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## A Proposed Concept for Determining the Need for Air Conditioning for Buildings Based on Building Thermal Response and Human Comfort

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# A Proposed Concept for Determining the Need for Air Conditioning for Buildings Based on Building Thermal Response and Human Comfort

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NBS Building Research Institute

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A Proposed Concept for Determining the Need for Air  
Conditioning for Buildings Based on Building Thermal Response and Human Comfort

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Abstract

Determining the need for air conditioning can be based on a wide variety of factors. To date, the only criteria that have been written and can be referenced are those of several federal organizations and many are not really criteria in the true sense of the word. They are guidelines to be used in the determination of fund allocation; in other words, provisions are made to air condition federal facilities in specific geographical locations if pertinent weather characteristics of that locality meet certain requirements. This paper presents the concept that a true criteria can be established based both on weather characteristics of the locality as well as characteristics of the building or structure under consideration.

The paper gives the details of a study showing the feasibility of such a scheme. A simulation was made of two proposed residences in several geographical localities. For the simulation, actual hour-by-hour weather data was used in conjunction with a sophisticated computer program. The results revealed for the non air-conditioned spaces, the extent and duration of undesirable indoor conditions based upon generally accepted comfort indices. The concept of a new "comfort" or "discomfort" index called Predicted Indoor Habitability Index (PIHI) is introduced. The authors indicate the way in which a criterion could be established that would be in the form of tables, indicating for a given specified building and geographical locality, whether mechanical cooling should or should not be installed.

Key Words: Air conditioning criteria; building thermal response; comfort indices; human comfort; predicted indoor habitability index

1. Introduction

At the present time, several United States government agencies make the decision to air condition single family or multifamily dwellings based on cost and general location of the housing unit (i.e., northern or southern part of the country). The United States Air Force, for example, specifies in their Manual 88-8 that if family housing is to be located in a region where the wet-bulb temperature is above 67°F for 1000 hours or more or the dry-bulb temperature is above 80°F for 400 hours or more during the hottest six consecutive months of the year, consideration should be given to installing mechanical cooling [1].\* Criteria similar to this were adopted by the Department of Housing and Urban Development for their Operation BREAKTHROUGH Program [2]. Using this as the basis for the decision to provide air conditioning is clear cut and definitive; however, it is felt that other factors besides weather should be considered. These include the thermal performance of the enclosing structure and the range of indoor thermal conditions under which people can remain reasonably comfortable. Other factors that are considered "secondary" and have not been recommended for inclusion here involve such things as the surrounding acoustical environment and human preferences for visual communication with the surroundings.

One of the most important items that govern the indoor environment is the "thermal performance" of the enclosing structure. J. F. van Straaten of the Building Research Institute of South Africa discusses in his recent book Thermal Performance of Buildings [3] the way different structures respond when subjected to periodically varying solar conditions

\* The number in the brackets refers to references at end of report.



and environmental temperatures. The overall heat transfer coefficient for wall, floor or ceiling which gives a direct measure of the resistance to heat flow under steady-state conditions, is not the sole indicator of the heat flow to the inside environment when unsteady-flow conditions exist. The mass of the wall, floor and ceiling, which governs the energy storage capacity, is also a pertinent parameter to be considered.

Several studies are summarized in the van Straaten book that help to illustrate the complex interaction between the building and the environment. Several four-room single-story structures of approximately 500 ft<sup>2</sup> (46 m<sup>2</sup>) of floor area were built in both Pretoria and Durban, South Africa. These unoccupied, non-air conditioned buildings were instrumented to observe the indoor environmental parameters as a function of time. The climate in Pretoria can best be described as warm and dry with large daily variations in solar radiation and outdoor air temperature (a daily range exceeding 20°F (11°C)). Under these conditions, massive brick buildings proved to be superior to lighter-weight buildings in minimizing the daily variation of the indoor temperature. The reason is that the "time lag" associated with the massive structure was such that the indoor environment remained cool during the hot part of the day (for example, a 79°F (26.1°C) indoor temperature compared with an 84°F (28.9°C) outdoor temperature at noon) and also remained warm during the night (74°F (23.3°C) compared with 61°F (16.1°C) outside at 5:00 a.m.). The lighter wood structures with essentially no "time lag" allowed the indoor temperature to increase to undesirable limits during the day (for example, 93°F (33.9°C) inside compared with 87°F (30.5°C) outside at 2:00 p.m.) and to decrease to correspondingly low levels during the night (a 62°F (16.7°C) indoor temperature compared with a 61°F (16.1°C) outdoor temperature at 5:00 a.m.).

The conclusions that van Straaten made from the experiments in Durban were just the opposite of those in Pretoria. The climate is generally warm but humid which is also accompanied by large solar radiation intensities and outdoor temperature variations smaller than those in Pretoria (for example, a daily outdoor temperature range of less than 10°F (5.5°C)). The massive buildings proved to be a distinct disadvantage. The walls could not cool down during the night enough to provide comfortable temperatures in the enclosures during the day.

Other interesting results of van Straaten's research include the improvement in performance of the lightweight structures in warm and dry climates by the addition of concrete floors and by painting the exterior of the structure white.

During 1971 and 1972, an experiment was conducted at the National Bureau of Standards where measurements of the dynamic heat transfer in an experimental masonry building were made in a large environmental chamber [4]. The structure was a one-room house 20 ft (6.1 m) wide, and 10 ft (3 m) high with walls of solid concrete block (8 in. (0.2 m) thick) and a flat roof made of reinforced precast concrete slabs (4 in. (0.1 m) thick). The building was exposed to a diurnal temperature cycle having a range of 60°F (33.4°C) extending from 40°F (4.4°C) to 100°F (37.8°C) for a series of tests where changes were made in the amount and location of insulation, and the amount of indoor mass. Tests were conducted where internal heating was used to maintain the indoor air temperature between specific limits as well as tests where no internal heating was supplied and the indoor air temperature was allowed to float.

For the floating tests, it was found that the combination of mass in the walls and roof facing the interior with the insulation placed on the outer surfaces of the building was very effective in reducing and controlling the variation of the indoor air temperature. Placing 2 in. (0.051 m) of commercial expanded polystyrene insulation on the inside building surface reduced the variation of the inside air temperature from 10.5°F (3.1°C) (for the uninsulated case) to 5.1°F (3.1°C). Furthermore, when this insulation was placed on the outside surface of the building, the variation in the inside air temperature was reduced to 2°F (1.1°C).

It should be apparent from the types of investigations cited above that climate as well as building construction plays a significant role in determining a need for air conditioning.

Obviously, another factor to be considered in establishing air conditioning criteria is the range of indoor thermal conditions under which people remain comfortable or not overly uncomfortable. The American Society of Heating, Refrigerating and Air-Conditioning Engineers' Standard 55-74 [5] is very specific in its stipulation of thermal comfort conditions. It states in part that at the center of and 2.0 ft (0.61 m) from each exposed wall and at the center of the room, the following should be met at all times:



1. When a dry-bulb temperature (DBT) equals the mean radiant temperature (MRT), the dry-bulb temperature equals the adjusted dry-bulb temperature ( $ADB\bar{T} = \frac{DBT + MRT}{2}$ ) and the values measured within the occupied zone shall be on the boundary or within the "comfort envelope." The "comfort envelope" is defined as a quadrangle with the following corner coordinates:

ADB $\bar{T}$  = 71.5 and 77.6°F (21.9 and 25.3°C) at 14 mm Hg (1.87 x 10<sup>3</sup> N/m<sup>2</sup>) vapor pressure and ADB $\bar{T}$  = 72.6 and 79.7°F (22.6 and 26.5°C) at 5 mm Hg (0.667 x 10<sup>3</sup> N/m<sup>2</sup>).

2. The water vapor pressure in the occupied zone shall be at or between 5.0 and 14.0 mm Hg (1.87 x 10<sup>3</sup> and 0.667 x 10<sup>3</sup> N/m<sup>2</sup>). These conditions correspond approximately to 20 and 65 percent relative humidity.
3. When the mean radiant temperature in the occupied zone differs from the dry-bulb temperature, the dry-bulb temperature shall be reduced by one degree for each degree mean radiant temperature elevation above air temperature and vice versa.
4. The air velocity in the occupied zone shall be 70 fpm (0.35 m/s) or less at any time.

In addition, it also states the allowable limits of oscillation in the temperature and relative humidity.

One might conclude based on this Standard then that if the indoor thermal environment of non-air conditioned buildings falls into this condition "most of the time", the building need not have mechanical cooling even if it is located in an area where climatic criteria might indicate a need for it. Obviously, the biggest unknown factor needed to be established in a study such as this, is how to quantify the phrase "most of the time" in the preceding sentence. In addition, as will be pointed out later in this paper, a better evaluation of the tolerance of people to varying indoor conditions above and below the recommended steady state comfort conditions is needed.

It should also be noted that the concept of determining a need for air conditioning based on building thermal performance is not new. Givoni in his latest book [6] introduces a "Building Bioclimatic Chart". His concept is based on the "Bioclimatic Chart", introduced earlier by Olgay [7]. Givoni's chart is essentially a psychrometric chart on which he has drawn an enclosed region indicating thermal comfort conditions. From experience and study, three additional regions have been drawn: one to indicate the range of outdoor conditions where choice of building materials and design features (large thermal resistance, large thermal mass, etc.) make comfort conditions inside attainable without air conditioning; a second region to indicate the outdoor conditions where efficient ventilation through the structure could result in comfort conditions; and a last region showing the range of outdoor conditions where mechanical cooling would be required.

Loudon [8] describes a method of calculating summertime indoor temperatures based on climatic and building factors which was developed at the Building Research Station in England. In addition, experimental data is presented showing that there was a strong correlation between the predicted peak temperatures in occupied schools and office buildings and users' comments on overheating in the summer, obtained from social surveys. He concludes, "... if temperatures are calculated on assumptions which have been set out, criteria can be set which enable one to decide in advance whether a given design of office or school is likely to be thermally comfortable". This is precisely the basis on which the study described in this paper was undertaken.

The present paper shows how a sophisticated building simulation computer program can be used in conjunction with actual weather data to predict the time-varying indoor thermal conditions. In addition, it is conceptually shown how such results could be used for establishing air conditioning criteria.

## 2. Proposed Concept of Air Conditioning Criteria

One of the ways to determine if a building should have mechanical cooling is to construct it without cooling equipment, determine if the indoor environment is acceptable, and if not, install the equipment. This is, of course, not feasible in most cases. However, the particular concept presented here is similar in many respects. By combining the pertinent weather parameters with those of the building under consideration, a simulation model predicts what would occur without mechanical cooling. The conditions are then compared with accepted indoor comfort data to determine whether the space should or should not be conditioned.

Anquez, et. al. of the Centre Scientifique et Technique du Batiment (CSTB) in France, published in 1965 the results of a study entitled "The Protection of Glazed Windows from Solar Radiation" [9]. Their objective was to develop standards for devices that are used to protect windows from solar radiation in non-air conditioned buildings of average and low thermal inertia. Their procedure was to divide France into four climatic regions and then through the use of mathematical simulations on "typical" buildings of specified dimensions, exposure of glazed areas, thermal inertia, and degree of ventilation, determine to what extent shading devices could be used to insure the maintenance of a comfortable indoor temperature during an average summer. The results were published in the form of tables, one of which is shown in Table 1. Someone considering a specific design who could locate his building at the proper place in this table, could tell at a glance what type of window shading, if any, could be used to insure comfortable conditions in the summer<sup>a</sup>.

The determination of air conditioning criteria by the present authors has not been carried to the point of publishing tables such as the one cited from the French study. However, it is felt that the ultimate goal of this project, which has been funded by the Department of Housing and Urban Development (HUD), would be to publish a document containing information analogous to the table. For a given climatic region of the United States and given building (characterized by the pertinent parameters), one could tell during the design phase whether mechanical cooling should or should not be installed.

The manner in which a computer program could be used for determining a need for air conditioning is depicted in Figure 1. Weather data from a specific climatic zone and adequate specifications of a building would be combined in the simulation model, the output of which would be the space conditions. The frequency and duration of the various indoor parameters would then be compared with a suitable indoor comfort index (identified in this paper as the Predicted Indoor Habitability Index (PIHI)) to determine whether the space should or should not be conditioned.

Before the project can successfully be completed, the following is required:

1. A computer program which has been proven accurate for predicting indoor temperatures,
2. A division of the United States into climatic zones and a knowledge of representative weather parameters from each zone,
3. A classification of buildings according to their thermal response, and
4. A clear definition of the Predicted Indoor Habitability Index (PIHI) as introduced in this paper.

Section 3. presents a description of the computer program used in this study and which adequately satisfies requirement 1. above.

Technical Committee 4.2 of the American Society of Heating, Refrigerating and Air-Conditioning Engineers is in the process of developing "typical weather data" for the purpose of computing building energy requirements. For the first phase of the study reported in this paper, hour-by-hour weather conditions obtained from the National Climatic Center in Asheville, North Carolina were used for the specific localities studied.

<sup>a</sup>The meaning of the "solar factor" referred to in Table 1 has not been explained in the present paper. It is felt not necessary for the purpose of the illustration.

Section 4. of this paper describes the analysis that has been done to date on the classification of buildings.

Section 5. describes the authors' concept of a Predicted Indoor Habitability Index and Appendix B contains a review of various comfort and heat stress indices that could be considered now as a basis for PIHI.

Section 6. describes what is called a feasibility analysis that has been done to give an indication of how successful the project might ultimately be.

### 3. Calculation of Indoor Space Conditions by Building Thermal Simulation

Numerous papers have been published and calculation manuals prepared in the area of heating/cooling load determination. Very few of these, however, have dealt with the indoor temperature estimates for the condition where air conditioning is non-existent or inadequate. Room temperature prediction is, on the other hand, very actively studied in Europe, Japan, Israel, and India where mechanical cooling is still very expensive for the majority of dwellings and consequently a determination of the basic need for air conditioning is very important.

The heat transfer calculations for room temperature prediction are similar to the heating/cooling load calculations; however, the former are somewhat more complex than the latter because they require exact heat balance calculations for the room air, surrounding walls and infiltrating outdoor air. Since the major importance is the hour by hour room temperature profile, it is necessary to account for the transient heat conduction and thermal storage in the building and internal mass.

In order to determine the temperature and humidity in non-air conditioned rooms responding to randomly fluctuating outdoor climatic conditions, a computer program to simulate hourly performance of building heat gain and heat storage has been developed at the National Bureau of Standards [10, 11, 12]. The program is called "NBSLD" and consists of various subroutines for calculating heat gains, which are similar to those recommended by the ASHRAE Task Group on Energy Requirements [13]. One major extension of the program beyond the recommended ASHRAE TG subroutines is a routine called RMTMP, which solves for room air temperature through the use of a series of simultaneous heat balance equations. The details of this routine is given in reference [12].

Figure 2 depicts the overall calculation sequence of NBSLD. Shown in the dash lined boxes are input data to be supplied where as those in solid lined boxes indicated calculations to be performed. The cycle indicators show the iteration cycles for the number of buildings, the number of rooms in a given building and the number of days for which the calculations are performed. Table 2 lists all the pertinent building data required for the calculations. More specific identification of the exact way in which the input data is prepared is described in reference [12].

This particular computer simulation has been verified by experimental work on two separate research projects at NBS [4, 14]. The first study [4] involved a small masonry building and the experiment was described previously in this paper. Figure 3 is a typical test result taken from reference [4] and shows to what degree NBSLD was able to account for the transient conduction occurring in the thick masonry walls (to within  $\pm 1.0^{\circ}\text{F}$  ( $0.55^{\circ}\text{C}$ )) for outdoor temperature variations from 45 to 100°F (7 to 38°C) and to compute the indoor temperature fluctuation. In the latter study [14], a more realistic living unit was used, namely a four-bedroom, lightweight house that was completely furnished and had the activity of a six-member family simulated within. The house was also tested inside the environmental chamber where the outdoor conditions were simulated and precisely controlled.



In order to evaluate indoor conditions for human comfort or physiological stress, it is desirable that the indoor air velocity be estimated. The indoor air velocity is, however, believed to vary depending upon the air leakage rate, ventilation rate, thermal gradient of the room, basic design of the room, and any local air moving device such as a portable fan. According to Givoni [6], the indoor air motion could vary between 5 to 60% of outdoor wind velocity depending upon the nature of the air passage resistance through the room.

Since the information available for predicting indoor air velocity as function of temperature distribution and wind velocity is very scanty, NBSLD has not been designed to calculate this parameter. It has been assumed in the present study that the indoor air velocity would be less than 20 ft per minute (0.1 m/sec). This assumption should yield an upper-bound value of comfort index or physiological index for summer conditions and is therefore safer to use than to overestimate the cooling due to elevated air velocities.

The form of NBSLD available at the start of this study did not allow for the calculation of mean radiant temperature (MRT). Since the room temperature calculation routine (RMTMP) does calculate the temperature of all the interior surfaces, it was very simple matter to modify the program to calculate this quantity. Then MRT was used as part of the input data to the calculation of the appropriate physiological or comfort indices that were used in this study. Appendix A describes the equations that were inserted into the program to calculate MRT.

#### 4. Classification of Buildings According to Their Thermal Response Characteristics

This part of the paper describes a method for classifying kinds of residential buildings in relation to their thermal behavior.

Construction data were taken from the proposals of 18 of the 22 participating Housing System Producers in the HUD Operation BREAKTHROUGH Program. Since the contractors involved in that program represented a cross section of the Housing System Producers in the building industry, it was felt that data contained in their proposals provided meaningful information about the practice, and the state of the art, in housing design. Consequently, it was felt that a realistic classification procedure could be established relative to the typical residential building based upon thermal parameters for composite structural components.

##### 4.1 Type of Building Data Compiled

From the drawings and specifications submitted by the Housing System Producers in the Operation BREAKTHROUGH Program, two types of data were collected. The first concerned the method of construction and materials used for the exterior enclosures and interior partitions of a building, and the associated thermophysical property data of the materials. Pertinent thermal performance parameters associated with the structural components such as the U-value, weight per unit area, thermal mass, and the thermal time constant were then computed. Their computation, physical meaning and usefulness will be discussed later in this section. The second type of data was of a geometric nature and involved the following:

1. Total floor area of a dwelling unit.
2. Floor area for each of the rooms in a dwelling unit.
3. Type of walls and openings, windows, doors, and their areas for each of the rooms in a unit.
4. Total glass area of a dwelling unit.
5. Crack length of the windows and doors. These data are required in order to know air movement and infiltration characteristics.
6. Shading coefficient for the glazed area.

## 4.2 Method of Data Presentation

Data collected from the drawings and specifications were processed by the NBS UNIVAC 1108 computer and printed out in the unified manner in tabular form. Two types of tables were developed, corresponding to the two types of data discussed in 4.1. Typical examples are given here as Tables 3 to 6.

Table 3 gives the building construction and material data for one of the dwellings of one of the 18 Housing System Producers surveyed. This table contains a typical layer by layer description and the thermophysical properties of the materials used in the construction of the structural components (exterior walls, interior partition, party wall, floor/ceiling, roof/ceiling, ground floor, basement wall, basement floor, window). The order of the layers are from the outside of a room toward the inside for the side walls and from top to bottom for roofs and floor/ceilings. The thermal property values were taken from the contractor's drawings and specifications and from the 1972 ASHRAE Handbook of Fundamentals [15]. Occasionally data from the specific heat ( $C_p$ ) of certain materials were not available, and a value of .20 Btu/(lb·°F) (.013 cal/(g·°C)) was assumed. Since the value of  $C_p$  does not vary much for most of the building materials (on the order of .15 (.0098) to .40 (.026) with a major portion of the materials in the lower range of the spectrum), the value of .20 (.013) was chosen. The surface air film resistance values were taken from the ASHRAE Handbook of Fundamentals also and based on the summer design conditions since the overall project was established for the purpose of determining summer air conditioning criteria.

Table 4 gives the four relevant parameters associated with and affecting the thermal performance of a building. They were computed from the data given in Table 3. A brief description follows:

1. U-value: The U-value is the overall heat transfer coefficient including the surface air film resistance (at 7.5 mph (3.4 m/s) wind outside and still air inside) under steady-state conditions. This is the major factor used by designers in estimating the cooling load of a building. As pointed out previously, under unsteady-state conditions the U-value is no longer the only controlling factor in heat flow through walls since it does not take into account the energy storage effect of the walls. However, it does give an indication of the amount of resistance the wall offers to heat flow and, therefore, acts as one of the parameters in determining the overall heat transfer through the walls.
2. Thermal Mass,  $\rho C_p L$ : The thermal mass is a counterpart of the U-value and gives an indication of the energy storage capacity of the walls. It is computed from the following equation:

$$\rho C_p L = \sum_{i=1}^N \rho_i C_{pi} L_i \quad (1)$$

where  $\rho_i$ ,  $C_{pi}$ ,  $L_i$  are the density, specific heat, and thickness, respectively, of the  $i$ th layer in a multilayer wall.  $N$  is the total number in the wall.

3. Weight per unit surface area,  $\rho L$ : Because of the small variations in the specific heat for most building materials, the energy storage capacity of a wall is almost directly proportional to the weight per unit surface area of the wall. This parameter is, therefore, closely related to the thermal mass in that a knowledge of the values of the specific heat, which are not available for certain materials, is not required. The weight per unit area of a wall is computed by

$$\rho L = \sum_{i=1}^N \rho_i L_i \quad (2)$$

4. Thermal Time Constant: The thermal time constant is a function of the thermal diffusivities of the layers in a multilayer wall and is defined [6] as the heat stored per unit of heat transmitted. It is, therefore, a combination of the thermal mass and the thermal resistance of the wall. It is derived on the basis of the analogy between the heat flow represented by a thermal circuit and the time constant of a R-C electrical circuit, and is given by Givoni [6]:

$$\text{Thermal Time Constant} = \sum_i (\tau_i)$$

where

$$\tau_i = (R_{os} + L_1/k_1 + \dots + L_i/2k_i) \cdot (L_i \rho_i C_{pi}) \quad (3)$$

where  $R_{os}$  is the resistance of the surface air film and  $k_i$  is the thermal conductivity of the material of the  $i$ th layer. In the case of an air space, the resistance of the air space is substituted for  $L_i/k_i$ .

