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Narrow-Angle Laser Scanning Microscope System for Linewidth Measurements on Wafers

D. Nyyssonen

CD Metrology, Inc. Germantown, MD 20874

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Prepared for: U.S. DEPARTMENT OF COMMERCE National Institute of Standards and Technology (Formerly National Bureau of Standards) National Engineering Laboratory Center for Manufacturing Engineering Precision Engineering Division Gaithersburg, MD 20899

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U.S. DEPARTMENT OF COMMERCE Robert Mosbacher, Secretary NATIONAL INSTITUTE OF STANDARDS AND TECHNOLOGY Raymond G. Kammer, Acting Director



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NARROW-ANGLE LASER SCANNING MICROSCOPE SYSTEM FOR LINEWIDTH MEASUREMENT ON WAFERS*

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ABSTRACT: The integrated-circuit industry in its push to finer and finer line geometries approaching submicrometer dimensions has created a need for ever more accurate and precise featuresize measurements to establish tighter control of fabrication processes. Under the auspices of the NBS Semiconductor Linewidth Metrology Program, a unique narrow-angle laser measurement system was developed. This report describes the theory, optical design, and operation of this system and includes computer software useful for characterizing the pertinent optical parameters and images for patterned thin layers. For thick layers, the physics is more complex, and only elements of the theory are included here. However, for more detail the reader is referred to several related reports listed in the references.

KEY WORDS: metrology, coherence, critical dimensions, linewidth measurements, micrometrology, scanning microscopy

INTRODUCTION

The push to submicrometer feature sizes on integrated-circuit (IC) wafers has resulted in a need for more accurate and precise dimensional measurements in order to establish tighter control of fabrication processes, improve yield, and ensure that lithographic

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^{**} Formerly with the National Bureau of Standards; collaboration continues under a Guest Worker Agreement.

and linewidth measurement systems meet specifications. Measurement systems used in the fabrication process must have accuracy and precision much better than the variation in the parts being measured and, in turn, the accuracy and precision of calibration standards must be still better than the instruments being calibrated.

Under the Semiconductor Metrology Program within the Center for Electronics and Electrical Engineering at NBS a project was initiated to develop improved instrumentation, calibration procedures and standard reference materials for linewidth measurement on IC wafers. The result was the development of the NBS narrow-angle laser linewidth measurement system. This system was first described in 1978 [1] and discussions of various aspects of this system have appeared in the literature since then [2-7]. However, there is no single report which adequately describes the details of its theory, design and operation. This report attempts to rectify this situation. In order to understand the motivation behind the development of this system, it is necessary to understand the optical characteristics of the patterned features on integrated circuits which this system was designed to measure.

CHARACTERISTICS OF PATTERNED THIN FILMS

The optical properties of patterned integrated circuit wafers are best described using the language of ellipsometry. Wafers are typically made up of layers of insulators and conductors with one or more of these layers patterned. These layers may vary in thickness from approximately 0.1 μ m to 0.5 μ m or more. In this report discussion is limited to thin layers, those less than onequarter of the illuminating wavelength. Thicker layers cannot be described by scalar theory and a vector treatment must be used. See ref. 19. For the moment consider a region on the wafer where only the top layer is patterned as shown in Fig. 1. A single

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plane wave of wavelength λ is incident at an angle Θ . This plane wave is refracted and reflected at each interface. To determine the complex reflectance, that is, both the amplitude and phase of the reflected wave, the Fresnel equations [8] are used. In matrix form [9], each layer is characterized by a matrix of the form

$$M_{j} = \begin{pmatrix} \cos v_{j} & \frac{-i}{u_{j}} \sin v_{j} \\ -i u_{j} \sin v_{j} & \cos v_{j} \end{pmatrix}$$
(1)
where $u_{j} = \begin{cases} \frac{\hat{\eta}_{j}}{\cos \theta_{j}} & \text{parallel polarization} \\ \hat{\eta}_{j} \cos \theta_{j} & \text{perpendicular polarization} \end{cases}$

and $\hat{\eta} = n_j + iK_j$ is the complex index of refraction of the jth layer. Θ_j is found from Snell's law:

 $\hat{n}_{o} \sin \Theta_{o} = \hat{n}_{i} \sin \Theta_{i} = a \text{ constant for all } j$

and v_i , the effective optical thickness, is given by

$$v_j = \frac{2\pi}{\lambda} (\hat{n}_j t_j \cos \Theta_j)$$

A. UNPATTERNED LAYERS

The characteristic matrix for the composite of N unpatterned layers is then given by the product of the characteristic matrices of the individual layers

$$M_{1,N} = M_{1} \cdot M_{2} \cdot \cdot \cdot M_{j} \cdot \cdot M_{N}$$
⁽²⁾

with

$$M_{1,N} = \begin{pmatrix} m_{11} & m_{12} \\ m_{21} & m_{22} \end{pmatrix}$$

The amplitude and phase of the reflected and transmitted waves are found from the characteristic matrix M. Let

$$x = m_{11} + \hat{\eta}_{s} m_{12}$$

 $Y = m_{21} + \hat{\eta}_{s} m_{22}$

then the complex reflectance is given by

$$r = \frac{X - Y}{X + Y}$$
(3)

If r = x + iy, then the phase of the reflected wave is given by

$$\Psi = \tan^{-1}\left(\frac{Y}{x}\right) \tag{4}$$

and

$$R = |r|^2$$

B. PATTERNED LAYERS

For the case of a patterned wafer (Fig. 1) where the relative reflectance and phase difference at an edge are needed, first the characteristic matrix $M_{1,N}$ for layers 1 through N is calculated and then the matrix $M_{2,N}$ for layers 2 through N. A relative reflectance, R, to be used later, is then defined by

$$R = \begin{cases} \frac{R_{1,N}}{R_{2,N}} \\ \frac{R_{2,N}}{R_{1,N}} \\ R_{2,N} \\ R_{2,N} \\ R_{1,N} \end{cases} \begin{pmatrix} R_{1,N} < R_{2,N} \\ R_{2,N} < R_{1,N} \\ R_{2,N} \\ R_{1,N} \end{pmatrix}$$
(5)

)

where the convention is chosen so that $R \leq 1$. The corresponding relative phase difference is defined by

$$\phi = \psi_{2,N} - \psi_{1,N} + 2k_0 t_1 \cos \Theta$$
 (6)

where $k_0 = \frac{2\pi}{\lambda}$ and t_1 is the thickness of the top layer. At normal incidence, there is no difference between incident waves with parallel or perpendicular polarization and these equations simplify. Appendix I includes a short computer program written in FORTRAN 77 which calculates R and Ø at normal incidence. The calculation of R and Ø represents the first step in modeling the image of a patterned wafer.

C. BEHAVIOR OF R AND ϕ

R and Ø vary with index and thickness of the layers, angle of incidence, polarization and wavelength. In addition, dielectrics behave differently from metals. Figures 2-5 illustrate variations of R and Ø as a function of these parameters. In Figs. 2(a) and (b), the curves for R and Ø as a function of t_1 are relatively simple for a single patterned layer on a silicon substrate. These same curves may also be plotted parametrically as $R(t_1)$ vs $Ø(t_1)$ as shown in Figs. 2(c) and 2(d).

In Fig. 3, the situation is more complex. With an oxide layer under the metal, one has the option of varying either the thickness of the metal layer or the thickness of the oxide layer

underneath. If the metal layer is held constant and the oxide is varied, the resulting curve is an ellipse.

Figures 2 and 3 are for the case of normal incidence and a single wavelength. Figures 4 and 5 illustrate the variations with wavelength and angle of incidence for a silicon dioxide layer on silicon. In real cases, the index of refraction also varies with wavelength, changing the behavior of the curves for silicon dioxide shown in Fig. 4.

For accurate linewidth measurements, R and \emptyset must be constant over the solid angle of illumination. It is possible to determine the maximum allowable angle for a given material (or combination of materials) using eqs. (1)-(6). For example, for SiO₂ on Si, if a 2% variation in R with Θ is allowed, Θ_{max} can be determined as a function of thickness of the oxide. See Fig. 5. Θ_{max} is then the maximum allowable illumination angle for the measurement system. For thick layers, this requirement rather than the coherence requirement will determine the illumination cone angle for the system.

OPTICAL DESIGN OF A METROLOGICAL MICROSCOPE

The variations in R and \emptyset with wavelength and angle of incidence are the driving force behind the design of the narrow-angle, laser linewidth microscope. As in ellipsometry, accurate dimensional measurements become exceedingly difficult and the data analysis time consuming if all of the experimental parameters are allowed to vary. Ideally then, the optimal solution to dimensional metrology would be a single wavelength, single-angle-of-incidence system analogous to that used in ellipsometry [10]. Single wavelength is readily achieved using a laser source. However, in optical microscopy, it is neither desirable nor necessary to use a single angle of incidence; a narrow illuminating cone angle. over which the resulting R and \emptyset of the specimen are essentially

-6-

constant is sufficient. The cone angle numerical aperture (N.A.), however, must be chosen with care for the particular index of refraction and thickness of the material to be measured.

A schematic of the layout of such a system built at NBS is shown in Fig. 6. The combination of the rotating ground glass disc and the illumination optics is used to control the illumination cone angle and the coherence at the back focal plane of the objective. With these parameters very tightly prescribed the microscope behaves like a modified bright-field microscope, that is, it operates as an effectively coherent imaging system. Although the system uses a one-dimensional piezo electric scanning stage [11] with interferometric readout of distance and a stationary slit in the image plane, it is also possible to scan the image plane with a moving slit arrangement. However, the system requirements for these two modes of operation are different.

The chief disadvantage of the single wavelength, narrow angle system is the low throughput. A 1-W laser is used on the NBS system and approximately 1 nW reaches the detector. The principal losses come from use of the rotating ground glass disc, overfilling of apertures to get uniform illumination, the small aperture limiting the illumination cone angle, the oversize illuminated area at the wafer, and the small slit in the image plane. The requirement on this slit width is that it be 1/6 or less of the Airy disc diameter of the objective when projected back to the wafer in order not to degrade the image waveform [12].

SPATIAL COHERENCE AND ANGLE OF INCIDENCE

In order to discuss the coherence aspects of the system, it is necessary to introduce some concepts related to coherence. It is conventional in microscopy to describe spatial coherence in a bright-field microscope in terms of a coherence parameter defined by the ratio of the numerical aperture of the condenser with respect to the N.A. of the imaging objective:

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$S_B = \frac{N.A. \text{ condenser}}{N.A. \text{ objective}}$

The limit $S \rightarrow 0$ is associated with coherent illumination as in the case of a collimated laser beam and the limit $S \rightarrow \infty$ with incoherent illumination. In conventional imaging in a microscope, neither of these limits is ever realized. However, it is useful to introduce the ideas of <u>effective</u> coherence and incoherence here. Effective coherence or incoherence means that the images of lines on wafers would be essentially the same as that seen in a fully coherent or a fully incoherent system.

For effective coherence:

- S_B < 2/3, for thin, high contrast objects such as opaque photomasks, and
- S_B < 1/5, for thick, low contrast objects with phase variations such as most wafer features.

For effective incoherence:

- S_B may have any value for thin low contrast objects with no phase variations present (rare), and
- $S_{\rm B} > 2$, for all other cases.

For practical purposes, the images formed for these values of S_B would be indistinguishable from those corresponding to completely coherent or incoherent images as illustrated in Fig. 7. One consequence of these considerations is that a high numerical aperture conventional bright-field imaging system with 0.9-N.A. dry microscope objective can <u>never</u> be effectively incoherent since S_B can never exceed 2; one must therefore deal with partially coherent or effectively coherent imaging with such a microscope.

For focused-beam scanning systems with the roles of the illumination and detection systems interchanged, the coherence parameter is defined analogously as the inverse of that given above, i.e.,

$$S_{F} = \frac{N.A.collector}{N.A.focused beam}$$
(8)

(See Ref. 13). For such systems, effective coherence and incoherence are similarly defined for this S_F . Therefore, it is possible to produce a system with an effectively coherent or incoherent response using either a laser or thermal source such as a tungsten-halogen lamp. By analogy, the narrow-angle, effectively-coherent NBS system could have been configured with a focused laser beam and narrow angle collector. However, because of the response of thin films to angle of incidence, these two configur-rations would not have produced the same response.

One major difference between coherent and incoherent imaging is sensitivity to phase changes in the object or feature being measured. This aspect will be discussed further with respect to the imaging characteristics of the system. The concepts of effective coherence and incoherence discussed here refer to the plane of the wafer and assume that the back focal plane of the objective is incoherently illuminated (which is not fully realizable in practice).

It is useful, therefore to discuss here the reciprocal relationship between coherence and size of the illuminated area at the back focal plane with respect to the same parameters at the wafer. This relationship has not yet made its way into textbooks but was introduced by Wolf [14]. As applied to the microscope, it states that the coherence at the back focal plane of the objective determines the illuminated area (and intensity distribution) at the wafer, while the size and distribution of the illuminated area at the back focal plane determines the coherence at the wafer, providing that: 1) the illuminated area is large

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compared to the coherence area, 2) the intensity is constant or slowly varying across the back focal plane, and 3) the region near the edges of the illuminated area is not being considered.

Because of throughput it is not desirable to require a high degree of incoherence at the back focal plane of the objective. In fact, if only small line objects are viewed a relatively small circular field of view is required and the diameter D_C^{BF} of the coherence area at the back focal plane can be found from

$$D_{C}^{BF} \leq \frac{0.6\lambda f}{D_{I}^{W}}$$
(9)

where D_I^W is the desired diameter of the illuminated area on the wafer, λ the wavelength, and f the focal length of the objective. It is also required that

$$D_{C}^{BF} << D_{I}^{BF}$$
(10)

where $D_I^{BF} = 2(N.A._{condenser})f$. Therefore, for a 4 mm focal length objective at a wavelength of 0.5 μ m and $D_I^W = 50 \mu$ m these parameters would be $D_I^{BF} \stackrel{\sim}{=} 1$ mm and $D_C^{BF} > 25 \mu$ m for an effectively coherent system. If the coherence area at the back focal plane is reduced, a larger area on the sample will be illuminated and lower throughput will result. On the other hand, if the coherence area is increased, a smaller area will be illuminated at the sample making it difficult to find the patterns which need to be measured and possibly violating the requirement that $D_C^W >> D_T^W$.

Only spatial coherence, that is, coherence in the plane of the wafer or lens aperture, has been discussed. The concept of

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coherence volume (coherence area times coherence length) is useful here as well. Because there are no differences in optical path length in an ideal imaging system, coherence length is not usually of concern. However, in coherent imaging systems, coherent noise or speckle becomes a problem due to the extremely long coherence length of the laser source. Normally, dust particles and scratches on optical surfaces produce diffraction patterns which may be observed in the image plane due to the long coherence length. As shown in Fig. 8(a), a system using unfiltered tungsten illumination (white light) has a very short coherence length and small volume compared to a laser source (Fig. 8(b)) and therefore will not exhibit these effects. The present narrow-angle laser system has a peculiar pencil-shaped coherence volume as shown in Fig. 8(c), which eliminates most of the coherence effects normally associated with coherent imaging.

ABERRATIONS

In a system with a stationary slit and moving wafer where only the axial image is used, only spherical aberration is of concern. When the image is scanned with a moving slit, the off-axis aberrations are also of concern. Because it is desirable to eliminate as many variables which effect the measurement as possible, diffraction-limited performance and aberration tolerances of $\lambda/4$ or less are desirable. The ultimate test, however, is whether the system produces a diffraction-limited image waveform. Although aberrations may be taken into account in edge detection formulas [4], this approach is not recommended.

ALIGNMENT

A bright-field microscope operating in an effectively coherent mode has much more severe requirements on alignment than a conventional microscope. Because of sensitivity to phase variation, the illumination must be not only uniform in intensity across the line pattern but also uniform in phase across the illuminated

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area. If this requirement is not met, the resulting nonsymmetric images invalidate the algorithms used for accurate edge detection. Because poor quality lines will also produce nonsymmetric images, it is necessary to distinguish between these two sources of nonsymmetry. One method is to rotate the specimen 180° and compare image waveforms. System asymmetry will stay the same while line irregularity will rotate. However, this test is difficult to interpret when both sources of nonsymmetry are present.

A special test wafer is therefore used for testing system performance. The ideal wafer is a patterned layer with R = 1, $\emptyset = \pi$. The waveform for a 180 nm thick layer of SiO₂ (R = 1, $\emptyset = 0.6\pi$) is shown in Fig. 9. This line pattern is ideal because of the symmetric waveform produced at each edge. Three sources of error readily show up in the image waveform: 1) misalignment of the illumination system including decentering of the aperture stop and tilt errors in the optical elements, 2) tilt of the wafer with respect to the focal plane of the objective and 3) tilt of the scanning plane with respect to the image plane when a moving slit is used.

