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TVSIR 80-2019
Technical Specifications of a Proposed Federal Information Processing Standard on the Modes of Operation for the Data Encryption Standard
Institute for Computer
Sciences and
Technology
April 1980


# Technical Specifications of a Proposed Federal Information Processing Standard on the Modes of Operation for the Data Encryption Standard 

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Issued April 1980

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The algorithm for the Data Encryption Standard (DES) was developed by the International Business Machines Corporation (IBM). It was adopted by the National Bureau of Standards (NBS) as a Federal Information Processing Standard (FIPS) in 1977. FIPS Publication \#46 [FIPS 46] specifies the DES algorithm which is to be used within the Federal government for the cryptographic protection of sensitive, but unclassified, computer data. A number of techniques for incorporating this algorithm into a cryptographic system have been identified by both Federal and private organizations. These implementation techniques, external to the DES algorithm, have come to be called the "modes of operation." The Institute for Computer Sciences and Technology within the NBS is proposing a Modes of Operation FIPS for the DES. The purpose of this FIPS will be to describe several techniques for using the DES with sufficient specificity as to facilitate the interoperability of equipment using these modes.

Four implementation techniques using the DES are described in this document: the electronic codebook (ECB) mode, the cipher block chaining (CBC) mode, the cipher feedback (CFB) mode, and the authentication-only mode. ECB is a direct implementation of the IBM algorithm (U.S. patents \#3798830 and \#3798359); IBM also developed and patented ( $\$ 4078152$ ) the basic concept of the CBC mode. The Federal Reserve Board, with the technical assistance of the National Security Agency, adopted an 8-bit CFB technique for experimental use on their nationwide data communication network. The authentication-only mode is really an application of CBC or CFB, but it is deemed sufficiently important to be included in a standard. The proposed FIPS is limited to these four modes because they are the only techniques recommended at this time in encryption standards being developed under the auspices of the Federal Telecommunication Standards Committee.

The purpose of this NBS Internal Report is to provide an expedient vehicle for the dissemination of the technical information being considered for the proposed Modes of Operation FIPS.

The proposed FIPS will mandate only those characteristics necessary to specify the mechanics of implementing the modes of operation. Requirements in other concomitant areas which affect the security of a cryptographic system, e.g., key management or cryptographic synchronization, are not addressed in this document. They may be defined in other security or application standards.

The American National Standards Institute has approved the creation of a technical committee (X3Tl) in order to begin drafting a national standard addressing the modes of operation for their Data Encryption Algorithm (DEA). The Federal DES and the ANSI DEA use the same cryptographic algorithm.

## 2. INTRODUCTION

Data to be cryptographically protected is called plain text. Encryption is the process of transforming plain text into cipher text ; decryption is the inverse mapping of cipher text to plain text. The encryption (E) of plain text $(P)$ under a key (K) into cipher text (C) is denoted by $E(K$, $P)=C . \quad T h e ~ l e t t e r ~ D ~ w i l l ~ r e p r e s e n t ~ t h e ~ i n v e r s e ~ t r a n s f o r m a-~$ tion, so that decryption under $K$ may be written as $D(K, C)=$ $D\{K, E(K, P)\}=P$.

Binary data may be cryptographically protected using the Data Encryption Standard (DES) [FIPS 46] in conjunction with a cryptographic variable. A cryptographic variable for the DES consists of sixty-four binary digits of which fifty-six bits are used directly as a key governing the algorithm. The remaining eight bits are employed as an odd parity check. A cryptographic period (or key period) is that interval of DES operation during which the same key is used between two or more cryptographic entities. Since the DES has been publicly defined, cryptographic security depends upon the security provided for the cryptographic variable -- both the key and its parity bits. Given the cipher text and the key, the plain text can be recovered easily.

Mathematically, the DES maps a 64-dimensional input space over the field $\{0,1\}$ onto itself. The number of elements in this space is two raised to the 64 th power (2**64), i.e., it consists of all possible 64-bit vectors. The cryptographic key space provides the user a choice of any one of 2**56 invertible (one-to-one and onto) mappings. A specific DES input value can be mapped to one of $2 * * 56$ output values -- the specific value depends upon the particular 56-bit key chosen. The DES mapping has a complementary effect in that if $E(K, P)=C$ then $E\left(K^{\prime}, P^{\prime}\right)=C^{\prime}$ or equivalently $E(K, P)$ $=\left\{E\left(K^{\prime}, P^{\prime}\right)\right\}^{\prime}$ where the apostrophe represents binary complementation.

FIGURE 1:


## FIGURE 2: THE DES TRANSFORMATION



The DES is a nonlinear, iterative, block, product cipher. This product cipher mixes transposition and substitution operations in an alternating manner in order to be most effective. Because this algorithm maps a 64-bit input block into sixty-four output bits, the DES is classified as a block cipher. Iterative refers to the use of the output of an operation as the input for another iteration or round of the same procedure. Nonlinearity is introduced into the algorithm through eight $S$ (substitution) boxes, each of which maps six input bits into four output bits. A block diagram of the encryption operation is illustrated in figure \#2. The cipher function, $f$, and the key schedule function are described in detail in [FIPS 46].

