



A11104 361173

NBSIR 78-1551

Access Functions for Packed Scatter Tables

Bruce E. Martin

Systems and Software Division
Institute for Computer Sciences and Technology
National Bureau of Standards
Washington, D.C. 20234

August 1978



U.S. DEPARTMENT OF COMMERCE

NATIONAL BUREAU OF STANDARDS

QC
100
.U56
73-1551
1978



National Bureau of Standards
APR 17 1979

NOT ACC REP
RD 100
-1236
NBSIR 78-1551

NBSIR 78-1551

**ACCESS FUNCTIONS FOR PACKED
SCATTER TABLES**

Bruce E. Martin

Systems and Software Division
Institute for Computer Sciences and Technology
National Bureau of Standards
Washington, D.C. 20234

August 1978

NBS Internal Report, NBSIR 78-1551
U.S. DEPARTMENT OF COMMERCE, Juanita M. Kreps, Secretary

Dr. Sidney Harman, Under Secretary

Jordan J. Baruch, Assistant Secretary for Science and Technology

NATIONAL BUREAU OF STANDARDS, Ernest Ambler, Director



NBSIR 78-1551

**ACCESS FUNCTIONS FOR PACKED
SCATTER TABLES**

Bruce E. Martin

Systems and Software Division
Institute for Computer Sciences and Technology
National Bureau of Standards
Washington, D.C. 20234

August 1978

U.S. DEPARTMENT OF COMMERCE, Juanita M. Kreps, *Secretary*
Dr. Sidney Harman, *Under Secretary*
Jordan J. Baruch, *Assistant Secretary for Science and Technology*
NATIONAL BUREAU OF STANDARDS, Ernest Ambler, *Director*



TABLE OF CONTENTS

	Page
SUMMARY OF THE ACCESS METHOD	2
USE OF THE ROUTINES	5
Declarations	6
Initializations	6
Node (De)allocation	7
APPENDIX A: Documentation of PASCAL code	8
APPENDIX B: Listings of access routines	16
APPENDIX C: Sample results	21

DISCLAIMER

The table functions described in this report have been written and tested carefully. The possibility of improper application requires that NBS expressly disclaim any and all consequences of using the functions. A particular warning must be issued on attempts to speed table access by storing indices: such schemes are guaranteed failure, since items move with new insertions.

Access Functions for Packed Scatter Tables

Bruce E. Martin

Three PASCAL access routines are given for packed scatter tables. INSERT packs tables of integer keys; FIND retrieves the keys; DELETE deletes keys. While the routines currently access integer keys (for use in performance testing with pseudo - random integers), they can easily be converted to access other data types -- character strings in a symbol table, for example. To enhance portability, the code is straightforward PASCAL without any input-output capabilities. Appendices contain specific comments on the routines, listings, and sample results.

SUMMARY OF THE ACCESS METHOD

Hashing techniques allow insertion and retrieval of keys by computing a function $h(\text{key})$ and storing the key in $T[h(\text{key})]$, where T is an indexed table. Since the function $h(\text{key})$ generally does not compute unique addresses, different keys may "collide". Simple collision-resolving methods search for an alternate location to store the key

being inserted. But such methods can cause slow retrieval of keys. More sophisticated methods search for alternate locations for other keys as well as for the key being inserted. INSERT uses a generalized collision-resolving method that recursively considers table rearrangement. The user controls the method to be used with the parameter DEPTH. Lyon gives a more detailed discussion of the algorithm in [1]. A summary of the method appears here. Specific comments on the PASCAL code appear in appendix A.

Integer keys are inserted in the scatter table by first calculating a table address using a primary hash function (key mod tablesize). If the slot in the table addressed by the primary hash function is not occupied, the key is inserted. Otherwise, the cost of displacing the contents of the slot is calculated by calling the function DISPLACE. Next, the cost of displacing the key is calculated by a second call of DISPLACE. DISPLACE returns a stack that indicates how the table should be rearranged. The table is rearranged using the stack returned by the call of DISPLACE with the least displacement cost.

