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# THE THERMODYNAMIC PROPERTIES OF SLUSH HYDROGEN AND OXYGEN

H.M. Roder

Cryogenics Division Institute for Basic Standards National Bureau of Standards Boulder, Colorado 80302

Final Report

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Prepared for: NASA-Johnson Space Center Houston, Texas 77058



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U.S. DEPARTMENT OF COMMERCE, Juanita M. Kreps, Secretary Sidney Harman, Under Secretary Jordan J. Baruch, Assistant Secretary for Science and Technology

NATIONAL BUREAU OF STANDARDS, Ernest Ambler, Acting Director

#### BACKGROUND

During the Gemini, Apollo, and Skylab programs, cryogenic systems were used as the source for fuel cell energy production. Throughout these programs the stored cryogens became one of the main limiting consumables involving vehicle lifetime. The critical nature of the cryogenic system required very accurate premission analyses. Not only were quantity calculations required but pressure range evaluation was also made to ensure that mission operations could be safely performed.

A potential major improvement in Space Shuttle operations involves the use of slush cryogens. Slush is the term used to describe a mixture of solid and liquid phases of a cryogen. The advantage of slush over liquid cryogens is a higher stored mass for the same occupied volume storage tank. Also, the latent heat of the solid in the slush increases storage time before venting occurs. This improved capacity and storage time make possible increased space flight time and distance.

The Cryogenics Division of the National Bureau of Standards provided the PVT data and the equations of state which were used during the Apollo and Skylab programs under the sponsorship of NASA. The basic data and computer programs are extended in the present report to provide the support necessary to an increased effort in slush research and mission analysis. This software technology is now available for all future space programs and is expected to have industrial application.

Paralleling the basic data effort NASA has been a prime driver in funding the development of slush cryogen technology. A slush hydrogen program conducted from 1965 to 1970 at NBS investigated several production methods, measured the pressure drop in flowing slush hydrogen, determined maximum solid fraction and investigated several instruments to measure solid fraction<sup>\*</sup>. An experimental program currently underway at NBS is expected to demonstrate the safe and reliable production, storage and handling of slush hydrogen and oxygen in ground support equipment at NASA launch facilities.

See page 21, 22 of Nat. Bur. Stand. Technical Note 664 for references.

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#### SYMBOLS

P	=	pressure	dP dT	=	derivative of vapor pressure or melting pressure
т	=	temperature	Т'	=	temperature shifted to a new scale
ρ	=	density	Cp	=	specific heat at constant pressure
V	=	volume = $1/\rho$	cv	=	specific heat at constant volume
Н	=	enthalpy	$\Delta \mathbf{H}$	=	enthalpy difference
S	=	entropy	Δs	=	entropy difference
U	=	internal energy	C <sub>SAT</sub>	=	specific heat of saturated solid or saturated liquid

Q = quality

A, B, C,  $\alpha$ , c, P = coefficients in vapor pressure or melting pressure equations

#### SUBSCRIPTS

liquid	=	liquid phase	fusion
vapor	=	vapor phase	sublimation
solid	=	solid phase	vaporization
t	=	triple point	
melt	=	melting line	

#### UNITS

The primary variables in the computer programs are Pressure in atmospheres Density in moles/liter, and Temperature in Kelvin.

Conversions to other SI units and units normally used in applied problems are given in Appendices E and F.

#### THE THERMODYNAMIC PROPERTIES OF SLUSH HYDROGEN AND OXYGEN

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The thermodynamic properties of hydrogen and oxygen have been calculated for temperatures both below and above the triple point. Values of the various physical properties required for the computations are either taken from the literature, or are extrapolated. If extrapolated, the extrapolations are based on the known behavior of other simple fluids. The results are presented in the form of computer programs which cover two regions of the phase diagram, solid-vapor, and solid-liquid. Input to the programs is temperature and quality. The properties returned include pressure, density, enthalpy, entropy and internal energy. The present programs for slush hydrogen and slush oxygen are an extension of and depend upon the equations of state developed previously for these gases.

Key words: Computer programs; enthalpy; entropy; hydrogen; internal energy; liquid; oxygen; PVT; quality; slush; solid; vapor.

#### 1. INTRODUCTION

Slush is the term used to designate a mixture of solid and liquid phases of the gas under consideration. There are two major reasons for the current interest in slush. First, since solid is more dense than liquid, slush offers a way to carry a larger quantity of the cryogen in a container of fixed volume, as compared to the liquid alone. Second, since the solid melts, absorbing heat, slush offers a way to lengthen the time that the cryogen can be stored in a fixed volume container before venting has to occur.

We have included the solid-vapor region in this study because slush is currently produced by a freeze-thaw process. This means the properties of the vapor at temperatures just below the triple point are also of concern. Further, the properties of this two phase region are of interest in another application, subliming refrigerators, which are used to cool infrared detectors.

The properties of concern in this study are temperature, pressure, density, enthalpy, entropy and internal energy. Internal energy was added to the set because the principal applications at present involve containers of fixed volume. The regions of the phase diagram covered in this report, solid-vapor and solid-liquid, are both two phase regions. In analogy to the familiar quality used in liquid-vapor problems, we have included quality as a parameter in this study. The thermodynamic properties described in this report are consistent with and should be viewed as an extension of the two equations of state developed previously, the equation of state for hydrogen by Roder and McCarty (1975), and the equation of state for oxygen by Weber (1977a, 1977b). The single phase regions of each gas for liquid, and fluid gas or vapor as well as the liquid-vapor two phase region are defined by these equations of state. The present slush routines call on the equations of state to define liquid properties along the melting line and vapor properties on the vapor boundary of the solid-vapor region.

#### 2. BASIC THERMODYNAMIC CONSIDERATIONS

#### 2.1 General

Consider a pressure temperature phase diagram shown schematically in figure 1. We recognize the melting line, the vapor pressure curve of the liquid and the vapor pressure of the solid. These curves define the boundaries of the various phases, solid, liquid, and vapor. They intersect at the triple point. It is from a plot such as this that the triple point takes its name. What this phase diagram does not show is the variation of density. One unique aspect of any two phase regime liquid-vapor solid-vapor or solid-liquid is that the pair P, T on a phase boundary encompasses a large range of densities. We could consider a plot in the three variables pressure, density and temperature, however, consider instead the more familiar T-S diagram shown schematically in figure 2. This diagram is also a phase diagram. We recognize the single phase regions solid, liquid and vapor. We can also see the various two phase regions where two phases are in equilibrium. In a diagram of this kind the triple point gets stretched into a line. The density variation can also be included. For example, the density at point 1 in figure 2 corresponds to the density of the solid at the triple point, point 2 to the liquid triple point density, and point 3 to the vapor density at the triple point.

The regions already defined by the major equations of state are shown shaded. We will, in this report, cover the two phase regimes solid-liquid and solid-vapor. If we assume that the P-T relation of the boundary is available, then to define a region we need only define the properties at the boundaries. For the true slush region, solid-liquid, we would have to know density, enthalpy, entropy and internal energy at both the liquid and solid boundaries. The liquid side is already defined for us by the intersection of the equation of state and the melting pressure curve. It remains to define the other boundary in this case the solid side. The actual approach depends on what pieces of experimental data are available to guide us, and these are discussed in detail in sections that follow.



Figure 2. Temperature vs. Entropy, schematic shaded area is covered by the 32-term MBWR.

A fundamental relation governs the various two phase regimes. This equation is called the Clausius-Clapeyron equation, and we will use it extensively. Written out for each of the three two phase regimes the equation reads as follows:

Solid-Liquid	Solid-Vapor	Liquid-Vapor
dP _ AH (Fusion)	$\frac{dP}{dP} = \Delta H$ (Sublimation)	$\frac{dP}{dP} = \frac{\Delta H}{\Delta H} (Vaporization)$
dT T(Vliquid Vsolid)	dT T(V <sub>vapor</sub> -V <sub>solid</sub> )	dT T(Vvapor <sup>-V</sup> liquid)

The equation relates a latent heat, the pressure-temperature derivative at the appropriate phase boundary and the volume change corresponding to the phase change in question. If the available data are redundant, then we are in a position to make thermodynamic consistency checks. Quite often the list of available data is minimal and the opportunity for consistency checks is lost. When elements of data are missing we are forced to calculate the unknown pieces of information from the Clausius-Clapeyron equation. For example, the volume change on fusion is usually not measured experimentally. The heat of fusion is normally measured only at the triple point, not at elevated temperatures or pressures. If we wish to know the volume change on fusion, say at the triple point, then we must calculate it from the experimentally measured heat of fusion and the derivative of the melting pressure equation.

#### 2.2 The Quality, Q

The concept of quality is familiar to most engineers who have solved liquid-vapor problems. The conventional quality is defined as the percent (by mass) of the vapor phase present, or:

Since it is easy to make an error we caution that the expression in terms of density is:

$$Q = \left[\frac{\rho_{\text{liquid}}^{\rho} \text{vapor}}{\rho} - \rho_{\text{vapor}}\right] / (\rho_{\text{liquid}}^{-\rho} \text{vapor})$$

From these equations it is apparent that Q = 0.0 on the liquid side, i.e., the denser side, and that Q = 1.0 on the vapor side, i.e., the less dense side.

For the other two phase regimes solid-liquid and solid-vapor we will use a defined quality Q defined in a manner quite analogous to that for liquid-vapor above. Q will be 0.0 on the dense side, i.e., the solid, and Q will be 1.0 on the less dense side. The equations read as follows:

		Solid-Liquid			Solid-Vapor
Q	=	(V-V <sub>solid</sub> )/(V <sub>liquid</sub> -V <sub>solid</sub> )	Q	=	(V-V <sub>solid</sub> )/(V <sub>vapor</sub> -V <sub>solid</sub> )
Q	=	(H-H <sub>solid</sub> )/(H <sub>liquid</sub> -H <sub>solid</sub> )	Q	=	(H-H <sub>solid</sub> )/(H <sub>vapor</sub> -H <sub>solid</sub> )
Q	=	(S-S <sub>solid</sub> )/(S <sub>liquid</sub> -S <sub>solid</sub> )	Q	=	(S-S <sub>solid</sub> )/(S <sub>vapor</sub> -S <sub>solid</sub> )
Q	=	(U-U <sub>solid</sub> )/(U <sub>liquid</sub> -U <sub>solid</sub> )	Q	=	(U-U <sub>solid</sub> )/(U <sub>vapor</sub> -U <sub>solid</sub> )

#### 3. THE SOLID-LIQUID REGION FOR HYDROGEN

Prior work on the thermodynamic properties of this region include the experimental work and the calculations by Dwyer, et al. (1965a,b) and by Cook, et al. (1965). In the present report the thermodynamic properties along the liquid boundary of this region are defined from the intersection of the 32-term modified Benedict-Webb-Rubin (MBWR) equation of state as presented by Roder and McCarty (1975) with the melting pressure equation (Goodwin, 1962). The elements of data available to describe the region are limited. In the sections that follow we describe the reference values chosen for the property calculations, the melting pressure equation of the solid, the heats of fusion at elevated pressures, the property calculations, and thermodynamic consistency checks.