Similar to the thermal diffusivity of a homogeneous single layer wall, the thermal time constant is a measure of the thermal damping capacity of a multilayer wall on the amplitude and time lag of the inner surface temperature, or indoor air temperature, with respect to a periodically varying outdoor temperature. It should be pointed out that the thermal time constant given by equation (3) also takes into account the order the layers of materials are arranged. A change in the order of the arrangement will change the rate of heat flow through the wall under transient conditions. This is because the outside surface temperatures of the walls with different orders of arrangement in their layers will be different during the transient states. For example, during the day, the outside surface temperature of a wall with an insulation layer next to the external surface layer will be higher than a wall constructed of the same layers of materials but with the insulation layer placed further away from the external surface layer. The former construction will result in more heat being transferred back to the external environment by convection and radiation, and consequently less heat being transferred into the interior space. It is noted that this phenomenon is not accounted for by either the U-value or the thermal mass where the order of arrangement of the layers is immaterial.

Table 5 gives the geometrical data for one of 28 dwelling units ranging from 1-bedroom to 4-bedrooms. The 28 units were chosen randomly from six of the 22 Housing System Producers. The survey of the 6 Housing System Producers was done for the purpose of obtaining some average values of unit size, floor area, and window area for a normal dwelling unit. The orientation of the unit is not specified since this is one of the factors that is influenced by site location, terrain, units group plan, etc. as much as by thermal performance consideration. For a group of attached units (single family attached, multi-family low rise or high rise), the unit at the ends, or corner, of the group was chosen since it has the largest amount of wall area exposed to the outside environment and consequently results in the most severe indoor temperature variation, or the largest cooling load, among the group, and represents the worst case as far as air conditioning is concerned. Table 5 also gives the crack lengths of the windows and doors which are required in an air infiltration study. Data for lighting (as an internal heat source) and furniture (as an internal heat sink) were not available. The data for the shading coefficient on windows were assumed values for regular sheet glass with light indoor venetian blinds shading. These data would, of course, be different values for other types of glass and shading.

Table 6 gives a summary of the different type areas associated with the dwelling, plus three parameters that can be used for the classification of dwelling units on a geometrical basis. These three parameters are:



1. Floor Area: The floor area represents the total amount of living space in a dwelling unit and gives an indication of the size of the unit among the same type of dwellings.
2. Ratio of Exterior Wall Area to Floor Area: The ratio gives an indication of the complexity of the shape of the unit. For example, a simple rectangular unit will have a lower ratio than a complex geometrically shaped unit.
3. Ratio of Window Area to Floor Area: This ratio indicates the relative amount of glass area in a unit which has a direct bearing on the amount of solar radiation transmitted directly into the interior space.

In general, data contained in Tables 3 to 6 are required by the computer program NBSLD for indoor temperature or load prediction purposes.

#### 4.3 Analysis of Data and Discussion

A study of all the data compiled in this part of the project indicates the following:

1. Unit Size: The range and average size of the dwelling units in terms of total ft<sup>2</sup> (m<sup>2</sup>) of floor area are tabulated below:

	Min. Area	Max. Area	Average	Total Units Used
4-Bedroom Unit	1065 (98.9)	1740 (161.6)	1340 (124.5)	11
3-Bedroom Unit	910 (84.6)	1480 (137.5)	1100 (102.2)	16
2-Bedroom Unit	700 (65.0)	1200 (111.5)	905 (84.1)	15
1-Bedroom Unit	580 (53.9)	960 (89.2)	735 (68.3)	8

It is noted that the total number of units upon which the average values were based is not statistically significant. However, for the study of air conditioning criteria where a typical size unit is to be used, slight variation from the above listed average values would not have any significant influence on the results.

2. Glass Area: The total glass area in the dwelling units ranged from 10% to 26% of the total floor area, with an average value of 17% for 50 units studied. The variation of 10 ~ 26% occurs in both the large size and the small size units (FHA Minimum Property Standards require 10% minimum for light). It can, therefore, be said that the size of a dwelling unit has no effect on the relative amount (with respect to floor area) of the glass in the design of a typical housing unit.
3. Individual Room Size: The variations in the sizes of the major rooms in a dwelling unit are quite large, and are listed below for reference:

	Range ft <sup>2</sup> (m <sup>2</sup> )	Average ft <sup>2</sup> (m <sup>2</sup> )
Living Room	140 ~ 270 (13.0 ~ 25.1)	200 (18.6)
Dining Room	95 ~ 125 (8.8 ~ 11.6)	110 (10.2)
Kitchen	50 ~ 150 (4.6 ~ 13.9)	95 (8.8)
1st Bedroom	125 ~ 220 (11.6 ~ 20.4)	165 (15.3)
2nd Bedroom	100 ~ 220 (9.3 ~ 20.4)	135 (12.5)
Other Bedrooms	80 ~ 180 (7.4 ~ 16.7)	115 (10.7)
Bathroom	35 ~ 45 (3.3 ~ 4.2)	40 (3.7)

Normally, the larger living rooms were associated with a 3 or 4-bedroom unit. The lower limits in the above list are controlled by the FHA Minimum Property Standards.

4. U-value! The U-values for the different designs of the walls and roof/ceiling constructions by the 18 housing system producers were fairly uniform within each weight class of construction. The ranges and average values for the exterior wall and the roof/ceiling elements were,

$$\text{Exterior wall} = .062 \sim .178 \text{ Btu}/(\text{h} \cdot \text{ft}^2 \cdot ^\circ\text{F}) \quad (.352 \sim 1.01 \text{ W}/(\text{m}^2 \cdot ^\circ\text{C}))$$

$$\text{average value} = .104 \quad (.59)$$

$$\text{Roof/ceiling} = .041 \sim .114 \text{ Btu}/(\text{h} \cdot \text{ft}^2 \cdot ^\circ\text{F}) \quad (.233 \sim .647 \text{ W}/(\text{m}^2 \cdot ^\circ\text{C}))$$

$$\text{average value} = .062 \quad (.35)$$

In general, for the exterior wall system, the higher than average U-values were associated with the heavy type construction such as concrete wall. For lightweight construction such as wood frame wall and sandwich panel wall with various cores and facings, the U-values were all comparable.

5. Weight per Unit Area: As stated previously, the weight per unit area and the thermal mass are closely related, having an almost linear relationship because of the slight variation in the values of the specific heat for different building materials. This linear relationship is shown in Figure 4. The weight can, therefore, be used to indicate the thermal storage capacity of a wall or roof/ceiling system. For the 18 Housing System Producers studied, the ranges of the weight of different building enclosures were,

$$\text{Exterior wall: } 2.5 \sim 98 \text{ lb}/\text{ft}^2 \quad (12 \sim 478 \text{ kg}/\text{m}^2)$$

$$\text{Roof/ceiling: } 2.5 \sim 69 \text{ lb}/\text{ft}^2 \quad (12 \sim 337 \text{ kg}/\text{m}^2)$$

$$\text{Floor/ceiling: } 4 \sim 86 \text{ lb}/\text{ft}^2 \quad (20 \sim 420 \text{ kg}/\text{m}^2)$$

$$\text{Ground floor: } 2 \sim 90 \text{ lb}/\text{ft}^2 \quad (10 \sim 439 \text{ kg}/\text{m}^2)$$

$$\text{Party wall: } 5 \sim 72 \text{ lb}/\text{ft}^2 \quad (24 \sim 351 \text{ kg}/\text{m}^2)$$

(including load bearing interior wall)

The types of the construction of the building included: wood frame, sandwich panel with various cores and facings, metal frame, brick wall, and concrete wall systems. A classification based on the weight of the exterior wall system is recommended as follows:

Lightweight (wood frame, sandwich panel): Less than  
20 lb/ft<sup>2</sup> (98 kg/m<sup>2</sup>)

Medium weight (wood frame with face brick, brick,  
lightweight concrete): 20 ~ 50 lb/ft<sup>2</sup> (98 ~  
244 kg/m<sup>2</sup>)

Heavyweight (brick, concrete): higher than 50 lb/ft<sup>2</sup>  
(244 kg/m<sup>2</sup>)

6. Thermal Time Constant: The ranges of values for the different building enclosures are,

Exterior wall: 3.2 ~ 115 h

Roof/ceiling: 4.1 ~ 165 h

Floor/ceiling: 3.4 ~ 86 h

Ground floor: 2.2 ~ 96 h

Party wall: 6.2 ~ 44 h

Interior Partitions: 1.7 ~ 10 h

It can be seen that the ranges of values for the thermal time constant are quite large and are comparable with the ranges for the weight of the structures. Figures 5 and 6 show the relation between the thermal time constant and the weight of exterior wall and roof/ceiling systems, respectively. The large scattering of the data points shows the effect of the arrangement of the layers of different materials and the placement of insulations and/or air spaces in a wall system. However, Figures 5 and 6 also show that even though the local scattering of data points is large, the overall trends of increasing thermal time constant with increasing weight is preserved, and the classification of buildings by weight may be sufficient. For a more refined and accurate classification of buildings, with respect to indoor thermal environment, the thermal time constant might be a better index because of its close functional resemblance with the thermal diffusivity of a single layer wall. This should, however, be verified by further work, using data on a variety of selected typical residential units of different design as input to the computer program NBSLD and comparing the results under identical external environmental conditions at various locations throughout the country.

## 5. Predicted Indoor Habitability Index

There are approximately fifteen published indices or groups of experimental data that have been presented to indicate man's comfort or discomfort when subjected to a certain environment. The majority are experimental in nature (i.e., human subjects have been exposed to a specified and controlled environment and asked to describe their feeling or at least have physiological measurements taken on them during the exposure). However, during the last several years there has been a great deal of interest in describing mathematically the thermal interaction between man and his environment, thus enabling one to predict what occurs or how one might feel in given surroundings. Appendix B contains a comprehensive review of those indices felt to be the most pertinent to this study.

The authors of this paper have introduced the concept of Predicted Indoor Habitability Index (PIHI) for several reasons. It is felt that the decision to air condition a building should be based on the fact that the value of certain chosen parameters describing the indoor environment would exceed a certain level for a specified amount of time during the "air conditioning" season unless mechanical cooling were installed. Therefore, it would be desirable to establish a new scale to satisfy this requirement. For example, a very simple arbitrarily chosen scale might be:

- PIHI = 0 if the KSU index never exceeds a value of 5 during the summer months (corresponds to slightly warm - see Appendix B)
- PIHI = 5 if the KSU index exceeds a value of 5 for 5% of the hours during the summer months
- PIHI = 10 if the KSU index exceeds a value of 5 for 10% of the hours during the summer months.

However, there are other factors that should also be included in the analysis to establish PIHI. These include among other things, consideration of the "persistency factor". Certainly a situation where the indoor environment is "uncomfortable" for long periods of time wouldn't necessarily be equivalent to one where it was just as uncomfortable for more but shorter periods of time. In addition, shouldn't consideration be given to the relative level of "discomfort" that occurs during these periods? An indoor environment where the KSU index was 6 (warm) for a certain period of time wouldn't be equal to one where it was 7 (hot) for the same period even though they did exceed 5 for the same amount of time.

Other important factors should also be noted at this point. Most of the indices reviewed in Appendix B are valid for, or at least have been developed for, quasi-steady situations. The subjects have been exposed to (or the models simulate the subjects being exposed to) steady-state environments for periods of time up to four hours and their response given accordingly. Very seldom does this occur in the average residence and the technique of extending these indices to a more transient environment needs at least a "close look". ASHRAE, in their Comfort Standard [5], recommend limiting the rate of change of dry-bulb temperature in a space to 4°F/h (2.2°C/h) and the rate of change of water vapor pressure to 4.5 mm Hg/h (600 N/m<sup>2</sup>)<sup>a</sup>. These limits have been verified somewhat by an experimental study at Kansas State University reported by Sprague and McNall [16]. College students wearing the "standard clothing" (see Appendix B) were subjected to an environment where the dry-bulb temperature and relative humidity was oscillated one at a time about the "comfort value" while the other parameter was maintained at the "comfort value". The conclusion of the study was that the Comfort Standard values are somewhat conservative but no change was recommended. In addition, Wyon et. al. [17] studied the cyclic variations of temperature about some optimum. Subjects were free to reverse the direction of change of temperature swings and could thus control the amplitude and period of swings to which they were exposed. It was found that "their subjective tolerance of temperature swings was very much greater than is supposed by existing regulations".

Another factor to be considered is the effect of nonuniform environments. There is a capability built into many of the indices to handle a situation where the wall temperatures are different than the ambient air temperature. McNall et. al. [18, 19] have done studies at Kansas State University which have shown that for "reasonable degrees" of temperature separations between the enclosing surfaces and the air, the subjects experienced no significant discomfort which could be attributed to asymmetry and that the use of the mean radiant temperature in the computation of environmental condition was satisfactory. Other studies had been done earlier at Kansas State University [20, 21, 22] and at CSTB in France [23] on the same subject.

Finally, it was felt at the beginning of the study that the PIHI scale should ideally take into account the type of occupant in the residential dwelling under consideration or at least there should be a different scale for the different types of occupants. Recent studies, both within the U.S. and at the Technical University of Denmark, have shown that comfort conditions do not significantly depend upon age, adaptation, sex, or seasonal and

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<sup>a</sup>This condition corresponds to approximately 20 percent relative humidity per hour.



circadian rhythm [24, 25, 26, 27, 28]. However, it should be noted that even though the preferred comfort conditions have been the same, conditions of discomfort, which are perhaps the relevant ones to consider here, could very well be different for different age groups, sex, etc. [29]. This latter field is one that is just beginning to be researched.

In summary, the concept of the Predicted Indoor Habitability Index has been introduced as a scale or index that is required in order to successfully complete the job of establishing air conditioning criteria.

The authors have pointed out a number of factors that should be accounted for in establishing the scale and it is hoped that a separate research task can be initiated so that the index can be established. During the first phase of the project described in this paper, the state-of-the-art comfort indices were used in the analyses as will be seen in the next section.

## 6. Preliminary Calculations and Analysis for Air Conditioning Criteria

In order to determine whether the approach outlined in Section 2 is feasible for determining a meaningful air conditioning criterion, some preliminary analysis was carried out. Different apartments within complexes planned as part of HUD's Operation BREAKTHROUGH Program have been simulated in the National Bureau of Standards' computer program (NBSLD) described in Section 3. Hourly values of the important weather parameters, outdoor dry-bulb temperature, wet-bulb temperature, wind velocity, and cloud cover were taken from the United States Weather Bureau tapes (available from the National Climate Center in Asheville, North Carolina). The output of the simulation was hourly values of indoor dry-bulb and wet-bulb temperature. Algorithms for pertinent physiological and/or comfort indices were written so that daily profiles showing values of these indices could be obtained.

The analysis was begun by arbitrarily taking the weather data for the years 1949 through 1958 in Jersey City, New Jersey and simulating the behavior of one of the heavyweight apartments to be built on that site. The building data that were used are as follows:

1. The apartment building was assumed to face west and the individual apartment chosen was one at approximately mid-height of the 130 feet (39.6 m) high structure. No building shadow was used and the adjacent apartments and hallway were assumed to always be at the same temperature as the apartment.
2. The exposed wall is constructed of 7 inches (17.8 cm) of concrete and 2 inches (5.1 cm) of insulation. It contains a 100 ft<sup>2</sup> (9.3 m<sup>2</sup>) glass window (shading coefficient = 0.22 corresponding to a double pane window with a white opaque roller shade). The total wall area is 212 ft<sup>2</sup> (19.7 m<sup>2</sup>) leaving 112 ft<sup>2</sup> (10.4 m<sup>2</sup>) of solid structure.
3. The floor/ceiling unit is composed of 5 1/2 inches (14 cm) of concrete and 1/8 inch (0.32 cm) cork tile with a total area of 550 ft<sup>2</sup> (51.1 m<sup>2</sup>). The floor to ceiling height is 8.5 ft (2.6 m).
4. The partition walls contain 6 inches (15.2 cm) of concrete.
5. The maximum number of occupants is 2, the maximum equipment load is 1/2 W/ft<sup>2</sup> (5.4 W/m<sup>2</sup>) of floor area, and the maximum lighting load is 3 W/ft<sup>2</sup> (32.3 W/m<sup>2</sup>) of floor area.
6. The infiltration or natural ventilation rate was simulated as 1 air change/h between 6 a.m. and 7 p.m. and 6 air changes/h from 7 p.m. to 6 a.m.

Typical results for the months of July and September in Jersey City are shown in Figures 7 through 24. The data is for the summer of 1952 which was hotter than the mean for the 10 year period that was examined. The outside dry-bulb temperature was equal to or greater than 80°F (26.7°C) for 615 hours during the four months, June through September (3rd highest in ten year period), and the outside wet-bulb temperature was equal to or greater than 67°F (19.4°C) for 1258 hours (3rd highest)<sup>a</sup>. Shown in Figure 7 is a plot of the solar energy falling on the west facade of the apartment (after modification by actual cloud cover) and a plot of outdoor dry- and wet-bulb temperature for the month of July. Figure 8 shows the output of the thermal simulation for this apartment; in other words, a monthly profile of indoor dry- and wet-bulb temperature. Since the ASHRAE Comfort Standard gives limits on the rate of change of indoor temperature and relative humidity, these values were computed and are shown in Figure 9. As can be seen, the suggested values of 4°F/h (2.2°C/h) and 20%/h were only exceeded once or twice during the month of the ten year period regardless of how hot the weather was.

Figures 10 through 15 show monthly profiles of several of the physiological indices discussed in Appendix B, calculated from the corresponding algorithms. Eight different indices are plotted in these figures for the month of July 1952. The particular indices selected were based on comfort votes of subjects exposed to selected environmental conditions for different periods of time, on calculated comfort responses using an analytical equation fitted to comfort data, and on several different expressions of heat stress related to the ratio of measured sweat rates to maximum possible sweat rates. Comments applicable to these profiles are as follows:

1. The new effective temperature (ET\*) was equal to or higher than 81°F (27.2°C) 60.8 percent of the time and equal to or higher than 85°F (29.4°C) only 27.0 percent of the time during the month (Figure 11).
2. The predicted mean vote for a person in standard clothing (0.6 clo) was equal to or exceeded 1 (slightly warm) 40.3 percent of the time but was equal to or above 1 only 19.4 percent of the time then the clothing was reduced (0.25 clo) (Figure 12).
3. There was little or not heat stress regardless of the particular index used (old or new) (Figure 14).
4. The Kansas State Index was equal to or above 5 (slightly warm) only 21.1 percent of the time (Figure 10).
5. More than 10 percent of the people were dissatisfied a significant portion of the time during the month regardless of whether light clothing or the "standard" clothing was worn (Figure 13).

Corresponding analysis could be made of the month of September from Figures 16 through 24. In addition, summary information for all ten years is given in Table 7. The table shows for the 10 summers in Jersey City, the number of total hours in each summer that the outdoor dry-bulb temperature exceeded 80°F (26.7°C) and the outdoor wet-bulb temperature exceeded 67°F (19.4°C). In addition, the percent of the time in each month that selected indices exceeded prescribed levels was calculated and are shown.

The point has already been raised in Section 5 that an entirely new index will have to be established to serve the needs of this study. To demonstrate one reason why this is so, Figures 25 and 26 have been included for two warm months in 1953 and 1958, respectively. Figure 25 shows that the indoor ET\* exceeded 85°F (29.4°C) 14 percent of the time during August of 1953. The specific way in which it occurred was for one two-hour period, twice it went above 85°F (29.4°C) for a duration of between 12 and 18 hours, and once for more than a 48 hour period. Figure 26 shows that in July of 1958, ET\* was above 85°F (29.4°C) for 13 percent of the time; however, the specific way in which it occurred was entirely different from that indicated in Figure 25. The question that arises is: would the feeling of discomfort be identical during these two months? If not, there appears to be justification for the establishment of a new scale (PIHI) that accounts for frequency and duration of uncomfortable conditions.

<sup>a</sup>Under these conditions, air conditioning should be considered according to the previously referenced Air Force guidelines[1].



It is felt that given the kind of information just shown for a specific structure and location, the decision to air condition could certainly be made. However, it would be neither practical nor economical to undertake such an analysis for each individual case. It is still questionable whether it is feasible to carry out the analysis for many combinations of building groups and climatic zones across the United States. Therefore, a short-cut method was sought by examining the results of this thermal simulation very closely.

In Figures 27 through 32, it can be seen that correlations were attempted between time (in 4 months) each year for 10 years that a chosen index was above a prescribed value inside and time the outdoor dry-bulb or wet-bulb temperature exceeded 80°F (26.7°C) or 67°F (19.4°C), respectively. Because of the structure of the present HUD criteria [2], it was felt that this would be one way to describe quantitatively the "thermal performance" of the unit. As the figures indicate, the correlations were not very significant.

Seeking a correlation covering a shorter period of time, Figures 33 and 34 show the daily maximum values of the KSU index inside as a function of maximum dry-bulb temperature and wet-bulb temperature outside for August of 1954 in Jersey City. The results are much better than the previous ones but still too scattered to be of much value. Additional similar correlations were tried where the independent variable was respectively, the outside dry-bulb temperature at 4 p.m., the outside dry-bulb temperature at 5 p.m., and the average of maximum dry-bulb temperatures the day before and on the day in question. However, when the same dependent variable was plotted as a function of average (over a 24 hour period) outdoor dry-bulb temperature the result was very much improved as shown in Figure 35. The correlation coefficient ( $r$ ) for this particular set of data was 0.97 (maximum possible value = 1.0)<sup>a</sup>. The same degree of success was attained with other indices such as the new effective temperature shown in Figure 36 and for other months (see Table 8). This is in agreement with the findings of Loudon [8] in which he states: "...heavy buildings screened from solar radiation do not rise more than a few degrees above the mean outside temperature unless there are appreciable heat gains from lighting, occupants or other heat sources. It is primarily the daily-mean temperature that has to be considered, rather than the maximum; diurnal temperature variations can be smoothed by the thermal capacity of the building".

The daily average temperature used was not the average of the twenty-four hourly values but rather the average of the daily maximum and daily minimum. The particular average was chosen due to the fact that many United States Weather Bureau Stations report this parameter [31]. The discrepancy is usually quite small as the curves of Figure 37 indicate.