The function DISPLACE makes probes into the table by increments of the secondary hash step ($\text{key mod (tablesize-2) + 1}$) until an open slot is found. Each slot probed during the search for an open slot is considered for displacement by recursive calls of DISPLACE. The recursion terminates

when the deepest level of recursion, as specified by the user with the parameter DEPTH, is reached or whenever displacement of further slots cannot possibly find a better solution. The deepest call of DISPLACE returns the additional penalty to probe to the free slot; that is, $PENALTY(\text{number of probes to free slot}) - PENALTY(\text{number of probes to table address})$, where PENALTY is a forcing function defined by the user (see [1]). The rearrangement stack returned by the deepest call of DISPLACE consists of the table address of the item being displaced and the address of the free slot. At higher levels, the total displacement cost of each subsequent slot is calculated to be the additional cost to probe to the slot plus its displacement cost, and the minimum is returned. The stack at higher levels of DISPLACE consists of the address of the item being displaced and the stack returned from the chosen call of DISPLACE.

A table of counters of search lengths is maintained for faster rejection of keys not in the table. As keys are inserted, the number of probes to find each key is recorded by incrementing a counter in the search length counter table, KICKOUT, where the search length is the index of KICKOUT. Since key insertion possibly causes other keys to be displaced, thus changing each displaced key's search length, old and new search lengths of displaced keys are also returned on the rearrangement stack to keep KICKOUT updated

and maintained. When a key is deleted, the appropriate search length counter is decremented.

Keys are retrieved by first calculating their original primary hash function and secondary hash step. Next, the table is probed until the key or an open slot is found or the number of slots probed equals the maximum search length. Generally, the performance of retrieving keys in the table does not improve as keys are deleted. For example, a table half filled performs much better than a table that is first completely filled and then has half of its keys deleted. Rejecting keys not in the table improves as keys are deleted provided deletions cause the maximum search length to decrease. Again, the half-filled table performs better than the table that is half-deleted. However, as keys are reinserted, both rejection and acceptance improve because insertion of keys causes the table to be rearranged more optimally. See Appendix C for measurements that are typical of correctly executing functions: Testing of the routines on a new system should give similar results.

USE OF THE ROUTINES

Declarations

The following must be declared by the calling program:

```
const
  tablesize      {the size of the table into which keys
                  will be inserted.  Must be prime!}
  maxreal        {largest real for particular instal-
                  lation.}
  kicksize       {size of the search counter table}*

type
  table=array[0..tablesize-1] of integer;
  kicktab= array[-1..kicksize+1] of integer;
  stkptr = ^stkelmnt;
  stkelmnt = record
                ind, oldlen, newlen: integer;
                next: stkptr
            end;

var
  oldnodes: stkptr;      {for node (de)allocation}
```

- * Kicksize should be the expected longest probe for a particular depth, penalty function and table filling. If the estimate of the maximum search length is too small, the rejection performance of the table may deteriorate. Therefore, a generous estimate of kicksize is desirable.

Initializations

The following must be initialized by the calling program:

VARIABLES	WHEN	INITIALIZED TO
of type TABLE	for new table	-1
OLDNODES	first use of routines	nil

of type KICKTAB for new table as follows:

```
kickout[-1]:=0; {no overflow with new table}
kickout[0]:=1;  {maximum probes with new table}
kickout[1..kicksizel]:=0;
```

Node (De)allocation

Since node (de)allocation differs from one PASCAL installation to the next, the INSERT routine, in the interest of portability, explicitly controls node (de)allocation for its rearrangement stack via procedures GETNODE and FREENODE. The procedures use a global variable OLDNODES, which points to a linked list of nodes that grows and shrinks during execution.

REFERENCES

- [1] Lyon, G.E. "Packed Scatter Tables", Comm. of the ACM (tentative October, 1978)
- [2] Lyon, G.E. "Batch scheduling from short lists", Information Processing Letters, (to appear)

APPENDIX A: Documentation of PASCAL code

Procedure insert

PARAMETER TYPE

tab	table	the table in which keys are inserted.
key	integer	the integer to be inserted.
depth	integer	depth of recursion for displacement.
kickout	kicktab	table of counters of search lengths. KICKOUT[1..KICKSIZE] are counters of search lengths, where the length is the index in KICKOUT. KICKOUT[0] = longest search length. KICKOUT[-1] = longest search length if an overflow occurs. KICKOUT[KICKSIZE+1] is counter of overflow search lengths. KICKOUT[0] traps to KICKSIZE+1 if overflow occurs.