#### 3.1 The Reference Values

Since the available set of data is limited we are forced to calculate changes in properties for this region from the Clausius-Clapeyron equation. To obtain values for the solid boundaries these changes are applied from the liquid boundary. In effect, for a given temperature the values obtained from the 32-term equation of state and the melting line are used as starting point, or point of reference. At the triple point temperature the procedure leads to values for the solid that are used as reference point for the solid-vapor region (see section 4.1).

#### 3.2 The Melting Pressure Equation

The equation used is the one developed by Goodwin (1962), except that we shift the temperature scale by 0.003 K to match the triple point temperature and pressure of the liquid vapor pressure curve used with the 32-term MBWR. The shift insures that the melting pressure equation and the liquid vapor pressure equation intersect at the triple point, 13.800 K and 0.0695 atm, which are the values chosen for the basic 32-term equation of

state. With the temperature shift Goodwin's equation becomes:

$$\frac{P - P}{T' - T_t} = A e - \frac{\alpha}{T'} + BT'$$

where T' = T + 0.003 in kelvin, A = 30.3312,  $\alpha = 5.693$ , B = 2/3, P<sub>t</sub> = 0.0695 atm and T<sub>t</sub> = 13.803.

3.3 The Heats of Fusion at Elevated Pressures

These values were determined experimentally by Dwyer, et al. (1965b). The authors represent the experimental results by a straight line in pressure. We select the value of 117.277 J/mol (28.03 cal/mol, Woolley, et al., 1948) for the heat of fusion at the triple point, partially to remain consistent with the earlier thermodynamic calculations, and partially because this value is quite close to the average of all experimental determinations (see table 9-3, Roder, et al., 1973). Shifting the Dwyer, et al. equation to pass through the selected value the equation used for the heats of fusion becomes:

$$\Delta H_{\text{function}} = (28.02693164 + 0.044149P) \cdot 4.184$$

where  $\Delta H_{fusion}$  is in J/mol and P in atm. The uncertainty in  $\Delta H_{fusion}$  remains essentially as estimated by Dwyer, et al. (1965b), around 1%.

#### 3.4 Property Calculations

To find the values of the various properties on the solid boundary we calculate the volume and entropy changes from the Clausius-Clapeyron equation. The melting pressure equation and the heats of fusion were given in the previous sections. The relations are:

 $P = P_{melt}(T)$ 

 $\frac{dP}{dT} = \frac{d(P_{melt})}{dT}$ 

 $V_{\text{solid}} = V_{\text{liquid}} - \Delta V_{\text{fusion}}$  with  $\Delta V_{\text{fusion}} = \frac{\Delta H \text{ (fusion)}}{T \frac{dP}{dT}}$ 

 $H_{solid} = H_{liquid} - \Delta H_{fusion}$ 

 $S_{solid} = S_{liquid} - \Delta S_{fusion}$ , with  $\Delta S_{fusion} = \Delta H_{fusion}/T$ .

The internal energy for the solid follows from the thermodynamic relation U = H - PV.

#### 3.5 Thermodynamic Consistency Checks

Since the available set of data is limited, the checks that can be made are limited also. We can examine the change of volume on fusion as a function of temperature. We expect the volume change to decrease as the temperature increases, it does. The values obtained from the heats of fusion through the Clausius-Clapeyron equation are in excellent agreement with the experimental volume changes published by Bartholome (1936) for normal hydrogen as shown in table 1.

	Table 1.	Volume Changes or	n Fusion at Elevated Temperatures	
т		Bartholome	This Report	90
13.96		2.83	2.81	.58
16.43		2.31	2.26	2.15
18.24		2.03	2.02	.61

Considering nitrogen and argon we would expect that the entropy change on fusion for hydrogen should decrease as the temperature increases. Quantitative comparisons cannot be made; however, this expectation is at least qualitatively fulfilled.

4. THE SOLID-VAPOR REGION FOR HYDROGEN

Prior work on the thermodynamic properties of this region include calculations by Mullins, et al. (1961), the T-S chart by Sindt and Mann (1966) and the survey by Roder, et al. (1973). The thermodynamic properties along the vapor boundary of this region are available from the intersection of the 32-term MBWR (Roder and McCarty, 1975) and the solid vapor pressure curve defining the boundary of the region. The elements required to complete the description of the region are the reference point for all properties, the vapor pressure equation of the solid, the density of the solid, and the heat capacity of the solid.

#### 4.1 The Reference Point

We wish to integrate this region in a thermodynamically consistent way with the basic 32-term equation of state. The simplest thing we can do is to refer the properties of the solid at the triple point to those obtained from the 32-term MBWR for the liquid at the triple point. Specifically, we require that at the triple point temperature:

vapor pressure of the solid = vapor pressure of the liquid

 $V_{solid} = V_{liquid} - \Delta V_{fusion}$  $H_{solid} = H_{liquid} - \Delta H_{fusion}$  $S_{solid} = S_{liquid} - \Delta S_{fusion}$ 

Internal energy of the solid follows through the thermodynamic relation U = H - PV.  $\Delta H_{fusion}$ , the heat of fusion selected for the triple point is 117.277 J/mol (see section 3.3).  $\Delta S_{fusion}$ , the entropy change on fusion is defined thermodynamically as  $\Delta H_{fusion}/T$ .  $\Delta V_{fusion}$ , the volume change on fusion is calculated from the Clausius-Clapeyron equation and the melting pressure derivative (see section 3.4). The result for the triple point with  $T_t = 13.800$  K is  $\Delta V_{fusion} \approx 2.86_4$  cm<sup>3</sup>/mol.

Having established a reference point or benchmark we can look next at the description of the remainder of the region.

4.2 Vapor Pressure of the Solid

One of the drawbacks of the earlier calculation by Mullins, et al. (1961) is that the authors presented no explicit equation for the vapor pressure of the solid, indeed they could not because one can either force exact thermodynamic consistency or use an explicit vapor pressure equation, but not both. Experimental measurements of the vapor pressure of solid hydrogen exist to quite low temperatures (Woolley, et al., 1948; Borovik, et al., 1960; and Harrison, et al., 1962). However, we will use these values only as a check on the extrapolation of the vapor pressure curve to low temperatures.

The form of the vapor pressure equation is dictated by thermodynamics. Integration of the Clausius-Clapeyron equation assuming the vapor phase to be an ideal gas leads to the Kirchhoff-Rankine equation:

 $\log P = A/T + B \log T + C .$ 

We use this equation but subject it to the following constraints:

- P<sub>t</sub> = 0.0695 atm, T<sub>t</sub> 13.800 K. To insure that this equation intersects the melting equation and the liquid vapor pressure equation at the triple point which is defined by the liquid vapor pressure equation used with the 32-term MBWR.
- 2.  $\frac{dP}{dT}$  at the triple point temperature = 0.04566744 atm/K. This constraint defines the derivative dP/dT of the solid vapor pressure curve at the triple point temperature, and through the Clausius-Clapeyron equation the heat of sublimation. The value of the derivative is chosen so that:

 $\Delta H_{sublimation} = \Delta H_{fusion} + \Delta H_{vaporization}$ 

where  $\Delta H_{fusion}$  is the value chosen in sections 3.3 and 4.1, and the  $\Delta H_{vaporization}$  is determined by the 32-term MBWR and its companion liquid vapor pressure equation.

3. That the vapor pressure at 10 K be 0.00255940 atm. The last requirement is the best compromise to insure thermodynamic consistency of the heat of sublimation down to 10 K. The point is discussed in more detail in the section on thermodynamic consistency below.

With 3 degrees of freedom and three constraints the coefficients of the solid vapor pressure equation are uniquely determined. They are:

A = -90.77568949 B = 2.489830940 and C = 4.009857354

where P is in mm Hg and T is in K.

Intercomparison to the available experimental vapor pressures shows the maximum deviation in pressure down to 10 K is less than 1%. The simple equation cannot, however, represent the data down to low temperatures, say 3 or 4 K. In this temperature range the departure between predicted and experimental vapor pressures increases to nearly 200%. Additional terms in the vapor pressure equation improve the representation of the vapor pressures but not the heats of sublimation calculated from the vapor pressure derivative.

#### 4.3 Density of the Solid

From the survey by Roder, et al. (1973) we select the solid volumes published by Ahlers (1963) primarily because we expect these values to be in accord with the heat capacity measurements selected in the next section. More recent publications (Anderson and Swenson, 1974) prefer values which differ by as much as 1.5% from the ones selected especially at the lower temperatures. Ahlers' results can be represented by a parabolic function from 6 to 13.8 K. We shift this function to pass through the designated value of the solid density at the triple point. The resulting relation is:

$$\frac{1}{\rho_{\text{solid}}} = V_{\text{solid}} = 22.77963478 - 0.031T + 0.005T^2$$

with  $V_{solid}$  in cm<sup>3</sup>/mol and T in K. We estimate that the values of the solid should be in error by no more than 0.4% at the triple point, and that the error could increase to as much as 1.5% at 4 K or lower.

