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# A Computerized Approach for Identifying Cost-Effective Fire Safety Retrofits in Health Care Facilities 

Robert E. Chapman

Center for Building Technology

William G. Hall
Center for Applied Mathematics

Phillip T. Chen

Center for Building Technology
National Engineering Laboratory
National Bureau of Standards
U.S. Department of Commerce

Washington, D.C. 20234

December 1979
Final Report
Issued January 1980

Sponsored by the:
Center for Fire Research
Vational Engineering Laboratory lational Bureau of Standards
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## U.S. DEPARTMENT OF COMMERCE, Philip M. Klutznick, Secretary

Luther H. Hodges, Jr., Deputy Secretary<br>Jordan J. Baruch, Assistant Secratary for Science and Technology<br>NATIONAL BUREAU OF STANDARDS, Ernest Ambler, Director

## PREFACE

This research was conducted under the sponsorship of the Center for Fire Research by the Applied Economics Group, Center for Building Technology, and the Operations Research Division, Center for Applied Mathematics, National Engineering Laboratory, National Bureau of Standards.

This study develops a computerized procedure which helps identify the least-cost means of retrofitting a designated area of a health care facility to achieve compliance to the Life Safety Code. The procedure also identifies from 10 to 20 retrofit alternatives, some of which are quite close to the least-cost solution. The procedure is intended to be used as a management tool to facilitate the design selection process by providing both information on relative costs and a chance to match common retrofit packages across areas of the health care facility designated as deficient.

Appreciation is extended to Dr. Harold E. Marshall and Ms. Kimberly A. Barnes, Applied Economics Group, who reviewed the economic aspects of this paper. Appreciation is also extended to Ms. Patsy Saunders, Dr. Howard Hung and Mr. Ralph Schofer, Operations Research Division, and Messrs. Harold E. Nelson and A. J. Shibe, Center for Fire Research, who provided many useful suggestions for improving the treatment of certain topics in this paper. Special appreciation is extended to Dr. Alan J. Goldman, Operations Research Division, whose stimulating discussions provided guidance and encouragement throughout this effort.

## ABSTRACT

This study focuses on how a computerized version of the Fire Safety Evaluation System developed by the Center for Fire Research at the National Bureau of Standards can be used to determine equivalence to the Life Safety Code in the least costly manner. This study presents a programmer-oriented discussion of the mathematical, economic and engineering considerations that went into the development of the linear programming algorithm for identifying cost-effective retrofits. Programmer-oriented topics treated in this report include: a discussion of user options; program documentation; format statements; flow charts; sample computer runs; and a complete listing of the computer program.

Keywords: Applied economics; building codes; economic analysis; fire safety; health care facilities; hospitals; life safety; mathematical programming; nursing homes; optimization; renovation.

## CONTENTS

Page
PREFACE ..... iii
ABSTRACT ..... iv
LIST OF FIGURES ..... vii
LIST OF TABLES ..... vii
LIST OF EXHIBITS ..... viii
SI CONVERSION UNITS ..... ix

1. INTRODUCTION ..... 1
1.1 Background ..... 1
1.2 Purpose ..... 2
1.3 Scope and Approach ..... 3
1.4 The Fire Safety Evaluation System ..... 4
2. COMPUTERIZED PROCEDURE FOR IDENTIFYING COST-EFFECTIVE RETROFITS. ..... 13
2.1 Method of Approach ..... 14
2.2 Problem Formulation ..... 15
2.3 Description of Computer Algorithm ..... 19
2.4 Applying the Computerized Procedure ..... 25
2.4.1 Data Requirements and User Options ..... 26
2.4.2 The Output Format and Its Interpretation ..... 38
3. SUMMARY ..... 40
APPENDIX A Unit Pricing Information ..... 42
APPENDIX B Documentation of Computer Algorithm/Program ..... 45
B. 1 Program Functional Description ..... 45
B. 2 Variable Definition ..... 49
B. 3 Definitions of Data Inputs ..... 53
B. 4 Description of Reports Produced ..... 55
APPENDIX C Sample Computer Runs ..... 60
APPENDIX D Listing of the Computer Programs ..... 83
D. 1 Listing of MAIN Program ..... 85
D. 2 Listing of Subroutine PRSOL (PRint SOLutions) ..... 97
Page
D. 3 Listing of Subroutine FEASIB (FEASIBility Test) ..... 98
D. 4 Listing of Subroutine MOTEST (MOdification TEST) ..... 99
D. 5 Listing of Subroutine RHTAB (Right Hand TABles). ..... 99
D. 6 Listing of Subroutine RVSMPX
(ReVised SiMPleX) ..... 100
D. 7 Listing of Subroutine PRSMX (PRint SiMpleX) ..... 112
REFERENCES ..... 114

## LIST OF FIGURES

Page
1.1 Delphi Method ..... 5
2.1 User Flowchart ..... 14
2.2 Optimal Solution: Graphical Method ..... 20
2.3 Alternative Solution: Graphical Method ..... 23
D. 1 Flowchart of Computer Program . . . . . . . . . . . . . ..... 84
LIST OF TABLES
Page
1.1 Values of Safety Parameters Corresponding to Strict Compliance to the Life Safety Code for Non-Sprinklered Health Care Facilities ..... 7
2.1 Abbreviations for Elements and Units to be Used in Reporting Data on Potential Retrofits ..... 27
2.2 Listing of Data Requirements ..... 28
2.3 User Options: Control and Modification Statements ..... 34

## LIST OF EXHIBITS

Page
1.1 Occupancy Risk Factor Calculation Worksheet ..... 8
1.2 Worksheet for Determining the Values of the Safety Parameters ..... 9
1.3 Worksheet for Calculating Containment Safety, Extinguishment Safety, People Movement Safety, and General Safety ..... 11
1.4 Worksheet for Evaluating Fire Zone Safety Equivalency ..... 12
2.1 Initial Inputs ..... 26
2.2 Sample Input Information on Potential Retrofits ..... 30
2.3 Sample Control/Modification Card Sequence ..... 35
2.4 Sample Output Format for Optimal and Prescriptive Solutions ..... 39
C. 1 Sample Input Run Stream ..... 62
C. 2 Sample Output Run Stream ..... 63

The conversion factors and units contained in this report are in accordance with the International System of Units (abbreviated SI for Systeme International d'Unites). The SI was defined and given official status by the llth General Conference on Weights and Measures which met in Paris, France in October 1960. For assistance in converting U.S. customary units to SI units, see ASTM E 380, ASTM Standard Metric Practice Guide, available from the American Society for Testing and Materials, 1916 Race Street, Philadelphia, PA 19103. The conversion factors for the units found in this Standard are as follows:

Length
1 in - 0.0254* meter
$1 \mathrm{ft}=0.3048^{*}$ meter
$1 \mathrm{mil}=0.001 * \mathrm{in}$
1 yd $=0.9144 *$ meter
Area
1 in $^{2}=6.4516 * \times 10^{-4}$ meter $^{2}$
$1 \mathrm{ft}^{2}=0.0929$ meter $^{2}$
$1 \mathrm{yd}^{2}=0.836$ meter ${ }^{2}$
Volume
1 in $^{3}=1.639 \times 10^{-5}$ meter $^{3}$
1 1iter $=1.00 * \times 10^{-3}$ meter $^{3}$
1 gallon $=3.785$ 1iters
Temperature

```
* C = 5/9 (Temperature }\mp@subsup{}{}{\circ}\textrm{F}-32
```

[^0]
## 1. INTRODUCTION

### 1.1 BACKGROUND

The identification of cost-effective levels of fire safety in health care facilities is a major concern to hospital administrators, fire safety engineers and public policy makers. Rising construction and operating costs coupled with more stringent building codes and continuing advances in medical and building technology have complicated the issue, forcing health care facility administrators to carefully assess the alternative means through which they can design, construct or update their facilities. Although multiple death fires in health care facilities are rare occurrences, the potential for major losses of life and property does exist and should be recognized in the selection of fire safety measures. This potential and the resulting need for a national commitment to fire safety in health care facilities has been emphasized in numerous congressional hearings. ${ }^{1}$

The National Fire Protection Association (NFPA) has long been recognized as a vehicle through which such a national commitment could be achieved. For over 60 years the NFPA has been a leader in the development of voluntary codes which establish acceptable fire safety levels. The Life Safety Code (NFPA 101-1973) is currently the most widely used guide for identifying the minimum level of fire safety in buildings. Although the code may be thought of as prescriptive since it prescribes fixed solutions for life safety in designated occupancies, performance concepts can be explicitly introduced through a provision which allows for equivalent solutions. In particular, Provision 1-3118 states:

Nothing in this code is intended to prevent the use of new methods or new devices, providing sufficient technical data is submitted to the authority having jurisdiction to demonstrate that the new method or device is equivalent in quality, strength, fire resistance, effectiveness, durability, and safety to that prescribed by this code. ${ }^{2}$

In light of this provision, the National Bureau of Standards' Center for Fire Research, through support from the Department of Health, Education and Welfare, has developed a system for determining how combinations of several widely accepted fire safety systems could be used to provide a

[^1]level of safety equivalent to (equal to) that required in the 1973 Life Safety Code. ${ }^{1}$ The equivalency methodology which emerged from this effort is particularly attractive since it lends itself to computer optimization techniques. Such an optimization technique should result in improved fire safety in health care facilities because it will resolve many of the differences of opinion surrounding the cost impacts of fire safety in health care facilities in general and the Life Safety Code in particular.

### 1.2 PURPOSE

The purpose of this report is to present a programmer-oriented description of the mathematical, economic, and engineering considerations that went into the development of a linear programming algorithm which permits the least cost means of achieving compliance to the Life Safety Code to be identified.

The computer program discussed in this report is particularly useful because it is based on the equivalency methodology developed by the Center for Fire Research. Since the NFPA is in the process of adopting this equivalency methodology into the Life Safety Code, any solutions from the computer program will satisfy Provision 1-3118 of NFPA 101-1973. Furthermore, since each of the parameters used in the equivalency methodology has a unique value which corresponds to strict compliance, it is possible to quantify the cost savings attributable to a performance based approach or equivalency methodology over that of strict compliance. Although the procedure is valid for both new and existing facilities, it is anticipated that its primary use will be in identifying alternative courses of action open to administrators faced with retrofitting existing facilities.

The computer program uses as its primary input information collected as an integral part of a thorough fire safety evaluation. This information permits the current state of the health care facility to be unambiguously identified. The least-cost or optimal combination of retrofits is identified using the following information:
(1) the current state of the health care facility;
(2) the minimum passing "score" needed to achieve compliance; and
(3) the anticipated costs of each retrofit measure.

The computer program then generates and analyzes a class of alternative retrofit combinations. The optimal combination of retrofits and any alternatives which the program produces, usually between 10 and 20 , are then summarized in tabular form and ranked from least costly to most costly. By using this approach, health care facility decision makers

[^2]have greater flexibility in choosing among retrofit combinations. In particular, by providing alternatives, the decision maker has the opportunity to assess very effectively the impact that nonconstruction costs would have on the choice of the optimal retrofit combination.

### 1.3 SCOPE AND APPROACH

The bulk of this report is composed of a set of technical appendices. These appendices are designed to be self-contained and hence may be read independently. The major thrust of each appendix is to lay out in detail the technical and theoretical considerations upon which the computerized version of the Fire Safety Evaluation System are based. In that sense the technical appendices are supporting evidence for results presented in the companion report, Economic Aspects of Fire Safety in Health Care Facilities: Guidelines for Cost-Effective Retrofits.

The final section of Chapter 1 outlines the Fire Safety Evaluation System and establishes a framework for the development of the linear programming package discussed in the remainder of the report.

The computer program and its method of solution are presented in Chapter 2. A mathematical discussion of the linear programming package used to identify the least-cost combination of retrofits is then given. The way in which the computer program generates alternative solutions using the optimal solution as a base is then presented. Explicit directions for using the computer program and interpreting its output are given in the final section of Chapter 2.

Appendix A presents the retrofit cost data used in the computerized procedure. The purpose of this appendix is to serve as a ready reference for potential users who may wish to adjust one or more of the retrofit costs to reflect local construction market conditions.

Appendix B gives a programmer-oriented description of the linear programming package. The appendix includes algorithmic and functional descriptions as well as user options and general requirements.

Appendix $C$ consists of a series of sample computer runs. These runs are designed to highlight the input and output format and the user options which have been built into the procedure.

The report concludes with a listing of the complete computer software package. All programs presented in Appendix D are written in FORTRAN.

[^3]
### 1.4 THE FIRE SAFETY EVALUATION SYSTEM

The Fire Safety Evaluation System is a quantitative evaluation system for grading fire safety in health care facilities. The primary use of the system is to determine how combinations of widely accepted fire safety equipment and building construction features may provide a level of safety equivalent to that required by the 1973 Life Safety Code. Three major concepts are basic to the Fire Safety Evaluation System. They are:

1) Occupancy Risk: the number of people affected by a given fire, the level of fire they are likely to encounter, and their ability co protect themselves.
2) Building Safety Features: the ability of the building and its fire protection systems to provide measures of safety commensurate with the risk.
3) Safety Redundancy: in-depth protection, through the simultaneous use of alternative safety methodologies such as Containment, Extinguishment, and People Movement. The design of the complete fire safety system is intended to ensure that the failure of a single protection device or method will not result in a major failure of the entire system.

The concept of safety redundancy is of central importance to the Fire Safety Evaluation System since Provision 2-1111 of the Life Safety Code requires:

> The design of exits and other safeguards shall be such that reliance for safety to life in case of fire or other emergency will not depend solely on any single safeguard; additional safeguards shall be provided for life safety in case any single safeguard is ineffective due to human or mechanical failure.

The task of ensuring that the Fire Safety Evaluation System satisfied Provision $2-1111$ of the Life Safety Code was the responsibility of a panel of fire safety experts. The goal of the panel was to reach consensus on all relevant fire safety issues. To facilitate this process, a management tool known as the Delphi Method was used. The Delphi Method, as used in developing the Fire Safety Evaluation System, consisted of four steps. These steps are illustrated in Figure 1.1. Notice that the steps illustrated in the figure form a closed loop. This is because a certain amount of recycling of ideas was needed in order to achieve consenus.

[^4]
## DELPHI METHOD

REASSESS/ RECYCLE

## SELECT SAFETY FACTORS



The first step in the process was to select a set of key safety factors, These factors were related to the concepts of Occupancy Risk and Building Safety Features mentioned earlier. (For example, Occupancy Risk includes as a factor Patient Mobility and Building Safety Features includes as a factor Interior Finish in the Corridor and Exits.) The second step focused upon the identification of a set of parameter associated with each factor. (For example, Patient Mobility includes as parameters Mobile, Limited Mobility, Not Mobile, Not Movable. Interior Finishes in the Corridor and Exits include Class A, Class B, and Class C flame spread ratings as parameters.) The third and most critical step was to assign a weight to each parameter which best reflects either the relative risk posed by that parameter or the net contribution to life safety provided by that parameter. More specifically, negative values reflected greater risks whereas positive values contributed toward a higher level of safety within the fire zone. ${ }^{1}$ The system treats a value of zero as "safety" neutral. (The values for the three parameters associated with the safety factor Interior Finish in the Corridor and Exits are: Class C, -5 points; Class B, 0 points; and Class A, 3 points.) In the fourth step, the value of each safety parameter assigned by the panel is reassessed for adequacy and consistency. In the event that the system which emerged from the panel was shown to be inadequate or inconsistent, the entire four-stage process was repeated. The end result of the panel's work was a series of worksheets which permitted the relative merits of each fire safety parameter to be carefully assessed. These worksheets are presented as Exhibits l.l through 1.4. In addition, since each of the 13 Building Safety Features (see Table 1.1) has a unique parameter which corresponds to strict compliance, it was possible to compute the score, or level of safety, provided by the Life Safety Code for Extinguishment, Containment and People Movement Safety. These values were then used as a base which any alternative to strict compliance to the Life Safety Code had to match or exceed.

The first worksheet, Exhibit l.l, consists of a brief description of the fire zone and the means for calculating Occupancy Risk. Occupancy Risk is calculated by selecting the appropriate value for each of the five factors shown in Table l of Exhibit l. These values are then entered into the coded spaces in Table 2 (Exhibit l.l) and multiplied together to get an unadjusted occupancy risk factor. The resultant is then entered either in Table 3A (Exhibit l.l) if the building is new or in Table 3 B if the building is existing. The occupancy risk factor for the fire zone is then calculated by taking the product of the weighting factor and the unadjusted occupancy risk factor. The Occupancy Risk factor is then used to establish the minimum level of General Safety which must be provided by the 13 Building Safety Features in order to be deemed in compliance to the Life Safety Code.

[^5]Table 1.1 VALUES OF SAFETY PARAMETERS CORRESPONDING TO STRICT COMPLIANCE TO THE LIFE SAFETY CODE FOR NON-SPRINKLERED HEALTH CARE FACILITIES

BUILDING TYPE
SAFETY
FACTOR

## Table 1. OCCUPANCY RISK PARAMETER FACTORS

## RISK PARAMETERS

RISK FACTOR VALUES

1. PATIENT

MOBILITY (M)

| MOBILITY <br> STATUS | MOBILE | LIMITED <br> MOBBLITY | NOT <br> MOBILE | NOT <br> MOVABLE |
| :---: | :---: | :---: | :---: | :---: |
| RISK FACTOR | 1.0 | 1.6 | 3.2 | 4.5 |

2. PATIENT

DENSITY (D)

| PATIENT | 1.5 | 6.10 | 11.30 | $>30$ |
| :---: | :---: | :---: | :---: | :---: |
| RISK FACTOR | 1.0 | 1.2 | 1.5 | 2.0 |

3. ZONE

LOCATION (L)

| FLOOR | 1ST | 2ND OR <br> 3RD | 4TH TO <br> 6TH | 7TH AND <br> ABOVE | BASEE <br> MENTS |
| :---: | :---: | :---: | :---: | :---: | :---: |
| RISK FACTOR | 1.1 | 1.2 | 1.4 | 1.6 | 1.6 |

4. RATIO OF

PATIENTS TO
ATTENDANTS

| PATIENTS <br> ATTENDANT | $\frac{1-2}{1}$ | $\frac{3.5}{1}$ | $\frac{6.10}{1}$ | $\frac{\text { 11 }}{1}$ | ONE OR* <br> $\frac{\text { MORE }}{\text { NONE }}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| RISK FACTOR | 1.0 | 1.1 | 1.2 | 1.5 | 4.0 |

5. PATIENT AVERAGE AGE (A)

| AGE | UNDER 65 YEARS <br> AND OVER 1 YEAR | 65 YEARS \& OVER <br> 1 YEAR \& YOUNGER |
| :---: | :---: | :---: |
| RISK FACTOR | 1.0 | 1.2 |

* RISK FACTOR OF 4.0 IS CHARGED TO ANY ZONE THAT HOUSES PATIENTS WITHOUT ANY STAFF IN IMMEDIATE ATTENDANCE


| Table 3A. (NEW BUILDINGS) |
| :---: |
| $1.0^{\times} \square=\square$ |


| Table 3B. (EXISTING BUILDINGS) |
| :---: |
| $0.5^{\times} \square=\square$ |



The second worksheet, Exhibit 1.2, provides the foundation for the computerized procedure discussed in Chapter 2 and Appendices B, C, and D. Table 4, Exhibit 1.2, gives the scores associated with the parameters for each of the 13 Building Safety Features. To evaluate each fire zone, it is necessary to identify the appropriate value associated with each of the 13 Building Safety Features. The existing state of the fire zone is then defined by recording (circling, marking, or checking) all of these values on Table 4 (Exhibit 1.2). In the evaluation, it is important to point out that the level of each Building Safety Feature is determined by the worst case condition within the fire zone. Referring once again to Exhibit 1.2 it can be seen, for each Building Safety Feature, that those parameters which have a higher score represent potential retrofits. For example, if in the current state the flame spread rating on Interior Finishes in the Corridor and Exits was Class C, then both Class B and Class A flame spread ratings would be potential retrofits. More importantly, by combining the improvement in score with the anticipated retrofit costs, it is possible to establish a means for upgrading the level of fire safety within the fire zone in the most cost-effective manner.

Table 5, the third worksheet, is shown in Exhibit 1.3. Table 5 Exhibit 1.3 Provides a means for calculating the score associated with the four safety redundancy requirements. (The four safety redundancy requirements are: 1) Containment Safety; 2) Extinguishment Safety; 3) People Movement Safety; and 4) General Safety.)

In order to calculate the score for each of the safety redundancy requirements, it is necessary to enter the value of the parameter identified in Table 4 (Exhibit 1.2) as corresponding to the existing state of the Building Safety Feature into the appropriate spaces in the coded rows of Table 5 (Exhibit 1.3). (No values are entered in the shaded spaces of Table 5, Exhibit 1.3.) Each of the four columns is then summed to get an overall score. These scores are labeled $S_{1}, S_{2}, S_{3}$ and $S_{G}$ in Table 5 of Exhibit 1.3.

The fourth worksheet provides the means for determining whether or not the fire zone generates a level of fire safety equivalent to that of the Life Safety Code. Basically, this is done by taking the four scores calculated in Table 5 (see Exhibit 1.3) and entering them in the boxes labeled $S_{1}, S_{2}, S_{3}$ and $S_{G}$. The user then selects the values from Table 6 (see Exhibit 1.4) for Containment Safety, Extinguishment Safety, and People Movement Safety for the appropriate building type and fire zone location. These values are entered in the boxes labeled $S_{a}, S_{b}, S_{c}$ in Table 7 of Exhibit 1.4. The Occupancy Risk factor calculated on the first worksheet is then entered in the box labeled R. Based on these two sets of numbers, it is possible to test if the fire zone provides a level of safety equivalent to the Life Safety Code. This test is performed by determining if the difference between the first set of numbers, $S_{1}$, $S_{2}, S_{3}$, and $S_{G}$, and the second set of numbers, $S_{a}, S_{b}, S_{c}$, and $R$, in Table 7 (see Exhibit 1.4) is greater than or equal to zero.

## Table 5. INDIVIDUAL SAFETY EVALUATIONS

| SAFETY <br> parameters | CONTAINMENT SAFETY $\left(s_{1}\right)$ | EXTINGUISHMENT SAFETY $\left\|S_{2}\right\|$ | PEOPLE MOVEMENT <br> SAFETY (S3) | GENERAL SAFETY [SG] |
| :---: | :---: | :---: | :---: | :---: |
| 1. CONSTRUCTION |  |  |  |  |
| 2. INTERIOR FINISH <br> (Corr. \& Exit) |  |  |  |  |
| 3. INTERIOR FINISH (Rooms) |  |  |  |  |
| 4. CORRIDOR PARTITIONS/WALLS |  |  |  |  |
| 5. DOORS TO CORRIDOR |  |  |  |  |
| 6. ZONE DIMENSIONS | (ll ${ }^{\text {a }}$ - ${ }^{\text {a }}$ |  |  |  |
| 7. VERTICAL OPENINGS |  |  |  |  |
| 8. hazardous areas |  |  |  |  |
| 9. Smoke Control |  |  |  |  |
| 10. EMERGENCY movement routes |  |  |  |  |
| $\begin{aligned} & \text { 11. MANUAL FIRE } \\ & \text { ALARM } \end{aligned}$ |  |  |  |  |
| 12. SMOKE DETECTION <br> \& ALARM |  |  |  |  |
| 13. AUTOMATIC SPRINKLERS |  |  | $\div 2=$ |  |
| total value | $s_{1}=$ | $s_{2}=$ | $S_{3}=$ | $S_{G}=$ |

Table 6. MANDATORY SAFETY REQUIREMENTS

|  | CONTAINMENT <br> $S_{a}$ |  | EXTINGUISHMENT <br> Sb |  | PEOPLE <br> MoVEMENT <br> So |  |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
| ZONE LOCATION | New | Exist. | New | Exist. | New | Exist. |
| FIRST FLOOR | 9.0 | 4.0 | 6.0 | 3.0 | 6.0 | 1.0 |
| ABOVE FIRST FLOOR | 14.0 | 8.0 | 8.0 | 5.0 | 9.0 | 3.0 |


| ZONE SAFETY EQUIVALENCY EVALUATION |  |  |  | YES | NO |
| :---: | :---: | :---: | :---: | :---: | :---: |
| CONTAINMENT SAFETY $\left(S_{1}\right)$ | less | $\begin{aligned} & \text { MANDATORY } \\ & \text { CONTAINMENT }\left(\mathrm{S}_{\mathrm{a}}\right) \quad \geq 0 \end{aligned}$ | $\square^{s_{1}}-\square^{s_{2}}=\square$ |  |  |
| EXTINGUISHMENT <br> SAFETY $\left\|S_{2}\right\|$ | less | $\begin{aligned} & \text { MANDATORY } \\ & \text { EXTINGUISHMENT }\left(S_{b}\right) \geq 0 \end{aligned}$ | $\square-\bar{s}^{s_{2}}=\square$ |  |  |
| $\begin{aligned} & \text { PEOPLE } \\ & \text { MOVEMENT } \\ & \text { SAFETY } \left.\mid S_{3}\right) \end{aligned}$ | less | MANDATORY PEOPLE MOVEMENT $\quad\left\|S_{\mathrm{C}}\right\| \geq 0$ | ${ }^{s_{3}}-s_{C}=$ |  |  |
| $\begin{aligned} & \text { GENERAL } \\ & \text { SAFETY }\left\|S_{G}\right\| \end{aligned}$ | ss | OCCUPANCY  <br> RISK (R) | $\square^{S_{6}}-\square^{\mathrm{R}}=\square^{\mathrm{G}}$ |  |  |

In the event that the fire zone fails to pass the equivalency test, it will be necessary to select a retrofit strategy which will ensure that the Building Safety factors produce scores which match or exceed each of the four redundancy requirements. A systematic means for doing this which explicitly introduces relative costs into the retrofit decision is the subject of the remainder of this report.

## 2. COMPUTERIZED PROCEDURE FOR IDENTIFYING COST-EFFECTIVE RETROFITS

The computerized procedure presented in this section is based on a mathematical technique known as linear programming. In its usual context linear programming deals with the problem of allocating limited resources among competing activities in an optimal way. At the foundation of any linear programming problem is a mathematical model which describes the problem of concern. In this case the mathematical model is the Fire Safety Evaluation System. The term "linear" refers to the requirement that all mathematical functions in the model are linear. ${ }^{1}$ The term "program" is used in the general sense in that it refers to a plan rather than a computer program per se. The basic reason why all mathematical functions involved in the problem are 1 inear may be explained through reference to Table 4 and Table 5 of the Fire Zone Safety Evaluation Worksheet (see Exhibits 1.2 and 1.3). In Table 4 there is one and only one level of each Building Safety Feature possible at any one time. ${ }^{2}$ This is due to the requirement that the most hazardous level associated with each feature determines the score for that feature. In Table 5 (Exhibit 1.3) the score for each of the four safety redundancy requirements (containment safety, extinguishment safety, people movement safety, and general safety) is the sum of the values of the appropriate parameter identified in Table 4 (Exhibit 1.2) as either the existing state or a potential retrofit.

1 A linear function is defined as a function of the form

$$
f(x)=a_{o}+a_{1} x_{1}+\cdots \cdot+a_{j} x_{j}+\cdots+a_{n} x_{n}
$$

where $a_{j}$ are coefficients not all zero and the $x_{j}$ are variables. The geometrical representation of a linear function is a straight line, a plane, or a hyperplane. For example, $f(x)=a+b x$, a straight line, is a linear function where $g(x)=c+d x^{2}$, a parabola, is not.

The above condition requires that all variables corresponding to factor levels must be either zero or one. The solution to a linear programming problem yields continuous variables; however, it can be shown that, because of the constraint structure of the model, the continuous solution is always "nearly" integer.

### 2.1 METHOD OF APPROACH

The method of approach taken in developing and using the linear programming procedure has the Fire Safety Evaluation System as its foundation. The steps which must be taken in order to go from the basics of the Fire Safety Evaluation System to the linear programming procedure are the subject of this section. To illustrate these steps a schematic diagram known as a flowchart is useful.

FIGURE 2.1 USER FLOWCHART


Figure 2.1 displays the sequence of steps between the Fire Safety Evaluation System and the computerized procedure. As a first step the Fire Zone Safety Evaluation Worksheet must be used to identify the existing state of each of the 13 Building Safety Features. Plugging this information into Table 5 of the worksheet (see Exhibit l.3) permits the existing state of each feature and each individual fire zone to be determined. Using the information on the existing state for each feature as a starting point, engjneering judgment may then be used to identify a set of potential retrofits. It is important to point out that based on engineering judgment some "theoretically" possible retrofits may be excluded. ${ }^{2}$ One important opportunity which should not be overlooked is the collection of information on potential retrofits during the safety inspection. As indicated in the third block, once a set of potential retrofits has been identified it is then necessary to count the number of elements which must be treated in order to move to a higher state. The fourth step in the sequence of events relates to the unit cost or cost per element. These costs are the ones actually used in performing the economic analyses. They are an integral part of the procedure and are stored in an "element cost matrix." This cost matrix interacts with the information on the number of elements in the following way. Associated with each potential retrofit is a set of information on the one or more elements which must be treated to move to a higher state. This "format" is followed when information
${ }^{1}$ Engineering input is important at all stages of the procedure but is particularly important in identifying potential retrofits.

2 This opportunity represents the first of three user options which will be addressed in Section 2.4. (A theoretically possible retrofit is any parameter which has a higher score than the parameter corresponding to the existing state.) By the same token the user has the option to require that a particular retrofit be undertaken, or not undertaken.
on the number of elements is input. All of this information is then stored in an "element count matrix." The product of the element count and element cost matrices yields the total cost associated with each potential retrofit. It is important to point out that the user has the option to accept or modify any information contained in the element cost matrix. The considerations underlying the per unit or per element costs are presented in Appendix A. Thus, should the user feel that the information in the element cost matrix does not adequately reflect the costs associated with the local construction market or is inappropriate on some other grounds, it can be modified either through the use of time-location factors or changing one or more of the engineering assumptions.

The information identified in the sequence of steps outlined above is the only information required to run the computerized procedure. Although the computerized procedure is only a "working prototype" a maximum amount of flexibility has been built into it. These efforts at simplifying the procedure are the subject of Sections 2.4 and 2.5 . The subject of the next two sections, however, is the formulation of the linear programming problem and a discussion of how the computer algorithm selects the optimal solution and generates a set of alternatives. Certain portions of the discussion which follows are more technical than previous sections. Therefore the reader who is primarily interested in obtaining a conceptual understanding of linear programming and how it may be applied to the problem of retrofitting a fire zone is directed to Section 2.3.

### 2.2 PROBLEM FORMULATION

To formulate the mathematical model (linear program) for this problem, we shall refer to information in Table 4 of the Fire Zone Safety Evaluation Worksheet. Table 4 may be thought of as matrix with 13 rows, one

1 Building Safety Feature 1 , Construction, is a special case. In Table 4 of the Worksheet there are four separate rows of scores corresponding to different floors of the building. Since a retrofit involving a change of floor need not be considered, only one of these rows (that for the appropriate floor) is included in the computer stored version of Table 4. Each row is divided into three segments: (1) Combustible-Wood Frame; (2) Combustible-Ordinary; and (3) Non-combustible. The first two segments contain two cells: (1) Unprotected; and (2) Protected. The third segment contains three cells: (1) Unprotected; (2) Protected; and (3) Fire Resistive. The procedure assumes that it is impossible to move from one segment to another. This assumption was made because of the difficulty in identifying cost elements and standard procedures for such retrofits. For computation purposes a dummy element is added to segments one and two. This permits an auxiliary 4 by 3 by 3 array to be used to store all values of the first Building Safety Feature and simplifies the construction of the computer stored version of Table 4. This approach may be changed when actual production runs begin
for each of the 13 Building Safety Features and 6 columns. ${ }^{1}$ There are up to 6 parameters (states) associated with any given safety feature. The variable $X_{i j}$ is used to identify the state of each factor. By definition, $X_{i j}$ is equal to one if the $i^{\text {th }}$ factor is in the $j^{\text {th }}$ state and is zero otherwise. (Recall that the score for each factor is determined by the most hazardous condition within the fire zone.) $V_{i j}$ is the score associated with the $i^{\text {th }}$ feature and $j^{\text {th }}$ state (entry in Table 4). These values are taken directly from Table 4. For example, if the $i^{\text {th }}$ factor is in the $j^{\text {th }}$ state the value, or score, associated with the $i{ }^{\text {th }}$ row is $V_{i j} X_{i j}$ since $X_{i j}$ ' is equal to zero for $j^{\prime}$ unequal to $j$. Score improvements are thus possible as a result of retrofits. If the $i^{\text {th }}$ factor is currently in the $j$ th state, $X_{i j c}$ would be the preretrofit or current state, and $X_{i j}$ would be the postretrofit or new state. It is of course required that $j_{j}>j_{c}$ otherwise no improvement has been made. An examination of the scores associated with $X_{i j}$ and $X_{i j}$ shows that $V_{i j}>V_{i j}{ }^{2}$ It is now time to show how costs may be introduced into the mathematical model. The variable $C_{i j}$ is used to record the cost of upgrading the $i^{\text {th }}$ Building Safety Feature from the $j^{\text {th }}$ state to the $j^{\text {th }}$ state. For each possible retrofit being considered, $C_{j} j_{\text {is }}$ a function of the number of elements and the unit cost or cost per efement. In mathematical terms $C_{i j}$ is the dot product of the $i$ th vector of element quantities and the $i^{\text {th }}$ vector of element costs.