In order to interpret the waveforms, it is necessary to understand the diffraction-limited behavior of this waveform with defocus. Figure 10(a) illustrates the nonsymmetry produced with defocus. On one side of focus, one of the maxima at the image edge is enhanced while the other is reduced. On the other side of focus, the opposite occurs. In addition, as defocus increases, the distance between these peaks increases as shown in Fig. 10(b).

When the only error is the tilt of the wafer with respect to the focal plane, one edge of the line will lead (or lag) the changing image waveform as a series of scans are made through focus. A similar effect occurs when the image plane is tilted with respect to the scanning plane. This effect is illustrated in Fig. 11.

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Misalignment can produce a large variation in waveforms. An example is illustrated in Fig. 12(a). In general, nonsymmetry is present as focus is varied but is different from that shown in Fig. 10(a). There is also a loss in resolution, so that the distance between peaks is larger than that shown in Fig. 10(b). With both wafer tilt and misalignment present, it is possible to get waveforms like that shown in Fig. 13 where there is symmetry, but of the wrong kind.

Given the difficulty of determining and correcting these errors when all of these effects (misalignment, wafer tilt, poor line edge quality) are present, a procedure which will now be discussed has been worked out for laser alignment of the microscope.

ALIGNMENT PROCEDURE

We have found that in a high quality microscope the individual microscope optics are usually aligned adequately in their own mounts. However, these components when assembled to form the microscope are generally improperly aligned. This is probably because manufacturing tolerances of conventional microscopes are not adequate for this highly demanding mode of operation. It is common practice, for example, to correct errors in one component by an offsetting adjustment in another. One can expect, therefore, to have to shim and in some cases redesign mounts and adjustments to achieve the desired alignment accuracy.

The required tools for this job are a small HeNe laser (1 mW or less), neutral density filters to reduce the power to a comfortable level for visual viewing through the microscope, a laser beam steerer or other method for controlling the position and tilt of the laser beam, a polished silicon wafer or other highly reflective, flat surface, and a wafer holder with tilt adjustment.

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The first step is to disassemble the microscope. If possible, remove all optics except the beam splitter in the head and the wafer on the stage. Then select a small aperture on the illumination side and one on the viewing side for reference. The center of these apertures together with the requirement that the return beam fall on the exit aperture of the laser determines the optical axis of the system. All components will be aligned to this axis as illustrated in Fig. 14.

The principle of this procedure is to add components one at a time and make sure that each is aligned to this axis. This is achieved by making sure that the return beam goes back to the laser aperture and the forward beam remains centered on the chosen reference aperture for each added optical element. In general, centering is done first and if the forward and return beams cannot both be returned to their reference points, then tilt must be adjusted by shimming or other means. In general, the tilt must be under- or over-corrected and the element recentered and these steps repeated until the desired alignment accuracy is achieved.

One difficulty with this method is that the laser beam changes diameter at the reference aperture as elements are added. In some cases, it may be necessary to temporarily remove an element already aligned if it can be replaced exactly in order to keep the beam size small and maintain the desired accuracy. No rule of thumb can be given for "tolerable errors." Because of the large number of components (9 lenses, a beam splitter and 2 apertures in the NBS system) and the variations in microscope design, it is best to align every element as accurately as possible, that is, within a small fraction of the laser beam diameter. Because of its high magnification, the microscope objective is left for last. The aperture pinhole, which determines the illumination cone angle, will be next to last. The ultimate test of the accuracy achieved is the symmetry of the resulting waveform in a series of profiles with increasing amounts of defocus.

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When all of the microscope optics have been aligned adequately, the argon or other high-power laser source is brought into coincidence with the alignment laser as shown in Fig. 15 and the beam expander and ground glass are aligned. Through these last steps, the aperture pinhole as viewed through the microscope with an auxiliary alignment telescope (such as used for centering the disc in phase contrast microscopy) or other device must remain stationary and uniformly illuminated.

One element that needs special attention is the rotating ground glass disc. If the normal to the surface precesses about the optical axis, fluctuations in intensity in the image plane will be observed. For this reason, a flexible coupling and a precision bearing at the drive motor are recommended.

After the alignment is completed, the alignment wafer is replaced with the SiO₂ test wafer. A scan of a line is made and the tilt of the wafer adjusted if indicated. If nonsymmetry due to misalignment is detectable, the alignment procedure was not performed accurately enough. Once alignment is deemed satisfactory, other adjustments of optical elements should be required or made thereafter. With each new wafer, only wafer tilt and focus are adjusted.

MEASUREMENT OF LINEWIDTH

The system must produce and maintain an ideal image waveform for the test line object because of the demands of accurate edge detection. An equally important requirement is the accurate measurement of distance (i.e. linewidth). To scan the image, the NBS laser system moves the wafer and measures the motion with a laser interferometer, thus providing traceability to fundamental standards of length. Aside from the usual demands of accurate laser interferometry, this system has some unique aspects principally involving alignment of the elements of the scanning system including scanning slit, line object, axis of stage motion and interferometer axis. The principal difficulty stems from the

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extremely short distance of motion of the piezo electric stage, typically less than 50 μ m.

The easiest method of alignment is to use the crosshair in the viewing eyepiece as a fiducial mark. The slit and line object can be centered and aligned to the vertical axis visually. In addition, the axis of stage motion can be aligned to the horizontal axis visually by inspecting the motion of a horizontal line object as it traverses the field of view. In order to align the interferometer axis parallel to the piezo electric stage axis, an auxiliary mirror has been used. This mirror has a mount that fits into the holes at the pivot points on the stage (See Ref. 11.) and is constructed so that the mirror face is accurately perpendicular to the direction of motion. Without this auxiliary mirror, the method is one of trial and error; minimizing a measured linespacing to eliminate the possible cosine error. Fortunately, because of the short distances scanned, the angle accuracy required for a given tolerance on a one micrometer linewidth is not very demanding. The final check, however, is measurement of a known linespacing traceable to national standards of length.

The major sources of distance measurement errors are vibration (the system should be mounted on a massive vibration isolation system), the least count of the interferometer, and temperature effects on the system. Because of the short distances, temperature effects on the wafers being measured are negligible.

In the NBS system, the precision of the interferometry is a fundamental limit on the precision of linewidth measurements. One cannot measure the size of an object to better precision than that of the distance measurement. This limitation is to some extent due to the basic design of the microscope, which is sensitive to both acoustic and mechanical sources of vibration and temperature.

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RADIOMETRIC SIGNAL/NOISE RATIO

In most microscope linewidth measurement systems employing tungsten sources, the radiometric precision is limited by photon noise. Here the laser power has been increased in order to maintain the single wavelength, narrow angle mode of operation. Thus photon noise has been traded for laser output fluctuations. However, the specifications on the laser (< 0.5% variation) are adequate in this case. In addition to increasing the power, the system uses a variable speed chopper and lock-in amplifier operating at approximately 350 Hz with high and low-pass filters. The resulting signal/noise ratio is better than 200/1.

SCALAR THEORY FOR THIN-LAYER IMAGING

Scalar theory of partially coherent imaging has been developed using several different approaches including convolution integrals and Fourier analysis. The most efficient approach for computer calculations is the use of the transmission crosscoefficient of the optical system [15] as applied to the imaging of line objects by Kintner [16]. Based on the methods of Fourier analysis, the complex amplitude transmittance of the patterned line object is described by

$$t(x) = \begin{cases} 1 & 0 < x < W/2 \\ \sqrt{R}exp(i\emptyset) & W/2 < x < P \end{cases}$$
(11)

which is expanded in the Fourier series

$$t(x) = \sum_{m} A_{m} \cos\left(\frac{2\pi m x}{P}\right)$$
(12)

where the line object is repeated at a period P which may be chosen arbitrarily large to describe isolated line objects. R and \emptyset are the relative reflectance and phase difference at the line edge as introduced earlier. (See Eqs. 5 and 6.) The image is calculated from the Fourier series equation

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$$I(y) = \sum_{n=-\infty}^{\infty} b_n \cos\left(\frac{2\pi n y}{P}\right)$$
(13)

where, for a symmetric line object,

$$b_{n} = \left\{ A_{n}A_{0}^{*}\Psi\left(\frac{n}{p};0\right) + \sum_{n'=1}^{\infty} \left[A_{n+n'}A_{n'}^{*}\Psi\left(\frac{n+n'}{p};\frac{n'}{p}\right) + A_{n-n'}A_{n'}^{*}\Psi\left(\frac{n-n'}{p};\frac{-n'}{p}\right) \right] \right\}$$
(14)

and

 $b_n = b_{-n}$ where A_n are the Fourier coefficients for the line object as given in Eq. 12.

The function is called the transmission crosscoefficient [14] and characterizes the optical system including the state of partial coherence of the illumination. For a one-dimensional line object, following Ref. 15, the transmission crosscoefficient is given by

$$\Psi(\xi_{1},\xi_{2}) = \int_{-\infty}^{\infty} \int_{-\infty}^{\infty} \mathcal{A}(\xi'',\eta'')$$
(15)

$$\cdot F(\xi_{1} + \xi'',\eta'')F^{*}(\xi_{2} + \xi'',\eta'')d\eta''d\xi''$$

where $\mathscr{A}(\xi'', \eta'')$ is the two-dimensional intensity

distribution in the condenser aperture, F is the two-dimensional equivalent of the pupil function, and * denotes the complex conjugate (wide-field Kohler or critical illumination assumed). The function \mathcal{A} is sometimes called the effective source function [17] (assumed to be incoherent, i.e., the coherence interval is small compared with the effective source size).

Because of the dependence of R and \emptyset on angle of incidence the image structure will also vary with angle of incidence. This

formulation assumes that R and \emptyset are constant over the illuminating solid angle. If they are not, it is still possible to calculate the image from these equations. However, R and \emptyset become functions of and η and the integrals can no longer be separated as shown in Eqs. 14 and 15.

In this scalar theory approach, the line object is described by the planar function t(x). Hence, there is no ambiguity about focus; the object thickness is much thinner than the depth of field of the optics. If the plane of the object is not coincident with the focal plane of the lens, the defocus aberration term is included in the pupil function,

$$F_{defocus}(\mu) = \exp(ika_2\mu^2) \operatorname{Rec} \mu \mid \frac{M}{P}$$
(16)

where a_2 is the constant that indicates the amount of defocus in number of waves (units of λ), k is the wave number, and Rec is the rectangular function of width M/P, which defines the aperture diameter.

With lines patterned in thin layers (less than approximately $\lambda/4$ thick) and vertical edges, the images can be accurately described by these scalar equations and the coherent optical edge detection threshold T_c can be used for linewidth measurement [4].

$$T_{c} = 0.25 (1 + R + 2 \sqrt{R} \cos \phi), \qquad (17)$$

However, in order to use T_c , R and Ø must be known. R (the ratio of reflectances on either side of the edge) is best determined from the image waveform. If Ø (the phase change at the edge from Eq. 6) is unknown, the dual threshold method [6] illustrated in Fig. 16(a) may be used to determine linewidth.

Because of the complex waveforms which result from the coherent imaging of line features of varying contrast with phase discont-

-19-

inuities present, best focus is difficult to determine. One objective criterion currently in use is minimization of as defined in Fig. 16(b). This distance can also be toleranced to ensure that measurements made with inaccurate focus are rejected. That is, at best focus is a minimum but by plotting versus the change in linewidth with defocus, an acceptable range for may be specified for a desired measurement accuracy.

In Fig. 17, calculated image waveforms are given for lines patterned in silicon dioxide on silicon and for chromium on glass. The computer software used to calculate the theoretical images is given in Appendix II. The reproducibility of these waveforms for linewidth measurement is determined principally by the accuracy of alignment of the line to be measured to the reference crosshair, accuracy of leveling of the wafer, and accuracy of focus. All of these operations should be automated so that they become operator independent and the required accuracy can be specified and maintained.

VECTOR THEORY FOR THICK-LAYER IMAGING

Scalar theory is unable to accurately predict the image profiles for line objects which violate the initial assumptions of infinitesimally thin (planar) objects and vertical edges characterized by abrupt discontinuities in R and \emptyset . For patterned layers thicker than approximately one-quarter of the illumination wavelength, the multiple reflections which occur within semi-transparent layers result in constructive and destructive interference, which affects R and \emptyset and the scattering patterns as well. In addition, both metals and dielectrics exhibit waveguide effects near edges which also influence the nature of the image waveforms. (See Fig. 18.) The major differences for thick layers as compared to thin layers are (1) the broadening of the minimum at the line edge, (2) enhanced maxima on either side of the edge particularly with sloping edge geometry, and (3) edge ringing which extends farther from the line edge in some cases.

Imaging of lines patterned in thick layers may be modeled using vector theory. For lines patterned in a thick layer with vertical edges, the complex dielectric constant of the material rather than the complex reflectance function is expanded in a Fourier series

$$\hat{\varepsilon}(\mathbf{x}) = \hat{\eta}_{\mathbf{c}}^2 = \sum_{\mathbf{m}} \varepsilon_{\mathbf{m}} \cos\left(\frac{2\pi \mathbf{m}\mathbf{x}}{\mathbf{P}}\right)$$
 (18)

The appropriate wave equation

$$\nabla^2 E_y + k_0^2 \hat{\epsilon} E_y = 0 \qquad (TE-mode)* \qquad (19)$$

and

$$\nabla^{2}H_{y} - \frac{1}{\varepsilon} \frac{\partial \varepsilon}{\partial x} \frac{\partial^{H}y}{\partial x} + k_{0}^{2}\hat{\varepsilon}H_{y} = 0 \qquad (\text{TM-mode}) \qquad (20)$$

where $k_0 = 2\pi/\lambda$ is solved for the E- and H-fields within the layer. In this case, when the Fourier series expansion for $\hat{\epsilon}(\mathbf{x})$ is substituted into Eq. (19), the resulting equation is Hill's equation [18], which has solutions of the form

$$E_{y}(x,z) = \sum_{m} A_{m} \exp(\alpha_{m}z) + A'_{m} \exp(-\alpha_{m}z)$$

$$\cdot \sum_{j} B_{j,m} \exp(2\pi i j x/P)$$

where the α_m 's are the eigenvalues and the $B_{j,m}$'s are the eigen vector solutions to Hill's equation. The A_m and A_m' are weighting constants which must be determined from the boundary conditions. Each of these terms represents an inhomogeneous eigenfunction or waveguide mode which is supported by the line structure.

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^{*} Defined as that polarization component with its electric field parallel to the line being measured.

With a single plane wave incident, the boundary condition equations allow for solution for the Fourier series coefficients in the plane wave expansion for the reflected (scattered) field

$$E^{R}(x,z) = \sum_{j} E^{R}_{j} \exp \left\{-ik_{o}\left[\left(\frac{\lambda j}{P}\right)x + K^{R}_{j}z\right]\right\}$$
(22)

For normal or nearly normal incidence, the magnitudes of the Eand H- fields are equal and no polarization effects are present. Therefore, the E_j^R coefficients in Eq. (22) can be substituted for the A_n 's in the scalar imaging equation (Eq.(14)). In this case, Eq. (22) may be regarded as representing the equivalent planar object which would produce the same image as the thick object of Eq. (18). The equivalent planar object is taken as located in the plane of the top surface of the thick layer. This concept is important to understanding the problem of focusing for thick layers.

For nonvertical edges, the single thick layer may be subdivided into a set of sublayers each of which may vary in linewidth, complex index of refraction and offset (to allow for asymmetric line objects). Such a representation is shown in Fig. 19. When boundary conditions are applied at each sublayer interface, the solution of the resulting equations yields the scattered field in the same form as Eq. (22). Thus any nonplanar structure can be represented by an equivalent planar structure and its image determined. For details of the method, see Refs. 5 and 19.

This method of computing both the reflected field and the corresponding microscope image requires no approximations of the type usually found in calculations of the scattered field, such as limits on the conductivity or slope of the surface. Limitations may be imposed, however, by the computation capability available. First, increasing the number of layers used to approximate the structure increases the computing time linearly. In most cases

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of interest seven to nine layers were sufficient to produce significant results.

The second limitation is in the truncation of the series, i.e., the matrix sizes used in the computations. In this case, as for a single layer [4], all of the reflected plane waves which have diffraction angles less than $\pm \pi 2$ in the air are included. With $P = 12 \ \mu m$ and $\lambda = 0.53 \ \mu m$, 22 diffracted orders are included. This requires a 45 x 45 complex eigenvalue matrix and a 90 x 90 complex matrix for solution of the boundary condition equations. This choice necessarily truncates the series which represents the fight in the layers with higher refractive index. This truncation does not appear to significantly affect the results except for very small linewidths and near resonances, that is, either where the thickness of the layer or the linewidth is approximately equal to the wavelength of the illumination.

