (9) Factorial designs and the direct product. Badrig Kurkjian (Harry Diamond Laboratories) and Marvin Zelen. Bulletin International Statistical Institute, XXXIX, Part 2, 509 519, 1962.
- (10) An analysis of pedestrian queueing. George Weiss. To appear in Journal of Research NBS, Section B (Mathematics and Mathematical Physics).
- (11) A note on contingency tables involving zero frequencies and the  $2\overset{\triangle}{1}$  test. H. Ku. To appear in Technometrics.
- (12) On a rank sum test for outliers. W. A. Thompson, Jr. and T. A. Willke. To appear in Biometrika.
- (13) Experimental statistics. Mary G. Natrella. To appear as NBS Handbook 91.

# MEASUREMENT OF RELIABILITY Task 1103-12-11130/56-182

Origin: NBS Authorized 3/23/56

Manager: Joan Raup Rosenblatt

Full task description: January - March 1956 issue, p. 13

Status: CONTINUED. George Weiss has completed a paper on optimal inspection programs for randomly failing equipment. The optimum periodic program is found for a system having an arbitrary reliability function. Such a program has the virtue of simplicity even if it may not be optimal in an absolute sense. Some results on random inspection programs are also given.

#### Publications:

- (1) Confidence limits for the reliability of complex systems. Joan R. Rosenblatt. Statistical Theory of Reliability, pp. 115 148 (edited by Marvin Zelen, The University of Wisconsin Press, Madison), 1963.
- (2) A survey of some mathematical models in the theory of reliability.

  George Weiss. Statistical Theory of Reliability, pp. 3 51 (edited by Marvin Zelen, The University of Wisconsin Press, Madison), 1963.

# HYPERVELOCITY IMPACT Task 1104-12-11418/63-1373

Origin and Sponsor: Applied Physics Laboratory,

Authorized 4/22/63

Johns Hopkins University

Manager: Barry Bernstein

Objective: To analyze for numerical solution the problem of determining the size and shape of cratering in hypervelocity impact of a projectile with a target.

Background: The basic mathematical model for hypervelocity impact is a fluid dynamical one. The assumptions on which this model is based are the usual conservation laws, others based on compressibility data, along with the assumption that there is no elastic or plastic shear, and that the fluid is inviscid. Very few results based on this model are known, and those that do exist are not illuminating. Further, the termination of cratering is of great importance, but no phenomenological model for this process exists.

Status: NEW.

# 4. MATHEMATICAL PHYSICS

# RESEARCH IN MATHEMATICAL PHYSICS AND RELATED FIELDS Task 1104-12-11141/55-57

Origin: NBS Authorized 9/1/54

Manager: W. H. Pell

Full task description: July - September 1954 issue, p. 27

Status: CONTINUED. In connection with its application to the solution of problems in the theory of non-linear ordinary differential equations, A. Ghaffari has been making a comparative study of the stroboscopic method of Minorsky, the Mandelstam-Papalexi (M.P.) method, and the asymptotic methods of Krylov-Bogoliubov-Mitropolsky (K.B.M.). It is seen that:

- (1) The M.P. method and the stroboscopic method are similar and derived directly from the theory of Poincaré. The stroboscopic method, however, transforms the initial nonautonomous system into the autonomous form, while the M.P. method operates directly with the nonautonomous system. As might by expected, the calculating procedure in these two methods is different.
- (2) The K.B.M. approach is, in its final stage, analogous to the stroboscopic method, although the intermediate procedure is different in the two methods.
- (3) The stroboscopic method occupies an intermediate position between the M.P. and K.B.M. methods. It has a common starting point with the M.P. method, while with the K.B.M. approach it has a common algebraic problem at the end of calculations, leading to the determination of the stationary state.
- A. Ghaffari has prepared a manuscript concerning the application of the stroboscopic method to Duffing Equation with viscous damping.
- B. Bernstein and E. A. Kearsley, of Section 6.05, have developed a new theory of elasticity for incompressible materials. In this theory there may be a cross effect between shear and pressure. In 1954, Ericksen (ZAMP 5, 466-489) derived all the deformations which are allowed by an arbitrary isotropic material satisfying the usual equations of incompressible elasticity. Bernstein and Kearsley have shown that, in general, the new theory admits the same deformations.
- L. E. Payne and J. H. Bramble have completed a paper which deals with the effect of errors in the elastic moduli appearing in the Navier equations on bounds for the solutions of these equations subject to appropriate boundary conditions. A byproduct of this research is an interesting theorem regarding the approach of the solution of this boundary value problem to the solution of the problem for an incompressible medium.
- Drs. J. P. Vinti and R. M. Langer have studied methods for measuring or compensating the drag on a manned satellite of the earth. In particular, they have shown that even at relatively low altitudes it is feasible to use external jets to maintain such a satellite in a purely gravitational orbit. With the jets turned off, they have shown that the drag, and thus the air density and the time of passage through perigee, can be measured both by a dynamical method and a static method. They suggest that equipping a manned satellite in this manner would provide a primitive zero-g space laboratory, whose operation would give valuable experience in the design of the large zero-g laboratories of the future.

#### Publications:

- (1) On Rayleigh's nonlinear vibration equation. A. Ghaffari. To appear in the Proceedings of the International Symposium on Non-linear Vibrations, sponsored by the Academy of Sciences of the Ukrainian SSR, Kiev, USSR, September 12 18, 1961.
- (2) Higher approximations with the stroboscopic method. A. Ghaffari. To appear in Proceedings of Second International Conference on Non-linear Vibrations, Warsaw, Poland, September 18 21, 1962.
- (3) Conditions for second order waves in hypo-elasticity. B. Bernstein. Transactions of the Society of Rheology 6, 263 273, 1962.
- (4) A study of stress relaxation with finite strain. B. Bernstein (with E. A. Kearsley and L. Zapas). To appear in the Transactions of the Society of Rheology.
- Pointwise bounds in the first biharmonic boundary value problem.
   L. E. Payne and J. H. Bramble. To appear in the Journal of Mathematics and Physics.
- (6) Error bounds in the pointwise approximation of solutions of elastic plate problems. J. H. Bramble and L. E. Payne. To appear in the Journal of Research NBS, Section B (Mathematics and Mathematical Physics).
- (7) Drag compensation and measurement in manned satellites: feasibility study. R. M. Langer and J. P. Vinti. To appear in the Journal of Research NBS, Section C (Engineering and Instrumentation).

# THEORY OF SATELLITE ORBITS Task 1104-12-11441/62-1166

Origin: NBS Authorized 1/9/62

Sponsor: National Aeronautics and Space Administration

Manager: J. P. Vinti

Full task description: January - March 1962 issue, p. 12

Status: CONTINUED. The analysis of the drag-free motion of an artificial satellite by J. P. Vinti has been continued. Current work is concerned with the study of perturbations of the orbit due to deviations from true oblateness such as equatorial asymmetry.

Vinti's standard orbit is the solution of a separable problem on the motion of a satellite in the gravitational field of an oblate planet with axial and equatorial symmetry. In the case of the earth it accounts for some 99% of the deviation of the earth's gravitational field from sphericity.

For a drag-free orbit the most important forces not accounted for are those arising from the higher zonal harmonics of the planet's field. Vinti has now evolved a scheme for including these effects in the orbit, with specific applications to the third harmonic, which is associated with the pear shape of the earth, and the residual fourth harmonic, which gives rise to the well known critical inclination. The secular and short-periodic effects of this remaining 1% of a spherical deviation are of the second order in the oblateness parameter  $J_2$  and that of the long-periodic effects is of the first order in  $J_2$ .

Although inclusion of these perturbing effects doubles the length of the algorithm for computing the orbit, the algorithm remains much shorter than that of any other method of comparable accuracy.

#### Publications:

- (1) The spheroidal method for satellite orbits. J. P. Vinti. To be published in Proceedings of the International Association of Geodesy.
- (2) The spheroidal method for satellite orbits. J. P. Vinti. Notes, Summer Institute for Dynamical Astronomy, Yale University, July 19, 1962.
- (3) Zonal harmonic perturbations of an accurate reference orbit of an artificial satellite. J. P. Vinti. Submitted to a technical journal.

# PLASMA RESEARCH Task 1104-12-11140/59-422

Origin: NBS Authorized 6/30/59

Manager: C. M. Tchen

Full Task Description: April - June 1959 issue, p. 15

Status: CONTINUED. C. M. Tchen has completed his investigation in the kinetic theory of rapidly varying plasmas and a report has been prepared. He has continued the investigation of the formulation of a kinetic foundation for the theory of turbulence, using the BBGKY method. Two papers were presented by Dr. Tchen at the 6th International Symposium on Ionization Phenomena in Gases, Paris, July 8 - 13, 1963, and he was an invited participant in the 4th International Space Science Symposium, Warsaw, Poland, June 3 - 11, 1963. He also presented lectures on kinetic theories of plasmas and magnetohydrodynamics at the following institutes in Europe: Plasma Physics Institute, Garching, Germany; Institute for High Temperature Research, Technical University, Stuttgart, Germany; Institute for the Structure of Materials, Philipps University, Marburg, Germany; Laboratorium voor Massascheiding, Amsterdam, Netherlands; Institute Battelle, Centre de Recherche de Genève, Geneva, Switzerland.

# DYNAMICS OF PLASMAS Task 1104-12-11417/62-1157

Origin: NBS Authorized 10/3/61

Sponsor: National Aeronautics and Space Administration

Manager: C. M. Tchen

Full Task Description: October - December 1961 issue, p. 12

Status: CONTINUED. C. M. Tchen has continued his investigations in the area of plasma oscillations with collective correlation. Four reports of a preliminary nature have been prepared, as follows:

- (a) Kinetic equation for rapidly varying plasmas
- (b) Diffusion of the correlation function for a plasma
- (c) Approximate theory on the collective correlation of plasmas
- (d) Plasma oscillations with collective correlations

Report (a) is concerned with the derivation of a kinetic equation for a plasma, in the form of a generalized Fokker-Planck equation, including the effects of "memory", so that it is applicable to rapidly varying processes. The dielectric property of the plasma was found to depend on the time varying distribution function and on a memory effect. The result may be applied to the calculation of the transport properties of plasma with high frequencies.

Report (b) considered the temporal development of the shielding process from an initial distribution into the equilibrium Debye-Hückel distribution. The result finds its applications in plasmas with unsteady correlations.

Report (c) extended the work of report (b) to include the collective behavior. The approximation referred to in the title was based on the transformation of the collective equation into a non-collective form.

In report (d) the longitudinal oscillations were investigated by including the effects of correlations. Since it is the collective behavior which sets up the oscillations, its role both in the singlet distribution function and the pair correlation function was investigated.

