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NATIONAL BUREAU OF STANDARDS REPORT

NBS PROJECT

NBS REPORT

1003-20-4702

June 4, 1953

2546

PROGRESS REPORT

Air Conditioning in Underground Structures

November 1, 1952 to April 30, 1953.

by

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Heating and Air Conditioning Section
Building Technology Division.



U. S. DEPARTMENT OF COMMERCE
NATIONAL BUREAU OF STANDARDS

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PROGRESS REPORT

Air Conditioning in Underground Structures

I. INTRODUCTION

During the period from November 1, 1952 to April 31, 1953, tests have been continued in the underground test chamber at Mount Weather, mathematical approaches to the theory of heat transfer to a rock mass bounding an underground space have been studied and are compiled and presented in this report, data from previous tests were analyzed, revisions were made in the Engineering Manual, Part XVI, Chapter 3, and preparations were made for future testing at Mount Weather, Va. and Fort Ritchie, Maryland.

II. TESTS PERFORMED IN UNDERGROUND TEST CHAMBER

- Test Condition 8 - Determination of heat and moisture load without ventilation or simulated occupancy from November 10 to November 26 while maintaining constant conditions of 75° DB and 50% R.H. with the air conditioning system.
- Test Condition 9 - Conditions were the same as test condition 8 except condenser water reheat was used to reduce the electric reheat November 26 to December 5.
- Test Condition 10 - Steady state heat at 75°F air temperature from December 5 to January 5, 1953. No dehumidification.
- Test Condition 11 - Steady state heating at 75°F air temperature with ventilation air from January 5 to February 11.
- Test Condition 12 - Test condition 10 repeat from February 11 to March 30.
- Test Condition 13 - Test condition 11 repeat now in progress.

THE PROBLEMS OF THE AIR FORCE

1. INTRODUCTION

During the period from November 1, 1955 to April 30, 1956, there have been changes in the composition of the Air Force, particularly in the number of active personnel. The number of active personnel has increased from 1,000,000 in November 1955 to 1,100,000 in April 1956. This increase is due to a number of factors, including the expansion of the Air Force's operations and the increase in the number of personnel assigned to the Air Force's various commands and units.

II. THE AIR FORCE'S OPERATIONS

The Air Force's operations are divided into three main categories: strategic, tactical, and support. Strategic operations are those operations that are designed to achieve the Air Force's overall mission. Tactical operations are those operations that are designed to achieve the Air Force's tactical objectives. Support operations are those operations that are designed to support the Air Force's strategic and tactical operations.

The Air Force's operations are also divided into three main categories: air-to-air, air-to-ground, and air-to-air-to-ground. Air-to-air operations are those operations that are designed to engage and destroy enemy aircraft. Air-to-ground operations are those operations that are designed to attack and destroy enemy ground targets. Air-to-air-to-ground operations are those operations that are designed to attack and destroy enemy ground targets from the air.

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III. MATHEMATICAL APPROACHES TO HEAT TRANSFER TO UNDERGROUND SPACES

A review of the mathematical approaches to the transfer of heat to the rock surrounding an underground chamber shows that mathematical treatment of the elementary shapes such as the plane surface, circular cylinder and sphere bounded by a medium approaching infinite thickness is found in Carslaw and Jaeger, "Conduction of Heat in Solids". While for the most part the actual equations involving heat transfer are complicated, they may be reduced by numerical integration or approximation and plotted in graphical or tabular form for design application.

Configuration of actual underground installations may be approximated by one or more of the elementary shapes. Considering an underground room to be an assembly of plane surfaces (floor, ceiling and walls) neglects the heat flow into the corners and edges, whereas likening it to a cylinder (lateral surface) neglects the heat flow into ends of the cylinder. A sphere would rarely be an approximation for an actual installation.

To the above named shapes two different boundary conditions can be applied; namely, the constant heat flux case and the constant surface temperature case.

I. Heat transferred to a solid bounding an elementary shape with a constant heat flux and the initial temperature of the solid equal to zero on an arbitrary datum plane.

A. Linear heat flow to a medium of semi-infinite depth from a plane surface.

1. Temperature at depth x

$$\theta = \frac{Q}{K} \sqrt{\alpha t} \left(2 \operatorname{ierfc} \frac{x}{2 \sqrt{\alpha t}} \right)$$

Values of '2 ierfc' of the argument are shown in tabular form in Table 2.

THE UNIVERSITY OF CHICAGO
DEPARTMENT OF MATHEMATICS

A series of the following problems will be assigned to students of the Department of Mathematics of the University of Chicago. The student should show that the following conditions are satisfied: (1) The function $f(x)$ is continuous on the interval $[a, b]$. (2) The function $f(x)$ is differentiable on the interval (a, b) . (3) The function $f(x)$ has a local maximum at $x = c$. (4) The function $f(x)$ has a local minimum at $x = d$. (5) The function $f(x)$ is concave up on the interval (a, c) . (6) The function $f(x)$ is concave down on the interval (c, d) . (7) The function $f(x)$ is concave up on the interval (d, b) . (8) The function $f(x)$ is concave down on the interval (a, d) . (9) The function $f(x)$ is concave up on the interval (d, b) . (10) The function $f(x)$ is concave down on the interval (a, d) .

Let $f(x)$ be a function defined on the interval $[a, b]$. Suppose that $f(x)$ is continuous on $[a, b]$ and differentiable on (a, b) . Let c and d be points in (a, b) such that $f'(c) = 0$ and $f'(d) = 0$. Suppose also that $f''(c) < 0$ and $f''(d) > 0$. Show that $f(x)$ has a local maximum at $x = c$ and a local minimum at $x = d$. Also show that $f(x)$ is concave up on (a, c) and (d, b) , and concave down on (c, d) and (a, d) .

To the student who solves the above problem, the following question may be asked: Why is it necessary to assume that $f''(c) < 0$ and $f''(d) > 0$? Can you give an example of a function $f(x)$ which has a local maximum at $x = c$ and a local minimum at $x = d$, but for which $f''(c) = 0$ and $f''(d) = 0$?

I. Let $f(x)$ be a function defined on the interval $[a, b]$. Suppose that $f(x)$ is continuous on $[a, b]$ and differentiable on (a, b) . Let c and d be points in (a, b) such that $f'(c) = 0$ and $f'(d) = 0$. Suppose also that $f''(c) < 0$ and $f''(d) > 0$. Show that $f(x)$ has a local maximum at $x = c$ and a local minimum at $x = d$. Also show that $f(x)$ is concave up on (a, c) and (d, b) , and concave down on (c, d) and (a, d) .

II. Let $f(x)$ be a function defined on the interval $[a, b]$. Suppose that $f(x)$ is continuous on $[a, b]$ and differentiable on (a, b) . Let c and d be points in (a, b) such that $f'(c) = 0$ and $f'(d) = 0$. Suppose also that $f''(c) < 0$ and $f''(d) > 0$. Show that $f(x)$ has a local maximum at $x = c$ and a local minimum at $x = d$. Also show that $f(x)$ is concave up on (a, c) and (d, b) , and concave down on (c, d) and (a, d) .

$$\left(\frac{1}{x^2} \right)' = -\frac{2}{x^3}$$

Let $f(x) = \frac{1}{x^2}$. Then $f'(x) = -\frac{2}{x^3}$. Let $c = 1$ and $d = -1$. Then $f'(1) = -2$ and $f'(-1) = 2$. Also $f''(1) = 6$ and $f''(-1) = -6$. Show that $f(x)$ has a local minimum at $x = 1$ and a local maximum at $x = -1$. Also show that $f(x)$ is concave up on $(1, \infty)$ and $(-\infty, -1)$, and concave down on $(-1, 1)$.

2. Temperature at $x = 0$.

$$\theta = \frac{2Q}{k} \sqrt{\frac{\alpha t}{\pi}} = 1.1284 \frac{Q}{k} \sqrt{\alpha t}$$

B. Heat flow to the solid bounded internally by a circular cylinder (radius = a).

1. Temperature at $r > a$ in the operational form

$$\bar{\theta} = \frac{Q}{k} \frac{K_0(qr)}{pq K_1(qa)}, \quad q^2 = P/\alpha$$

Solution of this operational form can be made for small values of time by use of asymptotic expansions of the Bessel functions and the use of a Laplace transform

2. Temperature at $r = a$.

$$\bar{\theta} = \frac{Q}{k} \frac{K_0(qa)}{pq K_1(qa)}$$

Solution for small values of time:

$$\theta = \frac{aQ}{k} \left(\frac{2\sqrt{B}}{\sqrt{\pi}} - \frac{B}{2} + \frac{B^{3/2}}{2\pi^{1/2}} - \frac{3}{16} B^2 \right)$$

where $B = \frac{\alpha t}{a^2}$ and is restricted to values

less than 0.3. Values of the function of B in the parenthesis appear in Table 1.

C. Heat flow to the solid bounded internally by a sphere (radius = a).

1. Temperature at radius $r > a$.

$$\theta = \frac{Qa}{k} \left\{ \operatorname{erfc} \left(\frac{r-a}{2\sqrt{\alpha t}} \right) - \frac{\left(\frac{r-a}{a} + \frac{\alpha t}{a^2} \right)}{e} \operatorname{erfc} \left(\frac{r-a}{2\sqrt{\alpha t}} + \sqrt{\frac{\alpha t}{a^2}} \right) \right\}$$

Values of 'erfc' of the argument are shown in tabular form in Table 2.

$$\sqrt{x} = \frac{1}{2} \sqrt{\frac{x}{\pi}} - \frac{1}{2} \sqrt{\frac{x}{\pi}} = 0$$

Let $f(x) = \frac{1}{2} \sqrt{\frac{x}{\pi}} - \frac{1}{2} \sqrt{\frac{x}{\pi}}$ be a function defined on $[0, \infty)$.

1. Derivative of $f(x) > 0$ in the interval $(0, \infty)$.

$$f'(x) = \frac{1}{4} \sqrt{\frac{1}{\pi}} - \frac{1}{4} \sqrt{\frac{1}{\pi}} = 0$$

Since $f'(x) = 0$ for all $x > 0$, the function $f(x)$ is constant on $(0, \infty)$. The only value of $f(x)$ is 0 for all $x > 0$.

2. Derivative of $f(x) = 0$.

$$f'(x) = \frac{1}{4} \sqrt{\frac{1}{\pi}} - \frac{1}{4} \sqrt{\frac{1}{\pi}} = 0$$

Since $f'(x) = 0$ for all $x > 0$, the function $f(x)$ is constant on $(0, \infty)$.

$$\left(\frac{1}{2} \sqrt{\frac{x}{\pi}} - \frac{1}{2} \sqrt{\frac{x}{\pi}} \right)' = \frac{1}{4} \sqrt{\frac{1}{\pi}} - \frac{1}{4} \sqrt{\frac{1}{\pi}} = 0$$

Since $f'(x) = 0$ for all $x > 0$, the function $f(x)$ is constant on $(0, \infty)$.

Let $f(x) = \frac{1}{2} \sqrt{\frac{x}{\pi}} - \frac{1}{2} \sqrt{\frac{x}{\pi}}$ be a function defined on $[0, \infty)$.

3. Let $f(x) = \frac{1}{2} \sqrt{\frac{x}{\pi}} - \frac{1}{2} \sqrt{\frac{x}{\pi}}$ be a function defined on $[0, \infty)$.