Keeping in mind that the objective is to match or exceed the scores for each of the four categories of safety (containment, extinguishment, people movement, and general) in the least costly manner, it is now possible to formulate the problem mathematically. The problem is to choose $X_{i j} j$, $j_{c}^{1} \leq j \leq j_{\text {max }}^{1}$, where $j_{c}^{1}$ is the current state of the $i^{\text {th }}$ factor and $j_{\text {max }}^{i}$ is the maximal state of the $i^{\text {th }}$ factor, so as to minimize total retrofit costs

$$
\sum_{i=1}^{13} \quad j_{j=j_{c}^{i}}^{i} \quad c_{i j} X_{i j} \quad x_{i j}=0 \text { or } 1
$$

1 There are no more than five real states for any of the safety factors, but the conditions $*, * *$, and ... footnoted in Table 4 are most easily accommodated by the introduction of contrived variables and constraints. Therefore the extra column is required. The contrivance is not observable by the user; pre-optimization and post-optimization processing transform the variables from and to those defined by Table 4.
2
Several of the $V_{i j}$ 's have alternative values due to the level of some other Building Safety Feature (other i). Whenever such a situation occurs it is called a row interdependence. Three distinct row interdependencies are possible. These interdependencies, which involve rows 4,5 and 6 , are defined in the footnotes at the bottom of Table 4. These interdependencies may result in up to 3 additional constraints, called interdependency constraints, and up to 3 additional variables, called dummy states.
subject to
(1) parameter value constraints for the cases where row interdependencies are not possible are given as:
$j_{\text {max }}^{i}$
$\sum_{j=j_{c}^{i}}^{i} X_{i j}=1 \quad$ for $i \neq 4,5,6$
parameter value constraints for the cases where a row interdependence is possible are given as:
$j_{\text {max }}^{i} 1$
$\sum_{j=i_{i}} X_{i j}=1 \quad$ for $i=4,5,6$
where $j_{\text {max }}^{i}+1$ denotes a dummy state
(2) parameter value interdependency constraints ${ }^{1}$

$$
\begin{aligned}
& x_{45}-x_{51}=0 \\
& x_{41}-x_{53}-x_{54}-x_{55}=0 \\
& x_{65}+x_{66}-x_{10,1}=0
\end{aligned}
$$

(3) total value requirements

$$
\mathrm{j}_{\max }^{\mathrm{i}}
$$

$$
\sum_{i \in S_{1}}^{\sum} \sum_{j=j_{c}^{i}}^{i} V_{i j} X_{i j}-Y_{1}=S_{a}
$$

$$
\mathrm{j}_{\max }^{\mathrm{i}}
$$

$$
\sum_{i \varepsilon S_{2}}^{\sum_{j=j_{c}^{i}}^{i} \quad V_{i j} X_{i j}-Y_{2}=S_{b}, ~}
$$

$$
\sum_{i \varepsilon S_{3}} \sum_{j=j_{c}^{i}}^{j} V_{\max }^{i} V_{i j} X_{i j}+\sum_{j=13_{c}}^{j=13_{\max }}\left(V_{13, j}\right) / 2-Y_{3}=S_{c}
$$

The dummy variables $X_{45}, X_{55}$ and $X_{66}$ represent dummy states should a row interdependence be in effect.

$$
\sum_{i=1}^{13} \sum_{j=j_{c}^{i}}^{j} V_{i j}^{i} X_{i j}-Y_{4}=R
$$

where

$$
\begin{aligned}
i= & \text { the factor index (row of Table } 4 \text { ), } \\
j= & \text { the state index (column of Table } 4 \text { ), } \\
V_{i j}= & \text { the score associated with the } i^{\text {th }} \text { feature and } \\
& j \text { th state (entry in Table } 4 \text { ), } \\
C_{i j}= & \text { the total retrofit cost of going from the } \\
& j \begin{array}{c}
\text { th state to the } j \text { th state, for the } i^{\text {th }} \text { feature }
\end{array}
\end{aligned}
$$

1 If $j^{i}<j_{c}^{i}$, corresponding to a regression in score, then

$$
C_{i j}=20 \text { times the maximum cost, that is, arbitrarily large. }
$$

If $j^{i}=j_{c}^{i}$ then

$$
\begin{aligned}
C_{i j}= & 0 \text { indicating that it is possible to remain in the current } \\
& \text { state at no cost. }
\end{aligned}
$$

If $j_{\max }^{i} \geq j^{i}>j_{c}^{i}$ and a potential retrofit is possible.

$$
c_{i j}=e_{i}^{!} \cdot c_{i}
$$

where
$e_{i}^{!}=$the transpose of the vector of element counts, and
$c_{i}=$ the vector of element costs
If $j_{\max }^{i} \geq j^{i}>j_{c}^{i}$ and
$j{ }^{i}$ precluded by the user then
$C_{i j}$ is made arbitrarily large.

If $j^{i}>j_{\text {max }}^{i}$, a dummy state due to a row interdependence, then

$$
C_{i j}=0 \quad \text { and } \quad V_{i j}=0
$$

$$
\begin{aligned}
S_{1} & =(1,2,3,4,5,7,8,13), 1 \\
S_{2} & =(1,8,11,12,13), 1 \\
S_{3} & =(2,5,6,7,9,10,12), 1 \\
S_{A}, S_{B}, S_{C} & =\text { mandatory safety requirements from Table } 6, \\
R & =\text { calculated risk factor from Tables } 1,2 \text {, and } 3 \text {, and, } \\
Y_{1}, Y_{2}, Y_{3}, Y_{4} & =\begin{array}{l}
\text { nonnegative surplus variables representing a } \\
\end{array}
\end{aligned}
$$

### 2.3 DESCRIPTION OF COMPUTER ALGORITHM

This section will draw upon the mathematical formulation of the problem presented in the previous section to show how an optimal combination of retrofit options can be selected. The way in which alternative solutions are generated will also be presented. In order to focus on the main concepts, a geometrical, rather than an algebraic, approach will be presented. Algebraic discussions which parallel the geometric illustrations will be presented in footnotes as needed. Those readers interested in a programmer oriented discussion of the computer algorithm are referred to Appendix $B$ of this report.

In order to illustrate graphically how the computerized procedure operates, it will be necessary to use an example in which it is assumed that the level of containment safety is a function of the fire rating in minutes of two techniques, "A" and "B." A graphical solution to the least-cost means of achieving a given level of containment safety is shown in Figure 2.2. In the figure, any movement up along the vertical axis indicates higher fire ratings for technique "A." Similarly any movement out along the horizontal axis indicates higher fire ratings for technique "B." Consequently, if one were to construct a straight line which passed through the origin, any movement outward along that line (i.e., a move in the north easterly direction) would indicate a movement to higher levels of containment safety.

In Part A of Figure 2.2, the lightly shaded region represents all the combinations of fire ratings on techniques "A" and "B" which match or exceed the containment safety requirements of the Life Safety Code. The lightly shaded region in Part A of Figure 2.2 is referred to as the feasible region since all points which lie along its boundary or within are

[^6]
## Part A

LEVEL OF A


LEVEL OF B
Part B

LEVEL OF A


LEVEL OF B
technically feasible. ${ }^{1}$ The boundary is all those combinations of the two techniques which exactly satisfy the containment safety requirements of the Life Safety Code.

In Part $B$ of Figure 2.2 a series of equal cost lines are shown. (Recall that an equal cost line shows all the combinations of technique "A" and technique "B" which cost the same. It is drawn based on the assumption that the unit prices for technique " $A$ " and technique " $B$ " are constant.) Higher equal cost lines imply greater costs are being incurred. By referring to Part $B$ of Figure 2.2, it can be seen that the first equal cost line does not touch the shaded region, implying that not enough funds are being allocated to attain the level of containment safety required by the Life Safety Code. The second equal line curve just touches a vertex of the shaded feasible region. Since no other equal cost line which is lower also touches the feasible region, it can be asserted that the point of contact is the least-cost combination of the two factors generating containment safety. Figure 2.2 also illustrates that if more money were spent it would still be possible to achieve the same level of safety, as shown by the vertex of the feasible region labeled "b". However, from the graph, it can be seen that it would be more cost effective to use those dollars to achieve a higher level

1 Algebraically the feasible region for this case may be expressed as

$$
\sum_{i=1}^{2} \underset{\substack{\mathrm{~L}=j_{c}^{i}}}{j_{\text {max }}^{i}} v_{i j} x_{i j} \geq S_{\text {containment }}
$$

$$
\text { where } \begin{aligned}
& i=1 \text { refers to technique " } A \text { " } \\
& i=2 \text { refers to technique " } B \text { "; and } \\
& X_{i j}=\text { either } 0 \text { or } 1 \text { and } \\
& j_{\max }^{i} \\
& \sum X_{j}^{i} X_{c}^{1}
\end{aligned}
$$

If a nonnegative surplus variable, $Y$, is included, the inequality can be turned into the following equality

$$
\sum_{i=1}^{2} \sum_{j=j_{c}^{i}}^{j_{\text {max }}^{i}} v_{i j} X_{i j}-Y=S_{\text {containment }}
$$

of containment safety than required by the code. Such a strategy would result in a point lying entirely within the feasible region such as "c." 1

One way in which alternative solutions are generated by the computerized procedure is shown graphically in Figure 2.3.

The procedure actually used in the computer program generates two classes of alternative solutions. Only the first class is illustrated in Figure 2.3. The optimal solution derived earlier is denoted by "a" in Figure 2.3.

For example, suppose $X_{i j}$ appears in the optimal solution as a retrofit (i.e., $X_{i j}=1$ ), then the cost, $C_{i j}$, of going from $X_{i j c}$, the preretrofit state, to $X_{i j}$, the postretrofit state is made arbitrarily high. ${ }^{2}$ This step guarantees that $X_{i j}$ can no longer be in the optimal solution. Graphically this would correspond to a rotation of the equal cost line. The new solution would thus be the point at which the lowest of the new class of equal cost curves just touches the feasible region. Such a point is designated a b in Figure 2.3. Exactly analagous is the case where $X_{i j}$ did not appear in the optimal solution (i.e., $X_{i j}=0$ ). In this case, the cost of going from $X_{i j}$ to $X_{i j}, C_{i j}$ is held fixed and all $C_{i k}, k \neq j$,

1 The problem is solved algebraically through the use of the simplex algorithm. As a first step, a simplex tableau is established similar to the one for the simplified problem shown below


The method then proceeds by first identifying a basic feasible solution, some vertex of the feasible region. Such a solution could be the highest state for each of the two techniques. The elements, $\mathrm{X}_{14}$ and $\mathrm{X}_{24}$, of the basic feasible solution are referred to as a basis. The next step is a basis changing process known as pivoting. Each pivot or basis change is the selection of an adjacent vertex. Elements are removed and included to produce another basis as long as the pivoting process results in reductions of the objective function (retrofit costs). The resulting solution is the minimum value of the objective function.

2 An arbitrarily high retrofit cost is defined as one which is 20 times the highest individual retrofit cost.

FIGURE 2.3 ALTERNATIVE SOLUTION: GRAPHICAL METHOD


are made arbitrarily high. This step guarantees that $X_{i j}$ will appear in the optimal solution as a retrofit. The number of solutlons generated in this class is equal to the number of variables in the original linear programming problem minus the number of retrofit states which cannot be attained (those within a row having a lesser value than the input and those precluded by an arbitrarily high cost). In the simple case illustrated graphically, up to six alternative solutions could be generated. The second class of alternatives is determined by the rows of Table 4. For example, suppose $X_{i j}$ appears in the optimal solution as a retrofit, then the cost of going from $X_{i j}$ to $X_{i j}$ for all $j^{\prime}, j_{c}<j^{\prime} \leq j_{\max }$ where $j_{\text {max }}$ is the maximal state in the $i^{\text {th }}$ row is made arbitrarily high. This step guarantees that no potential retrofits associated with that factor, say automatic sprinkler systems, can appear in the optimal solution. The number of solutions generated is equal to the number of factors (rows in Table 4) which moved to a higher state (were retrofitted) in the optimal solution.

The two classes of alternative solutions described above are very interesting because they are "close" to the optimal solution. "Close" is put within quotation marks because through reference to Figure 2.3 it can be seen that the alternative solutions are adjacent vertices of the boundary of the feasible region. ${ }^{1}$ Thus "close" means a small change in the basis rather than a small change in the objective function. Although these solutions will be more costly than the optimal solution, some of them will be extremely close (in dollar terms) to the least-cost combination of retrofits.

All of the discussion has proceeded as if the continuous solution to the optimization were actually the integer solution. In general, this is not true; however, there are several strong arguments for the approach used. The first is the "near integer" property of the solutions; the second, the judicious selection of the family of alternate solutions; and the third, the computational cost, efficiency, and reliability of the algorithm. Each of these is discussed in turn.

The near integer property occurs because of the structure of the constraint matrix. Ignoring, for the moment, the contrived constraints ${ }^{2}$ a solution will have exactly 17 variables. The 13 equations corresponding to the Building Safety Features in Table 4 have no variables in common and each has a right hand side of 1 . Therefore, there are 13 mutually

[^7]exclusive subsets of the 17 variables which must sum to 1 . Since it requires at least two fractions to sum to 1 , there must be at least nine variables which are exactly one. Nine or more integers among the 13 variables of interest is defined as near integer. Nine integers is the worst case; some of the variables may be zero and/or some of the surplus variables (the Y's in Section 2.2) may be non-zero. Should either condition occur, there are fewer than 17 variables to be included in the 13 subsets and more than ten of the variables may be integer.

Regardless of the integer characteristics of the optimal solution, it represents a lower bound on the total retrofit cost. It is obvious that the introduction of an additional constraint cannot improve the cost. In production work, although not in the development work to date, a heuristic integerization procedure would be applied to each solution generated. This would produce an integer solution by making a minimal change in the basic continuous solution.

One of the criteria used in the design of the alternate solution family was that any variable appearing as a fraction in the optimal solution must appear in at least one of the alternates as one and be suppressed in at least one of the alternates. Other criteria were that the alternates should be amenable to generation via a systematic but comprehensive specification, that they meet (at least our conception of) user needs, and that the number of alternates be adequate but not burdensome.

Thus the solutions presented, while not guaranteed to include the optimum integer solution, do contain:
(1) a bounding value on the retrofit cost;
(2) costs corresponding to the alternates most likely to be considered by the user; and
(3) one or more costs close to the integer optimum.

To solve the optimization problem as an integer model is actually possible. The reasons for selecting a continuous model are completely pragmatic. Computation time for an integer solution can be expected to be an order of magnitude higher. Off-the-shelf software existed for the continuous but not for the integer solution; this is quite important since its impact is not merely on development costs but on reliability and system maintenance costs while operating in the production mode. For production, some satellite software (again off-the-shelf, proven, and reliable) is available which can reduce the costs of alternate solutions by about a factor of three. No analogous method is known for the integer problem.

### 2.4 APPLYING THE COMPUTERIZED PROCEDURE

Thus far the focus has been on how the computerized procedure operates. The purpose of this section is to build on that base and illustrate how the procedure can be applied in an actual case. Two subsections have been prepared to achieve this objective. The first subsection is con-
cerned with the input portions of the computer program (data requirements and user options). The second subsection is concerned with the output of the computer program. For those readers wishing a more detailed treatment of the computerized procedure, including formatting, documentation and sample computer runs, two technical appendices have also been. prepared.

### 2.4.1 Data Requirements and User Options

Before the computerized procedure can be exercised, all potential retrofits must first be identified. Once this information is available, it is possible to identify and count the elements which require treatment in order to move to a higher state. These data requirements are listed in Table 2.2. Table 2.1 defines the abbreviations for the elements which appear in Table 2.2. Under the assumption that all elements have been counted, it becomes possible to examine the computer input in detail. A sample computer run will be used in order to illustrate the input data requirements.

The first three lines of input specify (1) the initial state of the fire zone, (2) the occupancy risk factor, and (3) information on the building and zone location. All information required for the first line of the input may be taken directly from Table 4 of the Fire Zone Safety Evaluation Worksheet. In particular, each Building Safety Feature has its parameters numbered from 1 to $n$, where $n$ could be 3,4 or 5 , depending on the feature. ${ }^{1}$ The number corresponding to the existing state of each feature is then identified for use as an input. All information required for the second line of input may be taken directly from Table lof the Fire Zone : Safety Evaluation Worksheet. As in the previous case, each parameter is numbered from 1 to $m$, where $m$ could be 2,4 or 5 . The number corresponding to the existing state is then identified for use as an input. The first three lines of the sample input are shown below as Exhibit 2.1.

Exhibit 2.1 Initial Inputs

Line

## Sample Input

$3,1,1,2,1,2,3,1,1,3,2,1,1$
$3,4,2,3,1$
$1,2,3,3,32$
${ }^{1}$ Recall that "Row 1 " of Table 4 is actually a 4 (Floor of Zone) by 3 (Combustible-Wood Frame, Combustible-Ordinary, Noncombustible) by 3 Unprotected, Protected, Fire Resistant) array. Consequently, "Row l" as used here refers to the vector whose elements correspond to the Unprotected, Protected, Fire Resistant and Combustible-Vood Frame, Combustible-Ordinary, Noncombustible condition specified in line 3 of the input.

Table 2.1 Abbreviation for Elements and Units to be Used in Reporting Data on Potential Retrofits


Table 2.2 Listing of Data Requirements

Parameters Values
Combustible
Noncombustible
1．CONSTRUCTION
Wood Frame Ordinary

FLOOR
Protected Protected Protected Fire Resist
$F t^{2}(C) \quad F t^{2}(C) \quad F t^{2}(C) \quad F t^{2}(C)$
Class B Class A
2．INTERIOR FINISH
［Corr．\＆Exit］
$F t^{2}(F), F t^{2}(W) \quad F t^{2}(F), F t^{2}(W)$

3．INTERIOR FINISH
Class B Class A
［Rooms］

$$
F t^{2}(F), F t^{2}(W) \quad F t^{2}(F), F t^{2}(W)
$$

| $<1 / 3 \mathrm{Hr}$ | $1 / 3-1.0 \mathrm{Hr}$ | $>1.0 \mathrm{Hr}$ |
| :---: | :---: | :---: |
| $\mathrm{Ft}^{2}(\mathrm{~W}), 0$ | $\mathrm{Ft}^{2}(\mathrm{~W}), 0$ | $\mathrm{Ft}^{2}(\mathrm{~W}), 0$ |
| $<20 \mathrm{~min} \mathrm{FR}$ | $>20 \mathrm{~min} \mathrm{FR}$ | $>20 \mathrm{~min} \mathrm{FR}$ |
| $\mathrm{D}, \mathrm{D}+\mathrm{F}, 0$ | $\mathrm{D}, \mathrm{D}+\mathrm{F}, 0$ | $\mathrm{D}, \mathrm{D}+\mathrm{F}, \mathrm{O}, \mathrm{C}$ |

4．CORRIDOR PARTITION WALLS


| 7．VERTICAL | Enclosed with Indicated Fire Resist |  |  |  |
| :--- | :---: | :---: | :---: | :---: |
| OPENINGS | $\geq 1 \mathrm{HR}<2 \mathrm{HR}$ | 2 HR |  |  |
|  | $\mathrm{Ft}^{2}(\mathrm{~W}), \mathrm{FD}, \mathrm{FD}+\mathrm{F}$ | $\mathrm{Ft}^{2}(\mathrm{~W}), \mathrm{FD}, \mathrm{FD}+\mathrm{F}$ | $\mathrm{Ft}^{2}(\mathrm{~W}), \mathrm{FD}, \mathrm{FD}+\mathrm{F}$ |  |

8．HAZARDOUS
AREAS

| Single Deficiency | No Deficiencies |
| :---: | :---: |
| $F t^{2}(F), F T^{2}(W), F D, F D+F$ | $\mathrm{Ft}^{2}(F), \mathrm{Ft}^{2}(W), F D, F D+F$ |

9．SMOKE
Smoke Partition
CONTROL

$$
\mathrm{Ft}^{2}(\mathrm{~W}), \mathrm{CPF}+\mathrm{D}
$$

Mechanically Assisted Systems
Fire Zone Corridor

Multiple Routes
10．EMERGENCY MOVEMENT
ROUTES

$$
F t^{2}(W), F t(P), C P F+D
$$

| $\frac{\text { Manual Fire Alarm }}{}$ |  |
| :---: | :---: |
| w／o F．D．Conn | w／F．D．Conn |
| $\# ⿰ ⿰ 三 丨 ⿰ 丨 三$ |  |

Corridor Only Rooms Only Corridor \＆Habit．Space Total Space
12．AUTOMATIC
DETECTION \＆
ALARM

13．SPRINKLERS

| Corridor | Corridor \＆Habit．Space | Total Space |
| :--- | :--- | :--- |
| $\mathrm{Ft}^{2}(\mathrm{~F})$ | $\mathrm{Ft}^{2}(\mathrm{~F})$ | $\mathrm{Ft}^{2}(\mathrm{~F})$ |

The first line of input, shown in Exhibit 2.1, gives the following information: the first feature, Construction, is in the third state; the second and third features, Interior Finishes, are in the first state; the fourth feature, Corridor Partition Walls, is in the second state; the fifth feature, Doors to the Corridor, is in the first state; the sixth feature, Zone Dimensions, is in the second state; the seventh feature, Vertical Openings, is in the third state; the eighth and ninth features, Hazardous Areas and Smoke Control, are in the first state; the tenth feature, Emergency Movement Routes, is in the third state; the eleventh feature, Manual Fire Alarm, is in the second state; and the twelfth and thireenth features, Automatic Smoke Detection and Alarm and Sprinklers, are in the first state.

The second line of input shows the following information on occupancy risk: Patient Mobility is in the third state (not mobile); Patient Density is in the fourth state ( $>30$ ); Zone Location is in the second state (2nd or 3 rd floor) ; Ratio of Patients to Attendants is in the third state (6-10); and Patient Average Age is in the first state. ${ }^{2}$

The third line of input shows the following information: the problem number is 1 ; the building age is 2 (existing); the construction code is 3 (noncombustible); the fire zone is located on the third floor; and the number of patients is 32. The first entry, problem number, may be used in case the floor has more than one zone or if the user wished to change slightly the formulation of the problem to see how the optimal combination of retrofits might change. The latter could be accomplished through the use of one of the three user options.

The second entry gives the building age, $1=$ New, $2=$ Existing. The third entry gives the construction type, $1=$ Wood Frame, $2=$ Ordinary, 3 = Noncombustible. The fourth entry, floor of zone, is self-explanatory. The last entry, number of patients, is included because the charge for no smoke control changes if more than 30 patients are in the zone.

1 The admissible states for each factor are: (1) Construction, 1-3; (2) Interior Finish (Corridor and Exit), 1-3; (3) Interior Finish (Rooms), 1-3; (4) Corridor Partition Walls, 1-4; (5) Doors to the Corridor, $1-4 ;(6)$ Zone Dimensions, $1-5 ;(7)$ Vertical Openings, 1-5; (8).Hazardous Areas, 1-5; (9) Smoke Control, 1-4; (10) Emergency Movement Routes, 1-5; (11) Manual Fire Alarm, 1-4; (12) Automatic Detection and Alarm, 1-5; (13) Sprinklers, 1-4.

2
The admissible states for each (occupancy risk) factor are:
(1) Patient Mobility, 1-4; (2) Patient Density, 1-4; (3) Zone Location, 1-5; (4) Ratio of Patients to Attendants, 1-5;
(5) Patient Average Age, 1-2.

Lines 4 through 16 of the computer input are patterned after the information contained in Table 4 of the Worksheet. They identify the number of elements which must be treated to move to a higher state. The entries use the format established in Table 2.1. A sample input is shown in Exhibit 2.2. In order to explain the input in some detail, a line-by-line description of Exhibit 2.2 will be given.

Note carefully that the only information which must be input on lines 4 through 16 is the factor ID and the element counts to go to a higher state for that factor. When inputting the factor ID and element count information each factor is input on a separate card. (For the eighth factor, Hazardous Areas, two cards, both numbered 8, may be used.) Consequently either 13 or 14 cards are required to input all of the necessary information on the potential retrofits. Thus, if the factor is already in the highest state, the only information required on that card is the factor ID number. It is important to point out that the first line of input (i.e., the first card) contains the current state for each factor. Since the current state dictates the set of potential retrofits for each factor, care must be exercised to ensure that the information recorded on cards 4 through 16 is consistent with the information on the first card.

Exhibit 2.2 Sample Input Information on Potential Retrofits

Line

Construction
Factor

Factor ID

Element Counts

$$
\begin{aligned}
& 2000,0,2000,0 \\
& 250,1200,250,1200 \\
& 0,3,-1,-1 \\
& 0,0,34,0,34,0,0,0 \text {, } \\
& 34,0,0,34 \\
& -1,1,-1 \\
& 0,0,3,0,0,3 \\
& -1,-1,-1,-1,350,0,0,0, \\
& --1,-1,-1,-1,700,0,0,7 \\
& 0,1,-1,-1,-1,-1,-1 \\
& 0,8,1,-1,-1,-1 \\
& 1 \\
& 2000,6000,8000,8700 \\
& 2000,8000,8700
\end{aligned}
$$

[^8]
## Line 4: Construction; Building Safety Feature ID: 1

The first column of the fourth card contains the single entry 1 indicating that this is the first feature (Construction). The only element count entry for this feature is a blank space indicating that this feature is already in the highest state and can stay there at zero cost.

Line 5: Interior Finish (Corridor and Exit); Building Safety Feature ID:
The first and second element count entries show that to move to the next highest state, Class $B, 2000$ square feet of floor area and 0 square feet of wall area must be treated. The third and fourth element count entries show that to move to the highest state, Class A, 2000 square feet of floor area and 0 square feet of wall area must be treated.

Line 6: Interior Finish (Rooms); Building Safety Feature ID: 3
The first and second element count entries show that to move to the next highest state, Class B, 250 square feet of floor area and 1200 square feet of wall area must be treated. The third and fourth element count entries show that to move to the highest state, Class $A, 250$ square feet of floor area and 1200 square feet of wall area must be treated.

## Line 7: Corridor Partition Walls; Building Safety Feature ID: 4

The first and second element count entries show that 0 square feet of corridor partition wall must be installed and 3 openings in the corridor partition walls require treatment to upgrade to a $1 / 3$ to 1 hour fire rating (the third state in Table 4 of the Worksheet). The third and fourth element count entries indicate that going to a fire rating of more than 1 hour is impossible (the highest state in Table 4 of the Worksheet).

## Line 8: Doors to Corridor; Building Safety Feature ID: 5

The first, second, third and fourth element count entries indicate that going from the "No Door" charge to a fire rating of less than 20 minutes would require the replacement of no doors and no complete door and frame systems, but would require that the openings (e.g., ordinary glass lites) in 34 doors be treated. The fourth element count is a place holder for automatic closers used only in the highest retrofit state. The fifth, sixth, seventh and eighth element count entries show that to go to a fire rating of more than 20 minutes would require 34 doors to be replaced, no complete door and frame systems to be replaced and no opening to be

1 In every case, for cards 4 through 16 the first entry will be the factor ID.
treated. ${ }^{1}$ Again a 0 is entered for the eighth element count since it is used as a place holder only. The ninth, tenth, eleventh and twelfth element count entries show that to go to a fire rating of more than 20 minutes with automatic closers would require 34 doors to be replaced, no complete door and frame systems to be replaced, no openings to be treated and 34 closers to be installed.

Line 9: Zone Dimensions; Building Safety Feature ID: 6
The first element count entry indicates that going to a situation with no dead ends greater than 30 feet and a corridor length greater than 150 feet is an impossible retrofit. The second element count entry indicates a potential retrofit, the installation of a stairwell to remove the dead end (the corridor length remains the same). The third element count entry indicates an impossible retrofit (no dead ends greater than 30 feet and a corridor length of less than 100 feet).

Line 10: Vertical Openings; Building Safety Feature ID: 7
The first, second and third element count entries show that 0 square feet of fire proofing, no fire doors, and 3 complete fire door and frame systems (Class B) are required to upgrade to a fire rating of between 1 and 2 hours. The fourth, fifth and sixth element count entries show that 0 square feet of fire proofing, no fire doors, and 3 complete fire door and frame systems (Class A) are required to upgrade to a fire rating of more than 2 hours.

Line 11: Hazardous Areas; Building Safety Feature ID: 8
The first, second, third and fourth element count entries indicate an impossible retrofit. ${ }^{2}$ The fifth, sixth, seventh and eighth element count

1 Note that an entry for doors and frames is included. In this case all doors can be fitted onto the existing frames. If the present frames were incompatible with the replacement doors then the first eight element count entries would be: $0,0,34,0,0,34,0,0$.

If 20 doors could be installed on existing frames, but the remaining 14 would require new frames, then the first eight element count entries would be: $0,0,34,0,20,14,0,0$.

2 It is important to point out that, unless some a priori retrofit scenario is hypothesized which makes explicit the cost dependence among hazardous areas in other fire zones, the costs of treating deficiencies in other fire zones will be assumed to be independent of the costs of treating deficiencies within the fire zone. Consequently no explicit cost charge for the treatment of hazardous areas in other fire zones is entered into the computer program. This approach implies that hazardous area retrofits in other fire zones are treated as impossible retrofits for the fire zone under consideration.
entries indicate that to move to a single deficiency 350 square feet of floor area must be sprinklered, 0 square feet of wall area must be fire proofed, no fire doors are required, and no complete fire door and frame systems are required. The ninth, tenth, eleventh and twelfth element count entries show that to remove all deficiencies in hazardous areas 700 square feet of floor area must be sprinklered, 0 square feet of wall area must be fire proofed, no fire doors are required, and 7 complete fire door and frame systems are required.

## Line 12: Smoke Control; Building Safety Feature ID: 9

The first and second element count entries indicate that to install a smoke partition requires 0 square feet of wall area to be fire proofed and 1 ( 8 foot wide) section of corridor partitioning with fire doors to be installed. The third, fourth, fifth and sixth element count entries indicate that both mechanically assisted system retrofits are impossible.

Line 13: Emergency Movement Routes; Building Safety Feature ID: 10
The first, second and third element count entries indicate that the installation of a horizontal exit requires 0 square feet of wall to be fire proofed, 8 linear feet of corridor paritition to be extended to the structural slab, and 1 ( 8 foot wide) section of corridor partitioning with fire doors to be installed. The fourth, fifth and sixth element count entries indicate that the installation of direct exits is an impossible retrofit.

## Line 14: Manual Fire Alarms; Building Safety Feature ID: 11

The single element count entry indicates that to move to the highest state requires the installation of a fire department connection.

Line 15: Automatic Detection and Alarm; Building Safety Feature ID: 12
Protection of corridors, the first element count entry, requires 2000 square feet of floor area to be treated. Protection of rooms, the second element count entry, requires 6000 square feet of floor area to be treated. Protection of corridor and habitable spaces, the third element count entry, requires 8000 square feet of floor area to be treated. Total protection, the fourth element count entry, requires 8700 square feet of floor area to be treated.

Line 16: Sprinklers; Building Safety Feature ID: 13
The first element count entry, sprinklering the corridor, requires 2000 square feet of floor area to be sprinklered. The second element count entry, sprinklering the corridor and habitable spaces, requires 8000 square feet of floor area to be sprinklered. The third element count entry, total sprinklering, requires 8700 square feet of floor area to be sprinklered.

The options available to the user to control or modify the data input begin with line 17. The admissible control/modification statements are defined in Table 2.3. Each statement will now be examined.

Table 2.3 User Options: Control and Modification Statements

| Control Statement | Function |
| :---: | :---: |
| SOLVE | Indicates that no further modifications to the fire zone are desired and to begin calculation of the family of solutions. |
| NEXT | Read in "lines" 1 through 16 for the next fire zone (see Exhibits 2.1 and 2.2). |
| END | Terminates run; no more fire zones to be analyzed. |
| Modification Statement | Function |
| CHANGE $\alpha, \beta, \gamma$ | ```\alpha = Building Safety Feature ID number \beta=State number \gamma= Option code The costs associated with feature \alpha, state \beta are modified \gamma}<0-> EXCLUDE r=0-> INCLUDE \gamma>0}0+\operatorname{COST``` |
| REQUIR $\delta, \varepsilon$ | The value of mandatory safety requirement $\delta$ is increased by $\varepsilon$ percent. $\delta=1 \text { for } S_{a}$ <br> $\delta=2$ for $S_{b}$ <br> $\delta=3$ for $S_{c}$ <br> $\delta=4$ for $R^{c}$ |

In order to provide the user with the maximum flexibility, it was necessary to require the user to exercise control over the program. Thus all of the Control/Modification cards (C/M cards) are of the same format. The user is required to supply a SOLVE card for every fire zone (or varition thereof) for which a solution is desired. The user is also required to supply a NEXT card when all of the required variants for a particular fire zone have been solved and solutions for another fire zone are desired. The END card terminates the run.

