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Abstract

This paper presents a simple model to demonstrate the effect on grass-fire propagation of the winds induced by structural fires in a Wildland-Urban Interface (WUI) setting. The model combines an empirical formula for wind-driven grass-fire spread and a physics-based analytical solution to the Euler equations to determine the ground-level wind produced by the burning structure. The scaling of the wind is based on the heat release rate (HRR) of the structural fire as well as other parameters. Also considered are an ambient wind and a topographical wind, assumed to be proportional to the ground slope. Data on grass and structure fires required by the model are discussed. The model can be presented using either a Lagrangian or an Eulerian description of the fire front. Methods used to solve each description are presented and compared, with the so-called Level-Set Method (LSM) used in the latter case. The LSM has the distinct advantage that it can follow front propagation during pinching off and disappearance of a portion of the front as well as mergers with other fronts, and examples are presented of each type of behavior. Prediction of the fire front propagation in the Lagrangian description is illustrated by several examples: a front passing a single burning structure on flat terrain, a front passing a burning structure on a hill, and a front passing several burning structures. The model predicts that a fire front will be accelerated toward the burning structure upon approach and decelerated after passing the structure, thereby spending more time near the burning structure than if the structure were absent. The model also shows, as expected, that the slope of a hill will accelerate or decelerate the front, depending upon the slope magnitude and sign. Finally, several burning structures multiply the effects of an individual burning structure, causing the front to linger longer in the vicinity of the structures.

Introduction

Over the past few years, Wildland-Urban Interface (WUI) fires have become of much greater concern. The WUI includes people and property, and, therefore, the costs of damage in the built environment, especially when measured in terms of injury to people, death and property damage, are far higher than in wildland settings, National Interagency Fire Center (2006). The WUI has been found to be large and growing rapidly in the United States as population expands and housing development in wildland areas continues. People are building more houses in a wildland setting every year, Environmental Literacy Council (2007). For example, data from year 2000 show that about 36 % or 42 million homes in the U.S. are in the WUI and the numbers are growing rapidly, Radeloff et al (2005) and Gustafson et al (2005). Also, as the average temperature, both within the United States and globally, has increased, earlier snowmelts have taken place, extending the number of weeks every year that forests are exposed to high temperatures and dangerously dry conditions, Andrews et al. (2007). Increasingly hot and dry conditions in the United States have led, in turn, to more acres of wildland fuel consumed by wildfire with greater threat to the WUI, Andrews et al (2007), National Interagency Fire Center (2006).

The philosophy of management of wildlands in the United States has undergone a major change over the past few decades, Andrews et al (2007), Berry (2007). Early in the twentieth century, management practice was to suppress wildfire completely. The Smokey-the-Bear campaign emphasized reporting and suppression of all fire in wildland settings. This practice, in turn, allowed the buildup of near-ground vegetative material in forests so that, when a fire did occur, it burned with a much higher intensity than if this material had been expunged by more frequent, but less intense fires. Today, the philosophy is that fire is a naturally occurring process in forests and that periodic, low-intensity fires help to keep the forest floor clear of vegetative debris that can turn low-intensity fires into high-intensity ones. The forests that have been cleared periodically by small fires are now believed to be healthier and much more able to resist the negative effects of wildfire.

Observations show that WUI fires can behave differently than wildland fires, Murphy et al (2007). Wildfires are found to spread as a fire line or fire front with distinct features, such as intensity, rate of spread (ROS), flame height, etc. that depend upon properties of the wildland fuel, the meteorological properties and topography. WUI fires are produced when wildfires invade a community. For example, Figure 1 shows a photograph, taken by John Gibbins of the San Diego Post Tribune, of a wildland fire front approaching the Scripps Ranch residential community during the Cedar Fire in October 2003.

In both wildland and WUI fires, spot fires ignited by brands are a primary fire-spread mechanism. In WUI fires, brands can ignite a house, producing a vigorous structure fire and substantial additional brand production while the surrounding trees remain untouched. Examples of such behavior, including photographs, are presented in the USDA report on the Angora Fire that occurred southwest of Lake Tahoe during 24-26 June, 2007, Murphy et al (2007). The brands were estimated to travel up to 1/4 mile downwind in this fire and were suspected of igniting additional houses.

While the danger and costs of WUI fires have increased dramatically, National Interagency Fire Center (2006), the tools to address these fires have not been developed, Mell et al (2007). The length and time scales associated with wildland and WUI fires vary greatly, ranging from the millimeter length scales and sub-second time scales associated with combustion of fuel elements to tens of kilometers and days associated with smoke transport and total burned area. This wide variation in scales, coupled with the highly nonlinear behavior of many of the physical processes, represents the major challenge faced in attempting to model such fires.

Models that hope to predict WUI rather than wildland fire spread are likely to be more complex because of the heterogeneity of the fuel. The usual conceptual models for the interaction of a wildfire with structures regard the structures as isolated and surrounded by wildland fuels and imply a density of houses that is so low that the burning of these houses has no effect on the progression of the wildfire, GAO Report (2005).

In reality, often there are many burning structures in addition to the wildfire itself that can contribute to the fire spread. For example, in the photograph of Gibbins, Figure 1, imagine that some unburned structures were to be ignited by brands. Also assume that the fire front were to invade the community. (The Cedar Fire actually did <u>not</u> invade the community because a road acted as a fire break.) Such a scenario is an example of the type of WUI fire envisioned for the analysis presented here.

Recently, an important study by Maranghides and Mell (2009) has appeared that emphasizes for the first time both the discrete nature of the fuels in WUI fires and the utilization of a systematic approach to the collection of post-fire data in and around a community with the intention of estimating the spatial and temporal characteristics of a WUI fire. The fire, known as the 2007 California Firestorm, occurred during October 2007, and was one of the top four fire incidents due to the number of structures destroyed and acres burned. The community studied was the Trails development of Rancho Bernardo, north of San Diego, California, which included 274 homes, of which 245 were within the fire perimeter. The two fires that invaded the community a little over two hours apart were the Witch and Guejito fires, named after the location of the initiation of each fire, the Witch and the Guejito Creeks respectively. The weather conditions during this time showed a rapid wind shift and increased wind (from the west to the east with a new sustained westward wind of 38 km/h and gusts up to 69 km/h) accompanied by reductions in humidity (from 30 to 40 % before the wind shift to 16 % after). The winds contributed significantly to the rapid fire spread.

Many important findings have arisen from this work. The study established a timeline for the fire spread through the wildland fuels surrounding the community first and then through the community. The Guejito fire was estimated to approach the community through the wildland fuel at a rate of 9 km/h and then to drop to a ROS of 0.35 km/h through the community itself. Embers from the approaching wildland fire began to hit the community an hour before the main fire front, traveling a distance of 9.0 km and igniting three homes and several patches of ornamental vegetation. The fire spread up to 500 m into the interior of the community. Although the embers from the wildland fire initiated several ignitions within the community, the majority of the damage was caused by the fire front arrival. Interventions by firefighters and homeowners were found to be very significant, saving 60 % of the defended structures. Direct ember ignitions accounted for one out of every three homes destroyed, while two out of every three destroyed homes were ignited directly or indirectly by embers. 40 % of the homes on the perimeter of the community were destroyed compared to 20 % in the interior. The peak ignition rate for structures destroyed with 29 (or 40 %) estimated to be burning at the same time.

Currently operational models for wildland fires might be satisfactory for some predictions of large wildfire behavior, where average data on wildland fuels is available from Geographical Information Systems (GIS) over elements measuring 30 m per side. Likewise, predictions of wildland or WUI fire behavior over areas measuring a few kilometers per side using field models might soon be possible, provided the detailed data necessary to make such predictions can be obtained. However, it is very unlikely that the capability for useful predictions of large-scale WUI fire spread by any model will be available within the next several years.