1. Derivative of $f(x) > 0$ in the interval $(0, \infty)$.

$$f'(x) = \frac{1}{4} \sqrt{\frac{1}{\pi}} - \frac{1}{4} \sqrt{\frac{1}{\pi}} = 0$$

$$\left(\frac{1}{2} \sqrt{\frac{x}{\pi}} - \frac{1}{2} \sqrt{\frac{x}{\pi}} \right)' = \frac{1}{4} \sqrt{\frac{1}{\pi}} - \frac{1}{4} \sqrt{\frac{1}{\pi}} = 0$$

$$\left(\frac{1}{2} \sqrt{\frac{x}{\pi}} - \frac{1}{2} \sqrt{\frac{x}{\pi}} \right)' = \frac{1}{4} \sqrt{\frac{1}{\pi}} - \frac{1}{4} \sqrt{\frac{1}{\pi}} = 0$$

Since $f'(x) = 0$ for all $x > 0$, the function $f(x)$ is constant on $(0, \infty)$.

2. Temperature at radius $r = a$.

$$\theta = \frac{Qa}{k} \left[1 - \frac{e^{-\frac{\alpha t}{a^2}}}{\text{erfc} \left(\frac{\alpha t}{a^2} \right)^{1/2}} \right]$$

II. Heat transferred to a solid bounding an elementary shape with a constant surface temperature and the initial temperature of the solid equal to zero on an arbitrary datum plane. It must be noted that for these conditions the heat flux is infinite for time equal to zero and therefore the equations are valid for t greater than zero.

A. Linear heat flow to a medium of semi-infinite depth from a flat plane.

1. Temperature at depth x .

$$\theta = V \text{erfc} \frac{x}{2 \sqrt{\alpha t}}$$

2. Heat flux at $x = 0$

$$H = \frac{kV}{\sqrt{\pi \alpha t}}$$

B. Heat flow to a solid bounded internally by a circular cylinder (radius = a)

1. Temperature at radius $r > a$.

$$\theta = V \left(\frac{a}{r} \right)^{1/2} \text{erfc} \left(\frac{r-a}{2 \sqrt{\alpha t}} \right) + \frac{V(r-a)}{8 \sqrt{\frac{ar^3}{\alpha t}}} \left(2 \text{ierfc} \frac{r-a}{2 \sqrt{\alpha t}} \right)$$

reasonable for $t < 20,000$ hrs., and $a > 10$ ft.

2. Heat flux at $r = a$

$$H = \frac{4kV}{a\pi^2} \int_0^{\infty} \frac{e^{-\alpha u^2 t}}{J_0^2(ua) + Y_0^2(ua)} \frac{du}{u}$$

$$= \frac{4kV}{a^2} I \left(0, 1; \frac{\alpha t}{a^2} \right)$$

where values of the integral

$I \left(0, 1; \frac{\alpha t}{a^2} \right)$ appear in tabular form

in Table 2.

C. Heat flow to a solid bounded internally by a sphere (radius = a).

1. Temperature at radius $r > a$.

$$\theta = \frac{aV}{r} \operatorname{erfc} \frac{r-a}{2\sqrt{\alpha t}}$$

2. Heat flux at $r = a$

$$H = kV \left[\frac{1}{\sqrt{\pi \alpha t}} + \frac{1}{a} \right]$$

Nomenclature:

- θ = temperature above arbitrary datum plane, °F
- V = temperature at $x=0$ or $r=a$ for constant temperature case, °F
- Q = constant heat flux, BTU/hr-ft²
- H = heat flux (variable), BTU/hr-ft²
- t = time, hrs
- k = thermal conductivity, BTU/hr-ft°F
- α = thermal diffusivity, ft²/hr
- x = depth into semi-infinite solid, ft.
- a = radius of circular cylinder or sphere, ft.
- r = radius of concentric cylinder or sphere composed of solid at $r > a$, ft.

$$B = \frac{\alpha t}{a^2}, \text{ dimensionless}$$

$$\operatorname{erfc} y = \frac{2}{\sqrt{\pi}} \int_y^{\infty} e^{-\beta^2} d\beta$$

$$\operatorname{ierfc} y = \frac{1}{\sqrt{\pi}} e^{-y^2} = y \operatorname{erfc} y$$

IV. REVISIONS OF ENGINEERING MANUAL

Part XVI - Chapter 3

Certain tentative revisions in the Engineering Manual, XVI Chapter 3, "Heating, Ventilating and Moisture Control", were made by B. A. Peavy of this Bureau and J. C. Letts of the O.C.E. The additions to the manual were mainly concerned with three conditions of occupancy for which the performance of an air conditioning system and related equipment must be designed. Some deletions were made in the manual because of their redundancy. Copies of the manual with these tentative revisions were presented to interested parties for their comment and review. Further work to be accomplished in writing of the manual will be concerned with work now being performed by this Bureau.

V. FUTURE EXPERIMENTATION - MT. WEATHER, VA.

1. Underground Test Chamber

Test Condition 14 - Test condition 3 repeat temperature drop with minimum heat supply and no ventilation.

Test Condition 15 - Apply refrigeration to chamber until room temperature reaches 40°F.

Test Condition 16 - Test condition 15 with use of ventilation air.

Test Condition 17 - Repeat test condition 1, constant heat input at about 75,000 BTU/hr until temperature of chamber is 75°F.

2. Underground Spray Pond Heat Exchanger

The spray pond was ready to operate before the finish of this period, but interference due to blasting by Bureau of Mines operations halted this test. Testing will begin May 11, with the test conditions for the various spray pond tests controlled as follows:

Test Condition 1 - A constant heat input rate to the spray water of approximately 60,000 BTU/hr will be used until the temperature of the pond water reaches 100°F.

Test Condition 2 - Maintain the temperature of the pond water at 100°F.

Test Conditions 3 and 4. Repeat test conditions 1 and 2 with use of stagnant pond instead of using sprays.

3. Tunnel Ventilation

Preparations are being made for determining the heat exchange between tunnel walls and an air stream. Tests will begin during the month of June.

VI. USE OF AN OCCUPIED UNDERGROUND SPACE FOR TEMPERATURE STUDIES.

Background:

Following a visit to an underground space near Fort Ritchie, Maryland, it was concluded that some of the data needed for correlation with present studies at Mount Weather, Va. could be obtained by making appropriate tests in the underground space there. Seasonal heating or cooling of the ventilation air by rock wall shafts will occur at this site and the amount of heat exchanged between ventilation air and the rock mass could be evaluated. Also studies of the heat transferred to the rock mass surrounding the occupied structure could be made.

Test Description 1 - ...
Test Description 2 - ...
Test Description 3 - ...

1. General Information

The purpose of this test is to determine the ...
The test is conducted under the following conditions ...
The test results are as follows ...

Test Description 4 - ...
Test Description 5 - ...

Test Description 6 - ...
Test Description 7 - ...

2. Test Results

The test results are as follows ...
The test results are as follows ...

IT IS THE POLICY OF THE COMPANY ...
TO MAINTAIN THE CONFIDENTIALITY OF ALL INFORMATION ...

Background

Following a visit to the ...
The test results are as follows ...
The test results are as follows ...
The test results are as follows ...

Proposed Work to be Done:

Temperature sensing elements will be installed on the rock surface and at selected depths in the rock in the ventilation air shafts and inside and outside of the structure proper. Other instruments will be provided to measure air flow, heat flux to rock mass, and relative humidity. These instruments and their locations will be carefully selected so that measurements would provide data for computations of heat transfer rates. During this reporting period thermocouples were installed at six positions on the rock surface and at selected depths in the rock. The remaining work will be finished during the month of June.

TABLE 1

B	f (B)	B	f (B)
.001	.0321	0.050	.2302
.002	.0495	0.052	.2341
.004	.0694	0.054	.2382
.006	.0844	0.056	.2422
.008	.0971	0.058	.2461
.010	.1081	0.060	.2499
.012	.1176		
.014	.1269	0.065	.2591
.016	.1348	0.070	.2677
.018	.1430	0.075	.2765
.020	.1503	0.080	.2843
.022	.1572	0.085	.2921
.024	.1636	0.090	.2996
.026	.1700		
.028	.1760	0.10	.3138
.030	.1819	0.11	.3273
.032	.1859	0.12	.3401
.034	.1910	0.13	.3519
.036	.1963	0.14	.3633
.038	.2009	0.15	.3741
.040	.2074	0.16	.3847
.042	.2123	0.17	.3937
.044	.2210		
.048	.2258		

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1917	1916	1915	1914
1000	1000	1000	1000
900	900	900	900
800	800	800	800
700	700	700	700
600	600	600	600
500	500	500	500
400	400	400	400
300	300	300	300
200	200	200	200
100	100	100	100
0	0	0	0
100	100	100	100
200	200	200	200
300	300	300	300
400	400	400	400
500	500	500	500
600	600	600	600
700	700	700	700
800	800	800	800
900	900	900	900
1000	1000	1000	1000

TABLE 2

Table of Functions Used in Heat Transfer Equations

y	erfc y	2 ierfc y	I (0, 1; y)
0.00	1.0000	1.1284	-
.01	.9887	1.1085	15.122
.02	.9774	1.0888	11.033
.03	.9662	1.0694	9.218
.04	.9549	1.0502	8.135
.05	0.9436	1.0312	7.359
.06	.9324	1.0124	6.846
.07	.9212	0.9939	6.421
.08	.9099	0.9756	6.076
.09	.8987	0.9575	5.790
0.10	.8875	0.9396	5.549
.11	.8764	0.9220	5.340
.12	.8633	0.9046	5.158
.13	.8542	0.8874	4.998
.14	.8431	0.8704	4.854
.15	.8320	0.8537	4.726
.16	.8210	0.8371	4.609
.17	.8101	0.8208	4.503
.18	.7991	.8047	4.405
.19	.7882	.7889	4.315
0.20	.7773	.7732	4.232
.21	.7665	.7578	4.155
.22	.7557	.7426	4.083
.23	.7450	.7275	4.016
.24	.7343	.7128	3.953
.25	.7237	.6982	3.894
.26	.7131	.6838	3.838
.27	.7026	.6697	3.785
.28	.6922	.6557	3.735
.29	.6818	.6420	3.688
.30	.6714	.6284	3.643
.31	.6611	.6151	3.600
.32	.6509	.6020	3.559
.33	.6408	.5891	3.520
.34	.6307	.5764	3.482
.35	.6206	.5639	3.446
.36	.6106	.5515	3.412
.37	.6008	.5394	3.379
.38	.5909	.5275	3.348
.39	.5813	.5158	3.317

- - -

TABLE 2 - continued

y	erfc y	2 ierfc y	I (0, 1; y)
.40	.5716	.5043	3.288
.41	.5620	.4929	3.259
.42	.5526	.4818	3.232
.43	.5431	.4708	3.206
.44	.5338	.4600	3.180
.45	.5245	.4495	3.156
.46	.5154	.4391	3.132
.47	.5063	.4289	3.109
.48	.4973	.4188	3.086
.49	.4884	.4090	3.065
.50	.4795	.3993	3.044
.51	.4708	.3898	3.023
.52	.4621	.3805	3.003
.53	.4535	.3713	2.984
.54	.4451	.3623	2.965
.55	.4367	.3535	2.947
.56	.4284	.3448	2.929
.57	.4202	.3364	2.912
.58	.4121	.3280	2.895
.59	.4041	.3199	2.878
.60	.3961	.3119	2.862
.61	.3883	.3040	2.847
.62	.3806	.2963	2.831
.63	.3729	.2888	2.816
.64	.3654	.2814	2.802
.65	.3580	.2742	2.787
.66	.3506	.2671	2.773
.67	.3434	.2602	2.760
.68	.3362	.2545	2.746
.69	.3292	.2467	2.733
0.70	.3222	.2402	2.720
.71	.3154	.2338	2.708
.72	.3086	.2276	2.695
.73	.3019	.2215	2.683
.74	.2953	.2155	2.671
.75	.2888	.2097	2.660
.76	.2825	.2040	2.648
.77	.2762	.1984	2.637
.78	.2699	.1929	2.626
.79	.2639	.1876	2.616