The DES input and output (I/O) blocks are sixty-four bit vectors with the least significant bit (LSB = 2**0) defined to be on the right and the most significant bit (MSB = 2**63) on the left. The bits of a DES I/O block are numbered from left to right: (1, 2, . . . , 64). When a 64-bit cryptographic variable is entered into the DES key schedule, its format in the key input block is: $(1,2, \ldots, 7, P l, 8,9, \ldots$, $14, P 2,15, \ldots, \ldots, 49, P 7,50,51, \ldots, 56, P 8)$, where $\{P i \mid i=1$, $2, \ldots, 8\}$ are odd parity bits computed on the preceding seven key bits.

There are two general techniques for incorporating the DES into a cryptographic system: a block cipher and an additive or stream cipher. In both modes each bit of cipher text is a function of every bit of the cryptographic key. In a block cipher, the DES input block is a function of the plain text to be encrypted and the DES output block defines the cipher text. In an additive cipher implementation, a pseudorandom binary sequence is generated using DES output blocks. The binary exclusive-OR operation, represented by a circled plus sign, combines this pseudorandom sequence with the plain text to define the cipher text. This operation is equivalent to bit-by-bit, modulo-2 addition (without carry). Since the exclusive-OR operator is its own inverse over $\{0,1\}$, the same pseudorandom binary stream, say 0 , is used for both the encryption of plain text, $P$, and the decryption of $c i p h e r$ text, $C$; i.e., $P \oplus O=C$ and $C \oplus O=P$.

The most basic mode of operation for the DFS is the electronic codebook (ECB). The analogy to a codebook arises because the same plain text block always produces the same cipher text block for a given cryptographic key. Thus, assuming that a manageable subset of the DES input space is used, a list (or codebook) of corresponding plain and cipher text pairs could be constructed.

In ECB encryption, the plain text data block (D1,D2,.., D64) directly defines the DES input block (Il,I2,...,I64). The input block is processed through a DES device which has been loaded with the appropriate cryptographic variable. The resultant output block (01,02,...,064) is used directly as cipher text (Cl,C2,..., C64).

The ECB decryption process is the same as ECB encryption except that the DES key schedule selection is reversed. In general, the DES key schedule function generates a new 48 -bit vector from the 56 -bit cryptographic key for each of the sixteen rounds of the DES algorithm. For a given cryptographic variable, let the sixteen key schedule encryption vectors be denoted by $\{K S 1, K S 2, .$. . KSl6\}. Then, the corresponding decryption process will use the same basic operation as encryption (figure \#2), but now \{KSl6, KS15, - . KSl\} will be successively invoked. An example of ECB encryption and decryption may be found in Appendix A.

Since each bit of an ECB output block is a complex function of every bit in the input block and the cryptographic key, a single bit error in a cipher text block will cause the decrypted plain text block to have an average error rate of fifty percent. However, an error in one ECB cipher text block will not affect the decryption of other blocks, i.e., there is no error extension between ECB blocks. An example of the effect of cipher text errors on ECB operations may be found in Appendix $B$.

If block synchronization is lost (e.g., a bit slip), then ECB cryptographic synchronization will also be lost until correct block boundaries are re-established.

Since the ECB mode is a 64-bit block cipher, an ECB device must encrypt information in integral multiples of sixty-four bits. If a user has less than sixty-four bits to encrypt, then the least significant bits of the unused portion of the input data block should be padded with random or pseudorandom binary digits prior to ECB encryption. The corresponding decrypting device will have to know when and to what extent padding has taken place so that these padding
digits can be ignored or discarded after decryption.
A potentially critical weakness of the ECB mode is the fact that the same plain text always produces the same cipher text under a fixed key. Thus, the compromise of the plain text underlying any cipher text block results in the compromise of all repetitions of this same rext for the remainder of the cryptographic period. This is sometimes referred to as a codebook analysis problem.

## FIGURE 3: ELECTRONIC CODEBOOK (ECB) MODE

ECB ENCRYPTION


ECB DECRYPTION


## 4. CIPHER BLOCK CHAINING (CBC) MODE

CBC is a block cipher in which the plain text is exclusive-ORed with a block of pseudorandom data prior to being processed through a DES device (see figure \#4). This technique greatly reduces the codebook analysis problem associated with the ECB mode, and also provides an error extension characteristic which is valuable in protecting against fraudulent data alteration.

In order to commence CBC encryption, the first DES input block is formed by exclusive-ORing the first data block with a 64-bit initialization vector (IV), i.e., (Il,I2,..., I64) $=(I V 1 \oplus D 1$, IV $2 \oplus D 2, .$. . IV64 $\oplus$ D64). This initial CBC input block is processed through a DES device producing a 64-bit DES output block which defines the cipher text, (01,02,...,064) $=(C l, C 2, \ldots, C 64)$. Then these first 64 bits of cipher text are exclusive-ORed with the second plain text data block in order to construct the second DES input block. The next DES operation produces the second cipher text block. This encryption process continuès to "chain" successive cipher and plain text blocks together until the last plain text block in the message is encrypted. The DES input block at time $t$ is the bit-by-bit, mod-2 sum of the plain text at time $t$ and the cipher text at time $t-1$ for $t>1$ or the IV at $t=1$. Appendix A contains an example of the CBC encryption and decryption of ASCII characters and Appendix C has a flow chart illustrating the basic CBC logic.