- C. M. Tchen and W. L. Sadowski have begun work in the direction of numerical solution of the non-linear Vlasov equation for a plasma. This investigation will be carried out on the IBM 7090 at NBS. They have recently visited the Plasma Physics Institute at Garching, Germany. A program which they have written was put on the 7090 of the Institute. The results and the code are being sent to NBS.
- C. M. Tchen presented two papers entitled "Plasma oscillations with collective correlations" and "Interaction of a plasma source with a uniform magnetic field", at the 6th International Symposium on Ionization Phenomena in Gases, Paris, July 8 13, 1963. He also was invited to, and participated in, the 4th International Space Science Symposium, Warsaw, Poland, June 3 11, 1963. Between these meetings, Dr. Tchen presented the following lectures:
- (1) "Kinetic Problems in Plasmas", Plasma Physics Institute, Garching, Germany, June 18, 1963.
- (2) "Kinetic Equation and Landau Damping", Institute for High Temperature Research, Technical University, Stuttgart, Germany, June 19, 1963.
- (3) "Kinetic Equations of Plasmas", Institute for the Structure of Materials, Philipps University, Marburg, Germany, June 21, 1963.
- (4) "Interaction of Plasma Flows with Magnetic Fields", Laboratorium voor Massascheiding, Amsterdam, Netherlands, June 24, 1963.
- (5) "Kinetic Theories of Plasmas", Institute Battelle, Centre de Recherche de Genève, Geneva, Switzerland, June 28, 1963.

#### Publication:

(1) Collective correlation of plasmas. C. M. Tchen. Czechoslovak Journal of Physics 12, 516 - 521 (1962).

# 5. OPERATIONS RESEARCH

# OPERATIONS RESEARCH Task 1105-12-11115/61-546

Origin and Sponsor: NBS Authorized 12/30/60

Manager: Alan J. Goldman

Full task description: October - December 1960 issue, p. 3

Status: CONTINUED. The following investigations in various fields of operations research were carried out by members of the staff:

- (1) C. Witzgall and A. J. Goldman continued investigating mathematical models of distribution networks. C. Witzgall studied several specific models, and topics in mathematical programming and topology, related to optimal location of a processing facility. The dual problem was shown in some cases to be of quadratic programming type.
- (2) J. Levy and W. Sillars investigated the effects of buffer capacity in a simple flow system. P. Meyers carried out a simulation study of a stochastic sorting process, and numerical studies of alternative policies for encoding information to be used in classification.
- (3) H. Fell and J. Mather investigated topics in linear algebras. A conjecture of D. Kleinman, that any number in (0,1) has an initial repeating block of digits in its representation to some base, was proved numerically using only bases ≤ 50.
- (4) J. Levy and A. J. Goldman (with W. G. Hall and S. Peavy of 11.02) participated in a Commerce Department analysis of a proposed transportation activity. L. S. Joel and A. J. Goldman (with D. Labovitz of 12.05) assisted the Interagency Committee on Oceanography in connection with an operations research study.
- (5) A. J. Goldman continued collaboration with M. Zelen (Mathematics Research Center, U. of Wisconsin) on a paper dealing with least squares estimation.

### Publications:

- (1) Maximal cellular Boolean functions. A. J. Goldman and B. K. Bender. Journal of Research NBS, 67B, pp. 77 84 (1963).
- (2) Recognition of completely mixed games. A. J. Goldman. Journal of Research NBS, 67B, pp. 23 29 (1963).
- (3) Review of "Systems: Research and Design." A. J. Goldman. Technometrics 5, pp. 130 131 (1963).

# AIR DEFENSE Task 1105-12-11415/61-544

Origin and Sponsor: U. S. Army Air Defense Command Authorized 9/30/61

Manager: Lambert S. Joel

Full Task Description: July - September 1961 issue, p. 13

Status: TERMINATED. L. S. Joel (with J. Beiman and W. G. Hall, 11.02) completed the computer program for the first simulation model. A. J. Goldman examined some related mathematical problems.

# COMBINATORIAL MATHEMATICS Task 1105-12-11455/62-1205

Origin: NBS Authorized 5/2/62

Sponsor: Office of Naval Research

Manager: Jack Edmonds

Full task description: April - June 1962 issue, p. 15

Status: CONTINUED. J. Edmonds completed papers (1) on an algorithm for matching, (2) on a polyhedron with 0,1-vertices, and (3) on the surface duality of graphs.

Paper (2) contains a theorem (generalizing the Birkhoff-von Neumann theorem) which describes the convex hull of the vectors of zeroes and ones associated with the matchings in a given arbitrary graph. The theorem is virtually the first of its kind--in that the convex hull is not the one suggested directly by the combinatorial problem.

Edmonds extended the matching theory to "optimum degree-constrained subgraphs": in a graph G with integer capacities  $\mathbf{d}_i$  at its nodes  $\mathbf{v}_i$  and numerical weights on its edges, find a subgraph H of G such that the weightsum of the edges in H is maximum and such that H contains no more than  $\mathbf{d}_i$  edges meeting node  $\mathbf{v}_i$ . A good algorithm is found. So far, this problem is unique among types of "integer programs" in being found to have an algorithm whose difficulty increases only algebraically rather than exponentially with the size of the graph G.

Witzgall and Zahn developed a modification of the algorithm for determining maximum-cardinality matchings of graphs which facilitates computer implementation and provides additional theoretical insight. Witzgall has coded the modified algorithm for the 7090 computer and codechecking problems were successfully run.

J. Mather presented at the Princeton Graph and Combinatorics Conference a classification of "The planar immersions of a graph."

While at Princeton this academic year, Edmonds directed (1) the weekly "Combinatorial problems and games seminar" and (2) a 3-day "Graph and Combinatorics Conference." The conference, attended by a hundred mathematicians from the U.S. and Canada, was devoted strictly to current research in combinatorial mathematics. Twenty invited papers were presented. Abstracts of these will be included in a Princeton Logistics Project report to the Office of Naval Research.

#### 6. MATHEMATICAL AND COMPUTATIONAL SERVICES

1102-40-11645/56-0166 SCF-LCAO SOLUTION OF SOME HYDRIDES Origin and Sponsor: NBS, Section 5.9 (now in Division 15)

Manager: P. J. Walsh

Full task description: January - March 1956 issue, p. 27

Status: CONTINUED. Work has been initiated to re-write the self-consistent-field programs. A new super-matrix program was completed by J. D. Waggoner. When the control program is re-written to avoid having to use a compatibility program, the speed of the overall routine will be greatly increased by all the modifications. Useful results that have been obtained with the present programs include approximate Hartree-Fock results for BH, CH, CH<sub>2</sub>, He, H<sub>2</sub>,  $CH_4$ ,  $NH_4^+$ , and  $BH_4^-$ .

1102-40-11645/56-0186 MECHANICAL MEASUREMENTS OF GAGE BLOCKS

Origin and Sponsor: NBS, Section 2.5

Manager: B. S. Prusch

Full task description: July - September 1956 issue, p. 33

Status: CONTINUED. Computations were performed for the checking of 36

laboratory sets of gage blocks.

1102-40-11647/58-0266 DEPOLYMERIZATION PROCESSES

Origin and Sponsor: NBS, Section 7.6

Manager: Maxine L. Rockoff

Full task description: July - September 1957 issue, p. 36 Status: CONTINUED. Results are being analyzed by sponsor.

1102-40-11645/58-0339 COMPUTATION OF VISCOELASTICITY PROPERTIES OF MATERIALS

Origin and Sponsor: NBS, Section 3.4

Manager: H. Oser

Full task description: January - March 1958 issue, p. 38

Status: CONTINUED. A paper entitled "Effect of molecular weight on viscoelasticity properties of polymers as predicted by a molecular theory", written together with R. S. Marvin (6.05), appeared in the April - June

issue of the Journal of Research NBS, 67B, pp. 87 - 90.

1102-40-11645/58-0366 RADIATION PATTERNS OF ANTENNAS

Origin and Sponsor: U. S. Information Agency, Department of State

Manager: P. J. Walsh

Full task description: April - June 1958 issue, p. 35

Status: REACTIVATED. Runs will be continued under sponsors' direction.

1102-40-11645/60-0476 GAS TUBE CHARACTERISTICS, II

Origin and Sponsor: Diamond Ordnance Fuze Laboratories

Manager: H. Oser

Full task description: October - December 1959 issue, p. 30

Status: CONTINUED. Program is run by sponsor.

1102-40-11645/60-0486 MORSE WAVE FUNCTIONS AND FRANCK-CONDON FACTORS

Origin and Sponsor: NBS, Section 3.0

Manager: Ruth Zucker

Full task description: January - March 1960 issue, p. 28

Status: CONTINUED. Production runs were made and results submitted to

the sponsor.

1102-40-11645/60-0513 RADIATIVE ENVELOPES OF MODEL STARS

Origin and Sponsor: National Aeronautics and Space Administration

Managers: P. J. Walsh and S. Haber (11.1)

Full task description: July - September 1960 issue, p. 23

Status: INACTIVE

1102-40-11645/61-0532 CALCULATION OF VIBRATIONAL ENERGY LEVELS FOR IONIC MOLECULES

Origin and Sponsor: Georgetown University

Managers: H. Oser and P. Walsh

Full task description: Oct.-Dec. 1960 issue, p. 21

New Objective: To determine with a precision of at least six decimals, the eigenvalues of the Schrödinger equation  $y'' + \lambda(E - V)y = 0$ , where  $\lambda$  is a constant, E the unknown eigenvalue and V(x) the Heitler-London potential. Both the ground state J=2 and the first rotational level J=4 are to be considered.

Status: REACTIVATED. Due to the properties of the H-L potential, the solution with  $y(0) = y(\infty) = 0$  shows enormous exponential rise on the left of the first turning point and to a lesser degree an exponential decay on the right of the second turning point. The changes in the order of magnitude are so great that they cannot be accommodated by conventional computers.

The following procedure was therefore used: Starting at x = x, which lies between zero and the first turning point, with y(x) = 0, y'(x) = 1, we integrate numerically to a point  $x_1$  near the minimum of V(x). Then, starting at  $x_2$  on the right of the second turning point, with the values  $y(x_2) = 0$ ,  $y'(x_2) = -1$ , we integrate again to  $x_1$ . The quantity

$$Q = \frac{y(x_1 - 0)}{y'(x_1 - 0)} - \frac{y(x_1 + 0)}{y'(x_1 + 0)}$$

is then computed for two different approximate values of E close to the expected eigenvalue. With the secant method, the eigenvalue is successively improved until the desired precision is reached.

The computations are then repeated with  $x_1$  moved further left, and  $x_2$  further right until there is no influence on the value E any more. Literature: H. Harrison and R. B. Bernstein: Iterative method for the one-dimensional wave equation... J. Chem. Phys. 38, No. 9, 1963, pp. 2135-2143.

1102-40-11645/61-0538 SPECTRAL REFLECTANCE

Origin and Sponsor: NBS, Section 9.4

Managers: S. Haber (11.1) and P. J. Walsh

Full task description: October - December 1960 issue, p. 23

Status: CONTINUED.

