## 10 kV DC Resistive Divider Calibration

## Raymond S. Turgel

U.S. DEPARTMENT OF COMMERCE<br>Technology Administration National Institute of Standards and Technology<br>Electronics and Electrical Engineering Laboratory Electricity Division<br>Gaithersburg, MD 20899

## QC

## 10 kV DC Resistive Divider Calibration

## Raymond S. Turgel

U.S. DEPARTMENT OF COMMERCE<br>Technology Administration National Institute of Standards and Technology<br>Electronics and Electrical Engineering Laboratory Electricity Division<br>Gaithersburg, MD 20899

January 1995

U.S. DEPARTMENT OF COMMERCE Ronald H. Brown, Secretary

TECHNOLOGY ADMINISTRATION
Mary L. Good, Under Secretary for Technology
NATIONAL INSTITUTE OF STANDARDS AND TECHNOLOGY
Arati Prabhakar, Director

## Table of Contents

INTRODUCTION ..... 3
Background ..... 3
Calibration Method ..... 3
Low-Voltage Calibration ..... 4
Calibration of the Digital Voltmeter ..... 5
CALIBRATION PROCEDURE FOR DIVIDER DECADES ..... 5
Equipment Configuration ..... 5
Voltmeter Circuit ..... 6
Data acquisition program ..... 7
Temperature Control ..... 8
Calibration Data ..... 9
DISCUSSION OF RESULTS. ..... 18
Low-Voltage Calibration (Table 1 to Table 7) ..... 18
Comparison with the Park Voltage Divider (Table 8) ..... 18
CONCLUSIONS ..... 19
ACKNOWLEDGEMENTS ..... 19
Appendix A: Detailed Experimental Calibration Procedures ..... 23

1. Introduction ..... 23
2. Setting Up the Calibration Experiment ..... 23
3. Resistor Network ..... 23
4. Temperature Control ..... 28
5. Operation of the Temperature Control Program. ..... 28
Appendix B: OIL-BATH TEMPERATURE CONTROL PROGRAM ..... 31
Appendix C: CONTROL PROGRAM FOR THE DIGITAL VOLTMETER ..... 41
Appendix D:
CALIBRATION OF THE DIGITAL VOLTMETER AGAINST A JOSEPHSON ARRAY STANDARD ..... 47
.•


#### Abstract

A calibration method for a 10 kV dc ratio divider was developed. The method uses a highprecision digital voltmeter, at the 10 V level, to establish a $10: 1$ voltage ratio for each decade of the resistive divider and combines these results to obtain an overall voltage ratio of $10000: 1$. The linearity of the voltmeter was checked using a Josephson-array voltage standard. The overall ratio agreed with measurements made at 10 kV using a Park-type divider to within the uncertainty limits.


## INTRODUCTION

## Background

A resistive ratio standard for dc input voltages up to 10 kV was designed and built at the National Bureau of Standards (now the National Institute of Standards and Technology [NIST]) in $1975^{1}$. The divider was constructed using three tapped resistor decades and a Kelvin-Varley circuit for the lowest two decades (Fig 1). The resistors, wound on cards, were surrounded by a guard circuit using similar-valued resistors to provide equipotential shields for each resistor card. The whole assembly was immersed in a temperature-controlled oil bath for insulation and ambient temperature control. At each node, the junction of the divider resistors and the junction of the corresponding guard resistors, respectively, were connected to the inner and outer conductors of a British Post Office-type (BPO) coaxial connector. Desired voltage ratios could be selected by appropriate connections to the nodes in the resistance network and the KelvinVarley divider.

The high-voltage divider was originally built for an absolute volt experiment and has not been in use for several years. Current interest in establishing a medium high-voltage dc divider calibration capability ( 10 kV to 1 kV ) prompted a decision to put the existing 1975 resistive-divider standard back into service. In preparation for the resumption of calibrations of dividers in this voltage range submitted to NIST by customers, the standard itself needed to be recalibrated. The following describes the steps taken and the results obtained in the recalibration.

## Calibration Method

In the original construction of the divider, materials had been selected that had resistors with small voltage and temperature coefficients to ensure stability. By using the same materials for all resistors, the stability of the ratio is further enhanced because external influences, such as temperature or applied voltage, will affect the resistances in proportion to their values and thus

[^0]leave the ratio substantially unchanged. It is possible, therefore, to calibrate the divider at low voltage and make only spot checks at rated voltage. The divider consist of a string of nine resistors with nominal resistance values of $2 \mathrm{M} \Omega$ each for the upper decade, $200 \mathrm{k} \Omega$ for the second decade, and $20 \mathrm{k} \Omega$ for the third decade, respectively (Fig. 1). The tenth 'member' of each decade string is the equivalent resistance of the resistor network of all the lower valued resistors. The lowest (fourth) divider decade is composed of a Kelvin-Varley divider using $2 \mathrm{k} \Omega$ individual resistors and a shunt to make its input resistance a nominal $20 \mathrm{k} \Omega$ (Fig. 2a and 2b). The most significant two digits of the Kelvin-Varley divider are selected using short, shielded (coaxial) jumper cables equipped with BPO connectors at each end. The remaining three digits can be selected by ten-position rotary switches. During the calibration tests described here, all switches were left in the zero position.

At the time the divider was built, a bootstrap calibration procedure using bridge circuits was used to establish the resistance ratios. The bridge measurements use sensitive dc detectors which can be susceptible to stray noise and ac pick-up. At the present time, using the bootstrap method with an available commercial bridge circuit yielded uncertainties for each resistor comparison of at least $1 \times 10^{-6}$ caused by electrical noise and induced parasitic ac signals, particularly when checking the $2 \mathrm{M} \Omega$ resistors. Since the uncertainties would accumulate at each step of the ratio determination, the overall uncertainty would have been unacceptably high.

An alternate method using a high-resolution digital-voltmeter provides a better way to obtain results. The voltmeter automatically averages readings to reduce noise and power-line induced disturbances and is sufficiently linear to establish accurate voltage ratios of ten-to-one. Higher ratios then can be determined by partitioning the divider and combining the measured ratios from each section.

Using the digital-voltmeter method, the determination of the divider ratio is carried out at low voltage. The ten-to-one ratios of the highest four decades of the divider are measured in turn, and by multiplying the intermediate results, a corrected value for the nominal ratio of 10000 to 1 can be computed. As a cross check, the divider can then be compared at the rated operating voltage with a Park-type high-voltage divider. The high-voltage comparison uses the same bridge configuration that is employed for routine calibrations of customer-owned dividers.

## Low-Voltage Calibration

A precision temperature controlled, Zener-stabilized voltage source with a nominal output of 10 V serves as the supply across the ratio resistors. A stabilized source is desirable to obtain consistent readings and lower electrical noise. To maintain sufficient resolution in the voltmeter readings, the measured ratios are kept at 10:1 or less for each determination. To get a ratio of 1000:1, the divider has to be calibrated in stages, and the resistor decades provide a convenient choice for such stages.

With the voltage source connected across each stage of the divider, four sets of dc-voltage readings are taken to determine the actual ratio of each decade. For both negative and positive polarity of the voltage source, readings are then taken across the whole of the decade stage and across the section connected between the chosen divider tap and the common terminal, with the tap usually one tenth of the decade.

For each measurement, the digital voltmeter is programmed to average ten readings spaced over an integral number of cycles of the power-line frequency to reduce any effects of induced 60 Hz voltages. A manually operated rotary switch is used to select the polarity of the dc source and the voltmeter connection either across the whole or the tapped section of the resistor decade. The standard deviation and variation from minimum to maximum of each set of digital voltmeter readings are calculated in real time and displayed so that unusually noisy readings could be detected and remeasured. At the completion of the four sets of digital voltmeter readings, the ratio of the divider section under test is computed from the measurements. The result is expressed in terms of the deviation (in parts in $10^{6}$ ) from the nominal ratio. The overall ratio is calculated by combining the corrected ratios for each stage. ${ }^{2}$

## Calibration of the Digital Voltmeter

Since the ratio determination depended critically on the linearity of the digital voltmeter, a thorough calibration of the voltmeter was undertaken by comparing the voltmeter readings with a series of voltage levels available from a 10 V Josephson-junction voltage standard over a ten-toone range. Applying this calibration to each of the four stages in the determination of the $10000 \mathrm{~V} / 1 \mathrm{~V}$ ratio, the lack of perfect linearity added a total additional uncertainty of only 1.5 parts-per-million (ppm). This is of the same order of magnitude as the uncertainty in the ratio determination and certainly much smaller than the uncertainty of the ratio intercomparison using the Park-resistor divider. Frequent recalibration of the voltmeter, therefore, does not appear to be necessary.

## CALIBRATION PROCEDURE FOR DIVIDER DECADES

## Equipment Configuration

The divider resistors are immersed in a temperature controlled, stirred oil bath. Four Peltier heating and cooling units are built into the oil bath wall. The current to the series-connected

[^1]Peltier units is supplied by a programmable current source controlled from an IBM ${ }^{3}$ compatible personal computer ( PC ). Four thermistors immersed in the oil bath provide the temperature input for the control program.

The moveable relay rack containing the computer, current source, and thermistor control circuit also houses the precision voltage source, digital voltmeter, and voltmeter switch selector. The voltmeter readings are controlled from a separate desktop, laboratory computer.

## Voltmeter Circuit

To determine the ten-to-one ratio of the most significant decade of the divider, the stabilized 10 V supply is connected to the " 10 kV " and the " 0 V " terminals. These two terminals form the top and bottom connection of the divider. Both the stabilized power supply and the digital voltmeter are connected to the resistor network through a switch box (see Fig. 3). A set of leads connects the supply voltage to the polarity reversing switch and a second set links the switch to the divider. A third set of leads connects the switch to the digital voltmeter. The leads to the voltmeter are wound on a coaxial choke to reduce common-mode ac signals as explained below. Two more sets of leads make connections between the divider and the digital voltmeter. One pair, the "A" leads, are connected to the divider in parallel with the supply leads, the other pair, the " B " leads, are connected to the " 1 kV " and " 0 V " terminals. These terminals form the 'output' of the first decade of the divider under test.

The source impedance the voltmeter sees is dependent on the selector switch position. When measuring the drop across the entire decade ("A" position of the switch), the source impedance seen by the digital voltmeter is low because it is essentially that of the voltage supply. However, when the voltmeter is connected to the "output" terminals of the resistor chain of the highest decade (" B " position of the switch), the source impedance is just slightly less than $2 \mathrm{M} \Omega$. The " B " readings, therefore, tend to be noisier than the " A " readings for measurements of the upper decades of the divider. On the lower decades, the difference in source impedance between the "A" and "B" configurations is proportionally less pronounced.

To reduce common-mode ac signals, the shielded, twisted pair of leads to the voltmeter input terminals are wound ( $\sim 22$ turns) through a toroidal high-permeability core to form a "coaxial choke." This choke provides a low-impedance circuit for the signal and return leads, because the magnetic induction is cancelled, but represents a relatively high-impedance path for external, common-mode ac currents.

[^2]The switch that selects the polarity and divider tap connections is a ganged, four-position, multicontact, low-thermal switch. It connects the input of the digital voltmeter across either the whole or part of the string of resistors and also controls the polarity of the applied voltage. For the test, it is rotated sequentially to each of the four settings, $\mathrm{A}+, \mathrm{A}-, \mathrm{B}+, \mathrm{B}-$ in any desired order. At each switch position, a series of voltage readings is recorded under computer control after the letter designation of the selected switch position has been entered through the keyboard.

## Data acquisition program

The voltmeter used for these calibration measurements is a Hewlett-Packard 34558A Multimeter. The meter can be programmed to take a chosen number of readings over a period defined by a given number of power-line cycles. Because of the integrating mode of operation, effects due to power-line ripple will be largely compensated. Built-in mathematical functions calculate the standard deviation and the high and low limits of each set of data. The external computer program displays the measured values and calculates the mean. For successive sets of readings on the same data point, the program stores the mean value and standard deviation of the current set of data as well as the mean of a set of previously recorded data having the lowest standard deviation. The software driving the voltmeter operation is programmed to accept a set of readings automatically if the standard deviation is less than or equal to one part per million. If the standard deviation is greater, the voltmeter will continue taking further sets of data. The operator can override this process (with key K1 or K2 on the Hewlett-Packard Model 85 computer) by accepting the current set of data or that with the lowest standard deviation. A printed record is kept of the "override" and the mean and standard deviation of the set of data that is accepted.

Readings of the voltage drops across the whole decade resistor chain and across the selected portion of the resistors are taken with both positive and negative polarities. Combining the averages of corresponding readings of opposite polarity (e.g., switch positions "A+","A-" and " $\mathrm{B}+$ ", "B-" ) tends to reduce the effects of small voltage offsets in the voltmeter circuit. From the averages of the four sets of voltmeter readings the desired ratio of the decade resistor string is calculated and recorded as a numerical ratio and as a correction (in ppm) to the nominal ratio selected $\left\{\right.$ e.g., $10+\left(\right.$ correction $\left.\left.\times 10^{-6}\right)\right\}$.