TABLE 2 - continued

y	erfc y	2 ierfc y	I (0, 1;y)
0.80	.2579	.1823	2.605
.81	.2519	.1772	2.595
.82	.2462	.1723	2.584
.83	.2405	.1674	2.574
.84	.2349	.1626	2.565
.85	.2293	.1580	2.555
.86	.2239	.1535	2.545
.87	.2186	.1490	2.536
.88	.2133	.1447	2.527
.89	.2082	.1405	2.518
0.90	.2031	.1364	2.509
0.91	.1981	.1324	2.500
0.92	.1932	.1285	2.492
0.93	.1884	.1247	2.483
0.94	.1837	.1209	2.475
0.95	.1791	.1173	2.467
0.96	.1746	.1138	2.459
0.97	.1701	.1103	2.451
0.98	.1658	.1070	2.443
0.99	.1615	.1037	2.435
1.00	.1573	.1005	2.427
1.02	.1492	.0944	
1.04	.1414	.0886	
1.06	.1339	.0831	
1.08	.1267	.0779	
1.10	.1197	.0729	2.357
1.12	.1132	.0683	
1.14	.1069	.0639	
1.16	.1009	.0597	
1.18	.0952	.0558	
1.20	.0897	.0521	2.259
1.25	.0771	.0438	
1.30	.0660	.0366	2.240
1.35	.0562	.0305	
1.40	.0477	.0253	2.191
1.50			2.147
1.60			2.106
1.70			2.069
1.80			2.036
1.90			2.004

y	I (0, 1; y)
2.0	1.975
2.5	1.856
3.0	1.767
3.5	1.697
4.0	1.639
4.5	1.591
5.0	1.550
6.0	1.483
7.0	1.429
8.0	1.386
9.0	1.349
10.0	1.317
20.0	1.138
30.0	1.052
40.0	0.997
60.	0.928
80	0.884
100	0.853

VII. RESULTS OF AN INITIAL WARM-UP PERIOD - APRIL 23 TO MAY 15, 1952.

Object:

The object of this test was to determine the time needed to bring the temperature of an underground chamber up to a temperature within the human occupancy comfort range by the means of a constant heat input rate, and also to determine empirically the equations of heat transfer to the mass bounding the chamber and the relation of these empirical equations to the theoretical approaches listed in Part III of this report.

Description of Underground Chamber and Equipment:

The underground chamber, the dimensions of which are 100'x35'x10' high, is contained in and adjacent to an experimental mine operated by the Bureau of Mines at Mount Weather, Virginia. The chamber is approximately 215 feet below the surface of the ground and 1200 feet from the surface in a horizontal direction. The rock mass bounding the chamber consists mainly of greenstone with a scattering of epidote and quartz, and traces of various other minerals. Petrographically, the greenstone is a metamorphic basalt partially colored green by the presence of chlorite.

Measurements of the surface area of the walls, floor and ceiling were made and showed that the projected surface area was approximately 10,000 square feet. Physical determinations of greenstone rock from the excavation were made at this Bureau and the results were:

Density, ρ	= 186 lbs/ft ³
Specific heat, c	= 0.2 BTU/lb. °F
Thermal Conductivity (cores), k	= 1.45 BTU/hr.ft.°F
Thermal diffusivity, α	= 0.039 ft ² /hr

The apparent porosity of greenstone samples tested by the Bureau of Mines was 0.50 percent.

As shown in Figures 11 and 12, the walls and ceiling are painted white and the floor paved with concrete. Figure 1 shows plan and elevation views of the chamber and arrangement of mechanical equipment and air distribution ductwork. Air was forced by the circulating fan (1) into the ductwork past electric strip heaters (5) to the diffusers (6) and the air from the chamber was returned to the circulating fan through the air return filters (7) and the plenum chamber.

1957. Summary of the initial findings
1957 - 1958. Summary of the initial findings

Summary

The object of this study was to determine the effect
of the various factors on the occurrence of the disease
in the various areas. The results of the study are
summarized in the following table. The results of the
study are summarized in the following table. The results
of the study are summarized in the following table.

Summary of the results of the study

The following table shows the results of the study
in the various areas. The results of the study are
summarized in the following table. The results of the
study are summarized in the following table. The results
of the study are summarized in the following table.

The following table shows the results of the study
in the various areas. The results of the study are
summarized in the following table. The results of the
study are summarized in the following table.

Area	1957	1958
A	100	120
B	150	180
C	200	250
D	250	300
E	300	350
F	350	400
G	400	450
H	450	500
I	500	550
J	550	600
K	600	650
L	650	700
M	700	750
N	750	800
O	800	850
P	850	900
Q	900	950
R	950	1000

The following table shows the results of the study
in the various areas. The results of the study are
summarized in the following table. The results of the
study are summarized in the following table.

The following table shows the results of the study
in the various areas. The results of the study are
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of the study are summarized in the following table.

Fifteen twelve-foot long thermocouple poles were placed at selected positions (Figure 2) in the rock. Thermocouples had been previously attached to these poles at intervals--one half foot intervals up to six feet and one foot intervals from six to twelve feet. Room air temperatures were measured at twenty plan positions and at each plan position at heights of 2, 30, 60, and 90 inches from the floor. The thermocouples were copper-constantan and temperatures were measured by them in conjunction with an indicating potentiometer located in an instrument shed built within the chamber.

Test Procedure:

With the initial temperature in the rock up to 12 feet in depth practically uniform at 53.5°F, a constant heat input of 17.8 kilowatt or 60,800 BTU/hr was supplied to the test chamber. At regular intervals during the test, temperatures of the rock surface, rock depth room air, wet and dry bulb were recorded as well as the electric energy input as measured by kilowatt-hour meters.

The test was arbitrarily terminated at the time when the average plane rock surface temperature reached 70°F. This time was 522 hours or 21.75 days.

Results:

Figure 3 is a plot of the average rock temperature (computed from the average of the temperatures on the fifteen poles) against depth in the rock, with time from the start of the test as a parameter. Figures 4-8 show temperature distributions at various crosssections in the rock.

Figure 9 is a log-log plot of time against average temperature rise above the initial rock temperature of 53.5°F with depth in the rock as a parameter, and also the average temperature rise of the room air with time. The average room air temperature was approximately 6°F above that of the rock surface temperature throughout the test and like the rock surface temperature rise plots as a substantially straight line on log-log paper. The heat transfer from the room air to the rock surface appears to obey Newtons Law:

$$Q = h A T \quad (1)$$

where the coefficient 'h' in this case was approximately 1.0 BTU/hr ft²°F.

An empirical equation of average rock surface temperature rise with time has been computed from the data by the method of averages, namely:

$$\theta = 0.69t^{1/2} \quad (2)$$

Referring to Part III of this report, equations relating temperature rise at the rock surface, with the elapsed time of heating for a constant heat flux into a mass approaching infinite thickness, are for the plane surface, and the cylindrical case:

$$\theta = \frac{2Q}{k} \sqrt{\frac{\alpha t}{\pi}} \quad (3)$$

$$\theta = \frac{2Q}{k} \left[\sqrt{\frac{\alpha t}{\pi}} + \frac{\alpha t}{4a} + \frac{(\alpha t)^{3/2}}{4a^2(\pi)^{1/2}} - \frac{3(\alpha t)^2}{32a^3} \right] \quad (4)$$

respectively (for nomenclature refer to Part III of this report), where the first term in the cylindrical case is the same as that for the plane surface.

Using the experimental surface temperature data, the constants determined at the Bureau for thermal conductivity and diffusivity, and assuming the equivalent cylindrical radius of the chamber was the average of the radii computed from a) the perimeter and b) the crosssectional area, the heat flux was determined to be 4.49 and 4.90 BTU/hr.ft² for the plane surface and cylindrical case, respectively. Using these values for determining temperatures at a depth in the rock the calculated values are compared with the actual experimental values in Figure 10.

Following is a table showing the heat input to the chamber from readings of watt hour meters compared with the heat stored in the rock computed from the mean temperature rise at various times from the start of the test. Also the depth of perceptible heat penetration is noted.

Time, Hrs.	Electric Heat Input, BTU	Heat in Rock BTU	Heat Penetration ft
49	3,010,300	2,900,000	5.5
100	5,960,000	6,700,000	7.8
170	10,256,000	11,450,000	9.0
290	17,928,000	19,020,000	11.2

to explain the results of the experiments
concerning the effect of the concentration
of the solution on the rate of reaction.

$$v = k[A]^m[B]^n$$

It is assumed that the reaction is of the
type $A + B \rightarrow C$ and that the rate of
reaction is proportional to the product
of the concentrations of the reactants.
The rate of reaction is measured by the
change in concentration of the reactants
over a certain period of time.

$$\frac{1}{v} = \frac{1}{k[A]^m[B]^n}$$

$$\ln \left[\frac{1}{v} \right] = \ln \left[\frac{1}{k} \right] + m \ln [A] + n \ln [B]$$

The above equation shows that the logarithm
of the reciprocal of the rate of reaction
is a linear function of the logarithm of
the concentration of the reactants.

From the above equation it can be seen
that the slope of the straight line
obtained from a plot of $\ln(1/v)$ against
 $\ln[A]$ is equal to the order of reaction
with respect to A. Similarly, the slope
of the straight line obtained from a plot
of $\ln(1/v)$ against $\ln[B]$ is equal to
the order of reaction with respect to B.

It is assumed that the reaction is of the
type $A + B \rightarrow C$ and that the rate of
reaction is proportional to the product
of the concentrations of the reactants.
The rate of reaction is measured by the
change in concentration of the reactants
over a certain period of time.

Time (min)	[A] (mol/l)	[B] (mol/l)	v (mol/l.s)
0	0.100	0.100	0.000
10	0.090	0.090	0.001
20	0.080	0.080	0.002
30	0.070	0.070	0.003
40	0.060	0.060	0.004
50	0.050	0.050	0.005

Discussion and Conclusion:

1. For the duration of this test, the temperature rise at the rock surface was proportional to the square root of the time (Equation 2). This is substantiated by theory (Equations 3 and 4) where the second, third and fourth terms of equation 4 are small in comparison to the first term for small values of time.
2. The coefficient of heat transfer between the air and rock was approximately 1.0 BTU/hr ft²(deg F). This value is approximately what would be expected for this case wherein heat transfer was by natural convection from nearly still air, with no radiation because all surfaces were nearly at the same temperature.
3. The heat balance showed that the heat stored in the rock as computed from the observed temperatures of the rock agreed to within 5% of the measured electrical heat input.
4. Figure 10 shows that the use of the equation for heat transfer to a medium surrounding a cylinder gave better agreement with the experimental data than the equation for heat transfer from a plane surface to a semi-infinite medium. (Refer to Part III of this report, sections I,A,1 and I,B,1.) For the cylindrical case, the agreement between the experimental and computed values was improved with increase in depth from the exposed rock surface.
5. Figures 4 through 8 show isotherms in the rock at various crosssections. The isotherms tend to approach elliptical shape, especially in the smaller crosssections.
6. The constant rate of energy input to the chamber, as measured electrically, was 60,800 BTU/hr, which gives an average heat flux of 6.08 BTU/hr ft² for the measured 10⁴ square feet of projected surface area. The heat flux computed from the heat transfer equations on the basis of surface temperatures and measured rock properties was 4.49 and 4.90 BTU/hrft² for the plane surface and cylindrical equations, respectively. The discrepancy between measured and calculated heat flux is believed to be due to the fact that heat flow from the chamber surfaces took place in three dimensions (diverging as do the radii of a sphere), whereas the equations apply strictly to one-dimensional flow (plane equation) or two dimensional flow (cylinder

1. The first part of the report deals with the general situation in the country during the year 1940. It is a very short and general survey of the situation in the country during the year 1940. It is a very short and general survey of the situation in the country during the year 1940.