For CBC decryption, the first cipher text block is processed through a DES device using the decrypt operation, i.e., the key schedule vectors are invoked in the reverse order from the encryption process. The first output block is exclusive-ORed with the CBC IV producing the first plain text block. The second cipher text block is then entered into the DES and the resultant output block is exclusiveORed with the first cipher text block in order to produce the second plain text block. The CBC decryption process continues to exclusive-OR the cipher text block at time t-l for $t>1$ with the DES output block to obtain plain text at time $t$ until the end of the message.

FIGURE 4: CIPHER BLOCK CHAINING (CBC) MODE


## LEGEND

Di=D ATA AT TIME $\quad O i=$ OUTPUT AT TIME $i$
li=INPUT AT TIME $i \quad I V=$ INITIALIZATION VECTOR
Ci=CIPHER AT TIME
(+) EXCLUSIVE-OR

The security of a CBC implementation depends, among other things, upon the management of CBC initialization vectors. Some recommendations in this area are provided in Appendix E .

The CBC mode reproduces the same cipher text whenever the same plain text is encrypted under a fixed key and IV. In the ECB mode, the cipher text repetition characteristic occurs at the block level; in the CBC mode, cipher text repetition is at the message level. If CBC users are concerned about this potential security problem, then their CBC systems should incorporate a unique identifier (e.g., a one-up counter) at the beginning of each CBC message in order to insure unique cipher text within a cryptographic period.

Since the CBC mode is a 64-bit block cipher, it must operate on a 64-bit input block with each CBC operation. Thus, partial data blocks (< 64 bits) will require special handing. For example, a partial data block may be padded in its least significant bit positions with arbitrary binary digits whenever the application environment can tolerate the overhead. The decrypting CBC device will have to know when and to what extent padding has occurred. This can be accomplished explicitly, e.g., using a control indicator, or implicitly, e.g., using constant length transactions. Another suggestion for handing partial data blocks is to switch to a l-bit cipher feedback (CFB) mode in order to process the final $k<64$ bits of a message. The last CBC cipher block would be used as an IV to initiate this CFB process. When using this scheme, the last bit of the message should not contain sensitive information.

In the CBC mode, one or more bit errors within a single cipher text block will affect the decryption of two blocks -- the block in which the error occurs and the succeeding block. If the errors occur in the $n$-th cipher text block, then each bit of the $n-t h$ plain text block will have an average error rate of about fifty percent. The ( $n+1$ ) st plain text block will have only those bits in error which correspond directly to the cipher text bits in error. Of course, if errors occur in the last cipher text block, then the last plain text block is the only one affected. An example of the effect of cipher text errors in CBC operations may be found in Appendix $B$.

If CBC block synchronization is lost, then CBC cryptographic synchronization will also be lost. However, cryptographic synchronization will automatically be reacquired sixty-four bits after block boundaries have been established.

## 5. CIPHER FEEDBACK (CFB) MODE

The CFB mode is an additive cipher technique in which the DES is used to generate a pseudorandom binary stream. This stream is exclusive-ORed with the binary plain text to form the cipher text. The cipher text is fed back to form the next DES input block. The pseudorandom binary stream is sometimes referred to as a key stream, and the DES is then called a key generator or KG. However, this terminology will not be used in order to avoid confusion with the cryptograpinic key.

One through sixty-four bit CFB operation may be used. A 64-bit initialization vector (IV) or starter input block is used to begin CFB operations. A CFB IV is placed in the DES input block so that any zero fill is left-justified. This 64-bit input block is encrypted through a DES device producing a 64-bit, pseudorandom output block. The DES device is operated once for each new $k$-bit ( $0<k<65$ ) character to be encrypted. In all CFB implementations, the leftmost or most significant $k$ bits of the DES output block are used in the exclusive-OR operation. These output block bits, (Ol,O2,..., Ok), are exclusive-ORed with the corresponding $k$ bits of data, (D1,D2,..., Dk) to form the cipher text: (Cl,C2,...,Ck) $=(D 1 \oplus O 1, D 2 \oplus 02, \ldots, D k \oplus O k)$. In order to define this operation when the length of the plain text character to be encrypted is less than $k$ bits, zeros are concatenated to the left hand side or most significant bits of the plain text. Obviously, users must agree on the representation of a plain text "character." Bits (Ok+1, Ok +2 , . . , 064) of the DES output block are discarded. The $k$ bits of cipher text are fed back to the LSB positions of the DES input (I) block such that:




As an example, consider an 8 -bit CFB implementation and an IV with forty-eight pseudorandom bits. After each encryption, the eight cipher bits are fed back into the DES input block such that:

```
AFTER
ENCRYP-
TION #
THE DES INPUT BLOCK CONTAINS:
```



```
    1
    (0,0,0,0,0,0,0,0,1,2,\ldots.....,47,48,C1,C2,\ldots....,C8)
    2 (1,2,\ldots....,47,48,Cl,C2,.....,C8,C9,Cl0,.....,Cl6)
```

After the eighth encryption the entire 64-bit IV will have been shifted out of the DES input block. Let the first character be a seven-bit ASCII character plus parity denoted by ( $\mathrm{P}, \mathrm{b} 7, \mathrm{~b} 6, \ldots, \mathrm{bl}$ ). If the first DES output block is (01,02,...,064), then the first cipher text character will be $(\mathrm{Cl}, \mathrm{C} 2, \ldots, \mathrm{C} 7, \mathrm{C} 8)=(\mathrm{P} \oplus 01, \mathrm{~B} 7 \oplus 02, \ldots, \mathrm{~b} 2 \oplus 07, \mathrm{~b} 1 \oplus 08)$. Appendix A contains a detailed example of 8 -bit CFB operations and Appendix $C$ has a flow chart diagramming the basic CFB procedures.