The objective of this paper is to present a simple physics-based model that demonstrates the effect on ground-fire propagation of the winds induced by structural fires. In this proposed model, the fuel system is regarded as having two components, a surface-fuel portion consisting of grass alone and the structural fuel portion. Propagation of fires in the surface fuel portion is treated as in the wildfire models discussed below. The structures on the other hand are treated as discrete fuel elements, which generate three-dimensional

buoyant plumes and entrain fresh air to sustain the combustion. These entrainment winds influence the surface-fire propagation. The approximate model utilizes an empirical formula for wind-driven grass-fire spread and a physics-based analytical solution to the Euler equations to determine the ground-level wind produced by the burning structure. This simple model does not resort to a costly Computational Fluid Dynamics (CFD) simulation. The model is based on research presented in studies reported by Rehm (2006).

In the following section of the paper, we briefly discuss physics-based models of fire behavior, focussing on those related to structure fires. Next, empirical relations and data needed for the model are given. In particular, an empirical relationship is given which relates the rate of spread (ROS) and the local wind velocity for Australian grass fires; also estimates are made of the heat release rate (HRR) for structural fires. Then, the coupled model is presented for the propagation of a grass fire driven by winds produced by the local meteorological conditions, entrainment flow from one or more burning houses, and from topographic features such as a hill. For the interested reader, details of the mathematical formulation of the model are given in the Appendix. Fire front propagation for this model is illustrated by examples in the next section. Finally, discussion and conclusions are presented.

Physics-Based Models of Fire Behavior

Physics-based mathematical models of fire behavior have undergone significant development since the early 70s, Rehm (2006). These models can be divided broadly into two categories: indoor, or enclosure fires, and outdoor fires. There are significant differences between these two types of fires. For example, indoor fires are generally limited by the oxygen that can reach the fire through openings in the enclosure. Outdoor fires, on the other hand, are limited by the supply of wildland fuel. Also, fuel moisture content is a critical factor controlling ignition and spread of wildfires, whereas fuel moisture content is much less important for the description of indoor fire behavior.

Here we discuss primarily models for structural fires. This limitation is introduced for two reasons. First, there are several recent papers that review models of wildfire. For example, a recent review of wildfire predictive capability by Andrews et al (2007) has appeared in Scientific American. More technical reviews of wildfire models are given by Mell et al (2007), Pastor et al (2003) and by Perry (1998) among others.

Second, models for structural fires have been developed to deal with fires inside single or multiple enclosures, as noted above, and not to predict behavior of fully involved structural fires. We are aware of no data on burning rate or heat release rate (HRR) for any scenario including ignition through burnout for a whole structure. Yet such information is required to develop a model for WUI fires. Acquisition of such data is very expensive since the complete burning of buildings is not generally sanctioned by fire authorities, and if sanctioned, not adequately instrumented to obtain the data required. The ignition location, the building materials, the interior fire-spread scenario, the prevailing wind conditions, and the response of the structure to severe burning conditions (such as wall, floor or ceiling penetration and/or collapse) would all be necessary data, for example, to adequately calibrate and test a model for a house burning down. A database to test the robustness of any outdoor structural-fire model would require many such full-scale burns. No such database exists.

Indoor fire models are further subdivided into two categories, zone models and field models. The formulation of both zone and field models start from the basic conservation laws of mass, momentum, energy and species, together with radiative transport. Zone models have been utilized to study fire dynamics in structures for about four decades. They take advantage of approximate mathematical submodels of the physical processes that occur in enclosure fires to simplify the conservation laws. As a result, they end up with nonlinear ordinary differential equations together with complex, nonlinear algebraic relations connecting dependent variables. These simplifications reduce both the data and the computational resources required to predict the progression of a fire in a structure. The model CFAST, Jones et al (2004), is a recent example from NIST of this class of models.

Field models begin with a partial differential equations (PDEs) description of the conservation laws and radiative transport, and attempt to integrate these equations directly using techniques from Computational Fluid Dynamics (CFD) and other disciplines. During the past three decades, field models have been developed and applied very successfully to fires in structures. Field models require considerably more data and computational resources to make predictions and can provide substantially more detail about fire behavior than zone models. There are several examples of field models; a recent example from NIST of this class of models is the Fire Dynamics Simulator (FDS), McGrattan et al (2004).

Physics-based models of wildland or outdoor fires have generally followed a similar, but somewhat delayed, evolution to that of indoor fires. The simpler models have generally been based on the Rothermel model, Rothermel (1972), which was developed over three decades ago. Field models for outdoor fires, on the other hand, have only begun serious development over the past several years, McGrattan et al (1996), Linn (1997), and Mell et al (2007). In general, field models describing both indoor and outdoor fires have lagged in development over the simpler models due to the previously prohibitive computer-resource requirements and the corresponding data requirements for such models.

Generally, the simple models of wildland fires treat the fuel as a locally homogeneous surface distribution of mass that varies slowly in the horizontal directions. The three-dimensional elevation of the ground surface is taken into account in determining the fire progression. However, usually, there is little consideration of the large-scale vertical distribution of the fuel, and the small-scale fuel structure is parameterized.

Heat Release Rates of Grass and Structure Fires

Rehm, et al (2001) reviewed the literature on the potential energy content of various wildland fuels and compared these numbers with the potential energy content of structures. The purpose of that comparison was to estimate the density of structures required for the potential energy content to be equal to that of a particular wildland fuel. That work emphasized the importance of the potential energy content in the burning of structures as part of the overall energy available for combustion. However, that study did not consider any dynamical processes such as ignition of the fuels, or HRRs required to sustain and propagate the fire. Furthermore, there was no estimate of the duration and completeness of the combustion processes during a WUI fire.

This section extends that previous work by considering time-dependent processes for two WUI fuels. An empirical relation for the propagation speed for grass fires is used, and the burning times or the HRR for ventilation-controlled structure fires is estimated.

Grass Fires

We utilize an empirical relationship presented in the paper of Cheney et al. (1998) for the rate of spread (ROS) of the fire line in Australian grass. This ROS, r_w , in m/s, is determined as a function of the ambient wind speed, V_a in m/s, the effective length W of the head portion of the fireline in m and the dead fuel moisture percentage M_f in %:

(1)
$$r_w = 0.165(1 + 3.24 V_a) \exp[(-0.859 - 2.04 V_a)/W] \cdot \exp(-0.108 M_f) [m/s]$$

For simplicity in the examples below, we have utilized the limit of very small moisture content and very long fire-lines, so that $r_w \approx 0.165(1+3.24 V_a)$.

Structure Fires

An estimate of the energy release rate during a house fire in the 1991 Oakland Hills fire was reported by Trelles and Pagni (1997). According to that estimate, a house burns at a peak rate of 45 MW for 1 hour (yielding about 160 GJ), and then dies down over another 6 hour period. The die-down of the fire is approximated as two steps, one 10 MW for 3 hours and the last as 5 MW for 3 more hours. The total burn time is 7 hours, and the total energy released by the house is about 320 GJ. Assuming brush around each house another 5 MW is released for one hour, yielding an additional 18 GJ. (The additional HRR and total energy produced by the burning brush around the structure are included in the calculations of Trelles and Pagni (1997). However, these estimates are unnecessary for our purposes here.) If we include this additional HRR and total energy, and if the house is assumed to be 15 m by 15 m by 5 m, then we estimate the total potential fuel loading per unit area to be of order 1.4 GJ/m², the peak HRR per unit area to be of order 0.2 MW/m². For comparison, oil yields a heat release rate per unit area of approximately 2 MW/m², see for example, McGrattan et al. (1996) and Baum et al. (1994).

Confirmation of this estimate for the magnitude of the peak HRR for a burning structure can be found in the chapter on compartment fires in the book on fire behavior by Quintiere (1997). Here, Quintiere describes the stages of a fire in a compartment and estimates the peak heating rates possible during the latter stages of a compartment fire when the fire is fully developed and the burning rate is ventilation limited, or restricted by the amount of air entering the enclosure through the vents. During a compartment fire, the flow in and around the enclosure is driven by buoyancy, which is generated by the burning taking place both inside and outside the compartment.

In one example, Quintiere estimates a total HRR of 9 MW for a compartment in which the fuel load is taken to be proportional to the floor area, that in this case is 12 m^2 . He points out that, this peak HRR could increase to over 60 MW if the fuel was proportional not only to the floor area, but to the whole inside area of the compartment. Furthermore, a multi-room structure, with a fuel loading of the more modest type, producing 9 MW for each room, could also easily exceed the roughly 50 MW peak HRR estimated by Trelles and Pagni (1997). Therefore, based on compartment fire analysis, it seems very plausible that structure fires could have peak HRR reaching several times the estimate of 50 MW, and the duration of these peak HRR would be measured in tens of minutes to hours.

