Application of the Pointer State Subgraph to Static Program Slicing

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Abstract

A new technique for performing static analysis of programs that contain unconstrained pointers is presented. The technique is based on the pointer state subgraph: a reduced control flow graph that takes advantage of the fact that in any program there exists a smaller program that computes only the values of pointer variables. The pointer state subgraph is useful in building static analysis tools. As an example the application of the pointer state subgraph to program slicing is considered. Finally, some experimental results, obtained using the ANSI-C slicer Unravel, are reported. These results show a clear reduction in the time taken to compute data-flow information from programs that contain pointers. They also shown a substantial reduction in the space needed to store this information.

Key Words

control-flow graph; data-flow analysis; pointer-state subgraph; program slicing; static analysis tools
1 Introduction

Static analysis tools help programmers understand software that must be enhanced or debugged. Unfortunately, unconstrained pointers, as found in languages such as ANSI C [ANS89], make static analysis difficult. Two reasons for this are the imprecision of this information and the use of dynamic storage allocation. Imprecision comes from indirect references (assignments or uses) through pointer variables: if a pointer potentially points to one of many objects, it is unknown which object is actually referenced. Dynamic storage allocation poses two difficulties. First, an unbounded number of objects may be created. Second, since these objects may contain pointers, an unbounded number of pointers may be created.

The pointer state subgraph introduced in this paper assists in performing program analysis of program with pointers. It reduces the space required to represent the pointer state by using a subgraph of the program's control-flow graph. This graph is annotated with a function that describes the behavior of pointer variables.

We show the usefulness of the pointer state subgraph by applying it to the problem of program slicing in the presence of pointers [Wei82, Wei84, LB93]. The slice of a program, with respect to program point p and variable x, consists of all statements and predicates of the program that may affect the value of x at point p. Program slicing has applications to program debugging [LW86, LW87, HDC88, JZR91], program testing [BH93, Bin95], program integration [HPR89, BHR95], parallel program execution [Wei84], software metrics [OT89], reverse engineering [Bec93], and software maintenance [GL91]. Frank Tip provides a survey of program slicing including these uses [Tip95a, Tip95b].

Section 2 formalizes the pointer state subgraph. Section 3 demonstrates its usefulness in building static analysis tools by applying it to the problem of program slicing in the presence of pointers. Section 4 presents experimental results collected using Unravel, an ANSI-C slicer that uses the pointer state subgraph [LWG+95]. Finally, Section 5 summarizes our work.

2 The Pointer State Subgraph

The pointer state subgraph is motivated by the observation that any program dealing with pointers contains a program that computes the pointer state. That is, it is possible to project out of the original program an embedded pointer state program that contains only those statements necessary to compute the values (i.e., addresses) held by pointer variables. This embedded pointer state program could, for example, be obtained by taking the slice of the program with respect to all definitions of pointer variables in the program.

The pointer state subgraph (PSS) is much smaller than the full control-flow graph since only assignments to pointer variables change the pointer state; thus, every program statement does not have to be analyzed to determine this state. This section describes the PSS in three steps: first, it defines the PSS, then it describes how the PSS is constructed, and, finally, it describes the construction of the pointer state function, which annotates the PSS.
2.1 Definition

The pointer state subgraph is a reduced control-flow graph annotated with a pointer state function:

**Definition (Control-Flow Graph).** A control-flow graph is a directed graph whose nodes represent source program components (e.g., assignment statements, or the predicate of an if or while statement). In addition, there are two special nodes labeled "entry" and "exit" that provide a "frame" for the other nodes. Control-flow graph edges represent the flow of control through the program. For example, the node representing an if statement has two outgoing edges that represent the condition of the if statement being true or false.

**Definition (Pointer State Subgraph).** The pointer-state subgraph (PSS) is a subgraph of the control-flow. It contains those control-flow-graph nodes that modify the pointer state (e.g., \( p = &m \), but not \(*p = 5\), which modifies an int not a pointer). The edges of the PSS are paths of edges from the control-flow graph: an edge connects node \( n \) to node \( m \) if a path in the control-flow graph connects \( n \) to \( m \) and no node on this path is in the PSS.

