Research for Electric Energy Systems - An Annual Report

William E. Anderson
Editor

U.S. DEPARTMENT OF COMMERCE
National Institute of Standards
and Technology
Electronics and Electrical Engineering
Laboratory
Electricity Division
Gaithersburg, MD 20899

Prepared for
Department of Energy
Division of Electric Energy Systems
1000 Independence Avenue, SW
Washington, DC 20585
Research for Electric Energy Systems - An Annual Report

William E. Anderson
Editor

U.S. DEPARTMENT OF COMMERCE
National Institute of Standards and Technology
Electronics and Electrical Engineering Laboratory
Gaithersburg, MD 20899

Prepared for
Department of Energy
Division of Electric Energy Systems
1000 Independence Avenue, SW
Washington, DC 20585

December 1990

Issued June 1991

U.S. DEPARTMENT OF COMMERCE
Robert A. Mosbacher, Secretary
NATIONAL INSTITUTE OF STANDARDS AND TECHNOLOGY
John W. Lyons, Director
This report summarizes the progress of four technical investigations conducted during CY 90. Although reasonable efforts have been made to ensure the reliability of the data presented, it must be emphasized that this is an interim progress report and that further experimentation and analysis may be performed before the conclusions from any of these investigations are formally published. It is therefore possible that some of the observations presented in this report will be modified, expanded, or clarified by our subsequent research.\(^1\)

\(^1\)The identification of commercial materials and their sources is made to describe the experiment adequately. In no case does this identification imply recommendation by the National Institute of Standards and Technology, nor does it imply that the product is the best available.
# Table of Contents

1 ELECTRIC FIELD MEASUREMENTS ........................................... 1
    1.1 Introduction .................................................. 1
    1.2 Examination of Experimental Designs for In Vitro Studies Using ELF Magnetic Fields ............................................. 2
    1.3 Experimental Geometry and Exposure Parameters .............. 2
        1.3.1 Rectangular Geometry .................................... 4
        1.3.2 Cylindrical Geometry: Magnetic Field Perpendicular to Axis .... 6
        1.3.3 Cylindrical Geometry: Magnetic Field Parallel to Axis .... 8
    1.4 Magnetic Fields from Parallel Plates .......................... 11

2 GASEOUS DIELECTRICS RESEARCH ..................................... 16
    2.1 Introduction .................................................. 16
    2.2 Detection of Trace $S_2F_{10}$ in $SF_6$ ......................... 17
        2.2.1 Measurement System ..................................... 18
        2.2.2 Data Acquisition and Analysis ............................ 19
        2.2.3 GC-MS Results and Calibration ............................ 20
        2.2.4 Mass-Spectrometric Investigation of $S_2F_{10}$ Pyrolysis .... 24
        2.2.5 Gas-phase Impurities ..................................... 30
        2.2.6 Reference Sample Stability ............................... 31
    2.3 Stochastic Properties of Pulsating Partial Discharges ....... 33
        2.3.1 Basic Considerations ..................................... 33
        2.3.2 Measurement System ..................................... 37
        2.3.3 Examples of Results from Investigation of Trichel Pulses ... 39
        2.3.4 Influence of a Dielectric Barrier on the Stochastic Behavior of Trichel-Pulse Corona ...................................... 46
        2.3.5 Limitations and Extensions of the SAPP Technique ........ 58

3 LIQUID DIELECTRICS RESEARCH .................................... 60
    3.1 Introduction .................................................. 60
    3.2 Streamer Initiation in Hexanes .................................. 61
        3.2.1 Apparatus and Procedure .................................. 61
        3.2.2 Results and Discussion .................................... 62
    3.3 DC Voltage Conditions .......................................... 69
        3.3.1 Experimental Apparatus ................................... 69
        3.3.2 Partial Discharge Records ................................. 69
    3.4 Conclusions .................................................... 72

4 FAST TRANSIENT MEASUREMENTS .................................... 73
    4.1 Introduction .................................................. 73
4.2 Resistive Voltage Divider Design ........................................ 74
  4.2.1 General Considerations ............................................ 74
  4.2.2 Configuration and Construction .................................. 75
4.3 The Unit Step Response (USR) and Its Application ................. 80
  4.3.1 Step Response Measurement ....................................... 80
  4.3.2 Convolution Calculation .......................................... 84
4.4 Conclusion ...................................................................... 88
Research for Electric Energy Systems – An Annual Report

William E. Anderson, Editor

Abstract

This report documents the technical progress in the four investigations which make up the project “Support of Research Projects for Electrical Energy Systems”, Department of Energy Task Order Number 137, funded by the U.S. Department of Energy and performed by the Electricity Division of the National Institute of Standards and Technology (NIST). The first investigation is concerned with the measurement of magnetic fields in support of epidemiological and in vitro studies of biological field effects. NIST cohosted a workshop on exposure and biological parameters that should be considered during in vitro studies with extremely low frequency (ELF) magnetic and electric fields. Additionally, equations were developed to predict the magnetic field in a parallel plate magnetic field exposure system. An IEEE standard prepared at NIST on measuring dc electric fields and ion related parameters was approved and published. Various site visits were made to characterize the electric and magnetic fields in biological exposure systems. The second investigation is concerned with two different activities: the detection of trace levels of $S_2F_{10}$ in $SF_6$ and the development of an improved stochastic analyzer for pulsating phenomena (SAPP). The detection of $S_2F_{10}$ in the presence of $SF_6$ using mass-spectrometric detection coupled to a gas chromatograph is difficult because of the similar mass spectra. Enrichment techniques, capable of sub parts per billion (ppb) detection in the case where the background gas is not $SF_6$, are unsuitable for this application. A technique is described that enables the detection of $S_2F_{10}$ in gaseous $SF_6$ down to the ppb level using a modified gas chromatograph-mass spectrometer. The SAPP has been improved to allow direct real-time measurements of conditional pulse-amplitude distributions of higher order than was previously possible. The new system was applied to an investigation of the stochastic behavior of negative corona (Trichel pulses) and the effect of a dielectric barrier on these discharges. The third investigation is concerned with breakdown and prebreakdown phenomena in liquid dielectrics. The activity reported here was a study of negative streamers preceding electric breakdown in hexanes. Using the image preserving optical delay, the growth of the streamers associated with partial discharges at a point cathode are photographed at high magnification. Simultaneous discharge current measurements enables a detailed description of the temporal and spatial
development of streamers and provide a basis for the evaluation of models for the initiation of negative streamers. The last investigation is concerned with the evaluation and improvement of methods for measuring fast transients in electrical power systems such as might be associated with an electromagnetic impulse. The new draft of IEC-60 recommends the use of an independent reference measurement system to verify the performance of the impulse voltage measuring system under test. A compact resistive divider, NIST4, was designed for this purpose. It is anticipated that this divider together with some Kerr electro-optical devices will be used as the reference system at NIST. The design details of NIST4 and its measurement capabilities are presented.
1 ELECTRIC FIELD MEASUREMENTS

Task 01
Martin Misakian
Electricity Division
National Institute of Standards and Technology

1.1 Introduction

The objectives of this project are to develop methods to evaluate and calibrate instruments which are used, or are being developed, to characterize the electrical parameters in the vicinity of power lines and in laboratory apparatus designed to simulate the power line environment. Electrical measurement support is also provided for the Department of Energy funded efforts to determine if there are biological effects due to ac fields and dc fields with ions.

During 1990, NIST organized and cohosted with Battelle Pacific Northwest Laboratories (BPNL) a workshop on exposure and biological parameters that should be considered during in vitro studies with extremely low frequency (ELF) magnetic and electric fields. The workshop was an outgrowth of discussions with BPNL following an NIST conference presentation late in 1989. It was evident at that time that all of the relevant exposure parameters during many in vitro bioeffect studies with ELF magnetic fields were not being adequately characterized. The NIST contribution to the workshop considered the electric field and current density distributions induced in culture medium. A portion of the workshop presentation is reproduced below. Also a related NIST paper describing an optimum experimental configuration for in vitro studies with ELF magnetic fields was published [1].

In addition efforts were also made to develop equations that would predict the magnetic field in a parallel plate magnetic field exposure system similar in principle to one developed at BPNL [2]. The results of the calculations are described below.

Other events and activities related to the NIST Fields Project during 1990 included (a) the approval and publication of an IEEE standard which provides guidance for measuring dc electric fields and ion related parameters (IEEE Std 1227-1990, IEEE Guide for the Measurement of DC Electric-Field Strength and Ion Related Quantities; draft standard prepared at NIST in collaboration with members of IEEE DC Fields and Ions Working Group), and (b) consultations with the Food and Drug Administration (electric and magnetic field measurements near electric blankets), the National Toxicology Program (experimental design and exposure parameters for rodent study with magnetic fields), and the Environmental Protection Agency (reviews of draft reports). NIST also coauthored two working group papers in the IEEE Power Engineering Society related to characterizing power line magnetic fields.
Both papers are scheduled for publication in the IEEE Transactions on Power Delivery in early 1991. Site visits were made to Southwest Research Institute on behalf of DOE and to the University of Rochester and BPNL on behalf of EPRI, during which electric and magnetic fields were characterized in biological exposure systems and calibration apparatus. Preliminary measurements of power frequency magnetic fields in and near the NIST-Boulder daycare facility were performed. The measurements were coupled with model calculations to better characterize the sources of magnetic fields.

NIST serves on advisory panels for the California Department of Health Services and the National Cancer Institute (NCI), and review panels for the National Institutes of Health (NIH). During 1990, NIST participated in meetings of the NCI and NIH panels.

1.2 Examination of Experimental Designs for In Vitro Studies Using ELF Magnetic Fields

There have been many laboratory studies since the mid 1970's examining the possibility of biological effects to cells in vitro due to power frequency magnetic fields. These studies have typically used Helmholtz coils to produce an approximately uniform magnetic field for exposure purposes. Significantly, the enclosures containing the cells and liquid growth medium have varied in shape and size. Because the geometry of the liquid volume, which is determined by the enclosure, has a major impact on the exposure parameters, the enclosure must be considered as an important part of the exposure system. This portion of the report examines the exposure parameters for several experimental configurations that have been used during in vitro studies and notes some of their advantages and limitations. The numerous biological constraints that must be considered for the different configurations will be the subject of a future report. Extensive use is made of the equations developed by McLeod et al. [3] for determining the current density and electric field induced in the liquid growth medium by the magnetic field.

1.3 Experimental Geometry and Exposure Parameters

In vitro studies with power frequency magnetic fields have often been conducted using circular plastic or glass petri dishes and rectangularly shaped vessels as the enclosures. When the enclosure containing the liquid and biological cells is introduced into the magnetic field, an electric field and an associated current are induced in the liquid by the time-varying magnetic field. Thus, the cells are exposed to three candidate parameters that may individually, or in combination, cause a biological effect, i.e., the magnetic field or flux density, $B$, the induced electric field strength, $E$, and the induced current density, $J$. While all the cells will experience essentially the same
1.3 Experimental Geometry and Exposure Parameters

magnetic field, the exposure to $E$ and $J$ will depend on the size and shape of the liquid volume, the direction of the magnetic field with respect to the liquid volume, and the location of the cell in the liquid volume.

We consider the three experimental configurations shown in figure 1a: a cylindrical liquid volume with the power frequency magnetic field parallel and perpendicular to the cylinder axis (figure 1a and 1c) and a rectangular liquid volume with the magnetic field perpendicular to one of the faces (figure 1b). It should be noted that the direction and magnitude of any dc magnetic field may be of significance if tests of a resonance model are being conducted. However such experiments are not considered here. As qualitatively indicated in figure 1, the induced electric field lines and current paths are circular when the magnetic field is parallel to the cylinder axis. In general, the electric field lines and current paths form noncircular loops for the remaining two cases. The equations for the induced current density and electric field are simplest when the magnetic field is parallel to the cylinder axis. Then the current density is given by [3]

\[
J = \sigma \pi f B_r \\
E = \pi f B_r
\]

Figure 1. Experimental configurations for in vitro studies with ELF magnetic fields.
where \( \sigma \) is the conductivity, \( f \) is the frequency and \( r \) is the radial distance from the cylinder axis. Because the current density is equal to the product \( \sigma E \), the electric field strength is just

\[
E = J/\sigma = \pi f Br.
\]

The expressions for the induced current density in the rectangular volume are more complicated and are given by [1]

\[
J_y \approx i \frac{\omega \sigma B2a}{\pi^2} \sum_{n=\text{odd}} \frac{4}{n^2} \left( \pm \cos \frac{n\pi y}{2a} \right) \left( \sinh \frac{n\pi z}{2a} \right) \left( \cosh \frac{n\pi h}{2a} \right),
\]

and

\[
J_z \approx -i \frac{\omega \sigma B2h}{\pi^2} \sum_{m=\text{odd}} \frac{4}{m^2} \left( \pm \cos \frac{m\pi z}{2h} \right) \left( \sinh \frac{m\pi y}{2h} \right) \left( \cosh \frac{m\pi a}{2h} \right),
\]

where \( 2a \) is the width of the liquid volume, \( 2h \) is the depth, and \( \omega \) is \( 2\pi \) times the frequency, \( f \). The \( \pm \) sign indicates that the terms in the summation are alternatively added and subtracted. As above, the corresponding expressions for the electric field are found by dividing equations (3) and (4) by the conductivity, \( \sigma \). As shown by McLeod et al. [3], the case of the cylindrical volume with the magnetic field perpendicular to the cylinder axis can be treated by cutting the cylinder into approximately rectangular volumes as shown in figure 1c and using equations (3) and (4) for each rectangular volume. The rectangular geometry is examined first.

1.3.1 Rectangular Geometry

With the rectangular configuration shown in figure 1b, it can be shown, using equations (3) and (4), that the induced current and electric field vanish along the x-axis as well as along the four edges parallel to the x-axis. The maximum values of the induced electric field and current density occur at the liquid boundary but the locations depend on the cross sectional shape of the volume. The cells will all experience the same magnetic field because the magnetic field is uniform throughout the liquid volume. However, the electric field and current density experienced by the cells will vary from zero to some maximum value depending on the location of the
cell. If the approximate region the cells occupied during exposure to the magnetic field were known, their exposure to a more limited range of $E$ and $J$ values could be determined using equations (3) and (4). Such information is, in general, not known when experiments are conducted with cells in suspension.

Our ability to describe the exposure conditions for the cells improves if the cells can be cultured on the bottom surface of the enclosure. Then the vertical components of $E$ and $J$ vanish and approximately uniform values of $E$ and $J$ in the horizontal direction can be produced along the bottom surface of the liquid if the liquid depth is small compared to the width, i.e., $2h \ll 2a$. Figure 2a shows normalized values of $E$ or $J$ calculated at the bottom surface of the liquid volume for $2a = 6$ cm and $2h = 0.2$ cm. It can be seen for this example that the region of approximately uniform $E$ or $J$ extends almost to the side edges where $E$ and $J$ rapidly decrease to zero. Increasing the depth of the liquid by 1 mm decreases the uniformity, but because the liquid depth, $2h$, is still much smaller than the side dimension, $2a$, the

Figure 2. Normalized values and directions of $E$ or $J$ along bottom surface of culture medium when $B$ is parallel to x-axis (a) culture medium is 2 mm deep (b) culture medium is 3 mm deep.
uniformity is still very good as shown in figure 2b. While the 1 mm difference in depth has had a small effect on the uniformity of $E$ and $J$ in this example, the increase in magnitude of $E$ and $J$ is not insignificant, amounting to 50% over most of the area. This sensitivity of $E$ and $J$ to liquid depth for the rectangular configuration may be an important consideration when attempts are made to replicate the results of an earlier in vitro study.

It should also be noted that cells cultured on the bottom surface of the enclosure will experience an "uneven" exposure to the approximately uniform $E$ and $J$ values described above because a portion of the underside of the cell, which is in contact with plastic or glass, will not be exposed to the electric field or current density in the liquid. This problem can be reduced if the cells can be cultured in agar that has the same conductivity as the liquid. However, the use of agar can introduce undesirable biological effects [4] and cause significant changes in the exposure conditions. For example, if liquid 2 mm deep covers a layer of agar 2 mm thick on the bottom of a rectangular enclosure 3 cm wide, and if cells are cultured near the upper surface of the agar, they will experience little or no exposure to $E$ or $J$ except near the side edges.

Summarizing the above discussion, the rectangular configuration allows for the exposure of large numbers of cells to uniform values of $B$, $E$, and $J$ if they are cultured on the bottom surface of the enclosure. The values of $E$ and $J$ are sensitive to liquid depth and can be calculated using equations (3) and (4). The equations for determining $E$ and $J$ are not elementary, but can be readily evaluated with a computer. The use of agar can significantly influence the exposure parameters and also have biological consequences.

