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# **A Study of Lunar Surface Radio Communication**



**U.S. DEPARTMENT OF COMMERCE  
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L. E. Vogler



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# A STUDY OF LUNAR SURFACE RADIO COMMUNICATION

L. E. Vogler

The problem of point-to-point radio communication on the moon is discussed, and equations and curves are presented to estimate power requirements in lunar communication systems. Assuming a smooth surface, consideration is given to ground wave attenuation over both layered and non-layered grounds, antenna ground losses in situations where ground screens are impractical, noise level estimates in the receiving system, and the effects on propagation of possible lunar ionospheres. An example of the calculation of required power for a particular communication system is given, and further studies are suggested.

## 1. INTRODUCTION

This monograph presents the results of a study investigating the problem of point-to-point radio communication on the surface of the moon. It is intended as a survey of all the work accomplished in a project sponsored by Jet Propulsion Laboratory and, consequently, much of the material has appeared in previous papers concerned with various phases of the study [Vogler, 1963a, 1963b; Vogler and Noble, 1963, 1964]; the rest of the material, notably the discussions on the effects of layered grounds and possible lunar ionospheres, has not been published before.

No attempt is made here to analyze in detail one particular type of communication system; rather, it is hoped that this study may provide part of the general information necessary to the design of any future lunar surface communication link. For example, the antenna used in a permanently based installation would most likely be much more elaborate than the one needed for communication by a mobile exploring party. Once the purpose of the system is determined, the curves herein may be used to help estimate the frequency, range, and power requirements.

Most of the curves, aside from those figures describing illustrative examples, are plotted in parametric terms for the simple reason that very little information exists at the present time concerning the exact nature of the lunar environment; however, as more and more data become available, the curves, using the better estimates of parametric values, will still be useful in the analysis of communication requirements.

The study is primarily concerned with the propagation aspect of lunar surface communication, although considerable emphasis has been placed on the evaluation of antenna power losses due to the proximity of the ground. For low antenna heights and poorly conducting soils, these losses may be far from negligible, especially where ground screens are impractical. The effects of noise and its relationship to the desired signal is discussed briefly, consideration being given to galactic and receiving system component noise.

The lunar model assumed is that of a smooth sphere of radius  $r_0 = 1738$  km. The effects of rough terrain on signal propagation are not included in this analysis, although it is recognized that such things as knife-edge diffraction, "obstacle gain", etc., might be important at some locations on the moon's surface; a study including these mechanisms could be undertaken for particular surface areas of interest. The present curves are expected to be most useful for applications in the frequency range from about 1 kc/s to 10 Mc/s. Throughout the present analysis, antenna heights are assumed to be low enough such that height gain effects are negligible.



## 2. SYSTEM LOSS

The concept of system loss [Norton, 1959; Wait, 1959; CCIR, 1963] will be used to describe the effects of the various system parameters. System loss  $L_s$  is defined as the ratio, expressed in decibels, of the radio frequency power input to the terminals of the transmitting antenna  $p_t$  and the resultant radio frequency signal power available at the terminals of the receiving antenna  $p_r$ :

$$L_s = 10 \log(p_t/p_r) = P_t - P_r. \quad (2.1)$$

Unless otherwise specified, capital letters will be used to designate the decibel equivalent of the corresponding lower case letters; e.g.,  $P_t = 10 \log_{10} p_t$ .

The system loss may be divided further into a free space component that would be the loss expected between isotropic antennas situated in free space, an attenuation  $A_t$  relative to a free space inverse distance field which accounts for the effects on propagation of the intervening terrain, and the transmitting and receiving antenna components  $L_t$ ,  $L_r$ , and  $G_p$  describing the effects of the particular antennas used. Thus, (2.1) may be written as

$$P_t = L_s + P_r = 10 \log(4\pi d_o/\lambda)^2 + A_t - G_p + L_t + L_r + P_r, \quad (2.2)$$

where  $d_o$  is the arc distance separating the two antennas and  $\lambda$  is the free space wavelength expressed in the same units as  $d_o$ . The term  $G_p$  denotes the path antenna gain which is a function of the transmitting and receiving antenna maximum directivity gains relative to isotropic antennas,  $G_t$  and  $G_r$ , and any aperture-to-medium coupling loss or polarization coupling loss. For the purposes of this analysis, the latter two losses will be assumed negligible such that  $G_p = G_t + G_r$ ; however, it should be noticed that, in general, the path antenna gain will be less than or equal to the sum of the maximum directivity gains. The symbols  $L_t$  and  $L_r$  denote antenna losses arising from the antenna's proximity to the ground:  $L_{t,r} = 10 \log(r/r_f)$ , where  $r$  is the actual input resistance and  $r_f$  the radiation resistance in free space. Notice that, in order to calculate transmitter power, any transmission line loss and appropriate circuit losses should be added to the right side of (2.2).

The power available at the receiver consists not only of the desired signal but also of radio noise arising both from within and from without the receiving system. If  $r(s/n)$  denotes the desired minimum signal-to-noise power ratio that will provide a given grade of reception as measured at the receiver predetection output, and an operating noise factor  $f^\dagger$  is defined as the ratio of (1) the signal to a reference Johnson-noise power ratio that is available from a loss-free receiving antenna to (2) the receiver predetection output signal-to-noise ratio  $r(s/n)$ , then  $p_r$  may be expressed as

$$p_r = f k_B t_o b r(s/n)/l_c, \quad (2.3)$$

<sup>†</sup>The relationship between  $f$  and the effective "noise temperature"  $T_{eff}$  used in some discussions is given by  $T_{eff} = t_o f$ .



where  $k_B t_o b$  is the reference Johnson-noise power. The symbol  $k_B$  denotes Boltzmann's constant ( $= 1.38054 \times 10^{-23}$  joules/degree),  $t_o$  is a reference temperature in degrees Kelvin,  $b$  is the effective noise bandwidth in cycles per second, and  $\ell_c$  is the ratio of the antenna input resistance to its radiation resistance.

Using the above definitions and assuming  $\ell_c \simeq \ell_r$ , (2.2) may now be expressed as

$$P_t = 32.45 + 20 \log d_o (\text{km}) + 20 \log f_{mc} + A_t - (G_t + G_r) + L_t + R + F + B + 10 \log (k_B t_o), \quad (2.4)$$

where  $d_o$  is measured in kilometers,  $f_{mc}$  denotes the radio frequency in megacycles per second, and  $R \equiv 10 \log r(s/n)$ . The following sections will discuss the various components of (2.4).

### 3. GROUND WAVE ATTENUATION $A_t$

Numerical procedures for the calculation of electromagnetic fields diffracted around a smooth homogeneous sphere have been developed by various authors [Norton, 1941; Bremmer, 1949]. The ground wave may be expressed as a series of residues that depend on the radius of the sphere  $r_o$ , the arc distance  $d_o$ , the antenna heights  $h_1$  and  $h_2$ , the free space wavelength  $\lambda$ , the relative dielectric constant  $\epsilon_r$  and conductivity  $\sigma$  of the ground, and the polarization of the wave. As stated in section 1, the present analysis assumes negligible height gain effects corresponding to antenna heights near zero; for elevated antennas, estimates of height gain may be obtained for beyond the horizon paths from another paper [Vogler, 1964].

In parametric form the ground wave attenuation relative to a free space inverse distance field  $A_t$  is conveniently plotted as a function of three parameters:  $K$ ,  $b^\circ$ , and  $x'_o$ . Through the recent work of Wait [1962a] both non-layered and layered grounds may be accounted for by generalizations of the definitions of  $K$  and  $b^\circ$ . Thus, with the subscripts  $h$  and  $v$  referring to horizontal and vertical polarization respectively,

$$K_h = \left[ (2\pi r_o / \lambda)^{1/3} |T_h| \cdot |Q_h| \right]^{-1}, \quad K_v = \left[ (2\pi r_o / \lambda)^{1/3} |T_v| \cdot |Q_v| \right]^{-1}, \quad (3.1)$$

where

$$|T_h| = \left[ (\epsilon_r - 1)^2 + s^2 \right]^{1/4}, \quad |T_v| = \left[ \sqrt{(\epsilon_r - 1)^2 + s^2} / (\epsilon_r^2 + s^2) \right]^{1/2}; \quad (3.2)$$

and

$$b_h^\circ = 180^\circ - \tan^{-1} \left( \frac{\epsilon_r - 1}{s} \right) - q_h^\circ, \quad b_v^\circ = 2 \tan^{-1} \left( \frac{\epsilon_r}{s} \right) - \tan^{-1} \left( \frac{\epsilon_r - 1}{s} \right) - q_v^\circ, \quad (3.3)$$

with

$$s = 2 \times 10^{-7} c \lambda \sigma \simeq 1.8 \times 10^4 \sigma (\text{mhos/m}) / f_{mc}.$$

Both  $\epsilon_r$  and  $s$  are dimensionless and refer to the top ground layer unless otherwise specified. The parameters  $\lambda$  and  $\sigma$  are in meters and mhos per meter respectively, and  $c$  is the velocity of light.

The symbols  $|Q|$  and  $q^\circ$  appearing in (3.1) and (3.3) denote the magnitude and phase of a "stratification factor",  $Q \equiv |Q| \exp(iq^\circ/2)$ , that accounts for the effect of layering in the ground. In general  $Q$  is a complex quantity dependent on the heights and electromagnetic ground constants of the various layers, whereas for a homogeneous (non-layered) ground,  $Q$  is equal to unity. Wait [1962b] has derived formulas for  $Q$  for the general case of  $n$  layers and has presented curves [Wait, 1962a] for two and three layer situations; however, unless specific values for the heights and ground constants of the various layers are given, a graphical representation becomes quite complicated for a multi-layered ground. For the present discussion, restriction to vertical polarization over a two-layered model will be assumed.

Letting the subscripts 1 and 2 refer to the upper and lower layers respectively,  $Q_v$  may be expressed as

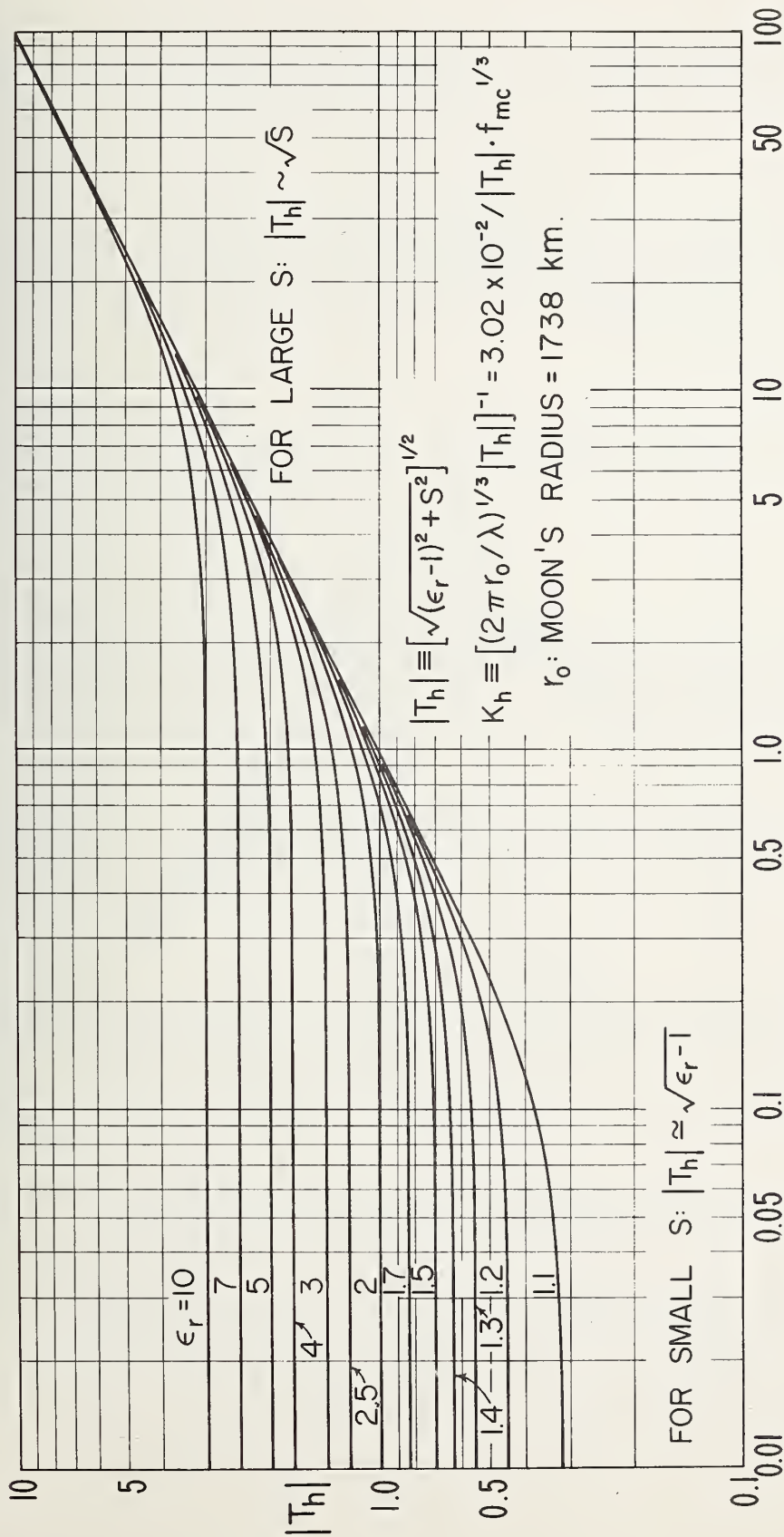
$$Q_v = \frac{\left( |T_{v2}| / |T_{v1}| \right) e^{i(b_{v1}^\circ - b_{v2}^\circ)/2} + \tanh\left\{ (2\pi\ell_1/\lambda) |T_{h1}| e^{i(270^\circ - b_{h1}^\circ)/2} \right\}}{1 + \left( |T_{v2}| / |T_{v1}| \right) e^{i(b_{v1}^\circ - b_{v2}^\circ)/2} \tanh\left\{ (2\pi\ell_1/\lambda) |T_{h1}| e^{i(270^\circ - b_{h1}^\circ)/2} \right\}} \equiv |Q_v| e^{iq_v^\circ/2}, \quad (3.4)$$

where  $\ell_1$  is the height of the upper layer measured in the same units as  $\lambda$ .  $|T_h|$  and  $|T_v|$  are given by (3.2) using the appropriate values of  $\epsilon_r$  and  $\sigma$  characterizing layer 1 or layer 2;  $b_h^\circ$  and  $b_v^\circ$  are obtained from (3.3) after setting  $q^\circ = 0$ . As  $\ell_1$  becomes very large (corresponding to homogeneous ground),  $Q_v$  approaches unity and  $|Q_v| = 1$ ,  $q_v^\circ = 0$ .

Graphs of  $|T_h|$  and  $|T_v|$  as functions of  $\epsilon_r$  and  $s$  are shown in figures 1 and 2 where the expressions for  $K_{h,v}$  refer to a homogeneous ground ( $|Q| = 1$ ); similar plots of  $b_h^\circ$  and  $b_v^\circ$  are given in figures 3 and 4, again for homogeneous ground ( $q^\circ = 0$ ). It can be seen that  $b^\circ$  is always positive for either polarization as long as no layering occurs.

The variation of  $K_v$  and  $b_v^\circ$  for a two-layered ground is shown in figures 5 through 8. The curves were calculated from (3.1), (3.3), and (3.4) using the values of the ground constants and upper layer heights indicated. Only values of  $K_v$  for  $0.01 \leq K_v \leq 10$  are plotted since the variation of  $A_t$  as a function of  $b^\circ$  is negligible outside this range (see figures 9 - 14). The curves of  $b_v^\circ$  indicate that, as the conductivity of the lower layer  $\sigma_2$  increases,  $b_v^\circ$  is more likely to become negative. Thus, if it is found that the moon consists of a highly conducting core underlying a thin poorly conducting crust, ground wave communication could encounter "fade-outs" for certain frequencies and ranges. This is indicated in figures 9 through 14 which show the ground wave attenuation  $A_t$  for zero antenna heights versus the distance parameter  $x'_o$ , where

$$x'_o = f^{\frac{1}{3}} \frac{1}{mc} d_o \text{ (km)}. \quad (3.5)$$



$$S = 60\lambda\sigma(\text{mhos/m}) = 1.8 \times 10^4 \sigma(\text{mhos/m}) / f_{mc}$$

Figure 1. The parameter  $|T_h|$  for horizontal polarization. The formula for  $K_h$  assumes a homogeneous ground.

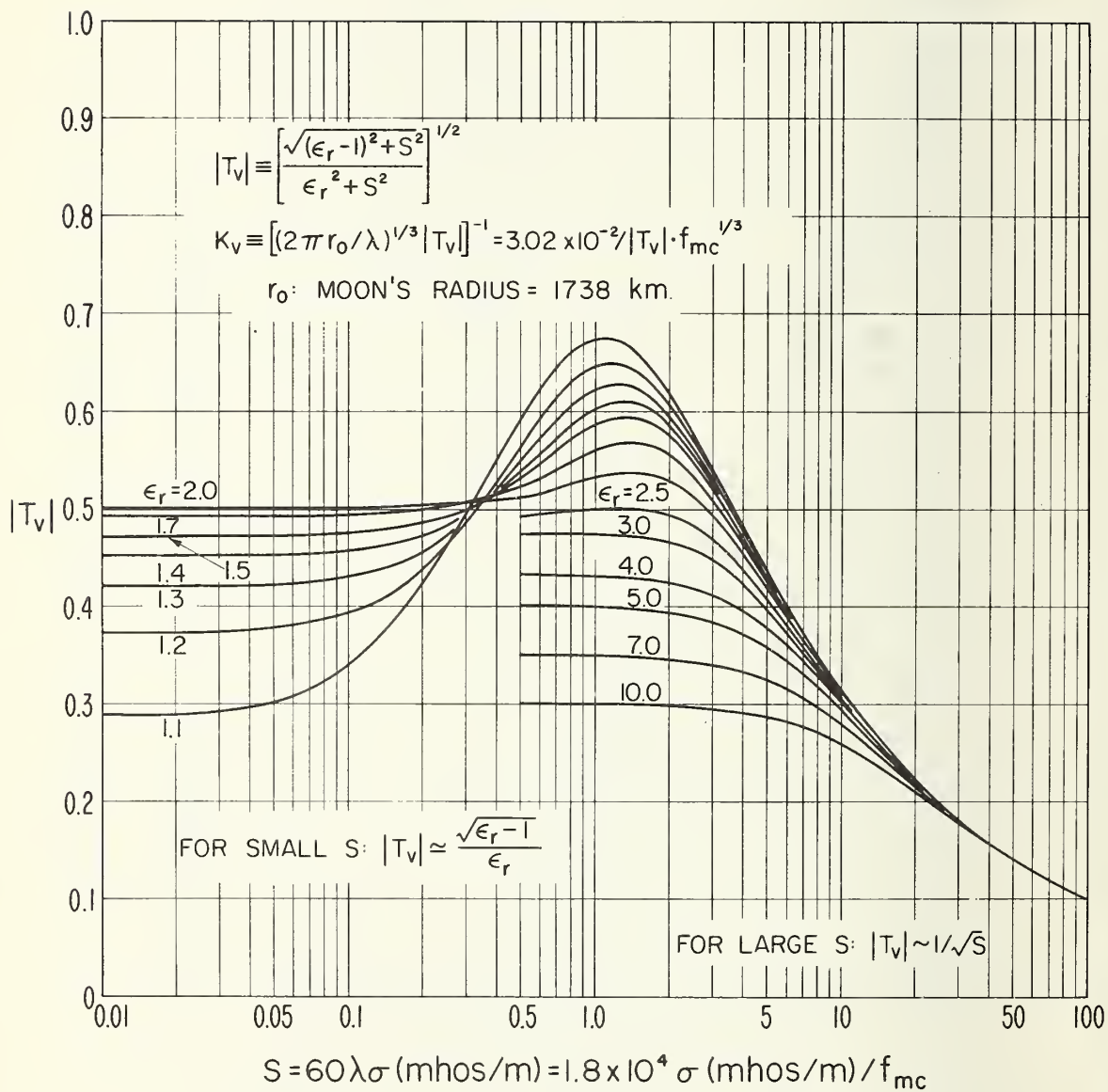
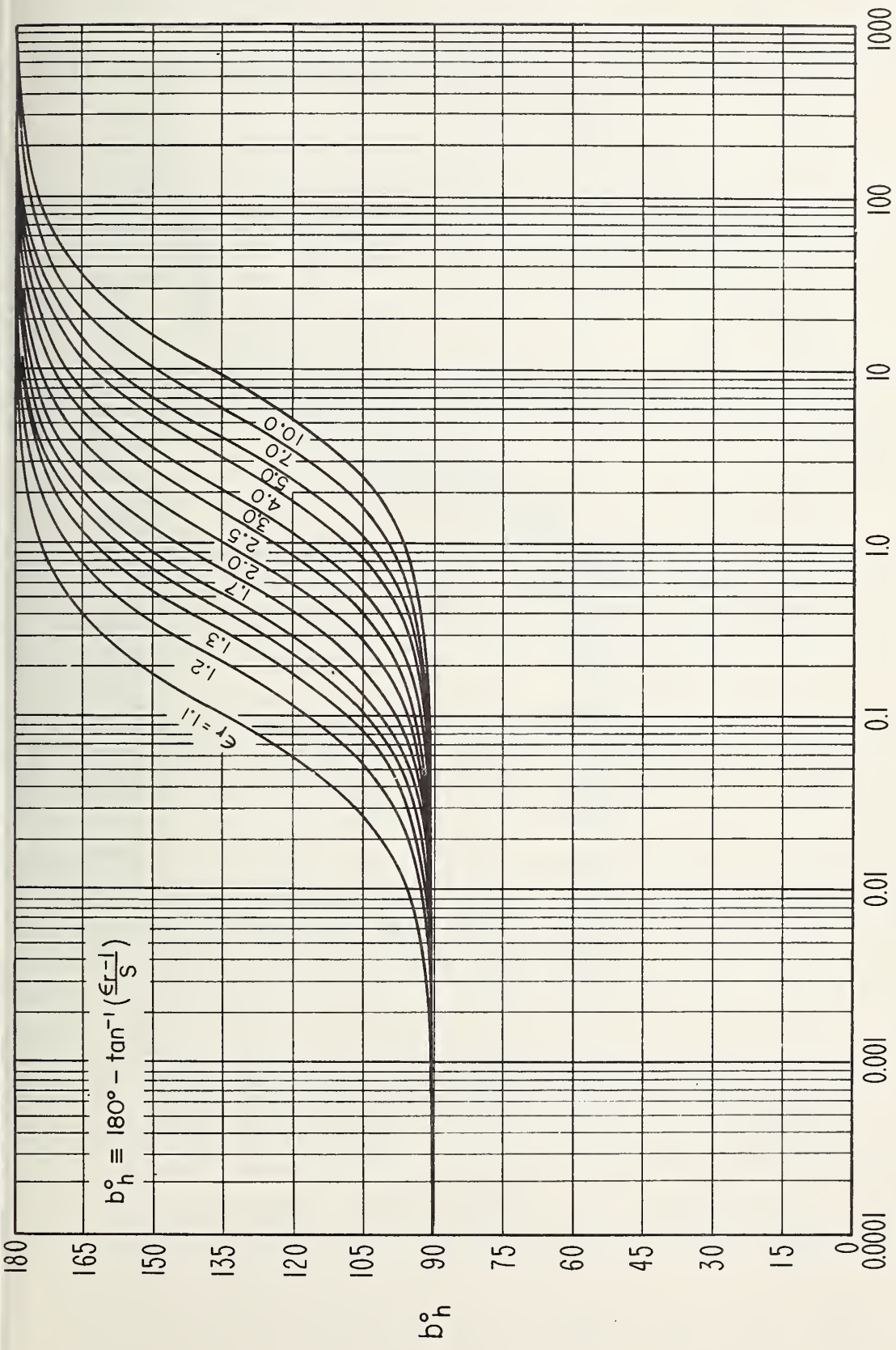


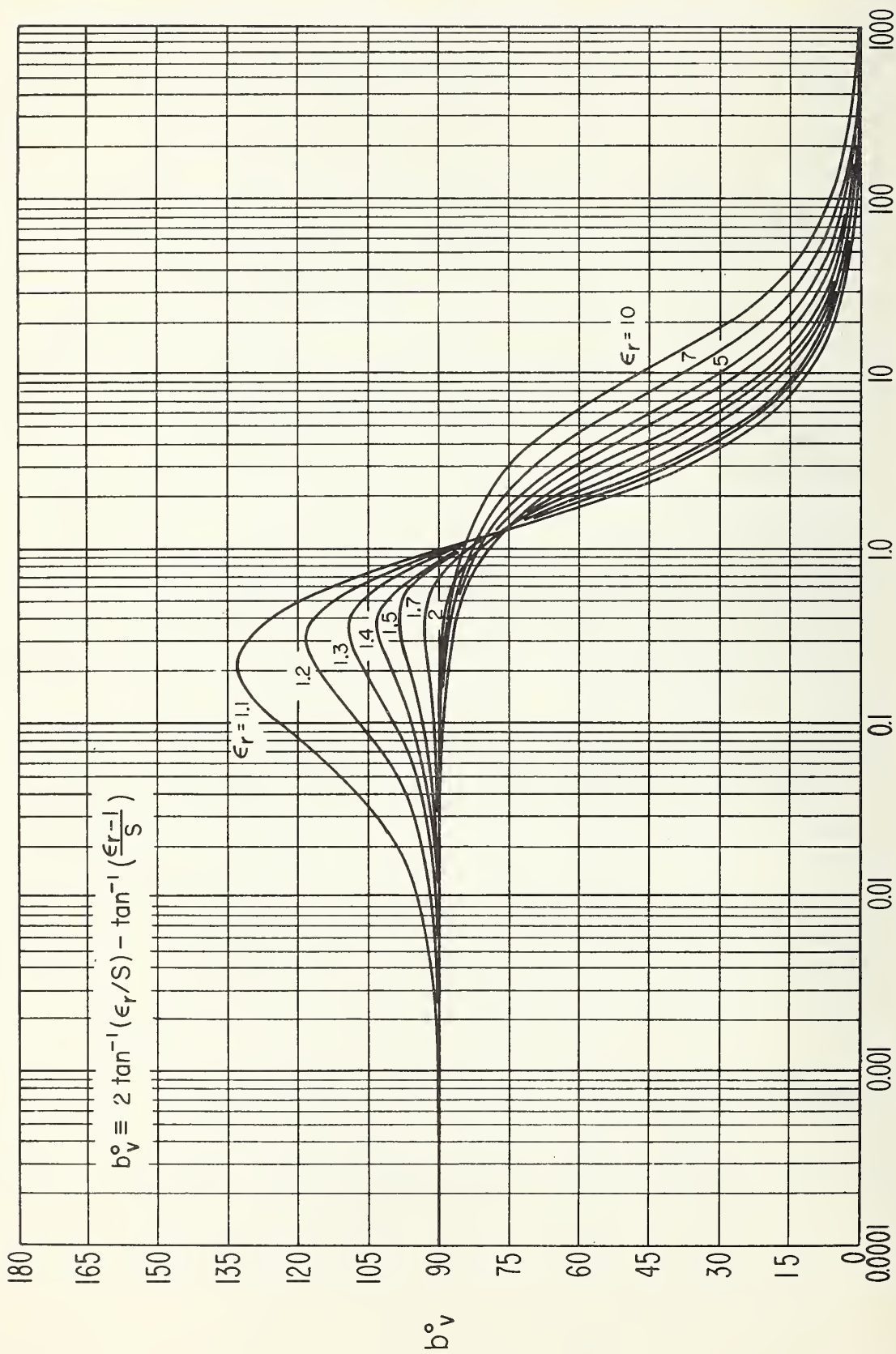
Figure 2. The parameter  $|T_v|$  for vertical polarization. The formula for  $K_v$  assumes a homogeneous ground.





$$S = 60 \lambda \sigma (\text{mhos/m}) = 1.8 \times 10^4 \sigma (\text{mhos/m}) / f_{mc}$$

Figure 3. The parameter  $b_h^0$  for horizontal polarization and homogeneous ground.



$$S = 60 \lambda \sigma (\text{mhos/m}) = 1.8 \times 10^4 \sigma (\text{mhos/m}) / f_{mc}$$

Figure 4. The parameter  $b_v^0$  for vertical polarization and homogeneous ground.



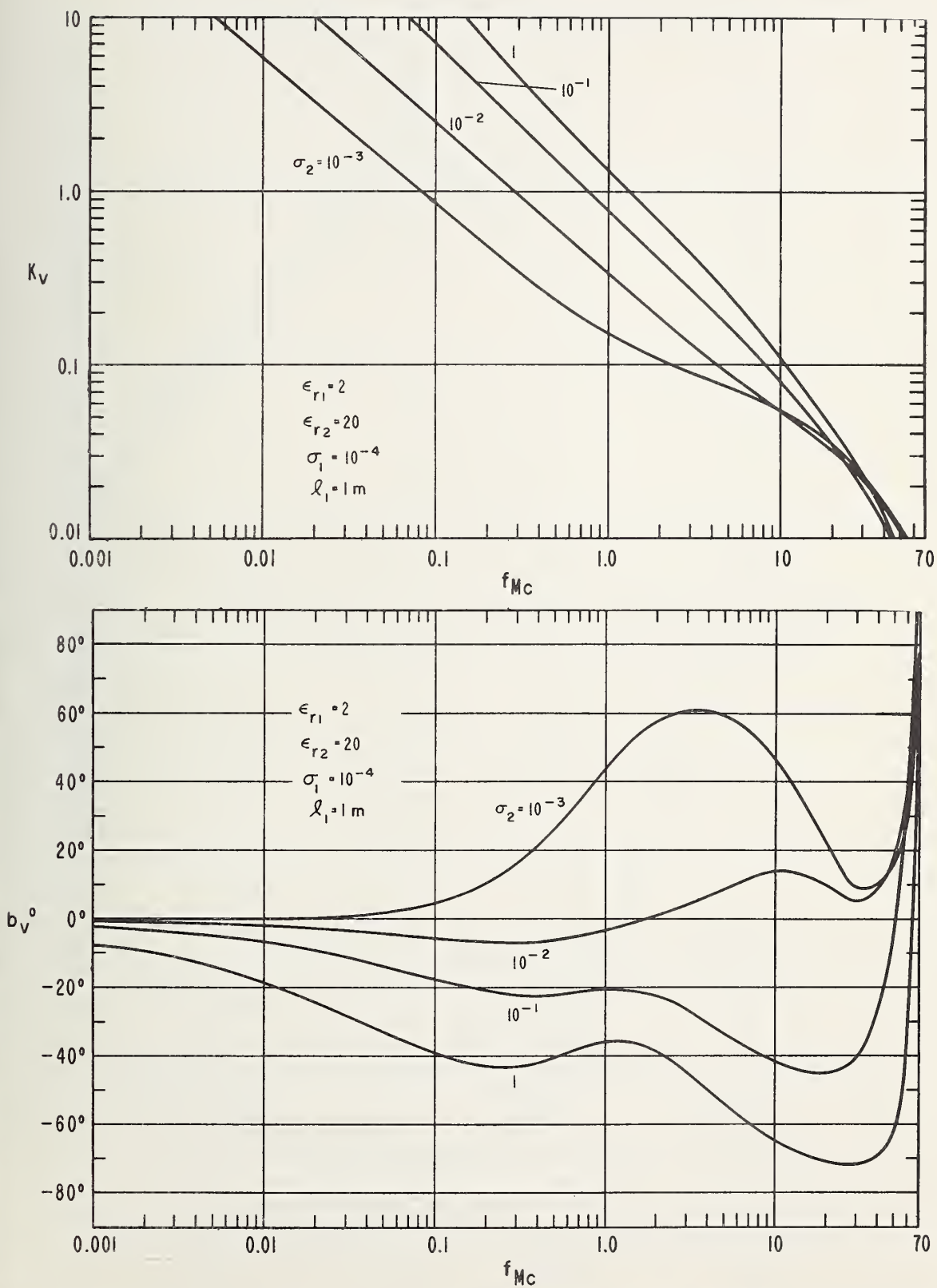


Figure 5.  $K_V$  and  $b_V^0$  for two layers, upper layer height: 1 m.

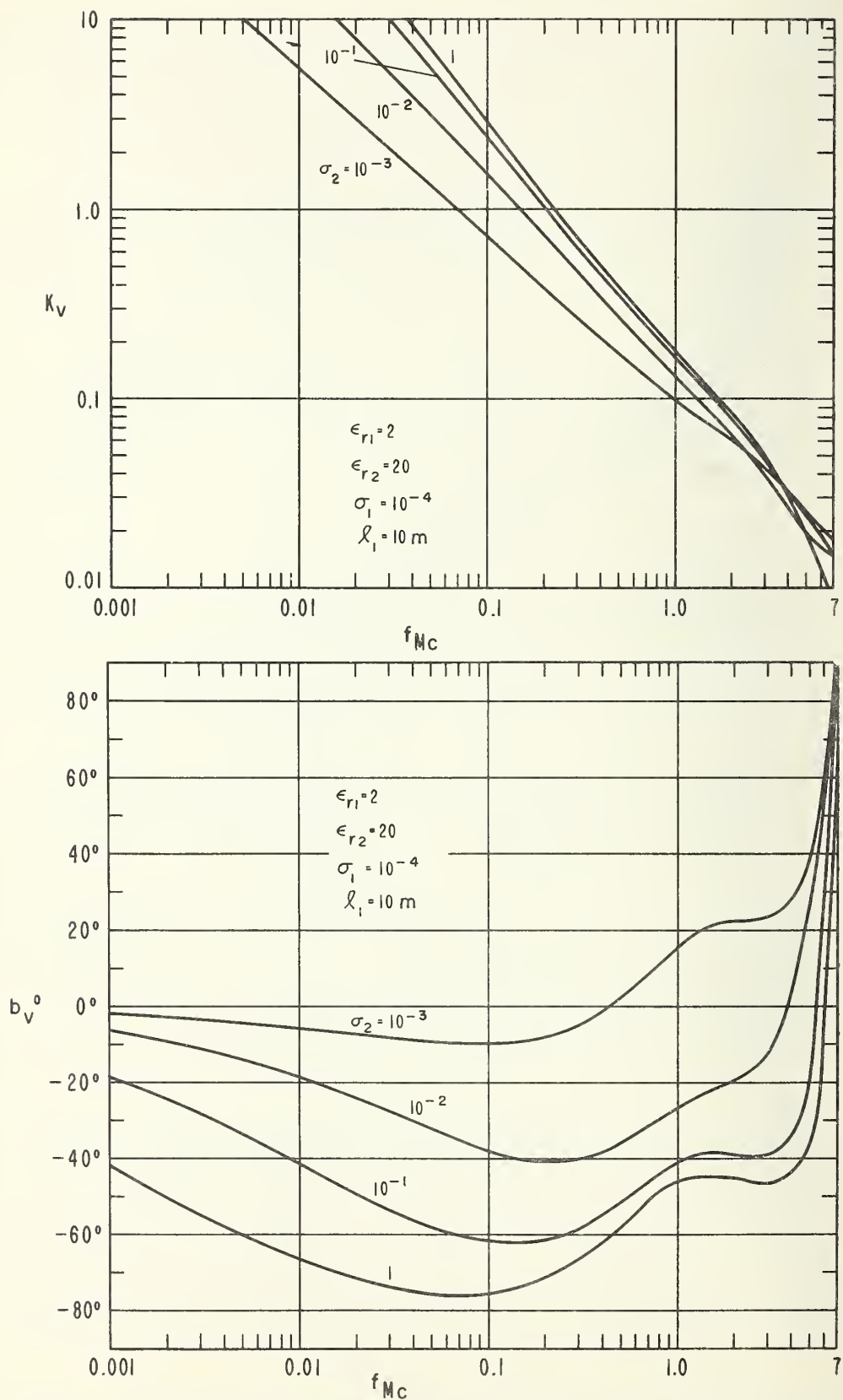


Figure 6.  $K_V$  and  $b_V^0$  for two layers, upper layer height: 10 m.

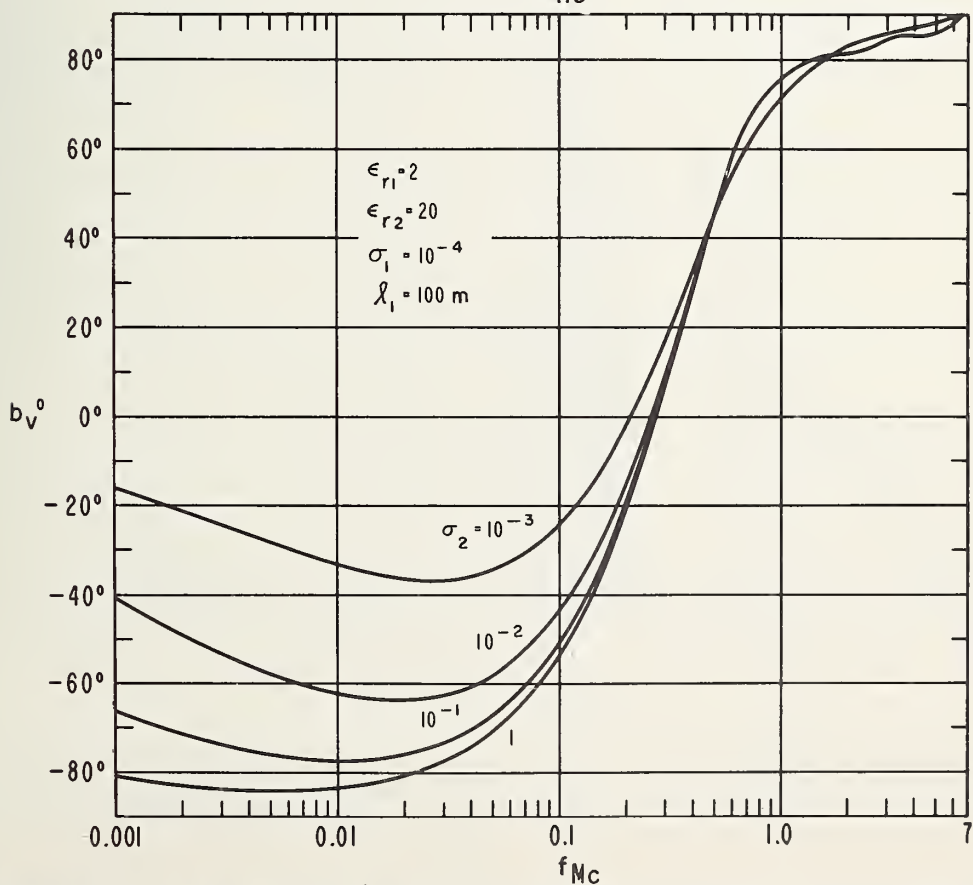
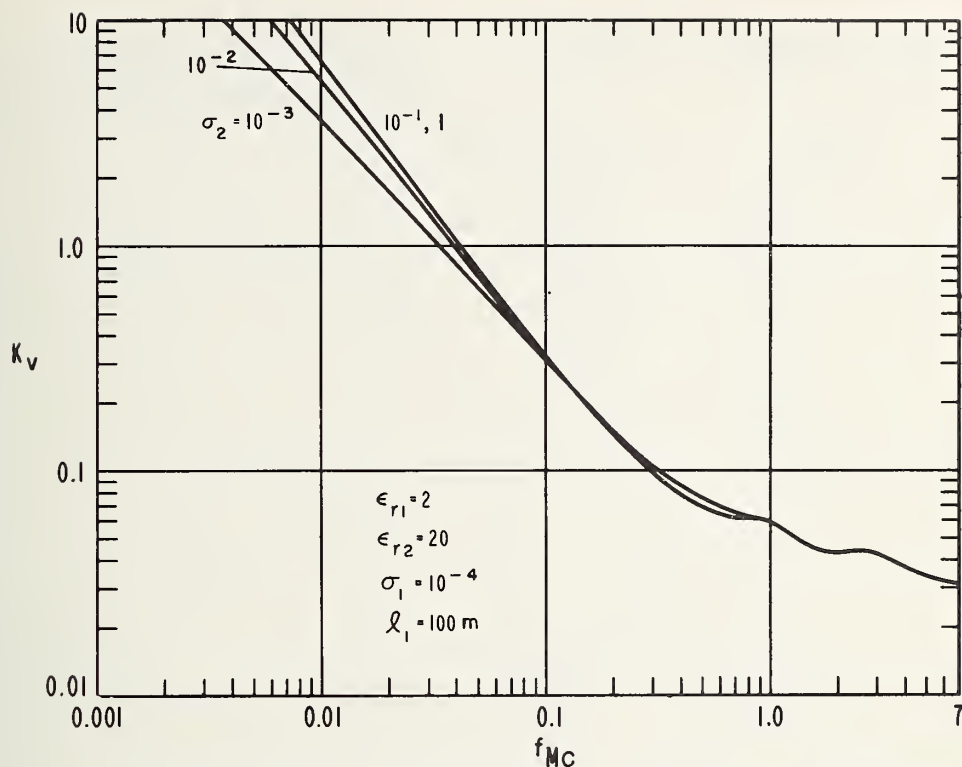


Figure 7.  $K_v$  and  $b_v^0$  for two layers, upper layer height: 100 m.

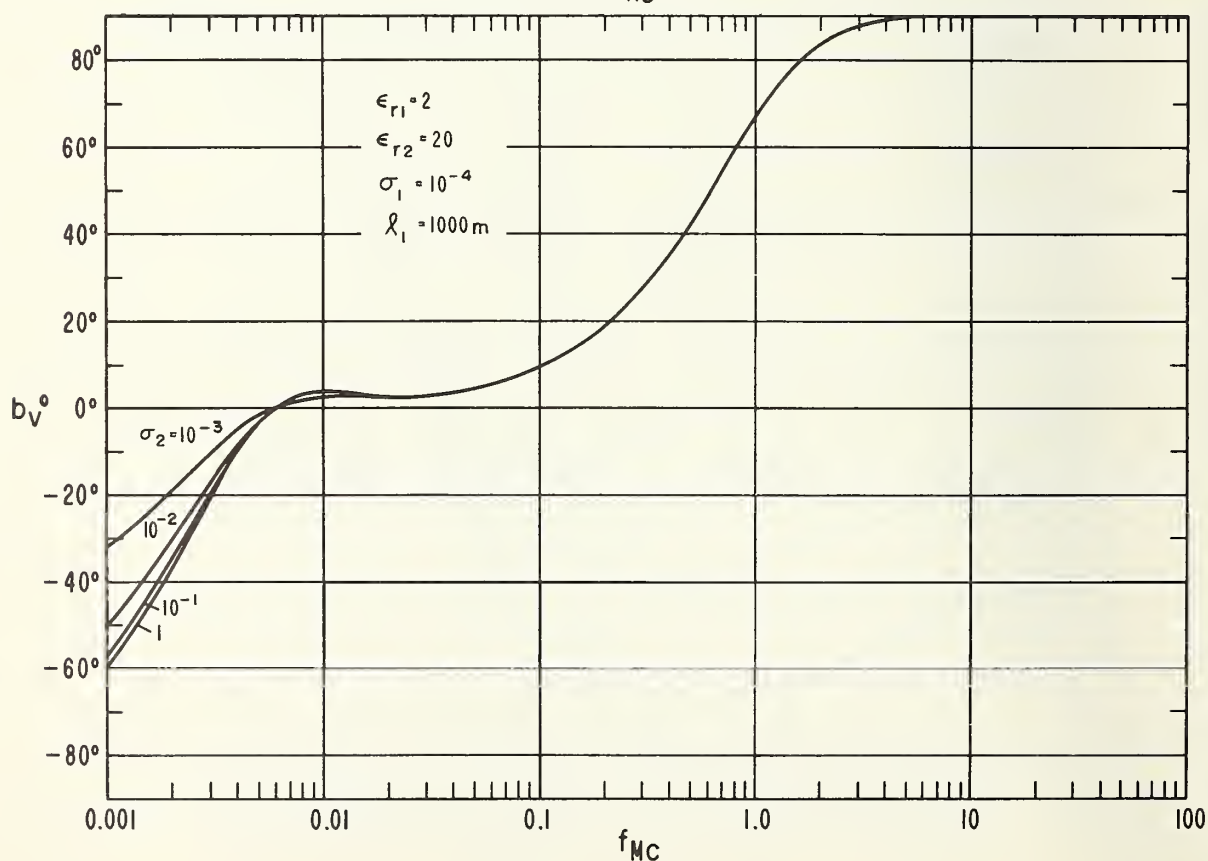
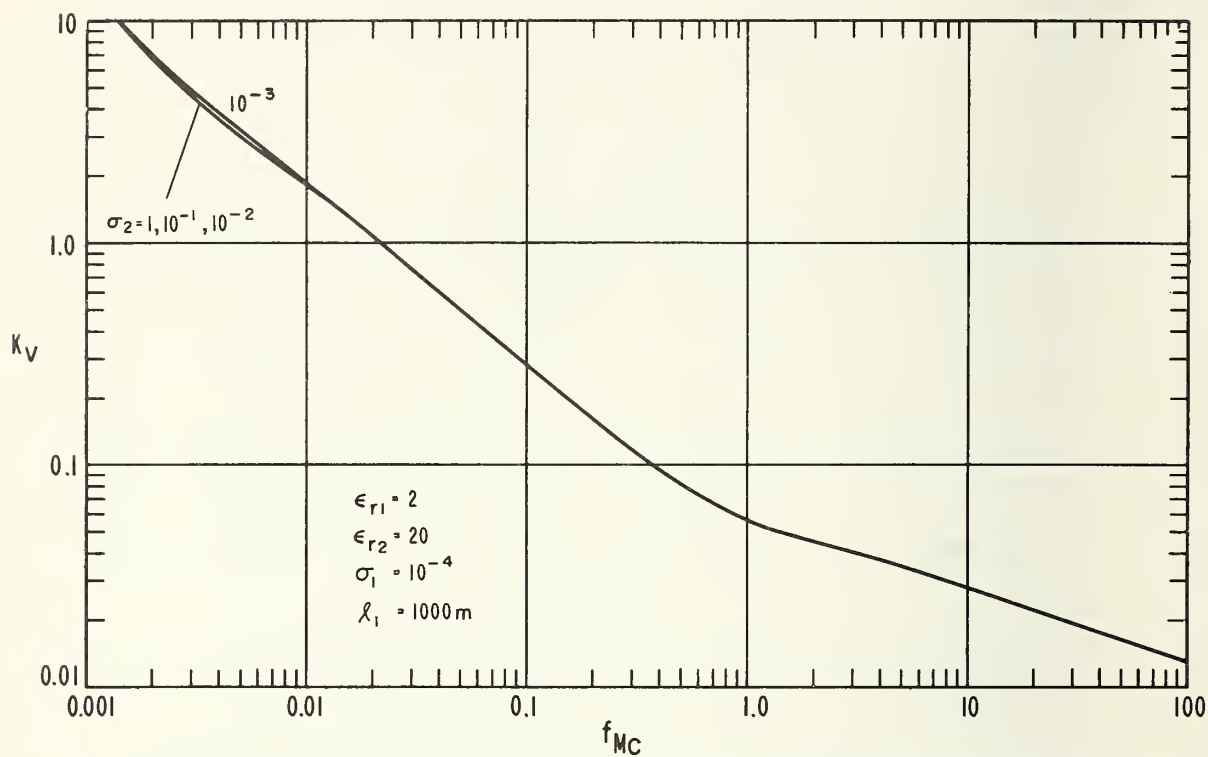


Figure 8.  $K_V$  and  $b_V^0$  for two layers, upper layer height: 1000 m.

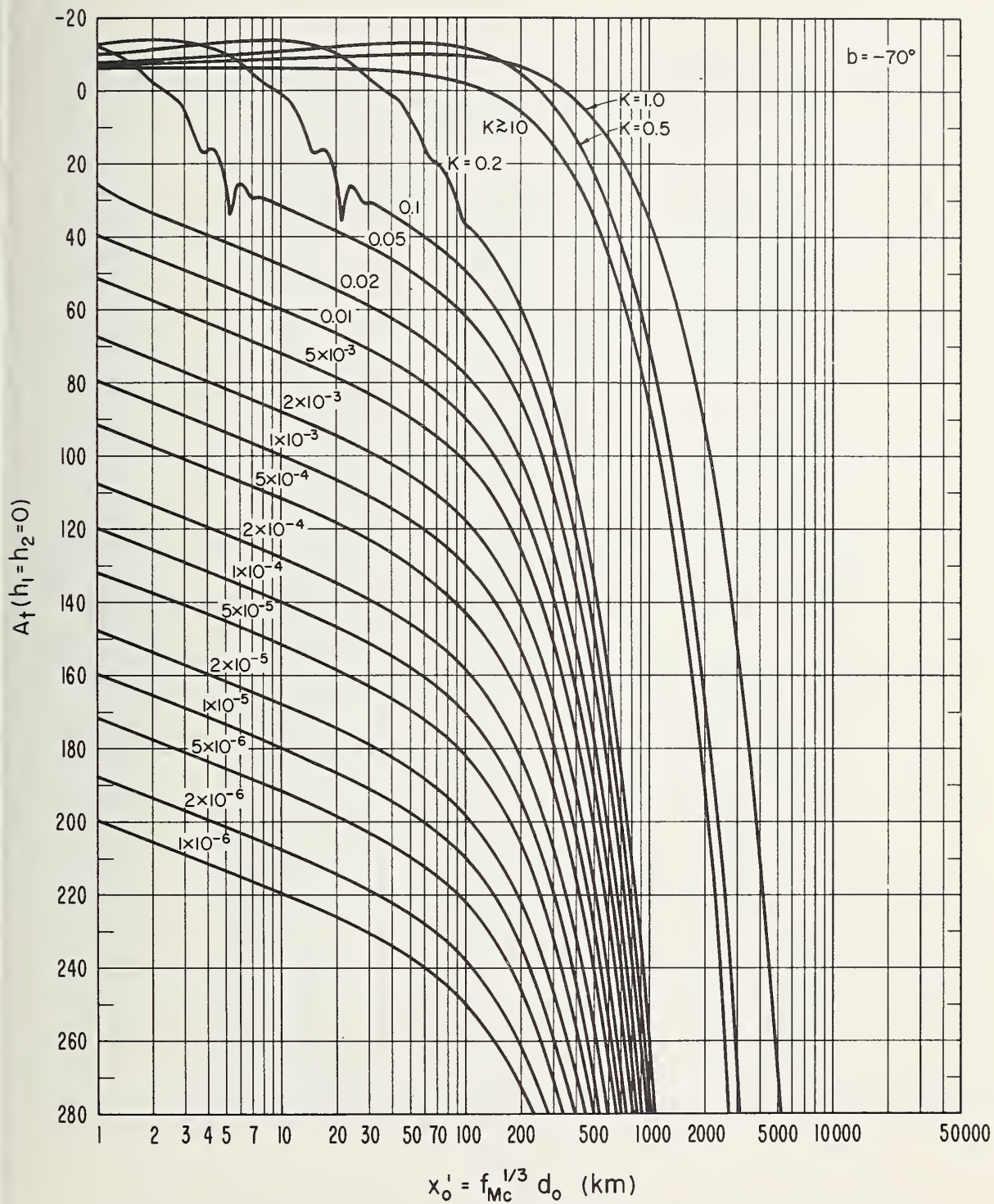


Figure 9. Ground wave attenuation for zero antenna heights,  $b = -70^\circ$ .



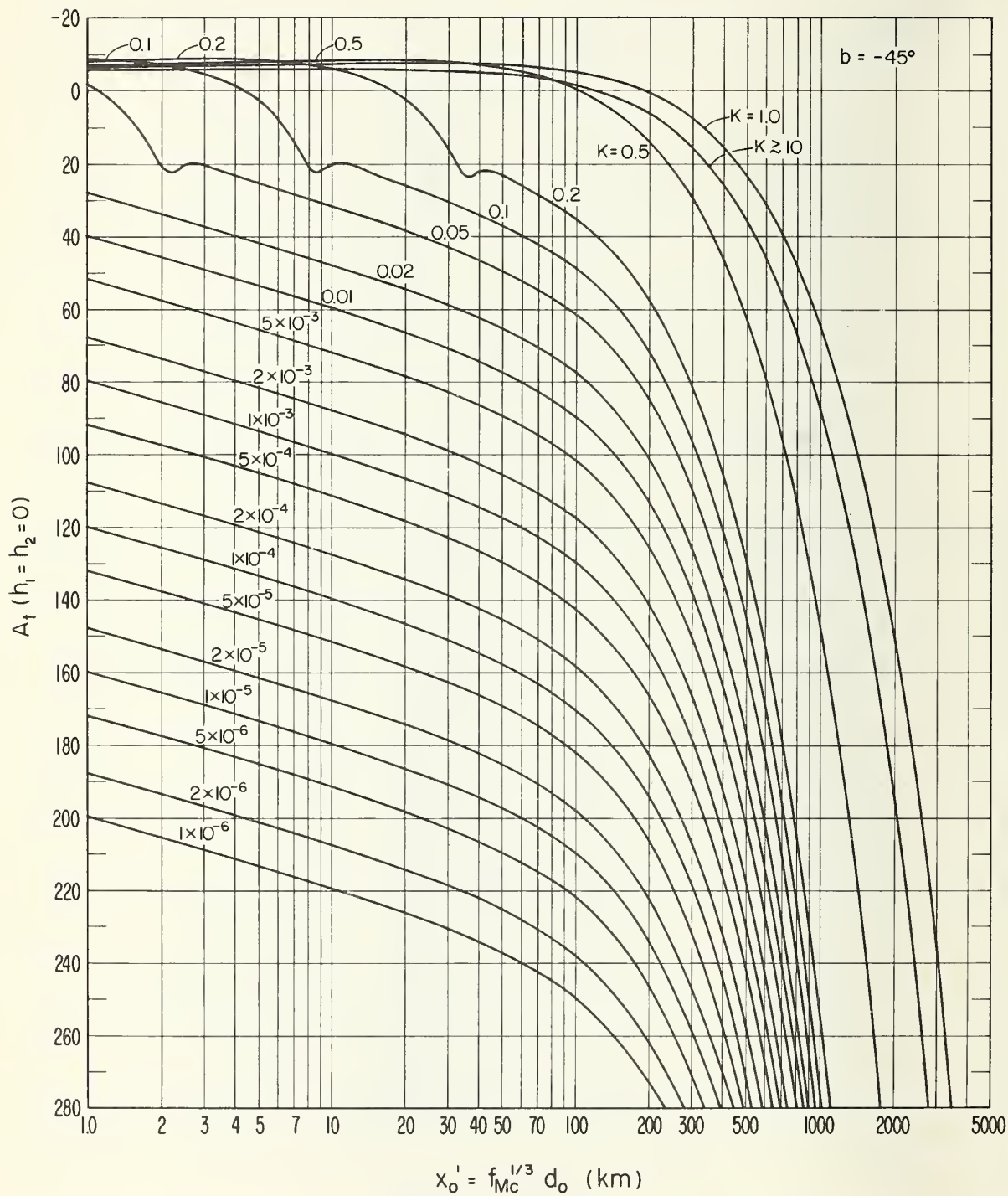


Figure 10. Ground wave attenuation for zero antenna heights,  $b = -45^\circ$ .