The security of a CFB system depends, among other things, upon the management of CFB IVs. Some recommendations in this area are provided in Appendix E.

To protect against undetected bit manipulation of the last k-bit cipher text character using k-bit CFB, the last character to be encrypted must consist of error detection, terminal flag, or permanently fixed data.

In CFB, each cipher bit is a function of one bit of the DES output block and one bit of plain text. Therefore, any bits of a CFB cipher text character may be changed without affecting the decryption of other bits within the same character so long as the bits which are fed back at the encrypting and decrypting stations are the same. An application of this characteristic would be the deletion of encrypted parity bits and their replacement with a new parity computed on the cipher text. This feature is useful in networks which are sensitive to parity checks.

Bit errors within one CFB cipher text character will affect not only the decryption of the garbled cipher text but also the decryption of succeeding characters until the bit errors are flushed out of the CFB input block. The first affected plain text character will be garbled in exactly those places where the cipher text character is in error. Succeeding plain text characters will experience an
average error rate of about fifty percent until all arrors have been shifted out of the DES input block. Assuming no additional errors are encountered during this time, the CFB decryption device will then automatically regain cryptographic synchronization. This characteristic is sometimes referred to as a limited error extension or a selfsynchronizing capability -- depending upon the point of view. In the previous 8-bit CFB example, errors in one cipher text character affect the decryption of nine characters. A detailed example of cipher text errors in CFB operations may be found in Appendix $B$.

If $k$-bit character boundaries are lost during decryption, then cryptographic synchronization will be lost until a cryptographic restart (new IV) is initiated or until after character boundaries have been re-established. In the latter case, if $64(\bmod k)=0$, then resynchronization will occur automatically after $64 / k$ characters with proper boundary definition have entered the DES input block; otherwise. one additional character will be required.

The encryption and decryption processes in the CFB mode invoke the DES key schedule vectors in the same order, i.e., both processes will use \{KSl, KS2, . . . , KSl6\}. This produces a partial involution under the same IV and key; i.e., if $E[K,(P 1, P 2, \ldots, P n)]=(C 1, C 2, \ldots, C n)$, then $E[K$, $(C 1, C 2, \ldots, C n)]=(P 1, N 1, N 2, \ldots, N(n-1))$ where $P, C$ ard iv represent $k$-bit plain text, cipher text, and nonsense ipseudorandom) characters, respectively.

The DES algorithm may also be used for the authentication of plain text. This technique is useful in applications which require maintaining data integrity but do not require that the plain text be protected from disclosure. The authentication-only mode protects against bit manipulation within the data as well as the insertion and deletion of messages, and the replay of a previously valid message. In the authentication-only mode, two message authentication codes (MACs) are independently computed on the same data -one at the data source and one at the data destination. This data consists of a unique message identifier (MID) and the text to be protected. If the data source MAC and the data destination MAC are in agreement and if the MID agrees with its expected value, then the plain text is accepted as authentic at the data destination. The authentication-only format is depicted in figure \#6. The MAC must be generated using either the CFB or the CBC mode.

## FIGURE 6:

AUTHENTICATION-ONLY FORMAT

| FIELD 1 | FIELD 2 | FIELD 3 |
| :---: | :---: | :---: |
| MID | PLAIN <br> TEXT | MAC |

In order to commence CFB authentication operations, a unique message identifier is used as an initialization vector. The plain text is encrypted in the normal CFB manner except that the cipher text is not communicated to the decrypting device. After the encryption of the final plain text unit (character or block), the last cipher text is fed back into the DES input block as if another plain text unit were to be encrypted. Then the DES device is operated one more time and the left-most or most significant $k$ bits $(0$ $<k<65$ ) in the next DES output block are used as the MAC.

To begin CBC authentication operations, the MID is again used as an initialization vector. However, for this application the first plain text block to be encrypted is the all zero block, i.e., the MID alone defines the first DES input block. Thereafter, the plain text is encrypted in the normal CBC manner. The CBC MAC is defined to be the
left-most or most significant $k$ bits of the DES output block resulting from encrypting the final plain text block. Messages which terminate in partial data blocks are to be padded on the right (LSB) with zeros.

The MID, plain text, and the MAC are conveyed to the data destination; the intermediate cipher text is not transmitted. The probability that one could randomly select a correct $k$-bit MAC is $l /(2 * * k)$. For most applications, MACs of at least 24 bits are strongly recommended. Two examples of the authentication-only mode may be found in Appendix $D$.