The straight lines of Figures 35 and 36 were determined by regression analysis (method of least squares) in order to fit the data as close as possible. In fact, similar regression lines were determined for June, July and August of all ten years. It was found that each of the 30 lines fell within the corridor of Figure 38.

The importance of such correlation results lie in the fact that if proven valid for a class of buildings with similar thermal response characteristics, a particular line could be determined for a given housing unit-weather data group by a small number of calculations compared to a lengthy hour by hour computation. The results for an extended period of time could then be determined by scanning of weather tapes alone.

Table 9 was constructed by using a special routine to scan the weather tape. It shows for the year 1949 in Jersey City, the number of days during the year (in the right-hand column) in which the daily outdoor average dry-bulb temperature is equal to or greater than the temperature in the left-hand column. Consequently, if a linear relationship, such as Figure 35 or Figure 36, is established for a particular building, then the number of days

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<sup>a</sup>According to reference [30], for the population chosen, a significant correlation exists for  $r > 0.4$ .

in which the indoor environment could be expected to be at or above a certain specified comfort condition could be determined at a glance. For example, Figure 38 shows that for the particular building being analyzed, a KSU value of 5 corresponds to an outside temperature of approximately 81°F (27.2°C)<sup>a</sup>. Table 9 indicates that the daily average temperature was equal to or exceeded this value 23 days during 1949 in Jersey City. This corresponds to approximately 20 percent of the summer days (4 months). From the detailed printout of the hour-by-hour simulation computer run, it was determined that the KSU value equalled or exceeded 5 on 32 different occasions<sup>b</sup>.

For the remainder of the feasibility study conducted to date, emphasis was placed on determining the validity of the above "short-cut" approach. There were several questions that had to be answered. Was the correlation with outside average dry-bulb temperature valid for other types of buildings? Did the correlation change when the building was moved to another climatic region or could one "line" be assumed valid for all localities. What is the minimum amount of hour by hour simulation needed to determine the relationship? What is the sensitivity of the correlation to changes in the configuration of a given building? The degree to which the above questions were satisfactorily answered is described in the remainder of this section.

The simulations and calculations done thus far did not include the calculation of mean radiant temperature in the space. Consequently in the calculation of the indices, the MRT was always assumed equal to the dry-bulb temperature. Once the equations described in Appendix A for the calculation of mean radiant temperature were included in the simulation model, some plots were made to determine if the effect was significant. Figure 39 shows to what extent the mean radiant temperature differs from the indoor dry-bulb temperature on a relatively cool day that followed several warm ones. As can be seen from the plot, the difference can be as much as 4°F (2.2°C) if the MRT is calculated near a cold surface but only 1°F (0.55°C) if calculated in the center of the space. In addition, the calculation showed that equation (8) of Appendix A was sufficiently accurate for the present application. Figure 40 shows the difference in the resulting correlation due to the inclusion of the MRT calculation. This was to increase the comfort vote by 0.5 at an average outdoor temperature of 75°F (23.9°C). Therefore, for the remainder of the study, the MRT calculation (in the center of the space) was included.

The air change rate assumed in the apartment simulation was most favorable for taking advantage of "natural cooling" that is, a high rate of air flow rate at night (6 volume changes per hour) to precool the apartment and a low flow rate during the day when the outdoor temperature is likely to be high. Perhaps an assumption such as this shouldn't be used as a base for establishment of the criteria tables since this "optimum control" of outside air introduction will seldom be used in actual practice. Consequently some of the calculations were repeated to determine the effect of this variable.

Hour-by-hour calculations were repeated three times for the year 1949 for three additional rates of air change. First the air change rate was assumed constant at 1 volume change per hour<sup>c</sup>. The calculations were repeated for the case where the flow rate was controlled according to the outdoor temperature. Finally, one other simulation was done where the air flow rate was controlled according to an empirical equation developed by Coblentz and Achenbach [32]. They measured actual infiltration rates in ten electrically-heated houses in Indiana. The homes were a variety of one- and two-storey brick and frame built over basements, crawl spaces, and concrete slabs. Based on the findings of earlier studies done at the University of Illinois [33], Coblentz and Achenbach expressed their results in terms of a polynomial expression where the infiltration rate was a linear function of the outdoor wind velocity (W) and inside-outside temperature difference (ΔT).

$$I = A + BW + C\Delta T \quad (4)$$

<sup>a</sup>Corresponding to the center of the corridor.

<sup>b</sup>Since 32 is larger than 23, the KSU index went above 5, dropped below, and rose above again on the same day.

<sup>c</sup>This is the common assumption in most design calculations.

Figure 41 shows the effect of the different assumptions on the indoor dry-bulb temperature during one particular day. Figure 42 is the corresponding plot for indoor wet-bulb temperature. Finally, Figure 43 shows the effect on the resulting correlation line. As can be seen, the Coblenz-Achenbach expression is perhaps the most "conservative" assumption to use, causing the comfort vote to be increased by 1.0 at an average outdoor temperature of 75°F (23.9°C) compared to the original assumption of 1 during the day and 6 at night. The assumption of 1 air change per hour resulted in an increase of 0.7 in the comfort vote at 75°F (23.9°C). Based on these results, it is felt that 1 air change per hour should be used as the base assumption in establishing the criteria.

The "thermal performance" of the apartment was, of course, expected to change if the pertinent building characteristics were changed. Hour by hour calculations were made for the summer of 1949 when the large picture window facing west was changed from double pane with a white opaque roller shade (S.C. = 0.22) to single pane with a medium colored venetian blind (S.C. = 0.64). Figure 44 shows the effect of this change on the resulting correlation "line" (an increase of 0.5 in the comfort vote at an average outdoor temperature of 75°F (23.9°C)) and Figure 45 shows the relationship between the new line and the previously determined corridor.

A simulation was done for the summer of 1949 when the originally defined building is simply reoriented so that the exposed wall and large picture window now face north. Figure 46 shows the relationship between the correlation "line" determined for this configuration and the previously determined corridor. Calculations were also done for the summer of 1949 when the above two changes (modified window and 90° rotation) were combined. In addition, computer runs were made for the summer of 1954 where the same configuration changes were made. Table 10 shows that with the configuration changes described, the correlation with the average outside dry-bulb temperature continued to be good.

The given building considered to this point had only 1 external surface (the west facing wall). Figure 47 shows the effect of first making all the walls exposed to the outside environment and then finally the walls and the roof. Compared to the originally defined apartment, the comfort vote is increased by 0.5 at an average outdoor temperature of 75°F (23.9°C) when all surfaces are exposed to the outside.

It is felt that from observing results similar to those of Figures 43 through 46, that the window specifications, building orientation, and the number of exposed surfaces in the external structure are all parameters that must be considered independent variables in the matrix of the air conditioning criterion.

One of the most important factors to determine during the latter part of this feasibility study was to what extent the good correlation with outside average dry-bulb temperature would hold when the relative weight or massiveness of the structure was changed and/or the weather conditions or locality.

Another building was selected for simulation from the plans of the various Housing System Producers in the Operation BREAKTHROUGH Program. Since the first apartment simulated was a rather heavyweight one, it was decided to select one with very light weight construction elements. As shown in Table 11, the weight of the walls was only 4 lb/ft<sup>2</sup> (20 kg/m<sup>2</sup>) compared to 81 lb/ft<sup>2</sup> (395 kg/m<sup>2</sup>) for the first one.

A more detailed description of the building and individual apartment simulated is as follows:

1. The apartment building is a 5-story, two-level structure, with windows facing north and south. The first level consists of 3-story, 4-bedroom dwelling units, and the second level of a mix of 2-story, 2-bedroom and 1-story, 1-bedroom units. The two levels are separated by 18-gage steel deck on a 1.33 inches (3.38 cm) thick concrete channel structure. The space chosen for simulation was one located at the third floor on level 1 and is part of a 3-story, 4-bedroom unit. No building shadow was used and the adjacent spaces were assumed to always be at the same temperature as the chosen space.



2. The exposed wall (north and south) is constructed of 0.5 inches (1.3 cm) of gypsum sheathing and 0.5 inches (1.3 cm) of gypsum wall board, with 4 inches (10.2 cm) of air space in between. The overall exterior wall area facing south is 112 ft<sup>2</sup> (10.4 m<sup>2</sup>), and contains 48 ft<sup>2</sup> (4.5 m<sup>2</sup>) of opaque surface and 54 ft<sup>2</sup> (5.9 m<sup>2</sup>) of single pane, 1/8 inch (0.32 cm) window glass. The exterior wall facing north has the same composition.
3. The floor is composed of carpet on 5/8 inch (.16 cm) plywood which is over an 8 inch (20.3 cm) air space, 5/8 inch (.16 cm) plywood, 6 inches (15.2 cm) air space, and 1/2 inch (1.3 cm) gypsum ceiling board. The ceiling is composed of 5/8 inch (.16 cm) plywood on 18-gage steel deck on 1.33 inch (3.38 cm) concrete channel structure and 3/8 inch (0.95 cm) plywood on 1/2 inch gypsum ceiling board with 6 inches (15.2 cm) air space in between the plywood and ceiling board. The floor to ceiling height is 8 ft (2.4 m) and the total floor area is 482 ft<sup>2</sup> (44.8 m<sup>2</sup>).
4. The partitioned walls are composed of 1/2 inch (1.3 cm) gypsum wall board and 3/8 inch (0.95 cm) plywood with 4 inches (10.2 cm) of air space in between.
5. The maximum number of occupants is 3, the maximum equipment load is 1/2 W/ft<sup>2</sup> (5.4 W/m<sup>2</sup>), and the maximum lighting load is 1 W/ft<sup>2</sup> (10.8 W/m<sup>2</sup>).
6. The infiltration or natural ventilation rate was simulated as 1 air change/hour constant.

The hour by hour simulation was again repeated for this apartment in Jersey City, New Jersey. Figure 48 is a correlation plot of the maximum value of the KSU index inside and the average outside dry-bulb temperature, the same variables that correlated well for the first apartment simulated. As can be seen, the correlation again was quite good, which was encouraging due to the "shortcut" technique that could possibly be used in establishing the criterion. Figure 49 indicates that for the same month in the same locality, the maximum comfort vote in the same apartment would be approximately 0.5 higher for a given average outdoor dry-bulb temperature. The effect of making more of the apartment exposed to the outside was examined here as before. Figure 50 shows that the effect on this lightweight building was even more pronounced than with the heavyweight one. When all four walls plus the roof were exposed and an additional window was added in the wall facing west (to make a more realistic unit) the comfort vote increased by 1.0 at an average outdoor dry-bulb temperature of 75°F (23.9°C).

Additional factors that were not examined in any previous calculations, were the effect of amount of floor area and relative shape of the floor. This, of course, affects the surface to volume ratio of the space and could in turn be expected to affect the resulting indoor conditions. Figure 51 shows the results of simulating the lightweight apartment in New Jersey with the maximum amount of exposure and then changing the shape of the floor area to square (22 ft (6.7 m) by 22 ft (6.7 m) instead of 14 ft (4.3 m) by 35 ft (10.7 m)) and then in turn reducing the floor area by a factor of three. As can be seen, the effect was minimal which should indicate that these variables not necessarily be included as independent parameters in the criterion matrix.

The only remaining factor to be examined in the feasibility study was the effect of moving to a different climate. Several additional hour by hour calculations or simulations were performed to investigate the effect of changing this parameter.

The heavyweight apartment was simulated on a hour by hour basis in Macon, Georgia for the year 1954. Table 12 indicates that for this apartment, a good correlation was still obtained with the average outside dry-bulb temperature. In fact, an entire corridor was established for Macon for the ten-year period 1949 to 1958 similar to that was done for New Jersey. The corridor is shown in Figure 52.

A disturbing fact was observed at this point. If one overlays the corridor of Figure 52. on that of Figure 38 (see Figure 57), he discovers that for a given average outdoor dry-bulb temperature, the comfort vote in Macon would be approximately 0.25 higher. This indicates that other factors such as incident solar radiation and frequency and duration of hot conditions affect the resulting indoor environment. Also, it gave an indication to the fact that it might not be possible to establish the correlation "line" under one set of environmental conditions and assume that it is valid for all others.

To examine this latter fact closer, some specific results will be cited. Figure 53 shows the effect of simulating the heavyweight building in three different localities. As can be seen, the correlation "line" for this apartment is almost 1.0 comfort vote higher at an average outdoor dry-bulb temperature of 75°F (23.9°C) in Phoenix, Arizona than in Jersey City. Although the effect of climate appeared to be less pronounced for the lightweight apartment (Figure 54) it was observed to be just as pronounced once all the surfaces were assumed exposed (Figure 55).

At this point in the study, it became obvious that at least a small number of hour-by-hour simulations would have to be done in each identified climatic zone. In addition, Table 13 indicates that the correlation with average outside dry-bulb temperature did not turn out to be the "best" of the limited number of variables that were examined as the building configuration and/or climatic zone was changed. Consequently, when this project was discontinued, it was felt that hour by hour simulations in conjunction with the histogram routines used to construct the data for Figures 25 and 26 would be the most desirable tools to use to complete the establishment of the criterion tables. Therefore, it was tentatively decided to abandon the concept of getting the final tabular values by a "shortcut", correlation "line" approach.

As noted previously, this will probably be an expensive (significant amounts of computer time are needed) and time consuming task to undertake because of the large number of variables to be accounted for. It appears that one "conservative" alternative is available. This alternative is as follows: Consider the apartment, building, or room in question exposed to the hot "design-day" conditions that air conditioning engineers use in sizing cooling equipment. The space would be exposed to this day's weather data for 4 to 7 consecutive days (until a steady periodic condition existed where the indoor environmental conditions were repeated from one day to the next). The peak value of one of the comfort indices would then be used to "grade" the environment either acceptable or not. The authors feel this approach should be studied only if the alternative would be to discontinue the work altogether.

To determine if this latter approach gives truly "conservative" results, additional calculations were carried out. The 1% design values of outdoor dry-bulb and wet-bulb temperature presented in the ASHRAE Handbook of Fundamentals [15] for several selected cities (see Table 14) were used in conjunction with the dimensionless daily temperature cycle of Figure 56 (determined from surveying actual weather tapes) to produce a design day cycle for these cities. The heavyweight apartment was then subjected to this design day cycle (in the computer program) for seven straight days using the actual solar radiation in these localities and assuming zero cloud cover. Shown in Figure 57 are the results of the calculations where the maximum value of the KSU index in the apartment during the second and fifth day are plotted for each city. There was no noticeable change after the fifth day. As can be seen, the data points lie on the upper side of the previously determined corridor. Using this type of calculation approach, the decision to air conditioning the various cities would be made entirely on what ordinate value on this plot (or value of comfort index) was deemed acceptable.

## 7. Conclusions and Recommendations

Based upon the preliminary study described in this paper, the following conclusions have been drawn:

1. The computer program "NBSLD" and the modifications and routines that were made or added to it during this study, can be used to supply all information necessary to the establishment of an air conditioning criterion on a sound technical base.

2. The degree to which a space or building would remain acceptable without the addition of mechanical cooling cannot be determined by the use of the "state-of-the-art", "steady-state" comfort indices alone. Other factors such as frequency and duration of hot conditions and consideration of the situations under which people are "uncomfortable" should be taken into account.
3. A criterion can be established in the form of tables that would specify whether or not mechanical cooling should be installed. The parameters that should be considered as independent variables in the tabular matrix are:
  - a. weight per unit area of the building enclosure,
  - b. number of exposed surfaces of the building enclosure,
  - c. degree of shading for the windows,
  - d. shape of roof if exposed (peaked or flat),
  - e. orientation of the building, and
  - f. geographical location

Other possible independent parameters might be

- a. air infiltration rate,
  - b. percent of the exposed surface area that is glass,
  - c. aspect ratio of the floor, and
  - d. floor area
4. On the basis of weight per unit area of a building enclosure, the following classification can be used:

Lightweight Structure: less than 20 lb/ft<sup>2</sup> (98 kg/m<sup>2</sup>)

Medium Weight Structure: 20 (98) to 59 lb/ft<sup>2</sup> (244 kg/m<sup>2</sup>)

Heavyweight Structure: greater than 50 lb/ft<sup>2</sup> (244 kg/m<sup>2</sup>)

The following recommendations are made, based upon the study described:

1. A research contract should be given to some organization or individual doing physiology or related research work to establish both the definition and acceptable limits of the Predicted Indoor Habitability Index as introduced in this paper.
2. A separate research task should be undertaken to divide the United States into a sufficiently large number of climatic regions with typical hour-by-hour summer weather data for June, July, and August established for each region.
3. Based upon the information within this paper and elsewhere, a sufficient number of "typical buildings" should be defined for simulation taking into account the pertinent independent variables in 3. above.
4. In light of the "Energy Problem" in the United States today, this study should be continued to completion so that the results could be used for showing those situations where mechanical cooling are unnecessary.



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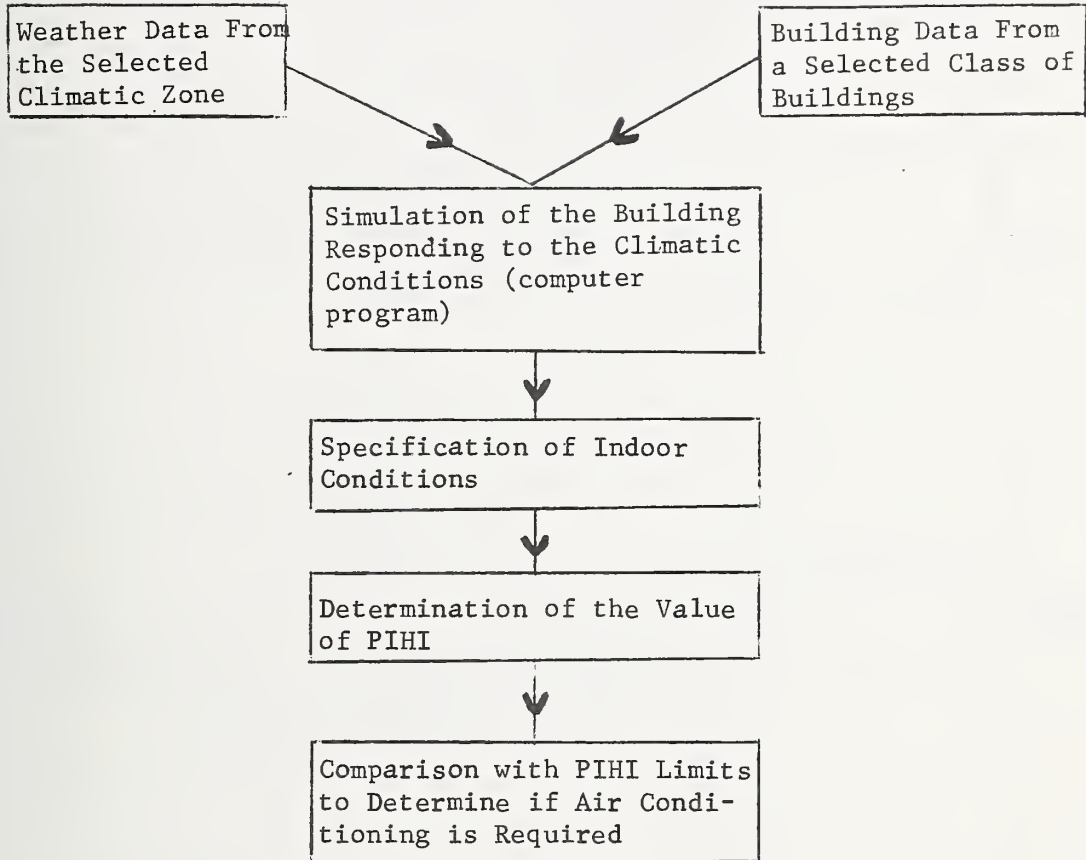