2. The second part of the report deals with the general situation in the country during the year 1941. It is a very short and general survey of the situation in the country during the year 1941.

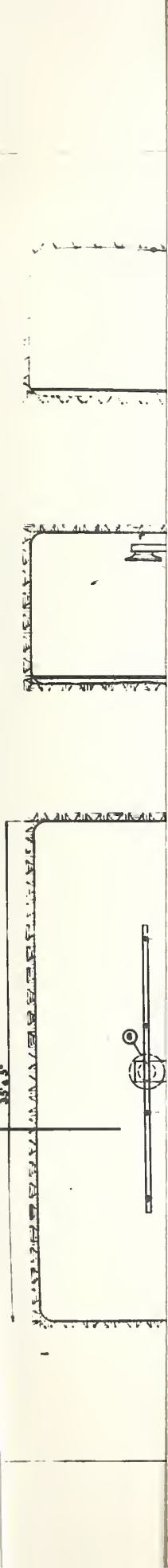
3. The third part of the report deals with the general situation in the country during the year 1942. It is a very short and general survey of the situation in the country during the year 1942.

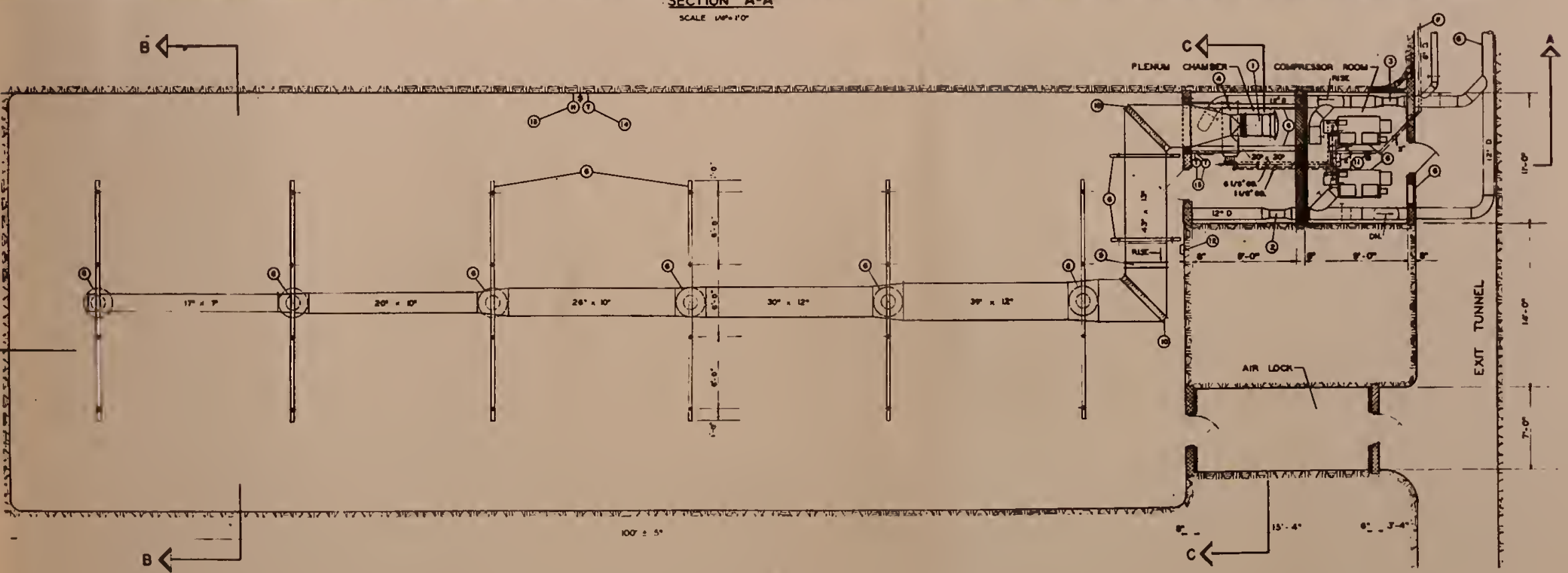
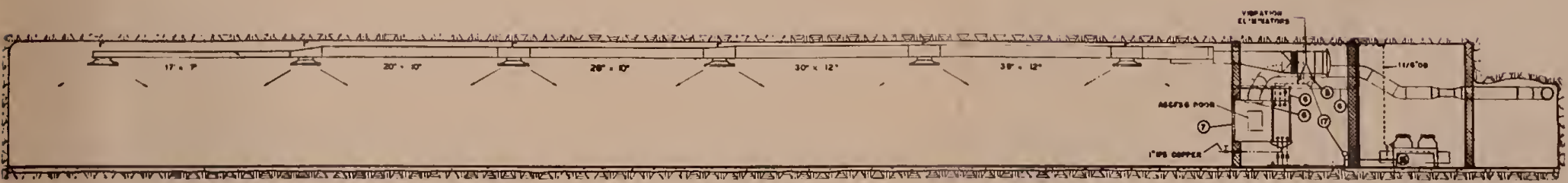
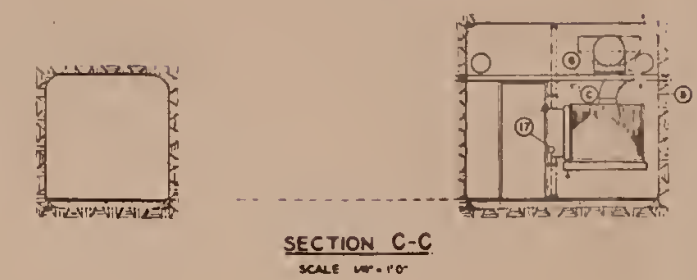
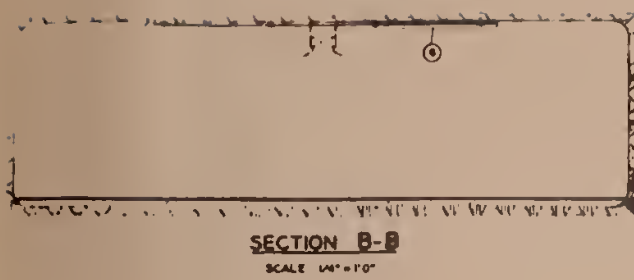
4. The fourth part of the report deals with the general situation in the country during the year 1943. It is a very short and general survey of the situation in the country during the year 1943.

5. The fifth part of the report deals with the general situation in the country during the year 1944. It is a very short and general survey of the situation in the country during the year 1944.

6. The sixth part of the report deals with the general situation in the country during the year 1945. It is a very short and general survey of the situation in the country during the year 1945.

equation). The difference between the measured average input flux and that calculated from the equations is considered due to the extra bulk of rock beyond edges and corners, which caused greater flux at nearby surface areas than at other areas of the chamber, thus causing the average flux to be greater than the value at other areas where the stated equations apply more correctly. For the chamber investigated, the flux which appears appropriate for use in the cited equations was about 30% of the measured input flux.





PLAN FIG. 1
SCALE 1/4" = 1'-0"

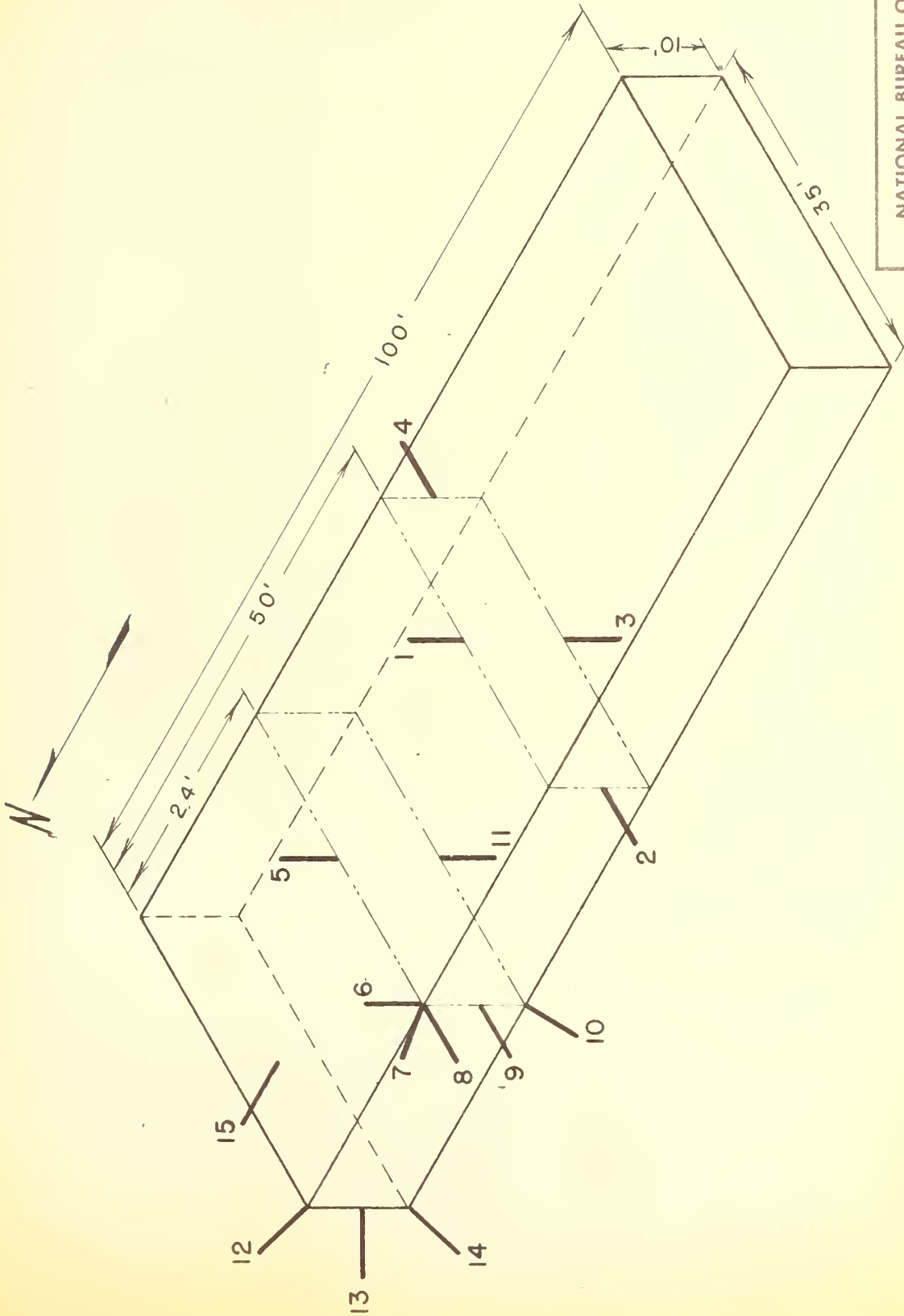
- CONSTRUCTION NOTES
- A ALL SLEEVE & LINTEL OPENINGS PROVIDED BY OTHERS
 - B FAN NO. 1 SUPPORT - 2-7/2 LB ANGLES 4" x 3" x 7/16" 4" LEG DOWN
 - C COOLING COIL SUPPORT - 2 L's 5" x 1 3/4" 87 LB
 - D COOLING COIL SUPPORT - 4 L's 1 1/2" x 1 1/2" x 3/16" 18 LB
 - E DUCTWORK INSTALLATION TO TERMINATE AT THIS POINT INSTALLATION TO OUTSIDE BY OTHERS
 - F CONDENSER WATER PIPING TO TERMINATE AT THIS POINT INSTALLATION TO COOLING TOWER BY OTHERS
 - G DUCTWORK & CONDUIT SUPPORT - 8 L's 3" x 3" x 1/4" 20 FT LONG INSTALLATION BY OTHERS
 - H DUCTWORK SUPPORT - 2 L's 3" x 3" x 1/4" 8 FT LONG INSTALLATION BY OTHERS