These estimates say nothing about the fact that the roof of the structure might develop a hole or even collapse under prolonged vigorous burning. In that case, the fire might then resemble more a burning crib than an enclosure fire. They also do not address the issue of the effects of winds on peak heat release rate or burn duration. It seems likely that winds would increase the peak HRR and reduce the burn duration, but the magnitude of these changes is not known. For our purposes here, the estimates above will be used without trying to assess these other effects.

Two comparisons can be made between structure fuels and grass fuels using the information given above and cited in the references. First, the energy density of grasses can be compared with the housing energy density. Rehm et al. (2002) quotes Albini (1984) who gives a value of 5.5 [m/s] for the ROS and a value of 1 [MW/m] for the fireline intensity I of a grass fire. Using the burnable energy density of the grass as $e_g = I/ROS$, we find $e_g \approx 0.2$ MJ/m². For Australian grass, Mell (2007) uses ROS = 5.5 m/s and I = 5MW/m, so that $e_g \approx 1$ MJ/m². These estimates can be compared to the corresponding energy density for a rectangular array of same-size houses of specified housing density, see Rehm (2006). A housing density of 2.5 houses per hectare (one acre lot per house), which can represent a suburban housing density in an affluent suburb, with an energy of 300 GJ per structure, yields a potential energy density $e_s \approx 75$ MJ/m². A housing density of 10 houses per hectare (1/4 acre lots), which is a much more typical suburban neighborhood, yields an energy density $e_s \approx 300 \text{ MJ/m}^2$. For these housing densities, the potential energy of the structures is much higher than that of the grass.

Next, the heat release rate (HRR) or Q_0 for grass line fires can be compared to the HRR for an array of structures, again see Rehm (2006). If we take the distance between houses \hat{L} as a characteristic fireline length and take 1 acre lots, then, for the structure, $Q_0 \approx 50$ MW, while for the corresponding grass fire front, HRR $\approx I \cdot \hat{L} = 64$ MW. For 1/4 acre lots, the fireline HRR is about 32 MW. The dynamics of the wind fields generated by burning fuels under low-wind conditions is determined by the HRR, and this argument demonstrates that the wildland and structure contributions to the dynamics can be comparable under common conditions.

A Simple Model for WUI Surface-Fire Spread

Plume Model of Baum and McCaffrey

In the paper of Baum and McCaffrey (1989), there is a fundamental analysis of the structure of a plume and its associated flow field produced by a pool fire in a quiescent atmosphere. The quiescent-atmosphere assumption implies that the plume remains upright and axially symmetric and requires the heat release rate of the burning house produces buoyant velocities large compared with the local wind around the structure. In this paper, an empirical correlation for centerline temperature and velocity is determined from the compilation of data obtained from a large number of pool-fire experiments carried out by many investigators over a wide range of pool-fire diameters. Based on the buoyant, inviscid equations of motion and this correlation, the analysis obtains the scaling relations for the characteristic length and velocity scales for a pool-fire plume. Furthermore, a detailed velocity profile is determined from a solution to these equations.

The model of Baum and McCaffrey (1989) is for a single buoyancy-driven plume in an inviscid, quiescent fluid of density ρ_0 , temperature T_0 and pressure P_0 at ground level. The magnitude of the heat release rate of the source is designated as Q_0 , and the specific heat of the air is denoted as C_p . The model starts with the equations for mass, momentum and energy, assuming axial symmetry. The velocity field is then decomposed into two components, one arising from the divergence and other from the curl. The divergence of the velocity results from thermal expansion of the gas, and the curl is the vorticity, and these components can be related to the plume centerline temperature and velocity correlations. From this analysis, the following set of scaling relations arise:

(2)
$$D^* = \left(\frac{Q_0}{\rho_0 C_p T_0 \sqrt{g}}\right)^{2/5}$$
$$V^* = \sqrt{g D^*}$$

where D^* =length scale [m], Q_0 =heat source [W], ρ_0 =ambient density [kg/m³], C_p =specific heat at constant pressure [J/kg], T_0 =ambient temperature [degrees K], g=acceleration of gravity [m/s²] and V^* =velocity scale [m/s].

Finally, a detailed solution for the velocity field, which is valid both inside and outside the plume, is found by Baum and McCaffrey. This velocity field at ground level is shown in Figure 2.

Baum and McCaffrey applied their model to the study of winds generated by mass fires. The plume model was also used by Ohlemiller and Corley (1994) to estimate the thermally-induced winds generated

during large-scale mass-fire experiments carried out by Forestry Canada. In both cases, the estimated winds were found to be consistent with the measured winds.

Similarly, Trelles and Pagni (1997) used the model to estimate the winds generated by multiple burning houses at several times during the Oakland Hills fire of 1991. These predicted winds were then compared with measured wind data at the same times, and it was found that significant wind changes occurred, consistent with the model predictions, at nearly the same times. Specifically during the Oakland Hills fire, over a 15 minute interval, from 11:45 AM to 12 noon on 20 October 1991, the number of houses burning was found to increase from 38 to 259, producing dramatic changes in the winds consistent with the increased burning.

The reader should note that the fire front generated by a surface fire itself also induces entrainment winds, see Dold et al (2006), and Mell et al (2007). However, as in all of the simpler wildfire models to date, except for that of Dold, the fireline entrainment winds have not been taken into account. This approximation represents a distinct limitation of the simpler wildfire models and this proposed model. However, the proposed model represents an attempt to couple wildfire and structural fire dynamically in a model that could make predictions fast enough to be included in current operational models, such as BehavePlus, Carlton et al (2004) and FARSITE, Finney (2004).

Fire-front Propagation on a Three-dimensional Surface

For the spread of a wildfire, it is usual to consider a fire front of arbitrary shape on a horizontal surface propagating normal to itself into unburned fuel. Behind the front, the fuel is assumed to be burned, and the front is taken to be thin relative to other dimensions of the problem. The model for the front propagation can then be formulated mathematically in two related but different descriptions. One is the so-called Lagrangian description and the other is an Eulerian description, see for example, Sethian (1999) and Fendell and Wolff (2001). In the former formulation, the advance of each Lagrangian particle on the front is related to the empirically determined normal rate of spread (ROS) of a fire at the locally determined wind speed. This normal ROS is the local front velocity perpendicular to the front. It is the most straightforward description and requires following only a one-dimensional, time-dependent array of these Lagrangian particles. The latter formulates the problem as a time-dependent, convection-diffusion partial differential equation, for which the fire front at any time is a curve representing a constant value of a dependent variable of the problem. According to Sethian (1999), this formulation offers some advantages for following the front progression. However, a distinct disadvantage of this formulation is that it requires solution of a partial differential equation (PDE) in multiple spatial dimensions and time. In this section, we utilize the Lagrangian description.

The governing equations are the ordinary differential equations (ODEs) describing the propagation of an element of the fire front along the surface:

(3)
$$\frac{d\vec{R}}{dt} = (\vec{U} \cdot \vec{n})\vec{n}$$

The equations are given in vector form $\vec{R} = x(s,t)\vec{i} + y(s,t)\vec{j} + z(s,t)\vec{k}$, where $\vec{i}, \vec{j}, \vec{k}$ are unit vectors in the x, y, z directions. $\vec{U} = U_x\vec{i} + U_y\vec{j} + U_z\vec{k}$ is the ROS vector of the fire front at the location (x, y, z), and n_x, n_y, n_z are the components of the unit normal to the fire front directed toward the unburnt fuel. *s* is the arc length along the curve. The vector $(\vec{U} \cdot \vec{n})\vec{n}$ is the normal ROS. The model predicts the fire front propagation.

Let the height of the surface be specified as a function of the horizontal location. Then, only the first two of the three vector-component equations need to be solved since the fire-front curve is constrained to the surface. Therefore, the surface function is used to eliminate the height in the component equations for x and

y, yielding two ODEs for x(s,t) and y(s,t). These are solved as outlined below, and the height is determined at any horizontal location from the equation for the surface.