A similar procedure is followed for the three lower decades, by connecting the " A " leads to the " 1 kV " and " 0 V " terminals and the " B " leads to the " 100 V " and " 0 V " terminals, and continuing with the pairs of

terminal connections. The overall ratio (or ratio correction) is then computed by combining the results from all the decade ratio determinations. If the divider needs to be calibrated for applied
voltages below 10 kV , the highest decade ratio can be chosen to match the nominal applied voltage.

## Temperature Control

The resistors of the voltage divider are immersed in a cylindrical oil bath equipped with a stirring device at the bottom center. The stirrer is driven by an external motor coupled through a belt to a pulley and shaft protruding from the bottom of the bath. The motor is located at one corner of a square support table so that the heat generated by the motor does not affect the temperature of the oil.

The oil bath has several functions: To insulate the high-voltage parts of the circuit, to prevent flash-overs and corona discharges, and to stabilize the temperature of the resistors forming the divider. Heating and cooling of the oil in the bath is accomplished with four Peltier units spaced evenly around the circumference of the metal enclosure. The Peltier units are powered from a programmable de power supply that is computer controlled. Four thermistors are inserted into the oil through openings in the acrylic top cover of the bath.

The thermistors are connected to a control unit that can be programmed to scan the thermistor resistances and convert them into bus-compatible numerical readouts in degrees Celsius (or Fahrenheit). A computer is programmed to interrogate the thermistor control unit periodically, average the measured temperatures, and compare the average to a reference temperature. If the average measured temperature is less than the reference, then the programmable dc power supply is set to send current through the Peltier units in a direction that will supply heat to the oil in the bath. If the average measured temperature is greater than the reference, the direction of current from the power supply is reversed so that the Peltier units will cool the oil. At each transition between heating and cooling commands, the power supply is turned off for one cycle between thermistor interrogations.

Since the thermistors are immersed in the main oil bath, the heat capacity of the oil will cause considerable thermal inertia. A response to a simple on-off control would result in significant temperature overshoot because of the thermal inertia. To obtain better control, the reference temperature is modulated with a waveform which is close to triangular. This results in a band of proportional control near the desired setpoint temperature. The reference temperature modulation is implemented in the control software with an algorithm based on a theoretical model and subsequent empirical adjustment of the amplitude and period of the quasi-triangular wave.

With the temperature-control algorithm developed, the standard deviation between successive runs was found to be $0.01{ }^{\circ} \mathrm{C}$ or less. Between days, the temperature at the set point could be reproduced to within $\pm 0.05^{\circ} \mathrm{C}$.

The computer program provides a color-coded bar-graph representation of the average and reference temperatures and indicates whether the quantities are increasing or decreasing by a change in color and by arrows pointing in the appropriate direction. The bar graph display alternates with the numerical display of the latest thermistor readings and average temperature, as well as extremes of the temperature fluctuations. Useful voltage ratio measurements can be performed while the average temperature is within $\mathrm{a} \pm 0.1^{\circ} \mathrm{C}$ interval around the setpoint. By changing the color of the text on the screen (from yellow to white), extra emphasis is given that the working temperature range has been attained. ${ }^{4}$

## Calibration Data

The following tables, Tables 1 through 5, list the data obtained in measuring the ten-to-one ratios of the divider decades on various dates. The tables are arranged by date and list the most significant resistor decade first. Tables 6 and 7 summarize the ratio corrections calculated for each decade (Table 6) and the overall 10 000:1 ratio (Table 7).

[^3]Table 1, RESULTS OF THE LOW-VOLTAGE CALIBRATION (December 1, 1993)
10 kV to 1 V Ratio Calibration Using the Digital-Voltmeter Method
Corrections to the Nominal 10:1 Ratio:
1 Dec 93 DVM Connections: $10 \mathrm{kV} / 1 \mathrm{kV} / 0 \mathrm{~V}$

| 11:27 am | Run 1; correction: | $+0.7 \times 10^{-6}$ | Oil Temperature: | $24.484^{\circ} \mathrm{C}$ |
| :--- | :--- | :--- | :--- | :--- |
|  | Run 2; correction: | +3.9 | Oil Temperature: | 24.483 |
|  | Run 3; correction: | +1.1 | Oil Temperature: | 24.496 |
|  | Avg. Ratio Correction: | +1.9 | Avg. Temperature: | $\mathbf{2 4 . 4 9}$ |
|  | Std. Dev.: | $\mathbf{1 . 7 4}$ |  | $\mathbf{0 . 0 0 7}$ |

1 Dec 93 DVM Connections: $1 \mathrm{kV} / 100 \mathrm{~V} / 0 \mathrm{~V}$

| 11:37 am | Run 1; correction: | $-8.0 \times 10^{-6}$ | Oil Temperature: | $24.494{ }^{\circ} \mathrm{C}$ |
| :--- | :--- | :--- | :--- | :--- |
| Run 2; correction: | -7.9 | Oil Temperature: | 24.491 |  |
|  | Run 3; correction: | -8.8 | Oil Temperature: | 24.497 |
|  | Avg. Ratio Correction: | $\mathbf{- 8 . 2}$ | Avg. Temperature: | $\mathbf{2 4 . 4 9}$ |
|  | Std. Dev.: | $\mathbf{0 . 4 9}$ |  | $\mathbf{0 . 0 0 8}$ |

## 1 Dec 93 DVM Connections: 100 V/10 V/0 V

11:45 am Run 1; correction: $\quad-1.5 \times 10^{-6}$ Oil Temperature: $\quad 24.499^{\circ} \mathrm{C}$
Run 2; correction: $\quad-1.7 \quad$ Oil Temperature: 24.495
Run 3; correction: $\quad-1.6 \quad$ Oil Temperature: 24.488
Avg. Ratio Correction: -1.6 Avg. Temperature: 24.49
Std. Dev.: $0.10 \quad 0.010$
1 Dec 93 DVM Connections: $10 \mathrm{~V} / 1 \mathrm{~V} / 0 \mathrm{~V}$
11:56 am Run 1; correction: $\quad+7.9 \times 10^{-6}$ Oil Temperature: $\quad 24.491^{\circ} \mathrm{C}$
Run 2; correction: $\quad+7.6 \quad$ Oil Temperature: $\quad 24.485$
Run 3; correction: $\quad+10.2 \quad$ Oil Temperature: $\quad 24.481$
Avg. Ratio Correction: +8.6 Avg. Temperature: 24.49
Std. Dev.: 1.42 0.011
Overall Ratio $=10000.007 \quad$ Correction: $\quad+0.7 \times 10^{-6}$ standard deviation: $\quad 6.90 \times 10^{-6}$

Overall average temperature: $\quad 24.490 \pm 0.038{ }^{\circ} \mathrm{C}$

Table 2, RESULTS OF THE LOW-VOLTAGE CALIBRATION (December 3, 1993)
10 kV to 1 V Ratio Calibration Using the Digital Voltmeter Method

Corrections to the Nominal 10:1 Ratio:

| 3 Dec 93 DVM Connections: $10 \mathrm{kV} / 1 \mathrm{kV} / 0 \mathrm{~V}$ |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
| 11:43 am | Run 1; correction: | $-3.3 \times 10^{-6}$ | Oil Temperature: | $24.528{ }^{\circ} \mathrm{C}$ |
|  | Run 2; correction: | -1.9 | Oil Temperature: | 24.521 |
|  | Run 3; correction: | -2.5 | Oil Temperature: | 24.517 |
|  | Avg. Ratio Correction: | -2.6 | Avg. Temperature: | 24.52 |
|  | Std. Dev.: | 0.70 |  | 0.008 |
|  | 3 Dec 93 DVM Connections: $1 \mathrm{kV} / 100 \mathrm{~V} / 0 \mathrm{~V}$ |  |  |  |
| 11:37 am | Run 1; correction: | $-8.3 \times 10^{-6}$ | Oil Temperature: | $24.520{ }^{\circ} \mathrm{C}$ |
|  | Run 2; correction: | -8.0 | Oil Temperature: | 24.516 |
|  | Run 3; correction: | -8.1 | Oil Temperature: | 24.522 |
|  | Avg. Ratio Correction: | -8.1 | Avg. Temperature: | 24.52 |
|  | Std. Dev.: | 0.15 |  | 0.006 |
|  | 3 Dec 93 DVM Connections: $100 \mathrm{~V} / 10 \mathrm{~V} / 0 \mathrm{~V}$ |  |  |  |
| 11:31 am | Run 1; correction: | $-2.3 \times 10^{-6}$ | Oil Temperature: | $24.533{ }^{\circ} \mathrm{C}$ |
|  | Run 2; correction: .. | -2.1 | Oil Temperature: | 24.533 |
|  | Run 3; correction: | -2.2 | Oil Temperature: | 24.528 |
|  | Avg. Ratio Correction: | -2.2 | Avg. Temperature: | 24.53 |
|  | Std. Dev.: | 0.10 |  | 0.005 |
|  | 3 Dec 93 DVM Connections: $10 \mathrm{~V} / 1 \mathrm{~V} / 0 \mathrm{~V}$ |  |  |  |
| 110:25 am | Run 1; correction: | $+9.0 \times 10^{-6}$ | Oil Temperature: | $24.535{ }^{\circ} \mathrm{C}$ |
|  | Run 2; correction: | +8.7 | Oil Temperature: | 24.530 |
|  | Run 3; correction: | +8.7 | Oil Temperature: | 24.527 |
|  | Avg. Ratio Correction: | +8.8 | Avg. Temperature: | 24.53 |
|  | Std. Dev.: | 0.17 |  | 0.004 |
|  | Overall Ratio = | 9999.959 | Correction: | -4.1 $\times 10^{-6}$ |
|  | 3 x standard deviation | $23.0 \times 10^{-6}$ |  |  |
|  | Overall average tempera | ature: 2 | $4.526 \pm 0.025{ }^{\circ} \mathrm{C}$ |  |

10 kV to 1 V Ratio Calibration using the DVM Method

# Table 3, RESULTS OF THE LOW-VOLTAGE CALIBRATION (May 1994) 10 kV to 1 kV Ratio Calibration Using the Digital Voltmeter Method 

 Corrections to the Nominal 10:1 Ratio:20-23 May 94 DVM Connections: $10 \mathrm{kV} / 1 \mathrm{kV} / 0 \mathrm{~V}$

Avg. Ratio Correction: $+24.2 \times 10^{-6}$ Avg. Temperature: $\quad 24.566{ }^{\circ} \mathrm{C}$ Std. Dev.: $\quad 1.1$ 0.066

## Table 4, RESULTS OF THE LOW-VOLTAGE CALIBRATION (June 4, 1994)

10 kV to 1 V Ratio Calibration Using the Digital Voltmeter Method
Corrections to the Nominal 10:1 Ratio:

## 1 Jun 94 DVM Connections: $10 \mathrm{kV} / 1 \mathrm{kV} / 0 \mathrm{~V}$

| 11:00 am | Run 1; correction: | $+26.4 \times 10^{-6}$ | Oil Temperature: | $24.564{ }^{\circ} \mathrm{C}$ |
| :---: | :--- | :---: | :--- | :--- |
| 11:02 am | Run 2; correction: | +24.1 | Oil Temperature: | 24.552 |
| 2:16 pm | Run 3; correction: | -1.3 | Oil Temperature: | 24.582 |
| 2:19 pm | Run 4; correction: | +0.5 | Oil Temperature: | 24.574 |
|  | Avg. Ratio Correction: | $+\mathbf{1 2 . 4}$ | Avg. Temperature: | $\mathbf{2 4 . 5 6 8}$ |
|  | Std. Dev.: | $\mathbf{1 4 . 8 6}$ |  | $\mathbf{0 . 0 1 3}$ |

1 Jun 94 DVM Connections: $1 \mathrm{kV} / 100 \mathrm{~V} / 0 \mathrm{~V}$

| 11:05 am | Run 1; correction: | $+11.8 \times 10^{-6}$ | Oil Temperature: | $24.549{ }^{\circ} \mathrm{C}$ |
| :--- | :--- | :---: | :--- | :--- |
| 11:07 am | Run 2; correction: | +11.3 | Oil Temperature: | 24.555 |
| 2:14 pm | Run 3; correction: | -6.3 | Oil Temperature: | 24.571 |
| 2:22 pm | Run 4; correction: | -6.7 | Oil Temperature: | 24.578 |
|  | Avg. Ratio Correction: | $+\mathbf{2 . 5 3}$ | Avg. Temperature: | $\mathbf{2 4 . 5 6 3}$ |
|  | Std. Dev.: | $\mathbf{1 0 . 4 2}$ |  | $\mathbf{0 . 0 1 4}$ |