Also, for grating objects with $P \le 12 \ \mu m$, the assumed periodicity is true. However, for isolated line objects near resonances, P =12 μm is not large enough to eliminate the effect of the assumed adjacent lines on the calculated image. In order to calculate images of isolated lines, a larger period and, therefore, larger matrix sizes would have to be used.

As discussed earlier, this approach to the imaging of lines patterned in thick layers involves replacement of the thick line object by its equivalent planar object located in the plane coinciding with the top surface of the patterned layer. It can also be shown that displacement of the top surface of the thick layer (or equivalent planar object) along the optical axis of the imaging system introduces a focus error as in conventional scalar imaging equations with the accompanying loss of resolution and distortion of the image profiles.

At this time, no universal, simple, and accurate edge detection methods have been found for thick layer imaging. The complex

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image structure in the vicinity of the line edge depends upon thickness and edge geometry as well as wavelength and other parameters of the imaging system. It is difficult to see how, in such a complex relationship of these parameters, a single number will be adequate to characterize line geometry.

Calculated images have been compared with experimentally measured images from the narrow-angle laser linewidth system. Some results are shown in Figs. 20 and 21. One of the major difficulties in getting agreement between theory and experiment is finding line objects with well characterized edge geometries.

ACCURACY AND PRECISION

Both the accuracy and precision of any metrology system needs to be established. Precision can be determined by repeated measurements on a control specimen. In the present case, the quality of the line specimens may limit precision. That is, specimens with rough edges cannot be placed in exactly the same position each time, and, therefore, the precision of the measurements is a function of edge roughness as well as system parameters. Unfortunately, the quality of most available processed wafers is not suitable for standard reference materials. Indications are that for the best thin layer materials available, the precision of the measurements when the coherent edge detection threshold is used is comparable to that of the photomask system used for calibration of SRM 475, which is approximately + 0.05 µm (three standard deviations). The narrow-angle laser system at NBS has not yet reached the operational level of the photomask system. Until such time, there will be operator dependence due to focus, alignment and leveling errors. The difference here is that at the operational level all image scans which do not meet specified tolerance criteria are rejected automatically with an accompanying improvement in the long term precision of the system. The laser system has not been in routine use at this level long enough to get an accurate number for measurement precision.

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Accuracy is customarily assessed based on fundamental physics considerations and/or comparison with other measurement techniques. In this case, at the level of accuracy being considered, comparison with other techniques cannot provide comparison numbers. There are no other fundamentally accurate optical techniques for dimensional measurements on thick objects with accuracies at the 0.05 μ m (λ /10) level available at this time. A common recourse is to compare optical with scanning electron microscope (SEM) measurements. However, it has been shown that at this level SEM measurements are suspect [20] due to both electron beam interactions with the specimen and instrument errors. Therefore, comparison with SEM can only be expected to indicate gross errors at best. Even edge slope (or geometry) for thin layers (< 200 nm) can only be determined crudely in the SEM. (Magnifications of more than 100,000X are required.)

Therefore, accuracy needs to be assessed in terms of fundamental physics of the measurement process. For the photomask calibration system, edge slopes greater than approximately 70° produce images which are indistinguishable from vertical (90°) edges. This is supported by the fact that structure or variations which occur within a distance less than approximately 1/6 the Airy disc diameter of the imaging objective do not affect the image. Hence, for lines with edge slopes greater than approximately 70° , there is an uncertainty in the measurement (for lines patterned in a 150 nm thick layer and 0.9 N.A.) of approximately \pm 0.05 µm (worst case) if the measurement is taken to be the mean width. See Fig. 22. For the photomask case, SEM measurements on Cr-CrO masks corroborated this value.

For thin layers on wafers, the same argument may be applied with similar results. However, the agreement between theoretical and experimental image profiles must also be considered. In the wafer case, there is much more variation in materials and image profiles as well as greater system sensitivity to optical alignment, leveling, and focus errors. Therefore, while the narrow-angle laser

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system has the capacity for accuracies on thin layers comparable to that of the photomask system, the accuracy should be assessed on a case-by-case basis with the above considerations taken into account.

For thick layers, assessment of accuracy is more complex. First, theory is based on a model which has yet to be fully evaluated. There are inappropriate assumptions in the modeling near resonances. Although the calculations are known to be in agreement for thin layers, the accuracy of the calculations for other cases has not been established. When discrepancies occur between calculated and experimentally measured image profiles, it is not known whether these differences are due to inaccuracies in the calculations, deviations of the system response from the ideal, poorly characterized line geometry, poorly known optical constants, or all of these. More work needs to be done on comparisons with line objects of known geometry, perhaps preferentially etched silicon samples, and on testing the accuracy of the calculated image profiles.

DESIGN OF LINEWIDTH CALIBRATION STANDARDS

Photomask materials have relatively little variation in optical constants. Hence, choice of a standard reference material was simplified. The most commonly used mask materials were chosen, CrO on Cr on glass, and an appropriate warning given about calibration of systems used to measure other materials was also given [21]. For wafers, there is an enormous variation in index of refraction and thickness of the layers found on wafers and, therefore, in R and Ø values as well. In fact, different combinations of materials may produce the same R, Ø values as well. Rather than sample all variables (R, Ø, and linewidth w) over the ranges of interest ($0 < R \le 1$, $0 \le Ø \le \pi$, $0.5 \mu m < w < 5 \mu m$) which is impractical, it is possible to determine the nature of the expected errors, that is, their dependence on the variables R, Ø, and w and apply experimental design methodology to the design of a

standard. For linewidth measurements on wafers, the expected errors are known to be of low order [6]. Work by Dr. James Lechner, Carol Croarkin, and Ruth N. Varner at NBS resulted in the proposed optimal six-point design illustrated in Fig. 23. The expected error surface shown in Fig. 7(a) of Ref. 6 was found to fit a polynomial of the form

$$E(R, \emptyset) = (1-R) (A + BR + CR2 + E \cos \emptyset + F \cos^2 \emptyset)$$
 (23)

A search for a D-optimal design [22] was made, based on the polynomial model of the expected error surface. In combination with other factors such as ease of fabrication, the six-point design of Fig. 23 was selected as optimal. It is also a good design for polynomial surfaces of lower order such as those of Fig. 7(b) and (c) of Ref. 6. The design points $(R_i, \cos \phi_i)$ can be fabricated from two materials with a silicon substrate using the combinations shown in Table 2. In each case, only the top layer is patterned. This design is also relatively insensitive to small changes in R and ϕ such as would occur in normal fabrication of the standard. Thin-layer standards could thus be provided and calibrated with the present narrow-angle laser microscope. However, these standards would not be directly applicable for applications involving thick layers on silicon.

SUMMARY

This report has described the development of the narrow-angle laser linewidth measurement system at NBS and its application to calibration of linewidth measurement standard reference materials for the IC industry. This system represents a major move toward optical systems with well characterized waveforms suitable for accurate linewidth measurements at dimensions on the order of the illumination wavelength. In the course of its development, major theoretical advances have also been made in the theory of optical scattering from and imaging of objects with dimensions on the order of a micrometer.

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ACKNOWLEDGMENTS

A number of people have contributed at various times to the developments described here. The original computer software for partially coherent imaging of line objects patterned in thin layers was written by Dr. Eric Kintner and later expanded and documented by Clinton R. Gable. Thanks are given to Ruth N. Varner for help in preparing the software for publication. Credit for the application of experimental design methodology to the design of a reference standard goes principally to Dr. James Lechner, Carol C. Croarkin, and Ruth N. Varner.

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Fig. 1 Schematic of multi-layer structure on a wafer with definition of parameters used for calculation of R and \emptyset .

-



Fig. 2(a) Relative reflectance R and phase difference \emptyset for silicon calculated from the Fresnal equations for varying thickness of silicon dioxide and monochromatic illumination (530 nm) at normal incidence.



Fig. 2(c) Relative reflectance vs. the cosine of the phase difference for silicon dioxide and silicon nitride on silicon. Some of the corresponding thicknesses are indicated along each of the curves.



Fig. 2(b) Same as Figure 2(a), except for chromium on silicon.



Fig. 2(d) Same as Figure 2(b), except for chromium and aluminum on silicon.



Fig. 3 Same as Fig. 2(b) for chromium with the addition of a silicon-dioxide layer of varying thickness between the chromium and silicon. The tangent point of each ellipse indicates the thickness of the chromium patterned layer. Varying the silicon dioxide between zero and 180 nm produces the ellipse.



Fig. 4 Variation of R and Ø with λ for a 600 nm thick layer of SiO_2 on Si.

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Fig. 5 Variation of R and \emptyset with angle of incidence Θ for thicknesses of SiO₂ on Si shown.



Fig. 6 Ray path for reflected-light laser-scanning microscope system.



Fig. 7 Comparison of edge profiles calculated for fully coherent imaging (dashed curve) and for a coherence parameter of 0.2 (solid curve). Edge is located at 5 μ m.



Fig. 8 Relative sizes of coherence volumes for microscopes using the sources indicated: (a) white light thermal source, (b) laser source, (c) narrow-angle laser system with rotating ground glass and laser source.



OTHORY -XHMXN-->

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DISTANCE IN MICROMETERS

Fig. 11 Image waveform with tilt present in wafer. Note nonsymmetry.



DISTANCE IN MICROMETERS





DISTANCE IN MICROMETERS

Fig. 13 Image waveform with slight misalignment and tilt (b) with correct alignment (a) shown for comparison.







Fig. 14(b) Alignment errors with addition of lens.



Fig. 15 Alignment laser beam and high power laser beam must be brought into coincidence at both A and B.



Fig. 16 a. Proposed dual-threshold edge detection criteria where $T_2 = RT$. In this paper, T_1 is taken to be 0.95 times the reflectance of either the line material or surround, whichever is higher.



Fig. 16(b) Dual-threshold focus criterion for wafers. The edge width δ is a minimum at focus. For wafers, the threshold T₁ and T₂ are taken the same as in Fig. 16(a).



Fig. 17(a) Comparison of experimental (---) and theoretical (•) image profiles for a window etched in a 150-nm-thick layer of silicon dioxide on silicon (0.85 objective N.A., 0.2 condenser N.A., and 530-nm wavelength).



Fig. 17(b) Calculated image profiles from thick (vector, solid line) and thin (scalar, dotted line) models for a chromium on glass line.



Fig. 18 Calculated image waveforms at edges of a single, vertical edge patterned layer for (a) Cr on SiO_2 on Si and (b) SiO_2 on Si.



Fig. 19 Cross section of a typical thick line object (a) and the corresponding multilayer representation (b).



Fig. 20 (a) Comparison of experimental (solid curve) and theoretical () (based on waveguide model) image profiles for a window etched in a 616-nm-thick layer of silicon dioxide in silicon. The calculated curve is based on $\eta_0 = 1.46$, $\hat{\eta}_8 = 4.1 + i(0.06)$, 0.85 objective N.A. 0.14 condenser N.A., a wavelength of 514 nm, and a linewidth of 4.85 μ m (b) SEM image of oxide line for wafer samples used in (a).



Fig. 21 Comparison of theoretical and experimental image profiles for 1 μ m thick resist on Si for (a) vertical and (b) non-vertical.

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Fig. 22 Schematic of the profile for an opaque line on SRM 474 showing uncertainty U.



Fig. 23 Values of R and cos \emptyset (o) for six-point design super imposed on error surface. Corresponding to using the minima at the line edge as the edge detection threshold.

Appendix I - Software for Calculation of R and \emptyset from the Fresnel Equations

1	-	PROGRAM TH2LR
2345		THIS PROGRAM COMPUTES THE RELATIVE REFLECTANCE AND PHASE DIFFERENCE FOR A PATTERNED LAYER WITH A SUBLAYER AND SUBSTRATE BOTH OF WHICH MAY HAVE COMPLEX INDICES.
67	Ċ	THIS DROCDAM WAS WRITTEN BY D NYVSSONEN OD METROLOGY INC
8	c	THIS PROGRAM WAS WRITTEN BY D. NIISSONEN, CD METROLOGY, INC.
9	C	***************************************
11 12 13 14	00000	INTERMEDIATE LAYER THICKNESS IS HELD CONSTANT, WHILE THE PATTERNED LAYER THICKNESS VARIES FROM 0 TO A MAXIMUM VALUE (TO BE INPUT). THE PATTERNED LAYER THICKNESSES ARE INCREMENTED IN STEPS OF 0.002 MICROMETERS (20 ANGSTROMS).
16	C	**********************
17 18 15	CCC	OUTPUT IS ON LOGICAL UNIT IOUT
20 21 22 23 24		<pre>DIMENSION T(2) COMPLEX CM(2,2,2),DEL(2),CN(2),CBASE,CML(2,2),WAVEL, * X,Y,R DATA IOUT/10/ OPEN(UNIT=IOUT,FILE='TAPE10')</pre>
25	С	
26 27	с с	WAVELENGTH OF LIGHT USED=0.53 MICROMETERS.
28 29	C	WAVEL=0.53
30 31 32		THICKNESS ENTERED FOR PATTERNED LAYER, T(1), IS MAXIMUM FOR WHICH CALCULATIONS ARE MADE, INCREMENT IS 0.002 UM
33 34 35	C	<pre>PRINT*, 'INPUT THICKNESS AND COMPLEX INDICES OF LAYERS WITH', * ' PATTERNED LAYER FIRST'</pre>
35 36 37	0000	ENTER MAX. THICKNESS OF PATTERNED LAYER IN MICROMETERS FOLLOWED BY THE COMPLEX INDEX OF THE PATTERNED LAYER
39 40 41 42	C	READ*, T(1), CN(1) PRINT*, 'INPUT THICKNESS AND COMPLEX INDEX OF', * ' INTERMEDIATE LAYER'
43		ENTER THICKNESS OF INTERMEDIATE LAYER IN MICROMETERS FOLLOWED BY THE COMPLEX INDEX OF THE INTERMEDIATE LAYER,
45 46 47		READ*, T(2), CN(2) PRINT*, 'INPUT COMPLEX INDEX OF SUBSTRATE'
48 49	C	ENTER COMPLEX INDEX OF SUBSTRATE (CBASE)
50	C	DEND* ODICE
5⊥ 52		KEADA, CEASE WRITE(IOUT.*) 'FOR PATTERNED LAYER, MAX THICKNESS IS ' T(1)
53		* 'AND INDEX IS ', CN(1)
54		WRITE(IOUT,*) 'FOR INTERMEDIATE LAYER, THICKNESS IS ', T(2),
22		AND INDEX IS ', CN(2)

56 57 58			<pre>WRITE(IOUT,*) 'INDEX OF SUBSTRATE IS ', CBASE WRITE(IOUT,*) WRITE(IOUT,*) 'THIS PROGRAM VARIES THICKNESS OF PATTERNED WRITE(IOUT,*)</pre>	LAYER'
59 60 61 62		t	WRITE(IOUT,*) WRITE(IOUT,*) ' THICK R-PAT R-INT P-PAT P-INT I * 'RNO RM PNORM COS-P' WRITE(IOUT,*)	DELAY',
63 64			TMAX=T(1) T(1)=0.0	
65		20	IF(T(1).GE.(TMAX-0.001)) GO TO 60	
66			DO 40 J=1,2 DDI $(J) = (-28218 \pm 0)(J) \pm 0(J) (U) = (-28218 \pm 0)(J) \pm 0(J)$	
68			CM(J,1,1) = CCOS(DEL(J))	
69			CM(J,1,2) = CSIN(DEL(J))/CN(J) * CMPLX(0.0,-1.0)	
70			CM(J,2,1) = CSIN(DEL(J)) * CN(J) * CMPLX(0.0,-1.0)	
71		40	CM(J,2,2) = CM(J,1,1)	
73		40	CML(1,1) = CM(1,1,1) * CM(2,1,1) + CM(1,1,2) * CM(2,2,1)	
74			CML(1,2) = CM(1,1,1) * CM(2,1,2) + CM(1,1,2) * CM(2,2,2)	
75			CML(2,1) = CM(1,2,1) * CM(2,1,1) + CM(1,2,2) * CM(2,2,1)	
/6 77			CML(2,2) = CM(1,2,1) * CM(2,1,2) + CM(1,2,2) * CM(2,2,2) X=CML(1,1) + CML(1,2) * CBASE	
78			Y = CML(2,1) + CML(2,2) * CBASE	
79			R=(X-Y)/(X+Y)	
80			S=CABS(R)	
81			$RL=S^{2}$ FL=ATAN2(ATMAG(R), REAL(R))	
83			EL=EL/3.14159	
84			X = CM(2,1,1) + CM(2,1,2) * CBASE	
85			Y = CM(2,2,1) + CM(2,2,2) * CBASE	
85			R = (X - Y) / (X + Y) $S = C A B S (P)$	
88			RS=S**2	
89			ES=ATAN2(AIMAG(R),REAL(R))	
90			ES=ES/3.14159	
92			C=4.U^T(I)/WAVEL TE(RS LT RL) THEN	
93			RO=RS/RL	
94			ELSE	
95			RO=RL/RS	
96			END IF FO-FS-FI+C	
98			$CSE=COS(3.14159 \times EO)$	
99			WRITE(IOUT,80)T(1),RL,RS,EL,ES,C,RO,EO,CSE	
100	С			
101	C		INCREMENT THE PATTERNED LAYER THICKNESS BY 0.002 UM	
102			T(1)=T(1)+0.002	
104			GO TO 20	
105		60	CONTINUE	
106			CLOSE(UNIT=IOUT)	
108		80	FORMAT(9F8.3)	
109			END	
110	(E	OF)		

