

NISTIR 7724

**A Next Generation Electrodynamic
Shaker for the Primary Calibration of
Accelerometers**

The NIST and AFMETCAL Super Shaker Project

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A Next Generation Electrodynamic Shaker for the Primary Calibration of Accelerometers

The NIST and AFMETCAL Super Shaker Project

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Introduction

A new shaker system was designed to allow direct primary calibration of accelerometers using both reciprocity and interferometer techniques over the frequency range 40 Hz to 10,000 Hz. The system uses dual magnets and a dual-coil moving element. The design uses damped flexures to support the moving element. The dual-coil feature eliminates the need for an additional shaker for reciprocity calibrations. To accommodate improved comparison calibrations, the moving element is compact in design and is equipped with axially-oriented mounting tables at each end. Provision of easy laser interferometer beam access to both ends of the moving element allows interferometric accelerometer calibrations.

In order to maximize the potential for design optimization, two Super Shaker systems were built: Super Shaker I located at the Air Force Metrology Laboratory (AFMETCAL) Heath, OH, and Super Shaker II located at NIST. The design also allows comparison calibrations to be performed over this same frequency range. This report gives performance data for both shakers, with the AFMETCAL shaker referred to in this report as SS1, and the NIST shaker as SS2. The SS2 shaker was the second shaker constructed and incorporates minor changes from the original design. The principal change was a more flexible flexure system for the moving element support.

Design Criteria

Primary calibration methods for accelerometers (reciprocity and laser interferometry) require high purity of the displacement signal wave form. This is especially true for reciprocity calibrations. For reciprocity measurements, the procedure does not take into account the fact that the accelerometer is measuring motion in only one direction, but rather the calculations involve measurement of current differences in the drive coil. Therefore, even a small amounts of distortion and cross-axis motion adversely affect the reciprocity calibration. A general rule is that cross-axis motion should be less than 5% and harmonic distortion less than 2% in order to perform reciprocity calibrations at 1 to 2% uncertainty. For laser interferometer fringe-counting calibration, only the

on-axis displacement amplitude is measured. Provided that the laser beam/interferometer is properly aligned, the cross-axis motion of the shaker is not as significant in a fringe-counting calibration as in the reciprocity calibration. In designing the Super Shaker [1,2], care was taken to minimize both harmonic distortion and cross-axis motion. Minimization of the latter was especially important to our goal of improving reciprocity calibrations. Among the critical factors considered were:

1. Magnet dimensions, especially the air gap size, roundness, symmetry, and finish.
2. Moving element dimensions, including diameter, symmetry, and roundness.
3. Position and repeatability of position of the moving element in the magnetic gap assembly.
4. Symmetry of coil windings and uniformity of coil wire.
5. Suspension system for the moving element in the magnetic gap assembly.
6. Isolation of critical parts of the shaker to prevent cross coupling of various vibrating parts of the assembly.

The dimensional tolerances for all Super Shaker assemblies were specified to be no greater than 30 μm (0.001 inch).

Description of the Shaker Assembly

The Super Shaker, shown in Fig. 1, is 0.64 m (25 in) wide, 1.22 m (48 in) long, by about 0.5 m (20 in) high. It is mounted on soft rubber pads on a heavy flat table, pneumatically isolated from ground vibration.

The frame consists of three supporting pedestals, one at each end and one in the middle, and four large diameter shafts running end to end, two clamped near the bottom of the three pedestals, and two clamped near the top of the pedestals. Two magnet assemblies, equipped with air bearings, are supported by the two horizontal rods which are the upper shafts of the frame assembly. The air bearings allow each magnet assembly to be moved away from the moving element to provide the access needed for attachment of accelerometers or masses. The operating axis is parallel to the upper shafts and centered in the plane bisecting them.

A common cause of calibration inaccuracy is interference from frame resonances. The interferences are resisted by internal dampers inside the three pedestals and by damping inside the four shafts. The pedestals and shafts are

also filled with sand to further dampen any vibration in the frame. These interferences are further resisted by the large magnet mass, and small resulting motion, as compared to the moving element mass. The small magnet motions are isolated from the frame by rubber pads.

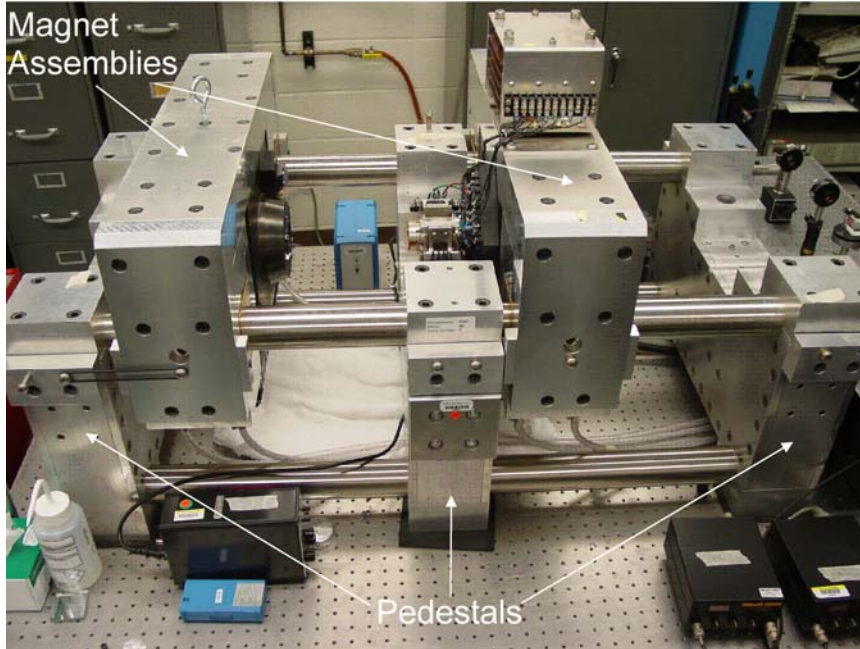


Figure 1a. SS2 at NIST

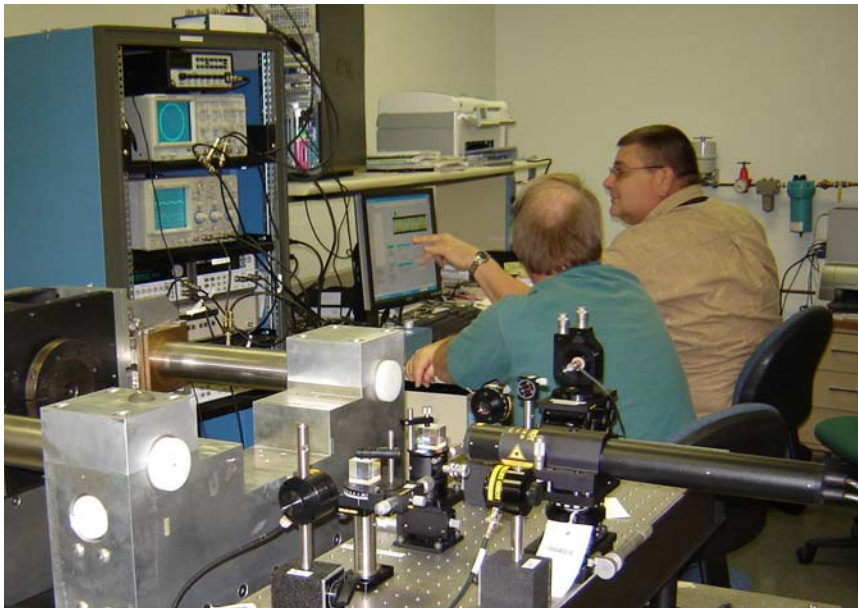


Figure 1b. SS1 with instrumentation and optical components of laser interferometer at AFMETCAL, Heath, OH

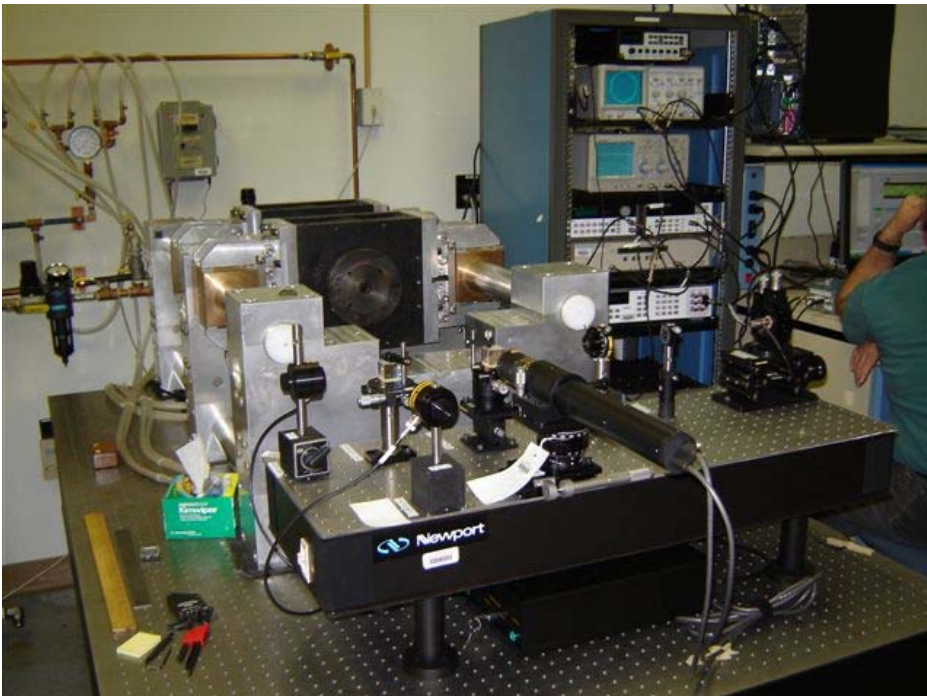


Figure 1c. SS1 mounted on isolation table at AFMETCAL, Heath, OH

A carriage on the middle pedestal supports the moving element, centered on the operating axis. The moving element is symmetrical, with coils on each end. Machined from a solid aluminum block, the moving element, shown in Fig. 2, is symmetrically shaped with respect to a bisecting plane perpendicular to the operating axis. The moving element, supported by damped flexures attached to the pedestal in the middle, carries the accelerometer to be calibrated.