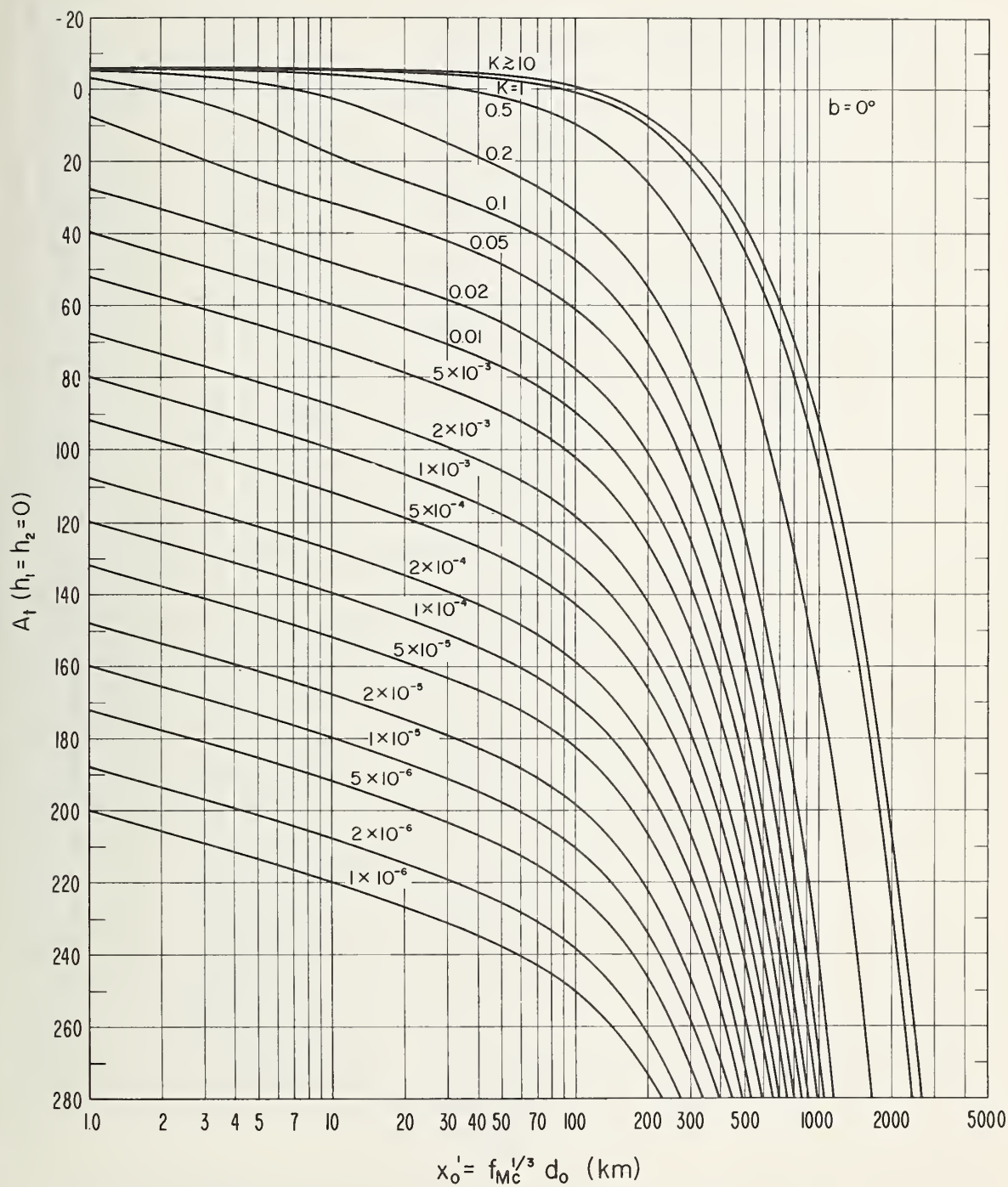


Figure 11. Ground wave attenuation for zero antenna heights,  
 $b = 0^\circ$ .

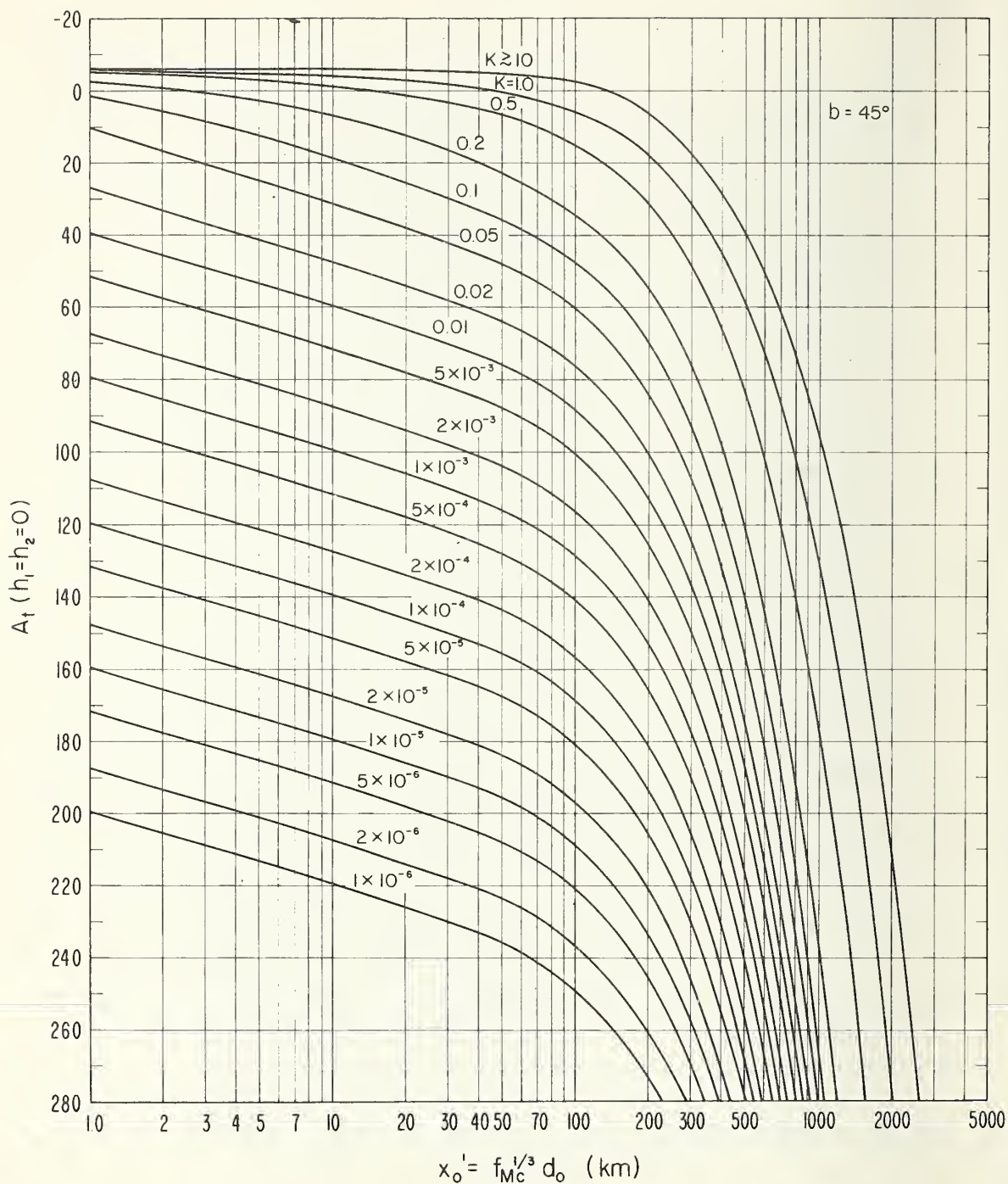


Figure 12. Ground wave attenuation for zero antenna heights,  
 $b = 45^\circ$ .

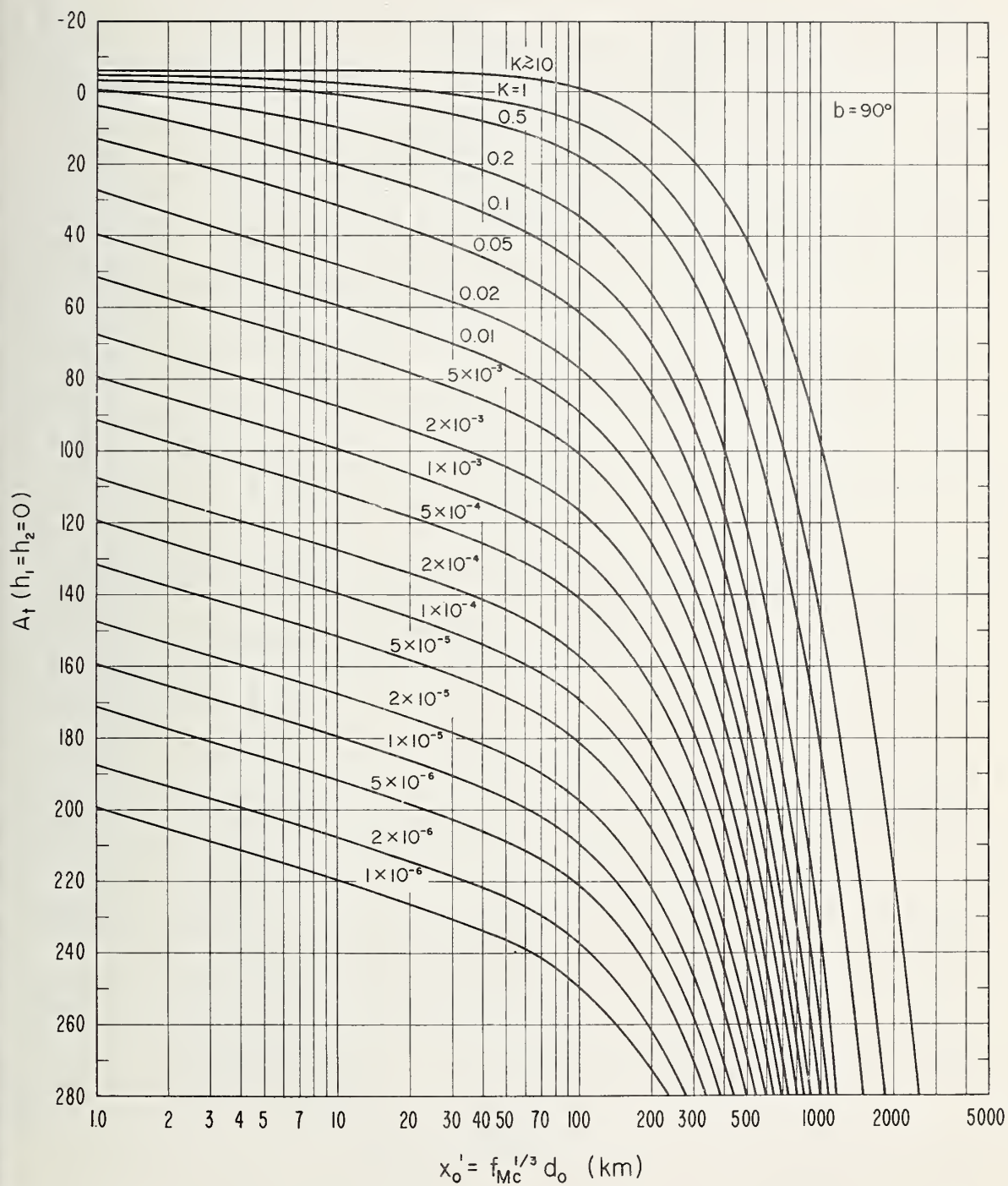


Figure 13. Ground wave attenuation for zero antenna heights,  $b = 90^\circ$ .

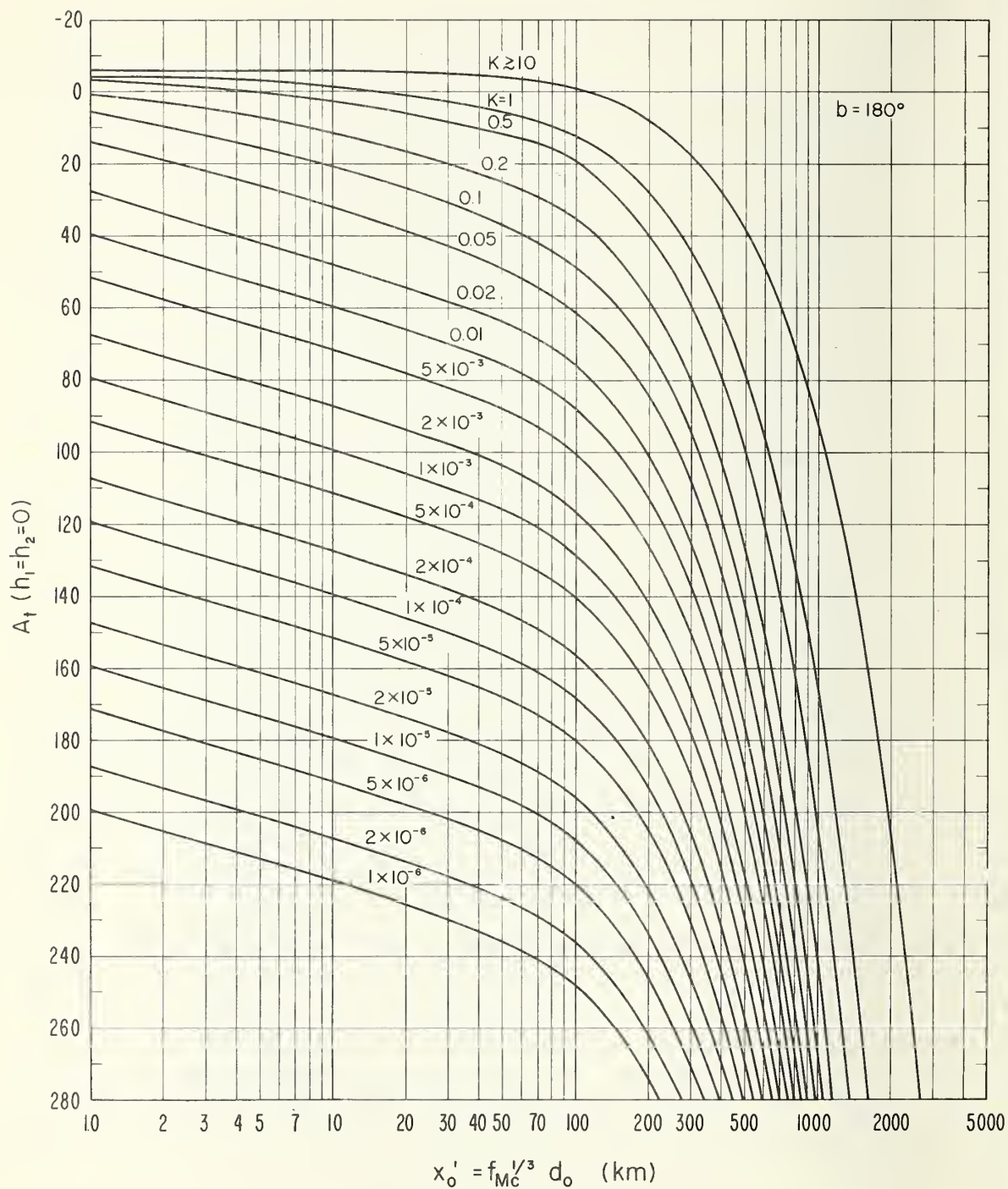


Figure 14. Ground wave attenuation for zero antenna heights,  
 $b = 180^\circ$ .



In figures 9 ( $b = -70^\circ$ ) and 10 ( $b = -45^\circ$ ) the curves show fading effects over short intervals of  $x'_0$  for certain values of  $K$ . As  $b$  becomes positive, these fade-outs disappear and  $A_t$  is seen to increase smoothly with distance.

The calculations of the attenuation curves were not done by numerically evaluating the complete residue series, since a prohibitive number of terms are necessary for small values of  $x'_0$ . In this region (the left hand portion of figures 9 - 14) use was made of the modified flat earth formula developed by Wait [1962b, see equation (108)] in which the leading term is the plane earth attenuation function and successive terms account for the curvature of the sphere. The formula with two curvature correction terms was employed wherever valid until  $x'_0$  became too large, at which point the first term of the residue series could be used from there on out.

Equation (2.4) is strictly applicable only for the case of antennas separated a sufficient distance apart ( $d_0 \gg \lambda$ ) such that the induction and static fields may be neglected. Because of this restriction,  $A_t$  is not shown in the figures for values of  $x'_0 < 1$ . As  $d_0$  (or  $x'_0$ ) goes to zero,  $A_t$  approaches  $20 \log(1/2) = -6.02$ , which would correspond to the surface wave field intensity expected between short vertical electric dipoles situated near each other on a perfectly conducting plane.

It is apparent from figures 9 - 14 that the attenuation is less for the larger values of  $K$ , these values corresponding to vertically polarized waves at the lower frequencies. For example, for  $K \geq 0.1$  and  $f_{mc} \leq 1.0$ , the attenuation is less than 50 db out to distances of 100 km. On the other hand, with horizontal polarization,  $K_h$  is usually much less than unity for all frequencies and the attenuation is greater.

#### 4. ANTENNA EFFECTS

The terms  $L_{t,r}$  and  $G_p = G_t + G_r$  (the subscripts  $t, r$  referring to either transmitting or receiving antenna) in (2.2) describe the effects of the particular transmitting and receiving antennas used in the communication system under consideration.  $L_{t,r}$ , called the ground proximity loss, is defined as the ratio expressed in decibels of the input resistance of the antenna  $r$  to its free space radiation resistance  $r_f$ . As the height of the antenna above the surface is increased, the ratio of the resistances approaches unity and  $L_t$  or  $L_r$  effectively become zero. For heights near the surface, the input resistance is a function of the electromagnetic ground constants  $\epsilon_r$  and  $\sigma$ , the radio frequency  $f_{mc}$ , and the antenna height  $h$  above the surface.

$G_{t,r}$  denotes the free space maximum directivity gain of an optimally oriented loss-free antenna above an isotropic antenna, e.g.,  $G_t = G_r = 10 \log(3/2) = 1.76$  for elementary dipoles and  $G_t = G_r = 2.15$  for half-wave dipoles.

Because present estimates indicate the conductivity of lunar surface material to be relatively poor, a numerical evaluation of input impedance was undertaken [Vogler and Noble, 1963, 1964] considering four types of antennas: vertical and horizontal electric and magnetic dipoles. Short dipoles of length  $dl$  are assumed, the current in which varies as  $I_0 e^{i\omega t}$  with  $I_0$  a constant along the antenna; the magnetic dipoles are then equivalent to small circular loop antennas of area  $dA$ , the axis being in the direction of the dipole. The ground beneath the antenna is assumed to be homogeneous and characterized by its relative dielectric constant  $\epsilon_r$  and conductivity  $\sigma$ .

The input impedance  $Z$ , obtained in terms of the field at the antenna, may be divided into a free space component  $Z_f$  and a component  $\Delta Z$  describing the effect of the presence of the ground:

$$Z = Z_f + \Delta Z. \quad (4.1)$$

Explicit expressions for the impedance change due to ground normalized by the free space radiation resistance,  $\Delta Z/r_f$ , where VED, HED, VMD, HMD refer to the initial letters of the four types of dipoles considered, are then given by

$$\text{VED: } \Delta Z/r_f = i(3/2 \alpha^3) \left[ I_1(N^2) + I_2(N^2) \right], \quad r_f = 20 \beta^2 (dl)^2, \quad (4.2a)$$

$$\text{HED: } \Delta Z/r_f = i(3/4 \alpha^3) \left[ I_1(1) + I_2(N^2) \right], \quad r_f = 20 \beta^2 (dl)^2, \quad (4.2b)$$

$$\text{VMD: } \Delta Z/r_f = i(3/2 \alpha^3) \left[ I_1(1) + I_2(1) \right], \quad r_f = 20 \beta^4 (dA)^2, \quad (4.2c)$$

$$\text{HMD: } \Delta Z/r_f = i(3/4 \alpha^3) \left[ I_1(N^2) + I_2(1) \right], \quad r_f = 20 \beta^4 (dA)^2, \quad (4.2d)$$

where

$$I_1(\delta) = \alpha^2 \int_{i\alpha}^{\infty} \left\{ \frac{\delta x - \sqrt{x^2 - \alpha^2(N^2 - 1)}}{\delta x + \sqrt{x^2 - \alpha^2(N^2 - 1)}} \right\} e^{-x} dx, \quad (4.3a)$$

$$I_2(\delta) = \int_{i\alpha}^{\infty} x^2 \left\{ \frac{\delta x - \sqrt{x^2 - \alpha^2(N^2 - 1)}}{\delta x + \sqrt{x^2 - \alpha^2(N^2 - 1)}} \right\} e^{-x} dx, \quad (4.3b)$$

$$\alpha = 2h\beta = 2h(2\pi/\lambda), \quad N^2 = \epsilon_r - is, \quad s = 60\lambda\sigma(\text{mhos/m}), \quad (4.4)$$

and  $h$  denotes the antenna height in meters above the ground.

The variable  $x$  in (4.3) assumes purely imaginary values from the lower limit to zero, and from there ranges over real values to the upper limit. The sign of the square root is chosen so that the real part is greater than zero. A derivation of the dipole impedances together with asymptotic expressions of (4.2) is contained in the appendix.

Ground proximity loss in terms of the input impedance as given by (4.1) may be expressed as

$$L_{t,r} = 10 \log(r/r_f) = 10 \log \left[ 1 + \text{Re}(\Delta Z/r_f) \right], \quad (4.5)$$



where  $\text{Re}(\Delta Z/r_f)$  denotes the real part of  $(\Delta Z/r_f)$ . Using the relationships of (4.2),  $L_{t,r}$  is plotted versus

$$s = 60 \lambda \sigma (\text{mhos/m})$$

in figures A-1 to A-28 for various values of  $\epsilon_r$  and  $\alpha$ . Notice that for  $\alpha$  greater than about 5, i.e.,  $h/\lambda \gtrsim 0.4$ , the ground loss is always negligible; however, as the antenna height in wavelengths approaches zero,  $L_{t,r}$  may become quite large for certain combinations of ground conductivity and frequency. It is often possible to reduce the effect of the ground through the use of appropriate ground screens. Discussions of this subject are contained in papers by Wait and Surtees [1954] and by Wait [1956].

To show the variation in the normalized input impedance change for both the resistance ( $\text{Re } \Delta Z/r_f$ ) and the reactance ( $\text{Im } \Delta Z/r_f$ ), equations (4.2) are evaluated and plotted in figures A-29 to A-64 as functions of  $|N|$ ,  $\phi/2$ , and  $\alpha$  where,

$$|N| = \left( \epsilon_r^2 + s^2 \right)^{1/4}, \quad \phi/2 = (1/2) \tan^{-1}(s/\epsilon_r), \quad (4.6)$$

with  $\alpha$  and  $s$  as defined in (4.4). It should be emphasized that figures A-29 to A-64 do not show the total input impedance, but only the variation due to the presence of the ground. Impedance curves such as those in the figures are useful not only in estimating antenna requirements for lunar communication systems, but also may be used in determining the electromagnetic characteristics of material composing the moon.

This section will conclude with a brief discussion of the Beverage wave antenna [Beverage, Rice, and Kellogg, 1923]. If considered for semi-permanent installations on the moon, it has the advantage of relatively simply construction and operates most efficiently over poorly conducting soils. The wave antenna in its simplest form consists of a long horizontal wire situated a short height above the ground and terminated at one end through its characteristic impedance. It is a uni-directional antenna with the maximum gain in the direction of the antenna axis and toward the terminated end.

Wait [1954] has shown that the vertical electric field component of a wave antenna is proportional to a complex factor  $T_v$ , termed the "wave tilt" and defined by

$$T_v = \left[ (\epsilon_r - 1) - is \right]^{1/2} / (\epsilon_r - is), \quad (4.7)$$

and a function  $S'$  which depends on the wavelength  $\lambda$ , antenna length  $\ell$ , an angle  $\phi'$  measuring the direction in which the antenna is pointing, and the propagation constant  $\Gamma$  defined as

$$\Gamma \equiv \alpha' + i\beta m, \quad (4.8)$$

where  $\alpha'$  and  $m$  are real and  $\beta = 2\pi/\lambda$ .

For low antenna heights  $h$  an approximate expression for the values of  $\alpha'$  and  $m$  has been given by Carson [1926]:

$$\alpha'/\beta \simeq m - 1 \simeq \left[ 2^{3/2} (\beta h) \sqrt{\epsilon_r^2 + s^2} \ln(4h/d_a) \right]^{-1}, \quad (4.9)$$

where  $d_a$  is the diameter of the antenna wire. For an uninsulated infinitesimally thin antenna actually lying on the ground,  $\Gamma$  may be expressed as [Coleman, 1950]

$$\Gamma \equiv \alpha' + i\beta m = \beta \sqrt{m^2 - (\frac{1}{2})(\epsilon_r + 1) + i(\beta/2)} \left[ \sqrt{(\epsilon_r + 1)^2 + s^2} + (\epsilon_r + 1) \right]^{1/2}. \quad (4.10)$$

The function  $S'$ , obtained by integrating the contributions of all the elements along the antenna, is given by

$$S' = \frac{1 - \exp [ - (\Gamma - i\beta \cos \phi') \ell ]}{(\Gamma - i\beta \cos \phi') \ell}. \quad (4.11)$$

It can be seen from (4.10) that the propagation constant of a wave antenna lying on the ground approaches its free space value  $i\beta$  if the relative dielectric constant is very near unity and the conductivity is extremely small; in this case  $S'$  approaches unity.

The wave antenna power gain [Martin and Wickizer, 1949] referred to an isotropic antenna,  $(P_{wa}/P_{iso})$ , may now be expressed as

$$(P_{wa}/P_{iso}) = (\beta \ell \cos \phi')^2 |S'|^2 \cdot |T_v|^2 (120 R_o / |Z_o|)^2, \quad (4.12)$$

where  $Z_o = R_o + i X_o$  is the characteristic impedance of the wave antenna. The factor  $|T_v|$ , which was discussed in section 3 and defined by (3.2), is shown in figure 2, and  $|S'|$  is graphed in figure 15 as a function of the two parameters  $(\alpha' \ell)$  and  $(\beta \ell)(m - \cos \phi')$ . An example of the wave antenna pattern,

$$|S| = (\beta \ell \cos \phi') \cdot |S'|,$$

as a function of the direction angle  $\phi'$  is shown in figure 16 for several values of  $\beta \ell = 2\pi(\ell/\lambda)$  and for  $m = 1$ ,  $\alpha' = 0$ . It is seen that the antenna is highly directional in the forward direction ( $\phi' = 0$ ); other values of  $m$  and  $\alpha'$  modify the pattern somewhat, but the general shape is the same.

A modification of the wave antenna which is also discussed in the paper by Wait [1954] is one in which the horizontal wire of length  $\ell = 2b$  is center-fed and the ends of the antenna are not terminated with a load impedance. Assuming a current distribution along the wire of

$$I(y) = I_o [\sinh(\Gamma b)]^{-1} \sinh \left\{ \Gamma (b - |y|) \right\}, \quad (4.13)$$

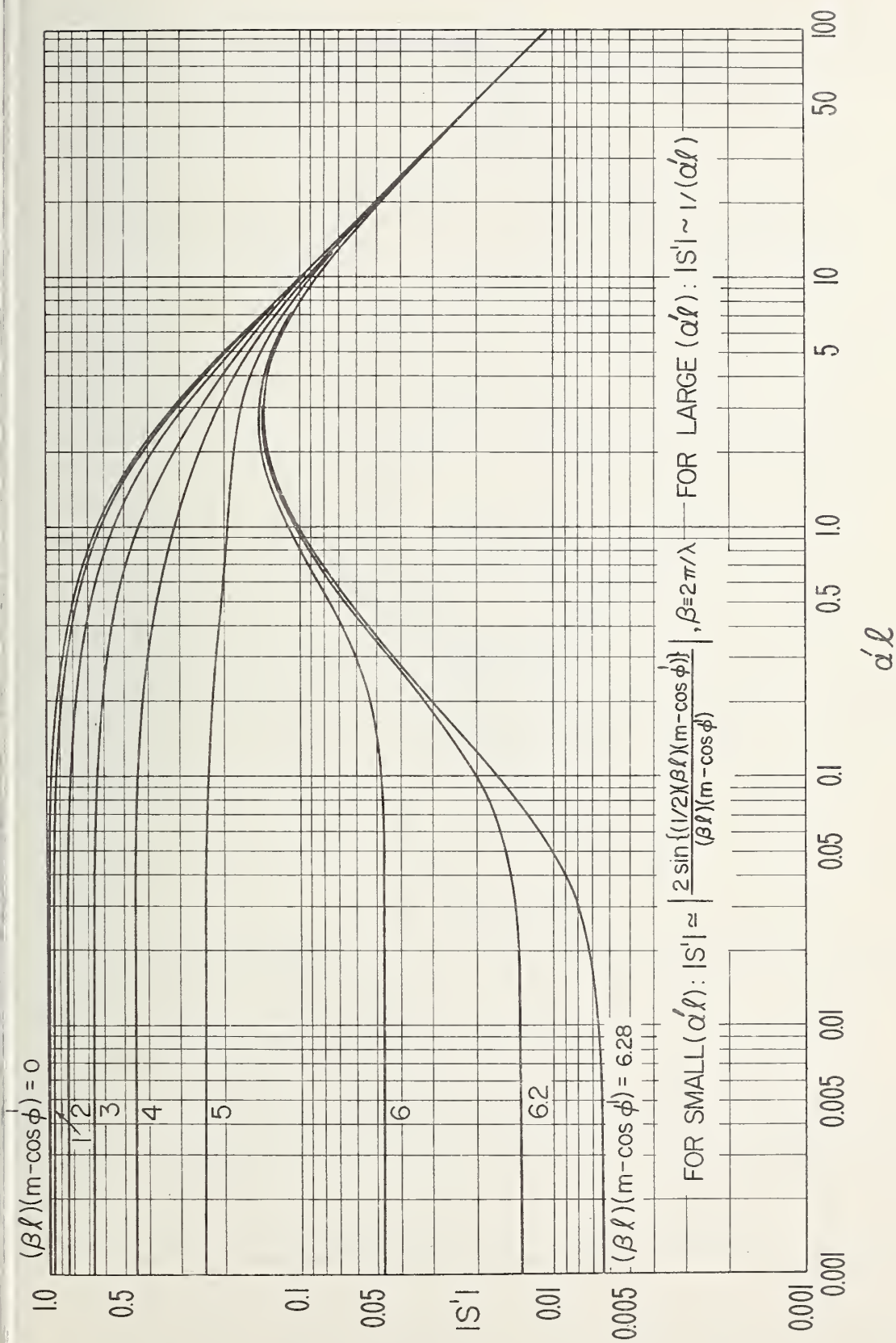


Figure 15. Pattern factor  $|S'|$  for wave antenna of length  $\ell$  and propagation constant  $\Gamma = \alpha' + i\beta m$ .

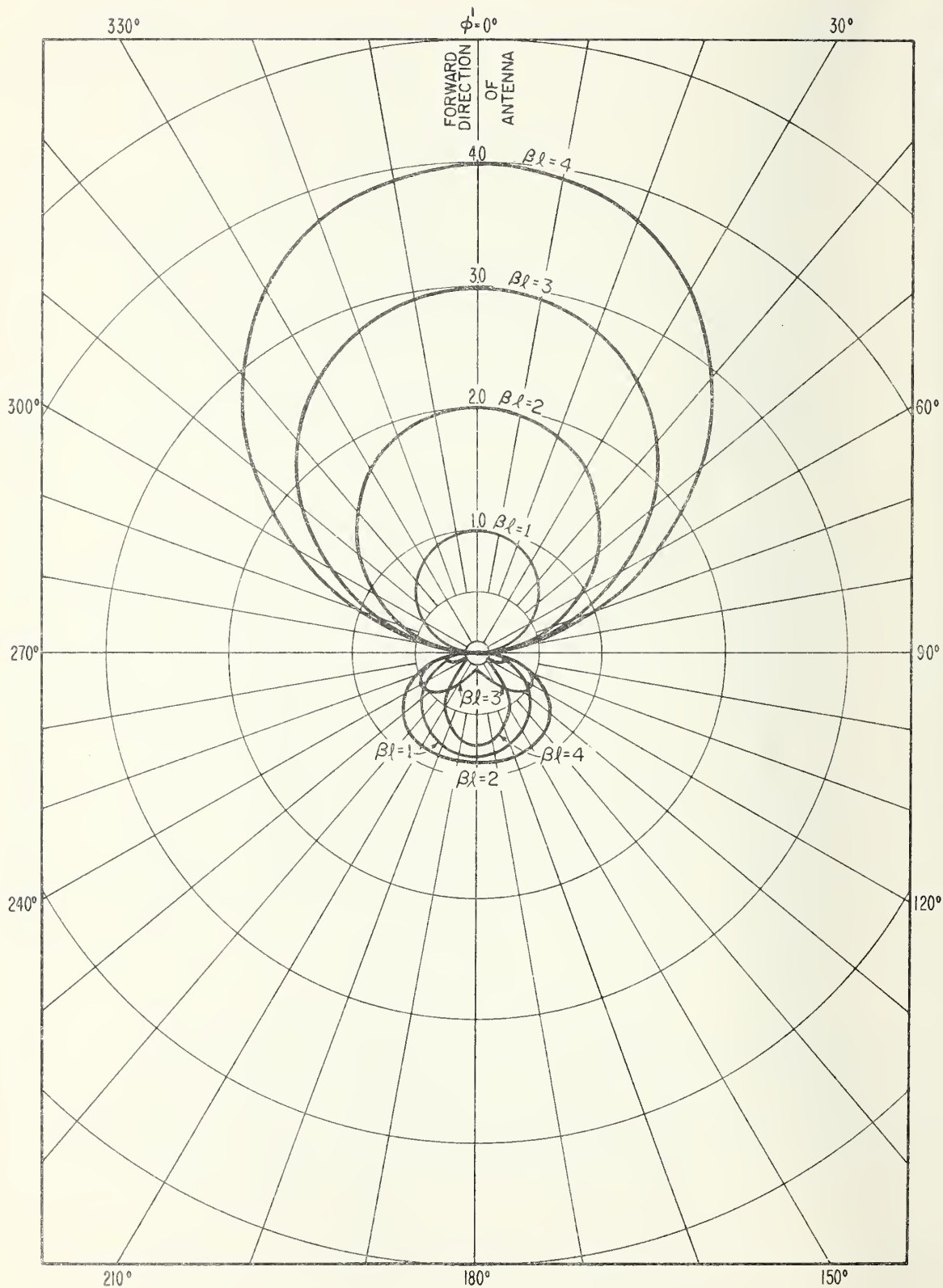


Figure 16. Wave antenna pattern  $|S| = \beta l \cos \phi'$ .  $|S'|$  for  $\alpha' = 0$ ,  $m = 1$ .

where  $I_0$  and  $y$  are respectively the current at and the distance from the feed point, an integration of the elements over the length of the antenna yields for the antenna pattern  $|S|$ :

$$|S| = |\beta b \cos \phi'| \cdot |S_1'|$$

$$= |x_3| \left[ \frac{2 \left\{ \cosh x_1 - \cos(x_2 - x_3) \right\}}{x_1^2 + (x_2 - x_3)^2} \times \frac{2 \left\{ \cosh x_1 - \cos(x_2 + x_3) \right\}}{x_1^2 + (x_2 + x_3)^2} \times \frac{x_1^2 + x_2^2}{\cosh^2 x_1 - \cos^2 x_2} \right]^{\frac{1}{2}}, \quad (4.14)$$

where  $x_1 = \alpha' b$ ,  $x_2 = \beta b m$ , and  $x_3 = \beta b \cos \phi'$ .

Graphs of (4.14) are shown in figure 17 for the case of  $\alpha' = 0$ , which corresponds to very poorly conducting ground. The values of  $|S|$  shown on the figure, however, should be used only with antenna lengths  $l$  such that the quantity  $(\alpha' l)$  is very near zero; if this is not the case,  $|S|$  should be calculated from (4.14). The center-fed wave antenna power gain corresponding to (4.12) is given by

$$\left( \frac{P_{wa}}{P_{iso}} \right) = |S|^2 \cdot |T_v|^2 \left( 120 R_o / |Z_o|^2 \right), \quad (4.15)$$

where  $|T_v|$ ,  $R_o$ , and  $Z_o$  have been defined previously.

The theoretical determination of  $L_t$  or  $L_r$  for a wave antenna in terms of its input resistance is quite difficult. However, considering these quantities essentially as power ratios measuring the effectiveness of the antenna, an estimate of their magnitude may be obtained from (4.12) by assuming that

$$L_{t,r} - G_{t,r} \simeq -10 \log \left( \frac{P_{wa}}{P_{iso}} \right). \quad (4.16)$$

## 5. NOISE EFFECTS

The operating noise factor  $f$  [Norton, 1962] appearing in (2.4) provides a measure of the effects of noise on the receiving system (in previous papers [Vogler, 1963a, 1963b]  $f$  is called the effective noise figure). It is defined by

$$f \equiv [p_a / (k_B t_o b)] / [r(s/n)], \quad (5.1)$$

where  $p_a$  is the signal power available from an equivalent loss-free receiving antenna,  $(k_B t_o b)$  is a reference Johnson-noise power [see (2.3)], and  $r(s/n)$  is the receiver predetection output signal-to-noise ratio.

Since  $p_a$  is the power available from a loss-free antenna, its relationship to the power available from the actual antenna,  $p_r$ , may be expressed as

$$p_a = \ell_c p_r, \quad (5.2)$$



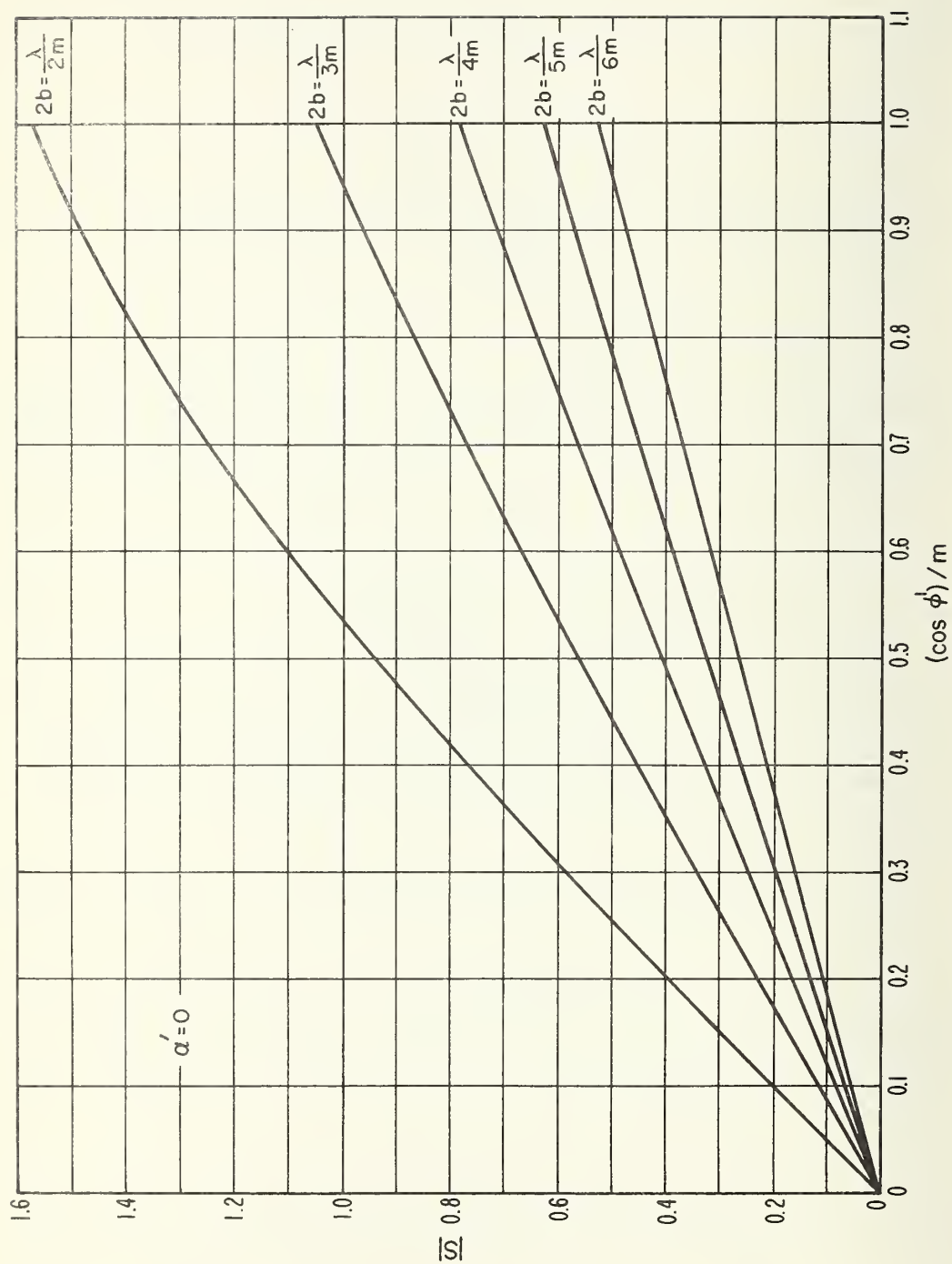


Figure 17.  $|S|$  for center-fed antenna of length  $\ell = 2b$  with  $\alpha' = 0$ .



where  $\ell_c$  is the antenna circuit loss factor. Because the present study is primarily concerned with low antennas over poorly conducting ground, the assumption is made throughout that  $\ell_c \simeq \ell_r$ , where  $\ell_r$  is the ground proximity loss discussed in section 4.

In terms of the noise factors of the receiving system's component parts,  $f$  can be expressed in the following form:

$$f = f_e - 1 + f_c + \ell_c (f_{tl} - 1) + \ell_c \ell_{tl} (f_r - 1), \quad (5.3)$$

where  $f_e$ ,  $f_c$ ,  $f_{tl}$ , and  $f_r$  denote respectively the noise factors of the external noise, antenna circuit, transmission line, and receiver. In terms of the loss factors  $\ell_c$  and  $\ell_{tl}$  of the antenna circuit and transmission line (i.e., the ratio of the available input to output powers of the component),  $f_c$  and  $f_{tl}$  are given by

$$f_c = 1 + (\ell_c - 1)(t_c/t_o), \quad f_{tl} = 1 + (\ell_{tl} - 1)(t_{tl}/t_o), \quad (5.4)$$

where  $t_c$  and  $t_{tl}$  designate the absolute temperatures of the corresponding components and  $t_o$  is a reference temperature.

Generally speaking, the factors  $f_e$  and  $f_c$  will predominate in calculating values of  $f$ , especially at the lower frequencies [Crichlow, Smith, Morton, and Corliss, 1955]; at high frequencies  $f$  depends more on  $f_{tl}$  and  $f_r$ , which are best obtained by direct measurement. By arbitrarily assuming the transmission line loss to be negligible ( $\ell_{tl} = 1$ ) and the antenna circuit temperature very near the reference temperature, (5.1) may be written as

$$f = f_e + \ell_c f_r - 1, \quad \ell_{tl} = 1, \quad t_c = t_o. \quad (5.5)$$

With the approximation  $\ell_c \simeq \ell_r$ , this then becomes

$$f \simeq f_e + \ell_r f_r - 1, \quad (5.6)$$

where  $\ell_r$  has been defined in section 4.

The principal sources of external noise received by an antenna located on the moon are (1) galactic or cosmic, (2) earth-based, and (3) solar. The amount of noise affecting the signal depends on the location, orientation, and directional gain of the particular antenna under consideration. Some preliminary studies [Page, 1962] of earth-based and solar noise components indicate that, in the case of a quiescent sun, solar noise is negligible compared with galactic noise unless the antenna beam is oriented directly toward the sun. On the other hand terrestrial atmospheric noise might become comparable to the galactic noise in the lower frequency range; however, this assumes a negligible ionospheric shielding effect.

Galactic noise levels have been fairly well established at the higher frequencies through earth-based measurements. Figure 18 shows an estimate of the external noise factor  $F_e = 10 \log f_e$  obtained from galactic noise data compiled by Menzel [1961] and by Hartz [1963]; the reference

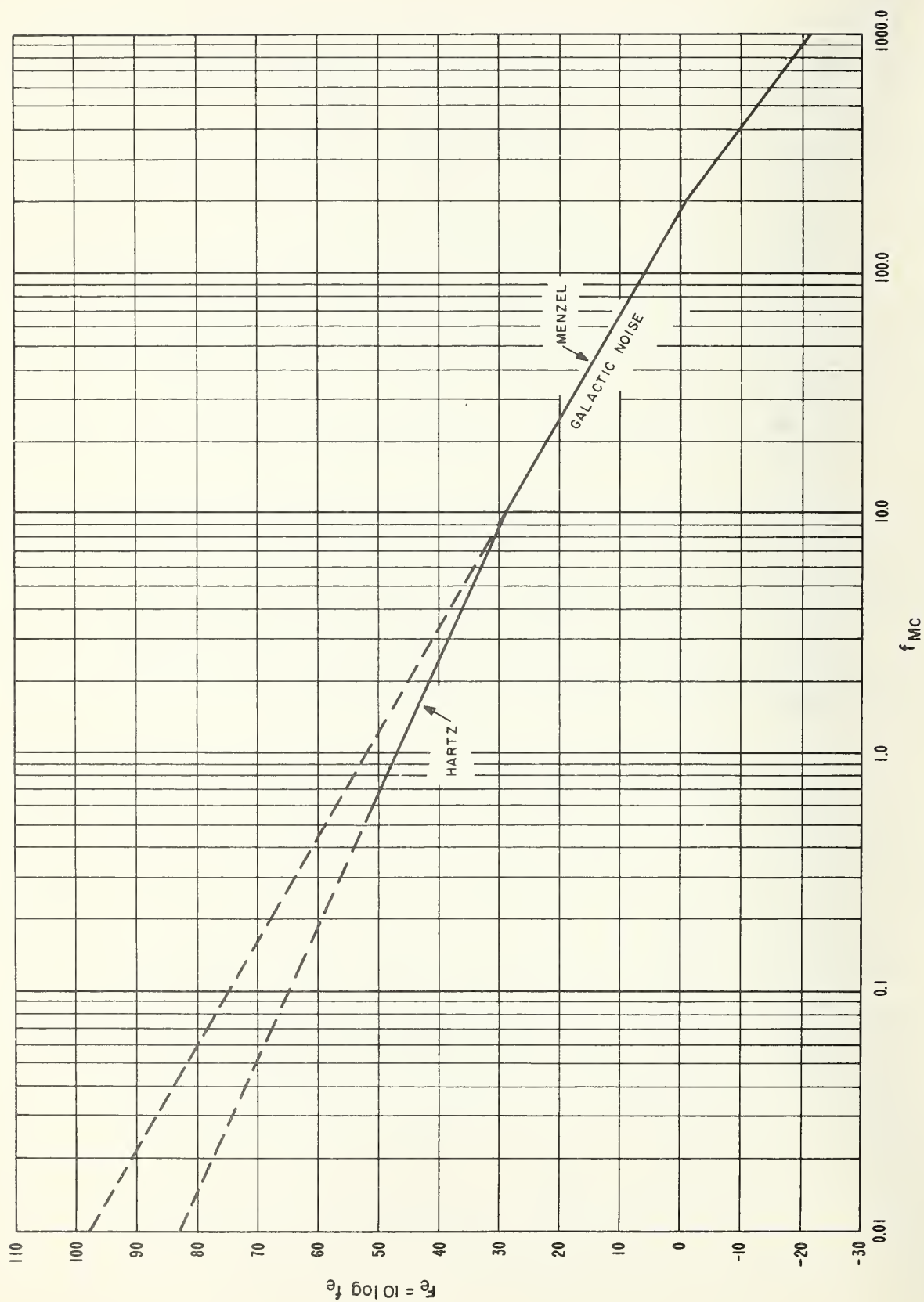


Figure 18. External noise factor,  $F_e$ , considering galactic noise only.

temperature assumed here is  $t_0 = 288.37^\circ \text{K}$ . Empirical expressions used to plot the galactic noise curve are

$$\begin{aligned} f_e &= 6.467 \times 10^6 f_{mc}^{-3}, & f_{mc} &\geq 200, \\ f_e &= 1.585 \times 10^5 f_{mc}^{-2.3}, & 10 &\leq f_{mc} \leq 200, \end{aligned} \quad (5.7a)$$

from the Menzel data, and

$$f_e = 5.012 \times 10^4 f_{mc}^{-1.8}, \quad 0.5 \leq f_{mc} \leq 10, \quad (5.7b)$$

from the Hartz data obtained from Topside Sounder measurements. The upper and lower dashed lines on the figure are extrapolations of the  $f_{mc}^{-2.3}$  and  $f_{mc}^{-1.8}$  frequency variations.

It is physically apparent that at some lower frequency the galactic noise curve will at least level off. Until information from low frequency measurements are available, the extrapolations of figure 18 may be used to provide (hopefully pessimistic) estimates of galactic noise.

## 6. POSSIBLE IONOSPHERIC EFFECTS

At the present time there is no indication that the moon possesses a neutral atmosphere of any significant magnitude. Because of this, it is unlikely that lunar surface propagation will be affected by ionospheric considerations to the same extent as terrestrial propagation. However, studies have been made showing the possible existence of a weak lunar ionosphere caused by solar wind. This section will discuss briefly the effect on propagation of two forms of possible ionospheres.

If a negligible magnetic field is assumed and the motion of heavy ions is neglected, the ionosphere may be characterized by its index of refraction  $N_i$  as follows:

$$N_i^2 = \left\{ 1 - \frac{f_{cr}^2}{f_{mc}^2 + f_v^2} \right\} - i \left\{ \frac{f_v f_{cr}^2}{f_{mc} (f_{mc}^2 + f_v^2)} \right\}, \quad (6.1)$$

where  $f_{mc}$  denotes the signal frequency,  $f_v$  the collision frequency, and  $f_{cr}$  the critical or plasma frequency, all measured in Mc/s. In terms of the electron density/cm<sup>3</sup>,  $n$ , the critical frequency is given by

$$f_{cr}^2 \approx 8.1 \times 10^{-5} n, \quad (6.2)$$

where, in general,  $n$  is a function of the height  $h$  above the ground:  $n = n(h)$ .

One form of ionosphere that may possibly occur extends from the moon's surface to some distance above, the electron density decreasing with height. Elsmore [1957], using studies of lunar occultation of the Crab Nebula, has hypothesized surface electron densities on the order of  $10^3$  to  $10^4$  electrons/cm<sup>3</sup>. For signal frequencies near or less than the collision frequency, this ionospheric model presents a propagation problem which, as far as the author is aware, has never

been investigated and is beyond the scope of the present paper. Considerable theoretical study would be necessary to determine propagation characteristics at these low frequencies.

For radio frequencies such that  $f_v/f_{mc} \ll 1$ , an estimate of the effect of a surface ionosphere on propagation at frequencies greater than the plasma frequency may be obtained through the concept of effective radius [Burrows and Atwood, 1949]. The effective radius,  $r_e$ , introduces a correction to the actual radius,  $r_o$ , that allows for the refraction of the radio wave as it travels through the medium (in this case the model ionosphere) above the ground. Expressed in terms of an effective radius factor  $k$  [Wait, 1961]:

$$k = \frac{r_e}{r_o} = \left[ 1 + \frac{r_o N_i'(h=0)}{N_i(h=0)} \right]^{-1}, \quad (6.3)$$

where  $N_i'(h=0)$  denotes the gradient of the refractive index with respect to height evaluated at the surface.

With the restriction that  $f_v/f_{mc} \ll 1$ , (6.1) may be rewritten as

$$N_i^2 \simeq 1 - f_{cr}^2/f_{mc}^2 = 1 - 8.1 \times 10^{-5} n(h)/f_{mc}^2, \quad (6.4)$$

and  $k$  then becomes

$$k \simeq \left[ 1 + \frac{4.05 \times 10^{-5} r_o \{-n'(0)\}}{N_i^2(0) \cdot f_{mc}^2} \right]^{-1} \simeq \left[ 1 + \frac{0.07 \{-n'(0)\}}{f_{mc}^2 - 8.1 \times 10^{-5} n(0)} \right]^{-1}, \quad (6.5)$$

where  $n(0)$  is the electron density/cm<sup>3</sup> at the surface and  $n'(0)$  is the electron density gradient with respect to height in km evaluated at the surface. It can be seen that (6.5) may be used only for radio frequencies such that

$$f_{mc} > f_{cr} = 9 \times 10^{-3} \sqrt{n(0)};$$

thus, for an electron density at the surface of, say,  $n(0) = 10^4$ , the effective radius concept should be restricted to frequencies of 1 Mc/s or greater.

The curves of figures 9-14 will now provide estimates of the attenuation  $A_t$  if they are read as functions of a modified  $x_o'$ ,  $x_o'(k)$ , and a modified  $K_{h,v}$ ,  $K_{h,v}(k)$ , where

$$x_o'(k) = k^{-\frac{2}{3}} f_{mc}^{\frac{1}{3}} d_o(km), \quad K(k) = 3.02 \times 10^{-2} k^{-\frac{1}{3}} / |T| \cdot |Q| \cdot f_{mc}^{\frac{1}{3}}, \quad (6.6)$$

and  $k$  is given by (6.5). Notice that  $x_o'(1)$  and  $K(1)$  are simply those parameters discussed in section 3 and defined by (3.5) and (3.1); the effective radius factor  $k$  does not modify  $b_{h,v}^o$ .

To show the variation of  $k$  with frequency, (6.5) is plotted in figure 19 for several values of the surface electron density gradient  $n'(0)$ . The values chosen do not represent any experimental evidence but are used merely to show the variation of  $k$  with the gradient. Figure 19 shows that, as the gradient becomes more negative,  $k$  decreases and, in general, a higher attenuation of the signal is to be expected. Should a positive gradient exist, less attenuation of the signal would occur.

Another possible lunar ionosphere that has recently been investigated [Weil and Barasch, 1963] is similar in form to the terrestrial ionosphere. Weil and Barasch, through theoretical considerations of solar wind influence near the moon together with solar stream data, postulate an ionized elevated layer with an electron density of about  $350/\text{cm}^3$  at 0.6 lunar radii above the surface. The layer occurs only in the general direction of the sun, and their numerical values are based on quiet sun data.

The theory of this form of ionospheric propagation is well established and, given the necessary data, will provide good estimates of propagation capabilities. The remainder of the section will discuss briefly the simple geometrical-optics approximation to ionospheric propagation. A detailed account of the subject is contained in a paper by Wait [1962c].

In the geometrical-optics approximation, the field at a point is considered to be the sum of multiply-reflected radio rays arriving from the transmitting source, the reflections occurring between the ground surface and the ionosphere. At distances less than its caustic, the single hop component of the field, i. e., the ray undergoing only one reflection from the ionosphere, will be the most significant. However, the total field is given by the sum of all the rays added together in proper phase; at short distances from the transmitting antenna, the ground wave component must also be included.