Figure 1 Concept of Determining the Need for Air Conditioning

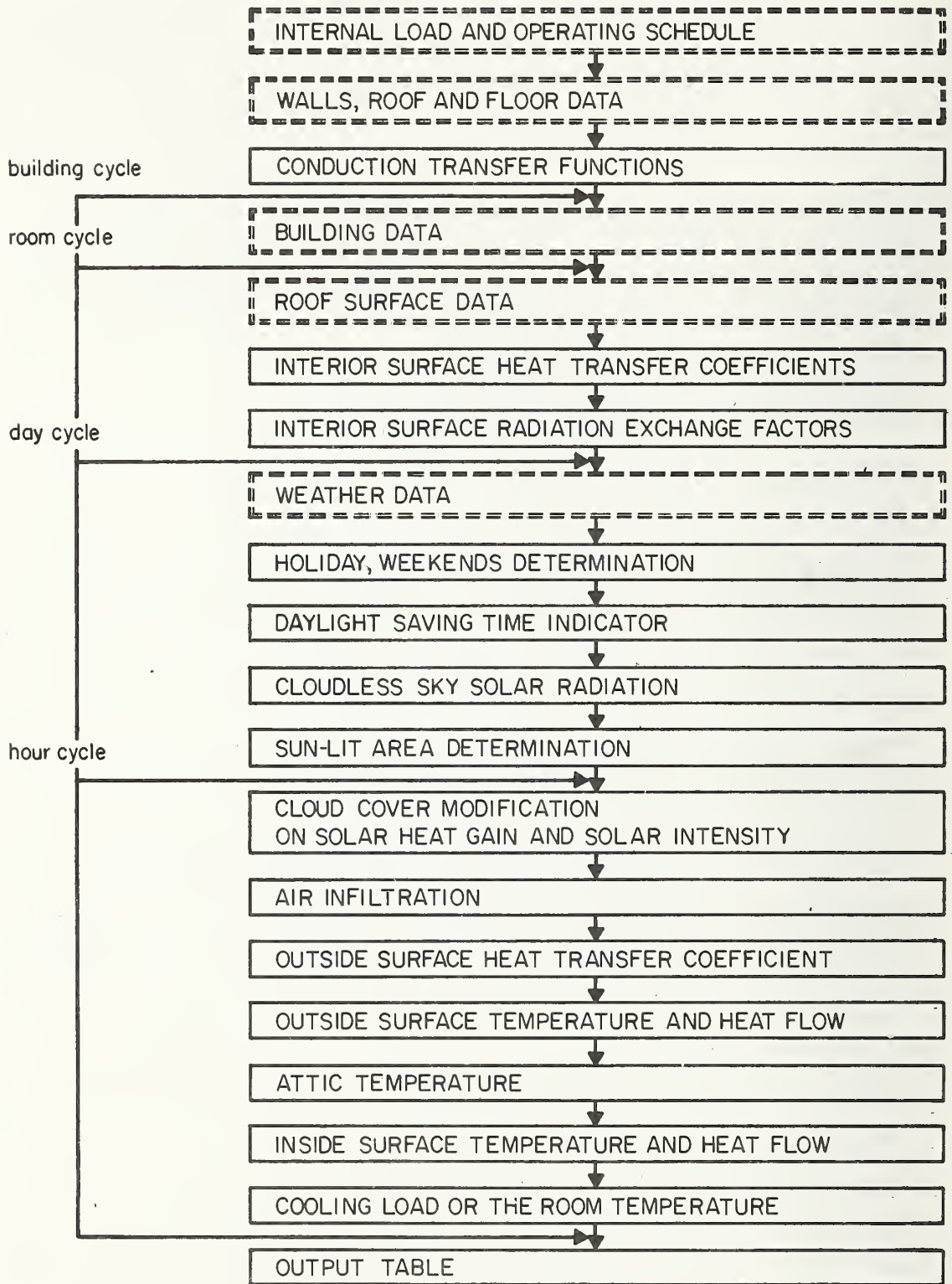
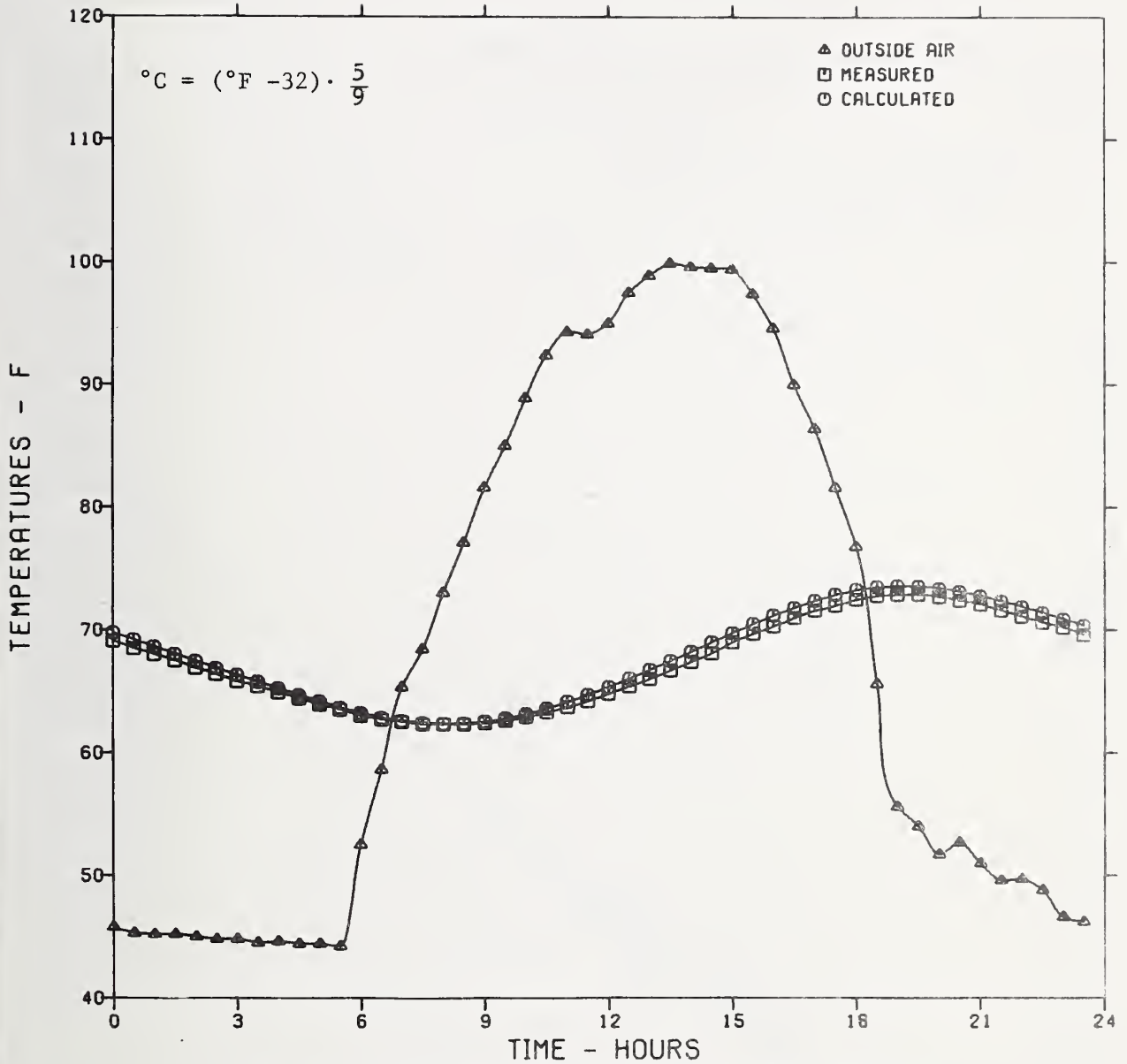


Figure 2 NBSLD Calculation Sequence



NO INSULATION, NO WINDOWS, INTERNAL MASS.

Figure 3 Comparison of Predicted and Measured Indoor Air Temperature for a 20 ft (6.1 m) by 20 ft (6.1 m) by 10 ft (3.1 m) Experimental Masonry Building

EXTERIOR WALL

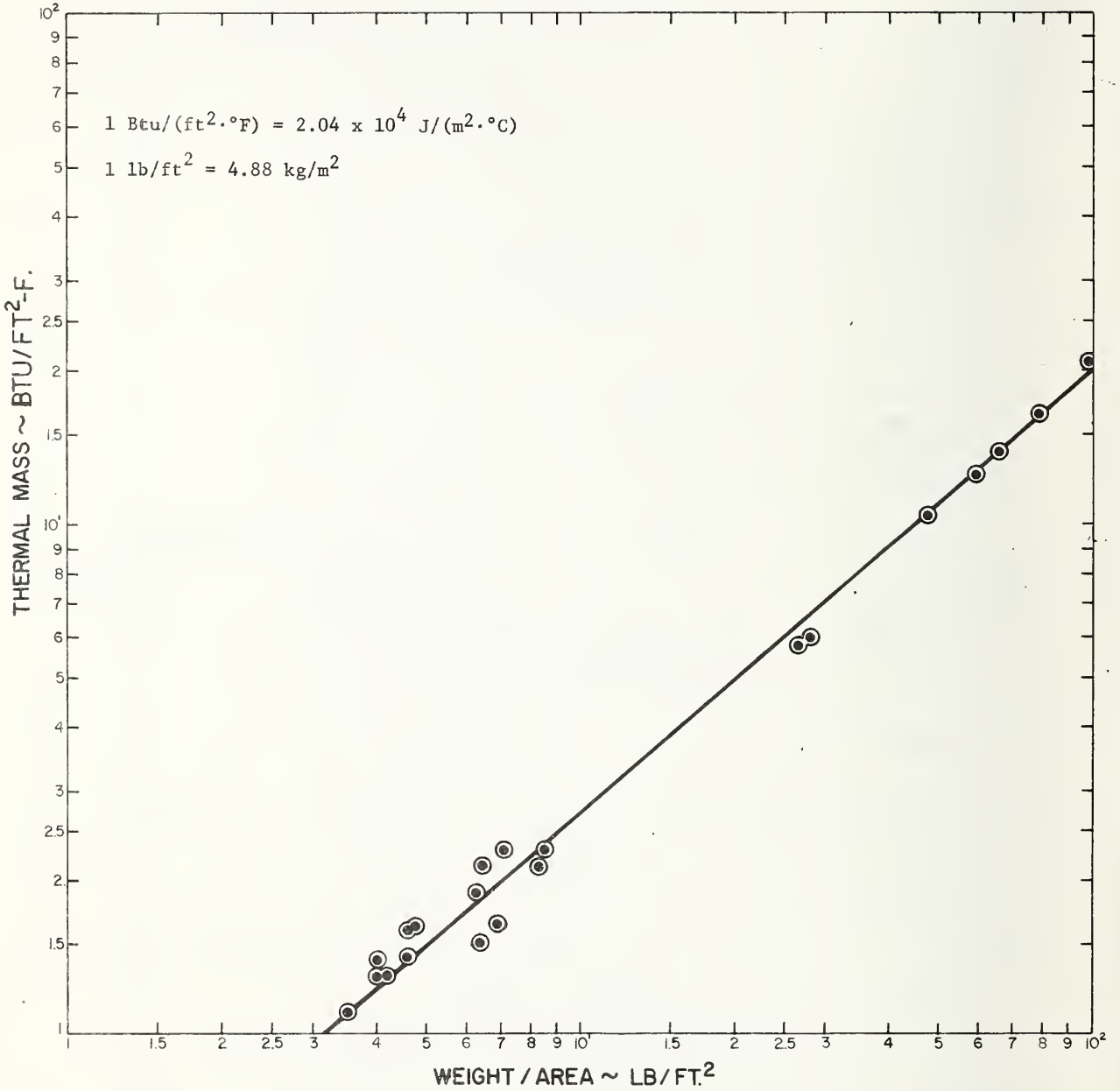


Figure 4 Relation of Thermal Mass to Weight for Selected Exterior Wall Constructions



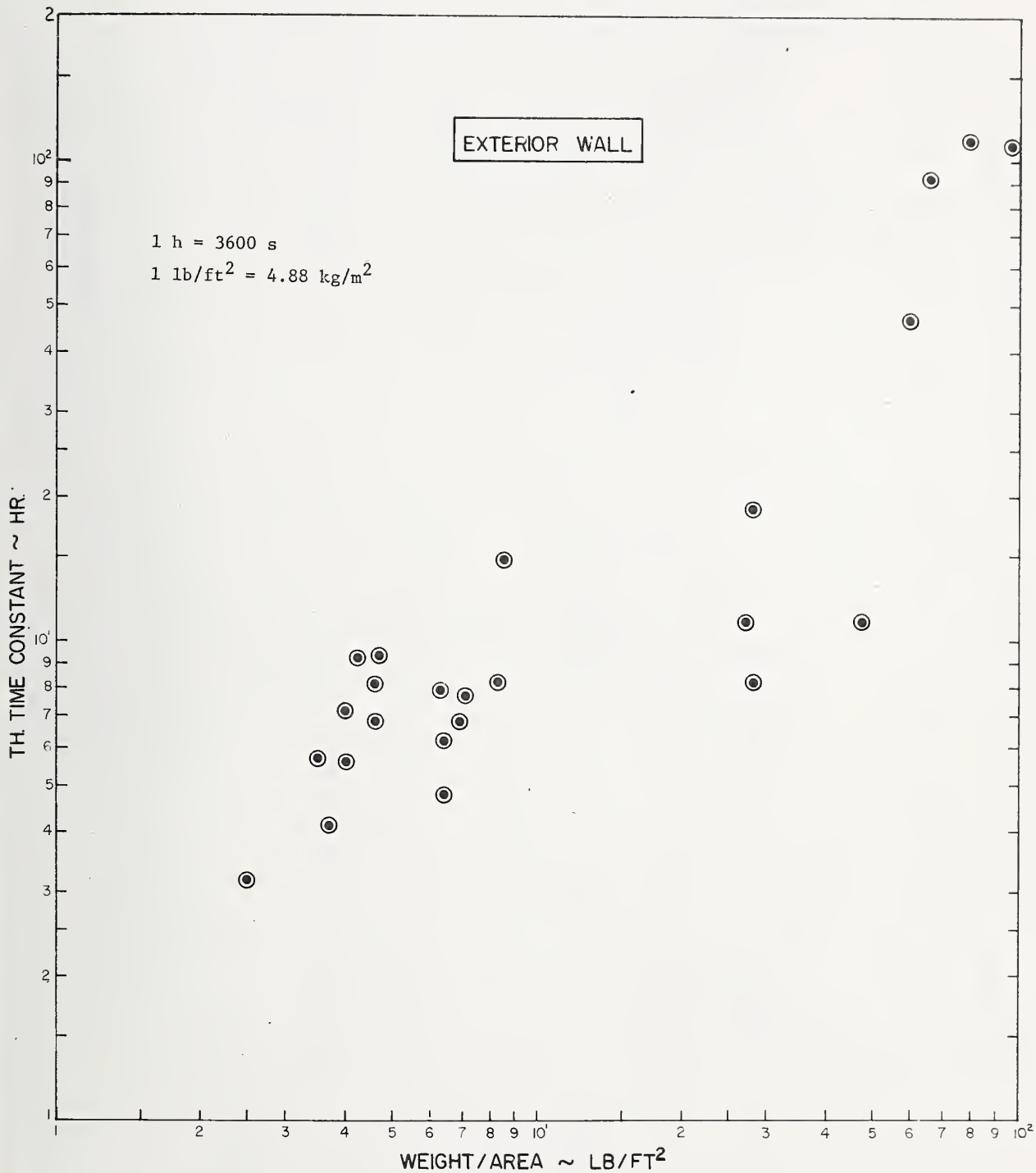


Figure 5 Relation of Thermal Time Constant to Weight for Selected Exterior Wall Constructions

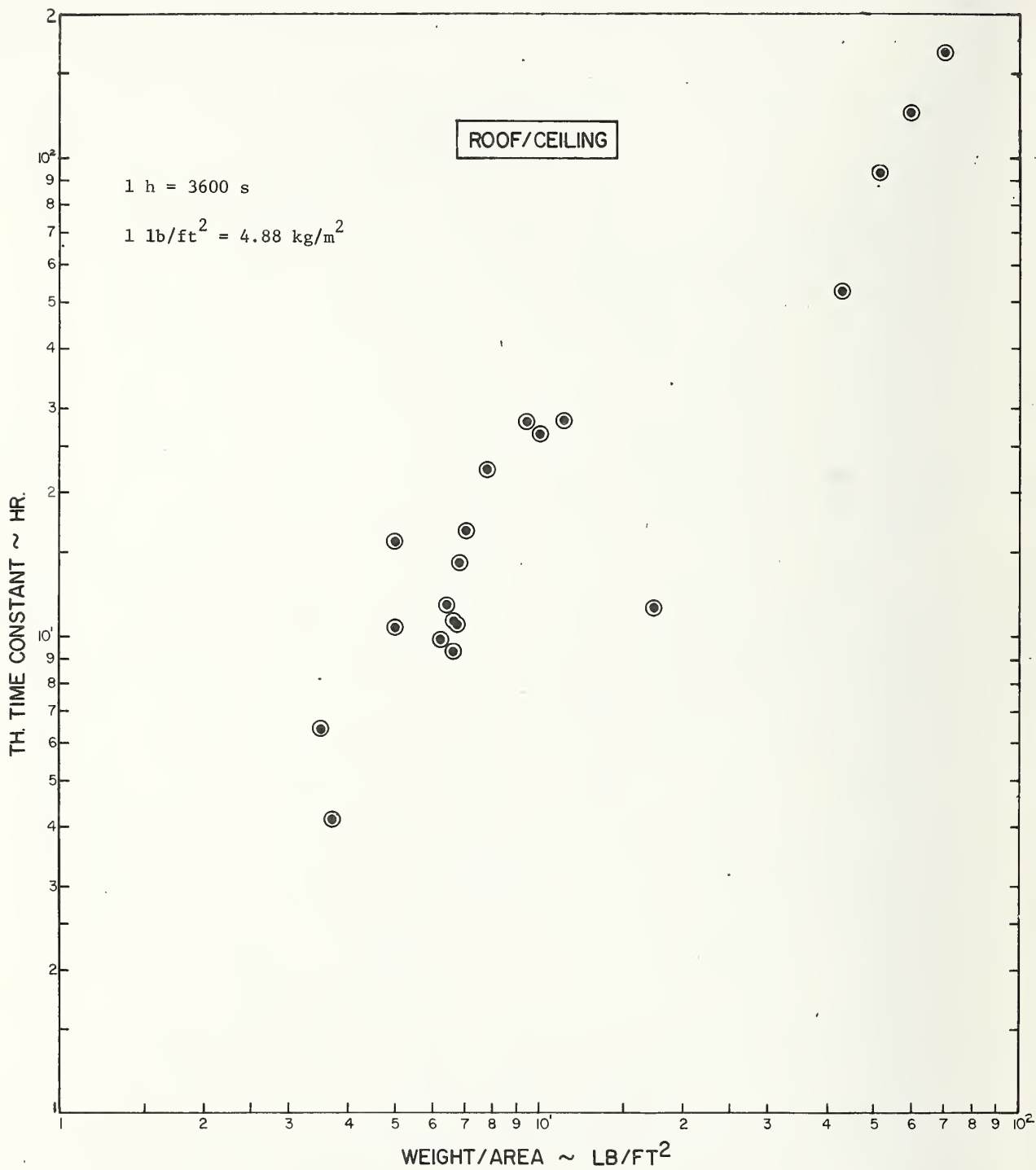


Figure 6 Relation of Thermal Time Constant to Weight for Selected Roof/Ceiling Constructions

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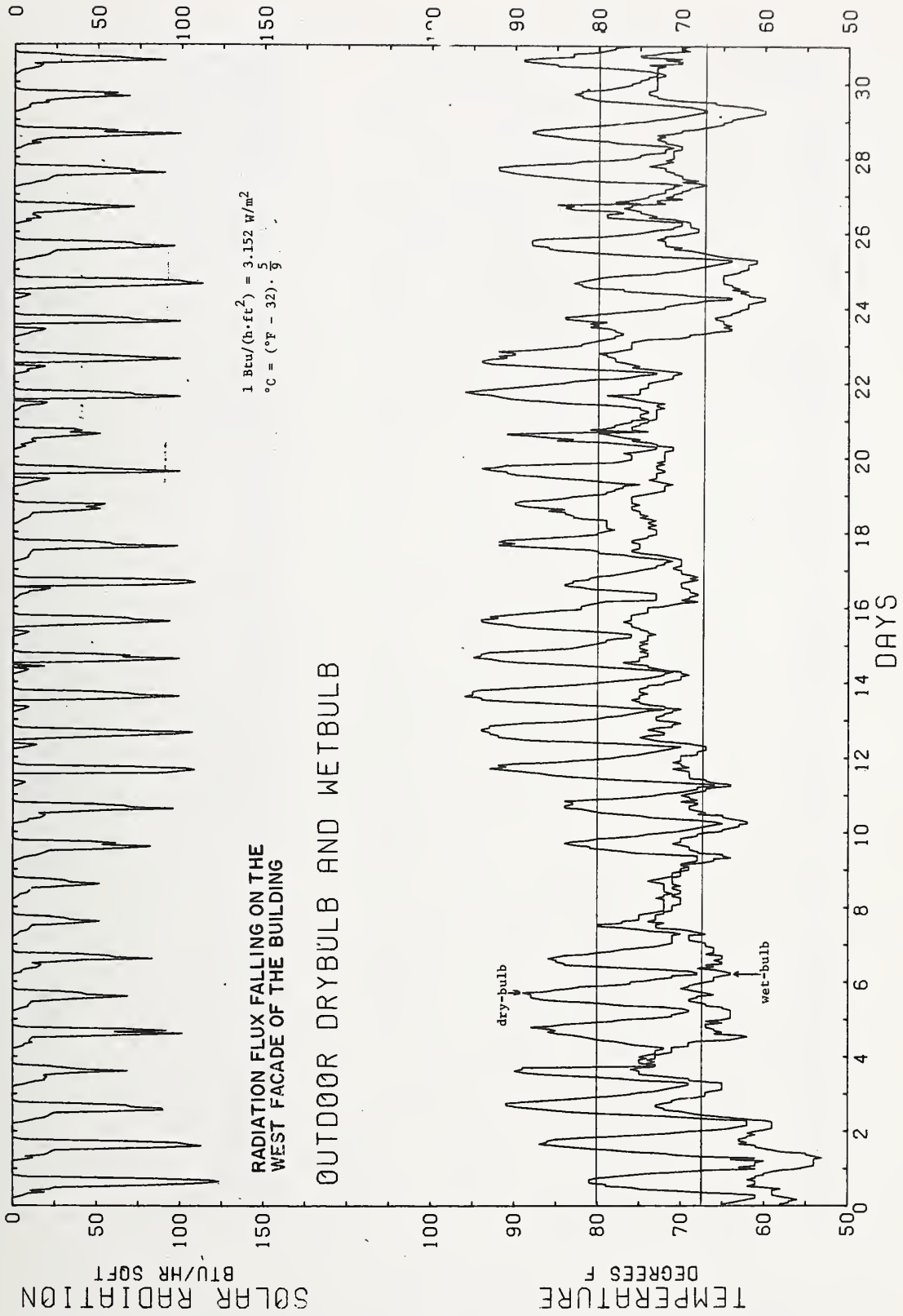


Figure 7 Observed Hourly Outdoor Dry-bulb and Wet-bulb Temperatures and Solar Radiation in the Month of July, 1952, Jersey City, N. J.