#### 4.4 Heat Capacity of the Solid

We require heat capacity values for the solid at saturation. The values selected were derived by Ahlers (1963) from his measurements of  $C_V$  in the single phase solid. We prefer these values to earlier measurements because

a closed loop third law check of entropy using these values is much more consistent than checks using the earlier measurements (See Roder, et al., 1965). Since several conventional representations do not seem to apply to the values for hydrogen, we settled on a simple interpolating polynomial which returns Ahlers' values to within 0.3% from 14 K down to 5 K. Maximum deviations down to 3 K are 1.65%, but the polynomial should not be used below 3 K. The power series used to represent  $C_{SAT}$  is:

 $C_{SAT} = -101. + 87.75 T - 26.95833333 T^2 + 4.25 T^3 - 0.0416666667 T^4$ 

with  $C_{\text{SAT}}$  in milli Joules/mole and T in K.

We use the heat capacity in the thermodynamic relations:

$$\Delta H = \int_{T}^{T} C_{SAT} dT \text{ and } \Delta S = \int_{T}^{T} C_{SAT} dT$$

to calculate the changes in enthalpy and entropy from the reference values for the solid at the triple point.

#### 4.5 Thermodynamic Consistency Checks

Once the vapor pressure of the solid is defined, we can perform a consistency check in the following way. We calculate the heat of sublimation first by taking the difference between vapor and solid enthalpies at the boundary, and second by calculating it from the Clausius-Clapeyron equation using solid and vapor volumes and the derivative of the solid vapor pressure curve. The enthalpy of the vapor is obtained from the 32-term equation of state, we note that these enthalpies depend on the specific heat of the ideal gas which is not defined below 10 K in the equation of state programs. The enthalpy of the solid is obtained from the integration of the heat capacity of the solid. The difference of these two values, the heat of sublimation, calculated in this way is not particularly sensitive to the value of pressure chosen. In the other calculation, however, the heat of sublimation depends on the vapor volume obtained from the equation of state and on the derivative of the solid vapor pressure curve and is quite sensitive to changes in pressure. We select the value of the pressure at 10 K, the third constraint, to minimize the departures between the heats of sublimation calculated by the two different methods between 13.8 and 10 K. The intercomparison of the heats of sublimation is shown in table 2; the departures do not exceed 0.1%.

	Table 2. Intercomparison o	of the Heats of Sublimati	on of Hydrogen
T K	∆H (sublimation) from the boundaries J/mol J/mol	ΔH (sublimation) from Clausius-Clapeyron Eq. J/mol	the Difference in percent
10	961.234	960.300	0.10
11	979.262	979.169	0.01
12	996.088	996.584	-0.04
13	1011.351	1011.900	-0.05
13.8	1022.137	1022.137 d	lefined to be the same

#### 5. THE SOLID-LIQUID REGION FOR OXYGEN

With the exception of the melting curve and the heat of fusion at the triple point prior work on the properties of this region is non-existent. We are therefore forced to <u>estimate</u> all of the thermodynamic properties from the Clausius-Clapeyron equation using other simple gases as model fluids. The thermodynamic properties along the liquid boundary of this region are defined from the intersection of the 32-term MBWR equation of state and the melting pressure equation presented by Weber (1977b). Weber's version of the 32-term MBWR rather than an earlier version (Stewart, et al., 1972) is used because it includes new values of PVT (Weber, 1977a) which go to high pressures ( $\sim$  800 bar). An additional advantage of Weber's formulation is that the vapor pressure curve and the melting line intersect at the defined triple point. In the sections that follow we describe the reference values chosen for the property calculations, the melting pressure equation of the solid, and the property estimation.

#### 5.1 The Reference Values

Since the available set of data is limited, we are forced to calculate changes in properties for this region from the Clausius-Clapeyron equation. To obtain values for the solid boundaries these changes are applied from the liquid boundary. In effect, for a given temperature the values obtained from the 32-term equation of state and the melting line are used as a starting point, or point of reference. At the triple point temperature the procedure leads to values for the solid that are used as a reference point for the solid-vapor region (see section 6.1). The enthalpy departure at the triple point has been estimated by Weber (1977b) to be about 3 J/mol.

#### 5.2 The Melting Pressure Equation

The equation used is the one developed by Weber (1970) as modified by him (Weber, 1977a,b) to pass through the defined triple point. The equation reads

$$P = P_{+} + P_{0} [(T/T_{+})^{C} - 1]$$

with  $T_t = 54.359 \text{ K}$ ,  $P_t = 0.0014451 \text{ atm}$ ,  $P_o = 2637.33 \text{ atm}$ , and c = 1.769. 5.3 Property Estimation

To estimate values of the various properties on the solid boundary of this region we will use the Clausius-Clapeyron equation. To do this we must make an educated guess as to how the heat of fusion, or the volume change on fusion, or the entropy change on fusion depends on pressure (or temperature). Considering the known behavior of hydrogen, argon, and nitrogen we postulate that oxygen should obey the following qualitative criteria:

- The heat of fusion should increase as either pressure or temperature is increased,
- The entropy of fusion should decrease as either pressure or temperature is increased, and
- The volume change on fusion should decrease as either pressure or temperature is increased.

Direct scaling of the volume change for oxygen from hydrogen, argon, or nitrogen (see page 53, Sindt, Ludtke and Roder, 1970) is not successful; one of the criteria remains unfulfilled. Adopting a sort of an average between the two extreme assumptions

1.  $\Delta H_{fusion}$  (T or P) = constant, and 2.  $\Delta S_{fusion}$  (T or P) = constant

allows us to fulfill all three criteria over a range of experimentally plausible pressures, say up to 5000 psia. As for hydrogen we express the heat of fusion of oxygen as a linear function of pressure

 $\Delta H_{fusion} = (106.3 + 0.01126 P) \cdot 4.184$ 

where  $\Delta H_{fusion}$  in in J/mol and P is in atm. The value 106.3 cal/mol is taken at the triple point from the paper by Giauque and Johnston (1929). The uncertainty in the estimated heat of fusion should be no larger than the variation estimated for it, i.e., a maximum of 6% at the highest pressures.

With an estimate for the heat of fusion in hand the property calculations follow the relations given in section 3.4. Obviously, consistency checks cannot be made for this region.

6. THE SOLID-VAPOR REGION FOR OXYGEN

Prior work on the thermodynamic properties of this region includes the calculations by Mullins, et al. (1962). The thermodynamic properties along

the vapor boundary of this region are available from the intersection of the 32-term MBWR (Weber, 1977b) and the solid vapor pressure curve defining the boundary of the region. The elements required to complete the description of the region are the reference point for all properties, the vapor pressure equation of the solid, the density of the solid, and the heat capacity of the solid.

#### 6.1 The Reference Point

The reference point for this region is defined in exactly the same way as for hydrogen (see section 4.1). The heat of fusion at the triple point was experimentally measured by Giauque and Johnston (1929) to be 106.3 cal/mol (444.8 J/mol). The triple point temperature, 54.359 K, and the melting pressure equation are taken from Weber (1977b). The volume change on fusion at the triple point becomes approximately 0.940  $_{\rm g}$  cm<sup>3</sup>/mol.

6.2 Vapor Pressure of the Solid

The same general remarks apply to oxygen as they did to hydrogen. The vapor pressure equation is of the Kirchhoff-Rankine type

 $\log P = \frac{-1096.562485}{T} - 2.025578307 \log T + 28.35976524$ with T in kelvin and P in mm Hg. The constraints used are:  $P_{t} = 0.0014451 \text{ atm}, T_{t} = 54.359 \text{ K},$   $2. \frac{dP}{dT}\Big|_{t} = 0.000482427 \text{ atm/K}, \text{ and}$ 

3. P = 0.000019200 atm at 44 K.

Intercomparisons with the available experimental vapor pressures of Aoyama and Kanda (1936) down to the  $\beta-\gamma$  solid transition show departures of up to 30% in pressure.

#### 6.3 Density of the Solid

Oxygen is an interesting solid because it occurs in three different solid structures. We are interested here only in the so-called  $\gamma$ -solid which exists between the temperatures of 43.801 K (Kemp and Pickup, 1972) and the triple point, 54.359 K. For this range of temperatures the thermal expansion measurements of Manzhelii, et al. (1966) the absolute measurement of Tolkachev and Manzhelii (1965) and the x-ray measurements of Barrett, et al. (1967) are in reasonable agreement, i.e., within 0.6%. We represent the experimental results with a parabolic function forced to pass through the designated value at the triple point. The relation is

 $\frac{1}{\rho_{\text{solid}}} = V_{\text{solid}} = 23.2808187 - 0.06772142868 \text{ T} + 0.001339285715 \text{ T}^2$ 

with  $V_{\text{solid}}$  in cm<sup>3</sup>/mol and T in K. The solid densities should be in error by no more than 0.6% in the range of temperatures covered.

#### 6.4 Heat Capacity of the Solid

The experimental measurements on the  $\gamma$ -solid by Giauque and Johnston (1929) were represented by Mullins, et al. (1962) with a simple polynomial which is retained here

 $C_{SAT} = 16.908081 - 0.24181777 T + 0.0024809089 T^2$ 

with  $C_{SAT}$  in cal/mol (4.184 J/cal) and T in kelvin. Departures of the polynomial from the measured points are no larger than the stated error in the measurements, i.e., about 0.5% in  $C_{SAT}$ .

6.5 Thermodynamic Consistency Checks

These checks are performed as described in section 4.5 for hydrogen, except that here the temperature limitation is that of the  $\beta$ - $\gamma$  transition, i.e., 43.801 K. Results are shown in table 3. Departures between the different ways of calculating the heat of sublimation do not exceed 0.06%.

Table 3. Intercomparison of the Heats of Sublimation of Oxygen

т, к	$^{\Delta H}$ sublimation from the boundaries J/mol	$^{\Delta H}$ sublimation from the C-C Eq. J/mol	Difference J/mol
44.000	8376.665	8376.109	.556
45.000	8359.501	8359.234	.267
46.000	8342.413	8342.344	.069
47.000	8325.380	8325.433	054
48.000	8308.379	8308.497	118
49.000	8291.388	8291.527	<b></b> 139
50.000	8274.383	8274.512	129
51.000	8257.341	8257.443	102
52.000	8240.238	8240.305	067
53.000	8223.050	8223.083	033
54.000	8205.751	8205.758	007
54.359	8199.509	8199.509	defined to be the same

#### 7. THE COMPUTER PROGRAMS FOR SLUSH HYDROGEN AND SLUSH OXYGEN

The phase boundaries and representations of the different properties along the phase boundaries described in the previous sections have been combined into two computer programs. The programs are in the form of subroutines:

SLH2(TT, QQ, TP, PSL, DSL, HSL, SSL, USL) SLO2(TT, QQ, TP, PSL, DSL, HSL, SSL, USL)

where the variables in the parameter list are temperature, quality, triple point key, pressure, density, enthalpy, entropy, and internal energy.