CHANGE and REQUIR cards are user options only. There is no requirement that they appear in the run sequence. If used, they must appear (in any order or combination) prior to an END card. That is to say SOLVE's and NEXT's may be legitimately interspersed throughout the run sequence, It is important to point out that the CHANGE and REQUIR cards are defined in such a way that their effect on the run sequence is cumulative. Thus the order in which the options appear controls the definition of the fire zone.problem solved. Consequently, the user is encouraged to use the SOLVE card as the first $C / M$ card in the run sequence. This will guarantee a solution to the original problem.

A sample C/M card sequence is given in Exhibit 2.3 as an illustration. As a means of reinforcing the functions of the $C / M$ cards defined earlier, a line-by-line description of the solution generated by the C/M card sequence given in Exhibit 2.3 will be presented.

Exhibit 2.3 Sample Control/Modification Card Sequence

| Control/Modification Card or Descriptor | Control/Modification Card Number | Probable Run Sequence Card Number |
| :---: | :---: | :---: |
| INPUT ON FIRST FIRE ZONE | - | 1-16 |
| SOLVE | 1 | 17 |
| CHANGE $\begin{array}{llll}1 & 3 & -1\end{array}$ | 2 | 18 |
| CHANGE 4020 | 3 | 19 |
| REQUIR 110 | 4 | 20 |
| CHANGE 6217500 | 5 | 21 |
| SOLVE | 6 | 22 |
| CHANGE 9 3 -1 | 7 | 23 |
| SOLVE | 8 | 24 |
| REQUIR 110 | 9 | 25 |
| NEXT | 10 | 26 |
| INPUT ON SECOND FIRE ZONE | - | 27-42 |
| CHANGE $31 \cdot-1$ | 11 | 43 |
| SOLVE | 12 | 44 |
| SOLVE | 13 | 45 |
| END | 14 | 46 |

This card causes the problem defined by run sequence card numbers 1 through 16 to be solved. The solution includes: (1) the least-cost means of achieving compliance to the Life Safety Code; (2) the cost of strict compliance to the Life Safety Code; and (3) a set of alternative means of achieving compliance to the Life Safety Code.

C/M Card 2: CHANGE 1 3 -1
This card causes state 3 of the first feature (Construction) to be precluded in the solution. Specifically, it implies that $\mathrm{C}_{13}$ (the cost of feature 1 , state 3 ) is made arbitrarily large.

C/M Card 3: CHANGE 420
This card causes state 2 of the fourth feature (Corridor Partition Walls) to be included in the retrofit package. This is accomplished by making $\mathrm{C}_{41}, \mathrm{C}_{43}$ and $\mathrm{C}_{44}$ arbitrarily large. Thus the second state is forced into the section.

C/M Card 4: REQUIR 110
This card causes the minimum passing score associated with the first safety redundancy requirement, $S_{a}$ (Containment), to be increased by 10 percent. This option is useful in those cases where the decision maker wishes to purchase extra units of safety in a particular category. For example, due to the configuration of the fire zone or for some other a priori reason, the decision maker wishes to purchase higher levels of Containment Safety than provided by the Life Safety Code. The linear programming package ensures that this is done in the most least-costly manner.

C/M Card 5: CHANGE 6217500
This card changes the cost of upgrading from the existing state (specified on run sequence card 3) to state 2 of the sixth feature (Zone Dimensions) to $\$ 17,500$.

C/M Card 6: SOLVE
This card causes the problem defined by run sequence card numbers 1 through 21 to be solved (see Exhibit 2.3).

C/M Card 7: CHANGE 9 3 -1
This card causes state 3 of the ninth feature (Smoke Control) to be precluded.

This card causes the problem defined by run sequence card numbers 1 through 21 and modified by run sequence card number 23 to be solved.

C/M Card 9: REQUIR 110
This card causes the minimum passing score associated with the first safety redundancy requirement, $S_{a}$ (Containment), to be increased by 10 percent. Since this $C / M$ card was already used (C/M Card 4) any solution would exceed the Containment Safety requirement by 21 percent. Note, however, that no SOLVE C/M card follows so that no solutions will be generated.

## C/M Card 10: NEXT

This card clears all options from the program and initiates the reading in of input for the next fire zone.

## C/M Card 11: CHANGE 3 1 -1

This card causes state 1 of the third feature (Interior Finish: Rooms) to be precluded.

C/M Card 12: SOLVE
This card causes the problem defined by run sequence card numbers 27 through 42 and modified by run sequence card number 43 to be solved. Note that the original problem was not solved since state 1 of feature 3 was precluded by $C / M$ card 11 .

## C/M Card 13: SOLVE

This card generates the same output as $C / M$ card 12. It illustrates the fact that care must be exercised by the user since legitimate commands if combined in the wrong way may generate meaningless output. Note that if the first SOLVE card had preceded the CHANGE 3 l -l card, $C / M$ card 13 's output would differ from the output generated by the first SOLVE card.

C/M Card 14: END
This card causes the run sequence to terminate.

It is important to reiterate that modifications are cumulative between fire zone "reads" (NEXT statements). Any number of fire zones is permissible. That is, there is no a priori limit on the number of NEXT cards. (Computer system limits such as page counts or CPU time, however, will limit the number of problems which can be solved.) Furthermore, there is no limit on the number of modifications to a fire zone as long
as the problem remains feasible. If a particular modification is not feasible, nothing catastrophic occurs; some computer time, but not a great deal, is used. As pointed out in the sample run sequence, the problem defined by the fire zone input (run sequence lines 1 through 16 and 27 through 42 in Exhibit 2.3) does not have to be solved. Unless the user has a good reason, the basic problem should be solved prior to any modification of the data input.

The set of solutions for a modified problem is the same as that for an unmodified problem except that those states which have been "forced in" (CHANGE $i$ j 0 ; denoted as an " $F$ " type change on the computer output) are not allowed to leave the basis.

### 2.4.2 The Output Format and Its Interpretation

The output format for each problem solved begins with a printback of Table 1 and Table 4. This printback is intended as a check so that the user can verify that the problem actually solved corresponds to the one intended. After the printback, information on the least cost and prescriptive solutions is given. This information identifies each of the 1.3 factors, the state number, the retrofit cost, the score, and one or more solution ID's. Five solution ID's are possible:
(1) S indicating that the state is in the optimal solution;
(2) I indicating that the state is the one input;
(3) $P$ indicating that the state is in the prescriptive solution;
(4) F indicating that the user modification which forces a state into the solution has been performed; and
(5) C indicating that a cost change modification has been performed.

The information shown in Exhibits 2.1 and 2.2 and $C / M$ card 1 in Exhibit 2.3 will generate the output given in Exhibit 2.4. ${ }^{1}$ Notice that under feature 9 , smoke control, an entry is marked by an asterisk. This is to indicate that the installation of a horizontal exit under feature 10 allows a smoke partition to be claimed at no cost under feature $9 .{ }^{2}$
${ }^{1}$ As was mentioned earlier, the continuous solution to the optimization problem may contain noninteger variables. However, given the "near integer" property of the solutions, this problem is easily handled. Consequently, the output shown in Exhibit 2.4 is not the output as it comes from the computer directly. It represents the result of a postoptimization integerization procedure which is presently done manually. As indicated in Section 2.3, in production work the user will receive an output like that presented in Exhibit 2.4.

2 The logic required to treat this interdependency is currently not in the computer program. Should a horizontal exit be installed, however, in the least-cost retrofit package, the user can claim two additional points in People Movement Safety and General Safety.

Exhibịt 2.4 Sample Output Format for Optimal and Prescriptive Solutions

|  | FACTOR | TABLE 4 | $\operatorname{cost}$ | SCORE |  | TOTAL COST 20400 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1. | CONSTRUCTION | 3 | 0 | 4 | SIP | SA $=13$ SURPLUS $=5$ |
|  |  |  |  |  |  | SA $=5$ SURPLUS $=0$ |
| 2. | INTERIOR FINISH | 1 | 0 | -5 | I | $S C=5$ SURPLUS $=2$ |
|  | CORRIDOR \& EXIT | 2 | 800 | 0 | P | $S G=13$ SURPLUS $=6$ |
|  |  | 3 | 800 | 3 | S |  |
| 3. | INTERIOR FINISH | 1 | 0 | -3 | I | PRESCRIPTIVE 38000 |
|  | ROOMS | 2 | 600 | 1 | P |  |
|  |  | 3 | 600 | 3 | S | SA $=8 . \quad$ SURPLUS $=0$ |
|  |  |  |  |  |  | $S B=5$ SURPLUS $=0$ |
| 4. | CORRIDOR PARTITION WALLS | 2 | 0 | 0 | SIP | SC $=3$ SURPLUS $=0$ |
|  |  |  |  |  |  | $S G=9 \quad$ SURPLUS $=2$ |
| 5. | DOORS TO CORRIDOR | 1 | 0 | -10 | I |  |
|  |  | 2 | 3000 | 0 | S |  |
|  |  | 3 | 9000 | 1 | P |  |
| 6. | ZONE DIMENSIONS | 2 | 0 | -4 | SI |  |
|  |  | 4 | 15000 | 0 | P |  |
| 7. | VERTICAL OPENINGS | 3 | 0 | 0 | I |  |
|  |  | 4 | 3750 | 2 | P |  |
|  |  | 5 | 3900 | 3 | S |  |
| 8. | HAZARDOUS AREAS | 1 | 0 | -11 | I |  |
|  |  | 5 | 7450 | 0 | SP |  |
| 9. | SMOKE CONTROL | 1 | 0 | -2 | I |  |
|  |  | 2 | 1400 | 0 | P |  |
|  |  | 2* | 0 | 0 | S |  |
| 10. | EMERGENCY MOVEMENT | 3 | 0 | 0 | IP |  |
|  | ROUTES | 4 | 4650 | 3 | S |  |
| 11. | MANUAL FIRE ALARM | 2 | 0 | 1 | SIP |  |
| 12. | SMOKE DETECTION | 1 | 0 | 0 | SIP |  |
|  | AND ALARM |  |  |  |  |  |
| 13. | SPRINKLERS | 1 | 0 | 0 | SIP |  |

The output format is designed to parallel Table 4 of the Worksheet. All entries marked with a correspond to the initial state of that feature. These entries are marked with an I in Exhibit 2.4. All entries marked with an $s$ and a number other than 0 , except for the smoke partition marked as $0 *$, are the retrofits included in the optimal solution. All entries marked with a $p$ and a number other than 0 are the retrofits included in the prescriptive solution. Counting from left to right in Table 4 (Exhibit 1.2) gives the state number in each case. This number is entered under the column labeled TABLE 4 in Exhibit 2.4. The cost figures associated with each possibility ( $I=0$ and $S, P \geq 0$ ) are then recorded in the column labeled COST in Exhibit 2.4. The cost figure which appears beside the state number is the total retrofit cost. It is based on the information stored in the element count and element cost matrices. The figure entered under the column SCORE in Exhibit 2.4 is taken directly from Table 4 of the Worksheet (see Exhibit 1.2). Note also that in the upper right hand corner of the output is printed out a cost summary statement. In this case the cost of equivalence is $\$ 20400$ whereas the cost of strict compliance is $\$ 38000$. The use of the equivalency methodology thus results in a cost reduction of almost 50 percent for this fire zone. Immediately below the cost summary are the scores for each of the four safety categories. Surplus scores are given to the right of each category.

The output format and its interpretation for each of the alternative solutions is exactly the same. The parameter or factor being forced into or out of the solution set is marked with an asterisk, *, to the left of the solution ID's (S, I, P, F, or C).

For modified fire zones (those for which at least one CHANGE or REQUIR modification has been performed) the solution ID will contain a $C$ (in addition to $S, I, P$ and $*$ ) if the cost has been changed by the user to reflect local market conditions (i.e., a better cost estimate) or the option has been forced out (i.e., $\gamma<0$ in Table 2.3) by an arbitrarily high cost. If the state has been forced in (i.e., $\gamma=0$ in Table 2.3) an $F$ will appear in the printout. The alternative solutions, whether for "input" or modified fire zones, are the same as the original solutions except that a $P$ no longer appears in the solution ID and the sub tableau, labeled PRESCRIPTIVE in Exhibit 2.4, which shows the prescriptive cost and requirement surpluses (if any) will not appear.

## 3. SUMMARY

The identification of cost-effective levels of fire safety in health care facilities is a major concern to hospital administrators, fire safety engineers and public policy makers. Rising construction and operating costs coupled with more stringent building codes and continuing advances in medical and building technology have complicated the issue, forcing health care facility administrators to carefully assess the alternative means through which they can design, construct or update their facilities. The Life Safety Code developed by the National Fire Protection Association (NFPA) is currently the most widely used guide for identifying the minimum level of fire safety in health care facilities. Although the

Life Safety Code may be thought of as a prescriptive code since it prescribes fixed solutions for life safety, performance concepts can be explicitly introduced through a provision which allows for equivalent solutions. In light of this provision, the National Bureau of Standards' Center for Fire Research through support from the Department of Health, Education and Welfare has developed a system, the Fire Safety Evaluation System, for determining how combinations of several widely accepted fire safety systems could be used to provide a level of safety equivalent to that required in the 1973 Life Safety Code.

This report has provided a programmer-oriented description of the mathematical, economic, and engineering considerations that went into the development of a computerized version of the Fire Safety Evaluation System which permits the least cost means of achieving compliance to the Life Safety Code to be identified. It was shown that each of the parameters used in the Fire Safety Evalution System had a unique value which corresponded to strict compliance to the Life Safety Code. Consequently, it was possible to quantify the cost savings attributable to a performance-based Fire Safety Evaluation System approach over that of strict compliance.

In the discussion of data requirements, it was also shown that the computer program uses as its primary input information collected as an integral part of a thorough fire safety evaluation. This information permits the current state of the health care facility to be unambiguously identified. Based on (1) the current state of the health care facility, (2) the minimum passing "score" needed to achieve compliance, and (3) the anticipated costs of each retrofit measure, the least cost or optimal combination of retrofits is identified. The computer program then analyzes other retrofit combinations to see if alternatives might exist which are close to the one identified as optimal. The optimal combination of retrofits and any alternative which the program produces, usually between 10 and 20, are then summarized in tabular form and ranked from least costly to most costly. By using this approach, health care facility decision makers have greater flexibility in choosing among retrofit combinations. In particular, by providing alternatives, the decision maker has the opportunity to assess the impact that non-construction costs would have on the choice of the optimal retrofit combination.

## APPENDIX A

## Unit Pricing Information

The unit pricing information presented in this section is based on anticipated costs in the Washington, D.C. area for the last Quarter of 1978. These figures are used as a resident element cost matrix for the computerized procedure discussed earlier in the report. They can be used to identify the least cost combination of the retrofits for a single zone as well as the costs of strict compliance and any alternative retrofit strategies. It is important to point out that the unit prices presented in this section are adequate only for the purpose of budget planning prior to the request for construction design. The actual cost estimates for a particular retrofit strategy will have to be made following the completion of the retrofit specification, design and material selection, and the establishment of the retrofit date. Most of the unit pricing information presented in this section was either obtained from the Central Office of the Veteran's Administration or the Building Construction Cost Data 1978 booklet published by the Robert Snow Means Company, Inc. The unit prices are IN-PLACE PRICES which include: demolition, waste removal, building materials, labor, installation and finishing, refinishing of adjacent areas and a markup for contractor overhead and profit. Similar unit pricing information can also be developed by local estimators for various retrofit strategies at specific locations. This information can be used to redefine the element cost matrix. The unit pricing information used in the computer program is given as follows:

Coat with Fire-Retardant Paint
Fireproof with Intumescent Mastic
$1 / 8^{\prime \prime}$ thick, $3 / 4$ hour $\$ 1.30 \mathrm{PSF}$

3/16" thick, 1 hour
7/16" thick; 2 hour
Fireproof Existing Wood Panel
Replace Carpeting
Install Drywall Including Painting
1/2" thick
5/8" thick
Replace Door to Achieve 20 Minute or More Fire Resistance

| $4^{\prime} \times 7^{\prime}$ door and hardware | $\$ 300$ each |
| :--- | :--- |
| $4^{\prime} \times 7^{\prime}$ door, frame and hardware | $\$ 700$ each |
| $7^{\prime} \times 7^{\prime}$ door, frame and hardware | $\$ 1100$ each |
| Add automatic closing device | $\$ 60$ each |

$\$ 0.75$ PSF
\$0.80 PSF

```
Replace Door to Achieve Class B & C
    Fire Rating
        4'x7' door and hardware
        4'x7' door, frame and hardware
        7'x7' door and hardware
        7'x7' door, frame and hardware
Replace Door to Achieve Class A
    Fire Rating
        4'x7' door and hardware
        4'x7' door, frame and hardware
        7'x7' door and hardware
        7'x7' door, frame and hardware
Replace Ordinary Glass Light With
        Wire Glass Light
Replace Defective Latch
Replace Window Frames in Corridor
        Partition Walls (1000 square
        inches)
Add Corridor Partitioning (8' wide)
    With Fire Door
    Class B and C Rating $3,800 each
    Class A Rating
Provide Partition Extension
        (average 3' high) From Existing
        Partition to Structural Slab
        Above
Install Coded Manual Fire Alarm Station
Connect Existing Manual Fire Alarm
        Stations to Fire Department
Install Detectors, Photoelectric
    and Ionization
Install Magnetic Door Release Each Leaf
Install Sprinklers in Nonhazardous
    Areas
Install Sprinklers in Hazardous Areas $ 2.25 PSF
$ 2.00 PSF
```

\$ 450 each
\$1,250 each
\$ 800 each
\$1,650 each
\$ 500 each
\$1,300 each
\$ 900 each
\$1,750 each
\$ 40 each
\$ 60 each
\$ 400 each
\$3,800 each \$3,900 each
\$ 30 Per Linear Foot; (PLF)
\$ 140 each
\$1,000 Per Fire Zone
\$ 2.25 PSF
\$ 425 each
\$ 2.00 PSF
\$ $\quad 2.25 \mathrm{PSF}$

```
Add a Fire Alarm to the Sprinkler
    $ 225 each
Install Halon Head for Mechanical
    and Electrical Areas
Add External Stairwell for Exit
$ 8,000 each
$15,000 Per Floor
```


## APPENDIX B <br> Documentation of Computer Algorithm/Program

This Appendix gives a programmer-oriented description of the computer software package. Algorithmic and functional descriptions are contained in the body of this appendix as are the user requirements and options. The appendix consists of four sections:

1) Functional descriptions of each subroutine and major functional block of the main program;
2) Definitions of each of the variables;
3) Definitions of input; and
4) Descriptions of each report produced.

## B. 1 Program Functional Description

A brief description of the function of each of the subroutines is given in this section. In addition, the calling sequence, the reports produced, and the program from which it is called are also given. Since many of the scalars in the calling sequence are array dimensions, a statement containing each multi-dimensional array is given as well. For the main program, a similar description is given by main functional blocks. The relevant variables are defined and the subroutines called within each block are identified. All variables except the Hollerith ones conform to the FORTRAN real-integer name convention.

Subroutine MOTEST: MOdification TEST:
Calling Sequence: (HFORCE, I1, I2, I4)
Il is the simplex variable corresponding to the first state (Table 4) of row I, where I is implied by the value of Il.

I2 is the simplex variable corresponding to the last state (Table 4) of row I.

I4 is subroutine output.
MOTEST is called from MAIN in each of the Alternate Solution Blocks. If the variation of the cost row dictated by the alternate solution logic is not compatible with user modifications, I4 is 0; otherwise I4 is 1.

Subroutine PRSOL: PRint SOLution:
Calling Sequence: (IPROB, IALT, C, Z, HFORCE, IST4, N1, N2, IT4X, X, IT4S, N3, HPAR, N4, N5, N6)

DIMENSION: IST4 (N1, N2), IT4S (N3, N2), HPAR (N4, N5), A (N4, N6)
PRSOL is called from MAIN, once from the Bounding Solution Block and once from each of the Alternate Solution Blocks. It, with repeated calls to RHTAB, prints a Solution Report if the solution is valid. If the solution is not valid (i.e., non-feasible, contains an illegal state, etc.), it prints a self-explaining error report and sets IALT to its negative.

Subroutine RHTAB: Right Hand TABles: Calling Sequence: (K, X)
RHTAB is called only from PRSOL. $K$ is a variable set to 0 upon entry to PRSOL. It prints the cost-requirement surplus tableaus of the solution report. $K$ is a line-space count advanced in the subroutine.

Subroutine PRSMX: PRint SiMpleX
Calling Sequence: (A, IA, IB, HPAR, IC, IST4, ID, IE, IALT)
DIMENSION: A (IA, IB), HPAR (IA, IC), IST\$ (ID, IE)
PRSMX prints the Simplex Matrix Report. It is called from MAIN just prior to the call to RVSMPX which produces the bounding solution. If IALT is zero or one, the multi-page report is printed. For any other value of IALT, the one page version is printed.

Subroutine FEASIB: FEASIBility Test
Calling Sequence: (A, I1, I2, X, L, X2)
DIMENSION: A(I2, I1)
FEASIB is called from MAIN immediately after each RVSMPX call. RVSMPX returns in $L(3)$ an indicator of an abnormal solution. However, since RVSMPX cannot recognize an illegal variable (i.e., one which has an arbitrarily high cost), FEASIB checks the solution for any such variable and returns $L(3)=2$ if one is encountered.

Subroutine RVSMPX: ReVised SiMPleX
Calling Sequence: (A, MA, B, MB, MT, NT, L, X, TOLP, INV, K9P)
DIMENSION: $A(M A, N T), B(M B, M B)$
The description of the RVSMPX routine given in this section is application oriented. For those readers wishing a complete documentation of the RVSMPX routine, the report by Hall, et al., is highly recommended. Several

[^9]of the variables in the calling sequence are fixed in this problem. The vector $L$ is used internally for several purposes but for this discussion $\mathrm{L}(1)$ through $\mathrm{L}(14)$ are the only relevant entries. Upon input, $\mathrm{L}(1)$ is the number of less than or equal to constraints of $A$ (Zero), L(2) is the number of greater than or equal to constraints of $A$ (Zero), and $L(3)$ through $L(14)$ are print switches. For this application, $L(5)$ and $L(14)$ are equal to one; the remaining elements are zero. This combination of switch settings suppresses all internal prints except warning and error messages.

Upon output $L(1)$ through $L(3)$ only will be changed. $L(1)$ is of no interest; $L(2)$ is the iteration count; and $L(3)$ indicates the cause of termination:
$0 \rightarrow$ optimal solution obtained
.1 optimal solution obtained but numerical difficulties encountered
$2 \rightarrow$ non-feasible problem
$3 \rightarrow$ unbounded problem
$4 \rightarrow$ system error.
$X(81)$ upon exit contains the negative of the minimum cost solution.
INV is the last of the variables of interest to the user. If INV is zero, the computation will start from scratch; otherwise, the vector X is used as a starting solution. In the program, INV is zero for the bounding solution call and one for all other calls.

MAIN - Initialization Block
This block performs system initialization; it includes the first executable statement through statement number 70. It produces the System Status Report and constructs that portion of the A matrix which is Fire Zone independent. The Fire Zone independent portion of A consists of the 13 state constraints corresponding to the building safety factors of Table 4 and, except for the right hand side, the mandatory safety requirement constraints corresponding to Table 5.

MAIN - Fire Zone Input Block
This block performs the Fire Zone initialization. It contains statements 100 through 170. Statement 100 is the reentry point when a NEXT is encountered. The functions comprising the initialization are:

Fire Zone Input
Modification of A to accommodate row interdependencies

Modification of $A$ to accommodate alternate fire safety level values
Incorporation of mandatory safety requirements into A
State change cost calculations and their incorporation into A
Calculation of prescriptive cost
Calculation of "arbitrarily high" costs
Printing of Fire Zone Report
The Fire Zone Input and Printing functions are dispersed throughout the block; the sequence is essentially either read-print or read-calculateprint for each line of the report. Other functions performed are isolated within the block.

The default row column interdependencies are incorporated into $A$ in the section from statement 902 through statement 903. It is assumed at this time that the interdependencies defined by Table 4 footnotes *, **, and . . . will not occur; thus constraints 14,15 , and 16 are each set to a dummy variable which equals 1.

The Table 1 indices are read (and defaulted to highest risk state if necessary), $R$ is calculated, a prototype solution ID is constructed, the problem-age input is read and the report print initiated in the next section. Statements run from 900 to 973.

The next section, up to statement 152 , modifies the fire safety level values (rows 17-20) of the A matrix according to the Table 4 footnotes ***, ., and .. . Then to statement 154 is a section which incorporates into A the interdependency defined by *, if required by the input. The section from 154 to 972 computes $F$ according to the building age, selects the appropriate entries for both row 1 of Table 4 and the mandatory safety requirements and incorporates them into $A$.

The section from 972 through 110 modifies the solution ID's (HFORCE) by appending "Input" and "Prescriptive" characters; then proceeds, by building safety factor, to read the element cost vectors, calculate the state transition costs, and print the Fire Zone Input Report.

The section through 170 then calculates Xl and X 2 , the two "arbitrarily high" costs used. X 1 is twenty times and X2 is nineteen times the largest legitimate state transition cost. Xl goes into $C$ where required, $C$ is incorporated into $A$, and $L$ and $Z$ are constructed as subsequently required by subroutines.

MAIN - Control and Modification Block
This block performs the control card reads. For CHANGE and REQUIR cards, there are internal loops for updating C, A, and HFORCE as required.

There are multiple exits from this block depending upon the control card which causes the exit. Exit may be to termination (END), to the Fire Zone Input Block (NEXT), or to the Bounding Solution Block (SOLVE). The statement numbers are 300 to 370 .

MAIN - Bounding Solution Block
This block calls PRSMX, RVSMPX, FEASIB, and PRSOL for the bounding solution. It also transfers the bounding solution into $Y$ so that the alternative solutions can be calculated from an existing basis. The normal exit is to the First Alternate Class Block, but there is an error exit (non-feasible, unbounded, etc.) to the Fire Zone Input Block since a no solution case for the bounding problem implies a no solution case for all alternates. This block begins at statement 370 and includes all statements through the fourth (unnumbered) statement past 178.

## MAIN - First Alternate Class Block

This block follows the Bounding Solution Block and extends through statement 230. It generates the class of solutions obtained by precluding, in turn, any retrofit for each of the Table 4 building safety factors. It calls MOTEST, RVSMPX, FEASIB, and PRSOL. It always exits to the Second Alternate Class block.

## MAIN - Second Alternate Class Block

This block follows statement 230 and extends through 270. It generates the second class of alternate solutions by switching the variables, in turn, of the bounding solution. That is, if a variable is in/out the bounding solution an alternate is produced with the variable forced out/in. It calls MOTEST, RVSMPX, FEASIB, and PRSOL. It always exits to the Restore Solution ID Block.

MAIN - Restore Solution ID Block
This block begins at 280 and continues to the end of the program. Its function is to transfer $Y$ into $X$ and restore the solution ID for reentry. It always exits to the Control-Modification Read Block.

## B. 2 Variable Definition

Scalars

```
IPROB: Problem number (input)
    NAGE: Building age code (input)
    NCON: Construction type code (input)
        IFL: Floor of fire zone (input)
        IPA: Number of patients in zone (input)
            Xl: The arbitrarily high cost used to preclude state changes.
                It is calculated in the Fire Zone Input Block as 20 times
                the largest legitimate state transition cost.
            X2:.95 x X1. X2 is used as a comparand in checking that no
                arbitrarily high costs appear in the objective function.
            IALT: The alternate problem identification
```

A(21,61): The Simplex matrix-dimensions as required by RVSMPX. Rows $1-13$ contain the Building Safety Feature constraints; rows $14-16$, the interdependency constraints; rows $17-20$, the mandatory requirements, and row 21 , the objective function. The matrix is initially constructed from G via the structure of Table 4 in the System Initialization Block. Costs (row 21), alternate values (rows 17-20), interdependency constraints (rows $14-16$ ), and the proper row 1 are inserted in the Fire Zone Input Block. Costs are modified by CHANGE inputs; the right hand side of the mandatory requirement constraints are modified by REQUIR inputs.
$B(23,23)$ : This matrix is required by RVSMPX. Its content is not relevant for the user.

X(150): This vector is required by RVSMPX. It contains the basic solution; upon exit from RVSMPX, the first sixty elements hold the variables. A positive element implies the variable is basic; a negative, that it is non-basic; $X(81)$ contains the negative of the minimum cost. Upon input to RVSMPX, if the advance start option is used, $X$ contains a feasible basis. Elements of $X$ with an index higher than 81 are used to store the prescriptive cost and surpluses for PRSOL and RHTAB.
$\mathrm{Y}(150)$ : This vector is used to store the bounding value solution. It is used to restore $X$ after each alternate solution so that the advance start option may be used.

L(153): This vector is required by RVSMPX. Only the first fourteen elements are of interest to the user. Upon input to RVSMPX, these are all zero except $L(5)$ and $\mathrm{L}(14)$, which are each 1 ; they are used to control warning and error prints internal in RVSMPX. Upon exit, $L(1)$ through $L(3)$ may be non-zero, but only $\mathrm{L}(3)$ is important. It contains an indicator as to whether RVSMPX exited with an optimum solution, an unbounded solution, a non-feasible solution, a numerically poor solution or because of a system error.

Tl(5,5): This matrix is comprised of the Risk Factor Values of Table 1. It is generated via a DATA statement.

T6(3,2,2): This array contains the Mandatory Safety Requirements of Table 6. The first subscript identifies $S_{a}, S_{b}$, and $\mathrm{S}_{\mathrm{c}}$; the second, age NEW or EXIST; the third, the floor. It is generated via a DATA statement.

IT4X(13): This vector contains the current state indices for each PARAMETER of Table 4. It is read in the Fire Zone Input Block; it may be modified via CHANGE cards.

HFORCE (53): This is a Hollerith vector; it contains the solution ID, as it appears in the solution prints, for each of of the state variables. It is assembled character by character in various blocks of the program as follows:

```
All blanks initially in System Initialization
I&P appended in Fire Zone Input Block
C&F appended in Control Modification Block
* appended in the Alternate Solution Blocks
S appended in PRSOL
Blanks are partially restored within each of the Alternate Solution blocks and in the Restore Block
```

It is not used in any calculations but for printing only.

G(13,5): This is the Safety Value matrix of Table 4. It is created via a DATA statement and never changed. Values for row one and those values for which there are alternates dependent upon fire zone are irrelevant. Necessary modification is done on A instead.
$\operatorname{HPAR}(21,5):$ This is a Hollerith matrix created via a DATA statement and never changed. Each row contains a five word (30 character) name for the corresponding row of $A$. It is printed in totality in the Simplex Matrix Report and in part in the System Initialization Report and the Solution Reports.

HOUT(6): This is a Hollerith vector which is the problem name of six words ( 36 characters). It is read in the Fire Zone Input Block and used only for printing. It appears in the Fire Zone Report and all Solution Reports.

| C(53) : | This vector contains the state transition costs for each of the fifty-three Simplex variables. It is constructed in the Fire Zone input block, modified in the Control-Modification block, and printed in PRSOL. |
| :---: | :---: |
| $\operatorname{IT} 4 \mathrm{~S}(13,2):$ | This is the Table 4 to A linkage matrix. It is created via a DATA statement and used throughout the program. The rows correspond to the rows of Table 4; column 1 contains the index, within the A matrix variables corresponding to the first state within the row. Column 2 contains the $A$ index for the last state (excluding the contrived ones) within the row. |
| IST4 (60, 2) : | This is the A matrix to Table 4 linkage matrix. It is created via a DATA statement. The rows correspond to the variable indices of $A$; columns 1 and 2 contain the row and column, respectively of Table 4 corresponding to the variable. |
| JPR(13) : | This vector contains the indices of the prescriptive states for each of the rows of Table 4. It is created via a DATA statement. |
| T4A(4, 3, 3) : | This is a safety value array corresponding to row 1 of Table 4. It is created via a data statement. The first dimension corresponds to FLOOR; the second, to construction type (WOOD FRAME, ORDINARY, or NONCOMBUSTIBLE); the third, to states. |
| IT1X(5) : | This is the current state vector for Table 1 . It is read in the Fire Zone input block. An illegal state index (i.e., less than 1 or greater than the maximum permissible) is defaulted to the index with the highest risk. It is used to calculate $R$ and is printed in the Fire Zone Report. |
| ITIM (5): | This vector contains the maximum length for each of the rows of Table 1. It is created via a DATA statement. |
| $\operatorname{HT1}(5,5):$ | This matrix is Hollerith; it contains the Table 1 line headings for the System Status Report. It is created via a DATA statement. |
| $\operatorname{IQ}(6,6):$ | This is a temporary matrix into which the element cost vectors are read in the Fire Zone Input block. It is not used in any other part of the program. |

LV(13): This vector contains the length of the element cost vector for each row of Table 4. It is created via a DATA statement.