VARIABLE TYPE

index	integer	primary hash index. TAB[INDEX] is considered for displacement if a collision occurs.
temp	integer	stores the contents of TAB[INDEX] while displacement of the new key is being considered.
len1	integer	length of the longest search returned when TAB[INDEX] is considered for displacement.

len2	integer	length of the longest search returned when the key is considered for displacement.
cost1	real	cost of displacing TAB[INDEX].
cost2	real	cost of displacing the key.
stk1	stkptr	rearrangement stack returned when TAB[INDEX] is considered for displacement.
stk2	stkptr	rearrangement stack returned when the key is considered for displacement.

LINE NUMBER(S)

142..144

The primary hash index is calculated. Another key has search length of 1 so KICKOUT[1] is incremented. If the slot is empty or marked deleted, the key is inserted and INSERT is exited. -1 indicates empty slots; -2 marks deleted slots;

148..149

The cost of displacing TAB[INDEX] is calculated provided DEPTH > 0. DEPTH=0 means the key should be inserted in the first free slot and no displacements occur.

150..152

The cost of displacing the key is calculated by temporarily storing TAB[INDEX] in TEMP. The key is inserted in tab[index] and DISPLACE is called. This was designed so that DISPLACE would have the table address as an parameter (necessary for recursive calls) and so INSERT would have the key as a parameter, making table addresses invisible to the user. Note that with the second call of DISPLACE, COST1 is the actual parameter corresponding to the DISPLACE

formal parameter MAX. This keeps the second call of DISPLACE from considering any displacements that are more costly than the displacement found by the first call of DISPLACE.

153..162

If both the key and TAB[INDEX] were considered for displacement, the table is rearranged by REARRANGE according to the stack returned by the call of DISPLACE returning the lower cost. If only the key was considered for displacement, the table is rearranged by STK2. Finally, after table rearrangement, both stacks are deallocated by FREENODE.

procedure getnode

7..15

A node is allocated from OLDNODES or by the pascal function NEW.

procedure freenode

16..27

A linked list is walked and deallocated to OLDNODES.

procedure rearrange

30

If the search length passed to it is greater than the current maximum in KICKOUT[0], KICKOUT[0] is updated.

31..47

Each node in the stack has four fields: IND, OLDLEN, NEWLEN and NEXT. For each node: a) OLDLEN and NEWLEN are tested for overflow. If so, KICKOUT[0] traps to the overflow counter. b) KICKOUT[NEWLEN] is incremented and KICKOUT[OLDLEN] is decremented. c) the contents of TAB[NEXT^.IND] are moved to TAB[IND]. d) the next node of the stack is used. When the last node is encountered, the key is moved to TAB[IND].

function displace

PARAMETER TYPE

index	integer	address of item to be considered for displacement.
depth	integer	depth of recursion for which displacement should be considered.
max	real	MAX is an upper limit on cost for displacement consideration. It is the best solution found so far at higher levels of recursion.
rjstack	stkptr	contains indicies of slots rejected at higher levels of recursion. A slot which is rejected at a higher level of recursion will not lead to a better solution at a deeper level.
stack	stackptr	returns the rearrangement stack for best solution at a given level. (var parameter)
length	integer	returns the length of the longest search. (var parameter)
VARIABLE TYPE		
ind	integer	used to calculate subsequent slots in the table.
probetoind	integer	number of probes to hash to TAB[INDEX].
probetofree	integer	number of probes to the first free slot.
counter	integer	slot counter. Used in calculating subsequent locations to probe the