In general, the MID is a unique and deterministic message identifier within a cryptographic period; the MID should also be varied across cryptographic periods. The value of the MID will be checked by the recipient of an authentication-only message to verify that messages have not been deleted, inserted, or replayed. The uniqueness within a cryptographic period may be achieved through the use of a one-up binary counter. MID values are not to be repeated within the same cryptographic period; this constraint also applies to multiuser environments under control of a common cryptographic key. The MID variation across cryptographic periods may be satisfied by selecting a random or pseudorandom starting value from the total range of a "withir" counter. In using this approach it is recommerded thet oryy a small (say << 5\%) segment of the MID's total range be used within any key period. Another acceptable technique would be to form the MID by concatenating a unique message identifier together with a unique identifier for each cryptographic period, e.g., a second one-up binary counter could be used for this purpose.

A MID is not encrypted. However, whenever MID values are exchanged through an unsecured channel to establish or re-establish MID synchronization, then these values must be protected. This protection includes the detection of bit alteration, the insertion of bogus messages, and the replay or deletion of valid messages.
7. REFERENCES
[FIPS 46] Federal Information Processing Standard Publication 46, Data Encryption Standard. 1977 January 15; FIPS PUB 46: 18 pages. Available from: National Technical Information Services; U.S. Department of Commerce; Springfield, Virginia 22l6l; NBS-FIPS-PUB-46.

AUTHENTICATION-ONLY: A DES technique for protecting the integrity of plain text which does not have to be protected from disclosure; see section 6 .

BLOCK: A binary vector consisting of sixty-four bits numbered from the left as 1,2 , . . . , 64.

CBC: Cipher block chaining; see section 4 .
CFB: Cipher feedback; see section 5 .
CIPHER TEXT: Encrypted data.
CRYPTOGRAPHIC KEY: The 56 random bits of the cryptographic variable which are used to govern the DES device. Also simply called KEY.

CRYPTOGRAPHIC PERIOD: That period of DES operation during which a unique data-encrypting key is used between two or more cryptographic facilities. Keys from different cryptographic periods are independent. Synonym: Key period.

CRYPTOGRAPHIC VARIABLE: The 64 bit vector containing the 56-bit DES key and its eight associated parity bits. Synonym: Key Variable.

DECRYPTION: The process of changing cipher text into plain text. Verb: DECRYPT.

DES: Data Encryption Standard; specified in [FIPS.46].
DES DEVICE: The hardware used to implement the DES algorithm. This is usually an integrated circuit chip which is sometimes referred to as a "crypto-engine.".

DES INPUT BLOCK: A 64-bit data vector that is entered into the DES device.

DES OUTPUT BLOCK: A 64-bit vector that is the final result of a DES device.

ECB: Electronic codebook mode; see section 3 .

ENCRYPTION: A process of changing plain text into cipher text. Verb: ENCRYPT.

EXCLUSIVE-OR OPERATION: the bit-by-bit modulo-2 addition without carry of binary numbers. This operation is represented by a circled + .

INITIALIZATION VECTOR (IV): A 64-bit vector used to help form the initial DES input block for the CFB and CBC modes of operation; a 64-bit cryptographic synchronizaioion vector.

KEY: Cryptographic key; the 56 random bits of the cryptographic variable.

KEY SCHEDULE FUNCTION: A logical unit within the DES algorithm which generates a different 48-bit vector from the 64-bit cryptographic variable for each of the sixteen rounds of the DES process.

LEAST SIGNIFICANT BIT (LSB): The right-most bit of a binary row vector. Synonym: Low order bit.

MAC: Message authentication code; see section 6 .
MESSAGE (MSG): A generic term used to describe a logical data entity. In general it is an ambiguous term; therefore, for specific applications it should be precisely defined.

MID: A message identifier used with the authentication-only mode.

MOST SIGNIFICANT BIT (MSB): The left-most bit of a binary row vector. Synonym: High order bit.

OCTET: A group of eight binary digits numbered from left to right: $1,2, \ldots .8$.

PLAIN TEXT: Decrypted data or data to be encrypted.
PSEUDORANDOM BINARY PROCESS: A deterministic technique for producing a sequence of binary digits which satisfy the statistical properties of a random bit stream.

APPENDIX A
SAMPLE DES ENCRYPTIONS AND DECRYPTIONS
 DES MODES OF OPERATION AN EXAMPLE OF THE ELECTRONIC CODEBDOK（ECB）MODE
 DES INPUT BLOCK DES OUTPUT BLOCK CIPHER TEXT


 $73 \mathrm{~b} 5 \mathrm{bcl} 3 \mathrm{ffcd8} 6 \mathrm{fd}$ ま0eseと8らもうま8き8きま The ECB mode in the decrypt state has been selected． | Cryptographic Key |  |
| :--- | :--- |
| TIME | CIPHER TEXT |
| 1 | 3 dlofae 4418 fb 83 d |
| 2 | 73 b 5 bcl 3 ffcd 6 fd |
| 3 | ff 8 f 8 fe 4583 a 5 ajf |