1102-40-11645/62-1009 MONTE CARLO NEUTRON STUDIES

Origin and Sponsor: NBS, Section 4.3

Manager: Sally T. Peavy

Full task description: April - June 1961 issue, p. 21

Status: COMPLETED.

1102-40-11647/62-1022 CALCULATIONS FOR SPECTRUM OF DIPOLE RADIATION

Origin and Sponsor: Naval Research Laboratory

Manager: R. J. Arms

Full task description: April - June 1958 issue, p. 33

Status: CONTINUED. There has been some activity in this project. Code

checking of a new program is under way.

1102-40-11645/62-1027 NEW SYSTEM

Origin and Sponsor: NBS, Section 11.2

Manager: R. J. Herbold

Full task description: July - September 1961 issue, p. 22

Status: CONTINUED. The IBM system (IBSYS) was obtained and several experimental runs were made. IBSYS consists of one supervisory system which handles one or more subsystems. The subsystems are Fortran II monitor, IBJOB and SORT, to mention three.

IBJOB, a new system developed by IBM, consists of Fortran IV, COBOL, Loader and MAP systems. Since IBJOB uses blocking technique when writing out the output, the 1410 tape-to-printer program has been modified to accommodate this.

Simple COBOL and Fortran IV programs were assembled and executed.

Studies are being made on how IBSYS should be used at the NBS computer facilities. Literature on various systems operating under IBSYS are being obtained and distributed. An accounting program has been incorporated into the IBSYS system.

Coding has been started on a supervisory program to handle OMNITAB runs, i.e., put OMNITAB program on the IBSYS tape.

Studies are being made on how the Bell system produced object decks can be run under IBSYS.

### 1102-40-11645/62-1030 ELECTROCARIOGRAPHIC ANALYSIS

Origin: NBS, Section 12.5

Sponsor: Veterans Administration

Full task description: April - June 1959, p. 29

Status: CONTINUED. Production runs, coding of new programs and modifi-

cations of old programs are being done as directed by the sponsor.

### 1101-12-11416/62-1091 BOUNDS FOR EIGENVALUES

Origin: Wright Patterson AFB

Manager: H. Oser

Full task description: October - December 1961 issue, p. 4

Status: CONTINUED. Work on Legendre's differential equation continued.

The applicability of Bazley and Fox's method to other differential operators

is currently under study.

### 1102-40-11647/62-1130 FALLOUT SHELTER COMPUTATIONS

Origin and Sponsor: Office of Civil Defense

Manager: D. I. Mittleman

Full task description: October - December 1961 issue, p. 25

Status: CONTINUED. A few special summaries were run.

### 1102-40-11647/62-1155 MORTGAGE LOAN SURVEY

Origin and Sponsor: Federal Home Loan Bank Board

Manager: Ruth Zucker

Full task description: January - March 1962 issue, p. 24

Status: CONTINUED. Production runs continued under direction of sponsor.

### 1102-40-11647/62-1178 LOGARITHMIC COEFFICIENTS

Origin and Sponsor: NBS, Section 5.3

Manager: R. J. Arms

Full task description: January - March 1962 issue, p. 27

Status: INACTIVE.

# 1102-40-11647/62-1179 CATALOGUE INFORMATION

Origin and Sponsor: Diamond Ordnance Fuze Laboratories

Manager: Ruth Varner

Full task description: January - March 1962 issue, p. 27

Status: CONTINUED. Additional work on the problem is being carried out

by the sponsor.

1102-40-11647/62-1182 FOURIER INTEGRAL

Origin and Sponsor: Diamond Ordnance Fuze Laboratories

Manager: H. Oser

Full task description: April - June 1962 issue, p. 25 Status: CONTINUED. Program is being run by sponsor.

1102-40-11647/62-1189 SEQUENTIAL METHODS TABLES

Origin and Sponsor: Quartermaster Research and Engineering Field

Evaluation Agency, U. S. Army

Manager: R. J. Arms

Full task description: April - June 1962 issue, p. 26

Status: Continued. It is expected that the project will be completed

before the end of June 1963.

1102-40-11647/62-1193 SOLUTION TO SECOND ORDER PARTIAL DIFFERENTIAL ELLIPTIC EQUATION

Origin and Sponsor: NBS, Section 3.08

Manager: P. J. Walsh

Full task description: April - June 1962 issue, p. 28

Status: CONTINUED. Production rums were made for different values of C and K, using the third version of the problem. The results have been

submitted to the sponsor.

 $1102-40-11647/62-1196 \quad \text{HEAT OF ADSORPTION} \\$ 

Origin and Sponsor: NBS, Section 15.2

Manager: Ruth Varner

Full task description: April - June 1962 issue, p. 29

Status: CONTINUED. All results have been transmitted to the sponsor who

will carry out any further calculations needed.

1102-40-11647/62-1201 UHF-TV

Origin and Sponsor: Federal Communications Commission

Manager: W. Hall

Full task description: April - June 1962 issue, p. 29

Status: COMPLETED.

1102-40-11647/62-1203 CYLINDRICAL SHOCK WAVE

Origin and Sponsor: NBS, Section 3.7 Managers: Sally Peavy and S. Haber

Full task description: April - June 1962 issue, p. 30

Status: CONTINUED. All the subroutines are checked except the one which

computes the inner boundary condition.

1102-40-11647/62-1212 COLOR DIFFERENCES Origin and Sponsor: NBS, Section 10.9

Manager: J. D. Waggoner

Full task description: April - June 1962 issue, p. 33

Status: INACTIVE. Some revisions were made in the original program, and

are being checked out.

1102-40-11647/63-1219 SHOCK TUBE DATA

Origin and Sponsor: Diamond Ordnance Fuze Laboratories

Manager: L. Joseph

Full task description: July - December 1962 issue, p. 32

Status: INACTIVE.

1102-40-11647/63-1223 CARDIOVASCULAR DYNAMICS

Origin and Sponsor: Univ. of Pennsylvania, Bockus Research Institute

Manager: M. Rockoff

Full task description: July - December 1962 issue, p. 32

Status: INACTIVE.

1102-40-11647/63-1240 SECRET SERVICE FORGERY PROJECT

Origin and Sponsor: Treasury Department, U. S. Secret Service

Manager: M. Paulsen

Full task description: July - December 1962 issue, p. 33

Status: CONTINUED. A production run was made in January which yielded so much output that the S.S. decided they would have to made certain changes in their classification rules, and this may necessitate changes in the computer program. This run gave the S.S. information that identified a multiple-check case where there were sacks of mail stolen in Cincinnati. Some of the Government checks were forged there and others in St. Louis, which is something they had not suspected.

1102-40-11647/63-1258 SPECTRAL ANALYSIS Origin and Sponsor: NBS, Section 15.03

Manager: H. Oser

Full task description: July - December 1962 issue, p. 33

Status: INACTIVE

1102-40-11647/63-1260 DENTAL RESEARCH Origin and Sponsor: NBS, Section 7.8

Manager: H. Oser

Full task description: July - December 1962 issue, p. 34

Status: COMPLETED. Project proved to be not feasible in its present

formulation.

1102-40-11647/63-1273 CRYSTAL GROWTH Origin and Sponsor: NBS, Section 8.5

Manager: J. Quinones

Full task description: July - December 1962 issue, p. 34

Status: COMPLETED. Further results will be reported under task 63-1319.

1102-40-11647/63-1275 SECURITIES MARKET STUDY

Origin and Sponsor: Securities and Exchange Commission

Managers: I. A. Stegun and Ruth Zucker

Full task description: July - December 1962 issue, p. 35

Status: COMPLETED. Results transmitted to sponsor.

1102-40-11647/63-1319 SOLUTION OF BIQUADRATIC AND BICUBIC EQUATIONS
Origin and Sponsor: NBS, Section 6.1 Authorized 1/24/63

Manager: Louis Joseph

Objective: To find the roots of the following two equations:

(1)  $Ez^4 + Fz^2 + G = 0$ , (2)  $Ay^8 + By^4 + Cy^2 + D = 0$  for various values of the complex coefficients A, B, C, D, E, F, and G.

Background: Equation (1) is a quadratic in  $z^2$  while Equation (2) is a cubic in  $y^2$ . Thus the equations can be solved using standard formulas for solution of quadratic and cubic equations, respectively, and then taking the square root.

Status: NEW. COMPLETED. A FORTRAN program was written to solve the equations. Production runs were made and results given to the sponsor.

1102-40-11647/63-1335 MATRIX OF POLYNOMIALS

Authorized 3/29/63

Origin and Sponsor: NBS, Section 13.1

Manager: Ruth Zucker

Objective: A program was written to evaluate

$$\alpha_{ij} = \frac{2}{N\pi} \sum_{n=0}^{M} (2n + 1) H_n(x_i) \Phi_n(r_j) \quad i \neq 0$$

$$\alpha_{\rm oj} + \frac{1}{N\pi} \sum_{n=0}^{M} (-1)^n (2n + 1) \, \hat{\phi}_n (r_j) \, M = 2, 6$$

where 
$$x_i = \frac{i}{N}$$
  $r_j = \frac{j}{N}$  i,  $j = 0, \dots, N-1$ 

$$\Phi_{n}(r) = P_{n}(2r^{2} - 1), \qquad P_{n}(t) \text{ is the Legendre Polynomial}$$

$$H_n(x) = \frac{\sin [(2n + 1) \arccos x]}{\sqrt{1-x^2}}$$

for given values of N and M.

Background: The above was written as a subroutine so the sponsor could use it readily as part of his larger program which dealt with the solution of Abel's Integral equation. The solution is necessary for reduction in plasma - arc spectroscopic data.

The problem was transmitted by John R. Solarski. (13.01) Status: NEW.

1102-40-11647/63-1341 LINE WIDTHS

Authorized 6/7/63

Origin and Sponsor: NBS, Section 13.2

Manager: Maxine Paulsen

Objective: The most tedious and most time consuming stage in the calculation involves finding a particular root of a somewhat complicated expression. This can be done with existing tabulated functions and trial and error procedures. Since in a typical calculation one may have several hundred of these equations to solve the calculations are hardly worth the time involved.

The objective was to have the computer solve these equations. Since several hundred equations can be solved in a few minutes on the computer, the major drawback to making these rather detailed calculations would be removed. With such a program it is feasible to investigate the detailed predictions of the theory for a wide choice of molecular constants and, if desired, over a range of temperatures.

Background: Anderson has developed a theory for pressure broadening of gases in the infrared region of the spectrum. The theory is applicable to both self broadening and foreign gas broadening. Detailed comparisons between the theory and experiment have not been too frequent, however, as the theoretical predictions involve a large amount of rather tedious numerical computation.

Status: NEW. The code was written, checked out, and the sponsor is now using it for production runs.