At each point, the fire front is advanced in the direction normal to the front at a speed determined by the local ROS for the fire. This ROS depends on the local wind speed normal to the front, which depends on the ambient velocity, an equivalent topographically induced velocity and the entrainment velocities produced by all burning structures. The topographically induced wind accounts approximately for the observation that the ROS increases uphill and decreases downhill due to buoyancy on uneven terrain, Rothermel (1972). Any local velocity induced by the fire front on itself is not taken into account. The vertical component of the velocity field is made consistent with the topography, as described in detail in the Appendix. For computational purposes, the fire front is discretized and then moved incrementally to its new location. We start with an approximation to the normal ROS, and then numerically solve the governing equations. We use the Method of Lines (MOL) and a centered difference scheme for the spatial discretization of the fire line. In the examples, we assume that the fire line initially is a straight line along the x-axis, running between -L and L (see the schematic diagram in Figure 3). Details of the mathematical equations for following the fire front are presented in the Appendix.

The model presented here and in earlier papers by the authors, is unique in that it attempts to describe the behavior of wind-blown WUI fires, not just wildland fires. Although Lagrangian models describing front propagation in wildland fuels, i.e., wildfires, have been around for a few decades, no one has attempted to extend the methodology to study WUI fires. In the next section, results from both the Lagrangian and Eulerian formulation of wind-blown WUI fires are presented and compared, and various observations are made about these results. The equations for both formulations are presented in Appendices A and B. The Level-Set methodology (LSM) is described in detail in Appendix C.

Model Results

Fire Front Propagation Past a Burning Structure

Two results using the methodology outlined above for computing a fire front propagating past a single burning structure are shown in Figure 4. These results were reported earlier by Rehm (2006) and are given here for comparison. In the plot at the left, the fire front progression is shown for a structure burning at 200 MW intensity with an ambient wind speed of 2 m/s blowing toward the top of the diagram. The structure is shown as a square 12 m on a side, and the fire front is shown every 25 s starting as a straight line 30 m below the center of the burning structure. The length of the initial fire line is 2L = 60m. For this case, the entrainment velocity produced by the burning structure accelerates the fire front as it approaches the structure and retards it after it passes. The fire front effectively spends more time in the vicinity of the burning structure.

In the plot on the right, the conditions are the same except that the fire front starts initially 10 m behind the structure; i.e., it is assumed that the peak heat release rate for the burning structure is achieved only after the fire front has passed it. In this case, the fire front is simply retarded by the entrainment flow as it tries to escape from the vicinity of the burning structure.

Fire Front Propagation over a 2D Hill with a Burning Structure

The next example using the methodology outlined above and presented in detail in the Appendix shows the computation of a fire front propagating along an elliptical hill in the presence of an ambient wind and the entrainment wind from a burning structure. The elevation of the hill is assumed to vary in the x- and

y-directions with the functional form

(4)
$$Z(x,y) = \frac{H}{1 + (x/W_x)^2 + (y/W_y)^2}$$

where *H* is the vertical amplitude of the hill in meters, here taken to be 50 meters, W_x is the length scale measured in meters in the x-direction and W_y is the length scale measured in meters in the y-direction; W_x and W_y give the horizontal dimensions of the hill, each assumed to be 100 meters (so the example hill is circular).

The equations of motion for the fire front then include an ambient wind, here assumed to be 2 m/s in the y-direction only and an entrainment wind generated by a burning structure having a heat release rate (HRR) of 100 MW located at x = 0, y = -70, and the effective wind generated by the topography. Figure 5 shows the result of such a computation for which the initial fire line is located at y = -90, meters from the peak of the hill and extends initially between x = -50 and x = 50 meters in the cross-stream direction.

Figure 5 shows the progression of the fire at equal intervals of time as it moves up the hill under the influence of three wind components, the ambient wind, the entrainment wind produced by the burning structure and the effective slope-generated wind. Using this model, the fire front progresses at a uniform speed, dependent on the ambient wind in the y-direction, in the absence of the hill and the burning structure. With no ambient wind and no burning structure, the model predicts that the topography-induced wind increases the ROS of the front up the hill and decreases it down the hill nonuniformly in the x-direction. Also for this example, comparison with and without the ambient wind shows that the ambient wind increases the ROS of the front as it propagates over the hill. The entrainment wind from the burning structure accelerates the front ahead of the structure and decelerates it behind the structure nonuniformly in the x-direction.

Fire Front Propagation over Several Burning Structures

Finally, we turn our attention to a larger area in which there are multiple burning structures at arbitrary, but specified locations. We wish to see how these burning structures can influence grass fire-front propagation as predicted by this model. We have simulated a fire front propagating on a 250 m by 250 m portion of Worley, Idaho (USA) located within the Couer d'Alene Indian Tribe Reservation Boundaries. Data sets that determine the location of non-fuel surfaces, vegetative fuels and structural fuels to 1 meter or 2 meter resolution for testing NIST modeling efforts have been developed under NIST sponsorship by the Couer d'Alene Indian Tribe GIS Program, Couer d'Alene (2007). The portion of the reservation used in this study is shown on the left of Figure 6. The 250 m by 250 m layout with eight structures is shown on the right of Figure 6. For simplicity, we have assumed that the slightly sloped land is flat and that it is covered with Australian grass, rather than trees and roads, as shown.

The results of this simulation are shown in Figure 7. We assumed a fire line initially 200 m long in the x-direction with an ambient wind of 2 m/s in the y-direction and that each house burned with a HRR of 100 MW. We allowed the simulation to run for 700 s of real time, requiring 423 CPU seconds. The time between each fire front in the simulation plot shown in Figure 7 is 70 s.

In Figure 7, note the rapid acceleration of the fire front toward the burning structures initially and the very slow progression of the front late in the simulation when the front tries to escape the influence of the eight burning structures. The net effect is for the fire front to become trapped in the vicinity of the burning structures. Therefore, it is likely that any unignited fuel in this vicinity would be exposed longer to the fire front and have an increased likelihood of ignition. As noted above, however, the model does not address ignition or burnout of the fuels.

Results using the Level-Set Method

The speed function $f(V, \theta)$ and the assumption that the front moves normal to itself into the unburned fuel determine how the fire front will propagate, Sethian (1999), Fendell and Wolff (2001), and Rehm and Mell (2009). A general form for the speed function has been suggested by Fendell and Wolff (2001). It appears that the speed function can be specified by three measurements: (1) the head-fire speed (measured in the direction of the wind), (2) the flank speed (measured in the cross-wind direction), and (3) the tail speed (measured opposite to the wind speed). However, neither the form nor the parameters used in this form are established generally for wildland fires, in large part because the field measurements are difficult to make. Earlier studies, Rehm (2008) and Rehm and Mell (2009), used a speed function appropriate for Australian grass fires $\tilde{r}_0(1 + c_f \vec{V} \cdot \vec{n})$, since both the form and the parameters were found by Cheney et al. (1998) to match field measurements reasonably well. Some results reported here use this speed function for the simulations, while others use a simplified version of the more general speed function of Fendell and colleagues (2001), (2007).

The two speed functions used in the simulations below are:

(5)
$$\tilde{f}(V,\boldsymbol{\theta}) = \tilde{r}_0(1 + c_f \vec{V} \cdot \vec{n}),$$

and the simplified speed function of Mallet et al (2007), expressed in our notation as:

(6)
$$\begin{split} \tilde{f}(V,\theta) &= \tilde{r}_0(1+c_f\sqrt{V}\cos^m\theta) & |\theta| \le \pi/2, \\ \tilde{f}(V,\theta) &= \tilde{r}_0(\alpha+(1-\alpha)\sin\theta) & \pi/2 < |\theta| \le \pi. \end{split}$$

Here, *m* and α are parameters, taken to be m = 1.5 and $\alpha = 0.5$ for the simulations shown in Figures 8 and 9, presented in the next section comparing the Lagrangian and Eulerian solutions. The remaining simulations, shown in Figures 10, 11 and 12, and also presented in the next section, used the speed function given in Eq. (5).