		table.
step	integer	equal to the secondary hash function for probing.
hash1	integer	equal to the primary hash function for probing.
next	integer	address of the next slot.
srchlen	integer	longest search from deeper levels of recursion.
uplim	real	the upper limit on displacement cost at a given level. UPLIM is the minimum of the cost to move TAB[INDEX] to a free slot and MAX (the least cost found at higher levels).
totcost	real	additional cost of probing to next slot plus cost of displacing next slot.
pentonext	real	additional cost of probing to next slot, that is PENALTY(probes to next slot) - PENALTY(probetoind).
thisnode	stkptr	pointer to node pushed on stack. It is used to update the new search length.
savrj	stkptr	saves a copy of rjstack upon first execution of DISPLACE.
bestack	stkptr	saves the stack returned by DISPLACE returning the lowest cost. BESTACK is in turn returned to higher levels of DISPLACE.
tstack	stkptr	temporary stack for calls of

DISPLACE.

LINE NUMBER(S)

84..95

The primary and secondary hash functions are calculated. Slots are probed to find the number of probes to INDEX and a free slot.

96..100

INDEX, number of probes to index, number of probes to free slot are pushed on STACK as IND, OLDLEN and NEWLEN, respectively. NEWLEN may have to be updated later if a better solution is found. Therefore, THISNODE saves the node. So far, the best solution found is to move TAB[INDEX] to a free slot so BESTACK is set to STACK. RJSTACK is saved.

101..103

The tentative longest search is PROBETO-FREE so LENGTH defaults to PROBETOFREE. The index of the free slot and two dummy constants are pushed on BESTACK. UPLIM is the additional cost of probing to the free slot.

104

If DEPTH=0, no subsequent slots are to be considered for displacement. The recursion has terminated. The stack with INDEX and the address of the free slot is returned. The value of DISPLACE is UPLIM. Otherwise, subsequent slots are considered for displacement.

105..109

If a better solution than UPLIM was found from a higher level of recursion then UPLIM is updated. The primary hash location is the first to be considered for relocation. The cost to probe to the first location is PENALTY(1) - PENALTY(probetoind).

110

While the cost to probe to the next slot is greater than UPLIM, the following is done:

112..135

If the next slot has not already been considered, it is considered for relocation. If the total cost, TOTCOST, is lower than the current lowest cost UPLIM, a better solution has been found and UPLIM, BESTACK and LENGTH are updated to TOTCOST, TSTACK and SRCHLEN, respectively. Otherwise, the slot being considered for relocation is pushed on the reject stack, RJSTACK. The next slot to be considered and the additional cost to probe to it are calculated.

136..140

The value of DISPLACE returned is the UPLIM. BESTACK is returned as the rearrangement stack.

procedure push

PUSH gets a new node and pushes the arguments I,OLDLEN,NEWLEN onto the stack.

function member

MEMBER returns true if its integer argument is a member of the stack. Otherwise it returns false.

function penalty

PENALTY is a forcing function defined by the user. Currently it is linear; it returns its argument. To force insertion of keys in a different manner the user must change the forcing function.

function find

FIND tries to find the key in the table. If found, its table location is returned, otherwise -1 is returned. The variable probes returns the number of probes to find (or reject) the key.

procedure delete

DELETE finds the key in the table by calling function FIND, deletes the key

and updates KICKOUT accordingly. A slot
is marked deleted by setting it to -2.

APPENDIX B: Listings of access routines

```

1  procedure insert (var tab: table; key, depth: integer;
2                      var kickout:kicktab);
3
3  var
4      index, temp, len1, len2: integer;
5      cost1, cost2: real;
6      stk1, stk2: stkptr;
7
7  procedure getnode(var p:stkptr);
8      begin
9          if oldnodes=nil then new(p)
10         else begin
11             p:=oldnodes;
12             oldnodes:=oldnodes^.next;
13         end;
14         p^.next:=nil
15     end;
16
16  procedure freenode (first,last:stkptr);
17  var
18      x:stkptr;
19  begin
20      if first<>last then
21          begin
22              x:=first;
23              while first^.next<>last do first:=first^.next;
24              first^.next:=oldnodes;
25              oldnodes:=x
26          end
27      end;
28
28  procedure rearrange (stack: stkptr; key, length: integer);
29  begin
30      if length > kickout[0] then kickout[0]:=length;
31      repeat
32          if stack^.newlen > kicksize then
33              begin
34                  if kickout[-1] < stack^.newlen then
35                      kickout[-1]:=stack^.newlen;
36                  kickout[0]:=kicksizes+1; { trap to overflow counter }
37                  stack^.newlen:=kicksizes+1
38              end;
39          if stack^.oldlen > kicksize then
40              stack^.oldlen:=kicksizes + 1;
41          kickout[stack^.newlen]:=kickout[stack^.newlen] + 1;
42          kickout[stack^.oldlen]:=kickout[stack^.oldlen] - 1;
43          if stack^.next <> nil then