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TEST CASE FOR TH2LR

FOR PATTERNED LAYER, MAX THICKNESS IS .2 AND INDEX IS (1.46,0.) FOR INTERMEDIATE LAYER, THICKNESS IS 0. AND INDEX IS (1.46,0.) INDEX OF SUBSTRATE IS (4.1,.1) 1 2 3

4

5	THIS PROC	GRAM VAR	IES THIC	KNESS OF	PATTERNED LAYER				
6 7	THICK	R-PAT	R-INT	P-PAT	P-INT	DELAY	RNORM	PNORM	COS-P
7 8 9 0 11 12 14 15 16 17 18 9	THICK .000 .002 .004 .006 .008 .010 .012 .014 .016 .018 .020	R-PAT .370 .369 .369 .367 .366 .363 .361 .358 .354 .354 .350 .346	R-INT .370 .370 .370 .370 .370 .370 .370 .370	P-PAT 996 982 968 954 940 926 911 897 882 868 853	P-INT 996 996 996 996 996 996 996 996 996 996 996	DELAY .000 .015 .030 .045 .060 .075 .091 .106 .121 .136 .151	RNORM 1.000 .999 .997 .993 .989 .983 .976 .968 .958 .958 .947 .936	PNORM .000 .001 .002 .003 .004 .005 .006 .007 .007 .007 .008 .008	COS-P 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000
20 21 22 23 24 25 26 27 28 20	.022 .024 .026 .028 .030 .032 .034 .036 .038 .040	.341 .336 .330 .324 .318 .311 .303 .296 .288 .280	. 370 . 370	838 823 807 792 776 760 743 726 709 692	996 996 996 996 996 996 996 996 996 996	.166 .181 .196 .211 .226 .242 .257 .272 .287 .302	.923 .908 .893 .877 .859 .840 .821 .800 .779 .756	.008 .008 .007 .006 .005 .004 .002 .000 003	1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000 1.000
31 32 33 35 36 37 39 40 41	.042 .044 .046 .048 .050 .052 .054 .056 .058 .060 .062 .064	.271 .262 .253 .244 .234 .225 .215 .206 .196 .187 .177 .168	.370 .370 .370 .370 .370 .370 .370 .370	674 655 636 617 597 576 554 532 510 486 461 436	996 996 996 996 996 996 996 996 996 996 996	. 317 . 332 . 347 . 362 . 377 . 392 . 408 . 423 . 438 . 453 . 468 . 483	.733 .709 .685 .660 .634 .608 .582 .556 .530 .505 .480 .455	009 013 017 022 028 034 041 049 057 067 077	1.000 1.000 .999 .999 .998 .996 .994 .992 .988 .984 .971
42 43 44 45 46 47 48 50 52 53 53	.066 .068 .070 .072 .074 .076 .078 .080 .082 .084 .086 .088	.159 .151 .143 .135 .128 .122 .117 .112 .108 .104 .102 .101	.370 .370 .370 .370 .370 .370 .370 .370	409 381 352 322 291 259 225 190 154 118 080 042 003	996 996 996 996 996 996 996 996 996 996 996 996 996	.498 .513 .528 .543 .558 .574 .589 .604 .619 .634 .649 .664 .664	.431 .408 .387 .366 .347 .330 .315 .302 .291 .282 .276 .272 .270	089 101 115 130 146 164 164 182 202 223 244 267 290 313	.961 .950 .935 .918 .896 .871 .841 .806 .765 .719 .669 .613

5567 55755 506123 4567 6901 771	.092 .094 .096 .098 .100 .102 .104 .106 .108 .110 .112 .114 .116 .118 .120 .122 .124	.100 .102 .104 .107 .111 .116 .121 .127 .134 .142 .149 .158 .167 .176 .185 .194 .204	. 370 . 370	.035 .073 .111 .148 .184 .219 .253 .286 .317 .347 .376 .404 .431 .457 .481 .505 .528	996 996	.694 .709 .725 .740 .755 .770 .785 .800 .815 .830 .845 .860 .845 .860 .875 .891 .906 .921 .936	.271 .275 .281 .289 .300 .313 .328 .344 .363 .344 .363 .383 .404 .427 .451 .475 .500 .526 .552	337 360 382 404 425 445 464 482 498 513 527 540 551 562 572 581 588	.491 .426 .361 .296 .233 .171 .113 .058 .007 041 084 124 124 161 194 224 250 274
72 73 74	.126 .128	.214 .223	.370 .370 .370	.551 .572 .593	996 996 996	.951 .966 .981	.578 .604	596 602 608	296 315 - 332
75 76	.132	.242	.370	.613	996 996	.996	.655	613 617	347 360
77 78 79	.136 .138 .140	.261 .270 .278	.370 .370 .370	.652 .670 .688	996 996 996	1.026 1.042 1.057	.705 .729 .752	621 625 628	372 382 391
80 81	.142	.286	.370	.706	996 996	1.072	.775	630 632	398 404
82 83 84	.148 .148 .150	.302 .309 .316	.370 .370 .370	.740 .757 .773	996 996 996	1.102 1.117 1.132	.817 .837 .856	634 636 637	409 414 417
85 86 87	.152 .154	.323 .329	.370.370	.789 .805	996 996	1.147 1.162	.874 .890	638 638	419 421
88 89	.158	.340 .345	.370 .370	.820 .835 .850	996 996	1.192	.920 .933	639 639	422 422 422
90 91 92	.162 .164	.350 .354 357	.370 .370 370	.865 .880 894	996 996 - 996	1.223 1.238 1.253	.945 .956 966	638 638 637	421 420 - 418
93 94	.168 .170	.360	.370	.909	996 996	1.268	.974	637 636	416 414
95 96 97	.172 .174 .176	.365 .367 .368	.370 .370 .370	.937 .951 .965	996 996 996	1.298 1.313 1.328	.988 .993 .996	635 634 633	412 409 406
98 99	.178	.369	.370	.979 .993	996 996	1.343	.999	632 631	403 400
100 101 102	.182 .184 .186	.370 .369 .368	.370 .370 .370	993 978 964	996 996 996	1.374 1.389 1.404	1.000 .999 .996	1.370 1.371 1.372	397 394 391
103	.188	.367	.370	950 936	996 996	1.419	.992	1.373	388
105 106 107	.192 .194 .196	.363 .360 .357	.370 .370 370	922 908 - 893	996 996 - 996	1.449 1.464 1.479	.981 .974 .965	1.375 1.376 1.377	382 380 378
108	.198	.353	.370	879	996	1.494	.956	1.377	377

1	0	PROGRAM TH2SV
2345		THIS PROGRAM COMPUTES THE RELATIVE REFLECTANCE AND PHASE DIFFER- ENCE FOR A PATTERNED LAYER WITH A SUBLAYER AND SUBSTRATE BOTH OF WHICH MAY HAVE COMPLEX INDICES.
7	C	THIS PROGRAM WAS WRITTEN BY D. NYYSSONEN, CD METROLOGY, INC.
9	C	******************
10 11 12 13 14		PATTERNED LAYER THICKNESS IS HELD CONSTANT, WHILE THE INTERMEDIATE LAYER THICKNESS VARIES FROM 0 TO A MAXIMUM VALUE (TO BE INPUT). THE INTERMEDIATE LAYER THICKNESSES ARE INCREMENTED IN STEPS OF 0.002 MICROMETERS 20 ANGSTROMS).
16	C	***************************************
18	C	OUTPUT IS ON LOGICAL UNIT IOUT
20 21 22 23 24	C	<pre>DIMENSION T(2) COMPLEX CM(2,2,2),DEL(2),CN(2),CBASE,CML(2,2),WAVEL, * X,Y,R DATA IOUT/10/ OPEN(IOUT.FILE='TAPE10')</pre>
25	C	WAVELENGTH OF LIGHT USED=0 53 MICROMETERS
27	C	WAVELENGIN OF EIGNI OBED 0.00 MICROMETERD.
20 29	С	WAVEL-0.55
30 31 32	C C C	THICKNESS ENTERED FOR INTERMEDIATE LAYER IS MAXIMUM THICKNESS FOR WHICH CALCULATIONS ARE MADE, INCREMENT IS 0.002 UM
33	с С	PRINT*, 'ENTER THE NUMBER OF DIFFERENT PATTERN LAYER'
35		PRINT*, 'THICKNESSES TO BE EXPLORED'
37 38 39 40		READ*,K DO 60 L=1,K PRINT*, 'INPUT THICKNESS AND COMPLEX INDICES OF LAYERS WITH', * ' PATTERNED LAYER FIRST'
42 43 44	C	READ *, T(1), CN(1) PRINT*, ' INPUT MAX. THICKNESS AND COMPLEX INDICES OF', * ' INTERMEDIATE LAYER'
46 47 48	c	READ*, T(2), CN(2) PRINT*, 'INPUT COMPLEX INDEX OF SUBSTRATE'
49 50 51 52 53 54		<pre>READ*, CBASE WRITE(IOUT,*) 'FOR PATTERNED LAYER, THICKNESS IS ', T(1), * 'AND INDEX IS ', CN(1) WRITE(IOUT,*) 'FOR INTERMEDIATE LAYER, THICKNESS IS ', T(2), * 'AND INDEX OF ', CN(2) WRITE(IOUT,*) 'INDEX OF SUBSTRATE IS ', CBASE</pre>

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55			WRITE(IOUT, *)
56			WRITE(IOUT, *) 'THIS PROGRAM VARIES THICKNESS OF INTERMEDIATE',
57		3	LAYER'
58			WRITE(IOUT, *) ' THICK R-PAT R-INT P-PAT P-INT DELAY'
59		3	RNO RM PNORM COS-P'
60			TMAX=T(2)
61			T(2)=0.0
62		20	DO 40 J=1,2
63			DEL(J) = 6.28318 * CN(J) * T(J) / WAVEL
64			CM(J,1,1)=COS(DEL(J))
65			CM(J,1,2) = SIN(DEL(J))/CN(J) * CMPLX(0.0,-1.0)
66			CM(J, 2, 1) = SIN(DEL(J)) * CN(J) * CMPLX(0.0, -1.0)
67			CM(J, 2, 2) = CM(J, 1, 1)
68		40	CONTINUE
69			CML(1,1) = CM(1,1,1) * CM(2,1,1) + CM(1,1,2) * CM(2,2,1)
/0			CML(1,2) = CM(1,1,1) * CM(2,1,2) + CM(1,1,2) * CM(2,2,2)
/1			CML(2,1) = CM(1,2,1) * CM(2,1,1) + CM(1,2,2) * CM(2,2,1)
72			CML(2,2) = CM(1,2,1) * CM(2,1,2) + CM(1,2,2) * CM(2,2,2)
/3			X = CML(1,1) + CML(1,2) * CBASE
74			Y = CML(2, 1) + CML(2, 2) + CBASE
75			R = (X - Y) / (X + Y)
0/ 77			
70			$K \Box = S^{2}$
70			EL-AIAN2(AIMAG(R), REAL(R))
80			V = CM(2 + 1) + CM(2 + 2) * CBASE
81			X = CM(2, 1, 1) + CM(2, 1, 2) + CBASE Y = CM(2, 2, 1) + CM(2, 2, 2) + CBASE
82			P = (X - V) / (X + V)
83			S=CABS(B)
84			BS=S**2
85			ES=ATAN2(ATMAG(R), REAL(R))
86			ES=ES/3.14159
87			C=4.0*T(1)/WAVEL
88			IF (RS.LT.RL) THEN
89			RO=RS/RL
90			ELSE
91			RO=RL/RS
92			END IF
93			EO=ES-EL+C
94			CSE=COS(3.14159*EO)
95			WRITE(IOUT,80)T(2),RL,RS,EL,ES,C,RO,EO,CSE
96	С		
97			IF(T(2).GE.TMAX)THEN
98			GO TO 60
99			ENDIF
100			T(2)=T(2)+0.002
101		~~	GO TO ZU
102		60	
103			CLOSE(UNIT=IOUT)
104		00	
104		٥U	EORIAL(310.3)
		יסי	
101		n J	

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TEST CASE FOR TH2SV

4									
5	THIS PRO	GRAM VARI	ES THIC	KNESS OF	INTERMED	DIATE LAN	YER		
6	THICK	R-PAT	R-INT	P-PAT 207	P-INT	DELAY	RNORM	PNORM	COS-P
/	.000	.647	.370	89/	996	.604	.572	.505	015
8	.002	.64/	.369	89/	982	.604	.5/1	.519	059
9	.004	.647	.369	897	968	.604	.570	.533	103
10	.006	.647	.367	897	954	.604	.568	.547	147
11	.008	.647	.366	897	940	.604	.565	.561	191
12	.010	.647	.363	89/	926	.604	.562	.575	234
13	.012	.647	.361	89/	911	.604	.558	.590	278
14	.014	.64/	.358	897	897	.604	.553	.604	321
15	.016	.647	.354	897	882	.604	.548	.618	364
16	.018	.647	.350	897	868	.604	.542	.633	406
17	.020	.647	.346	897	853	.604	.535	.648	448
18	.022	.647	.341	897	838	.604	.527	.663	490
19	.024	.647	.336	897	823	.604	.519	.678	531
20	.026	.647	.330	897	807	.604	.510	.693	571
21	.028	.647	.324	897	792	.604	.501	.709	611
22	.030	.647	.318	897	776	.604	.491	.725	649
23	.032	.647	.311	897	760	.604	.480	.741	687
24	.034	.647	.303	897	743	.604	.469	.758	724
25	.036	.647	.296	897	726	.604	.457	.774	759
26	.038	.647	.288	897	709	.604	.445	.792	793
27	.040	.647	.280	897	692	.604	.432	.809	826
28	.042	.647	.271	897	674	.604	.419	.827	856
29	.044	.647	.262	897	655	.604	.405	.846	885
30	.046	.647	.253	897	636	.604	.391	.865	911
31	.048	.647	.244	897	617	.604	.377	.884	934
32	.050	.647	.234	897	597	.604	.362	.904	955
33	.052	.647	.225	897	576	.604	.348	.925	972
34	.054	.647	.215	897	554	.604	.333	.946	986
35	.056	.647	.206	897	532	.604	.318	.968	995
36	.058	.647	.196	897	510	.604	.303	.991	-1.000
37	.060	.647	.187	897	486	.604	.288	1.015	999
38	.062	.647	.177	897	461	.604	.274	1.040	992
39	.064	.647	.168	897	436	.604	.260	1.065	979
40	.066	.647	.159	897	409	.604	.246	1.092	959
41	.068	.647	.151	897	381	.604	.233	1.119	930
42	.070	.647	.143	897	352	.604	.221	1.148	894
43	.072	.647	.135	897	322	.604	.209	1.178	847
44	.074	.647	.128	897	291	.604	.199	1.209	791
45	.076	.647	.122	897	259	.604	.189	1.242	725
46	.078	.647	.117	897	225	.604	.180	1.276	648
47	.080	.647	.112	897	190	.604	.173	1.310	561
48	.082	.647	.108	897	154	.604	.166	1.346	464
49	.084	.647	.104	897	118	.604	.161	1.383	359
50	.086	.647	.102	897	080	.604	.158	1.421	247
51	.088	.647	.101	897	042	.604	.155	1.459	129
52	.090	.647	.100	897	003	.604	.155	1.497	009
53	.092	.647	.100	897	.035	.604	.155	1.536	.112
51	094	617	102	_ 007	073	604	157	1 574	770