1102-40-11647/63-1352 NEAR NATIONAL EMERGENCY ALARM REPEATER

Origin and Sponsor: OCD Authorized 4/29/63

Manager: Louis Joseph

Objective: Computation Laboratory is serving as a consultant to the Office of Civil Defense in helping to evaluate work previously done at Midwest Research Institute.

Background: The NEAR (National Emergency Alarm Repeater) system is an emergency warning system that utilizes electrical power networks to transmit the alarm signal. Midwest Research Institute has been investigating methods of determining requirements for NEAR signal generators.

Status: NEW.

1102-40-11647/63-1355 STUDY OF ELECTRONIC ENERGY BANDS IN THE RUTILE CRYSTAL Authorized 4/2/63

Origin and Sponsor: NBS, Section 13.4

Managers: P. Walsh and A. Gregg

Objective: To compute the energy matrices of rutile crystals and to diagonalize them.

Background: This is a theoretical study of the electronic energy bands in the rutile crystal (TiO<sub>2</sub>). The Bloch functions are represented by linear combinations of atomic orbitals (LCAO). The energy matrices are then formed from the LCAO functions.

Status: The program for generating energy matrices is written and code checking has been started. A standard subroutine for diagonalizing the symmetric energy matrices will be used.

1102-40-11647/63-1364 Baf ELEMENT RESPONSE TIME BARIUM FLORIDE

Origin and Sponsor: NBS, Section 14.4 Authorized 5/17/63

Manager: Maxine Paulsen

Objective: The objective of the computer program was to provide an analysis of the paper tape data. An empirical equation was to be used to determine the first, second, and third differences (ratios of these differences were to be calculated) of indicated relative humidity with respect to time from which the response time of the hygrometer element could be inferred. Background: As part of a program of research and development on electric hygrometer elements, ten thin film hygrometer elements were mounted on radiosondes and sent aloft on balloons to make measurements of relative humidity in the atmosphere. The radiosonde transmitted a signal of audio frequency which varied with the electrical resistance of the hygrometer element and, therefore, with the ambient relative humidity. The transmitted signal was recorded by a pen recorder and by a magnetic tape recorder. The magnetic tape recorder data had been analyzed and a frequency "count" for each half second of time during each balloon flight was printed out on paper tape.

Status: NEW. The code was written, checked out, and the results of the production run were given to the sponsor.

1102-40-11647/63-1368 HEART DISEASE CONTROL

Authorized 4/11/63

Origin and Sponsor: Public Health Service

Manager: Sally Peavy

Objective: Nutrients are needed for tabulating nutrient contents of food in every day diets. Although tables may exist itemizing the nutrient content of each food, it is a laborious task to tabulate consumption of individuals. To help solve the problem, a computer program can be formulated to do a table retrieval and compute the consumption of each nutrient for individuals.

Background: In epidemiologic studies nutrients are used as a factor to differentiate between normal and diseased cardiac subjects.

Status: NEW. A program is in the process of being written.

1102-40-11647/63-1377 WHISKER GROWTH IN A VAPOR ATMOSPHERE

Origin and Sponsor: NBS, Section 8.5 Authorized 6/27/63

Managers: H. Oser and J. A. Simmons (8.5)

Objective: To find the solution of the following partial differential

equation:

$$D \frac{\partial^2 u}{\partial x^2} + M = \frac{\partial u}{\partial t} + \frac{T}{u} \qquad 0 \le x \le x (t)$$

under the boundary conditions:

$$u \equiv 0$$
 for  $x > x(t)$  (moving boundary)

$$\frac{\partial u}{\partial x} = 0$$
 at  $x = 0$ ,

the initial condition:

$$u(x,0) = 0$$
 for all x,

and the conditions for the boundary x(t):

$$\frac{dx(t)}{dt} = -\frac{D}{C} \frac{\partial u}{\partial x} \Big|_{x=x(t)} t > 0$$

$$x(0) = \ell \qquad x(t) > 0 \qquad t > 0$$

Background: The equations above describe the temporal growth of a one-dimensional crystal whisker, where D is the linear diffusion coefficient for the transport of material to the end of the whisker, T is a characteristic time which governs the evaporation of deposited material back into the vapor atmosphere and  $\alpha$  relates the rate of deposition at the end of the whisker to the rate of growth of the whisker tip. N is the deposition rate of atoms which are captured on the surface where they begin to tiffuse towards the tip.

Status: NEW. The problem has been analyzed and transformed into a system of two non-linear integral equations. Using asymptotic relations, which can be derived easily from the integral form, starting values are found which lead to a stable iterative algorithm. Preliminary runs turned out to be rather promising. Currently a machine program is being written with an aim for six-place accuracy in the boundary-function x(t).

#### 7. STATISTICAL ENGINEERING SERVICES

# COLLABORATION ON STATISTICAL ASPECTS OF NBS RESEARCH AND TESTING Task 3911-61-39951/51-1

Origin: NBS Authorized 7/1/50

Managers: W. J. Youden, J. M. Cameron

Full task description: July - September 1950 issue, p. 60

Status: CONTINUED. During this period members of the section provided statistical assistance to a number of Bureau personnel. The following are examples:

- (1) Churchill Eisenhart is preparing for publication an article entitled "Expression of the uncertainties of calibrations". In this article, the terms used to describe the precision and accuracy of measurements are defined and discussed. Specific rules are recommended for expressing the uncertainty of a reported value for four cases distinguished according to the relative magnitudes of the imprecision and the likely systematic error of the measurement process employed. Examples of recommended uncertainty statements are given.
- (2) The section participated in a number of studies aimed at evaluating the precision and accuracy of measurement processes. Notable among these were the work on proving rings, voltage cells, and mass calibration.

Collaboration with the Mass and Scale Section provides an excellent example of the use of statistical methods in calibration work. New weighing designs in which a standard is incorporated as an "unknown" have been worked out; techniques for surveillance as to whether the measurement process is in a state of statistical control have been put into operation, and a computer program has been worked out for the analysis and record keeping features of these procedures.

(3) George Weiss is preparing a paper jointly with B. D. Coleman (Mellon Institute) and F. Gornick (NBS Macromolecules: Synthesis and Structure Section) on the statistics of irreversible termination in anionic polymerization.

### Publications:

- (1) Uncertainties in calibration. W. J. Youden. IRE Transactions on Instrumentation I-11, Nos. 3 and 4, 133 138, December 1962.
- (2) The collaborative test. W. J. Youden. Journal of the Association of Official Agricultural Chemists, 46, 55 62, February 1963.
- (3) Mean first passage times and the dissociation of diatomic molecules. Kurt Shuler (Institute for Defense Analysis) and George Weiss. Journal of Chemical Physics, 38, 505 509, January 1963.
- (4) Statistics in chemical analysis. W. J. Youden. Handbook of Analytical Chemistry, pp. 14-1 to 14-9 (edited by Louis Meites, McGraw-Hill Book Co., Inc., New York), 1963.
- (5) Statistical interpretations. W. J. Youden. Standard Methods for Chemical Analysis, pp. 318 325 (6th ed., D. Van Nostrand Co., Inc., New York), 1963.

- (6) Long term distribution of received power. M. M. Siddiqui (Boulder Laboratories) and George Weiss. To appear in Journal of Research NBS, Section D (Radio Propagation).
- (7) Mathematical models for personnel promotion. E. L. Crow (Boulder Laboratories) and George Weiss. Submitted to a technical journal.
- (8) An editorial for "The Physics Teacher". W. J. Youden. Submitted to The Physics Teacher.
- (9) Simplified statistical quantity control. W. J. Youden. To appear in Proceedings 48th National Conference on Weights and Measures.
- (10) Mathematics and experimental science. W. J. Youden. Submitted to The Science Teacher.
- (11) Measurement agreement comparisons. W. J. Youden. To be published by NBS in Proceedings, National Conference of Standards Laboratories.

# STATISTICAL SERVICES Task 1103-40-11625/58-346

Origin and Sponsors: Various Agencies Authorized 3/31/58

Manager: J. M. Cameron

Full Task Description: January - March 1958 issue, p. 45

Status: INACTIVE.

This is a record of the use of the IEM 7090 for the period of January 1 through June 30, 1963.

TASK NUMBER	TITLE	ASSEMBLY TIME	CODE	PRODUCTION TIME	TOTAL TIME ON COMPUTER
NBS SERVICES		( M	I N U	J T E	S )
51-0002 11.3 54-0030 13.1 54-0031 13.1 54-0033 13.1 54-0034 13.1 55-0055 11.1 55-0065 11.2 55-0082 3.1 56-0166 15.0 57-0219 3.2 57-0236 3.8 57-0250 2.1 57-0252 4.4 58-0256 10.6 58-0272 3.7 58-0298 5.2 58-0314 3.7 58-0339 6.5 59-0403 2.1 59-0403 2.1 59-0403 2.1 59-0403 2.1 59-0403 2.1 59-0403 2.1 59-0403 3.8 61-0523 4.7 61-0538 9.4 61-0559 3.1 61-0856 11.2 61-0995 11.2 62-1000 12.5 62-1003 15.4 62-1005 4.3	STATISTICAL ENGINEERING SPECTRUM ANALYSIS++ SPECTRUM ANALYSIS++ SPECTRUM ANALYSIS++ SPECTRUM ANALYSIS++ RESEARCH IN NUMERICAL ANALYSIS AUTOMATIC CODING THERMOMETER CALIBRATION+ SCF-LCAO SOLUTION OF HYDRIDES+ THERMAL PROPERTIES+ SCF EIGENVALUES+ SPECTROPHOTOMETRIC DATA+ NEUTRAL MESON EXPERIMENTS++ COMPOSITE WALL STUDIES++ EQUATION OF STATE++ CODE REVISION+ APPROXIMATIONS FOR GAS MIXTURES+ VISCOELASTICITY PROPERTIES COMPUTATION OF COLOR FADINGS+ COLOR OF SIGNALS++ NUMERICAL MAPPING++ INVERSION OF LINE PROBE DATA+ POISSON DISTRIBUTION FUNCTION++ NEUTRON CROSS SECTION STUDIES++ SPECTRAL REFLECTANCE DATA THERMOCOUPLE CALIBRATION+ IBM 7090 FORTRAN INSTRUCTION+++ ERROR DETECTION+++ POST OFFICE OPERATIONS STUDY++ MOLECULAR SPECTROSCOPY+ RADIATION INTERACTION++	25 · 2 8 · 2 • 0 134 · 4 11 · 5 24 · 7 4 · 5 • 0 11 · 1 10 · 7 2 · 2 2 · 0 131 · 4 16 · 9 42 · 2 3 · 0 22 · 6 • 0 • 0 • 0 • 0 • 0 • 0 • 0 • 0	80.1 5.9 .0 1.2 24.0 27.6 76.0 3.2 335.1 23.1 1.5 44.7 333.8 155.0	376.1 1066.6 30.5 1456.9 144.0 154.2 56.7 167.9	481.4 1080.7 30.5 1592.5 179.5 206.5 137.2 171.1 1044.3 57.5 144.2 76.9 973.4 411.5
62-1007 4.3 62-1009 4.3 62-1011 13.5 62-1013 7.0	RADIATION SHIELDING++ MONTE CARLO NEUTRON STUDIES DISPERSION INTEGRALS++ STATISTICAL METHODS++	•0 1•9 •0 3•3	53.1 12.9 5.4 16.5	10.1 .0 2.7 .8	63.2 14.8 8.1 20.6