1.3.2 Cylindrical Geometry: Magnetic Field Perpendicular to Axis

As noted earlier, the case of a cylindrical liquid volume with the magnetic field perpendicular to the cylindrical axis can be treated by imagining the cylinder being cut into rectangular sections and using the theory for rectangular geometry. Thus, the above remarks regarding the characterization of exposure conditions for cells in suspension and cells cultured on the bottom of the enclosure again apply to each section. Figure 3 shows normalized values of $E$ and $J$ at the bottom surface of a liquid volume 6 cm in diameter and 0.2 cm deep. The uniformity is again seen to be very good over most of the surface area and is a consequence of the fact that $2h$ is still much smaller than the width of the imaginary sections at most locations. As for the examples considered in figure 2, the magnitude of $E$ or $J$ is sensitive to the liquid depth.
1.3 Experimental Geometry and Exposure Parameters

Normalized E, J Values at Bottom of Cylindrical Volume of Liquid

\[ B \perp \text{to axis} \]
\[ \text{diameter} = 6 \text{ cm} \]
\[ 2h = 0.2 \text{ cm} \]

Figure 3. Normalized values and directions of \( E \) and \( J \) along bottom surface of culture medium when \( B \) is parallel to \( x \)-axis.
1.3.3 Cylindrical Geometry: Magnetic Field Parallel to Axis

When the magnetic field is parallel to a cylindrical volume, the problem of describing the exposure conditions for the cells becomes more simple. The equations describing $E$ and $J$ (equations (1) and (2)) are elementary and indicate that both $E$ and $J$ increase linearly with radial distance from the cylinder axis. As noted earlier, the electric field lines and current density form concentric circular loops and are thus more easily visualized than for the rectangular geometry. Significantly, equations (1) and (2) indicate that $E$ and $J$ are independent of liquid or agar depth.

Figure 4 shows normalized $E$ and $J$ values for a cylindrical volume 6 cm in diameter. While the lack of uniformity of these exposure parameters may at first seem to be a disadvantage when characterizing cell exposure, it is possible to make use of the nonuniformity to obtain several ranges of exposure to $E$ and $J$ during the same experimental run [1]. For example, cells can be segregated into annular sections with circular walls and the range of $E$ and $J$ values experienced by the cells in each section can be determined from equations (1) and (2) and the radii that define the section. The exposure geometry and design of an enclosure that would be suitable for short term studies with cells in suspension are shown in figure 5.

While the cylindrical volume in figure 5 has been partitioned into three sections, more or fewer sections could be used. For more extended periods of exposure, lasting as
Figure 5. Experimental design for short term in vitro studies with cells in suspension.
long as six or seven days, the enclosure can be fitted with a cap and “sealed” with commercially available laboratory film which prevents significant evaporation but allows adequate air exchange [5]. Vertical stacking of the enclosures is one technique for increasing the number of cells that are exposed during a single experimental run. Introducing a layer of agar at the bottom of the enclosure as shown in figure 5 provides for a more uniform exposure of the cells (top and underside) to $E$ and $J$. Unlike the rectangular geometry case, introduction of the agar will not affect the values of $E$ and $J$ because $E$ and $J$ are independent of liquid or agar depth. However, use of agar can have significant biological effects as noted previously.

If the circular walls shown in figure 5 introduce an impediment for cells plated directly on the enclosure surface, it may be possible to replace the walls with painted concentric circles on the underside of the enclosure as shown in figure 6.

Other techniques for characterizing the radial positions of the cells in the cylindrical enclosure include growing the cells on a glass cover slip placed in the enclosure (the cover slip can be removed later for measurements with a rule and compass) or indicating the annular regions on a flat surface, as shown in figure 7, upon which the enclosure is placed.

Because of the spatial uniformity of $B$ and the readily determined variation of $E$ and $J$ with position in the enclosure, the experimental configuration described in this section can be used to investigate directly questions regarding the relative significance of interaction mechanisms involving the magnetic field and/or induced electric field and current density. For example, the observation of a biological effect at the same level in all sections of the enclosure would suggest a mechanism involving direct magnetic interaction, whereas an effect that differed between sections could be indicative of a mechanism involving the induced electric field and magnetic field combination. For the latter case, a single experiment could provide data for a range of $E$ or $J$ exposure levels.

Figure 6. Method for characterizing radial positions of cells.
1.4 Magnetic Fields from Parallel Plates

Annular regions indicated with circles painted in well

Form with shallow well for petri dish

Figure 7. Method for characterizing radial positions of cells.

Summarizing this section, the cylindrical configuration with the magnetic field parallel to the cylinder axis results in induced electric fields and current densities that are easily visualized, and elementary equations for calculating $E$ and $J$ that are independent of liquid depth. In addition, the amount of information pertaining to dose-response during a single experimental run can be maximized, and it may be possible to distinguish between a purely magnetic field bioeffect and a bioeffect that involves the electric field or current density-magnetic field combination. The configuration in this section does not permit exposure of large numbers of cells to the same $E$ and $J$ values. The use of agar does not have a significant effect on $E$ and $J$ values, but can have biological effects as noted earlier.

1.4 Magnetic Fields from Parallel Plates

Magnetic fields for ELF bioeffect studies have typically been produced with solenoids, Helmholtz coils, or rectangular coils with a common axis. Because stray fields from such coil systems can extend to considerable distances and because of the difficulty in shielding sham exposed animals or cells from these fields, it is of interest to consider an experimental apparatus recently reported by Miller et al. [2], that has low stray fields. Figure 8 shows a schematic view of the apparatus which consists, in part, of three stacked parallel plates. The ac current in the central plate divides equally between the upper and lower plates and produces a magnetic field parallel to the plates in each half of the apparatus as shown schematically in figure 8 at some instant. Because the fields in the two sections are in opposite directions, stray fields from the apparatus decrease more rapidly than the field from either section alone. This section describes attempts to theoretically describe the magnetic field for a similar parallel plate apparatus.
Figure 8. Schematic view of parallel plate apparatus (after Ref. 2) showing direction of ac current at some instant and direction of magnetic field between parallel plates.

Figure 9. Half-section view of current distribution in flat conductor that changes in width by a factor of four.

Efforts to calculate the field for the apparatus shown in figure 8 are complicated by the nonuniformity of the current density at the points of connection between the plates and the electrodes that provide current. Figure 9 shows how the current distribution departs from uniformity when a single connecting electrode is one-fourth as wide as the plate [6].

The nonuniformity of the current density due to connections of metal of uneven widths can be overcome by the modification shown in figure 10. The electrodes providing current to the plates are expanded in width to match the parallel plates and the shape has been changed to resemble two rectangular solenoids. Attempts were made to determine the magnetic field theoretically by applying the law of Biot-Savart to just the upper half of the arrangement as shown in figure 11. Because of the quasistatic nature of the field, it was assumed that the time dependence of the magnetic field

Figure 10. Modified parallel plate apparatus.
1.4 Magnetic Fields from Parallel Plates

Figure 11. Geometry and coordinates for upper half of parallel plate exposure apparatus. The law of Biot-Savart takes the form of a double integral (example shown above) and is applied to all surfaces of the apparatus.

could be predicted by multiplying the dc magnetic field (obtained from the law of Biot-Savart) by a \( \sin \omega t \) term.

Figure 12 shows comparisons of measured horizontal magnetic field profiles at frequencies of 25 Hz and 1 kHz in a rectangular apparatus as shown in figure 11 with dimensions of 50 cm \( \times \) 50 cm \( \times \) 10 cm side dimension. The measurements were performed with a miniature coil probe 5.7 mm long and 4.4 mm in diameter. Agreement is fair at 25 Hz and poor at 1 kHz. At 60 Hz, the magnetic field is about 3.5\% less than the dc value at the center of the apparatus. The departure from the dc theory is due to a skin effect [7] which causes the current to concentrate along the edges of the plate as shown schematically in figure 13.

The concentration results because of the larger inductance (and correspondingly increased impedance) along a central path through the plates. It is noted that even with nonuniform current distributions, regions of approximately uniform magnetic field can be obtained between the parallel plates with an apparatus similar to that shown in figure 8 [2]. The field magnitude and uniformity must be determined by measurement, however.

The problems with current nonuniformity (including the skin effect) can be overcome by replacing the metal plates with two adjacent rectangular solenoids as shown in figure 14.
Figure 12. Horizontal magnetic field profiles midway between top and bottom plates of parallel plate apparatus 50 cm x 50 cm x 10 cm spacing. Magnetic field values for dc, 25 Hz, and 1 kHz frequencies are indicated.

Figure 13. Edge-on view of plate showing increased current density concentration at edges of plate.

Figure 14. Arrangement of “coupled” rectangular solenoids to reduce stray magnetic fields.
The fields in each section as well as the stray fields from the "coupled" arrangement can be calculated using equations for rectangular loops of wire [8] and the principle of superposition. The design shown in figure 14 eliminates significant skin effects and requires less current than the plates to produce the same field because of the many turns of wire. As for the parallel plate arrangement, the stray field from the "coupled" rectangular solenoids will decrease faster than either solenoid alone.
2 GASEOUS DIELECTRICS RESEARCH

Task 02
Richard J. Van Brunt and James K. Olthoff
Electricity Division

John T. Herron
Chemical Kinetics Division
National Institute of Standards and Technology

Sanjay V. Kulkarni
Guest Scientist
Plasma Research Institute, India

Vishnu K. Lakdawala
Guest Scientist
Old Dominion University, Norfolk, VA

2.1 Introduction

The objectives of this project are the development of measurement capabilities and the providing of fundamental data as part of the Department of Energy’s basic research concerned with the development and evaluation of advanced compressed-gas-insulation technology.

To reduce space requirements and improve the efficiency of high-voltage transmission systems, the electric power industry has turned toward more extensive use of compressed-gas insulation. To design meaningful tests of system performance and establish specifications for the quality of materials used in such systems, more information is needed about the fundamental physical and chemical processes which lead to insulation deterioration and electrical breakdown. The research includes applications of gas chromatography-mass spectrometry to characterize corona discharge by-products; and the acquisition of fundamental data, such as, reaction-rate coefficients, corona-inception voltages, production rates of corona by-products, the effects of contaminants on discharge initiation, and the rates of discharge-induced decomposition of the gas.

This section of the report highlights the progress of research in two areas. The first is concerned with the development of a sensitive method for detecting trace levels of disulfur decafluoride (S$_2$F$_{10}$) in sulfur hexafluoride (SF$_6$) by gas chromatography mass spectrometry. The second area of research has to do with development of an improved stochastic analyzer for pulsating phenomena (SAPP) and its application to the investigation of negative-corona discharge pulses in gases.
2.2 Detection of Trace $S_2F_{10}$ in $SF_6$

The work on $S_2F_{10}$ detection was carried out in collaboration with scientists at the Oak Ridge National Laboratory and results have already been reported in one archival [9] and two conference papers [10, 11]. The work on stochastic behavior of corona pulses involved participation by guest scientists from the Plasma Research Institute of India and Old Dominion University. Results from the latter investigation have appeared in one archival [12] and two conference papers [13, 14]. Three other archival papers covering different aspects of this work have also recently been submitted for publication [15-17].

2.2 Detection of Trace $S_2F_{10}$ in $SF_6$

The ability to detect gaseous disulfur decafluoride ($S_2F_{10}$) at trace levels in sulfur hexafluoride ($SF_6$) has become of interest because of its known high level of toxicity [18-22] and because of recent measurements [23, 24] and calculations [25, 26] which show that $S_2F_{10}$ can be produced during electrical-discharge activity in $SF_6$. The concern about $S_2F_{10}$ production in $SF_6$ stems in part from the increasingly wide spread use of $SF_6$ as a gaseous dielectric in high-voltage electric-power transmission systems. The Occupational Safety and Health Administration (OSHA) has recently set peak exposure limits (PEL) for $S_2F_{10}$ at 10 ppb [27]. However, due to the difficulty of detecting low concentrations of $S_2F_{10}$ in $SF_6$, enforcement of the PEL has been stayed until the development of suitable detection techniques.

There are previous preliminary reports by Janssen [28, 29] of having achieved a detection sensitivity for $S_2F_{10}$ in helium gas of 0.04 ppb by using a gas chromatograph equipped with an electron capture detector. In order to achieve this level of sensitivity, however, it was necessary to employ a complex $S_2F_{10}$ enrichment procedure requiring long analysis times (~ 45 minutes). When $SF_6$ is a major constituent of the gas in which $S_2F_{10}$ is to be detected, the sensitivity for $S_2F_{10}$ detection drops dramatically (to > 10 ppb) despite the enrichment process. This drop in sensitivity is a consequence of increased background signal in the detector output due to the favorable electron attaching properties of the residual $SF_6$ which interferes with the $S_2F_{10}$ signal. Reduced sensitivity for $S_2F_{10}$ detection in the presence of $SF_6$ also occurs when flame photometric detectors [28] or thermal conductivity detectors [11] are used.

Mass-spectrometric detection, when coupled to a gas chromatograph, suffers from the specific limitation that $S_2F_{10}$ has a positive-ion mass spectrum which is very similar to that of $SF_6$, especially at the standard electron-impact energy of 70 eV [29, 30, 31]. For electron-impact energies greater than 20 eV, all of the significant ions that appear in the $S_2F_{10}$ mass spectrum also appear in the $SF_6$ spectrum. Thus, even when chromatographic separation of $S_2F_{10}$ from $SF_6$ is used, ions from $SF_6$ can sufficiently increase the background level to interfere with $S_2F_{10}$ detection. Recent claims [32] of using a mass spectrometer operated at low electron-impact energies to detect trace levels of $S_2F_{10}$ in $SF_6$ have been disputed [31].
A new method is described here in which a gas chromatograph-mass spectrometer (GC-MS) system is easily modified to allow detection of S$_2$F$_{10}$ in gaseous SF$_6$ down to the ppb level without the necessity of a complex and time-consuming pre-enrichment procedure. With this method, a fraction of the S$_2$F$_{10}$ is converted to thionyl fluoride (SOF$_2$) in a heated jet-separator at the interface between the GC and MS. Because the major ions that appear in the 70-eV mass spectrum of SOF$_2$ differ from those in the SF$_6$ spectrum, interference of SF$_6$ with the S$_2$F$_{10}$ peaks in single-ion chromatograms can be avoided. Elimination of the enrichment step significantly reduces the gas analysis time and improves the reliability of the detection method.

2.2.1 Measurement System

The analytical method proposed for sensitive detection of S$_2$F$_{10}$ in SF$_6$ utilizes a GC-MS with a heated metal tube on the lower-pressure side of the interface between the GC and MS. As shown in figure 15, a jet separator serves as the heated metal tube in the GC-MS system used to obtain the results presented here. The jet separator is a standard design consisting of a stainless steel tube of 8 cm length and 5 mm diameter which is heated to a temperature of about 180°C. As discussed later, a fraction of the S$_2$F$_{10}$ undergoes thermal decomposition in the heated tube and converts to SOF$_2$ via surface-catalyzed wall reactions with H$_2$O. The SOF$_2$ can then be detected by the mass spectrometer without interference by the ion signals from SF$_6$. The efficiency of the conversion is not known but appears, from experiments discussed below, to depend on the length, shape, and temperature of the heated surface upon which conversion takes place. The conversion efficiency is most sensitive to the tube temperature and relatively insensitive to details of the tube geometry and material composition. A high sensitivity for S$_2$F$_{10}$ detection is obtainable with a wide range of heated inlet tube configurations.
2.2 Detection of Trace $S_2F_{10}$ in $SF_6$

The GC-MS system used for the experiments presented here is a Hewlett Packard\textsuperscript{1} 5992A with a Hewlett Packard jet separation inlet. In this particular instrument the jet separator is heated by the diffusion pump heater. For other systems the conversional region may be heated externally. The GC column is similar to that described by Hanrahan and Patterson\textsuperscript{33}, namely a 24' × 1/8'' Teflon tube containing 30% SP-2100 (Supelco) on 80/100 chromosorb WAW. The column was operated using helium as a carrier gas (20–30 ml/min. flow rate) which had not been predried. The GC oven temperature was maintained between 25 and 50 °C and the sample injections were made using a gas-tight syringe. Detection sensitivities for $S_2F_{10}$ in $SF_6$ of nearly 1 ppb were obtainable using the instrument described above.

Pure $S_2F_{10}$ samples, synthesized at Clemson University, were provided to us as liquid under its own vapor pressure (~ 600 torr at room temperature) in 30 ml stainless steel cylinders. Identity and purity of the sample were established by IR spectroscopy and GC-MS analysis. Gas-phase reference mixtures were prepared immediately prior to use, either by injection or needle valve, in argon (99.999 %) or $SF_6$ (99.99 %) in a stainless steel vacuum manifold housed in a vented hood. The argon and $SF_6$ were not dried before use.

2.2.2 Data Acquisition and Analysis

Data acquisition was performed using the manufacturer-supplied software and analysis was performed using software developed in-house. For $S_2F_{10}$ samples in buffer gases other than $SF_6$, trace amounts of $S_2F_{10}$ could be detected by single ion monitoring of $SF_2^+$, $SF^+_2$, $SF^+_3$, $SF^+_4$ and $F^+$ ($m/z = 127, 108, 89, 70, and 19$) produced by direct ionization of $S_2F_{10}$\textsuperscript{31}. When mixed with $SF_6$, sensitive $S_2F_{10}$ detection required the monitoring of ion signals characteristic of the $SOF_2$ produced by surface conversion in the heated inlet tube mentioned above. These ions include $SOF^+_3$, $SOF^+_4$, or $SO^+$ ($m/z = 86, 67$, and 48). For the data presented here, as many as 8 ions could be monitored at a given time with dwell times ranging from 10 to 200 ms.