55	.096	. 647	.104	897	.111	. 604	161	1 612	311
5.0			. 104	.057	• • • •		. 101	1.012	• 7 4 4
56	.098	.647	.107	897	.148	.604	.165	1.649	.450
57	100	617	111	_ 007	104	601	171	1 (05	E 4 0
57	.100	.04/	• + + +	09/	.104	.004	• 1 / 1	1.080	. 548
58	.102	.647	.116	897	.219	.604	.179	1.720	637
50	104	647	101	007	000			1.720	.007
59	.104	.64/	.121	897	. 253	.604	.187	1.754	.715
60	106	647	127	- 207	286	601	107	1 796	702
00	.100	.04/	• 1 2 /	097	.200	• 0 0 · ·	• 1 9 /	1./00	. / 0 3
61	.108	.647	.134	897	.317	.604	.207	1.818	. 840
60	110	617	140	007	347	604	210	1 0 4 0	0.00
02	.110	.04/	•142	897	.34/	.004	.219	1.848	.888
63	.112	.647	.149	- 897	. 376	604	231	1 877	926
<u> </u>							• 2 3 1	1.077	
64	•114	.64/	.128	89/	.404	.604	.244	1.905	.956
65	116	647	167	- 897	431	604	258	1 932	977
0.5	. 110	.047	. 107	.057	. 401	.004	. 200	1.932	• 311
66	.118	.647	.176	897	.457	.604	.272	1.957	.991
67	120	617	195	- 207	491	604	286	1 0 9 2	000
07	.120	.047	.107	091	• 40 L	.004	,200	1.902	
68	.122	.647	.194	897	.505	.604	.301	2.006	1.000
60	104	C 17	204	007	500	604	215	2 0 2 0	000
69	• 1 2 4	• 0 4 /	.204	09/	. 520	.004	* 2 T 2	2.029	. 990
70	.126	. 647	. 214	897	. 551	.604	.330	2.051	.987
	100	647	222	007		C 0 4	245	2 072	074
/ 1	.128	.647	. 223	897	.572	.004	.345	2.073	.9/4
72	.130	647	233	- 897	. 593	. 604	.360	2.094	957
72	. 100	.047	. 2 3 3	.027				2.034	
73	.132	.647	.242	89/	.613	.604	.375	2.114	.937
71	13/	617	252	- 897	633	604	280	2 1 2 2	012
/ 4	• 1 7 4	.04/	. 252	057	.055	.004		2.100	. 212
75	.136	.647	.261	897	.652	.604	.403	2.152	.888
76	120	617	270	- 907	670	601	117	2 171	050
/0	. 720	.04/	.270	09/	.0/0	.004	.41/	2.1/1	.009
77	.140	.647	.278	897	.688	.604	.430	2.189	.829
70	1 4 3	647	200	007	700	C D A	4 4 3	2 207	700
10	.142	• 0 4 7	.200	09/	./00	.004	.443	2.207	./90
79	.144	. 647	. 294	897	.723	.604	. 455	2.224	. 762
	140	6 4 7	200	007	740	<u> </u>	467	2 2 4 1	
80	.146	.64/	.302	897	./40	.604	.40/	2.241	.121
81	148	647	309	- 897	.757	. 604	. 479	2.257	. 690
00	1 5 0	C 4 7		007			400	0.074	
82	.150	.64/	.316	89/	.//3	.604	.489	2.2/4	.653
83	152	647	222	- 897	789	604	499	2,290	614
0.5	• 1 7 2	.047		.057	. / 0 /		500	2.220	.014
84	.154	.647	.329	897	.805	.604	.509	2.305	.5/4
85	156	617	335	- 897	820	604	518	2 321	534
0.5	.100	.047		.057	.020		. 510	2.021	
86	.158	.647	.340	897	.835	.604	.526	2.336	. 493
87	160	617	315	- 207	850	604	531	2 351	451
07	.100	.04/	. 545	051	.0.00	.004		2.001	• 4 7 1
88	.162	.647	.350	897	.865	.604	.541	2.366	.409
00	161	617	254	- 007	000	604	517	2 280	367
07	• 104	• 0 4 /	.304	09/	.000	.004	• 247	2.300	. 507
90	.166	.647	.357	897	.894	.604	.552	2.395	.324
01	1 0	647	200	007	000	C 0 4	5 5 7	2 100	201
91	.108	.04/	.360	89/	.909	.004	. 227	2.409	.201
92	.170	.647	.363	897	.923	.604	.561	2.424	.237
0.0	170	647	200	007	007	C 0 4	ECE	2 120	101
93	• 1 / 2	.64/	.305	89/	.937	.604	. 202	2.430	.174
94	.174	. 647	. 367	897	. 951	. 604	.568	2.452	.150
0.5	171				0.75	C 0 4	570	2 400	100
95	.1/6	.64/	.368	897	.965	.604	.5/0	2.400	.100
96	178	647	369	- 897	979	604	. 571	2.480	.062
20	. 170	.047		.057				2.100	010
97	.180	.647	.370	897	.993	.604	.512	2.494	.018
0.0	190	617	270	- 997	- 003	604	572	508	- 026
20	.102	• 04 /	. 370	071		.004	. 212	. 500	.020
99	.184	.647	.369	897	978	.604	.571	.522	070
100	100	C 17	200	007	064	604	560	526	- 11/
100	• 190	•04/	. 308	89/	904	.004	. 202	. 220	
101	.188	.647	.367	- 897	-,950	.604	.567	.550	158
100	100	C 4 7					ECA	ECE	- 201
102	.130	• 64 /	.365	89/	936	.004	. 204	. 202	201
103	. 192	. 647	363	- 897	-,922	. 604	.561	.579	245
101						C 0 4	E E 7	500	- 200
104	.194	.64/	.360	897	908	.604	. > > /	. 2.2.2	200
105	196	647	357	- 897	- 893	.604	.552	.607	331
100		.047		.027		C 0 4	EAC	600	- 274
T06	.198	.647	.353	897	8/9	.604	.546	.022	5/4
107	200	647	210	- 207	- 864	.604	.540	.637	416
107	.200	.047	• • • • •	.091	.004			650	AEO
T08	.202	.647	.345	897	849	.604	.533	.652	408

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Appendix II - Software for Calculation of Partially Coherent Imaging of Planar Line Objects

PROGRAM PCIMAG2 1 2 C PROFPLAY.MAIN 3 C 5 C 6 C THIS IS THE MAIN PROGRAM FOR COMPUTING PARTIALLY COHERENT 7 C IMAGERY OF 1-D PERIODIC OBJECTS. 8 C 9 C THE COMPUTATIONS EMPLOY THE METHODS OF FOURIER OPTICS. 10 C 11 C THIS PROGRAM CONTROLS THE FLOW OF THE CALCULATIONS BY TESTING 12 C CERTAIN INPUT PARAMETERS. IT ALLOWS FOR THE CHOICE OF 1-D OR 2-D OPTICS, AND THE INPUT PARAMETERS CAN BE CHANGED WITHOUT HALTING 13 C 14 C THE EXECUTION OF THE PROGRAM. 15 C 17 C 18 C PARAMETER DEFINITIONS -19 C LINEWIDTH OF OBJECT IN MICROMETERS 20 C WIDTH WT HALF-WIDTH OF FOREGROUND OBJECT 21 C 22 C PER ----PERIOD 23 C XIR -FUNDAMENTAL FREQUENCY 24 C 26 C 27 CHARACTER*2 ANSWER CHARACTER*5 TYPE 28 CHARACTER*12 SIZE 29 COMMON WIDTH, WAVE, OBJ, SSO, SAO, AB2, AB4, AP, TBO, PB, TTO, PT, SLIT, 30 31 DATAS(13) COMMON/PAR/PI, TWOPI 32 COMMON/MN/XIR, WT, PER, NX 33 COMMON/IM/DUM1(2000),NX1,DUM2,DUM3,DUM4 34 35 COMMON/IO/INA, IOUTA, IOUTB 36 DATA INA, IOUTA, IOUTB/10, 16, 40/ 37 PI=4.0 * ATAN(1.0)38 TWOPI=2.0*PI 39 OPEN (UNIT=INA, FILE='INDATA') OPEN (UNIT=IOUTA, FILE='PRTDATA') 40 OPEN (UNIT=IOUTB, FILE='PLOTDAT') 41 42 C 44 C SUMMARY OF THE INPUT/OUTPUT STRUCTURE. 45 C 46 C-----47 C LOGICAL UNIT DEFINITION 48 C FILE VARIABLE 49 C INPUT DATA FILE INDATA 10 50 C INA IOUTA OUTPUT DATA FILE - PRINTER 51 C PRTDATA 16 52 C OJTPUT DATA FILE - PLOTTER IOUTB 40 PLOTDAT 53 C 55 C 56 PRINT* 57 READ(INA, *)ANSWER 58 C 60 C

61 C READ THE INPUT PARAMETERS THAT CHARACTERIZE THE OPTICAL SYSTEM. 62 C CONVERT INPUT DATA FOR INTENSITY TRANSMITTANCE (OR REFLECTANCE) 63 C AND PHASE OF THE OBJECT TO COMPLEX AMPLITUDE TRANSMITTANCE 64 C (OR REFLECTANCE). 65 C 67 C 68 100 CALL RDATA 69 C 71 C TEST 'WIDTH' INPUT PARAMETER. 72 C THE WIDTH CAN VARY FROM 0.01 TO 10.00 MICROMETERS. 73 C 74 C 75 C NOTE: WIDTH IS MULTIPLIED BY 2 WHEN CALCULATING 'NX' IN ORDER 76 C TO VIEW THE BEHAVIOR OF THE INTENSITY PROFILE OF LINES 77 C OR SPACES FURTHER FROM THE EDGE. 78 C 79 C AN ERROR MESSAGE OCCURS IF THE WIDTH LIES OUTSIDE THIS RANGE-80 C THE PROGRAM THEN DEMANDS A NEW SET OF INPUT DATA 81 C 83 C 84 200 IF(WIDTH.GT.2.5.OR.WIDTH.LE.10.0) THEN WT=0.1 85 86 PER=5.0*WIDTH SIZE='GREATER THAN' 87 NX=100.0*WIDTH+0.0001 88 ELSEIF(WIDTH.LE.2.5.AND.WIDTH.GT.0.0) THEN 89 90 WT=WIDTH/10.0 PER=5.0 91 SIZE='LESS THAN' 92 NX=100.0*WIDTH*2.0+0.0001 93 94 ELSE 95 PRINT*, 'ERROR IN WIDTH. PROGRAM STOPS.' 96 STOP 97 ENDIF 98 XIR=WAVE/(PER*OBJ) 99 C 101 C 102 C COMPUTE THE COMPLEX FOURIER COEFFICIENTS, A(N), OF A PERIODIC 103 C OBJECT WITH A SYMMETRIC RECTANGULAR WAVEFORM. 104 C 106 C 107 CALL OBJECT 108 C 110 C 111 C COMPUTE THE REAL FOURIER COEFFICIENTS, C(N), WHICH CHARACTERIZE 112 C 'THE INTENSITY DISTRIBUTION IN THE IMAGE PLANE. 113 C 114 C ('CROSID' IS CALLED FOR 1-D OPTICS, WHILE 'CROS2D' IS CALLED FOR 115 C 2-D OPTICS.) 116 C 118 C 119 IF (ANSWER.EQ. '1D') THEN

120

CALL CROS1D

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ELSE 121 122 CALL CROS2D 123 ENDIF 124 C 126 C 127 C INCLUDE THE EFFECT OF A SCANNING SLIT IN THE IMAGE PLANE BY 128 C ADJUSTING THE VALUES OF THE REAL FOURIER COEFFICIENTS, C(N). 129 C (THIS IS NOT NECESSARY IF THE SLIT IS LESS THAN 0.01 MICRCMETERS 130 C IN WIDTH.) 131 C 133 C IF(SLIT.GE.0.01) CALL CSLIT 134 135 C 137 C 138 C CALCULATE THE INTENSITY DISTRIBUTION OF A PLANAR OBJECT USING 139 C PARTIALLY COHERENT IMAGING FORMULAS. 140 C 142 C 143 CALL IMAGE 144 C 146 C 147 C TEST FOREGROUND TRANSMITTANCE IN ORDER TO SET CERTAIN PARAMETERS 148 C PRIOR TO NORMALIZATION. 149 C 151 C 152 IF(TTO.EQ.1.0)THEN 153 NUM=1 154 TYPE='SPACE' 155 ELSE 156 NUM=NX1 157 TYPE='LINE' 158 ENDIF 159 C 161 C 162 CALL YNORM(NUM) 163 C 165 C 166 C PRINT A TABLE OF NORMALIZED INTENSITY VERSUS DISTANCE ONTO AN OUTPUT DEVICE. ALSO PRINT TWO COLUMNS OF INTENSITY AND 167 C 168 C DISTANCE OUT TO FILE PLOTDAT FOR PLOTTING PURPOSES. 169 C 171 C 172 CALL PRINT(TYPE, SIZE, ANSWER) 173 C 175 C 176 CLOSE(UNIT=INA) 177 CLOSE(UNIT=IOUTA) 178 CLOSE(UNIT=IOUTB) 179 STOP 180 END

181 C 183 C THIS SUBROUTINE COMPUTES THE COMPLEX FOURIER COEFFICIENTS, A(N), OF 184 C 185 C A PERIODIC OBJECT WITH A SYMMETRIC RECTANGULAR WAVEFORM. 186 C 187 C THE COMPUTED COEFFICIENTS ARE STORED IN LABLED COMMON/ACOEF/. 188 C 190 C 191 SUBROUTINE OBJECT 192 C 194 C 195 COMPLEX TB, TT, A(100), A0, CC COMMON/ACOEF/ A, A0 196 COMMON/MN/DUM1,WT,DUM2,DUM3 197 198 COMMON/RD1/TB,TT 199 COMMON/PAR/PI, TWOPI 200 C 202 C SEE EQUATION #21A, 'METHOD FOR THE CALCULATION OF PARTIALLY COHERENT 203 C 204 C IMAGERY', ERIC KINTNER, J. APPLIED OPTICS, VOL.17, NO.17, PAGE 2747 205 C 206 A0=TB+2.0*(TT-TB)*WT207 C 208 C COMPUTE CONSTANT COMMON TO ALL COEFFICIENTS. 209 C 210 CC=(TT-TB)/PI 211 C 212 C NOTE THE USE OF THE IDENTITY -213 C SIN(N*X) = 2.0*COS(X)*SIN((N-1)*X) - SIN((N-2)*X).214 C 215 COSN=COS(TWOPI*WT) 216 S=0.0 217 S1=-SIN(TWOPI*WT) 218 DO 300 N=1, 100 219 S2=S1 220 S1=S 221 S=2.0*COSN*S1-S2222 $A(N) = CC \times S/N$ 223 300 CONTINUE 224 RETURN 225 END 226 C 228 C THIS SUBROUTINE COMPUTES THE REAL FOURIER COEFFICIENTS, C(N), WHEN 229 C 230 C THE 1-D OPTION OF THE PROGRAM IS SELECTED. 231 C 233 C 234 SUBROUTINE CROS1D 235 C 237 C 238 COMMON WIDTH, WAVE, OBJ, SSO, SAO, AB2, AB4, AP 239 COMMON/MN/XIR, DUM1, DUM2, DUM3 240 COMMON/RD2/SS,SA

COMMON/CROS/C(325),LJ,LJ1,CO 241 COMPLEX CCF1D, A 242 243 C 245 C 246 C SEE EQUATION #18, 'METHOD FOR THE CALCULATION OF PARTIALLY COHERENT 247 C IMAGERY', ERIC KINTNER, J. APPLIED OPTICS, VOL.17, NO.17, PAGE 2747 FOR THE MATHEMATICAL FORMULATION OF THE FOURIER COEFFICIENTS, C(N). 248 C 249 C 251 C 252 C COMPUTE THE NUMBER OF FOURIER COEFFICIENTS NEEDED IN THE SUMMATION 253 C WITHOUT EFFECTING THE ACCURACY. 254 C 255 LJ=2.0/XIR+1.0 256 LJ1=LJ+1257 LN0=(1.0+SS)/XIR+1.0258 C 259 C TEMPORARILY SET AB2 AND AB4 TO ZERO BEFORE ENTERING CCF1D FUNCTION 260 C THROUGH CNORM1. 261 C 262 TEMP1=AB2 263 TEMP2=AB4 264 AB2=0.0 265 AB4=0.0 266 C 267 C COMPUTE NORMALIZING FACTOR FOR COEFFICIENTS (CNO). THIS IS DONE 268 C THROUGH THE FUNCTION CNORM1. 269 C 270 CN0=CNORM1(SA) 271 C 272 C SET AB2 AND AB4 BACK TO THEIR ORIGINAL VALUES. 273 C 274 AB2=TEMP1 275 AB4=TEMP2 276 C 277 C CALCULATE THE FOURIER COEFFICIENTS CORRESPONDING TO THE PRIMARY 278 C AXIS FIRST (CO). 279 C CO=CABS(A(0)) * * 2.0 * CCF1D(0.0,0,0)280 281 DO 300 N=1, LNO 282 CO=CO+REAL(CABS(A(N))**2*CCF1D(XIR,N,N))283 +CABS(A(-N)) * *2*CCF1D(XIR,-N,-N))1 300 CONTINUE 284 285 C0=C0/CN0286 C 287 C COMPUTE FOURIER COEFFICIENTS, C(N), VIA EQUATION #18 (KINTNER'S REF.) 288 C 289 DO 500 J=1, LJ 290 LN=LN0+J 291 CT=REAL(A(J)*CONJG(A(0))*CCF1D(XIR,J,0))292 DO 400 N=1, LN 293 CT=CT+REAL(A(J+N)*CONJG(A(N))*CCF1D(XIR,J+N,N)294 +A(J-N)*CONJG(A(-N))*CCF1D(XIR,J-N,-N))1 400 295 CONTINUE 296 C(J) = CT/CN0297 500 CONTINUE 298 RETURN 299 END 300 C