```



```

44         tab[stack^.ind]:=tab[stack^.next^.ind]
45         else tab[stack^.ind]:=key;
46         stack:=stack^.next
47         until stack=nil;
48         while kickout[kickout[0]] = 0 do kickout[0]:=kickout[0]-1;
49     end;

50 function displace (index,depth:integer; max:real; rjstack:stkptr;
51                 var stack: stkptr; var length: integer):real;

52 var
53     ind, probetoind, probetofree, counter, step, hashl,
54     next, srchlen: integer;
55     uplim, totcost, pentonext: real;
56     thisnode, savrj, bestack, tstack: stkptr;

57 procedure push (i,oldlen,newlen:integer; var stack:stkptr);
58 var
59     node: stkptr;
60     begin
61         getnode(node);
62         node^.ind:=i;
63         node^.newlen:=newlen;
64         node^.oldlen:=oldlen;
65         node^.next:=stack;
66         stack:=node
67     end;

68 function member (i:integer; stk: stkptr):boolean;
69 var
70     found: boolean;
71     begin
72         found:=false;
73         while (stk <> nil) and (not found) do
74             if stk^.ind=i then found:=true
75                 else stk:=stk^.next;
76         member:=found
77     end;

78 function penalty(i:integer): real;
79     {to be defined as desired; currently linear}
80     begin
81         penalty:=float(i)
82     end;

83 begin { function displace }
84     step:=(tab[index] mod (tablesize-2))+1;
85     hashl:=tab[index] mod tablesize;
86     probetoind:=0;
87     repeat

```

```

88     ind:=(hash1 + probetoind * step) mod tablesiz;
89     probetoind:=probetoind + 1
90     until ind=index;
91     probetofree:=0;
92     repeat
93         ind:=(hash1 + probetofree * step) mod tablesiz;
94         probetofree:=probetofree + 1
95         until (tab[ind]=-1) or (tab[ind]=-2);
96     push(index,probetoind,probetofree,stack);
97     thisnode:=stack;
98     tstack:=stack;
99     bestack:=stack;
100    savrj:=rjstack;
101    length:=probetofree;
102    uplim:=penalty(probetoind)-penalty(probetoind);
103    push(ind,1,1,bestack);
104    if depth > 0 then
105        begin
106            if uplim > max then uplim:=max;
107            counter:=0;
108            next:=hash1;
109            pentonext:=penalty(1) - penalty(probetoind);
110            while uplim > pentonext do
111                begin
112                    if (not member(next,stack)) and (not member(next,rjstack))
113                        then
114                            begin
115                                totcost:=pentonext + displace(next, depth-1, uplim-pentonext,
116                                                                    rjstack, tstack, srchlen);
117                                if totcost < uplim then
118                                    begin
119                                        uplim:=totcost;
120                                        freenode(bestack,stack);
121                                        bestack:=tstack;
122                                        thisnode^.newlen:=counter+1;
123                                        if 1+counter > srchlen then length:=1+counter
124                                            else length:=srchlen;
125                                    end
126                                else begin
127                                    push(next,1,1,rjstack);
128                                    freenode(tstack,stack)
129                                end;
130                                tstack:=stack;
131                            end;
132                            counter:=counter+1;
133                            next:=(hash1 + counter * step) mod tablesiz;
134                            pentonext:=penalty(1+counter) - penalty(probetoind)
135                        end;
136                    freenode(rjstack,savrj)
137                end;
138            stack:=bestack;
139            displace:=uplim