1 Jun 94 DVM Connections: 100 V/10 V/0 V

| 11:09 am | Run 1; correction: | $+2.5 \times 10^{-6}$ | Oil Temperature: | $24.567{ }^{\circ} \mathrm{C}$ |
| :--- | :--- | :---: | :--- | :--- |
| 11:12 am | Run 2; correction: | +2.5 | Oil Temperature: | 24.568 |
| 2:12 pm | Run 3; correction: | -0.2 | Oil Temperature: | 24.577 |
| 2:24 pm | Run 4; correction: | -0.1 | Oil Temperature: | 24.574 |
|  | Avg. Ratio Correction: | $+\mathbf{1 . 1 8}$ | Avg. Temperature: | $\mathbf{2 4 . 5 7 2}$ |
|  | Std. Dev.: | $\mathbf{1 . 5 3}$ |  | $\mathbf{0 . 0 0 5}$ |

1 Jun 94 DVM Connections: $10 \mathrm{~V} / 1 \mathrm{~V} / 0 \mathrm{~V}$

| 11:18 am | Run 1; correction: | $+6.3 \times 10^{-6}$ | Oil Temperature: | $24.584{ }^{\circ} \mathrm{C}$ |
| :---: | :---: | :---: | :---: | :---: |
| 11:19 am | Run 2; correction: | +6.2 | Oil Temperature: | 24.586 |
| 2:08 pm | Run 3; correction: | +7.1 | Oil Temperature: | 24.579 |
| 2:26 pm | Run 4; correction: | +4.0 | Oil Temperature: | 24.574 |
|  | Avg. Ratio Correction: | +5.90 | Avg. Temperature: | 24.581 |
|  | Std. Dev.: | 1.33 |  | 0.005 |
|  | Overall Ratio = | 10000.219 | Correction: +21.91 | $1 \times 10^{-6}$ |
|  | 3 x standard deviation: | $54.79 \times 10^{-6}$ |  |  |
|  | Overall average tempera | ature: 24 | .571 $\pm 0.008{ }^{\circ} \mathrm{C}$ |  |

Table 5, RESULTS OF THE LOW-VOLTAGE CALIBRATION (August 8, 1994)
10 kV to 1 V Ratio Calibration Using the Digital Voltmeter Method
Corrections to the Nominal 10:1 Ratio:
8 Aug 94 DVM Connections: $10 \mathrm{kV} / 1 \mathrm{kV} / 0 \mathrm{~V}$

| 11:30 am | Run 1; correction: | $-1.44 \times 10^{-6}$ |  | Oil Temperature4.557 |
| :---: | :---: | :---: | :---: | :---: |
| ${ }^{\circ} \mathrm{C}$ |  |  |  |  |
| 2:57 pm | Run 2; correction: | -1.47 | Oil Temperature: | 24.560 |
| 3:00 pm | Run 3; correction: | -0.33 | Oil Temperature: | 24.571 |
|  | Avg. Ratio Correction: | -1.08 | Avg. Temperature: | 24.563 |
|  | Std. Dev.: | 0.65 |  | 0.007 |
| 8 Aug 94 DVM Connections: $1 \mathrm{kV} / 100 \mathrm{~V} / 0 \mathrm{~V}$ |  |  |  |  |
| 11:35 am | Run 1; correction: | $-7.86 \times 10^{-6}$ | Oil Temperature: | $24.593{ }^{\circ} \mathrm{C}$ |
| 11:36 am | Run 2; correction: | -8.33 | Oil Temperature: | 24.602 |
| 2:53 pm | Run 3; correction: | -6.62 | Oil Temperature: | 24.572 |
| $2: 55 \mathrm{pm}$ | Run 4; correction: | -6.85 | Oil Temperature: | 24.566 |
|  | Avg. Ratio Correction: | -7.42 | Avg. Temperature: | 24.583 |
|  | Std. Dev.: | 0.81 |  | 0.017 |
| 8 Aug 94 DVM Connections: $100 \mathrm{~V} / 10 \mathrm{~V} / 0 \mathrm{~V}$ |  |  |  |  |
| 11:41 am | Run 1; correction: | $-1.52 \times 10^{-6}$ | Oil Temperature: | $24.594{ }^{\circ} \mathrm{C}$ |
| 11:42 am | Run 2; correction: | -1.56 | Oil Temperature: | 24.585 |
| 2:48 pm | Run 3; correction: | -0.41 | Oil Temperature: | 24.561 |
| 2:50 pm | Run 4; correction: | -0.44 | Oil Temperature: | 24.567 |
|  | Avg. Ratio Correction: | -0.98 | Avg. Temperature: | 24.577 |
|  | Std. Dev.: | 0.64 |  | 0.015 |
|  | 8 Aug 94 DVM Connections: $10 \mathrm{~V} / 1 \mathrm{~V} / 0 \mathrm{~V}$ |  |  |  |
| 11:45 am | Run 1; correction: | $+2.77 \times 10^{-6}$ | Oil Temperature: | $24.567^{\circ} \mathrm{C}$ |
| 11:47 am | Run 2; correction: | +2.77 | Oil Temperature: | 24.555 |
| 2:36 pm | Run 3; correction: | +4.26 | Oil Temperature: | 24.566 |
| 2:37 pm | Run 4; correction: | +4.08 | Oil Temperature: | 24.567 |
|  | Avg. Ratio Correction: | +3.47 | Avg. Temperature: | $24.564{ }^{\circ} \mathrm{C}$ |
|  | Std. Dev.: | 0.81 |  | 0.006 |
|  | Overall Ratio = | 9999.940 | Correction: -6 | $-6.01 \times 10^{-6}$ |
|  | 3 x standard deviation: | $4.39 \times 10$ |  |  |
|  | Overall average temper | ature: 2 | $4.571 \pm 0.008{ }^{\circ} \mathrm{C}$ |  |

## Comparison of Ratios by Resistor Decade

Date Correction to the Nominal Ratio Oil Bath Temperature

DVM Connections: $10 \mathrm{kV} / 1 \mathrm{kV} / 0 \mathrm{~V}$

| 1 Dec 93 | $+1.9 \pm 1.74 \times 10-6$ | $24.49 \pm 0.007{ }^{\circ} \mathrm{C}$ |
| :--- | :---: | ---: |
| 3 Dec 93 | $-2.6 \pm 0.70 \times 10^{-6}$ | $24.52 \pm 0.008^{\circ} \mathrm{C}$ |
| $20-23$ May 94 | $+24.2 \pm 1.10 \times 10^{-6}$ | $24.566 \pm 0.066{ }^{\circ} \mathrm{C}$ |
| 1 Jun 94 | $+12.4 \pm 14.86 \times 10^{-6}$ | $24.568 \pm 0.013^{\circ} \mathrm{C}$ |
| 8 Aug 94 | $-1.08 \pm 0.65 \times 10^{-6}$ | $24.563 \pm 0.007{ }^{\circ} \mathrm{C}$ |

DVM Connections: $1 \mathrm{kV} / 100 \mathrm{~V} / 0 \mathrm{~V}$

| 01 Dec 93 | $-8.2 \pm 0.49 \times 10^{-6}$ | $24.49 \pm 0.00 \circ^{\circ} \mathrm{C}$ |
| :--- | :--- | :--- |
| 3 Dec 93 | $-8.1 \pm 0.15 \times 10^{-6}$ | $24.52 \pm 0.006{ }^{\circ} \mathrm{C}$ |
| 1 Jun 94 | $+2.53 \pm 10.42 \times 10^{-6}$ | $24.563 \pm 0.014{ }^{\circ} \mathrm{C}$ |
| 8 Aug 94 | $-7.42 \pm 0.81 \times 10^{-6}$ | $24.583 \pm 0.017{ }^{\circ} \mathrm{C}$ |

DV்M Connections: $100 \mathrm{~V} / 10 \mathrm{~V} / 0 \mathrm{~V}$

| 1 Dec 93 | $-1.6 \pm 0.10 \times 10^{-6}$ | $24.49 \pm 0.010^{\circ} \mathrm{C}$ |
| :--- | :--- | :--- |
| 3 Dec 93 | $-2.2 \pm 0.10 \times 10^{-6}$ | $24.53 \pm 0.005^{\circ} \mathrm{C}$ |
| 1 Jun 94 | $+1.18 \pm 1.53 \times 10^{-6}$ | $24.572 \pm 0.005^{\circ} \mathrm{C}$ |
| 8 Aug 94 | $-0.98 \pm 0.64 \times 10^{-6}$ | $24.577 \pm 0.015^{\circ} \mathrm{C}$ |

DVM Connections: $10 \mathrm{~V} / 1 \mathrm{~V} / 0 \mathrm{~V}$

| 1 Dec 93 | $+8.6 \pm 1.42 \times 10^{-6}$ | $24.49 \pm 0.011{ }^{\circ} \mathrm{C}$ |
| :--- | :--- | :--- |
| 3 Dec 93 | $+8.8 \pm 0.17 \times 10^{-6}$ | $24.53 \pm 0.004{ }^{\circ} \mathrm{C}$ |
| 1 Jun 94 | $+5.90 \pm 1.33 \times 10^{-6}$ | $24.581 \pm 0.005^{\circ} \mathrm{C}$ |
| 8 Aug 94 | $+3.47 \pm 0.81 \times 10^{-6}$ | $24.564 \pm 0.006{ }^{\circ} \mathrm{C}$ |

## Table 7, RATIO DETERMINATION SUMMARY

## Overall Ratio $\pm 3$ Standard Deviations.

| Date | Actual ratio | Correction to the nominal ratio $\times 10^{6}$ |
| :--- | :---: | :---: |
| 1 Dec 93 | 10000.007 | $+0.7 \pm 6.90$ |
| 3 Dec 93 | 9999.959 | $-4.1 \pm 2.23$ |
| 1 Jun 94 | 10000.208 | $+20.83 \pm 54.79$ |
| 8 Aug 94 | 9999.940 | $-6.01 \pm 4.39$ |
| Mean (excluding data from May and June 94) | $-3.1 \pm 4.9$ |  |

## DISCUSSION OF RESULTS.

## Low-Voltage Calibration (Table 1 to Table 7)

The computed ratio corrections have a mean value of $(-3.1 \pm 4.9) \times 10^{-6}$ to the nominal ratio of $10000: 1$ if the readings taken in May and June 1994 are excluded. Both the June ' 94 readings and the partial ratio determinations in May of that year give a result that differs from the mean by more than four times the standard deviation. In addition, the uncertainty of the June result is almost ten times greater than any of the other uncertainties. The exact cause of this large uncertainty has not been established. The observed anomaly could be attributed to excessive electrical noise due either to outside interference through the power line, or to improper grounding of the oil bath enclosure or shielding of the sensing leads. As a precaution, the wiring was partially reworked before the next set of readings were taken. Because of the large discrepancy of the results in May and June from those obtained earlier and later, it seemed reasonable to assume that they were an artifact of the measuring system rather than a real change in the resistance ratios. They were, therefore, excluded from the overall results. The remainder of the results fall well within the estimated statistical uncertainty and differ from the nominal ratio by about $5 \times 10^{-6}$.

Over the eight-month period from December 1993 to August 1994 no statistically significant drift in the calibration could be detected. The time needed to perform a recalibration using the digital voltmeter method is approximately one work day including the time required for the oil bath to reach operating temperature.

## Comparison with the Park Vọltage Divider (Table 8)

The intercomparison with the Park resistors is carried out by means of a manually adjusted bridge circuit using the both the Park divider and the 10 kV divider in parallel, each adjusted for a nominal 10000 to 1 ratio. The high-voltage side of the Park divider consists of three sections in series of $100 \mathrm{M} \Omega$ each, while the low-voltage section is composed of three nominal $10 \mathrm{k} \Omega$ resistors in series with an adjustable resistor. The low-voltage section is part of the bridge circuit used for the intercomparison. The measurements were made with 10 kV applied to the highvoltage terminals of the dividers.

To compare the two dividers, the one-volt taps of the 10 kV divider is connected as one input to the bridge and the $10 \mathrm{k} \Omega$ sections in series with an adjustable resistor forms the low-voltage end of the Park divider. Setting the adjustable resistor effectively changes the ratio of the Park divider until the bridge detector indicates a null. The actual ratio of the Park divider can then be inferred from the resistance setting. The sensitivity of this arrangement allows the ratio to be adjusted in steps of about $7 \times 10^{-6}$. The data from measurements made on several days varied over a range of $40 \times 10^{-6}$ and with a standard deviation of $8.9 \times 10^{-6}$.

The three configurations referred to as "A," "B," and "C," in the table of results correspond to the use of three, two, or one section ( $100 \mathrm{M} \Omega$ ) of the Park divider and correspondingly three, two, or one $10 \mathrm{k} \Omega$ resistors in the lower leg of the divider. The values obtained do not show a significant dependence on the configuration.

Averaging the data from both the 10 kV divider and the Park divider shows that the ratio values agree to within the uncertainties stated in the tables and are very close to the nominal ratio of $10000: 1$. The bridge comparison is sensitive to ground impedance and care has to be taken use the shortest possible ground connections. However, the ground impedance cannot be completely eliminated and thus contributes to the measurement uncertainty.