Each node of the PSS is annotated by a pointer state function, which describes the pointer state for each pointer variable visible at the node in the current scope. This function maps variables to objects: storage locations allocated either statically by variable declarations or dynamically by calls to malloc (malloc is used to represent any function that returns a newly allocated block of storage). NULL is one of the possible objects.

**Definition (Pointer State Function).** For pointer variable \( v \) at node \( n \), the pointer state function \( P(n, v) \) contains the set of objects that \( v \) may point to (i.e., objects that \( v \) may dereference to). \( P(n, v) \) is broken down "level-by-level;" thus \( P_0(n, v) \) is the value obtained starting with \( v \) and dereferencing zero times (i.e., \( v \)); \( P_1(n, v) \) is the value obtained starting with \( v \) and dereferencing one time (i.e., \(*v\) ); and so on. More formally

\[
P_0(n, v) = \{v\}
\]

\[
P_1(n, v) = \{\text{object } o \mid v \text{ holds the address of } o\}
\]

\[
P_k(n, v) = \{x \mid x \in P_{k-1}(n, y) \text{ and } y \in P_k(n, v)\}.
\]

**Example.** In the program shown in Figure 1 the pointer state changes three times (the pointer state immediately after each statement is shown to the right of the statement). All three changes are for variable \( \text{min} \), which is initially undefined, and eventually contain all of the formal parameters. The PSS for this example includes the nodes for the statements on Lines 7-11.

In the absence of dynamically allocated objects, a pointer variable can take on a finite (and usually small) number of values. Thus, it is possible to precisely identify non-heap objects. However, approximation techniques are necessary for tracking dynamically allocated objects. The reason for this is illustrated by the following example.

3
/* call: square_min (&a,&b,&c) */
return square of the minimum of a, b, and c */
int square_min (int *x, int *y, int *z)
{
    int *min, square, w;
    /* Pointer State for: x y z min */
    min = z;
    /* a b c - */
    if (*y < *min) /* a b c a */
        min = y;
        /* a b c a */
    if (*z < *min) /* a b c a */
        min = z;
        /* a b c a */
    w = *min;
        /* a b c a[b|c */
    square = w * w;
        /* a b c a[b|c */
    return square;
        /* a b c a[b|c */
}

Figure 1: Pointer State Function Example

typedef struct List_struct
{
    int value;
    List_struct *next;
} List;

List *node;
...
node = (List *) malloc (sizeof(List));

Each time Line 7 is executed, node receives the address of a new block of memory from the heap. It is not possible to statically determine how many blocks are allocated or to track individual blocks. This implies that an approximation that summarizes dynamically allocated storage blocks must be introduced. For example, the heap could be viewed as an array where assignments to individual members are treated as both an assignment and a reference to the entire array.

The approximation used in annotating the PSS divides objects by allocation site (and thus by type): all objects allocated by the same statement are summarized as one pseudo-variable. For pseudo-variables that represent structures, additional pseudo-variables are created for each field of the structure. Pseudo-variables
are given special treatment when assigned. A definition of a pseudo-variable is also treated as a reference to the pseudo-variable, because these variables represent more than one block of storage. (In the following discussion, the address of a variable may refer to the address of a pseudo-variable and, thus, to a block of memory returned by malloc.) Using this approximation, there are a finite number of possible values for a pointer variable, because there are a finite number of allocation sites.

2.2 Constructing the PSS

Conceptually, for program $P$, the PSS is constructed from the embedded pointer state program of $P$. This program contains all statements of $P$ that modify the value (i.e., the address) contained in a pointer. It does not contain the statements that compute the values contained in these addresses. The actual construction begins with $P$'s control-flow graph and casts out nodes that do not change the pointer state. This is done by applying the following three rules until none can be applied.

1. If node $n$ has a single successor $k$, a single predecessor $j$, and does not change the pointer state then eliminate $n$ and connect $j$ to $k$.
2. If node $n$ has multiple successors, node $j$ is where all the paths from $n$ rejoin ($j$ dominates $n$), and all the nodes between $n$ and $j$ have been removed then remove $n$ and $j$ and connect $n$'s predecessor to $j$'s successor.
3. The framing nodes “entry” and “exit” are never removed.

Example. The control-flow graph and PSS for the program in Figure 2 are shown in Figure 3. Nodes 2, 4, 11 and 12 in the control-flow graph do not change the pointer state and are eliminated by Rule 1. Since node 4 is eliminated, Rule 2 eliminates the branch and join nodes (Nodes 3 and 5), and connects Node 1 to Node 6. Note that the same PSS is obtained by slicing at Line 13 with respect to min.