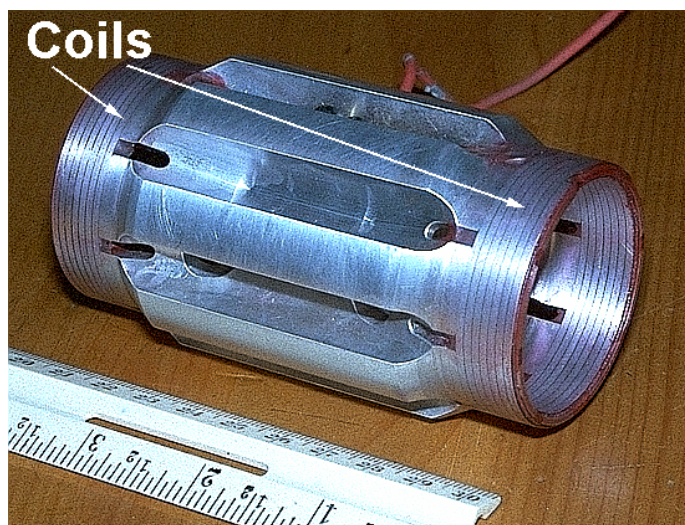


Figure 2. Moving element of SS1

Placement of the specimen (accelerometer) mounting tables at the ends of deep central cavities of the moving element allows specimens to be mounted close to the bisecting plane and inside the envelopes of the coils located at each end. The outer structure between the two coils is enlarged to provide axial stiffness for high frequency operation. The shaker is equipped with removable mounting tables (or cones), made from beryllium with a nickel coating to prevent scratching, Fig. 3a. The cones have threaded steel inserts for mounting accelerometers. The beryllium mounting cones extend the frequency range of the shaker to 10,000 Hz. Special wrenches were designed to enable easy removal or attachment of the cones to the moving element, Fig. 3b and 3c.



Figure 3a. Nickel-coated beryllium mounting tables for the moving element, shown with titanium threaded inserts



Figure 3b. Wrench for attaching and removing mounting tables, shown with table on wrench



Figure 3c. Wrenches for attaching and removing mounting tables, shown with tables loaded on wrench

Moveable Magnet Assemblies

The magnet assembly is shown in Fig. 4. Each magnet assembly has two major parts: the outer permanent magnet and an inner air gap assembly. The mass of the permanent magnets, 68kg, has been maximized within practical constraints in order to minimize the motion of the magnet assembly relative to the moving element, 225g. This reduces interference to the rectilinear motion of the moving element. Residual magnet motions are isolated from the frame by rubber pads.

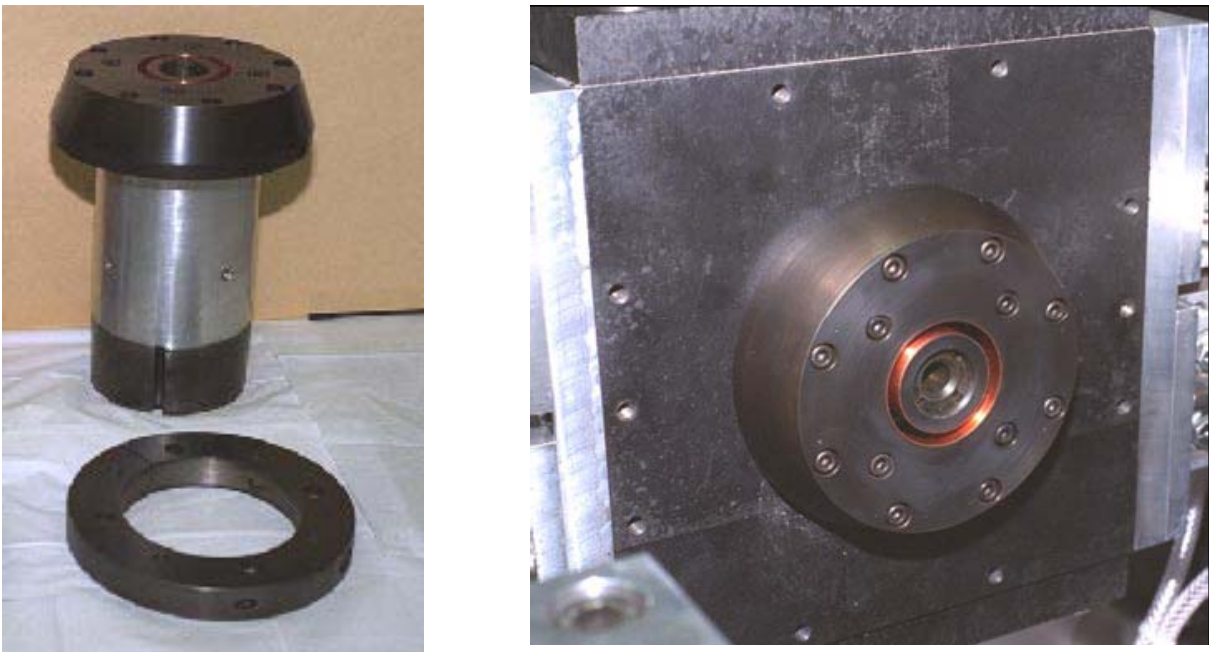


Figure 4. Inner gap assembly (left) and complete magnet assembly (right)

Each air gap assembly is equipped with inner and outer copper shading sleeves, a large axial port for the accelerometer cable, and four small ports for interferometer beam access. Each assembly is also equipped with additional ports for air cooling as needed. The air gap assemblies are de-mountable to facilitate installation of new assemblies of different air gap sizes, should future applications require moving elements of different size. Magnetic keepers are provided to allow this to be done without demagnetizing the permanent magnets.

Moving Element and Carriage Description

The moving element and carriage assembly are shown in Fig. 5, attached to the middle pedestal of the shaker. The length of the assembly is 101.6 mm (4 in) and the diameter is 63.5 mm (2.5 in). The structure is aluminum and the mounting tables are of beryllium as described above, and are 25.4 mm (one inch) in diameter. The first axial resonance is approximately 22 kHz. The diameter of the mounting table is adequate to allow the laser beam the access required for multiple-reflection interferometer calibrations.

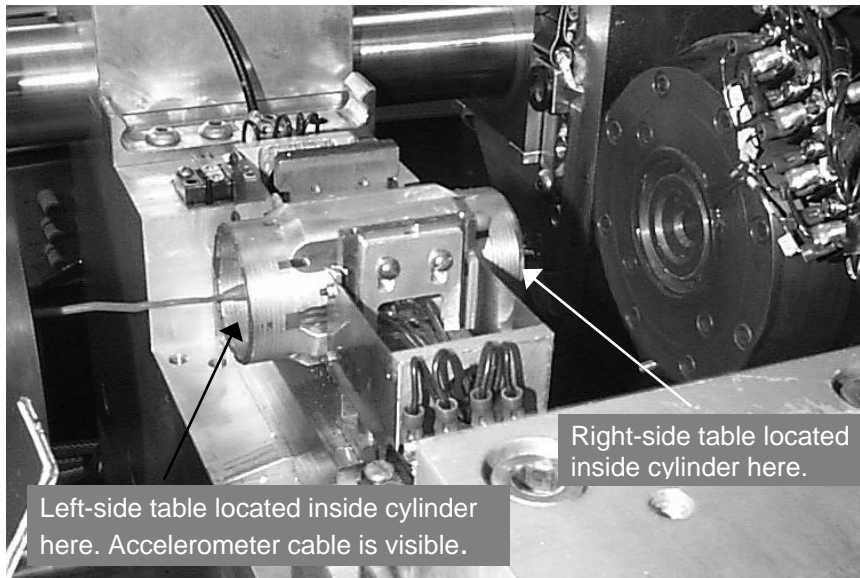


Figure 5. Moving element and carriage assembly, shown with accelerometer attached

To maximize versatility, the four laser beam ports provided in each air gap assembly for this purpose are positioned at 90 degree intervals.

The carriage of the Super Shaker supports the moving element on four damped beryllium copper flexures. These flexures establish the rest position of the moving element, guide its motion along the system axis, and resist motions perpendicular to the system axis.

Shaker Operation

The vibratory drive force for the moving element is generated by an alternating current in one or both of the drive coils in the air gap magnetic fields. For reciprocity calibrations, only one moving element coil is driven. For interferometric or comparison calibrations, either or both of the coils may be driven. Both coils are driven when large displacements and accelerations are desired.

A low-distortion power amplifier amplifies a signal from an external signal source to provide the alternating current. As necessary, power amplifier heating is reduced by connecting high-power resistors in series with the amplifier output. The use of these resistors is important for high frequency interferometric operation and critical for pulse operation. The current applied to the drive coil(s) must have low levels of harmonic distortion in order to minimize interference caused by excitation of high frequency (typically above 20 kHz) resonances of the accelerometer or moving element.

Shaker Performance Tests

Extensive performance tests were conducted on shakers SS1 and SS2. These tests examined harmonic distortion, cross-axis motion, relative motion between the two mounting surfaces of the moving element, unwanted movement of the optics relative to the shaker, and random effects on repeated measurements (repeatability). The first three of these factors were observed to have a significant influence on the uncertainty of calibrations performed on this system. Tests and results for these factors are detailed below.

A Fast Fourier Transform (FFT) signal analyzer was used to measure the harmonic distortion components of an accelerometer mounted on the shaker. The tests were run at approximately 20 m/s^2 ($2 g_n^1$) and the maximum harmonic component at each frequency is shown in Fig. 6. Harmonic distortion can be minimized by careful design of the moving element and magnet structure, as described in the Design Criteria section above.

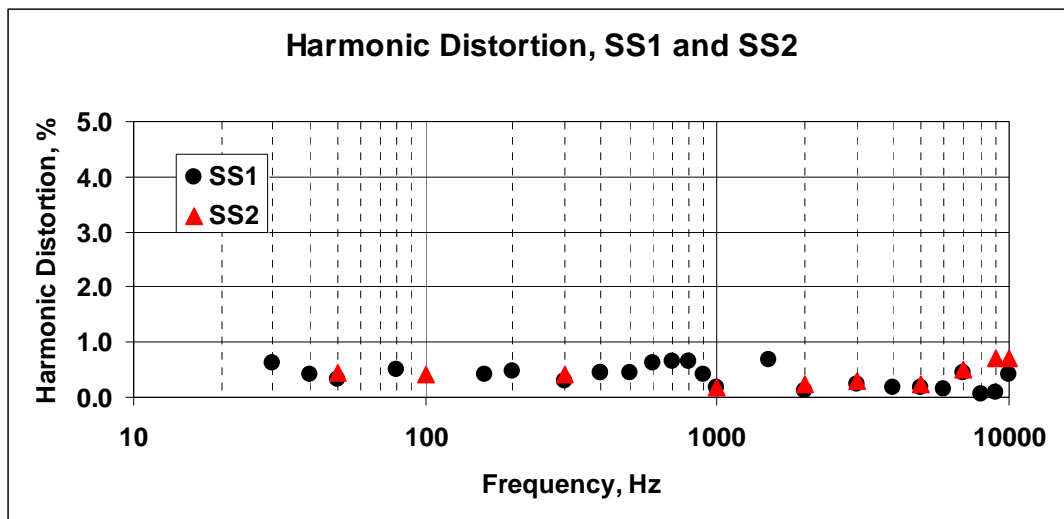


Figure 6. Total harmonic distortion for SS1 and SS2

¹ $g_n = 9.80665 \text{ m/s}^2$

The cross-axis motion was measured with a small tri-axial accelerometer having a mass of 5 grams. The cross-axis data is plotted in Fig. 7. These data should be considered as an approximate indication of the true cross-axis motion since calibration masses could not be attached to the table at the same time the lightweight accelerometer was attached.