## CONCLUSIONS

A 10 kV dc divider consisting of resistor networks immersed in a temperature controlled oil bath has been recalibrated to be used as a laboratory standard for ratio calibration of other instruments. A calibration method was developed to determine the ratio of each decade of the divider using a precision digital voltmeter at low voltage. The overall ratio could then be calculated from the decade ratios. The average, taken over an eight-month period, of the determinations of the 10000 to 1 ratio of the divider was 9999.967 with an uncertainty of $\pm 4.9 \times 10^{-6}$ ( 3 standard deviations). This ratio was compared at 10 kV with a Park-type divider on several occasions and the results agreed within the combined experimental uncertainties. The digital voltmeter method provides a relatively simple and quick method to recalibrate the divider.

With this recalibration of the nearly twenty-year old divider, the National Institute of Standards and Technology is now in a position to offer a dc divider calibration service in the 1 kV to 10 kV voltage range. The estimated uncertainty of such calibrations would be of the order of $\pm 10 \times 10^{-6}$.

## ACKNOWLEDGEMENTS

The author would like to thank Martin Misakian for help with setting up the experiment and for obtaining the Park resistor ratio data at 10 kV , and Richard L. Steiner for providing the Josephson calibration data.

## Table 8, Park-System Data Summary



## Table 8, Park-System Data Summary (continued)



## APPENDIX A: Detailed Experimental Calibration Procedures

## 1. Introduction

The calibration of the high-voltage divider consist of a series of four-step resistance ratio determinations making use of the highly linear 10 -volt range of the voltmeter function of the HewlettPackard Model $3458 \mathrm{~A}^{5}$ digital multimeter to measure ratio. The linearity of the 10 V range has been proven to be highly stable and has been calibrated against a 10 V Josephson array standard. The results of this linearity check show a departure from linearity over a ten-to-one ratio which does not exceed one part per million.

## 2. Setting Up the Calibration Experiment

The experimental system comprises the resistor network in an oil bath, a rack with the electronic control equipment including a personal computer (PC), and an additional table-model computer that is used for the voltage-ratio measurements. Two separate IEEE-488 Interface bus circuits are used. One bus, connected to the PC (IBM Model XT). controls the oil-bath temperature by interconnecting the thermistor control unit (Instrulab System Thermometer Model 3312-14-15) and the programmable power supply (Kepco Bipolar Operational Power Supply/Amplifier, Model BOP 20-20M 488D). The other IEEE-488 bus links the digital multimeter (Hewlett-Packard Model 3458A) to the table-model computer (Hewlett-Packard Model 85) which is programmed to control the digital voltmeter readings.

## 3. Resistor Network

a. Physical Layout ${ }^{6}$

## i. Upper Decades

The resistor network, which forms the actual voltage divider (Fig. 1), is composed of three decades of wire-wound resistors ( $2 \mathrm{M} \Omega, 200 \mathrm{k} \Omega$, and $20 \mathrm{k} \Omega$ ). Each decade has nine nominally equal resistors with the tenth (virtual) resistor consisting of the combined resistance of all lower resistors. Each node of the network is tied to the center pins of two BPO connectors in parallel. The outside conductors of the connectors are connected to the nodes of the guard circuit consisting of an auxiliary network of resistors having the same resistances as the main wire-wound resistors. Nodes of the guard circuit are also connected to (equipotential) metal shields surrounding the main divider resistors. The nodes

[^4]are marked with the nominal input voltages near their respective connectors ranging from 10 kV to 10 V .

## ii. Lower Decades (Kelvin Varley)

The lower decades of the ratio divider consist of a Kelvin-Varley divider that is shunted to give it a $20 \mathrm{k} \Omega$ input impedance (see Fig. 2(a).). The Kelvin-Varley has two decades of wire wound resistors, with a guard circuit similar to that used for the upper decades of the main divider followed by a six-dial commercial Kelvin-Varley divider (see Fig. 1). Ratio connections for the upper two decades are made with pairs of jumper cables equipped with BPO plug connectors. The remaining six decades of the commercial Kelvin-Varley divider use rotary dial switches.

Note: For the purpose of this calibration the dials of the commercial Kelvin-Varley are not used and are set to zero. The upper two decades are connected (see section b. vi. below) to give a one-volt output for a 10 kV input applied to the main divider.
b. Connections for the Calibration

## i. Supply Leads

Calibrations are carried out with a ten-volt stabilized dc source. The dc voltage is connected from the source to the divider decade under test through a multipole rotary switch. The switch has several functions one of which is the reversal of the polarity of the applied voltage.

The leads from the source to the switch and from the switch to the divider consist of a pair of twisted leads with a shield. Near the connections to the divider, the cable is split into two separate shielded leads that connect to the divider (Fig. 3). The shields of the cable from the source to the switch and from the switch to the cable junction are connected to ground to reduce interference. The shield sections for the two single conductor lead wires, from the cable junction to the divider, are tied to the outer conductors of the respective BPO connectors.

Note that while the inner conductor of the male BPO connector is tied to a node of the divider resistance network, the outer conductor is not grounded but tied to the corresponding node of the guard circuit. The outer conductor, therefore, should not be at ground potential but at nominal the same voltage as the inner conductor. This requires that the shield attached to the mating outer shell of the connector also not be at ground potential. Therefore, the shield of the cable leading to the connector has to be isolated from the grounded shields of other parts of the cable. For convenience, the break in the shields has been made at the cable junction point by trimming the shielding braid back a short distance.

To establish effective guard potentials, the supply leads must feed both the main divider as well as the guard circuit, since the resistor network making up the guard circuit is by itself electrically
isolated from the main divider. To feed both the divider and guard circuits, the inner conductor and outer shield of each of the (single-conductor ends (see Fig. 3) of the) supply leads are connected together so that the main divider and the guard circuit are at the same voltage at their corresponding endpoints. The intermediate nodes of the divider network, however, remain without a direct connection to the corresponding nodes of the guard circuit but are at approximately the same dc voltage.

## ii. Sensing Leads

There are two pairs of otherwise identical sensing leads referred to as "A" and "B" leads. These are routed from the divider to the channel selector switch and from the switch to the digital voltmeter. Similar to the arrangement of the supply leads, the cables to and from the switch consist of a pair of twisted conductors that are shielded except for about a decimeter of the cable at the divider end where the cables are each split into two single-conductors. The shields of the two-conductor portions are connected to ground, while the shields of the single-conductor cables are connected only to the respective outer conductors of the (female) BPO connectors and isolated from the shields of the twoconductor cables. Unlike the supply leads, the inner (divider circuit) and outer (guard circuit) of the sensing leads are not connected together so that the voltage sensed is that across the divider network only.

## iii. Divider Calibration Supply Connections

To calibrate the highest decade ( 10 kV to 1 kV ) the supply leads (labeled current) are connected to one of the " $10 \mathrm{kV}{ }^{77} \mathrm{BPO}$ connectors and the other supply lead is connected to the " 0 " input terminal of the Kelvin-Varley divider (see Fig. 2(a).). To check whether the polarity is correct, measure the voltage applied to the divider when the switch is in the " $\mathrm{A}+$ " position. The voltage at the " 10 kV " terminal should be +10 volts (nominal). If the voltage is -10 volts, interchange the supply leads.

## iv. Kelvin-Varley Connections

The Kelvin-Varley divider is electrically a separate unit from the main voltage-divider resistance network and is connected to it by two jumper cables (Fig. 2(a).). An additional jumper cable is used to configure a chain of three $10 \mathrm{k} \Omega$ resistors into a $25 \mathrm{k} \Omega$ shunt which combined with the input resistance of the Kelvin-Varley divider forms the equivalent of the tenth $20 \mathrm{k} \Omega$ resistor of the lowest decade of the main divider.

The 1 V tap of the divider is obtained by connecting the first set of jumper leads of the Kelvin-Varley circuit from the " X " and " Y " terminals to the connectors on either side of the " 1 " marking and connecting the other set of jumper cables across the " 0 " marking on the next ( $10^{-1}$ ) range. All

7 The numbers and units enclosed by quotation marks correspond to labelling on the cover of the oil bath placed next to the BPO connectors.
switches in the switched section of the Kelvin-Varley divider should be set to zero. The output connectors of the Kelvin-Varley circuit are then the 1 V tap of the overall divider network.

## v. Digital Voltmeter Connections

The rotary channel selector switch connects the input of the digital voltmeter either to the " A " or " B " leads, and it also selects the polarity of the supply voltage so that there are four active switch positions: "A+, A-, B-, B+." Intermediate switch position are open circuits. The control software for the digital voltmeter (on the Hewlett-Packard Model 85 computer) assumes that the " A " leads are connected across the higher voltage. In most cases that means that the "A" leads are connected to the same divider nodes as the supply leads. The " B " leads are normally connected to the divider tap and the bottom connection of the resistor network under test.

The pair of twisted, shielded leads from the switch to the input terminals of the digital voltmeter are wound around a toroidal, high-permeability magnetic core forming a coaxial choke. The co-axial choke presents a low impedance path for signals going to the voltmeter, in one lead and returning through the other. For any ac leakage or induced currents that are asymmetrically going in one lead and returning through an alternate path, the coaxial choke represents a relatively high impedance. The choke, therefore, acts as a filter for unwanted common-mode signals. This is important since the divider is not particularly well shielded against stray ac pickup that would appear as noise in the digital voltmeter readings.

At the digital voltmeter, the white lead of the cable is connected to the " HI " (two-wire) input terminal at the front of the meter, and the black lead to the "LO" terminal. The green lead is connected to the "Guard" terminal.

## vi. Divider-Voltage Connection, "A" Leads

One of the BPO female connectors attached to the "A" leads is plugged into the male connector which is in parallel with that connected to the supply (e.g., 10 kV terminal for the highest decade). The other connector is plugged into a special adaptor plug which allows two BPO plugs to be connected in parallel. The parallel connection ensures a common point in the measurements of the ratio voltages. The adaptor is plugged to the male BPO connector marked " 0 " and is located near the "LO" output terminal on the pie-shaped section covering the Kelvin-Varley divider (see Fig. 2(a).). To check the polarity of the lead connections, set the switch to position " $\mathrm{A}+$ " and read the digital voltmeter; a reading of a nominal +10 V should be obtained. If the reading is -10 V , interchange the connection of the "A" leads.

## vii. Divider-Voltage Connection, "B" Leads

The " B " leads are connected across the divider decade tap and the common point to obtain the desired ratio voltage, a fraction (usually $1 / 10$ th) of the voltage applied across the entire decade section. The BPO connector for the signal return is plugged into the special adaptor mentioned in
vi. above. The other connector is plugged into one of the pair of parallel male BPO connectors at the desired voltage tap. A polarity check similar to that described above should be carried out.
viii. Selection of Connections for the "A" and "B" Leads.

The following sets of divider connections are used to calibrate the decades of the divider. The order in which the decades are calibrated is not significant.

| "A" Leads |  | "B" Leads |  |
| :---: | :---: | :---: | :---: |
| High | Low | High | Low |
| Terminals |  | Terminals |  |
| 10 kV | 0 V | 1 kV | 0 V |
| 1 kV | 0 V | 100 V | 0 V |
| 100 V | 0 V | 10 V | 0 V |
| 10 V | 0 V | 1 V | 0 V |

The " 1 V " connection is made at the output of the Kelvin-Varley divider, at the plug connection marked "LO". (See also section iv, above).
ix. Ratios Other Than Ten-to-One

If ratios other than 10000 to 1 are required, for instance if the voltage applied to the divider is 5 kV , the supply and "A" leads are connected to the desired input voltage, e.g., 5 kV and 0 V , while the " B " leads remain connected to 1 kV and 0 V as before when testing the highest decade string of resistors.
c. Combining Decade Calibrations
i. In Terms of Ratios

The overall ratio of the divider for a nominal 10000 to 1 ratio is the product of the ratios determined for all four decades. Note that the individual ratios printed out by the Hewlett-Packard Model 85 desktop computer are rounded to six decimal places and have thus limited resolution. Better resolution can be obtained by using the indicated ratio corrections ( $\times 10^{6}$ ) and applying them to the nominal ratios.

## 4. Temperature Control

To keep the resistance of the wire-wound ratio resistors stable, the temperature of the resistors and the oil in which they are immersed has to be closely controlled. Temperature control is accomplished with the heating/cooling control subsystem. The temperature measuring subsystem consists of four thermistor sensors connected to a "thermometer" unit that converts the thermistor resistances into corresponding digital temperature values. The thermistors are immersed in the oil through openings in the translucent acrylic cover of the oil bath. Each thermistor is connected individually to the thermometer unit which is mounted on the rack with the rest of the electronic equipment.

The heating/cooling subsystem consists of a set of four Peltier units powered from a programmable power supply and designed to change the temperature of the oil. The four Peltier heating and cooling units are mounted evenly spaced on side of the cylindrically shaped oil bath. Small fan units remove the heated air from each of these units. The fans are powered directly from the $120 \mathrm{~V}, 60 \mathrm{~Hz}$ line using a flexible twin-lead line cord. The Peltier units are electrically connected in series and are powered from a rack-mounted, programmable, dc current supply. The current can be varied remotely via the IEEE 488 -interface bus from minus to plus full scale. Also, the supply has provisions for limiting the output current to protect the Peltier units.