EQUIPMENT LIST

ITEM NO.	DESCRIPTION	QUANTITY
1	FAN AXIAL - 8000 CFM 3" TP 440 V 3 Ø 80 -	1
2	FAN AXIAL - 800 CFM 1 1/2" TP 440 V 3 Ø 80 -	1
3	FAN AXIAL - 800 CFM 1 1/2" TP 440 V 3 Ø 80 -	1
4	COOLING COIL 10 Ø SEE DETAIL SHEET M-8	1
5	STRIP HEATER 440 V 3 Ø 80 - SEE DETAIL SHEET M-8	1
6	DIFFUSERS - 1000 CFM EACH	6
7	AIR FILTERS 8500 CFM (20" x 28")	4
8	AIR FILTERS 800 CFM (20" x 20")	2
9	10 HP SELF CONTAINED WATER CHILLER	2
10	VAREO TURBS	2
11	COOLING TOWER PUMP	1
12	STEP CONTROLLER	1
13	HUMIDISTAT	1
14	MODULATING THERMOSTAT (15-90°F)	1
15	MODULATING THERMOSTAT DUCT TYPE (15-85°F)	2
16	CHILLED WATER CONTROL (10-70°F)	1
17	THERMOMETERS (SEE DRAWING M-2)	6

NLS

REVISION	DATE	APP'D	DESCRIPTION	BY
MECHANICAL PLAN				
NATIONAL BUREAU OF STANDARDS WASHINGTON, D.C.				
UNDERGROUND STRUCTURE PILOT PROJECT				
FOR THE OFFICE OF THE CHIEF OF ENGINEERS U.S. ARMY				
DESIGNED BY: T.M.H.		DATE: MAY 5 1954		
DRAWN BY: S.B.		5 55 M 1		
TRACED BY: S.B.		THOMAS H. URDAHL CONSULTING ENGINEER 34 JACKSON PLACE, N.W. WASHINGTON, D.C.		
CHECKED BY: T.M.H.		DATE: MAY 5 1954		
APPROVED:		DATE: MAY 5 1954		



NATIONAL BUREAU OF STANDARDS
WASHINGTON 25, D. C.

DRAFTSMAN DATE SCALE

W. C. G.

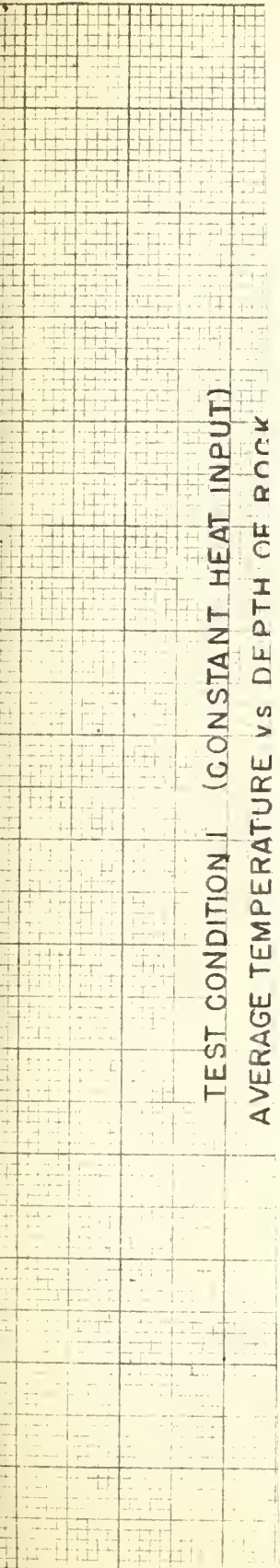
DIV SEC

UNDERGROUND
LABORATORY

FIGURE 2

70

TEST CONDITION I (CONSTANT HEAT INPUT)
AVERAGE TEMPERATURE vs DEPTH OF ROCK



TEST CONDITION I (CONSTANT HEAT INPUT)
AVERAGE TEMPERATURE vs DEPTH OF ROCK

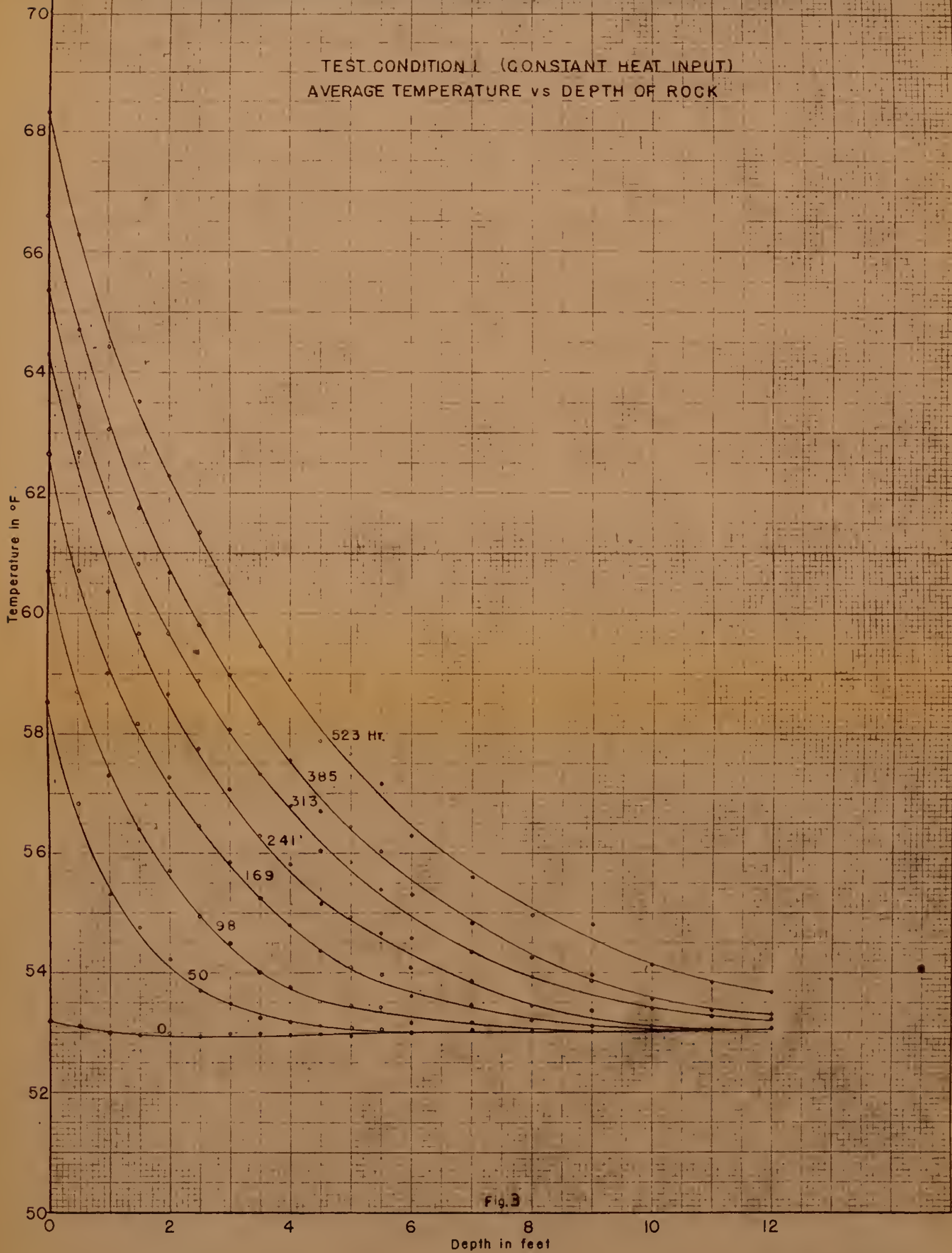
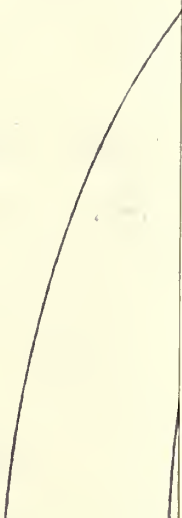