Current	Applications	of	Automatic	Computer
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TASK NUMBER	TITLE	ASSEMBLY TIME	CODE CHECKING	PRODUCTION TIME	TOTAL TIME ON COMPUTER
NBS SERVICES		( M )	ט א ט	T E	s )
62-1015 15.1	THERMAL FUNCTIONS++	25.0	16.7	5.1	46.8
62-1019 41.0	NBS PERSONNEL REPORT++	4.4		117.4	
62-1020 3.3	EIGENVALUES+	• 0		331.2	
62-1027 11.2	NEW SYSTEM	8.0	33.3	42.2	83.5
62-1029 9.7	D-SPACING CALCULATIONS+	• 0	• 0	35.5	35.5
62-1033 9.7	CRYSTAL STRUCTURE CALIBRATION++	5.7	8 • 1	667.9	
62-1034 30.0	PHOTOIONIZATION CROSS SECTION++	156.5	12.9	34.3	203.7
62-1035 7.7	CREEP DATA ANALYSIS++	13.5	19.7	33.5	66.7
62-1036 7.7	FILM THICKNESS++	• 0	• 0	25.2	25.2
62-1038 7.5	STANDARDIZATION ANALYSES++	22.4	36.7	10.8	69.9
62-1055 8.4	ELLIPSOIDAL COMPUTATION++	• 0	• 0	1.3	1.3
62-1060 15.0	BLACK BOX COMPUTER SERVICE+	• 0	• 0	1.0	1.0
62-1064 2.4	GAGE BLOCK STUDIES++	• 0	• 4	17.7	18.1
62-1066 1.2	STANDARD CELLS++	• 0	• 0	15.1	15.1
62-1080 9.2	BLACK BOX COMPUTER SERVICE+	• 0	• 0	80.6	80.6
62-1089 9.6	ELASTIC CONSTANTS++	• 0	5.1	9.8	14.9
62-1102 6.8	BLACK BOX COMPUTER SERVICE+	• 0	3.4	30.2	33.6
62-1123 10.3	BLACK BOX COMPUTER SERVICE+	• 0	1.1	1.4	2.5
62-1125 9.5	MATRIX COMPUTATIONS	156.7			348.4
62-1133 5.0	CHEMISTRY CALCULATIONS++	• 0	•0	. 4	• 4
62-1157 11.4	PLASMA RESEARCH++	.4	• 0	.0	.4
62-1162 10.7	CEMENT AGING STUDIES++	53.6	80.6		139.5
62-1163 14.1	TRANSISTOR AGING BEHAVIOR++	14.3	27.4	17.0	58.7
62-1165 15.2	NMR SPECTRA ANALYSES+	•0	2 • 8	7.6	10.4
62-1181 12.4	NTDC++	8.6 50.7	15.3	•0	23.9
62-1185 10.3 62-1193 3.8	HEAT TRANSFER CALCULATIONS+		_	30.5	274.6
62-1194 15.1	ELLIPTIC DIFFERENTIAL EQUATIONS MEMBRANE TRANSPORT++	20.9	•0 34•7		55.6
62-1194 13-1	LIGHT SCATTERING++	•0	38.7	• 0	38.7
62-1203 3.7	CYLINDRICAL SHOCK WAVE	7.8	51.3	22.9	82.0
62-1211 12.5	TECHNICAL INFO RETRIEVAL++	3.0	7.7	.0	10.7
62-1212 10.9	COLOR DIFFERENCES	•0	12.5	•0	12.5
63-1224 9.7	ATOM PACK++	21.1	•0	19.5	40.6
63-1226 12.0	OTS - KWIC++		123.1	40.0	188.8
63-1228 3.7	SHOCK DISSOCIATION	17.2	66.9	46.1	130.2
63-1229 10.0	MORTAR BOND INVESTIG++	5.3	1.3	38.2	44.8
63-1230 15.2	LEAST SQUARES+	•0		. 4	• 4
63-1231 13.0	BLACK BOX COMPUTER SERVICE+	3.4		4.8	27.0
63-1233 9.7	BLACK BOX COMPUTER SERVICE+	•0		.0	1.1
63-1234 10.3	VAPOR TRANSMISSION++	5.2		6.5	54.2
63-1237 3.1	PYROMETRY++	•0		• 0	2.6
63-1238 10.3	CT TRUCK DATA ANALYSIS++	• 0		15.4	

TASK NUMI	BER	TITLE	ASSEMBLY TIME	CODE	PRODUCTION TIME	TOTAL TIME ON COMPUTER
NBS SERVI	ICES		( M	I N U	T E	s)
63-1241	12.5	IICASP++	3.7	37.6	18.9	60.2
63-1245	10.2	FIRE RESEARCH++	• 0	• 0	• 3	• 3
63-1248	15.4	CALCULATION OF FORCE CONSTANTS+	• 0	1.5	• 0	1.5
63-1250	12.0	KWIC++	1.9	35.8	7.5	45.2
63-1252	11.5	ARMY ORDNANCE++	• 0	15.8	• 0	15.8
63-1257	7.8	CALC OF CALCIUM PHOSPHATE++	• 0	• 0	12.6	12.6
63-1258	15.5	SPECTRUM ANALYSIS	• 0	15.8	43.4	59.2
63-1259	11.3 7.8	RESEARCH IN PROBABILITY++	• 0	2 • 8	20.7	23.5
63-1260	15.5	DENTAL RESEARCH	10.3	53.1	• 0	63.4
63-1263 63-1276	14.2	LINEAR CLASSICAL SYSTEM++ INSTRUMENTATION++	66.5	3 • 4	227.9	297.8
63-1277	1.2	BLACK BOX COMPUTER SERVICE++	3.7	26.1	.0	29.8
63-1278	4.7	TIME OF FLIGHT SPECTRUM++	-0	6.2	5.4	11.6
63-1281	2.4	CORRECTION-SMEARING	25.0	111.0	73.1	209.1
63-1285	11.5	RTS FUNDS++	. 0	5.5	.0	5.9 399.3
63-1287	3.7	DATA ANALYSES OF GASES++	41.5	255.9	101.9	160.9
63-1288	10.3	TRUCK INFILTRATION++	•0 3•1	15.4	1.2	19.7
63-1289	3.8	IONIZED GASES++	88.4	105.4	26.4	220.2
63-1290	3.0	MOLECULAR ENERGY LEVELS++	• 0	20.3	.0	20.3
63-1291	7.1	JOB CALCULATIONS++	•0	44.9	13.4	58.3
63-1300	4.1	MAXIMUM SIGMA++	15.0	128.8	127.1	
63-1302	7.3	COMPUTER CALCULATIONS++	• 0	3.9	1.8	5.7
63-1308	2.5	BUTTRESS THREADS++	• 0	4.1	• 0	4.1
63-1309	4.2	LINEAR REGRESSION ANALYSIS++	• 0	• 0	15.3	15.3
63-1311	3.1	OMNITAB+	• 0	• 9	• 0	• 9
63-1312	3.7	CRO TRACE++	• 0	1.8	2.3	4.1
63-1315	3.3	VIRIAL COEFFICIENTS++	• 0	9.4	• 0	9.4
63-1316	13.7	RECOMBINATION++	14.4	3 • 2	50.8	68.4
63-1318	10.3	THERMISTOR PROGRAM++	1.1	1.0	2.7	4.8
63-1319	6.1	BIQUADRATIC-BICUBIC EQUATION	• 0	6.2	• 0	6.2
63-1321 63-1321	9.7	CRYSTAL STRUCTURE	• 0	22.2	23.1	45.3
63-1322	13.6 7.1	OMNITAB+	• 0	• 0	7.4	7.4
63-1323	3.0	CHEMIST GENERAL++	• 0		• 0	13.1
63-1325	4.7	PLASMA TRANSPORT++	2.6		115.9	118.5
53-1326	3.2	THERMOFLUX++ HEAT MEASUREMENT++	18.6		32.5	120.1
63-1328	10.7	LONG-TIME CEMENT STUDY 2++	• 5	-21.8	52.0	74.3
63-1329	10.7	LONG-TIME CEMENT STUDY 1++	15.6		115.5	131.4
63-1331	6.1	BLACK BOX COMPUTER SERVICE+	75.5		126.3	208.2
63-1332	3.1	TEMPERATURE PHYSICS++	• 0		• 0	1.2
63-1333	2.2	BLACK BOX COMPUTER SERVICE+	•0 24•1	19.1	4 • 1 5 • 8	49.0
63-1334	15.0	PHASE TRANSITION++	•0	53.8	2.7	56.5
		-	• 0	77.0	2,01	2002

TASK NUMBE	<u>R</u>	TITLE	ASSEMBLY TIME	CODE	PRODUCTION TIME	TOTAL TIME ON COMPUTER
NBS SERVICE	ES		( M	I N U	T E	s )
	3.7	MATRIX OF POLYNOMIALS	• 0	15.6	• 0	15.6
	2.0	RICASIP PT1++	1.6	• 5	29.7	31.8
	5.4	SECTION COMPUTATIONS++	28 • 4	11.8	21.7	61.9
	3.3	FUNCTION OF TEMPERATURE++	• 0	8.7	31.5	40.2
	3.2	LINE WIDTH	5.9	9•8	3.6	19.3
	5.1	OMNITAB+	• 0	• 4	• 5	• 9
	3.1	OMNITAB+	• 0	12.8	• 0	12.8
	5.2	SPECTROMETER	• 0	5.2	• 0	5.2
	2.5	COAST AND GEODETIC SURVEY++	51.6	20.5	• 0	72.1
	1.2	TEST DATA++	• 0	• 0	48.8	48.8
	5.3 3.4	WAVES IN STRATIFIED FLUID RUT(LE BAND STRUCTURE	• 0	2.6	1.6	4.2
	3.5	OMNITAB+	• 0	• 0	2.4 10.9	2.4 16.0
	4.4	BAF ELEMENT RESPONSE TIME	•0 3•6	5•1 •4	10.9	5.1
	3.7	THERMAL PROPERTIES+	31.0	37.9	563.3	632.2
	5.0	OMNITAB+	•0	1.5	•0	1.5
	3.5	WHISKER GROWTH EQUATION	7.5	21.0	• 0	28.5
	2.5	DCA++	12.4	6.0	2.0	20.4
	3.8	POLY-ELECTROLYTES	10.6	34.0	7.6	52.2
	2.3	SIGMA COMPUTATIONS	1.5	2.2	1.9	5.6
63-1383 9	9.0	KEY WORD INDEX++	• 0	4.6	• 0	4.6
	6.4	PROVING RINGS++	• 0	11.1	2.8	13.9
	0.0	FOKKER-PLANCK	1.5	37.0	29.4	67.9
	2.4	INSTRUMENTAL SMEARING++	• 0	2.4	3.4	5.8
	1.2	MACHINE TIME ONLY+++	25.5	69.8	• 8	96.1
	1.2	FREE MACHINE TIME+++	• 0	10.0	• 0	10.0
	1.2	SECRETARYS MACHINE TIME+++	149.6	396.3	306.8	852.7
63-3010 11	1.2	NEW SYSTEMS+++	• 0	1.8	34.1	35.9