2.3 Annotating the Pointer State Subgraph

After the PSS is constructed, each node is annotated with the pointer state function $P_k(n,v)$. (Note that in the implementation $P_k$ for $k > 1$ is not recorded but rather is derived when needed from $P_1$.) $P_1$ is constructed by first identifying statements where object addresses are introduced and then tracking these addresses as they are propagated along the edges of the PSS. Addresses are introduced into the pointer state from two sources: taking the address of a variable (i.e., by applying the C & operator) and obtaining storage from the heap. Object addresses are propagated along the edges of the PSS using the rules in the following table. In each rule, the pointer state output of a node is the pointer state input to the node with the entry for $P_1(n,a)$ (or $P_1(n,y)$ in the case of the last two rules) replaced as shown. The rules are iterated until a fixed point is reached. (The notation $*^k b$ denoted $b$ dereferenced $k$ times.)
Figure 2: An example program

```c
/* call: square_min_var (&a, &b, &c)
   return the square of the minimum of a, b, and c */
int square_min_var (int *x, int *y, int *z)
{
    int *min, square, w;

    w = *z;
    if (*y < w)
        w = *y;
    min = &w;
    if (*z < *min)
        min = z;
    w = *min;
    square = w * w;
    return square;
}
```

Figure 3

<table>
<thead>
<tr>
<th>Node Number</th>
<th>Line Number</th>
</tr>
</thead>
</table>
| 1           | 1           | /* call: square_min_var (&a, &b, &c) */
| 2           | 2           | return the square of the minimum of a, b, and c */
| 3           | 3           | int square_min_var (int *x, int *y, int *z) |
| 4           | 4           | {                                             |
| 5           | 5           | int *min, square, w;                         |
| 6           | 6           |                                                 |
| 2           | 7           | w = *z;                                      |
| 3           | 8           | if (*y < w)                                   |
| 4           | 9           | w = *y;                                      |
| 5           | 10          | min = &w;                                     |
| 6           | 11          | if (*z < *min)                                |
| 7           | 12          | min = z;                                      |
| 8           | 13          | w = *min;                                     |
| 9           | 14          | square = w * w;                               |
| 10          | 15          | return square;                                |
| 11          | 16          | }                                             |

Figure 2: An example program
entry

w = *x

if (*y < w)
    w = *y;

min = &w;

if (*z < *min)
    min = z;

w = *min;

sq = w*w

return sq;

exit

Flowgraph

Figure 3: Control-flow graph and PSS for the program shown in Figure 2.
<table>
<thead>
<tr>
<th>Statement</th>
<th>Propagation Rule</th>
</tr>
</thead>
<tbody>
<tr>
<td>$a = &amp; x$</td>
<td>$P_1(n, a) = {x}$</td>
</tr>
<tr>
<td>$a = b$</td>
<td>$P_1(n, a) = P_1(n, b)$</td>
</tr>
<tr>
<td>$a = \ast b$</td>
<td>$P_1(n, a) = \bigcup P_1(n, x), \forall x \in P_1(n, b)$</td>
</tr>
<tr>
<td>$a = \ast \ast b$</td>
<td>$P_1(n, a) = \bigcup P_1(n, x), \forall x \in P_2(n, b)$</td>
</tr>
<tr>
<td>$\ast a = &amp; x$</td>
<td>$P_1(n, y) = P_1(n, y) \cup {x}, \forall y \in P_1(n, a)$</td>
</tr>
<tr>
<td>$\ast \ast a = &amp; x$</td>
<td>$P_1(n, y) = P_1(n, y) \cup {x}, \forall y \in P_k(n, a)$</td>
</tr>
</tbody>
</table>

**Example.** In Figure 3, $P_1(6, \text{min})$ is assigned the value $\{w\}$ by the first rule. Further on, the pointer state for min at Node 9, $P_1(9, \text{min})$, is the union of the pointer states on the incoming flow edges from Nodes 7 and 8. Thus, $P_1(9, \text{min}) = P_1(7, \text{min}) \cup P_1(8, \text{min}) = \{w\} \cup \{c\} = \{w, c\}$.