In order to gain some idea of the effect on lunar propagation of an elevated ionosphere, the attenuation of the single-hop sky wave is evaluated, assuming the Weil and Barasch model ionosphere with a sharp lower boundary. The assumption of a sharp boundary rather than a more realistic one will give a lower estimate of the attenuation than is actually obtainable, but will still provide a reasonable estimate for the purposes of the present study. Letting  $\theta (= d_0/r_0)$ ,  $\rho (= h/r_0)$ ,  $\phi_g$ , and  $\phi_i$  denote the geometrical quantities indicated in figure 20, the sky wave attenuation  $A_s$  may be expressed as

$$A_s \sim -20 \log \left[ \left( \frac{C \sin^2 \phi_g}{2 \theta_1 / \theta} \right) |1 + R_g|^2 \cdot |R_i| \right], \quad (6.7)$$

where  $R_g$  and  $R_i$  are Fresnel reflection coefficients of the ground and ionosphere respectively:

$$R_g = \frac{N_g^2 \cos \phi_g - \sqrt{N_g^2 - \sin^2 \phi_g}}{N_g^2 \cos \phi_g + \sqrt{N_g^2 - \sin^2 \phi_g}}, \quad N_g^2 = \epsilon_g - i s_g, \quad (6.8)$$



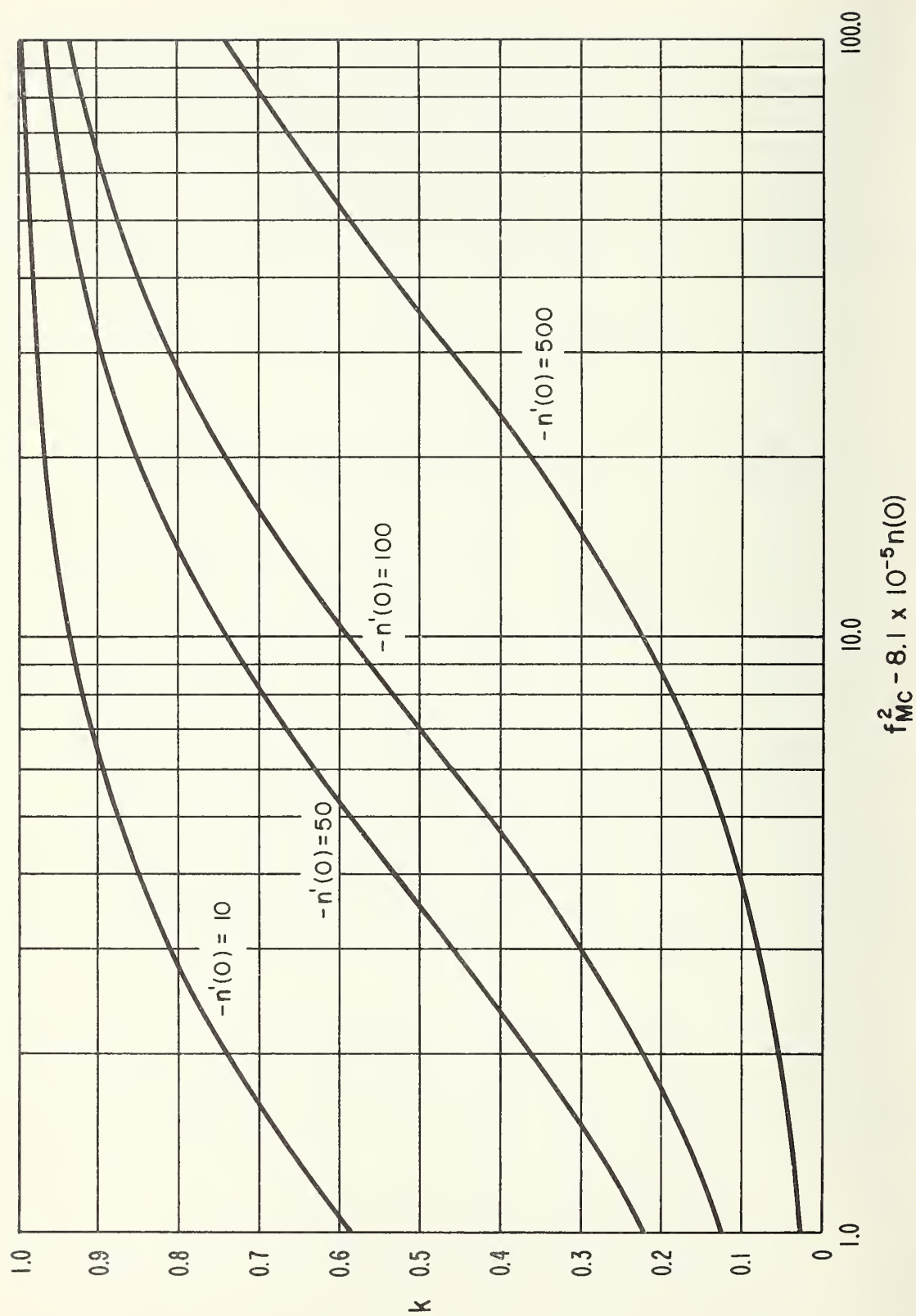


Figure 19. Effective radius factor  $k$  as a function of the surface electron density gradient,  $-n'(0)$ .

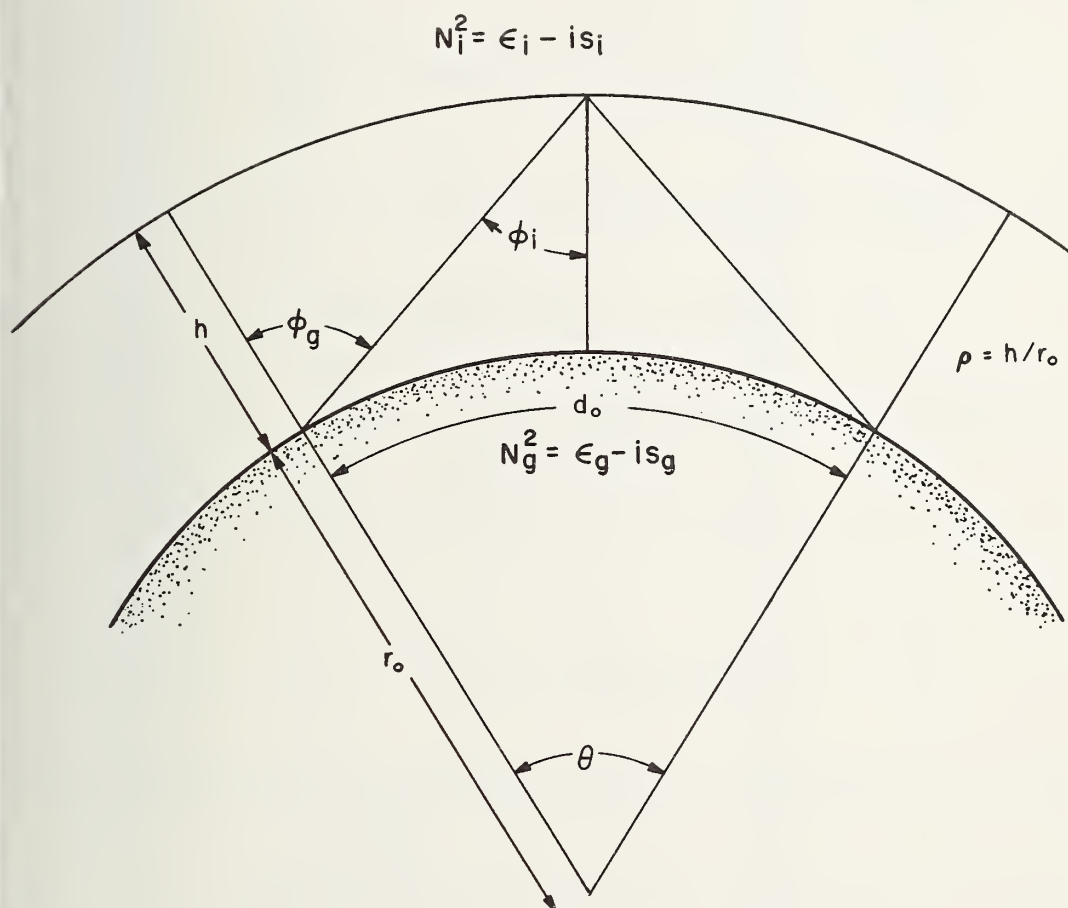


Figure 20. Geometry for single-hop sky wave propagation.

$$R_i = \frac{N_i^2 \cos \phi_i - \sqrt{N_i^2 - \sin^2 \phi_i}}{N_i^2 \cos \phi_i + \sqrt{N_i^2 - \sin^2 \phi_i}}, \quad N_i^2 = \epsilon_i - i s_i, \quad (6.9)$$

and the angles  $\phi_g$  and  $\phi_i$  may be calculated from

$$\phi_g = \tan^{-1} \left[ \frac{(1+\rho) \sin(\theta/2)}{(1+\rho) \cos(\theta/2) - 1} \right], \quad \phi_i = \sin^{-1} \left[ \frac{\sin \phi_g}{1+\rho} \right]. \quad (6.10)$$

The quantity  $C$  in (6.7) is a convergence coefficient defined by

$$C = \left[ \frac{1+\rho}{\cos(\theta/2)} \right] \left[ 1 + \frac{\sin^2(\theta/2)}{(1+\rho) \cos(\theta/2) - 1} \right]^{1/2}, \quad (6.11)$$

and  $\theta_1$  is related to the total distance traversed by the ray:

$$\theta_1 = \sqrt{\rho^2 + 4(1+\rho) \sin^2(\theta/4)}. \quad (6.12)$$

Notice that (6.11) [and therefore (6.7)] is valid only as long as

$$\theta < \theta_c = 2 \cos^{-1} [1/(1+\rho)].$$

$\theta_c$  corresponds to the distance at which a caustic is encountered, and other formulas must be used to calculate the attenuation in this region. The distances considered here will be only those such that  $\theta < \theta_c$ .

At VLF and for the distances of interest, the reflection coefficient of the ground  $R_g$  is near unity even for the very poorly conducting ground expected on the moon. On the other hand, the ionospheric reflection coefficient  $R_i$  can have a pronounced effect on propagation estimates. Figure 21 shows a plot of  $|R_i|$  as a function of the ionosphere height  $\rho = h/r_0$  and

$$s_i = f_v f_{cr}^2 / f_{mc} \left( f_{mc}^2 + f_v^2 \right)$$

obtained from (6.1). Notice that  $|R_i|$  depends quite critically on the parameter  $\epsilon_i$  and, hence, on estimates of  $n$  and  $f_v$ . If an elevated lunar ionosphere does exist, data concerning these quantities are necessary for VLF propagation predictions. The purely geometric factor

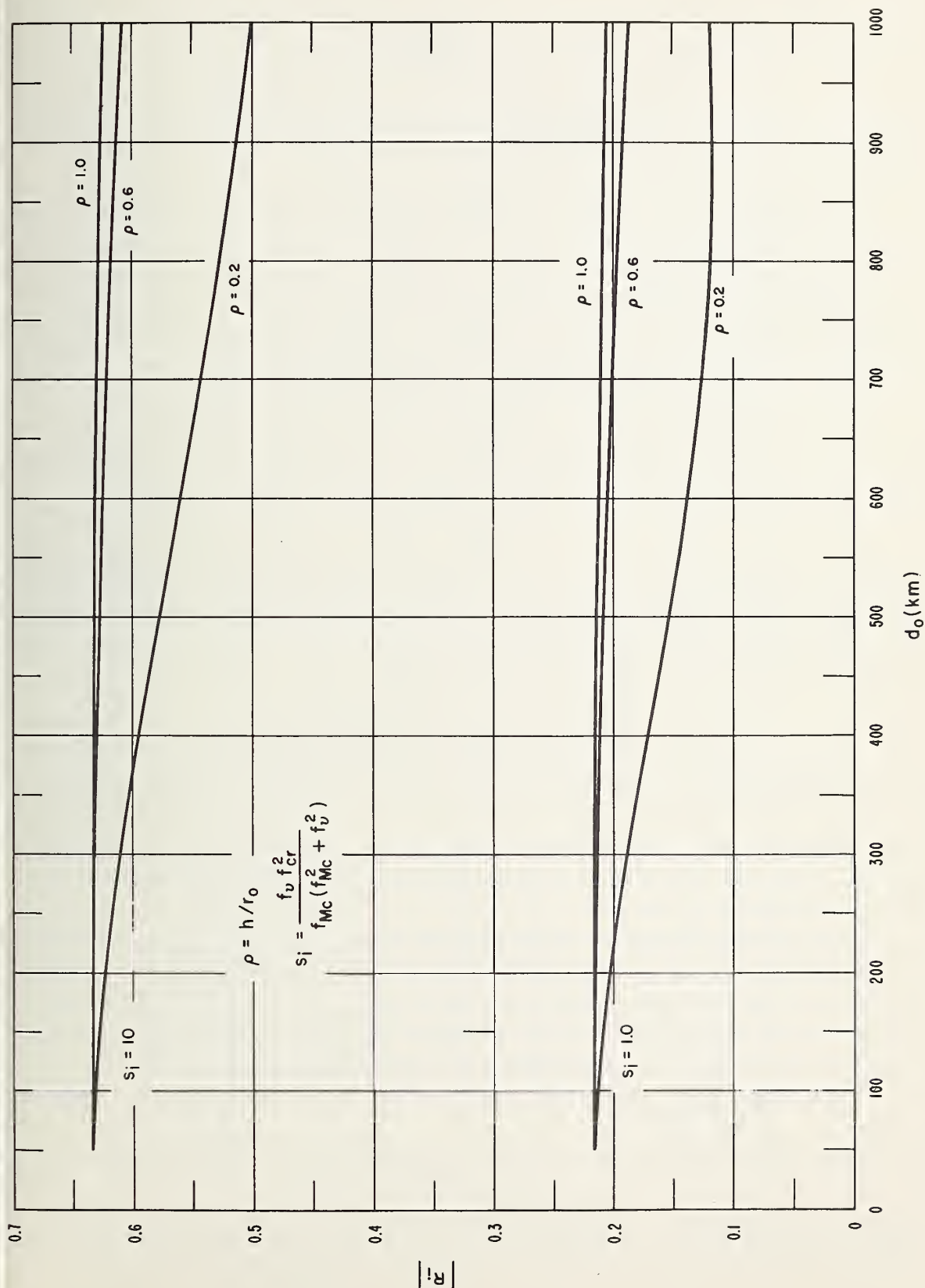


Figure 21. Magnitude of the ionospheric reflection coefficient,  $|R_i|$ .

$$\left( C \sin^2 \phi_g \right) / \left( 2 \theta_1 / \theta \right)$$

appearing in (6.7) depends only on the distance  $d_0$  between the transmitting and receiving points and on the height of the ionosphere; curves of this factor are presented in figure 22 for various values of  $\rho$ .

The attenuation  $A_g$  of a single-hop sky wave relative to a free space inverse distance field is shown in figure 23 as calculated from (6.7). For these curves the ground is described by  $N_g^2 = 2 - i 180$ , and the ionosphere at a height  $\rho = 0.6$  is described by  $N_i^2 = 1 - i s_i$ , where  $s_i$  assumes the values 1 and 10. At a radio frequency of  $f_{mc} = 0.01$ , for example, the curves would be valid for a ground conductivity  $\sigma_g = 10^{-4}$  mhos/m and an ionosphere described by two values of the ratio  $(n/f_v) \simeq 125$  and  $(n/f_v) \simeq 1250$ ; the latter values assume  $f_v \gg f_{mc}$ . The dashed curves in the figure show the vertically polarized ground wave attenuation  $A_t$  for  $f_{mc} = 0.01$  and 0.1; this component of the field is dominant at the shorter distances. It can be seen that over the range of distance shown, the difference in attenuation between the two sky wave curves is about 10 db, this difference arising from the ionospheric reflection coefficient  $R_i$ . A change in ground constants at VLF produces very little difference in attenuation for a given  $s_i$ .

According to Weil and Barasch [1963] the ionosphere would exist (with any appreciable magnitude) only within about  $60^\circ$  from the sun-moon line; thus, it would not be a dependable mechanism for long-term propagation. It should be remembered, however, that it could occasion interference effects in VLF ground wave communication circuits at those distances where the ground wave and sky wave components are comparable in magnitude.

## 7. CALCULATION OF REQUIRED POWER

Attempts have been made recently to deduce the electromagnetic properties of the moon's surface material through the use of radar data [Senior and Siegel, 1960]. Although differences exist concerning the exact interpretation of the data [Brown, 1960; Daniels, 1961], there is general agreement that the relative permittivity is not far above unity and that the conductivity is quite low. In any case, most of the graphs discussed in the preceding sections are applicable to a wide range of values of  $\epsilon_r$  and  $\sigma$ .

Senior and Siegel estimate the relative dielectric constant and conductivity of lunar surface material to be  $\epsilon_r = 1.1$  and  $\sigma = 3.4 \times 10^{-4}$  mhos/m. Materials constituting the earth's crust have been found with conductivities of this order, but not with such a low permittivity. For the purpose of arriving at some estimate of lunar propagation conditions, it will be assumed that  $\epsilon_r$  ranges from 1.1 to 2.0 and  $\sigma$  lies between  $10^{-3}$  and  $10^{-4}$  mhos/m.

By choosing a reference temperature  $t_0 = 288.37^\circ \text{K}$  (as in section 5), the required power given by (2.4) may be rewritten as

$$P_t = L_p - (G_t + G_r) + L_t + R + F + B - 204 \quad (7.1)$$

where the propagation loss  $L_p$  for ground wave attenuation between isotropic antennas is given by



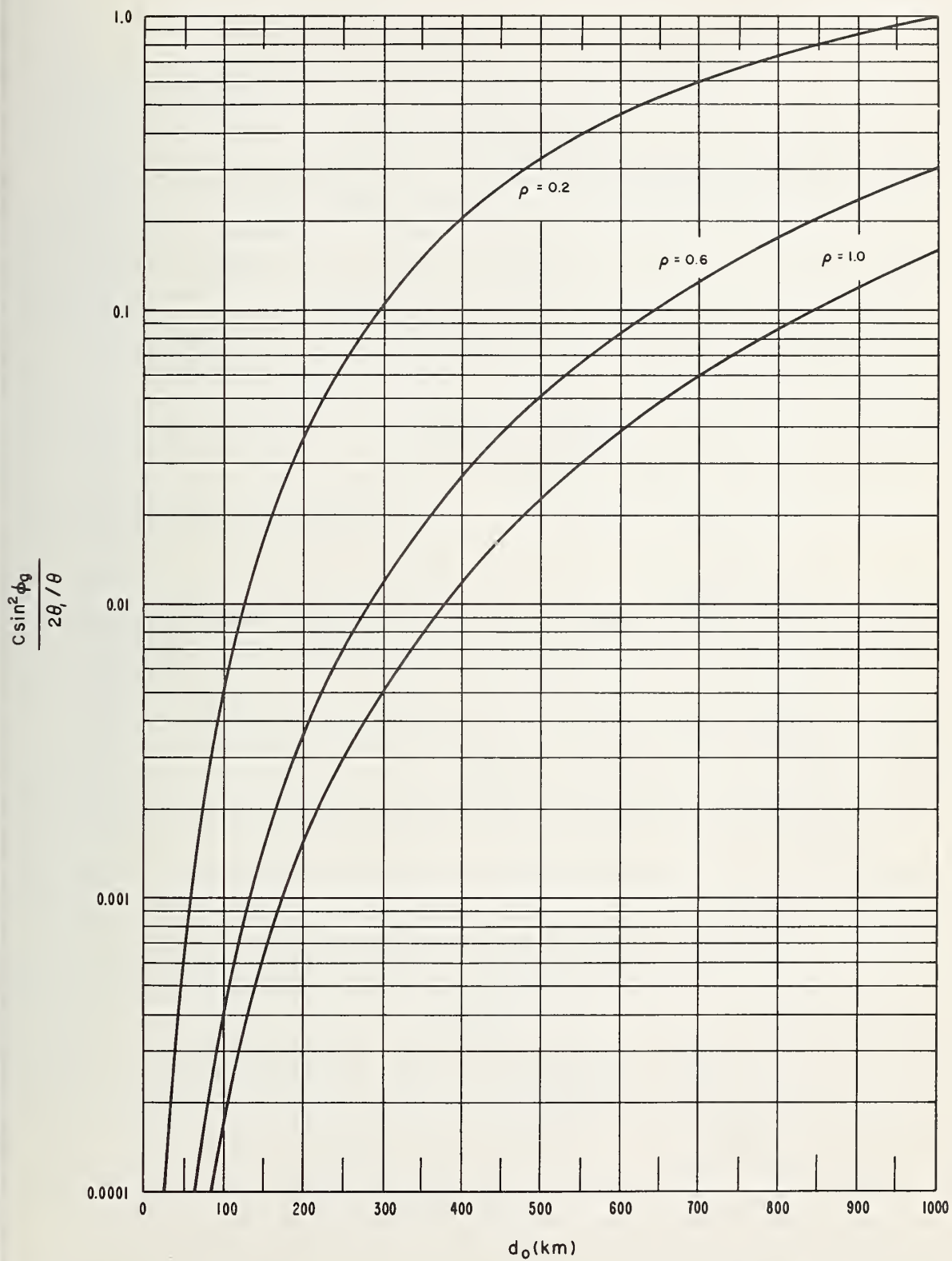


Figure 22. The geometric factor,  $(C \sin^2 \phi_g) / (2 \theta_1 / \theta)$ , for use in (6.7).

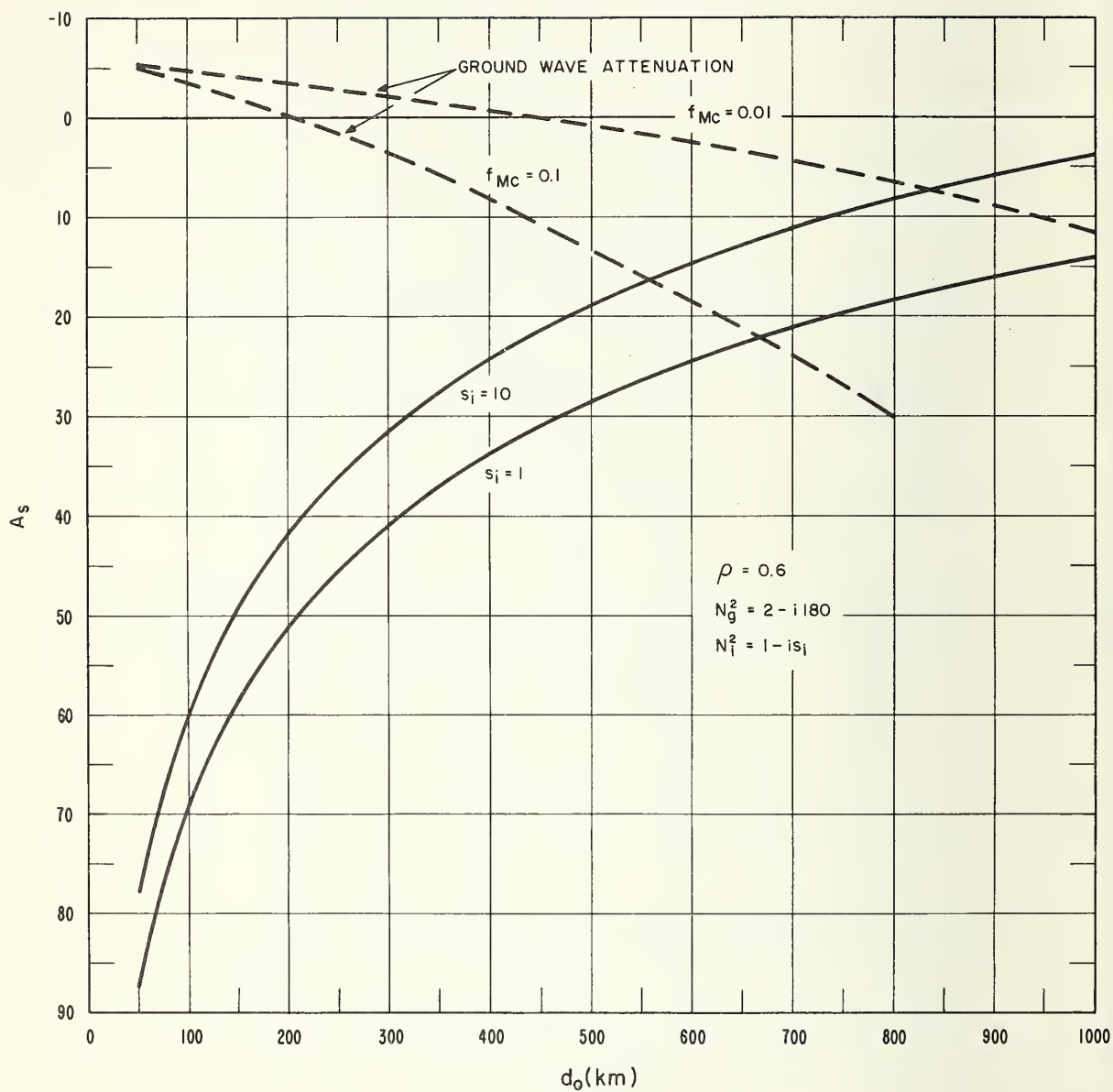


Figure 23. Single-hop sky wave attenuation  $A_s$ .

$$L_p = 32.45 + 20 \log d_o(\text{km}) + 20 \log f_{mc} + A_t . \quad (7.2)$$

For sky wave propagation,  $L_p$  would be calculated by (7.2) after replacing  $A_t$  by the  $A_s$  discussed in section 6.

Figure 24 shows curves of  $L_p$  for a vertically polarized ground wave over homogeneous ground as a function of frequency and distance. Values of  $A_t$  were obtained from figures 11 through 14 by linear interpolation in both the  $K_v$  and  $b_v^\circ$  directions,  $K_v$  being given by figure 2 and (3.1) with  $|Q_v| = 1$ , and  $b_v^\circ$  being read from figure 4. Notice that  $L_p$  varies inversely with conductivity at the lower frequencies, while at high frequencies the effect of  $\sigma$  variation becomes negligible.

To show the use of (7.1) in estimating required power for a particular communication system, the following example will be considered. Assume a communication system consisting of a wave antenna lying on the moon's surface and transmitting towards a short vertical electric dipole placed some distance away and in an optimum direction from the transmitter ( $\phi' \simeq 0^\circ$ ). An estimate of  $L_t - G_t$  may be obtained from (4.16) and (4.12) by assuming the free space value for the wave antenna characteristic impedance:

$$|Z_o| \simeq R_o \simeq 120\pi .$$

For the case of an antenna of length  $l = \lambda/4$ ,  $L_t - G_t$  is plotted versus frequency in figure 25. Again, the antenna loss varies noticeably with conductivity at the lower frequencies, but not at the higher ones.

A comparison of figure 18 and figures A-1 and A-2 shows that for a dipole at a height of, say,  $h = \lambda/16$  the external noise tends to "blanket out" the effect of the antenna circuit loss. This is shown in figure 26, which is a plot of the operating noise factor as given by (5.6) with an assumed receiver noise factor of  $f_r = 4$ . Now by using figures 24, 25, and 26, and the dipole gain of  $G_r = 1.76$ , the required power delivered to the transmitting antenna terminals for a given type of service may be estimated from (7.1). Figure 27 shows values of  $P_t - (R+B)$  as a function of frequency for antenna separation distances of 10, 100, and 500 km.

To estimate the required power delivered to the terminals of the transmitting antenna, the type of communication service desired must be designated, thus specifying  $R$  and  $B$ . For example, with standard broadcast service and a bandwidth of 10 kc/s,  $R$  may have the value 39 db [CCIR, 1951] and  $B = 40$  db so that 79 db should be added to the curves of figure 27 to obtain the required power in decibels above 1 watt. Thus the power required for this type of service in the example system at a range of 10 km and for a frequency of 300 kc/s would be about 10 db or 10 w. For a low-grade voice communication service and 6 kc/s bandwidth,  $R = 9$  db [CCIR, 1951],  $B = 38$  db, and 47 db would be added to the curves. The required power in this case at a distance of 100 km and for a frequency of 100 kc/s would be about 16 w.

If fixed wave antenna lengths and dipole heights are considered, rather than the variable lengths and heights assumed for figure 27, ground proximity loss curves may be recalculated from the equations and graphs of section 4 and required power estimates obtained from (7.1). Figure 28

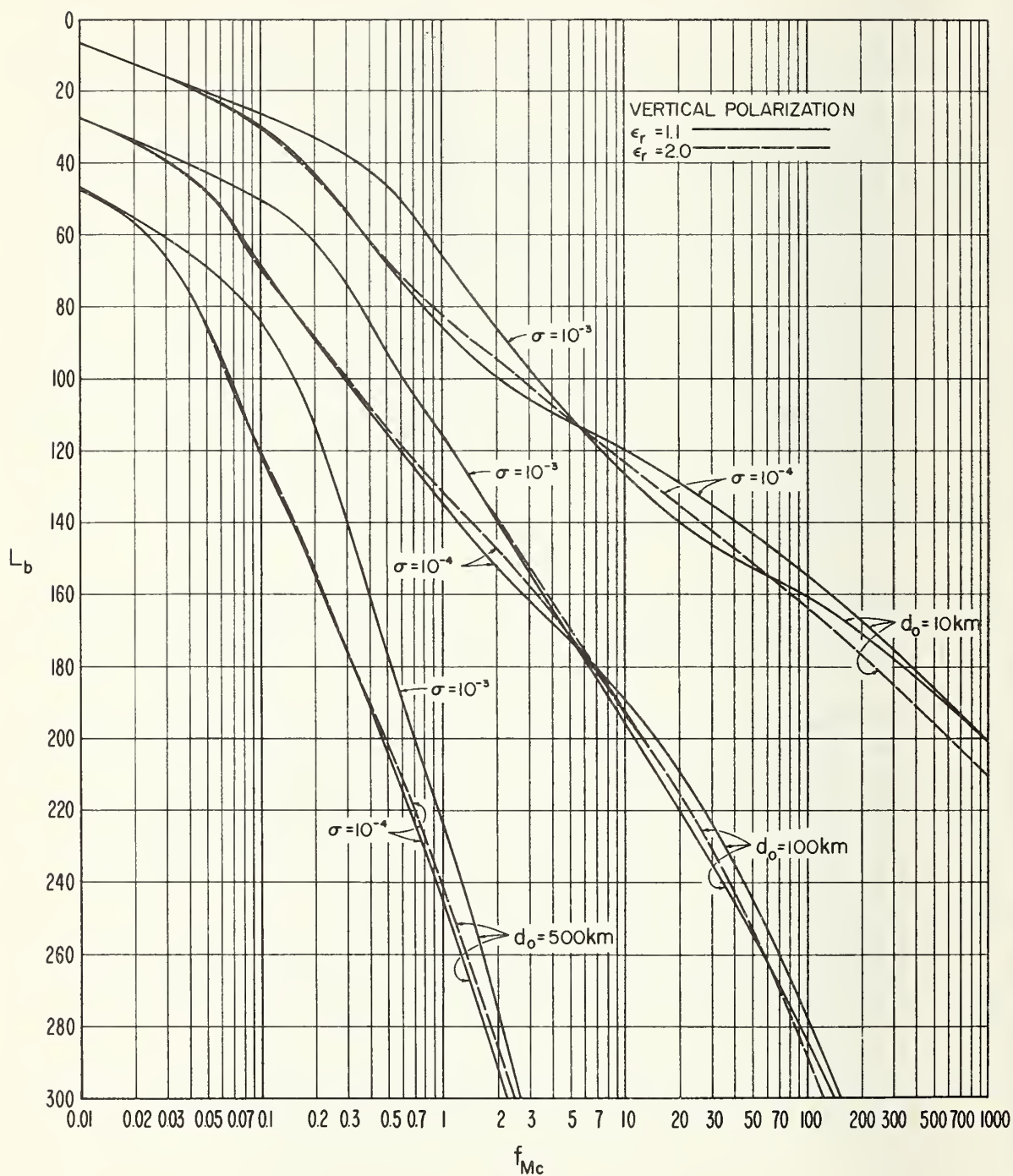


Figure 24.  $L_b$  for vertically polarized ground waves over homogeneous ground.

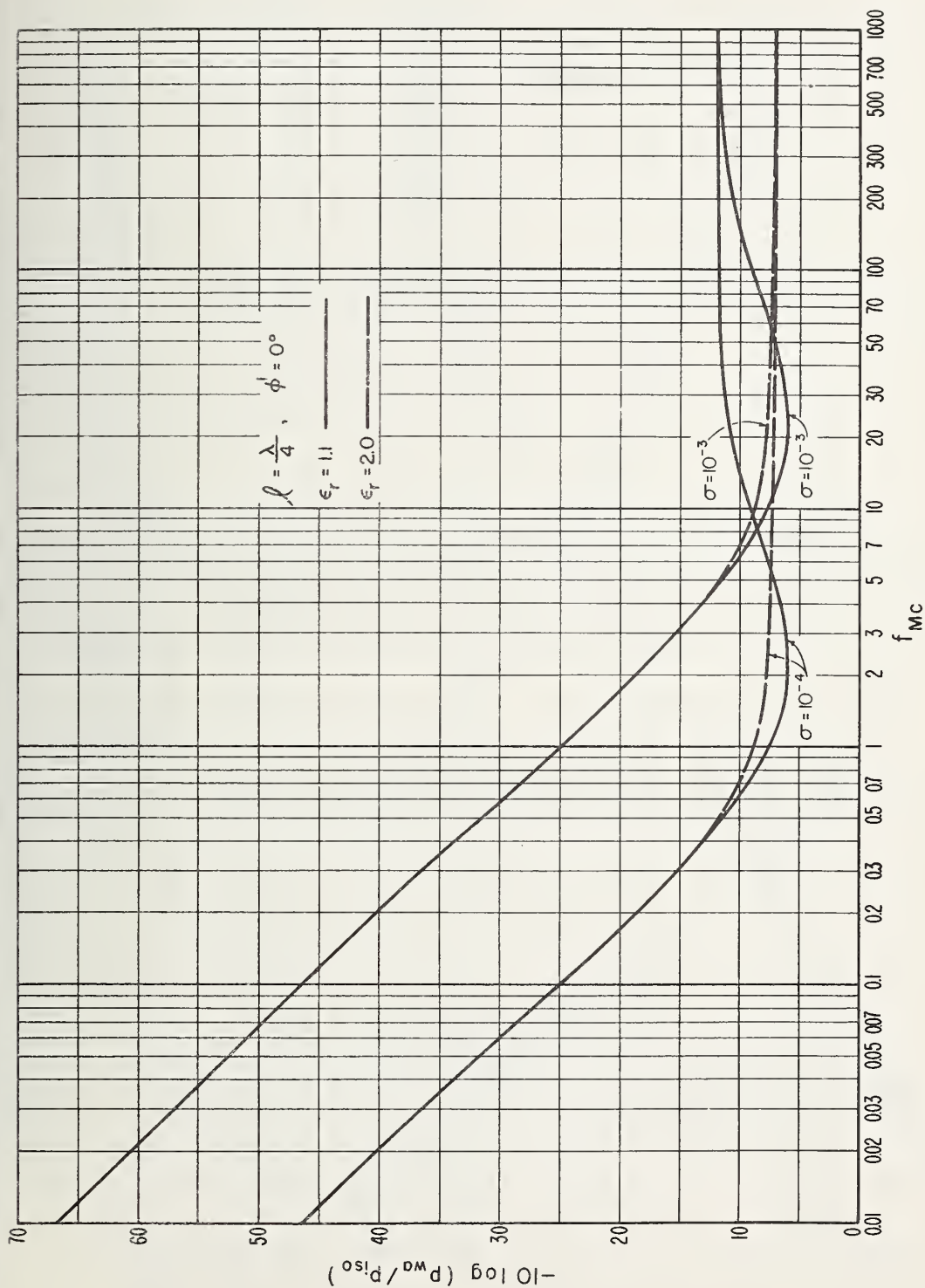


Figure 25. Estimates of  $L_t - G_t$  for a wave antenna of length  $l = \lambda/4$  lying on the ground.



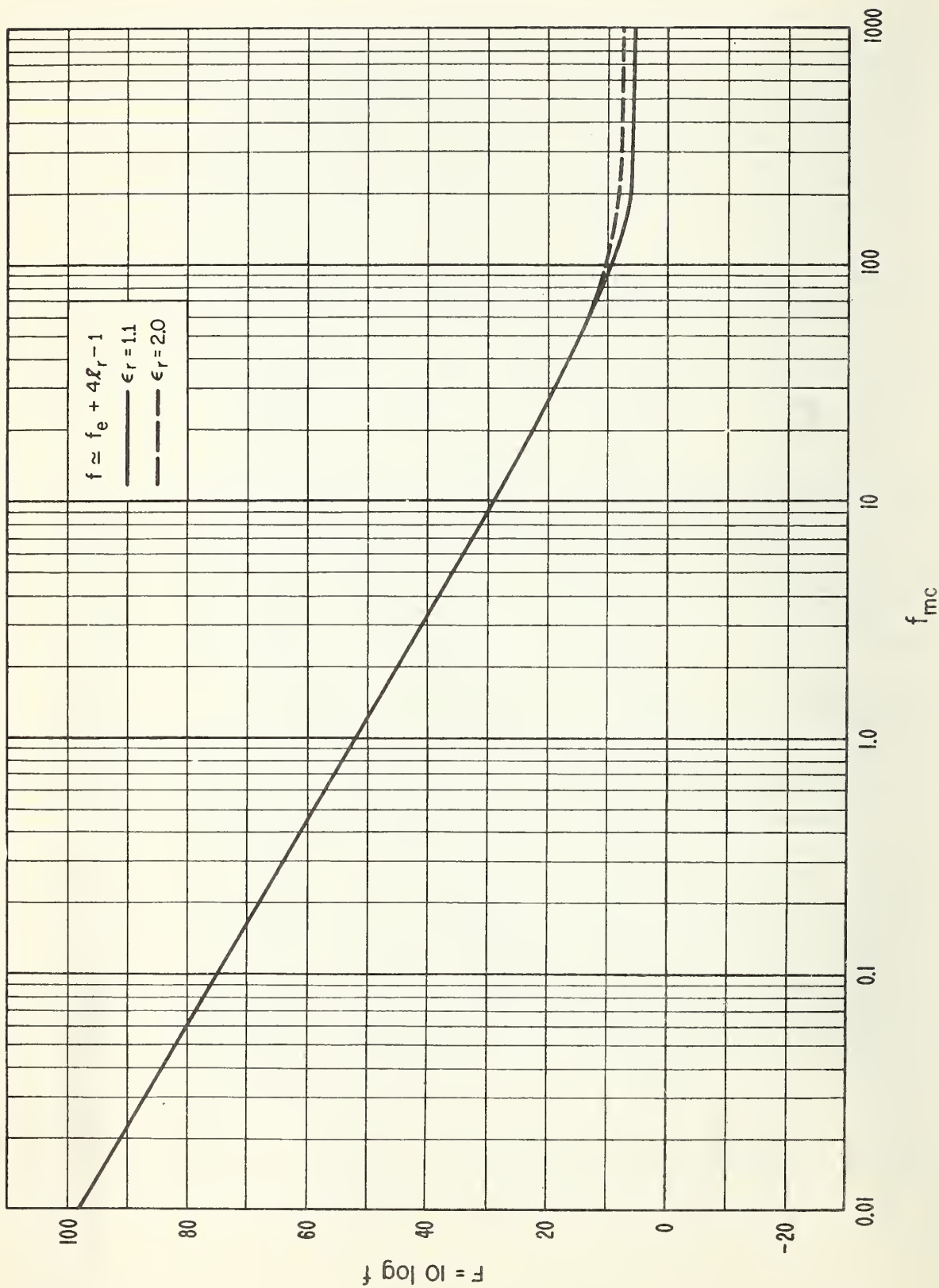


Figure 26. Operating noise factor  $F$  using (5.6) and assuming VED at a height  $h = \lambda/16$ .

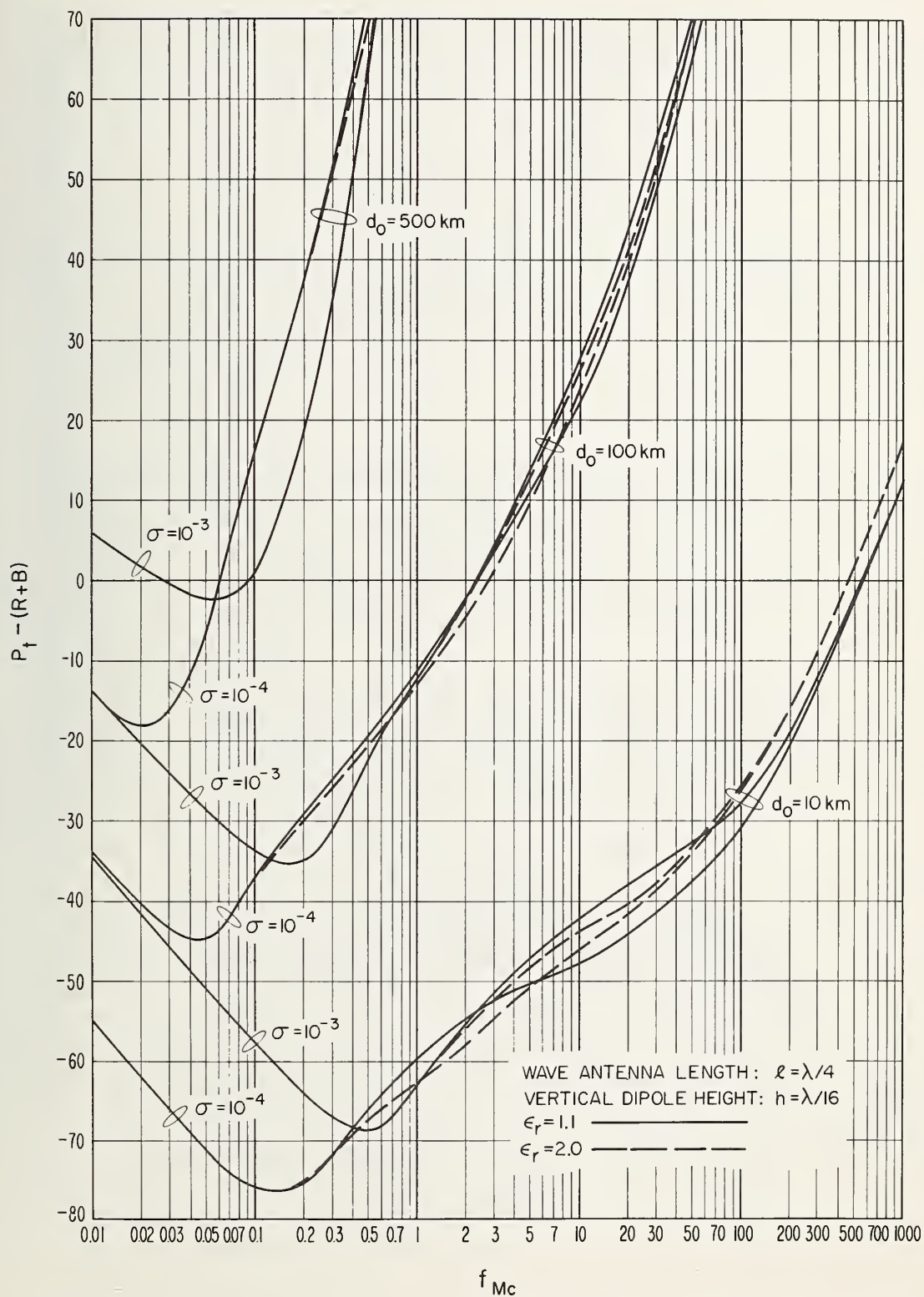


Figure 27.  $P_t - (R+B)$  for wave antenna and vertical dipole over homogeneous ground.

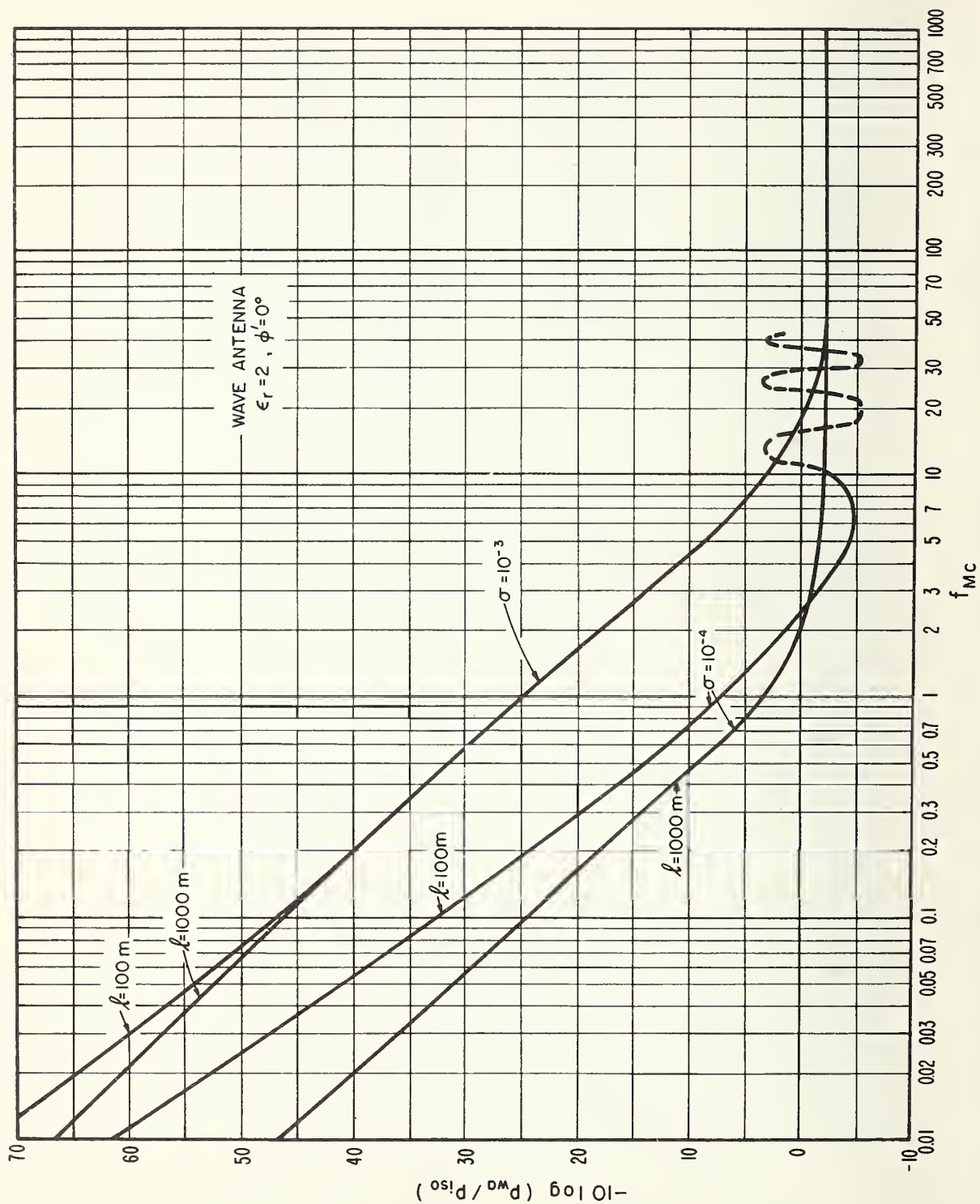


Figure 28. Estimates of  $L_t - G_t$  for a wave antenna of fixed lengths  $l = 100 \text{ m}$  and  $1000 \text{ m}$ .

shows a plot of the quantity  $L_t - G_t$  for fixed wave antenna lengths of  $l = 100$  m and  $1000$  m and ground conductivities of  $\sigma = 10^{-3}$  and  $10^{-4}$  mhos/m with  $\epsilon_r = 2$ . It can be seen that, at the lower frequencies, the loss associated with the  $1000$  m antenna is about the same as that shown in figure 25; however, a higher loss occurs at the lower frequencies if the  $100$  m length wave antenna is used.

The ground proximity loss for a short vertical electric dipole at fixed heights  $h = 10$  m and  $100$  m is shown in figure 29 for the same ground constants assumed in figure 28. As before, the extrapolated values of the external noise factor of figure 18 will tend to override the dipole loss at the lower frequencies, but it should be emphasized that this loss will contribute significantly to the calculation of  $f$  at low frequencies if future measurements show  $f_e$  to be considerably lower than the extrapolated values assumed here.

Using figures 24, 26, and 28, the quantity  $P_t - (R+B)$  is shown in figure 30 for the case of a wave antenna of length  $l = 100$  m transmitting in the optimum direction towards a short vertical electric dipole at a height  $h = 10$  m. For the example of standard broadcast service used previously, the required power  $P_t$  at a range of  $10$  km and for a frequency of  $300$  kc/s would be about  $12$  db or  $16$  w. For the low-grade voice communication service the required power at a distance of  $100$  km and for a frequency of  $100$  kc/s would be about  $30$  w. At high frequencies the estimates of  $P_t$  shown in figure 30 will be somewhat pessimistic, since a small height gain effect will occur due to the height of the dipole. Graphs for calculating this effect may be obtained from another paper [Vogler, 1964].

The combination of a wave antenna and dipole and the particular lengths and heights used in the preceding example were arbitrarily chosen. As pointed out in section 1, the purpose of the communication system together with the necessary restrictions placed on its physical components must first be established before specific power requirements may be estimated. Combinations of antennas other than the one assumed in the present example should be investigated before a decision is made as to what will constitute an efficient lunar communication system.

In the particular idealized system described by figures 27 and 30, a number of points should be noted: (1) the required power does not vary appreciably over the range of  $\epsilon_r$  assumed, but does depend significantly on the conductivity at low frequencies; (2) propagation out to somewhat beyond  $100$  km is practical for most types of systems and service, at least at MF or below; (3) the curves indicate an optimum frequency exists, depending on the conductivity of the lunar surface and the range of propagation; for the model assumed and for the conductivities and distances shown, the optimum frequency lies in the LF band. It should be kept in mind that the operating noise factor of the receiving system was considered to be a function only of the galactic noise (which, of course, is extrapolated at the lower frequencies) and a rather low receiver noise factor. If the receiving antenna loss  $l_c$  were large enough, it is apparent from (5.3) that  $F$  would have higher values than those assumed. Also, during the lunar day, the antenna temperature  $t_c$  would increase, thus making the operating noise factor even higher.



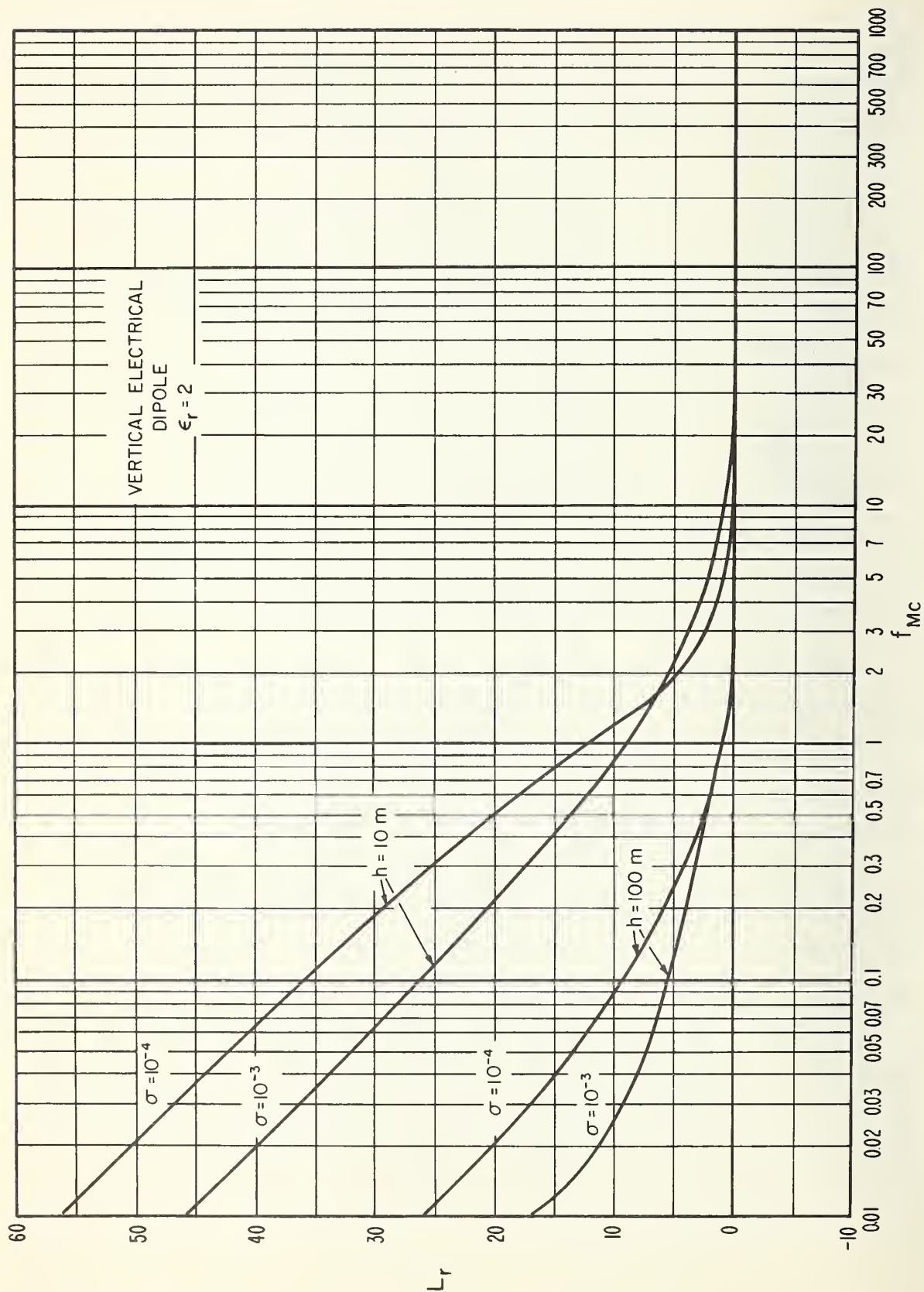


Figure 29. Ground proximity loss  $L_r$  for a short vertical electric dipole at fixed heights  $h = 10 \text{ m}$  and  $100 \text{ m}$ .



