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CSIR: A Two-Dimensional Finite Element Charge-Sheet Model of MOSFET's Including Radiation-Induced Interface and Oxide Charge

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CSIR: A TWO-DIMENSIONAL FINITE ELEMENT CHARGE-SHEET MODEL OF MOSFET'S INCLUDING RADIATION-INDUCED INTERFACE AND OXIDE CHARGE

C. L. Wilson and J. L. Blue

U.S. DEPARTMENT OF COMMERCE National Bureau of Standards National Engineering Laboratory Center for Electronics and Electrical Engineering Semiconductor Devices and Circuits Division Washington, DC 20234

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U.S. DEPARTMENT OF COMMERCE, Malcolm Baldrige, Secretary NATIONAL BUREAU OF STANDARDS, Ernest Ambler, Director

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CS1R: A Two-Dimensional Finite Element Charge-Sheet Model of MOSFETs Including Radiation-Induced Interface and Oxide Charge

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Abstract

A two-dimensional charge-sheet model including radiation-induced interface and oxide effects in short-channel MOS transistors has been developed. The unique feature of the model is that the effects of channel inversion layer charge, interface charge, and oxide charge are included as a nonlinear integral boundary condition on the two-dimensional electrostatic field in the transistor. The average inversion layer charge density and source-drain current are obtained directly from the model rather than from the electron density or electron quasi-Fermi level. The model retains all of the physical detail of more complex two-dimensional models such as sensitivity to source-drain profile shape, channel profile, and oxide field shape. This allows the model to represent the changes in drain current associated with short-channel effects while still allowing simple comparison with long-channel models.

The numerical solutions were obtained using general-purpose software for solving elliptic partial differential equations. Problems with exact solutions have been solved to test the correctness and accuracy of the codes. Also, the physics included in this model and the geometry of the transistor can be easily changed. The finite element method used allows refinement of oblique triangles which is important in achieving computational efficiency.

Key words: finite elements; interactive graphics; MOS transistors; radiation effects.

1. Introduction

A two-dimensional formulation of a charge-sheet model of an MOS transistor and an associated computer program are presented. This formulation differs from the formulation of De La Moneda [1] in that it includes the effects of source-drain channel shape and arbitrary channel doping profile shape. The formulation differs from the formulation proposed by Brews [2] in that strong two-dimensional electro-† The work of the first author sponsored by the Defense Nuclear Agency under Task X99QAXVX, Work Unit 00076. static effects are included by solving Poisson's equation using adaptive finite element techniques in the bulk semiconductor. In this formulation, a new approach that differs from both [1] and [2] is used to couple the one-dimensional current to the two-dimensional potential. The effects of the charge in the inverted channel of the transistor are included as a nonlinear boundary condition at the interface between the semiconductor and the gate oxide.

The principal modification of the program, from the original CS1 [3,4] program, is accomplished by modifying the surface boundary condition. The primary effect of ionizing radiation on MOSFETs is the introduction of oxide trapped charge (OTC), interface trapped charge (ITC), and the reduction of channel mobility caused by scattering from charge in interface traps. Both of the charge effects must be included in the oxide interface boundary condition. The OTC is independent of device operating voltage after irradiation, while the charge state of the ITC is dependent on gate bias in the subthreshold and weak inversion regions since the probability of these traps being occupied is a function of the local surface potential in the two-dimensional model. Inclusion of these two charge components in device models introduces a nonscalable component into the calculation of the total effective channel charge in short-channel transistors.

The charge-sheet formulation allows the two-dimensional electrostatic field and drain current to be calculated without the inclusion of a two-dimensional current continuity equation. This results in a great improvement in computational efficiency which allows finite element model calculations to be performed on a minicomputer. This model is accurate in all regions of inverted transistor operation and works well even in regions of operation where the channel current produces large changes in the electrostatic potential in the channel. The model retains the computational efficiency of single equation models [5] without imposing the computer requirements of coupled equation models [6,7,8]. The complexity and cost of the model lie between the long-channel one-dimensional model of Brews, which runs well on a desk top calculator, and the coupled equation models [5], the two-dimensional charge-sheet model works in all regions of inverted transistor operation including weak inversion. Use of the finite-element method also allows the adaptive mesh procedures [9] previously applied to MESFETs [10] to be applied to MOSFETs.

In section two, the formulation of the two-dimensional charge-sheet model and the effect of ITC and OTC at the semiconductor-oxide interface are discussed. In this formulation, the total channel current is computed as a function of the twodimensional electrostatic potential. The computation of total channel current allows the effects of these mobile and fixed charges to be treated as an effective surface charge and to be included in subsequent calculations of the electrostatic potential as a nonlinear integral boundary condition.

In section two, the numerical procedures used to calculate the electrostatic potential in two dimensions with a nonlinear boundary condition are also discussed. The partial differential equation is transformed into a system of nonlinear equations using adaptive, computer-generated, finite elements. The nonlinear field equations are solved using a damped Newton's method. The resultant system of linear equations is solved either by direct methods or by a multilevel iteration.

In section three, the specific procedures used to implement the model are discussed. The structure of the computer program is discussed and the function of each of the principal modules is outlined. The installation requirements of the program are discussed as are the sources of the software components which were developed by other authors. The physical limitations of the model are then discussed.

In section four, the modeling of a set of irradiated MOS transistors is discussed.

2. Theory

A. Two-Dimensional Charge-Sheet Model

The two-dimensional charge-sheet model used in this work couples the effects of the interface trapped charge and the oxide trapped charge to short-channel effects seen in unscaled MOSFETs. In this work, a two-dimensional finite element model of short-channel MOSFETs is applied which allows the effects of ITC and OTC, as well as radiation-induced channel mobility degradation, to be included in a twodimensional short-channel MOSFET model. The basic formulation of the model includes a two-dimensional calculation of the electrostatic potential in the channel region and in the oxide and a one-dimensional calculation of the channel inversion layer current. This simplification is achieved by making assumptions based on the basic semiconductor equations:

$$\nabla \cdot (\kappa \nabla \psi) = -\frac{q}{\epsilon_0} (p - n + N) \tag{1}$$

$$\nabla \cdot (\mu_n \, n \, \nabla \, \phi_n) = \frac{\partial n}{\partial t} + R \tag{2}$$



Figure 1. Geometry of the charge-sheet model.

$$\nabla \cdot (\mu_p \, p \, \nabla \, \phi_p) = \frac{\partial p}{\partial t} - R, \tag{3}$$

where the electron density, n, and the hole density, p, are:

$$n = n_i \exp(q(\psi - \phi_n)/kT) \tag{4}$$

$$p = n_i \exp(q(\phi_p - \psi)/kT), \tag{5}$$

and where Shockley-Read-Hall recombination is given by:

$$R = \frac{(pn - n_i^2)}{\tau_{n0}(n + n_1) + \tau_{p0}(p + p_1).}$$
(6)

The symbols have their usual meaning as defined in [12].

The simplification to a single two-dimensional equation and one-dimensional current flow is achieved by assuming that R = 0, which eliminates (6), and that the hole quasi-Fermi potential is pinned at the substrate potential, $\phi_p = V_{sub}$. This is then used to replace (5) and eliminate (3). If in addition the channel current is assumed to flow only in a one-dimensional sheet at the surface, the problem is reduced to solving (1) and:

$$n(y) = \frac{n_i}{\mu_n^*} \int_0^\infty dx \exp(\beta \psi) \mu_n \left[1 + (\exp(-\beta V_D) - 1) \frac{\int_0^y \frac{dy_0}{\int_0^\infty dx \exp(\beta \psi) \mu_n}}{\int_0^L \frac{dy_0}{\int_0^\infty dx \exp(\beta \psi) \mu_n}} \right].$$
 (7)

Equation (7) then replaces (2). The effects of OTC and ITC are included in the oxide solution and in the interface boundary condition connecting the oxide field solution to the solution in the bulk semiconductor. One of the advantages of the finite element formulation of the model is that the interfacial charge can be treated exactly in the calculation of the finite element equations and in oxide boundary conditions. If in addition the depletion in the source and drain regions is neglected, the problem is reduced to the geometry shown in figure 1.

In this formulation of the problem, the OTC and ITC are given by:

$$Q_{itc} = f(Dose) \tag{8}$$

$$Q_{otc} = g(Dose) \nabla \psi_{ox} \tag{9}$$

where:

$$Q_{itc}(\phi_S) = \int_{E_v}^{E_c} \frac{Q(E_d)dE_d}{1 + g_d \exp((\phi_S - E_d)/kT)} - \int_{E_v}^{E_c} \frac{Q(E_a)dE_a}{1 + g_a^{-1} \exp((E_a - \phi_S)/kT)}$$
(10)

$$Q_{itc}(\phi_S) \approx \sum_{\Delta E} \frac{Q(E_d) \Delta E_d}{1 + g_d \exp((\phi_S - E_d)/kT)} - \sum_{\Delta E} \frac{Q(E_a) \Delta E_a}{1 + g_a^{-1} \exp((E_a - \phi_S)/kT)}$$
(11)

The specific relationships between dose and these charge components in (8) and (9) are very technology specific and must be determined by the program user.