## 3 Applying the PSS to Program Slicing

This section discusses application of the PSS to static program slicing in the presence of pointer variables. Before doing so, some definitions are introduced and a brief discussion of program slicing in the absence of pointer variables is given.

**Defs**($n$). The set of variables defined (assigned to) at statement $n$.

**Idefs**($n$). The set of indirect definitions at statement $n$. Each element is a pair containing a variable and a level of indirection. Level 0 indicates a direct assignment to the variable, Level 1 indicates that the variable contains the address of the object assigned, and so on. (Note that def($n$) = $\{v | (v, 0) \in idefs(n)\}$).

**Irefs**($n$). The set of indirect references at statement $n$. Each element is a pair containing a variable and the level of indirection. Level 0 indicates a direct reference to the variable, Level 1 indicates that the variable contains the address of the object referenced, and so on. (Note that refs($n$), defined below, is $\{v | (v, 0) \in irefs(n)\}$).

**Program Slice.** $P'$ is a slice of program $P$ taken with respect to variable $v$ at statement $n$ (written $S_{<n,v>}$), iff

1. $P'$ is derived from $P$ by deleting zero or more tokens from $P$, and
2. when $P$ and $P'$ are executed on the same input for which $P$ terminates, the same values are produced for $v$ immediately before $n$ by $P$ and $P'$. 

---

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The slice taken with respect to a set of variables is defined as the union of the slices taken with respect to each variable in the set.

Refs(n). The set of variables referenced at statement n.

Slicing Criterion. A tuple \(<n, v>\) where n is a program statement and v is a variable or a set of variables.

Succ(n). The set of successor statements for statement n. This include all statements whose execution can immediately follow n.

### 3.1 Program Slicing in the Absence of Pointer Variables

Program slicing is a program decomposition technique based on extracting statements relevant to some sub-computation in a program. The relevant sub-computation is identified by a slicing criterion, which specifies a set of program variables and a location in the program. A slice can be computed beginning from the slicing criterion by including each predecessor that assigns a value to any variable within the slicing criterion, and generating new slicing criteria for the predecessor by deleting any assigned variables from the original slicing criterion and adding any referenced variables.

More formally, statement n is included in a slice if the slicing criteria for a successor of n includes a variable in \(\text{defs}(n)\) \((i.e., S_{\text{succ}(n), v})\) include n if \(v \in \text{defs}(n))\). If n is included then the slice also includes the slices taken with respect to the each variable in \(\text{refs}(n)\) \((i.e., S_{\text{refs}(n)}, v)\) and the control statements that directly control n's execution \((i.e., S_{\text{refs}(n)}, c)\) for each control statement c whose execution determines whether or not n is executed.

### 3.2 Program Slicing in the Presence of Pointer Variables

This section considers simple pointers to non-structures and then pointers to structures. In each case, we first describe the slices necessary to capture the execution behavior of a pointer reference that is included in the slice and then the conditions under which a statement with an indirect assignment is included in the slice.

**Indirect Reference by Pointers**

If a statement with an indirect reference is included in a slice, each variable that may be referenced, including the pointer variable, is relevant to the computation and further slices for each must be generated. For the simple case of a single level of indirection:

\[ n: \ldots * b \ldots \]

the necessary slices are

\[ S_{<n, P_0(n,i)>} \cup (S_{<n, P_1(n,z)>} \text{ where } (z, 1) \in \text{refs}(n)). \]
For example, if the pointer state for \( b \) is \( P_1(n, b) = \{ E, F \} \), then the new slices for everything that \(*b\)'s value may depend on are \( S_{<n,E>} \), \( S_{<n,F>} \), and \( S_{<n,b>} \) (recall that \( P_0(n, b) = \{ b \} \)).

Now consider a general reference having \( k \) levels of indirection:

\[
\begin{align*}
  n: \ & \cdots \ast^k b \cdots \\
\end{align*}
\]

If statement \( n \) is included in the slice then the following slices should also be included:

\[
S_{<n,P_k(n,x)>} \text{ where } (x, k) \in \text{irefs}(n) \text{ and } 0 \leq i \leq k.
\]

**Indirect Assignment by Pointers**

To determine if an expression statement with an indirect assignment should be included in a slice, every possible location that the assignment may modify must be known. This is complicated by the use of multiple levels of indirection.