The response of the GC-MS to $S_2F_{10}$ is defined here to be the area under the peak identified with this species in a chromatogram. This area was computed from the GC-MS data by numerical integration after performing a background subtraction. No attempts were made to “smooth” or average data and unless specified, the data presented here corresponds to chromatograms from single sample injections. Retention time was measured from the time of sample injection.

\textsuperscript{1}The identification of commercial materials and their sources is made to describe the experiment adequately. In no case does this identification imply recommendation by the National Institute of Standards and Technology, nor does it imply that the product is the best available.
GASEOUS DIELECTRICS RESEARCH

Figure 16. Chromatograms of representative ion signals due to ions from direct ionization of $S_2F_{10}$ and from ionization of surface conversion products for a 500 ppm sample of $S_2F_{10}$ in 100 kPa argon buffer gas.

2.2.3 GC-MS Results and Calibration

When a gas sample containing $S_2F_{10}$ is injected into the column of the GC-MS in which the interface is heated, the conversion of $S_2F_{10}$ into SOF$_2$ discussed in the next section becomes evident from single-ion chromatograms at $m/z = 43, 67,$ and $86$ (SO$^+$, SOF$^+$, and SOF$_2^+$). Examples of such chromatograms are shown in figure 16 for a 500 ppm sample of $S_2F_{10}$ in argon. Ions produced by direct ionization of $S_2F_{10}$ are observed (F$^+$ and SF$^+_2$) as are ions from SOF$_2$ produced by surface conversion (SOF$_2^+$ and SO$^+$).

The $m/z = 20$ chromatogram in figure 16 also exhibits a peak at the retention time characteristic for $S_2F_{10}$, thus indicating that HF is also a by-product of $S_2F_{10}$ decomposition in the heated tube. This peak, however, exhibits structure which can be accounted for by interference from HF originally present as a contaminant in the sample mixture. Analysis of dilute HF mixtures showed that HF has nearly the same
2.2 Detection of Trace $S_2F_{10}$ in $SF_6$

Figure 17. Single ion chromatograms of a 660 ppb $S_2F_{10}$ sample in 200 kPa argon buffer gas.

retention time as $S_2F_{10}$ for the column conditions used here. Thus, although HF may be formed by thermal decomposition of $S_2F_{10}$ in the heated gas inlet tube, it cannot, by itself, be relied upon to give an unambiguous indication of $S_2F_{10}$.

For the results shown in figure 16, ions due to direct ionization of $S_2F_{10}$ are observable because no $SF_6$ was present in the sample. However, in the presence of $SF_6$, $S_2F_{10}$ signals in the single-ion chromatograms at $m/z = 19$ and 127 are obscured by the $SF_6$ contribution to the signal at these masses. This is demonstrated by data presented in figure 17 from a gas sample containing 660 ppb $S_2F_{10}$ in $SF_6$. These results show the effect of $SF_6$ in limiting the sensitivity for $S_2F_{10}$ detection when conventional mass-spectrometric monitoring is used, and clearly show the advantages of using the $S_2F_{10}$ conversion technique discussed here.

Figure 18 shows a chromatogram for $m/z = 86$ for an "unknown" $SF_6$ sample from a container in which the gas had been subjected to a weak electrical corona discharge. The discharge produced trace amounts of the oxyfluorides $SOF_2$, $SOF_4$, and $SO_2F_2$ in
Figure 18. Single ion chromatogram of an "unknown" sample of SF₆ that was partially decomposed in a dc corona discharge.
2.2 Detection of Trace $S_2F_{10}$ in $SF_6$

Figure 19. Detection response curves for various concentrations of $S_2F_{10}$ and SOF$_2$ in argon using a chromosorb GC column discussed in the text. Open symbols represent detection of $S_2F_{10}$ and SOF$_2$ by direct ionization, while closed symbols represent detection of $S_2F_{10}$ by ionization of SOF$_2$ produced by surface catalysis. The measured responses were normalized to the observed responses of a reference sample containing 750 ppm $S_2F_{10}$ and 750 ppm SOF$_2$ in argon. Similar response curves are obtained for samples diluted in SF$_6$.

addition to $S_2F_{10}$. It is seen that the retention times of the SOF$_2$ and SOF$_4$ produced by the discharge are much shorter than for $S_2F_{10}$ (2.1 and 2.3 minutes compared to 4.0 minutes). The oxyfluorides are known from previous work [34–36] to be the major gaseous by-products from decomposition of SF$_6$ in corona discharges when at least trace levels of oxygen and water vapor are present. The production of $S_2F_{10}$ in SF$_6$ electrical discharges has only recently been verified [23, 24].

Under the conditions used to obtain the data in figures 16 and 17, the response of the GC-MS was measured as a function of the $S_2F_{10}$ concentration in reference gas samples. Typical response curves obtained using known concentrations of $S_2F_{10}$ mixed with argon are shown in figure 19 for the indicated $m/z$ values. The $S_2F_{10}$ response is compared with that for SOF$_2$ which was also added to the mixture in known concentrations. The $S_2F_{10}$ response curves for $m/z = 48$ and 86, corresponding to the chemical conversion of $S_2F_{10}$ into SOF$_2$, are seen to be distinctly nonlinear. The deviation from linearity is greatest at the highest $S_2F_{10}$ concentrations and indicates a saturation effect possibly associated with depletion of H$_2$O from the heated jet separator tube surface during the conversion of $S_2F_{10}$ into SOF$_2$. By contrast, the $S_2F_{10}$ response curve for $m/z = 127$, corresponding to unreacted $S_2F_{10}$, is seen to be nearly linear over 5 orders of magnitude. Likewise the responses to SOF$_2$ originally present in the sample at $m/z = 48$ and 86 are also nearly linear. The small deviations
from linearity observed at low concentrations (< 200 ppb) may be attributable to uncertainties in the preparation of samples by successive dilutions.

The shape and slope of the response curves for the \( S_2F_{10} \) conversion process are quite reproducible for a given set of instrument operating conditions. Nevertheless, when attempting accurate measurements of \( S_2F_{10} \) concentrations in \( SF_6 \), frequent checks on the GC-MS calibration may be necessary and reference sample concentrations should ideally be as close to the unknown sample concentration as possible. The response of the present GC-MS system to \( S_2F_{10} \) was periodically checked and found to be stable for long periods of time (typically more than a day). When performing a quantitative analysis of \( S_2F_{10} \) content in \( SF_6 \), it is desirable to bracket the unknown sample injection with reference injections of comparable concentration.

It should be noted that although the response at high \( S_2F_{10} \) concentrations shows evidence of \( H_2O \) removal, the surface apparently recovers to its former condition in a relatively short time (\( \sim 5-10 \) min.) as indicated by responses from successive injections of samples at high concentrations (\( \sim 100 \) ppm). In general, the larger the quantity of \( S_2F_{10} \) injected, the longer the surface recovery time of the inlet tube. For samples containing less than 10 ppm \( S_2F_{10} \), the recovery time of the system used here was found to be less than the typical \( S_2F_{10} \) retention time of 4 min.

The limit of \( S_2F_{10} \) detection in \( SF_6 \) depends, of course, on the operating conditions of the GC-MS equipped with the heated inlet line. For the instrument used here, under conditions identical to those used to obtain the results shown in figures 16, 17 and 18, the limit of detection (signal-to-noise ratio = 2) was estimated to be about 2 ppb for a 2 ml injection at 200 kPa. Figure 20 shows an example of a result obtained for a 4 ppb mixture of \( S_2F_{10} \) in \( SF_6 \) which gives an indication of the limit of detection sensitivity for this instrument. The single-ion chromatogram at \( m/z = 56 \) is an average of data from four injections each with a volume of 2 ml at a total gas pressure of 200 kPa. The \( S_2F_{10} \) peak is statistically significant and is indicated by the vertical arrow. The presence of \( S_2F_{10} \) in \( SF_6 \) at the 10 ppb level (the PEL) gives a much larger peak than that shown in figure 20 and is easily detected using a single injection. If necessary, additional improvements in signal-to-noise ratios needed for higher sensitivity applications can be achieved through more signal processing, (i.e., averaging of results from more injections coupled with appropriate background subtraction) or using heated MS inlet-tube conditions that optimize the efficiency of \( S_2F_{10} \) conversion into \( SOF_2 \).

### 2.2.4 Mass-Spectrometric Investigation of \( S_2F_{10} \) Pyrolysis

In order to determine the optimum operating temperature range for the heated gas inlet tube and to better understand the thermal \( S_2F_{10} \) conversion mechanism discussed in the previous section, it was necessary to investigate the pyrolysis of \( S_2F_{10} \) on heated metal surfaces at low pressure and at different temperatures. The
Figure 20. Single ion chromatogram (ion 86) of 4 ppb S$_2$F$_{10}$ in 200 kPa SF$_6$. 
specific purposes of this investigation were to: 1) show evidence that it is surface chemistry that is involved in the \( \text{S}_2\text{F}_{10} \) conversion; 2) indicate the temperature range over which this conversion is effective; 3) demonstrate that \( \text{SF}_6 \) does not chemically decompose in this temperature range; and 4) provide an independent verification that \( \text{SOF}_2 \) is indeed one of the products of the \( \text{S}_2\text{F}_{10} \) conversion process.

An Extrel quadrupole mass spectrometer was used for these measurements, and the sample gas was admitted to the MS via a heated stainless steel bellows connected to a variable leak valve. The temperature of the bellows could be varied from 20 to 300°C and the mass spectra could be observed as a function of the temperature of the inlet system. The gas pressure in the bellows was estimated to be lower than 1 millitorr (~0.13 Pa) and the pressure in the MS ion-source was below \( 5 \times 10^{-5} \) torr.

Shown respectively in figures 21 and 22 are mass spectra obtained from mixtures of 1500 ppm \( \text{SF}_6 \) and 1500 ppm \( \text{S}_2\text{F}_{10} \) in argon for different temperatures of the inlet bellows. At 30°C, the mass spectra of \( \text{S}_2\text{F}_{10} \) and \( \text{SF}_6 \) are seen to be nearly identical in agreement with previously published data [30,31,37,38]. Other than minor differences in the relative intensities of the \( \text{SF}_x^+ \) ions \( (x=1-4) \), the only significant difference between the mass spectra of \( \text{S}_2\text{F}_{10} \) and \( \text{SF}_6 \) is the appearance of a peak at

---

**Figure 21.** Electron-impact mass spectra of 1500 ppm \( \text{SF}_6 \) in argon buffer gas at (a) 30°C and (b) 220°C.
2.2 Detection of Trace $S_2F_{10}$ in $SF_6$

Figure 22. Electron-impact mass spectra of 1500 ppm $S_2F_{10}$ in argon buffer gas at various temperatures.
$m/z = 54$ (SF$_4^{++}$) in the SF$_6$ spectrum which is not present in S$_2$F$_{10}$ spectrum. Peaks at masses 48, 64, 67, and 86 in the S$_2$F$_{10}$ spectrum at 30°C are due to small impurities of SO$_2$ and SOF$_2$ present in the S$_2$F$_{10}$ sample. At 220°C, the SF$_6$ mass spectrum remains essentially unchanged, indicating that SF$_6$ does not undergo a measurable chemical transformation in the heated inlet tube. The S$_2$F$_{10}$ spectrum, on the other hand, exhibits a significant change for temperatures above about 100°C. In going from 30°C to 200°C, the ratio of the SF$_5^+$ (m/z = 89) to SF$_5^-$ (m/z = 127) peaks in the S$_2$F$_{10}$ mass spectrum increases indicating conversion of S$_2$F$_{10}$ into SF$_3$ or SF$_5$. Peaks associated with SOF$_2$ at m/z = 48, 67, and 86 become more prominent above 100°C and dominate the spectrum at 270°C, indicating that S$_2$F$_{10}$ is nearly completely destroyed at this temperature with SOF$_2$ as the predominant stable by-product.

Tests performed using different inlet tubes appear to indicate that, at any given temperature, the conversion of S$_2$F$_{10}$ into SOF$_2$ becomes more efficient as the effective surface area encountered by the incoming gas is increased, e.g., a bellows gives a more complete conversion than a straight tube of the same length. This trend is consistent with chemical conversion via a surface catalyzed reaction. There are indications that some surface materials may be more effective than others in converting S$_2$F$_{10}$ to SOF$_2$, however, an extensive investigation appeared to be unwarranted in view of the relatively high efficiency achieved with commonly used stainless steel. Temperature and presence of adsorbed water appear to be more important than either surface configuration or composition.

The detailed mechanisms of S$_2$F$_{10}$ conversion to SOF$_2$ on heated surfaces are not presently known. It is speculated that the process involves thermally induced dissociation of S$_2$F$_{10}$ along the weak sulfur-sulfur bond followed by a fast reaction of SF$_3$ with H$_2$O adsorbed on the surface, i.e.,

$$S_2F_{10} \rightarrow SF_5 + SF_5$$

$$SF_5 + H_2O \rightarrow SOF_2 + 2HF + F.$$  

Previous work [39–41] has shown that S$_2$F$_{10}$ is thermally unstable in the gas phase at temperatures above 100°C. The thermal unimolecular gas-phase decomposition rate at high pressures [39] has a temperature ($T$) dependence given by:

$$k = 3 \times 10^{19}\exp(-46400/RT),$$  \hspace{1cm} (5)

which is based on reaction data [39] obtained in the temperature range 435–454.5 K ($RT$ is given in units of calories and $k$ in s$^{-1}$). Assuming this expression applies at room temperature, the half-life of S$_2$F$_{10}$ in the gas phase is predicted to be about 10$^7$ years. The half-life drops dramatically to 10$^2$ seconds at 475 K. However, the S$_2$F$_{10}$ decomposition rate implied by the present mass-spectrometric results is significantly higher than predicted by the above gas-phase rate and unlikely to apply at the low pressures typically encountered here in the heated inlet tube, further supporting the likelihood of a surface catalyzed reaction mechanism.
2.2 Detection of Trace \( S_2F_{10} \) in \( SF_6 \)

Figure 23. Signal intensity of several selected ions from a 1500 ppm \( S_2F_{10} \) sample in argon as a function of time as the inlet temperature is rapidly increased from room temperature to 270°C.

An indirect indication of the role of adsorbed water was obtained from measurements made with the quadrupole mass spectrometer under conditions where the inlet line temperature was allowed to rise relatively rapidly after the \( Ar/S_2F_{10} \) mixture was introduced. The mass spectra obtained in this way differ from those shown in figure 22 which correspond to equilibrated conditions achieved after keeping the inlet line at the indicated temperatures for many minutes. The results obtained from monitoring selected ions as a function of time under the “transient” conditions of continuous rising inlet-line temperature are shown in figure 23. Presented in this figure are time-dependent peak intensities for ions at \( m/z = 86 \) and 67 which are indicators of \( SOF_2 \); \( m/z = 127 \), indicator of \( S_2F_{10} \) and \( SF_6 \); and \( m/z = 89 \), indicator of \( S_2F_{10}, SF_6, \) and \( SF_4 \). Unlike the results given in figure 22, the yield of \( SOF_2 \) is seen to go through a maximum at a time of 6 minutes, which corresponds to a temperature of 160°C. The data for \( m/z = 127 \) indicate that \( S_2F_{10} \) is nearly completely decomposed at this temperature, i.e., the intensity for this ion ceases to decrease significantly beyond this temperature. The \( m/z = 127 \) signal that appears at higher temperatures is
undoubtedly associated with SF$_6$ which can be a product of S$_2$F$_{10}$ decomposition. As noted by Herron [41] (see also Ref. [42]), SF$_4$ and SF$_6$ can be formed in the gas phase by the disproportionation reaction

\[ \text{SF}_5 + \text{SF}_5 \rightarrow \text{SF}_4 + \text{SF}_6. \]

As the temperature increases, the $m/z = 89$ signal does not fall off quite as rapidly as the $m/z = 127$ signal, thus suggesting formation of SF$_4$ whose primary electron impact ion is SF$_3^+$. The increase in SOF$_2$ production with time can be attributed to an increase in the decomposition rate of S$_2$F$_{10}$ and an increase in the surface hydrolysis rate of the decomposition products as the surface temperature is increased. However, as the amount of water adsorbed on the surface decreases due to heating, the rate of S$_2$F$_{10}$ conversion into SOF$_2$ drops. It should be noted that at the highest temperatures the production of SOF$_2$ has decreased with no corresponding increase in any of the other compounds which are being monitored. This suggests that at high temperatures the S$_2$F$_{10}$ or its by-products are being converted into compounds which are presently unidentified.

Although there is evidence [43] that SOF$_2$ hydrolyzes slowly in the gas phase at 300 K and may react with H$_2$O on surfaces, little is known about its decomposition at higher temperatures. These results indicate that there is an optimum temperature range at which conversion of S$_2$F$_{10}$ into SOF$_2$ is most efficient. If the temperature is too low, the conversion rate is low, and if the temperature is too high, SOF$_2$ itself may be destroyed.