Lagrangian and Eulerian Solutions Compared

Simulations were carried out to compare the Lagrangian and Eulerian methodologies. The initial comparison was for the trivial case of a straight-line front in a wind blowing perpendicular to the front with periodic boundary conditions in the cross-wind direction. The spread function was for Australian grass, Eq. (1), with a wind speed of 3 m/s. For both the Lagrangian formulation using the Method of Lines (MOL) solution technique and for the LSM procedure, the front progressed with a propagation speed found to be within a few percent of that calculated from Eq. (1), even with coarse meshes such as JJ = 10, or 21 nodes for the MOL solution, and $N_x = N_y = 30$ for the LSM. Next, a more challenging example was chosen.

Figures 8 and 9 below show comparisons between the two methods for the simulation of fire front propagation for a nontrivial case, an initially circular fire front blown by a uniform wind of 3 m/s in the y-direction. The initial front is taken to have a radius of 10 m, centered at x =0, y = 50. The speed function given in Eq. (6) with $\tilde{r}_0 = 0.165$ m/s, $c_f = 3.24$ s/m, m=1.5, $\alpha =$ 0.5, is used. In Figure 8, the front is shown at five equal time intervals 6 s apart. The Eulerian formulation, using the Level-Set solution method, is shown on the left; at each time, the zero contour is obtained by interpolation from the Eulerian solution. For comparison, the Lagrangian formulation using the method of lines solution of the same problem is shown on the right. For this method, successive Lagrangian nodes have simply been joined by straight lines; therefore, the fire front in the windward direction gradually loses its smooth appearance as time increases. (A higher order interpolation of the front between Lagrangian nodes would provide a smoother contour with better visual agreement.)

Each simulation requires the selection of several parameters to carry out the simulation. For example, the Eulerian formulation requires the simulation domain be discretized in both the x- and y-directions, and boundary conditions along each of the edges of this domain must be specified. Therefore, the LSM formulation is two-dimensional and has $N_x \times N_y$ computational nodes. For the case shown in Figures 8 and 9, a domain 100 m on a side ($L_x = L_y = 100$ m with $0 \le y \le L_y, -L_x/2 \le x \le L_x/2$) was considered, with the discretization being 30 nodes ($N_x = N_y = 30$) in each direction. Therefore the total number of computational nodes for the LSM is 900. On the other hand, the Lagrangian formulation requires that the initial fire front be discretized along its circumference, which is one-dimensional and periodic. For the case shown in Figures 8 and 9, 120 nodes were used along the circumference.

In Figure 9, the fire fronts from each simulation are compared directly. In the first frame of Figure 9, the initial fire fronts are shown together, while the second compares the fronts after 6 s, the third frame after 12 s, etc. (Note that the fire-front contours obtained from each simulation have not been smoothed.) As a reference, during the 30 s of simulation time, the head velocity is expected to be 1.09 m/s, for a wind speed of 3 m/s, so that after 30 s, the head of the fire should be at x = 0, y = 92.7 m. The level-set simulation determines the head location to be at y = 93.9 m while the Lagrangian, MOL simulation, determines the head location to be at y = 92.0 m, exhibiting that both simulations seem to do a reasonable job quantitatively of determining the fire head location.

Variation of any of the parameters noted above can cause significant differences in the simulations, making detailed comparisons between simulation results and between simulation efficiencies difficult. However, several computations with different values of the parameters were performed for the case of the initially circular front shown in Figures 8 and 9, and generally it was found that the Lagrangian formulation with the MOL solution required less computational time than the LSM for similar accuracy. This conclusion is in part due to the fact that the Lagrangian formulation of the fire front is described by the temporal evolution of a one-dimensional set of nodes along the initial front, whereas the Level-Set Method requires calculating the time evolution for a scalar function on a two-dimensional set of nodes. Furthermore, the computational advantage of the Lagrangian formulation is enhanced because all of the simulations were carried out using the software package Mathematica, Wolfram (1999), in which the Ordinary Differential Equation (ODE) solver used by the MOL technique is carefully programmed and compiled and therefore very computationally efficient. However, as shown in the examples below, the LSM can handle a much wider variety of problems, ones in which fronts merge or disappear, and these more challenging problems cannot easily be solved using Lagrangian methods.

In the next two figures, these capabilities of the Level-Set methodology are illustrated. The merger of fire fronts is illustrated in Figures 10 and 11, where fronts are shown spreading and joining to form an extended front or to form an island or pocket of unburned fuel that is subsequently consumed. Figure 10 shows four frames from a Level-Set simulation of the merger of two fire fronts, one a straight line progressing in the positive y-direction, and the other generated by a growing spot fire ahead of the straight-line front. Figure 11 shows four frames from a Level-Set

simulation of the merger of three fire fronts, producing an island or a pocket of unburned fuel, which is subsequently consumed.

Finally, in Figure 12, six frames from a level-set simulation of a straight-line fire front merging with three point-ignition fronts. In the first two frames, the straight-line front and a single point-ignition front are shown, with the line moving upward at a uniform speed and the point ignition growing with time. In the third frame, a second point ignition appears to the right and down-wind of the original point ignition. In the fourth frame, the front from the original point ignition is seen to merge with the line front while the second point ignition front grows with time. In the fifth frame, a third point ignition is shown to the left and down-stream of the other two ignitions. In the final frame, both of the first two ignition fronts are seen to merge with the line front, while the third ignition front grows with time.

Discussion and Conclusions

Our analysis utilizes the plume model of Baum and McCaffrey (1989) to describe the flow field generated by a single burning house and to estimate the effects of this flow field on the progression of a surface fire. The import of the analysis, we believe, is that it demonstrates with a simple physics-based model and an inexpensive computational scheme that a house, once ignited, becomes part of the fuel system and affects fire-line progression. It also allows us to investigate the changes in the fire-line spread as various parameters are changed, such as the number and location of burning structures.

The time scale associated with burning wildland fuels is measured in tens of seconds to a few minutes. In contrast, the time scale for a burning structure is measured in tens of minutes to hours, This disparity in time scale is due, in part, to the fact that the fuel distributions for a structure and for wildland fuel differ substantially, Rehm et al (2002). For a structure, for example, the fuel loading per unit area is usually much higher and the footprint much smaller than for a parcel of wildland fuel. Because of this difference, burning structures and burning wildland fuels will not couple well in general. For example, it is shown here that burning houses can substantially influence grass fire propagation through entrainment winds. In contrast, burning grass, excluding the potential for ignition of the structure (which is not addressed in this model), is not expected to alter structure burning. (Fires propagating in wildland fuels will also generate entrainment winds that might influence structure fires; but this model cannot yet address this more difficult issue.)

Because of the disparity in time scales, however, it will be difficult to utilize a field model to compute multiple burning houses and vegetative (WUI) fires over large areas in any detail due to constraints on computational resources. An advantage of this model is that it is very fast and resolves the fire front with a minimum number of nodes, even when several burning structures are assumed involved. All examples shown have been computed in real time or less in a computational development environment (using Mathematica, see Wolfram (1999)), orders of magnitude faster than current field models. Therefore, this methodology for calculating WUI fire spread could potentially be incorporated into current operational models. Using field models for operational guidance on large-area WUI fires in the near term is unlikely.

The heat release rate of a structure fire determines the strength of its plume and defines a characteristic length scale and a characteristic velocity scale for the entrainment of the plume. This model requires that the plume stand upright, and, therefore, that the ambient wind be much

less than the characteristic plume velocity.

The surface level entrainment velocity resulting from the plume model of Baum and McCaffrey decays slowly at large distances from the burning structure. The mass-fire results of Baum and McCaffrey illustrate this fact. In the present model, the slow decay can be characterized by an amplification factor, which is the ratio of the entrainment wind due to multiple burning structures to the entrainment wind produced by a single burning structure, Rehm (2006). The entrainment factor is found to grow as the HRR of each house increases, as the number of houses increases, and as the housing density increases, as discussed by Rehm (2006).