#### 7.1 Input

The user must specify temperature and quality. He may specify the triple point key depending on the temperature.

<u>Temperature</u>. The input temperature in kelvin should be between 10 and 22.60 K for hydrogen and between 44 and 58.2 K for oxygen. The programs will return answers for temperatures less than the lower limit, but the values returned become less and less reliable the lower the temperature. For temperatures greater than the upper limit an error message is printed: "T is too high, P will exceed 5000 psia."

Quality. A value for quality must be entered such that  $0.0 \le Q \le 1.0$ . A quality of 0.0 will cause the subroutine to return values on the denser side, i.e., the values of the solid. A quality of 1.0 causes the subroutine to return values on the less dense side, i.e., values of the vapor for the solid-vapor region (temperatures below the triple point), and values of the liquid for the solid-liquid region (temperatures above the triple point). If the input Q is fractional the subroutine calculates the values of the properties on both boundaries of the region and then performs the ratio according to the equations given in section 2.2.

Triple point key. For the special case when the input temperature is exactly equal to the triple point temperature, 13.800 K for hydrogen and 54.359 K for oxygen, the user must specify through the triple point key, TP, in which region he wants the subroutine to calculate the properties. TP = 0.0 means that the program will return properties from the solid-liquid region, while TP = 1.0 insures that the program calculates the triple point properties in the solid-vapor region.

#### 7.2 Output

The output from the program is handled through the parameter list. For a given input of T and Q (TP if appropriate) the output is unique, i.e., single-valued. The values returned are the slush pressure PSL in atm, the

slush density DSL in mol/L, the slush enthalpy HSL in J/mol, the slush entropy SSL in J/mol-K, and the slush internal energy USL in J/mol.

#### 7.3 Flow Charts

The slush routines are detailed in the flow chart of figure 3. The various phase boundaries and the interiors of the solid-liquid and solid-vapor regions are keyed according to the inset, which is just a repeat of the phase diagram already shown in figure 2.

#### 7.4 Program Listings, Hydrogen

A listing of the hydrogen program is given in Appendix A. The slush hydrogen routine calls on the program deck of the parent 32-term MBWR (Roder and McCarty, 1975). Those routines of the parent deck that had to be modified to insure consistency around the triple point are also listed in Appendix A. They are:

FUNCTION PRESSM(TT), and SUBROUTINE RHOl(PP,DD,TT).

New routines developed for the slush application and listed in Appendix A are:

FUNCTION DPDTMP(TT), and

FUNCTION FINDM(P,T,D).

The first is simply the temperature derivative of the melting pressure curve, while the latter is an additional density finder. The FINDM routine differs from the normal FINDD density finder in that it requires a reasonable trial density in its calling parameters.

#### 7.5 Program Listings, Oxygen

A listing of the oxygen program is given in Appendix B. The slush oxygen routine calls on the program deck of the parent 32-term MBWR (Weber, 1977b). Routines not available with the parent deck, or those that had to be modified are listed in Appendix B as well. They are:

```
FUNCTION FINDT(P,D)
SUBROUTINE Tl(PP,DD,TA)
FUNCTION PMELT(PP)
FUNCTION PRESSM(TT)
FUNCTION DPDTMP(TT)
```

#### 7.6 Test Programs, Sample Output

A sample program for hydrogen is shown in Appendix C; in Appendix D for oxygen. The output from the test program for hydrogen in the form of an abbreviated table of values with particular attention to the triple point is given in table 4; the companion output for oxygen in table 5.

#### Subroutine SLH<sub>2</sub> (TT,QQ,TP,PSL,DSL,HSL,SSL,USL) Subroutine SLO<sub>2</sub> (TT,QQ,TP,PSL,DSL,HSL,SSL,USL)



The sample programs are intended to serve as test decks for running at other installations. They include a call to every possible combination of T and Q in the regions solid-liquid and solid-vapor. To round out the list of examples the liquid-vapor region, which is obtained from the parent 32-term MBWR, has also been illustrated.

The astute observer will note that the various properties in lines 4 and 7 of tables 4 and 5 and also lines 6 and 14 and lines 9 and 13 should be pairwise identical, except of course for Q and TP. To the extent that these lines are not identical thermodynamic inconsistencies remain. One of the inconsistencies arises from the fact that we carry 10 digits in the coefficients of the vapor pressure equations and the melting line. The pressures returned from each of the different functions at the triple point temperature are very nearly the same, however, they are not identical in every bit of the computer word. Entering the 32-term equation of state with slightly different values of the pressure results in slightly different values of vapor densities returned. The disagreement in entropy between lines 6 and 14 arises from an inconsistency inherent in the equation of state. This is shown simply by the fact that the  $\Delta H$  between lines 13 and 14 of tables 4 and 5 divided by the triple point temperature is not equal to the  $\Delta S$  between lines 13 and 14. Several other discrepancies are attributable to rounding errors.

#### 7.7 Unit Conversions

Common conversion factors for use with hydrogen are given in Appendix E, while those for use with oxygen are shown in Appendix F.

#### 8. ERROR ESTIMATES, FURTHER WORK

Whenever possible estimates of uncertainty were given in the sections that described the fitting or representation of a particular piece of experimental data. We summarize these uncertainties as maximum errors in the different properties used in the computer programs in table 6.

					•			
SULID-VAPOR I.		a	Ч1	P. AIM	RHJ, MOL/L	H. J/MOL	S. J/MOL-K	UH/L .U
12.00	16 SOLIU.	0.0		.01829542	43.238317	-748.379	. 869	-748.422
12.00	JO MIX, Q IS FRACTIONAL =	• 2		.01829542	.037373	-250.087	42.393	-299.689
12.ju	.U VAPOR.	1.0		.01829542	.018695	248.205	83.917	149.044
13.81	JO SULID.	Ū•0	1.0	.06950.000	42.911024	-740.206	1.500	-740.370
13.30	06 MIX, Q IS FRACTIONAL =	•2	1.0	.06950000	.124584	-229.138	38.534	-285.663
13.00	JU VAPOR.	1.0	1.0	.06950000	.062382	281.930	75.568	169.044
SOLID-LIQUID T.		Э	ТР	P, AIM	RHD. MOL/L	H, J/MOL	S. J/HOL-K	Nº J/HOL
13.80	JŪ SOLIC.	0•0	0•0	.06950000	42.911024	-740.206	1.500	-740.370
13.31	JU MIX, Q IS FRACTIONAL =	2	ũ. 0	.06950,000	40.426679	-681.568	5.749	-681.742
13.8(	so LIQUID.	1.0	0•0	.06950000	38.214254	-622.929	966°6	-623.113
15.00	JO SOLID,	0•0		36.97621298	43.462170	-646.201	2.008	-732.405
15.01	ון MIX, ע IS FRACTIONAL =	• 22		36.97621298	41.191453	-584.153	6.144	-675.109
15.00	JO LIQUID.	1.0		36.97621298	39.146225	-522.106	10.281	-617.814
LIGUID-VAPOR I.	< FROM THE 32 TERM EQ.	a	ЧI	P. AIM	RHJ, MOL/L	H, J/MOL	S. J/MOL-K	U, J/MOL
13.80	JD LIQUID.	0 • Ū		.06950000	38.214255	-622 • 929	866°6	-623.113
13.61	10 VAPOR.	1.0		.06950000	.662382	281.931	75.562	169.045
15.00	ud LIQUID.	0•0		.13255089	37.701467	-605.065	11.225	-605.421
15.00	JU VAFUM.	1.0		.13255089	.110456	303.714	71.613	182.121

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Table 4. Test Values, Hydrogen

		Table	5.	Test Values,	Oxygen			
SOLID-VAPOR T,K		0	ЧI	P, AIM	RH0. МОL/L	H, J/MOL	S, J/MOL-4	C N, J/MOL
50 • 0 00	SOLID.	0 • 0		.00029489	43.023777	-6827.487	55.065	-6927.488
50.00	MIX, Q IS FRACTIONAL	= • 5		•00029489	.000143760	-2690.231	137.810	-2898.074
50.000	VAPOR,	1.0		.00029489	.000071880	1447.026	220.555	1031.339
54 • 359	SOL ID .	0•0	1.0	.00144510	42.450216	-6625.977	58.92A	-6625.981
54.359	MIX, Q IS FRACTIONAL	= • 5	1.0	.00144510	.000648120	-2526.223	134.348	-2752.145
54.359	VAPOR,	1.0	1.0	.00144510	.000324062	1573.532	209.768	1121.691
SOLID-LIQUID T,K		J	цр	P. AIM	КНО, МОL/L	H, J/MOL	- 10W/F •S	<pre>n J/MOL</pre>
54 • 359	SOLID.	0•0	0.0	.00144510	42.450216	-6625.977	58.928	-fé25,981
54.359	MIX, C IS FRACTIONAL	یں •	0°C	.00144510	41.619127	-6403.598	63.019	-6403.601
54.359	LIQUIG,	1 • 0	0.0	.00144510	40.819955	-6181.218	67.110	-f181.222
56.00	SOLID.	0.0		142.47358043	42.695008	-6257.056	59.469	-6595.178
56.000	MIX, Q IS FRACTIONAL	ш • #		142.47358043	41.884860	-6031.320	63.500	-6375.982
56.000	LIQUID,	1.0		142.47358343	41.10484	-5805.584	67.531	-6156.797
LIQUID-VAPOR T,K	FROM THE 32 TERM EQ.	J	ЧI	P. ATM	R40, MOL/L	H. J/MOL	S, J/MOL-1	K U, J/MOL
. 54.359	LIQUID.	0•0		.00144516	40.819955	-6181.218	67 • 1 1 0	-6181.222
54.359	VAPOR,	1.0		.00144510	.000324062	1573.531	209.813	1121.690
56.000	LIGUID.	0°0		.00233370	40.595344	-6193.793	68.695	-£093.799
56.000	VAPOR,	1.0		.00238370	.000518945	1621.103	206.515	1155.681

Table 6. Estimates of Maximum Uncertainties Variable Hydrogen Oxygen temperature 0.01 K 0.01 K 1% at the triple point 1% at the triple point pressure increasing to 200% at very increasing to 31% at 44 K. low temperatures. Negligible Negligible for pressures above for pressures above 1 atm. l atm. 0.2% at temperatures above 0.2% at temperatures above density T.P. 0.4% at the triple T.P. 0.6% for temperatures point increasing to 1.5% at below the triple point and 4 K. above the  $\beta-\gamma$  transition. enthalpy, 1.2 J/mol for solid-liquid 3 J/mol at the triple point increasing to 27 J/mol at the internal highest pressures. energy 1.5 J/mol for solid-vapor 3 J/mol at the triple point increasing to 6 J/mol at the lowest temperature. 0.08 J/mol-K for solid-0.05 J/mol-K at the triple point entropy liguid increasing to 0.46 J/mol-K at the highest pressures. .146 J/mol-K for solid-vapor 0.05 J/mol-K at the triple point increasing to 0.13 J/mol-K at the lowest temperature.