B. Numerical Procedures

An important feature of this work is that the numerical solutions were obtained using general-purpose software for solving elliptic partial differential equations (PDEs). Although some efficiency is sacrificed, the benefits obtained by using the generalpurpose software far outweigh the loss in efficiency. Problems with exact solutions have been solved to test the correctness and accuracy of the codes and to determine optimal strategies and optimal values for parameters in the code. The physics included in the model and the geometry of the problem can be easily changed. The numerical software was inspired by finite-element software of Bank and Sherman [9] and retains most of their philosophy.

This version of the package solves the PDE

$$\nabla \cdot [a(x, y, u)\nabla u] = f(x, y, u, \partial u/\partial x, \partial u/\partial y)$$
(12)

in a region bounded by straight line segments and circular arc segments. On each segment of the boundary, u must obey one of two types of boundary conditions (1):

$$g(x, y, u) = 0 \tag{13}$$

or (2)

$$\partial u/\partial \mathbf{n} + g(x, y, u) = 0.$$
 (14)

This is a fairly general example of a PDE arising from conservation of a flux and includes both Poisson's equation and the hole and electron continuity equations (in the multiple-PDE version).

At the heart of the package is a module which solves a linear elliptic PDE using linear finite elements on a mesh of triangles. (Boundary "triangles" may have one curved side.) The initial triangulation is an input to the package; succeeding triangulations are calculated adaptively by the package.

For a given triangulation with M vertices, the calculation proceeds as follows.

The M finite-element basis functions $\{b_m\}$ are linear on each triangle; b_m is 1 at vertex m and 0 at all other vertices. The set of vertices on type 1 boundaries is denoted by D (for Dirichlet). The solution is approximated by a sum of basis functions

$$u(x,y) = \sum_{m=1}^{M} \alpha_m b_m(x,y). \tag{15}$$

The coefficients are determined by a Galerkin method [13]; the error in the PDE is made orthogonal to each of the basis functions except those in D:

$$\int \int [(-\nabla \cdot (a\nabla u) + f)b_m = 0].$$
m not in D
(16)

The remaining conditions on the b's are that the type 1 boundary conditions hold exactly [13]:

$$g(x_m, y_m, u(x_m, y_m)) = 0, m \text{ in } D.$$
(17)

Equation (16) is integrated by parts to yield

$$\int \int (a\nabla u \cdot \nabla b_m + fb_m) + \int_2 agb_m = 0, \qquad (18)$$

where the single integral is over the type-2 parts of the boundary only. Equations (17) and (18) comprise M nonlinear equations in M unknowns, the coefficients $\{\alpha_m\}$.

The M nonlinear equations are solved by an iterative process, a damped Newton's method. Let v be the Newton step and use a fraction of v as a correction to u; v has the same form as u,

$$v(x,y) = \sum_{m=1}^{M} \beta_m b_m(x,y).$$
 (19)

To calculate v, replace u by u + v in eqs (17) and (18) and linearize in v. The linearization of eq (17) yields

$$g(x_m, y_m, u_m) + \frac{\partial g(x_m, y_m, u_m)}{\partial u} \beta_m = 0, \text{m in } D, \qquad (20)$$

and the linearization of eq (18) yields

$$\begin{cases} a\nabla v \cdot \nabla b_m + \frac{\partial a}{\partial u} v\nabla u \cdot \nabla b_m + b_m \left(\frac{\partial f}{\partial u}v + \frac{\partial f}{\partial(\partial u/\partial x)}\frac{\partial v}{\partial x} + \frac{\partial f}{\partial(\partial u/\partial y)}\frac{\partial v}{\partial y}\right) \\ + \int_2 \left(g\frac{\partial a}{\partial u} + a\frac{\partial g}{\partial u}\right) b_m = -\int \int \left(a\nabla u \cdot \nabla b_m + fb_m\right) - \int_2 agb_m \equiv r_m \end{cases}$$
(21)

Substituting for u and v from eqs (15) and (19) and doing the integrals numerically gives a set of M linear equations for the correction coefficients $\{\beta_m\}$. These linear equations are sparse; there are typically only nine nonzero elements per row, on average, and M can be a few hundred or a few thousand. A satisfactory way to solve these equations is directly, with Gaussian Elimination, using the Yale Sparse Matrix Package [14].

Unless u is close to a solution of the nonlinear finite-element equations, u + v may be worse than u. A damped Newton's method is used: replace u by $u + \lambda v$, where λ is chosen so that $\max_{m} |r_{m}(u+v)| < \max_{m} |r_{m}(u)|$. This avoids divergence of the iterative process.

In practice, the initial triangulation may be too coarse to give the desired accuracy or may need local refinement to represent the solution accurately in a region of high curvature. After the package has converged to an approximate solution on the initial triangulation, the approximate solution may be used to estimate the error and produce a new and finer triangulation adaptively. There are various ways to approximate the error in each triangle. For the present work, a simple method is used. In the silicon, the PDE is

$$\nabla^2 \psi = -\rho/\epsilon. \tag{22}$$

Since ψ is linear in each triangle, $\nabla^2 \psi = 0$. We estimate the relative error in each triangle by

$$\left| \int \int_{triangle} \rho(x, y) \right|. \tag{23}$$

The refined triangulation is obtained by dividing the triangles with the largest

estimated errors, such as all triangles with estimated error larger than 1/4 of the largest error.

For the refined triangulation, the previously calculated u is a good guess at the new u, so that few Newton iterations should be necessary. The hardest work is done on the initial triangulation, the one with the fewest vertices.

If there are two or more triangulations, the linear equations on the finest triangulation may be solved by a multilevel iteration [15,9], saving both time and storage space. However, for the present problem, sufficient accuracy could be obtained with M of only a few hundred, so that a direct solution using the Yale Sparse Matrix Package was quite adequate.

Using this procedure, the solution of eqs (1) and (7) is started by first obtaining a trial solution for the linearized form of eq (1), using the solution of eq (7) obtained from the one-dimensional charge-sheet model with the total charge as a boundary condition. The Jacobian of g required for the solution of eq (20) contains the Jacobian of eq (1). This Jacobian is approximated by

$$\frac{\partial g}{\partial u} = q\beta(n(y) + Q_{itc} + Q_{otc}).$$
⁽²⁴⁾

Once the surface charge and approximate local field term are obtained from the one-dimensional model and a local-field condition, the field term associated with the oxide is obtained using a fast Poisson solver [16]. The trial solution is then used to obtain a solution for eq (7) by quadrature and an additional fast Poisson solution in the oxide. This iterative procedure is repeated for each Newton step until the requested convergence is obtained or the specified maximum iteration count is reached.

3. Computer Implementation

A. Software Modules

The distributed source of the CS1R program is divided into four files: CS1R.FOR, SYSTEM.FOR, PDESUB.FOR, and DEVLIB.FOR. These four files conform to ANSI 66 FORTRAN IV and can be compiled on any FORTRAN compiler which meets this standard. The files CS1R.HLP, CS1R.EXP, and CS1R.LNK are also provided. CS1R.HLP provides a set of user instructions identical to Appendix A of this report. CS1R.EXP contains an example set of program input and output which is identical to Appendix B of this report. The file CS1R.LNK is a sample set of linkage control statements which have been used to link the program on the DEC VAX 11/780^{*} under the VMS^{*} system.

The file CS1R.FOR is the actual charge-sheet model program. This file contains the subroutines which control input and output, model initial approximations, find the oxide field solution, and contain the calls to the subroutines which solve the partial differential equation. The starting approximation is identical to the charge-sheet model originally developed by Brews [2]. The output of this long-channel model is printed at the beginning of each CS1R calculation. The oxide solution is calculated using the fast methods discussed in reference [16]; these subroutines are in the file DEVLIB.FOR. A complete copy of the Swarztrauber and Sweet package [16] is not included. Only those parts of the package that are used by CS1R are included.

The CS1R module of the program contains parameters TOL and IP(6) which are used to control the accuracy of the solution. The parameter TOL is used to control the iteration accuracy at each multigrid level. The parameter IP(6)is used to control the number of multigrid levels. These parameters are set to yield very accurate solutions in the version of the program which is distributed. This level of accuracy greatly exceeds that required for most applications, but is necessary, during installation and testing, to verify that the program has been correctly installed. Resetting these parameters to lower accuracy by increasing the iteration tolerance and/or decreasing the number of multigrid levels will greatly improve run times.

The file SYSTEM.FOR contains subroutines which are used in the other three program files but which are system dependent. The subroutines FOPEN and FCLOSE are used to open and close input and output files. In the VAX VMS version supplied on the tape, the file FCLOSE is a dummy subroutine. The subroutines ISTIME and IFTIME are used to start and stop clocks which are used to measure the execution times of the parts of the partial differential solution process. If these routines are not used and dummy subroutines are substituted, ISTIME must be less than, NOT equal to, IFTIME. If these subroutines are dummy routines, then the timing information in the output summary will be incorrect.