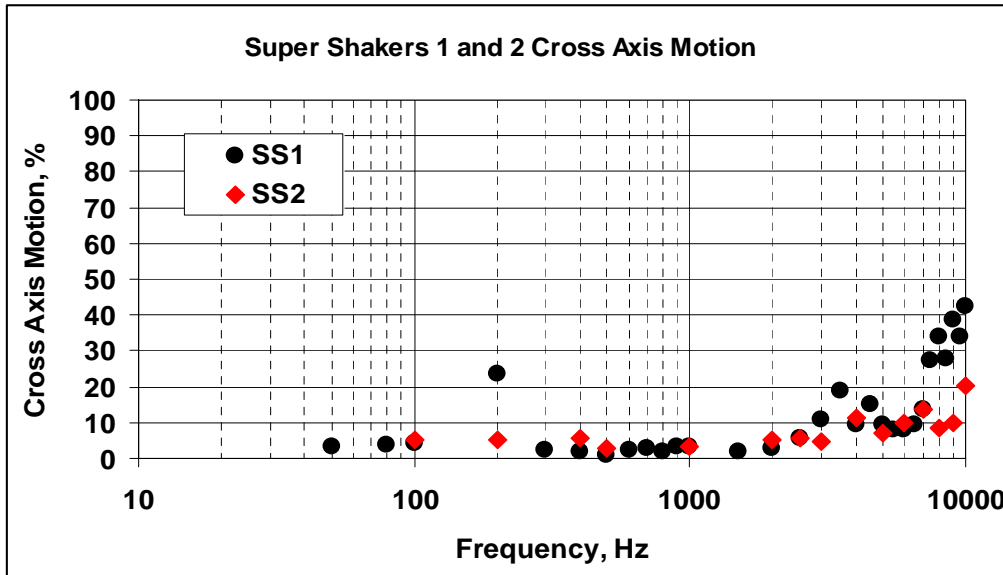


Figure 7. Cross axis motion for SS1 and SS2

Relative motion between the two mounting tables was measured by placing a polished 20 gram tungsten dummy mass on the mounting table where the test accelerometer is normally mounted. A single point laser vibrometer was used to measure the displacement at three positions on the mass, approximately 120 degrees apart. The average displacement taken at the three positions was then compared to the displacement as measured by the quadrature laser interferometer on the other mounting table which has a small mirror attached in the axial center. The differences (%) in the measured displacement of the two mounting tables are shown graphically in Fig. 8.

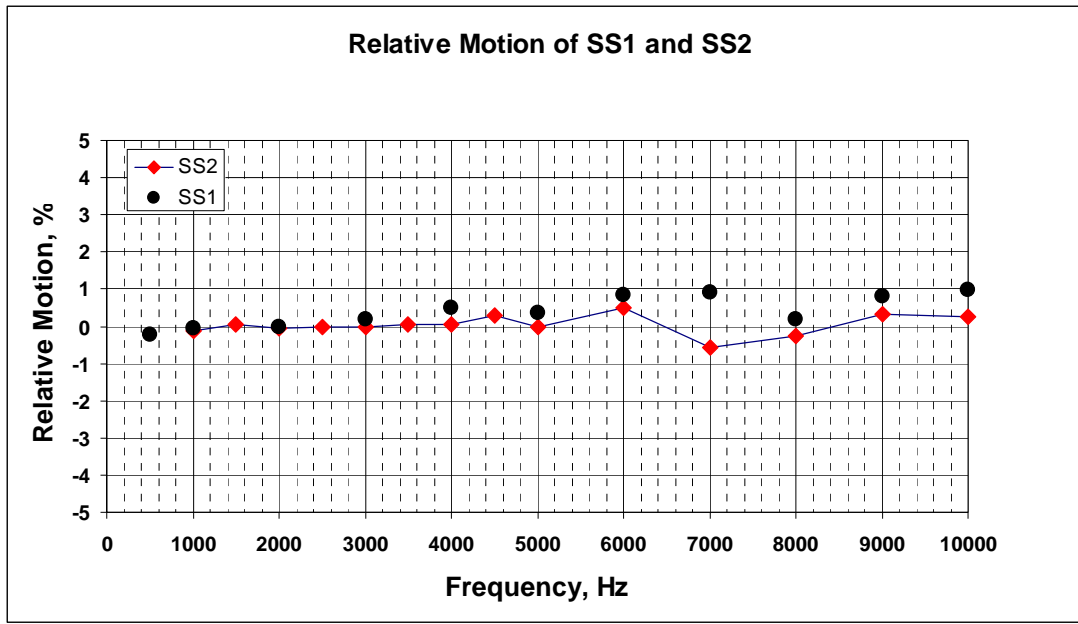


Figure 8. Relative motion between the two mounting tables of the shaker

Calibration by Reciprocity

Reciprocity calibration of accelerometers has been in use at NIST for many years as a primary method for calibration. It is distinct in that it does not rely on optical instrumentation. It is not based on the wavelength of light, but upon mass for its primary reference. For reciprocity calibrations, a series of five small tungsten carbide precision masses are attached one at a time to the right mounting table, with the accelerometer to be calibrated on the left mounting table (see figure 5). The calibration is briefly describe below, and in more detail in the references listed at the end of this paper [3], [4], and [5].

Since the current in the driver coil is one of the measured quantities, it is necessary to keep the mean position of the moving element constant relative to the magnet. The Super Shaker's moving element operates in a horizontal orientation (figure 5). This avoids the problem encountered in vertical oriented shakers of repositioning the driver coil to the exact same position in the magnetic field when different masses are attached. The flexures of the Super Shaker tend to keep the moving element in approximately the same position relative to the magnet, regardless of the value of the mass attached. Better repositioning of the moving element between mass changes is obtained by delaying the next measurement by a few minutes, to allow the flexures to reposition.

For reciprocity calibration, the test accelerometer is mounted on the left, as shown in Fig. 5; the mirror is removed from the right, and the right mounting table

is used for attaching the calibration masses. At sufficiently low frequencies the magnitude of the accelerometer sensitivity (S) may be approximated [3-5] by:

$$S = [(JR)/(2\pi f)]^{1/2}, \quad (1)$$

where:

parameter J equals the zero intercept of a linear fit of $m/(Y_m - Y_0)$ vs. m , where Y_m and Y_0 are the measured transfer admittance with and without the calibration mass, m .

The transfer admittance is calculated by dividing the current of the driver coil by the output voltage of the accelerometer while the shaker is energized by the left coil. In a separate measurement, R is the voltage ratio of the output voltage of the accelerometer to the output voltage across the left coil when used as a velocity sensor while the shaker is energized by the right coil. For the voltage ratio measurements no calibration mass is attached to the right table. The test frequency is represented by f .

It is critical that the coil of the reciprocal transducer remain in the same static position in the magnetic gap so that the magnetic field to which the coil is exposed will not vary as a function of mass loading. This position must remain stable so that changes in coil current for different masses can be measured accurately. Temperature should remain constant so that the physical dimensions of the shaker, the transduction characteristics of the reciprocal transducer, and the resistance used for current measurements will remain constant. For greater stability, the coil is driven at about 20 m/s^2 ($2 g_n$) and allowed to remain energized throughout the measurements for all five masses. This results in measured voltages of typically 5 mV to 500 mV. The two digital voltmeters are placed close to the moving element so that the connecting cables can be kept short to reduce electrical noise. A thermocouple was attached to the accelerometer and the temperature was stabilized to about $\pm 0.2 \text{ }^\circ\text{C}$.

Figure 9 shows data for reciprocity and fringe-counting calibrations on a single-ended accelerometer at 100 Hz.

The estimated combined expanded uncertainty associated with the calibration results obtained by reciprocity at 100 Hz is 0.26 % based on the current implementation of the measurement apparatus. This combined expanded uncertainty was calculated in accordance with methodologies described in the Guide to the Expression of Uncertainty in Measurement [6] using Type A and Type B evaluations of uncertainty components, including those contained in ISO documents on the calibration of vibration and shock transducers [7]. Using a coverage factor of 2, the estimated expanded relative uncertainty, U , at 100 Hz is: 0.5 %.

For a set of ten calibrations by each method, the maximum difference between any two data points of either of the two methods was never more than 0.3 %, and the averages of the results obtained with the two methods agree within 0.04 %.

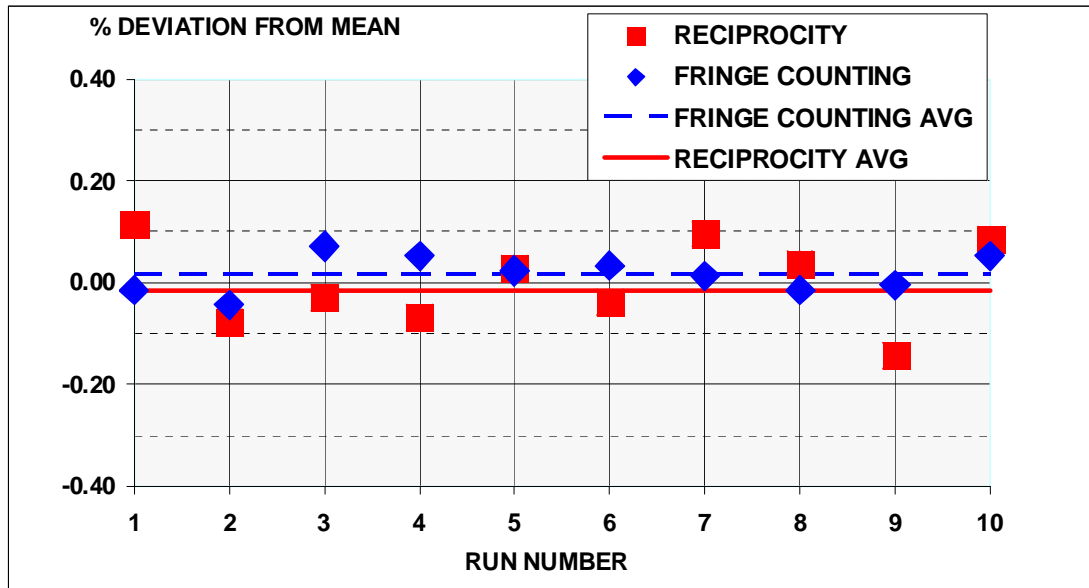


Figure 9. Data for reciprocity and fringe-counting calibrations on a single-ended accelerometer at 100 Hz

Calibration by Laser Fringe-Counting Interferometry

A flat mirror is mounted on the table located on the right side of the moving element opposite the table upon which the accelerometer is mounted (Fig.10). The shaker design allows optical access to the shaker mounting tables through a center hole in the magnet (figure 4). The acceleration, in meters per second squared, is given by

$$A = \lambda \nu \pi^2 f^2 / 2, \quad (2)$$

where λ is the wavelength of He-Ne laser light in meters, ν is the number of fringe counts per vibration cycle, and f is frequency in hertz [2,8]. To provide additional displacement, both the right and left coils can be driven in a push-pull configuration.