Entropy errors are approximated by considering enthalpy errors divided by the temperature and vice versa. For hydrogen the entropy departure for the solid-vapor region is taken from the closed loop third law calculation of Roder, et al. (1965). For the solid-liquid region we use the experimental estimate of 1% in measured heats of fusion published by Dwyer, et al. (1965b). For oxygen we use a value of 3 J/mol as error estimate in enthalpy (Weber, 1977b) and add to this either 6% of the heat of fusion to get the solid-liquid departures, or the enthalpy equivalent of 0.5% of the values of  $C_{\rm SAT}$  to get the solid-vapor deviations. The rather large discrepancies described in an earlier version of this report (letter report, June 1977) have indeed been resolved, i.e., reduced considerably, by using a PVT surface which is consistent with the melting line and the triple point.

The work described here has led indirectly to a review of the molar volume of solid oxygen (Roder, 1977). One conclusion of that review is that the volume change on fusion at the triple point is uncertain by about 0.6%. Further experimental work to accurately measure this volume change at essentially zero pressure is recommended. Additional experimental work on oxygen may be required particularly if large scale use of slush oxygen and hydrogen is likely. The sponsor should arrange to have the dielectric

constant of oxygen reviewed and measured for the solid since this property will be required for quantity gaging. In section 5 we indicate that the thermodynamic properties for the solid-liquid region for oxygen had to be estimated. Some experimental measurements are required to define the properties adequately. We suggest that measurements of the heat of fusion or the volume change on fusion be conducted for oxygen at elevated pressures. An alternative possibility is to measure heat capacity values for oxygen in the solid state. Finally, a review of Prandtl and Grashoff numbers should be made, to include values of  $C_p$ ,  $C_v$  thermal conductivity and viscosity. Several of these properties are presently not defined for a slush regime, yet they will be needed to define heat transfer characteristics.

#### 9. SUMMARY

Computer programs to describe the thermodynamic properties of slush hydrogen and slush oxygen have been developed. The range of temperature for these programs is from several degrees below the triple point to several degrees above the triple point. The upper temperature limit coincides with a pressure limit of about 5000 psia  $(34 \text{ MN/m}^2)$ . In the case of oxygen the experimental data are very limited and the properties calculated are in the nature of a "best estimate." The equilibrium and thermodynamic properties included are temperature, pressure, density, enthalpy, entropy, internal energy, and quality. Input to the programs is temperature and quality, the remaining variables are outputs.

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#### APPENDIX A. PROGRAM LISTINGS HYDROGEN

```
SUBROUTINE SLH2(TT,QQ,TP,PSL,DSL,HSL,SSL,JSL)
  THERMODYMAMIC PROPERTIES FOR SOLID-VAPOR OR SOLID-LIQUID REGIONS
  TEMPERATURE IT MUST BE BELOW 22.6 K
  QUALITY QQ, 0. IMPLIES PROPERTIES ON THE DENSER SIDE
              1. IMPLIES PROPERTIES ON THE LESS DENSE SIDE
              FRACTIONAL QQ BETWEEN J. AND 1. PERMISSABLE
              OTHER VALUES OF QQ INVALID
  FOR THE SPECIAL CASE OF T=TRIPLE POINT TP=0. MEANS SOLID-LIQUID
                                          TP=1. MEANS SOLID-VAPOR
  DATA (VP1=-90.77568949), (VP2=2.489830940), (VP3=4.009857354)
  JATA (CP1=-101.), (CP2=87.75), (CP3=-26.95833333), (CP4=4.25),
 1 (CP5=-0.04166666667)
  DATA (V1=22.77963473), (V2=-0.031), (V3=0.005)
  DATA (TTP=13.800), (TUP=22.63), (HTP=-743.206291), (STP=1.4999590)
  T = TT
  Q=20
  PSL=DSL=HSL=SSL=JSL=0.
  IF(T.LT.TUP) GO TO 1
  PRINT 2
2 FORMAT(5X,39HT TOO HIGH, P WILL EXCEED 5000 PSIA)
  RETURN
1 IF (Q.GE.G. .AND. Q.LE.1.J) GO TO 5
  PRINT 4
4 FORMAT(5X, 14HQ OUT OF RANGE)
  RETURN
5 IF(T-TTP) 6,7,8
  ENTER HERE FOR TRIPLE POINT
7 IF(TP.EQ.0.0) GO TO 8
  ENTER HERE FOR SOLID-VAPOR PROPERTIES
D PSL=EXP(VP1/T+VP2*ALOG(T)+VP3)/760.
  DPDT=PSL+(-VP1/T++2+VP2/T)
  VSOL= V1+V2*T+V3*T**2
  05L=1000./V50L
  HSL=HTP-(CP1*(TTP-T)+CP2/2.*(TTP**2-T**2)+CP3/3.*(TTP**3-T**3)
 1 +CP4/4.*(TTP**4-T**4)+CP5/5.*(TTP**5-T**5))/1000.
  SSL=STP-(CP1*(ALOG(TTP)-ALOG(T))+CP2*(TTP-T)+CP3/2.*(TTP**2-T**2)
 1 +CP4/3.*(TTP**3-T**3)+CP5/4.*(TTP**4-T**4))/1000.
  USL=HSL-PSL/0SL+101.325
 USOL=USL
  IF (Q.EQ.G.L) RETURN
  CONTINUE HERE FOR VAPOR PROPERTIES
  DVAP=FINDH(PSL,T.0.06)
  VVAP=1030./DVAP
  DELV=VVAP-VSOL
  DELH=BELV*T*DPDT*0.101325
  DELS=DELH/T
  UVAP=HSL+DELH-PSL/(1000./(DELV+1000./OSL))*101.325
  DELU=UVAP-USOL
  IF(Q.NE.1.3) GO TO 9
  USL=1000./(UELV+1000./DSL)
  HSL=HSL+DELH
  USL=HSL-PSL/DSL+131.325
  SSL=SSL+DELS
  RETURN
  CONTINUE HERE WITH FRACTIONAL Q
9 0SL=1030./(Q*DELV+1030./0SL)
  HSL=Q#DELH+HSL
  SSL=Q*DELS+SSL
```

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USL=3\*DELU+USL RETURN ENTER HERE FOR SOLID-LIQUID PROPERTIES 3 PSL=PRESSM(T) DFOT=OPCIMP(T) DSL=FINDM(PSL,T,43.) HSL=ENTHAL (PSL, DSL, T) USL=HSL-PSL/DSL\*101.325 ULIG=USL SSL=ENTROP(JSL,T) IF (Q.EQ.1.0) RETURN CONTINUE HERE FOR SOLID PROPERTIES DELH=(23.02693164+0.044149\*PSL)\*4.184 DELV=DELH/T/OPDT/0.0242179/4.1 8+ DELS=DELH/T DSL=1000./(1000./CSL-CELV) USOL=HSL-DELH-PSL/DSL\*101.325 JELU=ULIQ-USOL IF(Q.NE.C.2) GO TO 10 HSL=HSL-DELH SSL=SSL=CELS USL=USOL RETURN CONTINUE HERE WITH FRACTIONAL Q 1) OSL=1000./(Q+DELV+1000./OSL) HSL=HSL-G+DELH SSL=SSL-Q\*DELS USL=USL-G\*DELU RETURN END FUNCTION PRESSM(TT) CALCULATES MELTING PRESSURE FROM AN INPUT TEMPERATURE T=TT+J.003 21 PS=.0695+(T-13.803)\*30.3312\*EXP (-5.693/T)+(T-13.803)\*2.0\*T/3.0 19 PRESSMEPS RETURN END SUBROUTINE RH01(PP,CO,TT) 1ST CUT AT RHO FROM P=A+B\*T REALLY AN ITERATION, BUT IT MAY BE SMALL ENOUGH AND FAST ENOUGH P IN ATM, T IN K, RHO IN MOLES/LITER JIMENSIUN RHO(43) + A(43) + B(+3) DATA((RHC(I),I=1,43)=1.,2.,3.,4.,5.,6.,7.,8.,9.,10.,11.,12.,13.,14 1.,15.,15.,17.,18.,19.,20.,21.,22.,23.,24.,25.,26.,27.,28.,29.,30., 231.,32.,33.,34.,35.,36.,37.,38.,39.,40.,41.,42.,43.) DATA((A(I), I=1,43)=-.29599325741,-1.1363466175,-2.4851378102,-4.30 141059317,-0.509655393,-9.2559185405,-12.336266965,-15.783961531,-1 29.573370659,-23.531041295,-28.036458235,-32.772558951,-37.72660671 33,-+2.9+2371352,-43.424-32541,-54.194465142,-60.237553106,-66.7267 +a+771,-73.516513375,-80.6+3765419,-88.J79905894,-95.751501825,-1J3 5.63363091,-111.727778-2,-113.7997-172,-127.786579,-135.94257761,-1 5+3.83334352,-151.265+996+,-157.995J8463,-163.7188357,-167.27870589 7,-169.71922308,-169.7699391+,-166.30726645,-160.22970454,-149.6301 3363,-13-.663u3216,-116.11756+01,-34.293117568,-67.824247269,-36.7+ 9239582+,=1.8295576977) JATA((B(I),I=1,-3)=.035039203549,.17575158596,.27172674979,.372976 113724,.47352311465,.53141278615,.73864366352,.83124634142,.9592344 2911+,1.59233u2553,1.2322367731,1.3776+55689,1.5294993193,1.6883212 3266,1.35+82+9913,2.030035+20,0.2151006109,2.411267-735,2.619508066