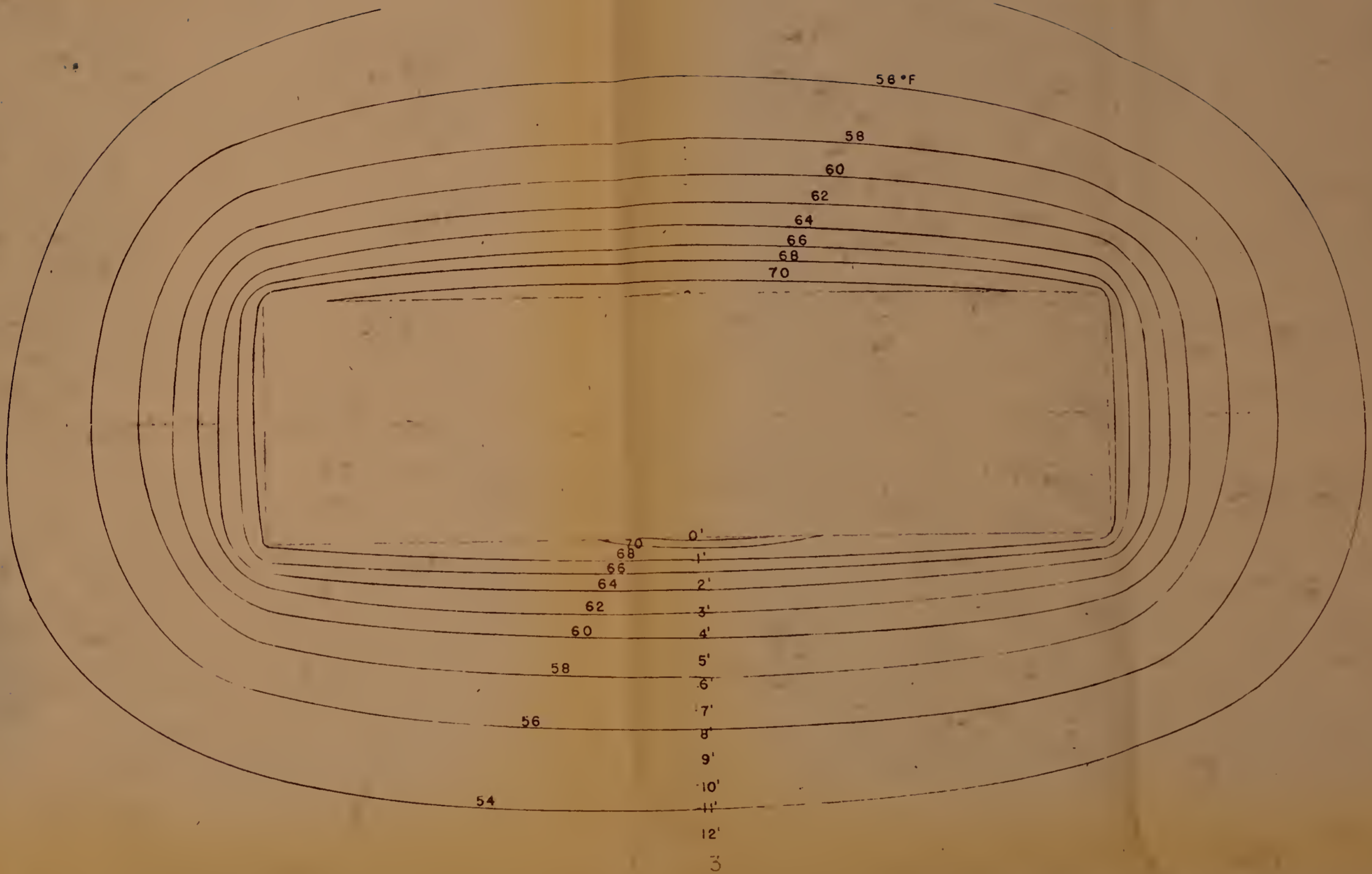
Fig. 3



2







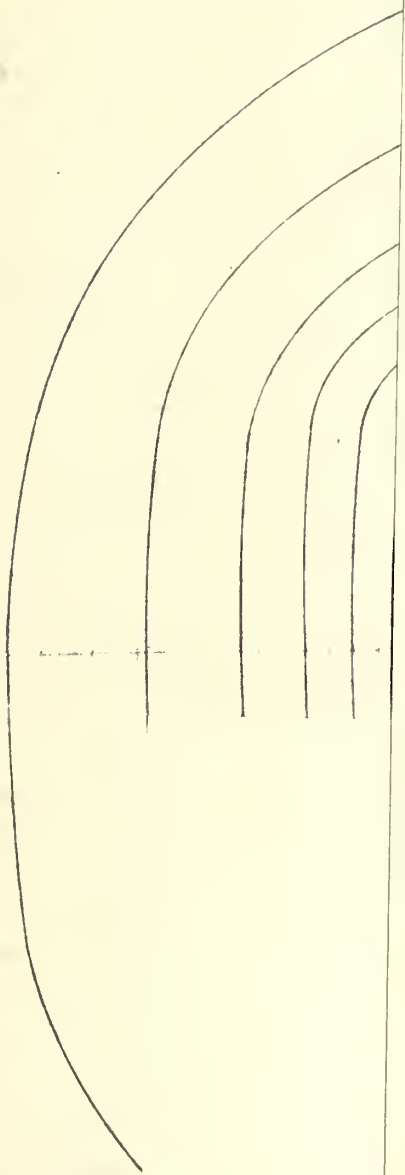
SECTION A-A

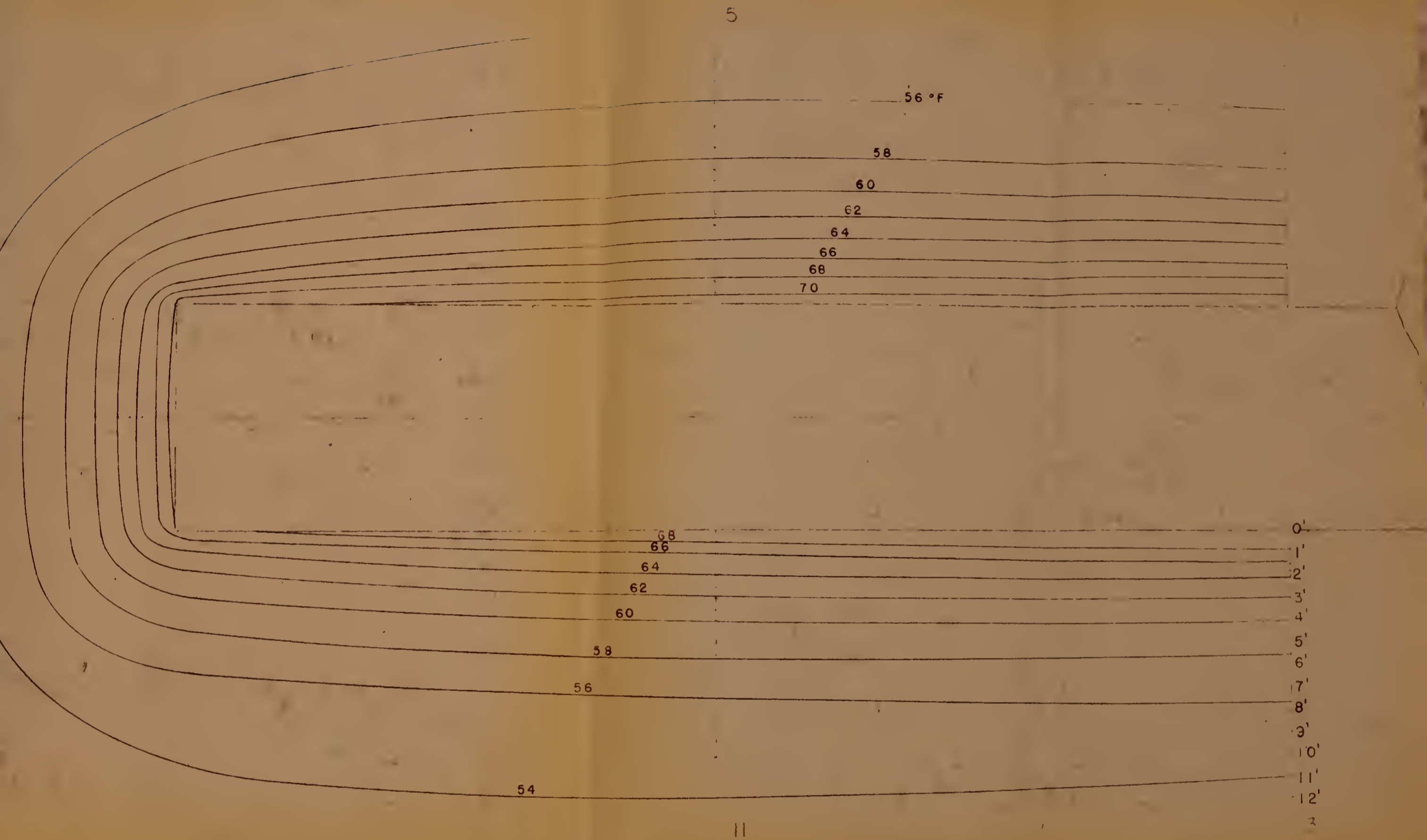
SCALE $\frac{1}{4}'' = 1'-0''$

TEST CONDITION No 1 - HEATING UP PHASE
 TEMPERATURE DISTRIBUTION IN ROCK
 AFTER 521 HOURS

FIGURE 4







SECTION 3-B

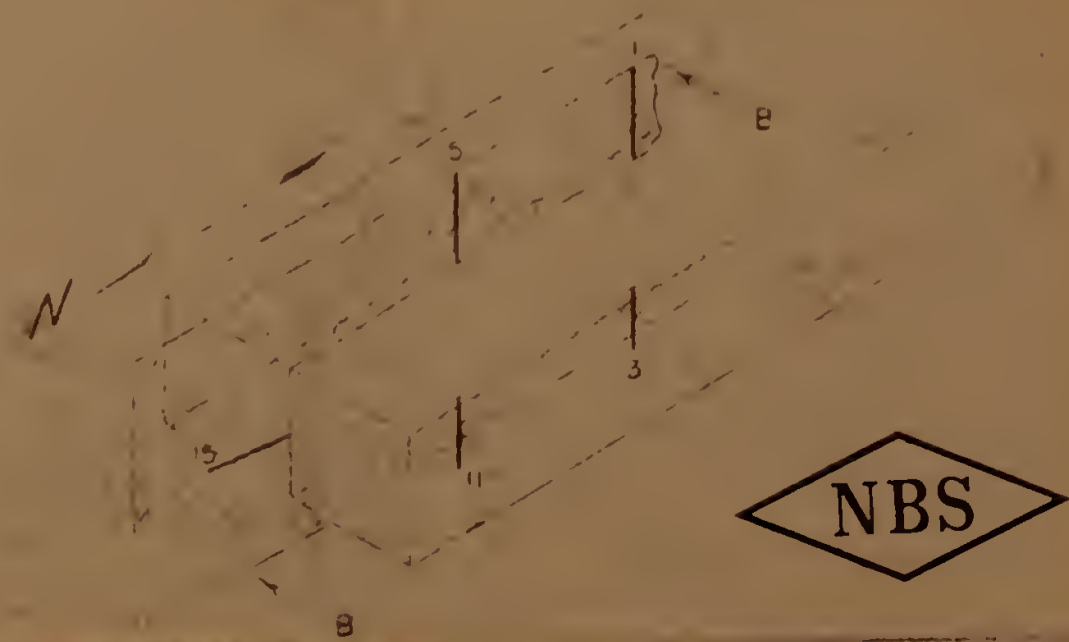