In addition to distortion and cross-axis motion which are critical to reciprocity calibrations, the critical elements of interferometer operation also include interferometer alignment and mechanical coupling between the shaker and the interferometer components. The shaker system was designed to minimize this coupling. The mass of the moving element (approximately 225 g) is very small

compared to the mass of the magnet (approximately 68 kg) in order to minimize magnet movement. The shaker system is installed on an air isolation table to minimize the effects of floor movements. The magnets are moved into place on air-bearing guides, and during operation the magnets are locked into place by turning off the air to the bearings.

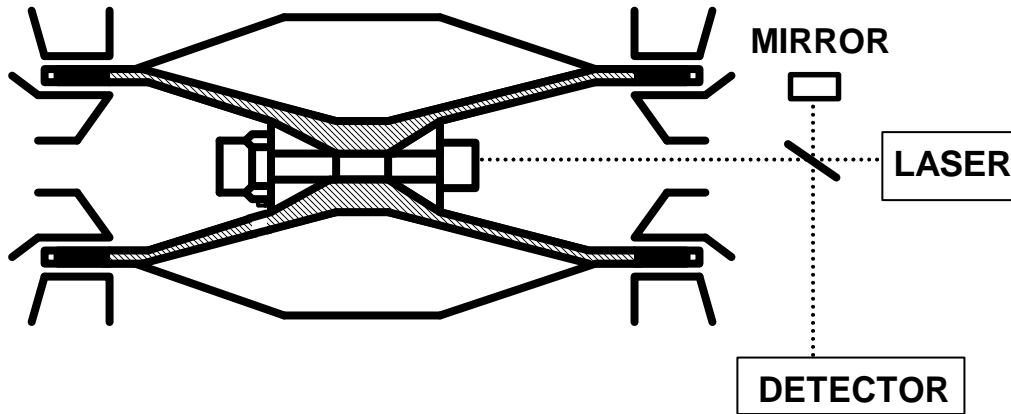


Figure 10. Schematic for fringe-counting interferometer setup on the Super Shaker

Calibration by Minimum-Point Method Laser Interferometry

The minimum-point method is based on the determination of displacement corresponding to the zero crossings of the Bessel function of the first kind and first order, J_1 . This method utilizes the same setup as shown in Fig. 10 for calibrations performed in the frequency range of 1 kHz to 5 kHz. In order to reject spectral components present in the output of the photo-detector except that corresponding to the fundamental frequency of vibration, the output of the photo-detector is filtered using a narrow band-pass filter centered at the fundamental frequency of vibration. The amplitude of vibration is then adjusted until the null corresponding to the desired zero crossing of J_1 is obtained. Peak displacement amplitudes of the first six zero crossings of J_1 for a He-Ne laser ($\lambda=632.8$ nm) are listed in Table 1. For minimum-point calibrations, at each tested frequency the number of the zero crossing was selected to obtain displacements corresponding to accelerations of approximately 50 m/s^2 or greater.

Table 1. Peak Displacement Amplitudes for the First Six Zero Crossings

Zero Crossing No.	Displacement (nm)
0	0.00
1	192.95
2	353.29
3	512.31
4	670.95
5	829.42

Once the displacement, d , is determined, the acceleration is calculated using the following equation:

$$A=(2\pi f)^2 d. \quad (3)$$

The sensitivity of the accelerometer is then obtained by dividing the accelerometer output voltage by the acceleration, A .

Calibration data using fringe-counting and minimum-point methods for a single-ended accelerometer is shown in Fig. 11.

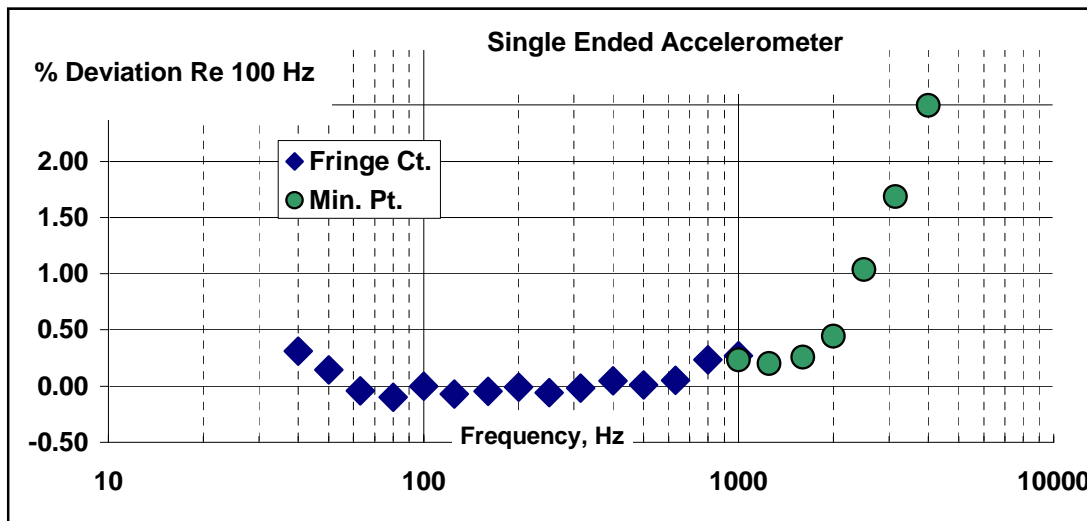


Figure 11. Calibration data for a single-ended accelerometer using fringe-counting and minimum-point methods

The estimated combined uncertainty associated with the calibration results obtained by minimum-point interferometry at 1 kHz is 0.22 % based on the current implementation of the measurement apparatus. This combined

uncertainty was calculated in accordance with methodologies described in the Guide to the Expression of Uncertainty in Measurement [6] using Type A and Type B evaluations of uncertainty components, including those contained in ISO documents [7] on the calibration of vibration and shock transducers. Using a coverage factor of 2, the estimated expanded relative uncertainty, U , for the minimum-point method at 1 kHz is: 0.5 %, and the estimated expanded relative uncertainty, U , at 100 Hz is: 0.3 % using fringe-counting. Data for the two calibration methods at the overlapping frequency of 1 kHz agree to within less than 0.1 %.

Calibration by Sine-Approximation Method Using Quadrature Laser Interferometry

A piezo-electric shaker, as illustrated in figure 12, with a single mounting table and a driving element on the opposite end is typically used for accelerometer calibrations. The accelerometer is mounted at the center of the shaker table and mirrors are mounted around the perimeter of the accelerometer.

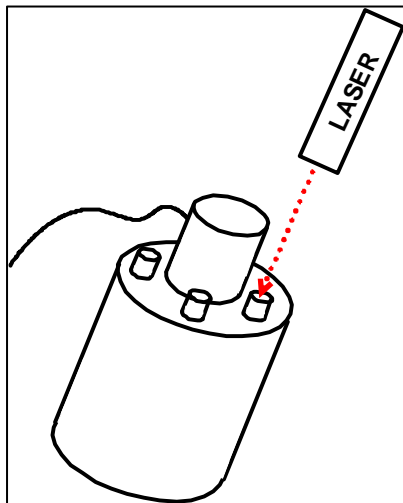


Figure 12. Conventional three-mirror method for calibration using a single coil or piezo-electric shaker for interferometric calibration

Displacement must be measured at three or more positions and then averaged to get a good representation of the displacement of the plane on which the accelerometer is mounted.

Another approach is shown in Fig. 13 using the dual-coil Super Shaker. Here the accelerometer is mounted on the table opposite the reflecting mirror. Using reflection from the center of the mirror will enable accurate measurement of the displacement of the accelerometer using only the center position of the moving mirror provided the relative motion between the surfaces of the two tables is small. Tests conducted at NIST have shown that significant relative motion is experienced between tables fabricated from stainless steel or aluminum for

frequencies higher than 5 kHz. Using a mounting table fabricated from beryllium with nickel plating provides for much smaller relative motion between the tables, and permits calibration of accelerometers up to 10,000 Hz using only one measuring point at the center of the mirror.

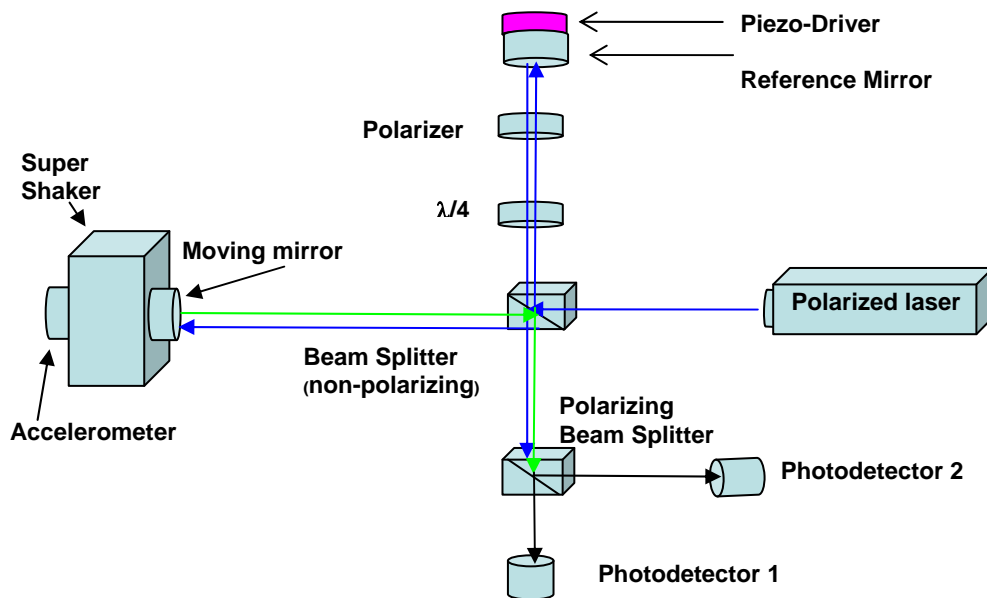


Figure 13. Setup using quadrature laser interferometer for sine-approximation, minimum-point, and fringe-counting methods

Using the setup shown in Fig. 13, calibration data can be obtained using the dual-coil shaker, for frequencies up to 1 kHz using fringe-counting, and up to 5 kHz using the minimum-point method by monitoring the output from either detector 1 or detector 2. These methods and procedures are documented in other NIST publications [9] and in ISO 16063 - Part 11 [7]. In order to calibrate at frequencies higher than 5 kHz, the sine-approximation method is used. This method is useful at higher frequencies where calibrations at smaller displacements must be made due to amplitude limitations in electro-dynamic shakers. The current implementation of the NIST dual-coil shaker limits the acceleration to approximately 200 m/s^2 . In actual practice the sine-approximation method gives good results over a wide frequency range, 100 Hz to 10,000 Hz. It is also much less demanding on the shaker, since it can operate at lower accelerations than the minimum-point method for higher frequencies. Typically,

the sine-approximation method is used at NIST for calibration of accelerometers at accelerations of 200 m/s² to 500 m/s² from 100 Hz to 10 kHz, and fringe-counting is used for frequencies of 100 Hz and below. This range of acceleration is used to minimize the heating effects on the shaker. The minimum-point method can be used as check on the other methods, but is not usually used at NIST on a daily basis.