JERSEY CITY JULY 1952

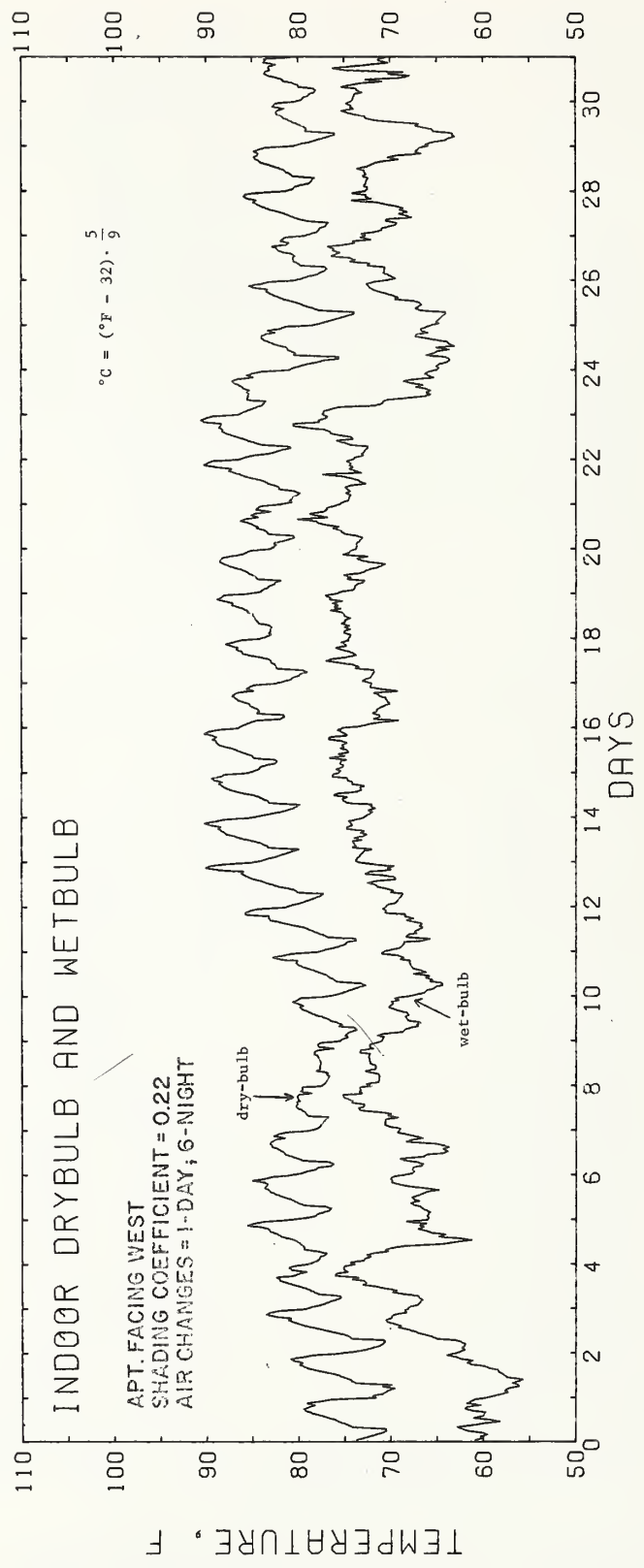
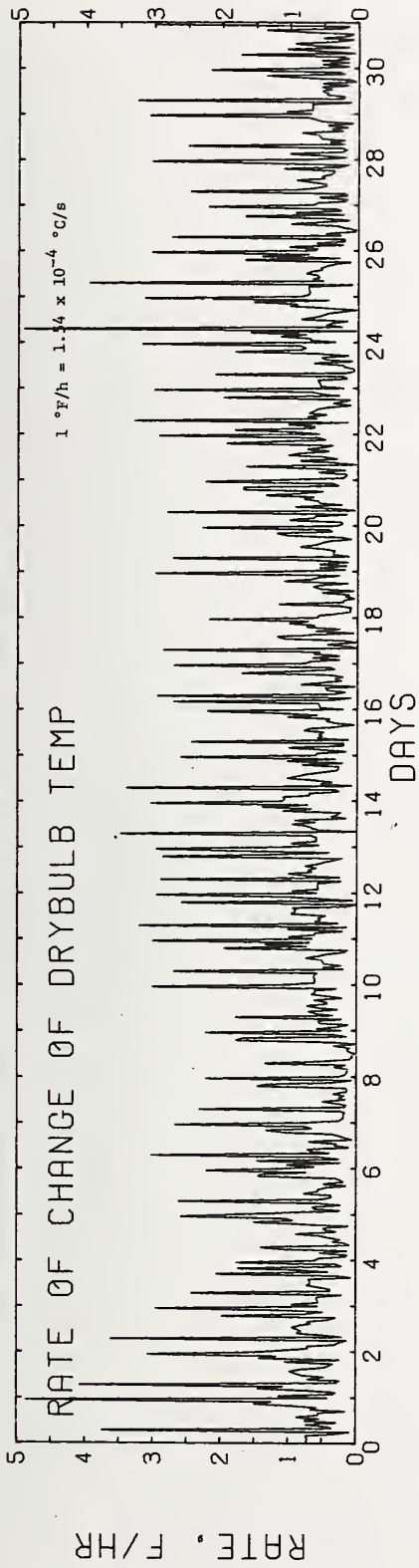


Figure 8 Predicted Hourly Indoor Dry-bulb and Wet-bulb Temperatures for a Heavyweight Apartment in the Month of July, 1952, Jersey City, N. J.



APT JERSEY CITY JULY 1952



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APT JERSEY CITY JULY 1952

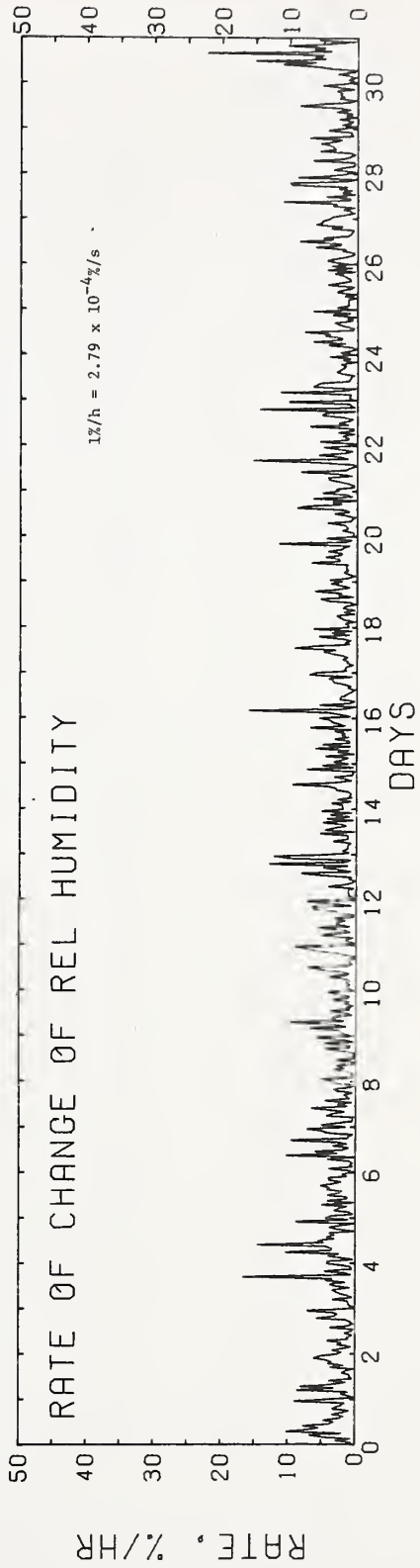
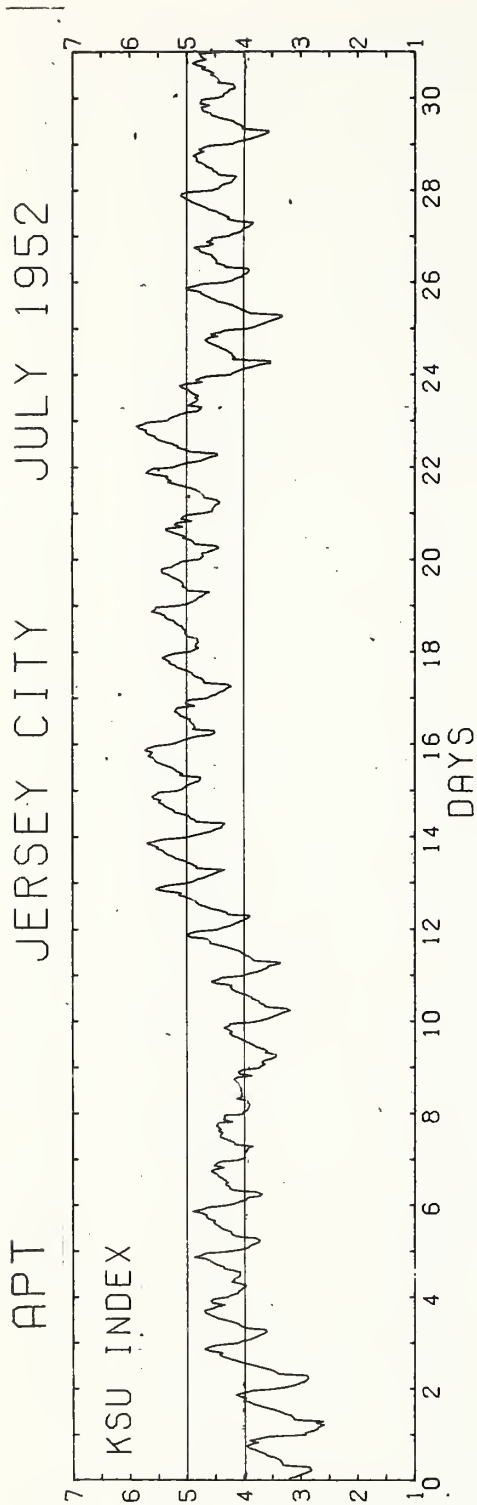


Figure 9 Predicted Hourly Rate of Change of Indoor Dry-bulb Temperature and Relative Humidity for a Heavyweight Apartment in the Month of July, 1952, Jersey City, N. J.



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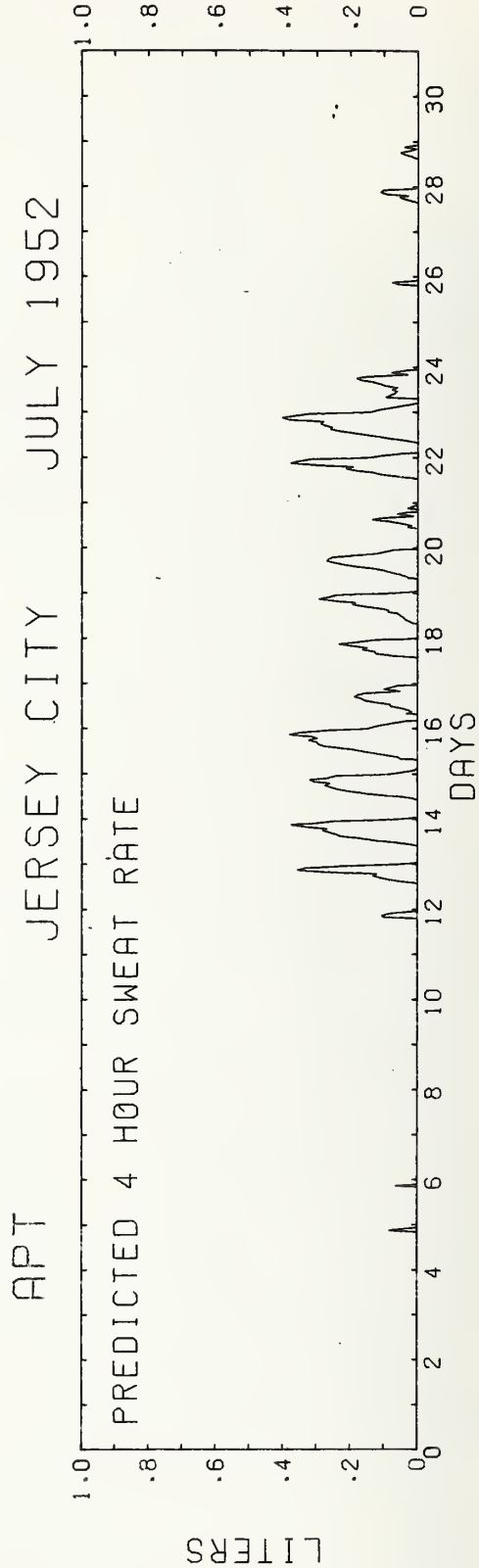
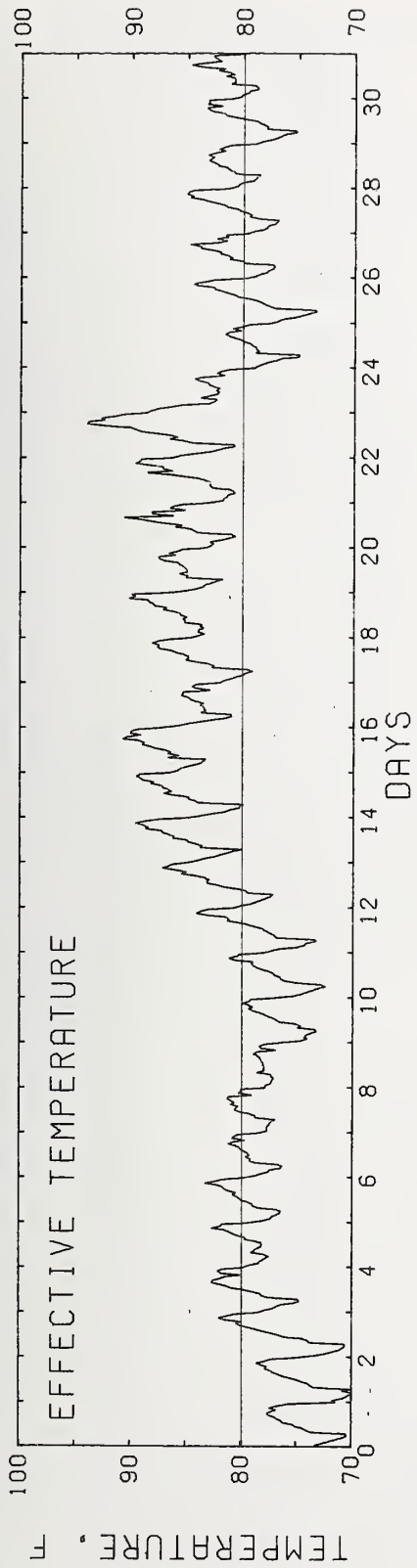


Figure 10 Hourly KSU Index and Predicted Four Hour Sweat Rate for a Heavyweight Apartment in the Month of July, 1952, Jersey City, N. J.

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$$^{\circ}\text{C} = (^{\circ}\text{F} - 32) \cdot \frac{5}{9}$$

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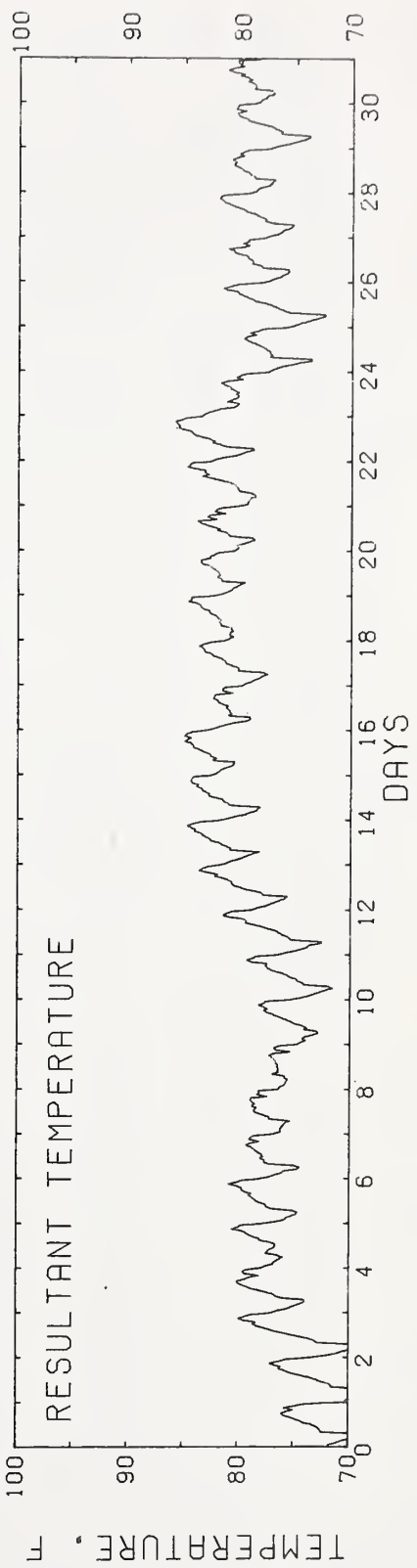
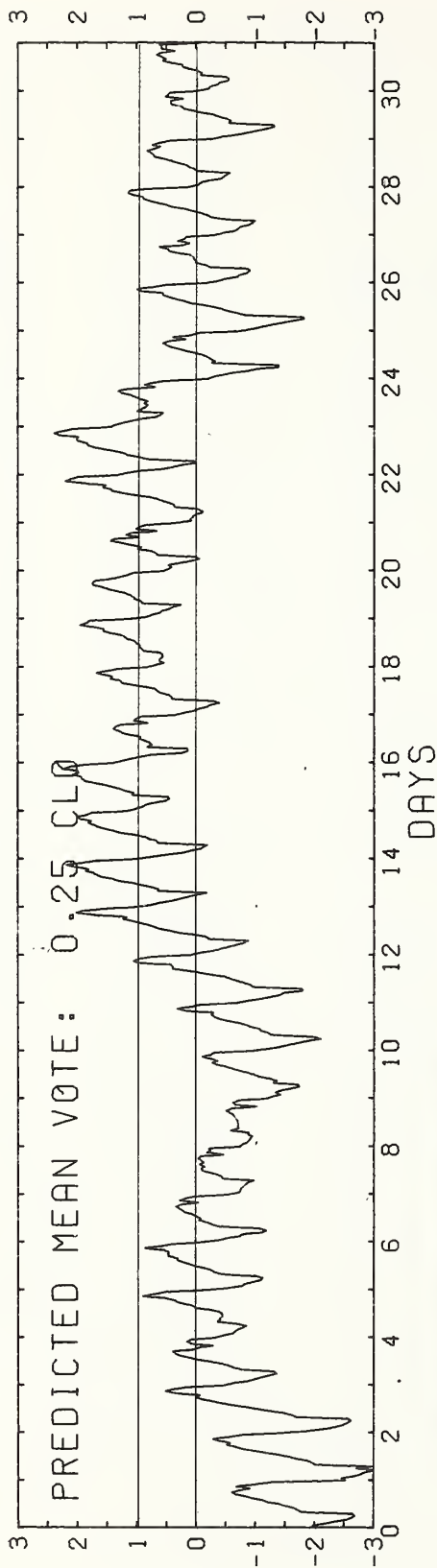


Figure 11 Hourly Effective and Resultant Temperature for a Heavyweight Apartment in the Month of July, 1952, Jersey City, N. J.

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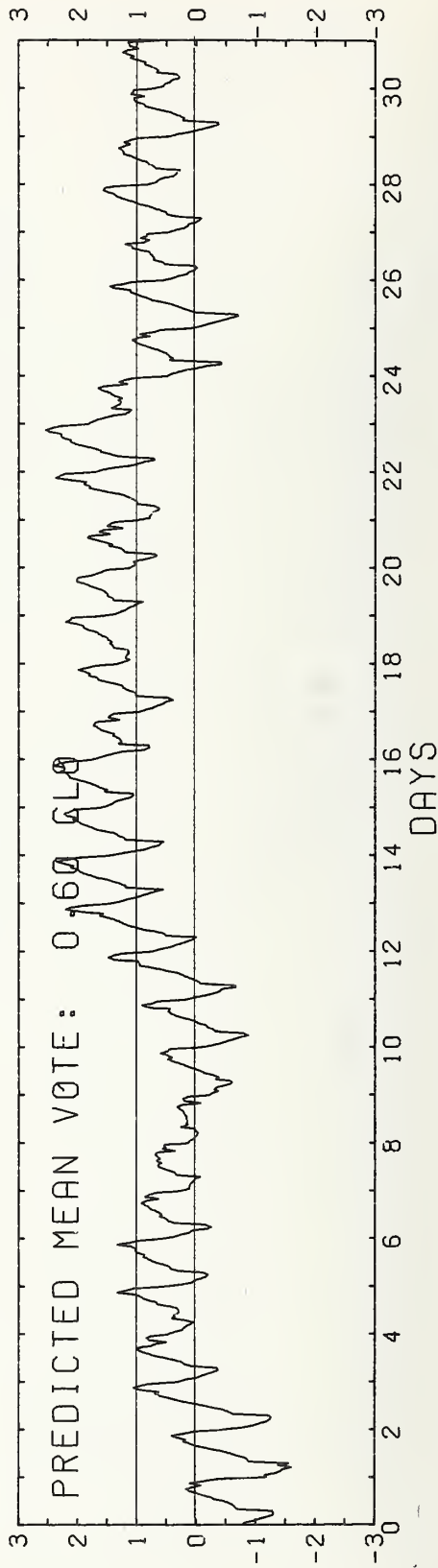
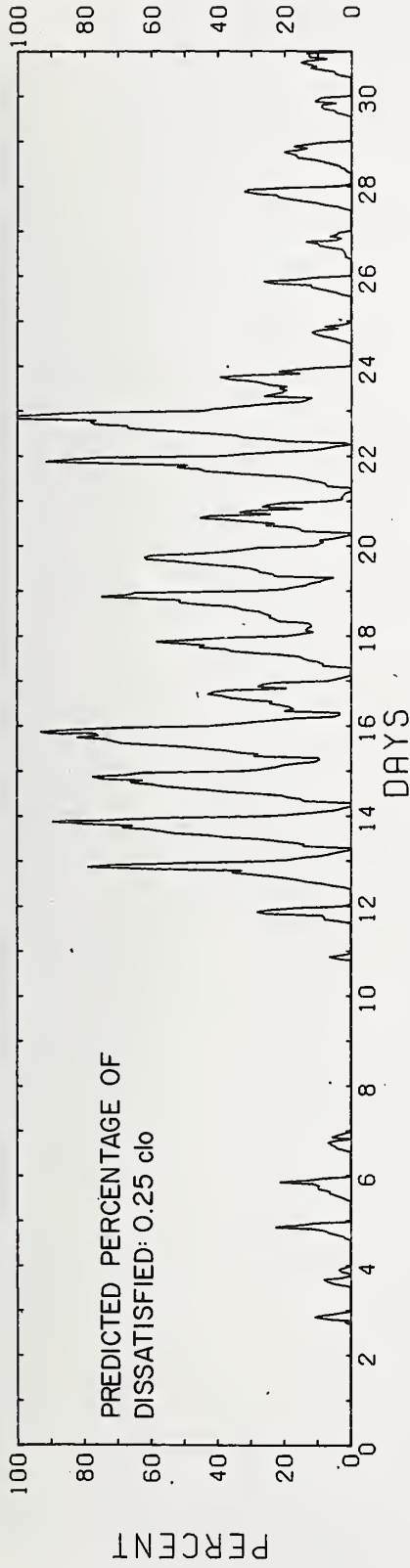


Figure 12 Hourly Predicted Mean Vote (.25 clo and .60 clo) for a Heavyweight Apartment in the Month of July, 1952, Jersey City, N. J.