The subroutines PLTUTL, CURVEA, and ISCALE contain calls to vector graphics subroutines. The calls in the supplied program can be used with the TCS software * Certain commercial equipment, instruments, or materials are identified in this paper in order to adequately specify the experimental procedure. Such identification does not imply recommendation or endorsement by the National Bureau of Standards, nor does it imply that the materials or equipment identified are necessarily the best available for the purpose. supplied by Tektronix* and can be used to drive either Tektronix or Hewlett-Packard* terminals. Other graphics packages can easily be substituted if the necessary initialization, absolute motion, and absolute vector drawing primitives are available in either software or terminal firmware. If these subroutines are made into dummy subroutines, graphics output will not be available from the program except through the plot output file. The data written into the plot output file, file 2, are a sequence of non-negative x- and y-coordinate pairs. The first line of the file contains the minimum and maximum values of the x- and y-coordinates. Each plot is terminated by a set (or sets) of negative coordinate pairs. The subroutines R1MACH, D1MACH, and I1MACH are used to set machine constants which are used in the other program modules to set machine-dependent quantities. The original versions of the functions are discussed in reference [17] as are the procedures used to generate these constants for a type of computer which is not presently included in the present list. The conversion of the program from one computer type to another should not require modification of any part of the program which is not in the SYSTEM.FOR module. This assumes that some plotting package is available and that timing subroutines are available on the target computer system.

The module PDESUB.FOR contains the subroutines used to solve the partial differential equations. The theory of these subroutines has been discussed in section 2B above.

The module DEVLIB.FOR contains subroutines used by the other three modules. These subroutines have been obtained from several sources. The error-handling software, memory management software, and machine-independent constant software were obtained from [17]. The fast elliptic solver was obtained from [16]. In the initial approximation, quadrature from [16] and root finding routines from [19] are used. In the PDESUB module, the Yale Sparse Matrix Package is used [14].

B. Physical Restrictions

Two physical restrictions have been imposed in the present implementation of the CS1R program. First, the two-dimensional electric field dependence of the mobility has not been included. Second, the detailed slopes of the source-and-drain doping profiles have not been included in the model.

The first limitation is more serious. In circuit models and in some two-dimensional device simulation programs, the field dependence of the mobility is empirically included using an expression of the form a/(1 + bE) where a and b are empirically determined parameters and E is the magnitude of the electric field. Recent work by Cooper and Nelson [20] suggests that this model is not adequate to characterize

the field dependence of the mobility. On the other hand, the Cooper and Nelson data do not include several effects which are known to affect the low field value of the mobility; these are the effects of bulk doping and oxide interface charge. Since no definitive model for the two-dimensional dependence of the mobility is available, none has been included.

The details of the two-dimensional source-and-drain profiles are included in the model only as two elliptic abrupt junctions. This allows the details of the majority carrier quasi-Fermi level to be neglected and greatly simplifies the program, making the charge-sheet calculation much more efficient. On the other hand, at high source-drain-voltages, this approximation can lead to convergence problems and/or to inaccurate modeling of the potential near the drain. In addition, this model places the burden of specifying lateral and vertical junction depths on the program user. Other available two-dimensional device simulation programs, such as MINIMOS [6], attempt to include simple two-dimensional process models in the device modeling programs. These simplified models do not agree with more complex two-dimensional models [21] or with experimental measurement of two-dimensional junction shape [20]. If the user of the program wishes to use these simplified models, then the work of Kennedy and O'Brien can be used [23]. If more complicated models [21] or experimental data are available, then these can be used.

4. Device Model Verification

The model is verified by comparing the results obtained with the model to n-channel MOSFETs of the type discussed in [24] for doses of 0, 10, 50, 100, and 500 Krad(Si). Prior to irradiation and after each irradiation, the current-voltage characteristics of the transistor were measured. Capacitance data were also taken on a MOS capacitor adjacent to the transistors. All devices were biased with +9 V on the gate or capacitor polysilicon electrode and the source, drain, and substrate grounded. The device used for model verification was chosen with a channel length of 7.8 µm to allow the effects of radiation to be separated from short-channel effects. In this model, the interface traps are treated as a continuous distribution of traps which are populated and depopulated as the surface potential is varied. At doses below 50 Krad(Si), the effect of the energy distribution of the traps is small. Above 50 Krad(Si), the energy distribution becomes important. At a dose of 500 Krad(Si), the effect of energy distribution on subthreshold current is most sensitive to the trap energy distribution. Two-dimensional simulations were then carried out which used fixed oxide charge, a variable distribution of interface traps and channel mobility degradation to model the effects of the radiation.

All of the transistors studied were modeled in the subthreshold region, the triode

region, and the saturation region. The parameters used in these simulations are given in table 1.

Table 1.Simulation Parameters

7.8 μ m
$0.0 \text{ to } 1.75 \times 10^{12} \text{ cm}^{-2}$
0.5 V to 4.0 V, 0.25 V
0.0523 μm
1.5×10^{16} cm ⁻³
$0.710 \mu m$
$0.875 \mu m$

Detailed comparison of the model with measured data shows excellent agreement between the model and measured current-voltage characteristics in the subthreshold region, the triode region, and the saturation region. A typical subthreshold region simulation is compared to measured data in figure 2 for an unirradiated sample. A typical subthreshold region simulation is compared to measured data in figure 3 for a 10 Krad(Si) dose. A typical subthreshold region simulation is compared to measured data in figure 4 for a 50 Krad(Si) dose. A typical subthreshold region simulation is compared to measured data in figure 5 for a 100 Krad(Si) dose.

As the dose is increased above 50 Krad(Si), the effects of the interface trapped charge energy distribution become increasingly important. This effect is illustrated in figures 6 and 7. In figure 6, the subthreshold characteristic of a device irradiated at 500 Krad(Si) is simulated with a uniform energy distribution of traps in the band. In figure 7, the subthreshold characteristic of a device irradiated at 500 Krad(Si) is simulated with an energy distribution of traps in the band that is peaked on the valence band side of the band gap. In both simulations, a total trap density of $1.75 \times 10^{12} \text{ cm}^{-2}$ was used. In the uniform case, the traps are populated continuously as the channel is inverted. In the second case, the populated trap density increases more rapidly as the transistor enters strong inversion.

A typical saturation region simulation is compared to measured data in figure 8 for an unirradiated sample. A typical saturation region simulation is compared to measured data in figure 9 for a 500 Krad(Si) dose. The triode region characteristics, as a function of dose, are compared to measured data in figure 10. In the radiation-hardened n-channel transistor modeled here, the effects of oxide charge and interface charge both increase linearly with dose. These two charges cancel to













Figure 5. A subthreshold region simulation compared to measured data for a 100 Krad(Si) dose, V_d =0.25 V.











Figure 8. A saturation region simulation compared to measured data for an unirradiated transistor.

(Aų) bl



Figure 9. A saturation region simulation compared to measured data for a 500 Krad(Si) dose.

(Ay) bl





(Au) bl

produce a total threshold shift of ≈ 0.25 V at 500 Krad(Si). The resulting increase in interface charge causes a decrease in channel mobility from 760 cm²/V-sec. in the unirradiated device to 257 cm²/V-sec. at 500 Krad(Si). The increase in interface charge also results in an increase in subthreshold current and a decrease in subthreshold slope. Simple linear relationships between dose and both oxide charge and interface charge are sufficient to account for all of these device characteristics.

The model shows that the I-V characteristics of the heavily irradiated device are similar to those of an unirradiated device of much shorter channel length. In the short-channel device, the subthreshold characteristic is degraded by the drain field. In the irradiated device, this subthreshold degradation is caused by the charge in the radiation-induced interface traps.

5. Conclusions

A two-dimensional charge-sheet model of a surface-channel MOS transistor has been developed. When this model is implemented using adaptive finite element methods, an efficient high-accuracy transistor simulation program is possible. The inclusion of interface trap energy distribution allows the characteristics to be modeled for n-channel transistors for doses of up to 500 Krad(Si).

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References

1. De La Moneda, F., Threshold Voltage from Numerical Solutions of the Two-Dimensional MOS Transistor, *IEEE Trans. Circuit Theory* CT-20, 666-673 (1973).

2. Brews, J. R., A Charge-Sheet Model of the MOSFET, Solid-State Electronics 21, 345-355 (1978).

3. Wilson, C. L., and Blue, J. L. Two-Dimensional Finite Element Charge-Sheet Model of a Short-Channel MOS Transistor, Solid-State Electronics 25, 461-477 (1982).

4. Wilson, C. L., and Blue, J. L., Two-Dimensional Finite Element Charge-Sheet Model of a Short-Channel MOS Transistor, National Bureau of Standards report NBSIR 82-2471 (1982). 5. Greenfield, J. A., and Dutton, R. W., Nonplanar VLSI Device Analysis Using the Solution of Poissons's Equation, *IEEE Trans. Electron Devices* ED-27, 1520-1532 (1980).

6. Scherherr, S., Schutz, A., and Potzl, H. W., MINIMOS - A Two-Dimensional MOS Transistor Analyzer, *IEEE Trans. Electron Devices* ED-27, 1540-1549 (1980).

7. Buturla, E. M., and Cottrell, P. E., Two-Dimensional Finite-Element Analysis of Semiconductor Steady-State Transport Equations, Int. Conf. on Computational Methods in Nonlinear Mechanics, Austin, Texas, 1974.

8. Fichtner, W., and Rose, D. J., On the Numerical Solution of Nonlinear Elliptic PDE's Arising from Semiconductor Device Modeling, *Elliptic Problem Solvers*, M. Schultz, Ed. (Academic Press, New York, 1981), pp. 277-284.