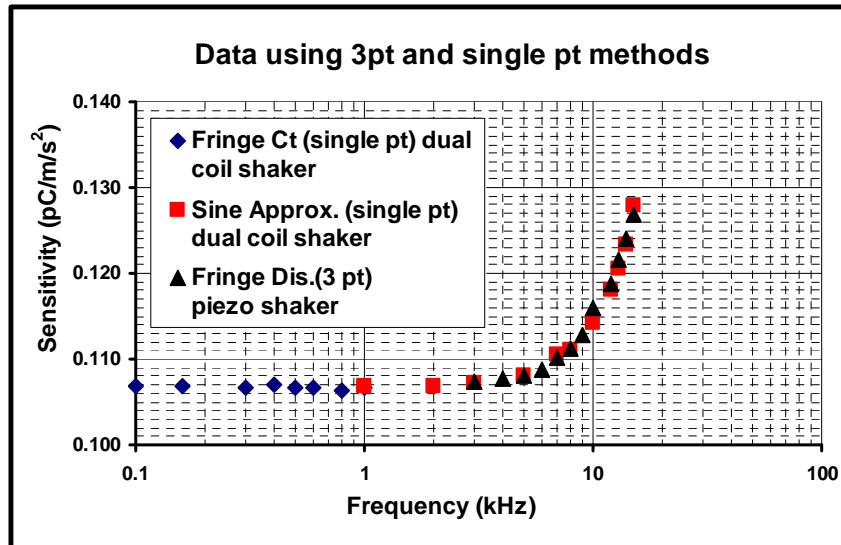


Figure 14. Calibration data on a single-ended accelerometer using single point (SS2 shaker) and three point (piezo-electric shaker) techniques

Calibration data using fringe-counting and sine-approximation methods for a single-ended accelerometer on SS2 is shown in Fig. 14. This calibration uses a single point measurement, and thereby requires minimal adjustment to the interferometer. Data using fringe-disappearance on a piezo-electric shaker is also shown in Fig. 14. This data requires measurements at three positions on the shaker and thus requires realignment for each position.

The combined relative uncertainties for both the fringe-counting and sine-approximation methods were calculated in accordance with methodologies described in the Guide to the Expression of Uncertainty in Measurement [6] using Type A and Type B evaluations of uncertainty components, including those contained in ISO documents [7] on the calibration of vibration and shock transducers. For the fringe-counting method, using a coverage factor of 2, the estimated expanded uncertainty, U , at 100 Hz is 0.5 %. For the sine-approximation method, again using a coverage factor of 2, the estimated expanded relative uncertainty, U , at 1 kHz is 0.5 %, at 5 kHz is 0.75 %, and at 10 kHz is 1% for the NIST Super Shaker.

Summary of Uncertainties

The overall uncertainties of the two shakers were calculated as stated above using the ISO 16063-11 standard [7]. Figure 15 gives the results of these calculations for the fringe-counting, minimum-point, and sine-approximation methods. The estimated expanded uncertainties, U , for frequencies 40 Hz to 100 Hz were found to be less than 0.5 % using fringe-counting. These results are published in BIPM/CIPM key comparison CCAUV.V-K1 (Vibration), 2001 [10] for SS1. Additional details on the uncertainty calculations are given in the Appendix of this document.

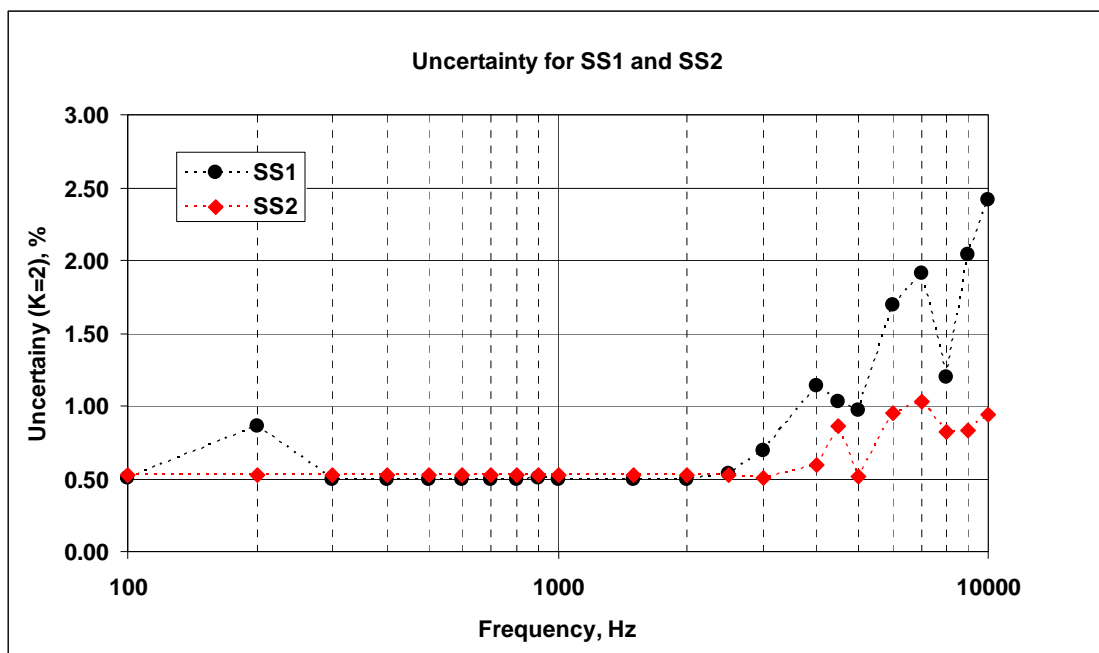


Figure 15. Calculated uncertainties for SS1 and SS2

Performance

The two shakers SS1 (AFMETCAL) and SS2 (NIST) were used to calibrate a single-ended accelerometer. The results, given in Fig. 16, show good agreement between the two systems and are within the uncertainty estimates.

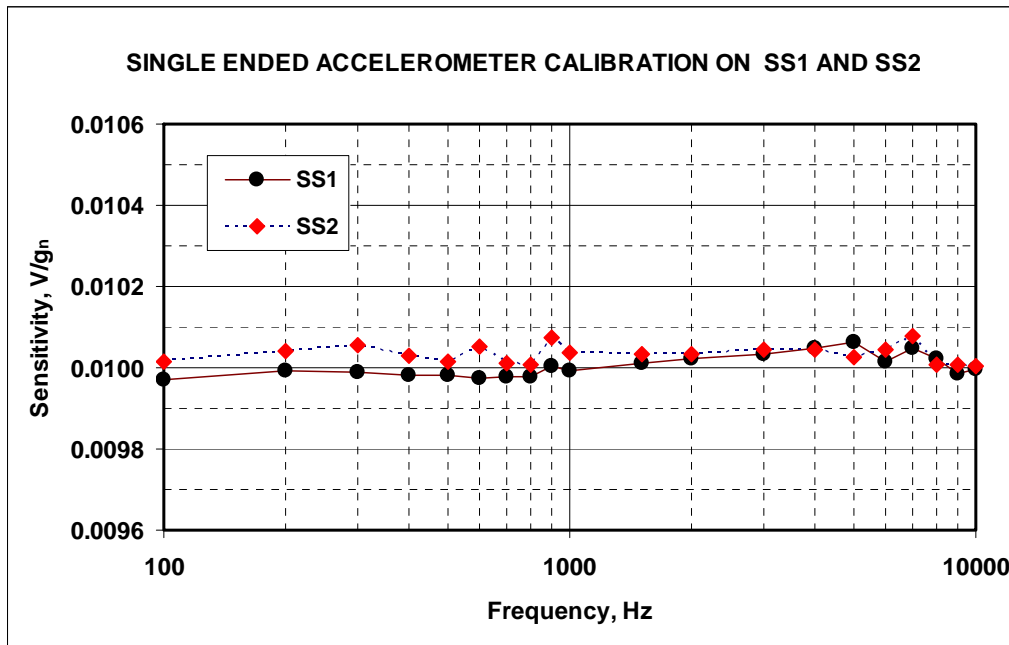


Figure 16. Calibration results of a single-ended accelerometer on NIST SS2 and AFMETCAL SS1

Summary

A dual-coil electrodynamic shaker has been developed for improved accelerometer calibration by both reciprocity and interferometric methods. The shaker uses a uniquely designed aluminum moving element with two mounting tables and a damped flexure support system for the moving element. The shaker has very low harmonic distortion and low cross motion over most of the operating range. Test results show that the shaker has a useful range of 30 Hz to 10 kHz for primary calibrations.

The shaker can utilize all four primary methods for accelerometer calibrations: reciprocity, fringe-counting, minimum-point, and sine-approximation. Reciprocity calibration is limited to frequencies of 1 kHz or less, because of inductive interaction between the two coils, unless special procedures are used to cancel these effects. Fringe-counting is used from 30 Hz to 1 kHz. The minimum-point method is used from about 100 Hz to 5 kHz. The upper limit is set by the upper acceleration limit of the shaker, which is about 200 m/s² at the higher frequencies. Sine-approximation is used from 100 Hz to 10 kHz.