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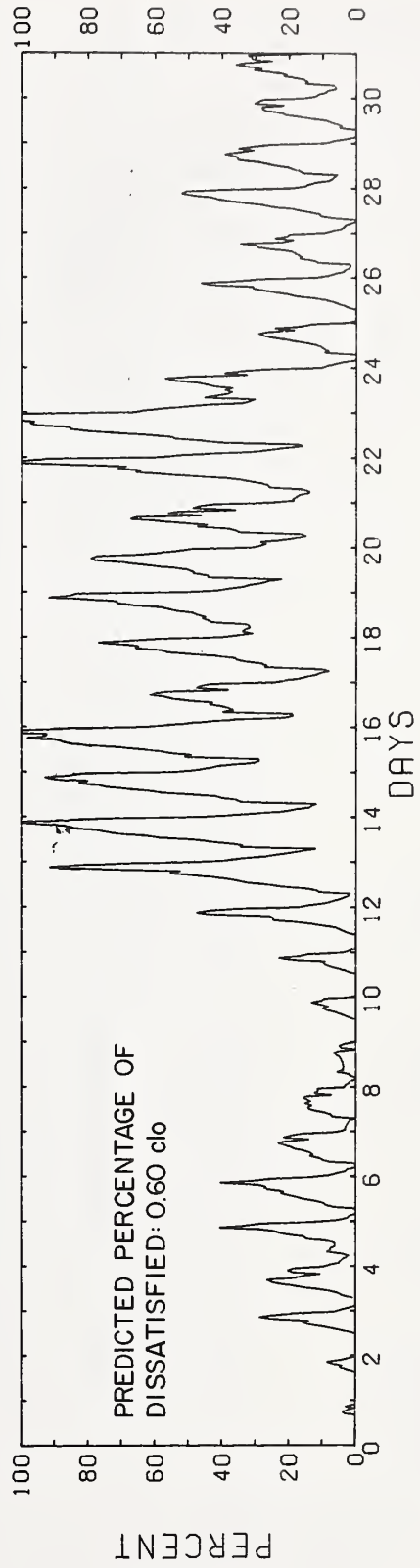
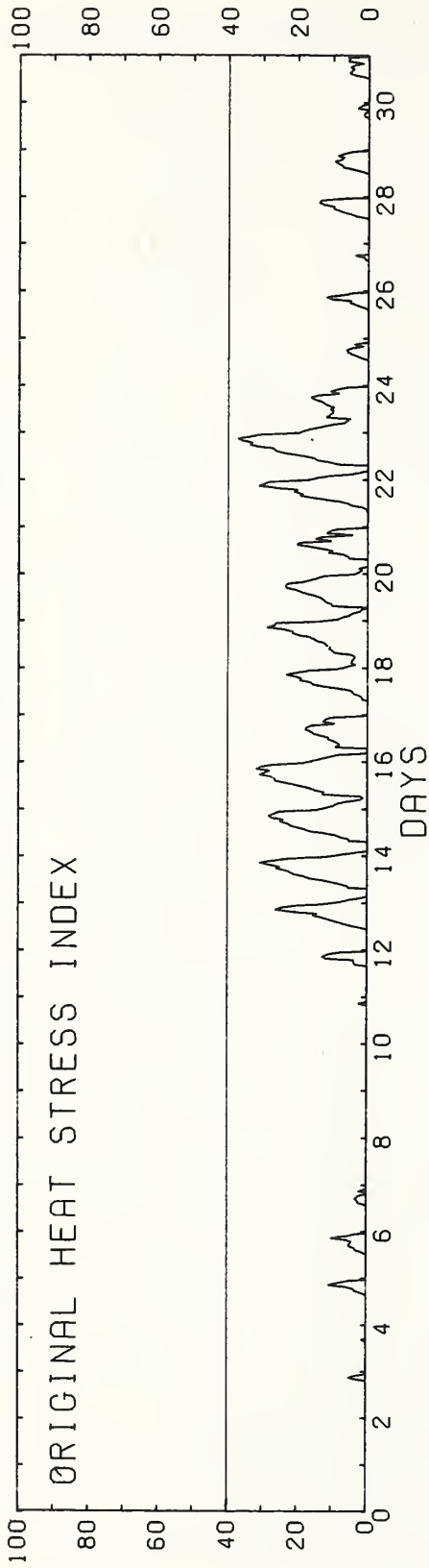


Figure 13 Hourly Predicted Percentage of Dissatisfied (0.25 clo and .60 clo) for a Heavyweight Apartment in the Month of July, 1952, Jersey City, N. J.

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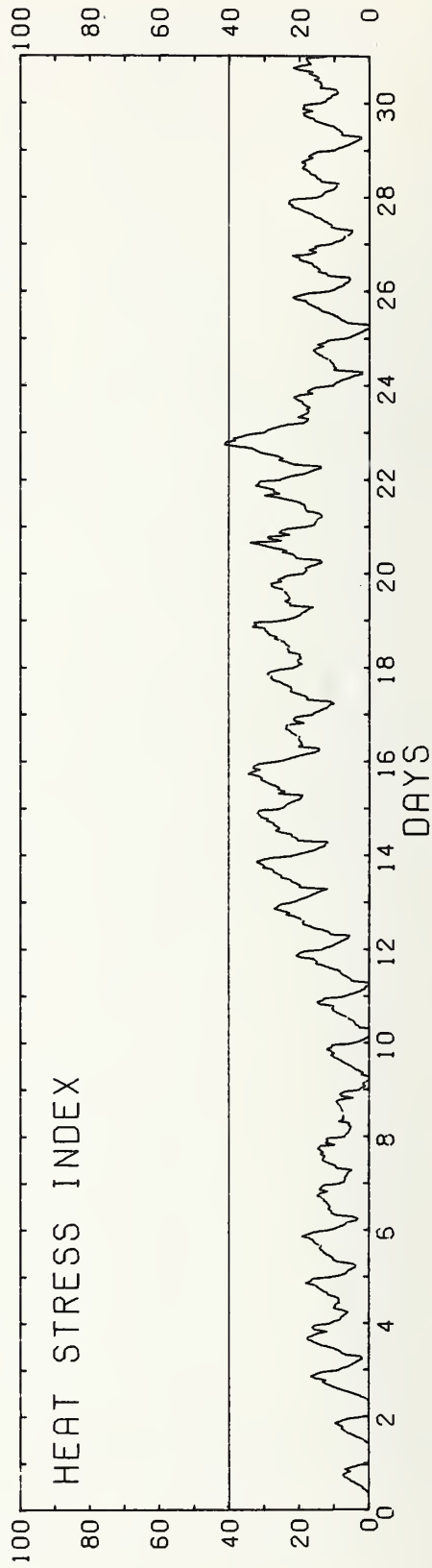
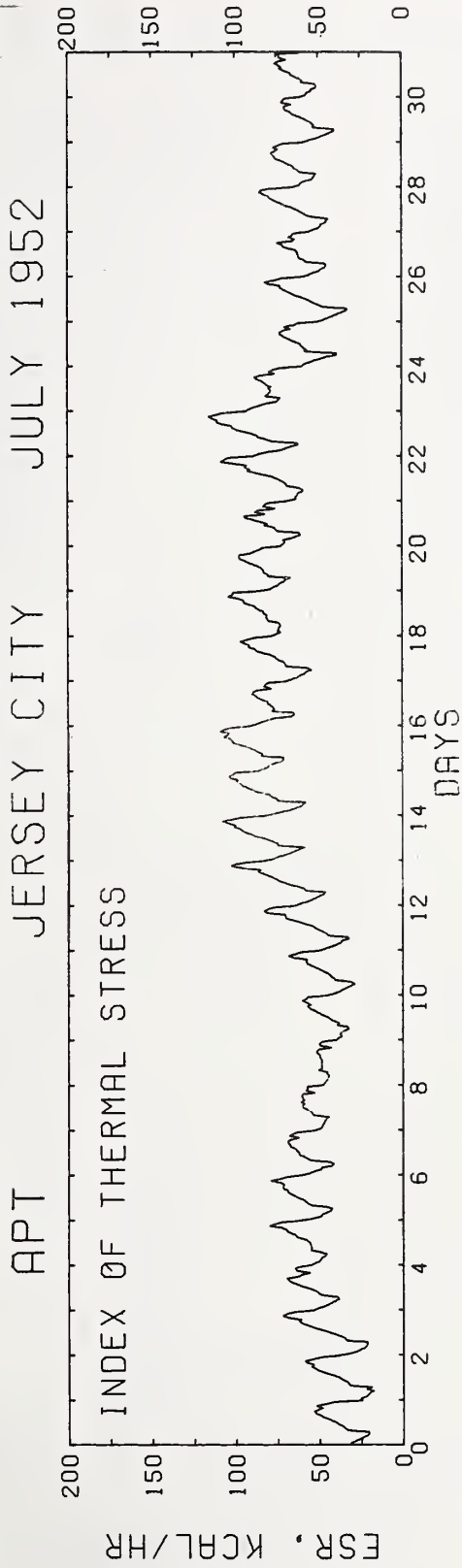


Figure 14 Hourly Original Heat Stress Index and Heat Stress Index for a Heavyweight Apartment in the Month of July, 1952, Jersey City, N. J.



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Figure 15 Hourly Index of Thermal Stress for a Heavyweight Apartment in the Month of July, 1952, Jersey City, N. J.

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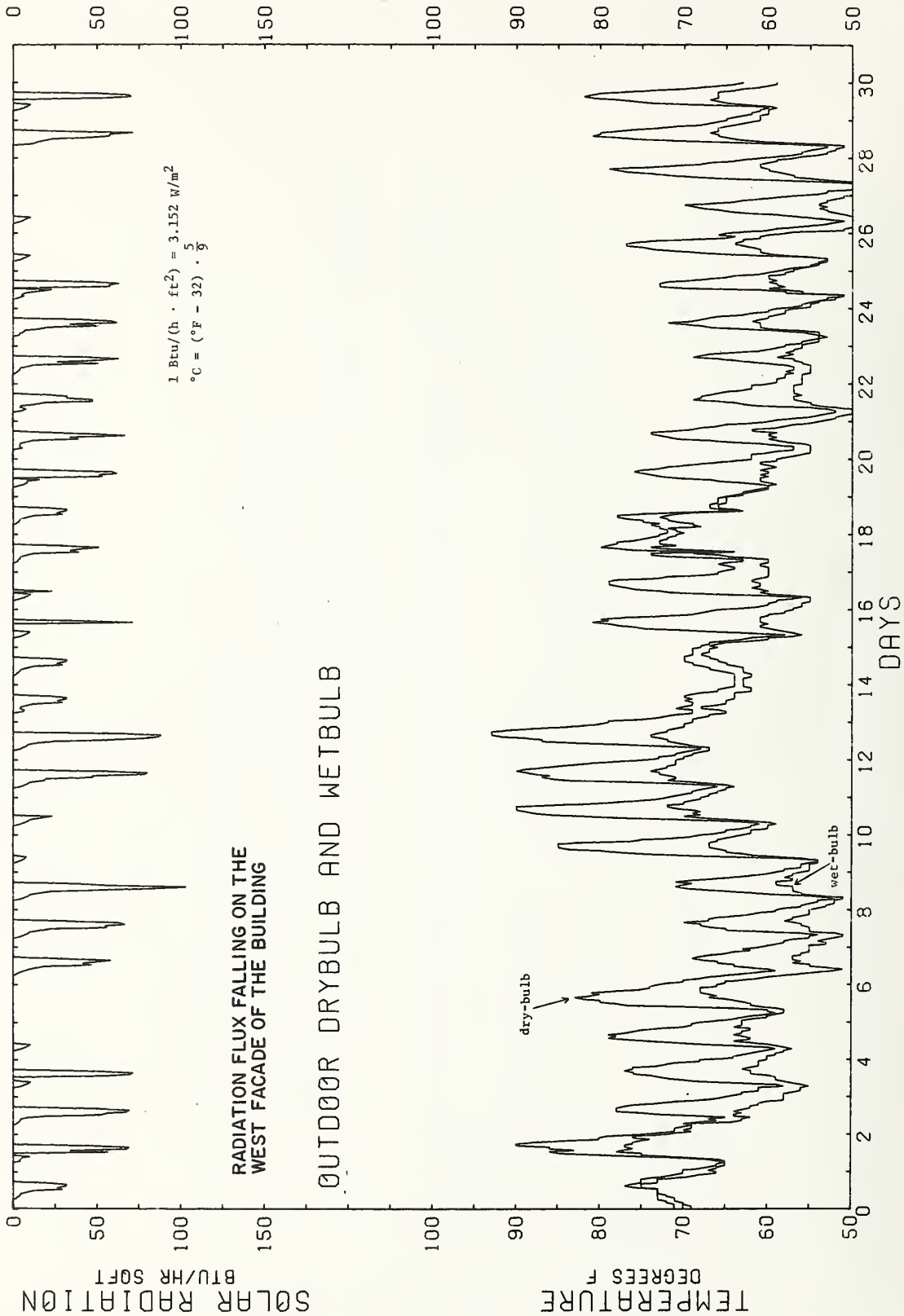


Figure 16 Observed Hourly Outdoor Dry-bulb and Wet-bulb Temperatures and Solar Radiation in the Month of September, 1952, Jersey City, N. J.



# JERSEY CITY SEPT 1952

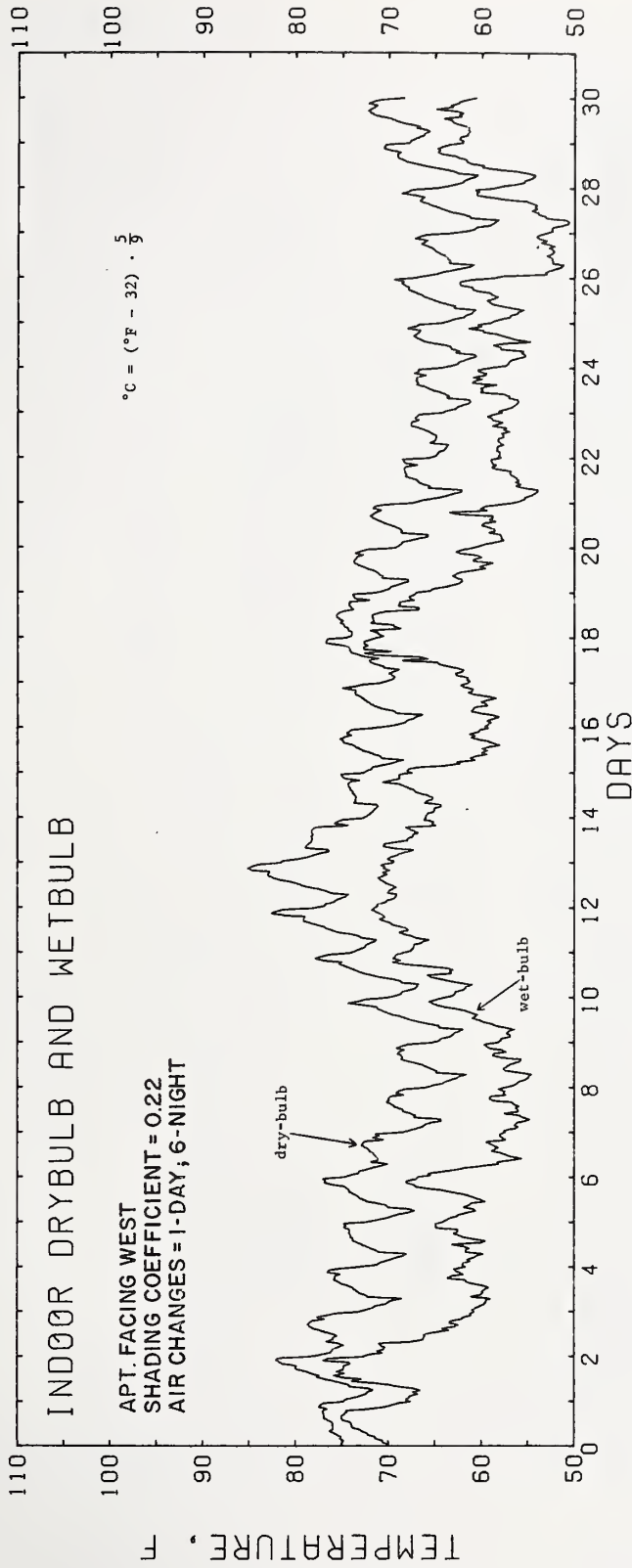
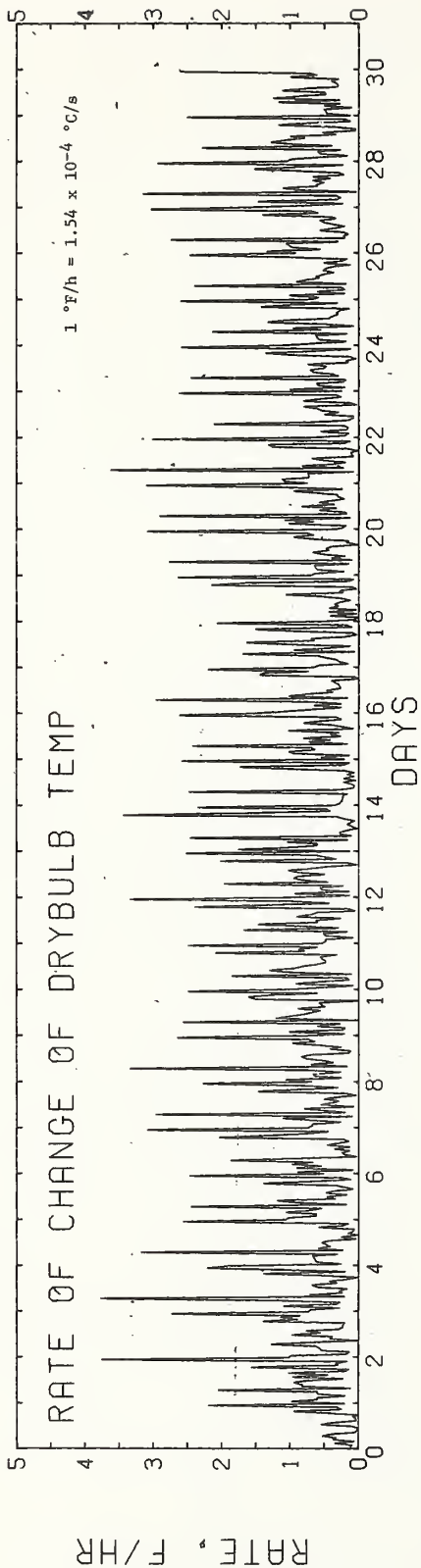


Figure 17 Predicted Hourly Indoor Dry-bulb and Wet-bulb Temperatures for a Heavyweight Apartment in the Month of September, 1952, Jersey City, N. J.

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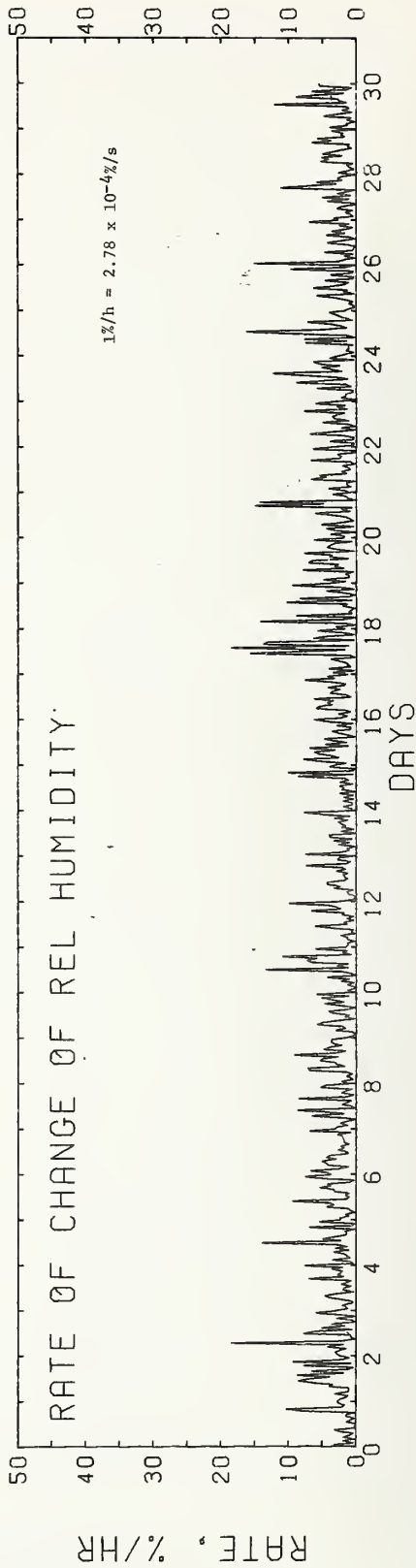
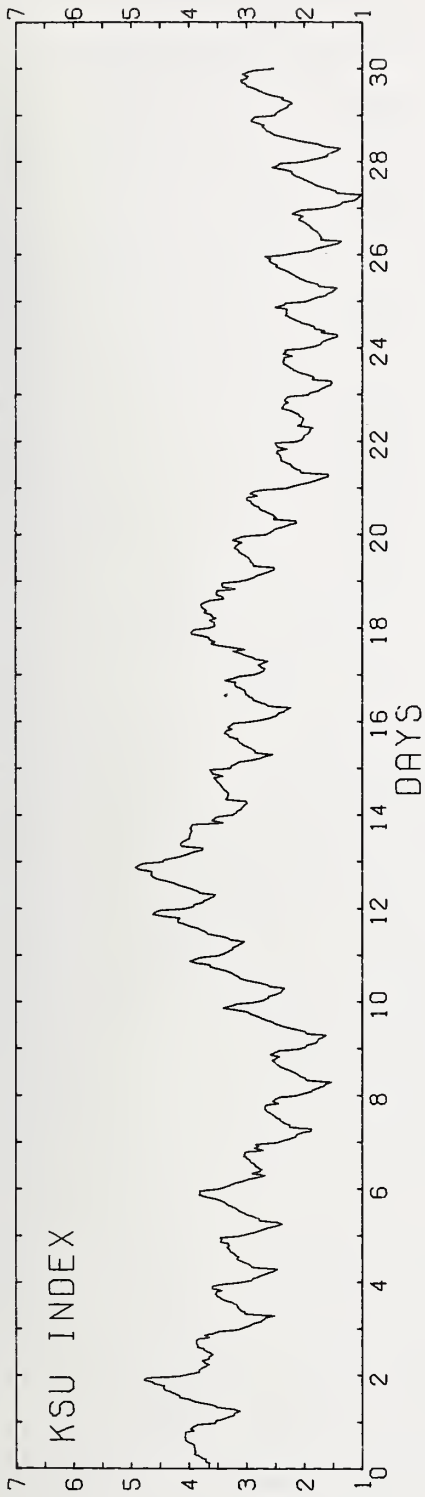


Figure 18 Predicted Hourly Rate of Change of Indoor Dry-bulb Temperature and Relative Humidity for a Heavyweight Apartment in the Month of September, 1952, Jersey City, N. J.