С

С

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0

```
45,2.3407043212,3.0756450876,3.325048554,3.5895525008,3.8696893541,
     54.1658593639,4.4782981944,4.8204022069,5.1840092761,5.569646053,5.
     69772524362, 6.4057175531, 6.3214242239, 7.2780697825, 7.7404616534, 8.1
     7972575502, d . 6358460465, 9. 0473286076, 9. + 260953807, 9. 8132635045, 10. 2
     822281363,10.63012984,11.05913823,11.565307194)
   10 P=PP
      T=TT
      IP=1
      PLO=0.
      CHECK INPUT DATA FOR RANGE
С
     INPUT RESTRICTIONS REMOVED
С
С
      IF(P.GT.350.) GO TO 15
      IF(T.GT.300.1) GO TO 15
С
      GO TO 13
С
С
   15 PRINT 16
C
   16 FORMAT(24H INPUT DATA OUT OF RANGE)
      00=0.0
С
С
      RETURN
      PTP=VPN(13.8)
      IF(P.GT.PTP) GO TO 18
      IF(T.GT.13.8) GO TO 18
      D0=0.00001
      RETURN
      CHECK MELTING LINE
С
   13 IF(T.GT.43.600) GO TO 23
      PS=PRESSM(T)
      IF(P-PS) 23,21,19
   19 PRINT 22
   22 FORMAT(26H INFUT CONDITIONS IN SOLID)
   21 00=39.5
      RETURN
С
      PHASEFINDER
   23 IF(T.LT.32.938) 50 TO 27
      PPHASE=-50.6002+1.920888*T
      IF (P.GT.PPHASE) IP=15
      GG TO 36
   27 PVAP=VPN(T)
      IF (P-FVAP) 36, 32, 35
   32 PRINT 33
   33 FORMAT(53H INFUT PLACES YOU EXACTLY ON THE VAPOR PRESSURE CURVE)
      DJ=DSATL(T)
      RETURN
   35 DENL=DSATL(T)
      IF=DENL
С
      START TABLE LOOKUP HERE
   36 CONTINUE
      00 40 I=IP,43
      PCALC=A(I)+B(I)+T
      IF(P.LT.PCALC) GO TO 41
      PLO=PCALC
   4J CONTINUE
      IF(P.LT.PCALC) I=+3
      IF(P.LT.PCALC) GO TO 41
      PRINT +7
   →7 FORMAT(35H HIGH DENSITY, DUT OF RANGE FOR NOW)
      30=44.
      RETURN
   41 CONTINUE
      00 54 J=1,1J
      RHOF=J
      RHOF=RHOF/16.
      IF(I.EQ.1) GO TO 50
      AA = A(I - 1) + (A(I) - A(I - 1)) + RHOF
```

```
38=8(I-1)+(8(I)-8(I-1))*RHOF
   GO TO 52
5J AA=A(I) *RHOF
   BB=B(I) *RHOF
52 PCALC=AA+B6*T
   IF(P.LT.PCALC) GO TO 55
54 PLO=PCALC
55 FRAC=(P-PL0)/(PCALC-PL0)/10.
   00 = I-1
     =00
            +RHOF-0.1+FRAC
   บิบิ
   RETURN
   ENTRY T1
   FIRST GUESS FOR TEMPERATURE ITERATION OF FINDT
   P = PP
   0=00
   00 6J I=1,43
   IF(D.LT.RHO(I)) GO TO 61
63 CONTINUE
   I = 43
61 FPAC=D-RHO(I-1)
   IF(I.EQ.1) GO TO 63
   AA = A(I - 1) + (A(I) - A(I - 1)) + FRAC
   BB=B(I-1)+(3(I)-B(I-1))*FRAC
   GO TO 02
63 FRAC=D
   AA=A(I) + FRAC
   B3=B(I) +FRAC
52 TT=(P-AA)/33
   END
   FUNCTION OPOTMP(TT)
   NEW FOR HYDROGEN, MELTING PRESSURE DERIVATIVE
   DATA (TTP=13.803), (A1=30.3312), (AL=5.693)
   T=TT+C.003
   A2=2./3.
   EXPP=A1*EXP(-AL/T)
   OPOTMP=(T-TTP)*(EXPP*AL/T**2+A2)+EXPP+A2*T
   RETURN
   END
   FUNCTION FIND M(P,T,D)
   CHANGED, TRIAL DENSITY VIA SUBROUTINE RH01/T1, 24 FEB 1975
   CHANGED TO AGHIT A TRIAL DENSITY FOR SLUSH USE 15 DEC 76
   COMMON/DATA/G, R, GAMMA, VP, OTP
   DIMENSION G(32), VP(3)
   TYPE DOUBLEG, R, GAHMA
   TT = T
   IF (D.NE.U.) GO TO 2
   CALL RHO1(P,0,TT)
 2 00=0
   00 1] I=1,50
   CALL PRESS(PP, JD, TT)
   P2=PP
   IF (A3S (P-P2)-1.E-7*P)20,20,1
 1 CALL OPDO(PP,00,TT)
   JP=PP
   CORR=(P2-P)/UH
   JU=UD
   IF(A3S (CORR) -1.E-7*0)23,20,10
1, 00=00-00RR
20 FINO M=00
   RETURN
   END
```

С

C

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29
```

```
SUBROUTINE SLO2(TT,QQ,TP,PSL,DSL,HSL,SSL,USL)
  THERMODYMAMIC PROPERTIES FOR SOLID-VAPOR OR SOLID-LIQUID REGIONS
  TEMPERATURE TT MUST BE BELOW 58.2 K
  QUALITY QQ, 0. IMPLIES PROPERTIES ON THE DENSER SIDE
              1. IMPLIES PROPERTIES ON THE LESS DENSE SIDE
              FRACTIONAL QQ BETWEEN D. AND 1. PERMISSABLE
              OTHER VALUES OF QQ INVALID
  FOR THE SPECIAL CASE OF T=TRIPLE POINT TP=0. MEANS SOLID-LIQUID
                                          TP=1. MEANS SOLID-VAPOR
  DATA (VP1=-1096.562485), (VP2=-2.025578307), (VP3=28.35976524)
  DATA (CP1=16.908081), (CP2=-0.24181777), (CP3=0.0024809089)
  DATA (V1=23.2808187), (V2=-0.06772142868), (V3=0.001339285715)
  DATA (TTP=54.359), (TUP=58.20), (HTP=-6625.97726), (STP=58.928478)
  T = TT
  Q = QQ
  PSL=OSL=HSL=SSL=USL=0.
  IF(T.LT.TUP) GO TO 1
  PRINT 2
2 FORMAT(5X,35HT TOO HIGH, P WILL EXCEED 5000 PSIA)
  RETURN
1 IF (Q.GE.O. . AND. Q.LE.1.0) GO TO 5
  PRINT 4
4 FORMAT(5X,14HQ OUT OF RANGE)
  RETURN
5 IF (T-TTP) 6,7,8
  ENTER HERE FOR TRIPLE POINT
7 IF(TP.EQ.0.0) GO TO 8
  ENTER HERE FOR SOLID-VAPOR PROPERTIES
6 PSL=EXP(VP1/T+VP2*ALOG(T)+VP3)/760.
  DPDT=PSL*(-VP1/T**2+VP2/T)
  VSOL=V1+V2*T+V3*T**2
  DSL=1000./VSOL
  HSL=HTP={CP1*TTP+CP2*TTP**2/2.+CP3*TTP**3/3.-{CP1*T+CP2*T**2/2.
 1 +CP3*T**3/3.))*4.184
  SSL=STP=(CP1*ALOG(TTP)+CP2*TTP+CP3*TTP**2/2.-(CP1*ALOG(T)+CP2*T+
 1 CP3*T**2/2.))*4.184
  USL=HSL-PSL/DSL*101.325
  USOL=USL
  IF(Q.EQ.0.0) RETURN
  CONTINUE HERE FOR VAPOR PROPERTIES
  DVAP=FINDM(PSL,T,0.0006)
  VVAP=1000./DVAP
  DELV=VVAP-VSOL
  DELH=OELV+T+OPDT+0.101325
  DELS=DELH/T
  UVAP=HSL+DELH-PSL/(100C./(OELV+100G./OSL))*101.325
  DELU=UVAP-USOL
  IF(Q.NE.1.0) GO TO 9
  DSL=1000./(OELV+1030./OSL)
  HSL=HSL+DELH
  USL=HSL-PSL/OSL*101.325
  SSL=SSL+OELS
  RETURN
  CONTINUE HERE WITH FRACTIONAL Q
9 DSL=10C0./(Q*DELV+1000./OSL)
  HSL=Q*DELH+HSL
  SSL=G*DELS+SSL
  USL=Q*DELU+USL
```

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RETURN С ENTER HERE FOR SOLID-LIQUID PROPERTIES 8 PSL=PRESSM(T) OPOT=OPOTMP(T) OSL=FINDM(PSL,T,40.87) HSL=ENTHAL(PSL,DSL,T) USL=HSL-PSL/0SL\*101.325 ULIQ=USL SSL=ENTROP(DSL,T) IF (Q.EQ.1.0) RETURN CONTINUE HERE FOR SOLID PROPERTIES С DELH=(106.3+0.01126\*PSL)\*4.184 DELV=DELH/T/DPDT/0.0242179/4.184 DELS=DELH/T DSL=1000./(1000./DSL-DELV) USOL=HSL-DELH-PSL/DSL\*101.325 DELU=ULIQ-USOL IF (Q.NE.0.0) GO TO 10 HSL=HSL-DELH SSL=SSL-DELS USL=USOL RETURN С CONTINUE HERE WITH FRACTIONAL Q 10 DSL=1000./(Q\*DELV+1000./DSL) HSL=FSL-Q\*DELH SSL=SSL-Q\*DELS USL=USL-Q+DELU RETURN END FUNCTION FIND T(P,D) С NEW FEB 1975 COPIED FROM HYDROGEN FOR USE WITH OXYGEN С COMMON/DATA/G, R, GAMMA, VP, DTP DIMENSION G(32), VP(8) TYPE DOUBLEG, R, GAMMA PP=P 00=0 USES A FIRST GUESS IN TEMPERATURE FROM T1 С CALL T1(PP,DD,TA) TT = TA00 10 I=1,10 CALL PRESS(PP, DD, TT) P2=PP IF (ABS (P-P2)-1.E-7\*P)20,20,1 1 CALL DPDT(PP,DD,TT) DP=PP CORR=(P2-P)/DP IF (ABS (CORR) -1.E-5 )20,20,10 13 TT=TT-CORR 20 FIND T=TT RETURN END SUBROUTINE T1(PP,DD,TA) С SPECIAL SETUP FOR TANK-P OXYGEN TA=99. RETURN END