Totals (NBS Services)

2188.2 5335.4 12106.2 19629.8

TASK NUMBER	TITLE	TIME	ASSEMBLY	CODE	PRODUCTION TIME	TOTAL TIME ON COMPUTER
NON-NBS SERVICES		(	M	I N	U T E	s )
57-0216 NSF	HANDBOOK OF MATHEMATICAL TABLES	•	4	1.7	• 0	2.1
58-0348 OOR	MACHINE TRANSLATION OF RUSSIAN	22.		38.1	1.7	62.3
58-0366 USIA	RADIATION PATTERNS OF ANTENNAS	•		• 0	2.0	2.0
59-0407 DOFL	FOURIER COEFFICIENTS+	18.		9.3	13.1	40.8
59-0409 FSLIC	BANK BOARD REPORTS++	13.			2281.3	
59-0425 CU		159		81.9	174.5	415.8
59-0434 GC	PETROLOGICAL COMPUTATIONS+	•		116.2	26.4	142.6
59-0441 USRED 60-0457 PHA	SYSTEMS ENGINEERING++ PUBLIC HOUSING PROBLEM++	8 •		225.9	57.6	291.9
60-0476 DOFL	GAS TUBE CHARACTERISTIC II	4 • '		30.7	181.9	217.5
60-0486 U ONT	MORSE WAVE FUNCTION++	•		• 0	538.1 24.7	538.1 24.7
60-0492 IMF	MONETARY RESEARCH REPORTS++	10.		107.1	94.3	211.4
60-0506 WBANK	WORLD BANK REPORTS++	•		•0	52.0	52.0
61-0513 NASA	ORBITING STUDIES	9.		• 0	25.1	35.0
61-0532 GU	VIBRATIONAL ENERGY LEVELS+	12.		49.1	54.2	115.9
61-0540 ACC	DIFFUSION CALCULATIONS+	3 ⋅	7	• 0	25.9	29.6
61-0550 GWU	LOGISTICS RESEARCH++	•	0	24.0	• 0	24.0
61-0569 AGO	HUMAN FACTORS RESEARCH++	65.	8	405.7	191.1	662.6
61-0830 BPR	HIGHWAY TRAFFIC STUDIES++	4.	6	4.2	722.1	730.9
61-0849 BPR	HIGHWAY TRAFFIC STUDIES++	•	0	• 0	540.0	540.0
61-0902 BPR	HIGHWAY TRAFFIC STUDIES++	•		• 0	385.9	385.9
61-0903 BPR	HIGHWAY TRAFFIC STUDIES++	39.			1489.3	
61-0945 WB	FORECASTING++	•			3943.0	
62-1004 BUSHP	RHOMBIC ANTENNAS+	287		18.7	124.8	143.5
62-1014 NIH 62-1018 NRL	METABOLIC DISEASES++ HYDROMAGNETIC PROBLEMS+	257. 100.		427.2		1499.5
62-1021 DCH	HIGHWAY STUDIES++	195.			1541.7 3382.4	
62-1022 NRL	SPECTRUM OF DIPOLE RADIATION	1770		•0	30.5	30.5
62-1023 NSF	IMAGE PROCESSING++		Ö	17.9	41.9	59.8
62-1030 VA	ELECTROCARDIOGRAPHIC ANALYSIS	438.		1634.4		2813.0
62-1044 FCC	RADIO INTENSITIES++	•		• 0.	10.7	10.7
62-1030 VA	ELECTROCARDIOGRAPHIC ANALYSIS	1.		• 0	• 0	1.0
62-1044 FCC	RADIO INTENSITIES++	11.		20.8	35.6	68.2
62-1046 BPR	TRAFFIC PREDICTION++	329.	8	977.1	846.5	2153.4
62-1056 DOFL	PD ENGINEERING++++	•	0	• 0	295.5	295.5
62-1071 DOFL	RHINITIS STUDIES++	4.		9.2	6.3	19.5
62-1076 NAS	EVALUATION OF APPLICATIONS+	43.		71.0	58.2	172.2
62-1096 DOFL	VULNERABILITY STUDY++++	30.		359.6	275.9	666.1
62-1110 ICC	ICC SYSTEMS STUDY++	34.		60.0	21.3	116.1
62-1113 DOFL	TRANSPORT ANALYSES++++	25.		26.4	177.4	229.7
62-1119 BPR 62-1121 CARIN	HIGHWAY TRAFFIC STUDIES++		0	. 72 2	310.1	310.1
OS-TIST CAKIN	CARNEGIE INSTITUTE STUDIES++	13.	Τ,	. 73.3	• 0	86.4

TASK NUMBER	TITLE	ASSEMBLY TIME	CODE	PRODUCTION TIME	TOTAL TIME ON COMPUTER
NON-NBS SERVICES	3	( M	I N	U T E	s )
NON-NBS SERVICES 62-1130 COENG 62-1131 USIA 62-1134 HARVU 62-1140 VA 62-1141 COENG 62-1144 UOFMD 62-1146 BPR 62-1158 GC 62-1169 U ONT 62-1171 VA 62-1172 PEACE 62-1175 DOFL 62-1177 DOFL 62-1179 DOFL 62-1179 DOFL 62-1188 FTBEL 62-1189 QM 62-1197 UOFMD 62-1201 FCC 62-1215 NASA 62-1216 BPR 63-1218 DOFL 63-1221 BPR 63-1221 BPR 63-1221 BPR 63-1221 BPR 63-1221 ROFL 63-1232 ROFL 63-1233 ROFL 63-1234 ROFL 63-1245 ROFL 63-1246 ROFL 63-1256 ROFL 63-1256 ROFL	FALLOUT SHELTER COMPUTATIONS CANTILEVER RETAINING WALL++ STATISTICAL DECISION THEORY++ VA MEDICAL++ FALLOUT SHELTER COMPUTATIONS THERMAL BOUNDARY LAYERS GRAVITY MODEL STUDIES++ MINERALOGY STUDIES++ ATOMIC COLLISIONS++ HOSPITAL PROGRAM PLANNING+ PEACE CORPS EVALUATIONS++ ION DISTRIBUTIONS+ ANALYSIS OF VARIANTS+ CATALOG INFORMATION+ STEPWISE REGRESSION+ TABLES FOR SEQUENTIAL METHODS HIGH ENERGY PHYSICS++ UHF TV MISSILE SATELLITE++ ARIZONA++ INTEGRAL EVALUATION RHODE ISLAND++ LINEAR AND NON LINEAR ESTIM++ ARMY GENERATOR NOISE++ MISSILES++ DATATROL++ PUBLIC HEALTH SERVICE++ SECRET SERVICE FORGERY HIGHWAY STUDIES++ SCREENING EVALUATION+ ISOTOPE TRACER ANALYSIS++ BLACK BOX COMPUTER SERVICE++ HIGH FREQUENCY PROPAGATION++ TRANSIT STUDY++	1.8 3.0 .0 3.4 .0 .0 1.4 1.2 23.6 152.9 3.8 .0 .0 .0 .0 .0 3.4 .0 .0 .0 .0 .0 .0 .0 .0 .0 .0 .0 .0 .0	74.8 15.5 16.8 .0 .0 .0 8.8 33.3 .0 247.6 3.6 3.6 3.8 .0 .0	382.8 3.0 1.8 839.7 92.5 28.8 449.9 219.9 37.7 108.3 8.4 68.2 3.5 11.3 192.5 1051.2 510.0 112.2 403.8 12.4 1.5 38.8 .0 25.7 81.9 31.6 21.2 40.5 37.7 81.9 31.6 21.2 40.5 37.7 81.9 37.7 81.9 37.7 81.9 37.7 81.9 81	s) 459.4 21.5 18.6 843.1 92.5 28.8 460.1 254.4 61.3 508.8 15.8 72.0 3.5 11.3 214.0 1099.2 510.0 147.5 423.1 15.4 1.5 41.5 1.0 75.1 574.5 140.8 21.2 14.5 43.0 80.7 3.8
63-1262 NRL 63-1264 NRL 63-1270 BPR 63-1271 COMM 63-1272 BPR 63-1274 FTBEL 63-1275 SEC 63-1280 UARIZ	NUCLEONICS++ NUCLEONICS++ MODAL SPLIT PROCEDURE++ ECONOMICS STUDY++ ROADS STUDY++ NUCLEAR UTILITY SERVICES++ SECURITIES MARKET STUDY++ NIH++	227.4 .0 .0 11.3 4.6 64.2	142.9	427.9 1029.4 917.3	798.2 1029.4 1002.9 187.7 484.6 78.0 531.6