AGE(2): This is a Hollerith vector containing NEW and EXIST. It is constructed via a DATA statement and is used in printing the Fire Zone Input report.
$\operatorname{CON}(3): \quad$ This is a Hollerith vector corresponding to the three construction types of row 1 of Table 4. It contains UNPROT, PROT, and FRSNT. It is created via a DATA statement.

Z(150): This vector holds the safety values of Table 4 corresponding to the A matrix indices of the corresponding states.

CS (13,5,5): This is the unit cost array. The first two dimensions correspond to the rows and columns of Table 4. The third dimension corresponds to the indices of the element cost vector.

## B. 3 Definitions of Data Inputs

There are two classes of input required: the first is that which defines the fire zone status; the second, that which allows user control of the problem variants to be solved. The description of the input is FORTRAN oriented. The input medium is assumed to be an 80 column card. Each card is given a name suggestive of the data contained therein and is defined by the FORTRAN format and the pertinent portion of the READ statement.

## Fire Zone Input

Card 1: Building Safety Factor Indices Card
(13I3, 6A6), [(IT4X(I), $I=1,13),(\operatorname{HOUT}(I), I=1,6)]$
The first thirteen fields are the indices of the current states of the Building Safety Factor values of Table 4. For factor 1, CONSTRUCTION, this is the index within FLOOR and COMBUSTIBLE-WOOD FRAME, COMBUSTIBLEORDINARY, and NON-COMBUSTIBLE. The next six fields may be considered as thirty-six characters of free form text. They are used only as an identification printed in several of the reports.

Card 2: Occupancy Risk Parameter Factors Card
(5I13), [(IT1X(I), I=1, 5)]
These fields are the indices of the current states of the Occupancy Risk Parameter Factors of Table 1.

Card 3: Problem - Floor Card
(513), [IPROB, NAGE, NCON, IFL, IPA]

IPROB is problem number, an identification field
NAGE is the building age:
$1 \rightarrow$ New
$2 \rightarrow$ Existing
NCON is the construction type:
1 + Combustible-Wood Frame
$2 \rightarrow$ Combustible - Ordinary
$3 \rightarrow$ Non-Combustible
IFL is the floor
IPA is the number of patients.
Cards 4-16: Safety Parameter Input Values
(I3, 12I6), [J,IQ (J1, J2), J2=1, K1, J1=J3, J4)]
One or more of these cards appear for each of the rows of Table 4. J is the row index. The array IQ ( $6 \times 6$ ) is used for temporary storage of the element cost vector pending calculation of the state transition cost; the rows correspond to the possible states of the Jth row; the columns contain the element cost vectors. Prior to the read operation, all elements are set to -1 , denoting an impossible or precluded retrofit. J 3 is the index of the current state +1 ; J 4 is the maximum index within the row; if J3 is greater than J 4 , the fields except for J are irrelevant. Kl is the length of the element cost vector. For J equal to 8, two cards may appear since the length of the element cost vector times the number of states may exceed the twelve fields allowed by the format. The trailer card is in exactly the same format with J repeated followed by the remaining cost element vectors. By Table 4 row, the cost element vector lengths are:

| Row | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Length | 1 | 2 | 2 | 2 | 4 | 1 | 3 | 4 | 3 | 3 | 1 | 1 | 2 |

## Control-Modification Card Input

$$
(A 6,2 I 3, I 7)[I, I 1, I 2, I 4]
$$

These cards allow the user to modify the definition of the preceding fire zone and to control the variants of the problem to be solved. Each of these and its function are defined. A $\Delta$ denotes a blank space.

SOLVE $\triangle$ - other fields irrelevant. This card indicates that the fire zone currently resident is to be solved. That is, the complete family of retrofit solutions is to be obtained.

NEXTA $\Delta$ - other fields irrelevant. This card indicates that the next fire zone is to be read. No further variants of the currently resident zone are desired.

END $\triangle \Delta \Delta$ - other fields irrelevant. This card indicates the end of the batch run.

CHANGE $\alpha$ B $\gamma$ This card indicates that a cost change is to be performed on the resident fire zone. The field $\alpha$ is the index of the row (Building Safety Factor) of Table 4 to be changed; $\beta$, the index of the column (state). The change to be made is dependent upon $\gamma$ as follows:
$\gamma<0$ the cost is made arbitrarily high. The indicated state is not to be considered.
$\gamma=0$ all costs in row $\alpha$, except $\beta$, are made arbitrarịy high. The indicated state is required to be in every solution and becomes the input state.
$\gamma>0 \gamma$ becomes the cost for row $\alpha$, column $\beta$.
REQUIR $\alpha \beta$ - remaining fields irrelevant. The mandatory safety requirement denoted by $\alpha$, where $\alpha=1 \rightarrow S_{a}, \alpha=2 \rightarrow S_{b}, \alpha=3 \rightarrow S_{c}$, and $\alpha=4 \rightarrow R$, is changed by the percentage $\beta$. For example, if $\alpha=1$. A new $S_{a}^{(n)}$ is calculated as $S_{a}^{(n)}=\left(1+\frac{\beta}{100}\right) \times S_{a}^{(0)}$.

## B. 4 Description of Reports Produced

The output is described in terms of the content (and interpretation) of the reports generated and the rules which determine the number and ordering of reports. Each report is a single page except where otherwise noted.

The first report is the System Status Report. It is produced only once for each batch of fire zones. It is a single page and is comprised of facsimiles of Tables 1,6 , and 4 as the tables have been constructed via DATA statements.

Fire Zone Input Report
The Fire Zone Input Report appears for each zone read. It is produced prior to the solution of the optimization problem and consists of cosmetically enhanced version of the fire zone input, augmented by the mandatory requirements and the retrofit costs for all possible changes.

The first line contains the fire zone identification and Table 1 indices as they appeared on the input except defaulted to highest risk if input was illegal. The second line corresponds to input card 3 with the age of building and construction numeric codes replaced by text and the remaining numeric fields identified by name. The third line contains the mandatory safety requirements.

The tabular portion of the report contains, for each fire safety factor and under appropriate column headings, the input state index, the prescriptive state index, the element cost vector, (as input or a default value) and the cost (computed or a default value) associated with a transition from the current state to the indicated state. The default rules are: for the existing state, both the element cost vector and the cost are defaulted to zero; for all states with lesser values (lower index) than the current state and all states precluded via a negative element cost vectors are defaulted to arbitrarily large numbers which appear on the report as fields of asterisks(*).

The remainder of the report consists of a simplified version of the modification cards (if any) encountered before a SOLVE card initiates a print of the SOLVE line and the calculation of the family of optimum solutions.

For a CHANGE card the line printed is CHANGE Row $\alpha$ Column $\beta$ Index $\gamma$ cost $\delta_{1}$, . . $\delta_{n}$ where $\alpha$ and $\beta$ are the row and column, respectively, modified by the CHANGE card, $\gamma$ is the input state index and $\delta_{1}$ through $\delta_{n}$ are the negatives of the costs associated with the modified row.

For a REQUIR ciard, the line printed is the index of the requirement which was changed, the percentage by which it was changed and the new requirement.

## Simplex Matrix Report

Following each SOLVE line (whether in a Fire Zone Input Report or a Modified Problem Report) is a Simplex Matrix Report. For the first
solution of the fire zone, this is a multi-page report containing the matrix used by the optimization algorithm. The row headings indicate the source of the equation ( $1-13$ from Table 4 rows, $14-16$ from the footnoted interdependencies, 17-20 from the mandatory requirements, and 21 the objective function), and the column headings indicate the variable index correspondence between the optimization matrix column and the row-column of Table 4. For modifications of the fire zone, this report is condensed into a single page report which contains only the last five rows of the optimization matrix. The condensed version contains all elements of the matrix subject to modification via the CHANGE and REQUIR cards.

## Modified Problem Report

The Modified Problem Report is produced for each set of CHANGE and/or REQUIR cards following a SOLVE. That is, for every modified fire zone, the report is produced, unless the problem as input is not solved. ${ }^{1}$ It consists of a one line print of MODIFIED PROBLEM $\alpha$, where $\alpha$ is the problem identification number, followed by the simplified version of the pertinent CHANGE and REQUIR cards exactly as in the Fire Zone Input Report and followed by a SOLVE.

## Solution Reports

Following each SOLVE line, regardless of the report in which it appears, is the Bounding Solution Report. Following this report are two sets of Alternate Solution Reports. All three solution reports are nearly identical; thus the descriptions will be combined with the differences noted.

The first line of each report contains the problem number, problem name, and an ALTERNATE index which is interpreted as follows:

## 0 - Bounding Solution-Input

1 - Bounding Solution Modified
$10 \alpha \beta \rightarrow$ first set of alternates; $\alpha \beta$ as a two digit number is the index of the row of Table 4 which is varied.
$2 \alpha \beta \gamma$ + Second set of alternates; $\alpha \beta$ is the row; $\gamma$ is the column of the cost varied.

The five line tableau(s) which may appear on the right hand side contain(s) information as follows:

[^10]TOTAL COST appears for every solution. It gives the total cost for the solution and indicates the surplus over each of the mandatory safety requirements attained by the solution.

PRESCRIPTIVE appears only for the Bounding Solution Report. The first line gives the cost of the prescriptive retrofits. Asterisks (*) indicate that one or more of the prescriptive indices is precluded. The remaining lines show the surplus, if any, over each of the requirements. Surpluses can only appear in the General Safety Requirement for the prescriptive solution.

The left hand portion of the report parallels Table 4. For each of the rows, the states appearing on input or in the solution generates a print line. For the Bounding Solution Report, the prescriptive solution generates a print line; for the modified problems, the state corresponding to a cost modification generates a print line; and for the alternates, each cost changed generates a print line. Each of the lines is identical in format except for the row heading on the first line printed from each row. Under the heading VARIABLE are the index (within the optimization matrix) and the value of the variable in the solution. Under the heading TABLE 4 is the column index of the state. Under COST is the total transition cost (from input to the indicated state). Asterisks (*) indicate a precluded state (i.e., an arbitrarily high cost). The GRADE is the Table 4 safety value associated with the state. The remaining information on the line shows the reason the line was included in the print. It will always consist of some combination of $S, I, P, *, F$, or C. These terms are defined as:

```
S + state is in solution
I * input state
P + prescriptive state
* + cost modified by alternate logic
F + state forced into solution via a CHANGE
C + state precluded by a CHANGE or cost input by a CHANGE
```

There are two classes of alternate solutions produced. They were selected to mitigate the impact of non-integer solutions and to give the user an automatic set of alternatives, thus enabling him to accommodate externalities, as well as answer some "what if" questions expected to be common to many users.

The first class of alternates precludes any retrofit within a row of Table 4 considering the rows in turn and one at a time. The number of solutions in this class will always be thirteen minus the number of rows for which no retrofit is allowed. However, one or more of these
may duplicate the bounding solution; this will occur for every row for which the bounding solution contained the existing state.

The second class of solutions is obtained by changing, in turn, the cost associated with each of the fifty-three variables. If the variable is in the bounding solution, its cost is adjusted so that it is precluded from an alternate solution. If the variable is not in the original solution; the costs of the other variables within the TABLE 4 row are adjusted so that the variable is forced into the optimal solution. The number of alternates in this class is exactly the number of allowable states with a maximum of fifty-three.

Some of the cost perturbations may result in non-feasible solutions (i.e., there is no acceptable way to attain compliance). This fact, the fact that alternatives may include duplicates, and the fact that the number of alternates generated is dependent upon both the input states and the retrofits precluded, means that there is no a priori way to get a good estimate for the number of unique solutions presented.

This appendix contains three computer output products: 1) a compilation of each of the programs used; 2) an annotated sample input listing; and 3) the abbreviated set of reports produced by processing the input shown. The program compilations are the versions used to produce the sample output shown in Chapter 2. All of the subroutines are exactly as they were for the case application presented in Chapter 2 and as described in Appendix B.

The Program MAIN has been changed for the example presented in this section in order to limit the number of alternative solutions. The first class of alternative solutions has been limited to two, the first two which would normally appear.

The second class ${ }^{2}$ of alternative solutions has been limited to three. Each of these changes involves only the changing of a limit on a DO loop. The only other deviation from the program description given in Appendix B consists of a patch executed after a NEXT card and prior to the fire zone input. This patch allows the CS array ${ }^{3}$ to be changed between fire zone inputs.

The sample input is identical to that for the third floor fire zone of the case application presented in Chapter 2. In addition, it consists

1 The first class of alternatives is determined by the rows of Table 4. For example, suppose $X_{i j}$ appears in the optimal solution as a retrofit, then the costs of all potential retrofits for the $i^{\text {th }}$ feature are made arbitrarily high. This step guarantees that no potential retrofits associated with that feature can appear in the optimal solution. The number of solutions generated in this class is equal to the number of features which moved to a higher state in the optimal solution.

2 This class of solutions is generated in the following manner: if $X_{i j}$ appears in the optimal solution as a retrofit then its cost is made arbitrarily high thus precluding it from consideration; or if $\mathrm{X}_{\mathrm{i}} \mathrm{d}$ did not appear in the optimal solution as a retrofit and it is a potential retrofit, then its cost is held constant and the costs of all other potential retrofits for that feature are made arbitrarily high. The number of solutions generated in the second class is equal to the number of variables in the origianl linear programming problem minus the number of retrofit states which cannot be attained.

3
CS is a 13 by 5 by 5 array containing the unit costs used in the linear programming problem. The first two dimensions correspond to the rows and columns of Table 4. The third dimension corresponds to the indices of the element cost vector.
of a set of modifications carefully chosen so as to illustrate the use of the CHANGE and REQUIR options. Exhibit C.l shows the input stream as it actually entered the computer.

Immediately following Exhibit C.l are the report sets produced by the input stream. The number of solutions presented was limited so as to keep the example reasonably sized. Since Section 2.4 .2 dealt with the output format and its interpretation, an extensive interpretation of the results will not be given. The intent of the example is to illustrate: 1) the flexibility of the system; 2) the inputs required; and 3) the form, content, and sequence of the reports produced. It is not intended to provide a line by line description of the input-output stream.

```
    3
    3
    3
    l
    22000 0 2000 0
    3 0
    4 0
    5
    6 1 1 1 1 
    7 0
    8
    8 1090 240 0 2
    9
    10 0 25 1 1 -1 
    11 1
    12 2000}505610 7610 8700
    13 2000 0 7610 0 7610 1090
SOLVE
CHANGE 9 2 0
CHANGE 11 3 1200
CHANGE 5 2 -1
REQUIR 2 20
SOLVE
END
```

Table 1. Occupancy Risk Factors

1. Patient
$\begin{array}{lllll}\text { Mobility } & 1.0 & 1.6 & 3.2 & 4.5\end{array}$
2. Patient
$\begin{array}{lllll}\text { Density } & 1.0 & 1.2 & 1.5 & 2.0\end{array}$
3. Zone
$\begin{array}{lllll}\text { Location } & 1.1 & 1.2 & 1.4 & 1.6\end{array}$
4. Ratio of
$\begin{array}{llllll}P & 1.0 & 1.1 & 1.2 & 1.5 & 4.0\end{array}$
5. Average
Age $1.0 \quad 1.2$

Table 6. Mandatory Safety Requirements

|  | Containment |  | Extinguishment |  | People Movement |
| :--- | :---: | ---: | :---: | :---: | :---: |
|  | SA |  | SB | SC |  |
| Zone Location | New Exist | New Exist | New Exist |  |  |
| First Floor | 9.0 | 4.0 | 6.0 | 3.0 | 6.0 |
| Above lst Floor | 14.0 | 8.0 | 8.0 | 5.0 | 9.0 |
| Ab |  |  |  |  |  |

Table 4. Parameter Values with Prescriptive Indices

1. Construction

First Floor Second Floor Third Floor 4th \& Above
2. Interior Finish Corr \& Exit
3. Interior Finish Rooms
4. Corridors Partitions/Walls
5. Doors to Corridor
6. Zone Dimensions
7. Vertical Openings
8. Hazardous Areas
9. Smoke Control
10. Emergency Movement Routes
11. Manual Fire Alarm
12. Smoke Detection \& Alarm
13. Automatic Sprinklers

3

$$
\begin{array}{rrrrrrr}
-2.0 & .0 & -2.0 & .0 & .0 & 2.0 & 2.0 \\
-7.0 & -2.0 & -4.0 & -2.0 & -2.0 & 2.0 & 4.0 \\
-9.0 & -7.0 & -9.0 & -7.0 & -7.0 & 2.0 & 4.0 \\
-13.0 & -7.0 & -13.0 & -7.0 & -9.0 & -7.0 & 4.0 \\
-5.0 & .0 & 3.0 & & & & \\
-3.0 & 1.0 & 3.0 & & & & \\
-10.0 & .0 & 1.0 & 2.0 & & & \\
-10.0 & .0 & 1.0 & 2.0 & & & \\
-6.0 & -4.0 & -2.0 & .0 & 1.0 & & \\
-14.0 & -10.0 & .0 & 2.0 & 3.0 & & \\
-11.0 & -5.0 & -6.0 & -2.0 & .0 & & \\
-2.0 & .0 & 3.0 & 4.0 & & & \\
-8.0 & -2.0 & .0 & 3.0 & 5.0 & & \\
-4.0 & 1.0 & 2.0 & & & & \\
.0 & 2.0 & 3.0 & 4.0 & 5.0 & & \\
.0 & 2.0 & 8.0 & 10.0 & & &
\end{array}
$$

## Exhibit C. 2 (Cont.)


${ }^{\text {a }}$ Numbers in this column are actual element counts.
${ }^{b}$ A cost of 0 implies the Building Safety Feature is already in that state.
A cost greater than or equal to 0 is an estimate of the retrofit cost.
A cost of ****** indicates a regression in score or impossible retrofit.

TABLE 1．OCCUPANCY RISK FACTORS

TABLE 6．MANDATORY SAFETY REQUIREMENTS

$$
\begin{aligned}
& \text { 1. PATIENT } \\
& \text { MOBILIY } \\
& \text { 2. PATIENT } \\
& \text { DENSITY } \\
& \text { 3. ZONE } \\
& \text { LOCATION } \\
& \text { 4. FATIO OF } \\
& \text { D TO A } \\
& \text { 5. AVERAGE } \\
& \text { AGE }
\end{aligned}
$$

$1.0 \quad 1.2$

## ZONE LOCATION <br> ABOVE IST FLOO？

CONTAINMENT
EXTINGUI SHMENT
1NヨWヨヘロW ヨาa0ヨa
$\begin{array}{lr}\text { NEW EXIST } \\ \text { E．O } & 1.0 \\ \text { C．0 } & 3.0\end{array}$ BS
$\begin{array}{rr}\text { NEW EXIST } \\ 6.0 & 3.0 \\ 8.0 & 5.0\end{array}$

1．4
$3 \cdot 2$
1.6
1.0

| 1.0 | 1.6 | 3.2 | 4.5 |
| :--- | :--- | :--- | :--- |
| 1.0 | 1.2 | 1.5 | 2.0 |
| 1.1 | 1.2 | 1.4 | 1.6 |
| 1.0 | 1.1 | 1.2 | 1.5 |

TABLE 4．PAFAMETER VALUES WITH PRESCRIPTIVE INDICES





| $\stackrel{c}{\sim} \underset{\sim}{N}$ | $00000$ | $0000:$ | $\bigcirc 00$ | $\circ \circ \circ$ | $\begin{array}{lll} 0 & 0 & 0 \\ 0 & 0 \\ 0 & 0 & 0 \\ 1 & 1 & 1 \end{array}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $\stackrel{M}{N} \stackrel{1}{1}$ | $00000$ | $00000$ | $\bigcirc 0 \bigcirc$ |  | $\begin{array}{lll} 0 & 0 & 0 \\ - & 0 & 4 \\ -1 & 1 & 1 \end{array}$ |
| $\begin{array}{ll} N & u_{1} \\ & 1 \\ \hline \end{array}$ | $00000$ | $00000$ | $\circ 0 \%$ | $\bigcirc 00$ | $0000$ |
| $\vec{N} \underset{1}{0}$ | $\because 0000$ | $\because 0: 00$ | $\because 0 \%$ | $\because \because 0$ | $\because 00:$ |
| $\begin{array}{lc} \circ & m \\ \\ \hline \end{array}$ | $\because 0: 0$ | $\because 0000$ | $\because 0 \%$ |  |  |
| $\begin{gathered} a \\ \hline 1 \\ 1 \end{gathered}$ | $00000$ | $\because 0000$ | $\because \circ$ |  | $\begin{array}{r} 0: 0 \\ 0 \\ 0 \\ 1 \end{array}$ |
| $\stackrel{\infty}{-1}$ | $\because 0000$ | $\because 0000$ |  | $000$ | $\therefore 000$ |
| $\underset{i}{i}$ | $\because 0: 00$ | $\because \because 0: 0$ |  |  | $\begin{array}{l:l} 0: O \\ \dot{N} & 0 \\ N \end{array}$ |
| $\begin{array}{cc} \approx & m \\ \vdots \\ u \end{array}$ | $\because \because 0:$ | $\because 0: 00$ | $\because 0:$ |  | $0000$ |
| $\stackrel{\cong}{\sim} \underset{u}{N}$ | $\because 0000$ | $\because 000$ |  | $0: 0$ | $\because 0:$ |
| $\pm \underset{i}{n}$ | $\because 0: 00$ | $\because 0000$ | $\because \because 0$ | $\begin{aligned} & 000 \\ & i \end{aligned}$ | $\begin{array}{lll} 0 & 0 & 0 \\ 0 & 0 & 0 \\ i & 1 & 1 \end{array}$ |
| $\xrightarrow{M}$ | $\because 0: 00$ |  |  | $\circ:$ | $\begin{array}{l:} 0 \\ \dot{N} \end{array}$ |
| $\begin{array}{cc} \sim \\ \\ & i \end{array}$ | $\because 0: 0:$ | $\because \because 0: \circ$ | $\because \because ?$ |  | $0 \because 0:$ |
| $\Rightarrow \begin{gathered} N \\ \Rightarrow 1 \end{gathered}$ | $\because 0000$ | $\because: 0: 0$ | $\because \because:$ | $0: 0$ | $\because 0: 0$ |
|  | - NM** | 0 Nooso | $\Rightarrow \mathrm{N}$ | $\pm 00$ | $\stackrel{\infty}{a} a \circ$ |


| $\begin{gathered} \omega_{1} \\ r_{1} \\ \vdots \\ 0 \end{gathered}$ | $\circ: 00:$ | $\because 0: 00$ | $\because \circ \circ$ | $\bigcirc 00$ | $\begin{array}{r} \circ 0: 0 \\ 0 \\ \vdots \\ i \end{array}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $\hat{m}$ | $\therefore 0: 00$ | $\circ \because 0: 0$ |  | $\because \because 0$ | $\begin{array}{cccc} \therefore & 0 & 0 \\ 0 & 0 \\ \infty & \alpha \\ 1 & 1 \end{array}$ |
|  |  | $\circ$ | $\because \circ \circ$ | $\because \circ \circ$ | $\because \because 0 \circ$ |
| $\begin{gathered} n \\ m \\ 0 \\ 0 \end{gathered}$ | $\circ \circ: \circ \circ$ | $\because: \circ \because 0$ |  | :O: | $\because \because \because$ |
| $\begin{gathered} \pm \\ \\ \\ \hline \end{gathered}$ | $\bigcirc \bigcirc \bigcirc 0:$ | $\because: \circ: \circ$ | $\bigcirc \bigcirc \bigcirc$ | $\bigcirc \bigcirc 0$ | ㅇㅇㅇㅇ |
| ${\underset{m}{m}}_{\square}^{1}$ | $\bigcirc \bigcirc \bigcirc \bigcirc$ | $\because \because: 口$ | $\bigcirc 00$ | $\bigcirc \bigcirc 0$ | $\because \because O O$ |
| $\underset{\sim}{N} \underset{\sim}{\sim}$ | ㅇ․ㅇ: | $\because \because: \circ:$ | $\bigcirc \bigcirc$ | $\bigcirc \bigcirc \bigcirc$ | ㅇㅇ： |
| $\vec{m}$ | $\because 0: \circ 0$ | $\because \because: \circ:$ | $\because: 0$ | $\bigcirc \bigcirc \bigcirc$ | $\begin{array}{c:c} 0 & 0 \\ \dot{\sim} \stackrel{\sim}{M} & \dot{\sim} \end{array}$ |
| $\begin{array}{cc} 0 \\ m \\ \vdots \\ \infty \end{array}$ | $\because 0: 0$ | $\because \because \because: 口$ | $\because \because$ | $\because \because 0$ | $\begin{aligned} & 0 \\ & 0 \\ & 0 \\ & 0 \\ & 1 \end{aligned} 1$ |
| $\begin{array}{cc} 0 \\ N & N \\ \hline \end{array}$ |  | $\because: \because \because:$ |  | ○：0 | $\begin{array}{cc:c} 0 & 0 & 0 \\ 0 & 0 \\ i & 1 & 0 \end{array}$ |
| $\stackrel{\infty}{\sim} \underset{\infty}{1}$ | $\because \because \circ: \circ$ | $\because \because \because: \circ$ | $\because \circ:$ | ㅇ․ | $\begin{aligned} & 0000 \\ & \vdots \vdots \\ & \vdots 1 \end{aligned}$ |
| $\hat{N}$ |  | $\because \because \because 0:$ | $\because \because:$ | $\because: 0$ | $\begin{gathered} \therefore \because O \\ \dot{m} \cdot \dot{m} \dot{m} \end{gathered}$ |
| $\stackrel{\circ}{\sim}$ | $\because \circ: \circ \circ$ | $\because \because \because: 口$ | $\because \because \circ$ | $\bigcirc \bigcirc 0$ | $\begin{gathered} \circ \because O \\ \dot{N} \cdot \stackrel{0}{N} \end{gathered}$ |
| $\stackrel{\sim}{\sim} \underset{\sim}{M}$ | : ㅇ: : : | $\because \because: 0:$ |  |  | ㅇㅇㅇ |
|  | －NMが | ○人moo | $こ \cong$ | $\pm \stackrel{せ}{\square}$ | $\wedge$－ |





| $w$ 0 0 0 0 | $\begin{aligned} & 0 \\ & 0 \\ & 0 \end{aligned}$ | $\begin{array}{lll} 0 & 0 & 0 \\ 0 & 0 \\ 0 & 0 \\ i & m \end{array}$ | $\begin{array}{lll} 0 & 0 & 0 \\ 0 & 0 & 0 \\ \dot{m} & 0 \\ 1 & m \end{array}$ | ㅇ | $\begin{array}{lll} 0 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 \\ 0 & 1 \end{array}$ | $\begin{aligned} & 00 \\ & 00 \\ & 0 \\ & 1 \end{aligned}$ | $\begin{aligned} & \circ 0 \\ & 00 \\ & 00 \\ & \text { Ni } \end{aligned}$ | $\begin{aligned} & 0 \\ & 0 \\ & 0 \end{aligned} 0$ | $\begin{array}{ll} O & 0 \\ 0 & 0 \\ \dot{N} & \\ 1 \end{array}$ | ㅇ | $\begin{aligned} & \circ \circ \\ & 00 \\ & -\dot{N} \end{aligned}$ | $\begin{array}{ll} \circ & 0 \\ 0 \\ \text { N } \\ \text { N } \end{array}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\begin{aligned} & \text { r } \\ & 0 \\ & 0 \end{aligned}$ | ㅇ | $\begin{aligned} & \circ \\ & 0 \\ & 0 \\ & 0 \\ & 0 \\ & 10 \\ & 0 \\ & 0 \\ & 0 \\ & 0 \\ & 0 \end{aligned}$ | $\begin{aligned} & 0 \\ & 0 \\ & 0 \\ & 0 \\ & 0 \\ & 0 \\ & 0 \\ & 0 \\ & 0 \\ & 0 \\ & 0 \end{aligned}$ | ㅇ | $\begin{array}{r} \circ \\ \circ \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ \text { m } \\ \text { m } \end{array}$ | $\begin{aligned} & 0 \\ & 0 \\ & 0 \\ & 0 \\ & 0 \\ & 0 \\ & 0 \\ & 0 \\ & 0 \\ & 0 \end{aligned}$ | $\begin{array}{lll} 0 & 0 & 0 \\ 0 & 0 \\ 0 & 0 \\ 0 & 0 \\ 1 & 0 \\ & 0 \\ m \end{array}$ |  | $\begin{array}{r} \circ \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ \text { I } \\ \hline \end{array}$ | ㅇ | $\begin{aligned} & \circ \\ & 0 \\ & 0 \\ & 0 \\ & 0 \\ & 0 \\ & 0 \\ & 0 \end{aligned}$ | $\begin{aligned} & \circ \\ & 0 \\ & 0 \\ & 0 \\ & 0 \\ & 0 \\ & 0 \\ & u \\ & 4 \end{aligned}$ |



| FLOOR 3 |  |
| :---: | :---: |
| VARIABLE |  |
| 3 | 1.000 |
| 4 | . 000 |
| 5 | . 000 |
| 6 | 1.000 |
| 7 | - 500 |
| 8 | - 000 |
| 9 | - 500 |
| 11 | 1.000 |
| 14 | . 000 |
| 15 | 1.000 |
| 16 | - 000 |
| 19 | 1.000 |
| 21 | - 000 |
| 25 | . 000 |
| 26 | - 000 |
| 27 | 1.000 |
| 28 | -000 |
| 30 | -333 |
| 32 | -66? |
| 33 | . 000 |
| 34 | 1.000 |
| 39 | 1.000 |
| 43 | - 000 |
| 44 | 1.000 |
| 45 | . 500 |
| 46 | - 500 |
| 50 | 1.000 |



$$
\begin{aligned}
& \dot{\sim} \\
& \stackrel{\mu}{\infty} \\
& \stackrel{\rightharpoonup}{\infty} \\
& \leftarrow
\end{aligned}
$$

ヨา8vIるマ^

$$
\begin{array}{lr}
3 & 1.000 \\
4 & 1.000 \\
5 & .000 \\
4 &
\end{array}
$$

$$
\begin{array}{lll}
\circ \circ & \circ \\
\circ & \circ & 8 \\
0 & 0 & \vdots \\
0 & \vdots &
\end{array}
$$

PAPAMETER
1．CONSTRUCTION
2．INTERIOF FINISH CORR E EXIT
3．INTERIOR FINISH ROOMS
4．CORRIDOFS PARTITIONS／WALLS
5．DOORS TO COFRIDOR
6．ZONE DIMENSIONS
7．VERTICAL OPENINGS
8．HAZAROOUS AREAS
9．SMOKE CONTROL
10．EMERGENCY MOVEMENT ROUTES
11．MANUAL FIRE ALARM
12．SMOKE DETECTION E ALARM
13．AUTOMATIC SPFINKIERS

$$
\begin{array}{r}
.000 \\
1.000 \\
1.000
\end{array}
$$

$$
\begin{aligned}
& \circ \\
& \circ \\
& \stackrel{\circ}{\circ} \\
& \vdots \\
& \vdots \\
& \vdots
\end{aligned}
$$

$$
\text { PROBLEM } 3
$$

$$
\begin{array}{r}
.000 \\
1.000
\end{array}
$$

$$
\begin{array}{lll}
\therefore \circ & \circ & 0 \\
0 & 0 \\
0 & \circ & 0 \\
00 & 0 & 0 \\
1 & 1 & 1
\end{array}
$$

$$
\begin{array}{lllll}
00 & m & n \\
m & \circ & \circ \\
\dot{q} & \text { in }
\end{array}
$$

$$
\begin{aligned}
& u \\
& \frac{j}{n} \\
& \frac{j}{n} \\
& i
\end{aligned}
$$

PARAMETE:

$$
\text { FLOO= } 3
$$

$$
000 \cdot 1 \text { II }
$$

$$
\begin{aligned}
& \text { 1. CUNSTRUCIIUN } \\
& \text { 2. INTEFIOF FINISH CUĀF E EXIT } \\
& \text { 3. INTEFIUF̈. FINISH FUCMS } \\
& \text { 4. COFFIDO-S DAFTIITIONS/WALLS } \\
& \text { 5. UUGFS TG CUFFIIOOA }
\end{aligned}
$$