2.2.5 Gas-phase Impurities

It should be realized that if gaseous species are present in the unknown sample that could react with S$_2$F$_{10}$ or its decomposition products at temperatures above 150°C, uncertainties can be introduced in the quantitative analysis for S$_2$F$_{10}$ by the method proposed here if the reference sample does not also contain these species in nearly the same amounts. It is known [44–47] that S$_2$F$_{10}$ can react at high temperatures with numerous gases such as NO, NO$_2$, NO$_2$Cl, (CF$_3$)$_2$NONO, CH$_3$ONO, Fe(CO)$_5$, ICl, C$_6$H$_6$, C$_2$H$_4$, (CH$_3$)$_2$NH, BCl$_3$, and NH$_3$. If it is suspected that gases may be present in the unknown sample that can react with S$_2$F$_{10}$ at temperatures above 150°C, then care must be taken to assess the influence of these gases on the GC-MS response to S$_2$F$_{10}$. Ideally the reference sample should have the same, or nearly the same composition as the unknown sample. It was found here that the response of the GC-MS to S$_2$F$_{10}$ was not significantly influenced by the presence of the oxyfluorides SOF$_2$, SO$_2$F$_2$, and SOF$_4$ which are commonly formed together with S$_2$F$_{10}$ during decomposition or oxidation of SF$_6$.

Of particular importance is the presence of water vapor as a contaminant in a sample. The gas-phase water vapor present in the sample can affect the amount of adsorbed
2.2 Detection of Trace $S_2F_{10}$ in $SF_6$

water on the inlet tube surface at any given time and thus the $S_2F_{10}$ to SOF$_2$ conversion efficiency. Low water-vapor concentrations in gas samples did not show significant effects. However, it was observed that the addition of excessive amounts of water vapor to an $S_2F_{10}$ sample can noticeably decrease the amount of SOF$_2$ detected from $S_2F_{10}$ conversion at surface temperatures above about 120°C. This is not understood but may be due to mechanisms which either inhibit the conversion if gas-phase water is present, or increase the rate of SOF$_2$ decomposition (for example by hydrolysis [35]) at elevated temperatures. The reactivities of gas-phase $S_2F_{10}$ and SOF$_2$ toward water vapor at temperatures above 100°C are presently unknown and require more investigation.

2.2.6 Reference Sample Stability

Surface conversion of $S_2F_{10}$ into SOF$_2$ also occurs at room temperature, although at a much slower rate than observed at elevated temperatures. This decomposition raises questions about the long-term reliability of reference gas samples containing known amounts of $S_2F_{10}$ that are needed for calibration of the GC-MS. In order to assess the stability of $S_2F_{10}$ in reference samples, a series of tests were performed to monitor the content of $S_2F_{10}$-containing cylinders over relatively long periods of time. Preliminary reports of these tests have already been given [10, 24].

It was found that the rate of $S_2F_{10}$ decomposition depended on such factors as temperature, cylinder material and surface-to-volume ratio, and moisture content. Data indicating the temperature and moisture content dependencies of $S_2F_{10}$ decomposition in 150 ml stainless-steel cylinders are shown respectively in figures 24 and 25. Shown in these figures are measured $S_2F_{10}$ concentrations in argon as a function of time after mixture preparation. The measurements were performed using the GC-MS method described above, and the “aged” samples were compared with reference samples prepared immediately prior to the measurements. The “wet” sample (H$_2$O added) results in figure 25 were obtained from a sample prepared by injecting 1 μl of liquid water into the cylinder under vacuum prior to introducing the Ar/$S_2F_{10}$ gas mixture. The data presented in figures 24 and 25 clearly demonstrate that the $S_2F_{10}$ decomposition rate increases with increasing temperature and moisture content.

The products of the $S_2F_{10}$ decomposition were found to include SOF$_2$ and SF$_6$, and thus it is speculated that the decomposition process involves a surface catalyzed reaction with adsorbed H$_2$O that may be similar to that observed at higher temperatures in the heated MS gas inlet tube. The SOF$_2$ produced from $S_2F_{10}$ also appears to react slowly on the stainless-steel surface and convert to other products that have yet to be identified. Once $S_2F_{10}$ disappears from the gas, SOF$_2$ will also eventually disappear [38]. From analyses of the decomposed gas using MS and GC-MS, it has not been possible to account for all of the sulfur originally present in the
Figure 24. Low temperature dependence for decomposition of 500 ppm $S_2F_{10}$ samples in argon stored in 150 ml stainless steel cylinders.

Figure 25. Decomposition of $S_2F_{10}$ as a function of time for two 1400 ppm, $S_2F_{10}$ samples in 1 atm Ar in 150 ml stainless steel cylinders. For one sample (□), 1 µl of liquid water was injected into the cylinder prior to filling with gas.
S\textsubscript{2}F\textsubscript{10}. The only identified gaseous compound resulting from S\textsubscript{2}F\textsubscript{10} decomposition that contains sulfur and exhibits long-term stability is SF\textsubscript{6}. Generally, less than 15\% of the sulfur can be accounted for by this product.

On the basis of the tests that were conducted, long-term storage of S\textsubscript{2}F\textsubscript{10} reference samples in the gas phase cannot be recommended. It was found that samples stored under even the most favorable conditions exhibited significant decomposition over sufficiently long periods of time. It is recommended that reference samples be prepared immediately prior to gas analysis, under conditions that are as dry as possible, and in cylinders that are as large as possible.

Preliminary tests of commercial grade SF\textsubscript{6} (99.8\% purity) have indicated that S\textsubscript{2}F\textsubscript{10} does not readily decompose in SF\textsubscript{6}-filled cylinders when compressed into the liquid phase. Analysis showed that S\textsubscript{2}F\textsubscript{10} was present as an impurity at a level of about 40 ppb in a 12-year old sample. It should be noted that S\textsubscript{2}F\textsubscript{10} is a possible by-product from the commercial production of SF\textsubscript{6} and can be present as a trace liquid impurity in the liquified SF\textsubscript{6} which exists in pressurized cylinders. The results of analyzing SF\textsubscript{6} stored as a liquid suggest that significant improvements might be achieved in maintaining sample stability by compressing reference samples into the liquid phase.

2.3 Stochastic Properties of Pulsating Partial Discharges

2.3.1 Basic Considerations

Partial-discharge (P-D) measurements have long been recognized as an important part of quality control for high-voltage apparatus. There is also increasing interest in the use of P-D measurement as a diagnostic tool for assessing insulation performance and integrity when subjected to electrical and mechanical stress. The measurement of P-D’s has been applied to a wide range of electrical apparatus including rotating machines, power transformers, and both low- and high-voltage cables [48].

The P-D phenomenon under consideration here is a self-quenching discharge that is localized in regions of high electrical stress within insulating systems. The high-stress regions might, for example, be associated with voids or "trees" in solid dielectrics, metal particles or sharp points on either solid conductors or insulators, or the presence of interfaces between different types of insulating or conducting media. Partial discharges are self-quenching because the surface or space charge produced during the discharge activity generally accumulates and acts to reduce the local electric-field magnitude to a level below which the discharge can be sustained.

Because of its self-quenching nature, the P-D phenomena is inherently pulsating and will manifest itself as current pulses in the external circuit. Partial-discharge activity occurs in regions that are at least partially in the gas phase such as occlusions in solids or "bubbles" formed by vaporization of a liquid. The partial-discharge phenomena
that occur around conductors in air or other gases is often referred to as corona. It should be noted that corona discharges can, under some conditions, exhibit a non-pulsating characteristic for dc voltages which is associated with the formation of a steady glow region [49, 50]. Because this type of corona discharge is steady and therefore not self-quenching, it does not fit into the category of P-D phenomena under consideration here.

Partial discharges can be observed by electrical, optical, or acoustical measurements that detect and record pulses. The determination of P-D pulse characteristics has been the subject of numerous previous investigations [51]. Techniques have been developed to measure such parameters as mean P-D pulse amplitude and repetition rate [52], pulse-height distribution [53-55], pulse shapes [56], correlation of pulse amplitude with phase of an ac voltage [57, 59], and correlation between optical, electrical, or acoustical pulses. Because of the complex, stochastic nature of P-D phenomena, the results of such measurements have often been difficult, if not impossible, to interpret in terms of meaningful physical models. The measurement scheme discussed here is an extension of a technique previously used to provide more refined information about the statistical characteristics of P-D pulses. From the additional information acquired by this method, it is possible to gain more insight into the physical bases of the phenomena which might prove useful in the design of P-D measurement systems of the future.

Partial discharge phenomena fit into a category of stochastic processes for which memory effects play an important role. The existence of memory is an inherent property of P-D phenomena because the occurrence of a discharge pulse is associated with the formation of residual ion space-charge, surface charges, and excited metastable species which can affect the initiation and growth of subsequent discharge pulses. As mentioned above, the pulsating characteristic of P-D's in various types of insulating media can be attributed to effects of space or surface charges. When the accumulation of discharge-generated space or surface charge causes the field to fall below a level sufficient to sustain the discharge, it ceases. Another P-D pulse will not occur at this site until the local field is restored such as can result from charge migration or changes in applied voltage.

Because of memory effects, correlations may exist among successive discharge pulses and measurement of these correlations can provide useful information on the nature of P-D phenomena. Recognition of this fact motivated the development of a system to extract information about memory effects. This system is described in a recent publication [60] and has been applied to an investigation of the stochastic behavior of Trichel-pulse, negative-corona discharges in electronegative gases [52, 61, 62] and dielectric-barrier-type discharges in air which will be discussed in the next three sections [13].

It is convenient to represent the P-D phenomenon as a random point process [63] in which each pulse is identified by a time \( t_n \) and is “marked” with a particular property,
2.3 Stochastic Properties of Pulsating Partial Discharges

**REPRESENTATION OF A MARKED RANDOM POINT PROCESS**

![Diagram](image)

**Figure 26.** Diagrammatic representation of the marked random point process corresponding to the Trichel-pulse discharge phenomenon. The $\Delta t_n$ are pulse time separations and the $q_n$ are pulse amplitudes.

In this case the pulse amplitude $q_n$, as indicated in figure 26, the stochastic process is thus defined by the set of ordered pairs \( \{q_n, t_n\}, \quad n = 1, 2, 3, \ldots \). Because of memory effects, $q_n$ and $t_n$ can depend on the set \( \{q_j, t_j\}, \) for all $j < n$. The process can also be defined by the set \( \{q_1, q_n, \Delta t_{n-1}\}, \quad n = 2, 3, \ldots, j, \) where $\Delta t_{n-1} = t_n - t_{n-1}$, which is more appropriate to this discussion since it is the time separations between pulses that are either measured or specified by the measurement process. The pulse amplitude was chosen as the relevant mark because it is a measure of discharge intensity. In defining the point process, one could also consider other marks such as the pulse-shape parameters.

If memory is important in the P-D process, the variables $q_n$, $\Delta t_n$, $q_{n-1}$ and $\Delta t_{n-1}$ associated with adjacent events may not be independent. For example, the amplitude, $q_n$, may depend on the time separation, $\Delta t_{n-1}$. Indeed, this is found to be the case for Trichel-pulse discharges [12, 13, 60-62, 64]. The dependence of $\Delta t_n$ on $q_n$ or $\Delta t_{n-1}$ is an indication of the influence of residuals from the previous pulse in either enhancing or retarding the *initiation* of the subsequent pulse. Likewise, the dependence $q_n$ on $\Delta t_{n-1}$ or $q_{n-1}$ is an indication of the influence of residuals from the previous pulse on the *growth* of the subsequent pulse.

Because of these dependencies, the unconditional pulse-amplitude and pulse time-separation distributions ($p_0(q_n)$ and $p_0(\Delta t_n)$) are not independent. If, for example, an external, radiation source is used to help initiate P-D’s, $p_0(\Delta t_n)$ will change with the intensity of this source since the probability of discharge initiation changes with intensity. The changes in $p_0(\Delta t_n)$ will then be reflected in $p_0(q_n)$ if $q_n$ depends on $\Delta t_{n-1}$. Results from measurements of only one distribution, $p_0(q_n)$ or $p_0(\Delta t_n)$, as are obtained with most conventional P-D-measurement systems, will be difficult to interpret if memory effects are significant.

The ability to detect correlations among successive discharge pulses is a valuable diagnostic that could be incorporated into existing P-D measurement systems.
either directly through filtering techniques described here, or indirectly through off-line data analysis. The NIST system allows "real-time" measurement of a set of conditional pulse-amplitude and pulse-time-separation distributions, namely

\[ p_1(q_n|\Delta t_{n-1}) \; \text{and} \; p_2(q_n|\Delta t_{n-1}) \; \text{for all allowed} \; \Delta t_{n-1} \; \text{such that} \; p_0(\Delta t_{n-1}) = 0 \; \text{and} \; q_n \; \text{and} \; \Delta t_{n-1} \; \text{are dependent variables. Similarly, if} \; p_2(q_n|\Delta t_{n-1}, q_{n-1}) \neq p_1(q_n|\Delta t_{n-1}) \; \text{for allowed} \; q_{n-1}, \; \text{then a dependence must exist between} \; q_n \; \text{and} \; q_{n-1} \; \text{at a fixed} \; \Delta t_{n-1}. \; \text{One can also use the measured conditional distributions to compute correlation coefficients that provide a quantitative measure of the extent to which any two variables in the set \{q_1, q_n, \Delta t_{n-1}\}_j \; \text{are correlated.}

Measurement of meaningful conditional distributions require the P-D process to be stationary, or at least quasistationary. If external factors that affect P-D behavior, such as the size of a void, or the electron emission properties of a surface, change during the measurement, the data obtained for conditional distributions
could give false indications of possible correlations. The extent to which external factors are important is perhaps best revealed by measurements of the unconditional distributions \( p_0(q_n) \) and \( p_0(\Delta t_n) \) which can be performed relatively more quickly than the measurements of conditional distributions. The Trichel-pulse corona discharge considered below is an example of a P-D phenomenon that is sufficiently stationary so as to allow measurement of all the conditional distributions for which the system is designed.

### 2.3.2 Measurement System

The modifications of the Stochastic Analyzer for Pulsating Phenomena (SAPP) originally described by Van Brunt and Kulkarni[60] have been made to: 1) allow direct real-time measurements of the conditional pulse-amplitude distributions \( p_1(q_n|\Delta t_{n-j}) \), \( j > 2 \) and \( p_2(q_n|\Delta t_{n-1}, \Delta t_{n-2}) \); 2) eliminate intermediate pulse errors associated with measurement of the \( p_2 \) distributions; and 3) reduce background associated with accidental sampling of the tails of discharge pulses. A diagram of the measurement system is shown in figure 27. It should be noted that another version of this system has recently been constructed at NIST which can be applied to investigation of P-D’s generated by ac voltages. This new system, which will be described later, allows measurement of distributions that are conditioned on a set of selectable phase intervals of the applied voltage.

The system in figure 27 may be configured to measure any of the indicated distributions by appropriate positioning of the switches (S1-S5). Data from all measurement configurations are accumulated by a 256-channel, computer-controlled multi-channel analyzer (MCA).

The system was first applied to an investigation of the stochastic behavior of negative corona (Trichel pulses) generated using a point-plane electrode gap configuration in electronegative gas mixtures[49]. The test gap is indicated in figure 27. The corona-discharge current pulses are detected electrically using a preamplifier (A1) connected to an impedance \( Z \) that is in series with the discharge gap. The detected pulses are then sent to a variable gain amplifier (A2) before being routed to the appropriate circuit path. For measurement of \( p_0(q_n) \), the discharge pulses from A2 are fed directly to the MCA through gate G3 which is kept open by proper positioning of S4.

The distribution \( p_0(\Delta t_n) \) is measured by sending the pulses from A2 to a pulse sorter used to trigger two time-to-amplitude converters (TAC1 and TAC2) which generate output pulses of amplitude proportional to the time between P-D pulses. The outputs of TAC1 and TAC2 are fed to the MCA through gate G2 by appropriate positioning of S3. As shown in ref. [60], this arrangement permits the recording of every sequential time interval, provided all time separations exceed the TAC reset time of 50 \( \mu s \).
The measurement of \( p_1(q_n|\Delta t_{n-1}) \) requires use of a logic-controlled digital-delay generator (DDG) to restrict the transfer of pulses from A2 to the MCA through G3 to a narrow preselected time interval \( \Delta t_{n-1} \pm \delta(\Delta t_{n-1})/2 \) for which \( \Delta t_{n-1} >> \delta(\Delta t_{n-1}) \). To measure \( p_2(q_n|\Delta t_{n-1}, q_{n-1}) \), a single-channel analyzer (SCA1) is inserted between A2 and the input to the DDG time-interval control logic circuit by proper positionings of S1 and S5. The SCA1 restricts triggering of the DDG to pulses having amplitudes within the selected range \( q_{n-1} \pm \delta(q_{n-1})/2 \) for which \( q_{n-1} >> \delta(q_{n-1}) \) [60]. To insure, in the case of \( p_2 \) measurements, that the time-interval control logic properly inhibits the opening of G3 if intermediate pulses occur before the selected time window, it is necessary to modify the circuit previously described [60] by adding the amplifier A3 with input at \( f \). This amplifier is identical to that defined by transistor \( T_1 \) in figure 16 of ref. [60]. In the present configuration, the input \( f \) is connected directly to the delay \( \tau_1 \) of figure 16 (ref. [60]) which has, in turn, been disconnected from \( T_1 \).

Unlike the system previously described [60], the present system allows direct measurement of \( p_3(q_n|\Delta t_{n-1}, \Delta t_{n-2}) \). For measurement of this distribution, the switches S1 and S5 are positioned so that the input to SCA1 is derived from TAC1. The time interval measured by TAC1 is restricted by SCA1 to lie within a narrow range \( \Delta t_{n-2} \pm \delta(\Delta t_{n-2})/2 \) for triggering the DDG, which, in turn, defines \( \Delta t_{n-1} \).