Calibrations on NIST's SS2 have estimated uncertainties of 0.5 % to 1.0 % over the frequency range 30 Hz to 10 kHz. SS1 (AFMETCAL) can obtain calibrations with estimated uncertainties of 0.5% to 2.4% over the frequency range of 30 Hz to 10 kHz. SS2 at NIST uses softer flexures for the moving element, which may

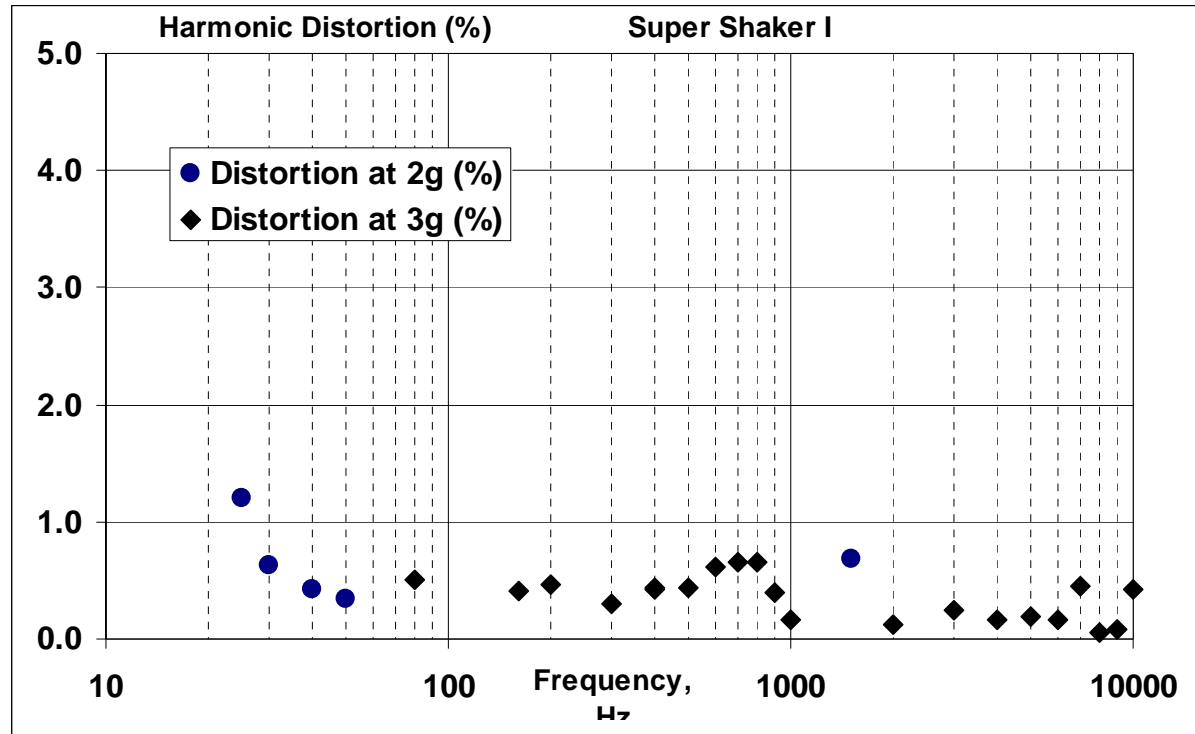
provide smaller relative motion between the two mounting tables. However the specific cause of the difference in uncertainties is not presently known.

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10. BIPM/CIPM key comparison CCAUV.V-K1 (Vibration), 2001

Appendix: Super Shaker Characterization

Frequency (Hz)	Distortion at 2g (%)	Distortion at 3g (%)
25	1.2	
30	0.63	
40	0.42	
50	0.34	
80		0.51
400		0.44
160		0.41
200		0.46
300		0.3
400		0.43
500		0.44
600		0.61
700		0.66
800		0.65
900		0.4
1000		0.17
1500	0.68	
2000		0.12
3000		0.25
4000		0.17
5000		0.19
6000		0.16
7000		0.45
8000		0.06
9000		0.08
10000		0.42

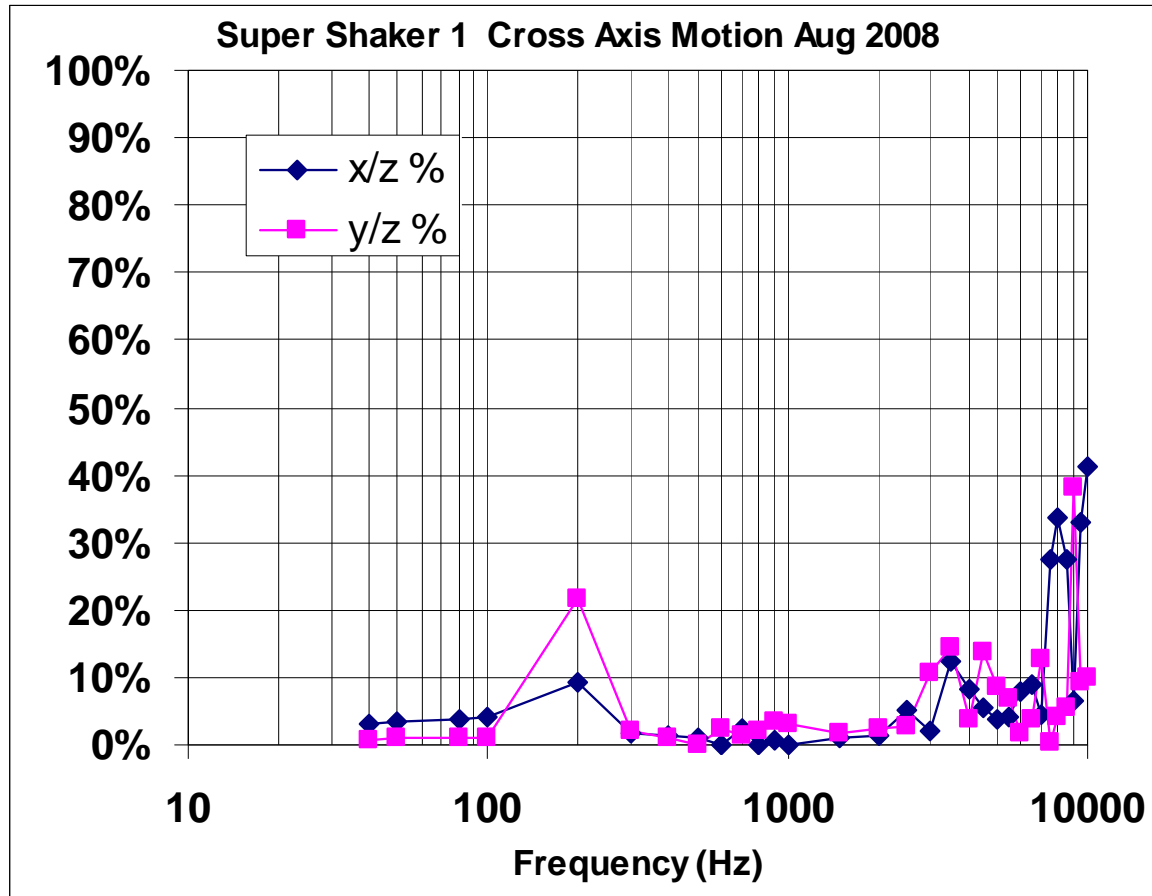


Super Shaker I

Cross Axis Motion

August 2008

Frequency (Hz)	X axis(mV)	z axis(mV)	y axis(mV)	x/z %	y/z %	RSS Total	% Uncert
						Cross Axis	Cross Axis
40	23.90	758.50	5.50	3.2%	0.73%	3.2%	0.06
50	23.00	684.10	6.10	3.4%	0.89%	3.5%	0.07
80	22.40	616.20	5.90	3.6%	0.96%	3.8%	0.08
100	46.00	1136.00	12.60	4.0%	1.11%	4.2%	0.08
200	99.10	1071.00	231.70	9.3%	21.63%	23.5%	0.47
300	17.10	1035.00	19.70	1.7%	1.90%	2.5%	0.05
400	14.00	1041.00	11.00	1.3%	1.06%	1.7%	0.03
500	6.00	570.00		1.1%	0.00%	1.1%	0.02
600	0.60	705.00	16.20	0.1%	2.30%	2.3%	0.05
700	16.60	706.00	9.10	2.4%	1.29%	2.7%	0.05
800	1.20	702.00	14.00	0.2%	1.99%	2.0%	0.04
900	5.50	970.40	32.70	0.6%	3.37%	3.4%	0.07
1000	0.18	709.00	23.00	0.0%	3.24%	3.2%	0.06
1500	10.20	966.00	17.60	1.1%	1.82%	2.1%	0.04
2000	10.70	699.50	17.80	1.5%	2.54%	3.0%	0.06
2500	53.00	1061.00	29.60	5.0%	2.79%	5.7%	0.11
3000	14.70	672.80	71.40	2.2%	10.61%	10.8%	0.22
3500	125.30	1003.00	144.90	12.5%	14.45%	19.1%	0.38
4000	54.30	650.90	25.30	8.3%	3.89%	9.2%	0.18
4500	53.70	967.40	134.60	5.6%	13.91%	15.0%	0.30
5000	23.70	643.50	54.70	3.7%	8.50%	9.3%	0.19
5500	39.90	964.60	66.80	4.1%	6.93%	8.1%	0.16
6000	51.10	641.70	10.70	8.0%	1.67%	8.1%	0.16
6500	82.20	931.80	35.60	8.8%	3.82%	9.6%	0.19
7000	27.70	606.10	77.60	4.6%	12.80%	13.6%	0.27
7500	266.10	966.00	2.80	27.5%	0.29%	27.5%	0.55
8000	267.30	793.90	31.70	33.7%	3.99%	33.9%	0.68
8500	224.00	814.90	44.70	27.5%	5.49%	28.0%	0.56
9000	46.10	700.00	266.70	6.6%	38.10%	38.7%	0.77
9500	238.40	725.40	67.90	32.9%	9.36%	34.2%	0.68
10000	252.00	610.80	60.00	41.3%	9.82%	42.4%	0.64