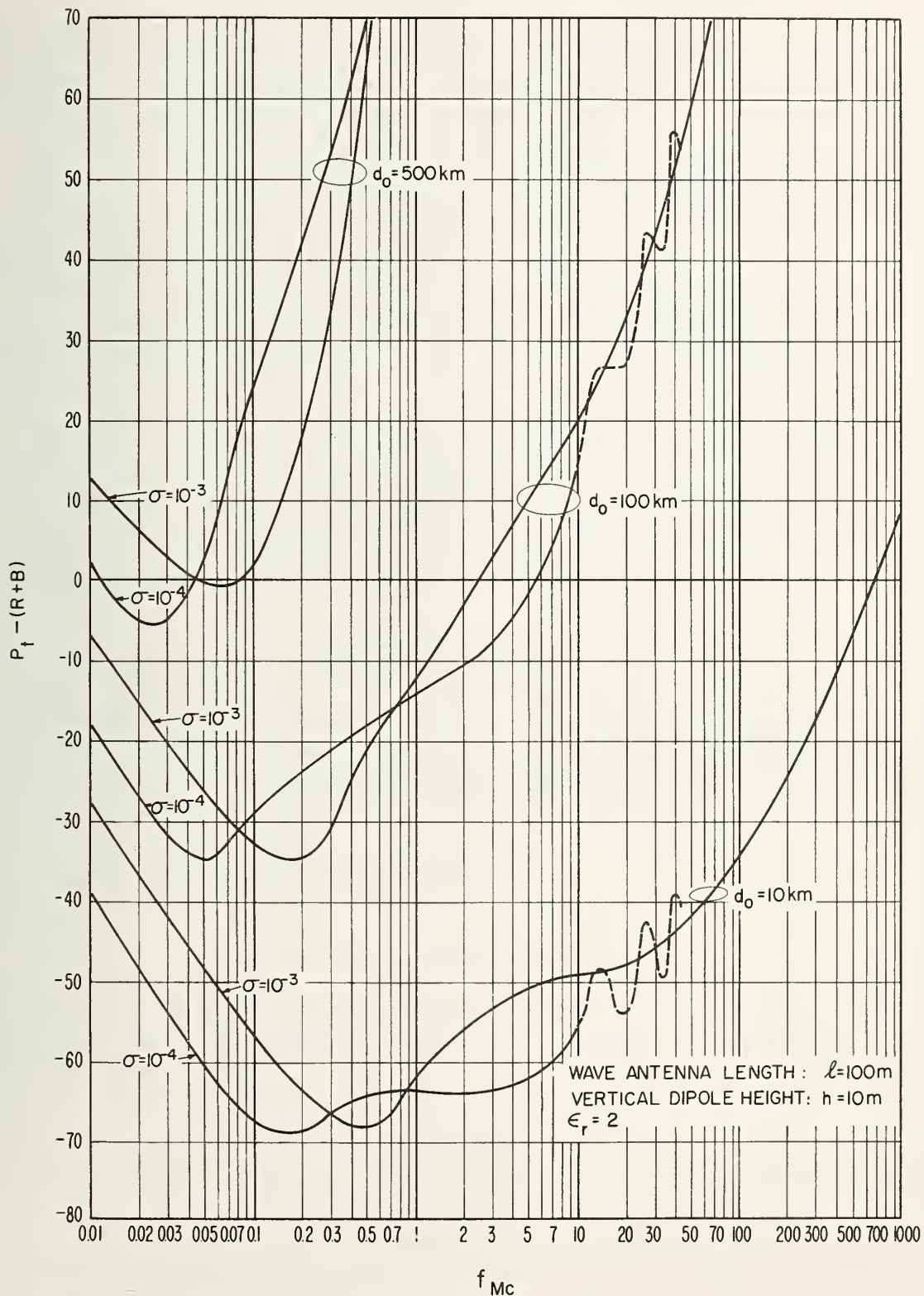


Figure 30.  $P_t - (R+B)$  for fixed length wave antenna and fixed height VED over homogeneous ground.

## 8. CONCLUSIONS

A study has been presented concerning various aspects of lunar surface communication; it is hoped that these results may serve as a basis for future investigations of the subject. An attempt has been made to present the main curves in a generalized form such that, as changes and refinements in our knowledge of the moon arise, the curves may still be useful in predicting lunar communication requirements.

It is apparent that further studies, both theoretical and experimental, would be useful in the following areas:

1. A more precise evaluation of lunar ground conductivity, together with more information concerning layering (if any) of the materials composing the moon.
2. Further investigation into the structure and magnitude of possible lunar ionospheres, especially the determination as to whether an ionized layer exists at the surface, and if so, its effects on propagation at the lower frequencies.
3. Further studies of noise effects including terrestrial noise sources, noise during high solar activity, and low frequency galactic noise.
4. Investigations of various antenna combinations, taking into account antenna ground losses for those situations in which a ground screen will be impractical.
5. A study of knife-edge diffraction and obstacle gain effects caused by irregularities in the moon's surface structure.

## 9. ACKNOWLEDGMENTS

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## 10. APPENDIX: INPUT IMPEDANCE OF DIPOLE ANTENNAS

It is assumed that an elementary dipole of length  $dl$  is located at the origin of a cylindrical coordinate system  $(\rho, \theta, z)$  at a height  $h$  above an isotropic and homogeneous conducting half-space characterized by a dielectric constant  $\epsilon_1$  and conductivity  $\sigma_1$ . The interface between the two media is the plane  $z = -h$ , and for  $z > -h$  the dielectric constant is assumed to be equal to the free space value  $\epsilon_0$ . The magnetic permeability of the whole space is taken as the free space value  $\mu_0$  (MKS units are used here). In the case of a vertical dipole, the antenna is oriented in the  $z$  direction, whereas for a horizontal dipole the orientation is in the  $\theta = 0$  direction. The elementary magnetic dipole may be considered equivalent to a small circular loop with its axis in the direction of the dipole and with an area  $dA = dl/\beta_0$ , where  $\beta_0$  is the free space wave number ( $= 2\pi/\lambda$ ). For practical short dipoles having a linear distribution of current,  $dl$  should be replaced by an effective length  $l_e = dl/2$ .

The electromagnetic field of an elementary dipole above a conducting plane may be obtained from the electric and magnetic Hertzian potentials,  $\vec{\Pi}_e$  and  $\vec{\Pi}_m$ , the components of which, if the vectors are referred to a cartesian coordinate system  $(x, y, z)$ , satisfy the scalar wave equation  $(\nabla^2 + \beta^2)\Pi = 0$ . Using the cylindrical coordinate form of the wave equation, particular solutions are found by the method of separation of variables resulting in expressions for the  $\Pi$  components involving combinations of the eigenfunction

$$\cos n\theta J_n(\lambda\rho) C(\lambda, \beta) \exp \left\{ \pm \sqrt{\lambda^2 - \beta^2} z \right\}, \quad (\text{A-1})$$

where  $\lambda$  denotes the eigenvalue (following Sommerfeld's notation),  $J_n$  is a Bessel function of the first kind and order  $n$ , and the  $C$ 's are functions determined from the boundary conditions. These conditions in the present instance require that the tangential components of the electric vector  $\vec{E}$  and the magnetic vector  $\vec{B}$  be continuous at the interface between the two media (air and ground).

In the case of vertical dipoles,  $\vec{E}$  and  $\vec{B}$  may be expressed in terms of Hertzian potentials having a  $z$ -component only. Thus in the upper medium

$$\vec{\Pi}_{\text{vert}} = \Pi_z \vec{z} = \left( \Pi_z^d + \Pi_z^r \right) \vec{z}, \quad (\text{A-2})$$

where the superscripts  $d$  and  $r$  refer to the direct or primary stimulation and the reflected or secondary stimulation, respectively. After solving for the coefficients  $C$  through the boundary conditions, one finds that for

$$\begin{aligned} \text{VED: } \Pi_{ez}^d &= \frac{iK_e}{\beta_0} \int_0^\infty J_0(\lambda\rho) e^{-z u_0(\lambda/u_0)} d\lambda, \\ \Pi_{ez}^r &= \frac{iK_e}{\beta_0} \int_0^\infty J_0(\lambda\rho) \left\{ \frac{N^2 u_0^2 - u_1^2}{N^2 u_0^2 + u_1^2} \right\} e^{-(z+2h)u_0(\lambda/u_0)} d\lambda, \end{aligned} \quad (\text{A-3})$$

$$\text{VMD: } \Pi_{mz}^d = \frac{iK_m}{\beta_o} \int_0^\infty J_o(\lambda\rho) e^{-zu_o} (\lambda/u_o) d\lambda, \quad (\text{A-4})$$

$$\Pi_{mz}^r = \frac{iK_m}{\beta_o} \int_0^\infty J_o(\lambda\rho) \left\{ \frac{u_o - u_1}{u_o + u_1} \right\} e^{-(z+2h)u_o} (\lambda/u_o) d\lambda,$$

where

$$u_o = \sqrt{\lambda^2 - \beta_o^2}, \quad u_1 = \sqrt{\lambda^2 - \beta_1^2}, \quad N^2 = (\epsilon_1/\epsilon_o) - i(\sigma_1/\omega\epsilon_o). \quad (\text{A-5})$$

$\beta_o$  and  $\beta_1$  are propagation constants of the upper and lower media, respectively, and the K's are amplitude factors given by

$$K_e = \frac{\beta_o I_o(d\ell)}{4\pi\omega\epsilon_o}, \quad K_m = \frac{\beta_o \mu_o I_o(dA)}{4\pi}. \quad (\text{A-6})$$

For horizontal dipoles, the Hertzian potentials require both an x- and a z-component. Thus, corresponding to (A-2),

$$\vec{\Pi}_{\text{hor}} = \Pi_x \vec{x} + \Pi_z \vec{z} = (\Pi_x^d + \Pi_x^r) \vec{x} + \Pi_z \vec{z}. \quad (\text{A-7})$$

After solving for the C's through the boundary conditions, one obtains:

$$\left. \begin{aligned} \text{HED: } \Pi_{ex}^d &= \frac{iK_e}{\beta_o} \int_0^\infty J_o(\lambda\rho) e^{-zu_o} (\lambda/u_o) d\lambda, \\ \Pi_{ex}^r &= \frac{iK_e}{\beta_o} \int_0^\infty J_o(\lambda\rho) \left\{ \frac{u_o - u_1}{u_o + u_1} \right\} e^{-(z+2h)u_o} (\lambda/u_o) d\lambda, \\ \Pi_{ez} &= -\frac{iK_e \cos \theta}{\beta_o} \int_0^\infty J_1(\lambda\rho) \left\{ \frac{2(u_o - u_1)}{N^2 u_o + u_1} \right\} e^{-(z+2h)u_o} (\lambda^2/\beta_o^2) d\lambda, \end{aligned} \right\} \quad (\text{A-8})$$

$$\left. \begin{aligned} \text{HMD: } \Pi_{mx}^d &= \frac{iK_m}{\beta_o} \int_0^\infty J_o(\lambda\rho) e^{-zu_o} (\lambda/u_o) d\lambda, \\ \Pi_{mx}^r &= \frac{iK_m}{\beta_o} \int_0^\infty J_o(\lambda\rho) \left\{ \frac{N^2 u_o - u_1}{N^2 u_o + u_1} \right\} e^{-(z+2h)u_o} (\lambda/u_o) d\lambda, \\ \Pi_{mz} &= -\frac{iK_m \cos \theta}{\beta_o} \int_0^\infty J_1(\lambda\rho) \left\{ \frac{2(u_o - u_1)}{N^2 u_o + u_1} \right\} e^{-(z+2h)u_o} (\lambda^2/\beta_o^2) d\lambda, \end{aligned} \right\} \quad (\text{A-9})$$

where  $u_o$ ,  $u_1$ ,  $N^2$ ,  $K_e$ , and  $K_m$  are defined in (A-5) and (A-6).

With the Hertz vector  $\vec{\Pi}$  determined, the electromagnetic field in the upper medium is derived through the following relationships:

$$\vec{E} = \text{grad div } \vec{\Pi}_e + \beta_o^2 \vec{\Pi}_e, \quad (\text{electric dipoles}) \quad (\text{A-10a})$$

$$\vec{B} = \text{grad div } \vec{\Pi}_m + \beta_o^2 \vec{\Pi}_m. \quad (\text{magnetic dipoles}) \quad (\text{A-10b})$$

The components (in cylindrical coordinates) of interest in this paper are found to be

$$\begin{aligned} \text{VED: } E_z(\rho, z) &= \left( \partial^2 / \partial z^2 + \beta_o^2 \right) \Pi_{ez} = \left( \partial^2 / \partial z^2 + \beta_o^2 \right) \left( \Pi_{ez}^d + \Pi_{ez}^r \right) \\ &= \frac{iK_e}{\beta_o} \int_0^\infty J_o(\lambda\rho) \left[ e^{-z u_o} + \left\{ \frac{N^2 u_o - u_1}{N^2 u_o + u_1} \right\} e^{-(z+2h) u_o} \right] (\lambda^3 / u_o) d\lambda, \end{aligned} \quad (\text{A-11a})$$

$$\begin{aligned} \text{HED: } E_\rho(\rho, z) &= (\partial / \partial \rho) \text{div } \vec{\Pi}_e + \beta_o^2 \cos \theta \Pi_{ex} \\ &= \frac{iK_e \cos \theta}{\beta_o} \int_0^\infty \left[ \left( \beta_o^2 J_o(\lambda\rho) - \lambda^2 \left\{ J_o(\lambda\rho) - \frac{J_1(\lambda\rho)}{\lambda\rho} \right\} \right) e^{-z u_o} \right. \\ &\quad + \left( \beta_o^2 J_o(\lambda\rho) - \lambda^2 \left\{ J_o(\lambda\rho) - \frac{J_1(\lambda\rho)}{\lambda\rho} \right\} \right) \left\{ \frac{u_o - u_1}{u_o + u_1} \right\} e^{-(z+2h) u_o} \\ &\quad \left. + \left( J_o(\lambda\rho) - \frac{J_1(\lambda\rho)}{\lambda\rho} \right) \left\{ \frac{2\lambda^2 u_o^2 (u_o - u_1)}{\beta_o^2 (N^2 u_o + u_1)} \right\} e^{-(z+2h) u_o} \right] (\lambda / u_o) d\lambda, \end{aligned} \quad (\text{A-11b})$$

$$\begin{aligned} \text{VMD: } B_z(\rho, z) &= \left( \partial^2 / \partial z^2 + \beta_o^2 \right) \Pi_{mz} = \left( \partial^2 / \partial z^2 + \beta_o^2 \right) \left( \Pi_{mz}^d + \Pi_{mz}^r \right) \\ &= \frac{iK_m}{\beta_o} \int_0^\infty J_o(\lambda\rho) \left[ e^{-z u_o} + \left\{ \frac{u_o - u_1}{u_o + u_1} \right\} e^{-(z+2h) u_o} \right] (\lambda^3 / u_o) d\lambda, \end{aligned} \quad (\text{A-11c})$$

$$\begin{aligned} \text{HMD: } B_\rho(\rho, z) &= (\partial / \partial \rho) \text{div } \vec{\Pi}_m + \beta_o^2 \cos \theta \Pi_{mx} \\ &= \frac{iK_m \cos \theta}{\beta_o} \int_0^\infty \left[ \left( \beta_o^2 J_o(\lambda\rho) - \lambda^2 \left\{ J_o(\lambda\rho) - \frac{J_1(\lambda\rho)}{\lambda\rho} \right\} \right) e^{-z u_o} \right. \\ &\quad + \left( \beta_o^2 J_o(\lambda\rho) - \lambda^2 \left\{ J_o(\lambda\rho) - \frac{J_1(\lambda\rho)}{\lambda\rho} \right\} \right) \left\{ \frac{N^2 u_o - u_1}{N^2 u_o + u_1} \right\} e^{-(z+2h) u_o} \\ &\quad \left. + \left( J_o(\lambda\rho) - \frac{J_1(\lambda\rho)}{\lambda\rho} \right) \left\{ \frac{2\lambda^2 u_o^2 (u_o - u_1)}{\beta_o^2 (N^2 u_o + u_1)} \right\} e^{-(z+2h) u_o} \right] (\lambda / u_o) d\lambda. \end{aligned} \quad (\text{A-11d})$$



To calculate the dipole input impedance using the emf method [Wait, 1953, 1962d; King, 1956 (p. 258)] requires a knowledge of the axial field at the antenna. This may be obtained by taking the limits of (A-11) as  $\rho$  and  $z$  approach zero (and with  $\theta = 0$  in the case of horizontal dipoles). The impedance  $Z$  is then given by

$$\begin{aligned} \text{VED: } Z &= \lim_{\substack{\rho \rightarrow 0 \\ z \rightarrow 0}} \left\{ E_z(\rho, z) d\ell / I_o \right\} \\ &= \frac{i K_e d\ell}{\beta_o I_o} \int_0^\infty \left[ 1 + \left\{ \frac{N^2 u_o - u_1}{N^2 u_o + u_1} \right\} e^{-2h u_o} \right] (\lambda^3 / u_o) d\lambda, \end{aligned} \quad (\text{A-12a})$$

$$\begin{aligned} \text{HED: } Z &= \lim_{\substack{\rho \rightarrow 0 \\ z \rightarrow 0}} \left\{ E_\rho(\rho, z) d\ell / I_o \right\} \\ &= \frac{i K_e d\ell}{\beta_o I_o} \int_0^\infty \left[ \left( \beta_o^2 - \lambda^2 / z \right) \left( 1 + \left\{ \frac{u_o - u_1}{u_o + u_1} \right\} e^{-2h u_o} \right) \right. \\ &\quad \left. + \left\{ \frac{\lambda^2 u_o^2 (u_o - u_1)}{\beta_o^2 (N^2 u_o + u_1)} \right\} e^{-2h u_o} \right] (\lambda / u_o) d\lambda, \end{aligned} \quad (\text{A-12b})$$

$$\begin{aligned} \text{VMD: } Z &= \lim_{\substack{\rho \rightarrow 0 \\ z \rightarrow 0}} \left\{ \omega B_z(\rho, z) dA / I_o \right\} \\ &= \frac{i \omega K_m dA}{\beta_o I_o} \int_0^\infty \left[ 1 + \left\{ \frac{u_o - u_1}{u_o + u_1} \right\} e^{-2h u_o} \right] (\lambda^3 / u_o) d\lambda, \end{aligned} \quad (\text{A-12c})$$

$$\begin{aligned} \text{HMD: } Z &= \lim_{\substack{\rho \rightarrow 0 \\ z \rightarrow 0}} \left\{ \omega B_\rho(\rho, z) dA / I_o \right\} \\ &= \frac{i \omega K_m dA}{\beta_o I_o} \int_0^\infty \left[ \left( \beta_o^2 - \lambda^2 / z \right) \left( 1 + \left\{ \frac{N^2 u_o - u_1}{N^2 u_o + u_1} \right\} e^{-2h u_o} \right) \right. \\ &\quad \left. + \left\{ \frac{\lambda^2 u_o^2 (u_o - u_1)}{\beta_o^2 (N^2 u_o + u_1)} \right\} e^{-2h u_o} \right] (\lambda / u_o) d\lambda. \end{aligned} \quad (\text{A-12d})$$

Notice that the effect of the ground is contained in terms involving the factor  $\exp(-2hu_0)$ ; thus, the change in impedance  $\Delta Z$  due to the presence of the ground may be defined as

$$\Delta Z \equiv Z - \lim_{h \rightarrow \infty} Z = Z - Z_f \quad (\text{A-13})$$

and the free space antenna resistance  $r_f$  is obtained from the relationship:

$$r_f = \text{Re} \left\{ \lim_{h \rightarrow \infty} Z \right\}. \quad (\text{A-14})$$

With the use of (A-13) and (A-14), one can now derive the expressions for the normalized input impedance change  $\Delta Z/r_f$  given by equations (4.2) of section 4; here, the change of variable

$$x = 2hu_0 = 2h\sqrt{\lambda^2 - \beta_0^2}$$

has been made and the following relationships used:

$$(\lambda d \lambda / u_0) = (dx/2h), \quad \alpha = 2h\beta_0, \quad u_1 = \sqrt{x^2 - \alpha^2(N^2 - 1)}/2h, \quad \lambda^2 = (\alpha^2 + x^2)/(2h)^2. \quad (\text{A-15})$$

Limiting expressions of (4.2), derived from integrations by parts of the integrals involved, are given by the following equations. For  $\alpha N < 1$ :

$$\text{VED: } \Delta Z/R_f \simeq \frac{3(N+1)}{4} \left[ F_1(D) + \left( \frac{N+1}{2} \right)^2 F_2(D) \right] + i \left\{ \frac{3(1+A)D}{\alpha^3} \right\} e^{-A}, \quad (\text{A-16 a})$$

$$\text{HED: } \Delta Z/R_f \simeq \frac{3(N+1)}{8} \left[ F_1(0) + \left( \frac{N+1}{2} \right)^2 F_2(D) \right] + i \left\{ \frac{3(1+A)D}{2\alpha^3} \right\} e^{-A}, \quad (\text{A-16 b})$$

$$\text{VMD: } \Delta Z/R_f \simeq \frac{3(N+1)}{4} \left[ F_1(0) + \left( \frac{N+1}{2} \right)^2 F_2(0) \right] + i \left\{ \frac{3(N^2+1)D}{8\alpha} \right\} e^{-A}, \quad (\text{A-16 c})$$

$$\text{HMD: } \Delta Z/R_f \simeq \frac{3(N+1)}{8} \left[ F_1(D) + \left( \frac{N+1}{2} \right)^2 F_2(0) \right] + i \left\{ \frac{3(N^2+5)D}{16\alpha} \right\} e^{-A}, \quad (\text{A-16 d})$$

where

$$F_1(X) = X + \{1 - X(1+X)\}d + \frac{1}{3}(1+X)(1-X^2)d^2, \quad (\text{A-17})$$

$$F_2(X) = -\frac{X}{3} + \{1+X(1-X)\}d + \{1-X(1+X)(2-X)\}d^2 + \frac{1}{3}\{1+X(1-X)(2-X^2)\}d^3 - \frac{1}{5}(1-X)(1-X^2)d^4, \quad (\text{A-18})$$

$$d \equiv \frac{N-1}{N+1}, \quad D \equiv \frac{N^2-1}{N^2+1}, \quad A \equiv \alpha\sqrt{N^2-1}. \quad (\text{A-19})$$

For  $\alpha N \gg 1$ :

$$\text{VED: } \Delta Z/R_f \sim \frac{3}{\alpha^3} \left\{ \frac{N-1}{N+1} \right\} \left[ (1 + 4/N) + i \left\{ \alpha + \frac{6}{\alpha N} \left( 1 - \frac{2N-3}{N^2} \right) \right\} \right] i e^{-i\alpha}, \quad (\text{A-20 a})$$

$$\text{HED: } \Delta Z/R_f \sim \frac{3}{2\alpha^3} \left\{ \frac{N-1}{N+1} \right\} \left[ (1 - \alpha^2 + 2/N) + i \left\{ \alpha + \frac{6}{\alpha N} \left( 1 - \frac{2N-3}{N^2} \right) \right\} \right] i e^{-i\alpha}, \quad (\text{A-20 b})$$

$$\text{VMD: } \Delta Z/R_f \sim -\frac{3}{\alpha^3} \left\{ \frac{N-1}{N+1} \right\} \left[ (1 - 4/N) + i \left\{ \alpha + \frac{6}{\alpha N} \left( 1 - \frac{2N+1}{N^2} \right) \right\} \right] i e^{-i\alpha}, \quad (\text{A-20 c})$$

$$\text{HMD: } \Delta Z/R_f \sim -\frac{3}{2\alpha^3} \left\{ \frac{N-1}{N+1} \right\} \left[ (1 - \alpha^2 - 6/N) + i \left\{ \alpha + \frac{6}{\alpha N} \left( 1 - \frac{2N+1}{N^2} \right) \right\} \right] i e^{-i\alpha}. \quad (\text{A-20 d})$$

For the case of dipoles above a perfectly conducting plane ( $N \rightarrow \infty$ ), equations (A-20) reduce to the well-known expressions:

$$\text{VED: } \Delta Z/R_f \rightarrow \left( \frac{3}{\alpha} \right) \left[ \{ \sin \alpha - \alpha \cos \alpha \} + i \{ \cos \alpha + \alpha \sin \alpha \} \right], \quad (\text{A-21 a})$$

$$\text{HED: } \Delta Z/R_f \rightarrow \left( \frac{3}{2\alpha} \right) \left[ \{ (1 - \alpha^2) \sin \alpha - \alpha \cos \alpha \} + i \{ (1 - \alpha^2) \cos \alpha + \alpha \sin \alpha \} \right], \quad (\text{A-21 b})$$

$$\text{VMD: } \Delta Z/R_f \rightarrow -\left( \frac{3}{\alpha} \right) \left[ \{ \sin \alpha - \alpha \cos \alpha \} + i \{ \cos \alpha + \alpha \sin \alpha \} \right], \quad (\text{A-21 c})$$

$$\text{HMD: } \Delta Z/R_f \rightarrow -\left( \frac{3}{2\alpha} \right) \left[ \{ (1 - \alpha^2) \sin \alpha - \alpha \cos \alpha \} + i \{ (1 - \alpha^2) \cos \alpha + \alpha \sin \alpha \} \right]. \quad (\text{A-21 d})$$

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12. GRAPHS OF GROUND PROXIMITY LOSS,  $L_{t,r} = 10 \log \{r/r_f\}$

for

Vertical Electric Dipoles (VED)

Horizontal Electric Dipoles (HED)

Vertical Magnetic Dipoles (VMD)

Horizontal Magnetic Dipoles (HMD)

$$s = 60 \lambda \sigma \text{ (mhos/m)}, \quad \alpha = (2h)(2\pi/\lambda),$$

$\epsilon_r$ : relative dielectric constant of ground

$\sigma$  (mhos/m): conductivity of ground

$h$ : height in meters of antenna above ground

$\lambda$ : wavelength in meters

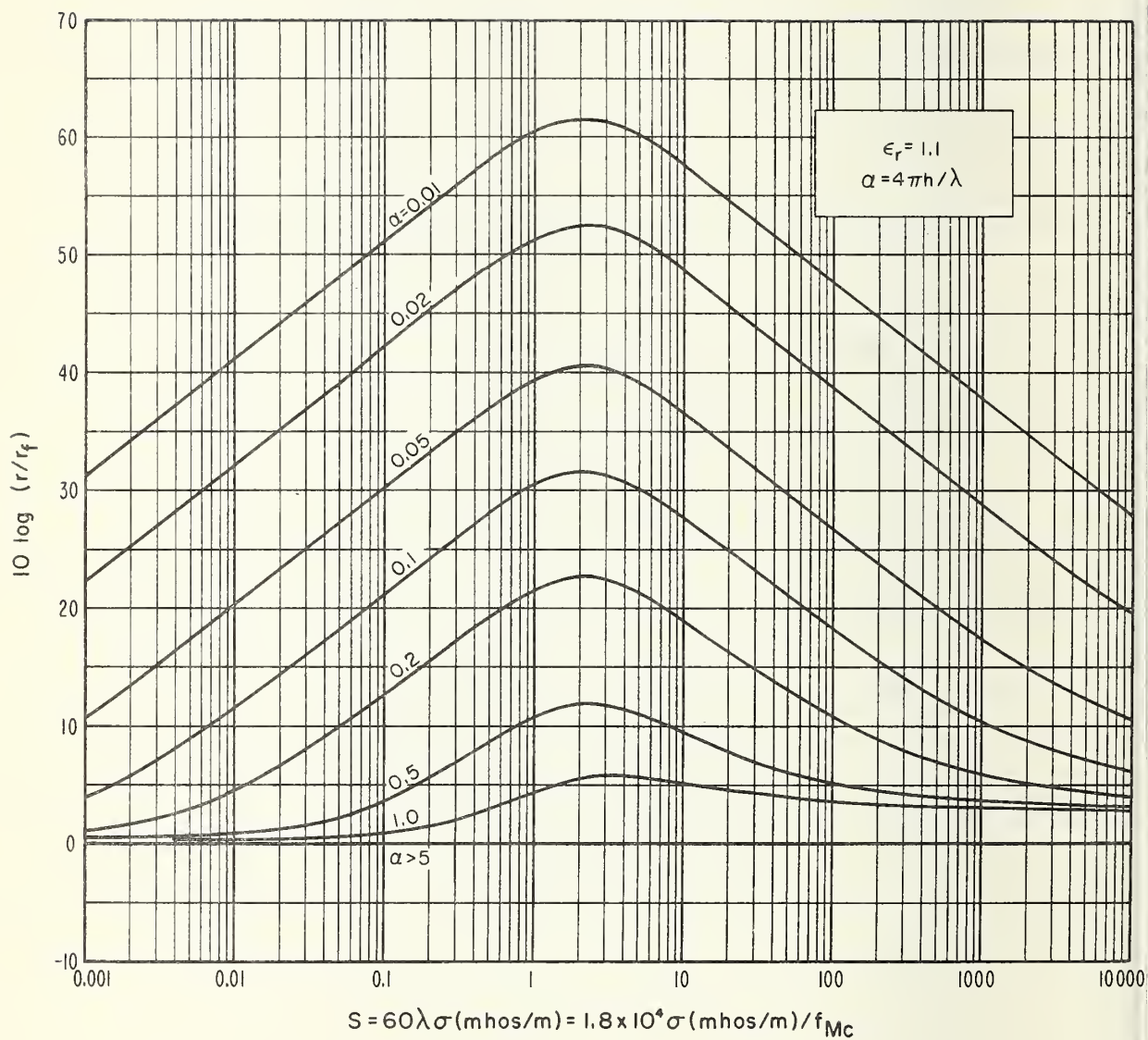


Figure A-1. Ground proximity loss  $L_{t,r}$  for VED,  $\epsilon_r = 1.1$ .

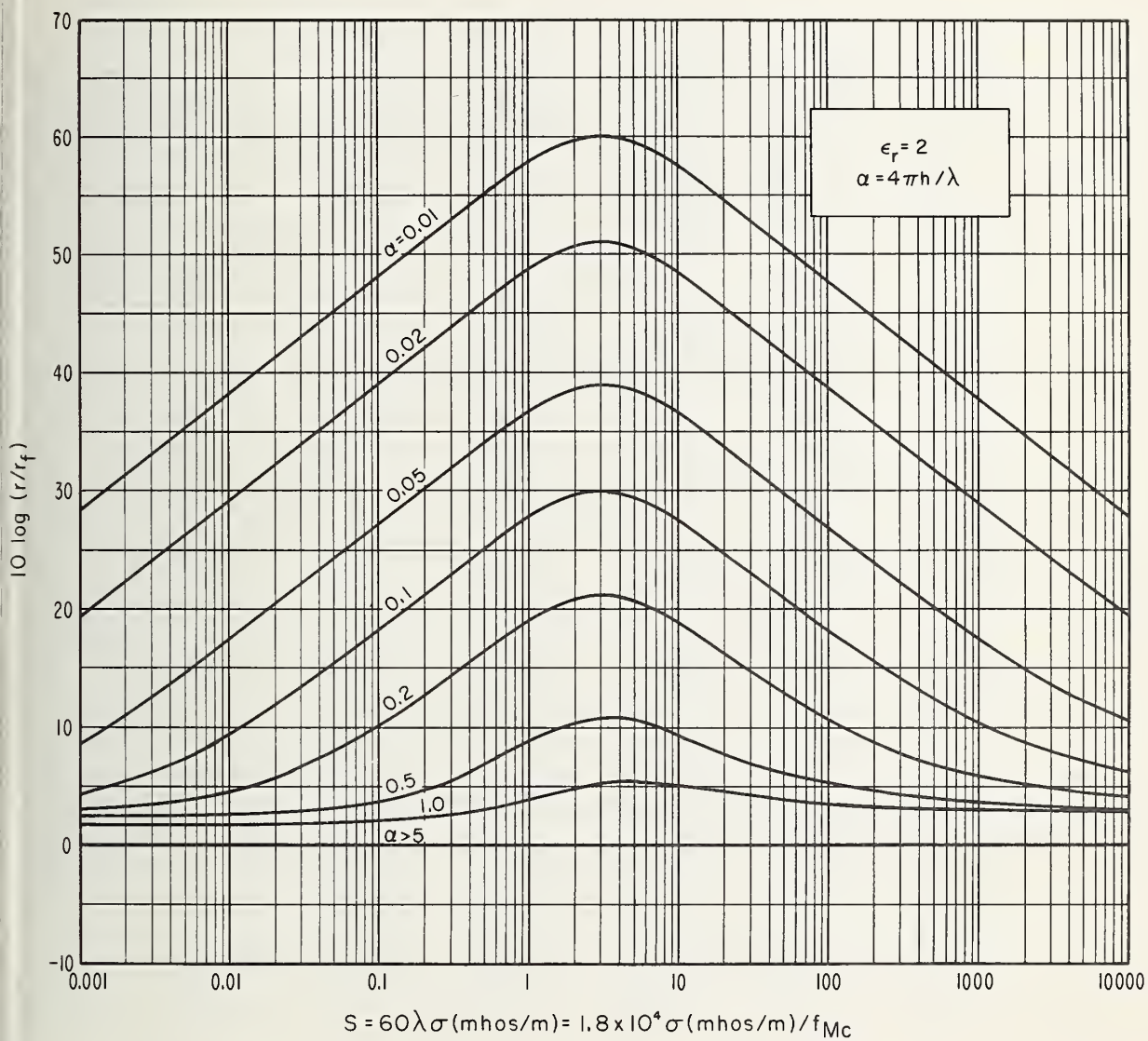


Figure A-2. Ground proximity loss  $L_{t,r}$  for VED,  $\epsilon_r = 2$ .

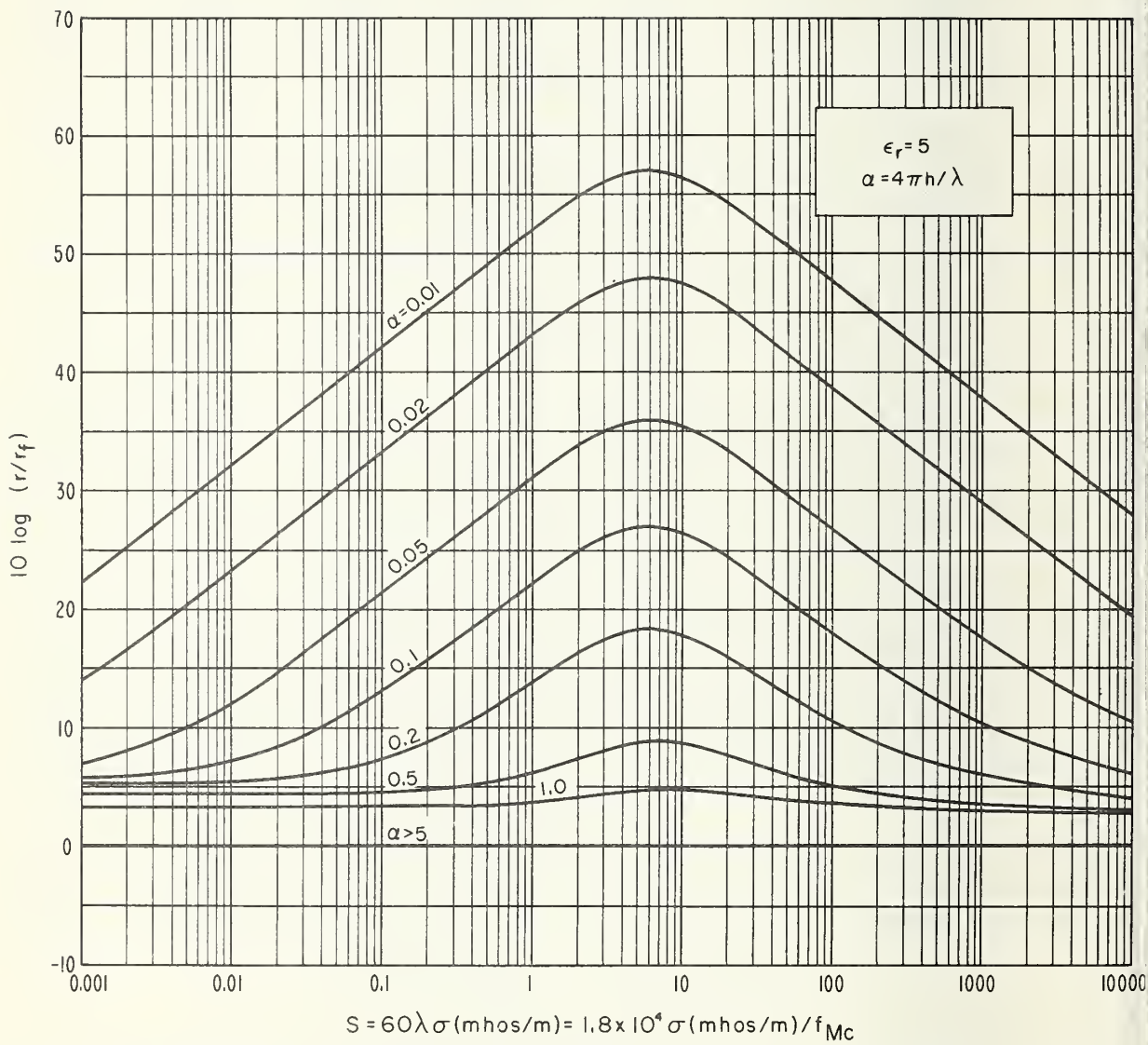


Figure A-3. Ground proximity loss  $L_{t,r}$  for VED,  $\epsilon_r = 5$ .

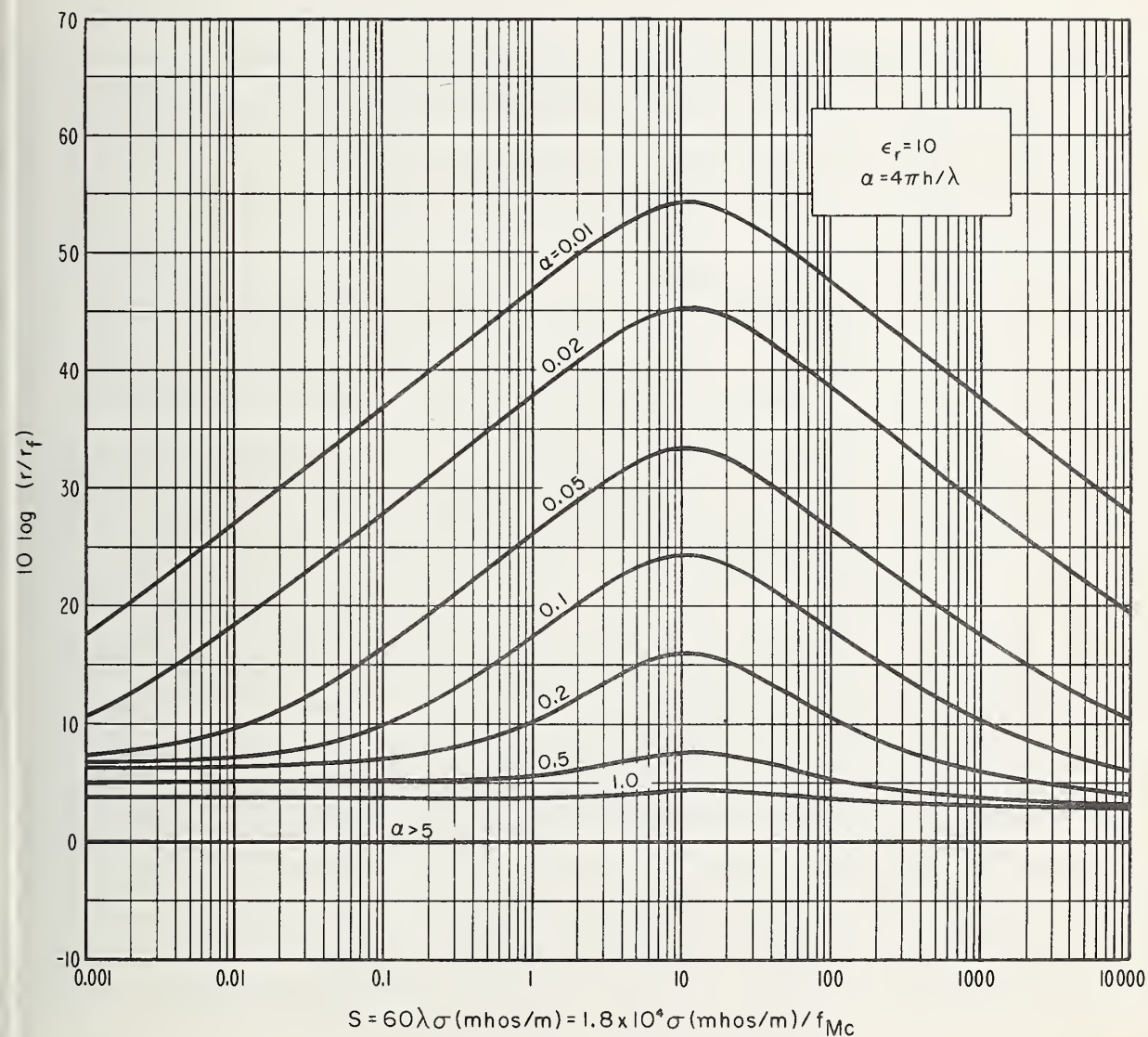


Figure A-4. Ground proximity loss  $L_{t,r}$  for VED,  $\epsilon_r = 10$ .



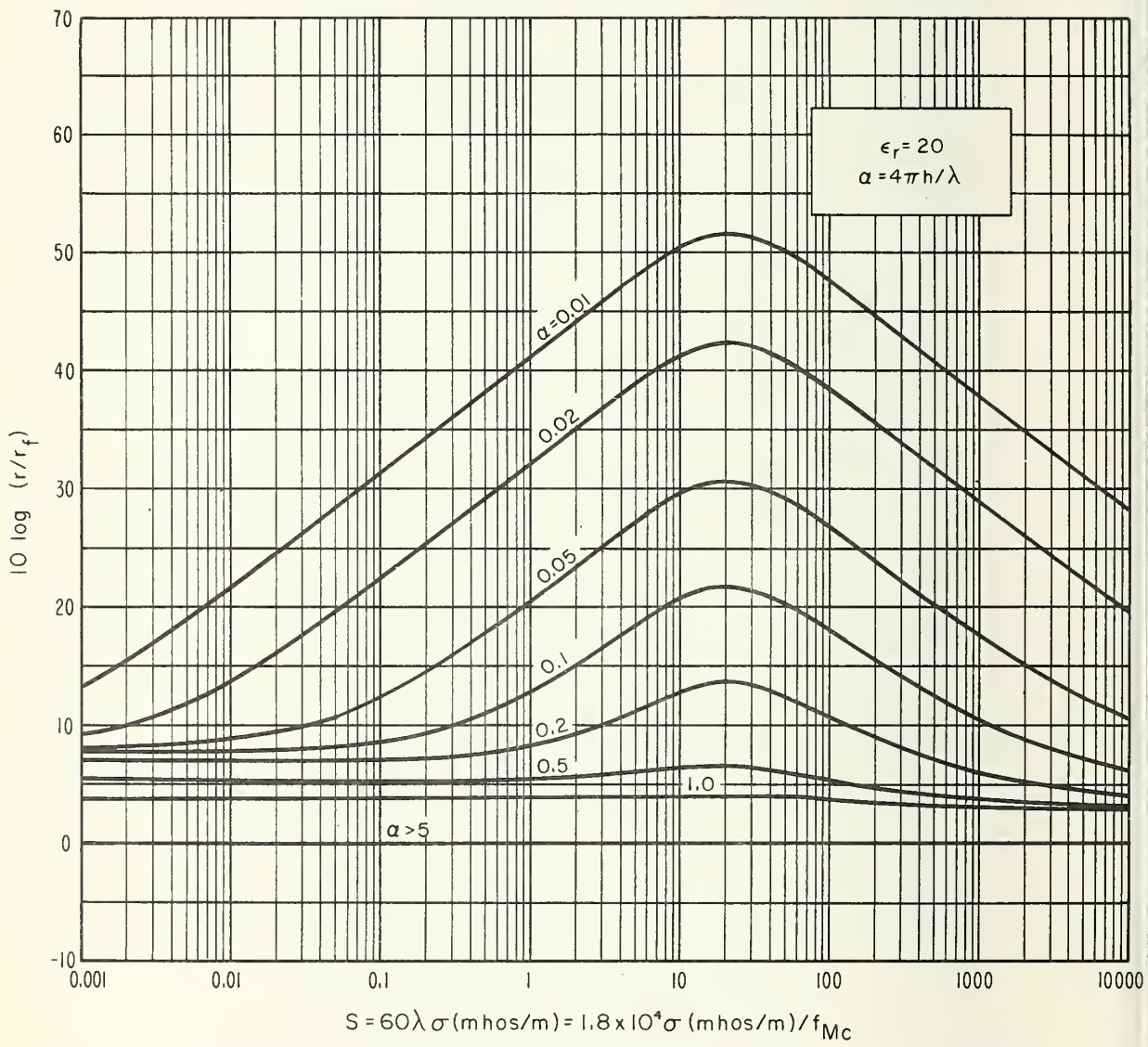


Figure A-5. Ground proximity loss  $L_{t,r}$  for VED,  $\epsilon_r = 20$ .

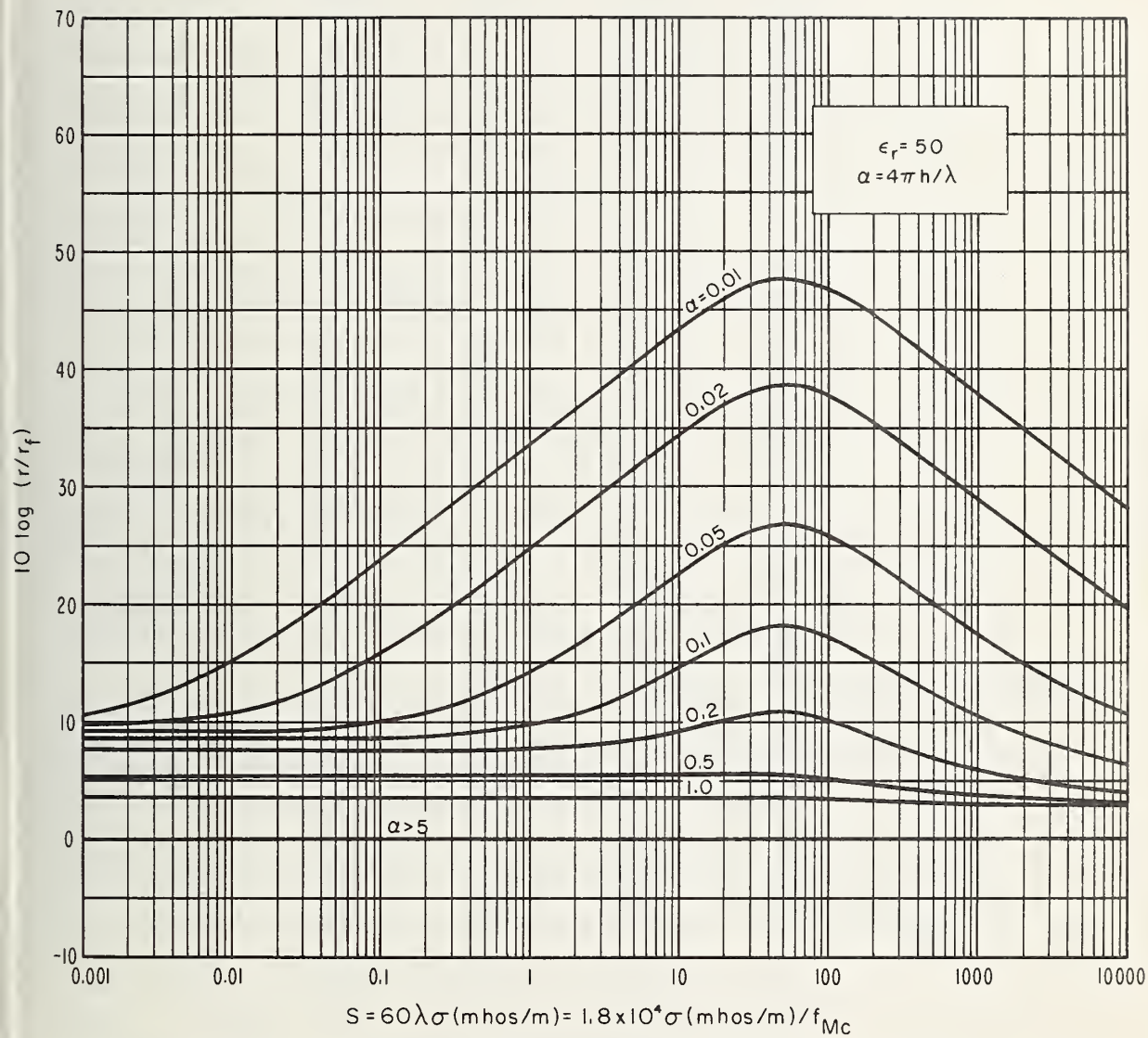


Figure A-6. Ground proximity loss  $L_{t,r}$  for VED,  $\epsilon_r = 50$ .

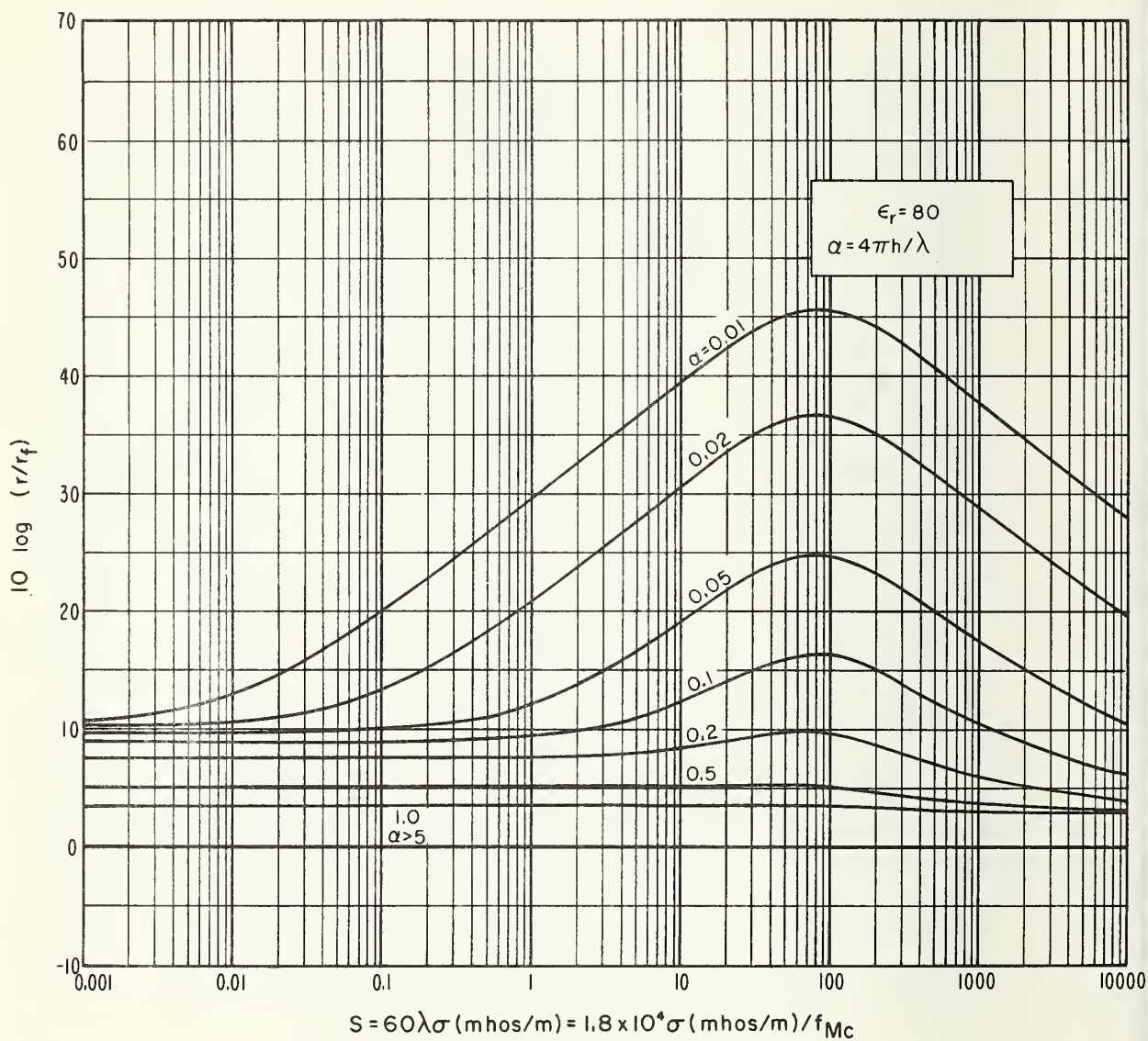


Figure A-7. Ground proximity loss  $L_{t,r}$  for VED,  $\epsilon_r = 80$ .

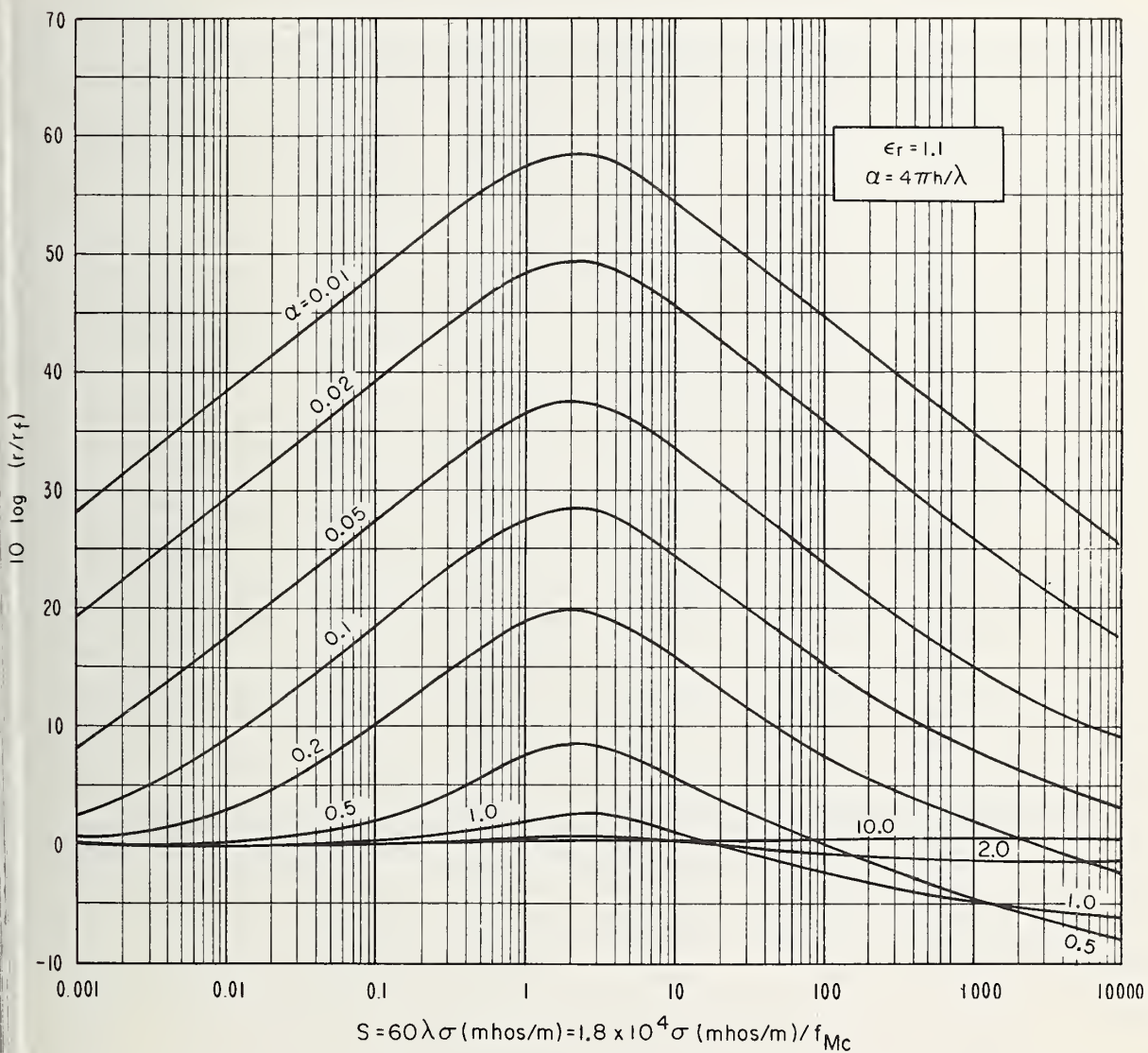


Figure A-8. Ground proximity loss  $L_{t,r}$  for HED,  $\epsilon_r = 1.1$ .