By the indicated positionings of switches S1, S2, and S5, it is possible to measure the conditional pulse time-separation distributions \( p_1(\Delta t_n|\Delta t_{n-1}) \) and \( p_1(\Delta t_n|q_n) \). For measurement of \( p_1(\Delta t_n|\Delta t_{n-1}) \), the output of TAC1 is fed to the input of the single-channel analyzer SCA2 which thus defines \( \Delta t_{n-1} \) and triggers TAC3 for measurement of the next time interval \( \Delta t_n \). In the case of the \( p_1(\Delta t_n|q_n) \) measurement, SCA2 is connected directly to amplifier A2 thereby used to define \( q_n \).

The present system also differs from that previously described in that the \( p_1(q_n|\Delta t_{n-j}) \) logic circuit now contains a pulse counter that can be set for any \( j \geq 2 \). By adjustment of the delays inherent to the time-interval control logic and with minor adjustments in the shape of the gate pulse from this circuit, it has been possible to largely eliminate the background problem illustrated by figure 19 of ref. [60].

In the present measurement system, the pulse detection-circuit conditions are similar to those described in ref. [60] so that the measured discharge-pulse amplitude is proportional to the net charge transported in the discharge given by

\[
Q'_n = \int_{-\infty}^{\infty} i_n(t) \, dt,
\]

where \( i_n(t) \) is the instantaneous discharge current at time \( t \) for the \( n \)th pulse. Given the impulse response \( h(t - t') \) of the detection circuit (defined here mainly by the filter characteristics of Z and A1), the observed pulse signal is given by

\[
q'_n(t) = \int_{-\infty}^{t} i_n(t') \, h(t - t') \, dt'.
\]
2.3 Stochastic Properties of Pulsating Partial Discharges

The impulse response in the present measurement system has a width, \( w_i \), of about 1.5 \( \mu \)s whereas the intrinsic width, \( w_p \), of a typical Trichel pulse is known \([56]\) to be on the order 10 to 50 ns. Therefore the condition \( w_i >> w_p \) allows the approximation

\[
i_n(t) \approx Q'_n \delta(t - t_n),
\]

where \( \delta(t - t_n) \) is the Dirac delta function. Using this in equation (7) gives

\[
q'_n(t) = Q'_n h(t - t_n).
\]

This means that the shapes of the observed Trichel pulses in the present experiment are governed primarily by the shape of \( h(t - t_n) \) and thus the maximum of \( q'_n(t) \), denoted here by \( q_n \), is directly proportional to \( Q'_n \). Therefore, \( q_n \) can be expressed in units of charge, and in the present case, it is convenient to use picocoulombs (pC). The method for calibrating the pulse-height measurements in terms of charge is the same as described previously \([55]\).

2.3.3 Examples of Results from Investigation of Trichel Pulses

The Trichel-pulse discharge \([63]\) was selected for initial test of the SAPP measurement concept because its properties are reasonably well understood \([66-70]\) and it can be easily generated and controlled in a simple point-plane gap. With some care, the Trichel-pulse discharge can be maintained in a stable condition for relatively long periods of time. The phenomenon is shown \([12]\) to be a clear example of a non-Markovian, marked random point process in which memory effects play an important role. Strong correlations are found to exist among the amplitudes and time separations of successive discharge pulses which can be interpreted in terms of the influences of ion space charge and metastable species from previous pulses on the initiation and growth of subsequent pulses.

As an example of the richness of information that can be extracted with the present measurement system, results obtained for self-sustained Trichel pulses in a neon-oxygen gas mixture are shown in figures 28–32. Data for the different sets of distributions were obtained at different times so that the cathode surface conditions that apply, for example, to the results in figure 28 differ slightly from those that apply to figure 29. This accounts for the difference in \( p_0(q_n) \) shown in these two figures.

A detailed interpretation of the results presented here would go beyond the scope of this report. However, salient features of the data and certain important conclusions that can be derived therefrom should be noted. A more complete discussion of the physical bases for the stochastic behavior of the Trichel-pulse phenomenon has been given by Van Brunt and Kulkarni \([12]\).

The fact that the second-order conditional distributions, \( p_2 \), differ from the corresponding first-order distributions, \( p_1 \), which in turn differ from the corresponding unconditional distributions, \( p_0 \), indicates unequivocally that the set of variables
Figure 28. Measured unconditional and conditional discharge pulse-amplitude distributions $p_0(q_n)$, $p_1(q_n|\Delta t_{n-1})$, and $p_2(q_n|\Delta t_{n-1}, q_{n-1})$ for the indicated fixed values for $\Delta t_{n-1}$ and $q_{n-1}$. The distributions have been normalized to the maxima. These results are for negative-corona pulses in a neon-oxygen/gas mixture.
2.3 Stochastic Properties of Pulsating Partial Discharges

Figure 29. Measured unconditional and conditional discharge pulse-amplitude distributions $p_0(q_n)$, $p_1(q_n|\Delta t_{n-1})$, and $p_2(q_n|\Delta t_{n-1}, \Delta t_{n-2})$ for the indicated fixed values for $\Delta t_{n-1}$ and $\Delta t_{n-2}$. The distributions have been normalized to the maxima. These results are for negative-corona pulses in a neon-oxygen/gas mixture.
Figure 30. Measured unconditional and conditional discharge pulse-time-separation distributions $p_0(\Delta t_n)$, $p_1(\Delta t_n|q_n)$, and $p_1(\Delta t_n|\Delta t_{n-1})$ for the indicated fixed values for $q_n$ and $\Delta t_{n-1}$. The distributions have been normalized to the areas under the curves. These results are for negative-corona pulses in a neon-oxygen/gas mixture.
Figure 31. Measured unconditional and conditional discharge pulse-amplitude distributions $p_0(q_n)$, $p_1(q_n|\Delta t_{n-2})$, and $p_1(q_n|q_{n-1})$ for the indicated fixed values for $\Delta t_{n-2}$ and $q_{n-1}$. The distributions have been normalized to the areas under the curves. These results are for negative-corona pulses in a neon-oxygen/gas mixture.
Figure 32. Measured unconditional and conditional discharge pulse-amplitude distributions $p_0(q_n)$, $p_1(q_n|\Delta t_{n-3})$, and $p_1(q_n|\Delta t_{n-4})$ for the indicated fixed values for $\Delta t_{n-3}$ and $\Delta t_{n-4}$. The distributions have been normalized to the maxima. These results are for negative-corona pulses in a neon-oxygen/gas mixture.
\{\Delta t_n, q_n, \Delta t_{n-1}, q_{n-1}, \Delta t_{n-2}, \ldots \} \text{ associated with adjacent pulses are not independent. For example, it is seen from figures 28 and 29 that } q_n \text{ has a strong positive dependence on } \Delta t_{n-1}. \text{ This dependence can be related to the influence of negative-ion space charge from previous pulses in suppressing the magnitude of the electric field at the cathode when the next pulse develops. It is also seen from figure 28 that the amplitude, } q_n, \text{ of a pulse can be either positively or negatively dependent on the amplitude of the previous pulse. The sign of this dependence can be explained in terms of the competing effects of negative-ion space charge and metastable species in respectively retarding or enhancing the growth of the next pulse. The negative dependence of } \Delta t_n \text{ on } q_n \text{ (and } \Delta t_{n-1} \text{) implied by the conditional time-separation distributions shown in figure 30 can be understood in terms of the influence of metastable species from the previous pulse in enhancing the probability for initiating the next pulse by ejecting electrons from the cathode surface during field-assisted quenching.}

Because of the correlations among the amplitudes and time separations of successive pulses, the distributions shown in figures 28–30 are all related. It can be shown, for example, from the law of probabilities that \( p_0(q_n), p_0(\Delta t_n), \text{ and } p_1(q_n|\Delta t_{n-1}) \) are related by the integral expression

\[
p_0(q_n) = \int_0^\infty p_0(\Delta t_{n-1}) p_1(q_n|\Delta t_{n-1}) d(\Delta t_{n-1}), \tag{10}
\]

and the distributions \( p_0(q_n), p_0(\Delta t_n), p_1(q_n|\Delta t_{n-1}), p_1(\Delta t_n|q_n), \text{ and } p_2(q_n|q_n, \Delta t_{n-1}) \) are related by

\[
p_0(\Delta t_{n-1}) p_1(q_n|\Delta t_{n-1}) = \int_0^\infty p_0(q_{n-1}) p_1(\Delta t_{n-1}|q_{n-1}) p_2(q_n|q_{n-1}, \Delta t_{n-1}) d q_{n-1}. \tag{11}
\]

Equation (10) indicates that if \( q_n \) is dependent on \( \Delta t_{n-1} \), then any externally-induced change in the time-interval distribution, \( p_0(\Delta t_n) \), will necessarily change the amplitude distribution, \( p_0(q_n) \).

Since, as seen from the data in figures 29, 31, and 32, the profiles for \( p_2(q_n|\Delta t_{n-1}, \Delta t_{n-2}) \) and for \( p_1(q_n|\Delta t_{n-j}), j = 2, 3, 4 \) do not match the profile for \( p_0(q_n) \), it can be stated that \( q_n \) depends on \( \Delta t_{n-j}, j > 1 \), and therefore, the process is one for which memory extends back in time beyond the most recent event, i.e., the process is non-Markovian. This observation is consistent with results reported in the recent work of Steiner [64]. It can, in fact, be shown [12] that because of the relatively strong dependence of \( q_n \) on both \( \Delta t_{n-1} \) and \( q_{n-1} \), it is possible for memory to propagate indefinitely back in time.
2.3.4 Influence of a Dielectric Barrier on the Stochastic Behavior of Trichel-Pulse Corona

The investigation discussed here was undertaken to examine the influence that a thin solid polytetrafluoroethylene (PTFE) dielectric barrier has on the stochastic behavior of negative (Trichel) pulse corona discharges in air. Although the effects of solid dielectrics on corona pulses have been examined in previous experiments [71], there were no attempts to characterize the stochastic behavior of the phenomenon in these investigations. It is shown here from the measurements of conditional pulse-amplitude distributions that corona-induced charging of dielectric barriers placed on the planar electrode introduces another memory effect that becomes increasingly important as the point-to-plane gap spacing is reduced. It is also shown that, because the PTFE dielectric acquires a "quasi-permanent" charge from the corona, there is a critical gap spacing below which the Trichel-pulses appear to cease.

The experiments were carried out using the SAPP technique described above. The electrode-gap configuration used to obtain the results presented here is shown in figure 33. A PTFE dielectric of 1.0 mm thickness and of diameter D was placed on the plane electrode and centered on the point-to-plane axis. The point-to-plane spacing, d, could be varied from 0 to 10 cm. A very sharp stainless-steel point electrode with a radius of curvature at the tip of less than 0.01 mm was used to insure that, at a sufficiently high gap voltage, V_a, the discharge could be sustained by field-induced electron emission. The measurements described here were performed using "room air" in the gap. The corona-discharge current pulses were detected electrically using

![Figure 33. Electrode configuration.](image-url)
2.3 Stochastic Properties of Pulsating Partial Discharges

Figure 34. The measured critical point-to-plane gap spacing, \( d_c \), below which the Trichel-pulse discharge ceases as a function of applied gap voltage for various indicated diameters of the PTFE insulator.

A preamplifier, \( A \), connected to an impedance, \( Z \), in series with the discharge gap as shown. The output of \( A \) was fed to the system shown in figure 27.

The system was used here to measure the unconditional pulse-height and pulse time-separation distributions, \( p_0(q_n) \) and \( p_0(\Delta t_n) \) respectively, and the conditional pulse-height distribution \( p_1(q_n|\Delta t_{n-1}) \).

It is found for the configuration shown in figure 33 that there is a critical point-to-plane spacing below which it is not possible to observe a recognizable continuous Trichel-pulse discharge behavior. Figure 34 shows the measured critical point-to-plane gap separations, \( d_c \), at which the Trichel-pulse discharge ceases for different indicated values of the diameter \( D \). A pulsating discharge may still occur for \( d < d_c \), but the time separation between pulses becomes very long (many seconds). It is seen that the larger the diameter of the dielectric, \( D \), and the lower the applied voltage, \( V_a \), the larger will be the critical distance \( d_c \) at which the corona extinguishes.

Examples of measured \( p_0(q_n) \) and \( p_0(\Delta t_n) \) at different indicated gap distances \( d \) are shown in figures 35 and 36 respectively for the conditions \( V_a = 6.5 \text{kV} \), \( D = 5.0 \text{cm} \) and \( V_a = 10.1 \text{kV} \), \( D = 7.5 \text{cm} \). For convenience in plotting, all of the
Figure 35. Measured pulse-height and corresponding time-interval distributions at $V_a = 6.5 \text{kV}, D = 5.0 \text{cm}$, for the various indicated gap spacings. The distributions have been normalized to the maxima.
Figure 36. Measured pulse-height and corresponding time-interval distributions at $V_a = 10.1$ kV, $D = 7.5$ cm, for the various indicated gap spacings. The distributions have been normalized to the maxima.
distributions shown in these figures have been arbitrarily normalized to the maximum values. The profiles of the distributions shown here exhibit features similar to those previously reported and explained by Van Brunt and Kulkarni [12]. For example, the distributions $p_0(\Delta t_n)$ indicate a previously observed [12,72] critical minimum time separation, $\Delta t_c$, between successive pulses. The rate of decrease in $p_0(\Delta t_n)$ for $\Delta t_n > \Delta t_{n,\text{max}}$, where $\Delta t_{n,\text{max}}$ is the maximum in $p_0(\Delta t_n)$, is controlled by the rate of electron emission at the point electrode [12] and is thus strongly dependent on the local electric field. It is known that $\Delta t_c$, which is controlled by the ambipolar diffusion of ions away from the point, also decreases exponentially with the field near the cathode. Examples of results for $\Delta t_c$ versus $d$ at different indicated values of $D$ are shown in figure 37. The fact that both $\Delta t_c$ and the width of $p_0(\Delta t_n)$ go through a minimum at a particular $d > d_c$ indicates that the electric field at the cathode goes through a maximum at this separation. This maximum in the field does not occur when the dielectric is removed as illustrated by the measured data for $p_0(q_n)$ and $p_0(\Delta t_n)$ shown in figure 38 that were obtained under conditions where no dielectric was present on the planar electrode. The corresponding $\Delta t_c$ extracted from these data are plotted in figure 39 and show the expected monotonic decrease with decreasing $d$ which, for a fixed $V_a$, is consistent with an increasing field strength at the point electrode.

The profiles of the pulse-height distributions, $p_0(q_n)$, are generally consistent with equation (6) and thus can be explained in terms of the physical processes that determine the profile of the corresponding $p_0(\Delta t_n)$ distribution coupled with the
Figure 38. Measured pulse-height and corresponding time-interval distributions at $V_a = 6.5$ kV for various indicated gap spacings when no dielectric is on the anode surface. The distributions have been normalized to the maxima.
Figure 39. Minimum possible pulse time separation, $\Delta t_c$, versus gap spacing for the different indicated values of the applied voltage $V_a$ and for the case where there is no dielectric on the anode surface.
known dependence of $q_n$ on $\Delta t_{n-1}$ as previously discussed [12]. The extent to which $q_n$ depends on $\Delta t_{n-1}$ is determined from measurements of $p_1(q_n|\Delta t_{n-1})$.

Examples of measured conditional distributions $p_1(q_n|\Delta t_{n-1})$ at different indicated values of $\Delta t_{n-1}$ and $d$ and for $V_a = 10.1$ kV and $D = 7.5$ cm are shown in figure 40 together with the corresponding unconditional distribution $p_0(q_n)$ indicated by the dashed line. A strong positive dependence of $q_n$ on $\Delta t_{n-1}$ is seen from these data. This behavior is consistent with data shown in the previous section and can again be explained by the effect that moving negative-ion space-charge clouds from previous pulses have on the electric field at the cathode when the next discharge pulse develops.

The data on the unconditional distributions such as those shown in figures 35 and 36 can be used to compute the expectation values $\langle Q_n \rangle$ and $\langle 1/\Delta t_n \rangle$ corresponding respectively to mean discharge-pulse magnitude and repetition rate. Examples of the results of such determinations for different values of $d$, $D$, and $V_a$ are shown in figure 41. Certain general trends are apparent from this figure. The mean discharge-pulse repetition rate generally decreases with decreasing $V_a$, and increasing $D$; whereas the mean discharge magnitude $\langle Q_n \rangle$, exhibits the opposite behavior, i.e., it decreases with increasing $V_a$ and decreasing $D$. Both $\langle 1/\Delta t_n \rangle$ and $\langle Q_n \rangle$ may either increase or decrease with $d$ depending on the values of $D$ and $d$.

Figures 42 and 43 show plots of the expectation values $\langle q_n(\Delta t_{n-1}) \rangle$ versus $\Delta t_{n-1}$, where

$$\langle q_n(\Delta t_{n-1}) \rangle = \int_0^\infty q_n p_1(q_n|\Delta t_{n-1}) dq_n. \quad (12)$$

These results which were derived from equation (8) using data on the conditional distributions such as shown in figure 42, indicate the strong dependence of $q_n$ on $\Delta t_{n-1}$ and are consistent with previous results [12] except at short distances ($d < 0.6$ cm) at which a change in slope becomes evident as $\Delta t_{n-1}$ increases. This is seen most clearly by the data at $d = 0.4$ cm in figure 43.