SCALE: $\frac{1}{4}'' = 1'-0''$

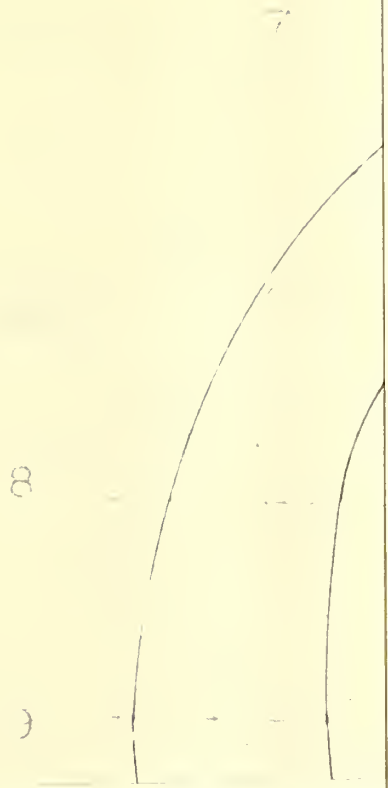
TEST CONDITION No. 1 - HEATING UP PHASE

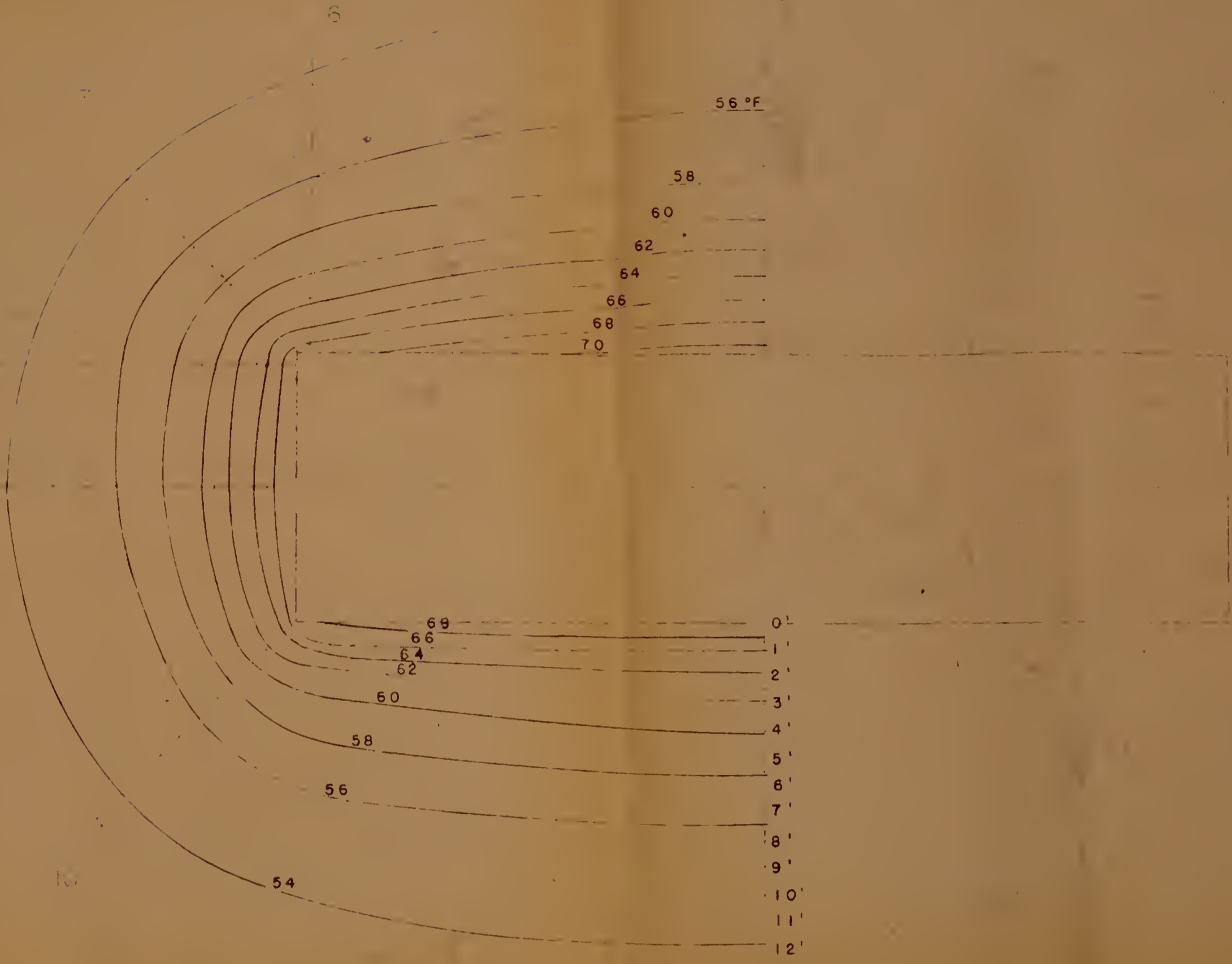
TEMPERATURE DISTRIBUTION IN ROCK

AFTER 521 HOURS

FIGURE 5





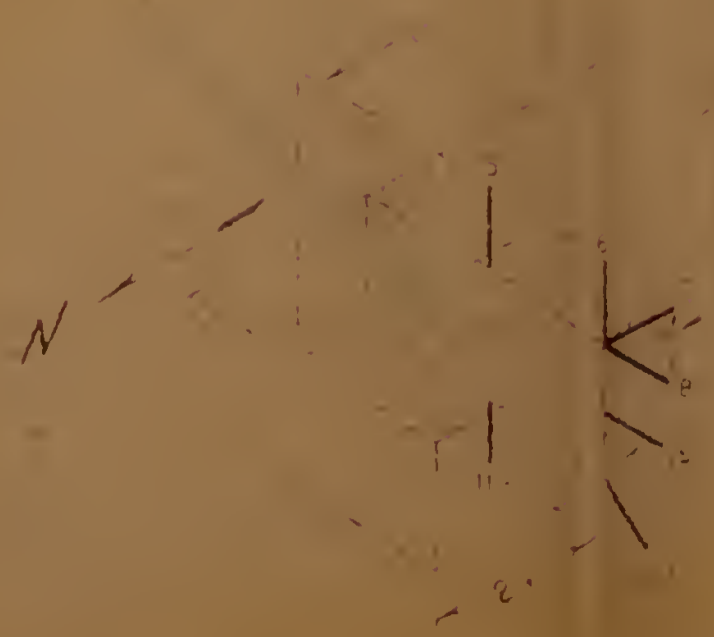


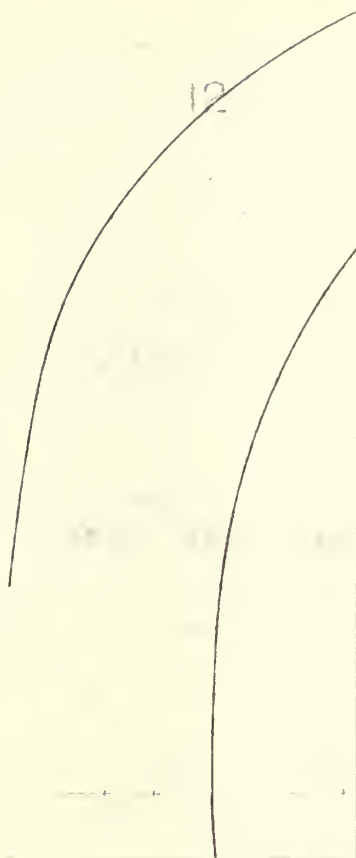
SECTION G-C

SCALE 1/4" = 1'-0"