```

```

140     end;

141     begin { procedure insert }
142     index:=key mod tablesize;
143     kickout[l]:=kickout[l]+1;
144     if (tab[index]=-1) or (tab[index]=-2) then tab[index]:=key
145     else begin
146     stk1:=nil;
147     stk2:=nil;
148     if depth>0 then
149     cost1:=displace(index, depth-1, maxreal, nil, stk1, len1);
150     temp:=tab[index];
151     tab[index]:=key;
152     cost2:=displace(index, depth, cost1, nil, stk2, len2);
153     if (depth =0) or (cost2 < cost1) then rearrange(stk2, temp, len2)
154     else begin
155     tab[index]:=temp;
156     rearrange(stk1, key, len1)
157     end;
158     freenode(stk1,nil);
159     freenode(stk2,nil)
160     end
161     end;
162 { procedure insert }

```

```

1  function find(var tab: table; key: integer; var kickout: kicktab;
2      var probes: integer): integer;
3
4  var
5      hash1,step,index,limit: integer;
6
7  begin
8      probes:=0;
9      hash1:= key mod tablesize;
10     step:= key mod (tablesize - 2) +1;
11     if kickout[0]=kicksize+1 then limit:=kickout[-1]
12     else limit:=kickout[0];
13     repeat
14         index:=(hash1 + probes * step) mod tablesize;
15         probes:=probes+1
16         until (tab[index]=key) or (tab[index]=-1) or (probes=limit);
17         if tab[index]=key then find:=index
18         else find:=-1
19     end;
20 { function find }

```

```

1  procedure delete(var tab: table; key: integer; var kickout: kicktab);
2
3  var
4      where,probes: integer;
5
6  begin
7      where:=find(tab,key,kickout,probes);
8      if where = -1 then writeln(output,key,' not found')
9      else begin
10         tab[where]:=-2;
11         if probes > kicksize then probes:= kicksize+1;
12         kickout[probes]:=kickout[probes]-1;
13         while (kickout[0]<>1) and (kickout[kickout[0]]=0)
14         do kickout[0]:=kickout[0]-1
15     end
16 end;
17 { procedure delete }

```

APPENDIX C: Sample results

The table was 98% filled. The following was done for DEPTH = 0,1,2,3,4,10: 4899 random integers were generated from a linear-congruential formula $i:=3309*i+885321 \pmod{4194304}$. The same 4899 keys were retrieved from the table to calculate retrieval performances. 4899 keys not in the table were generated and rejected to calculate rejection performances. This was repeated 18 times.

```

TABLESIZE:                4999
NUMBER OF KEYS INSERTED:  4899
PERCENT OF TABLE FILLED:    98
DEPTH OF RECURSION:       0
PENALTY FUNCTION USED:    LINEAR
    
```

TRIAL	LONGEST PROBE	MEAN PROBES	MEAN REJECTION
-----	-----	-----	-----
1	179	4.05429	48.17125
2	154	3.96142	47.80567
3	266	4.00204	49.21779
4	181	3.93957	48.19289
5	158	4.06940	48.14002
6	407	3.84057	48.72545
7	210	3.92712	49.15839
8	131	3.84057	45.55154
9	171	3.92733	47.68626
10	170	3.84751	48.78914
11	144	3.96366	47.68279
12	155	3.92998	47.07409
13	220	4.03184	50.97244
14	249	3.96529	48.20759
15	142	3.82384	45.78485
16	264	4.08389	50.35047
17	195	4.03123	48.02571
18	169	3.89957	48.48152
MEAN	198.05	3.95217	48.22322

TABLESIZE: 4999
 NUMBER OF KEYS INSERTED: 4899
 PERCENT OF TABLE FILLED: 98
 DEPTH OF RECURSION: 1
 PENALTY FUNCTION USED: LINEAR