```
FUNCTION PMELT(PP)
      INVERSE MELTING PRESSURE FOR 02, INPUT P, ATM OUTPUT T,K
С
      NEW WEBER REFERENCES
С
      DATA (P0=2637.33), (CC=1.769), (TTP=54.359), (PTP=0.0014451)
      BRA= (PP-PTP )/P0+1.0
      TEMP=ALOG(BRA)/CC
      PMELT=EXP(TEMP)*TTP
      RETURN
      END
      FUNCTION PRESSM(TT)
      MELTING PRESSURE FOR 02, INPUT T,K OUTPUT P,ATM
С
С
      NEW WEBER REFERENCES
      DATA (P0=2637.33), (CC=1.769), (TTP=54.359), (PTP=0.0014451)
      PRESSM=PTP+PO*((TT/TTP)**CC-1.0)
      RETURN
      END
      FUNCTION DPDTMP(TT)
      DERIVATIVE OF MELTING CURVE FOR OXYGEN
С
С
      NEW WEBER REFERENCES
      DATA (P0=2637.33), (CC=1.769), (TTP=54.359), (PTP=0.0014451)
      DPOTMP=PO*CC/TTP**CC*TT**(CC-1.0)
      RETURN
      END
```

```
PROGRAM VALUES (INPUT, OUTPUT)
      THIS PROGRAM TESTS THE SLUSH HYDRUGEN SUBROJTINE
С
      CALL DATAPH2
      COMBINATIONS OF SOLID - VAPOR
С
      PRINT 1
      T=12.
      Q = 0.
      CALL SLH2(T,Q,O.,PSL,OSL,HSL,SSL,USL)
      PRINT 2, T,Q,
                      PSL, DSL, HSL, SSL, USL
      Q=0.5
      CALL SLH2(T,Q,J.,PSL,CSL,HSL,SSL,USL)
                      PSL, DSL, HSL, SSL, USL
      PRINT 3, T, Q,
      Q=1.
      CALL SLH2(T.Q.J., PSL.OSL.HSL.SSL.USL)
      PRINT +,T,Q,
                      PSL, OSL, HSL, SSL, USL
      T=13.800
      TF=1.
      Q = \hat{U}.
      CALL SLH2(T,Q, TP, PSL, DSL, HSL, SSL, USL)
      PRINT 5, T, J, TP, PSL, DSL, HSL, SSL, USL
      Q=3.5
      CALL SLH2(T,Q,TP,PSL,DSL,HSL,SSL,USL)
      PRINT 6, T, U, TP, PSL, DSL, HSL, SSL, USL
      2=1.
      CALL SLH2(T,0,TP,PSL, DSL, HSL, SSL, USL)
      PRINT 7, T, Q, TP, PSL, DSL, HSL, SSL, USL
      COMBINATIONS OF SOLID - LIQUID
С
      PRINT 3
      T=13.200
      TF=ú.
      Q=G .
      CALL SLH2(T, Q, TP, PSL, DSL, HSL, SSL, USL)
      PRINT J,T,Q,TP,PSL,DSL,HSL,SSL,USL
      Q=0.5
      CALL SLH2(T,Q,TP,FSL,CSL,HSL,SSL,USL)
      PRINT10, T, Q, TF, PSL, DSL, HSL, SSL, JSL
      Q=1.
      CALL SLH2(T,Q,TP,PSL,DSL,HSL,SSL,USL)
      PRINT11, T, Q, TP, PSL, DSL, HSL, SSL, USL
      T=15.
      2=0.
      CALL SLHEUT, Q, J., PSL. DSL, HSL, SSL, USL)
      PRINT12, T, G,
                      PSL, CSL, HSL, SSL, USL
      2=0.5
      CALL SEH2(T,Q,0.,PSL,OSL, HSL,SSL,USL)
      PRINT13.T.Q.
                      PSL, DSL, HSL, SSL, USL
      3=1.
      CALL SLH2 (T, C, J., PSL, CSL, HSL, SSL, USL)
      PRINT14, T, G, PSL, DSL, HSL, SSL, USL
      COMBINATIONS OF LIQUID - VAPOR FROM THE 32 TERM EQ.
      PRINT 15
      T=13.300
      2=3.
      PSL=VPN(T)
```

```
OSL=FINDM(PSL.T.38.)
  HSL=ENTHAL (PSL, DSL, T)
  USL=HSL-PSL/DSL+101.325
  SSL=ENTROP(DSL,T)
  PRINT16, T, Q, PSL, DSL, HSL, SSL, USL
  Q=1.
  DSL=FINOM(PSL,T,0.36)
  HSL=ENTHAL (PSL, DSL, T)
  USL=HSL-PSL/DSL+101.325
  SSL=ENTROP(DSL,T)
  PRINT17, T.G.
                 FSL, ÜSL, HSL, SSL, USL
  T=15.000
  Q=3.
  PSL = VPN(T)
  DSL=FINDM(PSL,T,38.)
  HSL=ENTHAL(PSL, DSL, T)
  USL=HSL-PSL/DSL+101.325
  SSL=ENTROP(DSL,T)
  PRINT16, T, G, PSL, OSL, HSL, SSL, USL
  Q=1.
  DSL=FINDM(PSL,T,0.36)
  HSL=ENTHAL(PSL, DSL, T)
  USL=HSL-PSL/05L+101.325
  SSL=ENTROP(USL,T)
   PRINT17, T.U.
                PSL, DSL, HSL, SSL, USL
 1 FORMAT(///,52H1SOLID-VAPOR T,K
                                                              Q
                                                                  TP
 1 * P. ATM
                                                          U. J/MOL*.//)
                     RHO, MOL/L
                                  H, J/MOL S, J/MOL-K
2 FORMAT(1ux,Fs.3,24H SOLID,
                                               ,F3.1,5X
                                                          .
 1 F13.5, F14.6, F11.3, F10.3, F11.3, /)
3 FORMAT(10X.Fo.3,2+H MIX, Q IS FRACTIONAL = ,F3.1,5X
 1 F13.8, F14.6, F11.3, F10.3, F11.3, /)
+ FORMAT(10X,F3.3,24H VAPOR,
                                                ,F3.1,5X
 1 F13.8, F1+.6, F11.3, F10.3, F11.3,/)
5 FORMAT(10X,F8.3,24H SOLID,
                                                .F3.1.F5.1.
 1 F13.8,F14.6,F11.3,F10.3,F11.3,/)
5 FCRMAT(10X,F3.3,24H MIX, Q IS FRACTIONAL = ,F3.1,F5.1,
 1 F13.3.F1+.6.F11.3.F10.3.F11.3./)
 7 FORMAT(10X, F8.3, 24H VAPOR,
                                                ,F3.1,F5.1,
 1 F13.d, F14.6, F11.3, F10.3, F11.3,/)
 3 FORMAT(///,52H SOLID-LIQUID T,K
                                                              1)
                                                                  TP
 1 * P, ATM
                   RHO, MOL/L H, J/MOL S, J/MOL-K U, J/MOL+,//)
9 FORMAT(10X,F8.3,24H SOLID,
                                                ,F3.1,F5.1,
 1 F13.8, F14.0, F11.3, F10.3, F11.3,/)
1] FORMAT(16X,F3.3,2+H MIX, Q IS FRACTIONAL = ,F3.1,F5.1,
 1 F13.3,F14.6,F11.3,F13.3,F11.3,/)
11 FORMAT(1CX,F8.3.24H LIQUID.
                                                .F3.1.F5.1.
  1 F13.3, F14.6, F11.3, F10.3, F11.3,/)
12 FORMAT(10X,F5.3,24H SOLI),
                                                ,F3.1,5X
  1 F13.5, F14.6, F11.3, F10.3, F11.3,/)
13 FORMAT(10x,F0.3,24H MIX, Q IS FRACTIONAL = ,F3.1,5x
  1 F13.8,F14.c,F11.3,F10.3,F11.3,/)
1+ FORMAT(10X,F3.3,24H LIQUID,
                                               ,F3.1,5X
  1 F13.3,F14.6,F11.3,F10.3,F11.3,/)
13 FORMAT(///,52H LIQUID-VAPOR T,K FRCM THE 32 TERM EG.
                                                             0
                                                                  TP
 1 * P. ATM
                   RHC, MOL/L H, J/MOL S, J/MOL-K U, J/MOL*,//)
10 FORMAT(10X,F3.3,244 LIQUID,
                                               ,F3.1,5X
                                                          .
  1 F13.8, F14.0, F11.3, F10.3, F11.3,/)
17 FORMAT(10X,Fd.3,24H VAPOR,
                                               ,F3.1,5X
                                                          ,
  1 F13.8, F14.0, F11.3, F10.3, F11.3,/)
  END
```

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PROGRAM VALUES (INPUT, OUTPUT)
THIS PROGRAM TESTS THE SLUSH OXYGEN SUBROUTINE
CALL DATA02
COMBINATIONS OF SOLID - VAPOR
PRINT 1
T=50.
Q = C.
CALL SLO2(T,Q,Q,PSL,DSL,HSL,SSL,USL)
PRINT 2,T,Q,
               PSL, DSL, HSL, SSL, USL
Q=0.5
CALL SLO2(T,Q,0.,PSL,DSL,HSL,SSL,USL)
PRINT 3, T, Q,
               PSL, DSL, HSL, SSL, USL
Q=1.
CALL SLO2(T,Q,0.,PSL,OSL,HSL,SSL,USL)
PRINT 4, T,Q,
               PSL, DSL, HSL, SSL, USL
T=54.359
TP=1.
Q = C.
CALL SLO2(T, Q, TP, PSL, DSL, HSL, SSL, USL)
PRINT 5, T, Q, TP, PSL, DSL, HSL, SSL, USL
Q=0.5
CALL SLO2(T,Q,TP,PSL,DSL,HSL,SSL,USL)
PRINT 6, T, Q, TP, PSL, DSL, HSL, SSL, USL
Q=1.
CALL SLO2(T,Q,TP,PSL,DSL,HSL,SSL,USL)
PRINT 7, T, Q, TP, PSL, OSL, HSL, SSL, USL
COMBINATIONS OF SOLID - LIQUID
PRINT 8
T=54.359
TP=0.
Q = 0
CALL SLO2(T,Q,TP,PSL,DSL,HSL,SSL,USL)
PRINT 9, T, Q, TP, PSL, DSL, HSL, SSL, USL
Q=0.5
CALL SLO2(T,Q,TP,PSL,DSL,HSL,SSL,USL)
PRINT10, T, Q, TP, PSL, DSL, HSL, SSL, USL
Q=1.
CALL SLO2(T,Q,TP,PSL,DSL,HSL,SSL,USL)
PRINT11, T, Q, TP, PSL, DSL, HSL, SSL, USL
T=56.
0=0.
CALL SLO2(T,Q,0.,PSL,DSL,HSL,SSL,USL)
PRINT12, T,Q,
               PSL, OSL, HSL, SSL, USL
2=0.5
CALL SLO2(T,Q,O.,PSL,DSL,HSL,SSL,USL)
PRINT13, T.Q.
              PSL.DSL,HSL,SSL,USL
Q=1.
CALL SLO2(T,Q,O.,PSL,DSL,HSL,SSL,USL)
PRINT14, T, Q,
               PSL, DSL, HSL, SSL, USL
COMBINATIONS OF LIQUID - VAPOR FROM THE 32 TERM EQ.
PRINT 15
T=54,359
```