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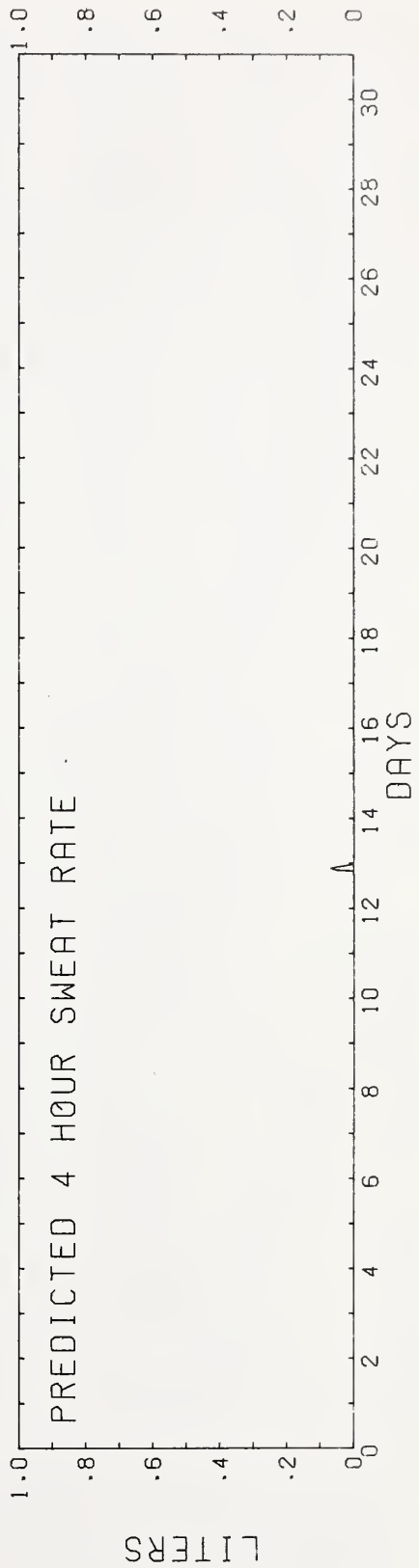
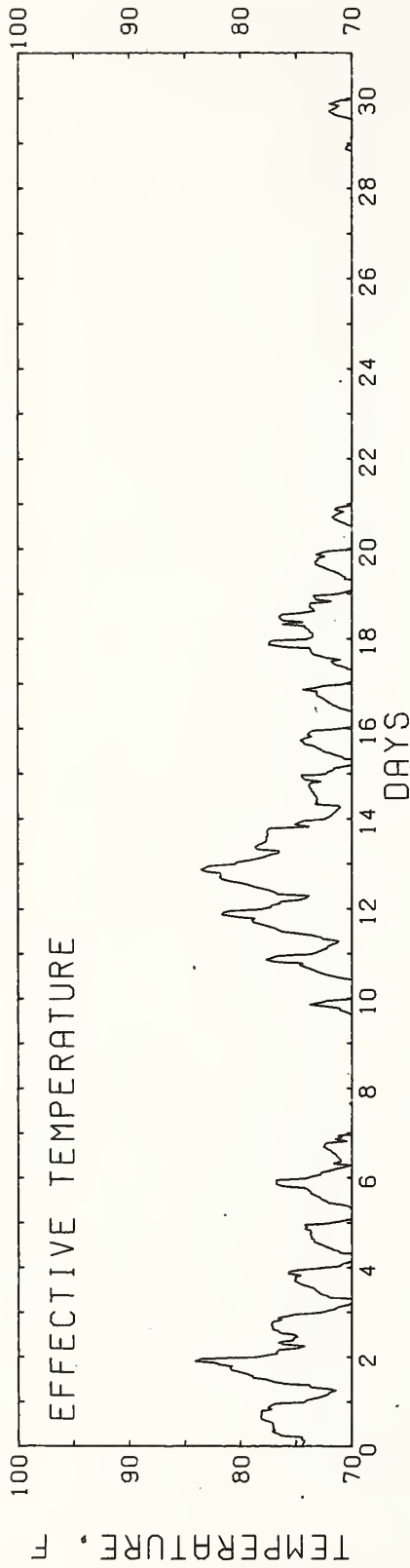


Figure 19 Hourly KSU Index and Predicted Four Hour Sweat Rate for a Heavyweight Apartment in the Month of September, 1952, Jersey City, N. J.

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$$^{\circ}\text{C} = ({}^{\circ}\text{F} - 32) \cdot \frac{5}{9}$$

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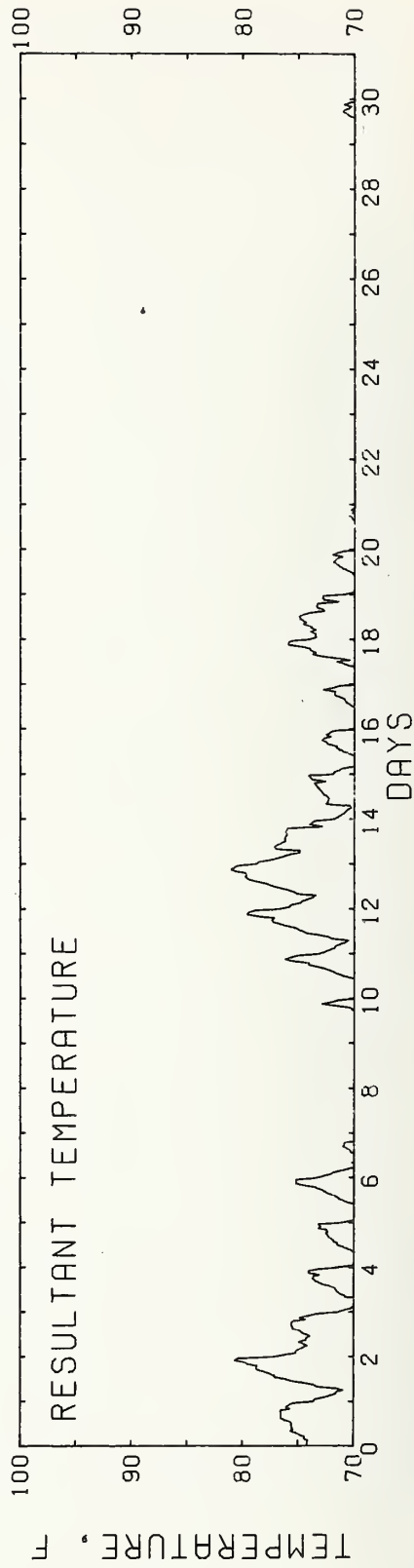
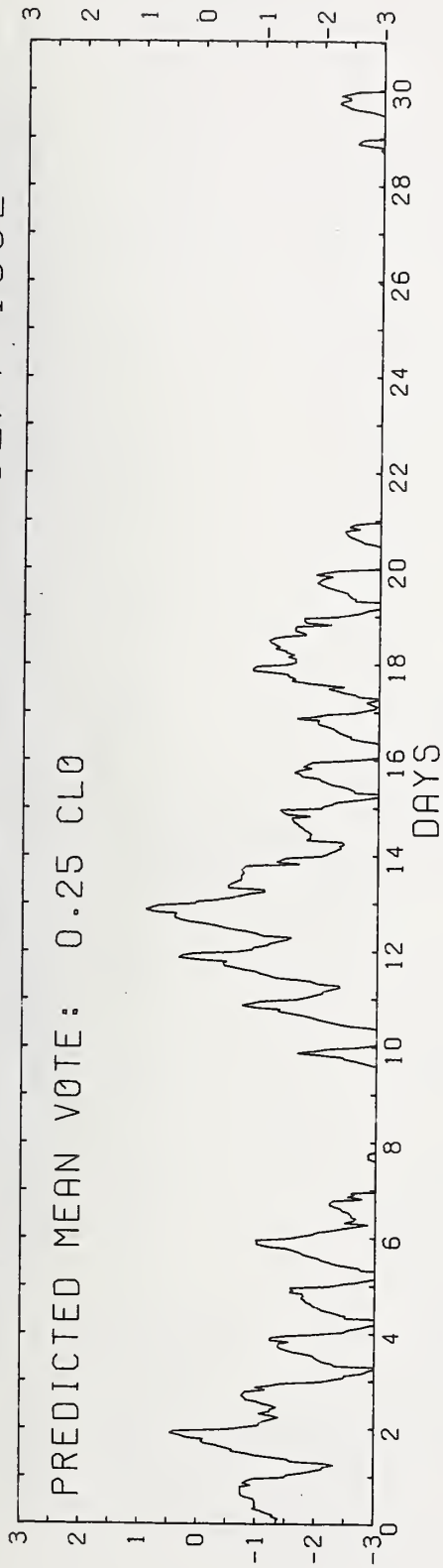


Figure 20 Hourly Effective and Resultant Temperatures for a Heavyweight Apartment in the Month of September, 1952, Jersey City, N. J.



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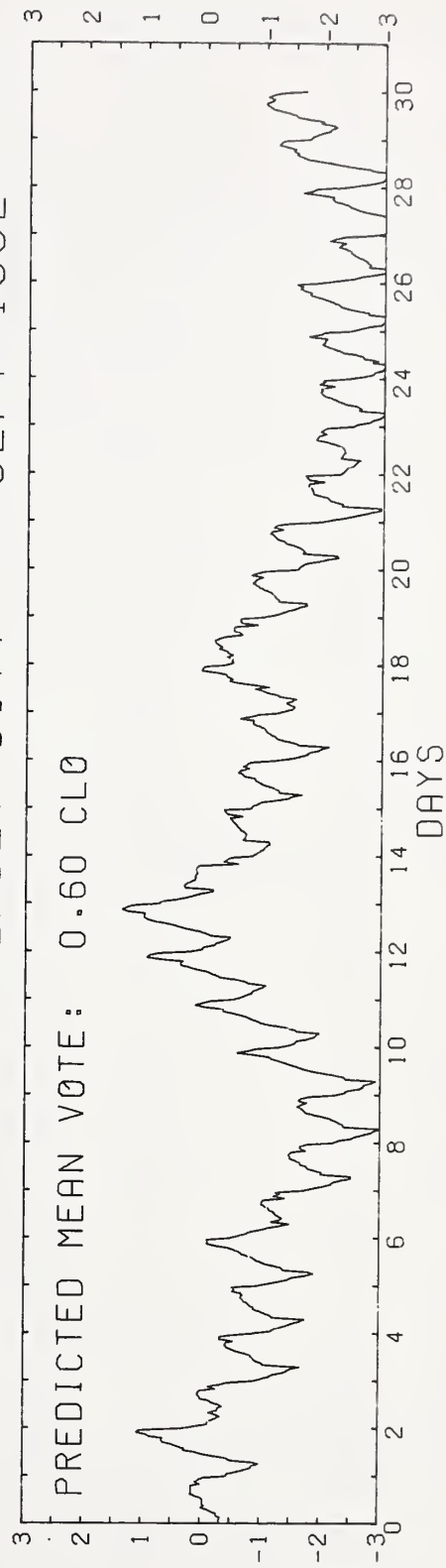
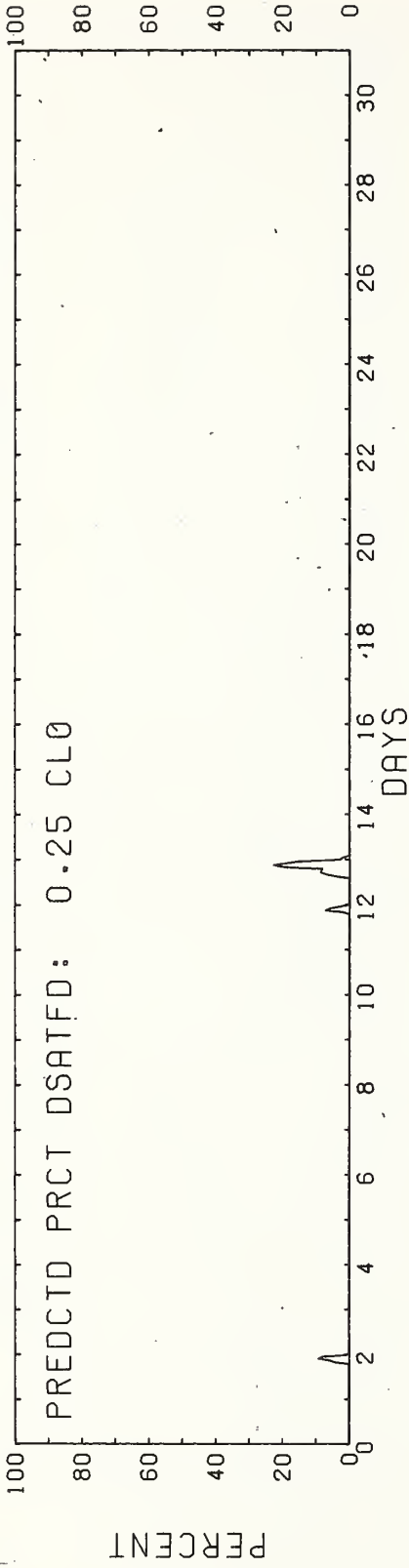


Figure 21 Hourly Predicted Mean Vote (.25 clo and .60 clo) for a Heavyweight Apartment in the Month of September, 1952, Jersey City, N. J.

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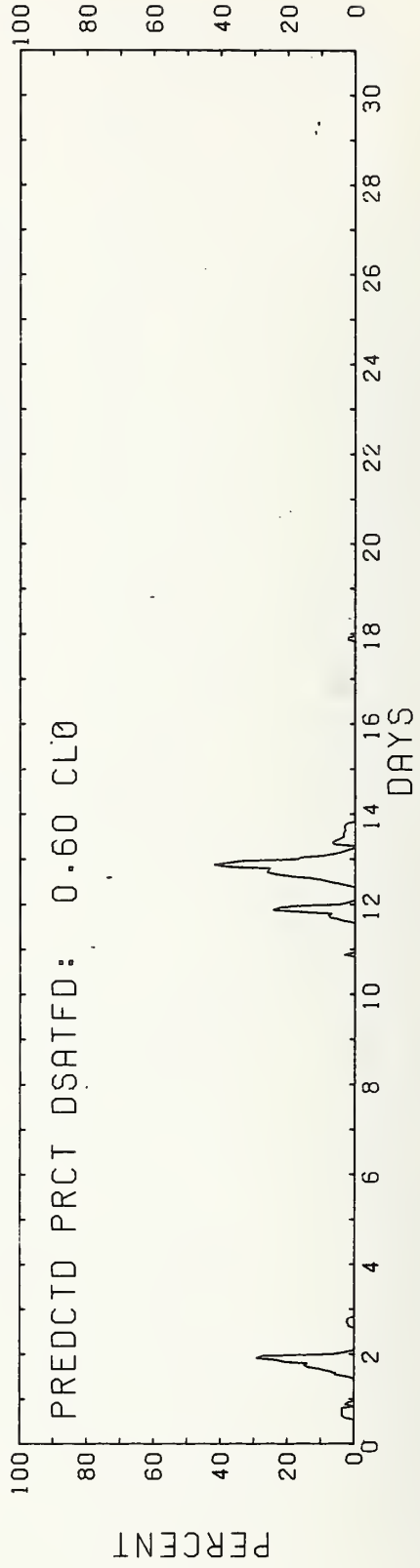
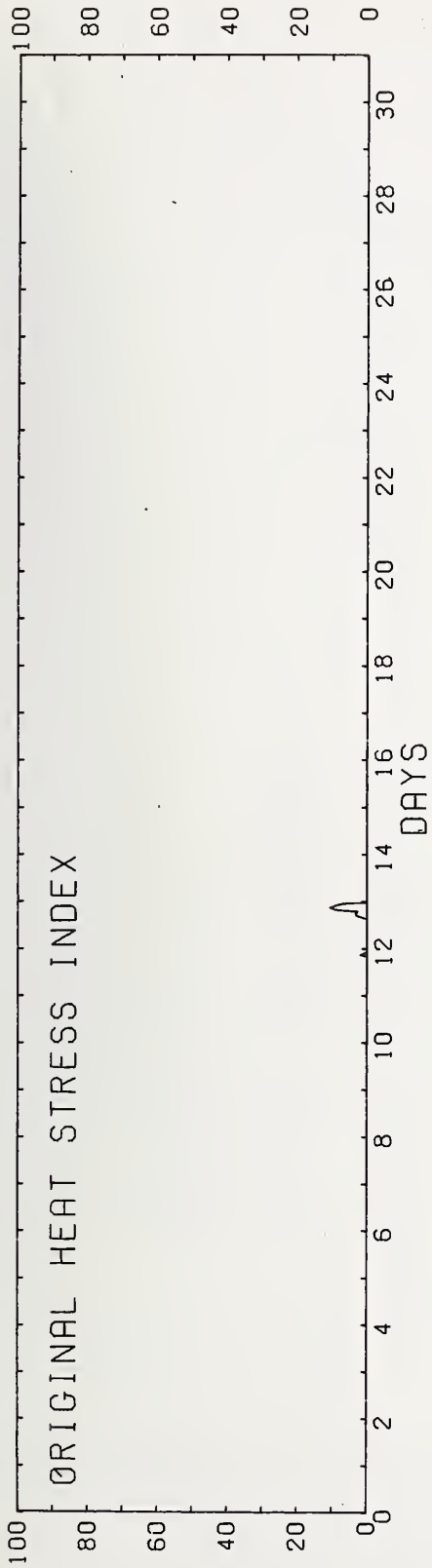


Figure 22 Hourly Predicted Percentage of Dissatisfied (.25 clo and .60 clo) for a Heavyweight Apartment in the Month of September, 1952, Jersey City, N. J.

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APT. FACING WEST SHADING COEFFICIENT=0.22 AIR CHANGES= 1-DAY; 6-NIGHT

APT JERSEY CITY SEPT 1952

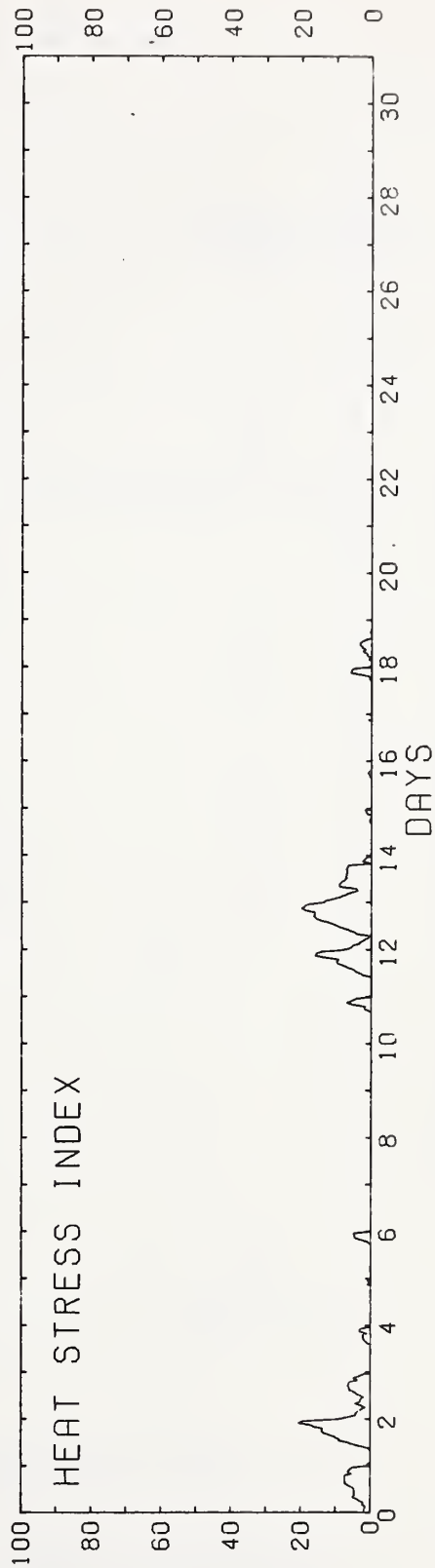
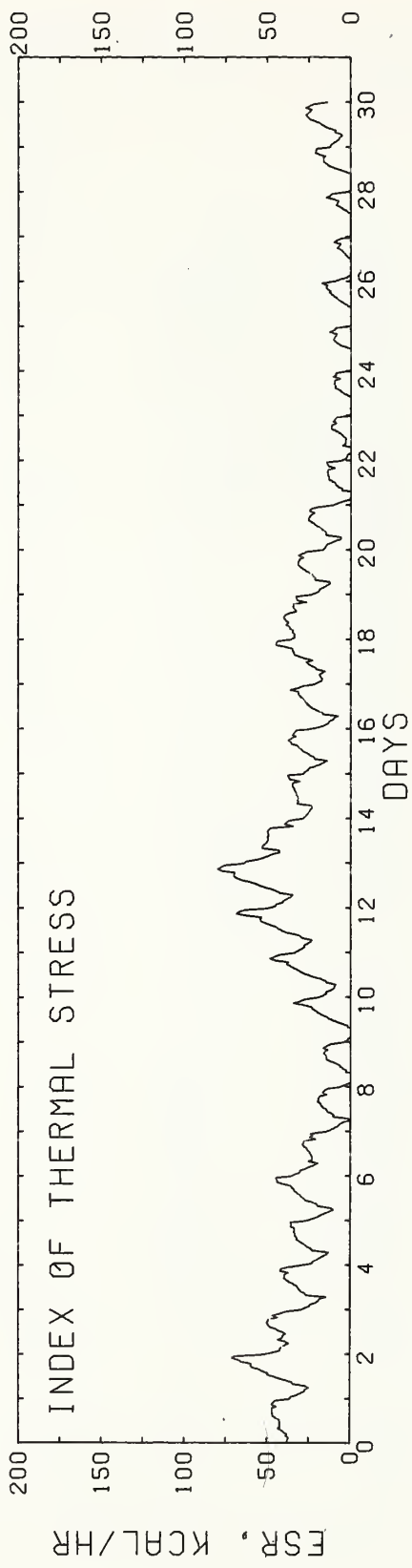


Figure 23 Hourly Original Heat Stress Index and Heat Stress Index for a Heavyweight Apartment in the Month of September, 1952, Jersey City, N. J.