The progression of a grass-fire front (and probably other vegetation fire fronts also) can be altered substantially by burning structures as shown by the examples presented here. These examples also show that, within the limitations of this simple model, these changes can be tracked in a computationally inexpensive and robust fashion. Even though the entrainment induced by the burning grass is not taken into account in this model, several parameters determine the details of the fire-front propagation, and only a few of these variations have been examined here.

A burning structure on a hill will increase the ROS of the fire front up the hill more quickly as it approaches the structure. It will also accelerate the front nonuniformly, with greater acceleration of the front closest to the structure and less so the further the front is from the structure. Likewise, as the front recedes from the burning structure, it retards the front nonuniformly.

The entrainment caused by multiple burning structures can cause the fire front to spend significantly more time in the vicinity of these structures. The fire front is first accelerated into the vicinity of the burning structures as it approaches and then is retarded as it tries to escape the vicinity. Because of this additional time lingering near these burning structures, the fire front may tend to ignite other fuels such as nearby structures which had not been ignited previously. As noted before, however, this simple model does not include mechanisms for ignition or burnout of the fuels. Therefore, this observation is suggested, but cannot be confirmed by the model.

Two methods for formulating and computing fire front propagation in a continuous fuel are presented. The Lagrangian formulation with the method of lines solution to the equations is one, and the Level-Set method using an Eulerian solution procedure is the other. Details of the mathematical formulations and solution procedures are presented in the Appendices. Examples of solutions obtained by both methods are presented, discussed and compared. While the Lagrangian formulation and solution seems to be computationally more efficient, the Eulerian method has the powerful advantage that it allows fronts to merge and to pinch off. Examples of this latter behavior are presented and discussed.

The ability to qualitatively describe mergers or pinching off of the fire fronts arises naturally from the Level-Set method and is a great advantage of the method. Although the behavior of the resulting fronts seems physically realistic, there is no assurance that the behavior is in fact quantitatively correct, and given the current lack of data on wildland fire-front mergers, there is little prospect for quantitative evaluation of this model behavior.

On the other hand, in the Lagrangian formulation, an algorithm that specifies either a front merger or the development of a fuel pocket behind a front under a variety of conditions is a daunting conceptual and programming task. To our knowledge, no physical description of a fire-front merger exists, nor do measurements of the phenomenon, for example. Furthermore, even if there were a valid theoretical description of the phenomena, programming the behavior of complex mergings of fronts would be tedious.

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Appendix A: Lagrangian Equations

In this Appendix, Lagrangian equations are presented for determining the fire front propagation on a specified surface or topography in the presence of burning structures. The governing equations are the ordinary differential equations (ODEs) describing the propagation of an element of the fire front along the surface:

(7)
$$\frac{d\vec{R}}{dt} = (\vec{U} \cdot \vec{n})\vec{n}$$

The equations are given in vector form $\vec{R} = x(s,t)\vec{i} + y(s,t)\vec{j} + z(s,t)\vec{k}$, where $\vec{i}, \vec{j}, \vec{k}$ are unit vectors in the x, y, z directions. $\vec{U} = U_x\vec{i} + U_y\vec{j} + U_z\vec{k}$ is the rate of spread (ROS) vector of the fire front at the location (x, y, z), and n_x, n_y, n_z are the components of the unit normal to the fire front directed toward the unburnt fuel. *s* is the arc length of the curve.

The linear relation given in Eq.(1) between the ROS and the local wind velocity is assumed. For a line of sufficient head width W and for very low moisture content of the grass, this reduces to:

$$U_n = ROS_0(1 + c_f V_{Tn})$$

where $U_n = \vec{U} \cdot \vec{n}$ and $V_{Tn} = \vec{V}_T \cdot \vec{n}$ with $ROS_0 = 0.165$ [m/s] and $c_f = 3.24$. Then

$$\frac{d\vec{R}}{dt} = ROS_0(1 + c_f \vec{V}_T \cdot \vec{n})\vec{n}$$

For notational simplicity, we will not explicitly show the time dependency of these functions as we obtain the tangent and the normal vectors to the fire front. The tangent to this curve is determined by $\vec{\tau} \equiv \frac{d\vec{R}}{ds}$ and can be written as:

(8)
$$\vec{\tau} \equiv \frac{d\vec{R}}{ds} = \frac{dx}{ds}\vec{i} + \frac{dy}{ds}\vec{j} + \left(\frac{\partial Z}{\partial x}\frac{dx}{ds} + \frac{\partial Z}{\partial y}\frac{dy}{ds}\right)\vec{k}$$

Define the normal vector to the fire front by the parameter *n* as follows:

(9)
$$\vec{N} \equiv \frac{d\vec{R}}{dn} = \frac{dx}{dn}\vec{i} + \frac{dy}{dn}\vec{j} + \left(\frac{\partial Z}{\partial x}\frac{dx}{dn} + \frac{\partial Z}{\partial y}\frac{dy}{dn}\right)\vec{k}.$$

 \vec{N} is determined by the requirement that the dot product of the normal and tangential vectors be zero: $\vec{\tau} \cdot \vec{N} = \frac{d\vec{R}}{ds} \cdot \frac{d\vec{R}}{dn} = 0.$

Define the following quantities:

(10)
$$\frac{dZ}{ds} \equiv \left(\frac{\partial Z}{\partial x}\frac{dx}{ds} + \frac{\partial Z}{\partial y}\frac{dy}{ds}\right)$$

and

(11)
$$\left(\frac{dA}{ds}\right)^2 \equiv \left(\frac{dx}{ds}\right)^2 \left[1 + \left(\frac{\partial Z}{\partial y}\right)^2\right] + \left(\frac{dy}{ds}\right)^2 \left[1 + \left(\frac{\partial Z}{\partial x}\right)^2\right] + \left(\frac{dZ}{ds}\right)^2 \left[2 + \left(\frac{\partial Z}{\partial x}\right)^2 + \left(\frac{\partial Z}{\partial y}\right)^2\right] - 2\frac{\partial Z}{\partial x}\frac{\partial Z}{\partial y}\frac{dx}{ds}\frac{dy}{ds}$$

Then, we can write the unit normal vector \vec{n} to the fire front on the prescribed surface as follows:

(12)
$$\vec{n} \equiv \frac{\vec{N}}{|\vec{N}|} = \frac{1}{\left|\frac{dA}{ds}\right|} \left[\left(\frac{dy}{ds} + \frac{dZ}{ds} \frac{\partial Z}{\partial y} \right) \vec{i} - \left(\frac{dx}{ds} + \frac{dZ}{ds} \frac{\partial Z}{\partial x} \right) \vec{j} + \left(\frac{\partial Z}{\partial x} \frac{dy}{ds} - \frac{\partial Z}{\partial y} \frac{dx}{ds} \right) \vec{k} \right]$$

At the wildland urban interface, houses as well as wildland fuels can be burning. In this model, we account for three elementary wind fields, the ambient wind, a topographically-induced wind and the entrainment wind produced by all burning structures. We assume that the total velocity at any location can then be determined by adding linearly the contributions of all the elementary wind fields. The total velocity locally is taken to be the sum of these velocity contributions:

(13)

$$V_{T,x}(x,y,z) = V_{a,x} + V_{t,x}(x,y) + V_{e,x}(x,y)$$

$$V_{T,y}(x,y,z) = V_{a,y} + V_{t,y}(x,y) + V_{e,y}(x,y)$$

$$V_{T,z}(x,y,z) = V_{a,z}(x,y) + V_{t,z}(x,y) + V_{e,z}(x,y)$$

We take for simplicity the horizontal components of the local ambient wind $(V_{a,x}, V_{a,y})$ to be uniform in space. Then, the z-component of the ambient wind is given by $V_{a,z}(x,y) = V_{a,x} \frac{\partial Z}{\partial x} + V_{a,y} \frac{\partial Z}{\partial y}$.