First, consider the special case of a statement \( n \) with an assignment through one level of indirection:

\[
\begin{align*}
  n: \ & \ast a = \cdots \\
\end{align*}
\]

For the slicing on criteria \( <\text{succ}(n), c> \), statement \( n \) is included in the slice if \( P_1(n, a) \) includes \( c \). In addition to slices necessary to capture computation on the right hand side of \( n \) (i.e., those described above), slices are generated to capture the statements that give \( a \) (not \(*a\)) its value. For example, if the statement \( a = &c \) had given \( a \) its value then the slice \( S_{<n,a>} \) captures the assignment of \&c to \( a \). If \( a \) may point to a variable other then \( c \) then the slice \( S_{<n,c>} \) is also included to capture the other assignments to \( c \).

Now consider the general case for \( k \) levels of indirection. Here each intermediate level must be captured. Thus, the statement

\[
\begin{align*}
  n: \ & \ast^k a = \cdots \\
\end{align*}
\]

is included in the slice \( S_{<\text{succ}(n), v>}, \) if \( v \) is any of the variables to which \(*^k a\) may point (i.e., \( n \) is included if \( v \in P_k(n, a) \) and \( (a, k) \in \text{idefs}(n) \)).

The additional slices generated must include only relevant intermediate indirect references. This is captured by the *relevant intermediate indirect references* function \( R_{i,k}(n, v, x) \), which returns the set of intermediate pointers that may be used at level \( i \) of indirection for an assignment at statement \( n \) using \( k \) levels of indirection through variable \( x \) to variable \( v \). Function \( R \) effectively prunes away indirect pointers in \( P \) that are not relevant to a particular slicing criterion. In other words, \( P_k(n, v) \) is the set of variables that \( v \) may point to. However, only those members of \( P_k(n, v) \) that may dereference to \( x \) (after \( k - i \) levels of indirection) are relevant.

\[
R_{i,k}(n, v, x) = \{ r \mid r \in P_1(n, a) \text{ and } v \in P_{k-i}(n, r) \}
\]

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\begin{verbatim}
{
    int w, z, y, *e, *f, *g, *h, *i, *j, **b, **c, **d, ***a;
    ...
    a = cond() ? (cond() ? &b : &c) : &d;
    ...
    b = cond() ? &e : &f;
    c = cond() ? &g : &h;
    d = cond() ? &i : &j;
    ...
    e = cond() ? &w : &x;
    f = &x; g = &y; h = &z; i = &w;
    j = cond() ? &w : &z;
    ...
    n: ***a = ...
    ...
}
\end{verbatim}

Figure 4: Pointer Code Fragment

**Example.** Figure 5 shows the pointer state represented as a directed graph for the variable \( a \) to three levels of indirection for the program fragment in Figure 4. In Figure 5, an edge from node \( n \) to node \( m \) means that \( n \) could point to \( m \). Figure 5 also shows the pruned sets of indirect pointers for the criteria <\text{succ}(n), w> and <\text{succ}(n), z>.

If \( S_{\text{succ}(n), v} \) includes statement \( n \) then in addition to the slices used to capture the computation of the right-hand side, the following slices are taken:

\[ S_{<n, R_i, k(n, a, v)>} \text{ where } 0 < i < k \text{ and } (a, k) \in \text{idefs}(n) \]

This is sufficient if there is only one member of \( P_k(n, a) \) because the object referenced by the pointer is unique and is definitely killed by the assignment. However, if there is more than one member of \( P_k(n, a) \), then any analysis must account for the possibility that the object is only potentially modified. Thus, if \( \exists (a, k) \in \text{idefs}(n) \) such that \( |P_k(n, a)| > 1 \) then the slice \( S_{<n, v>} \) must be included.

**References to Structure Members via Pointer**

This section, considers *pointer chain expressions*, references to fields of structures accessed through pointer variables. Pointer chain expressions are composed of a pointer variable \( p \) followed by one or more structure field-names \( f_i \) separated by "→" (the dereference then field select operator). For pointer chains, it is necessary
Figure 5: Pruned Pointer State For \* \* \*a
to identify the variables associated with a field of the pointer chain. This is done by the field function $F$:

$$F(v, f) = \text{the variable that represents field } f \text{ of variable } v \text{ (i.e., } "v.f"\text{)}.$$

First, consider the case of a length one pointer chain expression

$$n: \cdots p \rightarrow f \cdots$$

If $n$ is included in a slice, then slices on $p$ and all the variables $x.f$ where $x$ is in $P_1(n, p)$ must be included (the entries of $P_1(n, p)$ are assumed to be structures). These slices are $S_{<n,v>$ and $S_{<n,F(x,f)>}$, where $x \in P_1(n, p)$.