6. LUNE UIMLNSLCISS
7. hazafdous af:eas
8. SMOKE CUNTRUL
9. EMEFGENCY MOVEZMENT ROUTES
10. SMUKE DETECTIUN E ALAI.A
I3. AUTGMATIC SPKINKLEES

$$
\begin{aligned}
& V A R I A B L E \\
& 31.300
\end{aligned}
$$

$$
\begin{array}{lr}
4 & 1.000 \\
7 & .000 \\
9 & 1.000
\end{array}
$$

$$
\begin{aligned}
& 14 \quad .000 \\
& 151.000 \\
& 191.000
\end{aligned}
$$

$$
\begin{aligned}
& 191.000 \\
& 25 \quad .000 \\
& 271.000
\end{aligned}
$$

$$
\begin{array}{lr}
28 & .000 \\
30 & 1.000
\end{array}
$$

$$
30 \quad 1.000
$$

$$
\begin{array}{lr}
33 & .000 \\
34 \quad 1.000
\end{array}
$$

$$
\begin{aligned}
& 35 \quad .000 \\
& 40 \quad 1.000
\end{aligned}
$$

$$
431.00 j
$$

$$
45 \quad .250
$$

$$
\begin{array}{ccc}
0 & 0 & 0 \\
H & H & 3 \\
\sim & 0 & 0 \\
0 & 0 & 0 \\
4 & 4 & 4
\end{array}
$$

$$
\begin{array}{ll}
0 & 0 \\
0 & 0 \\
\hdashline & \text { n } \\
0 & 1 \\
0 & m \\
\text { ur } & \text { s) }
\end{array}
$$

\& พ习ารกyy

21 SEE.87
SUFPLUS $=-.0$
SUFPLUS $=-.00$
SURPLUS $=-.0$
SURPLUS $=.04$




Fluun 3

| VAFIABLE |  |
| ---: | ---: |
|  | 1.000 |
| 4 | .000 |
| 5 | 1.000 |
| 7 | .000 |
| 9 | 1.000 |
| 11 | 1.000 |
| 14 | .000 |
| 15 | 1.000 |
| 15 | 1.000 |
| 25 | .000 |
| 27 | 1.300 |
| 25 | .000 |
| 30 | 1.000 |
| 23 | .000 |
| 34 | 1.000 |
| 35 | 1.000 |
| 43 | 1.000 |
| 45 | .000 |
| 45 | 1.000 |
| 60 | .000 |
| 33 | .400 |




Exhibit C. 2 (Cont.)
FLOOR 3






MODIFIED PROBLEM
SOLVE


$\begin{array}{rrrr}0 N & 0000 & 00000000000 \\ M & 0 & 0 & 0 \\ 1 & 0 & 0 & 0 \\ 1\end{array}$
$\hat{M} \because 0000 \quad 00000 \quad 000 \quad 000 \quad 000000$



$m \mathrm{~m} 000000000000000000000$
NNOOOOOOOOOOOOOOOO
$\overrightarrow{1} \quad 00000 \quad 00000 \quad 000 \quad 000 \quad 0000$
PARAMETEG
TABLE 4 INDICES

1. CONSTRUCTION
2. INTERIOF FINISH CORP E EX
3. INTERIOR FINISH ROOMS
4. CORRIDOFS PARTITIONS/WALLS
5. DOOFS TO CORGIDOR
6. ZONE DIMENSIONS
7. VEOTICAL OPENINGS
8. HAZAFDOUS AREAS
9. SMOKE CONTROL
10. EMEFGENCY MOVEMENT FOUTES
11. MANUAL FIFE ALAPM
12. SMOKE DETECTION E ALARM
13. AUTOMATIC SPRINKLERS
14. ROW 4 QOW 5
15. QOW 6 ROW IO
16. FOW 5 FOW 4
17. SA \# CONTAINMENT
18. SB * EXTINGUISHMENT
19. SC \# PEOPLE MOVEMENT
20. SG * GENERAL
21. COST FOW
PARAMETEG
TABLE 4 INDICES
22. CONSTRUCTION
23. INTERIIOR FINISH CORP \& EX
24. INTERIOR FINISH ROOMS
25. CORRIDOFFS PARTITIONS/WALLS
26. DOOFS TO CORGIDOR
27. ZONE DIMENSIONS
28. VEPTICAL OPENINGS
29. HAZARDOUS AREAS
30. SMOKE CONTROL
31. EMEFGENCY MOVEMENT ROUTES
32. MANUAL FIFE ALAPM
33. SMOKE DETECTION \& ALARM
34. AUTOMATIC SPRINKLERS
35. ROW 4 QOW S
36. ROW 6 ROW IO
37. FOW 5 ROW 4
38. SA \# CONTAINMENT
39. SB * EXTINGUISHMENT
40. SC \# PEOPLE MOVEMENT
41. SG * GENERAL
42. COST FOW
PARAMETEG
TABLE 4 INDICES
43. CONSTRUCTION
44. INTERIOF FINISH CORP \& EX
45. INTERIOR FINISH ROOMS
46. CORRIDOFS PARTITIONS/WALLS
47. DOOFS TO COREIDOR
48. ZONE DIMENSIONS
49. VEOTICAL OPENINGS
50. HAZAFDOUS AREAS
51. SMOKE CONTROL
52. EMEFGENCY MOVEMENT ROUTES
53. MANUAL FIFE ALAPM
54. SMOKE DETECTION E ALARM
55. AUTOMATIC SPRINKLERS
56. FOW 4 QOW 5
57. QOW 6 ROW IO
58. FOW 5 ROW 4
59. SA \# CONTAINMENT
60. SB * EXTINGUISHMENT
61. SC \# PEOPLE MOVEMENT
62. SG * GENERAL
63. COST FOW
PARAMETEG
TABLE 4 INDICES
64. CONSTRUCTION
65. INTERIOF FINISH CORP \& EX
66. INTERIOR FINISH ROOMS
67. CORRIDOFS PARTITIONS/WALLS
68. DOOFS TO COREIDOR
69. ZONE DIMENSIONS
70. VEOTICAL OPENINGS
71. HAZAFDOUS AREAS
72. SMOKE CONTROL
73. EMEFGENCY MOVEMENT ROUTES
74. MANUAL FIFE ALAPM
75. SMOKE DETECTION E ALARM
76. AUTOMATIC SPRINKLERS
77. FOW 4 QOW 5
78. QOW 6 ROW IO
79. FOW 5 ROW 4
80. SA \# CONTAINMENT
81. SB * EXTINGUISHMENT
82. SC \# PEOPLE MOVEMENT
83. SG * GENERAL
84. COST FOW
PARAMETEG
TABLE 4 INDICES
85. CONSTRUCTION
86. INTERIOF FINISH CORP \& EX
87. INTERIOR FINISH ROOMS
88. CORRIDOFS PARTITIONS/WALLS
89. DOOFS TO COREIDOR
90. ZONE DIMENSIONS
91. VEOTICAL OPENINGS
92. HAZAFDOUS AREAS
93. SMOKE CONTROL
94. EMEFGENCY MOVEMENT ROUTES
95. MANUAL FIFE ALAPM
96. SMOKE DETECTION E ALARM
97. AUTOMATIC SPRINKLERS
98. FOW 4 QOW 5
99. QOW 6 ROW IO
100. FOW 5 ROW 4
101. SA \# CONTAINMENT
102. SB * EXTINGUISHMENT
103. SC \# PEOPLE MOVEMENT
104. SG * GENERAL
105. COST FOW
PARAMETEG
TABLE 4 INDICES
106. CONSTRUCTION
107. INTERIOF FINISH CORP \& EX
108. INTERIOR FINISH ROOMS
109. CORRIDOFS PARTITIONS/WALLS
110. DOOFS TO COREIDOR
111. ZONE DIMENSIONS
112. VEOTICAL OPENINGS
113. HAZAFDOUS AREAS
114. SMOKE CONTROL
115. EMEFGENCY MOVEMENT ROUTES
116. MANUAL FIFE ALAPM
117. SMOKE DETECTION E ALARM
118. AUTOMATIC SPRINKLERS
119. FOW 4 QOW 5
120. QOW 6 ROW IO
121. FOW 5 ROW 4
122. SA \# CONTAINMENT
123. SB * EXTINGUISHMENT
124. SC \# PEOPLE MOVEMENT
125. SG * GENERAL
126. COST FOW
PARAMETEG
TABLE 4 INDICES
127. CONSTRUCTION
128. INTERIOF FINISH CORP \& EX
129. INTERIOR FINISH ROOMS
130. CORRIDOFS PARTITIONS/WALLS
131. DOOFS TO COREIDOR
132. ZONE DIMENSIONS
133. VEOTICAL OPENINGS
134. HAZAFDOUS AREAS
135. SMOKE CONTROL
136. EMEFGENCY MOVEMENT ROUTES
137. MANUAL FIFE ALAPM
138. SMOKE DETECTION E ALARM
139. AUTOMATIC SPRINKLERS
140. FOW 4 QOW 5
141. QOW 6 ROW IO
142. FOW 5 ROW 4
143. SA \# CONTAINMENT
144. SB * EXTINGUISHMENT
145. SC \# PEOPLE MOVEMENT
146. SG * GENERAL
147. COST FOW
PARAMETEG
TABLE 4 INDICES
148. CONSTRUCTION
149. INTERIOF FINISH CORP \& EX
150. INTERIOR FINISH ROOMS
151. CORRIDOFS PARTITIONS/WALLS
152. DOOFS TO COREIDOR
153. ZONE DIMENSIONS
154. VEOTICAL OPENINGS
155. HAZAFDOUS AREAS
156. SMOKE CONTROL
157. EMEFGENCY MOVEMENT ROUTES
158. MANUAL FIFE ALAPM
159. SMOKE DETECTION E ALARM
160. AUTOMATIC SPRINKLERS
161. FOW 4 QOW 5
162. QOW 6 ROW IO
163. FOW 5 ROW 4
164. SA \# CONTAINMENT
165. SB * EXTINGUISHMENT
166. SC \# PEOPLE MOVEMENT
167. SG * GENERAL
168. COST FOW
PARAMETEG
TABLE 4 INDICES
169. CONSTRUCTION
170. INTERIOF FINISH CORP \& EX
171. INTERIOR FINISH ROOMS
172. CORRIDOFS PARTITIONS/WALLS
173. DOOFS TO COREIDOR
174. ZONE DIMENSIONS
175. VEOTICAL OPENINGS
176. HAZAFDOUS AREAS
177. SMOKE CONTROL
178. EMEFGENCY MOVEMENT ROUTES
179. MANUAL FIFE ALAPM
180. SMOKE DETECTION E ALARM
181. AUTOMATIC SPRINKLERS
182. FOW 4 QOW 5
183. QOW 6 ROW IO
184. FOW 5 ROW 4
185. SA \# CONTAINMENT
186. SB * EXTINGUISHMENT
187. SC \# PEOPLE MOVEMENT
188. SG * GENERAL
189. COST FOW
PARAMETEG
TABLE 4 INDICES
190. CONSTRUCTION
191. INTERIOF FINISH CORP \& EX
192. INTERIOR FINISH ROOMS
193. CORRIDOFS PARTITIONS/WALLS
194. DOOFS TO COREIDOR
195. ZONE DIMENSIONS
196. VEOTICAL OPENINGS
197. HAZAFDOUS AREAS
198. SMOKE CONTROL
199. EMEFGENCY MOVEMENT ROUTES
200. MANUAL FIFE ALAPM
201. SMOKE DETECTION E ALARM
202. AUTOMATIC SPRINKLERS
203. FOW 4 QOW 5
204. QOW 6 ROW IO
205. FOW 5 ROW 4
206. SA \# CONTAINMENT
207. SB * EXTINGUISHMENT
208. SC \# PEOPLE MOVEMENT
209. SG * GENERAL
210. COST FOW
PARAMETEG
TABLE 4 INDICES
211. CONSTRUCTION
212. INTERIOF FINISH CORP \& EX
213. INTERIOR FINISH ROOMS
214. CORRIDOFS PARTITIONS/WALLS
215. DOOFS TO COREIDOR
216. ZONE DIMENSIONS
217. VEOTICAL OPENINGS
218. HAZAFDOUS AREAS
219. SMOKE CONTROL
220. EMEFGENCY MOVEMENT FOUTES
221. MANUAL FIFE ALAPM
222. SMOKE DETECTION E ALARM
223. AUTOMATIC SPRINKLERS
224. FOW 4 OOW 5
225. QOW 6 ROW IO
226. FOW 5 ROW 4
227. SA \# CONTAINMENT
228. SB * EXTINGUISHMENT
229. SC * PEOPLE MOVEMENT
230. SG * GENERAL
231. COST FOW
PARAMETEF
TABLE 4 INDICES
232. CONSTRUCTION
233. INTERIOF FINISH CORP \& EX
234. INTERIOR FINISH ROOMS
235. CORRIDOFS PARTITIONS/WALLS
236. DOOFS TO CORQIDOR
237. ZONE DIMENSIONS
238. VEOTICAL OPENINGS
239. HAZARDOUS AREAS
240. SMOKE CONTROL
241. EMEFGENCY MOVEMENT ROUTES
242. MANUAL FIFE ALAPM
243. SMOKE DETECTION E ALARM
244. AUTOMATIC SPRINKLERS
245. FOW 4 QOW 5
246. QOW 6 ROW IO
247. FOW 5 ROW 4
248. SA \# CONTAINMENT
249. SB * EXTINGUISHMENT
250. SC \# PEOPLE MOVEMENT
251. SG * GENERAL
252. COST FOW

| $\begin{gathered} +2 \\ \sim \\ N \end{gathered}$ | $00000$ | $\begin{aligned} & 0 \\ & 0 \end{aligned} 000$ | $\because 0 \%$ | $000$ | $\begin{array}{cccc} 0 & 0 & 0 \\ 0 & 0 \\ 0 & 0 & 0 \\ 1 & 1 & 1 \end{array}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $\stackrel{M}{N} \underset{1}{N}$ | $\bigcirc 0000$ | $00000$ | $\bigcirc 00$ | $\because 00$ | $\begin{array}{lll} 0 & 0 & 0 \\ 0 & 0 \\ j & \pm & \vdots \\ 1 & 1 & 1 \end{array}$ |
|  | $00000$ | $\begin{array}{r} 0 \\ -1 \end{array} 00$ | $\because 0:$ | $\bigcirc 00$ | $0000$ |
| N | $\because 0: 00$ | $0: 000$ | $\because \because 0$ |  | $\bigcirc 000$ |
| $\begin{array}{cc} \circ & m \\ i \\ 1 \end{array}$ | $\because 0: 00$ | $\because 0: 00$ | $\because:$ | $\because \because 0$ | $\begin{array}{r} 0 \because O \\ \bullet \\ \sim \\ 1 \end{array}$ |
| $\begin{array}{r} 0 \\ \hline 1 \\ 1 \end{array}$ | $00000$ | $00000$ | $\because 0 \%$ |  | $\begin{array}{rl} 0 & 0 \\ 1 & 0 \\ 0 & i \\ 1 & 1 \end{array}$ |
| $\stackrel{\infty}{-1}$ | $\because 0: 00$ | $\because 0: 00$ |  | $000$ | $\begin{array}{r} 0: 0 \\ 0 \\ 0 \\ i \end{array}$ |
| $\underset{i}{i}$ | $00000$ | $00000$ | $000$ | $000$ | $\begin{array}{lll} 0 & 0 & 0 \\ \dot{N} & \dot{N} \end{array}$ |
| $\because \begin{gathered} m \\ i \end{gathered}$ | $\because 0000$ | $00: 00$ | $\circ \circ 0$ | $\because 00$ | $0000$ |
| $\begin{array}{cc} \underset{\sim}{n} \\ i \\ i \end{array}$ | $\because 0000$ | $\because 0: 00$ | $\bigcirc 00$ | $\because 00$ | $\because 00:$ |
| $\pm \underset{n}{a}$ | $00000$ | $\bigcirc 0000$ | $\bigcirc 0$ | $0: 0$ | $\begin{array}{cccc} 0 & 0 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 1 \\ 1 & 1 & 1 \end{array}$ |
| $\stackrel{m}{m}$ | $\because \because 00$ | $00: 00$ |  | $\circ \circ 0$ | $\begin{array}{lll} 0 \\ \dot{N} & 0 \\ N \end{array}$ |
| $\underset{\sim}{N}$ | $\because 000 ?$ | $\circ \div 0: 0$ | $\because 0:$ | $000$ | $0000$ |
| $=\begin{gathered} N \\ 1 \end{gathered}$ | $0000 \%$ | $0 \because 0:$ | $000$ |  |  |
|  | $\cdots$ NM\&い | $0 \wedge \infty 00$ |  | $\pm \underset{\sim}{n}$ | $\underset{\sim}{\infty} \underset{\sim}{\infty}$ |



M

$$
\text { : } \because \underset{\sim}{\sim}
$$



| $\begin{gathered} m \\ \infty \end{gathered}$ | i | $\begin{aligned} & 0 \\ & i \end{aligned}$ | i | i | $\begin{aligned} & \circ \\ & \text { in } \end{aligned}$ | － | $0$ | $\bigcirc$ | ～ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0 |  |  |  |  | $\sim$ |  | ， |  |  |
| w |  | 11 | 11 | 11 | ${ }_{0}^{6}$ | ${ }^{1}$ | 11 | 11 | 11 |
| $m$ | $\stackrel{\sim}{0}$ | 0 | 0 | 0 | $\stackrel{N}{N}$ | $\stackrel{\sim}{0}$ | $\sim$ | $\sim$ | $\stackrel{\sim}{0}$ |
|  | ？ | ？ | $\bigcirc$ | $\bigcirc$ | ＊ | כ |  | 3 |  |
|  | $\stackrel{1}{\mathrm{a}}$ | 岩 | $\stackrel{1}{1}$ | $\stackrel{\square}{\square}$ |  | $\frac{1}{0}$ | $\stackrel{1}{1}$ | 1 | $\stackrel{1}{4}$ |
|  | 荭 | 世 | $\stackrel{\sim}{\sim}$ | $\stackrel{\rightharpoonup}{\underline{\alpha}}$ |  | $\stackrel{\rightharpoonup}{\underline{\alpha}}$ | $\stackrel{\text { r }}{ }$ | 5 | 4 |
|  | n | 0 | 0 | u | $>$ | u | n | is | in |
| $\vdash$ |  |  |  |  | － |  |  |  |  |
| 0 |  |  |  |  | $\stackrel{\square}{6}$ |  |  |  |  |
| U | $\bigcirc$ | 0 | $\bigcirc$ | $\omega$ | $\square$ | － | － | $\bigcirc$ | $\omega$ |
|  |  | $\bullet$ | － | $\bullet$ | ${ }_{4}$ | － | － | $\stackrel{\square}{\circ}$ |  |
| $\frac{1}{4}$ | $\infty$ | $\bigcirc$ | m | $\leftrightarrow$ | u | $\cdots$ | $\checkmark$ | m | 0 |
| $\stackrel{-}{5}$ | $\frac{11}{8}$ | 11 | U＇ | 11 | $\underline{W}$ | $\frac{11}{8}$ | 11 | ＂ | 110 |
| $\stackrel{1}{1}$ | $\cdots$ | $\backsim$ | $\checkmark$ | in | 4 | u | 0 | u | u |

altefnate




| FLLOOR 3 |  |
| :---: | ---: |
| VAFIABLE |  |
| 3 | 1.000 |
| 4 | .000 |
| 5 | .000 |
| 6 | 1.000 |
| 7 | .621 |
| 8 | .000 |
| 9 | .379 |
| 11 | 1.000 |
| 14 | .000 |
| 15 | .000 |
| 16 | 1.000 |
| 19 | 1.000 |
| 21 | .000 |
| 25 | .545 |
| 26 | .000 |
| 27 | .455 |
| 28 | .000 |
| 30 | .106 |
| 32 | .894 |
| 33 | .000 |
| 34 | 1.000 |
| 39 | 1.000 |
| 43 | 1.000 |
| 44 | .000 |
| 45 | .182 |
| 46 | .818 |
| 50 | 1.000 |

$\varepsilon$ พヨาย0ชd
$\varepsilon$ พヨาย0ชd PAFAMETES
INTERIOR FINISH CORR E EXIT
4．COFFIDORS PAFTITIONS／WALLS
dOOPS TO COFFIDOR
ZONE DIMENSIONS
vefitical openings
hazafdous areas
SMOKE CONTROL
emergency movement routes
automatic spfinklers

## APPENDIX D

## Listing of the Computer Programs


#### Abstract

The purpose of this section is to provide a complete listing of all programs (including subroutines) contained in the software package. Figure D.l, a flowchart outlining the inputs, outputs and interrelationships among programs and subroutines, has been provided to promote a better understanding of the software package. Since the number, length, and complexity of the various portions of the software package vars considerably, readers are encouraged to familiarize themselves with the flowchart prior to any serious study of the programming details of the software package. Since the MAIN program is considerably more involved than any of the subroutines listed in this appendix, those readers seeking a fuller knowledge of the package are encouraged to refer frequently to the MAIN program documentation section of Appendix B. Most of the subroutines in the remaining sections of this appendix can be easily read and understood by users having some familiarity with FORTRAN. It is worth noting that subroutine RVSMPX was developed independently of this project. It is a mathematical programming package which may be used to solve a wide variety of optimization problems. Those readers interested in a detailed description of subroutine RVSMPX are encouraged to obtain a copy of the report by Hall et al.


[^11]

FOR S 4F1 E-05/02/79-17:22:15 (.0)
MAIN PROGRAM

DIMENSION
DIMENSION
DIMENSION
DIMENSION
DIMENSION
DIMENSION
DIMENSION
DIMENSION
DIMENSION
DIMENSION
DIMENSION
DIMENSION
DIMENSION
DIMENSION


DIMENSION HOUT（6）
DIMENSION CS（13．5．5）
© ST COSTS＊PAFA，COLUMN，VECTOF LENGTH TABLE 6 ＊FACTOF，AGE，FLODF
TABL 4 ＊ROW 1 \＄FLODF．PROT，INDEX
TABLE 1 INPUT INDICES
TABLE 1 IFOW MAXIMA
TABLE 1 LINE HEADS
TABLE 1
a UNIT INPUT＊COLUMN，VECTOF LENGTH
๑ VECTOR LENGTH BY PARAVETER

DIMENSION AGE（2）
DIMENSION CON（3）
DATA（ $(1$ T4S $(1, j), 1=1,13), J=1,2)$ ，



```
    \(21.0 .1 \cdot 0.1 \cdot 0.1 \cdot 0.1 \cdot 0\).
    3 15000.0.1.0.1.0.1.0.1.0.
    \(419650 \cdot 0,1 \cdot 0,1,0,1 \cdot 0,1 \cdot 0\).
    \(51.0 .1 \cdot 0.1 \cdot 0,1 \cdot 0.1 \cdot 0\) /
    DATA ((CS( 7,I,J),J=1,5),I=1,5)
    1 1.0.1.0.1.0.1.0.1.0.
    \(21,0,1,0,1,0,1,0,1,0\).
    3 1.0.1.0.1.0.1.0.1.0.
    \(42 \cdot 7,450 \cdot 0,1250 \cdot 0,1 \cdot 0,1 \cdot 0\).
    \(53.9 .500 .0 .1300 .0,1.0,1.0\)
        DATA ((CS( \(8, I, J), J=1, E), I=1,5)\)
    1 1.0.1.0.1.0.1.0.1.0.
    \(21,0,1,0,1,0,1,0,1,0\),
    \(32,25,10.00,500,0,1300.0,1 \cdot 0\),
    4 1.0.1.0.1,0.1.0.1.0.
    \(52.25,10,00,500,0,1300 \cdot 0,1,0\)
        DATA \(((\operatorname{CS}(9, I, J), J=1,5), I=1, E)\)
    1 1.0.1.0.1.0.1.0.1.0.
    2 3.9.1400.0.1•0.1•0.1.0.
    \(31,0,1,0,1,0,1,0,1,0\),
    \(41,0,1,0,1,0,1,0,1,0\).
    \(51,0,1 \cdot 0,1,0,1,0,1 \cdot 0\)
        DATA \(((\operatorname{CS}(10, I, J), J=1,5), I=1,5)\)
    1 1.0.1.0.1.0.1.0.1.0.
    2 1.0.1•0,1•0.1•0.1.0.
    \(31 \cdot 0,1 \cdot 0,1 \cdot 0,1 \cdot 0,1 \cdot 0\),
    4 3.9.30.0.3900.0.1.0.1.0,
    \(51 \cdot 0,1 \cdot 0,1 \cdot 0,1,0,1 \cdot 0\)
        DATA \(((\operatorname{CS}(11, I, J), J=1,5), I=1,5)\)
    1 1.0.1.0.1.0.1.0.1.0.
    \(21 \cdot 0.1 \cdot 0.1 \cdot 0.1 \cdot 0.1 \cdot 0\).
    \(31000 \cdot 0,1,0,1,0,1 \cdot 0,1 \cdot 0\).
    \(41,0,1,0,1,0,1,0,1 \bullet 0\).
    5 1.0.1.0.1.0.1.0.1.0 /
    DATA ((CS(12,I,J),J=1, E), \(1=1,5)\)
    1 1.0,1.0,1•0,1•0,1•0.
    2 2.25,1,0,1,0,1,0,1.0,
    3 2.25,1.0.1.0.1.0.1.0,
    4 2. 25, 1.0, 1, 0, 1, 0, 1.0.
    \(52 \cdot 25,1 \cdot 0,1 \cdot 0,1 \cdot 0,1 \cdot 0\),
    DATA \(((\operatorname{CS}(13, I, J), J=1,5), I=1, E)\)
    1 1.0.1.0.1.0.1.0.1.0.
    2 2.00, 1.0.1.0.1.0,1,0,
    3 2.00, 1.0,1,0,1,0,1•0.
    4 2.0.2.25.1.0.1.0.1.0,
    5 2.0.1.0.1.0.1.0.1.0
    DATA LV / 1.2.2.2.4.1.3.4.2.3.1.1.2
\(C\) L(3) 3 MEANS GOOD ** 1 NUMERICAL BUT SOLVED ** 2 INFEASIBLE **3 UNBOUNDED
            ** 4 SYSTEM ERFOF *
\(X(83)\) SHOULD HAVE COST
    WRITE (6.910)
S10 FORMAT (•1 •)
        WRITE (6.911)
        WRITE (6.911)
        WRITE (6.911)
```



```
        WRITE (6.924)
    924 FOFMAT (. \({ }^{\circ}\)
```

190*
191*
192*
193*
194*
195*
196*
197* 198* 199* 200* 201* 202* 203* 204* 205* 206* 207* 208* 209* 210* 211* 212* 213* 214* 215* 216* 217* 218* 219* 220* 221* 222* 223* 224* 225* 226* 227* 228* 229* 230* 231* 232* 233* 234* 235* 236* 237* 238* 239* 240* 241* 242* 243* 244* 245* 246* 247*

```
    OO 100.0 I=1.5
    II=IT1M(I)
    WFITE (6.912) I,(HT1(I,J),J=1,2)
    912 FORMAT ('0'.11.'. •,AE,A2)
    WFITE (6,913) (HT1(I,J),J=3,4),(T1(I,J),J=1,I1)
    913 FORMAT (5X,AG,A2,2X,5F5.1)
1000 CONTINUE
    WRITE (6.914)
    WRITE (6.914)
    914 FORMAT ('0 ')
    WRITE (6.915)
    WRITE (6.915)
    WRITE (6.915)
    915 FORMAT ('+`.8X,'TABLE 6. MANDATOFY SAFETY FEQUIREMENTS')
    WFITE ( }\epsilon,924
    WRITE (6.91E)
    916 FORMAT (23X, 'CONTAINMENT', EX, 'EXTINGUISHMENT', 2X,'PEOPLE MOVEMENT'
        1)
        WRITE (6.917)
    917 FORMAT (27X,`SA`.15X,•SB',1EX,.SC•)
        WRITE (6.918)
    918 FORMAT (' ZONE LOCATION '.3(8X.'NEW EXIST'))
    WRITE (6,919) ((TG(I,J,1);J=1,2),I=1,3)
    919 FORMAT (0 FIRST FLDOR •.3(5X.2F6.1))
    WRITE (6,920) ((TG(I,J,2),J=1,2),I=1,3)
    920 FORMAT (: ABOVE IST FLODR',3(5X,2FE.1))
    WRITE (E.914)
    WRITE (6.914)
    WFITE (6.921)
    WRITE (6.921)
    WRITE (6.921)
    921 FORMAT (`+TABLE 4. PARAMETER VALUES WITH PRESCRIPTIVE INDICES*)
    WRITE (\epsilon.924)
    DO 1010 I=1.13
    11=1T4S(1, 2)-1T4S(1, 1)+1
    IF (I.NE.1) GO TO 1005
    WFITE (6,922) I.(HOAF(I,J),J=1,5),JPR(I)
    WRITE (6.927) (TAA(1,2,J).J=1,2).(T4A(1,2,J),J=1,2),(TAA(1,3,J),J
    1=1,3)
    WRITE (E,928) (T4A(2,2,J),J=1,2),(T4A(2,2,J),J=1,2),(T4A(2,3,J),J
    1=1.3)
    WRITE (6,929) (T4A(3,2,J),J=1,2),(T4A(3,2,J),J=1,2),(T4A(3,3,J),J
    1=1,3)
    WRITE (6,930) (T4A(4,2,J),J=1,2),(T4A(4,2,J),J=1,2),(T4A(4,3,J),J
    1=1,3)
    927. FORMAT (18X, FIRST FLOOR •, 12X,7FE.1)
    928 FORMAT (18X,.SECOND FLOOR',12X,7FE.1)
    929 FORMAT (18X, 'THIRD FLOOR •.12X,7FE.1)
    \varrho30 FORMAT (18X,.4TH & ABOVE •,12X,7FE,1)
    go TO 1010
    1005 WFITE (6.922) I,(HPAR(I,J),J=1,5 ),JこR(I),(G(I,J),J=1,II)
    922 FORMAT (13... .,5AG.I6,5F6.1)
    1010 CONTINUE
    BLANK=0 -
    STAR=0********
    PRES='PFPPPP.
    DO 20 I=1,21
    DO 10 J=1,61
                                    ๑ INITIALIZE SIMFLEX MATFIX
```

24 8\％ 249＊ 250＊ 251＊ 252＊ 253＊ 254＊ 255＊ 256\％ 257＊ 258＊ 259＊ 260＊ 2ヒ1ヵ 262＊ 263＊ 264＊ 265＊ 266＊ 267＊ 268＊ 269＊ 270＊ 271 ＊ 272＊ 273＊ 274＊ 275＊ 276＊ 277＊ 278＊ 279＊ 280＊ 281＊ 282＊ 283＊ 284＊ 285＊ 286＊ 287＊ 288＊ 289＊ 290＊ 291＊ 252＊
 294＊ 295＊ 296＊ 297＊ 298＊ 2¢ ＊$^{*}$ 300＊ 301＊ 302＊ 303＊
304＊
305＊
$A(I, J)=0.0$
10 CONTINUE
20 CONTINUE
DO 70 I $=1.13$－SIMPLEX ENTRIES BY ROW
A $(I, E 1)=1.0$ © FIGHT HAND SIDE
II＝IT4S（I．1）
$12=1 T 4 S(I, 2)$
oo $\in 0 \quad 13=11.12$
$J 1=I S T 4(13,2)$ D TABLE 4 ROW FUR SIMMLEX VAFIABLE I3
$A(I, I 3)=1.0$
IF（I．EQ．6）GO TO 30 （ NOT IN SI
IF（I•GE．9．AND．I．LE•12）GO TO 30 a NOT IN SI
$A(17, I 3)=G(I, J 1) * 1,0001$
30 IF（I•GE•2•AND．I•LE．7）
GO TO 40
© NOT IN S2
IF（I．GE．9．AND．I．LE．1．0）GO TO 40
－NOT IN S2
$A(18, I 3)=G(I, J 1) * 1,0001$
$40 \times 1=1.0$
IF（I．EQ．1．OF．I．EQ．3．OF．I．EQ．4）GO TO 50 a NOT IN 53
IF（I．EQ．8．OR．I．EQ．11）GO TO 50 ब NOT IN S3
IF（I．EQ．13）$\quad \times 1=.5$
$A(19, I 3)=X 1 * G(I, J 1) * 1.0001$
巨0 $A(20, I 3)=G(I, J 1) * 1,0001$
EO CONTINUE
70 CONTINUE
$I A=1$
100 READ（5．902）（IT4X（I）．I＝1．13）．（HOUT（I）．，I＝1．5）a CUECRENT INDICES I
WRITE（6．910）
I CHAN＝0
902 FOFMAT（1313．6A6）
$L(3)=0$
$A(14,54)=1.0$
$A(15.55)=1.0$
$A(16.56)=1.0$ a $\times 55-\times 41$
$A(14.14)=0.0$
A（ 4.54$)=0.0$
$A(15.37)=0.0$
$A(10.55)=0.0$
$A(16,14)=0.0$
$A(16.15)=0.0$
$A(16.10)=0.0$
A $(5,56)=0.0$
$A(17,57)=-1.0$
$A(18,58)=-1.0$
$A(19.59)=-1.0$
$A(20,60)=-1.0$
900 FORMAT（23I3）
903 FORMAT（••，2X，6A6．1）
READ（5．902）（IT1X（I），I＝1，E）
$R=1.0$
DO $1020 \quad I=1.5$
$\mathrm{I} 1=\mathrm{IT} 1 \times(\mathrm{I})$
IF（II．LE．O．OR．II．GT．IT1M（I））II＝ITIM（I）
ITIX（I）＝II
K＝R＊T1（I．I1）
1020 CONT INUE
DO $105 \quad I=1.60$
HFOFCE（I）＝－
105 CONTINUE