TIME PLAIN TEXT
The ECB mode in the encrypt state has been selected．
Cryptographic

$$
=0123456789 a b c d e f
$$



DES INPUT BLOCK

$$
666 \mathrm{f} 7220616 \mathrm{c} 6 \mathrm{c} 20
$$



$=0123456789$ abcdef
INPUT BLOCK －－－－－－－－－－－－－－－－－

PじN
 0てG99969をL0てS989 0てつG09โ90ててLき999



DES MODES OF OPERATION


$$
(0, b 7, b 6, \ldots, b l) \text {. }
$$




## DES MODES OF OPERATION

AN EXAMPLE OF THE EIGHT-BIT CIPHER-TEXT EEEDBACK (CFB) MODE The 8 -bit CFB mode in the encrypt state has been selected. Cryptographic Key $=0123456789$ abcdef Initialization Vector $=1234567890$ abcdef

The plain text is the ASCII code for "Now is the." These seven-bit characters are written in hexadecimal notation $(0, b 7, b 6, \ldots, b 1)$. The $\oplus$ represents bit-by-bit, modulo-2 addition.

| TIME | DES INPUT BLOCK | DES OUTPUT BLOCK | P | $\oplus$ | 0 | $=C$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 1234567890 abcdef | 3494 ccf 2 bda 243 a | $4 e$ | $\oplus$ | 34 | 7 a |
| 2 | 34567890 abcdef7a | bd914d9386653541 | 5 f | $\oplus$ | bd | $=\mathrm{d} 2$ |
| 3 | $567890 \mathrm{abcdef7ad2}$ | adaf3c45c53flf92 | 77 | $\oplus$ | ad | da |
| 4 | 7890 abcdef7ad2da | e3a3acc86c429d97 | 20 | $\oplus$ | e3 | = c3 |
| 5 | 90 abcdef7ad2dac3 | 5cblebb5lb70388d | 69 | $\oplus$ | 5 c | $=35$ |
| 6 | abcdef7ad2dac335 | f 3af29ce4cb966lf | 73 | $\oplus$ | f 3 | $=80$ |
| 7 | cdef7ad2dac33580 | aa22a74f73723adl | 20 | $\oplus$ | a | 8 a |
| 8 | ef7ad2dac335808a | 92d94ccel88fl5af | 74 | $\oplus$ | 92 | = e6 |
| 9 | $7 \mathrm{ad} 2 \mathrm{dac} 335808 \mathrm{ae5}$ | $4 \mathrm{fbbeal5ld3cfc54}$ | 68 | $\oplus$ | 4 f | $=27$ |
| 10 | d2 dac335808aé27 | 6 dabadlfdbasbc3b | 65 | (1) | 6d | $=08$ |


The 8-bit CFB mode in the decrypt state has been selected.


[^0]
## DES MODES OF OPERATION

AN EXAMPLE OF THE ONE-BIT CIPHER-TEXT FEEDBACK (CFB) MODE
The l-bit CFB mode in the encrypt state has been selected.
Cryptographic Key $=0123456789$ abcdef
Initialization Vector $=1234567890$ abcdef
The plain text is the ASCII code for "Now." These seven-bit characters are written in binary as (0,b7,b6,..., bl). The DES input and output blocks are written in hexadecimal notation. The $\oplus$ represents bit-by-bit, modulo-2 addition. Note: A draft, ANSI X3S3.8, link encryption standard requires that the bits of an ASCII character be processed in the reverse order of this example for l-bit CFB. This draft data communications standard is designed for the transmission of ASCII characters in the standard, serial-by-bit manner (bl,b2,..., b7).


## APPENDIX B <br> EFFECTS OF CIPHER TEXT ERRORS

DES MODES OF OPERATION

text errors．

> PLAIN TEXT

 656£7220515c6c20

<<<<<<<<<<<<<<<<<<<<<<<<<<<<<<<<<<<<<<<<<<<<<>>>>>>>>>>>>>>>>>>>>>>>>>>>>>>>>>>>>>>>>>>>>>>>>>
DES MODES OF OPERATION
CIPHER TEXT ERRORS AND THE CBC MODE

## The CBC mode in the decrypt state has been selected.

$$
\begin{aligned}
& \text { is the time for all } \\
& \text { hexadecimal notation ( } 0, b 7, b 6, \ldots, b_{\text {) }} \text {. } \\
& \text { er text block has been changed to } \\
& \text { he first plain text block should have } \\
& \text { bit errors affect the decryption } \\
& \text { nization is re-established. } \\
& l \text { be in error with a probability of } \\
& \text { ry errors are expected in this block. } \\
& 30 \text { errors in the first plain } \\
& \text { ly those bits in error which } \\
& \text { to the garbled cipher text bits. } \\
& \text { text block \#2 are incorrect. } \\
& \text { are unaffected by bit errors } \\
& \text { are used to identify the blocks } \\
& \text { rs. }
\end{aligned}
$$

PLAIN TEXT


fd84acf0148d654a 5б6f7220616c6c20
<<<<<<<<<<<<<<<<<<<<<<<<<<<<<<<<<<<<<<<<<<<<<>>>>>>>>>>>>>>>>>>>>>>>>>>>>>>>>>>>>>>>>>>>>>>>>>1