Several significant conclusions can be drawn from the results presented here. First, it is evident from the measured distributions $p_0(q_n)$, $p_0(\Delta t_n)$, and $p_1(q_n|\Delta t_{n-1})$ that, except for point-to-dielectric spacings very close to the critical value $d_c$ at which Trichel-pulse activity ceases, the presence of the dielectric surface has little or no effect in modifying the general stochastic behavior of the phenomenon. For sufficiently large spacings, the observed profiles of the unconditional pulse-amplitude and pulse-time separation distributions and the correlations between the amplitudes and time separations of successive pulses are consistent with those reported previously [12] for Trichel pulses that occur in air or $N_2 - O_2$ mixtures when there is no dielectric on the planar electrode.

It can be argued from the data that give the dependencies of $\Delta t_c$ and $\langle 1/\Delta t_n \rangle$ on $D$ shown in figures 37 and 41, that the primary effect of the dielectric on Trichel-pulse development at any spacing $d$ arises from a reduction in the electric-field magnitude at the point electrode caused by the negative charge that accumulates on the dielectric
Figure 40. Measured conditional pulse amplitude distributions $p_1(q_n|\Delta t_{n_1})$ at the indicated values for $\Delta t_{n-1}$ and gap spacing, and the corresponding unconditional pulse-amplitude distributions $p_0(q_n)$ shown by the dashed lines. The distributions have been normalized to the maximum values.
Figure 41. Dependencies of the mean pulse amplitude \( (Q_n) \) and repetition rate \( 1/(\Delta t_n) \) on gap spacing for the indicated values of \( V_a \) and \( D \) calculated from the distributions \( p_0(q_n) \) and \( p_0(\Delta t_n) \) such as shown in figures 35 and 36.
Figure 42. The expectation value \( \langle q_n(\Delta t_{n-1}) \rangle \) versus \( \Delta t_{n-1} \) at \( V_a = 10.1 \text{kV}, D = 7.5 \text{ cm} \) for the indicated gap spacings.

Figure 43. The expectation value \( \langle q_n(\Delta t_{n-1}) \rangle \) versus \( \Delta t_{n-1} \) for \( V_a = 10.1 \text{kV}, D = 7.5 \text{ cm} \) and \( d = 0.4 \text{ cm} \).
2.3 Stochastic Properties of Pulsating Partial Discharges

surface during the discharge. This conclusion is supported by the \( p_0(\Delta t_n) \) data in figures 35 and 38 for \( d = 2.0 \) to 5.0 cm that were obtained respectively with and without a dielectric on the anode surface. The observed increases in both \( \Delta t_c \) and the width of \( p_0(\Delta t_n) \) which occur when the dielectric is introduced are consistent with a reduction of the electric-field magnitude equivalent to that which can be achieved by reducing the gap voltage. As previously noted, the parameters \( \Delta t_c \), \( (1/\Delta t_n) \), and the width of \( p_0(\Delta t_n) \) are sensitive to small changes in electric-field magnitude at the point [12]. The effect of increasing the diameter of the dielectric surface is also similar to that of decreasing the gap voltage. The appearances of corresponding minima in \( \Delta t_c \) and the widths of the \( p_0(\Delta t_n) \) distributions at a particular gap spacing indicate that the field at the point electrode must attain a maximum at that spacing for a fixed \( V_d \) when the dielectric is present.

It can be seen from figures 42 and 43 that the presence of the dielectric begins to influence the dependence of \( q_n \) on \( \Delta t_{n-1} \) significantly for small point-to-dielectric gap spacings close to the critical value \( d_c \). From an examination of the data shown in figure 43, it can be argued that for \( \Delta t_{n-1} < \Delta t_c \), the dependence of \( q_n \) on \( \Delta t_{n-1} \) is due predominantly to the previously mentioned negative-ion space-charge effect which is a prominent characteristic in the stochastic behavior of Trichel pulses in the absence of the dielectric barrier [12]. The slope of the \( (q_n(\Delta t_{n-1})) \) versus \( \Delta t_{n-1} \) curve, however, is seen to decrease significantly at \( \Delta t_c \). It is speculated that at \( \Delta t_{n-1} = \Delta t_c \), the negative ions clear the gap and are presumably deposited on the dielectric. Thus, for \( \Delta t_{n-1} > \Delta t_c \), the dependence of \( q_n \) on \( \Delta t_{n-1} \) could be governed primarily by the rate of charge dissipation or migration on the dielectric surface. It should be noted that the additional surface charge deposited by an earlier discharge pulse which is present when the next pulse initiates will act to reduce the field at the point electrode when this pulse develops and will thereby tend to inhibit its growth. Therefore, a dissipating residual surface charge from a previous pulse acts like the moving residual negative-ion space charge to cause \( q_n \) to have a positive dependence on \( \Delta t_{n-1} \).

Measurements performed with a vibrating plate type electric-field probe [73, 74] showed that after the corona discharge is turned off, the PTFE retains a quasi-permanent negative surface charge that decays slowly with a time constant \( (> 10^4 \) seconds) which is much greater than the mean time between Trichel pulses. This observation suggests that if the dependence of \( q_n \) on \( \Delta t_{n-1} \), for \( \Delta t_{n-1} < \Delta t_c \) in figure 43 is indeed due to an effect of surface-charge dissipation, it must correspond to a component of the charge density that is much more mobile than that detected with the field probe, i.e., it must decay with a time constant comparable in magnitude to the mean time between discharge pulses. This is consistent with recent observations of Jonscher and Owede [75] which indicate that the charge deposited on insulating surfaces can become increasingly more mobile as the charge density is increased.

The conclusions drawn here about the influence of a PTFE dielectric surface on Trichel-pulse discharge can be expected to apply in general to other types of insulating materials to the extent that these materials can acquire permanent or
quasi-permanent charge from the corona. A preliminary survey made using other materials suggested that this is indeed the case.

2.3.5 Limitations and Extensions of the SAPP Technique

The system, as shown in figure 27, has certain limitations. First, it is designed to operate with dc voltages. Second, as discussed in ref. [60], it cannot give reliable measurements of certain conditional distributions if the time separations between events become shorter than either the TAC reset time or the MCA analog-to-digital conversion time. Third, it cannot be applied to nonstationary phenomena that drift on a time scale comparable to the time required to acquire statistically significant data. Fourth, it can only measure one distribution at any given time. Fifth, independent of the problems associated with timing in either the TAC or MCA, it does not employ broad-band detection methods and therefore cannot resolve pulses separated by times less than the width of the impulse response. Because of this limitation, it could not, for example, be applied to investigate P-D pulse bursts which as shown below occur in liquids and are known to occur in the positive corona of some highly electronegative gases like SF₆ [55].

The restriction to dc voltages can be overcome by incorporating a phase marker such as a zero-crossing sensor to identify the phase associated with any given pulse time separation. The system has, in fact, been recently modified to allow measurement of conditional distributions restricted to specific phase intervals. For example it now allows measurement of the phase conditioned distributions, \( p_1(q_i(\phi) | \Delta \phi_j) \) where \( q_i \) is the amplitude of any P-D pulse that occurs with phase \( \phi_i \) contained in the specified interval \( \Delta \phi_j \). This type of distribution has been considered recently by others [58, 59]. However, in addition to this distribution, our system is capable of measuring many others in which phase is specified. These include the distributions \( p_1(q_1(\Delta \phi_{j+}^2) | Q(\Delta \phi_{j}^1)) \) and \( p_1(q_1(\Delta \phi_{j-}^2) | Q(\Delta \phi_{j}^1)) \), where \( q_1 \) is the amplitude of the first pulse to occur in either the positive or negative half cycle specified respectively by the phase intervals \( \Delta \phi_{j+}^2 \) or \( \Delta \phi_{j-}^2 \) and

\[
Q(\Delta \phi_{j}^1) = \sum q_i(\phi_{j}^1); \quad \phi_{j}^1 \in \Delta \phi_{j}^1, \tag{13}
\]

is the total charge associated with all P-D pulses occurring within phase interval \( \Delta \phi_{j}^1 \) of the preceding half cycle. Preliminary data obtained on these distributions for dielectric-barrier discharges at 60-Hz voltages show that the charge deposited on a dielectric surface by partial discharges during one half cycle significantly affect the development of partial discharges during the subsequent half cycle.

Limitations on minimum time separations can be overcome in principle by using prerecorded data that can be obtained with fast-transient digitizers. However, if prerecorded data are to be used, it may be preferable to use computer software to
determine the conditional distributions, rather than the hardware presented here. It should be emphasized that an important advantage of the method described here is that the conditional distributions are measured directly in real time. This is an advantage because it overcomes the problem of having to store enormous quantities of data required to determine conditional distributions by the software approach. For example, some of the second-order conditional distributions shown in figures 28 and 29 required about 10 minutes of data acquisition time in order to obtain acceptable statistics. This means that data on all but a very small fraction of the discharge events that occurred in this 10 minute period were discarded by the filtering procedure. Using the software approach, all the pulses that occurred during that time would have to be stored, which for the data shown means that more than $10^9$ pairs of numbers would have to be acquired just to determine one distribution. Also, because the present system works in real time, the distributions can be seen immediately as the data are accumulated.

If the P-D phenomenon is, or can become, nonstationary, then an independent method may be needed to determine the extent to which it is nonstationary. A periodic check of the unconditional pulse-amplitude and/or time-separation distribution will, in most cases, provide an indication of deviations from stationary behavior.

In the case of multiple P-D discharge sites, an ambiguity can occur in the interpretation of data from measurement of conditional distributions, particularly if the discharges from the different sites occur with nearly equal intensity. The measurement scheme discussed here works best if there is only one site at which P-D discharges are being generated with an intensity that is significantly above the background P-D level. The existence of pronounced correlations among successive P-D pulses would, in fact, indicate that the discharges are occurring at one, or a limited number of sites. The determination of this fact might be important in some diagnostic applications.

Finally, it should be pointed out that the present system could be modified to allow a more efficient use of the available data. One could, for example, use multiple MCA's in parallel to measure simultaneously more than one distribution.
3 LIQUID DIELECTRICS RESEARCH

Task 03
Kenneth L. Stricklett, H. Yamashita (Guest Scientist),
and Charles Fenimore
Electricity Division
National Institute of Standards and Technology

3.1 Introduction

Electric breakdown of liquid dielectrics is preceded by the growth of a streamer in the liquid. Recent studies of these phenomena, see for example Hebner [76] for a review, reveal that as a streamer propagates it follows a well defined pattern: Each stage or mode of growth may be distinguished by its structure, speed of propagation, and relative extent. Considerable effort has been devoted to describing the conditions that influence streamer propagation and initiation [77]. However, despite this activity, no clear consensus has been reached as to the mechanism for the initiation of the discharge. Proposals put forward have included: electron avalanche [78], cavitation [79], and electrostatic forces acting on the dielectric [80].

The mechanisms responsible for the initial growth of negative streamers appear to be distinct from those during its latter stages. Watson and Chadband [81] show initial growth of negative streamers to be consistent with the propagation of a cavity within the liquid. Similar results are reported for partial discharges (PD's), where photographic and optical studies [78, 82, 83] have established a clear correspondence between the growth of a cavity in the liquid and bursts of discrete current pulses emitted from a cathode. The results presented in this report were obtained during experimental investigations of the initiation and early growth of negative streamers in hexanes [84, 85]. In section 3.2, the initial growth of negative streamers generated by an impulse voltage is examined at pressures ranging from 0.1 to 1.1 MPa. The pressure dependence of the streamer initiation and inception voltages are shown. In section 3.3, partial discharges generated by the application of dc voltages are examined. A non-uniform field geometry is employed and the growth of cavities associated with partial discharges at a point cathode are photographed at high magnification. A simultaneous record of the discharge current is also obtained. This study employs an image-preserving optical delay [82, 82], and the use of this device allows photography of the discharge at its inception. Such data allow detailed description of the temporal and spatial development of the cavity and provide a basis for the evaluation of models for the initiation of negative streamers.
3.2 Streamer Initiation in Hexanes

For hydrocarbon-based dielectric liquids, four modes of streamer growth are suggested [76, 87] for negative streamers; these are shown schematically in figure 44. The 1st mode appears to be a single, relatively linear channel emanating from the cathode surface and connecting directly to a much more bushy structure, mode 2. During modes 1 and 2, the streamer propagates at subsonic speeds. Although the 3rd mode originates at the 2nd mode, its structure differs from that of the 2nd mode, and its speed of propagation is significantly higher, approaching the sonic velocity. The transition from the 2nd to the 3rd mode is not continuous: streamer growth often stalls after the formation of the 2nd mode [88]. The 4th mode directly precedes breakdown and it appears to be a single streamer that propagates at supersonic speeds.

Experimental conditions influence streamer propagation; for example, the relative extent of the 2nd mode is sensitive to both the ambient pressure [89-91] and the purity of the fluid [92]. Indeed, it has been suggested that at sufficiently high pressures, the 1st and 2nd modes may not exist at all [89, 90, 93]. Further systematic study of these effects is of value; and the present work was undertaken to examine the inception and early growth of negative streamers. For this purpose, highly magnified frame photographs of streamer growth at a needle tip as well as photographs of the full gap are obtained at pressures ranging from 0.1 – 1.1 MPa.

3.2.1 Apparatus and Procedure

Streamer growth is photographed using conventional shadowgraphic techniques and an image-converter camera [87, 89]. The optical resolution is improved over that obtained in previous studies by mounting a microscope objective within the test cell. This configuration provides an optical resolution of approximately 1 μm at 100× magnification.

The test gap consists of a steel gramophone needle and a stainless steel rod; the electrodes are enclosed within a brass cell and are immersed in the test fluid. The curvature of the needle is approximately parabolic, having a radius of curvature at its tip of approximately 40 μm. The rod electrode is 6.4 mm in diameter and has a hemispherical tip. The needle and rod are separated by a distance of 5 mm.

A voltage impulse, having negative polarity, is applied directly to the needle and the rod electrode is connected to ground. The voltage waveform is approximately trapezoidal: the rise and fall times are 3 μs (10-90 %) and the voltage varies by less than ±10 % within a 4 μs interval centered about the peak voltage. A precision resistive voltage divider and digital oscilloscope are used to record the waveform. The camera monitor pulse is also recorded and, together with the voltage waveform, these data determine the voltage at each frame within a photograph. Two measures
of the effects of pressure are determined by these methods: the average streamer inception voltage, \( V_{\text{inc}} \), and initiation voltage, \( V_{\text{init}} \). For purposes of this study, \( V_{\text{init}} \) is the lowest voltage for which one streamer is observed in eight impulses, and is a measure of the minimum voltage required to produce a prebreakdown streamer. For voltages greater than or equal to the inception voltage, a second useful quantity may be determined: the average voltage at the inception of the streamer \( V_{\text{inc}} \). Values of \( V_{\text{init}} \) and \( V_{\text{inc}} \) are measured using high magnification; furthermore, to avoid rapid deterioration of the needle tip and of the liquid, they are obtained without breakdown.

Ultra-pure grade hexanes are used both for this study and for the work discussed in section 3.3. The liquid is used as received without degassing or purification other than by filtration. While at atmospheric pressure, the liquid is continuously circulated and filtered through a 2\( \mu m \) pore size paper filter. The pressure within the cell is increased by compressing the liquid, which is accomplished by the use of small hydraulic cylinder connected to the cell. The application of pressure did not allow continuous filtration; however, pressure was released and the liquid circulated and filtered every 8–10 impulses.

3.2.2 Results and Discussion

Photographic Observation of Streamer Behavior.

Photographs of the full gap obtained at pressures of 0.1, 0.7, and 1.1 MPa are shown in figure 45. The effects of pressure are made evident in these photographs by a dramatic reduction in the extent of the 2nd mode and by changes in the structure of the 3rd mode: it may be noted that the latter is less dense and has fewer branches at high pressure. The 1st and 2nd modes may be readily identified in the photographs obtained at atmospheric pressure and remain visible up to 0.7 MPa, however they are not resolved in the low-magnification photographs for pressures of 0.9 MPa and above.

For comparison, high-magnification photographs obtained at pressures of 0.1, 0.5, and 1.1 MPa are shown in figure 46. In contrast to the photos taken at low magnification, the characteristic stem and bush structure is clearly evident at all pressures. Furthermore, the images are sufficiently well-resolved to indicate the dynamical behavior of the streamer: upon close examination of these photographs, it is evident that the 1st mode expands and contracts repeatedly as the streamer propagates. It was further noted, that the frequency and amplitude of oscillation of the 1st mode increase with pressure. Indeed, at the highest pressure examined, the 1st mode completely disappears and reappears. The maximum diameter and length of the 1st cathode mode are, however, relatively insensitive to pressure and are on the order 4\( \mu m \) and 3\( \mu m \) respectively. The 2nd mode did not exhibit such dramatic oscillations.
3.2 Streamer Initiation in Hexanes

The oscillations in the diameter of the 1st cathode mode may be consistent with intermittent light emission and charge injection observed during the propagation of negative streamers [94, 95]. Studies of partial discharge phenomena at a point cathode in the same material [85] show current to be highly correlated with the presence of a bubble-like structure at the electrode. It seems likely that significant charge injection can only occur when the streamer is in contact with the electrode; and thus that the prebreakdown streamer provides a preferred path for current flow. Indeed, studies of full breakdown show the conducting channel to lie along the path of a prebreakdown streamer.