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FEAD (5.900) IPROB,NAGE,NCON,IFL,IDA
WRITE (E,973) IPROB,(HOUT(I),I=1, E), (ITIX(I),I=1,5)
573 FOFMAT ('+PFOBLEM•, I4,3X,6AE,3X, 'TABLE 1 INDICES •, 5I2)
IF (NAGE.NE,2) NAGE=1 D DEFAULT AGE OF BUILDING
IF (NCON•LT.1.OR.NCON.GT.3) NCON=1 @ DEFAULT PROTECTION
WPITE ( 6,971 ) IFFOB,AGE(NAGE), CON(NCON),IFL,IDA
971. FORMAT ('OPROBLEM•, I4,3X,AG,3X,AG,' FLOOR'.I3." PATIENTS•, IA) A $(17.26)=0.0$ a GRADE OPTIONS FOW 7 COLS 4 AND 5
$A(17,27)=0.0$
$A(19,26)=0.0$
$A(19.27)=0.0$
$A(20,26)=0.0$
$A(20,27)=0.0$
IF (IFL.EQ.1.OR.NCON•EQ.1) GO TO 140 © FIRST FLOOR OR UNPROTECTED
$A(17.26)=2.0$
$A(19.26)=2.0$
$A(20,26)=2.0$
$A(17,27)=3.0$
$A(19,27)=3.0$
$A(20,27)=3.0$
$140 \mathrm{~A}(17,51)=0.0$
$A\left(18, E_{1}\right)=0.0$
$A(19.51)=0.0$
$A(20.51)=0.0$
IF (NCON.EQ.1) GO TO 150 a UNPROTECTED TYPE OF CONSTRUCTION
$A(17.51)=2.0$
$A(18,51)=2 \cdot 0$
$A(20,51)=2.0$
$A(19,51)=1.0$
$150 \quad A(19.33)=0.0$
$A(20,33)=0.0$
IF (IPA•LT.31) GO TO 152
$A(19.33)=-2.0$
$A(20,33)=-2.0$
$152 A(14,61)=1.0$
$A(15,61)=1.0$
$A(16,61)=1.0$
IF (IT4X(5),GT.1) GO TO 154
$A(14,14)=-1.0$ a $-\times 51+\times 45=0$
$A(14,54)=1.0$
( ADD $\times 45$ TO FOW 4
A( 4.54$)=1.0$
A( 14,61$)=0.0$
C CONDITIONS ** AND •.. AFE NOT ACCOMMODATED IN THIS SECTION NOW 154 IF (NAGE.EQ.2) $F=0 \cdot 6 * F$ a EXISTING BUILDING
$I=I F L$
IF (I.GT.4) I=4
DO $165 \quad 11=1,3$
$A(17, I 1)=T 4 A(I, N C O N, I 1)$
$A(18,11)=T 4 A(I, N C O N, I 1)$
$A(20,11)=T 4 A(I, N C O N, I 1)$
G(1,II) =T4A(I,NCON,I1)
165 CONT INUE
IF (I.GT.1) I=2
A(17,61)=T6(1,NAGE,I)
$A(18,61)=T 6(2, N A G E, I)$
$A(19,61)=T \in(3, N A G E, I)$
$A(20.61)=R$
WFITE (6.923)
(A(I.61), I=17.20)


```
    WRITE (6.972)
```



```
    DO 110 I=1.13 @ OVER ALL TABLE 4 EOWS
    II=IT4S(I.1) @ FIFST SOMPLEX VARIABLE OF ROW I
    I2=IT4S(I.2) @ LAST SOMPLEX VAEIABLE OF DOW I
```

    \(13=11+1\) T4X(I)-1
    HFORCE (I3)=0 I •
    901 FORMAT (I3.5F8.0)
    I 3=1 \(1+J\) PR (I) - 1
    \(\operatorname{FLD}(30,6, \operatorname{HFORCE}(13))=F L D(30,6, P R E S)\)
    DO \(510 \quad J 1=1.5\)
    DO 500 J2=1. 5
    \(1 Q(J 1, J 2)=-1\)
    500 CONTINUE
510 CONTINUE @ FLAG BUFFER
$J 3=I T 4 X(I)+1$ - INDEX OF $1 S T$ TO READ
$J 4=12-11+1$ © INDEX OF LAST TO FEAD
K1 $=L V(I)$ a VECTOR LENGTH
$K 2=J 4-J 3+1$ - NUMBEF OF OLUMNS
K4=K2 D ASSUME ONE CAPD INDUT
513 J1=K1*K4
a WORDS IN READ
IF (J1•LE.12) GO TO 516 - ONE CAED INJUT ONLU
$K E=J 4$
$K 4=K 4-1$
J4= J4-1
GO TO 513
516 FEAD (5.965) J.( (IQ(J1,J2),J2=1,K1),J1=J3,J4)
9E5 FORMAT (13.1216)
IF (J3.GT.J4) IQ(J3.1) =-1
IF (J.NE.I) GO TO 540
IF (K2.EQ.K4) GO TO 520 a C NO SECOND CAFD
READ (5, $9 \in 5) \mathrm{J},((I Q(J 1, J 2), J 2=1, K 1), J 1=K 5, K 2)$ a READ TRAILER
IF (J.NE.I) GO TO 540
520 K4 $=1 \mathrm{~T} 4 \mathrm{X}$ (I)
J4 = $12-11+1$
DO $530 \quad \mathrm{~J} 2=1.6$
$I Q(K 4, J 2)=0$ a CLEAF CUFPENT STATE VECTOF
530 CONTINUE
DO 560 J $1=1, \epsilon$ ALL COLUMNS
IF (IQ(JI.1).GE,O) GO TO SEO a NO SUPFRESS FLAG -EITHEP IN OE COST
DO 550 J2=1 • $\quad$ F FLAG LOOD
IQ(J1, J2) = ¢ 9 S¢ 99999
550 CONTINUE
560 CONTINUE
J6=I 1 - 1 ST SIMPLEX VAFIABLE INDEX
DO 620 ग $2=1 . J 4$ © NUMBER OF COLUMNS IN INPUT
$x_{1}=0$ 。 0
IF (J2.EQ.IT4X(I)) GO TO 610
X1 = 999995999
IF (J2.LT.IT4X(I)) GO TO 610
IF (IQ(J2.1).GT.999¢99990) GO TO 610 - SUPPRESS FLAG
$590 \times 1=0.0$ - INITIAL COST STORAGE FOR SUM
DO $600 \mathrm{~J} 1=1, K 1$ ه ALL ELEMENTS OF VECTOR
X2=1Q(J2, J1)
$\mathrm{X}_{1}=\mathrm{X}_{1}+\mathrm{X}_{2} * \operatorname{CS}(\mathrm{I}, \mathrm{J} 2, \mathrm{~J} 1)$
EOO CONTINUE
$610 c(J 6)=X 1$

422*

```
            x1=x 1+.99
            L(J6)=x1
            J6=J6+1
620 CONTINUE
                            K2=12-I 1+1
                            WFITE (6,966) J,(HPAF(I,JE),JE=1,E), IT4X(I),JPR(I),
    1((IQ(J3.1), L(I1+J3-1)),J3=1,K2)
    IF (K1\bulletLE.1) GO TO 110 的 ONLLY ONE ELEMENT IN COST VECTOR
SEG FORMAT ('0',I2.'. ',4AG,A5,2I2,2X,5(1X,IG,1X,I7,2X))
    DO 630 Jl=2,K1
    WFITE (6,967) (IQ(J3,J1),J3=1,K2)
967 FORMAT (31X,5(11X,Ió))
630 CONTINUE
110 CONTINUE
    GO TO 640
540 WRITE (6,968) I
968 FORMAT ("OPARAMETER CARD*.I 3,' INCOFRECT - FUN ABORTED')
    STOP
640 X1=0.0 @ INITIALIZE SEAFCH FOF MAXIMUM COST
    DO 120 I= 1,53
    IF (C(I).GT.XI.AND.C(I).LT.999OES590) XI=C(I) D MAXIMUM LEGITIMATE CO
120 CONT INUE
    XI=20.0*X1 & MAGNITUDE OF SIMPLEX DUMMY COST
    DO 130 I=1,53
    IF (C(I).LT,O\bulletO\bulletOR\bulletC(I)\bulletGT\bulletXI) C(I)=XI a ZEELACE FLAGS WITH AETIFICIA
130 CONTINUE
    X2=.95* X1
                            \otimes LIMIT FOF OBJECTIVE FUNCTION
    Z(54)=x2
    IALT=0
    DO 5 I=1,14
    L(I)=0
    5 CONTINUE
    L(5)=1
    L(14)=1
    DO 170 I=1.53
    A(21,I)=-C(I)
    Z(I)=A(20,I)
170 CONTINUE
300 PEAD (5,960) I,I1,I2,I4 © FEAD CHANGE INPUT
970 FOCMAT (1X,A6,2I3,I7,413)
960 FORMAT (AG.2I3,I7)
    IF (I\bulletEQ.*SOLVE •) GO TO 370
    IF (I.EQ.*NEXT \bullet) GO TO 800
    IF (I.EQ.'END :) STOP
    IF (I.EQ.'CHANGE*) GO TO 320
    IF (I.NE.'FEQUIF.) GO TO 310
    J=11+16
    X3=12
    A(J,61)=(1,0+.01*X3)*A(J,61)
    GO TO 320
310 W&ITE (6,9E1) I,I1,I2,I4
961 FORMAT ('OUSER MOD INCORFECT , AE,2I3,IT," - FJN ABORTED')
    STOP
320 IALT=1
    IF (ICHAN.EQ.0) WRITE (6,9E2) IPROB,(HOUT(J4),J4=1,6)
SE2 FORMAT ('OMODIFIED PROBLEM',I4,3X,EA6)
    ICHAN=1
    IF (I.NE.'REQUIF') GO TO 325
```

```
    WRITE (6.963) I.II .X3.A(J.E1)
9€3 FORMAT ('O',AE, 13.FE.2.F11.2)
    GO TO 300
325 J1=1T4S(I1.1)
    s2=1 T4S(I1.2)
    J4=J1+12-1
    J=11
    IF (J4.LT.J1.OR.J4.GT.J2) GO TO 310 D INDEX OUT OF FANGE
    FLD(E,G,HFORCE(S4))=FLD(0,6, 'CCCCCC*)
    IF (I4.LT,O) GO TO 330 @ SUPPFESS
    IF (I4,EQ,0) GO TO 340 © FOPCE IN W OPIGINAL COST
    A(21,54)=-14 @ COST GIVEN ON INPUT
    C(J4)=14
    GO TO 360
330 A(21,J4)=-X1 @ COST AS INPUT
    C(54)=x1
    GO TO 360
340 IT 4 X (J)= 12
    DO 350 J3=J1.J2
    IF (J3.EQ.J4) GO TO 350 © INPUT STATE
    A(21,J3)=-X1
    C(J3)=x1
```



```
350 CONTINUE
360 WRITE (6,964) I,I1,I2,IT4X(J),(A(21,J3),J3=J1,J2)
```



```
    GO TO 300
370 ICHAN=0
    WRITE (6,963) I
    DO 375 I=1.13
    II=IT4S(I,1)+JPR(I)-1
    FLD(30,6, HFORCE(I1))=FLD(30,6,PRES)
375 CONTINUE
    L(1)=0
    L(2)=0
    L(3)=0
9 5 0 ~ F O F M A T ~ ( 1 X , 1 O F 1 2 . 2 ) ~ @ ~ * ~ * ~ * ~ * ~ * ~ * ~ * ~ * ~ * ~ * ~ * ~ * ~ * ~ * ~ * ~ * ~ * ~ * ~ * ~ * ~ * ~ * ~ * ~ * ~ * ~ * ~
    WRITE (6.910)
    CALL PRSMX (A,21,61,HPAF,5,1ST4,60,2,IALT)
172 CALL RVSMPX(A,21,B,23,21,E1,L,X,0,0,0)
    CALL FEASIB(A,61,21,X,L,X2)
    IF (L(3).GT.1) GO TO 280
    DO 180 I=1.150
    Y(I)=X(I)
180 CONT INUE
    x(81)=-x(81)
    DO 175 13=1,4
    X(13+81) =A(13+16,61)
    x(13+90)=-x(13+81)
175 CONTINUE
    X(90)=0.0
    00 178 I 3=1.53
    J=! -
    FLD(30,6,J)=FLD(30,6,HFORCE(13))
    IF (J.EQ.BLANK) GO TO 178
    15=13
    I6=IST4(13,1) @ TABLE 4 FOW FOF THIS VAFIABLE
    IT=ITAX(IE)-JPR(IG) a CUFFENT COLUMN MINUS DFESCEIOTIVE COLUMN
```

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## 590＊

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IF（I7．GT．0）IE＝15＋I7
QCURFENT BETTEF THA PFESCRIPTIVE
IF（ $\mathrm{X}(90$ ）•LT•0．0）GO TO 176 （ PFESCFIPTIVE COST IMPOSSIBLE
$x(90)=x(90)+C(I 5)$ © CUMULATIVE PRESCRIPTIVE COST
IF $(C(15), G E \cdot X 2) \quad X(90)=-1.0$
$17 \epsilon$
DO 177 I4 14,4 a ACCUMULATE GZADES FO？PFEESCFIPTIOM
$X(14+90)=X(14+90)+A(I 4+16,15)$
177 CONTINUE
178 CONT INUE
$X(150)=\times 2$
CALL PRSOL（IPFOB，IALT，C，Z，HFORCE，IST4，EO， $2, I T 4 X, X, I T 4 S, 13, H P A R, 21$
1．5．L．A．E1，HOUT）
IF（L（3）．GT．1）GO TO 280
IF（IALT．LT．O）GO TO 280
DO $230 \quad I=1.2$
＊13＊＊＊＊＊
$L(1)=0$
$L(2)=0$
$L(3)=0$
I ALT $=1+1000$
II＝IT4S（I，1）a FIFST SOMPLEX INDEX FOP THIS POW
12＝IT4S（I．2）－LAST SOMPLEX INDEX FOF THIS FOW
CALL MOTEST（HFORCE，I1，I2，I4）
IF（I4．NE．O）GO TO 230
$I 4=1 T 4 X(I)+I 1-1$ © SIMFLEX OF CUPRENT STATE
IF（X（I4）．GT．0．99）GO TO 230
200 DO 210 I $3=1,150$
$x(13)=Y(13)$
IF（I3．GT．53）GO TO 210
$Z(I 3)=A(20,13)$ © PRESENT GRADE VALUES
$A(21,13)=-C(13)$
FLD（ 0，6．HFORCE（13））＝FLD（ 0，E，BLANK）
$\operatorname{FLD}(12,12, \operatorname{HFORCE}(13))=F \operatorname{FL}(12,12, \operatorname{BLANK})$
$\operatorname{FLD}(30,6, \operatorname{HFOFCE}(13))=F L D(30, \in, B L A N K)$
210 CONTINUE
DO 220 I3＝11．12
IF（I3．EQ．I4）GO TO 220
$\operatorname{FLD}(0,6, \operatorname{HFORCE}(I 3))=F L D(0,6, S T A R)$
$A(21, I 3)=-X 1$
220 CONT INUE
CALL FVSMPX（A，21，B，23，21，61，L，X，0，1，0）
CALL FEASIB（A，61，21，X，L，X2）
IF（L（3）．GT．1）GO TO 230
$x(81)=-x(81)$
DO 225 13＝1，4
$x(13+81)=A(13+16.61)$
225 CONTINUE
$X(150)=X 2$
CALL PFSOL（IPROB，IALT，C，Z，HFORCE，IST4，EO，2，IT $4 X, X, I T A S, 13, H D A F, 21$
1．5．L．A．E1，HOUT）
230 CONTINUE
$1 A=2$
DO $270 \mathrm{I}=1.3$＊53＊＊＊＊＊
$14=1$ ST4（I，1）
$11=1 \mathrm{~T} 4 \mathrm{~S}(14,1)$
$12=1 \mathrm{~T} 4 \mathrm{~S}(14,2)$
CALL MOTEST（HFOFCE，11，12．I4）
IF（I4．NE．O）GO TO 270
$L(1)=0$
$L(2)=0$

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597*
E98*
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E0S*
E10*
\epsilon11*
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\epsilon13*
\epsilon14*
ヒ15*
\epsilon16*
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\epsilon18*
\epsilon19*
620*
\epsilon21*
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E55*
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```
    L(3)=0
```

    L(3)=0
    IALT=2000+10*IST4(I,1)+IST4(I,2)
    IALT=2000+10*IST4(I,1)+IST4(I,2)
    IF (C(I).GE.X2) GO TO 270
    IF (C(I).GE.X2) GO TO 270
    DO 240 II=1.150
    DO 240 II=1.150
    X(I1)=Y(I1)
    X(I1)=Y(I1)
    IF (I1.GT.53) GO TO 240
    IF (I1.GT.53) GO TO 240
    Z(I1)=A(20,I1) D PFESENT GRADE VALUES
    Z(I1)=A(20,I1) D PFESENT GRADE VALUES
    A(21, I1)=-C(11)
    A(21, I1)=-C(11)
    FLD( 0. 6.HFOFCE(I1))=FLD( 0, Є.BLANK)
    FLD( 0. 6.HFOFCE(I1))=FLD( 0, Є.BLANK)
    FLD(12,12,HFORCE(11))=FLD(12,12,BLANK)
    FLD(12,12,HFORCE(11))=FLD(12,12,BLANK)
    240 CONTINUE
240 CONTINUE
FLD(O,G,HFOFCE(I ))=FLD(O,\epsilon,STAR)
FLD(O,G,HFOFCE(I ))=FLD(O,\epsilon,STAR)
14=0
14=0
II=IST4(I.1) a TABLE 4 FOW
II=IST4(I.1) a TABLE 4 FOW
I5=IT4S(II,1) a INDEX OF FIFST SIMPLEX VAFIABLE THIS RD
I5=IT4S(II,1) a INDEX OF FIFST SIMPLEX VAFIABLE THIS RD
I2=IT4S(I1,2) a INDEX DF LAST SIMFLEX VAPIABLE THIS RO
I2=IT4S(I1,2) a INDEX DF LAST SIMFLEX VAPIABLE THIS RO
I6=15+IT4X(I1)-1
I6=15+IT4X(I1)-1
00 250 I3=15.12
00 250 I3=15.12
IF (I3.EQ.I6) GO TO 250
IF (I3.EQ.I6) GO TO 250
IF (C(I3).GT.X2) GO TO 250
IF (C(I3).GT.X2) GO TO 250
14=14+1
14=14+1
250 CONTINUE
250 CONTINUE
IF (I4.EQ.O) GO TO 270
IF (I4.EQ.O) GO TO 270
IF (Y(I).GE.0.05) GO TO 256
IF (Y(I).GE.0.05) GO TO 256
DO 253 13=15.12
DO 253 13=15.12
IF (I3.EQ.I) GO TO 253
IF (I3.EQ.I) GO TO 253
A(21,I3)=-X1 \& ALL COSTS EXCEPT IETH
A(21,I3)=-X1 \& ALL COSTS EXCEPT IETH
253 CONTINUE
253 CONTINUE
GO TO 260
GO TO 260
256 A(21.I)=-X1 a FOFCE OUT
256 A(21.I)=-X1 a FOFCE OUT
260 13=1 D DUMMY TO GET STATEMENT NUMBEF.
260 13=1 D DUMMY TO GET STATEMENT NUMBEF.
CALL FVSMPX(A,21,B,23,21,E1,L,X,0,1,0)
CALL FVSMPX(A,21,B,23,21,E1,L,X,0,1,0)
CALL FEASIB(A,61,21,X,L,X2).
CALL FEASIB(A,61,21,X,L,X2).
IF (L(3).GT.1) GO TO 270
IF (L(3).GT.1) GO TO 270
X(81)=-X(81)
X(81)=-X(81)
DO 2\epsilon5 I 3=1.4
DO 2\epsilon5 I 3=1.4
X(13+81)=A(13+16.61)
X(13+81)=A(13+16.61)
265 CONTINUE
265 CONTINUE
X(150)=X2
X(150)=X2
CALL PRSOL (IPROB,IALT,C,Z,HFORCE,IST4,EO,2,ITAX,X,ITAS,13,HPAR,21
CALL PRSOL (IPROB,IALT,C,Z,HFORCE,IST4,EO,2,ITAX,X,ITAS,13,HPAR,21
1.5.L.A.61.HOUT)
1.5.L.A.61.HOUT)
270 CONTINUE
270 CONTINUE
280 WRITE (6.910)
280 WRITE (6.910)
DO 290 I 1=1.150
DO 290 I 1=1.150
X(I1)=Y(II)
X(I1)=Y(II)
IF (II.GT.53) GO TO 290
IF (II.GT.53) GO TO 290
Z(I1)=A(20,11)
Z(I1)=A(20,11)
A(21.11)=-C(11)
A(21.11)=-C(11)
FLD( 0. 6.HFOP.CE(II))=FLD( 0. 6.BLANK)
FLD( 0. 6.HFOP.CE(II))=FLD( 0. 6.BLANK)
FLD(12,12,HFORCE(I1))=FLD(12,12,BLANK)
FLD(12,12,HFORCE(I1))=FLD(12,12,BLANK)
290 CONTINUE
290 CONTINUE
GO TO 300
GO TO 300
800 READ (5,815) I,I1,(X(I2),I2=1,E)
800 READ (5,815) I,I1,(X(I2),I2=1,E)
IF (I.GT.13) GO TO 100
IF (I.GT.13) GO TO 100
DO 810 12=1.5
DO 810 12=1.5
CS(I,I1,I2)=X(I2)
CS(I,I1,I2)=X(I2)
810 CONTINUE
810 CONTINUE
81E FORMAT (2I3.5F6.0)
81E FORMAT (2I3.5F6.0)
GO TO 800
GO TO 800
END

```
    END
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```
            SUBFOUTINE PRSOL (IPRJB,IALT,C,Z,HFORCE,IST4,N1,N2,IT4X,X,IT4S,N3,
            1 HPAR,N4,N5,L,A,NG,HOUT)
                DIMENSION C(1),Z(1),HFORCE(1),IST4(N1,N2),IT4X(1),X(1),IT4S(N3,NE
        1),HPAR(N4,N5),L(1),A(N4,N6),HOUT (1)
            SOLN=' SSSSSS*
            X(100)=0.0
            IF (IALT.NE.O.AND.IALT.NE.1) 
C CONDITIONS ** AND ... ARE NOT ACCOMMODATED IN THIS SECTION NOW
    IF (X(14)0LT00.05) GO TO 60 - X5I NOT IN BASIS SIDE CONDITICNS
    DO 10 I=10.13 © CLEAR BASIS AND GRADES FOR ROW 4 WHICH CANNOT BE
    X(I)=0.0 a FOUND WITH X51 IN THE SOLUTION. THIS IS CONCITI
    Z(I)=0.0 & * FROM TABLE 4
10 CONTINUE
    DO 20 I=1.4 a INITIALIZE CONSTRUCTED SURPLUS GRADES
    X(I+56)=-X(I+81) © INITIAL SURPLUS IS NEGATIVE OF REQUIREMENT
    20 CONTINUE
    DO 40 I=1.53 D OVER ALL VARIALBES
    DO 30 J=1.4 D OVER ALL REQUIREMENTS
    IF (A(J+16,I)OLTOD。OOOROA(J+1\epsilon,I).GT,0.0) X(J+56)=X(J+56)+X(I)*
    1Z(I)
    30 CONTINUE
    40 CONTINUE
    DO 50 I=57.60 - OVER SURPLUS VARIABLES
    IF (X(I).GE.-0.01) GO TO 50 a SOLUTION IS SSTILL VALID
    WRITE (6,916) ((X(J),X(J+25)),J=57,60) & WRITE INVALID SOLUTION
    RETURN
    5 0 ~ C O N T I N U E ~
    60 WRITE (6,900) IPROB,(HOUT(I),I=1,6),IALT
    WRITE (6.901)
    K=0
    IF (L(3).GE.2) GO TO }6
    DO 62 I=1.53
    IF (X(I)OLTOO.005) GO TO 62
    IF (C(I)\bulletLT•X(150)) GO TO 62
    L(3)=2
    GO TO 64
    6 2 ~ C O N T I N U E ~
    6 4 ~ I F ~ ( L ( 3 ) . E Q . 2 ) ~ W R I T E ~ ( 6 . 9 1 2 ) ~
    IF (L(3).EQ.3) WRITE (6.513)
    IF (L(3)0GEO4) WRITE (6.914)
    IF (L(3).GT.1) RETURN
    DO }80\quadI=1,5
    II=IST4(I.1) a ROW
    I2=IST4(I.2) a COLUMN
    IF (I2.NE.1) GOTO 70
    WRITE (6.909)
    CALL RHTAB (K,X)
                                WRITE (6,903) I1,(HPAR(I1,J),J=1,5) a FIRST OF T4 ROW
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83*

```
CALL RHTAB \((K, X)\)
```


## 65 I 3=3

```
70 IF (X(I).GT.0.05) FLD(12.6.HFORCE(I))=FLD(12.6.SOLN)
IF (HFORCE(I).EQ.' \({ }^{\prime}\) ) GO TO 80
IF (I 3oEGeO) GO TO 75
WRITE (6.909)
CALL RHTAB ( \(K, X\) )
75 13=1
XI \(=\mathrm{X}(\mathrm{I})\)
IF \((X I \bullet L E, 000) \quad X I=300\)
\(C I=C(I)\)
IF (C(I).GT.X(150)) CI=1.0E 15
WRITE (6.902) I.XI •IST4(I.2).CI , Z(I).HFORCE(I)
80 CONTINUE
IF \((x(81) \cdot L T \cdot 0.05) \quad\) IALT \(=-1\)
IF (X(81).LT.0.05) WRITE (6.910)
IF (L(3).EGO1) WRITE (6.911)
IF (L(3)。EQ.2) WRITE (6.912)
IF (L(3).EQ.3) WRITE (6.913)
IF (L(3).GE.4) WRITE (6.914)
FETURN
900 FCKMAT ('1.,19X,'PROBLEM'. I4.3X.6A6.3X,'ALTERNATE'.I5)
901 FORMAT ('OPARAMETER'. \(25 \times\).'VARIABLE TABLE 4 COST GRADE'/)
902 FORMAT ( \(\left.{ }^{\circ}+\cdot, 34 \mathrm{X}, \mathrm{I} 2, F 6,3,16,4 \mathrm{X}, F 8 \cdot 2, F 8,2,3 \mathrm{X}, \mathrm{A} 6\right)\)
903 FDRMAT (* •.I2.'. •. 5AE)
909 FORMAT (0 •)
919 FORMAT ('OINITIAL STATE PASSES ALL REQUIREMENTS')
911 FORMAT ("OBAD NUMERICAL PROBLEM * SMALL PIVOT USED*)
912 FORMAT ('ONON-FEASIBLE PROBLEM•)
913 FOFMAT ('OUNBOUNDED PROBLミM•)
914 FORMAT ('OSYSTEM EFROR')
915 FORMAT ("OILLEGAL STATE INCLUDED IN OPTIMUM SOLUTION * IGNORE') 916 FORMAT ('ONEXT ALTERNATE INVALID * FOW 4 AND 5 CONDITIONS * SURPLU
IS AND RHS: \(4(2 F 5,1,3 X))\) END
```

D. 3 Listing of Subroutine FEASIB (FEASIBility test)

SUBROUTINE FEASIB (A,I1,I2,X,L,X2)
DIMENSION A(I2,I1), X(1),L(1)
$\times 3=-\times 2$
$0010 \quad I=1.53$
IF (X(I)OLTOO.OO1) GO TO 10
IF (A(21.I).LT.X3) GO TO 20
10 CONTINUE
RETURN
$20 L(3)=2$
QETURN
END

```
    1*
    2*
    3*
    4*
    5*
    6*
    7*
    8*
    9*
10*
11*
12*
```

1*
2* 3* 4* 5* 6* 7*

```
        SUBROUTINE MOTEST (HFORCE.I1,I2,I3)
        DIMENSION HFORCE(1)
        J=! -
        13=0
        DO 10 I= 11.12
        F\perpD(6,6,J)=FLD(6,6,HFORCE(I))
        IF (J.EQ.' *.OR.J.EQ.' C |) GOTO 10
        I3=1
        RETURN
        10 CONTINUE
        RETURN
        END
```

D. 5 Listing of Subroutine RHTAB (Right Hand TABles)


```
    SUBROUTINE RVSMPX (A,MA,B,MB,MT,NT,L,X,TOLP,INV,KQP)
    2*
    c #######**********************#****************************************
    C
        DIMENSION A(MA,1),B(MB,1),L(1),X(1),IB(5),IP(5),PR(5)
    C
    C * * CHECK FOR NEGATIVE RIGHT HAND SIDES.
    C
    DO 10 I= 1,M
        IF (A(I,NT),GE.O) GO TO 10
        WFITE (6.1140)
        L(3)=2
        RETURN
        CONTINUE
    1 0
C
C * * SET UF CONSTANTS FOR LATER USE.
C
    N=NT-1
        M=MT-1
        N2=M+2
        INVC=M/2+5
        ML=L(1)
        MSMX=14
        MG =L(2)
        MPN=M+N
        MP 1 = M+1
        ME=M-ML-MG
        NMAX=N+ML+ME+2*MG
        ASTAR=0**
        ITP=N-KQP
        ITC=KQP+ML+MG
        L(2)=0
        IF (INV.GT.O) INV=1
C
C * * COMPUTE EPSILON AND CAPITAL EPSILONo
C
    EPS=TOLP
    IF (EPS.GT.O.O) GO TJ 30
    XX=1,OE-5
    IF (EPS.LT.0.0) XX=-EPS
    Y=0.0
    DO 20 I=1,M
        DO 20 J=1,N
        EPS=A(I,J)
        IF (EPS.LT.0.0) EPS=-EPS
20 Y=Y+EPS
    EPS=XX*Y/(M*N)
    IF (L(3).EQ.O) GO TO 50
    DO 40 I=3.MSMX
        L(I)=0
        L(4)=1
        L(5)=1
        L(8)=1
        L(12)=1
        L(13)=1
        L(MSMX)=1
        50 CEPS=10.0*EPS
        L(1)=0
        DO 60 I=1.M
        DC 60 J=1,N
        XX=ABS(A(I,J))
```

    63*
    64* C
    66* C
    67*
    68*
    65*
    70*
    71*
    72*
    73*
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10 5*
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117*
118*
119*

```
```

```
60 IF (XX.LT.EPS.AND.XX.GT.0.0) L(1)=L(1)+1
```

```
60 IF (XX.LT.EPS.AND.XX.GT.0.0) L(1)=L(1)+1
```

```
60 IF (XX.LT.EPS.AND.XX.GT.0.0) L(1)=L(1)+1
    IF (L(4),NEOO) WRITE (6.980) EPS.CEPS,L(1)
    IF (L(4),NEOO) WRITE (6.980) EPS.CEPS,L(1)
    IF (L(4),NEOO) WRITE (6.980) EPS.CEPS,L(1)
    65* . C * * SET UP LI(.)-VARIABLE TYPE INDICATOR.
    65* . C * * SET UP LI(.)-VARIABLE TYPE INDICATOR.
    65* . C * * SET UP LI(.)-VARIABLE TYPE INDICATOR.
```