## DES MODES OF OPERATION

## CIPHER TEXT ERRORS AND THE CFB MODE

The 8 -bit CFB mode in the decrypt state has been selected.
The plain text is the ASCII code for "Now is the time for." These seven-bit characters are written in hexadecimal notation (0,b7,b6,....,bl). The cipher text character at time \#4 has been changed to "c4" instead of the correct value "c3." In the general k-bit CFB mode, bit errors within a k-bit character will affect the decryption of one character in those bit positions corresponding to the errors. Succeeding characters will experience an error probability of approximately fifty percent until the garbles have been flushed from the DES input block. In 8-bit CFB, errors within a character affect the decryption of nine cipher text characters before cryptographic synchronization is re-established.
The $\oplus$ represents bit-by-bit, modulo-2 addition.
Cryptographic Key = 0123456789 abcdef Initialization Vector $=1234567890$ abcdef

TIME DES INPUT BLOCK

| 1 | 1234567890 abcdef |
| :---: | :---: |
| 2 | 34567890 abcdef7a |
| 3 | 567890 abcdef7ad2 |
| 4 | 7890 abcdef7ad2da |
| 5 | 90 abcdef 7 ad 2 dac 4 |
| 6 | abcdef7ad2dac435 |
| 7 | cdef7ad2dac43580 |
| 8 | ef7ad2dac435808a |
| 9 | $7 \mathrm{ad} 2 \mathrm{dac} 435808 \mathrm{ae6}$ |
| 10 | d2dac435808ae627 |
| 11 | dac435808ae62708 |
| 12 | c435808ae627080f |
| 13 | 35808 ae6 $27080 \mathrm{f60}$ |
| 14 | 808 ae627080f6dfc |
| 15 | 8 ae627080f6dfcbl |
| 16 | e627080f6dfcbl 32 |
| 17 | 27080 f 6 dfcbl 3248 |
| 18 | 080 f6dfcbl 324817 |
| 19 | 0f6dfcbl 324817 d |

DES OUTPUT BLOCK
------------------$3494 c c f 2 b d a 243 a 6$ bd914d9386658541 adaf8c45c53flf92
e3a3acc86c429d97 c4 $\oplus$ e3 $=27$ $23 a e 7 d 3 f 645 f 7 d a a \quad 35 \oplus 23=16$ aca8467513ba93ae 383b374dc55ba5ll fbebefl88f6ceab0 $307 a 55324$ bc7d098 a3179850047a27f9 0 d 0 eaf 64 dc 7 e 5 ccb 5 cc 2582 fc 7 ca 06 f 3 953d fbl2d8a4cf4 fc $\oplus 95=69$ dc365b7e426e726e $57 c b 75$ f 386 e 76662 68 bbd6 da0 37 c 3 ebl 71e50a54bd8clfld b91c8fd54dld45f5 009 b 705 bb 2 ef 50 d 6

ERROR IN NEXT CIPHER = 31 AUTORESYNC ON NEXT CIPHER

| $C \oplus 0$ | $=P$ |
| :---: | :---: |
| $7 a \oplus$ | $=4 \mathrm{e}$ |
| $\mathrm{d} 2 \oplus \mathrm{bd}$ | $=6 \mathrm{f}$ |
| $\mathrm{da} \oplus \mathrm{ad}$ | $=77$ |


bl $\oplus \mathrm{dc}=6 \mathrm{~d}$
$32 \oplus 57=65$
$48 \oplus 68=20$
$17 \oplus 71=66$
$\mathrm{d} 6 \oplus \mathrm{~b} 9=6 \mathrm{f}$
$72 \oplus 00=72$

## APPENDIX C

CBC AND CFB FLOW CHARTS
(FOR ILLUSTRATIVE PURPOSES ONLY)

FIGURE C.1: CIPHER BLOCK CHAINING (CBC) OPERATIONS

LEGEND:

$$
\begin{aligned}
\text { K } & =\text { CRYPTOGRAPHIC KEY } \\
\text { IV } & =\text { INITIALIZATION VECTOR } \\
\text { li } & =\mathrm{i}-\text { TH DES INPUT BLOCK } \\
\text { Oi } & =\mathrm{i}-\text { TH DES OUTPUT BLOCK } \\
\text { Pi } & =\mathrm{i}-\text { TH PLAIN TEXT BLOCK } \\
\text { Ci } & =\mathrm{i}-\text { TH CIPHER TEXT BLOCK } \\
\oplus & =\text { EXCLUSIVE-OR }
\end{aligned}
$$



FIGURE C.2: CIPHER FEEDBACK (CFB) OPERATIONS


## APPENDIX D <br> EXAMPLES OF AUTHENTICATION-ONLY MODE


des modes of operation
an example of the authentication-only mode using cbc


> Key $=0123456789$ abcdef
Initialization Vector $=00006 a c l 03 b 28 f 99$

## INPUT BLOCK

DES OUTPUT BLOCK
efd5218cc2439930
40 f 0 al 601 d 7547 c 9
b 50 e 378 f 6058 b 74 a
7 ab 019 e 4 dd 481 bca
நə6T0qeL =
MAC
よ甘W



## DES MODES OF OPERATION

AN EXAMPLE OF THE AUTHENTICATION-ONLY MODE USING 8-BIT CFB
The 8 -bit $C F B$ mode in the encrypt state has been selected. For this example the MID structure consists of a 32-bit date-time code concatenated with a $32-b i t$, one-up binary counter. The date-time code designates the year (0), day of the year (003), hour of the day (l0 or 1000 hours), and minutes (15). This value is used to uniquely identify the cryptographic period. The binary counter has been initialized to 00000001 ; it is incremented by "l" for each message to be authenticated within the same DES key period. A $24-$ bit MAC was selected for this example. The plain text is the ASCII code for "Now is the time for." These seven-bit characters are written in hexadecimal notation (0,b7,b6,...,bl). The $\oplus$ represents bit-by-bit, modulo-2 addition.