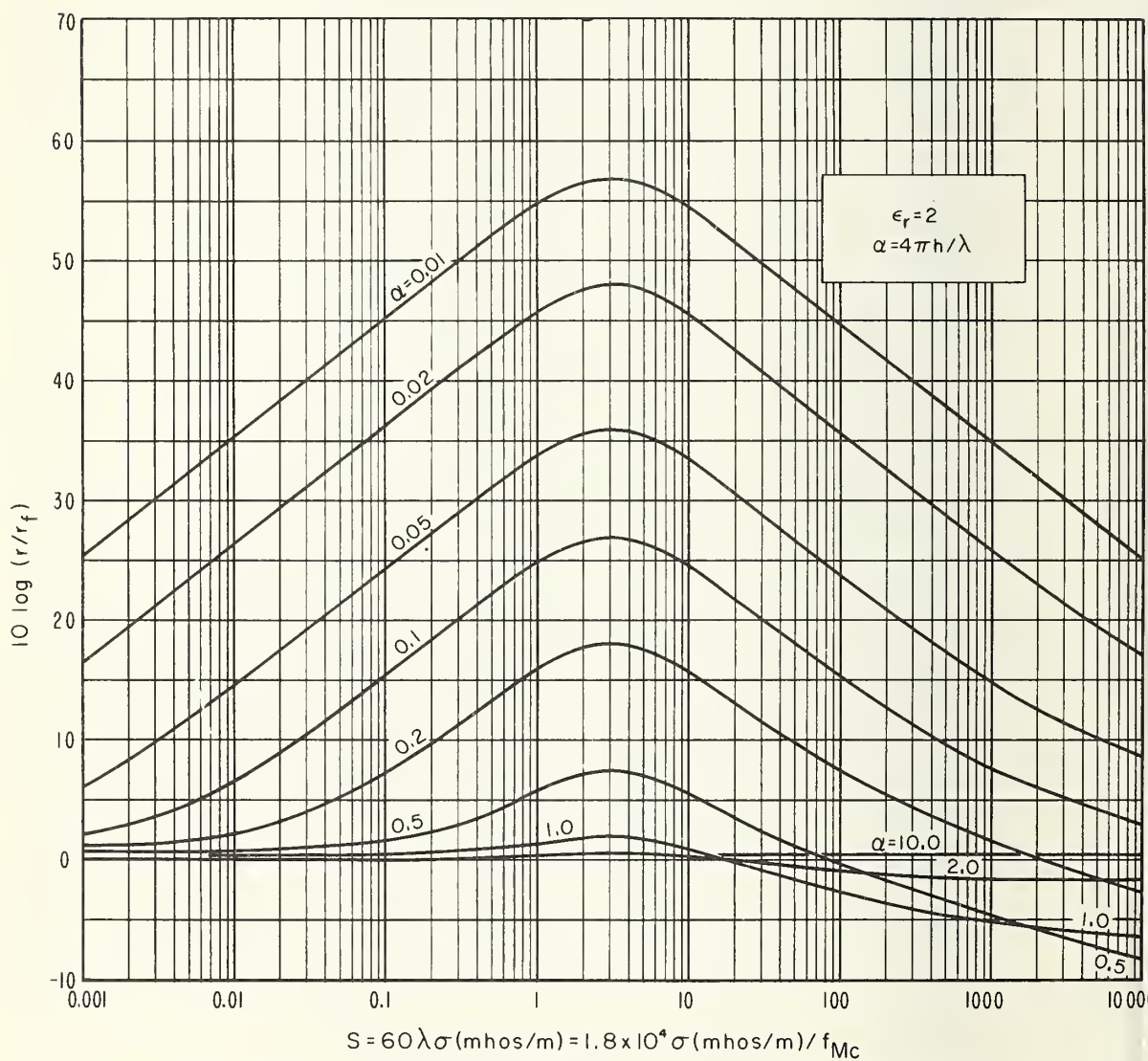


Figure A-9. Ground proximity loss  $L_{t,r}$  for HED,  $\epsilon_r = 2$ .



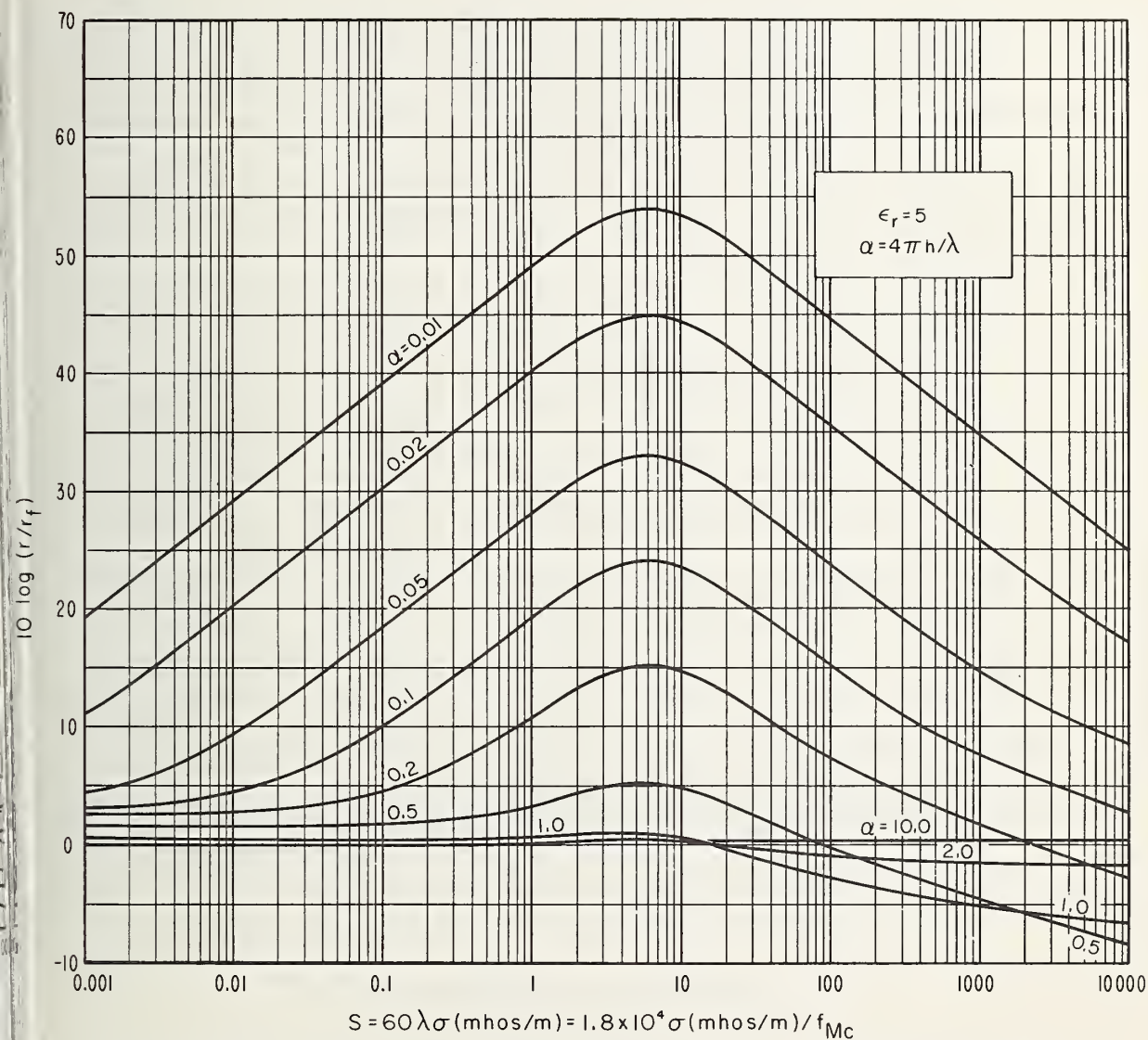


Figure A-10. Ground proximity loss  $L_{t,r}$  for HED,  $\epsilon_r = 5$ .

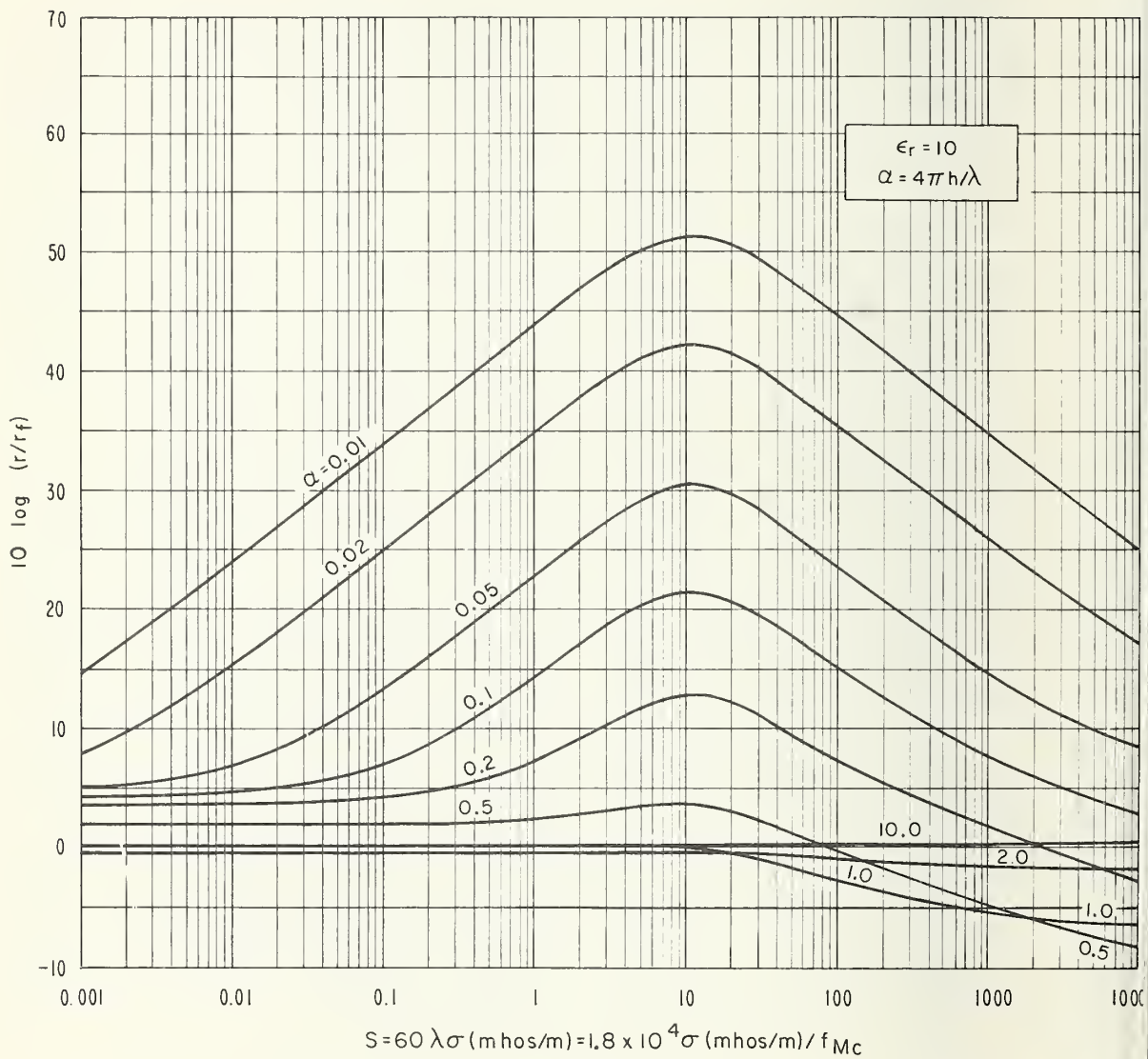


Figure A-11. Ground proximity loss  $L_{t,r}$  for HED,  $\epsilon_r = 10$ .

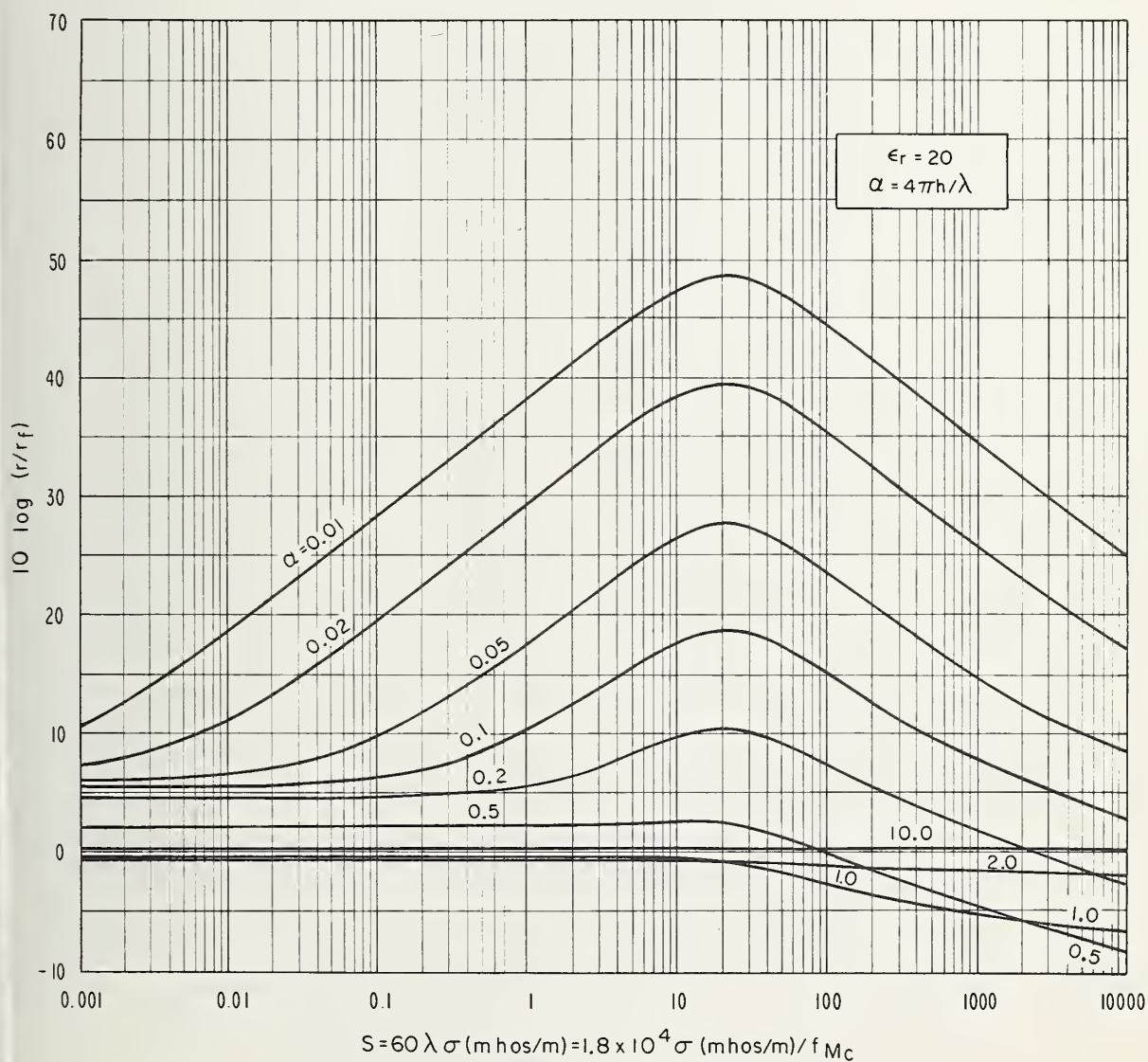


Figure A-12. Ground proximity loss  $L_{t,r}$  for HED,  $\epsilon_r = 20$ .

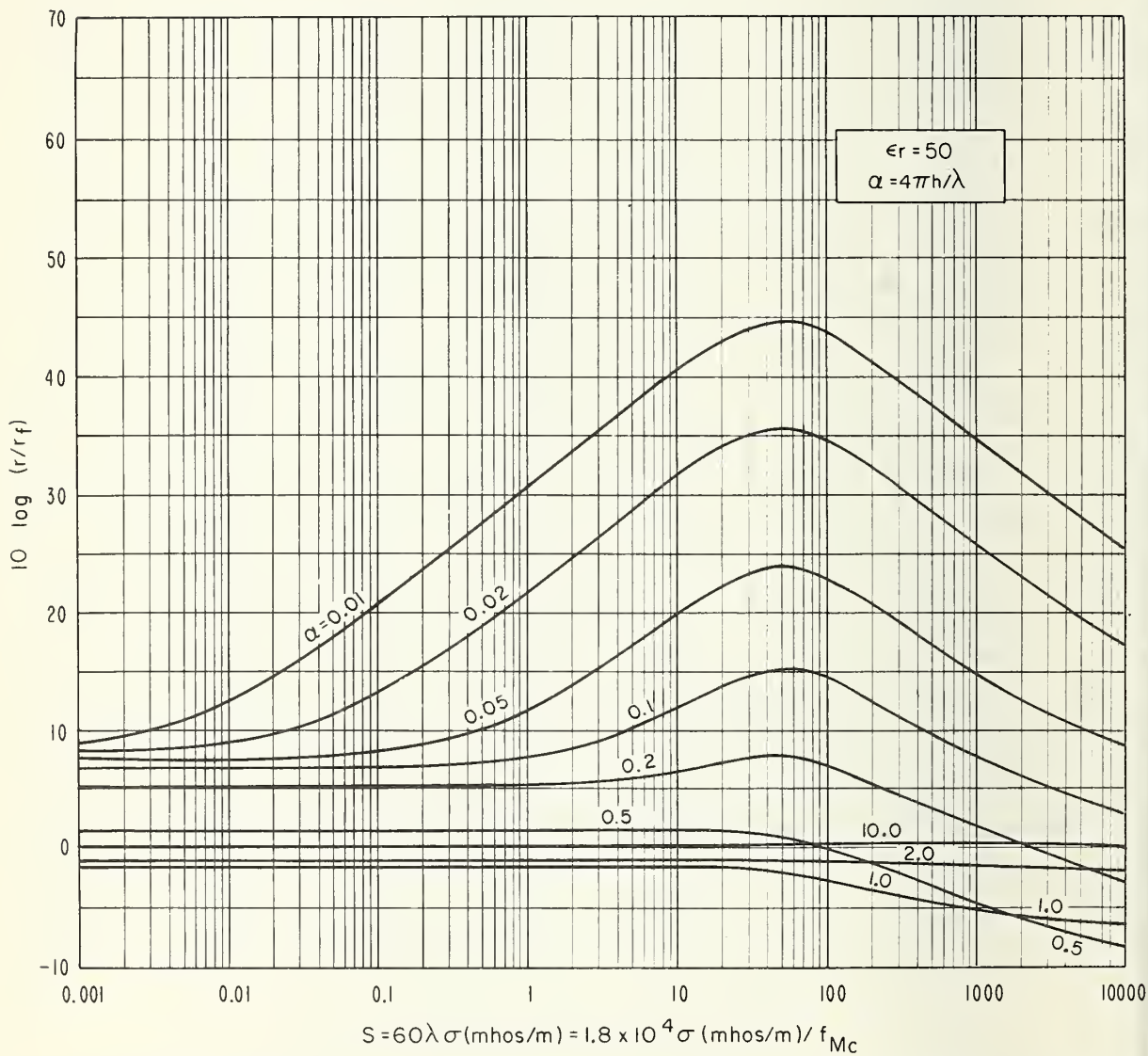


Figure A-13. Ground proximity loss  $L_{t,r}$  for HED,  $\epsilon_r = 50$ .



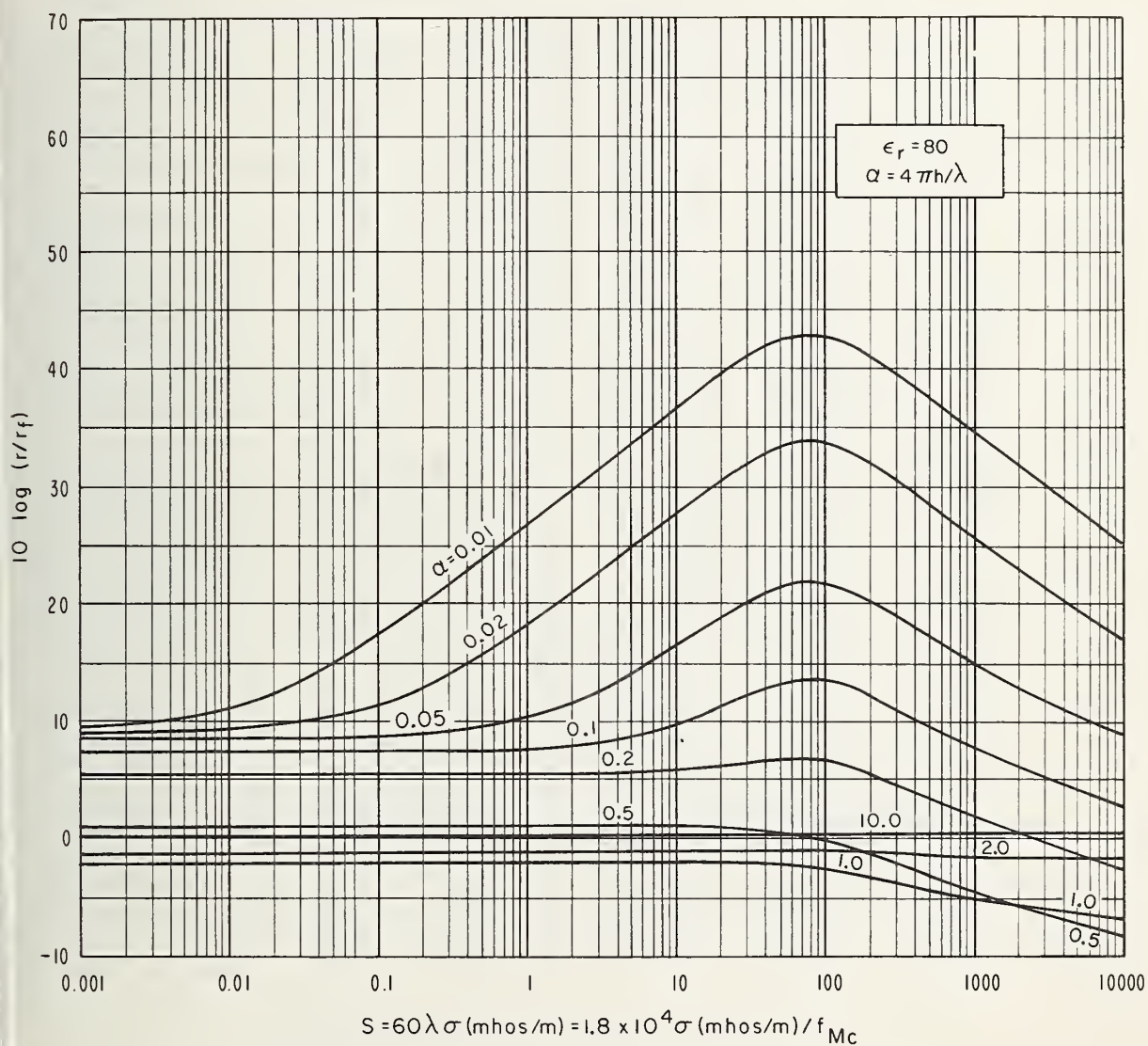


Figure A-14. Ground proximity loss  $L_{t,r}$  for HED,  $\epsilon_r = 80$ .



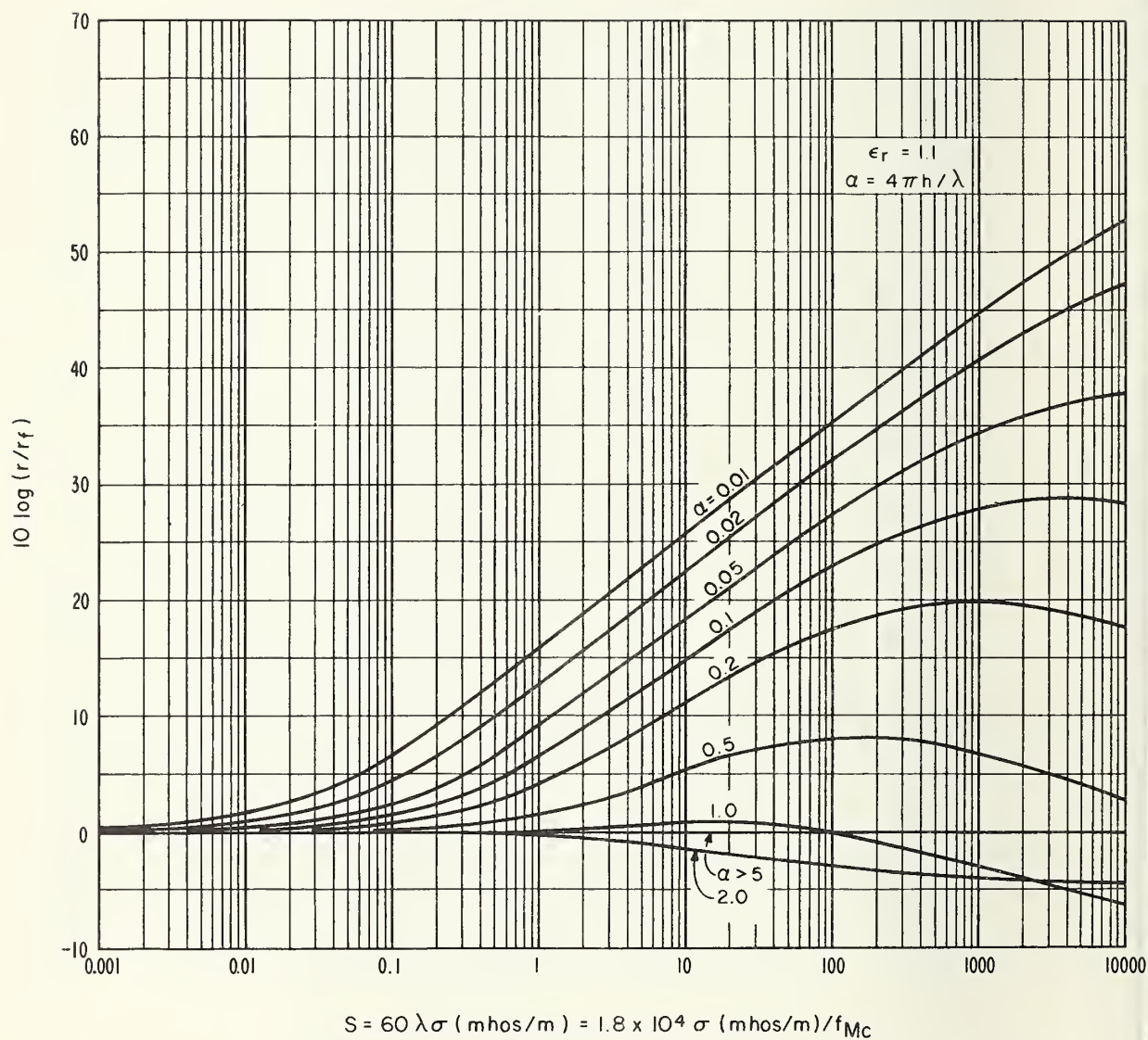


Figure A-15. Ground proximity loss  $L_{t,r}$  for VMD,  $\epsilon_r = 1.1$ .

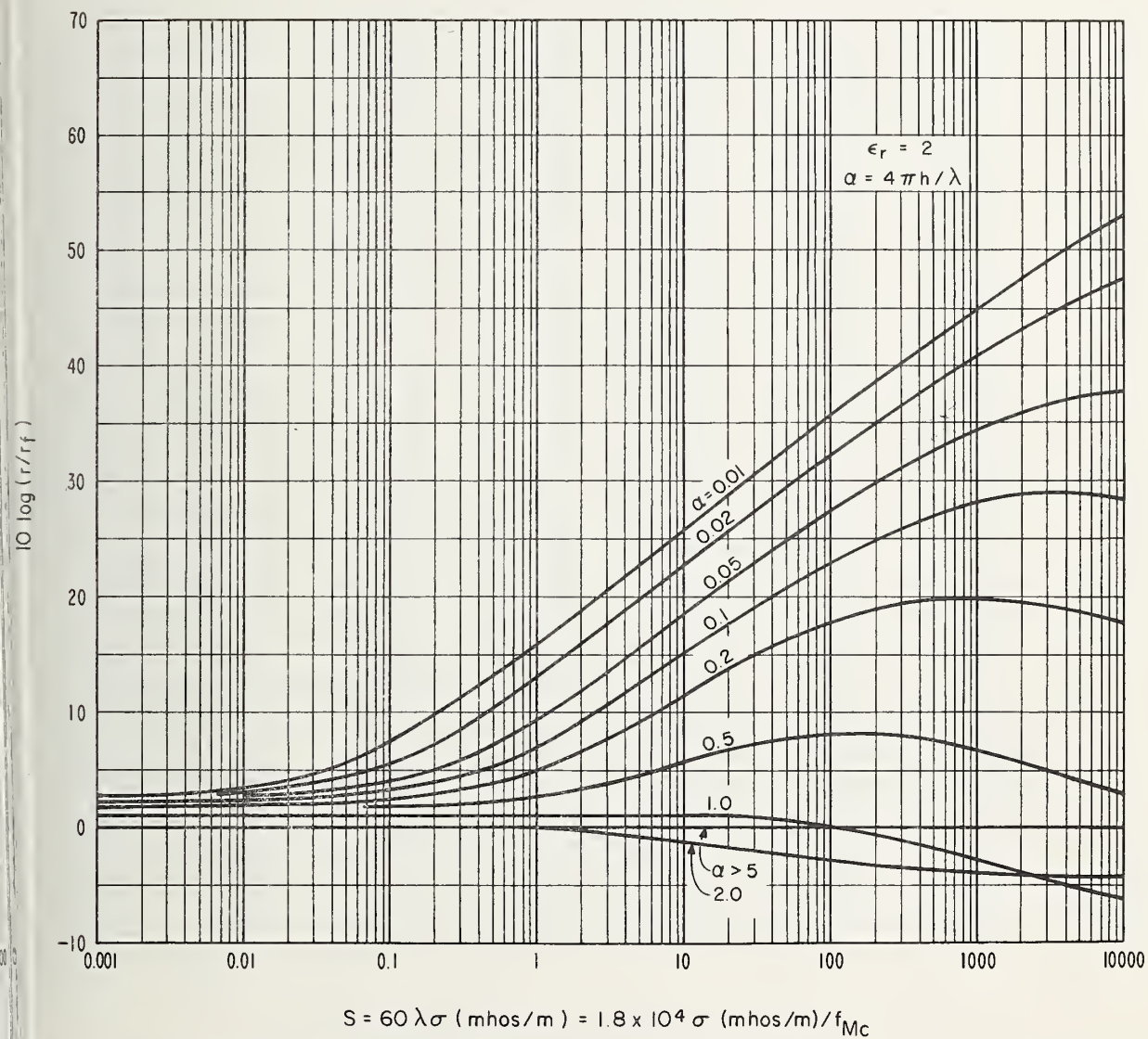


Figure A-16. Ground proximity loss  $L_{t,r}$  for VMD,  $\epsilon_r = 2$ .

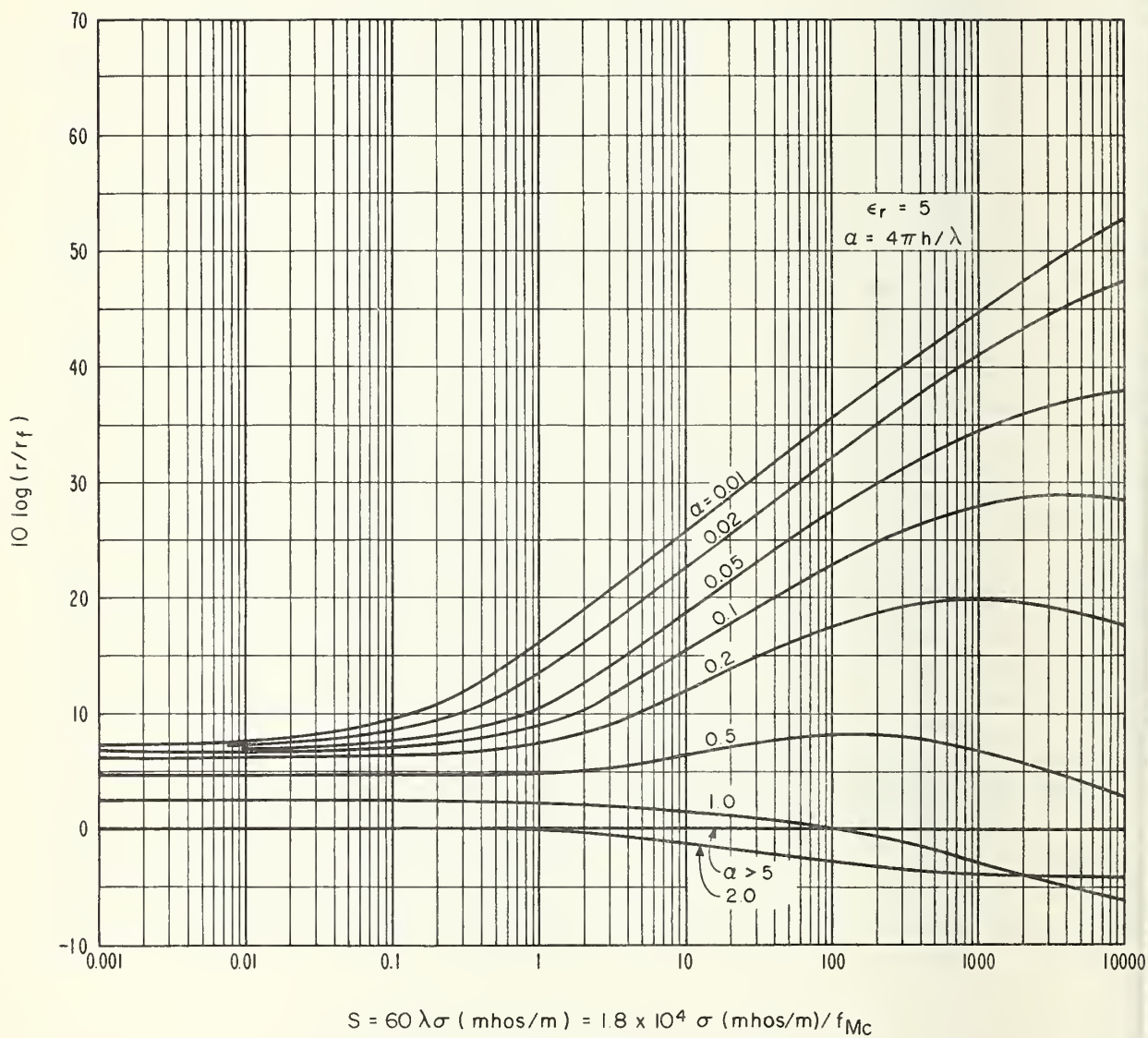


Figure A-17. Ground proximity loss  $L_{t,r}$  for VMD,  $\epsilon_r = 5$ .

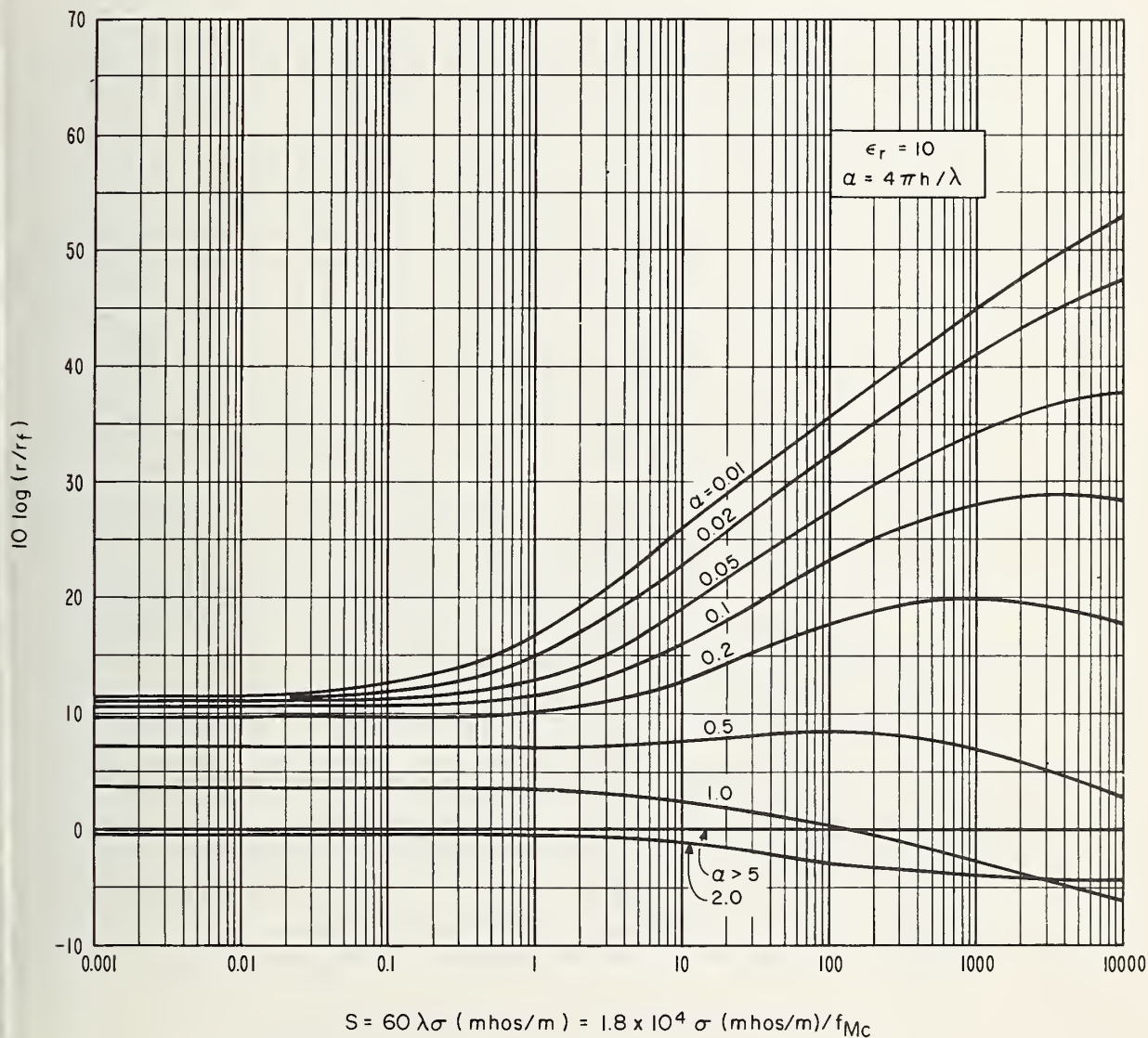


Figure A-18. Ground proximity loss  $L_{t,r}$  for VMD,  $\epsilon_r = 10$ .



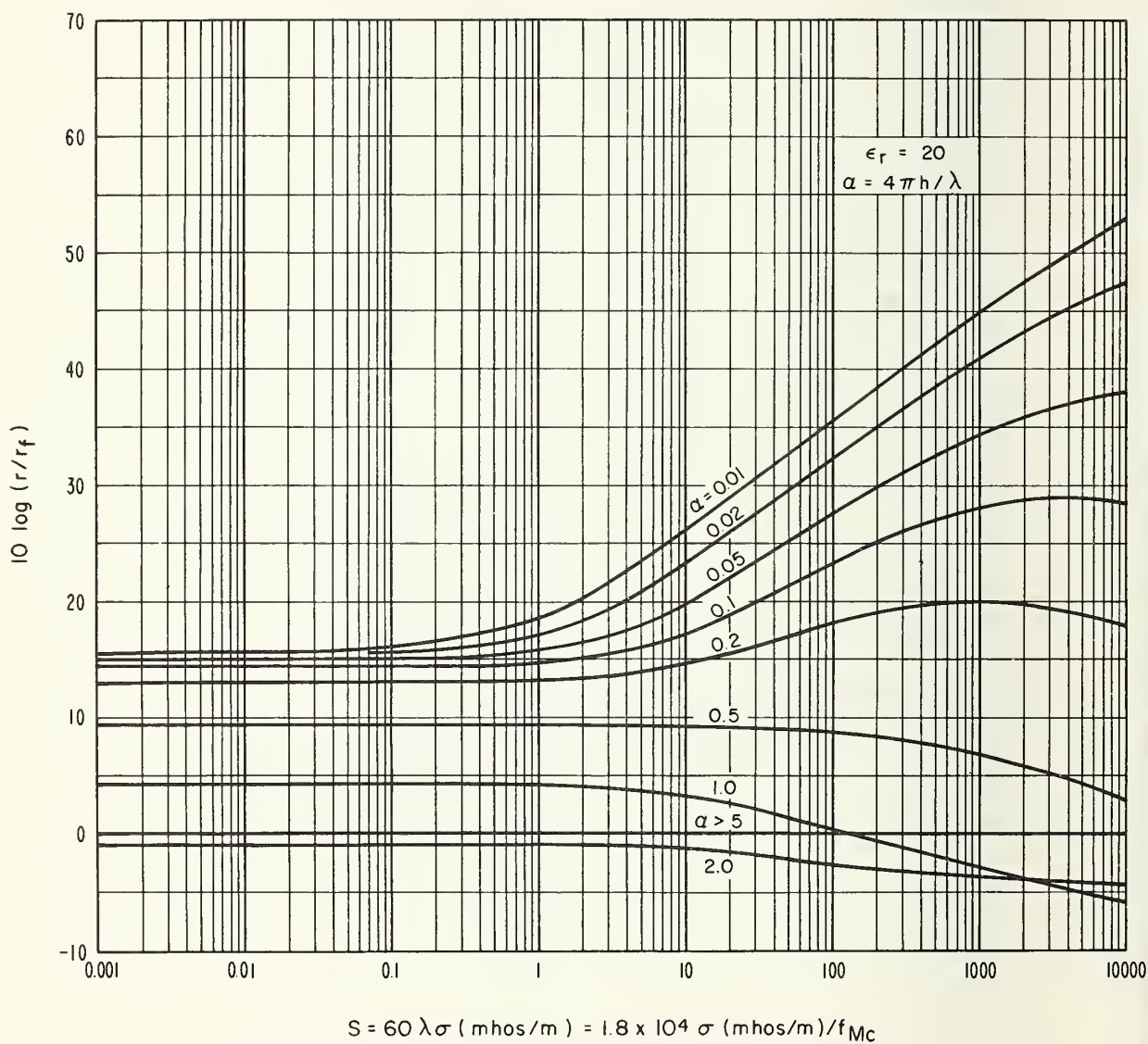


Figure A-19. Ground proximity loss  $L_{t,r}$  for VMD,  $\epsilon_r = 20$ .



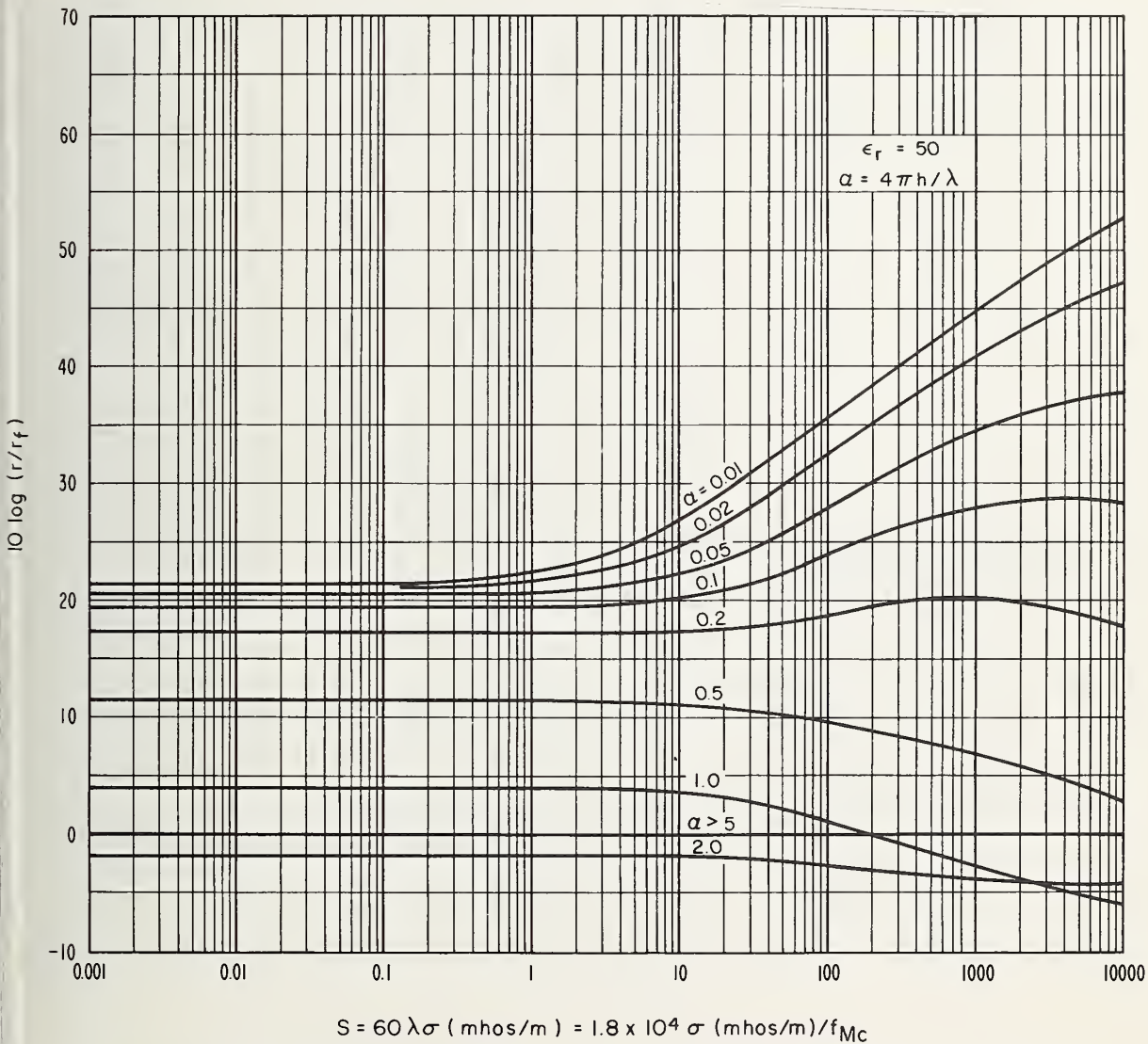


Figure A-20. Ground proximity loss  $L_{t,r}$  for VMD,  $\epsilon_r = 50$ .

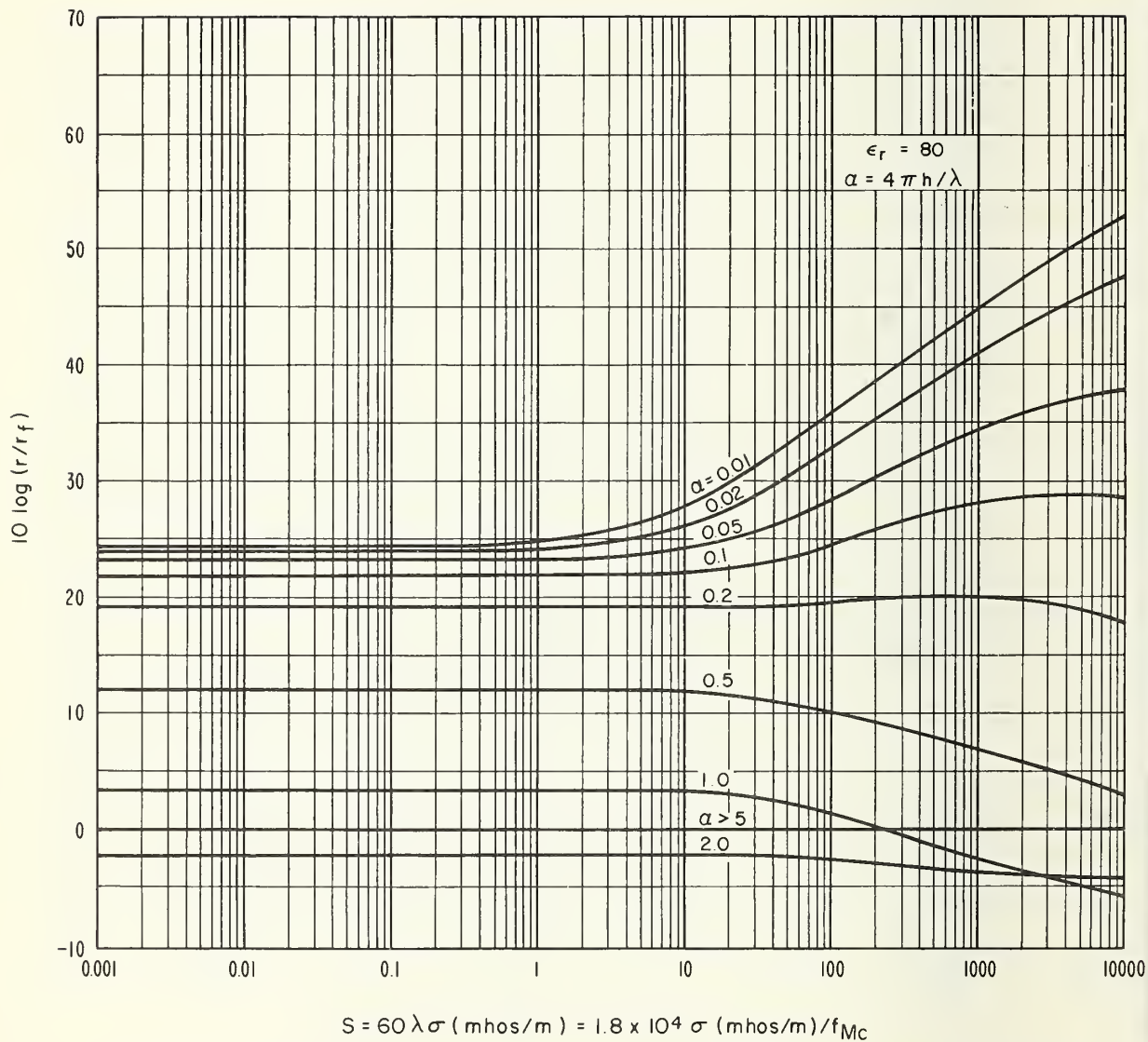


Figure A-21. Ground proximity loss  $L_{t,r}$  for VMD,  $\epsilon_r = 80$ .

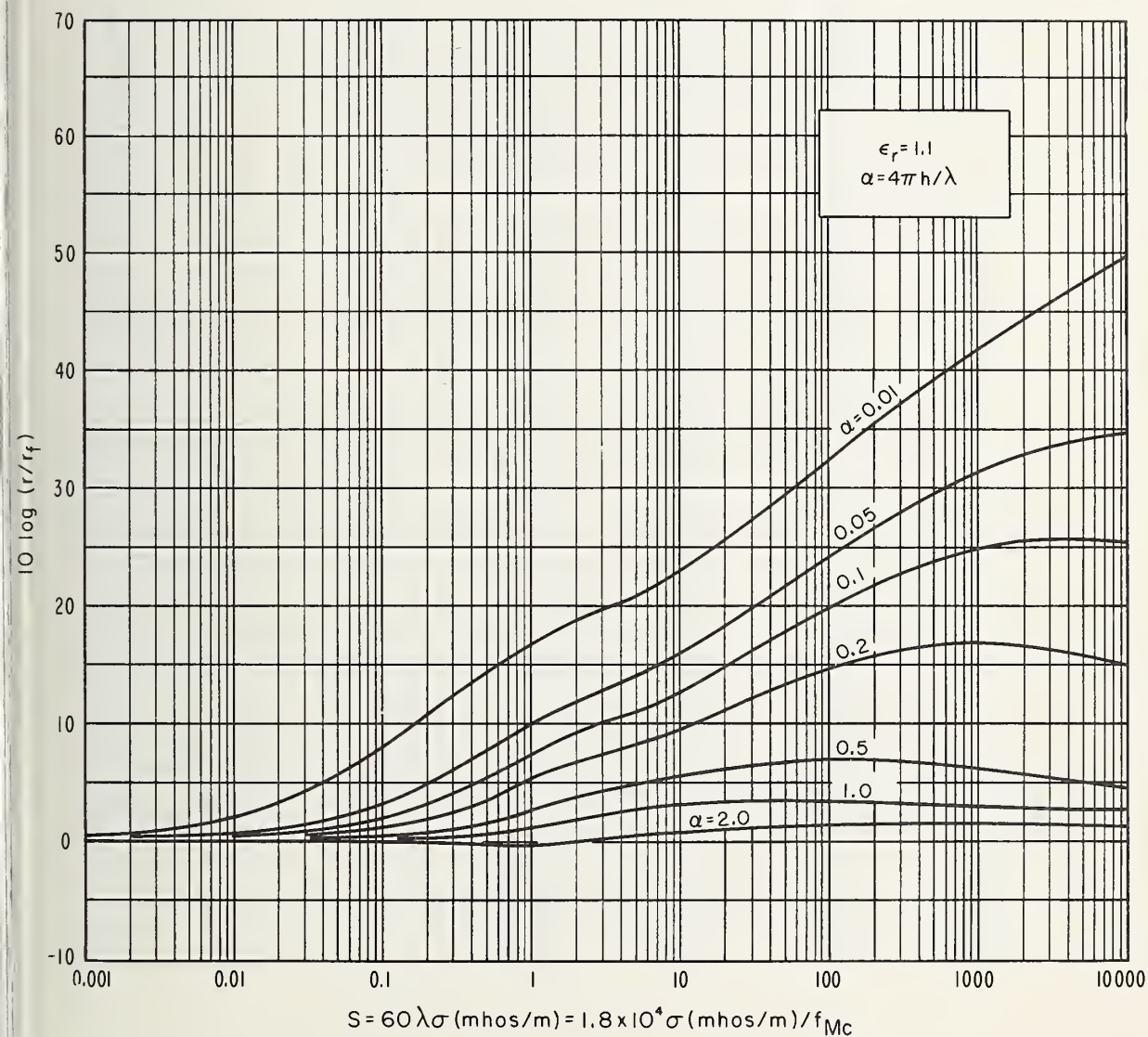


Figure A-22. Ground proximity loss  $L_{t,r}$  for HMD,  $\epsilon_r = 1.1$ .