9. Bank, R. E., and Sherman, A. H., PLTMG User's Guide, CNA-152, Center for Numerical Analysis, University of Texas at Austin, September 1979.

10. Laux, S. E., and Lomax, R. I., Numerical Investigation of Mesh Size Convergence Rate of Finite Element Method in MESFET Simulation, *Solid-State Electronics* 24, 485-493 (1981).

11. Brews, J. R., Fichtner, W., Nicollian, E. H., and Sze, S. M., Generalized Guide for MOSFET Miniaturization, *Electron Device Letters* EDL-1, 2-4 (1980).

12. Wilson, C. L., and Blue, J. L., Semiconductor Device Simulation, *Elliptic Problem* Solvers, M. Schultz, Ed. (Academic Press, New York, 1981), pp. 435-439.

13. Strang, G., and Fix, G. J., An Analysis of the Finite Element Method (Prentice-Hall, Englewood Cliffs, N.J., 1973).

14. Eisenstat, S. C., Gursky, M. C., Schultz, M. A. and Sherman, A. H., Yale Sparse Matrix Package I. The Symmetric Codes, Research Report #112, Department of Computer Science, Yale University, 1976.

15. Brandt, A., Multi-Level Adaptive Solutions to Boundary-Value Problems, Math. Comp. 31, 333-390 (1977).

16. Swarztrauber, P., and Sweet, R., Efficient FORTRAN Subprograms for the Solution of Elliptic Partial Differential Equations, NCAR Technical Note, NCAR-TN/IA-109, 1975.

17. Fox, P. A., Hall, A. D., and Schryer, N. L., The PORT Mathematical Subroutine

Library, ACM Trans. Mathematical Software 2, 104-126 (1978).

18. Blue, J. L., Automatic Numerical Quadrature - DQUAD, Bell Labs Comput. Sci. Tech. Rep. 25, February 1975; also, Automatic Numerical Quadrature, Bell Syst. Tech. J. 59, 1651-1678 (1977).

19. Brent, R. P., Algorithms for Minimization Without Derivatives (Prentice-Hall, Englewood Cliffs, N.J., 1973), pp. 188-189.

20. Cooper, J. A., Jr., and Nelson, D. F., Measurement of High-Field Drift Velocity of Electrons in Inversion Layers on Silicon, *IEEE Electron Device Letters* EDL-2, 171-173 (1981).

21. Warner, D. D., and Wilson, C. L., Two-Dimensional Concentration Dependent Diffusion, Bell Syst. Tech. J. 59, 1-41 (1980).

22. Wilson, C. L., Scanning Electron Microscope Measurements on Short Channel MOS Transistors, *Solid-State Electronics* 23, 345-356 (1980).

23. Kennedy, D. P., and O'Brien, R. R., Analysis of the Impurity Atom Distribution Near the Diffusion Mask for a Planar p-n Junction, *IBM J. Res. Dev.* 9, 179-186 (1965).

24. Dressendorfer, P. V., Soden, J. M., Harrington, J. J., and Nordstrom, T. V., The Effects of Test Conditions on MOS Radiation-Hardness Results, *IEEE Trans. Nucl. Sci.* NS-28, 4281-4287 (1981).

Appendix A File CS1R.HLP

1. Interactive Execution On a VAX 11/780 the program is executed by entering:

RUN CS1R.EXE

A prompt will appear for the next input; enter a file name after each prompt, followed by a carriage return (denoted $\langle cr \rangle$)

FILENAME1 < cr > FILENAME2 < cr > FILENAME3 < cr > FILENAME4 < cr > FILENAME5 < cr > FILENAME5 < cr > FILENAME6 < cr >

The first and third files must have been created prior to this execution. They contain input data used by the program. The second file may be created during execution. The FILENAMEs must be legal VMS file names; they are limited to eight characters by an internal buffer in CS1R.

A. FILES

- 1) File1 contains data for each point to be calculated. The file format is shown below.
- 2) File2 is an empty file for output of plotting data if the plots are to be saved. This file name must be entered when if no plotting is to be done. VMS will create the file if plotting data are to be stored; other operating systems may require the file to be created before the run begins.
- 3) File3 contains a table of channel doping profiles.
- 4) File4 contains a table of acceptor trap density vs energy.
- 5) File5 contains a table of donor trap density vs energy.
- 6) File6 contains a table of oxide charge density vs distance.
- B. Examples of FILE FORMATS.
 Each point to be calculated requires 5 lines of input.
 Data on a given line are free-format. Comments may appear after all required data fields. After each point

is calculated, the program will look for additional data until a source doping of zero is found (first line of input), after which the program will terminate. EXAMPLE OF File1: Data are in units given. Line 1: Source doping/cm**3 3.0e19 Line 2: Vertical junction depth(um), Lateral junction depth(um), Poly-Si length(um) note: Channel length = Poly-Si length- 2^* Lateral junction depths 0.55 0.84 5.00 Line 3: Drain(volts), Gate(volts), Substrate(volts) note: Source voltage = 0.0. 0.15 + 1.158 0.0Line 4: Oxide thickness(um), Oxide dielectric constant, Interface charge(cm**2) 0.057 4.0 0.0 Line 5: Channel mobility(cm**2/V-sec), Channel width(um), Flatband voltage(V) 400.0 20.0 -.580 Line 6: Line 6 may contain 0.0 for stopping program, or may be first line of data for next point to be calculated. Last line in data file must be zero. EXAMPLE of File3: Data for doping density. Line 1: Contains integer, Ndop, denoting the length of the profile table. Lines 2 through Ndop+1: Each contains an x (um) and the doping density at x $(1/cm^{**}3)$ 0.0 3.e15 100.0 3.e15 EXAMPLE of File4: Data for acceptor trap density. Line 1: Contains integer, Nga, denoting the length of the table and a scale factor. 4 0.144 Lines 2 through Nqa+1: Each contains an energy referred to mid-band (Ev) and the density 1/(Ev-cm**2).

-0.500	0.0
-0.499	1.0e11
0.499	1.0e11
0.500	0.0

EXAMPLE of File5: Data for donor trap density.

Line 1:

Contains integer, Nqd, denoting the length of the table and a scale factor.

4 0.144

Lines 2 through Nqd+1:

Each contains an energy referred to mid-band (Ev) and the density $1/(Ev-cm^{**2})$.

-0.500	0.0
-0.499	1.0e11
0.499	1.0e11
0.500	0.0

EXAMPLE of File6: Data for oxide charge density.

Line 1: Contains integer, Nqox, denoting the length of the table and a scale factor. 4 1.00 Lines 2 through Nqox+1: Each contains a distance referred to the source (um) and the density 1/(cm**2).

0.000	0.0
0.100	1.0e11
5.000	1.0e11
5.500	0.0

C. OUTPUT DISPLAY

All outputs (except the drain current) are in intrinsic Debye lengths (33um) and thermal volts (25mV), or units derived from these such as, Thermal volts/Debye length. 1. After program execution, the following prompts appear on the display:

ENTER 0,1,2,3 FOR CURRENT AND NEXT POINT, 2D PRINTING, 2D PLOTTING, CURRENT AND STOPPING.

- 0 print current. Continue to next point in data file, if any.
- 1 print additional information about point just calculated.
- 2 plot additional information about point just calculated.
- 3 print current and terminate execution. Do not continue to next data point in data file, if any.

If response 1 or 2 is given, further prompts will be furnished.

2. OPTIONS for printing (response 1)

The prompt is ENTER SUMMARY,NX,NY

SUMMARY – for a summary of the number of mesh points and triangles

created, how much memory allocated, and how much time used, enter 1. If not desired, enter 0.

- NX NY how many points along X and Y are to be printed in the print matrix. If NX and NY are both negative, a scaled integer printer plot of the potential will result. If NX and NY are both positive, a rectangular grid is placed on the region; at each point X, Y, U (the potential), UX, and UY (the derivatives of U in the X and Y directions) will be printed. At grid points outside the region, large numbers will be printed.
- 3. OPTIONS for plotting (response 2)

The prompt is 1:TRIANGLES, 2:CONTOURS, 3:SURFACE, 4:PROFILES

Enter 1, 2, 3, or 4, to plot on screen. Enter 101, 102, 103, or 104, to save plot data on File2.

Enter 0 to terminate plotting.

Each plot mode will furnish one or more further prompts. In every screen-plotting case, the final prompt before drawing the plot is

Enter g or G to when ready to plot

This gives the user time to clear the screen or to do any work necessary to put the terminal in plotting mode.

After each plot is drawn on the screen, the program will wait for a carriage return, and then re-issue the above prompt. This gives the user time to clear the screen or to do any work necessary to change the terminal out of plotting mode.

1: TRIANGLE PLOTS

The prompt is ENTER LEVEL

Enter level number (1, 2, ...) to plot the mesh of that level. Enter 0 to terminate triangle plotting.

After the triangle plot has been drawn, the program waits for a carriage return, and then reissues the Triangle Plot prompt.

2: CONTOUR PLOTS

The first prompt is 1:FUNCTION, 2:ABS(GRADIENT)

Enter 1 to plot the function (potential), or 2 to plot the absolute value of its gradient (absolute value of electric field; units are thermal volts/Debye length).

Enter 0 to terminate contour plotting.