Initially, when the bath is at room temperature, the heating current is limited to approximately 7.5 A . After the oil temperature comes to within $\pm 0.1^{\circ} \mathrm{C}$ of the set point $\left(24.5^{\circ} \mathrm{C}\right)$, the current limit is reduced to 5 A for both heating and cooling.

## 5. Operation of the Temperature Control Program.

The program is written in GW Basic for use with the National Instruments 488 Interface Card. Following the instructions for interface programming provided by National Instruments, the default parameters have been set up for the two subsystems, such as time-outs, etc.

After switching on the computer, and after it has completed the initialization, type "run" at the DOS prompt and follow the instructions displayed on the screen. The "run" command will start the basic program. When the program is running, the first two statements are queries to make sure the oil is stirred and that the fans are cooling the Peltier units. It will take about three to four hours to bring the oil up to operating temperature.

## a. Program Screen Display

While the program is running, the screen alternately displays numerical data and a graphic (bar graph) display. The program samples the temperature data about every 15 seconds during normal operation. Four thermistors are actually connected; a maximum of six thermistors could be plugged into existing connectors. The thermometer unit is programmed to scan five of the six possible connections. (Since, normally, there are only four thermistors, one position is shown as "OPEN"). The program computes the correct average of the temperature irrespective of how many thermistors are connected and into which connectors they are plugged in.

## b. Numerical Display

The display shows the following:
i. Elapsed time in seconds since the beginning of the run.
ii. The number of the measurement cycle; i.e., the number of times the thermometer unit has been queried.
iii. The five scanned outputs of the thermometer unit.
iv. The average temperature and the number of active thermistor probes.
v. The current Reference Temperature and the set-point temperature
vi. The range of average (measured) temperatures. [Minima and maxima displayed are valid only after the measured temperature reaches the set-point temperature minus $0.1^{\circ} \mathrm{C}$. Up to that time Min=26 and Max=0]
vii. The range of the reference temperature (rMin, rMax). These values should be symmetrical about the set-point temperature.
viii. The cumulative number of seconds that the reference temperature has ramped up and down.
ix. The state of the heating/cooling function is indicated by a text message and by the color border of the display. A red background indicates that heating is turned on, blue that cooling is turned on, and green indicates that both are turned off.
c. Bar-graph display.

The bar-graph display alternates with the numerical display. The bar graphs picture the average temperature measured and the reference temperature, as well as indicating the set point.
i. The upper bar graph provides an indication of the measured temperature. Temperature is plotted from left to right. To obtain greater resolution, the temperature zero is displaced off-screen to the left. The setpoint temperature is approximately at the center of the display. Change from the last reading is shown by a change in color; red (brown) for increases in temperature, blue for decreases in temperature. The trend, increasing or decreasing, is also indicated by arrows pointing to the right or left respectively.
ii. The lower bar graph shows the reference temperature. As with the measured temperature, arrows indicate the increasing or decreasing trend.
iii. The temperature is shown, rounded to three decimal places, at the left-hand extreme of the bar graph. The setpoint temperature is indicated by a vertical arrow.

## d. <br> Error Conditions

The program monitors the 488 -Interface bus status, and if a malfunction occurs in the Thermometer unit or if the power supply (heater current source) does not respond, a diagnostic message is displayed on the screen. If the malfunction can be cleared, for instance, by turning off the thermometer unit and turning it back on again which reinitializes various functions, the temperature control program can be restarted (continued) by pressing the ENTER key. Instructions are shown on the screen.
6.

Terminating the Program
The temperature control program can only be terminated by pressing the control+break keys which stops execution of the BASIC routines. On the "OK" prompt, after BASIC program execution has terminated, type SYSTEM [ENTER] which will cause the program to exit BASIC and return control to DOS.

Before shutting off the computer, the hard disk should be "parked" with a BYE [ENTER] command.

## Appendix B

## OIL-BATH TEMPERATURE CONTROL PROGRAM

Appendix B contains an annotated listing of the temperature control program. The program is written in GW BASIC and the statements 1 to 67 follow the code published by National Instruments for their IEEE-488 interface bus. The remainder of the program was written for this application by the author.

This program is designed to control the temperature of the oil bath for the high-voltage de divider within $\pm 0.1 \cdot C$. The temperature is measured with up to five probes using and INSTROLAB Thermometer system and a EEPCO* power supply in the current mode (limited to a maximum of 5 A) that feeds thermoelectric (Peltier) modules for beating and cooling.

## Lines 1 through 67 initialize the functions and constants necessary for operation of the IEEE-488 Interface Bus



```
    CNLL IBINITICIBFINO, IBTRG, IBCLR, IBPCT, IBSIC, IBLOC, IBPPC, IBBMA, IBONL, IBRSC, IBSRE, IBRSV, IBPAD, IBSND
    IBIST, IBOM, IBEOS, IBMO, IBEOT, IBRDF, IBLRTF, IBTRAP, IBDEV, IBLM, IBLINES, IBCONFIG)
    CALL IBIMIT2CIBGTS, IBCAC, IBMAIT, IBPOKE, IBLRT, IBLRTA, IBCND, IBCMDA, IBRD, IBRDA, IBSTOP, IBRPP, IBRSP,
    IBDIAG, IBXTRC, IBRDI, IBURTI, IBRDIA, IBLRTIA, IBEVENT, IBSTAK, IBERR%, IBCNT%)
    CALL IBIMITJCSEMDCNDS, SEMDSETUP, SEMDOATABYTES, SEMD, SEMDLIST, RECEIVESETUP, RCVRESPMSG, RECEIVE, SENDIFC,
    dEvCLEAR, DEVCLEARLIST, EMABLELOCAL, EMABLEREMOTE, SETRILS, SENDLLO)
    CALL IBIMITLCPASSCONTROL, READSTATUSBYTE, TRIGGER, TRIGGERLIST, PPOLLCONFIG, PPOLLLUNCONFIG, PPOLL, RESETSYS,
    FIMOROS, ALLSPOLL, FIMDLSTM, TETSYS, IBRDKEY, IBLRTKEY, MAITSRO, TESTSRQ)
REM
REM GPIB Commands:
REM
```



```
    OCL% = &H14: PPUK = &H15 : SPE% = &H18: SPOK = &H19: PPE% =&H60:PPOK =&H70
REM
REM GPIB status bit vector:
REM
    EERR = 2H8000 : TIMO = &M4000: EEMD = &H2000 : SRQI = 2H1000 : ROS = &H800 : SPOLL =&H400: EEVENT = &H2OO
    OMPL = &H100 : LOK = &HBO : RREM = &HEO : CIC = &H2O : MTM = &H10 : TACS = &H8 : LACS= &H4: DTAS = &HZ : DCAS
    = EH1
REM
REM Error messages returned in global variable iberr:
REM
    EDVR = 0: ECIC = 1:ENOL =.2.: EADR = 3:EARG = 4:ESAC = 5:EABO = 6:ENEB = 7
    EOIP = 10: ECAP = 11: EFSO = 12: EBUS = 14: ESTB = 15: ESRQ = 16: ETAB = 20
REM
REM EOS mode bits:
REM
    BINZ = &H1000 : XEOS% = &H800 : REOS% = &H400
REM
REM Timeout values and meanings:
REM
    TMONEX = 0: T10US% = 1: T3OUS% = 2: T100US% = 3: T300US% = 4: T1MS% = S:T3MS%=6: T10NS% = 7
    T30N5% = 8: T100N5% = 9: T300N5% = 10: T15% = 11: T3S% = 12: T105% = 13:T305% =14: T1005% = 15
    13005% = 16: T10005% = 17
REM
REM Miscellaneous:
REM
    S% = &H8 : LF% = &HA
REM
REM IBLM Constants:
REM
    ALL.SADK = -1 : NO.SAOK = 0
REM
REM IBEVENT Constants
REM
    EVENTDTAS% = 1 : EVENTOCAS% = 2
REM
REM "OPTION" Selection codes for IBCONFIG function:
REM
```

| 46 |  |  |
| :---: | :---: | :---: |
| 47 |  |  |
| 48 |  |  |
| 8417 |  |  |
| 50 |  | 18CSPOLLTIMEX = \&H18: 1BCPPOLLTIMEX $=$ EH19: 18CNOEMDBITONEOS\% $=$ EH1A |
| 51 | REM | These values are used by the Send 488.2 command: |
| 52 | REM |  |
| 53 | REM |  |
| 54 | MLLEMOK $=2 H 0:$ MLEMDK $=2 H 1:$ DABEMOK $=2 H 2$ |  |
| 55 | REM | This value is used by the 488.2 Receive commend: |
| 56 | REM |  |
| 57 | REM |  |
| 58 | STOPEMDK $=24100$ |  |
| 59 | REN |  |
| 60 | REM The following values are used by the IBLIMES function: |  |
| 61 | REM |  |
| 62 | ```VALIODAV = ent``` |  |
| 63 | ```EUSEOI = 2M8000 : EUSATM = &H4000 : CUSSRO = &H2000 : BUSREM = &H1000 : EUSIFC =&H800 : BUSNRFO = &H400 : CUSUDAC = 2H200 : EUSDAV =2H100``` |  |
| 64 | REM |  |
| 65 | REM This value is used to terminate an address list. It should be assignedREM to the last entry. |  |
| 66 |  |  |  |
| 67 | REM <br> Iines 100 controller |  |
|  |  |  |  |
|  |  |  |  |
| 100 | REM Parameter Values |  |
| 110 | CONTROLLERS ${ }^{\text {m }}$ GPIB0 : CALL IBFIMD (CONTROLLERS, BRDK) |  |
| 120 | THERMONETERSmTSYS" : CALL IBFIMD (THERMOMETERS, TEMP\%) |  |
| 130 | DEVUNES-mKEPCOn : CALL IBFIND (DEVNAMES, PWR\%) |  |
| 140 | DIM TSTORE (500). TEMPSTORE(500), AVESTORE(500) |  |
| 150 |  |  |
| 160 |  |  |
| 170 | COLOR 14, 2, 2 'green beckground=heating/cooling off |  |
| 180 | TAVG=0 : $\mathrm{T}=0: \mathrm{NOH}=0$ : SPAN=-. 2 : SETPOIMT=24.5 : OFFSET=ABS(SPAN/2) |  |
| 190 | SMMPLES=10 : IMTERVAL=5 : PERIC0=SMAPLES * IMTERVAL : IMCR=0 : REFTEMP=SETPOIMT 4 OFFSET |  |
| 200 MIM=26: MAX=0 : MFLAG=1 : DFLAG=0 : RMIM=100 : RMAX=0 : COUNT=0 : ERMUM=0 |  |  |
|  | The temperature measurement control crcle starts by determining the |  |
|  | elapsed time from the start of the program in seconds. IE this |  |
|  | time is a multiple of the innterval daefined as one of the program |  |
|  | parameters), then a set of temperature readings is taken ta |  |
|  | additional i-second delar is introduced before readings are |  |
|  | actual1\% taken. |  |
| 300 start of measurement/control cycle |  |  |
| 310 | On ERROR COTO 1810 |  |
| 320 | PRIMT *determine sampling time |  |
| 330 | cosus 400 : |  |
| 340 | IF TIME MOD IMTERVAL > 0 THEM 330 |  |
| 350 | PRIMT melepsed time m;TIME;m seconds" : TIMEI=TIME |  |
| 360 | COSUB 400 : If TIME $>$ TIMEI+1 THEN 450 ELSE COTO $360{ }^{\circ}$ loop until sampling time |  |
| 370 |  |  |  |
|  | Subroutine to convert time' into elapsed seconds |  |
| 400 |  | - tre DETERMIME TIME AND CONVERT TO SECONDS |
| 410 |  | TIME = VAL (MIOS(TIMES, 1, 2))*3600+VAL(MIDS(TIMES, 4, 2))*60+VAL(MIDS(TIMES, 7, 2)) |
| 420 |  | If TIMEO $=0$ THEM TIMEO=TIME |

            TIME=TIME-TIMEO
            RETURM
    ```
remperature measurement routine: definition of bus address, bus 'name' of the temperature measurement system, and temperature 'read' command. The 'RESULT\$' string variable is filled with the appropriate number of blanks, and the interface and the 'device' are initialized. If a bus error is detected, the bus status (10 most recent values) is stored in a register. A command to read outputs of 5 thesmocouples is then sent to the temperature measurement system. Again the bus status is checked, and if an error has occurred the status is stored, and the program branches to an error routine that turns off the power supply and permits the temperature system to be reset. If no error occurs, a two-second waiting period allows the thermometer unit to settle before the reading is fetched and stored in the computer.
```

450 - measure thermocouple outputs
460 IF DFLAGOO THEN }80
500 otwot measure temperature
510 ACTIVES=m Instrulebm
520 BONRO%=0 : ADOR% = 7 : COMMANDS=MMEAS:DATA ? (21, 2, 3. 4, 5)
530 1FOR \x1 TO 10
540 M=N+1
550 RESULTS=SPACES(106)
560 CALL SEMDIFC (BOARD%)
570 CNLL DEVCLEAR (BOARD%, ADORZ)
580 IF 18STA% >1 THEM ERRORVAR(ER MOD 10)=18STA% : ER=ER+1
S90 CALL SEMD(BOARDZ, ADOR%, COMMANDS. MLEMOK)
600 IF IBSTAZ >1 THEM ERRORVAR(ER MOD 10)=18STAS : ER=ER+1
6 1 0 ~ I F ~ I B S T A \% ~ A N D ~ E E R R ~ T H E M ~ 1 8 \& 0 ~
62 COSUB 400 : DELAYSTART=TIME '2 s delay between command reading data to prevent hangups
630 COSUB 400 : DELAY=TIME-DELAYSTART : IF DELAY < 2 THEM 630
640 CALL RECEIVE(BONRD%, ADDR%, RESULTS, STOPEND%)
650 IF IBSTAZ >1 THEM ERRORVAR(ER MOD 10)=IBSTAK : ERaER+1 'record 10 previous error messages
660 PRIMT M. MIDS(RESULTS, 1. 15)+m + mMIOS(RESULTS, 18, 15) "print temperature readings
670 PRIMT M. MIDS(RESURTS, 35, 15)4\& + m+MIDS(RESULTS, 52, 15)
680 PRINT M, MIDS(RESULTS, 69, 15)+m + m+MIOS(RESULTS, 86, 15)
690 N=0 : AVETEMP=0

```

Temperature is averaged by scanning the input strings, summing values in non-blank in fields, and dividing by the number of values found. The individual readings and the average is displayed.