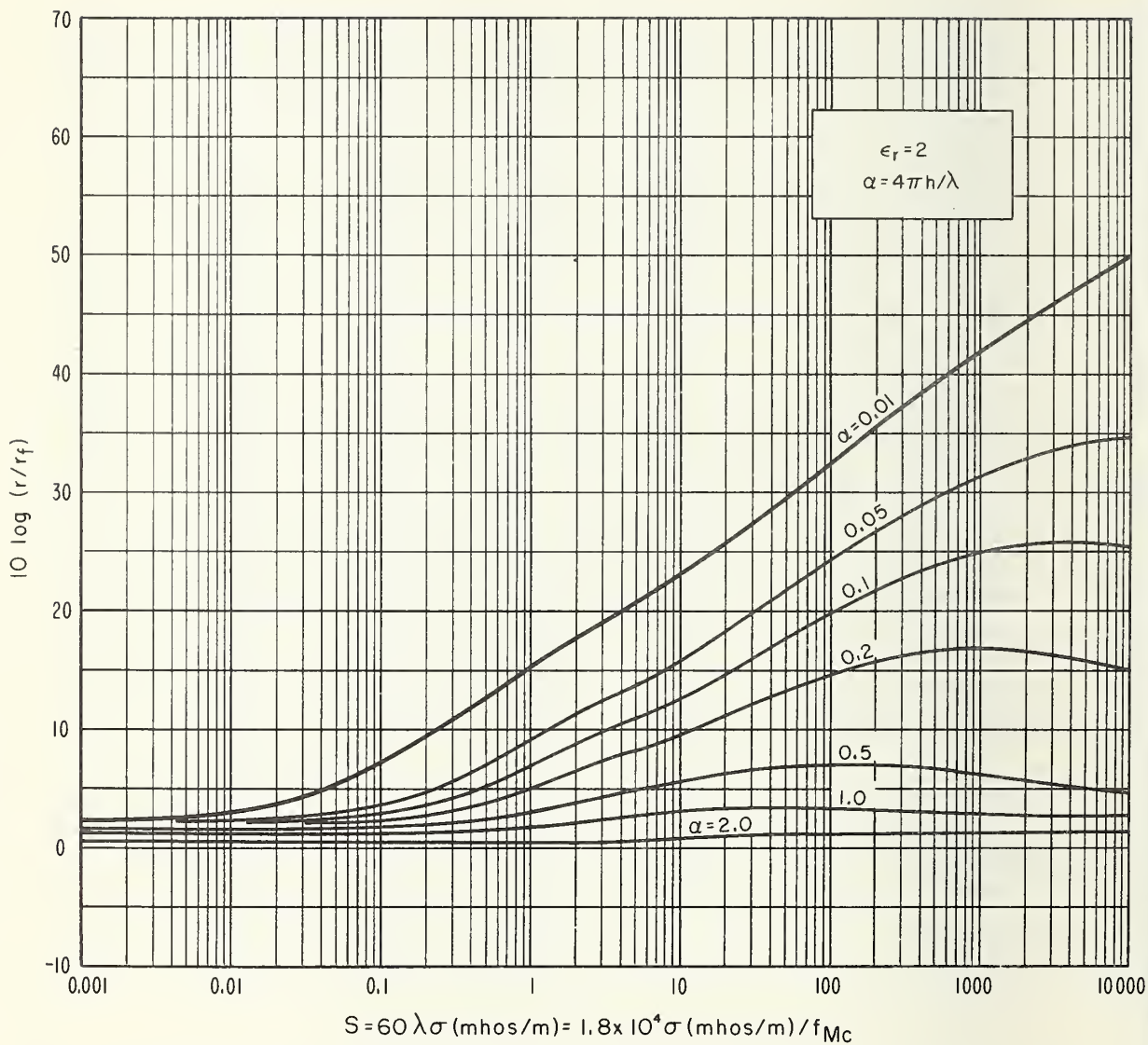


Figure A-23. Ground proximity loss  $L_{t,r}$  for HMD,  $\epsilon_r = 2$ .



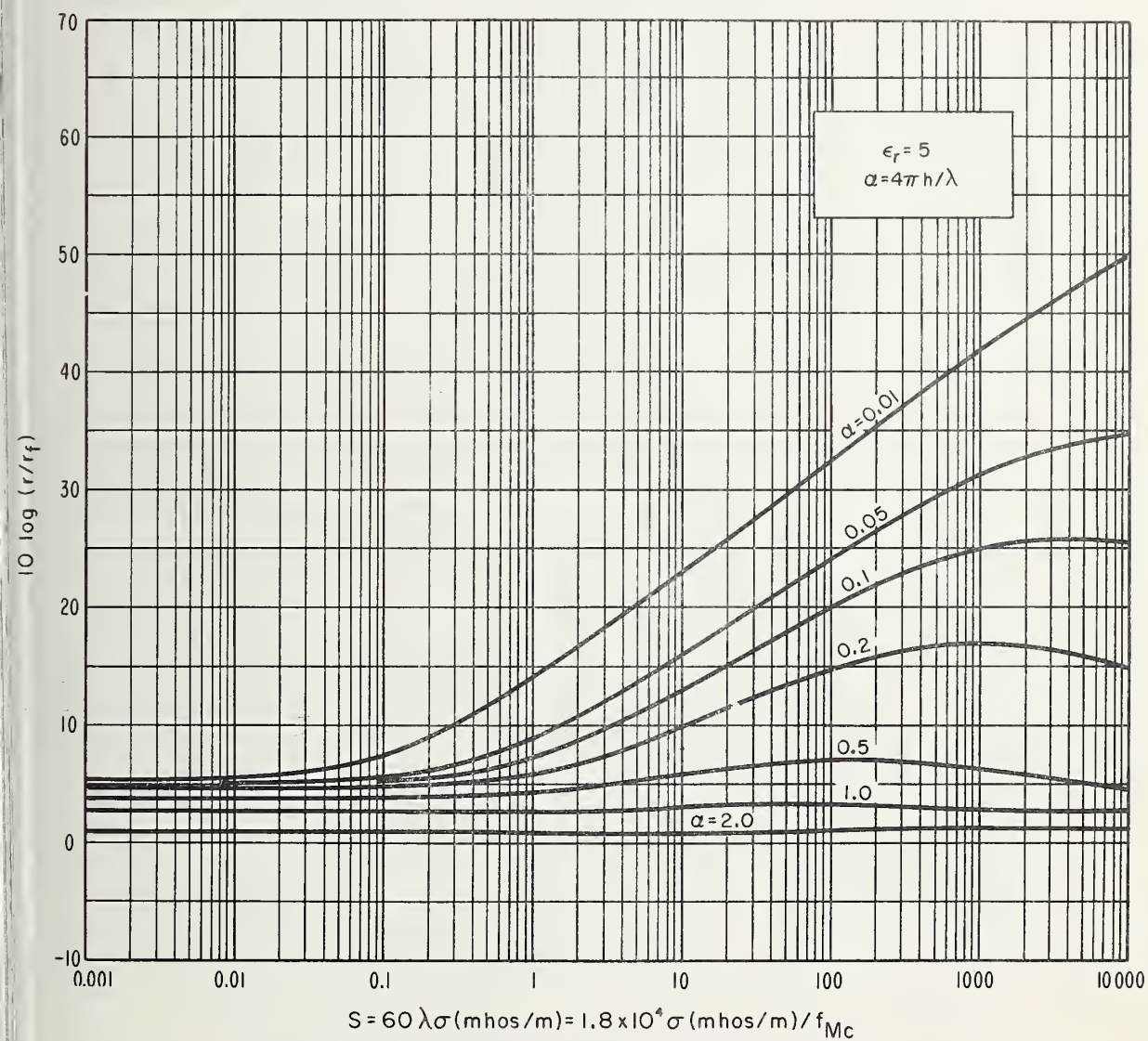


Figure A-24. Ground proximity loss  $L_{t,r}$  for HMD,  $\epsilon_r = 5$ .



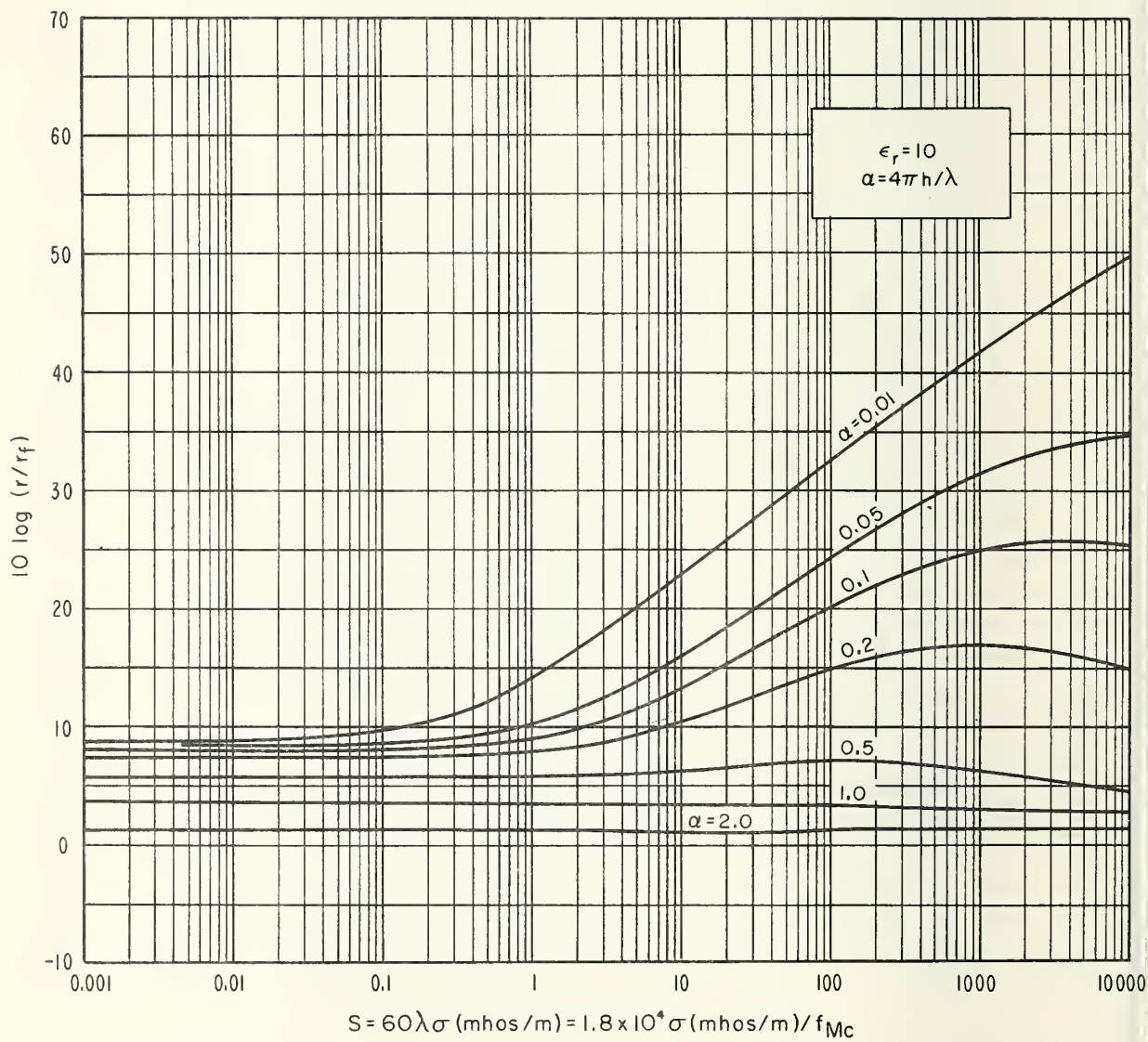


Figure A-25. Ground proximity loss  $L_{t,r}$  for HMD,  $\epsilon_r = 10$ .

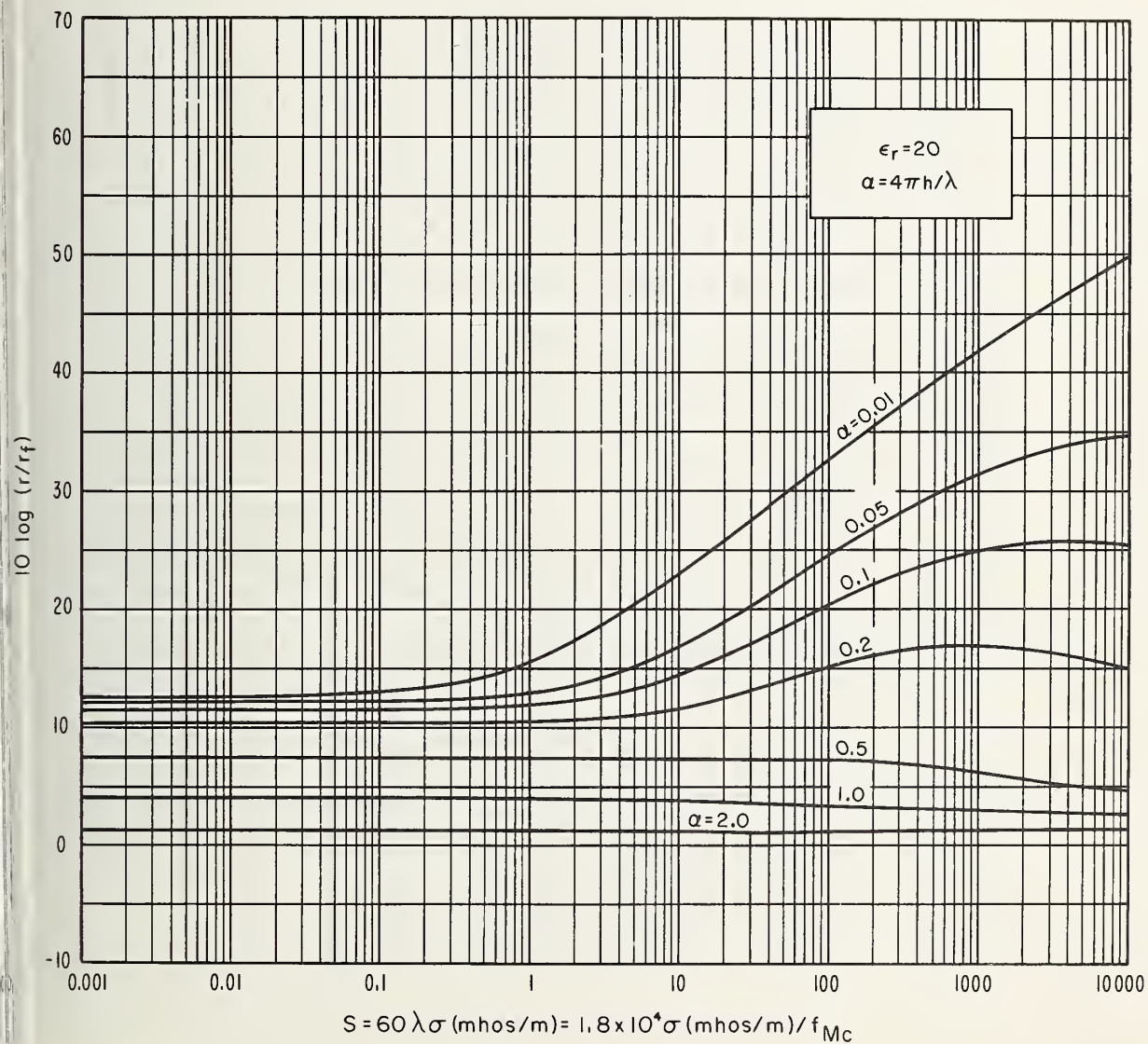


Figure A-26. Ground proximity loss  $L_{t,r}$  for HMD,  $\epsilon_r = 20$ .

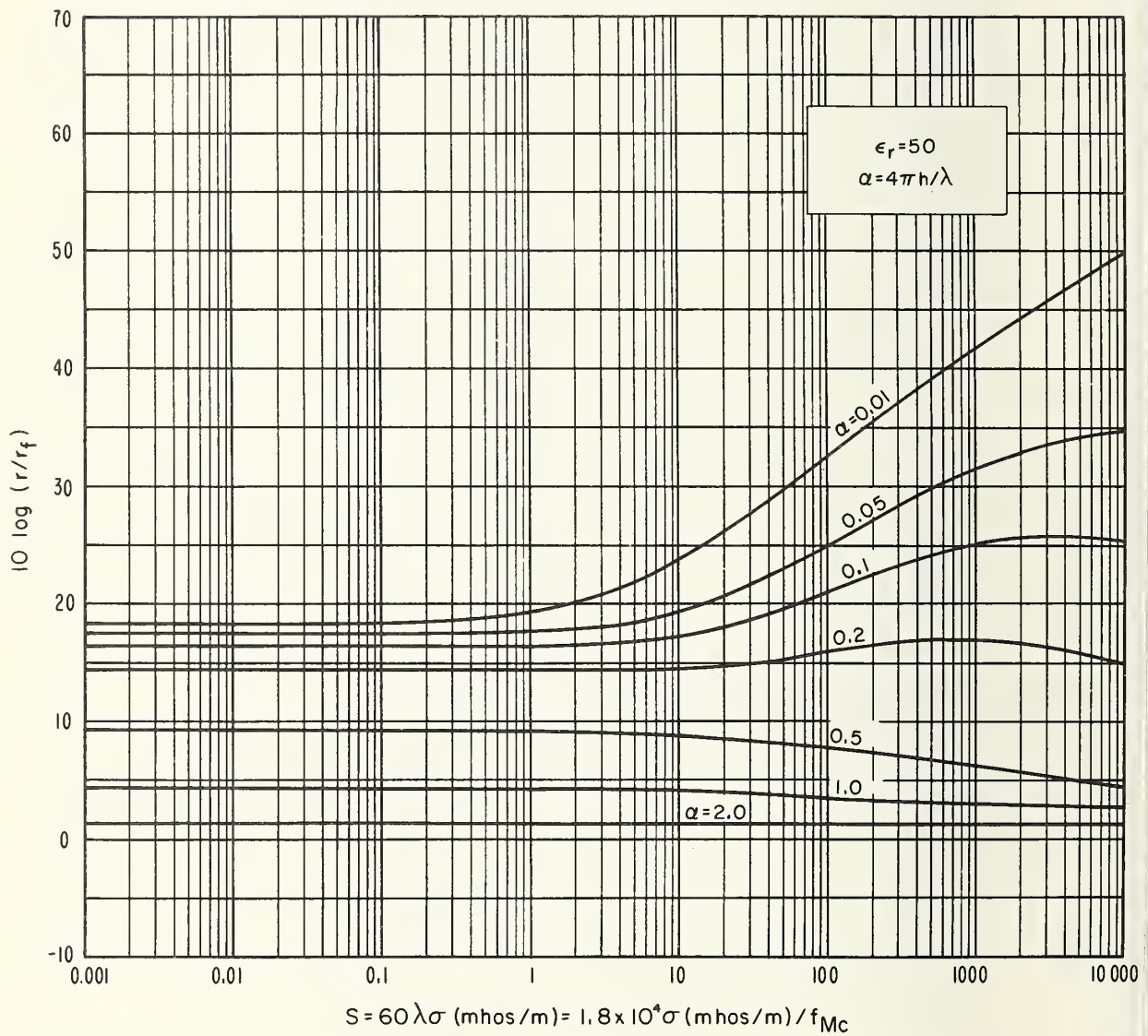


Figure A-27. Ground proximity loss  $L_{t,r}$  for HMD,  $\epsilon_r = 50$ .

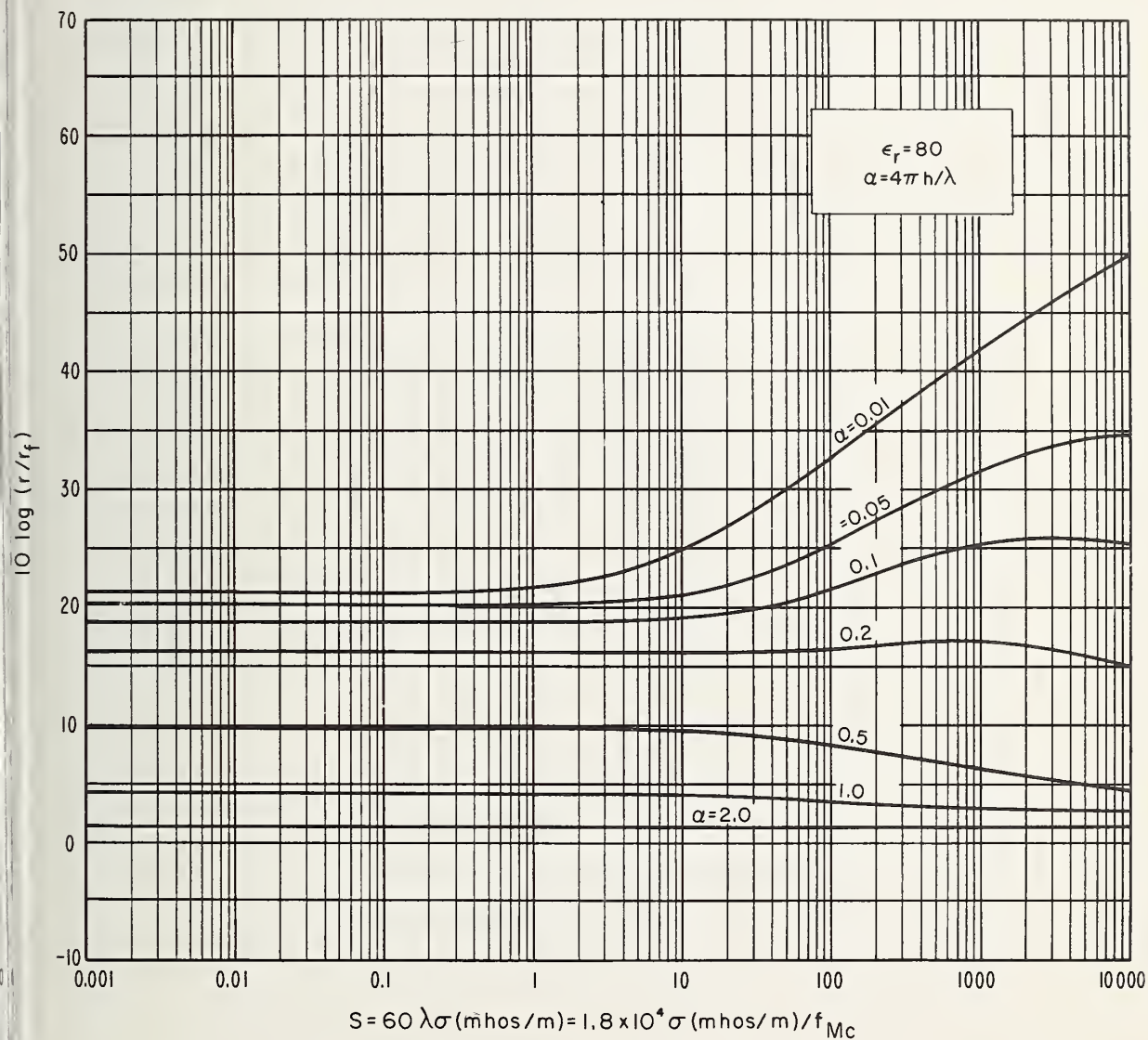


Figure A-28. Ground proximity loss  $L_{t,r}$  for HMD,  $\epsilon_r = 80$ .





13. GRAPHS OF NORMALIZED INPUT IMPEDANCE CHANGE,  $\Delta Z/r_f$

for

Vertical Electric Dipoles (VED)

Horizontal Electric Dipoles (HED)

Vertical Magnetic Dipoles (VMD)

Horizontal Magnetic Dipoles (HMD)

$$|N| = \left[ \epsilon_r^2 + s^2 \right]^{1/4}, \quad \phi/2 = (1/2) \tan^{-1}(s/\epsilon_r),$$

$$s = 60 \lambda \sigma (\text{mhos/m}), \quad \alpha = (2h)(2\pi/\lambda),$$

$\epsilon_r$ : relative dielectric constant of ground

$\sigma$ (mhos/m): conductivity of ground

$h$ : height in meters of antenna above ground

$\lambda$ : wavelength in meters

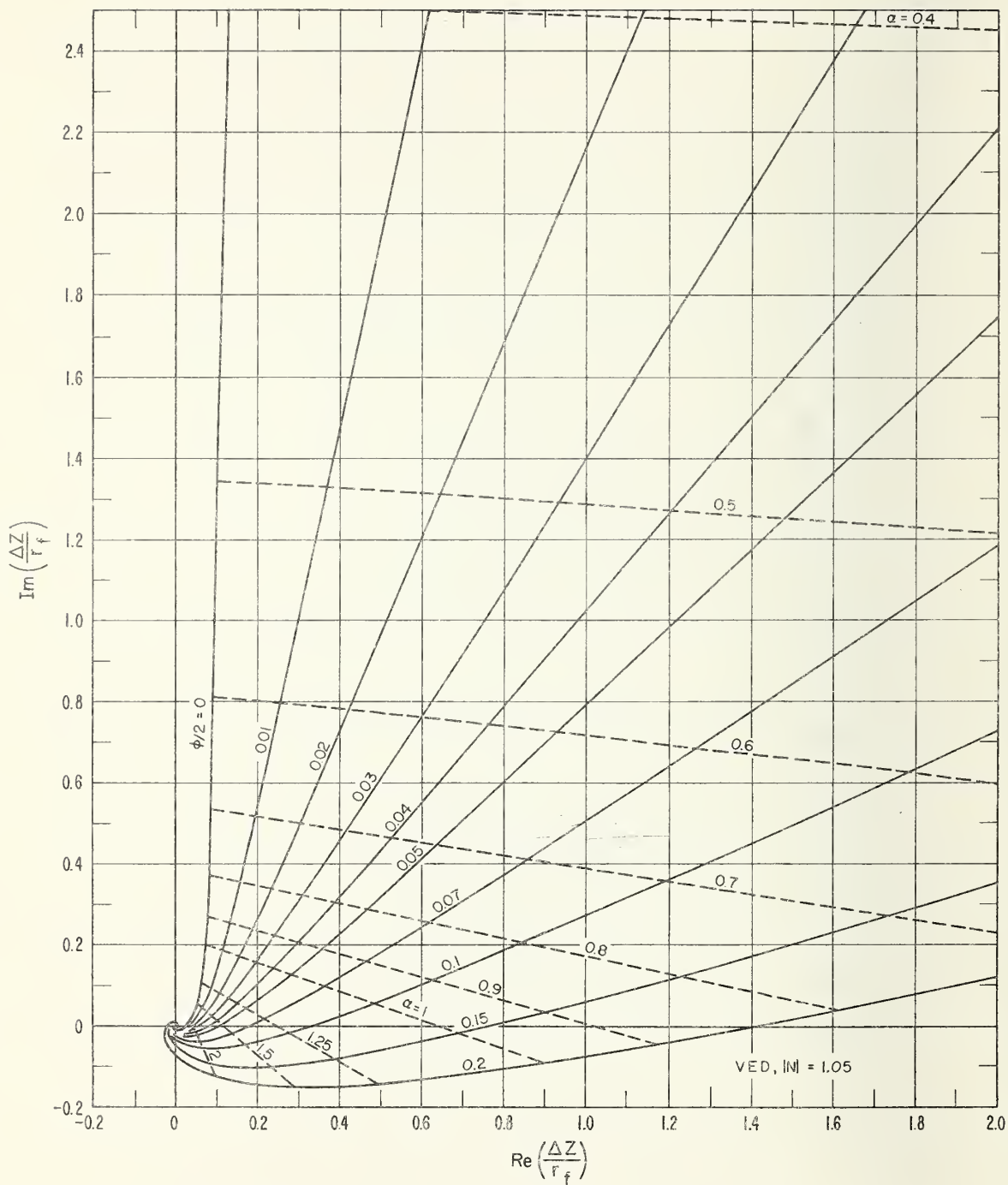


Figure A-29. Normalized input impedance change for VED,  $|N| = 1.05$ .

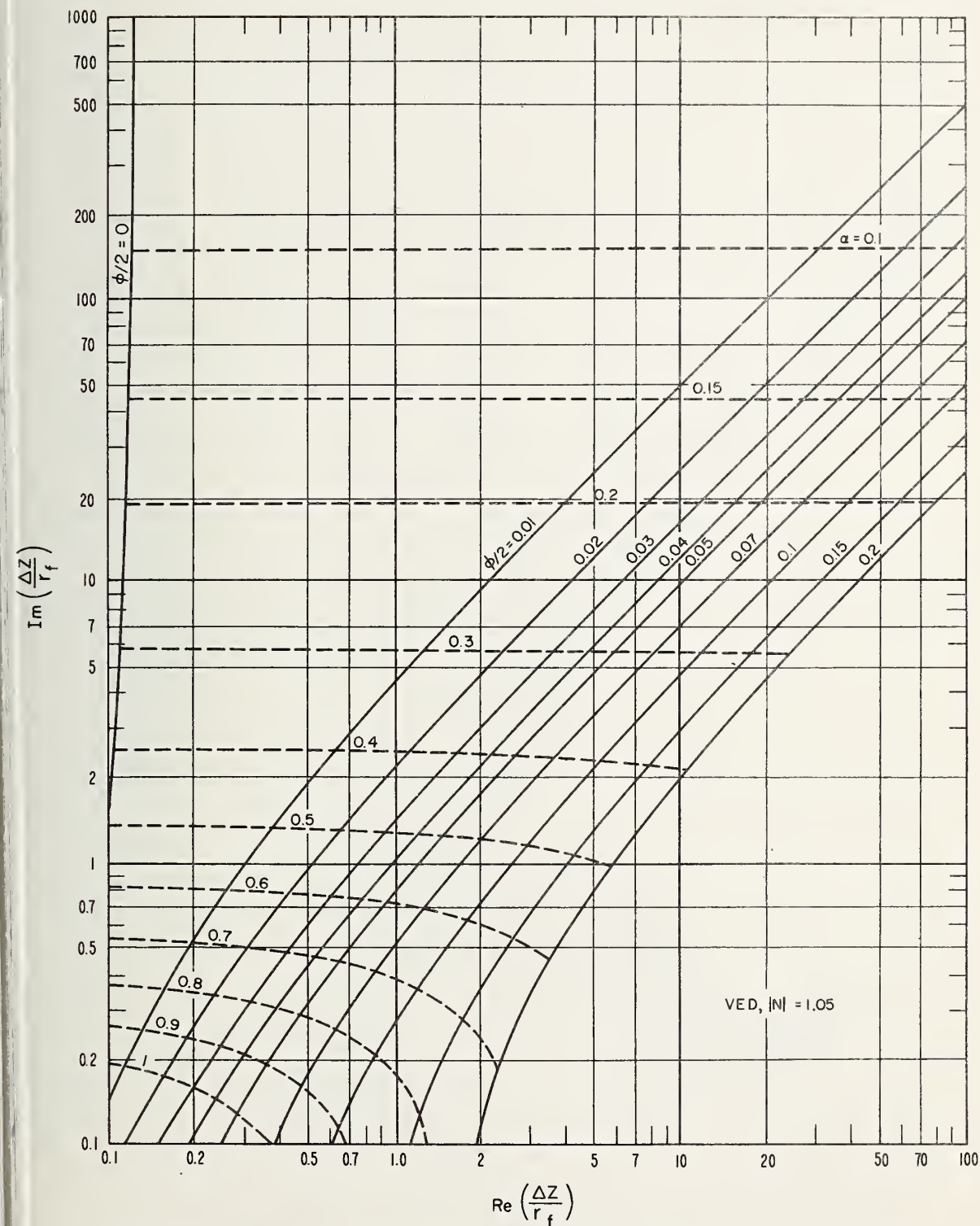


Figure A-30. Normalized input impedance change for VED,  $|N| = 1.05$ .

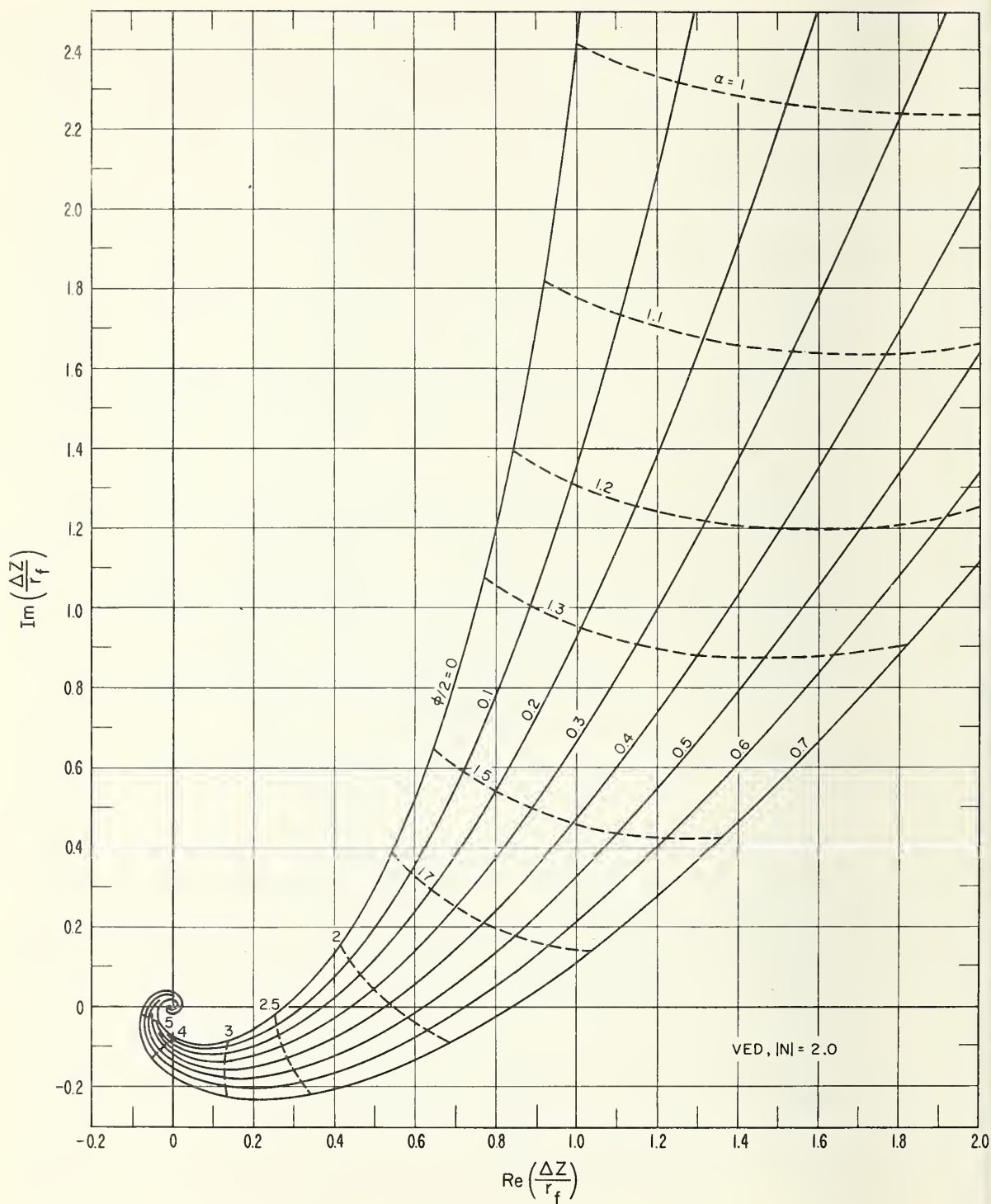


Figure A-31. Normalized input impedance change for VED,  $|N| = 2$ .

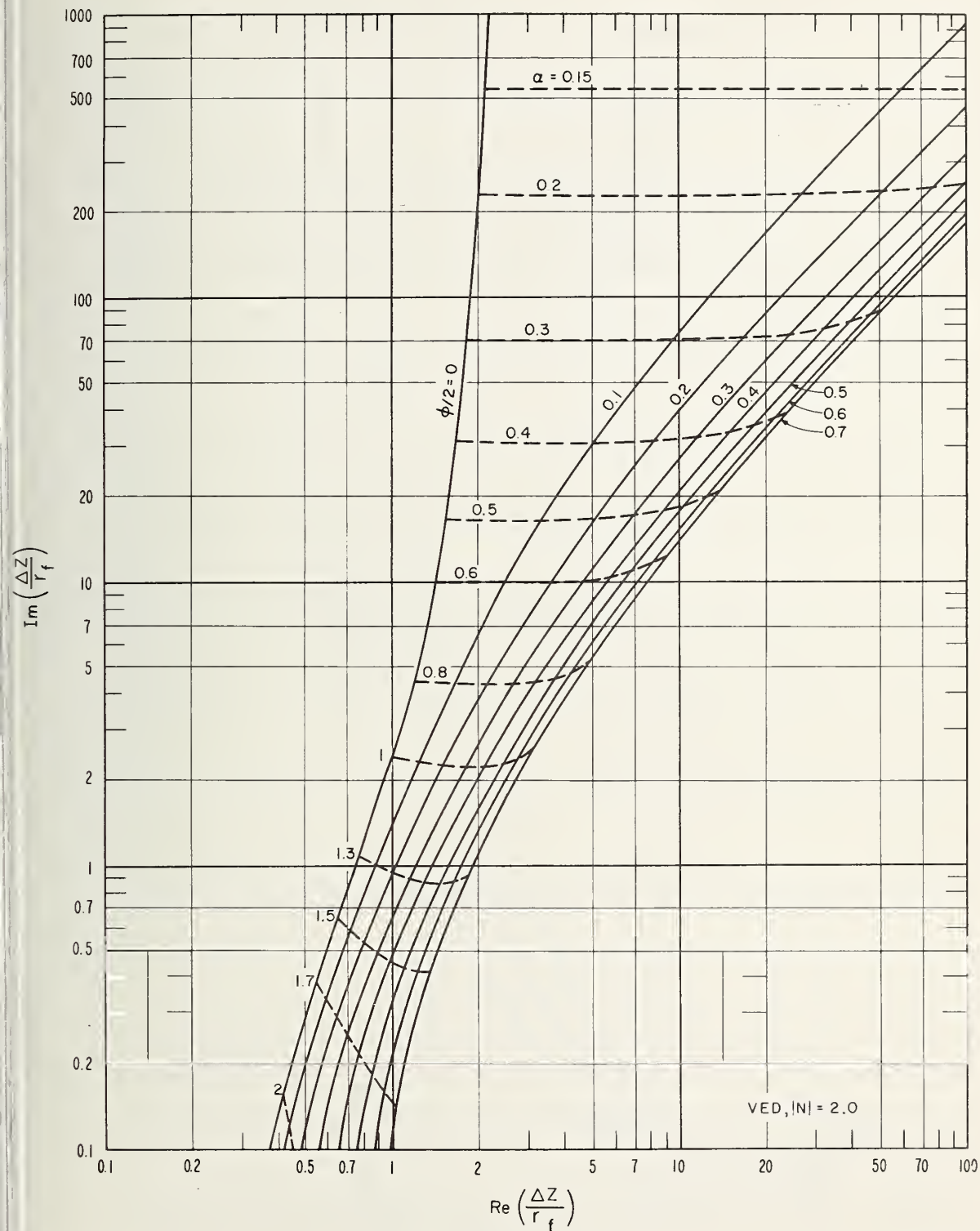


Figure A-32. Normalized input impedance change for VED,  $|N| = 2$ .



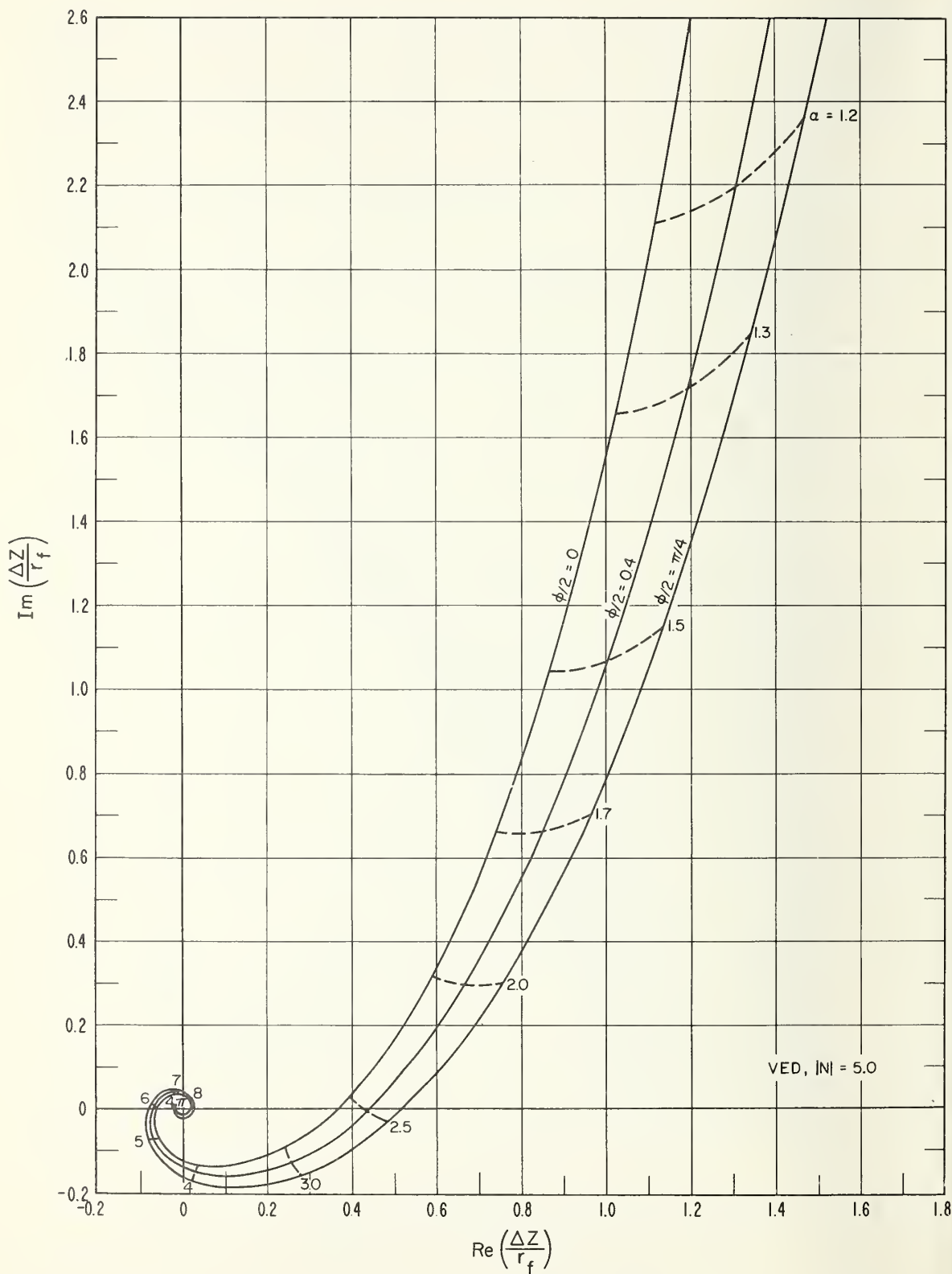


Figure A-33. Normalized input impedance change for VED,  $|N| = 5$ .

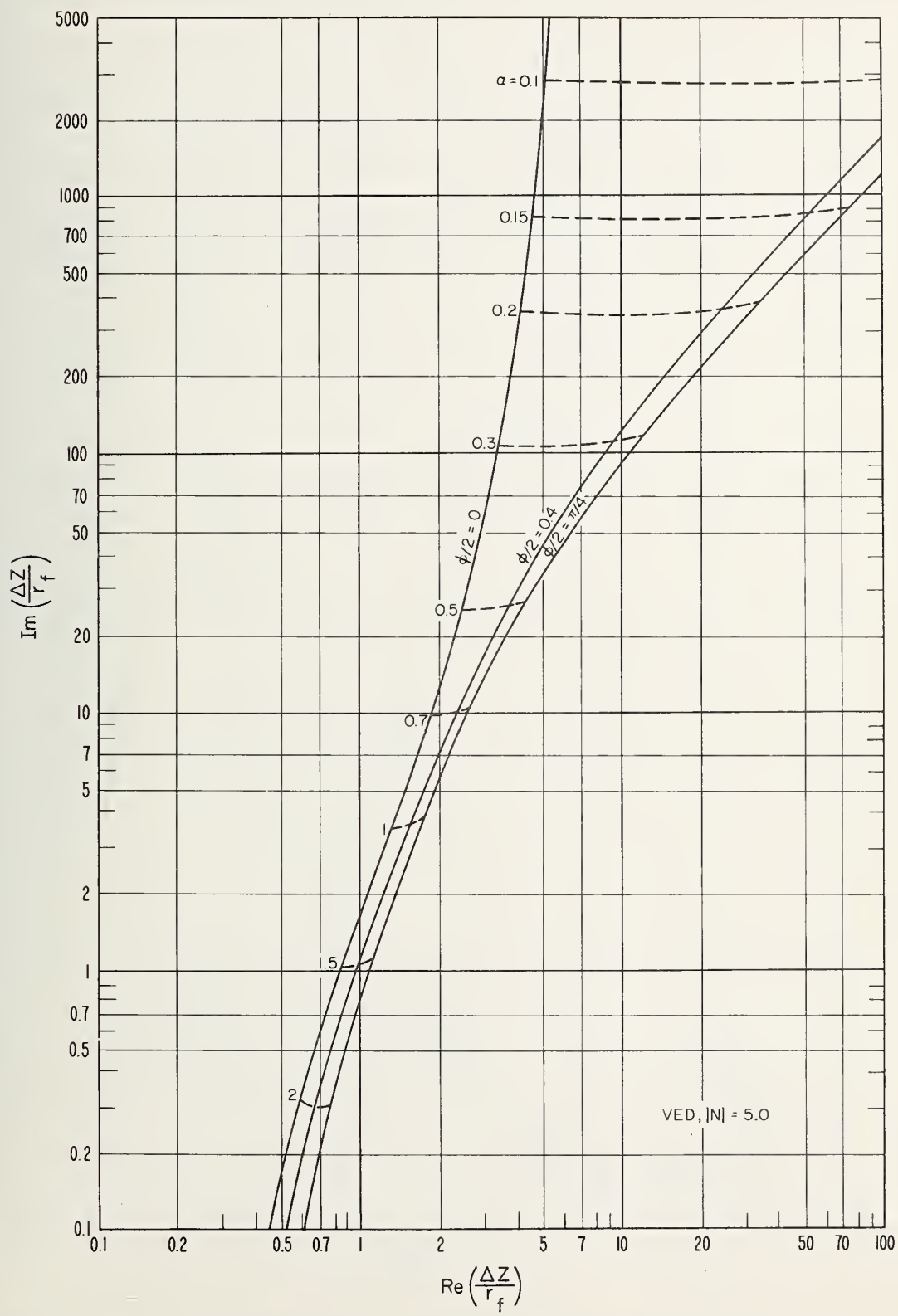


Figure A-34. Normalized input impedance change for VED,  $|N| = 5$ .

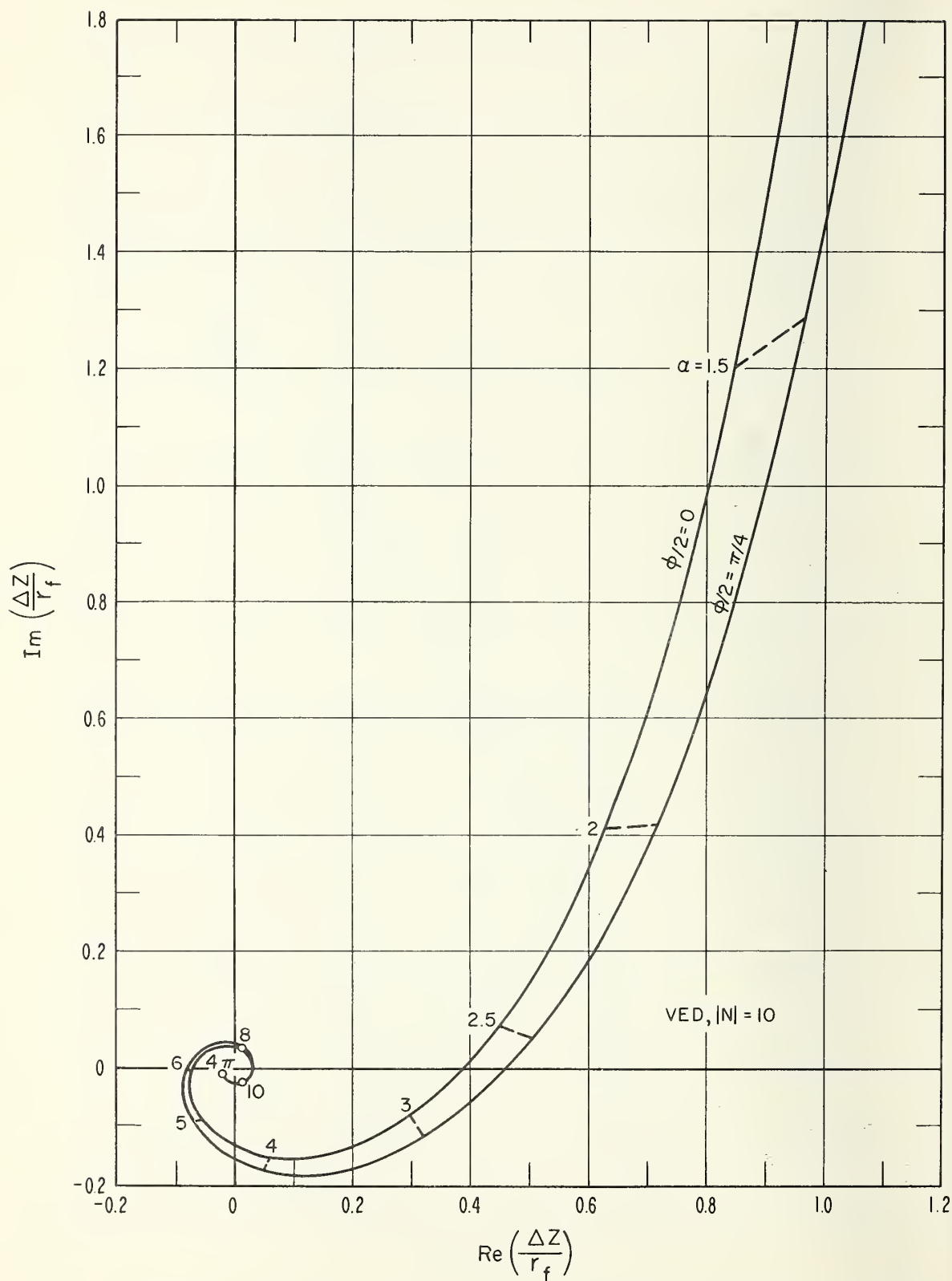


Figure A-35. Normalized input impedance change for VED,  
 $|N| = 10$ .

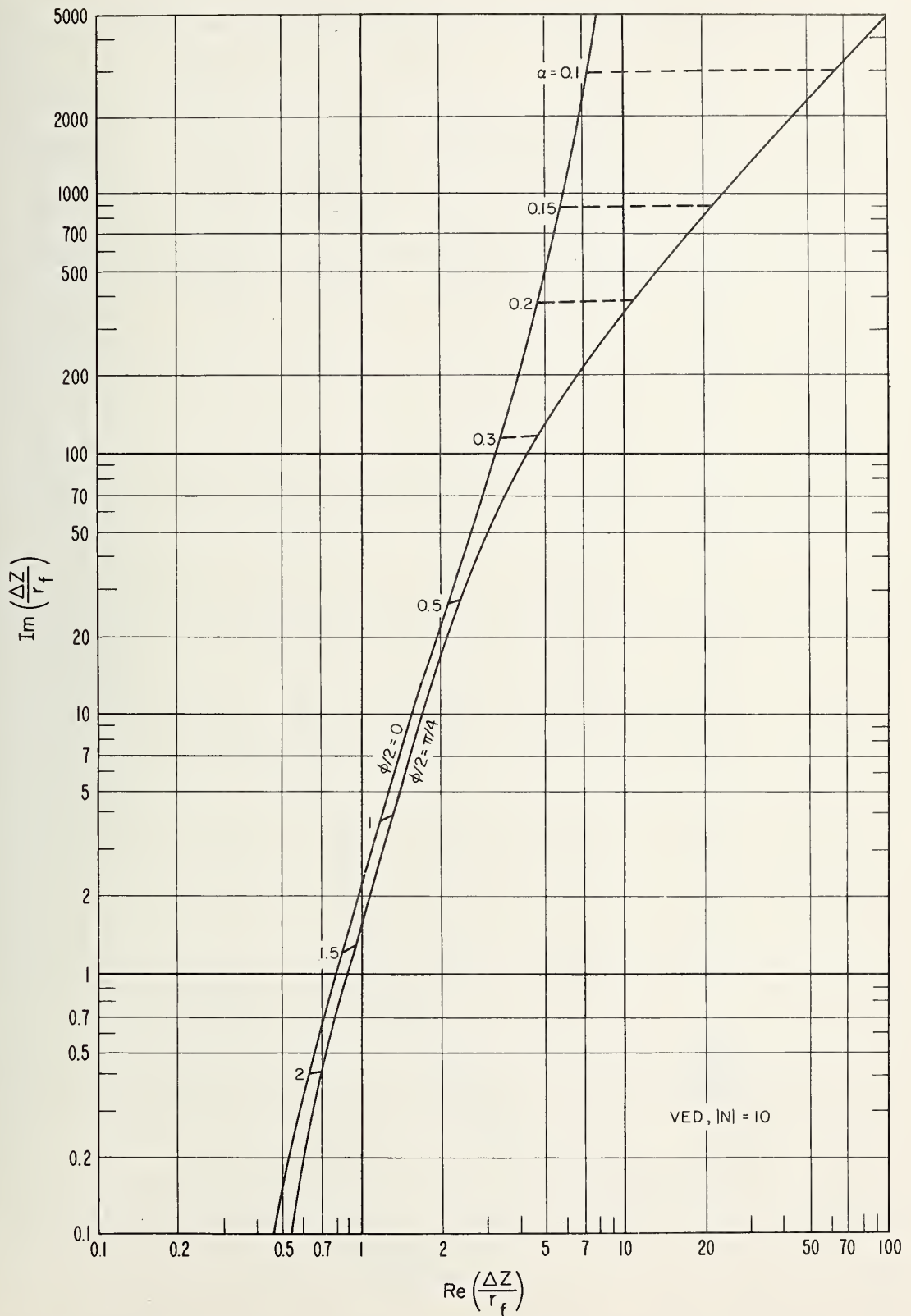


Figure A-36. Normalized input impedance change for  $\text{VED}, |N| = 10$ .