TASK NUMBER	TITLE	ASSEMBLY TIME	CODE	PRODUCTION TIME	TOTAL TIME ON COMPUTER
NON-NBS SERVICE	'S	( M	I N U	J T E	s )
63-1284 DOFL	STATISTICAL ANALYSIS++	• 0	• 0	2.4	2.4
63-1286 UOFMD	OPTIMAL EXAMINATION	• 0	34.0	• 0	34.0
63-1293 COMM	BODDY CALCULATION++	• 0	38.6	• 4	39.0
63-1296 DOFL	OPTIMUM LIFE++	74.2	374.7	1.5	450.4
63-1298 DOFL	LITTLE JOHN SPARE PARTS++	• 0	• 0	82.8	82.8
63-1301 DOFL	SERGEANT SPARE PARTS++	• 0	• 0	85.1	85.1
63-1303 UCLA	LOS ANGELES HEART STUDY++	• 0	16.7	6.5	23.2
63-1305 DSA	ARMY++		1019.3		
63-1307 DOFL 63-1310 DOFL	MISCELLANEOUS PROGRAMMING++	• 8	9.7	• 0	10.5
63-1313 IDA	SHOCK WAVE TEST++ OMNITAB+	• 7	43.7	3.2	47.6
63-1314 BPR	FLORIDA HIGHWAYS++	• 0	• 5	95.7	96.2
63-1317 AID	SORTING AND TABULATING	• 0	• 0	42.7	42.7
63-1324 HEW	GENERAL KINETICS++	2 • 8 89 • 6	2•7	8.9	14.4
63-1330 BROOK	INVESTMENT++	•0	547.1	42.0	678.7
63-1336 NAVWE	ARC++	70.6	• 0 1 • 8	61.9 5551.5	61.9
63-1339 DOFL	TRAPEZOIDAL PLATE++	10.1	23.6	,0 0	33.7
63-1345 DOFL	ROCKET TRAJECTORIES++	56.7	71.6	22.5	150.8
63-1352 OCDM	NEAR	• 0	1.2	524.3	525.5
63-1356 NIH	COMPUTER CONSULTING	195.9	14.9	55.3	266.1
63-1357 BPR	HIGHWAY STUDIES++	3.4	19.6	252.8	275.8
63-1358 PHS	TRAINING GRANTS	128.2	171.1	224.8	524.1
63-1360 FPC	FEDERAL POWER COMMISSION++	• 0	• 0	35.2	35.2
63-1361 DOFL	ANTENNA CALCULATION++	4.7	8.0	21.7	34.4
63-1362 VA	RESEARCH++	• 0	• 0	107.5	107.5
63-1367 BPR	PUBLIC ROADS++	1 • 1	• 0	28.4	29.5
63-1368 PHS	HEART DISEASE	5.0	• 0	• 0	5.0
63-1371 TREAS	ALTERNATE TAX PLANS++	18.0	3.5	30.4	
63-1374 OCDM	FEDERAL RESEARCH++	46.1	67.6	138.7	
63-1379 BPR	PUBLIC ROADS++	• 0	• 0	12.4	12.4
63-1386 BPR	PUBLIC ROADS++	• 0	• 0	10.3	10.3
63-1387 DOFL	MAGNETOSTATIC MODES++	• 0	• 0	1.9	1.9

Totals ( (NON-NBS Services) 3557.4 10074.1 37811.7 51443.2

TOTAL TIME FOR THE QUARTER (MINUTES) 5745.6 15409.5 49917.9 71073.0

- + Problem programmed in the Computation Laboratory, production runs continued under direction of sponsor.
- ++ Problem programmed by the sponsor and run under his direction.
- +++ Functions pertain to the internal operations of the Computation Laboratory.
- ++++ Classified task.

Note: In general, copies of papers or talks listed in this section are not available from the National Bureau of Standards. If and when a paper is to be published, it will be listed in the section of this report on Publication Activities.

## Applied Mathematics Division Lectures

- MARCUS, M. (University of California, Santa Barbara, California) Series five lectures on selected topics in linear algebra. April 8, 1963 to April 12, 1963.
- OSTROWSKI, A.M. (Graduate Institute for Mathematics and Mechanics, Indiana) (i) Positive Matrices. April 22, 1963. (ii) Runge's Rule of Signs in the Theory of Algebraic Equations. April 23, 1963.
- GOODWIN, E.T. (National Physical Laboratory, Great Britain) On Richardson's Deferred Approach to the Limit. May 7, 1963.
- HELLER, I. (Stanford University) Representation and Classification of Unimodular Sets. May 20, 1963.
- MORDELL, L.J. (University of Arizona, Arizona) On a Certain Diophantine Equation. May 27, 1963.
- GUPTA, H. (Panjab University, India) Recent Results in the Theory of Partitions. June 12, 1963.

## Seminar in Mathematics

A series of weekly seminars led by Dr. Seymour Haber with the cooperation of Dr. B. Bernstein, was conducted to cover the Princeton lecture notes, "Advanced Calculus" by H. K. Nickerson, D.C. Spencer, and N. E. Steenrod (D. Van Nostrand Co., 1959). January to April, 1963.

## Papers and Invited Talks

## Presented by Members of the Staff

## at Meetings of Outside Organizations

- ARMS, R. J. On the Limit Behavior of Steepest Descent, Preliminary
  Report. Presented before the American Mathematical Society.
  Berkeley, California January 21, 1963
- DAVIS, P. J. The Computation of Highly Multiple Integrals. Presented at NBS Boulder.

  Boulder, Colorado January 30, 1963
  Of Men and Mathematics. Presented at the Maryland,
  Delaware, Virginia section of the MAA.
  Annapolis, Maryland April 1963
- EDMONDS, J. Maximum Degree-Constrained Subgraphs. Presented at the Graph and Combinatorics Conference, Princeton University.

  Princeton, New Jersey May 18, 1963
- GOLDMAN, A. J. Examples of OR Applications in the Federal Government.

  Presented at the Operations Research Orientation. General Accounting Office.

  Washington, D.C. April 2, 1963

  Examples of OR Applications in the Federal Government.

  Presented at the Management Sciences Orientation. General Accounting Office.

  Washington, D.C. April 24, 1963

  A Theorem on Convex Programming. Presented at the Mathematical Association of America. U.S. Naval Academy.

  Annapolis, Maryland April 27, 1963
- MATHER, J. The Planar Immersions of a Graph. Presented at the Graph and Combinatorics Conference, Princeton University.

  Princeton, New Jersey May 16, 1963
- MEYERS, P. A Comparison of One and Two Stage Coding for Mail.

  Presented at the 23rd National Meeting of Operations

  Research Society of America.

  Cleveland, Ohio May 28, 1963
- NEWMAN, M. Normal Congruence Subgroups of the Modular Group. Presented at Combinatorial Seminar.
  Princeton, New Jersey March 25, 1963
- RHODES, I. Mechanical Translation by Means of Computers. (Westing-house Science Talent Search, Statler Hilton Hotel.)
  Washington, D.C. February 28, 1963

- ROCKOFF, M. L. On the Numerical Solution of Finite Difference Approximations which are not of Positive Type. Presented before the Am. Math. Society. Berkeley, California. January 24, 1963
- ROMANO, Albert, Distributions in Reliability Studies. Presented in the 1963 Reliability Training Program of the Washington Section, American Society for Quality Control at Georgetown Univ.

  Washington, D.C. April 16, 1963
- ROSENBLATT, Joan R., Moderator on "Ask the Scientists" panel discussion.

  Sponsored by Joint Board on Science Education, Georgetown
  Visitation School.

  Washington, D.C.

  Panel discussion on activities of the Committee on Women
  in Science, of the Joint Board on Science Education. This
  discussion was taped and broadcast by the Georgetown Univ.
  Forum over Radio Station WTTG and TV Channel 5.

  Washington, D.C.

  April 7, 1963
  Applications of Statistics in Colorimetry. Presented at
  the Department of Statistics, Harvard University.
  Cambridge, Massachusetts

  April 10, 1963
- TCHEN, C. T. Participated in the 4th International Space Science Symposium. Warsaw, Poland June 3-11, 1963 Kinetic Problems in Plasmas. Presented at Plasma Physics Institute. Garching, Germany June 18, 1963 Kinetic Equation and Landau Demping. Presented at the Institute for High Temperature Research, Technical Univ. Stuttgart, Germany June 19, 1963 Kinetic Equations of Plasmas. Presented at the Institute for the Structure of Materials, Philipps University. Marburg, Germany June 21, 1963 Interaction of Plasma Flows with Magnetic Fields. Presented at the Laboratorium voor Massascheiding. Amsterdam, Netherlands June 24, 1963 Kinetic Theories of Plasmas. Presented at the Institute Battelle, Centre de Recherche de Geneve. Geneva, Switzerland June 28, 1963 Plasma Oscillations with Collective Correlations, and Interaction of a Plasma Source with a Uniform Magnetic Field. Presented at the 6th International Symposium on Ionization Phenomena in Gases. July 8-13, 1963 Paris, France

WEISS, George, The Theory of Pedestrian Queueing. Presented at the
Operations Research Society Meeting.
Cleveland, Ohio May 27, 1963

WITZGALL, C. On Edmond's Algorithm for Maximum Matchings of Graphs.

Presented for the Department of Mathematics, The Institute for Fluid Dynamics and Applied Mathematics, University of Maryland.

College Park, Maryland March 8, 1963
On Convex Metrics. Presented at the Mathematical Association of America, U. S. Naval Academy.

Annapolis, Maryland April 27, 1963

YOUDEN, W. J., Measurement and Science. Presented at the Maryland-D.C. Conference on Junior High School Science, Nicholas Orem Junior High School. Hyattsville, Maryland February 16, 1963 Measurement and Science. Presented at the Science Seminar, Immaculata High School. Washington, D.C. February 18, 1963 Checking Calibrations. Presented at the Cleveland Electronics Conference. Cleveland, Ohio April 17, 1963 Interpretation and Evaluation of Analytical Data. Presented at a meeting of the American Chemical Society. Philadelphia, Pennsylvania April 18, 1963 Precision and Accuracy in Spectrochemical Analysis. Presented at a meeting of Baltimore-Washington Chapter of the Spectroscopy Society. Washington, D.C. April 23, 1963 Precision and Accuracy in Spectrochemical Analysis. Presented before the Society for Applied Spectroscopy. Cleveland, Ohio May 15, 1963 Picking Winners and Losers. Symposium at Virginia Polytechnic Institute. Blacksburg, Virginia April 25, 1963 Picking Winners and Losers. Presented before the American Society for Quality Control. Detroit, Michigan May 1, 1963 Analytical Procedures. Seminar presented to the Statistical Group of the Food and Drug Administration.

Washington, D.C.

June 4, 1963
Simplified Statistical Quantity Control. Presented at the
48th National Conference on Weights and Measures.

Washington, D.C. June 13, 1963

#### 1. PUBLICATIONS THAT APPEARED DURING THIS PERIOD

#### 1.1 Mathematical Tables

Tables Describing Small-Sample Properties of the Mean, Median, Standard Deviation, and Other Statistics in Sampling from Various Distributions. Churchill Eisenhart, Lola S. Deming and Celia S. Martin. NBS Technical Note 191. June 1963.

## 1.2 Manuals, Bibliographies, Indices

Selected Bibliography of Statistical Literature: supplement, 1958-1960. Lola S. Deming. Journal of Research NBS, Section B (Mathematics and Mathematical Physics). 67B, pp. 91-133, April-June 1963.

Statistical Interpretations. W. J. Youden. Standard Methods for Chemical Analysis, 6, pp. 318-325, D. Van Nostrand Co., Inc., New York, 1963.

Statistics in Chemical Analysis. W. J. Youden. Handbook of Analytica. Chemistry, pp. 14-1 to 14-9, McGraw-Hill Book Co. Inc., New York, 1963

## 1.3 Technical Papers

An Algorithm for Obtaining an Orthogonal Set of Individual Degrees of Freedom for Error. J. M. Cameron. Journal of Research NBS, Section B (Mathematics and Mathematical Physics) 67B, 19-22, January - March 1963.

The Segmental Variation of Blaschke Products. G. T. Cargo. Duke Mathematical Journal, 30, No. 1, pp. 143-150, March 1963.

Packing Inequalities for Circles. P. Davis. Michigan Math. J. 10, pp. 25-31, March 1963.