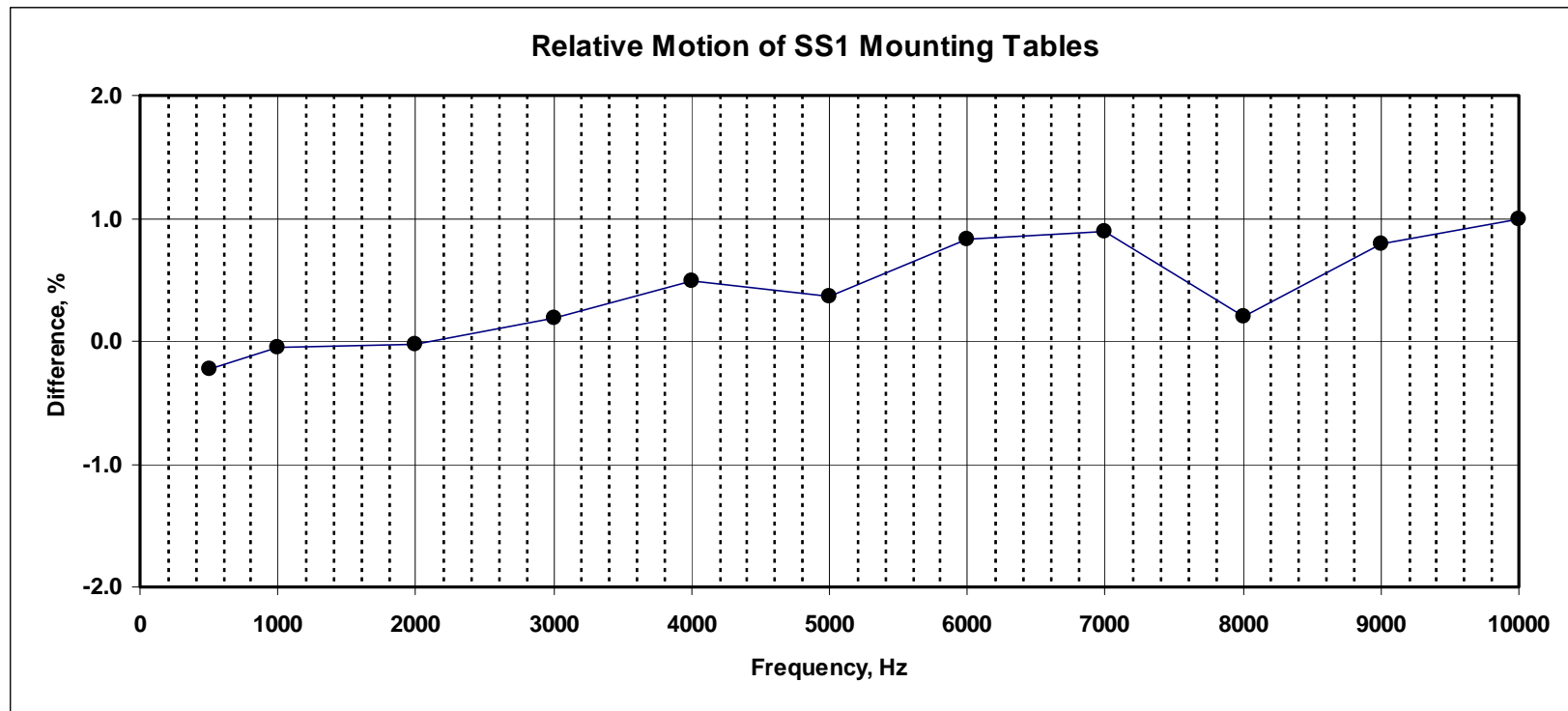
Super Shaker I

Relative Motion

September 2009

Freq (Hz)	VIB Pos* 1 (nm)	QLI Pos 1 (nm)	% diff.	VIB Pos 2 (nm)	QLI Pos 2 (nm)	% diff.	VIB Pos 3 (nm)	QLI Pos 3 (nm)	% diff.	AVG
500	5890.0	5875.0	-0.3	5912.0	5892.0	-0.3	6939.0	6933.0	-0.1	-0.23
1000	1254.0	1255.0	0.1	1472.0	1476.0	0.3	1758.0	1749.0	-0.5	-0.05
2000	341.6	341.1	-0.1	364.0	363.8	-0.1	442.9	443.5	0.1	-0.02
3000	175.3	175.0	-0.2	162.0	162.2	0.1	193.2	194.4	0.6	0.19
4000	102.5	102.6	0.1	88.3	89.4	0.7	106.3	107.0	0.7	0.485
5000	63.6	64.0	0.6	66.3	66.7	0.5	66.4	66.4	0.0	0.36
6000	46.4	47.0	1.1	45.2	45.7	1.0	46.4	46.5	0.3	0.83
7000	32.9	33.2	0.8	32.5	32.9	1.1	32.7	32.9	0.73	0.90
8000	26.3	26.4	0.3	26.0	26.1	0.6	26.4	26.3	-0.3	0.21
9000	20.1	20.4	1.5	20.2	20.3	0.7	20.1	20.2	0.2	0.79
10000	16.1	16.5	2.3	16.4	16.3	-0.1	16.2	16.4	0.7	0.99

*VIB Pos = location (on mirror mounted on first mounting table) off of which the vibrometer laser was reflecting; similarly QLI Pos = location (on mirror mounted on second mounting table) off of which the laser from the quadrature interferometer was reflecting. Each system measured three points about the center sequentially. These were averaged to yield an estimate of the motion of the center of each mirror.



Super Shaker I

Repeatability Tests

May 2009

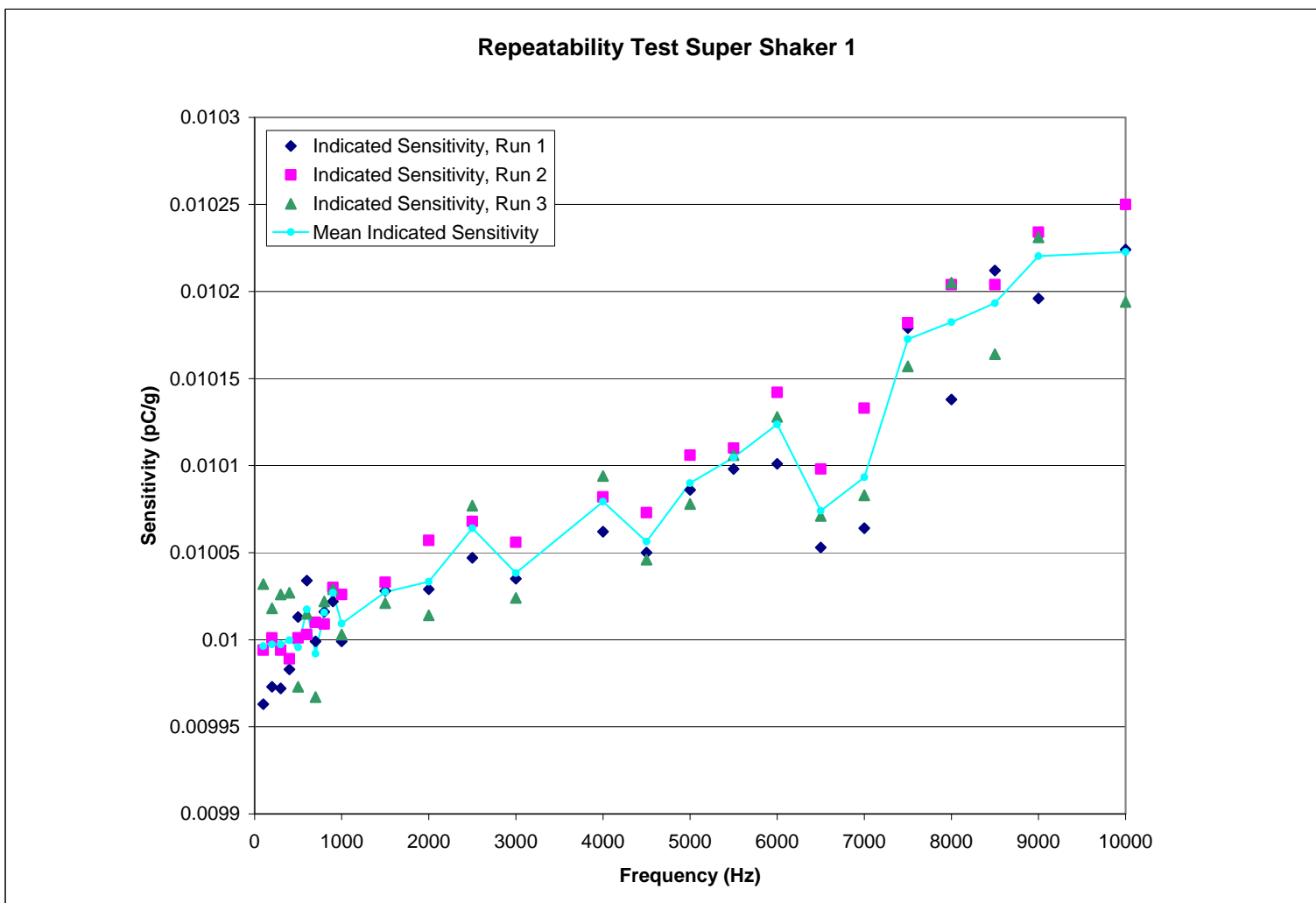
Repeatability Test SS1

Both coils in use; acceleration amplitude: 2-3g

AF accelerometer May 28 2009

Freq	S(run1)	S(run2)	S(run3)	Mean	Run1_Run2 %	Run1_Run3 %	Run2_Run3 %	Prob. Error	Prob Error(%)
100	0.009963	0.009994	0.010032	0.01000	-0.3	-0.7	-0.4	1.35E-05	0.13
200	0.009973	0.010001	0.010018	0.01000	-0.3	-0.5	-0.2	8.85E-06	0.09
300	0.009972	0.009994	0.010026	0.01000	-0.2	-0.5	-0.3	1.06E-05	0.11
400	0.009983	0.009989	0.010027	0.01000	-0.1	-0.4	-0.4	9.29E-06	0.09
500	0.010013	0.010001	0.009973	0.01000	0.1	0.4	0.3	7.99E-06	0.08
600	0.010034	0.010003	0.010015	0.01002	0.3	0.2	-0.1	6.09E-06	0.06
700	0.009999	0.01001	0.009967	0.00999	-0.1	0.3	0.4	8.70E-06	0.09
800	0.010016	0.010009	0.010022	0.01002	0.1	-0.1	-0.1	2.53E-06	0.03
900	0.010022	0.01003	0.010029	0.01003	-0.1	-0.1	0.0	1.70E-06	0.02
1000	0.009999	0.010026	0.010003	0.01001	-0.3	0.0	0.2	5.67E-06	0.06
1500	0.010028	0.010033	0.010021	0.01003	0.0	0.1	0.1	2.35E-06	0.02
2000	0.010029	0.010057	0.010014	0.01003	-0.3	0.1	0.4	8.50E-06	0.08
2500	0.010047	0.010068	0.010077	0.01006	-0.2	-0.3	-0.1	6.00E-06	0.06
3000	0.010035	0.010056	0.010024	0.01004	-0.2	0.1	0.3	6.33E-06	0.06
4000	0.010062	0.010082	0.010094	0.01008	-0.2	-0.3	-0.1	6.30E-06	0.06
4500	0.01005	0.010073	0.010046	0.01006	-0.2	0.0	0.3	5.67E-06	0.06
5000	0.010086	0.010106	0.010078	0.01009	-0.2	0.1	0.3	5.62E-06	0.06
5500	0.010098	0.01011	0.010106	0.01010	-0.1	-0.1	0.0	2.38E-06	0.02
6000	0.010101	0.010142	0.010128	0.01012	-0.4	-0.3	0.1	8.12E-06	0.08
6500	0.010053	0.010098	0.010071	0.01007	-0.4	-0.2	0.3	8.82E-06	0.09
7000	0.010064	0.010133	0.010083	0.01009	-0.7	-0.2	0.5	1.39E-05	0.14
7500	0.010179	0.010182	0.010157	0.01017	0.0	0.2	0.2	5.32E-06	0.05
8000	0.010138	0.010204	0.010205	0.01018	-0.6	-0.7	0.0	1.50E-05	0.15
8500	0.010212	0.010204	0.010164	0.01019	0.1	0.5	0.4	1.00E-05	0.10
9000	0.010196	0.010234	0.010231	0.01022	-0.4	-0.3	0.0	8.23E-06	0.08
10000	0.010224	0.01025	0.010194	0.01022	-0.3	0.3	0.5	1.09E-05	0.11

Probable Error of the mean calculated according to CRC "Standard Mathematical Tables"