TEST CONDITION No. 1 - HEATING UP PHASE
 TEMPERATURE DISTRIBUTION IN ROCK
 AFTER 521 HOURS

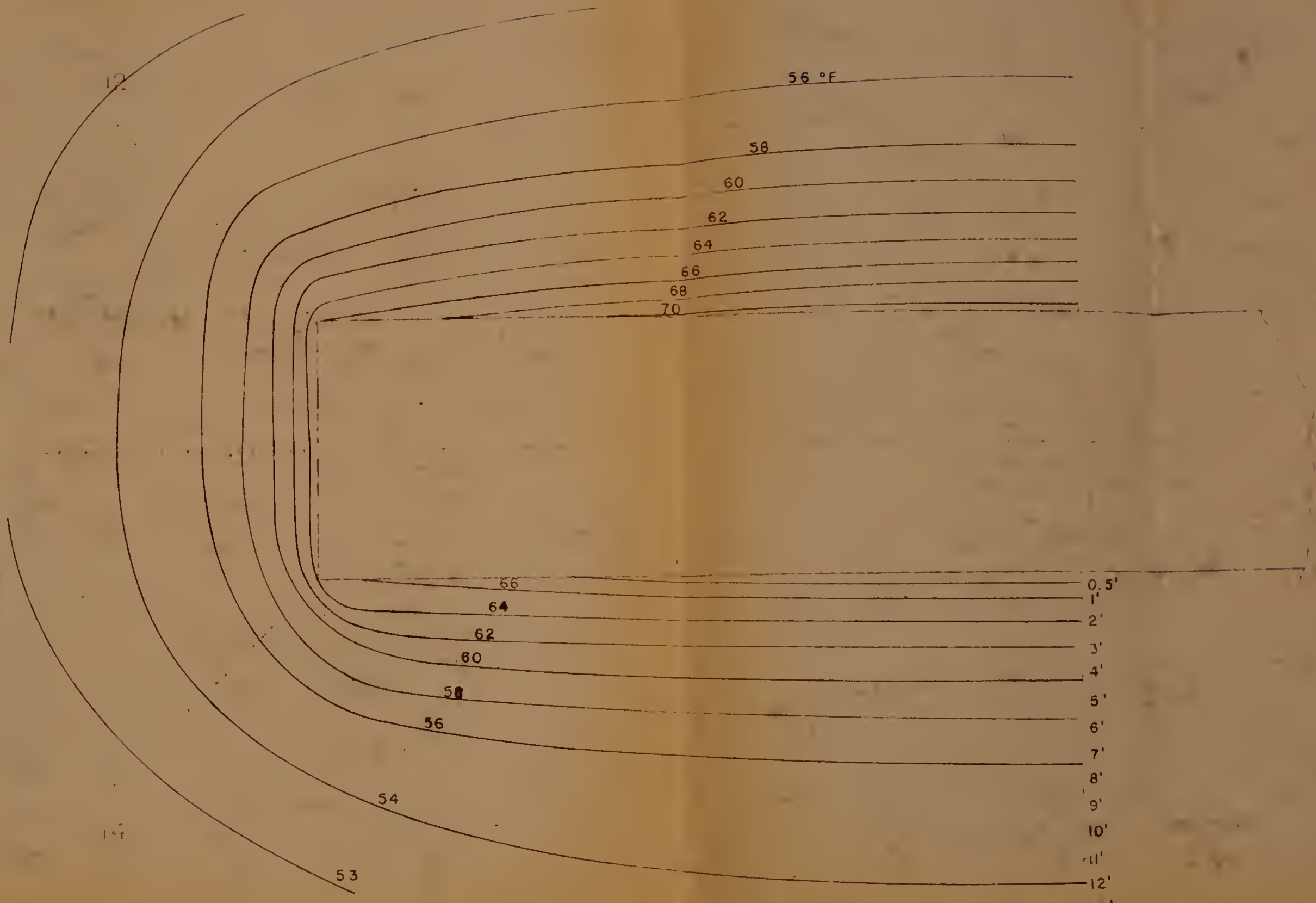
FIGURE 6





12

13

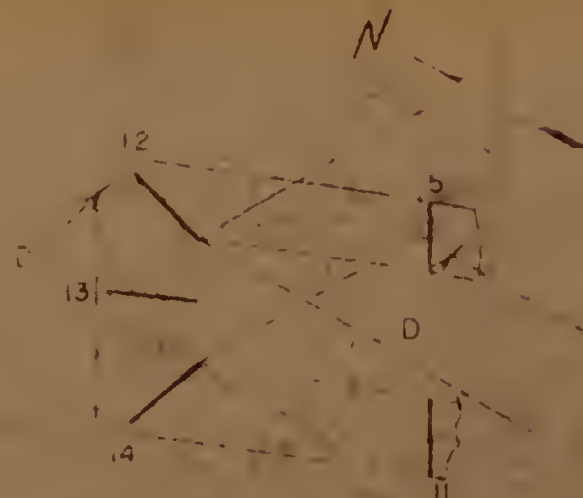


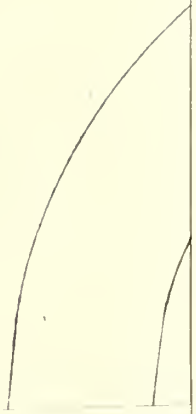
SECTION D-D

SCALE $\frac{1}{4}'' = 1'-0''$

TEST CONDITION No. 1-HEATING UP PHASE
TEMPERATURE DISTRIBUTION IN ROCK
AFTER 521 HOURS

FIGURE 7





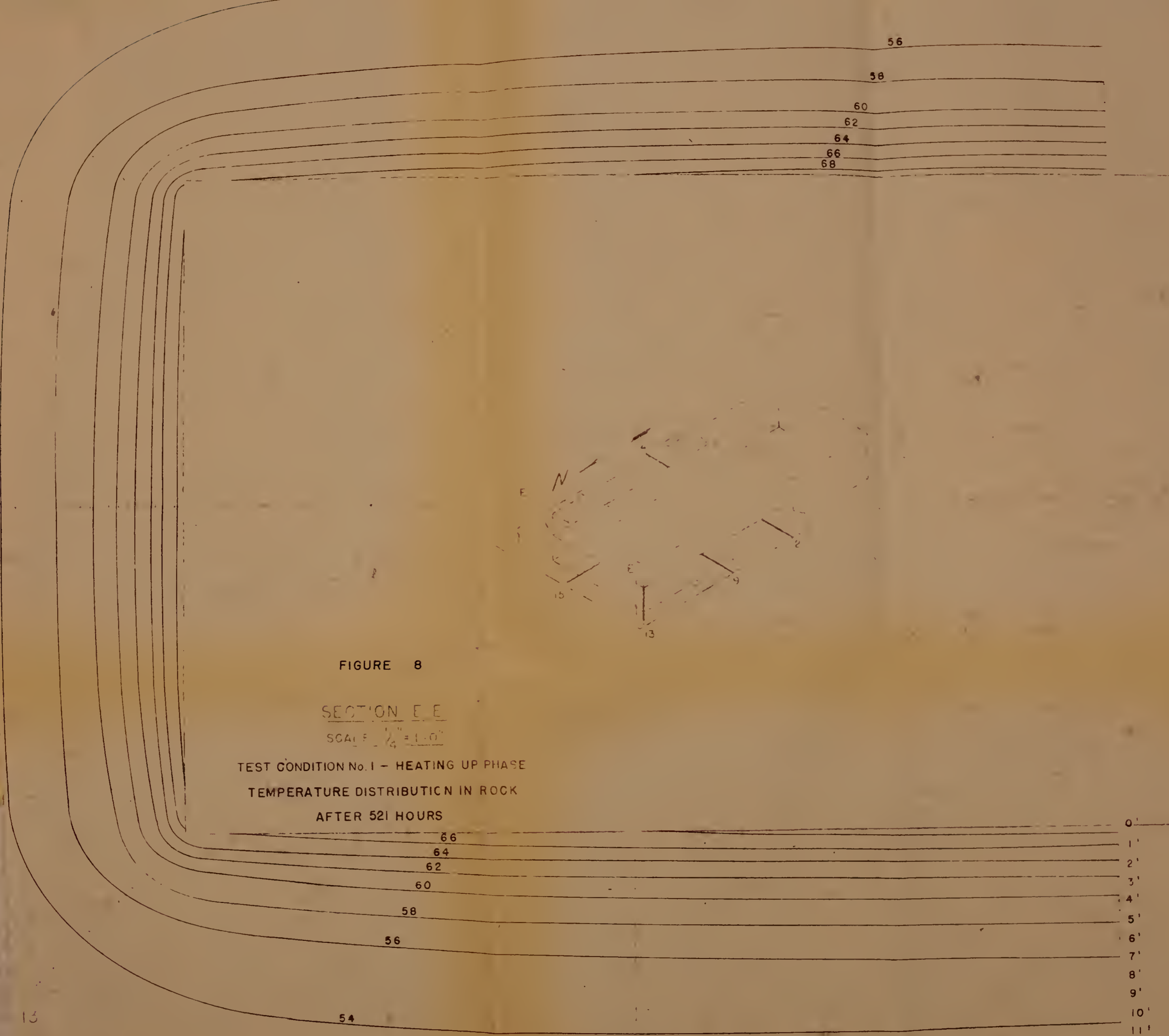


FIGURE 8

SECTION E E

SCALE $\frac{1}{4}'' = 1'-0''$

TEST CONDITION No. 1 - HEATING UP PHASE
 TEMPERATURE DISTRIBUTION IN ROCK
 AFTER 521 HOURS



13

0'
1'
2'
3'
4'
5'
6'
7'
8'
9'
10'
11'
12'



TIME IN HOURS

FIGURE 10



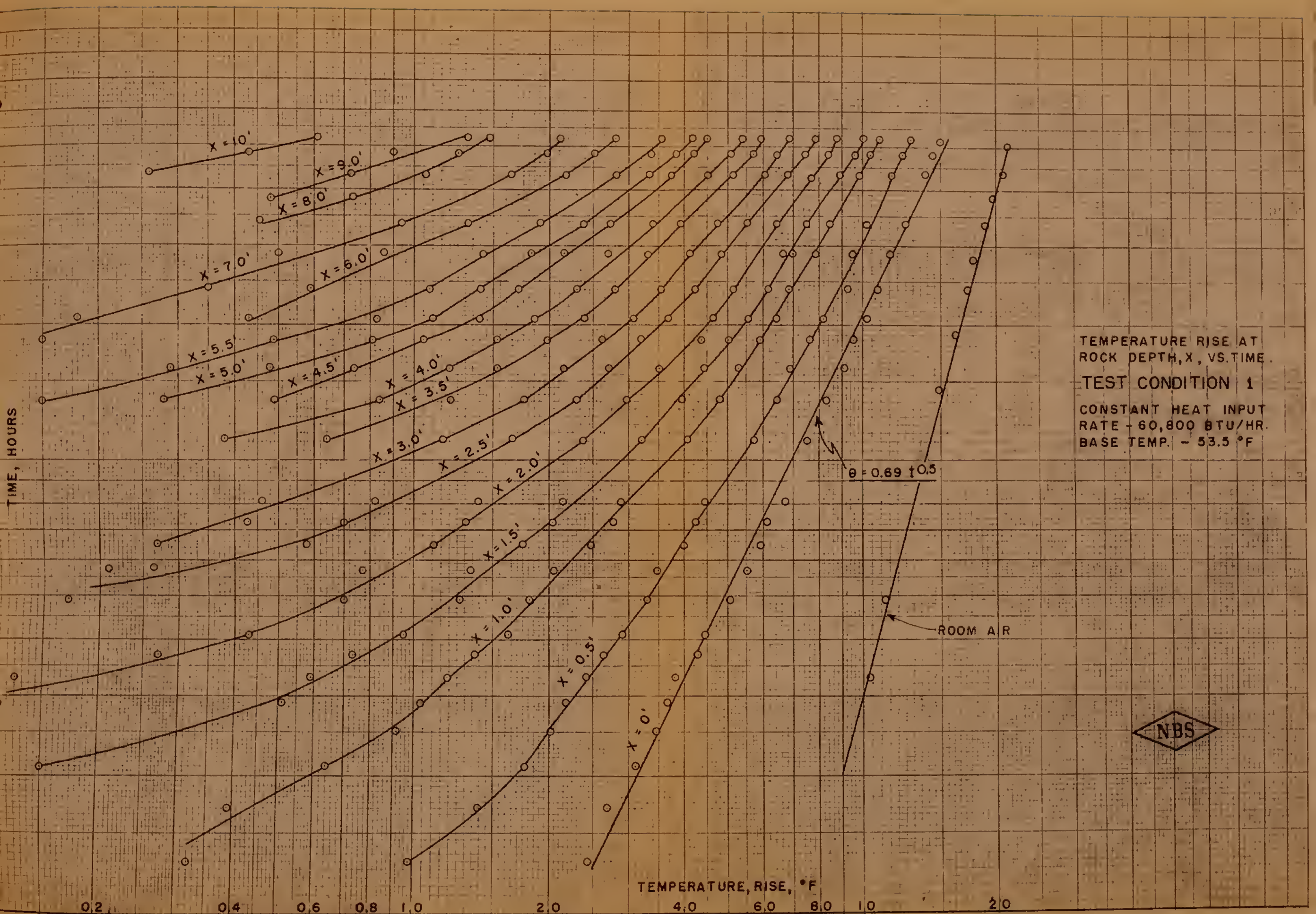


FIG. 9

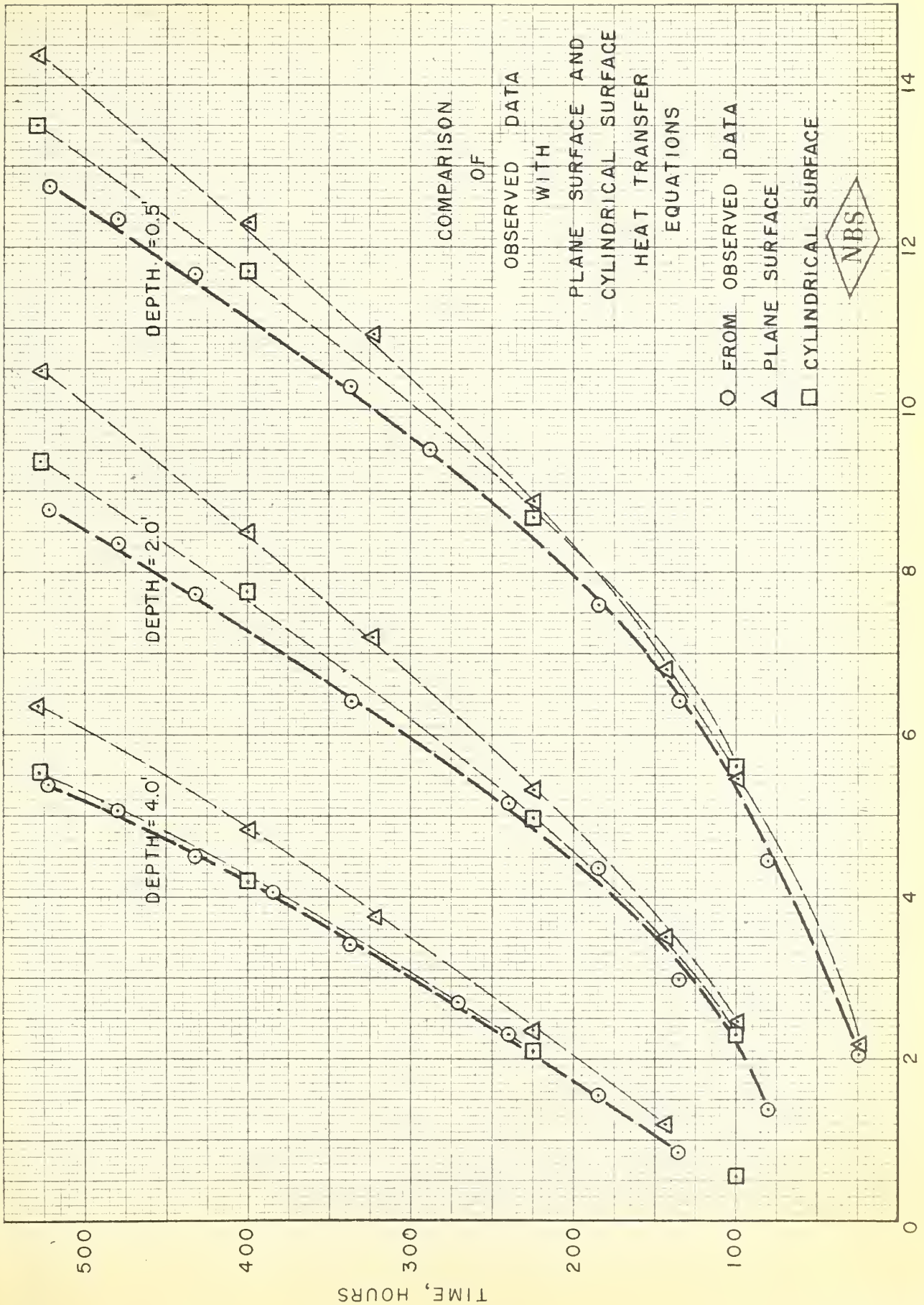




Figure 11. Underground Chamber - Entrance door on right, door to plenum chamber on left.



Figure 12. Underground Chamber - Room