When a slice includes a statement with a general pointer chain expression, such as

$$n: \cdots (p \rightarrow f_1 \rightarrow \cdots \rightarrow f_k) \cdots$$

then the slice must also included slices with respect to all the variables to which the end of the chain ($f_k$) may point, and all variables to which the intermediate links of the chain ($p, f_1, \cdots, f_{k-1}$) may point. An example will help explain the need for these slices.

```c
typedef struct
{
    int c;
} alpha;

typedef struct
{
    int value;
    alpha *b;
} beta;

beta *a;
beta r,s,t,u;
alpha w,x,y,z;

foo(\cdots)
{
    n: \cdots a \rightarrow b \rightarrow c \cdots
}
```
Assume that at statement \( n \) the pointer state function is as follows:

\[
P_1(n, a) = \{s, t\} \quad F(s, b) = s.b \quad F(y, c) = y.c \\
P_1(n, r.b) = \{w, x, z\} \quad F(r, b) = r.b \quad F(z, c) = z.c \\
P_1(n, s.b) = \{w, y\} \quad F(t, b) = t.b \\
P_1(n, t.b) = \{y, z\} \quad F(u, b) = u.b \\
P_1(n, u.b) = \{w, z, y\} \quad F(w, c) = w.c
\]

If statement \( n \) is included in a slice, then slices on any variable pointed to by \( a \rightarrow b \rightarrow c \) must be included to account for variables that the entire chain may reference. These slices are \( S_{<n,w,c>} \), \( S_{<n,y,c>} \), and \( S_{<n,z,c>} \). Slice \( S_{<n,w,c>} \), for example, is included because \( a \) points to \( s \) (\( s \in P_1(n, a) \)) and \( F(s, b) = s.b \), which points to \( w \) (\( w \in P_1(n, s.b) \)). This example chain has one intermediate link, \( a \rightarrow b \). Slices for this link are \( S_{<n,s,b>} \) and \( S_{<n,t,b>} \).

In general, if statement \( n \) is included in the slice then the following slices are needed to capture the relevant statements for each pointer chain expression

\[
S_{<n,w_i>}, \text{ where } w_0 = \{p\}, \text{ and } \\
w_i = \{F(z, f_i) \mid z \in P_1(n, r) \text{ and } r \in w_{i-1}\}.
\]

Assignment to Structure Members via Pointer

Consider first the case of a single field reference

\[
n: p \rightarrow f = \cdots
\]

Statement \( n \) is included in the slice \( S_{<\text{succ}(n),v>} \) if \( v \) is one of the variables identified by \( p \rightarrow f \). Thus, \( n \) is included if

\[
z \in P_1(n, p) \text{ and } v = F(z, f)
\]

In the general case of a statement with \( k \) field references

\[
n: p \rightarrow f_1 \rightarrow \cdots \rightarrow f_k = \cdots
\]

Statement \( n \) is included in the slice \( S_{<\text{succ}(n),v>} \) if \( v \) is one of the variables identified by \( p \rightarrow f_1 \rightarrow \cdots \rightarrow f_k \). Thus, \( n \) is included if

\[
v \in X_k, \text{ where } X_0 = \{p\}, \text{ and } \\
x_i = \{F(z, f_i) \mid z \in P_1(n, X_{i-1})\}
\]

Parallel to the absence of structures, in addition to slices necessary to capture computation on the right hand side of \( n \) (described above), slices are generated to capture the statements that give \( p, p \rightarrow f_1, \ldots, p \rightarrow f_1 \rightarrow \cdots \rightarrow f_k-1 \) (but not \( p \rightarrow f_1 \rightarrow \cdots \rightarrow f_k \)) their values.
```c
main()
{
    int a, b, s, u, z;
    int *w, *y, **z;
    s = 1;
    a = 2;
    b = 3;
    scanf("%d %d", &x, &u);
    if (x) y = &a;
    else y = &b;
    if (u) z = &y;
    else z = &w;
    w = &s;
    **z = 4;
    printf("a %d b %d s %d\n", a, b, s);
}
```

Figure 6: Missing Execution Example

### 3.3 Other Uses of the PSS in Program Slicing

A further example of the use of the PSS in program slicing is illustrated by Figure 6 where the PSS can reduce the number of statements in a slice. Consider the slice on \( s \) at Line 20 in Figure 6. Weiser's initial definition of a slice required the slice to be executable. Later definitions relax this requirement. They define a slice to contain all the statement that may affect the computation at a particular point in the program [HRB90].