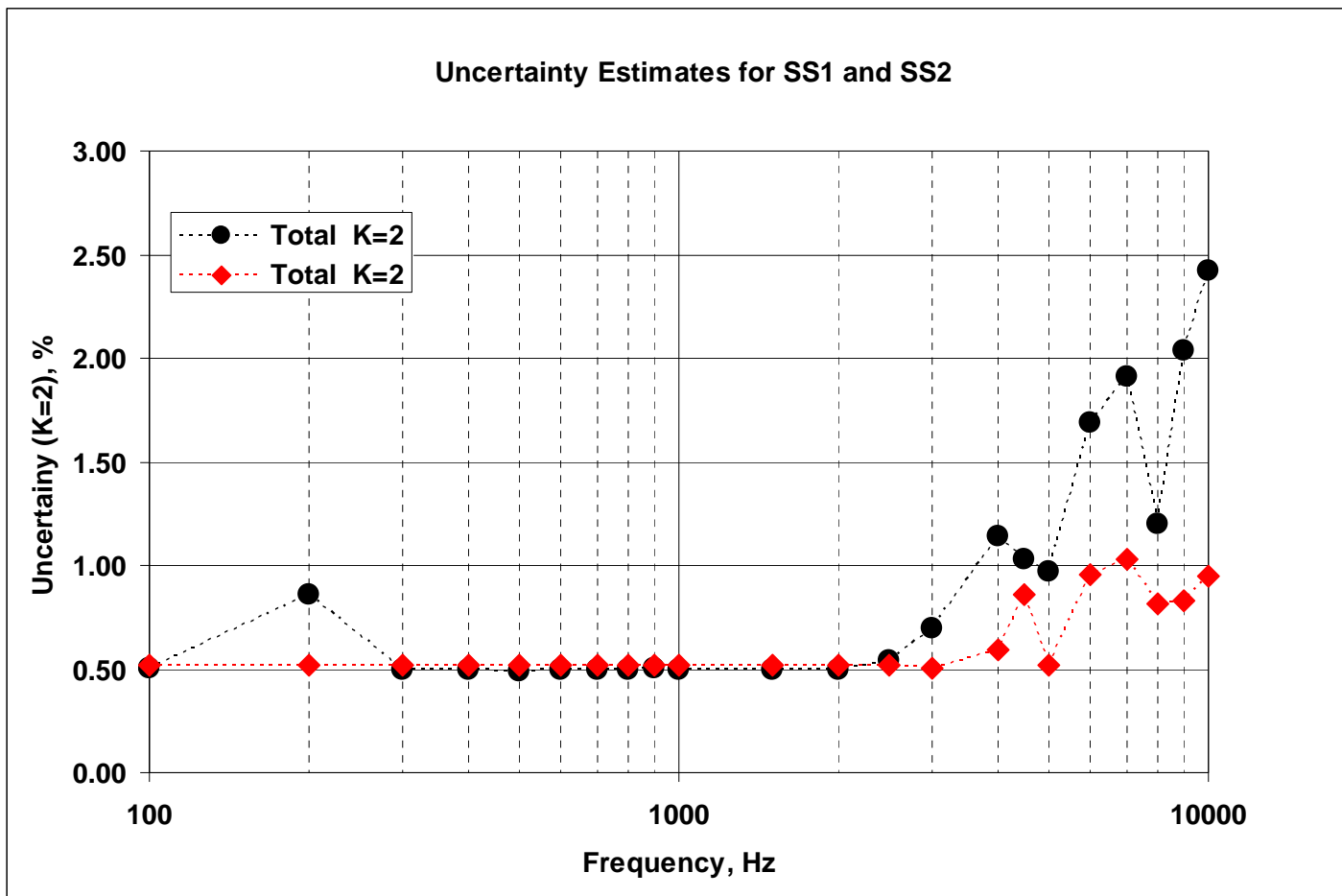
Super Shakers I and II

Uncertainty Estimates

August 2010

Uncertainty Estimates for Super Shakers I and II

Freq. (Hz)	Voltage	SS1	SS2	SS1	SS2	SS1	SS2	SS1	SS2	SS1	SS2	SS1	SS2	SS1	SS2	Freq. (Hz)	SS1 Root-sum-square Total	SS2 Root-sum-square Total	SS1 Total K=2	SS2 Total K=2
		Cross Axis Motion	Cross Axis Motion	Frequency stability	Frequency stability	Amplifier calibration	Amplifier calibration	Amplifier stability	Amplifier stability	Distortion	Distortion	Repeat-ability	Repeat-ability	Relative Motion	Relative Motion					
100	0.04	0.06	0.1	0.01	0.01	0.01	0.01	0.01	0.01	0.05	0.05	0.07	0.07	0.07	0.05	100	0.25	0.26	0.51	0.52
200	0.04	0.35	0.1	0.01	0.01	0.01	0.01	0.01	0.01	0.05	0.05	0.07	0.07	0.07	0.05	200	0.43	0.26	0.86	0.52
300	0.04	0.04	0.1	0.01	0.01	0.01	0.01	0.01	0.01	0.05	0.05	0.07	0.07	0.07	0.05	300	0.25	0.26	0.50	0.52
400	0.04	0.03	0.1	0.01	0.01	0.01	0.01	0.01	0.01	0.05	0.05	0.07	0.07	0.07	0.05	400	0.25	0.26	0.49	0.52
500	0.04	0.02	0.1	0.01	0.01	0.01	0.01	0.01	0.01	0.05	0.05	0.07	0.07	0.07	0.05	500	0.25	0.26	0.49	0.52
600	0.04	0.03	0.1	0.01	0.01	0.01	0.01	0.01	0.01	0.05	0.05	0.07	0.07	0.07	0.05	600	0.25	0.26	0.50	0.52
700	0.04	0.04	0.1	0.01	0.01	0.01	0.01	0.01	0.01	0.05	0.05	0.07	0.07	0.07	0.05	700	0.25	0.26	0.50	0.52
800	0.04	0.03	0.1	0.01	0.01	0.01	0.01	0.01	0.01	0.05	0.05	0.07	0.07	0.07	0.05	800	0.25	0.26	0.49	0.52
900	0.04	0.05	0.1	0.01	0.01	0.01	0.01	0.01	0.01	0.05	0.05	0.07	0.07	0.07	0.05	900	0.25	0.26	0.50	0.52
1000	0.04	0.05	0.1	0.01	0.01	0.01	0.01	0.01	0.01	0.05	0.05	0.07	0.07	0.07	0.05	1000	0.25	0.26	0.50	0.52
1500	0.04	0.032	0.1	0.01	0.01	0.01	0.01	0.01	0.01	0.05	0.05	0.07	0.07	0.07	0.05	1500	0.25	0.26	0.49	0.52
2000	0.04	0.045	0.1	0.01	0.01	0.01	0.01	0.01	0.01	0.05	0.05	0.07	0.07	0.07	0.05	2000	0.25	0.26	0.50	0.52
2500	0.04	0.086	0.1	0.01	0.01	0.01	0.01	0.01	0.01	0.05	0.05	0.07	0.07	0.1	0.05	2500	0.27	0.26	0.54	0.52
3000	0.04	0.163	0.07	0.01	0.01	0.01	0.01	0.01	0.01	0.05	0.05	0.07	0.07	0.2	0.05	3000	0.35	0.25	0.70	0.50
4000	0.04	0.138	0.17	0.01	0.01	0.01	0.01	0.01	0.01	0.05	0.05	0.07	0.07	0.5	0.06	4000	0.57	0.30	1.14	0.59
4500	0.04	0.225	0.2	0.01	0.01	0.01	0.01	0.01	0.01	0.05	0.05	0.07	0.07	0.4	0.30	4500	0.52	0.43	1.03	0.86
5000	0.04	0.139	0.11	0.01	0.01	0.01	0.01	0.01	0.01	0.05	0.05	0.07	0.07	0.40	0.00	5000	0.48	0.26	0.97	0.52
6000	0.04	0.122	0.15	0.01	0.01	0.01	0.01	0.01	0.01	0.05	0.05	0.10	0.10	0.8	0.38	6000	0.85	0.48	1.69	0.95
7000	0.04	0.204	0.21	0.01	0.01	0.01	0.01	0.01	0.01	0.05	0.05	0.10	0.10	0.9	0.40	7000	0.95	0.51	1.91	1.03
8000	0.04	0.509	0.13	0.01	0.01	0.01	0.01	0.01	0.01	0.05	0.05	0.10	0.10	0.2	0.30	8000	0.60	0.41	1.20	0.82
9000	0.04	0.580	0.15	0.01	0.01	0.01	0.01	0.01	0.01	0.05	0.05	0.10	0.10	0.8	0.30	9000	1.02	0.42	2.04	0.83
10000	0.04	0.636	0.3	0.01	0.01	0.01	0.01	0.01	0.01	0.05	0.05	0.10	0.10	1.00	0.27	10000	1.21	0.47	2.42	0.94



Comparison of Calibration Results for Same Accelerometer Tested on Both Super Shakers

Freq. (Hz)	RUN1	RUN2	RUN3	RUN4	RUN5	AVG SS1	SS2
						SEPT 09	SEPT 09
100	0.009976	0.009978	0.009926	0.009965	0.01001	0.00997	0.01001
200	0.009976	0.009987		0.010002	0.010001	0.00999	0.01004
300	0.009988	0.009983		0.009995	0.009983	0.00999	0.01006
400	0.009988	0.009979	0.009982	0.009981	0.00998	0.00998	0.01003
500	0.009973	0.009979	0.009985	0.00998	0.009998	0.00998	0.01002
600		0.009971	0.009981	0.00997	0.009969	0.00997	0.01005
700		0.009979	0.009968	0.009981	0.009981	0.00998	0.01001
800	0.00998	0.009973	0.009981	0.009977	0.009969	0.00998	0.01001
900	0.010008	0.010002	0.010024	0.009995	0.00999	0.01000	0.01007
1000	0.010000	0.009993	0.00999	0.00998	0.009998	0.00999	0.01004
1500		0.010017	0.010009	0.010017	0.010005	0.01001	0.01004
2000	0.010018	0.010022	0.010028	0.010025	0.010019	0.01002	0.01003
3000	0.010037	0.010036	0.010038	0.010023	0.010039	0.01003	0.01004
4000	0.010011	0.010052	0.010041	0.010104	0.01004	0.01005	0.01005
5000	0.010093	0.010069	0.010024	0.01009	0.010032	0.01006	0.01003
6000	0.010032	0.01001	0.010043	0.010028	0.009953	0.01001	0.01004
7000	0.010024	0.010019	0.01002	0.01009	0.010091	0.01005	0.01008
8000	0.010005	0.010046	0.010034	0.010021	0.010014	0.01002	0.01001
9000	0.009994	0.009988	0.009987	0.009998	0.009957	0.00998	0.01001
10000	0.009966	0.010045	0.009987	0.009984	0.010008	0.01000	0.01000

Plot of Comparison of Calibration Results for Same Accelerometer Tested on Both Super Shakers