Streamer Initiation and Inception Voltages.

The methods described allow the effects of changes in the ambient pressure and in the peak voltage on the streamer inception voltage to be examined. Values of $\bar{V}_{inc}$ are estimated from eight trial pulses and are measured using a 217 ns frame interval. The results of these measurements for pressures of 0.1, 0.5, and 0.9 MPa are shown in figure 47, where $\bar{V}_{inc}$ are plotted on representative traces of the voltage waveform. Clear trends in both the formation time and inception voltage are apparent. At 0.1 MPa, $\bar{V}_{inc}$ has a strong dependence on the voltage waveform: the time required for streamer inception decreases and the voltage at inception increases with applied voltage. Although the formation time decreases with faster rising impulses, it may be noted that the inception voltage is relatively constant for the data obtained at 0.9 MPa. Indeed $\bar{V}_{inc}$ appears to approach a value that is relatively independent of pressure as the peak voltage is increased. These observations lend support to the results of Kao and McMath [96], who show for both transformer oil and n-hexane that increased pressure has little or no influence on breakdown voltage for fast rising voltages. In their study, the effect of increased pressure was found to be negligible when the rate of rise of the applied voltage exceeded $4 \text{MV/cm}\mu\text{s}$. For the results presented here, the rate of rise increases with applied voltage. Numerical methods [97] used to estimate the electric field at the needle tip yield $5.5 \times 10^6 \text{V/cm}$ at a 30 kV applied potential. This value together with the greatest rate of voltage rise shown in the figure yield $6.6 \text{MV/cm}\mu\text{s}$ which compares favorably with the value given by Kao and McMath.

The effect of pressure on the streamer initiation voltage is shown in figure 48. $V_{init}$ is seen to increase with pressure from 0.1 to 0.5 MPa and to be relatively independent of pressure above 0.5 MPa. Peak voltages of $-33$ and $-46 \text{kV}$ were used at 0.1 and 0.3 MPa, respectively, and $-53 \text{kV}$ for pressures of 0.5 MPa and above. In each case, streamer initiation occurred near the peak voltage.
Figure 44. Cathode streamer development. The four modes of streamer growth are shown, (Hebner [76]).
Figure 45. Low magnification photographs of prebreakdown streamers. The needle electrode is shown on the right in each of these photographs. Modes 1 and 2 may be readily identified in the photographs obtained at 0.1 MPa. The frame interval is 512 ns and the frame sequence is shown in (a). An impulse having a peak voltage of $-93 \text{kV}$ is applied to the needle.
Figure 46. High-magnification photographs of prebreakdown streamers. The pressure and peak voltages are indicated beside each photograph and the frame interval is 217 ns.
3.2 Streamer Initiation in Hexanes

Figure 47. Pressure and waveform effects on streamer inception. The average streamer inception voltages $V_{\text{inc}}$, are plotted on representative traces of the voltage waveform. Values obtained at pressures of $\odot$, 0.1; $\triangle$, 0.5; and $\square$, 0.9 MPa are shown.

Figure 48. Pressure dependence of the streamer initiation voltage, $V_{\text{init}}$. 
Figure 49. Partial discharge record obtained at 17.5 kV. The frame interval and exposure are 51 and 10 ns respectively. The current waveform and the extent of the cavity are plotted in the upper panel.
3.3 DC Voltage Conditions

For dc voltages near the threshold for P-D activity, P-D’s occur infrequently and are separated by time intervals that are widely distributed. Furthermore, significant current may only persist for times of the order of microseconds. These characteristics present a technical challenge: photographing a short lived event that may occur essentially at random. The methods employed allow two independent records of the P-D to be obtained simultaneously: measurement of P-D current and frame photography of the cavity.

3.3.1 Experimental Apparatus

The test gap consists of a steel needle and stainless steel rod separated by 3.2 mm. The electrodes are enclosed within a brass cell and are immersed in the test liquid. The liquid is used as received without degassing or further purification. The rod electrode is 6.4 mm in diameter and has a hemispherical tip, and is connected to a high-voltage dc power supply. The needle electrode is 1.0 mm in diameter and has a conical point with an apex angle of 30° and a tip radius of 1 μm.

A continuous-wave argon laser is used to illuminate the needle tip, and frame photographs of the discharge are obtained by shadowgraphic methods and the use of an image-converter camera. The total magnification is 200 × and the optical resolution is sufficient to fully resolve objects less than 2 μm in diameter. The use of an image-preserving optical delay allows the framing sequence to begin much closer to, and for some frame intervals before, the on set of the partial discharge.

A broadband transimpedance amplifier [98, 99] is used to measure the P-D current. The amplifier is designed to provided a low-noise background against which low-level P-D currents may be detected. The amplifier has three stages: a low-noise, broad-bandwidth, current-sensitive preamplifier and low-gain and high-gain buffer amplifiers. The combined system bandwidth is estimated to be 35 MHz and the equivalent noise is 30 nA (rms). The charge sensitivity of the system is estimated to be less than 0.7 fC. The amplifier is connected directly to the needle electrode and the current waveform is recorded digitally. A digital oscilloscope having a sample rate of 10⁸ samples/s is used to obtain the results shown here. Both the digital oscilloscope and the framing camera derive their trigger signals from the P-D current.

3.3.2 Partial Discharge Records

An example of a P-D record, obtained at an applied potential of 17.5 kV, is shown in figure 49. Note that the first few camera frames precede the initiation of the current waveform. The data at hand allow an estimate of the time interval between the
initial current pulse and the onset of cavity growth. As shown, the current waveform begins \( 51 \pm 5 \) ns before the midpoint of the sixth frame, the first frame in which clear evidence of the cavity appears. The estimated uncertainty in the position of frame six is \( \pm 8 \) ns; combining these uncertainties in quadrature yields \( 51 \pm 9 \) ns and thus provides an upper bound of 60 ns. The extent of the cavity in the sixth frame, however, suggests that the time interval is likely to be significantly less. In the upper panel, the length of the cavity is plotted against the frame number and fit to a linear function. Such a fit provides an estimate for the origin of the cavity that is nearly coincident with the initiation of the current waveform. However, in the absence of a more accurate determination of the instantaneous rate of expansion of the cavity at its inception, we are reluctant to apply this correction and prefer to report the upper bound.

The correlation between the onset for cavitation and PD current noted here lends support to recent experimental results obtained in cyclohexane [78]. Results obtained in nitrobenzene suggest that significant charge may be injected into the liquid prior to streamer initiation [100, 101], and, that the onset for charge injection precedes that for cavitation by as much as 4 \( \mu \)s [100]. The presence of charge in the fluid would result in a force on the fluid of the proper sign to produce the observed cavitation.

The linear fit also provides an estimate of the average rate of expansion of the cavity. Furthermore, since the rate of expansion depends on the forces acting on the liquid, an estimate of the effective pressure within the cavity, \( P_{in} \), may be obtained. Assuming inviscid incompressible flow, and approximating the cavity by an expanding sphere of radius \( r \), the instantaneous work done in expanding the cavity is

\[
P_{in} \, dv = P_{amb} \, dv + \frac{2S}{r} \, dv + \frac{3}{2} \rho r^3 \, dv.
\]

The terms include: the work done against ambient pressure, \( P_{amb} \), and surface tension, \( S \); and the kinetic energy imparted to the surrounding liquid. The average rate of expansion of the cavity, \( \dot{r} \), is approximately 20 m/s and the density, \( \rho \), and surface tension of hexanes are approximately 0.66 g/cm\(^3\) and 1.8 \( \times \) 10\(^{-2}\) N/m respectively. For the conditions described, the kinetic energy is the largest term and \( P_{in} \) is approximately 0.4 MPa.

The required pressure may be provided by local heating of the liquid, as may occur during electron avalanche, and by electrostatic forces. The form of the cavity, however, suggests that the forces acting on the liquid are highly directional, and thus that the gas dynamic pressure within the cavity is of limited importance. We believe these observations lend support to the results reported by Watson and Chadband [81] and further suggest that, from its inception, the growth of the cavity may be described by the electrostatic forces acting on the liquid.

The current waveform is relevant to describing the conditions at the initiation of the P-D. In over 90% of the current waveforms, clear evidence of a continuous current
3.3 DC Voltage Conditions

is detected at the initiation of the waveform. Furthermore, whereas the later current pulses tend to grow monotonically in amplitude, the first two pulses are frequently of comparable amplitude. Indeed, P-D’s are observed that consist of only a double-pulse structure. These observations suggest that the mechanisms producing the measured current at the origin of the cavity growth differ from those at later times. Two mechanisms that give rise to continuous currents are suggested: the motion of charge trapped in the liquid or at the interface between the liquid and the metal electrode would produce a current in the external circuit [102], also the reduction in the capacitance of the cell due to a reduction in the dielectric constant of the material near the needle tip would produce a continuous current.
3.4 Conclusions

The effects of increased ambient pressure on the initiation and growth of negative streamers in hexanes are observed using a 100× high-magnification optical system with 1 μm resolution. The existence of the 1st cathode streamer mode is clearly shown at pressures ranging from 0.1 to 1.1 MPa. The 1st cathode mode is approximately 4 μm in diameter and 8 μm in length at the transition to the 2nd mode. Dynamical behavior of the 1st cathode mode is shown; the diameter of the stem appears to oscillate as the streamer grows and, at high pressure, the stem completely disappears and reappears although the 2nd mode continues to exist. The behavior of the 1st cathode mode may be associated with intermittent charge injection and the stepped propagation of negative streamers noted in previous studies. The 3rd mode becomes thinner and less branched at higher pressure. The streamer-initiation voltage increases with pressure, but the effect of pressure on the streamer-inception voltage decreases at higher applied voltage.

Highly resolved photographs of the initiation of P-D's in liquid hexanes are obtained for dc voltages. The cavity growth at a point cathode is nonisotropic, which suggests that electrostatic forces are of primary importance in driving its expansion. The onset for P-D current precedes or is simultaneous with the initial growth of the cavity. An upper bound of 60 ns between the first current pulse and the growth of the cavity is estimated.
4 FAST TRANSIENT MEASUREMENTS

Task 04
G.J. FitzPatrick and Y.X. Zhang (Guest Scientist)
Electricity Division
National Institute of Standards and Technology

4.1 Introduction

The purpose of an impulse voltage measuring system is to provide a means of reducing the high voltage signal to levels which are compatible with data recording equipment and this requires that the scale factor of the system be constant throughout the frequency range of interest. Most impulse measurement systems used by industrial laboratories invariably introduce some distortion of the input signal due primarily to inadequate bandwidth, voltage coefficient, and some other factors. This distortion may be either negligible or totally unacceptable, depending on the allowable error associated with the particular measurement requirement. According to IEC and IEEE standards [103, 104], a system which is used to measure standard lightning impulses should have errors of less than 3% and 10% for peak voltage and front time, respectively. The standards also recommend that certain aspects of the dynamic behavior of the measurement system should be evaluated by using parameters obtained from the step response. There is, however, no reliable relationship between the errors of a measurement system and its step response parameters. In fact, it has been shown that some measurement systems exhibit step response parameters that fall within the limits given by IEC and IEEE but that actually produce unacceptably large errors in the measurement of high voltage impulses [105, 106].

A more reliable and simplified method has been recommended in the new draft of IEC-60 that is based on simultaneous measurements of a high voltage impulse by an independent reference system and the system under test [107]. As a first step, international comparative measurements were made in four National Laboratories and the relative differences among them were reported [109]. Investigations have also been made of the interactions between two systems configured for simultaneous measurements, and of methods for minimizing these interactions [106].

The comparative method establishes the uncertainty in measurements of a particular type of impulse for a measurement system by comparison against a reference measurement system having overall uncertainties for peak voltage of less than 1% over its range of use [107]. The key to the comparative measurement technique is that the reference system has to be built and carefully characterized. Without a stable and precise reference system, it is usually impossible to use the comparative method to estimate the uncertainty of another system. There are, however, techniques that
utilize a pair of complementary measurement systems to detect measurement errors in each system, but the technique requires that the measurement systems have different error sources [108].

As a part of a series of investigations into high voltage impulse measurements, a resistive impulse measurement system was specially designed, built, and calibrated at NIST. It is anticipated that this system along with some Kerr electro-optical devices will be used as the NIST reference systems. This report documents the design, construction, and characterization of this fast impulse voltage measurement system, which is rated for peak voltages up to 300 kV.

4.2 Resistive Voltage Divider Design

4.2.1 General Considerations

The resistive voltage divider, designated as NIST4, serves as the primary component of the reference measurement system. It was designed to accurately measure full lightning impulses up to 300 kV. The voltage range was selected for several reasons. First, it was similar to devices used as reference systems in the national laboratories of other countries so that direct comparison between the devices would be reasonable. Second, compared with a divider rated for megavolt impulses, construction was simplified because of its smaller physical size. Additionally, the proposed draft, IEC 60-2, permits the qualification of a larger divider by the comparative measurement technique with a smaller reference divider at 20% of the rated voltage of the larger one [107]. A reference divider rated at 300 kV can therefore be used to compare with dividers having ratings of up to 1500 kV [107]. The NIST4 divider has a nominal resistance of 10 kΩ, which is typical for most resistive dividers. A divider ratio of 1000:1 was selected rather than a larger one to give a signal-to-noise ratio that was high enough that degradation of the divider output signal by pickup of radiated noise would be minimized. Both digital recorders and digital storage oscilloscopes require lower signal levels than this ratio provides at voltages exceeding 200 kV and further attenuation is needed. Attenuators are used at the recorder end of the signal cables. The divider and attenuators must have adequate bandwidth for the frequency range of interest. A resistive divider must have sufficiently fast transient response to precisely measure steep impulse voltages such as the 1.2 μs front time standard lightning impulse. It must have a stable divider ratio for the voltage, temperature and humidity range of use. The voltage coefficient and environmental effects must be negligible. Mechanical effects that unfortunately have been ignored in many cases are also important. The divider ratio must not be affected by these factors as well.
4.2 Resistive Voltage Divider Design

4.2.2 Configuration and Construction

The dimensions of the NIST4 divider are shown in figure 50. The high voltage arm consists of a noninductive wire-wound resistor immersed in an oil-filled column, permitting a compact configuration. The high-voltage arm can be physically shorter in oil than in air since the flashover voltage along the arm when immersed in transformer oil is much higher than in air. The high-voltage arm is only 0.3 m in length while those of most conventional 300 kV free-standing dividers are typically more than three times that length. The diameter of the high-voltage arm is only 2.54 cm, which is also smaller than most other dividers having comparable voltage ratings.

There are several advantages to make the divider so compact. The compact configuration makes the high-voltage arm’s stray capacitance and self-inductance much less than what is possible when air is used as the insulating medium. Lower stray capacitance gives the divider a faster transient response. Because the high-voltage arm is shorter, it has a more uniform voltage distribution along its length than otherwise possible, which provides a more linear scaling of the voltage at the divider output.
A high voltage measuring system consists of more than just the divider, however. A high voltage lead is used to connect the test object to the divider, and this lead makes the step response for the entire measurement system slower than that for the divider alone. To reduce effects arising from other grounded or charged objects on the measurements, the IEC Standard recommends that the lead be at least as long as 1.5 times the height of the divider [103]. A shorter divider means that a shorter high voltage lead may be used without introducing significant proximity effects, and the measurement system will have a faster overall transient response.

Other advantages of using oil insulation are better heat dissipation and reduction of environmental effects. A high-voltage arm immersed in oil has much better heat conduction than one in air so that temperature effects are smaller. Leakage currents on the surface of the high-voltage arm are negligible and unaffected by humidity, since the arm is in oil. The column containing the oil and the high-voltage arm is placed on a grounded metal cylinder so that the high-voltage arm’s resistance and the voltage divider ratio would be unaffected by column’s surface resistance regardless of how high the humidity in the test area is.

Most external mechanical forces act on the oil-filled column instead of acting directly on the high-voltage arm itself as is the case with most free-standing resistive dividers. In this way, effects of mechanical strain on the resistance of the high-voltage arm are minimized. It is shown later in this section how important these effects are to the value of the resistance.

It is important the there be no significant corona from the divider or leads when high voltage is applied. It was found that the high-voltage arm immersed in oil was corona-free under 300 kV impulse by observation with a micro-channel plate image intensifier camera in a darkened room. Different high-voltage leads were also investigated in this manner. Leads of 2.54 cm or smaller diameter were seen to have substantial corona at that voltage. Although leads having diameters exceeding 10.2 cm (4 in) were seen to be corona-free, it is not convenient to use such large leads. It was found that a 1 mm diameter lead in an oil-filled tube was also corona-free. Use of this type of lead can provide a corona-free impulse measuring system, at least to the 300 kV level.