The next prompt is NUMBER OF CONTOURS Enter the number of contour lines to be drawn. They will be drawn equally-spaced between (and including) the minimum and maximum values found.

After the contour plot has been drawn, the program waits for a carriage return, and then reissues the first Contour Plot prompt.

3: SURFACE PLOTS

The first prompt is 1:FUNCTION, 2:ABS(GRADIENT)

Enter 1 to plot the function (potential), or 2 to plot the absolute value of its gradient (absolute value of electric field; units are thermal volts/Debye length).

Enter 0 to terminate surface plotting.

The next prompt is ENTER LEVEL Enter level number (1, 2, ...) to make a plot of the surface using the mesh of the given level. Enter 0 to return to the First Surface Plot prompt

The next prompt is ENTER VIEWING DIRECTION-NX,NY,NZ Enter three integers. The surface plot is a (parallel) projection of the surface as seen from indicated direction. Thus (0,0,1) will give a top view (like a Triangle Plot), and (0,-1,0) will give a side view.

After the surface plot has been drawn, the program waits for a carriage return, and then reissues the first Surface Plot prompt.

4: PROFILE PLOTS

The first prompt is ENTER NUMBER OF PROFILES Enter an integer, the number of profiles to be drawn. Enter 0 to terminate profile plotting.

The next prompt is ENTER INDICES OF PROFILE PLANE(S), NX AND NY Enter two integers. A profile plot is a slice through the solution, perpendicular to the given direction. Thus (0,1) will give a slice parallel to the X axis.

After the profile plot has been drawn, the program waits for a carriage return, and then reissues the first Profile Plot prompt.

2. BATCH EXECUTION (for VAX-VMS only)

A. Submit File

Create a submit file which contains:

\$ RUN CS1R.EXE FILENAME1 FILENAME2 FILENAME3 FILENAME4 FILENAME5 FILENAME6 (Any other input used for the the equivalent interactive execution).

B. Output will be printed on the line printer.

3. SUMMARY OF MODEL

A two-dimensional charge sheet model of a surface-channel MOS transistor has been developed. When this model is implemented using adaptive finite element methods, an efficient high-accuracy transistor simulation program is possible.

The primary effect of ionizing radiation on MOSFETs is the

introduction of oxide trapped charge (OTC) and interface trapped charge (ITC). The OTC is independent of device operating voltage after irradiation, while the charge state of the ITC is dependent on gate bias in the subthreshold and weak inversion regions. Inclusion of these two charge components in device models introduces a nonscalable component into the calculation of the total effective channel charge in short-channel transistors.

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Appendix B File CS1R.EXP

INPUT FILE NAME FOR INPUT DATA, FILE specification MUST BE <= 40 CHARACTERS. s8.dat (user input) INPUT FILE NAME FOR OUTPUT DATA PLOTTING (user input) plot.dat INPUT FILENAME FOR DOPING PROFILE DATA dops8.dat (user input) INPUT FILENAME FOR QIA ENERGY DATA (user input) ga.dat INPUT FILENAME FOR QID ENERGY DATA qd.dat (user input) INPUT FILE NAME FOR QOX VS DISTANCE DATA (user input) qox.dat BETA = 3.868472E+01PSIB = 3.466497E-01 LB = 4.086666E-06COX = 6.207734E-08BPSO = 2.331485E+01 BPSI = 3.318985E+01 PS(0) =8.579575E-01 NO = 1.106634E+12 PS(L) =1.104439E+00 NL = 9.657040E+11 ID = 8.584329E-05IO = 5.349826E+01 I... = 9.999379E+02VG = 1.547389E+02 VSD = 9.671180E+002.481457E-01 LCH =

level 1

1	dpsi	-1.553E+01	a	-2.540E+08	umax	4.639E+01
2	dpsi	9.854E+00	a	-1.500E+08	umax	1.042E+01
3	dpsi	4.886E+00	a	-1.088E+08	umax	1.042E+01
4	dpsi	8.537E+00	a	-9.717E+07	umax	8.693E+00
5	dpsi	8.361E+00	a	-1.199E+08	umax	8.575E+00
6	dpsi	4.273E+00	a	-1.731E+08	umax	4.311E+00
7	dpsi	2.256E+00	a,	-2.395E+08	umax	2.277E+00
8	dpsi	1.012E+00	a	-3.043E+08	umax	1.016E+00

g	dpsi	-8.973E-0	1 a	-3.470E+08	umax	9.037E-01
10) dpsi	-8.854E-0	1 a	-3.421E+08	umax	8.919E-01
11	. dpsi	-8.539E-0	1 a	-2.968E+08	umax	8.614E-01
12	dpsi	-7.848E-0	1 a	-2.413E+08	umax	7.944E-01
13	dpsi	-6.455E-0	1 a	-1.945E+08	umax	6.582E-01
14	dpsi	-4.437E-0	1 a	-1.631E+08	umax	4.455E-01
15	dpsi	4.279E-0	1 a	-1.538E+08	umax	4.455E-01
level	2					
1	dpsi	7.609E-0	2 a.	-1.529E+08	umax	4.455E-01
2	dpsi	1.169E+0	0 a.	-1.408E+08	umax	2.663E+01
3	dpsi	1.234E+0	0 a	-1.366E+08	umax	1.977E+01
4	dpsi	3.674E+0	0 a	-1.372E+08	umax	1.429E+01
5	dpsi	2.572E+0	0 a	-1.846E+08	umax	2.737E+00
e	dpsi	2.915E-0	1 a	-1.920E+08	umax	1.188E+00
7	dpsi	2.092E-0	1 a	-1.994E+08	umax	1.064E+00
8	dpsi	2.829E-0	3 a	-1.996E+08	umax	1.057E+00
level	3					
1	. dpsi	4.082E-0	4 a.	-1.996E+08	umax	1.057E+00
2	dpsi	7.940E-0	1 a.	-2.113E+08	umax	7.997E+00
3	dpsi	5.418E-0	1 a	-2.552E+08	umax	1.191E+00
4	dpsi	-2.892E-0	1 a	-2.826E+08	umax	9.930E-01
5	dpsi	-2.685E-0	1 a.	-2.875E+08	umax	5.127E-01
6	dpsi	-2.579E-0	1 a.	-2.772E+08	umax	2.583E-01
ENTER C	FORCU	RRENT AND NE	XTPOINT			
1	FOR 2D	PRINTING				
2	FOR 2D	PLOTTING				
з	FOR CU	RRENT AND ST	OPPING			
4	FOR CH	ANNEL PRINTI	NG			
1		(user int	out)			
enter s	ummary.		. ,			
1 -6 -1	.1	(user int	out)			
		()			
	3 MUL	TI-GRID LEVE	LS			
VERTICE	S	146	340	517		
TRIANG	ES	322	852	1344		

STORAGE ALLOCATION

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	ALLOCATED	USED
MAXT	17655	1349
MAXV	6621	517
MAXVSM	8828	1006
MAXJA	35877	3766
MAXU	1099	1099
MAXJU	1099	1062
TOTAL	200000	19992

TIMING DISTRIBUTION

	S	ECONI	DS	PER	CENT			
GRID		0.54	40	0	. 298			
ASMBLY	1	33.74	40	73	.784			
MG		38.62	20	21	. 306			
ADAPT		8.36	60	4	.612			
TOTAL	1	81.26	60	100	. 000			
scaled va	alues	from	-1.	410E+01	to :	3.344E+01	scale	3.344E+01

9999	999	9 -	·39	-41	-40	-38	
9999	999	9 -	42	-41	-40	-38	
100	-4	2 -	42	-41	-40	-38	
96	-4	2 -	·42	-41	-40	-38	
92	-4	2 -	42	-41	-40	-38	
88	-4	2 -	42	-41	-40	-38	
85	-4	2 -	42	-41	-40	-38	
81	-4	2 -	42	-41	-40	-38	
77	-4	2 -	42	-41	-40	-38	
9999	999	9 -	42	-41	-40	-38	
9999	999	9 -	41	-41	-40	-38	
ENTE	0 5	FOR	CUR	RENT	AND	NEXTPO	DINT
	1	FOR	2D	PRINT	ING		
	2	FOR	2 D	PLOTT	ING		
	3	FOR	CUR	RENT	AND	STOPP	ING
	4	FOR	CHA	NNEL	PRIN	TING	
1				(*	user	input)	
enter	r su	mnar	y,n	x,ny			
06	11			(user	input)	

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41E+38 26E+02 69E+00 84E-01
26E+02 69E+00 84E-01
69E+00 84E-01
84E-01
13E-01
41E+38
41E+38
53E+00
50E-02
93E-02
00E+00
73E+01
39E-01
56E-01
83E-02
83E-02
00E+00
25E+01
54E-01
27E+00
08E-02
83E-02
00E+00
78E+01
35E-01
55E+00
05E-02
35E-02
35E-02 00E+00
35E-02 00E+00 88E+01
35E-02 00E+00 88E+01 34E-01
35E-02 00E+00 88E+01 34E-01 55E+00
35E-02 00E+00 88E+01 34E-01 55E+00 12E-01
35E-02 00E+00 88E+01 34E-01 55E+00 12E-01 35E-02
35E-02 00E+00 88E+01 34E-01 55E+00 12E-01 35E-02 00E+00
35E-02 00E+00 88E+01 34E-01 55E+00 12E-01 35E-02 00E+00 48E+01
35E-02 00E+00 88E+01 34E-01 55E+00 12E-01 35E-02 00E+00 48E+01 49E-02
35E-02 00E+00 88E+01 34E-01 55E+00 12E-01 35E-02 00E+00 48E+01 49E-02 57E+00
35E-02 00E+00 88E+01 34E-01 55E+00 12E-01 35E-02 00E+00 48E+01 49E-02 57E+00 95E-02