In the absence of any ambient wind and over flat terrain, a fire front is found to propagate with the uniform rate of spread ROS₀, as discussed above. When there are topographical features, Z(x,y), but no ambient wind, it is found that the ROS of the fire front increases uphill and decreases downhill because of buoyancy effects. This observed behavior can be treated by defining a topographically-induced horizontal velocity that is proportional to the gradient of the hill, Rothermel (1972). Here, we take this equivalent horizontal velocity to be given by the relations $V_{t,x}(x,y) \equiv \alpha \frac{\partial Z}{\partial x}$ and $V_{t,y}(x,y) \equiv \alpha \frac{\partial Z}{\partial y}$, where α is a proportionality constant, Rothermel (1972). The z-component of the topographically-induced velocity is given by $V_{t,z}(x,y) = V_{t,x} \frac{\partial Z}{\partial x} + V_{t,y} \frac{\partial Z}{\partial y}$.

For a fire front exposed to the velocity field generated by a single burning structure of HRR Q_0 , the characteristic length and velocity scales are D^* and V^* as discussed earlier. Let $\vec{r'}$ denote the vector distance from the center of the structure to the element of the fire front. The velocity at this point will be $V_e(r') = V^*G(r'/D^*)$, where $G(r'/D^*)$ is the dimensionless velocity and D^* is the length scale defined above, and the dimensionless vector distance, \vec{r} , is $\vec{r} = \vec{r'}/D^*$.

The detailed solution for the dimensionless velocity function at ground level, G(r) was obtained analytically by Baum and McCaffrey in terms of special functions. For computational purposes, however, this solution was replaced in the example calculations presented here by the functional form given below, which closely approximates the analytical solution:

$$G(r) = ar + br^{2}/2 + cr^{3}/3 + dr^{4}/4 \qquad 0 \le r \le r_{0};$$

$$f_{0}(r - r_{0})^{2} = f_{0}(r_{0} - r_{0})^{2} = f_{0}(r_{0} - r_{0})$$

$$G(r) = ar_0 + br_0^2/2 + cr_0^3/3 + dr_0^4/4 - \frac{f_0(r-r_1)^2}{2(r_1 - r_0)} + \frac{f_1(r-r_0)^2}{2(r_1 - r_0)} + \frac{f_0(r_1 - r_0)}{2} \qquad r_0 \le r \le r_1;$$

$$G(r) = \left[ar_0 + br_0^2/2 + cr_0^3/3 + dr_0^4/4 + \frac{(f_0 + f_1)}{2(r_1 - r_0)} \right] \left(\frac{r_1}{r}\right)^{(1/3)} r_1 \le r;$$

where $r_0 = 0.8, r_1 = 1.0, f_0 = 0.407199, f_1 = 0.045029, a = -2.39441, b = 11.2283, c = -13.6154, d = 4.9468.$

Therefore, for a single burning structure at (x = h, y = H), the induced horizontal entrainment velocity components at any point (x, y) are

(14)
$$V_{e,x} = \frac{x-h}{\sqrt{(x-h)^2 + (y-H)^2}} V^* G(\sqrt{(x-h)^2 + (y-H)^2}/D^*)$$
$$V_{e,y} = \frac{y-H}{\sqrt{(x-h)^2 + (y-H)^2}} V^* G(\sqrt{(x-h)^2 + (y-H)^2}/D^*)$$

The vertical component of the entrainment velocity is taken to be $V_{e,z}(x,y) = \alpha(\frac{\partial Z}{\partial x}V_{e,x}(x,y) + \frac{\partial Z}{\partial y}V_{e,y}(x,y))$.

The total entrainment from all of the burning structures is obtained by simple summation, Rehm (2006). If, for example, the *j*th structure has an entrainment velocity V_j^* and a characteristic length scale D_j^* determined by the heat release rate Q_j of the burning structure (as described in Rehm (2006)), and if the location of the structure is given by $x = h_j$, $y = H_j$, then the total entrainment velocity is given by

(15)
$$V_{e,x}(x,y) = \sum_{j=1}^{J} \frac{x - h_j}{\sqrt{(x - h_j)^2 + (y - H_j)^2}} V_j^* G\left(\sqrt{(x - h_j)^2 + (y - H_j)^2/D_j^*}\right)$$
$$V_{e,y}(x,y) = \sum_{j=1}^{J} \frac{(y - H_j)}{\sqrt{(x - h_j)^2 + (y - H_j)^2}} V_j^* G\left(\sqrt{(x - h_j)^2 + (y - H_j)^2/D_j^*}\right)$$

where we have assumed that the entrainment velocity from each burning structure is only dependent upon the vector distance in a horizontal plane between the observational location (x, y) and the location of the burning structure (h_i, H_i) .

Only the first two of the three vector-component equations for the fire-front spread need to be solved, since the front is constrained to the surface z = Z(x, y) (assuming that we can describe the surface explicitly in this form). The functional form for the surface is used to eliminate z in the component equations for x and y, yielding two ODEs for x(s,t) and y(s,t). These are solved as described below, and z is determined at (x,y) from the equation for the surface.

At each point, the fire front is advanced in the direction normal to the front at a speed determined by the local ROS for the fire. This ROS, in turn, depends on the wind speed at that location. For computational purposes, the fire front is discretized and then moved incrementally to its new location. We consider the fire line initially to be a straight line along the x-axis, running between -L and L and divide this interval into 2 *I* panels each of length δ , where $\delta = 1/I$. We start with an approximation to the normal ROS, and then numerically solve the governing equations. We use the Method of Lines (MOL) and a centered difference scheme for the spatial discretization at all interior nodes of the fire front. For the end nodes, we use a one-sided difference scheme with the neighboring interior node.

Appendix B: Eulerian Equations

Here we turn to the development of the equations for the front propagation in Eulerian form. As in the book of Sethian [5], assume that the front is defined by the contour $\phi(x, y, t) = 0$ of the front function ϕ . Let U_x, U_y be the components of the spread velocity normal to the front, $\vec{U} = U_x \vec{i}_x + U_y \vec{i}_y$.

If, as above, we take the parameter *s* to be the distance along the surface $\phi(x, y, t) = 0$ from a specified point along the front, then

(16)
$$\left(\frac{\partial \phi}{\partial x}\right)\frac{dx}{ds} + \left(\frac{\partial \phi}{\partial y}\right)\frac{dy}{ds} = 0$$

so that $\frac{dx}{ds} \approx -\frac{\partial \phi}{\partial y}$ and $\frac{dy}{ds} \approx \frac{\partial \phi}{\partial x}$. Then, the unit tangent vector can be written

(17)
$$\vec{\tau} = \frac{1}{|\nabla \phi|} \left(-\frac{\partial \phi}{\partial y} \vec{i}_x + \frac{\partial \phi}{\partial x} \vec{i}_y \right)$$

while the unit normal vector becomes

(18)
$$\vec{n} = \frac{1}{|\nabla \phi|} \left(\frac{\partial \phi}{\partial x} \vec{i}_x + \frac{\partial \phi}{\partial y} \vec{i}_y \right)$$

where $|\nabla \phi| = \sqrt{(\partial \phi/\partial x)^2 + (\partial \phi/\partial y)^2}$.

Write out the complete Eulerian equations:

(19)
$$\frac{\partial \phi}{\partial t} + U_x \frac{\partial \phi}{\partial x} + U_y \frac{\partial \phi}{\partial y} = 0$$

where

(20)
$$U_x = \tilde{r}_0 (1 + c_f \vec{V} \cdot \vec{n}) n_x \equiv f(|\vec{V}|, \vec{V} \cdot \vec{n}/|\vec{V}|) n_x,$$
$$U_y = \tilde{r}_0 (1 + c_f \vec{V} \cdot \vec{n}) n_y \equiv f(|\vec{V}|, \vec{V} \cdot \vec{n}/|\vec{V}|) n_y.$$

The spread vector, (U_x, U_y) , is normal to the fire front and has a magnitude equal to the "speed function" defined by Wolff and Fendell [6], For the examples shown below, the speed function is taken to be $\tilde{r}_0(1 + c_f \vec{V} \cdot \vec{n})$. Generally, the speed function depends upon the wind speed $|\vec{V}|$ and the angle θ between the normal to the front and the wind velocity: $\vec{V} \cdot \vec{n}/|\vec{V}| \equiv \cos \theta$.

Appendix C: Level Set Numerical Method

In this Appendix we present our method for solving the level set equation (19). The method is generally second-order in space and time but uses flux limiting schemes to preserve monotonicity of the scalar field.