302 C 303 C THIS FUNCTION RETRIEVES THE FOURIER COEFFICIENTS FROM COMMON/A/. 304 C IT IS CALLED FROM THE FUNCTION CCF1D AND CCF2D. 305 C 307 C 308 COMPLEX FUNCTION A(N) 309 C 311 C 312 COMPLEX AA(100), A0 313 COMMON/ACOEF/ AA, AO 314 C 316 C NA=IABS(N) 317 IF (NA .GT. 100) THEN 318 310 A=(0.0,0.0) 320 RETURN 321 ELSEIF(NA .EQ. 0) THEN 322 A=A0 323 RETURN 324 ELSE 325 A=AA(NA)326 RETURN ENDIF 327 328 END 329 C 331 C 332 C FUNCTION TO NORMALIZE IMAGERY. 333 C FOR BRIGHT-FIELD IMAGERY, FIELD IS UNITY. 334 C FOR DARK-FIELD IMAGERY, FIELD WITHOUT SOURCE STOP IS UNITY. 335 C 336 C THIS FUNCTION IS CALLED FROM THE SUBROUTINE CROS1D (ONLY NEEDED 337 C WHEN THE 1-D OPTION OF THE PROGRAM IS USED). 338 C 340 C 341 FUNCTION CNORM1(SA) 342 C 344 C 345 IF(SA .GE. 1.0) THEN 346 CNORM1=1.0 347 RETURN 348 ELSE 349 CNORM1 = REAL(CCF1D(0.0,0,0))350 RETURN 351 ENDIF 352 END 353 C 355 C 356 C FUNCTION TO NORMALIZE IMAGERY. 357 C FOR BRIGHT-FIELD IMAGERY, FIELD IS UNITY. 358 C FOR DARK-FIELD IMAGERY, FIELD WITHOUT SOURCE STOP IS UNITY. 359 C 360 C THIS FUNCTION IS CALLED FROM THE SUBROUTINE CROS2D (ONLY NEEDED

361 C WHEN THE 2-D OPTION OF THE PROGRAM IS USED). 362 C 364 C 365 FUNCTION CNORM2(SA) 366 C 368 C IF(SA .GE. 1.0) THEN 369 370 CNORM2=1.0371 RETURN 372 ELSE 373 CNORM2 = REAL(CCF2D(0.0,0,0))374 RETURN 375 ENDIF 376 END 377 C 379 C 380 C FUNCTION TO COMPUTE THE TRANSMISSION CROSS-COEFFICIENT FOR A 381 C ONE DIMENSIONAL PARTIALLY COHERENT IMAGING SYSTEM WITH 382 C DEFOCUSING, SPHERICAL ABERRATION, AND GAUSSIAN APODIZATION OF 383 C BOTH SOURCE AND PUPIL. 384 C 385 C (USED ONLY WITH THE 1-D OPTION OF THE PROGRAM) 386 C 388 C 389 COMPLEX FUNCTION CCF1D(XIR,N1,N2) 390 C 392 C 393 C PARAMETER DEFINITIONS -394 C XIR - FUNDAMENTAL FREQUENCY. 395 C N1 - HARMONIC FOR FIRST FREQUENCY. 396 C N2 - HARMONIC FOR SECOND FREQUENCY. 397 C SS - SOURCE SIZE. 398 C SA - SOURCE APODIZATION. 399 C AB2 - DEFOCUSING 400 C AB4 - SPHERICAL ABERRATION. AP - PUPIL APODIZATION. 401 C 402 C 403 C ROUTINE ASSUMES THAT (N1 .GE. N2) 404 C 406 C 407 COMPLEX ZERO, SUM, Y 408 COMMON WIDTH, WAVE, OBJ, SSO, SAO, AB2, AB4, AP 409 COMMON/RD2/SS,SA 410 COMMON/PAR/PI, TWOPI 411 DATA ZERO, EPS/(0.0 ,0.0),0.01/ 412 DATA N0/10/ 413 C 415 C 416 X1=N1*XIR 417 X2=N2*XIR 418 CCF1D=ZERO 419 C 420 C IN THE COHERENT LIMIT, USE ALTERNATE ROUTINE.

421 C 422 IF(SS .LT. EPS) GOTO 100 423 C RETURN WITH ZERO IF SOURCE AND TWO PUPILS DO NOT INTERSECT. 424 C 425 C IF((X1-X2) .GT. 2.0) RETURN 426 427 IF((X1-1.0) .GT. SS) RETURN 428 IF(-(1.0+X2) .GT. SS) RETURN429 C 430 C DETERMINE LIMITS OF INTEGRATION. ASSUMI! LIMITS DETERMINED BY 431 C PUPILS UNLESS SOURCE IS SMALLER. 432 C 433 RL2=1.0-X1 434 RL1 = -(1.0 + X2)435 IF(SS .LT. RL2) RL2=SS 436 IF(-SS .GT. RL1) RL1=-SS 437 C SET UP INTEGRATION BY SIMPSON'S RULE. 438 C SCALE THE INTEGRATION INTERVAL TO BE APPROXIMATELY EQUAL FOR 439 C 440 C ALL CASES. (NO IS THE APPROXIMATE NUMBER OF INTERVALS PER UNIT LENGTH.) 441 C 442 C 443 NC=1.0+(RL2-RL1)*N0 DC=(RL2-RL1)/NC 444 445 DC2=DC/2.0446 Q=RL1 447 Q1=Q+X1 448 Q2=Q+X2449 001=01*01 QQ2=Q2*Q2 450 451 AR=SA*Q*Q+AP*(QQ1+QQ2)452 AI=TWOPI*(AB2*(QQ1-QQ2)+AB4*(QQ1*QQ1-QQ2*QQ2)) 453 SUM=CEXP(CMPLX(AR,AI)) DO 50 N=1, NC 454 455 QN=RL1+N*DC 456 Q=QN-DC2 457 Q1=Q+X1 458 Q2=Q+X2459 QQ1=Q1*Q1 QQ2=Q2*Q2 460 461 AR=SA*Q*Q+AP*(QQ1+QQ2)462 AI=TWOPI*(AB2*(QQ1-QQ2)+AB4*(QQ1*QQ1-QQ2*QQ2)) 463 Y=CEXP(CMPLX(AR,AI)) 464 SUM=SUM+4.0*Y Q=QN 465 466 Q1=Q+X1 467 Q2=Q+X2468 QQ1=Q1*Q1 469 $QQ2 = Q2 \times Q2$ 470 AR=SA*Q*Q+AP*(Q01+0Q2) 471 AI=TWOPI*(AB2*(QQ1-QQ2)+AB4*(QQ1*QQ1-QQ2*QQ2)) 472 Y=CEXP(CMPLX(AR,AI)) 473 SUM=SUM+2.0*Y 474 50 CONTINUE 475 C 476 C EXTRA FACTOR OF TWO IN DENOMINATOR CORRECTLY NORMALIZES RESULT. 477 C 478 CCF1D=(SUM-Y)*DC2/6.0479 RETURN 480 C

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481 C ALTERNATE ROUTINE FOR COHERENT LIMIT.
482 C
     100 IF(ABS(X1) .GT. 1.0) RETURN
483
        IF(ABS(X2) .GT. 1.0) RETURN
484
485
        QQ1=X1*X1
486
        QQ2=X2*X2
487
        AR=AP*(QQ1+QQ2)
        AI=TWOPI*(AB2*(QQ1-QQ2)+AB4*(QQ1*QQ1-QQ2*QQ2))
488
489
        CCF1D=CEXP(CMPLX(AR,AI))
490
        RETURN
491
        END
493 C
494 C
     FUNCTION TO COMPUTE TRANSMISSION CROSS-COEFFICIENT FOR CIRCULAR
495 C
     OPTICAL SYSTEM (ANNULAR SOURCE) WITH NO ABERRATIONS OR
496 C
     APODIZATION.
497 C
498 C
     (USED ONLY WITH THE 2-D OPTION OF THE PROGRAM)
499 C
501 C
502 C
     PARAMETER DEFINITIONS -
503 C
            XIR - FUNDAMENTAL FREQUENCY.
504 C
              - HARMONIC FOR FIRST FREQUENCY.
            N1
505 C
            N2
              - HARMONIC FOR SECOND FREQUENCY.
506 C
            SS
              - OUTER RADIUS OF SOURCE ANNULUS.
507 C
            SA
              - INNER RADIUS OF SOURCE ANNULUS.
508 C
509 C
        ROUTINE ASSUMES THAT (N1 .GE. N2).
510 C
512 C
513
        COMPLEX FUNCTION CCF2D(XIR,N1,N2)
514 C
516 C
517
        COMMON/RD2/SS,SA
518
        COMMON/PAR/PI, TWOPI
519 C
521 C
522
        X1=N1*XIR
523
        X2=N2*XIR
        CCF2D = (0.0, 0.0)
524
525 C
526 C
     USE ALTERNATE ROUTINE FOR COHERENT SOURCE.
527 C
        IF(SS .LT. 0.01) THEN
528
529
         GOTO 2000
530
        ENDIF
531 C
532 C
     RETURN WITH ZERO IF SOURCE AND PUPILS DO NOT INTERSECT.
533 C
        IF((X1-X2) .GT. 2.0) RETURN
534
535
        IF((X1-1.0) .GT. SS) RETURN
536
        IF(-(1.0+X2) .GT. SS) RETURN
537 C
538 C
     MAXIMUM AND MINIMUM EXTENT OF INTERSECTION OF TWO PUPILS.
539 C
540
       XMAX=X2+1.0
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XMIN=X1-1.0 541 IFLAG=0 542 543 C SET FLAG IF SOURCE IS ANNULAR - TWO SEPARATE PASSES REQUIRED. 544 C 545 C IF(SA .GT. 0.01) IFLAG=1 546 547 XS=SS 548 100 XS2=XS*XS 549 C 550 C IF SOURCE SIZE IS LESS THAN PUPIL SIZE, USE ALTERNATE ROUTINE. 551 C 552 IF(XS .LT. 1.0) GOTO 400 553 IF(XS .LT. XMAX .OR. -XS .GT. XMIN) GOTO 200 554 C 555 C IF SOURCE ENVELOPES AREA COMMON TO BOTH PUPILS, CALCULATE THIS 556 C AREA. 557 C 558 Y = AREA(1.0, 1.0, (X1-X2))559 GOTO 1100 560 200 IF(XS2 .LE. (X1*X2+1.0)) GOTO 300 561 C 562 C IF REQUIRED AREA IS BOUNDED BY SOURCE AND BOTH PUPILS, CALCULATE 563 C THIS AREA. 564 C 565 Y=AREA(1.0,1.0,(X1-X2))+AREA(XS,1.0,AMIN1(ABS(X1),ABS(X2)))-PI 566 GOTO 1100 567 C 568 C IF REQUIRED AREA IS BOUNDED ONLY BY SOURCE AND ONE PUPIL, 569 C CALCULATE THIS AREA. 570 C 571 300 Y=AREA(XS, 1.0, AMAX1(ABS(X1), ABS(X2)))572 GOTO 1100 573 C 574 C ALTERNATE ROUTINE FOR SOURCE SMALLER THAN PUPIL. 575 C 576 C FIND WHETHER BOUNDARY OF SOURCE EXTENDS BEYOND THE AREA COMMON 577 C TO BOTH PUPILS, IN EITHER DIRECTION. 578 C 579 400 IFL1=0 580 IFL2=0581 IF (XMIN .LE. -XS) IFL1=1 582 IF(XMAX .GE. XS) IFL2=1 IF(IFL1+IFL2-1) 900, 600, 500 583 584 C 585 C IF SOURCE IS ENVELOPED BY AREA COMMON TO BOTH PUPILS, CALCULATE 586 C AREA OF SOURCE. 587 C 588 500 Y=PI*XS2 589 GOTO 1100 590 C 591 C IF REQUIRED AREA IS BOUNDED BY SOURCE AND EITHER PUPIL (ALONE), 592 C CALCULATE AREA IN COMMON BETWEEN SOURCE AND THIS PUPIL. 593 C (ZERO IS IMPOSSIBLE IN IF-STATEMENT AT 600.) 594 C 595 600 IF(IFL1-IFL2) 700, 1100, 800 596 700 Y = AREA(1.0, XS, ABS(X1))597 GOTO 1100 598 800 Y=AREA(1.0,XS,ABS(X2)) 599 GOTO 1100 600 900 IF((X1*X2+1.0) .LE. XS2) GOTO 1000

601 C 602 C IF REQUIRED AREA IS BOUNDED BY SOURCE AND BOTH PUPILS, CALCULATE 603 C THIS AREA. 604 C 605 Y = AREA(1.0, XS, ABS(X1)) + AREA(1.0, XS, ABS(X2)) - PI * XS2606 GOTO 1100 607 C 608 C IF SOURCE ENVELOPES AREA COMMON TO BOTH PUPILS, CALCULATE THIS 609 C AREA. 610 C 611 1000 Y = AREA(1.0, 1.0, (X1-X2))612 GOTO 1100 613 C 614 C CHECK FLAG FOR CIRCULAR SOURCE, OR FIRST OR SECOND PASS WITH 615 C ANNULAR SOURCE. 616 C 617 1100 IF(IFLAG-1) 1500, 1600, 1700 618 C 619 C FOR CIRCULAR SOURCE, NORMALIZE AND RETURN. 620 C 1500 CCF2D=Y/PI 621 RETURN 622 623 C FOR FIRST PASS WITH ANNULAR SOURCE, SAVE RESULTS FROM OUTER 624 C BOUNDARY OF ANNULUS, SET INNER BOUNDARY AS BOUNDARY OF INNER 625 C 626 C SOURCE. 627 C 628 1600 IFLAG=2 629 CCF2D=Y Y=0.0 630 631 XS=SA IF((X1-1.0) .GT. SA) GOTO 1100 632 IF(-(X2+1.0) .GT. SA) GOTO 1100 633 634 GOTO 100 635 C 636 C FOR SECOND PASS WITH ANNULAR SOURCE, SUBTRACT RESULTS OF INNER 637 C SOURCE FROM SAVED RESULTS OF OUTER SOURCE. NORMALIZE AND RETURN. 638 C 639 1700 CCF2D=(CCF2D-Y)/PI 640 RETURN 641 C 642 C ALTERNATE ROUTINE FOR COHERENT SOURCE. 643 C 644 2000 IF(ABS(X1) .GT. 1.0) RETURN 645 IF(ABS(X2) .GT. 1.0) RETURN 646 CCF2D = (1.0, 0.0)647 RETURN 648 END 649 C 651 C 652 C FUNCTION TO COMPUTE THE AREA COMMON TO TWO DISPLACED CIRCLES. 653 C FOR THE MATHEMATICAL FORMULATION PERTAINING TO THIS FUNCTION, 654 C SEE THE APPENDIX OF 'METHOD FOR THE CALCULATION OF PARTIALLY COHERENT 655 C IMAGERY', ERIC KINTNER, J. APPLIED OPTICS, VOL.17, NO.17, PAGE 2750. 656 C 657 C 659 C 660 C PARAMETER DEFINITIONS -
R1 - RADIUS OF FIRST CIRCLE. 661 C 662 C R2 - RADIUS OF SECOND CIRCLE. 663 C D - SEPARATION BETWEEN FOCII OF TWO CIRCLES. 664 C ROUTINE ASSUMES SOME CONTACT EXISTS, AND EXPECTS ALL THREE 665 C 666 C PARAMETERS TO BE POSITIVE. 667 C 669 C 670 FUNCTION AREA(R1,R2,D) 671 COMMON/PAR/PI, TWOPI 672 C 674 C 675 C TRAP FOR CONCENTRIC CIRCLES. 676 C 677 IF(D .LT. 0.001) GOTO 100 678 C 679 C FIND ANGLE IN EACH CIRCLE SUBTENDED BY COMMON AREA. NOTE TRAPS 680 C TO SUPPRESS ERRORS IN ARC-COSINE ROUTINES. 681 C 682 D2=D*D683 RADII=R1*R1-R2*R2 684 DENOM=2.0*D 685 T=(D2+RADII)/(DENOM*R1)IF(T .GT. 1.0) T=1.0 686 687 THETA1=ACOS(T) 688 T=(D2-RADII)/(DENOM*R2)IF(T .GT. 1.0) T=1.0 689 690 THETA2=ACOS(T) 691 C 692 C COMPUTE HALF-LENGTH OF CHORD COMMON TO THE TWO COMPUTED ANGLES. 693 C 694 C=R1*SIN(THETA1) 695 C 696 C COMPUTE THE AREA OF THE REGION OF OVERLAP. 697 C 698 AREA=(R1**2*THETA1+R2**2*THETA2)-C*D 699 RETURN 700 C 701 C IF CIRCLES ARE CONCENTRIC, CALCULATE AREA OF SMALLER CIRCLE. 702 C 703 100 AREA=PI*(AMIN1(R1,R2))**2 704 RETURN 705 END 707 C 708 C THIS SUBROUTINE CORRECTS THE FOURIER COEFFICIENTS, C(N), FOR THE 709 C EFFECT OF THE SCANNING SLIT IN THE IMAGE PLANE. 710 C 712 C 713 SUBROUTINE CSLIT 714 C 716 C 717 COMMON WIDTH, WAVE, OBJ, SSO, SAO, AB2, AB4, AP, TBO, PB, TTO, PT, SLIT 718 COMMON/MN/XIR, DUM1, DUM2, DUM3 719 COMMON/CROS/C(325),LJ 720 COMMON/PAR/PI, TWOPI