    L1OFF=MSMX
    ```
    L1OFF=MSMX
```

    L1OFF=MSMX
    L2OFF=L1OFF+NMAX
    L2OFF=L1OFF+NMAX
    L2OFF=L1OFF+NMAX
        I=1
        I=1
        I=1
        DO 70 J=1,N
        DO 70 J=1,N
        DO 70 J=1,N
        L(L1OFF+I)=0
        L(L1OFF+I)=0
        L(L1OFF+I)=0
    70 I=I+1
70 I=I+1
70 I=I+1
IF (ML.EQ.O) GO TO 90
IF (ML.EQ.O) GO TO 90
IF (ML.EQ.O) GO TO 90
DO 80 J=1,ML
DO 80 J=1,ML
DO 80 J=1,ML
L(L1OFF+I)=1
L(L1OFF+I)=1
L(L1OFF+I)=1
I=I+1
I=I+1
I=I+1
IF (MG.EQ.O) GO TO 110
IF (MG.EQ.O) GO TO 110
IF (MG.EQ.O) GO TO 110
DC 100 J=1,MG
DC 100 J=1,MG
DC 100 J=1,MG
L(LIOFF+I)=2
L(LIOFF+I)=2
L(LIOFF+I)=2
L(LIDFF}+I+MG)=
L(LIDFF}+I+MG)=
L(LIDFF}+I+MG)=
I=I+1
I=I+1
I=I+1
IF (ME.EQ.O) GO TO 130
IF (ME.EQ.O) GO TO 130
IF (ME.EQ.O) GO TO 130
DO 120 J=1.ME
DO 120 J=1.ME
DO 120 J=1.ME
L(LICFF+I+MG)=3
L(LICFF+I+MG)=3
L(LICFF+I+MG)=3
120 I=I+1
120 I=I+1
120 I=I+1
C
C
C
C * * INITIALIZE B(...), THE EASIS INVEFSE, TO THE IDENTITY MATRIX.
C * * INITIALIZE B(...), THE EASIS INVEFSE, TO THE IDENTITY MATRIX.
C * * INITIALIZE B(...), THE EASIS INVEFSE, TO THE IDENTITY MATRIX.
C * * ALSO SET B(..M2), THE VALUES OF THE BASIC VARIABLESO
C * * ALSO SET B(..M2), THE VALUES OF THE BASIC VARIABLESO
C * * ALSO SET B(..M2), THE VALUES OF THE BASIC VARIABLESO
C
C
C
130 DD 150 I=1,M2
130 DD 150 I=1,M2
130 DD 150 I=1,M2
DO 140 J=1,M2
DO 140 J=1,M2
DO 140 J=1,M2
B(I,J)=0.0
B(I,J)=0.0
B(I,J)=0.0
IF (I.GT.M) GO TO 150
IF (I.GT.M) GO TO 150
IF (I.GT.M) GO TO 150
B(I,I)=1.0
B(I,I)=1.0
B(I,I)=1.0
B(I,M2)=A(I,NT)
B(I,M2)=A(I,NT)
B(I,M2)=A(I,NT)
CONTINUE
CONTINUE
CONTINUE
IF (INV.GT.O) GO TO 170
IF (INV.GT.O) GO TO 170
IF (INV.GT.O) GO TO 170
C
C
C
C * * INITIALIZE THE X'S. B(M2,.)-THE MULTIPLIERS, AND B(M2,M2)-THE
C * * INITIALIZE THE X'S. B(M2,.)-THE MULTIPLIERS, AND B(M2,M2)-THE
C * * INITIALIZE THE X'S. B(M2,.)-THE MULTIPLIERS, AND B(M2,M2)-THE
C * * ARTIFICIAL OBJECTIVE FUNCTION VALUEO FOR ANY ZERO-VALUED
C * * ARTIFICIAL OBJECTIVE FUNCTION VALUEO FOR ANY ZERO-VALUED
C * * ARTIFICIAL OBJECTIVE FUNCTION VALUEO FOR ANY ZERO-VALUED
C * * \&RTIFICIALS IN THE BASIS. RESET B(.,M2) TO O.
C * * \&RTIFICIALS IN THE BASIS. RESET B(.,M2) TO O.
C * * \&RTIFICIALS IN THE BASIS. RESET B(.,M2) TO O.
C
C
C
DC 160 I=1,NMAX
DC 160 I=1,NMAX
DC 160 I=1,NMAX
X(I)=-EPS/100.0
X(I)=-EPS/100.0
X(I)=-EPS/100.0
J=1
J=1
J=1
DO 200 I=1,NMAX
DO 200 I=1,NMAX
DO 200 I=1,NMAX
I I=L(LIOFF+I)
I I=L(LIOFF+I)
I I=L(LIOFF+I)
IF (II.EQ.O.OR.II.EQ.2) GO TO 200
IF (II.EQ.O.OR.II.EQ.2) GO TO 200
IF (II.EQ.O.OR.II.EQ.2) GO TO 200
IF (INVOGTOO) GO TO 180
IF (INVOGTOO) GO TO 180
IF (INVOGTOO) GO TO 180
X(I)=A(J,NT)
X(I)=A(J,NT)
X(I)=A(J,NT)
L(L2:OFF+J)=I
L(L2:OFF+J)=I
L(L2:OFF+J)=I
IF (I1,EQ.5) B(J.M2)=0.0
IF (I1,EQ.5) B(J.M2)=0.0
IF (I1,EQ.5) B(J.M2)=0.0
IF (I1.LT.3) GO TO 190
IF (I1.LT.3) GO TO 190
IF (I1.LT.3) GO TO 190
B(M2.J)=100
B(M2.J)=100
B(M2.J)=100
B(M2,M2)=B(M2,M2)+B(J,M2)
B(M2,M2)=B(M2,M2)+B(J,M2)
B(M2,M2)=B(M2,M2)+B(J,M2)
J=J+1
J=J+1
J=J+1
CCNTINUE
CCNTINUE
CCNTINUE
IF (INVOEQ.2) GO TO 820
IF (INVOEQ.2) GO TO 820
IF (INVOEQ.2) GO TO 820
C

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C
```

C

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```
```

C * * INITIALIZATIONS FOR PHASE I.

```
C * * INITIALIZATIONS FOR PHASE I.
C
C
            NA=0
            NA=0
            IPHASE=1
            IPHASE=1
            MOBJ=M2
            MOBJ=M2
            IT ER=0
            IT ER=0
            FI VM=1.0E28
            FI VM=1.0E28
            I MP=0
            I MP=0
            CBJ=-B(MDBJ,M2)
            CBJ=-B(MDBJ,M2)
            IF (INV.EQ.1) GO }7082
            IF (INV.EQ.1) GO }7082
C
C
C * * CHECK FOR IMMEDIATE BASIC FEASIBLE SOLUTION。
C * * CHECK FOR IMMEDIATE BASIC FEASIBLE SOLUTION。
    IF (MLOLTOM) GO TO 220
    IF (MLOLTOM) GO TO 220
C
C
C * * INITIALIZATIONS FOR PHASE II.
C * * INITIALIZATIONS FOR PHASE II.
C
C
210 MOBJ=MP1
210 MOBJ=MP1
            IPHASE=2
            IPHASE=2
            ITER=0
            ITER=0
            FI VM=1.0E28
            FI VM=1.0E28
            IMP=0
            IMP=0
            DBJ=-B(MOBJ.M2)
            DBJ=-B(MOBJ.M2)
C
C
C *+****+*+*+**+*+*+*+*+*+*+*+*+*+*+*+*+*+*+*+*+*
C *+****+*+*+**+*+*+*+*+*+*+*+*+*+*+*+*+*+*+*+*+*
C *+* STEPS 1 AND 2-COMPUTE THE C* TO GET S.*+*
C *+* STEPS 1 AND 2-COMPUTE THE C* TO GET S.*+*
C *t*+*+*+*+*+*+*+*+*+*+*+*+*+*+*+*+*+*+*+*+***
C *t*+*+*+*+*+*+*+*+*+*+*+*+*+*+*+*+*+*+*+*+***
C
C
220 ICPS X=0
220 ICPS X=0
230 NA=0
230 NA=0
            IF (INV.GT.O) GO TO 240
            IF (INV.GT.O) GO TO 240
            JS=0
            JS=0
            IF (L(2)OEQ*OOOROICPSXOEQO1) GC TO 240
            IF (L(2)OEQ*OOOROICPSXOEQO1) GC TO 240
            IF (L(2)/INVC*INVC.EQ.L(2)) INV=2
            IF (L(2)/INVC*INVC.EQ.L(2)) INV=2
            IF (INV.EQ.2) GO TO 130
            IF (INV.EQ.2) GO TO 130
C
C
C * * CALCULATE THE INDICATORS-C*.
C * * CALCULATE THE INDICATORS-C*.
C
C
240 B(MOBJ.MP1)=0.0
240 B(MOBJ.MP1)=0.0
    DO 340 J5=1,NMAX
    DO 340 J5=1,NMAX
                IF (INV.EQ.O) GE TO 250
                IF (INV.EQ.O) GE TO 250
                J=JS
                J=JS
                GO TO 260
                GO TO 260
                J=J5
                J=J5
                IF (X(J).GE.0.0) GO TO 340
                IF (X(J).GE.0.0) GO TO 340
                IF (KOP.EQ.O) GO TO 2\inO
                IF (KOP.EQ.O) GO TO 2\inO
                IF (JOLEOITCORNDOX(ITP+J)OGEOVOO) GD TO 340
                IF (JOLEOITCORNDOX(ITP+J)OGEOVOO) GD TO 340
                IF (J.GT.ITP.AND.J.LE.ITP+ITC.AND.X(J-ITP).GE.O.O) GO TO 340
                IF (J.GT.ITP.AND.J.LE.ITP+ITC.AND.X(J-ITP).GE.O.O) GO TO 340
                    260 JI=L(LIOFF+J)
                    260 JI=L(LIOFF+J)
                IF (J1.EQ.4) GO TO 340
                IF (J1.EQ.4) GO TO 340
                IF (Jl.EQ.O) GO TO 270
                IF (Jl.EQ.O) GO TO 270
                J2=J-N
                J2=J-N
                IF (J.GT.N+ML+MG) J2=J2-MG
                IF (J.GT.N+ML+MG) J2=J2-MG
C
C
C * * COMPUTE C* FOR SLACK. SURPLUS, OR ARTIFICIAL VARIABLESO
C * * COMPUTE C* FOR SLACK. SURPLUS, OR ARTIFICIAL VARIABLESO
C
C
XX=(-1)**(J1+1)*B(MOBJ,J2)
XX=(-1)**(J1+1)*B(MOBJ,J2)
IF (J1.EQ.3) }xX=XX-1.
```

IF (J1.EQ.3) }xX=XX-1.

```
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179* C
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E30*
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```
```

C * * COMPUTE C: FOR REAL VARIABLESO

```
C * * COMPUTE C: FOR REAL VARIABLESO
270 XX=0.0
270 XX=0.0
    IF (IPHASE.EQ.2) XX=A(MP1,J)
    IF (IPHASE.EQ.2) XX=A(MP1,J)
    DO 280 I=1.M
    DO 280 I=1.M
280 XX=XX+B(MOBJ,I)*A(I,J)
280 XX=XX+B(MOBJ,I)*A(I,J)
C
C
C * * TRANSFER IF INVERTING OR PIVOTING OUT ARTIFICIALS.
C * * TRANSFER IF INVERTING OR PIVOTING OUT ARTIFICIALS.
C
C
290 IF (INVOGT.O.OROICPSXOEQO1) GO TO 300
290 IF (INVOGT.O.OROICPSXOEQO1) GO TO 300
C
C
C * * TEST FOR MINIMUM C' IF DOING A NORMAL PIVOTO
C * * TEST FOR MINIMUM C' IF DOING A NORMAL PIVOTO
C
C
IF (XX,LE.B(MOBJ,MP1)) GO TO 340
IF (XX,LE.B(MOBJ,MP1)) GO TO 340
300 B(MOBJ,MP1) =XX
300 B(MOBJ,MP1) =XX
JS=J
JS=J
J3=J2
J3=J2
IF (INV.GT.O) GO TO }35
IF (INV.GT.O) GO TO }35
IF (ICPSX.EQ.O) GD TO 343
IF (ICPSX.EQ.O) GD TO 343
C
C
C * * IF TRYING TO PIVOT OUT ARTIFICIALS, CHECK THIS COLUMN. IF OK TO
C * * IF TRYING TO PIVOT OUT ARTIFICIALS, CHECK THIS COLUMN. IF OK TO
C * * ENTER, COMPUTE PIVOT ELEMENT. IF PIVOT IS BIG ENOUGH, PIVOTO
C * * ENTER, COMPUTE PIVOT ELEMENT. IF PIVOT IS BIG ENOUGH, PIVOTO
C * * CTHERWISE, CONTINUE CN TO NEXT CCLUMN.
C * * CTHERWISE, CONTINUE CN TO NEXT CCLUMN.
C
C
IF (XXOLTO-EPS) GO TO 340
IF (XXOLTO-EPS) GO TO 340
JS=J
JS=J
IF (J1.EQ.0) GO TO 310
IF (J1.EQ.0) GO TO 310
B(IR,MP1)=(-1)**(J1+1)*B(IR,J2)
B(IR,MP1)=(-1)**(J1+1)*B(IR,J2)
GO TO 330
GO TO 330
B(IR,MPI)=0.0
B(IR,MPI)=0.0
DO 320 K=1.M
DO 320 K=1.M
                                    B(IR,MP1)=B(IR,MP1)+B(IR,K)*A(K,JS)
                                    B(IR,MP1)=B(IR,MP1)+B(IR,K)*A(K,JS)
IF (B(IR,MP1)囵昭S) GO TO 350
IF (B(IR,MP1)囵昭S) GO TO 350
IF (B(IR,MPI)OGTO-EPS) GO TO 340
IF (B(IR,MPI)OGTO-EPS) GO TO 340
GO TO 350
GO TO 350
340 CONTINUE
340 CONTINUE
IF (ICPSX,EQ,1) GC TO 680
IF (ICPSX,EQ,1) GC TO 680
IF (B(MOBJ,MP1).LT.EPS) GO TO 580
IF (B(MOBJ,MP1).LT.EPS) GO TO 580
C
C
C *+*+*+*+*+*+*+*+*+*+*+*+*+*+******
C *+*+*+*+*+*+*+*+*+*+*+*+*+*+******
C *+* STEP 3-CALCULATE A( (I,S). *+*
C *+* STEP 3-CALCULATE A( (I,S). *+*
C *+*+*+*+*+*+*+*+*+*+*+*+*+*+*+*+*
C *+*+*+*+*+*+*+*+*+*+*+*+*+*+*+*+*
C
C
350 I1=L(LICFF+JS)
350 I1=L(LICFF+JS)
            IB(1)=0 X(
            IB(1)=0 X(
            IP(1)=JS
            IP(1)=JS
            IF (I1.EQ.O) GO TO 360
            IF (I1.EQ.O) GO TO 360
            IB(1)=' S(
            IB(1)=' S(
            IP(1)=JS-N
            IP(1)=JS-N
            IF (I1.LT.3) GO TO 360
            IF (I1.LT.3) GO TO 360
            IB(1)=0 A(
            IB(1)=0 A(
            IP(1)=IP(1)-ML-MG
            IP(1)=IP(1)-ML-MG
360 DC 410 I=1,MP1
360 DC 410 I=1,MP1
C
C
C * * COMPUTE REAL OBJECTIVE COST IF NOT ALREADY CCMPUTED.
C * * COMPUTE REAL OBJECTIVE COST IF NOT ALREADY CCMPUTED.
C
```

C

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```
```

                            IF (IOLTOMP1) GD TO 370
    ```
                            IF (IOLTOMP1) GD TO 370
                    IF (IPHASE.EQ.2) GO TO 410
                    IF (IPHASE.EQ.2) GO TO 410
B(I,MP1)=OcO
B(I,MP1)=OcO
IF (I1,EQ,O) B(I,MP1)=A(MP1,JS)
IF (I1,EQ,O) B(I,MP1)=A(MP1,JS)
IF (I1.EQ.3) B(I.,MP1)=-1.0
IF (I1.EQ.3) B(I.,MP1)=-1.0
GO TO 380
GO TO 380
c
c
C * * generate the rest df the columN.
C * * generate the rest df the columN.
C
C
370
370
B(I,MP1)=0.0
B(I,MP1)=0.0
I 2=L(L2OFF+I)
I 2=L(L2OFF+I)
IF (I2.EQ.-1) GO TO 380
IF (I2.EQ.-1) GO TO 380
IF (L(L1DFF+I2).EQ.5) GO TO 410
IF (L(L1DFF+I2).EQ.5) GO TO 410
IF (II-EGOO) GO TO 390
IF (II-EGOO) GO TO 390
B(I,MP1)=B(I,MP1)+(-1)**(II+1)*B(I,J3)
B(I,MP1)=B(I,MP1)+(-1)**(II+1)*B(I,J3)
GO TO 410
GO TO 410
DO 400 K=1,M
DO 400 K=1,M
                                    B(I,MP1)=B(I,MP1)+B(I,K)*A(K,JS)
                                    B(I,MP1)=B(I,MP1)+B(I,K)*A(K,JS)
CONT INUE
CONT INUE
4C0
4C0
4 1 0
4 1 0
c
c
C * * IF PIVOTING OUT AN ARTIFICIAL, SET THE VALUE OF THIS ARTIFICIAL
C * * IF PIVOTING OUT AN ARTIFICIAL, SET THE VALUE OF THIS ARTIFICIAL
C * * TD ZERO. IF IT IS GTEPS SET L(3)=1 (COMPUTATIONAL INCONSISTENCY)
C * * TD ZERO. IF IT IS GTEPS SET L(3)=1 (COMPUTATIONAL INCONSISTENCY)
C
C
IF (ICPSX.EQ.O) GO TO 420
IF (ICPSX.EQ.O) GO TO 420
IF (B(IR,M2).GT.EPS) L(3)=1
IF (B(IR,M2).GT.EPS) L(3)=1
B(IR,M2)=0.0
B(IR,M2)=0.0
GC TO 480
GC TO 480
C
C
C *+**+*+*+*+*+*+*+*+*+*+*+*+*+*+*+****+*+*
C *+**+*+*+*+*+*+*+*+*+*+*+*+*+*+*+****+*+*
C *+* STEP 4-FORM QUDTIENTS TO GET R. *+*
C *+* STEP 4-FORM QUDTIENTS TO GET R. *+*
C *+*+*+*+*+*+*+*+*+*+*+*+*+*+*+*+*+*+*+*
C *+*+*+*+*+*+*+*+*+*+*+*+*+*+*+*+*+*+*+*
C
C
420 IR=0
420 IR=0
            APS=1.0E28
            APS=1.0E28
            IF (INV.GT.O) APS=0.0
            IF (INV.GT.O) APS=0.0
            DO 450 I=1,M
            DO 450 I=1,M
                IF (INV.GT.O) GO TO 430
                IF (INV.GT.O) GO TO 430
                IF (B(I,MP1).LE.0.0) GO TO 453
                IF (B(I,MP1).LE.0.0) GO TO 453
                XX=B(I,M2)/B(I,MP1)
                XX=B(I,M2)/B(I,MP1)
                    IF (XX.GT.APS) GO TO 450
                    IF (XX.GT.APS) GO TO 450
                    IF (XX.LT.APS.OR.IR.EQ.O) GO TO 440
                    IF (XX.LT.APS.OR.IR.EQ.O) GO TO 440
                    IF (B(IR,MP1)OGEOB(I,MP1)) GO TO 450
                    IF (B(IR,MP1)OGEOB(I,MP1)) GO TO 450
                    GO TO 440
                    GO TO 440
C
C
C * * IF INVERTING, FIND THE LARGEST ABSOLUTE ELEMENT AMONG
C * * IF INVERTING, FIND THE LARGEST ABSOLUTE ELEMENT AMONG
C * * THOSE ROWS NOT ALREADY PIVOTED INo
C * * THOSE ROWS NOT ALREADY PIVOTED INo
C
C
430 IF (L(L2OFF+I).NE.-1) GO TO 450
430 IF (L(L2OFF+I).NE.-1) GO TO 450
                    XX=ABS(B(I,MP1))
                    XX=ABS(B(I,MP1))
                    IF (XX.LE.APS) GO TO 450
                    IF (XX.LE.APS) GO TO 450
440 IR=I
440 IR=I
                    APS=xx
                    APS=xx
450 CCNTINUE
450 CCNTINUE
            IF (IR.GT.O) GO TO 460
            IF (IR.GT.O) GO TO 460
C
C
C * * IF INVERTING, AND THERE IS NO PLACE TO PUT THIS
C * * IF INVERTING, AND THERE IS NO PLACE TO PUT THIS
C * * VARIABLE, SKIP IT AND TRY AGAIN LATERO
C * * VARIABLE, SKIP IT AND TRY AGAIN LATERO
C
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C

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294＊ 295＊ 29€＊ 297＊ 298＊ 299＊ 300＊ 301＊ 302＊ 303＊ 304＊ 305＊ 306＊ 307＊ 308＊ 309＊ 310＊ 311＊ ミ12＊ ミ13＊ 314＊ 315＊ 316＊ 317＊ 318＊ 319＊ 320＊ 321＊ 322＊ 323＊ 324＊
```

    IF (INV.GT.O) GO TO 863
    C
C * * THE PROBLEM IS UNBOUNDED.
C
L(3)=3
IX=1
IF (L(MSMX).EQ.O) RETURN
WRITE (6.1100) (ASTAR.I=1.120).JS
WRITE (6.1120) ITER.IPHASE.OBJ.(ASTAR.I=1.120)
GO TO 720
460 XX=ABS(B(IR,MP1))
IF (XX,GT.CEPS) GO TO 480
C
C * * IF PIVOT IS TOO SMALL, SET TO ZERO AND TRY AGAINO
C
IF (XX@LTOEPS) GO TO 470
C
C * * IF EPS.LT.PIVOT.LT.CEPS. PRINT WARNING ANO CONTINUE.
C
IF. (L(5),NEOO) WRITE (6.1020) ITER,IPHASE,B(IR,MP1)
GC TO 480
470 E(IR,MP1)=0.0
GO TO 420
C
C \#t*t*+*+*+**t***+*+*+*+*+*+*+*+*+*+*+*+*+*+*
C *+* STEP 5-CALCULATE NEW B(.,MT) AND X. *+*

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C
483 IF (INV.GT.O) GO TO 490
I1=L(L2OFF+IR)
I2=L(L1OFF+I1)
X(I1)=-EPS/100.0
IF (L(L1OFF+I1)\cdotEQ.3) L(LIOFF+11)=4
IB(2)=0 XC
IP(2)=II
IF (I2oEQ,O) GO TO 490
IB(2)=0 S(
IP(2)=I 1-N
IF (I20LT03) GO TO 490
I日(2)=! A( -
IP(2)=IP(2)-ML-MG
490 L(L2DFF+IR)=JS
B(IR,M2)=B(IR,M2)/E(IR,MP1)
CO 510 I=1.M2
IF (I*EQ*IR) GO TO 500
B(I,M2)=B(I,M2)-B(IR,M2) \#B(I,MP1)
IF (I.GT.M) GO TO 510
500 IF (INV.GT.O) GO TO 510
I1=L(L2OFF+I)
X(IL)=日(I,M2)
510 CONTINUE
IF (INV.EQ.2) GO TO }52
X(NMAX+1)=-B(MP1,M2)
OBJ=-日(MOBJ,M2)
C
C *+*+*+*+*+*+*+*+*+*+*+*+*+*+*+*+*+*+*+*+*+*+*+*+\#+*+*+*+\#+*+*
C *+* STEPS 6 AND 7-UPDATE THE INVERSE AND THE MULTIPLIERS. *+*
C }*+*+*+*+*+\#+*+*+\#+*+*+*+*+*+*+*+*+*+*+*+*+*+*+*+*+*+*+*+*+*+

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520 DO 530 K=1,M

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520 DO 530 K=1,M
                B(IR,K)=B(IR,K)/B(IR,MPI)
                B(IR,K)=B(IR,K)/B(IR,MPI)
530 CONTINUE
530 CONTINUE
    DO 550 I=1,M2
    DO 550 I=1,M2
        IF (I.EQ.IR) GO TO }55
        IF (I.EQ.IR) GO TO }55
        IF (I.EQ.M2.AND.IPHASE.EQ.2) GO TO 550
        IF (I.EQ.M2.AND.IPHASE.EQ.2) GO TO 550
        DO.540 K=1,M
        DO.540 K=1,M
                B(I,K)=B(I,K)-B(I,MPI)*B(IR,K)
                B(I,K)=B(I,K)-B(I,MPI)*B(IR,K)
                CONTINUE
                CONTINUE
        CONTINUE
        CONTINUE
        IF (INVOGT.O) GO TO }85
        IF (INVOGT.O) GO TO }85
        ITER=ITER+1
        ITER=ITER+1
        L(2)=L(2)+1
        L(2)=L(2)+1
C
C
C * * STORE THE MINIMUM PIVOT.
C * * STORE THE MINIMUM PIVOT.
C
C
        IF &B(IR.MPI).GT.PIVM) GO TO 560
        IF &B(IR.MPI).GT.PIVM) GO TO 560
        PIVM=B(IR,MPI)
        PIVM=B(IR,MPI)
        IMP=ITER
        IMP=ITER
560 II=5*(IPHASE-1)*4
560 II=5*(IPHASE-1)*4
c
c
C * * CHECK TO PRINT ITERATION SUMMARY.
C * * CHECK TO PRINT ITERATION SUMMARY.
C
C
        IF (L(II+1),EQ.0) GO TO 570
        IF (L(II+1),EQ.0) GO TO 570
        IF (ITER/L(II+1)*L(I1+1).NE.ITER) GO TO 570
        IF (ITER/L(II+1)*L(I1+1).NE.ITER) GO TO 570
        WRITE (6.1060) IPHASE,ITER,B(IR,MP1),OBJ,(IB(I),IP(I),I=1.2)
        WRITE (6.1060) IPHASE,ITER,B(IR,MP1),OBJ,(IB(I),IP(I),I=1.2)
C
C
C * * CHECK TG PRINT ITERATION BASISO
C * * CHECK TG PRINT ITERATION BASISO
C
C
570 IF (L(II+2).EQ.0) GO TO 220
570 IF (L(II+2).EQ.0) GO TO 220
    IF (ITER/L(II+2)*L(II+2).NE.ITER) GO TO 220
    IF (ITER/L(II+2)*L(II+2).NE.ITER) GO TO 220
        IX=2
        IX=2
        GO TC 720
        GO TC 720
C
C
C *+*+*+*+*+*+*+*+*+*+*
C *+*+*+*+*+*+*+*+*+*+*
C *+* END OF PHASE. *+*
C *+* END OF PHASE. *+*
C *+*+*+*+*+*+*+*+*+*+*
C *+*+*+*+*+*+*+*+*+*+*
C
C
580 IX=3
580 IX=3
        IF (IPHASE.EQ.2) GD TO 700
        IF (IPHASE.EQ.2) GD TO 700
        IQ=0
        IQ=0
C
C
C * * COMPUTE THE NUMBEf OF ARTIFICIALS STILL IN THE bASIS.
C * * COMPUTE THE NUMBEf OF ARTIFICIALS STILL IN THE bASIS.
C
C
            NA=0
            NA=0
            OO 590 J=1,NMAX
            OO 590 J=1,NMAX
                IF (L(LIOFF+J).NE.3) GO TO 590
                IF (L(LIOFF+J).NE.3) GO TO 590
                IF (X(J).GT.CEPS) GO TO 600
                IF (X(J).GT.CEPS) GO TO 600
                NA=NA+1
                NA=NA+1
                        CONTINUE
                        CONTINUE
            IF (B(MCBJ.M2)OGT*(ME+MG)*CEPS) GO YC 600
            IF (B(MCBJ.M2)OGT*(ME+MG)*CEPS) GO YC 600
C
C
C * * IF THE ARTIFICIAL OBJECTIVE FUNCTICN IS ACCEPTABLE BUT ARTIFICIALS
C * * IF THE ARTIFICIAL OBJECTIVE FUNCTICN IS ACCEPTABLE BUT ARTIFICIALS
C * * ARE STILL IN THE BASIS, GO TRY TO PIVOT THEM OUTO
C * * ARE STILL IN THE BASIS, GO TRY TO PIVOT THEM OUTO
C
C
    IF (NA.GT.O) GO TO 620
    IF (NA.GT.O) GO TO 620
C
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C

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C * * IF ND ARTIFICIALS ARE IN THE BASIS AND THE ARTIFICIAL OBJECTIVE

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C * * IF ND ARTIFICIALS ARE IN THE BASIS AND THE ARTIFICIAL OBJECTIVE
C * * FUNCTION IS NOT QUITE ZERO. PFINT WARNING OF ROUND-DFF ERROR.
C * * FUNCTION IS NOT QUITE ZERO. PFINT WARNING OF ROUND-DFF ERROR.
C
C
    IF (B(MOBJ,M2)OGTOEPS) GO TO 610
    IF (B(MOBJ,M2)OGTOEPS) GO TO 610
    GC TO }70
    GC TO }70
C
C
C * * THE PFOBLEM IS INFEASIBLE.
C * * THE PFOBLEM IS INFEASIBLE.
C
C
600 L(3)=2
600 L(3)=2
    IF (L(MSMX),EQ.O) RETURN
    IF (L(MSMX),EQ.O) RETURN
    WRITE (6.1090) (ASTAR,I=1.120).B(MOEJ,MP1)
    WRITE (6.1090) (ASTAR,I=1.120).B(MOEJ,MP1)
    WRITE (6,1120) ITER,IPHASE,OBJ.(ASTAR,I=1,120)
    WRITE (6,1120) ITER,IPHASE,OBJ.(ASTAR,I=1,120)
    IX=1
    IX=1
    GO TO 720
    GO TO 720
610 IF (L(MSMX).NE.0) WRITE (6.1130) (ASTAR.I=1,240)
610 IF (L(MSMX).NE.0) WRITE (6.1130) (ASTAR.I=1,240)
    L(3)=1
    L(3)=1
    GO TO 700
    GO TO 700
C
C
C * * FIND THE ARTIFICIAL STILL IN THE BASIS.
C * * FIND THE ARTIFICIAL STILL IN THE BASIS.
C
C
620 I Q1=0
620 I Q1=0
    DO 630 J=1,NMAX
    DO 630 J=1,NMAX
        J1=L(LIOFF+J)
        J1=L(LIOFF+J)
        IF (J1,EQ.3) IQ1=IQ1+1
        IF (J1,EQ.3) IQ1=IQ1+1
        IF (IQI.GT.IQ) GO TO 650
        IF (IQI.GT.IQ) GO TO 650
        CONTINUE
        CONTINUE
    630
    630
        IF (L(MSMX).NE.O) WRITE (6.970)
        IF (L(MSMX).NE.O) WRITE (6.970)
        IX=1
        IX=1
        GOTO 720
        GOTO 720
    C
    C
    C * * DETERMINE WHICH BASIC VARIABLE IT IS.
    C * * DETERMINE WHICH BASIC VARIABLE IT IS.
C
C
650 DO 660 IR=1.M
650 DO 660 IR=1.M
        I=L(L2OFF+IR)
        I=L(L2OFF+IR)
        IF (I.EQ.J) GO TO 670
        IF (I.EQ.J) GO TO 670
        CONTINUE
        CONTINUE
        GO TO 640
        GO TO 640
C
C
C * * SET &RTIFICIALS IN AT ZERO SWITCH. AND GO TRY TO PIVOT IT OUT.
C * * SET &RTIFICIALS IN AT ZERO SWITCH. AND GO TRY TO PIVOT IT OUT.
C
C
670 ICPSX=1
670 ICPSX=1
    GO TO 230
    GO TO 230
C
C
C * * INCREMENT IQ. THE COUNTER FOR CURRENT NUMBER OF ARTIFICIALS THAT
C * * INCREMENT IQ. THE COUNTER FOR CURRENT NUMBER OF ARTIFICIALS THAT
C * * CAN*T 日E PIVOTED OUT。
C * * CAN*T 日E PIVOTED OUT。
C
C
680 IQ=IQ+1
680 IQ=IQ+1
    IF (NA.GT.IQ) GO TO 620
    IF (NA.GT.IQ) GO TO 620
C
C
C * * COUNT AND CHECK THE ARTIFICIALS STILL IN THE BASISO
C * * COUNT AND CHECK THE ARTIFICIALS STILL IN THE BASISO
C
C
    JS=0
    JS=0
    DO 690 I=1.M
    DO 690 I=1.M
                II=L(L2OFF+I)
                II=L(L2OFF+I)
                IF (L(LIOFF+I1).NE.3) GO TO 690
                IF (L(LIOFF+I1).NE.3) GO TO 690
        JS=JS+1
        JS=JS+1
C
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C

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492* 493* 494* 495*

496* 497* 498* 499* 500* 591* 502* 503* 594* 505* 536* 507* 50 8* 509* 510* 511* 512* 513* 514*
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c
9
IF (JS.EQ.O) GO TO 640
IF (L(3).\&EQ.1) GO TO 610
C

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C *+* SUMMARY PRINT.
C *+*+*+*+*+*+*+*+*+*+*+*
C
700 I.1=5+(IPHASE-1)*4
IF (L(II+3).EQ.0) GO TO }71
WRITE (6.1050) (ASTAR.I=1.120).IPHASE,OBJ,ITER
IF (ITER.EQ.0) PIVM=0.0
WRITE (6,990) PIVM,IMP
IF (IPHASE.EQ.1) WRITE (6.1010) X(NMAX+1)
WRITE (6.1030) (ASTAR.I=1.120)
C
C *+*+*+***+*+*****+*+*
C *+* BASIS PRINT. *+*
C *+*+*******+*+*+*+*+*
C
710 IF (L(I1+4).EQ.0) GO TO 810
720 WRITE (6.1080)
DO 730 I 2=1.5
IB(I2)=0
PF(I2)=0.0
IP(I2)=0
I 3=0
I4=0
IQ1=0
CO 800 I 2=1.NMAX
IF (X(I2).LT.O.O.AND.X(I2).GT.-EPS) GO TO 800
IF (I4.EQOL(LIOFF+I2)) GO TO 740
IF (14.EGOIOANDOL(LIOFF+I2).EQ.2) GO TO }74
IF (I4.EQ.3.AND.L(LIOFF+I2).EQ.5) GO TO 740
IF (L(LIOFF+I2)OEQO4) GO TO 780
IQ1=1
GO TO 790
740 I4=L(L1OFF+I2)
IF (I3.EQ.5) GO TO 790
I 3=13+1
PR(I3)=X(I2)
I5=14+1
G0 T0 (750.760.760.770.780. 770). I5
IB(I3)=' X(
IP(I3)=I2
GO T0 800
IB(I3)=' S\ -
IP(I3)=I2-N
G0 TO 800
IB(I3)=0 A( .
IP(I.3)=I2-N-ML-MG

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780 L(3)=4

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780 L(3)=4
IX=1
IX=1
WFITE (6.970)
WFITE (6.970)
GO TO 800
GO TO 800
790 IF (I3.EQ.O) GO TO 740
790 IF (I3.EQ.O) GO TO 740
WRITE (6.1070) (IB(J),IP(J),PR(J),J=1,I3)
WRITE (6.1070) (IB(J),IP(J),PR(J),J=1,I3)
IF (IQ1.EQ.1) WRITE (6.1110)
IF (IQ1.EQ.1) WRITE (6.1110)
IQ1 =0
IQ1 =0
I 3=0
I 3=0
GO TO 740
GO TO 740
CONTINUE
CONTINUE
    IF (I3.GT.0) WRITE (6.1070) (IB(J).IP(J),PR(J),J=1.I3)
    IF (I3.GT.0) WRITE (6.1070) (IB(J).IP(J),PR(J),J=1.I3)
810 IF (IX.EQ.1) RETURN
810 IF (IX.EQ.1) RETURN
    IF (IX\odotEQ* 2) GO TO 220
    IF (IX\odotEQ* 2) GO TO 220
    IF (IPHASE.EQ.2) FETURN
    IF (IPHASE.EQ.2) FETURN
    GO TO 210
    GO TO 210
C
C
C #+*+*+*+*+*+*+*+*+*+*+*+*+*+*+*+*
C #+*+*+*+*+*+*+*+*+*+*+*+*+*+*+*+*
C *+* TOTAL INVERSION ROUTINE. *+*
C *+* TOTAL INVERSION ROUTINE. *+*
c*+*+*+*+*+*+*+*+*+*+*+*+*+*+*+*+*
c*+*+*+*+*+*+*+*+*+*+*+*+*+*+*+*+*
C
C
820 J=0
820 J=0
    DO 830 I=NT, NMAX
    DO 830 I=NT, NMAX
                IF (L(L1DFF+I).EQ.2) GO TO 830
                IF (L(L1DFF+I).EQ.2) GO TO 830
                J=J+1
                J=J+1
                L(L2OFF+J)=-1
                L(L2OFF+J)=-1
                IF (X(I)&LTOOOO) GO TO 83J
                IF (X(I)&LTOOOO) GO TO 83J
                X(I)=-EPS/100.0
                X(I)=-EPS/100.0
                L(L2DFF+J)=I
                L(L2DFF+J)=I
                CONTINUE
                CONTINUE
840 I4=0
840 I4=0
    JS=0
    JS=0
    GO TO }86
    GO TO }86
C
C
C * * I4=1 INDICATES THAT A PIVDT WAS PERFORMED.
C * * I4=1 INDICATES THAT A PIVDT WAS PERFORMED.
850 I4=1
850 I4=1
    X(JS)=-EPS/100.0
    X(JS)=-EPS/100.0
860 I5=JS
860 I5=JS
    IF (I5.EQ.NMAX) GD TO 880
    IF (I5.EQ.NMAX) GD TO 880
C
C
C * * FOR EACH X(I) THAT IS NON-NEGATIVE, GO TRY TO PUT IT IN THE BASIS.
C * * FOR EACH X(I) THAT IS NON-NEGATIVE, GO TRY TO PUT IT IN THE BASIS.
C
C
    I5=15+1
    I5=15+1
    CO 870 JS=15,NMAX
    CO 870 JS=15,NMAX
                IF (X(JS).GE.0.0) GD TO 220
                IF (X(JS).GE.0.0) GD TO 220
870 CONTINUE
870 CONTINUE
C * * IF AT LEAST ONE FIVOT OPERATION WAS DONE, GO THFOUGH X AGAIN.
C * * IF AT LEAST ONE FIVOT OPERATION WAS DONE, GO THFOUGH X AGAIN.
C
C
88) IF (I40EG01) GO TO }84
88) IF (I40EG01) GO TO }84
    DO 890 J=1,NMAX
    DO 890 J=1,NMAX
890 X(J)=-EPS/10000
890 X(J)=-EPS/10000
C
C
C * * SET X TO PRJPER VALUES AND CHECK FOR FEASIBILITY.
C * * SET X TO PRJPER VALUES AND CHECK FOR FEASIBILITY.
C
C
    I 5=0
```