The 2D spatial domain is $L_x \times L_y$ with uniform grid spacings Δx and Δy in the x and y directions, respectively. The scalar $\phi(i\Delta x, j\Delta y, n\Delta t)$ and the speed function (i.e. rate of spread) $\vec{U}(i\Delta x, j\Delta y, n\Delta t)$ are node centered: $i = 0:N_x$, $j = 0:N_y$, n is time step index. No flux, or zero gradient, boundary conditions are applied along each of the boundaries. The initial condition for ϕ is arbitrary, except that there must be some initial curve or curves representing the fire front initially for which $\phi(x, y, t = 0) = 0$.

In general, the speed function depends on the scalar gradient at the node location. However, to preserve monotonicity of the scalar field, the scalar gradient is obtained from a flux limiter which is based on the speed function. We avoid this circular problem by computing the speed function using a scalar gradient obtained from a central difference (no limiter). This speed function is then used in the PDE and also in determining the limited scalar gradient for the PDE. The basic steps of the numerical procedure are as follows:

Step 1: Given the scalar field at time t^n , the first step in the numerical procedure is to compute the node-centered scalar gradient by a central difference,

(21)
$$\left(\frac{\delta\phi}{\delta x}\right)_{i,j}^{n} = \frac{\phi_{i+1,j}^{n} - \phi_{i-1,j}^{n}}{2\Delta x},$$

(22)
$$\left(\frac{\delta\phi}{\delta y}\right)_{i,j}^{n} = \frac{\phi_{i,j+1}^{n} - \phi_{i,j-1}^{n}}{2\Delta y},$$

where $\delta/\delta x$, for example, represents the numerical approximation to the partial derivative. In what follows we will drop the time stamp until discussion of the time integration scheme.

Step 2: Use the differences obtained in Step 1 to determine the fire front unit normal vector (18) and compute the speed function via (20).

Step 3: Given the front velocity at each node from Step 2, $\vec{U}_{i,j}^n$, determine the monotonicity preserving scalar gradient for the PDE. The limiter scheme choices in our level set code (in order of increasing accuracy) are: (1) first-order upwinding, (2) minmod, and (3) Superbee, Toro (1999). As an example of how the flux limiter is implemented, consider the computation of the limited scalar gradient in the *x* direction. We imagine a cell of width Δx centered at the node location. The gradient is determined from a central difference of the scalar face values for the cell,

(23)
$$\frac{\delta\phi}{\delta x} = \frac{\phi_{east} - \phi_{west}}{\Delta x}$$

The scalar face values are determined from the flux limiter scheme. In this example, let us compute the value for the east face $(i + \frac{1}{2})$ and assume that $U_x > 0$. In the limiter scheme, the first step is to compute the local and upwind *data variations*,

(24)
$$\Delta_{loc} = \phi_{i+1,j} - \phi_{i,j},$$

(25)
$$\Delta_{up} = \phi_{i,j} - \phi_{i-1,j}$$

These values are used to form the local data ratio,

(26)
$$r = \frac{\Delta_{up}}{\Delta_{loc}}$$

In practice, we set r = 0 if $\Delta_{loc} = 0$. The face value is now simply determined from

(27)
$$\phi_{east} = \phi_{i,j} + \frac{1}{2}B(\phi_{i+1,j} - \phi_{i,j}),$$

where *B* is the flux limiter function evaluated from one of the following, Toro (1999):

(28)
$$B(r) = 0$$
 first-order upwinding,

$$B(r) = \max(0, \min(1, r))$$
 minmod,

$$B(r) = \max(0, \min(2r, 1), \min(r, 2))$$
 Superbee.

Note that when B = 1, the scheme recovers second-order central differencing.

Step 4: Time integration. We have now discussed all the details associated with computing the right hand side (RHS) of the scalar partial differential equation (PDE). To advance the field in time, we use a second-order Runge-Kutta scheme, Gottlieb et al (2001). This scheme is simply a linear combination of two Forward Euler steps. Let $F(\phi) = \vec{U} \cdot \nabla \phi$ denote the advective terms of the PDE obtained via Steps 2 and 3 above; ∇ denotes the limited discrete gradient operator. The time integration proceeds as follows:

(29)
$$\begin{aligned} \phi_{i,j}^* &= \phi_{i,j}^n - \Delta t F_{i,j}(\phi^n), \\ \phi_{i,j}^{n+1} &= \frac{1}{2} \phi_{i,j}^n + \frac{1}{2} \left(\phi_{i,j}^* - \Delta t F_{i,j}(\phi^*) \right). \end{aligned}$$

The fire front is obtained from the zero level crossing of the scalar field.

Figure Captions

Figure 1. Photograph of a fire front approaching the Scripps Ranch residential community during the Cedar Fire in October 2003. (Photograph by John Gibbins of the San Diego Post Tribune.)

Figure 2. TOP: Dimensionless entrainment velocity at ground level induced by a structure fire. The velocity is plotted as a function of the dimensionless radial distance from the structure. BOTTOM: Dimensionless entrainment velocity vectors at ground level induced by the burning structure. See Equation (2) in the text for the length scale used for the nondimensionalization.

Figure 3. A schematic diagram showing the initial location, the ambient velocity (V_a) and the extent (between the vertical bars in the x-direction) of the horizontal fire line, The burning structure is initially a vertical (y) distance h from the front.

Figure 4. The fire front at several equal time intervals for a burning structure with an ambient wind of 2 m/s, a 200 MW fire and L = 30 m. Distances are shown in meters. TOP: House is burning before arrival of fire front. BOTTOM: House ignites and becomes fully involved after passage of fire front.

Figure 5. The fire front at several equal time intervals propagating up a hill under a an ambient wind, an entrainment wind from the burning structure and the topography-induced wind caused by the hill. Distances are measured in meters.

Figure 6. Diagram showing the location of an area under study in Worley, Idaho, at the left and a small section of the study area that includes the positions of eight structures. This small section is used as an example for model fire predictions in the WUI.

Figure 7. The propagation of a fire front through the small area shown in the previous figure, assuming all of the structures are burning. Distances are measured in meters.

Figure 8. LEFT: The progression of a wind-blown fire front from an initially circular fire is shown. The model is formulated as a two-dimensional Eulerian partial differential equation (PDE) and solved with a level-set methodology. For initial conditions, the front is taken to be circular with a radius of 10 m, centered at x = 0, y = 50. The scenario shows what might be expected during the growth of a spot fire when a steady wind is blowing in the positive y-direction. RIGHT: The same scenario as shown on the left, except that these results were obtained using the Lagrangian formulation for the front progression and solving the resulting ordinary differential equations (ODEs) by the method of lines (MOL).

Figure 9. Comparison of the solutions obtained by the two methods, initially and every six seconds.

Figure 10. Four frames from a level-set simulation of the merger of two fire fronts, one a straight-line front progressing normal to itself in the positive y-direction, and the other generated from a spot fire ahead of the line fire. The order of the frames is upper left first, upper right second, lower left third and lower right last.

Figure 11. Four frames from a level-set simulation of the merger of three fire fronts, producing an island or a pocket of unburned fuel, which is subsequently consumed.

Figure 12. Six frames from a level-set simulation of a straight-line fire front merging with three point-

ignition fronts. In the first two frames the straight-line front and a single point-ignition front are shown with the line moving upward at a uniform speed and the point ignition growing with time. In the third frame, a second point ignition appears to the right and down-wind of the original point ignition. In the fourth frame, the front from the original point ignition is seen to merge with the line front while the second point ignition front grows with time. In the fifth frame, a third point ignition is shown to the left and down-stream of the other two ignitions. In the final frame, both of the first two ignition fronts are seen to merge with the line front, while the third ignition front grows with time.

Figure 1. Rehm and McDermott



Photo by JOHN GIBBINS / Union-Tribune Cedar Fire about to engulf the Scripps Ranch residential community





Figure 3. Rehm and McDermott



Figure 4a, 4b. Rehm and McDermott



Figure 5. Rehm and McDermott



Figure 6. Rehm and McDermott



Figure 7. Rehm and McDermott







Figure 9. Rehm and McDermott











Figure 11. Rehm and McDermott