42	0.08580	0.19996	-1.28544E+01	2.14624E+01	0.00000E+00
43	0.00000	0.23328	3.19591E+01	-8.33355E+03	2.53904E+01
44	0.01716	0.23328	-1.41009E+01	1.41400E+01	1.46553E+00
45	0.03432	0.23328	-1.39964E+01	1.55038E+01	-1.51089E+00
46	0.05148	0.23328	-1.36036E+01	2.28469E+01	-1.40815E-02
47	0.06864	0.23328	-1.32227E+01	2.19575E+01	1.05458E-02
48	0.08580	0.23328	-1.28544E+01	2.13845E+01	0.00000E+00
49	0.00000	0.26661	3.34385E+01	-8.54575E+03	1.13276E+02
50	0.01716	0.26661	-1.40937E+01	-2.87519E+00	-7.03582E-01
51	0.03432	0.26661	-1.40099E+01	2.75868E+01	5.18849E-01
52	0.05148	0.26661	-1.36035E+01	2.29437E+01	-5.59664E-03
53	0.06864	0.26661	-1.32223E+01	2.19575E+01	1.05458E-02
54	0.08580	0.26661	-1.28544E+01	2.13845E+01	0.00000E+00
55	0.00000	0.29993	1.70141E+38	1.70141E+38	1.70141E+38
56	0.01716	0.29993	1.70141E+38	1.70141E+38	1.70141E+38
57	0.03432	0.29993	-1.40225E+01	4.93789E+01	7.53808E+00
58	0.05148	0.29993	-1.36073E+01	2.36961E+01	-2.07513E-02
5 9	0.06864	0.29993	-1.32227E+01	2.19793E+01	-6.87528E-02
60	0.08580	0.29993	-1.28544E+01	2.13406E+01	0.00000E+00
61	0.00000	0.33326	1.70141E+38	1.70141E+38	1.70141E+38
62	0.01716	0.33326	1.70141E+38	1.70141E+38	1.70141E+38
63	0.03432	0.33326	-1.29085E+01	-3.49977E+02	2.29821E+02
64	0.05148	0.33326	-1.36006E+01	2.27103E+01	-3.52586E-01
65	0.06864	0.33326	-1.32178E+01	2.21573E+01	1.15992E-01
66	0.08580	0.33326	-1.28544E+01	2.10266E+01	2.88546E-01
ENTER	O FOR CURREN	IT AND NEX	TPOINT		
	1 FOR 2D PRI	NTING			
	2 FOR 2D PLC	TTING			
	3 FOR CURREN	IT AND STO	PPING		
	4 FOR CHANNE	L PRINTIN	IG		
2		(user inp	ut)		
1:tria	ingles, 2:cor	tours, 3:	surface, 4:pro	files	
101		(user inp	ut)		
writii	ng co-cordina	tes inste	ad of plotting		
enter	Teast				
1		(user inp	ut)		
Writii	ng to file 21	. (see figur	е В-1)		
enter	TGAGT		- 4.)		
2 		(user inp			
WF1C1I	lerrel	. (see ligur	e D-2)		
enter	Tevel				

```
3
                    (user input)
writing to file 21 (see figure B-3)
enter level
                    (user input)
0
1:triangles, 2:contours, 3:surface, 4:profiles
                    (user input)
0
writing co-cordinates instead of plotting
103
                     (user input)
1: function, 2: abs(gradient)
1
                    (user input)
enter level
1
                     (user input)
enter viewing direction -- nx,ny,nz
3 -1 1
                     (user input)
writing to file 21 (see figure B-4)
1:function, 2:abs(gradient)
                     (user input)
1
enter level
2
                     (user input)
enter viewing direction -- nx,ny,nz
3 -1 1
                     (user input)
writing to file 21 (see figure B-5)
1:function, 2:abs(gradient)
1
                     (user input)
enter level
3
                     (user input)
enter viewing direction -- nx,ny,nz
3 -1 1
                     (user input)
writing to file 21 (see figure B-6)
1:function, 2:abs(gradient)
0
                     (user input)
1:triangles, 2:contours, 3:surface, 4:profiles
102
                     (user input)
writing co-cordinates instead of plotting
1: function, 2: abs(gradient)
                     (user input)
1
number of contours
-8
                     (user input)
umin and umax
-10 25
                     (user input)
ulev
```

```
-1.000E+01 -5.000E+00
                           0.000E+00
                                        5.000E+00
                                                     1.000E+01
   1.500E+01
               2.000E+01
                           2.500E+01
writing to file 21 (see figure B-7)
1:function, 2:abs(gradient)
                   (user input)
0
1:triangles, 2:contours, 3:surface, 4:profiles
0
                   (user input)
ENTER O FOR CURRENT AND NEXTPOINT
      1 FOR 2D PRINTING
      2 FOR 2D PLOTTING
      3 FOR CURRENT AND STOPPING
      4 FOR CHANNEL PRINTING
0
                   (user input)
V_g = 4.000 Vd = 0.250 Vfb = -0.560 Q = 0.0000E+00 current 9.7684E-05
BETA =
           3.868472E+01
PSIB =
           3.466497E-01
  LB =
         4.086666E-06
COX =
           6.207734E-08
BPSO =
           2.331485E+01
BPSI =
           3.252674E+01
PS(0) =
           8.408164E-01
NO
      =
           7.291709E+11
PS(L) =
          1.085300E+00
NL
     =
           5.889478E+11
ID
           5.458326E-05
      =
IO
           5.349826E+01
     =
 I... =
           6.358082E+02
VG
           1.160542E+02
      =
VSD =
           9.671180E+00
LCH =
           2.481457E-01
level
        1
      1
          dpsi
                 -1.479E+01
                                   -2.528E+08
                                                        4.639E+01
                                                unar
                               а.
      2
          dpsi
                  5.689E+00
                                   -1.356E+08
                                                        7.711E+00
                               a
                                                umar
      3
          dpsi
                  5.550E+00
                                   -8.503E+07
                                                unar
                                                        7.711E+00
                               а
      4
          dpsi
                  7.272E+00
                                   -6.459E+07
                                                umax
                                                        7.478E+00
                               a
          dpsi
                                                        5.711E+00
      Б
                  5.560E+00
                                   -6.957E+07
                                                umar
                               a
      6
          dpsi
                                                        4.678E+00
                  1.788E-02
                                   -6.970E+07
                                                umar
                               a
      7
          dpsi
                  1.779E-02
                                   -6.983E+07
                                                        4.853E+00
                               a
                                                unar
      8
          dpsi
                  1.768E-02
                                   -6.996E+07
                                                        4.828E+00
                               a.
                                                umar
                                   -7.009E+07
      9
          dpsi
                  1.759E-02
                                                        4.803E+00
                               a
                                                umax
                                   41
```

10	dpsi	1.749B	E-02	a	-7.022E+0	07 umax	4.578E+00
11	dpsi	1.739E	5-02	a	-7.035E+0	07 umax	4.552E+00
12	dpsi	<mark>4.428</mark> 1	S+00	a	-9.768E+0	07 umax	4.527E+00
13	dpsi	2.440	E+00	a	-1.370E+0	08 umax	2.482E+00
14	dpsi	1.050	E+00	а	-1.765E+0	xsmu 80	1.058E+00
15	dpsi	-5.8591	E-01	a	-2.047E+0	08 umax	5.868E-01
level	2						
1	dpsi	2 . 9371	E-02	a	-2.033E+0	08 umax	5.868E-01
2	dpsi	3.419	E-01	a	-1.896E+0	08 unax	2.649E+01
3	dpsi	3.6571	E-01	a	-1.829E+0	08 umax	1.966E+01
4	dpsi	3.4251	E-01	a	-1.795E+0	08 unax	1.420E+01
5	dpsi	2 . 933I	E-01	a	-1.777E+0	08 umax	9.663E+00
6	dpsi	9.516	E-01	a	-1.721E+0	08 umax	6.125E+00
7	dpsi	-4.3381	E-01	a	-1.653E+0	08 umax	1.003E+00
8	dpsi	3.3211	E-01	a	-1.504E+0	08 umax	7.332E-01
9	dpsi	3.2511	E-01	a	-1.405E+0	08 umax	3.254E-01
level	3						
1	dpsi	1.5071	E-02	a	-1.402E+0	08 umax	: 3.254E-01
2	dpsi	4.210	E-01	a	-1.275E+0	08 umax	8.837E+00
3	dpsi	4.5591	E-01	a	-1.400E+	08 umax	7.946E-01
4	dpsi	2.6631	E-01	a	-1.507E+0	08 umax	2.676E-01
ENTER O	FOR CU	RRENT AND	NEXTP	OINT			
1	FOR 2D	PRINTING					
2	FOR 2D	PLOTTING					
3	FUR CU	RRENT AND	STOPP	ING			
4	FUR CH	ANNEL PRII	NTING				
1		(user	input)				
enter s	ummary,	nx,ny	in most)				
1 11 11		(user	input)				
	2 WIII	TT_CDID II	TVEL C				
VERTICE	S S	146	340		726		
TRIANGL	ES	322	858		1900		
INTIMAL		022	000		1000		
	STOR	AGE ALLOCA	ATION				
	AL	LOCATED		US	ED		
MAXT		17655		19	05		
MAXV		6621		7	26		
MAXVSM		8828		12	17		
MAXJA		35877		45	95		
					42		