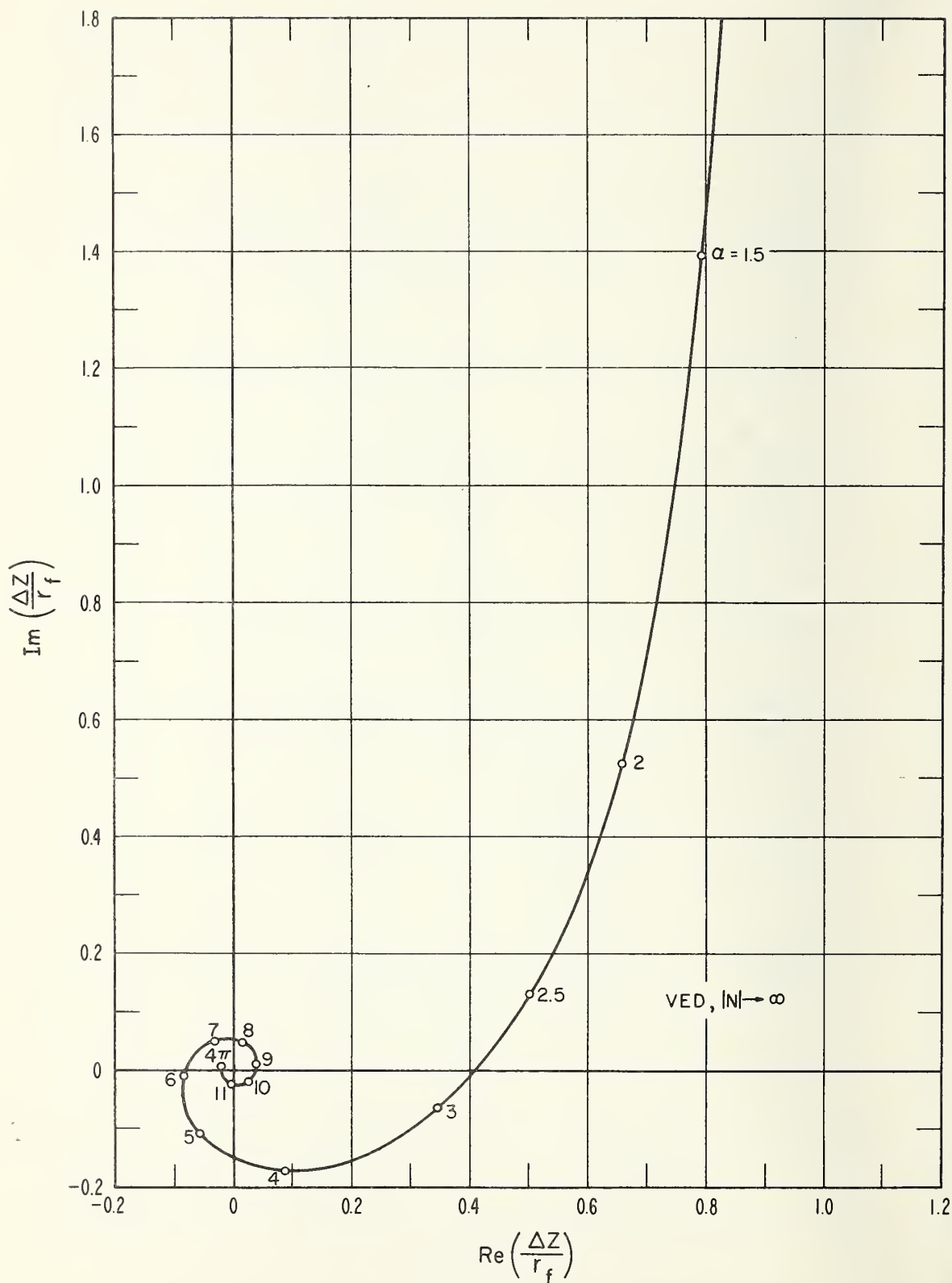
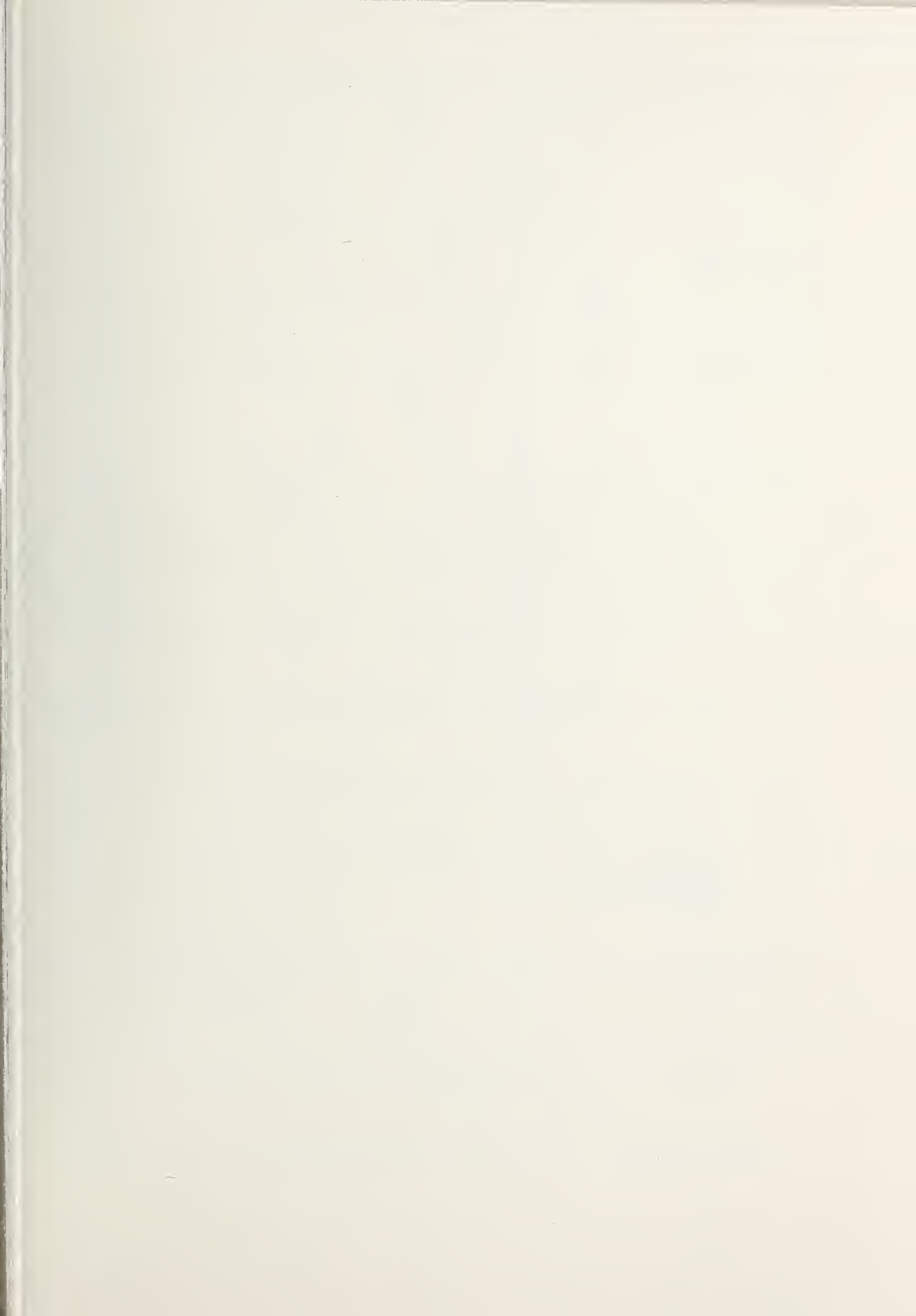


Figure A-37. Normalized input impedance change for VED,  $|N| \rightarrow \infty$ .





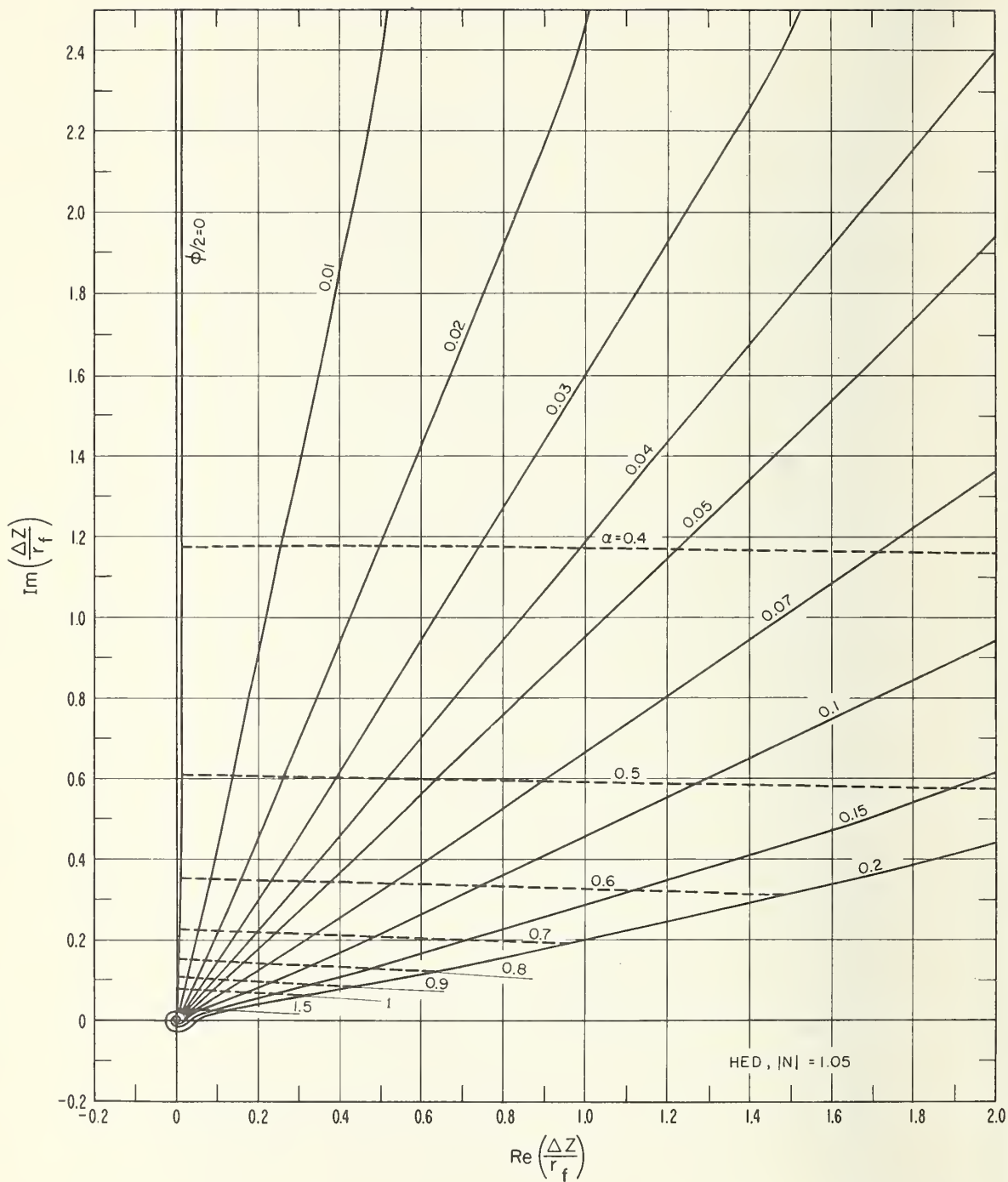


Figure A-38. Normalized input impedance change for HED,  $|N| = 1.05$ .

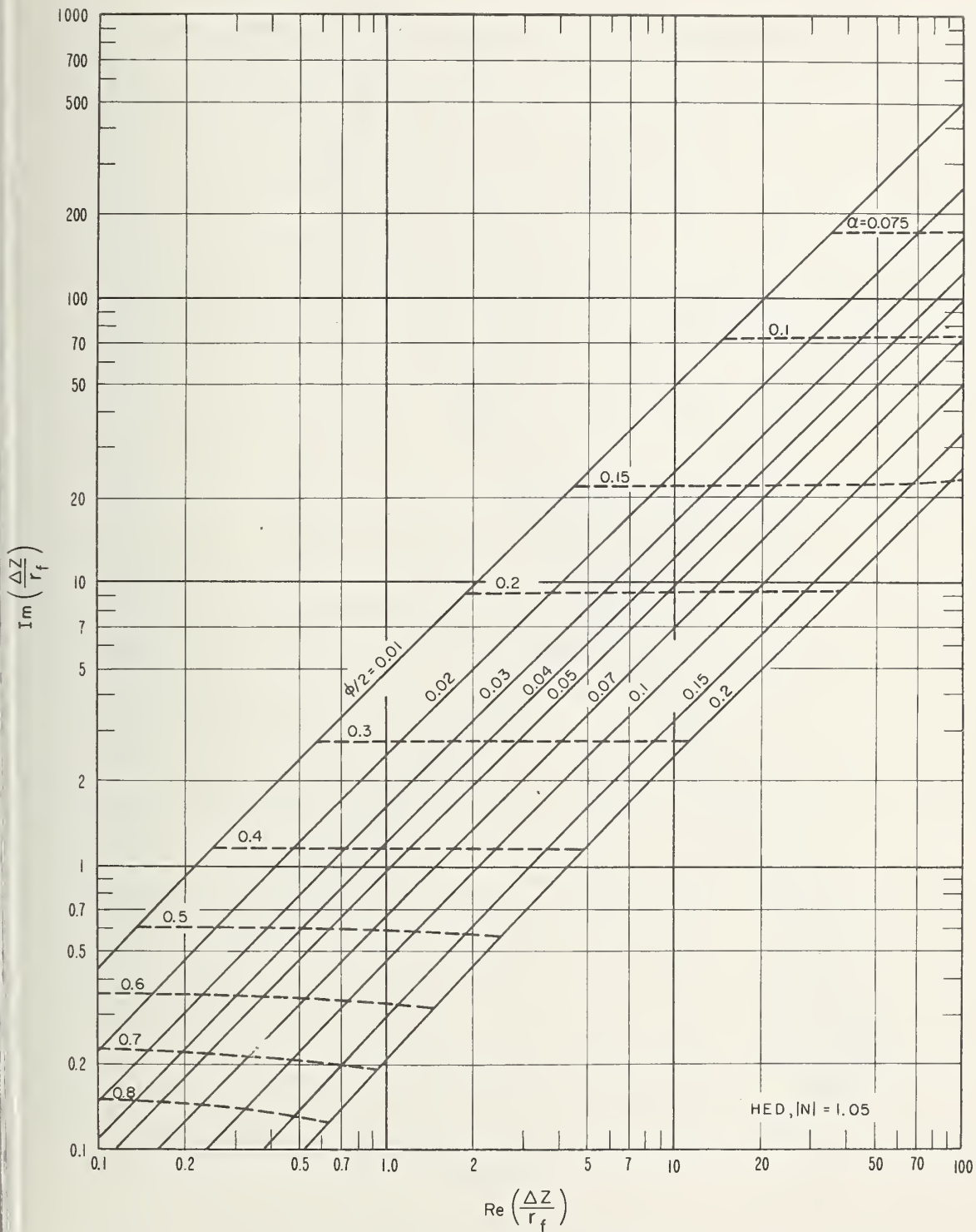


Figure A-39. Normalized input impedance change for HED,  
 $|N| = 1.05$ .

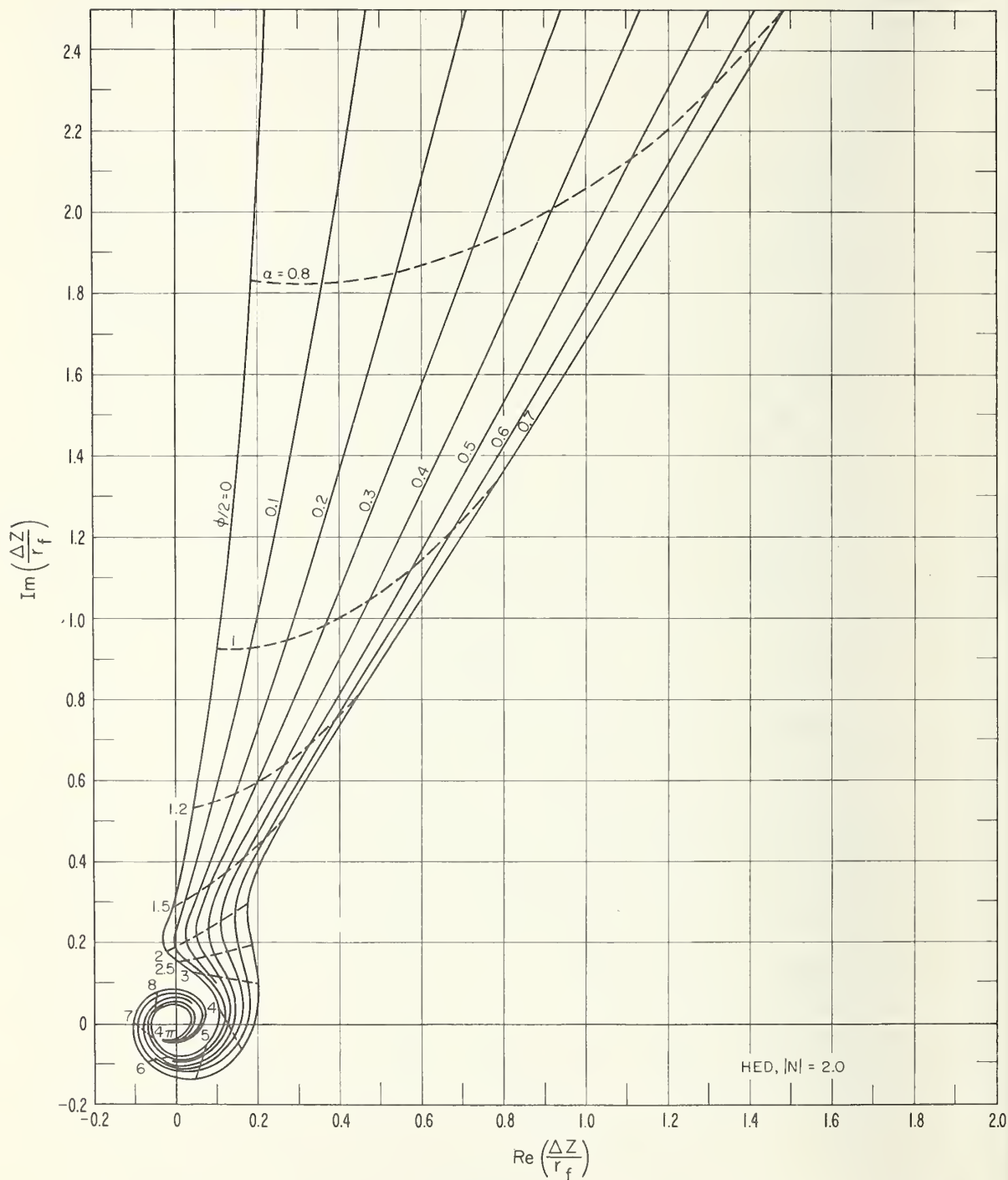


Figure A-40. Normalized input impedance change for HED,  
 $|N| = 2$ .

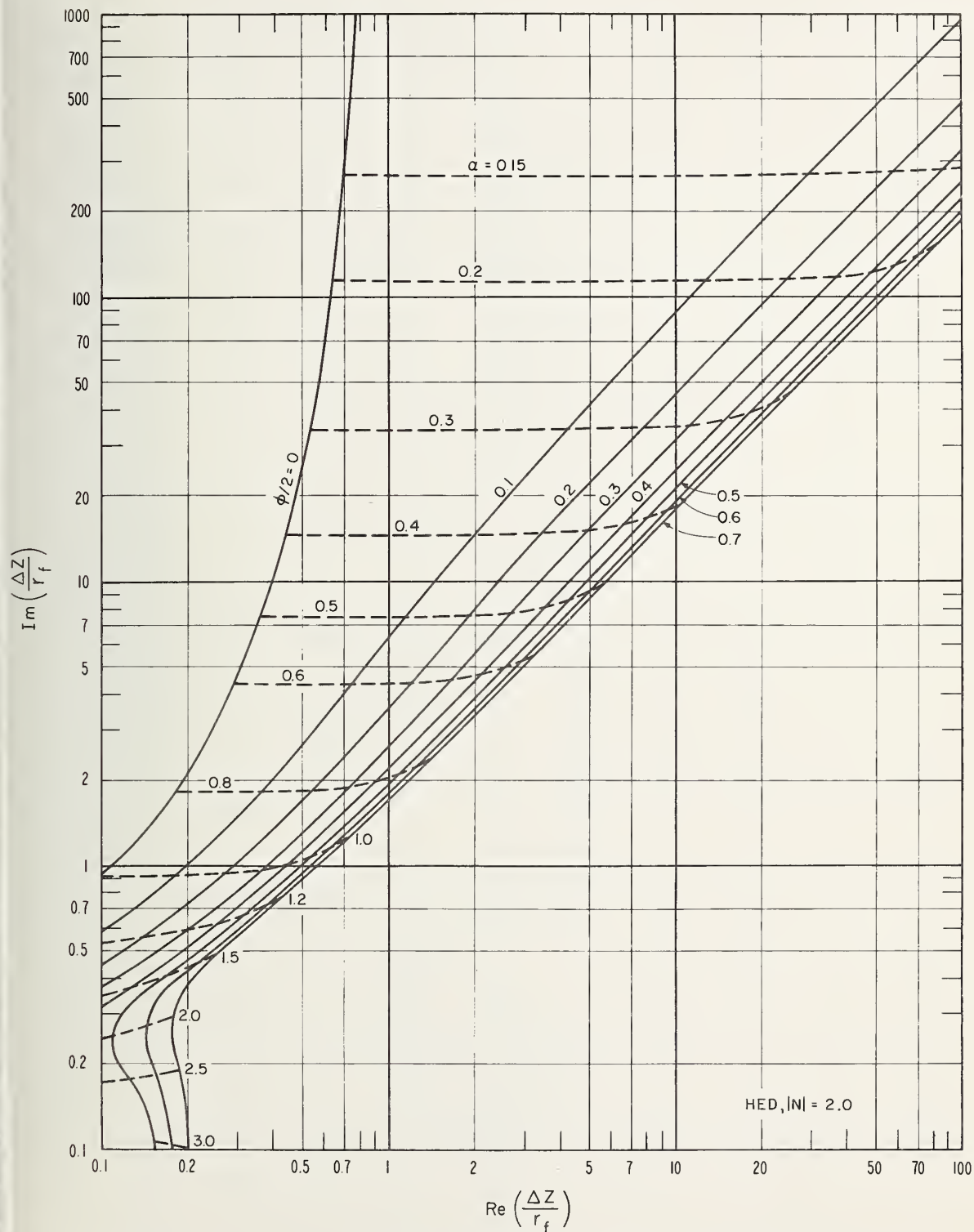


Figure A-41. Normalized input impedance change for HED,  
 $|N| = 2$ .



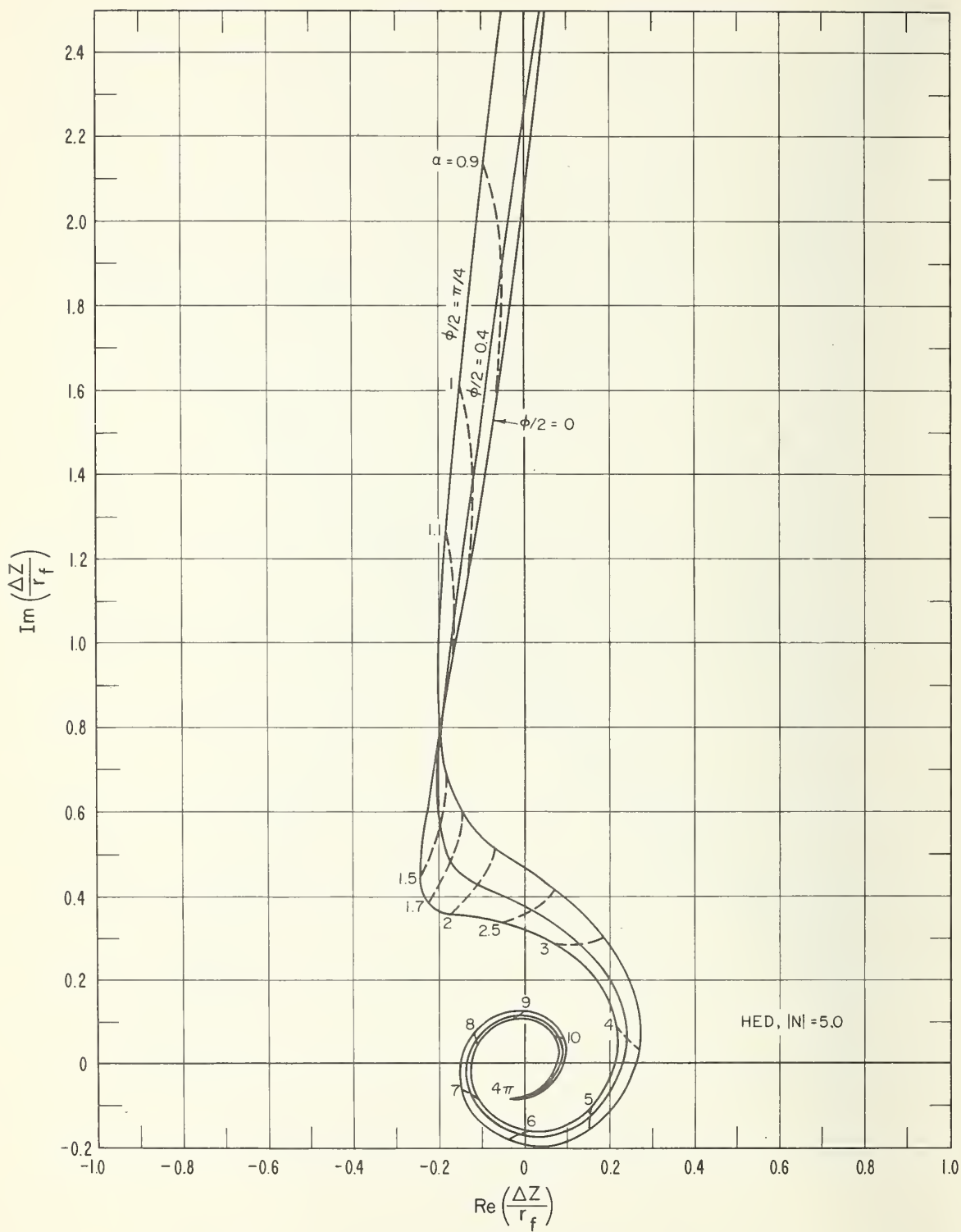


Figure A-42. Normalized input impedance change for HED,  
 $|N| = 5$ .

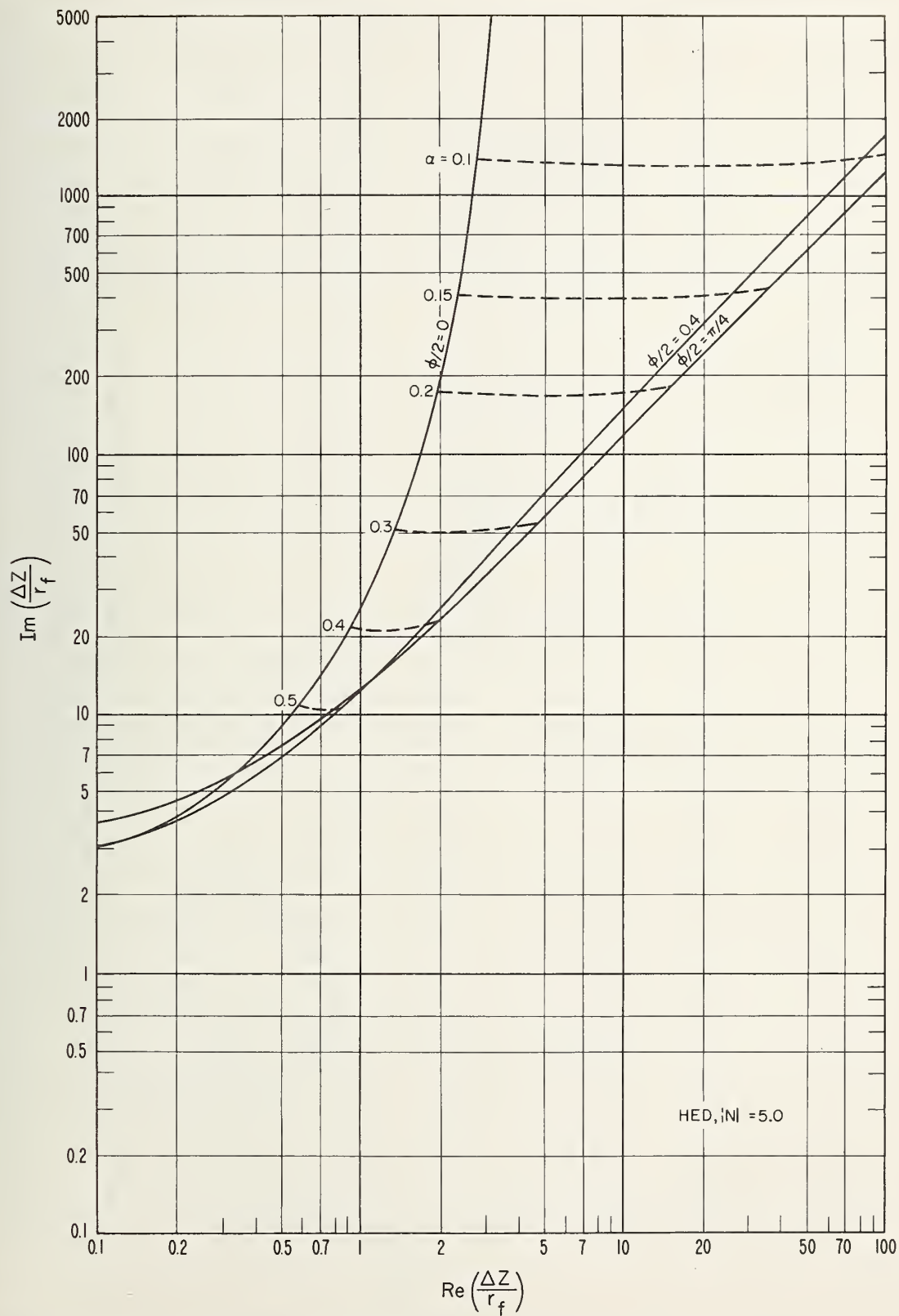


Figure A-43. Normalized input impedance change for HED,  $|N| = 5$ .

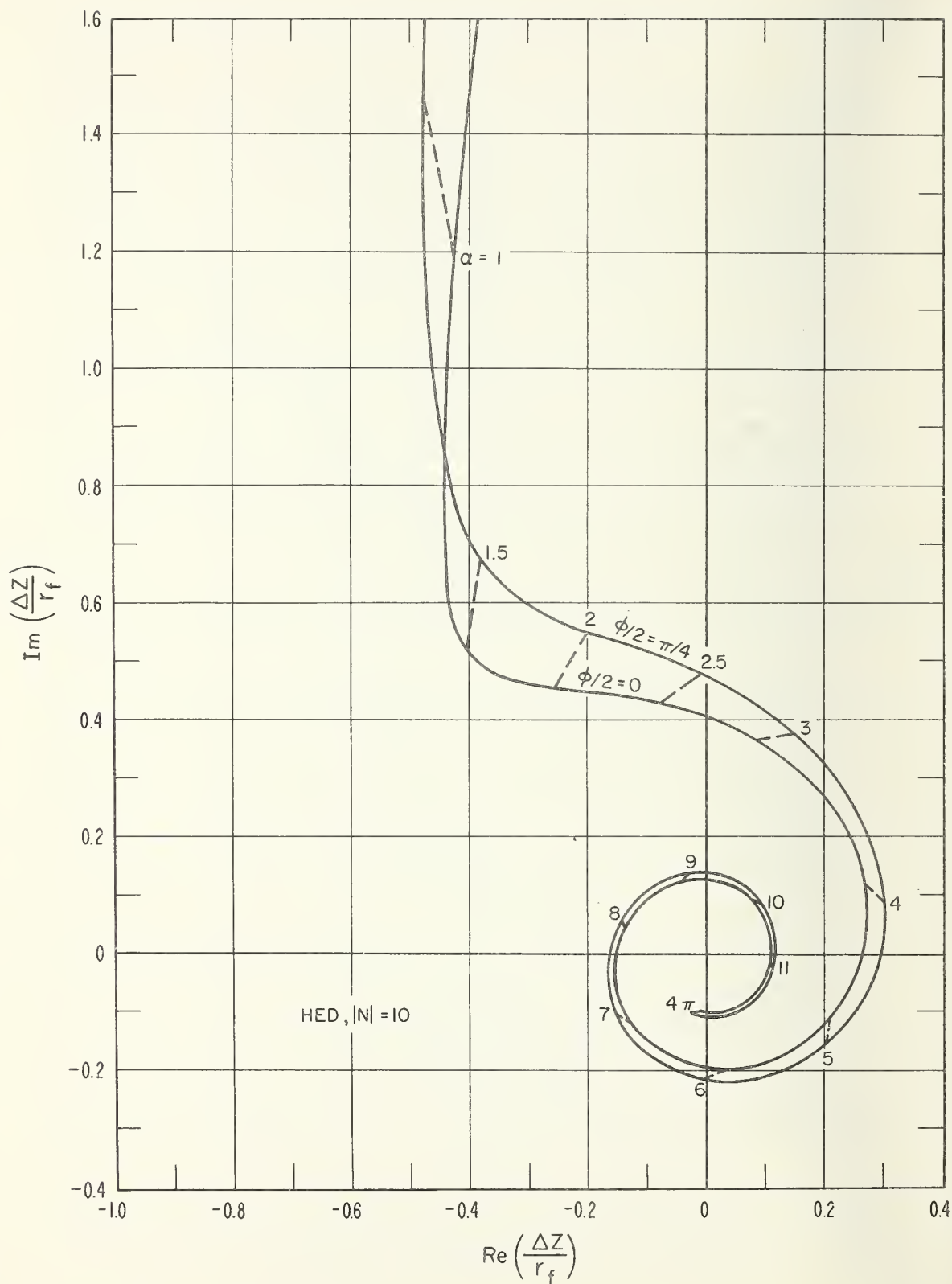


Figure A-44. Normalized input impedance change for HED,  $|N| = 10$ .

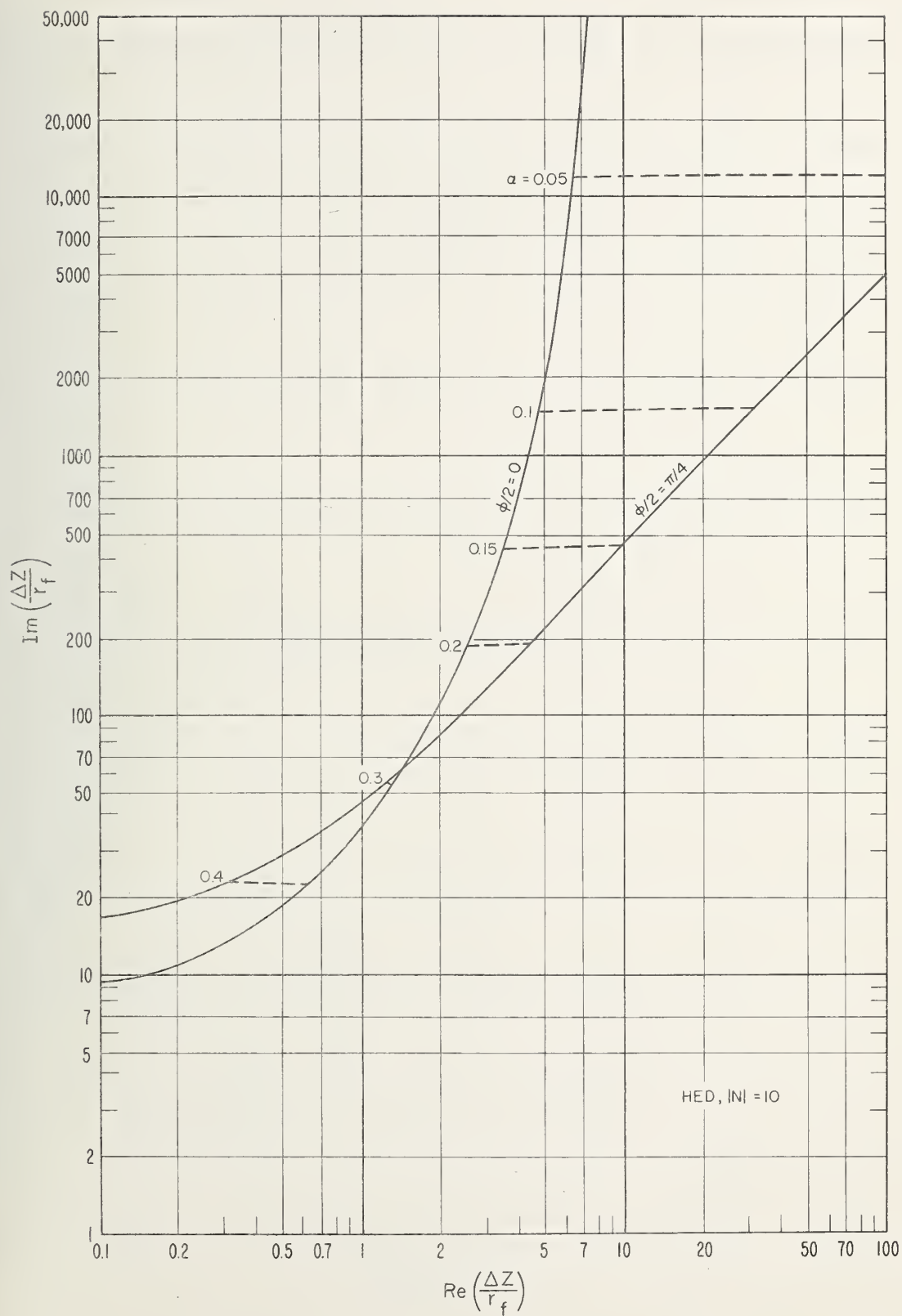


Figure A-45. Normalized input impedance change for HED,  $|N| = 10$ .

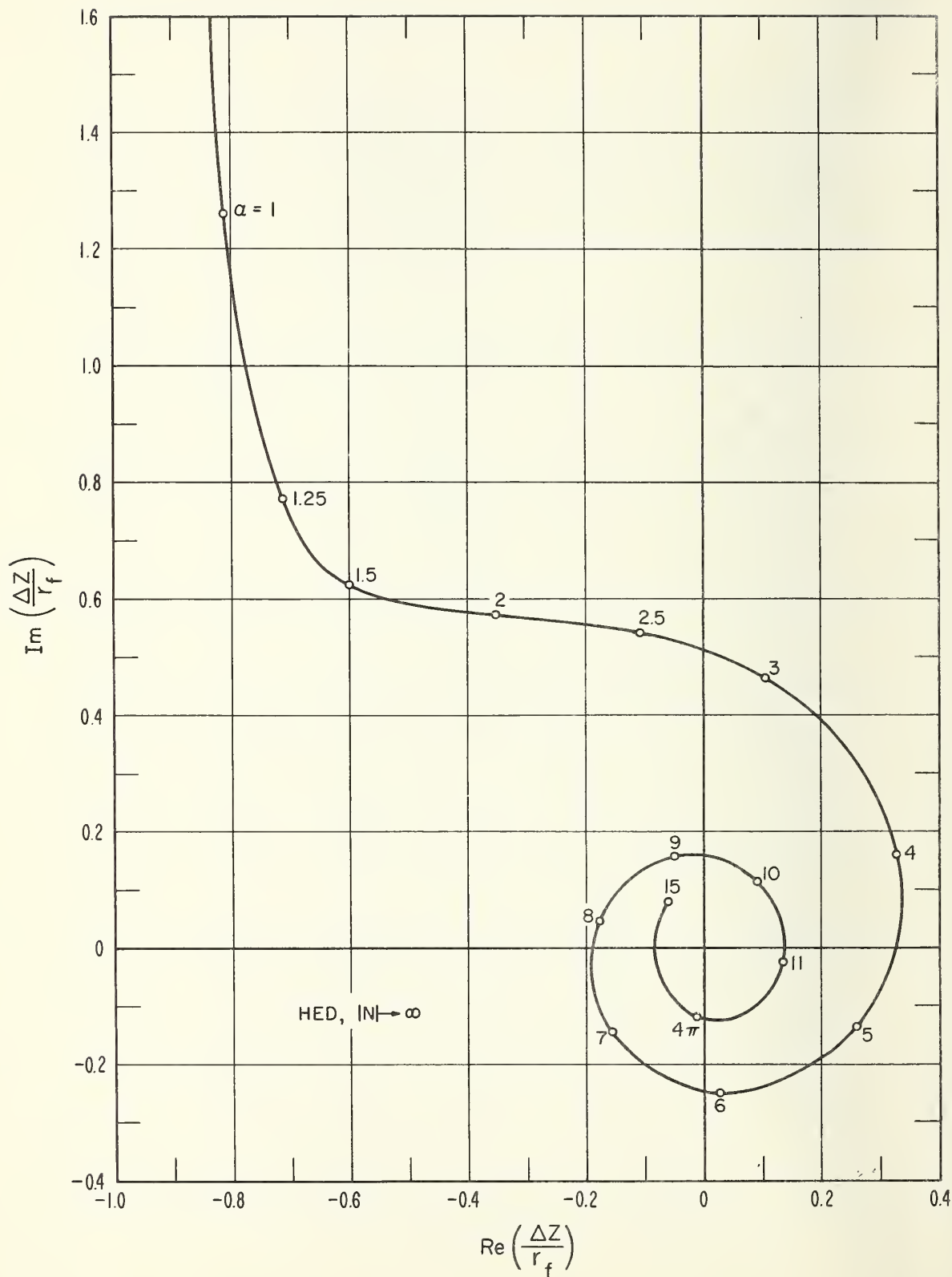


Figure A-46. Normalized input impedance change for HED,  $|N| \rightarrow \infty$ .





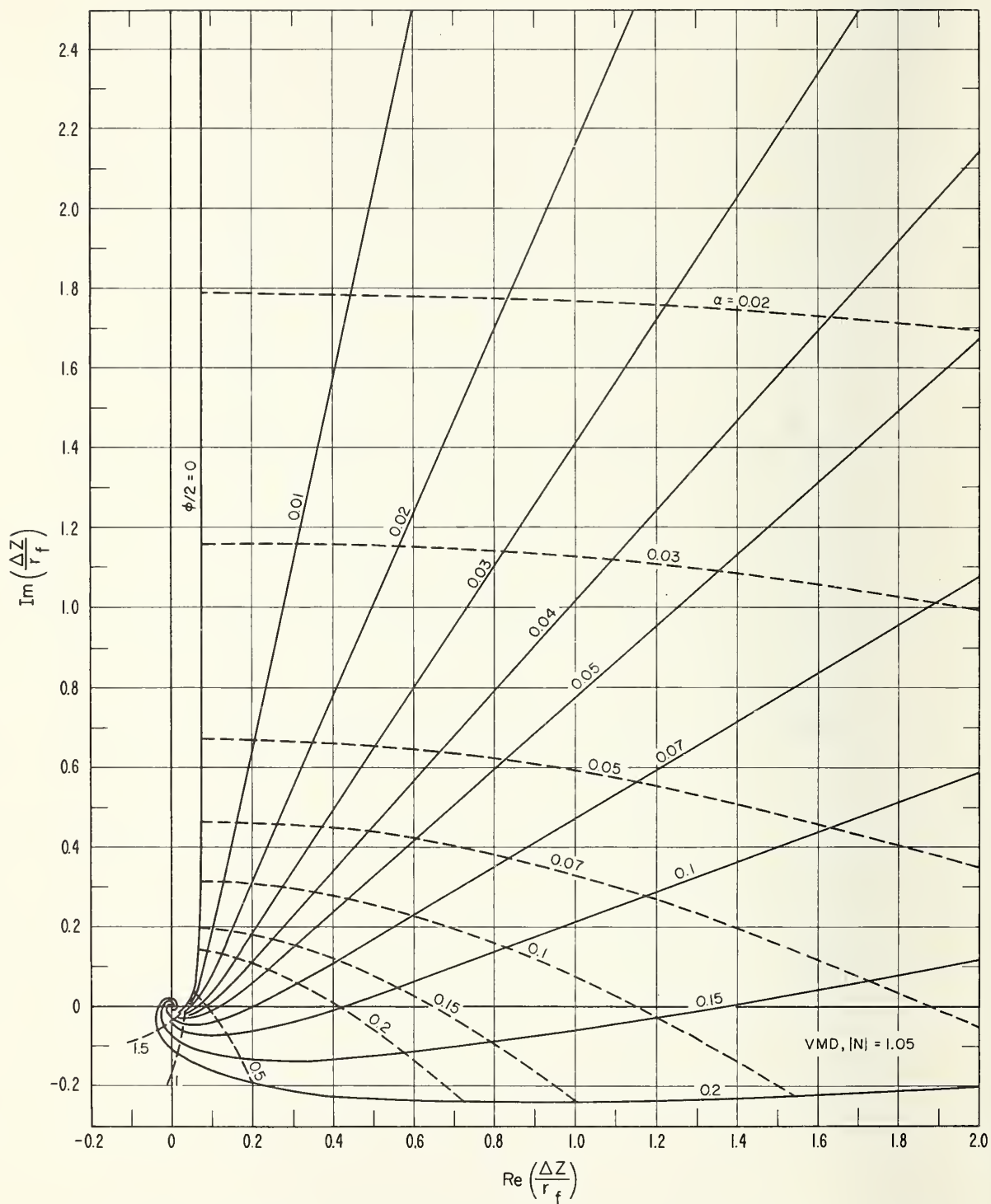


Figure A-47. Normalized input impedance change for VMD,  $|N| = 1.05$ .

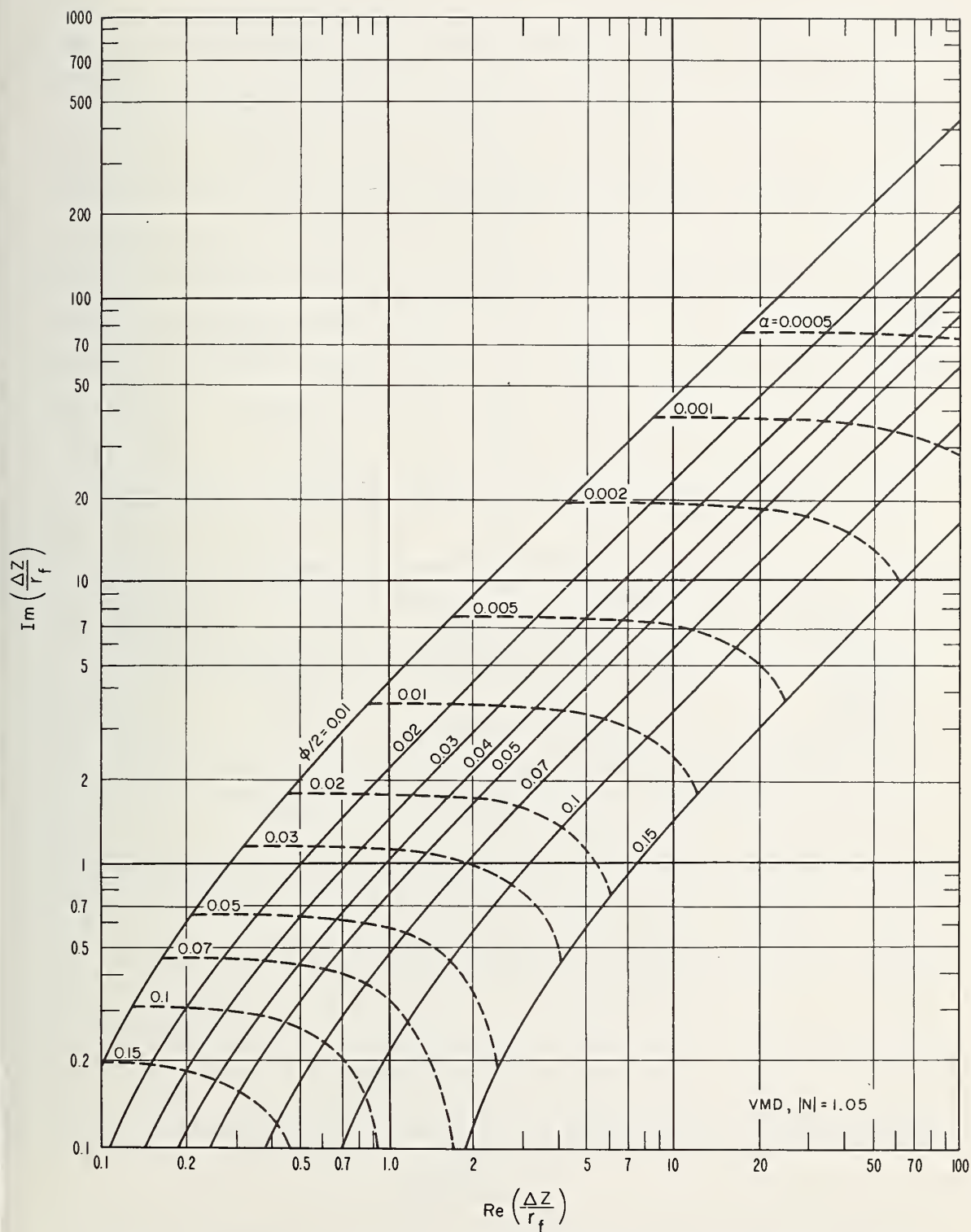


Figure A-48. Normalized input impedance change for VMD,  $|N| = 1.05$ .

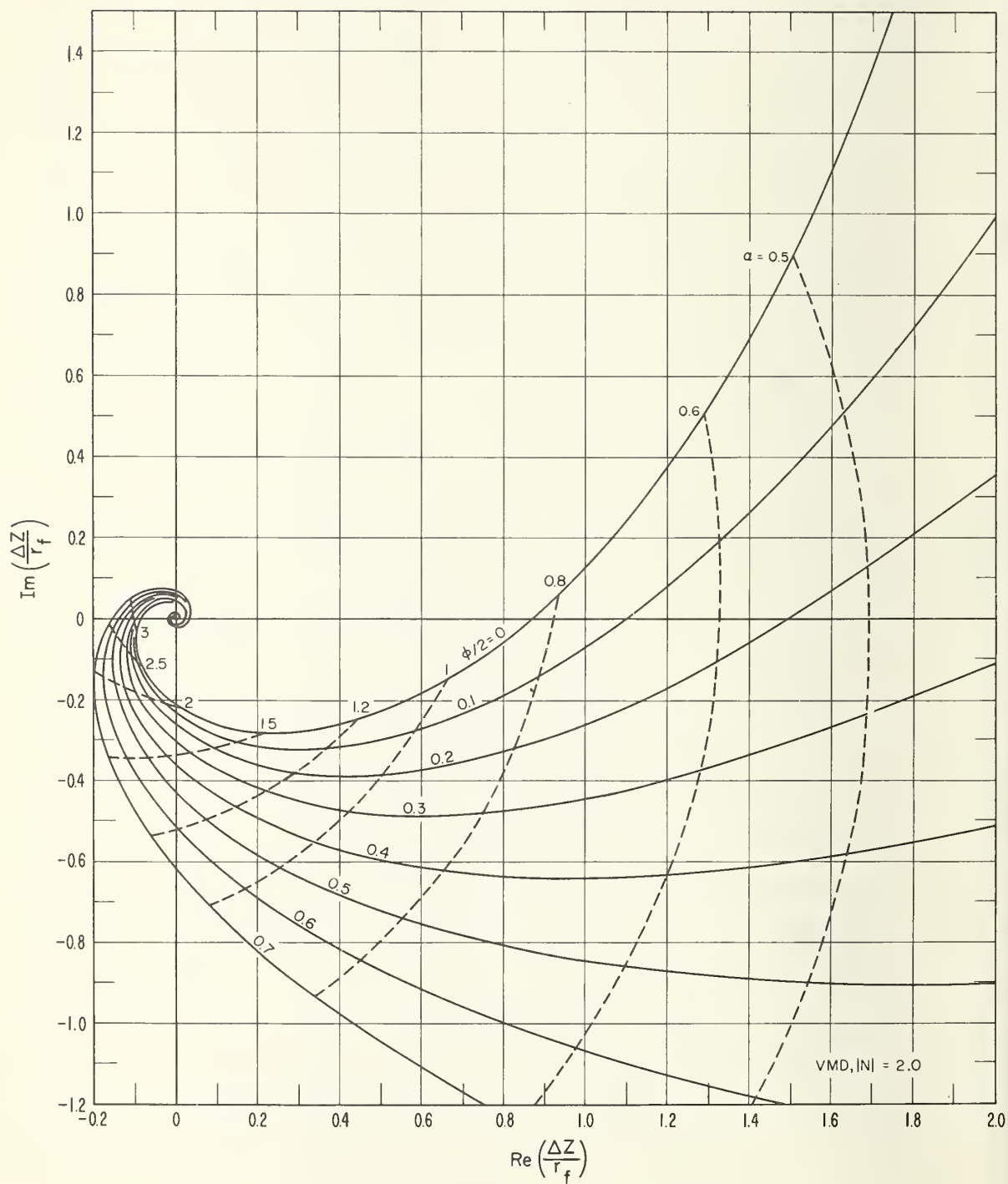


Figure A-49. Normalized input impedance change for VMD,  
 $|N| = 2$ .

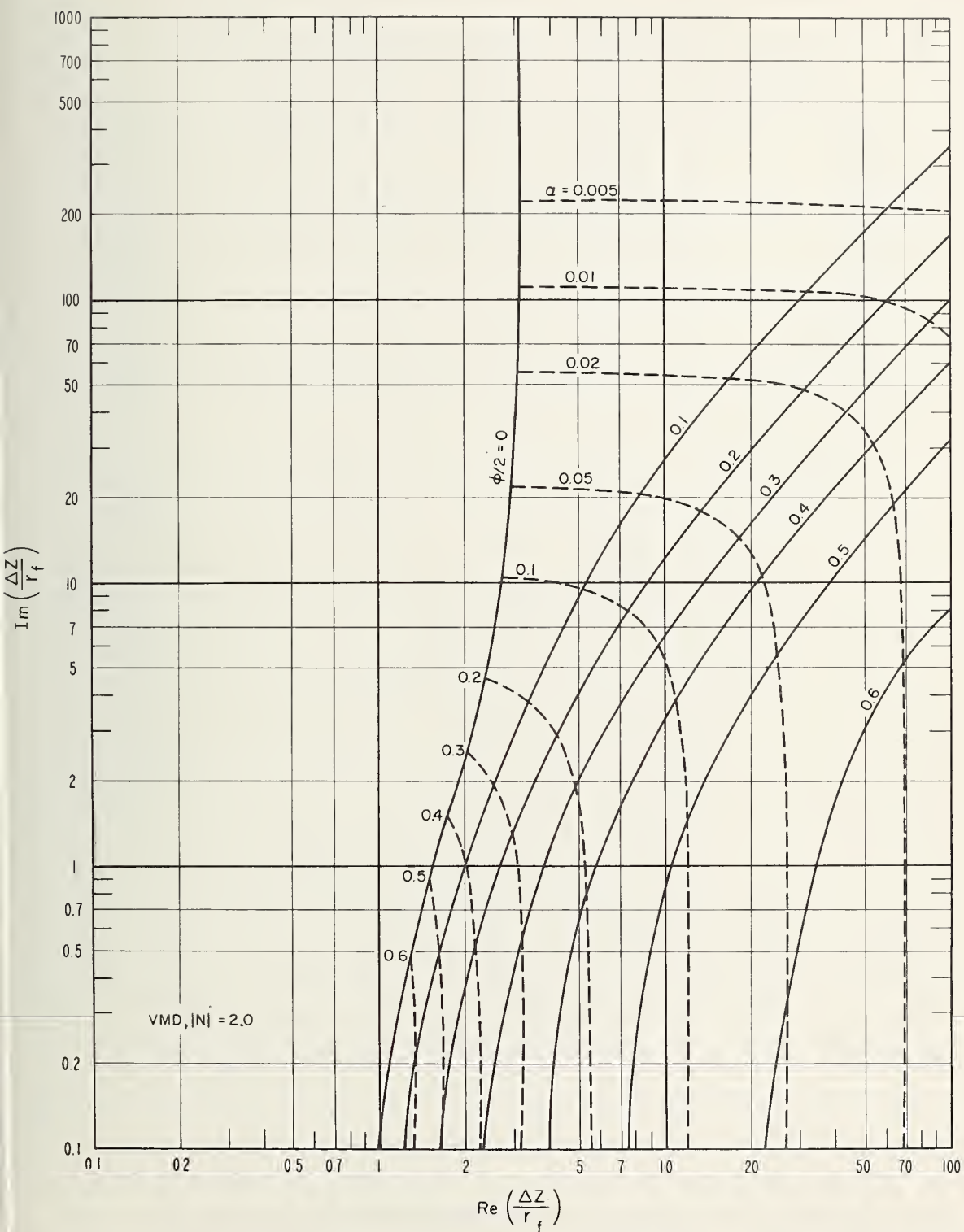


Figure A-50. Normalized input impedance change for VMD,  $|N| = 2$ .