The “relaxed” slice with respect to \(<20, s>\) consists of the following statements: \{1, 2, 6, 9, 14, 15, 17, 18, 21\}. However, by omitting Lines 11 and 12, the slice is not executable (\( *z \) may be undefined and cause a run-time error when attempting to assign to \( *z \) on Line 18). The variable \( z \) could contain either the address of \( w \) or the address of \( y \). If \( z \) contains the address of \( w \) then executing Line 18 sets the value of \( s \) since \( w \) points to \( s \). However, if \( z \) contains the address of \( y \) then executing Line 18 has no effect on the value of \( s \). Lines 11 and 12 are not relevant to the computation of \( s \); anything could be executed so long as \( y \) is given the address of a variable not used in the slice. Since only \( w \) contains the address of \( s \), Line 18 is only needed in the slice when the condition \( z \) points to \( w \).
A program slicer producing executable slices has two possible solutions:

1. Add statements to the slice that are irrelevant to the slicing criterion but are required to keep the slice executable.

2. Add conditions to guard against executing statements that would cause a run-time error when the slice is executed.

Having the PSS available a slicer can determine that Line 18 has no effect on the variable s. A tool using the PSS can alert the user of any indirect assignments that may be to more than one possible object. The user could instruct the tool to assume assignment to a particular object and display the result.

4 Experimental Results

Table 1 illustrates the effectiveness of the PSS in computing pointer state information. The data was collected using Unravel (an ANSI-C program slicer developed at NIST [LWG'95]) on a Sun Sparc Station 2 with 64MB memory. The first group of programs were used by Pande et. al., to study def-use associations for single level pointers (i.e., no pointers to pointers) [PLR94]. They include several UNIX library functions and programs from the TACTIC [Ost90] test suite used to examine data-flow based test coverage for C programs. The second group of programs contains multi-level pointers (i.e., pointers to pointers) and pointer chains. They include the implementation of several abstract data-types (pdg is a program dependence graph implementation [FOW87]) and two more UNIX library functions: qsort and strtod. The last two programs are part of the Unravel implementation itself: the analyzer program provides the X11 interface for Unravel; the project program projects a source program given a set of nodes in a slice.

The data collected is summarized in Table 1. For reference this table includes the number of source lines (non-blank lines after removing comments) and compile time (without optimization) for each program. Note that the compile time should not be directly compared with the other times as it includes the time taken to write the compiled code to disk.