    I 5=0
    ```

584\% 585* 586* 587* 588* 589* 590* 591* 592* 593* 594* 595* 596* 597* 598* 59 \% * 600* E01* EO2* 603* 604* 605* 606* 607* 60 8* 609* 610* 611* 612* E13* 614* 615* 616* 617* 61 8* €1 \(9 *\) 620* 621* 6こ2* 623* 624* 625* 626* 627* 628* 629* 630* €31* 632* 63ミ* 634* 635* €36* 637* 638* 639* 640* 641*
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            DO 910 I=1.M
    ```
            DO 910 I=1.M
                IF (B(I.M2).LT.-EPS) I5=1
                IF (B(I.M2).LT.-EPS) I5=1
                IF (B(I,M2).LT.O०OOAND.B(I.M2)OGE.-EPS) B(I.M2)=0.0
                IF (B(I,M2).LT.O०OOAND.B(I.M2)OGE.-EPS) B(I.M2)=0.0
                    I1=L(L2OFF+I)
                    I1=L(L2OFF+I)
                    IF (Il.LT.O) GO TO 900
                    IF (Il.LT.O) GO TO 900
            X{I1)=B(I.M2)
            X{I1)=B(I.M2)
                GO TO 910
                GO TO 910
                15=1
                15=1
                CONTINUE
                CONTINUE
            IF (IS.EQ.O) GO TO 920
            IF (IS.EQ.O) GO TO 920
C
C
c * * INFEASIBLE AFTER INVERSION*
c * * INFEASIBLE AFTER INVERSION*
C
C
    L(3)=2
    L(3)=2
    IF (L(MSMX).EQ.O) RETURN
    IF (L(MSMX).EQ.O) RETURN
    IF (INV.EQ.1) WRITE (6.1040) (ASTAR.I=1.120)
    IF (INV.EQ.1) WRITE (6.1040) (ASTAR.I=1.120)
    IF (INV.EQ.2) WRITE (6,1000) (ASTAR,I=1,120)
    IF (INV.EQ.2) WRITE (6,1000) (ASTAR,I=1,120)
    WRITE (6.1120) ITER,IPHASE,OBJ,(ASTAR,I=1.120)
    WRITE (6.1120) ITER,IPHASE,OBJ,(ASTAR,I=1.120)
    IX=1
    IX=1
    GO TO 720
    GO TO 720
C
C
C * * IF INVERTING BECAUSE OF INITIAL BASIS. FIX UP LI(.).
C * * IF INVERTING BECAUSE OF INITIAL BASIS. FIX UP LI(.).
920 IF (INV.EOo2) GO TO }96
920 IF (INV.EOo2) GO TO }96
    I5=N+ML+MG+1
    I5=N+ML+MG+1
    IF (IS.GT.NMAX) GO TO 950
    IF (IS.GT.NMAX) GO TO 950
    EO 930 J=I5.NMAX
    EO 930 J=I5.NMAX
                L(LIOFF+J)=4
                L(LIOFF+J)=4
        I 5=0
        I 5=0
        DO 940 J=1.M
        DO 940 J=1.M
            J1=L(L2OFF+J)
            J1=L(L2OFF+J)
            IF (L(LlOFF+J1).NE.4) GO T0 }94
            IF (L(LlOFF+J1).NE.4) GO T0 }94
            L(L1OFF+J1)=3
            L(L1OFF+J1)=3
            15=1
            15=1
940 CONTINUE
940 CONTINUE
    IF (IS.EQ.1) GO TO 960
    IF (IS.EQ.1) GO TO 960
950 INV=0
950 INV=0
    GO TO 210
    GO TO 210
    INV=0
    INV=0
    GO TO 240
    GO TO 240
C
C
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C
97
97
FORMAT ('OSYSTEM ERROR- COMPUTATIONAL IMPOSSIBILITY')
FORMAT ('OSYSTEM ERROR- COMPUTATIONAL IMPOSSIBILITY')
FORMAT ("EPSILON = 'G130G." CAPITAL EPSILON = 'G1306." "IS*
FORMAT ("EPSILON = 'G130G." CAPITAL EPSILON = 'G1306." "IS*
    2 ' NON-ZERO ENTRIES ARE EFFECTIVELY EQUAL TO ZERO.')
    2 ' NON-ZERO ENTRIES ARE EFFECTIVELY EQUAL TO ZERO.')
G90 FORMAT (" ** 14X'MINIMUM PIVOT WAS*G12.5.' AT ITERATION*I4.
G90 FORMAT (" ** 14X'MINIMUM PIVOT WAS*G12.5.' AT ITERATION*I4.
    2 •.'57X***)
    2 •.'57X***)
1000 FORMAT (//////" •120A1/" **118X**•/
1000 FORMAT (//////" •120A1/" **118X**•/
    2 * ERROR - THE PROBLEM IS INFEASIBLE. INFEASIBILITY INDICATED
    2 * ERROR - THE PROBLEM IS INFEASIBLE. INFEASIBILITY INDICATED
    3DURING RE-INVERSION OF THE BASIS MATRIX0'16X**')
    3DURING RE-INVERSION OF THE BASIS MATRIX0'16X**')
1010 FORMAT (1H+65X`REAL OBJECTIVE FUNCTION =`G1508)
1010 FORMAT (1H+65X`REAL OBJECTIVE FUNCTION =`G1508)
1020 FORMAT ('O* * WARNING * * SMALL PIVOT ELEMENT AT ITERATION'I4.
1020 FORMAT ('O* * WARNING * * SMALL PIVOT ELEMENT AT ITERATION'I4.
    2 ' OF PHASE`I2.'. PIVOT =`G1407)
    2 ' OF PHASE`I2.'. PIVOT =`G1407)
1030 FORMAT (* *`118X`*`/! •120A1)
1030 FORMAT (* *`118X`*`/! •120A1)
1040 FGRMAT (/////" •120A1/" **118x***/
1040 FGRMAT (/////" •120A1/" **118x***/
    2 * EFROR - THE VARIABLES SPECIFIED AS COMPRISING AN INITIAL SOL
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    2 * EFROR - THE VARIABLES SPECIFIED AS COMPRISING AN INITIAL SOL
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    \XiUTION DO NOT FORM A BASIC FEASIBLE SOLUTION.'12X**')
    ```
    \XiUTION DO NOT FORM A BASIC FEASIBLE SOLUTION.'12X**')
1050 FORMAT (/////' •120A1/' **118X'*'/! *'14X'END OF PHASE'I2.
1050 FORMAT (/////' •120A1/' **118X'*'/! *'14X'END OF PHASE'I2.
    2.. OBJECTIVE FUNCTION =`G18.8.4X'THERE WERE'I4,
    2.. OBJECTIVE FUNCTION =`G18.8.4X'THERE WERE'I4,
    3 ! ITERATIONS.'17X'**)
    3 ! ITERATIONS.'17X'**)
1060 FORMAT ////'OPHASE*,IE," ITERATION*.I 4,*O PIVOT=*,G1306.
1060 FORMAT ////'OPHASE*,IE," ITERATION*.I 4,*O PIVOT=*,G1306.
    2 " QBJECTIVE FUNCTION='G15.8," ",A3.I3.') ENTERED THE BASIS.",
    2 " QBJECTIVE FUNCTION='G15.8," ",A3.I3.') ENTERED THE BASIS.",
    3 A3.I3.') LEFT.')
    3 A3.I3.') LEFT.')
    FOFMAT (5(3XA3,I 3,0)=0F1206))
    FOFMAT (5(3XA3,I 3,0)=0F1206))
    FORMAT ('OBASIC VARIABLES*/)
    FORMAT ('OBASIC VARIABLES*/)
    FORMAT (/////" '120A1/" *`118X***/
    FORMAT (/////" '120A1/" *`118X***/
    2 * EFRCR - THE PROBLEM IS INFEASIBLE. THE CONSTRAINTS ASSOCIATE
    2 * EFRCR - THE PROBLEM IS INFEASIBLE. THE CONSTRAINTS ASSOCIATE
    3D WITH THE ARTIFICIAL VARIABLES BELOW ARE INCONSISTENT。*!/
    3D WITH THE ARTIFICIAL VARIABLES BELOW ARE INCONSISTENT。*!/
    4 * IF NCNE APPEAR, NUMERICAL DIFFICULTIES HAVE BEEN ENCCUNTERED
    4 * IF NCNE APPEAR, NUMERICAL DIFFICULTIES HAVE BEEN ENCCUNTERED
    5. THE LARGEST ENTRY IN THE OBJECTIVE FUNCTION ROW`,7X, **!/
    5. THE LARGEST ENTRY IN THE OBJECTIVE FUNCTION ROW`,7X, **!/
    6.* IS *.G12.5.131X,**')
    6.* IS *.G12.5.131X,**')
1100 FORMAT (/////" '120A1/" *'118***!/
1100 FORMAT (/////" '120A1/" *'118***!/
    2 * * EFRROR - THE PROBLEM IS UNGDUNDED. THE VARIABLE X&`I3,
    2 * * EFRROR - THE PROBLEM IS UNGDUNDED. THE VARIABLE X&`I3,
    3 •) CAN ASSUME AN ARBITRARILY LAFGE VALUE, THEREBY YIELDING* 7X***/
    3 •) CAN ASSUME AN ARBITRARILY LAFGE VALUE, THEREBY YIELDING* 7X***/
    4 * * AN ARBITRARILY LARGE VALUE OF THE OBJECTIVE FUNCTION.`63X***
    4 * * AN ARBITRARILY LARGE VALUE OF THE OBJECTIVE FUNCTION.`63X***
    5)
    5)
1110 FORMAT (1H)
1110 FORMAT (1H)
1120 FORMAT (***118X***/" * THE ERPOR WAS DETECTED AT ITERATION'I4,
1120 FORMAT (***118X***/" * THE ERPOR WAS DETECTED AT ITERATION'I4,
    2 OF PHASE'I2.
    2 OF PHASE'I2.
    3 *.AT THAT TIME THE OBJECTIVE FUNCTION VALUE WAS'G1508.4X***/
```

    3 *.AT THAT TIME THE OBJECTIVE FUNCTION VALUE WAS'G1508.4X***/
    ```


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    5.120A1)
    ```
    5.120A1)
1130 FORMAT (////' 120A1/" *'118X**'/
1130 FORMAT (////' 120A1/" *'118X**'/
    2 * WARNING - COMPUTATIONAL INCCNSISTENCY INDICATED AT THE END C
    2 * WARNING - COMPUTATIONAL INCCNSISTENCY INDICATED AT THE END C
    3F PHASE 10 THE ALGORITHM WILL CONTINUE WITH PHASE 2.04X'**/
    3F PHASE 10 THE ALGORITHM WILL CONTINUE WITH PHASE 2.04X'**/
    4 * * EUT THE USER IS ADVISED TO CRITICIZE THE RESULTS.*67X***/
    4 * * EUT THE USER IS ADVISED TO CRITICIZE THE RESULTS.*67X***/
    5**!118X***/" 120A1)
    5**!118X***/" 120A1)
1140 FORMAT ('O* * AT LEAST ONE ELEMENT OF THE RIGHT HAND SIDE COLUMN
1140 FORMAT ('O* * AT LEAST ONE ELEMENT OF THE RIGHT HAND SIDE COLUMN
    2IS LESS THAN ZEROO SUBROUTINE TEFMINATESO')
    2IS LESS THAN ZEROO SUBROUTINE TEFMINATESO')
c
c
    END
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    END
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    SUBRQUTINE PRSMX (A,IA,IB,HPAR,IC,IST4,ID,IE,IALT)
    ```
    SUBRQUTINE PRSMX (A,IA,IB,HPAR,IC,IST4,ID,IE,IALT)
    DIMENSION A(IA,IB),HPAF(IA,IC),IST4(ID,IE)
    DIMENSION A(IA,IB),HPAF(IA,IC),IST4(ID,IE)
    DIMENSIDN L(61)
    DIMENSIDN L(61)
    DO 5 I=1,61
    DO 5 I=1,61
    L(I)=A(21,I)
    L(I)=A(21,I)
    5 CJNTINUE
    5 CJNTINUE
    K=1
    K=1
    IF (IALToNEOO&ANDoIALTONEO1) K=17
    IF (IALToNEOO&ANDoIALTONEO1) K=17
    WRITE (6.900) (II).I= 1.10)
    WRITE (6.900) (II).I= 1.10)
    WRITE (6,901) ((IST4(I,1).IST4(I,2)),I=1,10)
    WRITE (6,901) ((IST4(I,1).IST4(I,2)),I=1,10)
    DO 10 I=K,21
    DO 10 I=K,21
    IF (I.EQ. 6.OR.I.EQ.11.OR.I.EQ.14) WRITE (E.933)
    IF (I.EQ. 6.OR.I.EQ.11.OR.I.EQ.14) WRITE (E.933)
    IF (I.EQ.17.OR.I.EQ.21) WRITE (6.933)
    IF (I.EQ.17.OR.I.EQ.21) WRITE (6.933)
    IF (IoNEO21)
    IF (IoNEO21)
    IWRITE (6,902) I,{HPAR(I,J),J=1,5),(A(I,J),J=1,10),I
    IWRITE (6,902) I,{HPAR(I,J),J=1,5),(A(I,J),J=1,10),I
    IF (I.EQ.21) WRITE (6,942) I.(HPRR(I.J),J=1,5),(L.(J),J=1,10).I
    IF (I.EQ.21) WRITE (6,942) I.(HPRR(I.J),J=1,5),(L.(J),J=1,10).I
10 CONTINUE
10 CONTINUE
    WRITE (6.9.31)
    WRITE (6.9.31)
    IF (K.EQ.1) WRITE (6,932)
    IF (K.EQ.1) WRITE (6,932)
    WRITE (6.910) ((I),I=11,24)
    WRITE (6.910) ((I),I=11,24)
    WRITE (6,911) ((IST4(I,1),IST4(I,2)),I=11,24)
    WRITE (6,911) ((IST4(I,1),IST4(I,2)),I=11,24)
    CO 20 I=K,21
    CO 20 I=K,21
    IF (IoEQo GoDRoI@EQoIIoORoIoEQo14) WRITE (E.933)
    IF (IoEQo GoDRoI@EQoIIoORoIoEQo14) WRITE (E.933)
    IF (IOEQ*17.OR.I.EQ.21) WRITE (6.933)
    IF (IOEQ*17.OR.I.EQ.21) WRITE (6.933)
    IF (I.NE.21)
    IF (I.NE.21)
    1WRITE (E,912) I,(A(I,J),J=11, ट4):I
    1WRITE (E,912) I,(A(I,J),J=11, ट4):I
    IF (I0EG021) WRITE (6,952) I,(L(J),J=11,24),I
    IF (I0EG021) WRITE (6,952) I,(L(J),J=11,24),I
20 CONTINUE
20 CONTINUE
    WRITE (6,931)
    WRITE (6,931)
    IF (K.EQ.1) WRITE (6.9こ2.)
    IF (K.EQ.1) WRITE (6.9こ2.)
    WRITE (6.910) ((I),I=25,38)
    WRITE (6.910) ((I),I=25,38)
    WRITE (6,911) ((IST4(I,1),IST4(I,2)),I=25,38)
    WRITE (6,911) ((IST4(I,1),IST4(I,2)),I=25,38)
    DO 30 I=K,21
    DO 30 I=K,21
    IF (I.EQ. 6.ORoIoEQo110ORoIoEQo14) WRITE (6.933)
    IF (I.EQ. 6.ORoIoEQo110ORoIoEQo14) WRITE (6.933)
    IF (IoEQo170ORoIoEQo21) WRITE (6.933)
    IF (IoEQo170ORoIoEQo21) WRITE (6.933)
    IF (I.NE.21)
    IF (I.NE.21)
    IWRITE (6,912) I,(A(I,J),J=25,38),I
    IWRITE (6,912) I,(A(I,J),J=25,38),I
    IF (I.EQ.21) WRITE (6,952) I,(L(J),J=25,38),I
    IF (I.EQ.21) WRITE (6,952) I,(L(J),J=25,38),I
30 CONTINUE
30 CONTINUE
    WRITE (6.931)
    WRITE (6.931)
    IF (K.EQ.1) WRITE (6,932)
    IF (K.EQ.1) WRITE (6,932)
    WRITE (6.910) ((I),I=39.52)
    WRITE (6.910) ((I),I=39.52)
    WRITE (6,911) ((IST4(I,1),IST4(I,2)),I=39,52)
    WRITE (6,911) ((IST4(I,1),IST4(I,2)),I=39,52)
    CO 40 I=K.21
    CO 40 I=K.21
    IF (I.EQ. 6.OR.I.EQ.110OROIoEQO14) WRITE (6.c33)
    IF (I.EQ. 6.OR.I.EQ.110OROIoEQO14) WRITE (6.c33)
    IF (IoEQo170ORoIoEQo 21)
    IF (IoEQo170ORoIoEQo 21)
                            WRITE (6,933)
```

                            WRITE (6,933)
    ```
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```

            IF (I.NE.21)
    ```
            IF (I.NE.21)
    IWRITE (6.912) I,(A(I,J),J=39,52),I
    IWRITE (6.912) I,(A(I,J),J=39,52),I
        IF (IOEG.21) WRITE (6.952) I.(L(J).J=39.52).I
        IF (IOEG.21) WRITE (6.952) I.(L(J).J=39.52).I
        40 CONTINUE
        40 CONTINUE
            WRITE (6.931)
            WRITE (6.931)
            IF (K.EQ.1) WFITE (6.932)
            IF (K.EQ.1) WFITE (6.932)
            WRITE (6.920) ((I),I=53.60)
            WRITE (6.920) ((I),I=53.60)
            WRITE (6.911) ((IST4(I,1),IST4(I,2)),I=53,60)
            WRITE (6.911) ((IST4(I,1),IST4(I,2)),I=53,60)
            OO 50 I=K.21
            OO 50 I=K.21
            IF (IOEQ0 GOOROIOEQO110ORcIOEQO14) WFITE (6.933)
            IF (IOEQ0 GOOROIOEQO110ORcIOEQO14) WFITE (6.933)
            IF (I.EQ.17.OR.I.EQ.21) WRITE (6.93こ)
            IF (I.EQ.17.OR.I.EQ.21) WRITE (6.93こ)
            IF (I.NE.21)
            IF (I.NE.21)
            1WRITE (6,922) I,(A(I,J),J=5ミ,61),I
            1WRITE (6,922) I,(A(I,J),J=5ミ,61),I
            IF (IOEGo21) WFITE (6,962) I,(L(J),J=53.61).I
            IF (IOEGo21) WFITE (6,962) I,(L(J),J=53.61).I
        50 CONTINUE
        50 CONTINUE
            RETURN
            RETURN
900 FCRMAT ("1PARAMETER", 21X,10I8,5X,"ROW*)
900 FCRMAT ("1PARAMETER", 21X,10I8,5X,"ROW*)
901 FORMAT (" TABLE 4 INDICES',1EX,10(I6,*-*,I1)/)
901 FORMAT (" TABLE 4 INDICES',1EX,10(I6,*-*,I1)/)
902 FOFMAT (I3,'% .,4A6,A2,10F801,I8)
902 FOFMAT (I3,'% .,4A6,A2,10F801,I8)
910 FORMAT (3X,14I8,5X,"RJW*)
910 FORMAT (3X,14I8,5X,"RJW*)
911 FORMAT ( \Xix,14(I6,"-*,I1)/)
911 FORMAT ( \Xix,14(I6,"-*,I1)/)
912 FORMAT (13,14F8.1,I 8)
912 FORMAT (13,14F8.1,I 8)
920 FORMAT ( }3\times,818,0=\mathrm{ FHS ROW`)
920 FORMAT ( }3\times,818,0=\mathrm{ FHS ROW`)
922 FDRMAT (13,8F8.1,' =',F8.1,I 8)
922 FDRMAT (13,8F8.1,' =',F8.1,I 8)
931 FCRMAT ('0 *)
931 FCRMAT ('0 *)
9ड2 FORMAT ('1 ()
9ड2 FORMAT ('1 ()
933 FORMAT (" *)
933 FORMAT (" *)
942 FORMAT (I3.'. '.4A6.AE,11I8)
942 FORMAT (I3.'. '.4A6.AE,11I8)
952 FORMAT (IE.15I8)
952 FORMAT (IE.15I8)
SE2 FORMAT (I3.8I8,0 = ',2I8)
SE2 FORMAT (I3.8I8,0 = ',2I8)
    END
```

    END
    ```
1. Building Construction Cost Data 1978, Robert Snow Means Company, Inc., New York, 1978.
2. Chapman, R. E., P. T. Chen and W. G. Hall, Economic Aspects of Fire Safety in Health Care Facilities: Guidelines for Cost-Effective Retrofits, National Bureau of Standards, NBSIR 79-1902, November 1979.
3. Code for Safety to Life from Fire in Büildings and Structures, National Fire Protection Association, NFPA 101-1.973, 1973.
4. Hall, W. G., R. H. F. Jackson and P. B. Saunders, The National Bureau of Standards Linear and Quadratic Programming Subroutines, National Bureau of Standards Repart 10695, February 1972.
5. Nelson, H. E. and A. J. Shibe, A System for Fire Safety Evaluation of Health Care Facilities, National Bureau of Standards, NBSIR 78-1555, November 1978.
6. Tragedy of Multiple Death Nursing Home Fires: The Need for a National Commitment to Safety, Select Committee on Aging, Subcommittee on Long-Term Care, September 1976.

\section*{FEDERAL INFORMATION PROCESSING STANDARD SOFTWARE SUMMARY}


\section*{14. Keywords}

Applied Economics; Building Codes; Economic Analysis; Fire Safety; Health Care Facilities; Hospitals; Life Safety; Mathematical Programming; Nursing Homes; Optimization; Renovation
\begin{tabular}{c|l|l|l}
\hline \begin{tabular}{c} 
15. Computer manuf'r and model \\
UNIVAC 1108A
\end{tabular} & \begin{tabular}{l} 
16. Computer operating system \\
NBS Computer Services \\
Division
\end{tabular} & 17. Programing language(s) & \begin{tabular}{l} 
18. Number of source program state- \\
ments \\
DORTRAN V
\end{tabular} \\
\hline \begin{tabular}{c} 
19. Computer memory requirements \\
14,500 words
\end{tabular} & \begin{tabular}{l} 
20. Tape drives \\
None
\end{tabular} & \begin{tabular}{l} 
21. Disk/Drum units \\
None
\end{tabular} & \begin{tabular}{c} 
22. Terminals \\
None
\end{tabular} \\
\hline
\end{tabular}
23. Other operational requirements

None
24. Software availability
Available
Limited
Operations Research Division
Building 101, Room A-428
National Bureau of Standards
Washington, D.C. 20234
25. Documentation availability
Available
\(\boxed{\boxtimes}\)
perations Research Division
\(\square\)

In-house only
\(\square\)
Operations Research Division
Building 101, Room A428
National Bureau of Standards
Washington, D.C. 20234
26. FOR SUBMITTING ORGANIZATION USE

NBS-114A (REV. 0.78)
U.S. DEPT. OF COMM.
BIBLIOGRAPHIC DATA
SHEET
1. PUBLICATION OR REPORT NO.

4. TITLE AND SUBTITLE

A COMPUTERIZED APPROACH FOR IDENTIFYING COST-EFFECTIVE FIRE SAFETY RETROFITS IN HEALTH CARE FACILITIES

NBSIR 79-1929
5. Publication Date
 January 1980
6. Performing Organization Code
8. Performing Organ. Report No.
10. Prolect/Task/Vork Unit No.
11. Contract/Grant No.
13. Type of Report \& Period Covered

Final

\section*{14. Sponsoring Agency Code}

\section*{15. SUPPLEMENTARY NOTES}

XXD Document describes a computer program; SF-185, FIPS Software Summary, is attached.
16. ABSTRACT (A 200-word or less factual summary of most significant information. If document includos a significant bibliography or literature survey, mention it here.)

This study focuses on how a computerized version of the Fire Safety Evaluation System developed by the Center for Fire Research at the National Bureau of Standards can be used to determine equivalence to the Life Safety Code in the least costly manner. This study presents a programmer-oriented discussion of the mathematical, economic and engineering considerations that went into the development of the linear programming algorithm for identifying cost-effective retrofits. Programmer-oriented topics treated in this report include: a discussion of user options; program documentation; format statements; flow charts; sample computer runs; and a complete listing of the computer program.
17. KEY WORDS (six to twelve entries; alphabetical order; capitalize only the first letter of the first key word unless a proper name; separated by semicolons)
Applied economics; building codes; economic analysis; fire safety; health care facilities; hospitals; life safety; mathenatical programmine; nursing homes; optimization; renovation
18. AVAILABILITY

XX Unlimited

For Official Distribution. Do Not Release to NTISOrder From Sup. of Doc., U.S. Government Printing Office, Washington, DC 20402, SD Stock No. SNOO3-003-
XX Order From National Technical Information Service (NTIS), Springfield, VA. 22161
\begin{tabular}{|l|c|}
\hline \begin{tabular}{c} 
19. SECURITY CLASS \\
(THIS REPORT)
\end{tabular} & \begin{tabular}{c} 
21. NO. OF \\
PRINTED PAGES \\
UNCLASSIFIED
\end{tabular}
\end{tabular}```


[^0]:    * Exactly

[^1]:    1 Tragedy of Multiple Death Nursing Home Fires: The Need for a National Commitment to Safety, Select Committee on Aging, Subcommittee on LongTerm Care, September 1976.

    2
    Code for Safety to Life from Fire in Buildings and Structures, National Fire Protection Association, NFPA 101-1973, p. 101-2.

[^2]:    ${ }^{1}$ H. E. Nelson and A. J. Shibe, A System for Fire Safety Evaluation of Health Care Facilities, National Bureau of Standards, NBSIR 78-1555, November 1978.

[^3]:    ${ }^{1}$ Robert E. Chapman, Philip T. Chen, and William G. Hall, Economic Aspects of Fire Safety in Health Care Facilities: Guidelines for Cost-Effective Retrofits, National Bureau of Standards, NBSIR 79-1902, November 1979.

[^4]:    1 Definitions are taken from the report by H. E. Nelson and A. J. Shibe, A System for Fire Safety Evaluation of Health Care Facilities, National Bureau of Standards, NBSIR 78-1555, November 1978.

    2 Code for Safety to Life from Fire in Buildings and Structures, National Fire Protection Association, NFPA 101-1973, p. 101-4.

[^5]:    1 A fire zone is defined as a space separated from all other spaces by floors, horizontal exits, or smoke barriers.

[^6]:    1 Numbers in parentheses denote rows of Table 5 of the Fire Zone Safety Evaluation Worksheet.

[^7]:    1 In $n$ dimensional space the alternative solutions correspond to the vertices of the polyhedron (feasible region) in the neighborhood of the optimal basis (optimal combination of retrofits). Therefore, they should map into a neighborhood about the optimal value of the objective function (least-cost combination of retrofits).

    2 Experience has shown that the contrived constraints help in reducing the number of non-integers.

[^8]:    ${ }^{1}$ An element count entry of " -1 " indicates an impossible retrofit.

[^9]:    ${ }^{1}$ W. G. Hall, R. H. F. Jackson, P. B. Saunders, The National Bureau of Standards Linear and Quadratic Programming Subroutines, National Bureau of Standards Report 10695, February 1972.

[^10]:    1 In this case, the report (minus the first line) actually appears as a coda to the fire zone input report.

[^11]:    l W. G. Hall, R. H. F. Jackson, and P. B. Saunders, The National Bureau of Standards Linear and Quadratic Programming Subroutines, National Bureau of Standards Report 10695, February 1972.