TRIAL	LONGEST PROBE	MEAN PROBES	MEAN REJECTION
1	20	2.14696	16.64258
2	15	2.12880	13.07817
3	26	2.12247	20.30557
4	20	2.13574	16.49112
5	21	2.11614	17.29679
6	18	2.16431	15.17922
7	20	2.13247	16.63400
8	25	2.14778	19.72320
9	20	2.11859	16.67462
10	20	2.12267	16.68748
11	20	2.14227	16.52582
12	21	2.14206	17.05817
13	19	2.13655	15.84547
14	19	2.12288	15.99224
15	27	2.15554	20.89773
16	19	2.15819	16.01285
17	21	2.15839	17.33210
18	18	2.14472	15.43233
MEAN	20.50	2.13870	16.87830

TABLESIZE: 4999
 NUMBER OF KEYS INSERTED: 4899
 PERCENT OF TABLE FILLED: 98
 DEPTH OF RECURSION: 2
 PENALTY FUNCTION USED: LINEAR

TRIAL	LONGEST PROBE	MEAN PROBES	MEAN REJECTION
1	13	1.89855	11.64564
2	11	1.90936	10.04123
3	12	1.90304	10.67605
4	15	1.89895	13.08532
5	11	1.92284	10.01408
6	13	1.89548	11.58522
7	11	1.91181	9.95264
8	12	1.91202	10.74402
9	11	1.92304	9.93794
10	14	1.91712	12.29271
11	12	1.89712	10.78138
12	13	1.87711	11.53031
13	12	1.91855	10.76546
14	13	1.91835	11.58236
15	11	1.92876	10.05409
16	14	1.89875	12.42600
17	11	1.91345	9.99183
18	12	1.90814	10.75648
MEAN	12.27	1.90847	10.99237

TABLESIZE: 4999
 NUMBER OF KEYS INSERTED: 4899
 PERCENT OF TABLE FILLED: 98
 DEPTH OF RECURSION: 3
 PENALTY FUNCTION USED: LINEAR

TRIAL	LONGEST PROBE	MEAN PROBES	MEAN REJECTION
1	11	1.83710	9.95407
2	9	1.84486	8.35211
3	11	1.83445	9.95733
4	11	1.81812	10.00489
5	10	1.81771	9.12349
6	9	1.80608	8.28373
7	10	1.84323	9.17962
8	10	1.81853	9.17350
9	11	1.82629	9.95611
10	11	1.84996	9.94284
11	11	1.85772	9.97958
12	9	1.83996	8.37170
13	10	1.81833	9.16084
14	11	1.83568	9.92794
15	9	1.81853	8.28965
16	10	1.83200	9.14064
17	10	1.81975	9.17228
18	8	1.81363	7.42416
MEAN	10.05	1.82955	9.18858

TABLESIZE: 4999
 NUMBER OF KEYS INSERTED: 4899
 PERCENT OF TABLE FILLED: 98
 DEPTH OF RECURSION: 4
 PENALTY FUNCTION USED: LINEAR

TRIAL	LONGEST PROBE	MEAN PROBES	MEAN REJECTION
1	8	1.80894	7.42559
2	10	1.79975	9.11900
3	8	1.77873	7.45621
4	9	1.80036	8.31006
5	9	1.79199	8.26495
6	10	1.80261	9.11696
7	8	1.78362	7.44886
8	9	1.81036	8.28026
9	10	1.79159	9.16411
10	10	1.80159	9.17452
11	9	1.80547	8.28271
12	9	1.80016	8.27434
13	9	1.79056	8.28699
14	9	1.78648	8.29067
15	8	1.79567	7.41192
16	8	1.80159	7.43702
17	8	1.82159	7.46540
18	8	1.79465	7.47846
MEAN	8.83	1.79809	8.14933

TABLESIZE: 4999
 NUMBER OF KEYS INSERTED: 4899
 PERCENT OF TABLE FILLED: 98
 DEPTH OF RECURSION: 10
 PENALTY FUNCTION USED: LINEAR