The data in the table clearly demonstrate that the PSS reduces the time and space needed to compute the pointer state. For the single-level pointer programs, the average size reduction is 75%; thus the PSS is, on average, a quarter the size of the control-flow graph (CFG). The size reduction for the multi-level pointer-programs, is smaller 56.4%, but still substantial. The reduction in size has significant impact on the time taken to compute pointer state information. For both the single-level pointer programs and the multi-level pointer program the average reduction is 54%.
<table>
<thead>
<tr>
<th>name</th>
<th>source lines</th>
<th>CFG nodes</th>
<th>PSS nodes</th>
<th>size reduction</th>
<th>Time without PSS</th>
<th>Time with PSS</th>
<th>savings</th>
<th>compile time</th>
</tr>
</thead>
<tbody>
<tr>
<td>strcpy</td>
<td>11</td>
<td>10</td>
<td>3</td>
<td>70%</td>
<td>&lt;1ms</td>
<td>&lt;1ms</td>
<td>-</td>
<td>800ms</td>
</tr>
<tr>
<td>strncat</td>
<td>18</td>
<td>23</td>
<td>3</td>
<td>87%</td>
<td>&lt;1ms</td>
<td>&lt;1ms</td>
<td>-</td>
<td>800ms</td>
</tr>
<tr>
<td>crypt</td>
<td>235</td>
<td>236</td>
<td>17</td>
<td>93%</td>
<td>6ms</td>
<td>&lt;1ms</td>
<td>-</td>
<td>1600ms</td>
</tr>
<tr>
<td>random</td>
<td>180</td>
<td>172</td>
<td>79</td>
<td>54%</td>
<td>5ms</td>
<td>3ms</td>
<td>40%</td>
<td>1300ms</td>
</tr>
<tr>
<td>parser</td>
<td>874</td>
<td>640</td>
<td>41</td>
<td>94%</td>
<td>8ms</td>
<td>2ms</td>
<td>75%</td>
<td>3700ms</td>
</tr>
<tr>
<td>fixoutput</td>
<td>342</td>
<td>340</td>
<td>35</td>
<td>90%</td>
<td>4ms</td>
<td>1ms</td>
<td>75%</td>
<td>1800ms</td>
</tr>
<tr>
<td>weather</td>
<td>118</td>
<td>109</td>
<td>85</td>
<td>22%</td>
<td>3ms</td>
<td>2ms</td>
<td>33%</td>
<td>1000ms</td>
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<tr>
<td>pattern</td>
<td>116</td>
<td>93</td>
<td>27</td>
<td>71%</td>
<td>1ms</td>
<td>&lt;1ms</td>
<td>-</td>
<td>1000ms</td>
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<tr>
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<td>164</td>
<td>9</td>
<td>95%</td>
<td>2ms</td>
<td>&lt;1ms</td>
<td>-</td>
<td>1300ms</td>
</tr>
<tr>
<td>sor</td>
<td>166</td>
<td>168</td>
<td>16</td>
<td>90%</td>
<td>2ms</td>
<td>&lt;1ms</td>
<td>-</td>
<td>1400ms</td>
</tr>
<tr>
<td>ht</td>
<td>189</td>
<td>145</td>
<td>82</td>
<td>43%</td>
<td>5ms</td>
<td>3ms</td>
<td>40%</td>
<td>1400ms</td>
</tr>
<tr>
<td>pdg</td>
<td>1143</td>
<td>704</td>
<td>55</td>
<td>92%</td>
<td>38ms</td>
<td>9ms</td>
<td>76%</td>
<td>5000ms</td>
</tr>
<tr>
<td>set</td>
<td>357</td>
<td>289</td>
<td>106</td>
<td>63%</td>
<td>9ms</td>
<td>4ms</td>
<td>56%</td>
<td>1700ms</td>
</tr>
<tr>
<td>qsort</td>
<td>171</td>
<td>302</td>
<td>197</td>
<td>35%</td>
<td>4ms</td>
<td>4ms</td>
<td>0%</td>
<td>1700ms</td>
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<tr>
<td>strtod</td>
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<td>1871</td>
<td>1241</td>
<td>34%</td>
<td>210ms</td>
<td>47ms</td>
<td>78%</td>
<td>8300ms</td>
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<tr>
<td>analyzer</td>
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<td>694</td>
<td>303</td>
<td>56%</td>
<td>48ms</td>
<td>15ms</td>
<td>69%</td>
<td>22300ms</td>
</tr>
<tr>
<td>project</td>
<td>407</td>
<td>305</td>
<td>85</td>
<td>72%</td>
<td>10ms</td>
<td>4ms</td>
<td>60%</td>
<td>2100ms</td>
</tr>
</tbody>
</table>

Table 1

5 Summary

This paper presented the pointer state subgraph. It is more efficient to annotate this graph with pointer state information than the standard control-flow graph. Pointer state information is useful in building static analysis tools. We demonstrate this by showing how the pointer state subgraph is used by Unravel to compute program slices from programs that contain pointers. Finally, we reported results obtained by running Unravel on a collection of C programs that contains pointers and pointer chains. The data clearly illustrates the effectiveness of the pointer state subgraph in reducing the space need to compute pointer state information and in reducing the time taken to compute this information.

Other uses of the PSS include providing an interactive static analysis tool where interesting subsets of the pointer state can be selected by the user. This could be useful when debugging a program with pointers where the user needs to understand how a given object is computed and manipulated.

Acknowledgments

We wish to thank Bill Landi for providing the single-level pointer code example.
References