MAXU	1	099	1099		
MAXJU	1	099	1062		
TOTAL	200	000	25205		
	TIMING D	ISTRIBUTIC	N		
	SECO	NDS	PERCENT		
GRID	0.	500	0.330		
ASMBLY	108.	470	71.635		
MG	33.	500	22.124		
ADAPT	8.	950	5.911		
TOTAL	151.	420	100.000		
I	х	Y	U	UX	UY
1	0.00000	0.00000	1.70141E+38	1.70141E+38	1.70141E+38
2	0.00858	0.00000	1.70141E+38	1.70141E+38	1.70141E+38
3	0.01716	0.00000	1.70141E+38	1.70141E+38	1.70141E+38
4	0.02574	0.00000	1.70141E+38	1.70141E+38	1.70141E+38
5	0.03432	0.00000	-1.37152E+01	-7.24994E+01	-9.86443E+01
6	0.04290	0.00000	-1.37948E+01	2.27971E+01	-1.43763E+00
7	0.05148	0.00000	-1.35992E+01	2.27971E+01	-1.43763E+00
8	0.06006	0.00000	-1.34068E+01	2.20188E+01	-1.99132E-01
9	0.06864	0.00000	-1.32178E+01	2.20188E+01	-1.99132E-01
10	0.07722	0.00000	-1.30350E+01	2.10478E+01	-2.70350E-01
11	0.08580	0.00000	-1.28544E+01	2.10478E+01	-2.70350E-01
12	0.00000	0.03333	1.70141E+38	1.70141E+38	1.70141E+38
13	0.00858	0.03333	1.70141E+38	1.70141E+38	1.70141E+38
14	0.01716	0.03333	1.70141E+38	1.70141E+38	1.70141E+38
15	0.02574	0.03333	-4.80514E+00	-3.49964E+03	-2.41980E+03
16	0.03432	0.03333	-1.40162E+01	3.50974E+01	6.71809E-02
17	0.04290	0.03333	-1.38026E+01	2.25781E+01	1.41791E-02
18	0.05148	0.03333	-1.36063E+01	2.34576E+01	1.62690E-02
19	0.06006	0.03333	-1.34112E+01	2.19170E+01	1.627 05E-02
20	0.06864	0.03333	-1.32227E+01	2.19880E+01	6.59292E-02
21	0.07722	0.03333	-1.30376E+01	2.14340E+01	6.59292E-02
22	0.08580	0.03333	-1.28544E+01	2.13398E+01	0.00000E+00
23	0.00000	0.06665	2.49507E+01	-7.58698E+03	5.04481E+01
24	0.00858	0.06665	-1.36085E+01	-1.46068E+02	3.19051E+01
25	0.01716	0.06665	-1.41009E+01	-1.58318E+00	8.35297E-01
26	0.02574	0.06665	-1.41098E+01	1.00770E+01	-3.55419E-01
27	0.03432	0.06665	-1.40100E+01	2.70126E+01	-6.84067E-01
28	0.04290	0.06665	-1.38036E+01	2.67176E+01	4.96515E-01

29	0.05148	0.06665	-1.36036E+01	2.29500E+01	1.03107E-02
30	0.06006	0.06665	-1.34109E+01	2.19880E+01	-3.18217E-03
31	0.06864	0.06665	-1.32223E+01	2.19563E+01	-1.07920E-02
32	0.07722	0.06665	-1.30378E+01	2.13398E+01	-1.07920E-02
33	0.08580	0.06665	-1.28545E+01	2.13848E+01	0.00000E+00
34	0.00000	0.09998	2.62073E+01	-7.72841E+03	4.12046E+01
35	0.00858	0.09998	-1.34399E+01	-1.46998E+03	1.20562E+02
36	0.01716	0.09998	-1.40998E+01	3.50989E+00	2.51406E-01
37	0.02574	0.09998	-1.41165E+01	-3.06538E+00	-2.80862E-01
38	0.03432	0.09998	-1.39963E+01	1.53389E+01	1.53542E+00
39	0.04290	0.09998	-1.38064E+01	2.29145E+01	-5.82507E-01
40	0.05148	0.09998	-1.36036E+01	2.28447E+01	1.29900E-02
41	0.06006	0.09998	-1.34111E+01	2.19563E+01	-1.07920E-02
42	0.06864	0.09998	-1.32227E+01	2.19563E+01	-1.07920E-02
43	0.07722	0.09998	-1.30379E+01	2.13848E+01	0.00000E+00
44	0.08580	0.09998	-1.28545E+01	2.13848E+01	0.00000E+00
45	0.00000	0.13330	2.75698E+01	-8.06315E+03	4.27771E+01
46	0.00858	0.13330	-1.32443E+01	-4.95397E+02	1.86663E+00
47	0.01716	0.13330	-1.40925E+01	-2.57716E+00	-6.32129E-01
48	0.02574	0.13330	-1.41251E+01	1.67888E+01	-5.20889E+00
49	0.03432	0.13330	-1.39811E+01	1.67888E+01	-5.20889E+00
50	0.04290	0.13330	-1.38154E+01	2.62370E+01	1.29900E-02
51	0.05148	0.13330	-1.36031E+01	2.28750E+01	1.84167E-02
52	0.08006	0.13330	-1.34106E+01	2.19563E+01	1.84166E-02
53	0.06864	0.13330	-1.32229E+01	2.18018E+01	-1.86626E-02
54	0.07722	0.13330	-1.30385E+01	2.13848E+01	-1.86626E-02
55	0.08580	0.13330	-1.28544E+01	2.14625E+01	0.00000E+00
56	0.00000	0.16663	2.90819E+01	-8.20106E+03	6.69754E+01
57	0.00858	0.16663	-1.32432E+01	-5.29061E+02	-2.71480E+01
58	0.01716	0.16663	-1.41034E+01	-2.96251E+00	-1.66998E+00
59	0.02574	0.16663	-1.41135E+01	-4.42085E-01	-3.11330E-01
60	0.03432	0.16663	-1.39724E+01	1.74443E+01	6.71829E+00
61	0.04290	0.16663	-1.38113E+01	2.38325E+01	-4.96427E-01
62	0.05148	0.16663	-1.36069E+01	2.38325E+01	-4.96427E-01
63	0.06006	0.16663	-1.34106E+01	2.18018E+01	-1.86626E-02
64	0.06864	0.16663	-1.32235E+01	2.18018E+01	-1.86626E-02
65	0.07722	0.16663	-1.30386E+01	2.14625E+01	0.00000E+00
66	0.08580	0.16663	-1.28544E+01	2.14625E+01	0.00000E+00
67	0.00000	0.19996	3.04268E+01	-8.36422E+03	4.10107E+01
68	0.00858	0.19996	-1.30226E+01	-6.30326E+02	7.11257E+00
69	0.01716	0.19996	-1.40915E+01	-2.04539E+00	9.85857E-01