С

С

C

```
Q = Q.
  PSL=VPN(T)
  DSL=FINDM(PSL,T,41.)
  HSL=ENTHAL(PSL, DSL, T)
  USL=HSL-PSL/DSL*101.325
  SSL=ENTROP(DSL.T)
                 PSL, DSL, HSL, SSL, USL
  PRINT16, T, Q,
  Q=1.
  DSL=FINDM(PSL,T,0.0003)
  HSL=ENTHAL(PSL,DSL,T)
  USL=HSL-PSL/DSL+101.325
  SSL=ENTROP(DSL,T)
  PRINT17, T,Q, PSL, DSL, HSL, SSL, USL
  T=56.
  Q=0.
  PSL=VPN(T)
   DSL=FINDM(PSL,T,41.)
  HSL=ENTHAL(PSL.DSL.T)
   USL=HSL-PSL/DSL*101.325
   SSL=ENTROP(DSL,T)
  PRINT16, T, Q, PSL, DSL, HSL, SSL, USL
  Q=1.
  DSL=FINDM(PSL,T,0.0003)
  HSL=ENTHAL(PSL,DSL,T)
  USL=HSL-PSL/DSL+101.325
   SSL=ENTROP(DSL,T)
  PRINT17, T, Q, PSL, DSL, HSL, SSL, USL
 1 FORMAT(///,52H1SOLID-VAPOR T,K
                                                               Q
                                                                   TP
 1 *
          P, ATM
                     RHO, MOL/L H, J/MOL
                                              S. J/MOL-K
                                                          U. J/MOL*.//)
 2 FORMAT(10X, F8.3, 24H SOLID,
                                                .F3.1.5X
                                                           .
  1 F13.8, F14.6, F11.3, F10.3, F11.3,/)
 3 FORMAT(10X+F8.3+24H MIX+ Q IS FRACTIONAL = +F3.1+5X
                                                           .
  1 F13.8,F14.9,F11.3,F10.3,F11.3,/)
 4 FORMAT(10X, F8.3, 24H VAPOR,
                                                ,F3.1,5X
  1 F13.8, F14.9, F11.3, F10.3, F11.3,/)
 5 FORMAT(10X,F8.3,24H SOLID,
                                                ,F3.1,F5.1,
 1 F13.8,F14.6,F11.3,F10.3,F11.3,/)
 6 FORMAT(10X,F8.3,24H MIX, Q IS FRACTIONAL = ,F3.1,F5.1,
  1 F13.8,F14.9,F11.3,F10.3,F11.3,/)
 7 FORMAT(10X, F8. 3, 24H VAPOR,
                                                ,F3.1,F5.1,
  1 F13.8, F14.9, F11.3, F10.3, F11.3,/)
                                                                  TP
 8 FORMAT(///,52H SOLID-LIQUID T,K
                                                               n
 1 *
                                              S, J/MOL-K U, J/MOL*,//)
         P, ATM
                     RHO, MOL/L H, J/MOL
 9 FORMAT(10X.F3.3.24H SOLID.
                                                .F3.1.F5.1,
  1 F13.8, F14.6, F11.3, F10.3, F11.3,/)
10 FORMAT(10X,F8.3,24H MIX, Q IS FRACTIONAL = ,F3.1,F5.1,
  1 F13.8,F14.6,F11.3,F10.3,F11.3,/)
11 FOPMAT(10X,F8.3,24H LIQUID,
                                                ,F3.1,F5.1,
  1 F13.8.F14.6.F11.3.F10.3.F11.3./)
12 FORMAT(10X,F3.3,24H SOLID,
                                                ,F3.1,5X
  1 F13.8, F14.6, F11.3, F10.3, F11.3,/)
13 FORMAT(10X, F8.3, 24H MIX, Q IS FRACTIONAL = , F3.1, 5X
  1 F13.8, F14.6, F11.3, F10.3, F11.3,/)
14 FORMAT(10X, F3.3, 24H LIQUID,
                                                ,F3.1,5X
                                                           ,
  1 F13.8, F14.6, F11.3, F10.3, F11.3,/)
15 FORMAT(///,52H LIQUID+VAPOR T,K FROM THE 32 TERM EQ.
                                                              Q TP
  1 *
         P. ATM
                      RHO, MOL/L H, J/MOL S, J/MOL-K U, J/MOL*,//)
16 FORMAT(10X,F8.3,24H LIQUID,
                                                ,F3.1,5X ,
  1 F13.8, F14.6, F11.3, F10.3, F11.3,/)
17 FORMAT(1JX, F8.3, 24H VAPOR,
                                                ,F3.1,5X
                                                          ,
  1 F13.8, F14.9, F11.3, F10.3, F11.3,/)
   END
```

1.8 R = 1 KTemperature 14.695949 psia = 1 atm =  $1.01325 \times 10^5 \text{ N/m}^2$ Pressure  $0.00794590 \text{ ft}^3/\text{lb}_m = 1 \text{ cm}^3/\text{mol}$ Specific Volume  $(1 \text{ cm}^3 = 0.001 \text{ liter} = 10^{-6} \text{ m}^3)$ 0.213405 BTU/1b<sub>m</sub> = 1 J/mol Internal Energy, Enthalpy 0.118558 BTU/1b<sub>m</sub>R = 1 J/mol-K Entropy, Specific Heat Thermal Conductivity 0.0578176 BTU/ft-hr-R = 1 mW/cm-K 0.067196897 lb<sub>m</sub>/ft-s = 1 g/cm-s Viscosity Speed of Sound 3.2808 ft/s = 1 m/s 2.01594 (on the  $C^{12} = 12.000$  scale) Molecular Weight  $0.5710147 \times 10^{-5} lb_{f}/in = 1 dyn/cm$ Surface Tension  $(1 \, dvn = 10^{-5} \, N)$ 

APPENDIX F. CONVERSION FACTORS, OXYGEN

Temperature Pressure Specific Volume Internal Energy, Enthalpy Entropy, Specific Heat Thermal Conductivity Viscosity Speed of Sound Molecular Weight Surface Tension 1.8 R = 1 K 14.695949 psia = 1 atm = 1.01325 x  $10^5 \text{ N/m}^2$ 0.0005005957 ft<sup>3</sup>/lb<sub>m</sub> = 1 cm<sup>3</sup>/g mol 0.0134446 BTU/lb<sub>m</sub> = 1 J/g mol 0.0074692 BTU/lb<sub>m</sub>R = 1 J/g mol-K 0.0578176 BTU/ft-hr-R = 1 mW/cm-K 0.067196897 lb<sub>m</sub>/ft-s = 1 g/cm-s 3.2808 ft/s = 1 m/s 31.9988 0.5710147 x  $10^{-5}$  lb<sub>f</sub>/in = 1 dyn/cm (1 dyn =  $10^{-5}$  N)

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The thermodynamic pro	perties of hydrogen and oxy	gen have been ca	iculated	for tempera-			
required for the comp	utations are either taken f	rom the literate	ire. or ar	e extrapolate			
If extrapolated, the	extrapolations are based or	the known behav	vior of ot	her simple			
fluids. The results	are presented in the form of	of computer progr	ams which	cover two			
regions of the phase	diagram, solid-vapor, and s	olid-liquid. In	put to the	e programs is			
cemperature and quali	ty. The properties returne	a include pressu	ire, densi	cy, enthalpy,			
are an extension of a	nd depend upon the equation	us of state devel	loped prev	iously for			
these gases.			L PLCV	.,			
17. KEY WORDS (six to twelve a name; separated by semicolo	entries; alphabetical order; capitalize on ons)	ly the first letter of the	first key word	unless a proper			
Computer programs; enthalpy; entropy: hydrogen; internal opprave liquid; opprave							
PVT; quality; slush	; solid; vapor.	-, -neerlar eller	sy, rrquid	, onygen,			
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