Uniqueness Classes for Difference Functionals. R. F. DeMar. Notices, American Mathematical Society, Vol. 10, No. 1, p. 91, January 1963.

Realistic Evaluation of the Precision and Accuracy of Instrument Calibration Systems. Churchill Eisenhart. Journal of Research NBS, Section C (Engineering and Instrumentation) 67C, No. 2, pp. 161-187, 1963.

Tables of Genera of Groups of Linear Fractional Transformations. H. Fell, M. Newman and E. Ordman. Journal of Research NBS, 67B, pp. 61-68, 1963.

Recognition of Completely Mixed Games. A. J. Goldman. Journal of Research NBS, 67B, pp. 23-29, 1963.

Maximal Cellular Boolean Functions. A. J. Goldman and B. K. Bender. Journal of Research NBS, 67B, pp. 77-84, 1963.

Copositive and Completely Positive Quadratic Forms. M. Hall and M. Newman. Proceedings of the Cambridge Philosophical Society, 59, pp. 329-339, 1963.

Factorial Designs and the Direct Product. Badrig Kurkjian. (Harry Diamond Laboratories) and Marvin Zelen. Bulletin International Statistical Institute, XXXIX, Part 2, pp. 509-519, 1962.

A Note on Modular Groups. M. Newman. Proceedings of the American Mathematical Society, 14, pp. 124-125, 1963.

Bounds for Cofactors and Arithmetic Minima of Quadratic Forms.

M. Newman. Journal of the London Mathematical Society, 38, pp. 215-217, 1963.

Modulary Groups of t x t Matrices. M. Newman and J. R. Smart. Duke Journal of Mathematics, 30, pp. 253-257, 1963.

Confidence Limits for the Reliability of Complex Systems. Joan Raup Rosenblatt. Statistical Theory of Reliability, (edited by Marvin Zelen, The University of Wisconsin Press, Madison) pp. 115-148, 1963.

Mean First Passage Times and the Dissociation of Diatomic Molecules. Kurt Shuler (Institute for Defense Analyses) and George Weiss. Journal of Chemical Physics, 38, pp. 505-509, January 1963.

Precision of Simultaneous Measurement Procedures. W. A. Thompson, Jr., Journal of the American Statistical Association, 58, No. 302, pp. 474-479, June 1963.

A survey of Some Mathematical Models in the Theory of Reliability. George Weiss. Statistical Theory of Reliability, (edited by Marvin Zelen, The University of Wisconsin Press, Madison) pp. 3-15, 1963.

On the Pedestrian Queueing Problem. George Weiss. Bulletin International Statistical Institute, XXXIX, Part 4, pp. 163-168, 1962.

The Collaborative Test. W. J. Youden. Journal of the Association of Official Agricultural Chemists, 46, pp. 55-62, February 1963.

Uncertainties in Calibration. W. J. Youden. IRE Transactions on Instrumentation I-11, Nos. 3 and 4, pp. 133-138, December 1962.

#### 1.4 Reviews and Notes

Review of "Systems: Research and Design." A. J. Goldman. Technometrics 5, pp. 130-131, 1963.

## 2. MANUSCRIPTS IN THE PROCESS OF PUBLICATION

## 2.2 Manuals, Bibliographies and Indices

"Experimental Statistics". Mary G. Natrella. To appear August 1, 1963 as NBS Handbook 91. In press.

#### 2.3 Technical Papers

A Study of Stress Relaxation with Finite Strain. B. Bernstein (with E. A. Kearsley and L. Zapas). To appear in the Transactions of the Society of Rheology.

Mathematical Models for Personnel Promotion. E. L. Crow (Boulder Laboratories) and George Weiss. Submitted to a technical journal.

A Uniqueness Theorem. R. F. DeMar. To be published in Proceedings of the American Mathematical Society.

On a Theorem Concerning Existence of Interpolating Functions. R. F. DeMar. Submitted to the Transactions of the American Mathematical Society.

Higher Approximations with the Stroboscopic Method. A. Ghaffari. To appear in the Proceedings of the Second International Conference on Non-linear Vibrations, Warsaw, Poland, September 18-21, 1962.

A Recurrance on Integral Vectors. K. Goldberg. In manuscript.

Hadamard Matrices of Order Cube Plus One. K. Goldberg. In manuscript.

Random Notes on Combinalysis. K. Goldberg. In manuscript.

The Powers of the Iterates of a Formal Power Series. K. Goldberg. In manuscript.

Incidence Spaces and Algebras. K. Goldberg and E. C. Dade. In Manuscript.

Group Generated Incidence Spaces and Applications. K. Goldberg and E. C. Dade. In manuscript.

A Proposed Computer Based Model. K. Goldberg and J. G. Reed. In manuscript.

A Note on Contingency Tables Involving Zero Frequencies and the 2Î Test. H. H. Ku. To appear in Technometrics.

Weierstrass' Points of  $\Gamma_{\!\scriptscriptstyle O}(n)$ . J. Lehner and M. Newman. To appear in Annals of Mathematical Statistics.

Syntactic Integration Carried out Mechanically. Ida Rhodes. Proceedings of the Nato Advanced Study Institute of Languages, Journal of Information Storage and Retreval, Pergamon Press Ltd. Venice, 1962.

The Method for Mechanical Translation Used by the NBS Group and the Structure of its Machine Glossary. Ida Rhodes. To appear in the Proceedings of the American Documentation Institute, Chicago, 1963.

Sympletic Modulary Groups. M. Newman and J. R. Smart. To appear in Acta Arithmetica.

Long Term Distribution of Received Power. M. M. Siddiqui (Boulder Laboratories) and George Weiss. To appear in Journal of Research NBS, Section D (Radio Propagation).

On a Rank Sum Test for Outliers. W. A. Thompson, Jr., and T. A. Willke. To appear in Biometrika.

Zonal Harmonic Perturbations of an Accurate Reference Orbit of an Artificial Satellite. J. P. Vinti. Submitted to a technical journal.

An Editorial for "The Physics Teacher". W. J. Youden. Submitted to The Physics Teacher.

Mathematics and Experimental Science. W. J. Youden. Submitted to The Science Teacher.

Measurement Agreement Comparisons. W. J. Youden. To be published by NBS in Proceedings, National Conference of Standards Laboratories.

Simplified Statistical Quantity Control. W. J. Youden. To appear in Proceedings, 48th National Conference on Weights and Measures.

Approximating Symmetric Relations by Equivalence Relations. C.T. Zahn, Jr. To be submitted to a technical journal.



#### THE NATIONAL BUREAU OF STANDARDS

The scope of activities of the National Bureau of Standards at its major laboratories in Washington, D.C., and Boulder, Colorado, is suggested in the following listing of the divisions and sections engaged in technical work. In general, each section carries out specialized research, development, and engineering in the field indicated by its title. A brief description of the activities, and of the resultant publications, appears on the inside of the front cover.

## WASHINGTON, D. C.

**Electricity.** Resistance and Reactance. Electrochemistry. Electrical Instruments. Magnetic Measurements. Dielectrics. High Voltage. Absolute Electrical Measurements.

Metrology. Photometry and Colorimetry. Refractometry. Photographic Research. Length. Engineering Metrology. Mass and Volume.

Heat. Temperature Physics. Heat Measurements. Cryogenic Physics. Equation of State. Statistical Physics. Radiation Physics. X-ray. Radioactivity. Radiation Theory. High Energy Radiation. Radiological Equipment. Nucleonic Instrumentation. Neutron Physics.

Analytical and Inorganic Chemistry. Pure Substances. Spectrochemistry. Solution Chemistry. Standard Reference Materials. Applied Analytical Research. Crystal Chemistry.

Mechanics, Sound, Pressure and Vacuum, Fluid Mechanics, Engineering Mechanics, Rheology, Combustion Controls,

Polymers. Macromolecules: Synthesis and Structure. Polymer Chemistry. Polymer Physics. Polymer Characterization. Polymer Evaluation and Testing. Applied Polymer Standards and Research. Dental Research.

Metallurgy. Engineering Metallurgy. Metal Reactions. Metal Physics. Electrolysis and Metal Deposition. Inorganic Solids. Engineering Ceramics. Glass. Solid State Chemistry. Crystal Growth. Physical Properties. Crystallography.

Building Research. Structural Engineering. Fire Research. Mechanical Systems. Organic Building Materials. Codes and Safety Standards. Heat Transfer. Inorganic Building Materials. Metallic Building Materials.

Applied Mathematics. Numerical Analysis. Computation. Statistical Engineering. Mathematical Physics. Operations Research.

Data Processing Systems. Components and Techniques. Computer Technology. Measurements Automation. Engineering Applications. Systems Analysis.

Atomic Physics. Spectroscopy. Infrared Spectroscopy. Far Ultraviolet Physics. Solid State Physics. Electron Physics. Atomic Physics. Plasma Spectroscopy.

Instrumentation. Engineering Electronics. Electron Devices. Electronic Instrumentation. Mechanical Instruments. Basic Instrumentation.

Physical Chemistry. Thermochemistry. Surface Chemistry. Organic Chemistry. Molecular Spectroscopy. Elementary Processes. Mass Spectrometry. Photochemistry and Radiation Chemistry.

Office of Weights and Measures.

#### BOULDER, COLO.

#### CRYOGENIC ENGINEERING LABORATORY

Cryogenic Processes. Cryogenic Properties of Solids. Cryogenic Technical Services. Properties of Cryogenic Fluids.

#### CENTRAL RADIO PROPAGATION LABORATORY

Ionosphere Research and Propagation. Low Frequency and Very Low Frequency Research. Ionosphere Research. Prediction Services. Sun-Earth Relationships. Field Engineering. Radio Warning Services. Vertical Soundings Research.

Troposphere and Space Telecommunications. Data Reduction Instrumentation. Radio Noise. Tropospheric Measurements. Tropospheric Analysis. Spectrum Utilization Research. Radio-Meteorology. Lower Atmosphere Physics.

Radio Systems. Applied Electromagnetic Theory. High Frequency and Very High Frequency Research. Frequency Utilization. Modulation Research. Antenna Research. Radiodetermination.

Upper Atmosphere and Space Physics. Upper Atmosphere and Plasma Physics. High Latitude lonosphere Physics. Ionosphere and Exosphere Scatter. Airglow and Aurora. Ionospheric Radio Astronomy.

### RADIO STANDARDS LABORATORY

Radio Standards Physics. Frequency and Time Disseminations. Radio and Microwave Materials. Atomic Frequency and Time-Interval Standards. Radio Plasma. Microwave Physics.

Radio Standards Engineering. High Frequency Electrical Standards. High Frequency Calibration Services. High Frequency Impedance Standards. Microwave Calibration Services. Microwave Circuit Standards. Low Frequency Calibration Services.

Joint Institute for Laboratory Astrophysics-NBS Group (Univ. of Colo.).



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