Cryptographic Key $=0123456789$ abcdef Initialization Vector $=0003101500000001$

| TIME | DES INPUT BLOCK |
| :---: | :---: |
| 1 | 0003101500000001 |
| 2 | $03101500000001 d 9$ |
| 3 | 101500000001 d 9 d 2 |
| 4 | 1500000001 d 9 d 26 e |
| 5 | 00000001 d 9 d 26 e 7 d |
| 6 | 000001 d 9 d 26 e 7 d 60 |
| 7 | $0001 d 9$ d26e7d608c |
| 8 | 01d9d26e7d608clf |
| 9 | d9d26e7d608clf06 |
| 10 | d26e7d608clf06f6 |
| 11 | $6 \mathrm{e} 7608 \mathrm{clf06f664}$ |
| 12 | $7 \mathrm{~d} 608 \mathrm{clf06f.6642b}$ |
| 13 | $608 \mathrm{clf06f6642bed}$ |
| 14 | $8 \mathrm{clf06f6642bedfc}$ |
| 15 | 1f06f6642bedfcdf |
| 16 | $06 \mathrm{f} 6642 \mathrm{bed} \mathrm{fcdf08}$ |
| 17 | f 6642 bed fcdf0863 |
| 18 | 642 bedfcdf0863c4 |
| 19 | $2 \mathrm{bedfcdf0863c438}$ |
| 20 | edfcdf0863c43824 |

DES OUTPUT BLOCK $973 c 7 b 54$ e 5 bdd $4 d a$ bde39e43bf3f2258 1998d46fe4175d64 5ddf40f5124917fa 09342 c 9870 b4fe85 ffedd60c4e72814e 3 f 873 ff 6 e 2 e 4 cd 39 724 f 0467 a 5 fffdeb 9ec1876e54493a52 01 a 5 d 888 c 472 bcd d 0b6f90e412246e54 992db95a018d92lf 95c9b701a4681991 b2e4f4318882ca59 6dfff2d406ea8lde 43148 a 850 bd 66 dc 8 a 26 e 7 ae5815d7b60 57 d 8 cc 8 f 837534 b 9 560 cccbc949bb350 63113f72e8a09991


MESSAGE FORMAT:
MID TEXT
00031015000000014 e ff77206973207468652074696d6520566f7263113f


## APPENDIX E

RECOMMENDATIONS FOR DES IV MANAGEMENT

The security of a CFB or CBC implementation depends, inter alia, upon cryptographic synchronization procedures. For these modes of operation, this means proper management of the DES initialization vectors (IVs). IV management encompasses the generation, distribution, protection, usage, and disposal of initialization vectors.

At least one standard (*) currently under development is specifying security requirements for $C F B$ and CBC IVs in telecommunication environments. It is conceivable that a special application standard may need to tailor IV management to fit a particular set of application requirements in order to make the standard reasonably efficient as well as effective.

This standard on the modes of operation does not mandate specific techniques in IV management. This standard specifies only those requirements which are essential for unambiguously describing the mechanics needed to implement the modes of operation.

The following suggestions are recommended as preliminary guidelines which may be used until the publication of official guideline(s) or standard(s) in the area of IV management.

CBC IVs: The CBC IV consists of sixty-four binary digits. A single IV may be used throughout an entire CBC cryptographic period, however, this IV should be protected from disclosure. CBC IVs should not be repeated across cryptographic periods (same key) with a probability greater than 2 to the (-64). A 64-bit random or pseudorandom generation technique will satisfy this characteristic.

CFB IVs: CFB IVs consist of 64 binary digits. As with other $\overline{D E S}$ additive stream ciphers, it is desirable that CFB IVs change as frequently as possible in order to insure a unique additive stream to protect the plain text. CFB IVs should not repeat within a specific cryptographic period or across different cryptographic periods with a probability greater than 2 to the ( -48 ). As a corollary, CFB IVs may only contain a maximum of sixteen fixed bits. A 48-bit random or pseudorandom process is sufficient to satisfy this property. CFB IVs do not need to be protected from disclosure, i.e., they may be transmitted unencrypted through an unsecured channel.

[^1]-NOTES-
-NOTES-
-42-


[^0]:    <<<<<<<<<<<<<<<<<<<<<<<<<<<<<<<<<<<>>>>>>>>>>>>>>>>>>>>>>>>>>>>>>>>>>>>

[^1]:    * Proposed Federal Standard 1027; Telecommunications: Security Requirements for Use of the Data Encryption Standard; 4 September 1979,18 pages.