70	0.02574	0.19996	-1.41255E+01	1.68276E+01	5.25861E+00
71	0.03432	0.19996	-1.39811E+01	1.68276E+01	5.25861E+00
72	0.04290	0.19996	-1.38153E+01	2.62277E+01	-1.37740E-02
73	0.05148	0.19996	-1.36031E+01	2.28749E+01	-1.85242E-02
74	0.06006	0.19996	-1.34106E+01	2.19569E+01	-1.85242E-02
75	0.06864	0.19996	-1.32229E+01	2.18018E+01	1.87087E-02
76	0.07722	0.19996	-1.30385E+01	2.13846E+01	1.87087E-02
77	0.08580	0.19996	-1.28544E+01	2.14625E+01	0.00000E+00
78	0.00000	0.23328	3.17745E+01	-8.37652E+03	3.19841E+01
79	0.00858	0.23328	-1.30848E+01	-2.02673E+03	-1.69270E+02
80	0.01716	0.23328	-1.41006E+01	1.12604E+01	8.60107E-01
81	0.02574	0.23328	-1.41169E+01	-3.41704E+00	2.02267E-01
82	0.03432	0.23328	-1.39964E+01	1.54589E+01	-1.52158E+00
83	0.04290	0.23328	-1.38064E+01	2.29022E+01	5.82274E-01
84	0.05148	0.23328	-1.36036E+01	2.28484E+01	-1.37740E-02
85	0.06006	0.23328	-1.34111E+01	2.19569E+01	1.05765E-02
86	0.06864	0.23328	-1.32227E+01	2.19569E+01	1.05765E-02
87	0.07722	0.23328	-1.30379E+01	2.13846E+01	0.00000E+00
88	0.08580	0.23328	-1.28544E+01	2.13846E+01	0.00000E+00
89	0.00000	0.26661	3.30732E+01	-8.50807E+03	4.09423E+01
90	0.00858	0.26661	-1.31670E+01	-2.92030E+02	-6.59520E+01
91	0.01716	0.26661	-1.40958E+01	-2.57167E+00	-7.99016E-01
92	0.02574	0.26661	-1.41124E+01	1.04042E+01	2.25980E-01
93	0.03432	0.26661	-1.40100E+01	2.75647E+01	5.13087E-01
94	0.04290	0.26661	-1.38035E+01	2.67078E+01	-4.94524E-01
95	0.05148	0.26661	-1.36035E+01	2.29433E+01	-6.04121E-03
96	0.06006	0.26661	-1.34108E+01	2.19811E+01	4.78094E-03
97	0.06864	0.26661	-1.32223E+01	2.19569E+01	1.05765E-02
98	0.07722	0.26661	-1.30378E+01	2.13405E+01	1.05785E-02
99	0.08580	0.26661	-1.28544E+01	2.13846E+01	0.0000E+00
100	0.00000	0.29993	1.70141E+38	1.70141E+38	1.70141E+38
101	0.00858	0.29993	1.70141E+38	1.70141E+38	1.70141E+38
102	0.01716	0.29993	1.70141E+38	1.70141E+38	1.70141E+38
103	0.02574	0.29993	-2.52721E-01	-4.59297E+03	3.12038E+03
104	0.03432	0.29993	-1.40262E+01	4.98050E+01	5.56818E+00
105	0.04290	0.29993	-1.38007E+01	2.20174E+01	-5.35175E-02
106	0.05148	0.29993	-1.36071E+01	2.36481E+01	-1.91827E-02
107	0.06006	0.29993	-1.34112E+01	2.19110E+01	-1.91827E=02
108	0.06864	0.29993	-1.32227E+01	2.19811E+01	-8.82150E-02
109	0.07722	0.29993	-1.30376E+01	2.14380E+01	-6.82150E-02
110	0.08580	0.29993	-1.28544E+01	2.13405E+01	0.0000E+00

111		0.00000	0.33326	1.70141E+38	1.70141E+38	1.70141E+38
112		0.00858	0.33326	1.70141E+38	1.70141E+38	1.70141E+38
113		0.01716	0.3 <mark>3</mark> 326	1.70141E+38	1.70141E+38	1.70141E+38
114		0.02574	0.33326	1.70141E+38	1.70141E+38	1.70141E+38
115		0.03432	0.33326	-1.29702E+01	-3.29089E+02	2.21887E+02
116		0.04290	0.33326	-1.37952E+01	2.27185E+01	-4.02840E-02
117		0.05148	0.33326	-1.36003E+01	2.27185E+01	-4.02840E-02
118		0.06006	0.33326	-1.34077E+01	2.21324E+01	1.30200E-01
119		0.06864	0.33326	-1.32178E+01	2.21324E+01	1.30200E-01
120		0.07722	0.33326	-1.30349E+01	2.10306E+01	2.85185E-01
121		0.08580	0.33326	-1.28544E+01	2.10306E+01	2.85185E-01
ENTER	0	FOR CURRE	NT AND NEX	TPOINT		
	1	FOR 2D PR	INTING			
	2	FOR 2D PL	OTTING			
	3	FOR CURRE	NT AND STO	PPING		
	4	FOR CHANN	EL PRINTIN	G		
			/			

3 (user input) Vg = 3.000 Vd = 0.250 Vfb = -0.560 Q = 0.0000E+00 current 5.3089E-05

01. Summary date 02. Summary prepared by (Name and Phone) 03. Summary action Yr. Mo. Day C. L. Wilson (301) 921-3541 8 4 0 3 2 1 05. Software title Image: Software title Image: Software title 04. Software date CS1R: A Two-Dimensional Finite Element Charge-Sheet Previous Internal Software Yr. Mo. Day Model of MOSFETs Including Radiation-Induced Inter- 07. Internal Software ID	Deletion
O6. Short title O9. Processing mode 10. Application area O8. Software type O9. Processing mode 10. General Management/ Automated Data System Interactive Support/Utility Business Process Control System Standards Scientific/Engineering Process Control Other 11. Submitting organization and address National Bureau of Standards 12. Technical contact(s) and phone National Bureau of Standards J. L. Blue 921-3395	
13. Narrative A two-dimensional charge-sheet model including radiation-induced interface and oxi effects in short-channel MOS transistors has been developed. The primary effect of ionizing radiation on MOSFETs is the introduction of oxide trapped charge (OTC), interface trapped charge (ITC), and the reduction of channel mobility caused by so tering from charge in interface traps. 14. Keywords Finite elements; MOS transistor; radiation effects	.de of :at-
15. Computer manuf'r and model 16. Computer operating system 17. Programing language(s) 18. Number of source pro	gram state-
VAX VMS FORTRAN	
19. Computer memory requirements 20. Tape drives 21. Disk/Drum units 22. Terminals	
200K 0 0	
23. Other operational requirements	
Requires local interactive vector-oriented graphics	
24. Software availability 25. Documentation availability	
Available Limited In-house only Available Inadequate In-ho	use only
C. L. Wilson 925-3541 9-track 1600bpi ASCII magnetic tape, DNA approved users only	

and the second se			
U.S. DEPT. OF COMM.	1. PUBLICATION OR	2. Performing Organ. Report No.	3. Publication Date
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SHEET (See instructions)	NBSIR 84-2874R		May 1984
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CSIR: A Two-Dimen	sional Finite Element	Charge-Sheet Model of Mo	OSFETs Including
Radiation-Induced	Interface and Oxide Ch	arge	
5. AUTHOR(S)			
C. L. Wilson and J	L. Blue		
	. D. DI		
6. PERFORMING ORGANIZA	TION (If joint or other than NBS	, see instructions) 7.	Contract/Grant No. Task No.
	STANDARDS	x99	9QAXVX, Work Unit 00076
DEPARTMENT OF COMM	ERCE	8.	Type of Report & Period Covered
WASHINGTON, D.C. 2023	4		.,,,,
9. SPONSORING ORGANIZAT	TION NAME AND COMPLETE A	DDRESS (Street, City, State, ZIP)	
			*
Defense Nuclear Ag	ency		
Washington, DC			
10. SUPPLEMENTARY NOTE	S		
X Document describes a	computer program: SF-185, FIP	S Software Summary, is attached.	
11. ABSTRACT (A 200-word o	r less factual summary of most s	ignificant information. If document	t includes a significant
bibliography or literature s	survey, mention it here)		
A two-dimensional	charge-sheet model inc	luding radiation-induced	d interface and oxide
effects in short-c	hannel MOS transistors	has been developed. The	he unique feature of
the model is that	the effects of channel	inversion layer charge	, interface charge,
and oxide charge a	re included is a peopli	near integral boundary	
	re included as a nonli	mear incegrar boundary	condition on the two-
dimensional electro	ostatic field in the t	ransistor. The average	inversion layer charge
dimensional electro density and source	ostatic field in the t -drain current are obt	aransistor. The average ained directly from the	inversion layer charge model rather than from
dimensional electro density and source the electron densi	ostatic field in the t -drain current are obt ty or electron quasi-F	aransistor. The average ained directly from the fermi level. The model a	inversion layer charge model rather than from retains all of the
dimensional electro density and source the electron densi physical detail of	ostatic field in the t -drain current are obt ty or electron quasi-F more complex two-dime	eransistor. The average ained directly from the ermi level. The model a ensional models such as a	inversion layer charge model rather than from retains all of the sensitivity to source-
dimensional electro density and source the electron densi physical detail of drain profile shap	ostatic field in the t -drain current are obt ty or electron quasi-F more complex two-dime e, channel profile, ar	eransistor. The average ained directly from the ermi level. The model r ensional models such as a d oxide field shape. The	inversion layer charge model rather than from retains all of the sensitivity to source- his allows the model
dimensional electro density and source the electron densi physical detail of drain profile shap to represent the c	ostatic field in the t -drain current are obt ty or electron quasi-F more complex two-dime e, channel profile, ar hanges in drain currer	aransistor. The average ained directly from the ermi level. The model a ensional models such as a d oxide field shape. The t associated with short.	inversion layer charge model rather than from retains all of the sensitivity to source- his allows the model -channel effects while
dimensional electro density and source the electron densi physical detail of drain profile shap to represent the c still allowing sim	ostatic field in the t -drain current are obt ty or electron quasi-F more complex two-dime e, channel profile, ar hanges in drain currer ple comparison with lo	aransistor. The average ained directly from the Permi level. The model s ansional models such as s ad oxide field shape. The associated with short- ong-channel models.	inversion layer charge model rather than from retains all of the sensitivity to source- his allows the model -channel effects while
dimensional electro density and source the electron densi physical detail of drain profile shap to represent the c still allowing sim	ostatic field in the t -drain current are obt ty or electron quasi-F more complex two-dime e, channel profile, ar hanges in drain currer ple comparison with lo	ransistor. The average ained directly from the ermi level. The model s instant models such as a ad oxide field shape. The associated with short- ong-channel models.	inversion layer charge model rather than from retains all of the sensitivity to source- his allows the model -channel effects while
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