A specially-designed ring is employed at the bottom of the high-voltage arm of the NIST4 divider. Unlike similar rings used for capacitive grading with most 300 kV resistive dividers, the ring used was specifically designed to shield the lower part of the high-voltage arm to reduce noise pickup instead of providing improved voltage distribution along the high-voltage arm. It was seen from calculations based on circuit models for 10 kΩ resistive dividers that high-frequency noise on the high voltage leads and top rings of the dividers should be greatly damped by the 10 kΩ resistance of the high-voltage arm. In step response measurements with most resistive dividers, however, significant noise still appears. It was found through comparison of different shielding configurations that most of the noise in the measured signal is picked up by the lower part of high-voltage arm where the resistance may not be high enough to
attenuate radiated noise. It is therefore necessary to have an effective shielding ring at the bottom of the high-voltage arm to eliminate this noise and provide an undistorted signal. Figure 51 shows the step response with and without several different bottom rings. The final version of the ring used in the NIST4 divider was located very close to the bottom part of high-voltage arm to obtain the best shielding. A compromise was made to get both minimal signal distortion and fast response. A larger ring of a small diameter surrounding the bottom end of the high-voltage arm would have been more effective for shielding, but the increased capacitance between the high-voltage arm and the ring would produce a slower transient response. Additionally, care must be taken to avoid flashover between the ring and high-voltage arm. The ring used here was small, having an inside diameter of 5.1 cm (2 in) and a height of 5.1 cm (2 in). The NIST4 divider’s step response shown in figure 52 is faster and less distorted by noise than those of the other 300 kV free-standing dividers, such as the NIST3 divider which has a large big bottom ring of 1 meter in diameter.

There are two parts that shield the top of the NIST4 divider. One is a sphere 10.2 cm (4 in) in diameter on top of the divider that is used to reduce electrical field stresses and eliminate corona. The second shield is a copper cap located inside the oil column to provide the fast response and better voltage distribution along the high-voltage arm. The cap was empirically designed so that the fastest step response possible was achieved with acceptable overshoot. The edge of the cap was made of a 1.27 cm

Figure 51. Step Response With and Without Bottom Rings.
Figure 52. NIST4 Step Response.
(0.5 in) diameter copper tube to ensure that corona would not be produced at the rated voltage.

The resistive wire used in the high-voltage arm of the NIST4 divider was an alloy-type wire having a temperature coefficient of -3 ppm per degree centigrade. Its diameter of 0.11 mm (0.0045 in) is thicker than that used in most other resistive dividers, giving the high-voltage arm a greater heat capacity and lower temperature increase after application of high voltage impulses. The low temperature coefficient, larger diameter of the wire, and the thermal conductivity of the oil keep the divider's resistance very stable during environmental temperature changes or when several applications of full lightning impulses are made. The resistance of the high-voltage arm was measured with a resistance bridge to be 10.074 kΩ at room temperature. Immediately following the application of ten consecutive standard lightning impulses of 325 kV peak voltage over a period of 75 seconds, the measured resistance was 10.075 kΩ. The difference in resistance can be considered a negligible change. The low-voltage arm's measured resistance had the same value of 12.513 Ω both before and after the ten impulses.

The temperature coefficient of resistance for the high-voltage arm depends not only upon heating of the wire but also upon the changing mechanical stresses of the wire. An interesting experiment investigating temperature and mechanical effects was conducted. Three sample resistors of the same diameter were made with resistive wire and placed into an oven. The first sample was a simple wire loop. The second was wound on a polyethylene rod and the third was wound on a machinable glass ceramic rod. Table 1 shows the change in resistance after heating the resistors from 20°C to 60°C. The resistance of the sample wound on the polyethylene rod had been changed 0.08 % after heating to 41°C. It is believed that this is not due to the temperature coefficient of the winding, but rather to the thermal expansion of the rod during heating which resulted in a strain-induced resistance change. Changes in resistance of this magnitude are unacceptable for reference measurement systems. The machinable glass ceramic had a very good resistance stability at high temperature. Table 2 shows the linear thermal coefficient of expansion for a few materials that are candidates for substrates on which to wind the resistive wire. The glass ceramic has an expansion coefficient ten times smaller than the other three commonly-used materials. As a result, it was selected for NIST4 divider as a base for the high-voltage arm.

The high-voltage arm was wound in the typical manner for resistive dividers. Two layers of windings are counterwound to minimize inductance. The inner one is wound in clockwise fashion and the outer one in counterclockwise fashion. The difference between the windings of the NIST4 divider and most air-insulated dividers is that the rod on which the wire is wound has a much smaller diameter and separation between turns. There are 65.7 turns per centimeter (167 turns per inch). From prior experience[110], it is known that the smaller the rod diameter and the more closer the spacing of the windings are, the smaller the net magnetic flux produced by the two windings will be. These are important considerations in minimizing the residual inductance of the wound resistor. The windings begin on a brass end cap and
Table 1. Resistance Change of Resistor Samples During Heating.

<table>
<thead>
<tr>
<th>T(°C)</th>
<th>Simple Wire Loop(kΩ)</th>
<th>Polyethylene Rod(Ω)</th>
<th>Glass Ceramic Rod(kΩ)</th>
</tr>
</thead>
<tbody>
<tr>
<td>20</td>
<td>0.59433</td>
<td>2.5204</td>
<td>10.0777</td>
</tr>
<tr>
<td>41</td>
<td>-</td>
<td>2.5224</td>
<td>-</td>
</tr>
<tr>
<td>62</td>
<td>0.59431</td>
<td>-</td>
<td>10.0784</td>
</tr>
</tbody>
</table>

Table 2. Linear Thermal Coefficients of Expansion of Candidate Substrates.

<table>
<thead>
<tr>
<th>Polyethylene</th>
<th>Polytetrafluoroethylene</th>
<th>Nylon</th>
<th>Glass Ceramic</th>
</tr>
</thead>
<tbody>
<tr>
<td>1.7 x 10^{-4}</td>
<td>1.0 x 10^{-4}</td>
<td>1.5 x 10^{-4}</td>
<td>9.4 x 10^{-6}</td>
</tr>
</tbody>
</table>

continue along the ceramic rod to the opposite brass end cap. After the first layer was wound, an epoxy coating was applied to provide insulation between the windings. The second layer of wire was then counterwound on top of the first. The epoxy layer used between the windings is thin, compatible with transformer oil, and long-lasting at temperatures below 105°C. Since it is thin, the diameters of the inner and outer windings are nearly the same, which also helps to reduce the overall inductance of the resistor. After both windings were complete, their ends were secured with screws to the brass end caps to ensure that there is no mechanical stress on the wires caused by moving the divider.

The low-voltage arm of the NIST4 divider has low inductance, high wattage, and good shielding. It comprises sixteen 200Ω, 1W tin oxide resistors in parallel. There are two shields for the low-voltage arm, an inner cylindrical copper shield and an outer steel cylinder. Together they provide excellent shielding to electromagnetic interference. The measured step response for the low-voltage arm is shown in figure 53, from which the risetime is calculated to be less than 1 ns.

4.3 The Unit Step Response (USR) and Its Application

4.3.1 Step Response Measurement

Step responses of the NIST4 divider were taken using different damping resistors in the circuit. The geometry used for the step response measurements is the horizontal loop configuration shown schematically in figure 54. In this configuration, the mercury-wetted relay used to generate the voltage step is mounted on a support
Figure 53. Step Response of the Low-Voltage Side of NIST4
at a height of about 1 m above the ground plane and connected to ground with a wide copper strip labeled G in the figure. As mentioned previously, the step response is changed by the diameter and length of the leads connecting the step generator to the divider. A comparison of the step responses for several different leads is shown in figure 55. As seen from the figure, the thinner and longer the lead, the worse the step response, having longer risetimes, greater overshoot, and more oscillations.

Table 3 compares the step response parameters $T_r$ (experimental response time), $T_o$ (partial response time), and $T_d$ (initial distortion time) for the NIST4, NIST3, and NIST1 dividers, taken with different damping resistances $R_d$. 

**Figure 54.** Horizontal Loop Configuration for Step Response Measurement
Figure 55. Comparison of Step Responses for Different Lead Lengths
The NIST3 and NIST1 dividers are conventional air-insulated, free-standing resistive devices rated for 300 kV and 1 MV impulses, respectively. Figure 56 shows a comparison of the step responses for these dividers. Compared with other 300 kV dividers used in reference systems such as NIST3, the NIST4 divider's step response was much faster and less distorted. For the undamped cases, (i.e., no external damping resistor in the step response circuit), the 10%–90% risetime of the step responses for the three dividers is summarized in table 4. The NIST4 divider clearly has a much-improved risetime.

4.3.2 Convolution Calculation

The convolution technique can be used with the measured step response to predict the output of an impulse measurement system for an assumed analytical or numerical input. This approach, performed in the time domain, has been presented previously [111]. A frequency-domain convolution method for estimating measurement errors is now described.

For a linear system with an input step voltage \( L(t) \) and an impulse response \( H(t) \), the step response \( G(t) \) is:

\[
G(t) = H(t) * L(t)
\]

(14)
4.3 The Unit Step Response (USR) and Its Application

Table 3. Step Response Parameters for Three Reference Dividers

<table>
<thead>
<tr>
<th>Divider</th>
<th>R_d (Ω)</th>
<th>T_n (ns)</th>
<th>T_α (ns)</th>
<th>T_o (ns)</th>
<th>Overshoot (%)</th>
</tr>
</thead>
<tbody>
<tr>
<td>NIST4</td>
<td>0</td>
<td>0.3</td>
<td>5.3</td>
<td>0.6</td>
<td>37.5</td>
</tr>
<tr>
<td></td>
<td>250</td>
<td>5.5</td>
<td>8.8</td>
<td>0.6</td>
<td>15.2</td>
</tr>
<tr>
<td></td>
<td>500</td>
<td>14</td>
<td>14.3</td>
<td>0.2</td>
<td>1.7</td>
</tr>
<tr>
<td>NIST3</td>
<td>0</td>
<td>19</td>
<td>17</td>
<td>2.6</td>
<td>24</td>
</tr>
<tr>
<td></td>
<td>150</td>
<td>23</td>
<td>20</td>
<td>1.8</td>
<td>11</td>
</tr>
<tr>
<td></td>
<td>350</td>
<td>28</td>
<td>29</td>
<td>1.3</td>
<td>3</td>
</tr>
<tr>
<td></td>
<td>550</td>
<td>36</td>
<td>36</td>
<td>0.8</td>
<td>1</td>
</tr>
<tr>
<td>NIST1</td>
<td>0</td>
<td>23</td>
<td>27</td>
<td>2.9</td>
<td>39</td>
</tr>
<tr>
<td></td>
<td>150</td>
<td>33</td>
<td>36</td>
<td>2.7</td>
<td>14</td>
</tr>
<tr>
<td></td>
<td>250</td>
<td>41</td>
<td>44</td>
<td>1.7</td>
<td>6</td>
</tr>
<tr>
<td></td>
<td>400</td>
<td>52</td>
<td>53</td>
<td>1.8</td>
<td>2</td>
</tr>
</tbody>
</table>

Table 4. Rise Time (ns) Comparison for Three Reference Dividers

<table>
<thead>
<tr>
<th></th>
<th>NIST4</th>
<th>NIST3</th>
<th>NIST1</th>
</tr>
</thead>
<tbody>
<tr>
<td>Rise</td>
<td>11</td>
<td>40</td>
<td>52</td>
</tr>
</tbody>
</table>
Table 5. Calculated Peak Voltage Outputs of NIST4 Divider

<table>
<thead>
<tr>
<th>$R_d$ (Ω)</th>
<th>Full lightning (front-time 0.915 μs)</th>
<th>Chopped lightning (Chopped at 88% of the peak, Time-to-chop 0.566 μs)</th>
<th>Chopped lightning (Chopped at 98% of the peak, Time-to-chop 0.957 μs)</th>
</tr>
</thead>
<tbody>
<tr>
<td>0</td>
<td>1.0000</td>
<td>0.9991</td>
<td>0.9993</td>
</tr>
<tr>
<td>250</td>
<td>1.0000</td>
<td>0.9948</td>
<td>0.9990</td>
</tr>
<tr>
<td>500</td>
<td>1.0000</td>
<td>0.9914</td>
<td>0.9983</td>
</tr>
</tbody>
</table>

where the "∗" represents the convolution integral. Similarly, for an input signal $X(t)$ the corresponding output signal $Y(t)$ is:

$$Y(t) = H(t) \ast X(t)$$  \hspace{1cm} (15)

In frequency domain, if $G(t)$, $L(t)$, $H(t)$, $X(t)$, and $Y(t)$ have Fourier transforms $G(f)$, $L(f)$, $H(f)$, $X(f)$, $Y(f)$ respectively, then

$$G(f) = H(f) \cdot L(f)$$  \hspace{1cm} (16)

$$Y(f) = H(f) \cdot X(f)$$  \hspace{1cm} (17)

From (16) and (17),

$$Y(f) = \frac{X(f) \cdot G(f)}{L(f)}$$  \hspace{1cm} (18)

From this formula, if a system’s step response is known, one can predict an output for any given input signal by taking the inverse Fourier transform of equation (18). Full standard lightning impulses along with the chopped lightning impulses shown in figure 57 were used as input signals to calculate corresponding output of the NIST4 divider. Table 5 gives some of the peak values of the output waveforms for normalized inputs.

The data of table 5 indicate that the NIST4 divider can measure the peak voltage of full lightning impulses with negligible error. The data also show that the NIST4 divider has less than 1% error in peak voltage measurement of front-chopped lightning impulses.
Figure 57. Typical (a) Full and (b) Chopped Lightning Impulses
4.4 Conclusion

A new, compact resistive voltage divider has been designed, constructed, and characterized for use as part of an impulse voltage measurement system. Although rated for impulse voltages up to 300 kV, it stands only 0.3 m tall. It has significant advantages over other free-standing dividers because of its small physical size, oil insulation, and shielding. The small physical size gives it a response time that is nearly a factor of four times faster than references dividers with comparable voltage ratings while the oil insulation provides much better insensitivity to environmental effects, such as temperature changes and humidity than air-insulated dividers do. A specially-designed shield for the bottom of the high-voltage side of the divider further reduces distortion of the divider output by minimizing the pickup of spurious signals. The divider's measured step response of 10 ns is much faster than comparable free-standing dividers. The NIST4 divider represents significant improvement in the measurement of high voltage standard lightning impulses with free-standing resistive voltage dividers.
REFERENCES

4. REFERENCES


[6] The theory of calculating current distributions in flat conductors that undergo a sudden change in width is described by Smythe [W.R. Smythe, Static and Dynamic Electricity, pp. 254-256 (McGraw-Hill, New York, 1968)] using a conformal mapping technique. Figure 9 shows a calculated current distribution assuming the conductor width changes by a factor of four.


REFERENCES


REFERENCES


REFERENCES


REFERENCES


4. TITLE AND SUBTITLE
Research for Electric Energy Systems - An Annual Report

5. AUTHOR(S)
William E. Anderson, Editor

6. PERFORMING ORGANIZATION (IF JOINT OR OTHER THAN NIST, SEE INSTRUCTIONS)
U.S. Department of Commerce
National Institute of Standards and Technology
Gaithersburg, MD 20899

9. SPONSORING ORGANIZATION NAME AND COMPLETE ADDRESS (STREET, CITY, STATE, ZIP)
Department of Energy
Division of Electric Energy Systems
1000 Independence Avenue, SW
Washington, DC 20585

11. ABSTRACT (A 200-WORD OR LESS FACTUAL SUMMARY OF MOST SIGNIFICANT INFORMATION. IF DOCUMENT INCLUDES A SIGNIFICANT BIBLIOGRAPHY OR LITERATURE SURVEY, MENTION IT HERE.)
This report documents the technical progress in four investigations which make up the project "Support of Research Projects for Electrical Energy Systems," funded by the U.S. Department of Energy and performed by the Electricity Division of the National Institute of Standards and Technology (NIST). Specifically these investigations include: 1) Measurements of magnetic fields in support of epidemiological and in vitro studies of biological field effects; 2) development of a technique to measure trace amounts of SF$_6$ in the presence of SF$_{10}$ and the development of an improved stochastic analyzer for pulsating phenomena; 3) optical and electrical measurements of negative streamers preceding electric breakdown in liquid dielectrics; and 4) the development of a reference resistive divider for high voltage impulse measurements. The work discussed in this report is part of an ongoing research activity at NIST.

12. KEY WORDS (4 TO 12 ENTRIES; ALPHABETICAL ORDER; CAPITALIZE ONLY PROPER NAMES; AND SEPARATE KEY WORDS BY SEMICOLONS)
corona discharges; dielectric liquids; electrical insulation; electro-optical measurements; fast transients; gaseous dielectrics; magnetic-field measurements; magnetic field probes; partial discharges; prebreakdown phenomena; SF$_{10}$; sulfur hexafluoride

13. AVAILABILITY
XX UNLIMITED

FOR OFFICIAL DISTRIBUTION. DO NOT RELEASE TO NATIONAL TECHNICAL INFORMATION SERVICE (NTIS).

ORDER FROM SUPERINTENDENT OF DOCUMENTS, U.S. GOVERNMENT PRINTING OFFICE,
WASHINGTON, DC 20402.

X ORDER FROM NATIONAL TECHNICAL INFORMATION SERVICE (NTIS), SPRINGFIELD, VA 22161.

14. NUMBER OF PRINTED PAGES
105

15. PRICE
A06