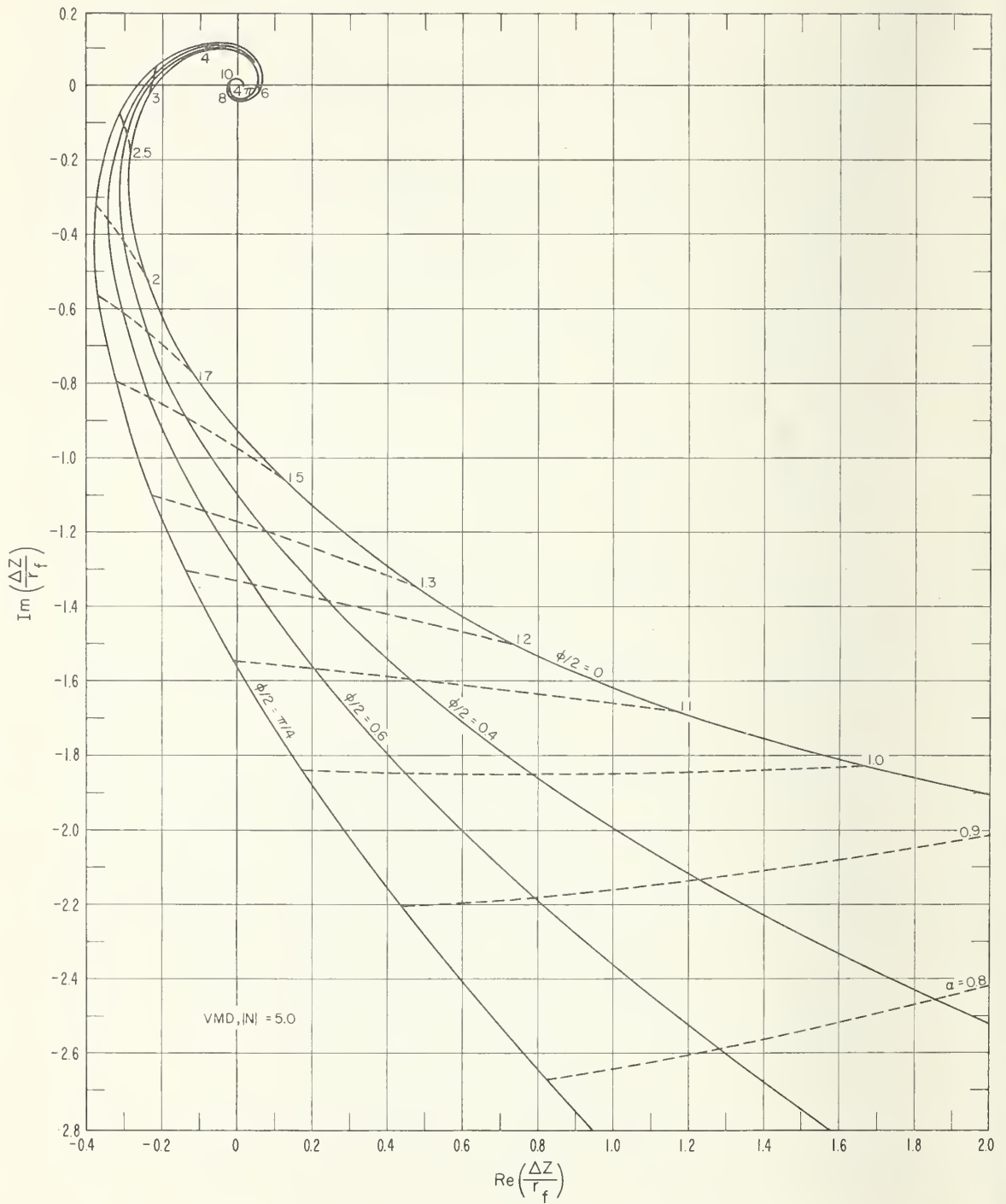


Figure A-51. Normalized input impedance change for VMD,  
 $|N| = 5$ .

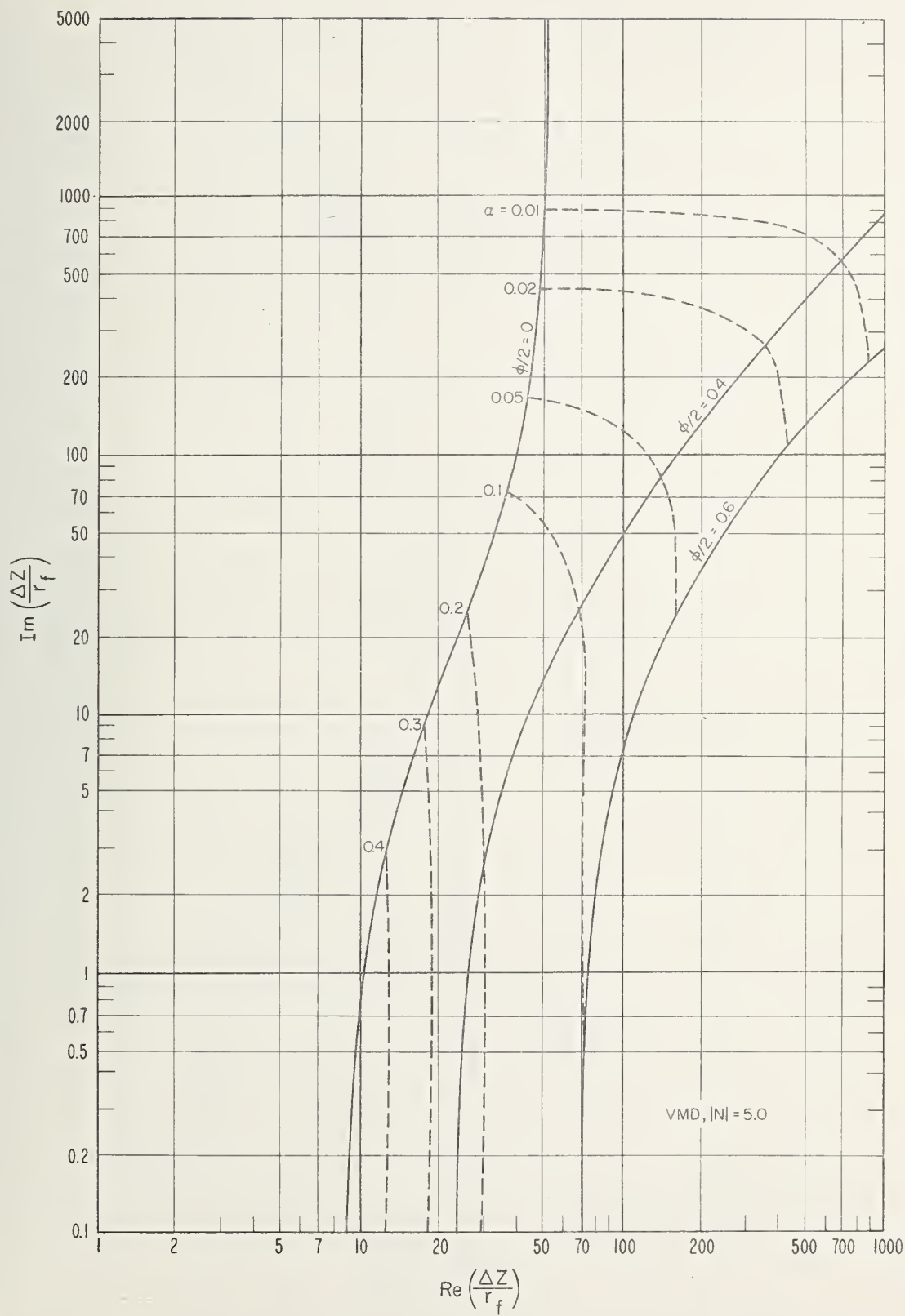


Figure A-52. Normalized input impedance change for VMD,  $|N| = 5$ .

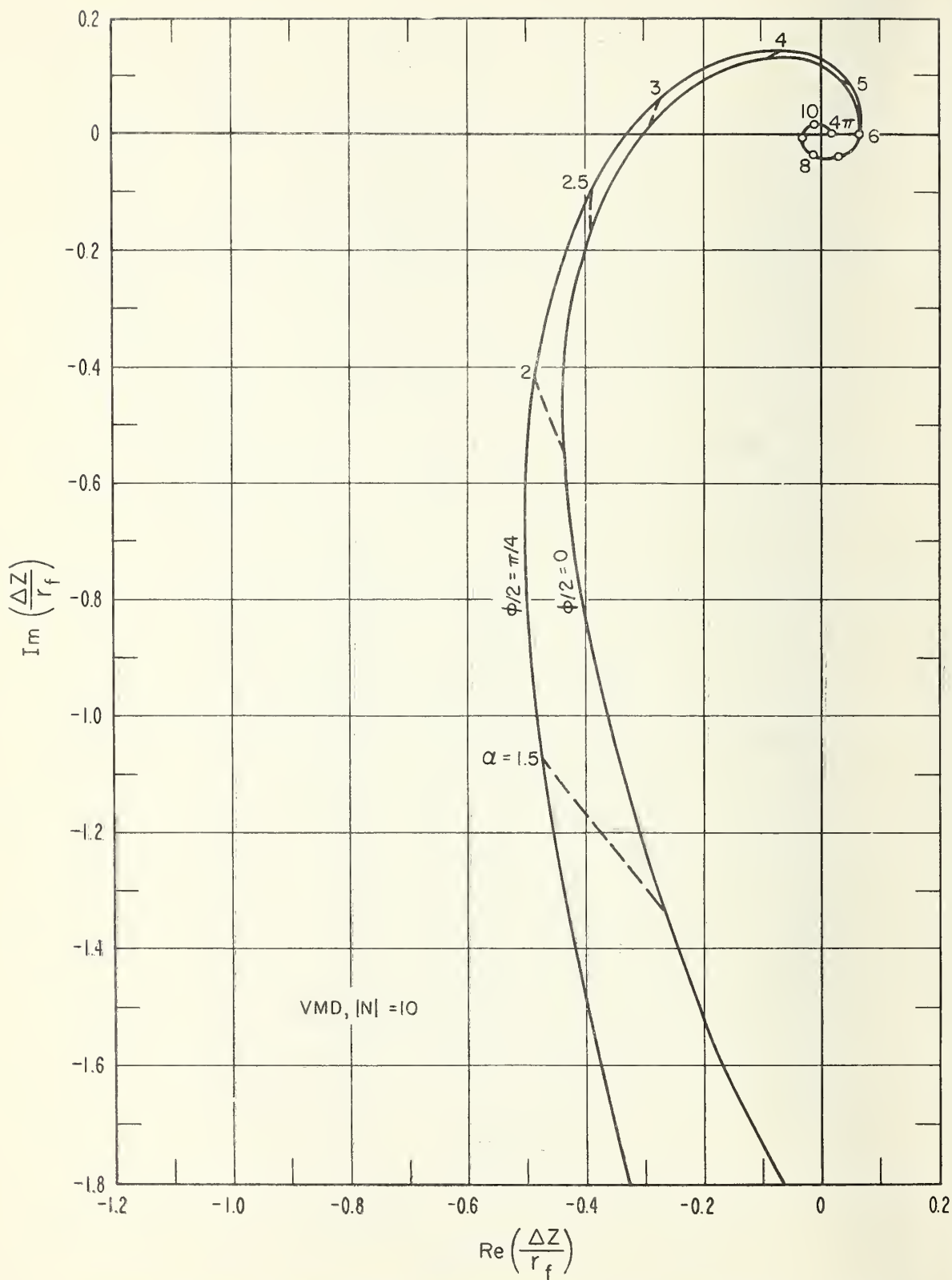


Figure A-53. Normalized input impedance change for VMD,  $|N| = 10$ .

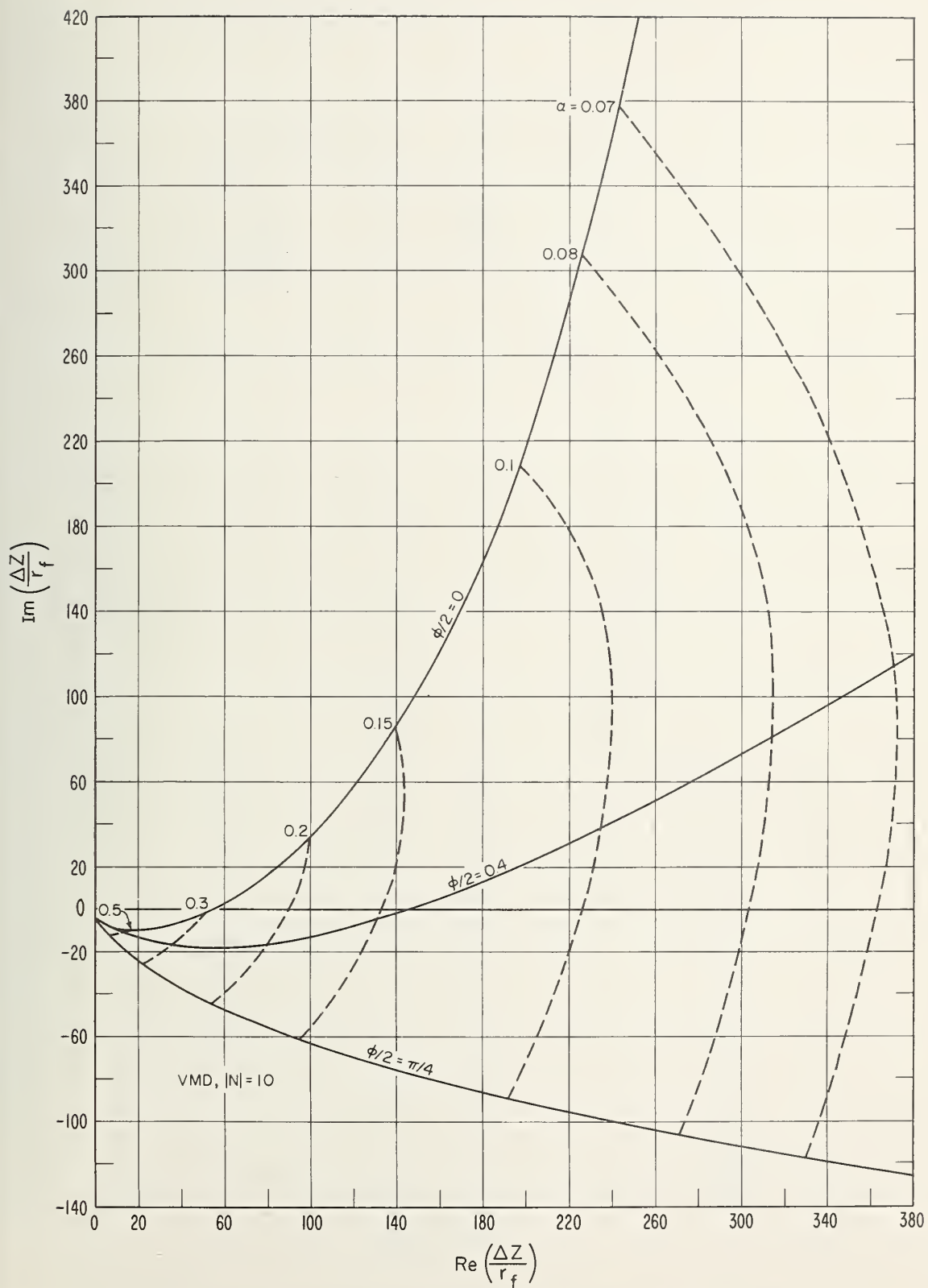
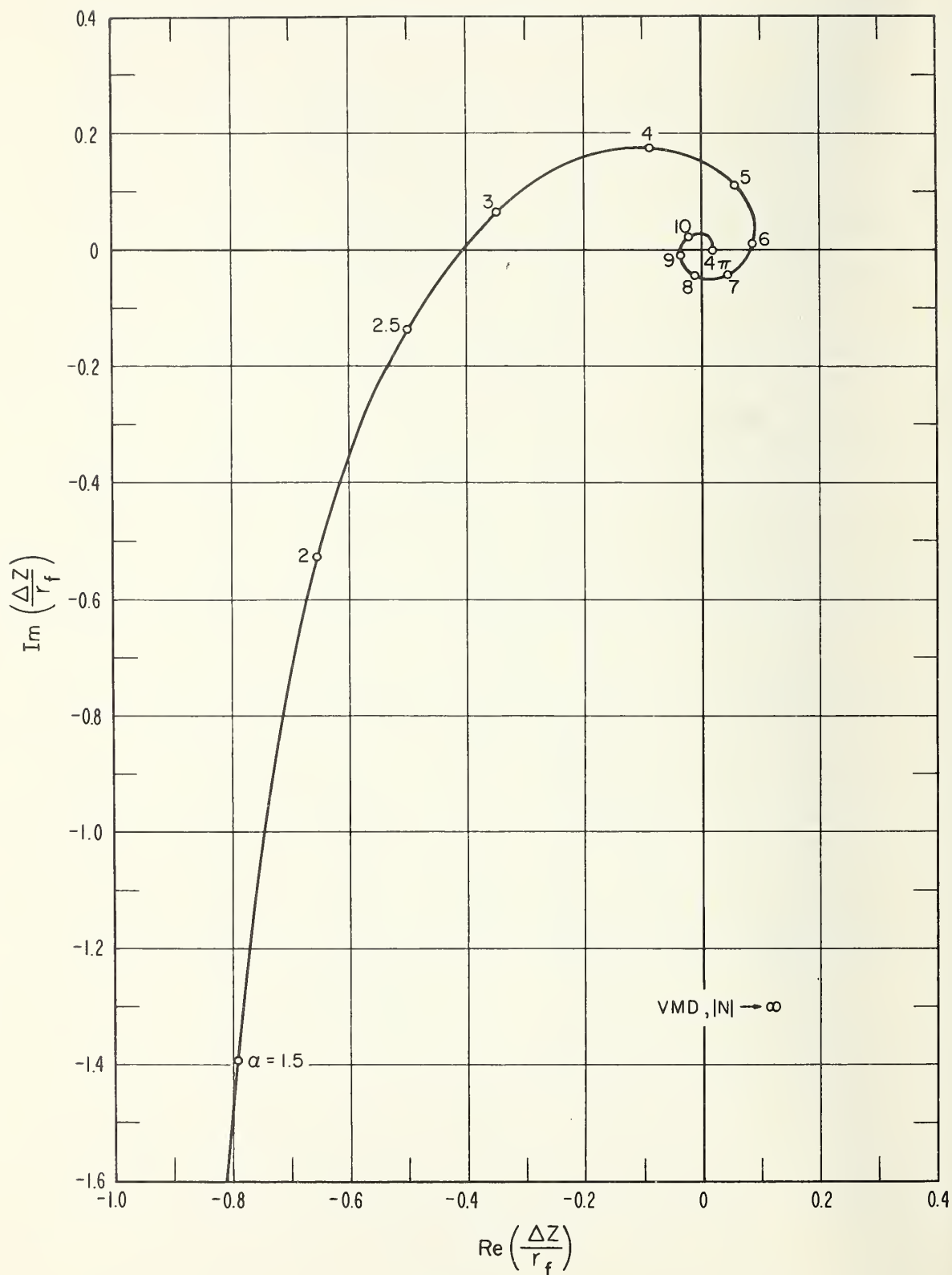


Figure A-54. Normalized input impedance change for VMD,  $|N| = 10$ .



Figure, A-55. Normalized input impedance change for VMD,  $|N| \rightarrow \infty$ .





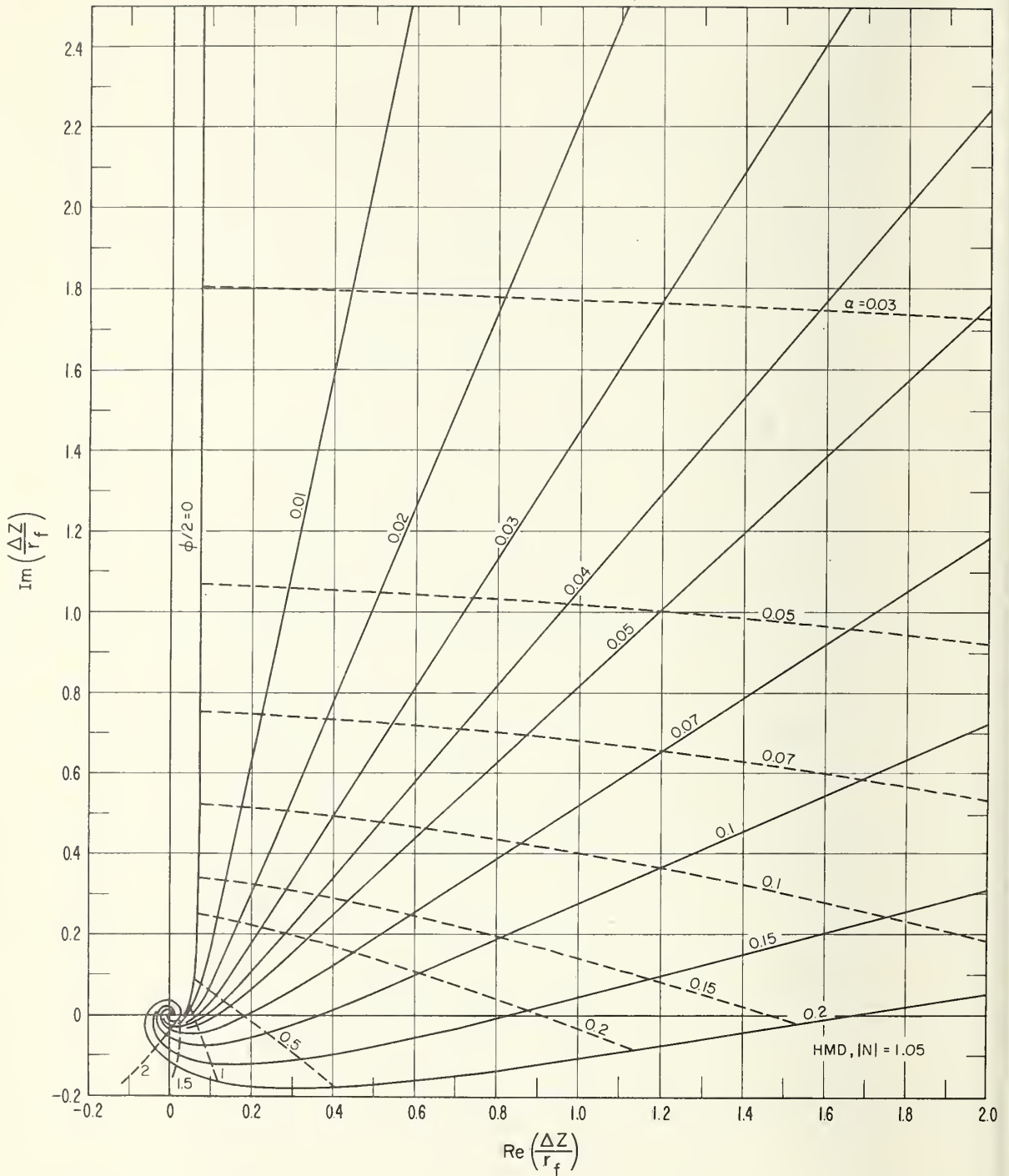


Figure A-56. Normalized input impedance change for HMD,  $|N| = 1.05$ .

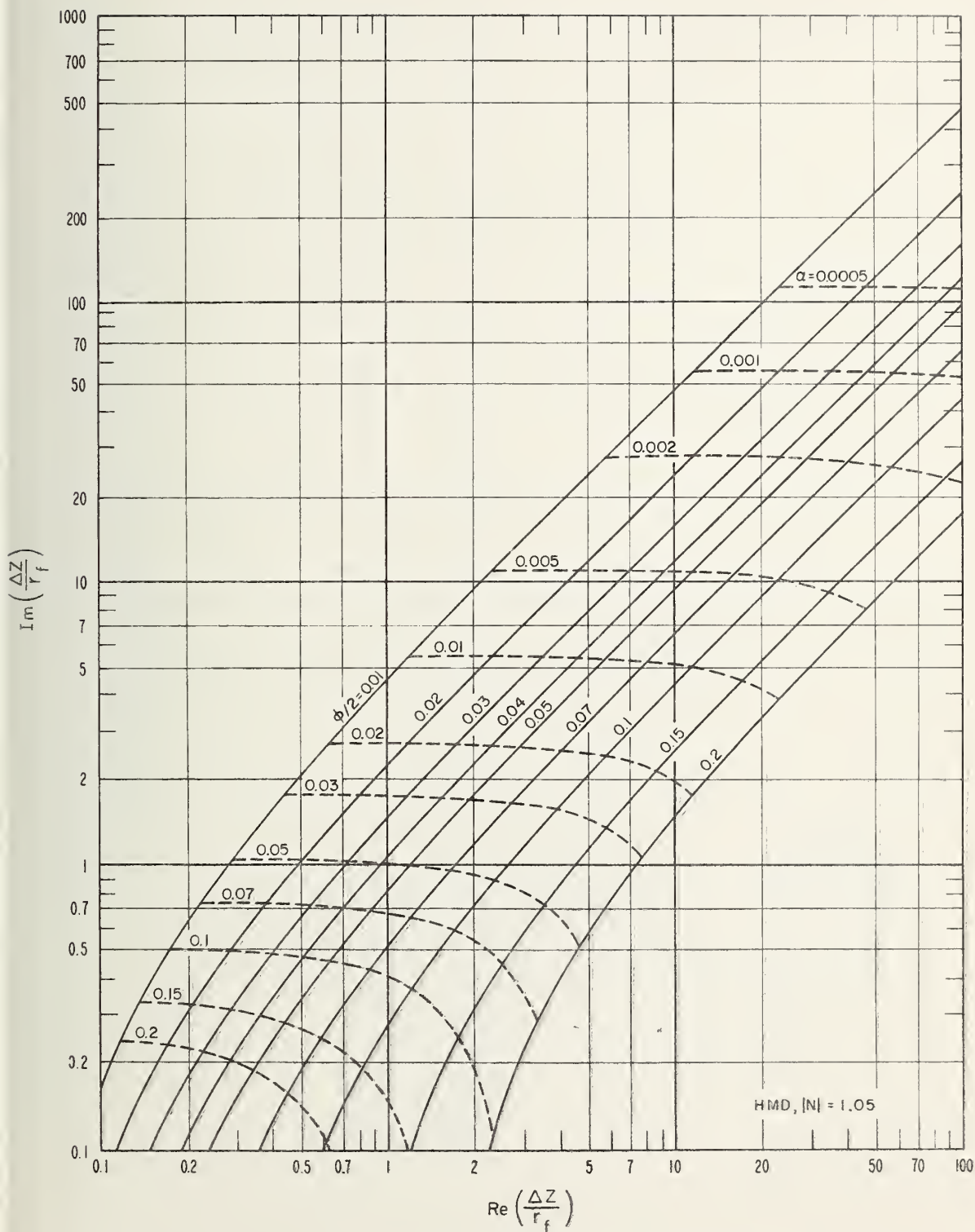


Figure A-57. Normalized input impedance change for HMD,  $|N| = 1.05$ .

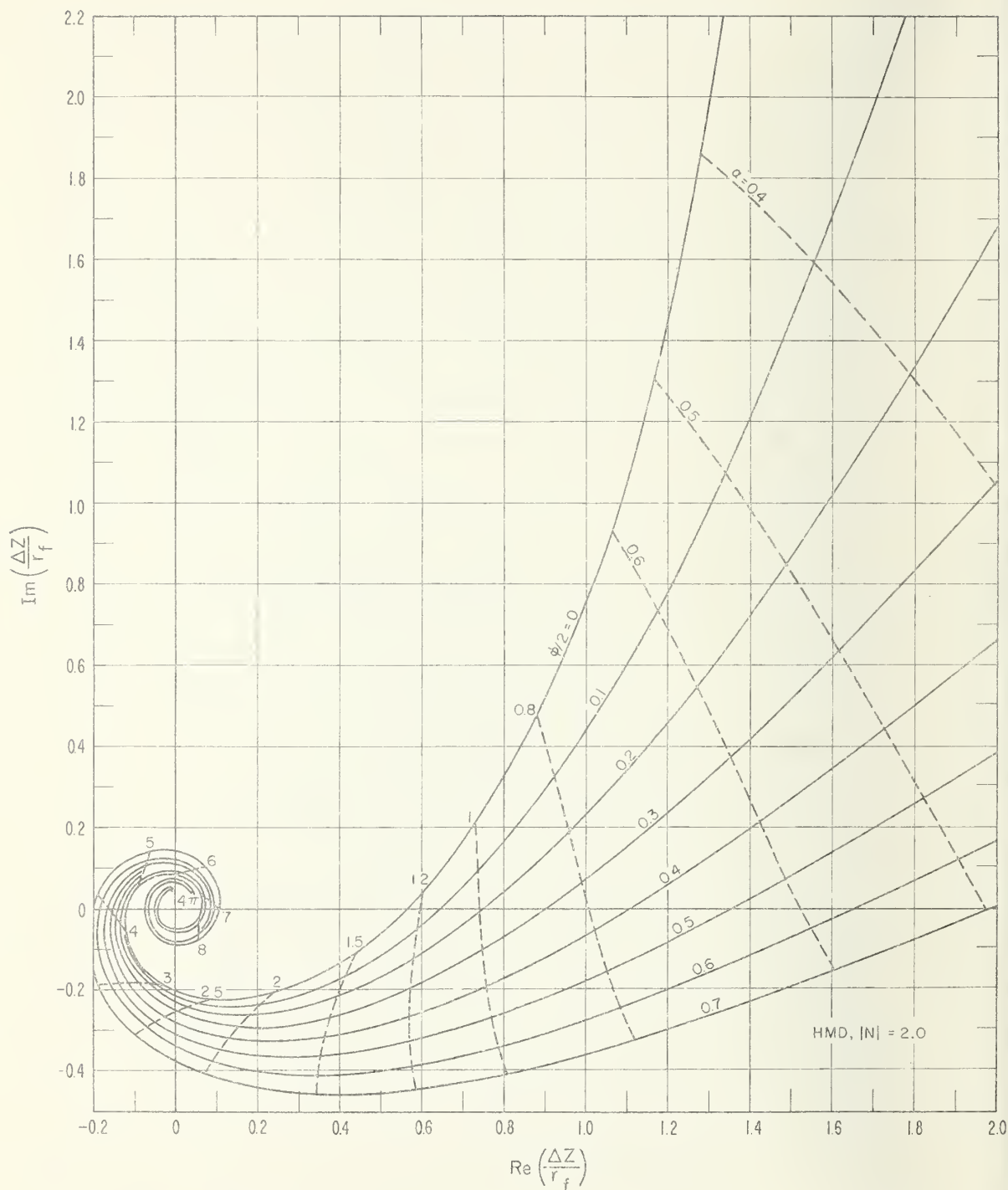


Figure A-58. Normalized input impedance change for HMD,  
 $|N| = 2.0$ .

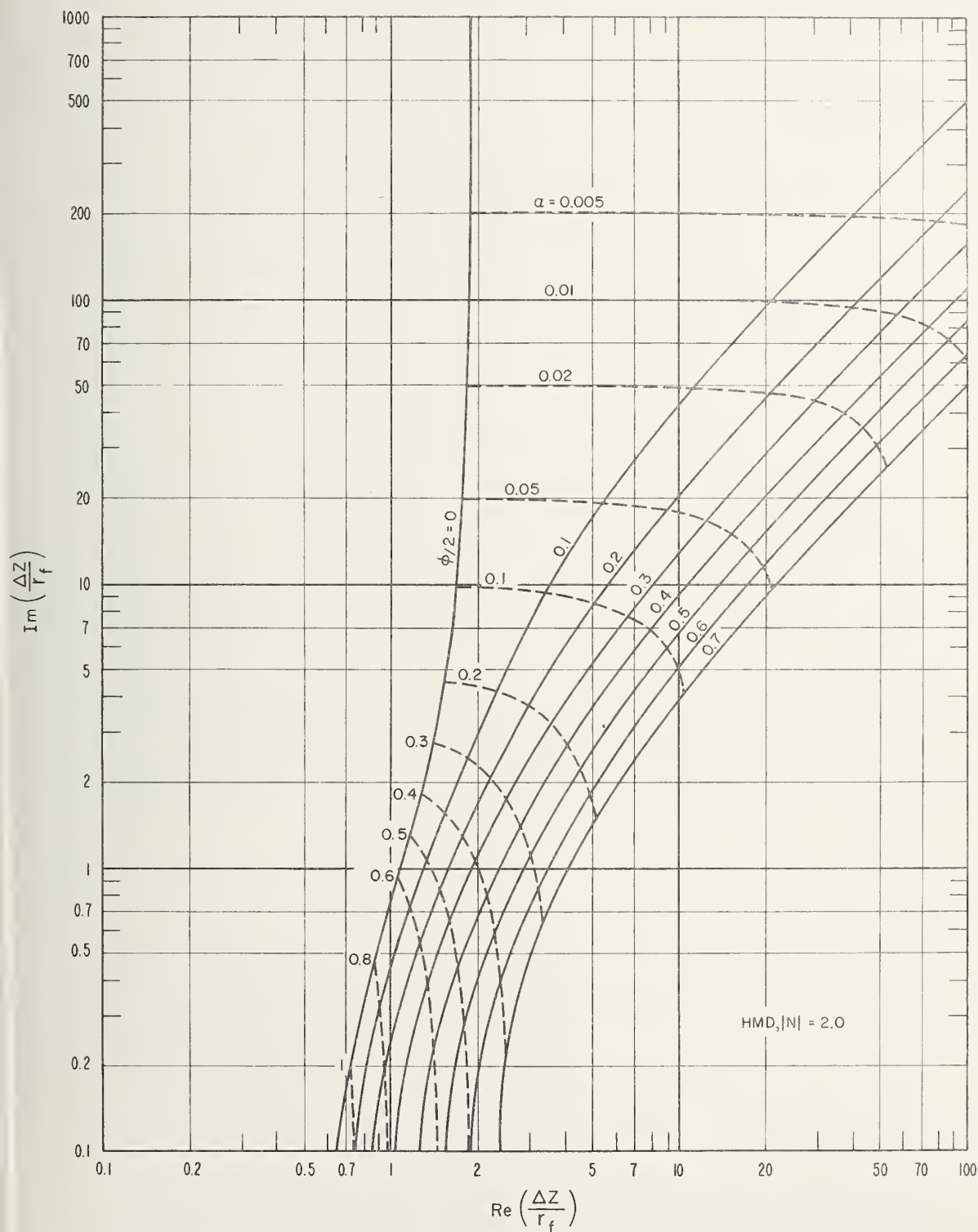


Figure A-59. Normalized input impedance change for HMD,  $|N| = 2$ .



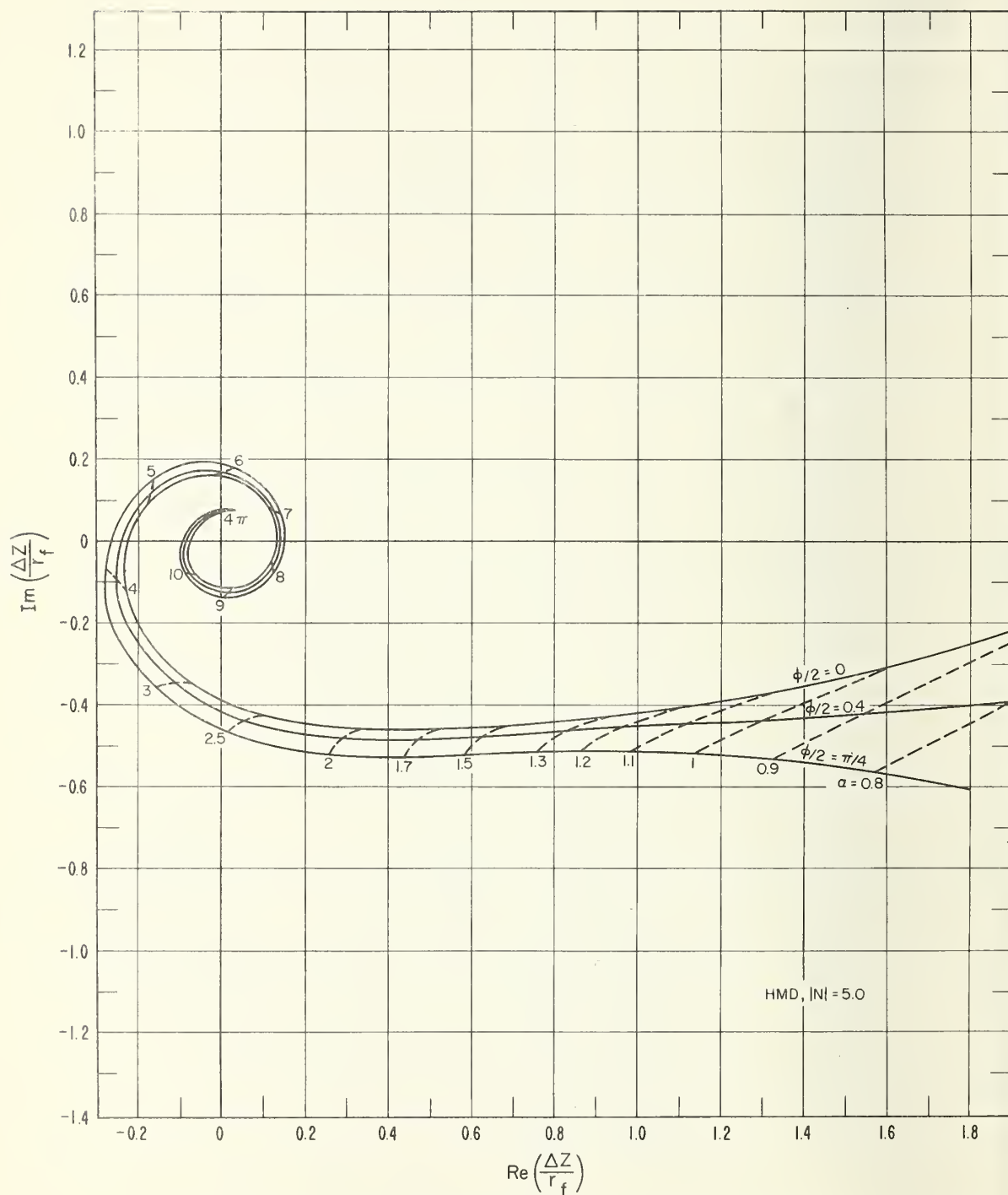


Figure A-60. Normalized input impedance change for HMD,  
 $|N| = 5$ .

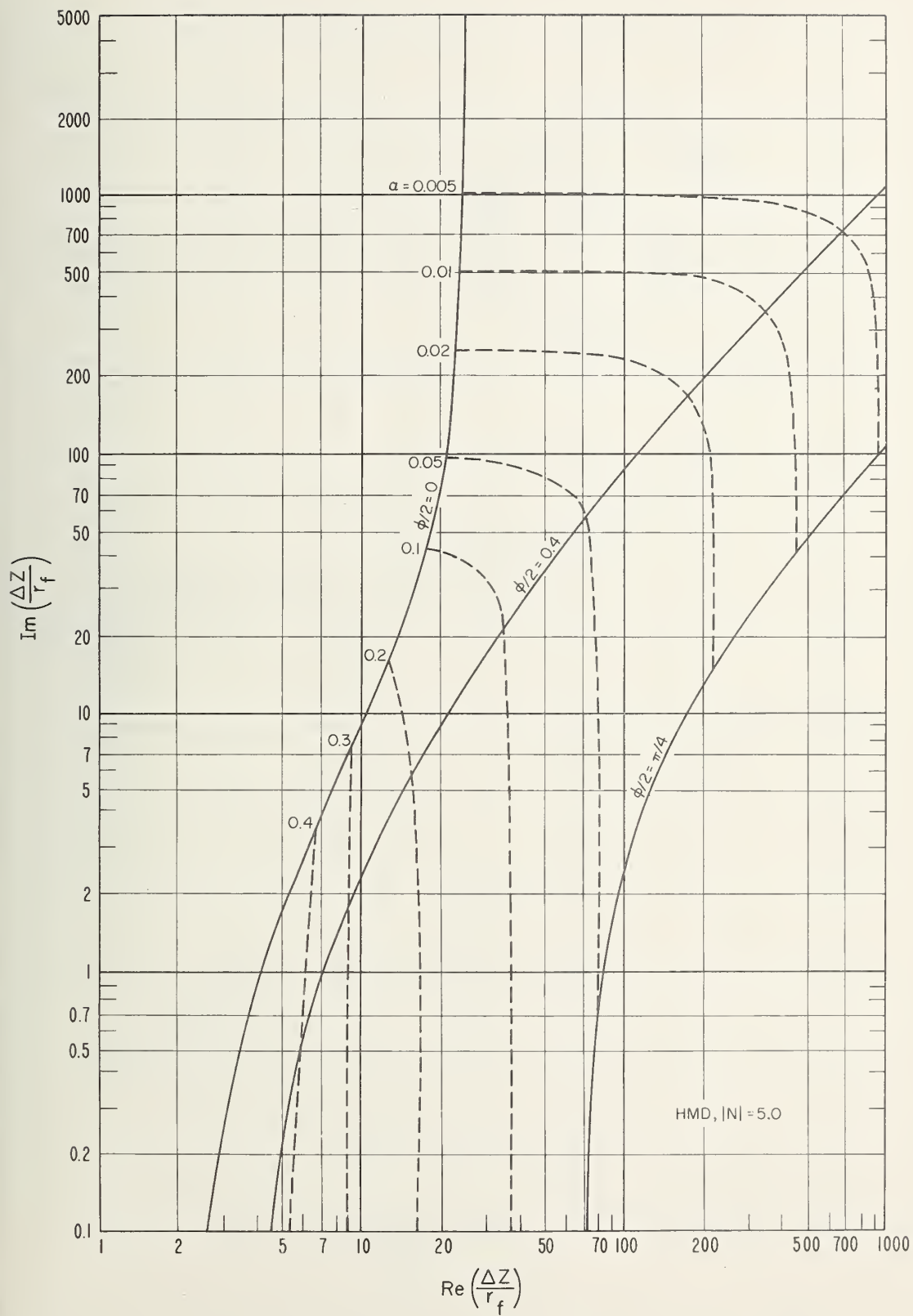


Figure A-61. Normalized input impedance change for HMD,  $|N| = 5$ .

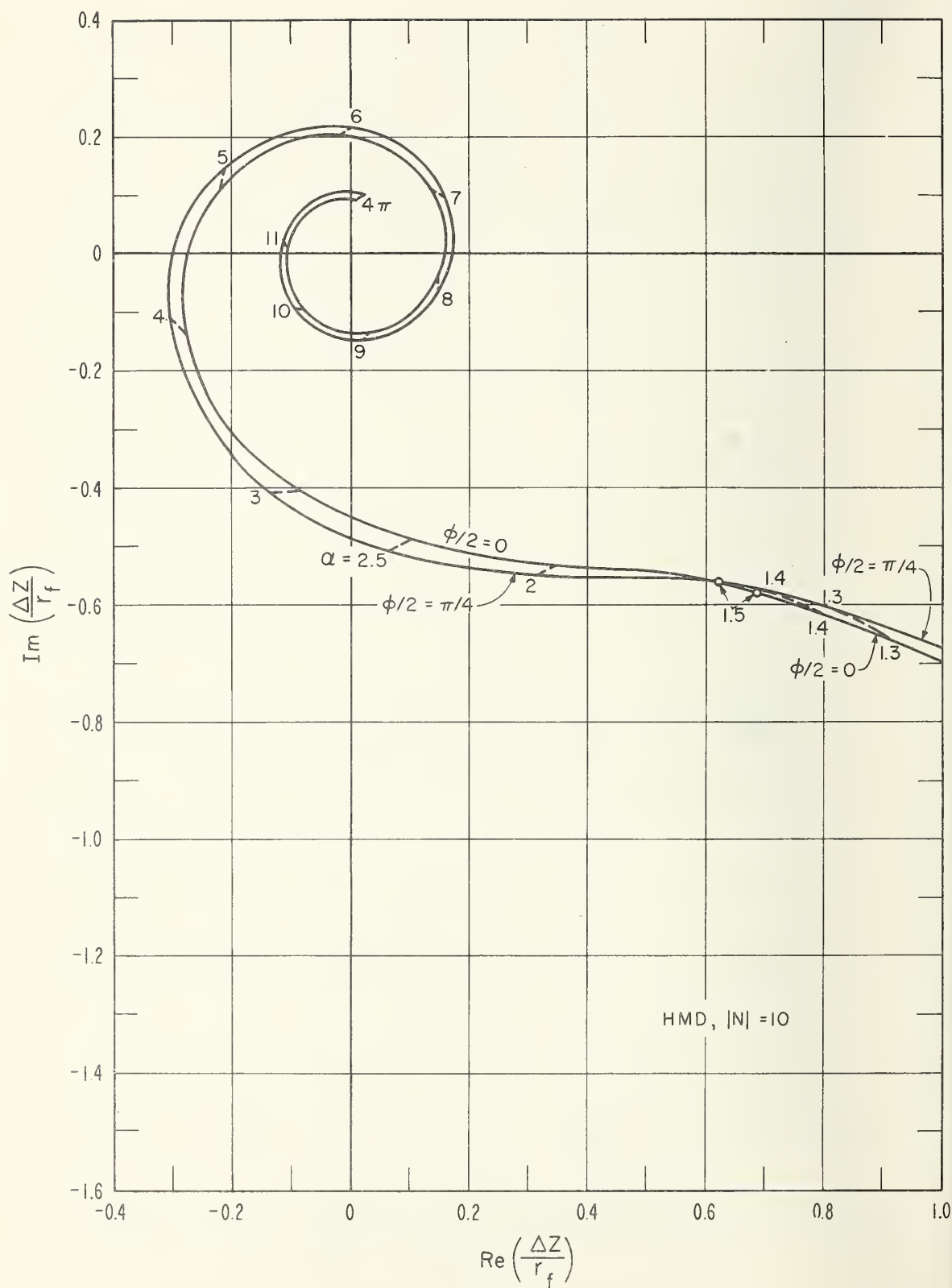


Figure A-62. Normalized input impedance change for HMD,  $|N| = 10$ .

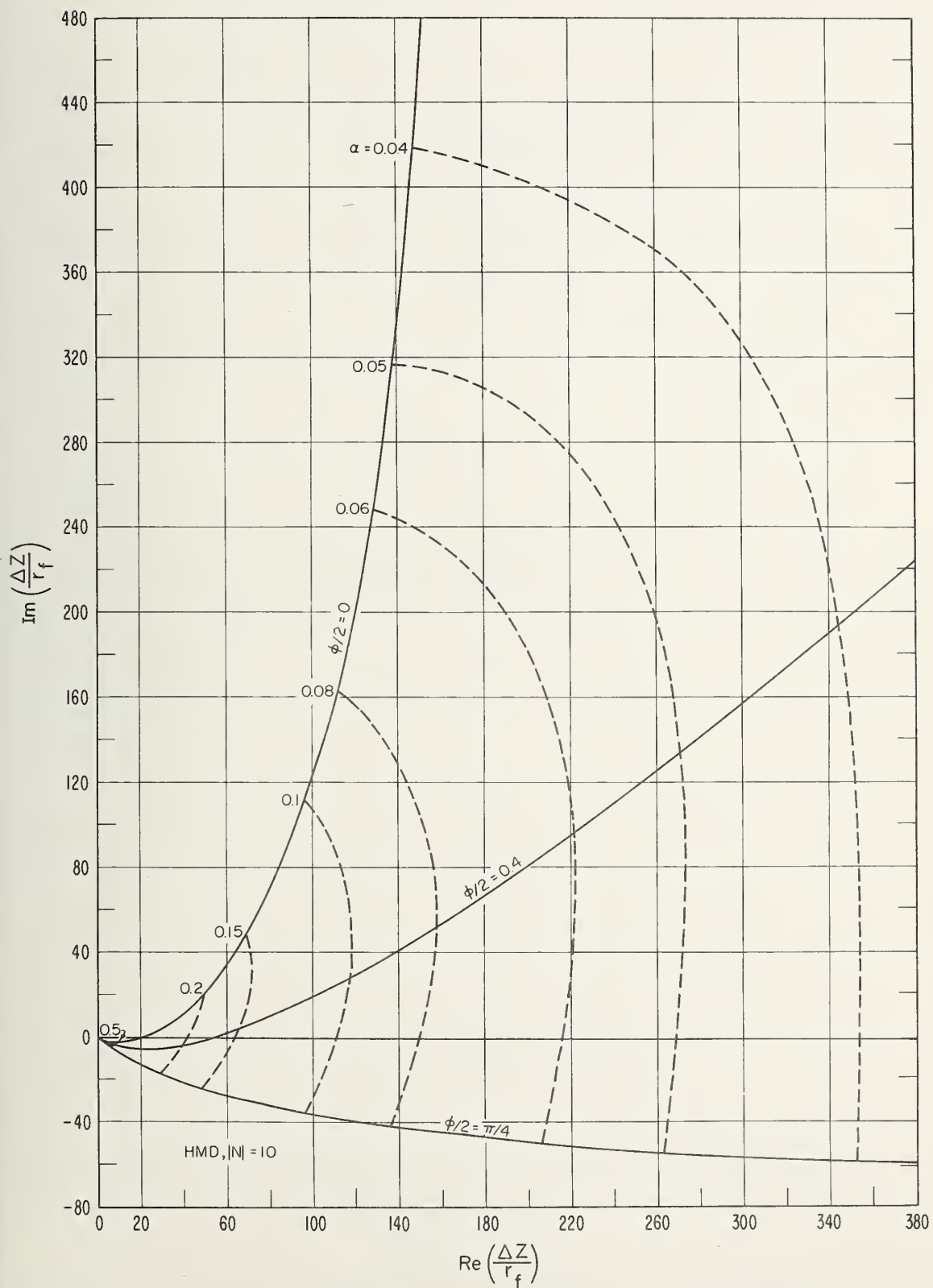


Figure A-63. Normalized input impedance change for HMD,  $|N| = 10$ .

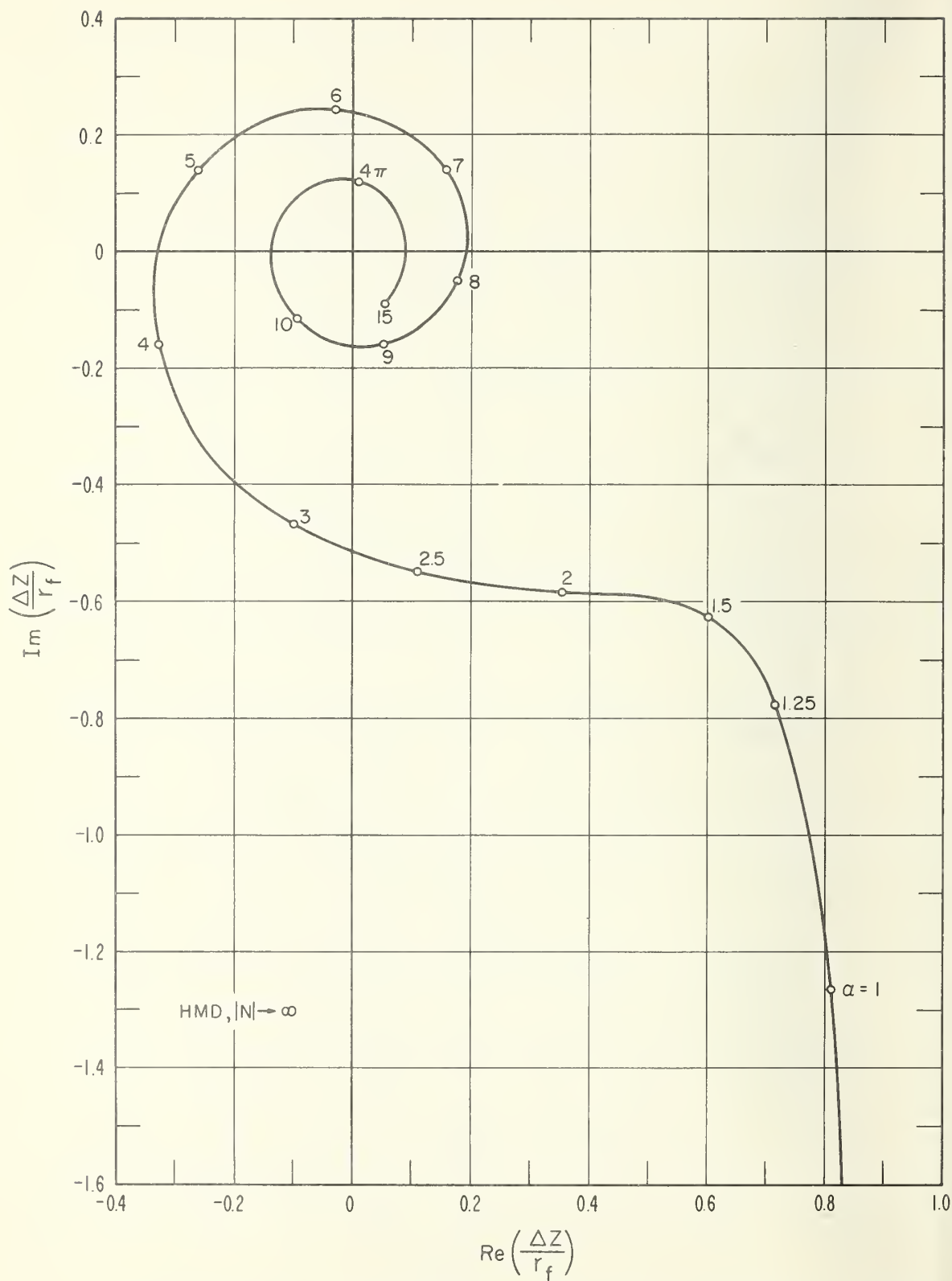


Figure A-64. Normalized input impedance change for HMD,  
 $|N| \rightarrow \infty$ .