700 FOR K=4 TO 103 STEP 17 ' determine average temperature
710 PRINT
720 IF MID (RESULT\$, K, 1) \(=\boldsymbol{\circ} \times\) THEN 760 ELSE
CHANNEL (N) =VAL (MID\$ (RESULT\$, K, 1))
730 IF MID (RESULT\$, \(K+8\), 4) \(=\) "OPEN" THEN 760 ELSE
TEMPERATURE (CHANNEL (N)) =VAL (MID\$ (RESULT\$, K+4, 8))
740 AVETEMP=AVETEMP +TEMPERATURE (CHANNEL (N) )
\(750 \mathrm{~N}=\mathrm{N}+1\)
760 NEXT K
770 IF \(\mathrm{N}=0\) THEN 1840 ELSE AVETEMP= AVETEMP/(N)

";AVETEMP;"N= "; N
\(790^{\circ}\)

> Because the temperature is being measured in the main vessel and because of the large thermal inertia of the oil, it is necessary to modulate the reference temperature to decrease the hysteresis in the controlled temperature fluctuations. The reference temperature is successively increased and decreased linearly.

800 - determine reference temperature (modulated about the setpoint)
810 COWNT \(=\) CONWT +1
820 IF COUNT MOD (Z"SAMPLES)=0 TMEN SPAM =-SPAM : TSTORE(TO MOD 500)=TIME : TEMPSTORE(TO MOD SOO)=REFTEMP : AVESTORE(TO MOO SOO)=AVETEMP: \(T 0=T 0+1:\) COWNT \(=0\)
830 IF SPAM 20 THEN UP~UP+TIME-LASTTIME : LASTTIME=TIME ELSE OONN=OONN+TIME-LASTTIME : LASTTIME=TIME
840 REFTEMP=REFTEMP + SPAM/PERIOD
850 'PRIMT T, SIN(T/100)*SPAM;INCR, REFTENP, (THSNMPLES MOD PERICO*SAMPLES)/SAMPLES, SPAM, OFFSET
Records the maximum and minimum excursions of the reference
temperature and counts the number of up and down gradients. (Ideally
these should average to zero.)
860 IF REFTEMP > RHAX THEM RMUX=REFTEMP
870 IF REFTEMP < RHIM THEN RMIN=REFTEMP
Records the maximum and minimum excursions of the average temperature after the temperature has reached the interval of ( \(\pm 0.10+\) setpoint temperature).

880 IF AVETEMP > SETPOINT-. 1 AND AVETENP < SETPOINT + 1 THEN MFLAG=0
890 IF MFLGG \(=0\) AND AVETEMP > MUX THEN MUX \(=\) AVETENP
900 If MFLLG \(=0\) AND AVETENP \& MIN THEN MIN=AVETENP
910 PRINT "Measured temperature ";AVETEMP;" Min. = ";MIM;" Max. = ";MUX
920 PRINT MReference temperature= ";REFTEMP;" MMin= ";RHIN;" MKax= ";RMAX
930 PRINT MSetpoint Teaperature \({ }^{-1}\); SETPOINT
و\%0 PRIMT "цр = ";UP;" doun=";DON
950 -
On the basis of the relative values of the reference and average measured temperatures, the power supply current is switched to heating, off, or cooling.

1000 .*** determine control points
1010 If AVETEMP < REFTEMP AND HEAT \(=0\) THEN MEAT 1 'heating
1020 IF AVETEMP > REFTEMP AND MEAT=1 THEN MEAT=0 'off between heating and cooling
1030 IF AVETEAP > REFTENP AND MEAT \(=0\) THEN MEAT \(=-1\) 'cooling
1040 IF AVETEMP < REFTEMP AND MEAT \(=-1\) THEN HEAT \(=0\) coff between cooling and heating
1050 If dflagoo then 320
The value of the 'HEAT' variable determines the code word that controls the magnitude and direction of the (power) supply current source.

1100 Heater control routine: Determine control code word
1110 ACTIVES="Kepco"
1120 KAMPL \(=5\) : DEVNAMES=ツKEPCO : LIMIT=5 : CONTROLLERS="GPI80"
1130 KEPCO \(=\) INT(ABS (KAMPL*HEAT)/20*999) : IF HEAT < 0 THEN PREFIX=5 ELSE PREFIX=4
1140 IF KEPCO \(>99\) THEN CONTROLWORDS \(=\) MIDS(STRS(PREFIX), 2, 1)4HIDS(STI:S(KEPCO), 2, 3)+HIDS(STRS(IMT(LIMIT/20^99)), 2, 2) \(+\cdots \cdots\)
 2)+MIDS(STRS(IMT(LIMIT/20*99)), 2, 2)+m m

1160 IF KEPCO < 10 THEN CONTROL WORDS=NIDS(STRS(PREFIX), 2, 1)+MOOM+MIDS(STRS(KEPCO), 2, 1) +MIDS(STRS(IMT(LIMIT/20M99)), 2. 2) \(+\infty=\)

\title{
The power supply control word is transmitted over the bus. If the supply does not respond to the bus command, the program branches to an error routine that permits the malfunction to be corrected before continuing the control function.
}
```

1200 **** Meater control routine: Send control code word to supply
1210 ON ERROR COTO 1810 : COSUB 1220 : COTO 1400 'set up power supply
1220 IF PLRK < 1 THEM PRINT MPower SUpply not foundm : EID 'Check supply is active
1230 EONRO%=0 : PADDR% = 6
1240 CALL SEMDIFC (BOARO%)
1250 CALL DEVCLEAR (BOARD%. PADORZ)
1260 CALL SENDPBOARD%, PADDR%, CONTROLWORDS, MLEMO%)
1270 POLERSTATUS(PS MCD 10)=1BSTAZ : PS=PS+1
1280 IF IESTAZ AND EERR THEM 2110
1290 BOARO\$=0 : ADDR% = 7
1300 RETURN

```

The state of the current supply (heating/off/cooling) is indicated by the screen background color (red/green/blue) and by text displayed when the power supply control function is executed.

1400 Change display background color to correspond to heater setting
1410 IF HEAT \(=1\) THEM COLOR 14, 4, 4
1420 IF HEAT \(=0\) THEM COLOR 14, 2, 2
1430 IF HEAT \(=-1\) THEM COLOR 14, 3, 3
1440 IF PREVIOUSMEAT © MEAT TMEN PREVIOUSHEAT FHEAT : PRIMT "Change in setting"
1450 IF HEAT=1 THEM PRIMT ©Heater turned on wi
1460 IF HEAT \(=0\) THEM PRINT meating/Cooling turned off ":
1470 IF HEAT \(=-1\) THEM PRIMT "cooling turned on ":
1480 cosub 2410 - display temperature bar graph
1490 сого 300 • next measurement cycle
This routine can generated simulated temperature fluctuations for test purposes.

1500 . simulate temperature fluctuations .- only used for program testing
1510 IMCR=IMCR+.5*MEAT : IF HEAT \(=0\) THEM IMCR=0
1520 AVETEMP \(=\) SIM (T/100)*SPAN +INCR
1530 RETURM
\(1540{ }^{\circ}\)
1550 •

\section*{This subroutine analyzes the Interface Bus status and displays the result on the screen.}
```

1600 0
1610 PRIMT wStatus Word is m: ACTIVES;IBSTA% : X=IBSTA% : IF IBSTAK=0 THEM 1770
1620 'IF IBSTAZ aND EERR THEM 237
1630 IF IBSTAZ AND I THEN PRIMT MGPIB-PC is in DEVICE CLEAR statem
1640 IF IBSTAZ AND 2 THEN PRIMT "GPIB-PC is in DEVICE TRIGGER state"
1650 IF IBSTAX AND 4 THEM PRINT *GPIB-PC is LISTENER"
1660 IF IBSTAX AND 8 THEN PRIMT "GPIB-PC is TALKER`1670 IF IBSTAZ NNO 16 THEM PRIMT mATTENTION is asserted" 1680 IF IBSTAZ ANO }32\mathrm{ THEN PRINT MGPIB-PC is CICM 1690 IF IBSTAZ AND 64 THEM PRINT NGPIB-PC is in REMOTE state" 1700 IF IBSTAK ANO 128 THEM PRINT "GPIB-PC is in LOCKOUT state" 1710 IF IBSTAK AND 256 THEM PRINT MI/O is completedm 1720 IF IBSTAX AND 2068 THEN PRIMT mevice requesting service" 1730 IF IBSTAZ AND 4096 THEM PRINT "SERVICE REQUEST (SRQ) bit on" 1740 If IBSTAX AND }8192\mathrm{ TMEM PRIMT`GPIB-PC detected END or EOS*
1750 IF IBSTAX AND 16384 THEN PRIMT Mrime limit exceeded"

```

1760 If ibstaz and eerr then print acsis errorm : beEp
1770 RETURM
\(1780^{\circ}\)
Routines to pause the program in case of malfunction or other program errors. If the temperature measuring systems fails, the power supply is turned off. The interface bus is reset, and the program pauses waiting for an input from the keyboard. This provides and opportunity to reset (turn off/on) the INSTRULAB system before continuing the program. Gimilarly, if the power supply does not respond to commands via the bus, the program pauses and waits for an input from the keyboard. For other types of errors, the error number (see GW Basic Manual) and program line on which the error was detected are displayed. The first five errors on the list are ignored.

1800 .
1810 ownem mon Errore Rourtine
1820 If ERR= 189 TMEM 2110 -Power Supply malfunction
1830 IF ERR< 188 THEM 2210 'Analyze status word or print error type
1840 PRIMT TIMES, DATES : COSUB 1600
1850 T1= TIMER
1860 T2 - TIMER : WHILE \(12<19+2\) : COTO 1860 : WEMD : COTO 1980 '2 s delay
1900 intor IMSTRULAB malfunction; shut down power supply
1910 COSUB 1920 : COTO 1980 ' Reset bus
1920 RINT mResetting Systemi: IBSTAK=0
1930 ADDRESSLISTX ( 0 ) \(=\) ADORX
1940 ADDRESSLISTY (1) \(=\) PADDRZ
1950 ADDRESSLISTY (2) \(=\) MONDDR
1960 CALL RESETSYS (80ARD\%, ADDRESSLISTK (0))
1970 OW ERROR COTO 1810 : RETURK
1980 CONTROLUORDS=M400000": COLOR 14, 2, 2 : COSUB 1220 'set power supply to zero
2000 - Thermometer system error
2010 PR : : BEEP : PRINT DATES, TIMES; "* ERROR \# : PRINT : PRINT
2020 PR」AT ©
2030 PRINT - * Reset imstrulab thermometer system *n

2050 PRIMT \({ }^{2}\) Hit EMTER key to continuem : IMPUT X : COTO 180 'restart
2060 •
2100 Power supply failure
2110 PRIMT : BEEP : PRINT OATES, TIMES; * ERROR** PRINT : PRINT
2120 PRINT"
2130 PRINT" \#EEPCO Pover Supply not responding *
2140 PRINT"
2150 COSUB 1600 : COSUS 1920 : PRINT MHit EMTER key to contimuem : IMPUT X : COTO 180 'restart
\(2160{ }^{\circ}\)
2200 other types of error

2220 ERMMH=ERMMN+1 : IF ERMMM < 5 THEM RESUME MEXT : COSUS 1920 : COTO 180 Reset system, start over
2230 PRINT "To reset system hit EMTER key : IMPUT X : COTO 170
2300 ・あtw Display routines
2310 CLS : VIEU PRIMT • set up for bar graph display
2320 SETPOINT \(=25\) : IAVETEMP \(=10\)
2330 REFTEMP \(=\) SETPOIMT \(+(R M D * 10)-5: R T=1 N T(R E F T E M P+.5):\) AVETEMP \(=R H D * 50:\) COSUB 2400 display temperature bar graph 2340 RETURM
subroutine to display the average oil-bath temperature and reference temperature in bar-graph format. The bar graphs have the following features:
- To achieve better resolution, the zero temperature point is offset to the left and is not shown.
- An arrow at the top of the screen marks the set Point
- The top horizontal bar indicates the average oil temperature; changes in temperature are differentiated with color (red for increases, blue for decreases). The trend is also indicated by an arrow at the end of the bar.
- The lower bar represents the Reference Temperature with an arrow at the end of the bar indicating the direction of change.
- An arrow below the two bars indicates the average measured temperature for emphasis.
- Numerical values of temperature are displayed on the left-hand side of the graph.
- The text color changes from yellow to white when the average temperature is within \(\pm 0.1\). C of the setpoint.