721 C 723 C SEE EQUATION #19 IN 'METHOD FOR THE CALCULATION OF PARTIALLY COHERENT 724 C IMAGERY', ERIC KINTNER, J. APPLIED OPTICS, VOL.17, NO.17, PAGE 2747 725 C 726 C FOR THE MATHEMATICAL FORMULATIONS RELATING TO THIS SUBROUTINE. 727 C 729 C 730 ARG=PI*XIR*(SLIT*OBJ/WAVE) 731 $COSN2=2.0 \times COS(ARG)$ 732 S=0.0 733 S1=-SIN(ARG) 734 DO 700 J=1, LJ 735 S2=S1 736 S1=S 737 S=COSN2*S1-S2738 C(J)=C(J)*S/(J*ARG)739 700 CONTINUE 740 RETURN 741 END 742 C 744 C 745 C THIS SUBROUTINE COMPUTES THE REAL FOURIER COEFFICIENTS, C(N), WHEN 746 C THE 2-D OPTION OF THE PROGRAM IS SELECTED. 747 C 749 C 750 SUBROUTINE CROS2D 751 C 753 C 754 COMMON/MN/XIR, DUM1, DUM2, DUM3 755 COMMON/RD2/SS,SA 756 COMMON/CROS/C(325),LJ,LJ1,C0 757 COMPLEX CCF2D, A 758 C 760 C 761 C SEE EQUATION #18 IN 'METHOD FOR THE CALCULATION OF PARTIALLY COHERENT IMAGERY', ERIC KINTNER, J. APPIED OPTICS, VOL.17, NO.17, PAGE 2747 762 C 763 C FOR THE MATHEMATICAL FORMULATION OF THE FOURIER COEFFICIENTS, C(N). 764 C 766 C 767 C COMPUTE THE NUMBER OF FOURIER COEFFICIENTS NEEDED IN THE SUMMATION 768 C LJ=2.0/XIR+1.0 769 770 LJ1=LJ+1771 LN0=(1.0+SS)/XIR+1.0772 C 773 C COMPUTE THE NORMALIZING FACTOR FOR THE COEFFICIENTS (CN0). THIS 774 C IS DONE THROUGH THE FUNCTION CNORM2. 775 C 776 CN0=CNORM2(SA)777 C CALCULATE THE FOURIER COEFFICIENTS CORRESPONDING TO THE PRIMARY 778 C 779 C AXIS FIRST (CO): 780 C

CO=CABS(A(0)) * *2*CCF2D(0.0,0,0)781 782 DO 300 N=1, LN0 783 CO=CO+REAL(CABS(A(N))**2*CCF2D(XIR,N,N))784 +CABS(A(-N)) **2*CCF2D(XIR,-N,-N))785 300 CONTINUE 786 C0=C0/CN0787 C 788 C COMPUTE FOURIER COEFFICIENTS, C(N), VIA EQUATION #18 (KINTNER'S REF.) 789 C 790 DO 500 J=1, LJ 791 LN=LN0+J 792 CT=REAL(A(J)*CONJG(A(0))*CCF2D(XIR,J,0)) DO 400 N=1, LN 793 794 CT=CT+REAL(A(J+N)*CONJG(A(N))*CCF2D(XIR,J+N,N)+A(J-N)*CONJG(A(-N))*CCF2D(XIR, J-N, -N))795 1 796 400 CONTINUE 797 C(J) = CT/CN0798 500 CONTINUE 799 RETURN 800 END 801 C 803 C THIS SUBROUTINE NORMALIZES ALL OF THE INTENSITY VALUES STORED IN 804 C 805 C THE ARRAY YLIST(N). 806 C 808 C 809 SUBROUTINE YNORM(NUM) 810 C 812 C 813 COMMON/IM/YLIST(2000), NX1, YMAXBN, DUM1, YMAXAN 814 C 816 C 817 C SINCE SCANNING IS ASSUMED TO START FROM THE CENTER OF THE LINE 818 C OBJECT (CORRESPONDING TO X=0), THE INTENSITY VALUES ARE NORMALIZED 819 C RELATIVE TO THE FOREGOUND INTENSITY WHEN THE INPUT VALUE FOR THE 820 C INTENSITY TRANSMITTACE (TTO) IS 1.0. 821 C OTHERWISE, THE INTENSITY VALUES ARE NORMALIZED RELATIVE TO THE 822 C BACKGROUND INTENSITY CORRESPONDING TO AN INPUT OF 1.0 FOR THE 823 C BACKGROUND INTENSITY (TBO). 824 C 826 C 827 C YMAXAN.....THE MAXIMUM INTENSITY VALUE AFTER NORMALIZATION 828 C 829 YMAXAN=YMAXBN/YLIST(NUM) 830 CONST=YLIST(NUM) DO 100 I=1,NX1 831 832 YLIST(I)=YLIST(I)/CONST 100 CONTINUE 833 RETURN 834 835 END 836 C 838 C 839 C THIS SUBROUTINE READS THE INPUT PARAMETERS THAT CHARACTERIZE THE 840 C OPTICAL SYSTEM TO BE MODELED. THE COMPLEX AMPLITUDE TRANSMITTANCE

841 C (OR REFLECTANCE) IS THEN CALCULATED FROM THE INPUTTED INTENSITY TRANSMITTANCE AND PHASE OF THE OBJECT. 842 C 843 C 845 C 846 SUBROUTINE RDATA 847 C 849 C 850 C PARAMETER DEFINITIONS -851 C 852 C WIDTH - LINEWIDTH OF OBJECT IN MICROMETERS WAVE - WAVELENGTH OF LIGHT IN MICROMETERS OBJ - OBJECTIVE NUMERICAL APERTURE 853 C 854 C 855 C SSO - CONDENSER NUMERICAL APERTURE 856 C SAO - NUMERICAL APERATURE OF CENTRAL OBSTRUCTION OF ANNULAR CONDENSER (SET TO ZERO FOR BRIGHT FIELD IMAGE) 857 C AB2 - AMOUNT OF DEFOCUS IN WAVES 858 C AB4 - AMOUNT OF SPHERICAL ABERRATION IN WAVES 859 C 860 C - GAUSSIAN APODIZATION PARAMETER AP 861 C (MUST BE ZERO UNLESS USING 1-D OPTICS) 862 C TBO - INTENSITY TRANSMITTANCE OF BACKGROUND 863 C PB - PHASE IN UNITS OF PI OF BACKGROUND 864 C TTO - INTENSITY TRANSMITTANCE OF LINE OBJECT - PHASE OF LINE OBJECT 865 C \mathbf{PT} 866 C SLIT - EFFECTIVE SCANNING SLIT WIDTH IN MICROMETERS 867 C SS - COHERENCE PARAMETER SA - NORMALIZED RADIUS OF CENTRAL OBSTRUCTION 868 C TB - COMPLEX AMPLITUDE TRANSMITTANCE OF BACKGROUND 869 C - COMPLEX AMPLITUDE TRANSMITTANCE OF LINE OBJECT 870 C \mathbf{TT} 871 C 873 C 874 COMMON WIDTH, WAVE, OBJ, SSO, SAO, AB2, AB4, AP, TBO, PB, TTO, PT, SLIT, * DATAS(13) 875 876 COMPLEX TB, TT COMMON/IO/INA,IOUTA,IOUTB 877 878 COMMON/RD1/TB,TT 879 COMMON/RD2/SS,SA 880 COMMON/PAR/PI, TWOPI 881 C 883 C 884 C READ THE INPUT PARAMETERS AND STORE THEM IN THE ARRAY 'DATAS(N)' 885 C 886 READ(INA, *)(DATAS(I), I=1, 13)887 C 888 C ASSIGN VARIABLE NAMES TO EACH ELEMENT OF ARRAY 'DATAS': 889 C 890 WIDTH=DATAS(1) 891 WAVE=DATAS(2) 892 OBJ=DATAS(3) 893 SSO=DATAS(4) 894 SAO=DATAS(5) 895 AB2=DATAS(6) 896 AB4=DATAS(7) 897 AP=DATAS(8) 898 IBO=DATAS(9) PB=DATAS(10) 899 900 TTO=DATAS(11)

901 PT=DATAS(12) 902 SLIT=DATAS(13) SS=SSO/OBJ 903 SA=SAO/OBJ 904 AMPL=SQRT(TBO) 905 906 PHASE=PI*PB 907 TB=CMPLX(AMPL*COS(PHASE),AMPL*SIN(PHASE)) 908 AMPL=SQRT(TTO) 909 PHASE=PI*PT 910 TT=CMPLX(AMPL*COS(PHASE), AMPL*SIN(PHASE)) 911 RETURN 912 END 913 C 915 C THIS SUBROUTINE PRINTS A TABLE OF DISTANCE VERSUS INTENSITY VALUES 916 C 917 C FOR THE PARTIALLY COHERENT IMAGING OF PERIODIC OBJECTS OUT TO 918 C FILE 'PRTDATA'. 919 C 920 C TWO COLUMNS CONSISTING OF X-VALUES AND CORRESPONDING INTENSITY 921 C VALUES ARE OUTPUT TO FILE 'PLOTDAT'. THESE VALUES MAY BE USED AS 922 C A PLOT FILE TO PRODUCE A THEORETICAL OPTICAL PROFILE FOR THE LINE 923 C OBJECT. 924 C 926 C 927 SUBROUTINE PRINT(TYPE, SIZE, ANSWER) 928 C 930 C 931 COMMON WIDTH, WAVE, OBJ, SSO, SAO, AB2, AB4, AP, TBO, PB, TTO, PT, SLIT 932 COMMON/IO/INA, IOUTA, IOUTB 933 COMMON/IM/YLIST(2000),NX1,YMAXBN,XMAX,YMAXAN 934 CHARACTER*5 TYPE **9**35 CHARACTER*12 SIZE 936 CHARACTER*2 ANSWER 937 C 939 C 940 C PRINT PERTINENT INFORMATION FOLLOWED BY A TABLE OF INTENSITY VALUES 941 C FOR THE DISTANCE TRAVERSED: 942 C 943 WRITE(IOUTA,1) TYPE, SIZE 944 WRITE(IOUTA,2) NX1 945 WRITE(IOUTA,3) YMAXBN 946 WRITE(IOUTA, 4) YMAXAN 947 WRITE(IOUTA, 5) XMAX 948 IF(ANSWER.EQ.'2D') THEN PRINT*, ' 2-D OPTION SELECTED' 949 950 ELSE 951 PRINT*, ' 1-D OPTION SELECTED' **9**52 ENDIF 953 WRITE(IOUTA, *) 954 WRITE(IOUTA, *) 955 WRITE(IOUTA,6) 956 WRITE(IOUTA,7)WIDTH,WAVE,OBJ,SSO,SAO,AB2,AB4,AP,TBO,PB,TTO,PT,SLIT **9**57 WRITE(IOUTA, 8) **9**58 WRITE(IOUTA,9) **9**59 WRITE(IOUTA, 10) 960 NA=1

NB=10961 X=0.0 962 100 WRITE(IOUTA,11) X, (YLIST(NP), NP=NA,NB) 963 964 NA=NA+10 965 NB=NB+10 966 X=X+0.1 967 IF(NB.GT.NX1) NB=NX1 968 IF(NA.GT.NX1) GOTO 200 969 GOTO 100 970 C 971 C THE FOLLOWING CODE PRINTS TWO COLUMNS OF DISTANCE AND INTENSITY VALUES OUT TO FILE 'PLOTDAT'. SINCE YLIST(N) ONLY CONTAINS INTENSITY 972 C VALUES STARTING FROM THE CENTER OF THE LINE OBJECT, A ROUTINE HAS BEEN 973 C DEVELOPED TO REPEAT THE CORRESPONDING INTENSITY VALUES FOR NEGATIVE 974 C X-VALUES (LYING TO THE LEFT OF THE LINE OBJECT'S CENTER). 975 C THIS ROUTINE ALSO COMPARES THE SLOPE OF A SET OF (X,Y) POINTS 976 C AND PRINTS ONLY THOSE POINTS WHICH HAVE INTENSITY VALUE DIFFERENCES 977 C 978 C GREATER THAN 0.001. IN THIS WAY, THE PLOT FILE GENERATED MAY 979 C BECOME MORE EFFICIENT BY ELIMINATING UNNECESSARY POINTS. 980 C THIS PORTION OF CODE PRINTS OUT CORRESPONDING NEGATIVE X-VALUES 981 C 982 C AND INTENSITY VALUES - STARTS FROM YLIST(NX1) AND GOES TO YLIST(1): 983 C 984 200 N=NX1 985 J=0986 C 987 C J IS COUNTER FOR NUMBER OF POINTS APART TO COMPARE WITH (UP TO 15) 988 C SUBTRACT J BECAUSE WE ARE HEADING TOWARDS CENTER OF PROFILE...YLIST(1) 989 C 990 300 N=N-J 991 J=0DO 400 I=1,15 992 993 J=J+1994 DIFF=ABS(YLIST(N)-YLIST(N-I)) 995 C IF YLSIT(1) HAS BEEN REACHED, SWITCH TO SECOND PART OF ROUTINE (BELOW) 996 C 997 C 998 IF((N-I).LE.1) GOTO 600 999 IF(DIFF.GE.0.001) GOTO 500 1000 400 CONTINUE 1001 500 X = (N - J - 1) * 0.011002 WRITE(IOUTB,12) YLIST(N-J), -X 1003 GOTO 300 1004 C THIS PORTION OF CODE PRINTS OUT THE POSITIVE X-VALUES AND 1005 C 1006 C INTENSITY VALUES - STARTS FROM YLIST(1) AND GOES TO YLIST(NX1): 1007 C 1008 600 X=0.0 WRITE(IOUTB, 12) YLIST(1), X 1009 1010 C START AT LOWEST INDEX NUMBER OF ARRAY AND WORK UP TO HIGHEST. 1011 C 1012 C N=11013 J=01014 1015 C 1016 C ADD J BECAUSE WE START WITH YLIST(1) AND PROCEED TO YLIST(NX1). 1017 C 1018 700 N=N+J 1019 J=0 1020 DO 800 I=1,15