TRIAL	LONGEST PROBE	MEAN PROBES	MEAN REJECTION
-----	-----	-----	-----
1	7	1.75199	6.62482
2	7	1.76546	6.58685
3	8	1.76484	7.40579
4	7	1.75688	6.56195
5	7	1.77709	6.59951
6	7	1.74321	6.59420
7	7	1.76811	6.60318
8	7	1.76219	6.59154
9	7	1.77342	6.56031
10	7	1.76260	6.58562
11	7	1.75750	6.62318
12	7	1.74239	6.60073
13	7	1.76423	6.58215
14	7	1.76832	6.58603
15	7	1.77995	6.62237
16	7	1.75423	6.59889
17	8	1.75729	7.48867
18	7	1.76382	6.58154
MEAN	7.11	1.76186	6.68874

The table was filled to 98% loading. All the keys in the table were retrieved to calculate retrieval performances. An equal number of keys not in the table were rejected to calculate rejection performances. 49% of the keys were deleted. Retrieval and rejection statistics were again calculated. The table was filled back to a 98% loading. Retrieval and rejection statistics were again calculated. These are the mean results of 18 trials:

TABLESIZE: 4999
 DEPTH OF RECURSION: 4
 PENALTY FUNCTION USED: LINEAR

ACTION	# OF KEYS IN TABLE	% TABLE LOADED	LONGEST PROBE	MEAN PROBES TO ACCEPT/REJECT
INSERT 4900	4900	97.9	9.06	
LOOKUP 4900				1.80268 AC
LOOKUP-4900				8.35276 RJ
DELETE 2450	2450	48.9	8.61	
LOOKUP 2450				1.78899 AC
LOOKUP-2450				7.98171 RJ
INSERT 2450	4900	97.9	9.50	
LOOKUP 2450				1.86280 AC
LOOKUP-2450				9.43040 RJ

AVERAGES OF EIGHTEEN TRIALS

U.S. DEPT. OF COMM. BIBLIOGRAPHIC DATA SHEET		1. PUBLICATION OR REPORT NO. NBSIR 78-1551	2. Gov't Accession No.	3. Recipient's Accession No.
4. TITLE AND SUBTITLE ACCESS FUNCTIONS FOR PACKED SCATTER TABLES			5. Publication Date August 1978	
			6. Performing Organization Code	
7. AUTHOR(S) Bruce E. Martin			8. Performing Organ. Report No.	
9. PERFORMING ORGANIZATION NAME AND ADDRESS NATIONAL BUREAU OF STANDARDS DEPARTMENT OF COMMERCE WASHINGTON, D.C. 20234			10. Project/Task/Work Unit No. 6401129	
			11. Contract/Grant No.	
12. Sponsoring Organization Name and Complete Address (Street, City, State, ZIP) see 9 above			13. Type of Report & Period Covered	
			14. Sponsoring Agency Code	
15. SUPPLEMENTARY NOTES				
16. ABSTRACT (A 200-word or less factual summary of most significant information. If document includes a significant bibliography or literature survey, mention it here.) Three PASCAL access routines are given for packed scatter tables. INSERT packs tables of integer keys; FIND retrieves the keys; DELETE deletes the keys. While the routines currently access integer keys (for use in performance testing with pseudo-random integers), they can easily be converted to access other data types -- character strings in a symbol table, for example. To enhance portability, the code is straightforward PASCAL without any input/output capabilities. Appendices contain specific comments on the routines, listings, and sample results.				
17. KEY WORDS (six to twelve entries; alphabetical order; capitalize only the first letter of the first key word unless a proper name; separated by semicolons) Access functions; fast retrievals; hashing; PASCAL; scatter storage				
18. AVAILABILITY <input checked="" type="checkbox"/> Unlimited <input checked="" type="checkbox"/> For Official Distribution. Do Not Release to NTIS <input type="checkbox"/> Order From Sup. of Doc., U.S. Government Printing Office Washington, D.C. 20402, SD Cat. No. C13 <input type="checkbox"/> Order From National Technical Information Service (NTIS) Springfield, Virginia 22151		19. SECURITY CLASS (THIS REPORT) UNCLASSIFIED		21. NO. OF PAGES 29
		20. SECURITY CLASS (THIS PAGE) UNCLASSIFIED		22. Price