2400 ०
2410 DEF FMTEMP (TEMP) \(=1\) MT (TEMP .5 )- 25
2620 IF ABS(AVETEMP-SETPOIMT) \(>=1\) THEN 2440
2630 DEF FMTEMP (TEMP) \(=1\) IT ( \((T E M P-S E T P O I M T) * 10+.5)\)
2460 A \(=\) FNTEMP (AVETEMP) \(+25: 1 A=F W T E M P(I A V E T E M P)+25: ~ R T=F N T E M P(R E F T E M P)+25: S P=F N T E M P(S E T P O I N T)+2 S\)
2450 IF \(A<0\) THEM \(A=0\)
2460 If IA \(<0\) THEN \(1 A=0\)
2470 IF RTSO TMEM RT=0
2480 TI= TIMER
2490 T2 = TIMER : MHILE T2 < T1 \(+2:\) COTO \(2490:\) HEND \(\cdot 2 \mathrm{~s}\) delay
2500 CLS : VIEW PRINT 1 TO 20
2510 COLOR 14, 0 : LOCATE 1 , SETPOIMT+7 : PRIMTMSET POINT ल;CHRS(25)
2520 COLOR 0, 0 : LOCATE 4, \(1: \$=1: X=1: Y=80:\) COSUB 2800
2530 IF ( \(A\)-I \(A\) ) < 0 TMEN COLOR 11, 4 ELSE COLOR 14, 4

2550 COLOR 0, \(0:\) LOCATE 2, \(17: S=1: x=1: Y=64:\) GOSUB 2800
2560 IF IMT(AVETEMP*1000) \(<=\) IMT(IAVETEMP*1000) THEN 2590
2570 COLOR 14, 0 : LOCATE 2, \(17: S=1: x=1: Y=1 A:\) COSUB 2800
2580 COLOR 12, \(0:\) LOCATE 2, 17 \(+1 A: S=1: X=1 A: Y=A-1\) : GOSUS 2800 : PRINT CHRS(8) + CMRS(26): GOTO 2610
2590 COLOR 14, 0 : LOCATE 2, \(17: S=1: X=1: Y=A:\) COSUB 2800
2600 COLOR 11, 0 : LOCATE 2, 17+A : PRIMT CHRS(8)+CMRS(27)
2610 COLOR 11, 0 : LOCATE 2, 18+A: \(s=1: x=A+2: y=1 A\) : COSUB 2800

2630 COLOR 0, 0 : LOCATE 3, \(17: S=1: x=1: Y=67\) : COSUB 2800
2640 IF SPAN > 0 THEM ARROWS=CHRS(26) ELSE ARROUS=CMRS(27)
2650 COLOR 13, 0 : LOCATE 3. 17 : \(S \pm 1: ~ X=1\) : \(Y=R T\) : COSUB 2800 : PRIMT CHRS(8): : PRINT ARRONS
2660 COLOR 0, 0 : LOCATE 4, \(1: s=1: x=1: y=80\) : COSUB 2800
2670 IF ABS(AVETEMP-SETPOINT)>. 1 THEM 2690

2690 COLOR 14, 0 : LOCATE 4. A+5 : PRIMT MTEMPERATUREN+CHRS(32)+CHRS(24)
2700 IAVETEMP =AVETEMP

2710 if MEAT=1 then COLOR 14, 4, 4 ELSE IF MEATm then COLOR 14, 2, 2 ELSE COLOR 14, 3, 3 2720 VIEU PRINT
\(2730{ }^{\circ}\) COLCR 14, 2, 2 : LOCATE 6, 17 : PRIKTM0123456789012345678901234567890123456789012345678901234567890123^ 2740 TI= TIMER
2750 T2 = TIMER : WHILE \(22<\) T1+5 : COTO 2750 : WEMD is a delay to read ber graph
2760 CLS : VIEU PRINT 'restore screen
2770 RETURN
Subroutine to draw bars on the graph


\section*{Appendix C}

\section*{CONTROL PROGRAM FOR THE DIGITAL VOLTMETER}

Appendix C contains as listing of the program that controls the operation of the digital voltmeter through a IEEE-488 interface bus and calculates the ratio of the voltages measured. The program was written Raymond S. Turgel in Hewlett-Packard BASIC (Model 85 Version). The program is interactive and requires entry of the date, terminals of the divider to which the voltmeter is connected separated by forward slashes, e.g., \(1 \mathrm{~K} / 100 / 0(1 \mathrm{kV}, 100 \mathrm{~V}\), and 0 V\()\), and the position of the selector switch ( \(+\mathrm{A},-\mathrm{A},+\mathrm{B}\), and -B ). The digital voltmeter is programmed to measure sets of ten readings during ten periods of the power-line frequency and calculate the highest reading, lowest reading and standard deviation of the set.

The computer screen displays all ten readings, the standard deviation, the peak-to-peak deviation (in ppm ), and the lowest standard deviation recorded on previous runs of the same measurement. If the standard deviation is less than 1106 , and the ratio between the highest and lowest reading differs by not more than 2 106, the average reading is recorded automatically. Otherwise, more sets of readings are taken. On "noisy" readings, where the standard deviation always exceeds 1106 , the operator can override the decision to take more readings by pressing K 1 or K 2 . K 1 will record the average of a set of previous readings with the lowest standard deviation. K2 records the latest set of readings taken. After readings corresponding to all four positions of the selector switch have been taken (in any desired order), the ratio is computed and printed on the tape of the built-in printer. The program then asks for the parameters of the next test point.

Digital Voltmeter Control Program
```

4 ! FILE "DVM RA"
5 ! REVISED JŪNE 8, 1994
10 ON ERROR GOTO 240
15 ON TIMEOUT 7 GOTO 5000 @ SET TIMEOUT 7;2000
20 DIM V (10),Al(2,2)
22 RO$="2 M RESISTORS"
28 V$=" "
30 N=10 @ Fl=0 @ F2=0 @ F3=0 @ F4=0 @ X$="1" @ Y$="0" @ Z$="00000" @ Tl=1 @ T2=2
5 @ Cl=0
35 S2=-1 @ M2=0
36 DISP "ENTER DATE" @ INPUT D3$
37 IF D3$<>"" THEN D9$=D3\$
40 ! Set up Voltmeter
45 DISP "VOLTAGE TERMINALS" @ DISP V\$ @ INPUT V1$@ IF V1$<>"" THEN V$=V1$
46 DISP "Enter TIME and TEMPERATURE" @ INPUT T1$,H$
47 F$=CHR$(171)\&CHR$(193)&CHR$(173)\&CHR$(193)&CHR$(171)\&CHR$(194)&CHR$(173)\&CHR\$
(194)
4 9 ~ I F ~ C l ~ T H E N ~ C L E A R ~
50 IF Cl THEN CLEAR
51 DISP "ENTER SWITCH POSITION (+A,-A;+B,-B)" @ DISP "Choose any underlined swit
ch position "
52 DISP " "\&F\$ @ INPUT S\$
55 S2=-1 @ Cl=0
56 CLEAR
6 0 ~ I F ~ S \$ = " + A " ~ T H E N ~ F l = 1 ~ @ ~ I l = 1 ~ @ ~ I 2 = 1 ~ @ ~ G O T O ~ 8 0
6 1 IF S\$="-A" THEN F2=1 @ Il=2 @ I2=1 @ GOTO 80
6 2 ~ I F ~ S \$ = " + B " ~ T H E N ~ F 3 = 1 ~ @ ~ I l = 1 ~ @ ~ I 2 = 2 ~ @ ~ G O T O ~ 8 0
6 3 ~ I F ~ S \$ = " - B " ~ T H E N ~ F 4 = 1 ~ @ ~ I l = 2 ~ @ ~ I 2 = 2 ~ @ ~ G O T O ~ 8 0
70 DISP "ENTRY ERROR" @ GOTO 50
80 ! Set up voltmeter
81 ON KEY\# 1,"ACTUAL" GOTO 3000
82 ON KEY\# 2,"LOWEST" GOTO 4000
83 ON KEY\# 5,"ACCEPT" GOTO 87
8 4 ~ I F ~ C l ~ T H E N ~ K E Y ~ L A B E L ~
87 F=2*(2*(I2-1)+I1) @ F$[F-1,F]=S$[1,1]\&CHR$(NUM(S$[2,2])+32)
88 OUTPUT 722 ;"PRESET NORM"
90 OUTPUT 722 ;"NRDGS 10 "
100 OUTPUT }722\mathrm{ ;"NPLC 10"
110 OUTPUT 722 ;"MATH STAT"
120 ! ENTER 722; V(1),V(2),V(3),V(4),V(5),V(6),V(7),V(8),V(9),V(10)
121 FOR I=1 TO 10 @ ENTER 722 ; V(I)@ NEXT I
130 OUTPUT 722 ;"RMATH SDEV"
140 ENTER 722 ; S1
150 OUTPUT 722 ;"RMATH UPPER"
160 ENTER 722 ; U
170 OUTPUT 722 ;"RMATH LOWER"
180 ENTER 722 ; L
190 M=0 @ FOR I=1 TO 10 @ DISP V(I);S\$ @ M=M+V(I) @ NEXT I
195 IF ABS(S1)<S2 OR S2=-1 THEN S2=S1 @ M2=M/N
200 DISP USING 201 ; ABS(S1*1000000),S2*1000000

```
```

Digital Voltmeter Control Program

```
201 IMAGE "sd=",DDDDDZ.D,10X,DDDDDZ.D/
202 IMAGÉ "p-p=",DDDDDZ.D
205 DISP USING 202 ; ABS(U/L-1)*1000000
210 A=12 MOD 2 @ \(B=(12+1)\) MOD 2 @ IF \(A B S(S 1 * 1000000)>T 1\) THEN KEY LABEL @ C1=1 @
GOTO 80 ELSE C1=0
220 IF ABS ( (U/L-1)*1000000) CT 2 THEN 80
230 GOSUB 1000 @ GOSUB 2000 @ GOTO 50
240 DISP "ERROR";ERRL;ERRN @ PAUSE
245 IF ERRN \(=2\) THEN 60
250 END
\(1000 \mathrm{Ml}=\mathrm{M} / \mathrm{N}\)
\(1010 \mathrm{Al}(\mathrm{I} 1, \mathrm{I} 2)=\mathrm{Ml}\)
1020 RETURN
```

2000! Calculate Averages
2001 IF F1*F2*F3*F4=0 THEN RETURN
2002 PRINT @ PRINT "INPUT ";Al(1,1) @ PRINT " ";Al(2,1)
2 0 0 3 ~ P R I N T ~ " O U T P U T ~ " ; A l ( 1 , 2 ) ~ @ ~ P R I N T ~ " ~ " ; A l ( 2 , 2 )
2015 PRINT @ PRINT "TERMINALS= ";V\$ @ PRINT T1$;" ";H$ @ PRINT
2017 PRINT D9$;" ";RO$
2020 PRINT USING 2025; (Al(1,1)-Al(2,1))/2
2025 IMAGE "REFERENCE VOLTAGE = ",DDZ.DDDDDD
2030 PRINT USING 2035 ; (Al(1,2)-Al(2,2))/2
2035 IMAGE "DIVIDER VOLTAGE = ",DDZ.DDDDDD
2040 PRINT USING 2045 ; (Al(1,1)-Al(2,1))/(Al(1,2)-Al(2,2))
2045 IMAGE "MEASURED RATIO= ",DDZ.DDDDDD
2050 IMAGE /"DEVIATION OF THE ACTUAL RATIO FROM THE NOMINAL ",SDDDDZ.DD,X,"ppm
|
2055 GOSUB 6000
2060 PRINT USING 2050 ; (ABS((Al(1,1)-Al(2,1))/(A1(1,2)-A1(2,2)))*N1-1)*1000000
2061 CLEAR @ DISP USING 2050 ; (ABS((A1(1,2)-Al(2,2))/(Al(1,1)-Al(2,1)))/N1-1)*1
000000
2070 PRINT @ DISP V\$ @ DISP
2080 PAUSE @ GOTO 30
2090 RETURN