1021		.1=.1+1
1021		$DTFF= \lambda BC(VITCT(N) - VITCT(N+T))$
1022		$\frac{DIT}{RDS(1DISI(N)-1DISI(N+1))}$
1023		IF((N+1), GE(NA1), GOTO, 1000)
1024	00	IF (DIFF.GE.U.UUI) GOIO 900
1025		(0, V = (N + 7, 1) + 0, 0)
1020	90	$V = (N+J-1) \wedge 0.01$
1027		WRITE(IOUTB,IZ) YLIST(N+J), X
1028	100	
1029	100	$V = (NXI-1) \times 0.01$
1030		WRITE(IOUTB, 12) YLIST(NXI), X
1031		WRITE(IOUTB,*)'END OF DATA'
1032	110	0 ENDFILE 40
1033		RETURN
1034		1 FORMAT(1X//1X, 'THE FOLLOWING DATA CORRESPONDS TO A ', A5/1X,
1035		* A12, ' 2.5 MICROMETERS IN WIDTH: '/)
1036		2 FORMAT(1X, 'THE NUMBER OF DATA POINTS = ', 14/)
1037		3 FORMAT(1X, 'THE MAXIMUM INTENSITY VALUE BEFORE NORMALIZATION =',
1038		* F7.4)
1039		4 FORMAT(1X, 'THE MAXIMUM INTENSITY VALUE AFTER NORMALIZATION =',
1040		* F7.4)
1041		5 FORMAT(1X, 'THE CORRESPONDING X-VALUE TO THESE MAXIMUM INTENSITIES
1042		*=', F6.2//)
1043		6 FORMAT(1X,5HWIDTH,6H WAVE,4H OBJ,5H SSO,5H SAO,5H AB2,5H AB4,
1044		* 5H AP, 6H TBO, 6H PB, 6H TTO, 6H PT, 6H SLIT)
1045		7 FORMAT(1X, 8($F5.2$), 4($F6.2$), $F5.2///$)
1046		8 FORMAT(1X, 'LEFT-MOST RELATIVE INTENSITY VALUES CORRESPONDING TO
1047		* STEPS OF')
1048		9 FORMAT(1X, 'X-VALUES 0.01 MICROMETERS FROM LEFT TO RIGHT')
1049	1	0 FORMAT(1X, '
1050		*'/)
1051	1	1 FORMAT(1X,F6.2,2X,10F6.3)
1052	1	2 FORMAT(1X,F7.4,3X,F7.2)
1053		END
1054	С	
1055	C***	***************************************
1056	С	
1057	СТ	HIS SUBROUTINE COMPUTES THE IMAGE INTENSITY IN THE OBJECT PLANE
1058	C B	Y AN INVERSE FOURIER TRANSFORM METHOD.
1059	С	
1060	C***	***************************************
1061	С	
1062		SUBROUTINE IMAGE
1063	С	
1064	C***	***************************************
1065	С	
1066		COMMON WIDTH, WAVE, OBJ
1067		COMMON/MN/DUM1, DUM2, PER, NX
1068		COMMON/CROS/C(325),LJ,LJ1,CO
1069		COMMON/IM/YLIST(2000),NX1,YMAXBN,XMAX,DUM3
1070	-	COMMON/PAR/PI,TWOPI
1071	C	
1072	C***	~~~~~~~~~~
1073	С	
1074	СТ	HE MATHEMATICAL FORMULATIONS RELATING TO THIS SUBROUTINE CAN
1075	CB	E FOUND IN EQUATIONS #14 AND #17 IN 'METHOD FOR THE CALCULATION
1076	с о	F PARTIALLY COHERENT IMAGERY', ERIC KINTNER, J. APPIED OPTICS,
1077	C V	OL.17, NO.17, PAGE 2747.
1078	С	
1079	C***	***************************************
I H X D	('	

1081 C PARAMETER DEFINITIONS -1082 C 1083 C - TOTAL NUMBER OF CALCULATED IMAGE POINTS NX1 YMAXBN - MAXIMUM INTENSITY VALUE BEFORE NORMALIZATION 1084 C 1085 C XMAX - X-VALUE CORRESPONDING TO THE MAXIMUM INTENSITY VALUE - TRANSVERSE DISTANCE ACROSS THE OBJECT (STARTING AT X=0) 1086 C X 1087 C - INTENSITY VALUE CORRESPONDING TO EACH X-VALUE OF Y OBJECT 1088 C 1089 C YLIST(N) - ARRAY THAT CONTAINS EACH INTENSITY VALUE CORRESPONDING 1090 C TO ACCENDING VALUES OF X. 1091 C 1093 C 1094 X0=0.01 1095 NX1=NX+1 1096 YMBN=0.0 1097 DO 900 N=1, NX1 1098 X = (N-1) * X01099 C 1100 C NOTE THE USE OF THE IDENTITY: COSNX = 2*COS(X)*COS(N-1)*X - COS(N-2)*X1101 C 1102 C COSN=COS(TWOPI*X/PER) 1103 COSN2=2.0*COSN 1104 1105 CK1=0.0 CK=0.0 1106 DO 800 J=1, LJ 1107 1108 CK2=CK1 1109 CK1=CK CK = COSN2 * CK1 - CK2 + 2.0 * C(LJ1 - J)1110 800 CONTINUE 1111 CK2=CK1 1112 CK1=CK 1113 CK=COSN2*CK1-CK2+C0 1114 1115 Y=CK-COSN*CK1 IF(Y .LE. YMBN) THEN 1116 1117 GOTO 850 ENDIF 1118 1119 XM=X 1120 YMBN=Y 850 1121 YLIST(N) = Y900 CONTINUE 1122 1123 XMAX=XM 1124 YMAXBN=YMBN 1125 RETURN 1126 END 1127 (EOR)

TEST CASE FOR PCIMAG2

INPUT DATA

Notes:

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Line

- 1) phase angles are given in units of $\boldsymbol{\pi}$
- 2) both defocus and spherical aberrations are given in "number of waves"
- 3) all distances are given in μm

-75-

THE FOLLOWING DATA CORRESPONDS TO A SPACE GREATER THAN 2.5 MICROMETERS IN WIDTH: THE NUMBER OF DATA POINTS = 301 THE MAXIMUM INTENSITY VALUEBEFORE NORMALIZATION = 1.2948 THE MAXIMUM INTENSITY VALUE AFTER NORMALIZATION = 1.2948 THE CORRESPONDING X-VALUE TO THESE MAXIMUM INTENSITIES = 1.17 WIDTH WAVE OBJ SSO SAO AE2 AB4 AP TEO PB TTO PT SI 3.00 .53 .85 .17 .00 .00 .00 .00 1.00 .00 1.00 1.00					001	PUI								
THE FOLLOWING DATA CORRESPONDS TO A SPACE GREATER THAN 2.5 MICROMETERS IN WIDTH: THE NUMBER OF DATA POINTS = 301 THE MAXIMUM INTENSITY VALUEBEFORE NORMALIZATION = 1.2948 THE MAXIMUM INTENSITY VALUE AFTER NORMALIZATION = 1.2949 THE MAXIMUM INTENSITY VALUE AFTER NORMALIZATION = 1.2948 THE MAXIMUM INTENSITY VALUE AFTER NORMALIZATION = 1.2949 THE CORRESPONDING X-VALUE TO THESE MAXIMUM INTENSITIES = 1.17 WIDTH WAVE OBJ SSO SAO AE2 AE4 AP TEO PE TTO PT SI 3.00 .53 .85 .17 .00 .00 .00 .00 1.00 .00 1.00 1.00														
GREATER THAN 2.5 MICROMETERS IN WIDTH: THE NUMBER OF DATA POINTS = 301 THE MAXIMUM INTENSITY VALUEBEFORE NORMALIZATION = 1.2948 THE MAXIMUM INTENSITY VALUE AFTER NORMALIZATION = 1.2989 THE CORRESPONDING X-VALUE TO THESE MAXIMUM INTENSITIES = 1.17 WIDTH WAVE OBJ SSO SAO AB2 AB4 AP TEO PE TTO PT SI 3.00 .53 .85 .17 .00 .00 .00 .00 1.00 .00 1.00 1.00	THE FO	THE FOLLOWING DATA CORRESPONDS TO A SPACE												
THE NUMBER OF DATA POINTS = 301 THE MAXIMUM INTENSITY VALUEBEFORE NORMALIZATION = 1.2948 THE MAXIMUM INTENSITY VALUE AFTER NORMALIZATION = 1.2989 THE CORRESPONDING X-VALUE TO THESE MAXIMUM INTENSITIES = 1.17 WIDTH WAVE OBJ SSO SAO AB2 AB4 AP TBO PB TTO PT SI 3.00 .53 .85 .17 .00 .00 .00 .00 1.00 .00 1.00 1.00	GREATE	JREATER THAN 2.5 MICROMETERS IN WIDTH:												
THE MAXIMUM INTENSITY VALUEBEFORE NORMALIZATION = 1.2948 THE MAXIMUM INTENSITY VALUE AFTER NORMALIZATION = 1.2989 THE CORRESPONDING X-VALUE TO THESE MAXIMUM INTENSITIES = 1.17 WIDTH WAVE OBJ SSO SAO AB2 AB4 AP TBO PB TTO PT SI 3.00 .53 .85 .17 .00 .00 .00 .00 1.00 .00 1.00 1.00	THE NUMBER OF DATA POINTS = 301													
THE CORRESPONDING X-VALUE TO THESE MAXIMUM INTENSITIES = 1.17 WIDTH WAVE OBJ SSO SAO AB2 AB4 AP TEO PB TTO PT SI 3.00 .53 .85 .17 .00 .00 .00 .00 1.00 .00 1.00 1.00	THE MA	XIMUM I XIMUM I	NTENSIT NTENSIT	Y VALU Y VALU	EBEFOR	E NORM R NORM	ALIZAT ALIZAT	ION = 1 ION = 1	1.2948					
WIDTH WAVE OBJ SSO SAO AE2 AB4 AP TEO PB TTO PT SI 3.00 .53 .85 .17 .00 .00 .00 1.00 .00 1.000 1.000	THE CO	RRESPON	DING X-	VALUE	TO THE	SE MAX	IMUM I	NTENSI	TIES =	1.17				
WIDTH WAVE OBJ SSO SAO AB2 AB4 AP TEO FB TTO FT SI 3.00 .53 .85 .17 .00 .00 .00 1.00 .00 1.00														
WIDTH WAVE OBJ SSO SAO AB2 AB4 AP TBO PB TTO PT ST 3.00 .53 .85 .17 .00 .00 .00 .00 1.00				C L C		154								
LEFT-MOST X-VALUES 0.01 MICROMETERS FROM LEFT TO RIGHT 0.01 MICROMETERS FROM LEFT TO RIGHT 0.01 MICROMETERS FROM LEFT TO RIGHT 0.00 1.000 1.000 1.000 .999 .999 .998 .998 .997 .996 10 .996 .995 .994 .994 .993 .993 .992 .992 .991 .995 20 .991 .991 .991 .992 .992 .993 .994 .995 .997 .996 30 1.000 1.002 1.004 1.006 1.009 1.011 1.014 1.017 1.020 1.022 40 1.027 1.030 1.033 1.037 1.040 1.041 1.041 1.047 1.020 1.022 40 1.027 1.030 1.038 1.037 1.040 1.043 1.046 1.049 1.051 1.055 .50 1.055 1.057 1.058 1.058 1.058 1.058 1.057 1.055 1.053 1.055 .60 1.047 1.043 1.038 1.033 1.027 1.021 1.014 1.007 1.000 .997 .70 .984 .976 .967 .959 .951 .943 .935 .928 .921 .914 .80 .909 .903 .899 .896 .893 .892 .891 .892 .894 .897 .90 .901 .907 .914 .923 .933 .944 .957 .971 .986 1.007 1.00 1.020 1.039 1.058 1.078 1.099 1.120 1.141 1.162 1.182 1.200 1.00 1.020 1.039 1.255 1.269 1.280 1.290 1.296 1.299 1.298 1.294 1.20 1.286 1.274 1.258 1.237 1.212 1.183 1.149 1.112 1.070 1.022 1.30 .977 .926 .872 .817 .759 .701 .643 .585 .528 .477 1.40 .420 .370 .324 .281 .243 .210 .182 .161 .145 .134 1.50 .132 .136 .146 .162 .184 .211 .245 .283 .326 .377 1.60 .423 .476 .531 .588 .646 .705 .763 .820 .875 .922 1.70 .980 1.028 1.073 1.114 1.152 1.181 1.213 1.238 1.248 1.237 1.80 1.285 1.293 1.296 1.296 1.292 1.285 1.275 1.263 1.248 1.237 1.80 1.285 1.293 1.296 1.296 1.947 .935 .925 .916 .908 .907 2.00 1.009 .991 .975 .961 .947 .935 .925 .916 .908 .907 2.00 1.009 .991 .975 .961 .947 .935 .925 .916 .908 .907 2.00 1.009 .991 .975 .961 .947 .935 .925 .916 .908 .907 2.00 1.009 .991 .975 .961 .947 .935 .925 .916 .908 .907 2.00 1.004 1.005 1.013 1.020 1.027 1.033 1.039 1.043 1.048 1.055 2.50 .998 1.005 1.013 1.020 1.027 1.033 1.039 1.043 1.048 1.055 2.50 .998 1.005 1.013 1.020 1.027 1.033 1.039 1.043 1.048 1.055 2.50 .050 1.047 1.044 1.040 1.036 1.033 1.029 1.025 1.021 1.015 2.50 .050 1.047 1.044 1.040 1.036 1.033 1.029 1.025 1.021 1.015 2.50 .050 1.041 1.010 1.007 1.004 1.001 .999 .997 .995 .993 .994 2.50 .990 .998 .988 .988 .988 .988 .987 .987 .985 .984 .988 .988 2.	3.00	.53 .	BJ SSO 85 .17	.00	AB2 .00	AB4 .	AP T 00 1.		PB T1 00 1.(ro P1 00 1.00	S SL			
LEFT-MOST X-VALUES RELATIVE INTENSITY VALUES CORRESPONDING TO STEPS OF 0.01 MICROMETERS FROM LEFT TO RIGHT														
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$\begin{array}{cccccccccccccccccccccccccccccccccccc$.60	1.04	7 1.043	1.038	1.033	1.027	1.021	1.014	1.007	1.000	.992			
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	2.90	.99	.998	.998	.999	1.000	1.000	1.001	1.001	1.002 1	.002			

OUTPUT

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List of Program Elements

- 1. MAIN
- 2. Subroutine OBJECT Calculates Fourier series coefficients for input line object.
- 3. Subroutine CROS1D Calculates Fourier coefficients of the image for 1-D optics using transmission cross-coefficients.
- Function A(N) Retrieves Fourier coefficients for the line object from calculated array assuming symmetric object.
- 5. Function CNORM1 Normalizes transmission crosscoefficients for 1-D optics.
- 6. Function CNORM2 Normalizes transmission crosscoefficients for 2-D optics.
- 7. Function CCF1D Calculates transmission crosscoefficients for 1-D optics.
- 8. Function CCF2D Calculates transmission crosscoefficients for 2-D optics.
- 9. Function AREA Calculates the overlapping area of circular lens apertures; used by CCF2D.
- 10. Subroutine CSLIT Multiplies image Fourier coefficients by scanning slit function.
- 11. Subroutine CROS2D Calculates Fourier coefficents of the image for 2-D optics using transmission cross-coefficients.
- 12. Subroutine YNORM Normalizes the image to 1.0 at either the center or the edge of the image, whichever has the higher intensity.
- 13. Subroutine RDATA Reads input data and sets up parameters used in calculations.
- 14. Subroutine PRINT Creates two print files, one for printing of a table of image data (optical intensity vs. distance) and the second for a plot file. The plot file reduces the number of data points by eliminating values for which there is less than a 0.1% change in intensiy.
- 15. Subroutine IMAGE Calculates the image intensity vs. distance from the image Fourier coefficients.





NOTES: PER = PERIOD WT = NORMALIZED WIDTH XIR = NORMALIZED FREQUENCY NX = INCREMENT OF DISTANCE IN IMAGE



2. FLOW DIAGRAM OF SUBROUTINE 'OBJECT'

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3. FLOW DIAGRAM OF SUBROUTINE 'CROS1D'



4. FLOW DIAGRAM OF THE FUNCTION 'A(N)'

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5. FLOW DIAGRAM OF THE FUNCTION 'CNORM1'



6. FLOW DIAGRAM OF FUNCTION 'CNORM2'







-87-



RETURN





8. FLOW DIAGRAM OF THE FUNCTION 'CCF2D'











9. FLOW DIAGRAM FOR FUNCTION 'AREA'

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10. FLOW DIAGRAM FOR SUBROUTINE 'CSLIT'

-70-









12. FLOW DIAGRAM FOR THE SUBROUTINE 'YNORM'



RETURN

13. FLOW DIAGRAM FOR THE SUBROUTINE 'RDATA'



14. FLOW DIAGRAM FOR THE SUBROUTINE 'PRINT'












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Acknowledgments

Support for documentation and publication of this software was provided by VLSI Standards, Inc. under an NBS Research Associate Agreement. A PASCAL version of this software has also been developed. In addition, the assistance of Ruth N. Varner and Carmelo Montanez in converting this software for use on the CYBER 855 is gratefully acknowledged.

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V. JUFFLEMEN FART NUTE	5		
Document describes a	computer program; SF-185, F	IPS Software Summary, is attached	
1. ABSTRACT (A 200-word o bibliography or literature	r less factual summary of mo survey, mention it here)	st significant information. If docum	nent includes a significant
The integrated-ci	rouit industry in it	s push to finor and fin	ar line competries
approaching submi	rcuit industry in it crometer dimensions	has created a need for a	er line geometries
approaching submicrometer dimensions has created a need for ever more accurate			
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Program, a unique narrow-angle laser measuremnt system was developed. This			
report describes	the theory, optical	design, and operation of	this system and
includes computer	software useful for	characterizing the pert	inent optical
parameters and images for patterned thin layers. For thick layers, the physics			
is more detail the reader is referred to several related reports listed in the			
references.			
2. KEY WORDS (Six to twelv	e entries; alphabetical order;	capitalize only proper names; and s	separate key words by semicolons;
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