```
3000 PRINT "OVERRIDE"
3010 PRINT "SETTINGS: ";V\$;" ";S\$
3020 PRINT "STD DEV MAX-MIN(ppm)"
3030 PRINT USING "2(DDDDDZ.D,X)" ; ABS(S1*1000000),ABS(U/L-1)*1000000
3040 GOTO 230
3060 GOTO 230
```

4000 PRINT USING 4010 ; S2*1000000,V$,S$
4010 IMAGE /"MIN STD DEV=",SDDDDZ.DD,"ppm"/"SETTING ",20A,X,2A
4020 Al(I1,I2)=M2
4030 GOSUB 2000 @ GOTO 50
5000 ABORTIO 7 @ CLEAR 7 @ RESET 7
5010 DISP "TIMEOUT"
5050 GOTO 50
6000 J1=1 @ Kl=0 ! Calculate nominal ratio
6001 FOR J=1 TO LEN(V$)
6 0 0 2 ~ I F ~ V \$ [ J , J ] < > " / " ~ T H E N ~ 6 0 1 0 ~
6003 Kl=Kl+1
6004 V2$=V$[J1,J-1] @ Jl=J+1
6005 V2(K1)=VAL(V2$) @ IF V2$[LEN(V2$),LEN(V2$)]="K" THEN V2(K1)=V2(K1)*1000
6 0 1 0 ~ N E X T ~ J ~
6020 V2$=V$[J1,LEN(V$)]
6030 Kl=Kl+1
6040 V2(K1)=VAL(V2$) @ IF V2$[LEN(V2$),LEN(V2$)]="K" THEN V2(K1)=V2(K1)*1000
6060 N1=(V2(2)-V2(3))/(V2(1)-V2(3))
6 0 6 6 RETURN

```

9999 END

To run QUME printer from HP Model 85
1. Use Serial Interface andspecial cable
2. Type 'CONTROL 10,\(3 ; 15 '\)
3. Type 'PRINTER IS 10,80 '

Any PRINT statement will then be printed onthe QUME printer
4. To change back to the Model 85 printer, type 'PRINTER IS 2'

\section*{Appendix D}

\section*{CALIBRATION OF THE DIGITAL VOLTMETER AGAINST A JOSEPHSON ARRAY STANDARD}

The data for the calibration of the digital voltmeter was obtained from R. L. Steiner of the Electricity Division, Electronics and Electrical Engineering Laboratory. The method used is described in the literature. \({ }^{8}\)

8 R. L. Steiner, R. J. Astalos,"Improvements for Automating Voltage Calibrations Using a \(10-\mathrm{V}\) Josephson Array," IEEE Trans. Instrum. \& Meas., Vol. IM-40, No. 2, April 1991.
\begin{tabular}{|c|c|c|c|c|c|}
\hline DUM & Calib & ation & Jose & ertson & -ay \\
\hline File & 0920806016 & Aug 1992 10: & :48:49 D & DUM_HP 545190 & HP3458 \\
\hline Pt \# & Voltage array (Volts) & DUM voltage (Volts) & St Dev (microv) & DUM-Array Lin (ppm) & ity Dev (ppm) \\
\hline 1 & +0.00000000 & +.000000286 & +.090 & 0 -.005 & -. 005 \\
\hline 2 & +1.00003458 & +1.000035049 & +.030 & 0 +. 013 & +.006 \\
\hline 3 & +2.00006917 & +2.000069782 & \(+.103\) & \(3+.028\) & +.015 \\
\hline 4 & +3.00040721 & +3.000408073 & +.084 & \(4+.053\) & +.033 \\
\hline 5 & +4.00044179 & +4.000442718 & +. 119 & \(9+.059\) & +.033 \\
\hline 6 & +5.00077983 & +5.000780890 & +0.000 & 0 +.072 & +.040 \\
\hline 7 & +6.00066269 & +6.000663940 & +. 138 & 8 +.091 & +.052 \\
\hline 8 & +6.99978691 & +6.999788086 & +0.000 & 0 +.084 & +. 038 \\
\hline 9 & +7.99982149 & +7.999822705 & +. 258 & 8 +.087 & +.035 \\
\hline 10 & +9.00000780 & +9.000009058 & +. 238 & 8 +.092 & +. 033 \\
\hline 11 & +9.99989065 & +9.999891651 & +. 138 & 8 +.065 & +0.000 \\
\hline 12 & +0.00000000 & +.000000369 & +. 120 & 0 +.003 & +.003 \\
\hline 13 & -1.00018631 & -1.000186332 & +. 135 & \(5-.036\) & +.017 \\
\hline 14 & -2.00052435 & -2.000524693 & +.091 & \(1-.068\) & +.037 \\
\hline 15 & -3.00040721 & -3.000407993 & +.097 & \(7-.112\) & +. 045 \\
\hline 16 & -4.00059352 & -4.000594787 & +. 119 & \(9-.160\) & +. 049 \\
\hline 17 & -5.00062810 & -5.000629726 & +. 138 & 8 -. 196 & +. 066 \\
\hline 18 & -6.00005578 & -6.000057932 & +0.000 & - -. 249 & +.065 \\
\hline 19 & -6.99993864 & -6.999941303 & +. 097 & \(7-.300\) & +. 066 \\
\hline 20 & -8.00012495 & -8.000128337 & +. 275 & \(5-.373\) & +.047 \\
\hline 21 & -9.00000780 & -9.000011502 & +0.000 & 0 -. 403 & +.068 \\
\hline 22 & -10.00019412 & -10.000199020 & +. 138 & 8 -. 524 & +0.000 \\
\hline 23 & +0.00000000 & +.000000356 & +.113 & \(3 \quad+.002\) & +.002 \\
\hline
\end{tabular}
DUM slope ( + ) \(=+1.000000065 \quad\) DUM slope \(\{-\) ) \(=+1.000000524\)
Measurement offset \(=\quad+.337\) microvolts
Number of points \(=23 \quad\) Frequency \(=73.374999996 \mathrm{~Hz}\)

St. Dev. of Zero Pt. \(=0.0000\) ppm Elapsed Time \(=00: 14: 05\)


DUM Calibration by Josephson Array
File D92080602 6 Aug 1992 11:40:22 DUM_HP 545190 HP3458 Pt \# Voltage array DUM voltage St Dev DUM-Array Linearity Dev (Volts) (Volts) (microU) (ppm) (ppm)
\begin{tabular}{|c|c|c|c|c|c|}
\hline 1 & +0.00000000 & +.000000163 & +. 058 & -.001 & -. 001 \\
\hline 2 & +. 50009316 & +. 500093465 & +. 068 & \(+.013\) & +.007 \\
\hline 3 & +1.00003458 & +1.000034915 & +.038 & +.015 & +.002 \\
\hline 4 & +1.50012774 & +1.500128299 & +. 106 & +.038 & +. 018 \\
\hline 5 & +2.00022090 & +2.000221399 & +0.000 & +.033 & +.006 \\
\hline 6 & +2.50046578 & +2.500466352 & +. 109 & +. 040 & +.007 \\
\hline 7 & +3.00055893 & +3.000559716 & +.049 & +.060 & +.021 \\
\hline 8 & +3.50034864 & +3.500349438 & +.069 & +.063 & +.818 \\
\hline 9 & +4.00044179 & +4.000442669 & +.069 & +.070 & \(\because 017\) \\
\hline 10 & +4.50068667 & +4.500687658 & +.069 & +.081 & +.021 \\
\hline 11 & +5.00062810 & +5.000628878 & +. 119 & \(+.060\) & -. 006 \\
\hline 12 & +5.50072126 & +5.500722259 & +. 154 & +.082 & +. 010 \\
\hline 13 & +6.00005578 & +6.000057070 & \(+.138\) & +. 112 & +.032 \\
\hline 14 & +6.49984548 & +6.499846480 & +0.000 & +.082 & -. 003 \\
\hline 15 & +6.99993864 & +6.999939729 & +. 169 & +.092 & -. 001 \\
\hline 16 & +7.50003179 & +7.500032860 & +. 169 & +.089 & -. 010 \\
\hline 17 & +8.00012495 & +8.000126105 & +. 138 & +.098 & -. 007 \\
\hline 18 & +8.49991465 & +8.499916301 & +. 238 & +. 148 & +.036 \\
\hline 19 & +9.00015953 & +9.000160837 & +. 195 & +. 113 & -. 006 \\
\hline 20 & +9.50010096 & +9.500101890 & +. 195 & +. 075 & -. 050 \\
\hline 21 & +10.00004239 & +10.000043882 & +. 238 & +. 132 & +0.000 \\
\hline 22 & +0.00000000 & +.000000149 & +.094 & -. 003 & -.003 \\
\hline 23 & -. 50009316 & -. 500093091 & +.053 & -. 011 & +.815 \\
\hline 24 & -1.00018631 & -1.000186551 & +. 034 & -. 042 & +.811 \\
\hline 25 & -1.50027947 & -1.500279906 & +.049 & -. 061 & +.017 \\
\hline 26 & -2.00037262 & -2.000373367 & +. 119 & -. 092 & +. 812 \\
\hline 27 & -2.50031405 & -2.500314819 & +.091 & -. 094 & +.036 \\
\hline 28 & -3.00040721 & -3.000408376 & \(+.109\) & -. 134 & +.022 \\
\hline 29 & -3.50050036 & -3.500501841 & +. 119 & -. 165 & +. 017 \\
\hline 30 & -4.00044179 & -4.000443531 & +.097 & -. 191 & +.017 \\
\hline 31 & -4.50053495 & -4.500537044 & +. 097 & -. 227 & \(+.007\) \\
\hline 32 & -5.00062810 & -5.000630416 & +. 138 & -. 249 & +. 012 \\
\hline 33 & -5.50072126 & -5.500723617 & +. 097 & -. 253 & +.033 \\
\hline 34 & -6.00005578 & -6.000058015 & +. 169 & -. 241 & +. 071 \\
\hline 35 & -6.50014893 & -6.500151748 & +. 097 & -. 299 & +. 040 \\
\hline 36 & -7.00024209 & -7.000244958 & \(+.138\) & -. 304 & +.060 \\
\hline 37 & -7.49988006 & -7.499883204 & +.097 & -. 332 & +. 059 \\
\hline 38 & -8.00012495 & -8.000128509 & \(+.138\) & -. 374 & +. 043 \\
\hline 39 & -8.49991465 & -8.499918517 & +. 138 & -. 404 & +.038 \\
\hline 40 & -8.99985608 & -8.999860198 & +. 308 & -. 430 & +.039 \\
\hline 41 & -9.49994923 & -9.499953579 & \(+.238\) & -. 452 & +.042 \\
\hline 42 & -10.00019412 & -10.000199147 & \(+0.000\) & -. 521 & \(+0.000\) \\
\hline 43 & +0.00000000 & +.000000215 & +.051 & +.004 & +.004 \\
\hline
\end{tabular}

DUM slope \((+)=+1.000000132 \quad\) DUM slope \((-)=+1.000000521\)
Measurement offset \(=\quad+.176\) microVolts
Number of points= \(43 \quad\) Frequency \(=73.374999986 \mathrm{~Hz}\)
St. Dev. of Zero Pt. = 0.0000 ppm Elapsed Time \(=00: 27: 27\)


Fig. 1 Circuit Diagram (except for guard circult) of 10 kV Ratio Standard

Fig. 2(a) Diagram Showing Transition to Keivin-Variey Divider
```


[^0]:    C. B. Childers, R. F. Dziuba, L. H. Lee, "A Resistive Ratio Standard for Measuring Direct Voltages to 10 kV," IEEE Transactions on Instrumentation and Measurements, IM-25, No. 4, December 1976.

[^1]:    2 The calibration of the digital voltmeter against a Josephson Array were carried out by Richard Steiner of NIST. The calibration data are included in Appendix C.

[^2]:    3 Throughout this report, commercial instruments are identified by manufacturer and model number only to describe the experiment. This does not imply an endorsement by the National Institute of Standards and Technology, nor does it imply that the equipment mentioned is necessarily the best available for the purpose.

[^3]:    4 An annotated listing of the BASIC program is given in Appendix B.

[^4]:    5 Commercial instruments are identified by manufacturer and model number only to describe the experiment and do not imply an endorsement by the National Institute of Standards and Technology, nor does it imply that the equipment mentioned is necessarily the best available for the purpose.
    C. B. Childers, R. F. Dziuba, L. H. Lee, "A Resistive Ratio Standard for Measuring Direct Voltages to 10 kV ," IEEE Trans. Instrum. \& Meas., Vol IM-25, No. 4, December 1976.