APT JERSEY CITY SEPT 1952



APT. FACING WEST SHADING COEFFICIENT=0.22 AIR CHANGES=1-DAY; 6-NIGHT

Figure 24 Hourly Index of Thermal Stress for a Heavyweight Apartment in the Month of September, 1952, Jersey City, N. J.



AUG. 1953 ( 14% )  
 JERSEY CITY

NUMBER OF TIMES ABOVE 85 ET\* ( INSIDE )

1 2 3 4 5 6 7 8 9 10 11 12 18 24 48

HOURS AT A TIME ABOVE 85 ET\* ( INSIDE )

Figure 25 Number of Times vs Hours at a Time Above 85 ET\* (Inside) in the Month of August, 1953 for a Heavyweight Apartment, Jersey City, N. J.

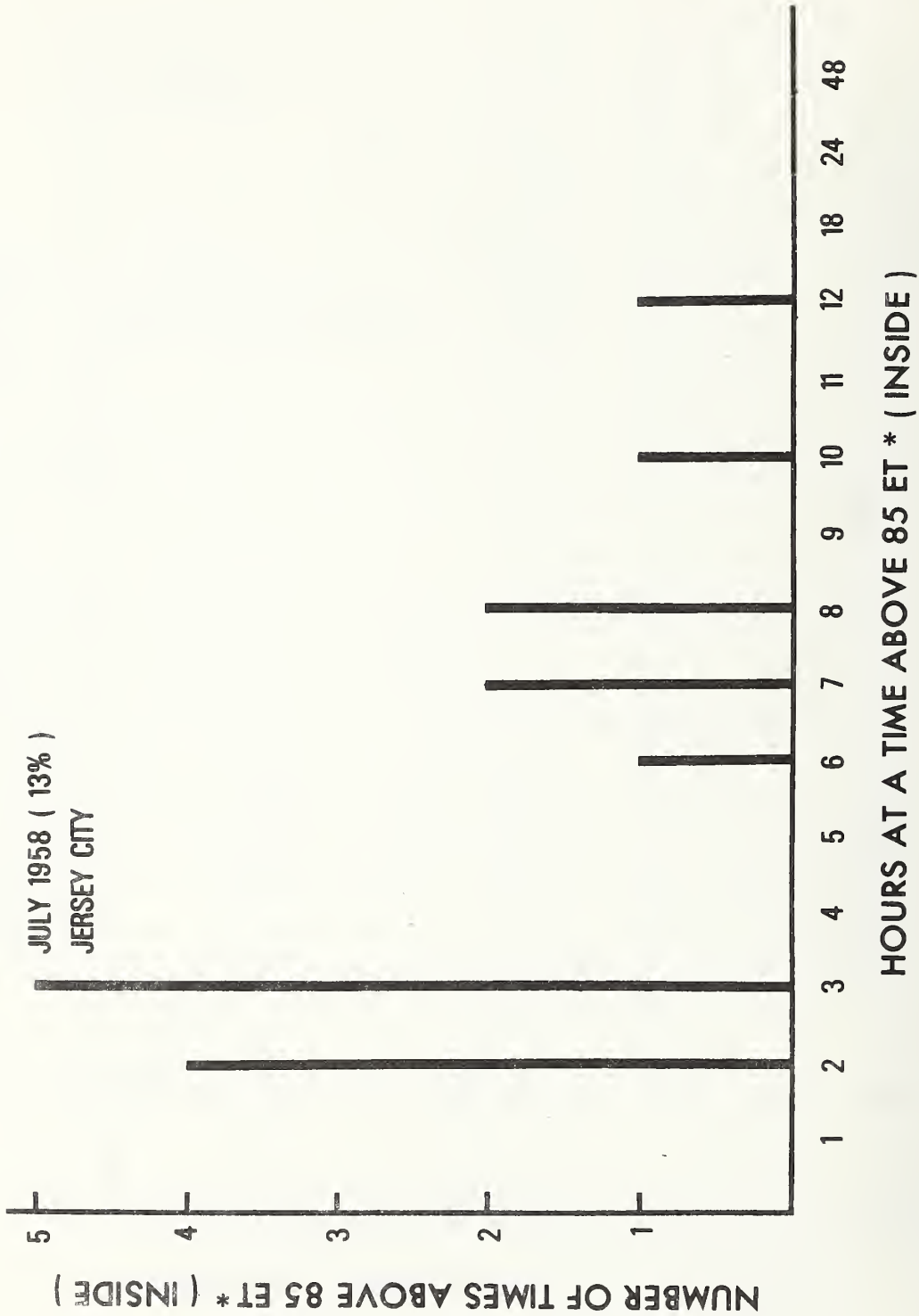
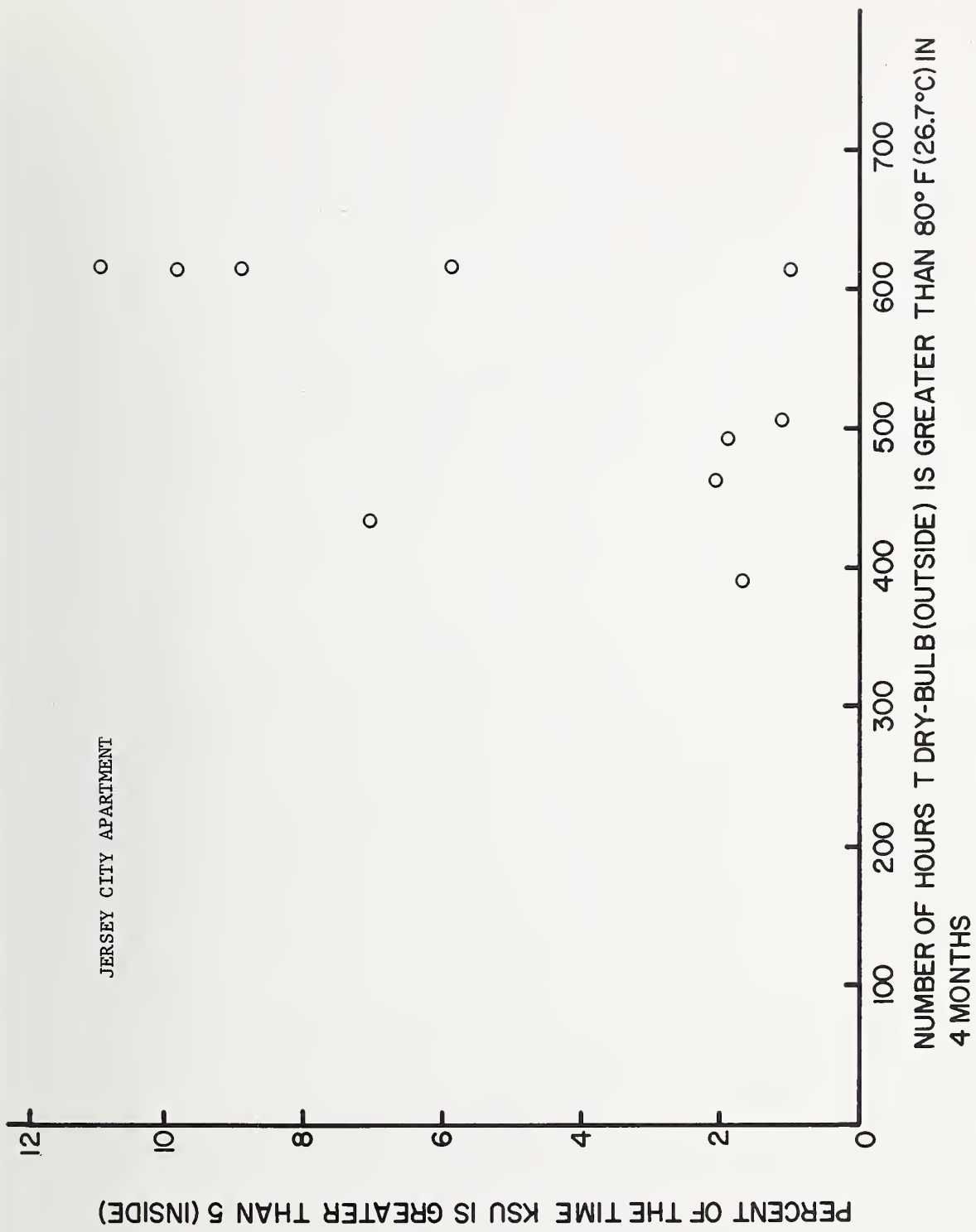


Figure 26 Number of Times vs Hours at a Time Above 85 ET\* (Inside) in the Month of July, 1953 for a Heavyweight Apartment in 4 Months, Jersey City, N.J.

JERSEY CITY APARTMENT



NUMBER OF HOURS T DRY-BULB (OUTSIDE) IS GREATER THAN 80°F (26.7°C) IN 4 MONTHS

Figure 27 Percent Time KSU Greater Than 5 (Inside) vs Number of Hours Each Year for 10 Years T<sub>dry-bulb</sub> (Outside) Greater Than 80 °F (26.7 °C) for a Heavyweight Apartment in 4 Months, Jersey City, N.J.

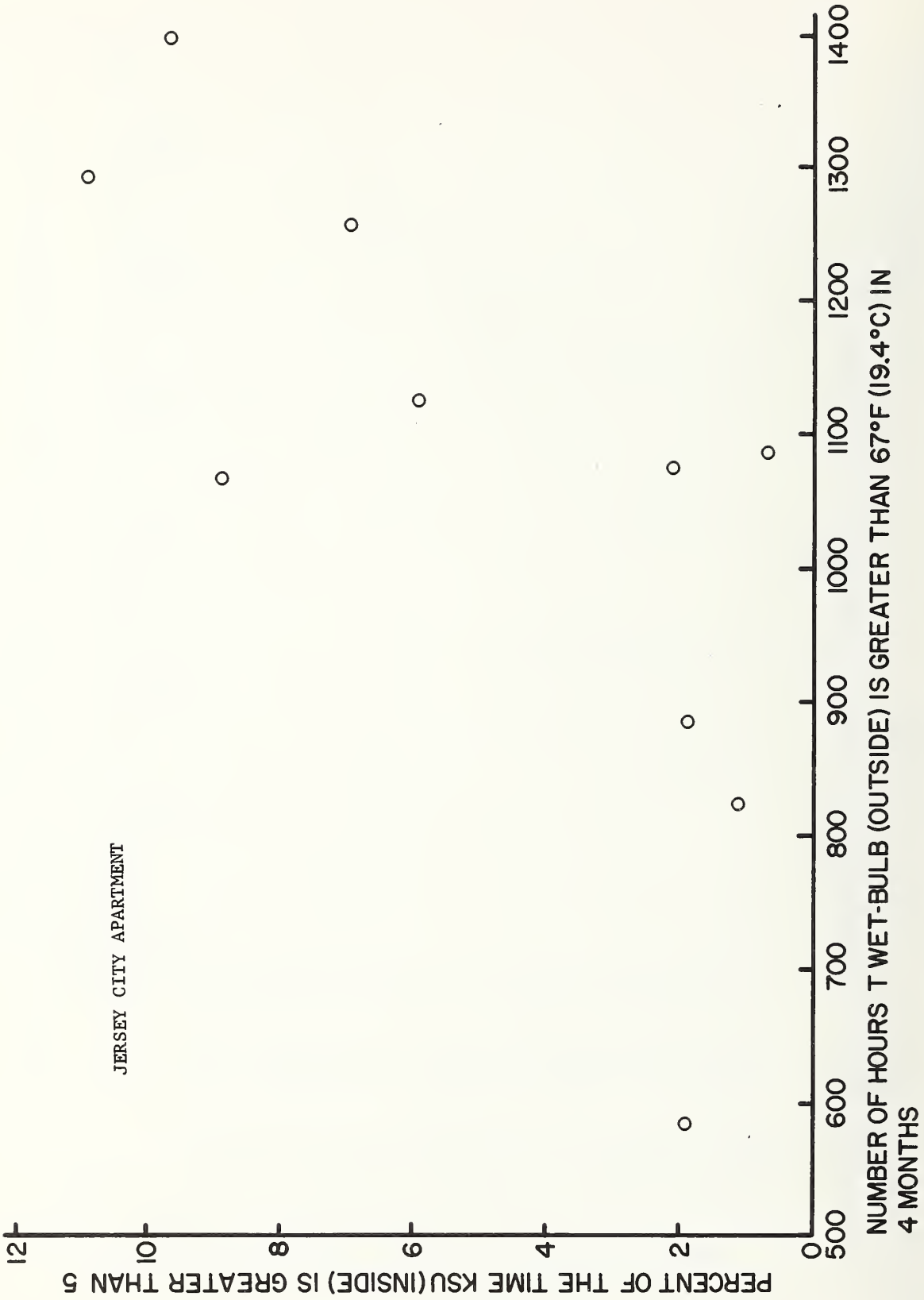


Figure 28 Percent Time KSU (Inside) Greater Than 5 vs Number of Hours Each Year for 10 Years T<sub>wet-bulb</sub> (Outside) Greater Than 67 °F (19.4 °C) for a Heavyweight Apartment in 4 Months, Jersey City, N.J.

JERSEY CITY APARTMENT

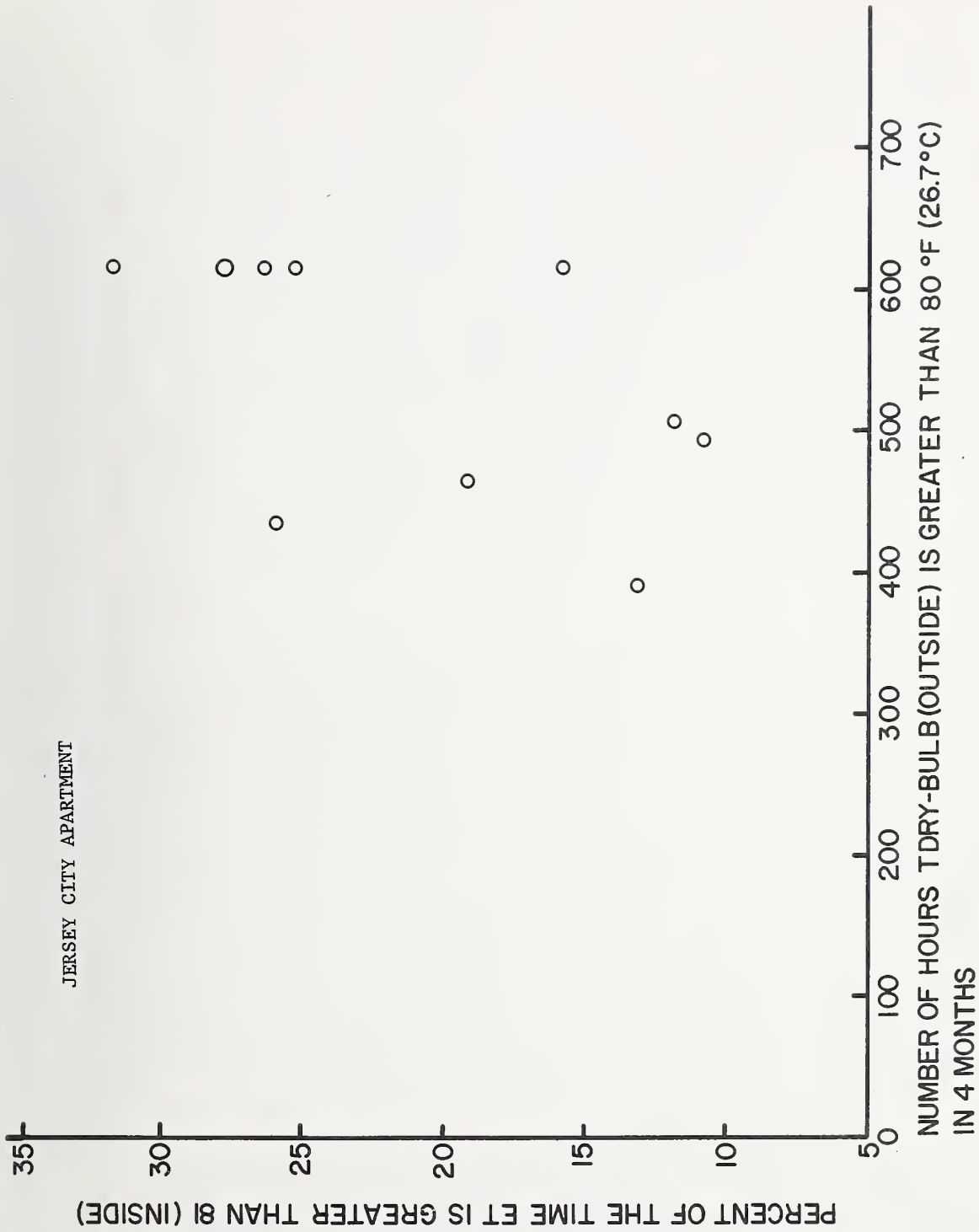
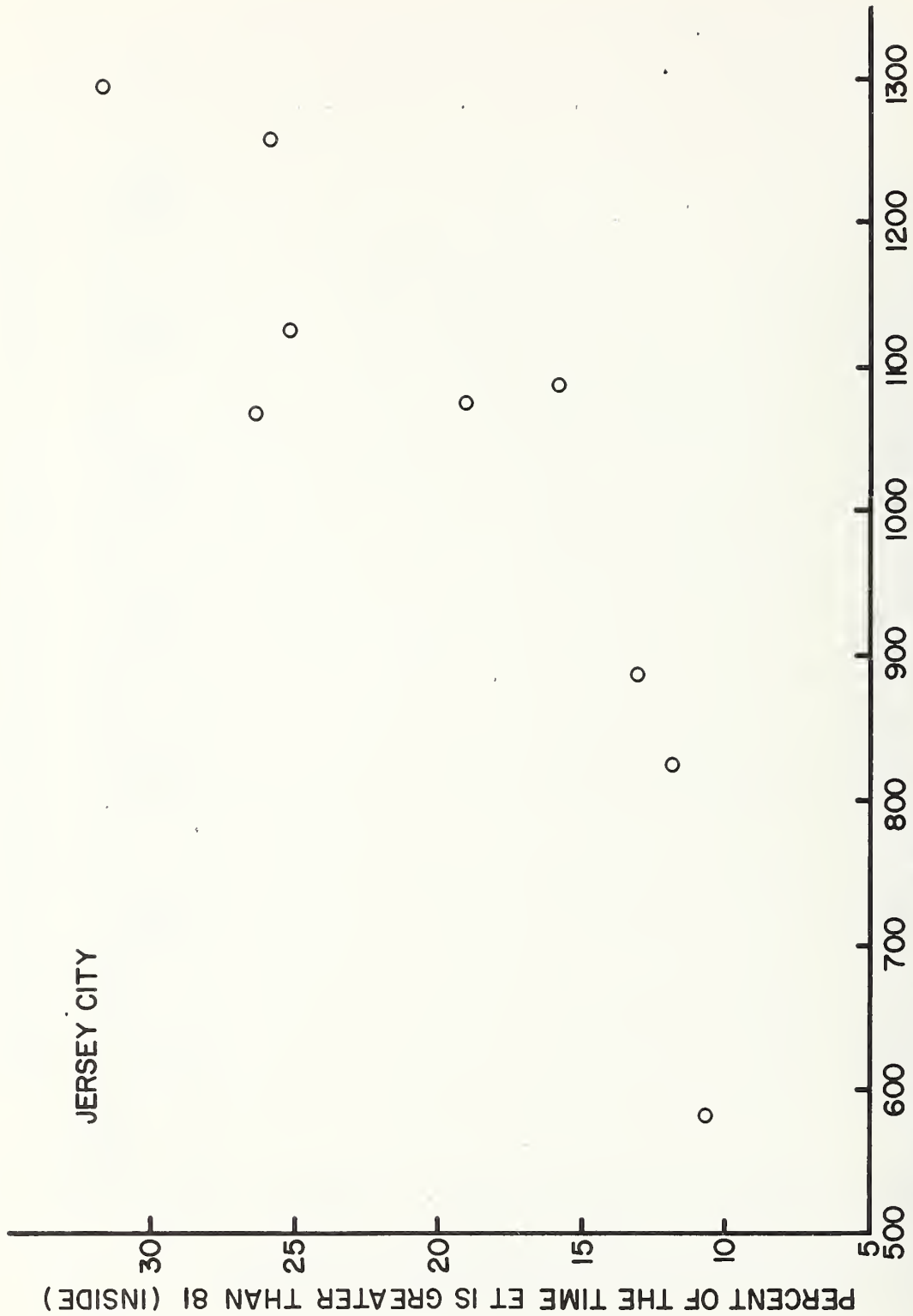


Figure 29 Percent Time ET\* (Inside) Greater Than 81 vs Number of Hours Each Year for 10 Years Tdry-bulb (Outside) Greater Than 80 °F (26.7 °C) for a Heavyweight Apartment in 4 Months, Jersey City, N.J.





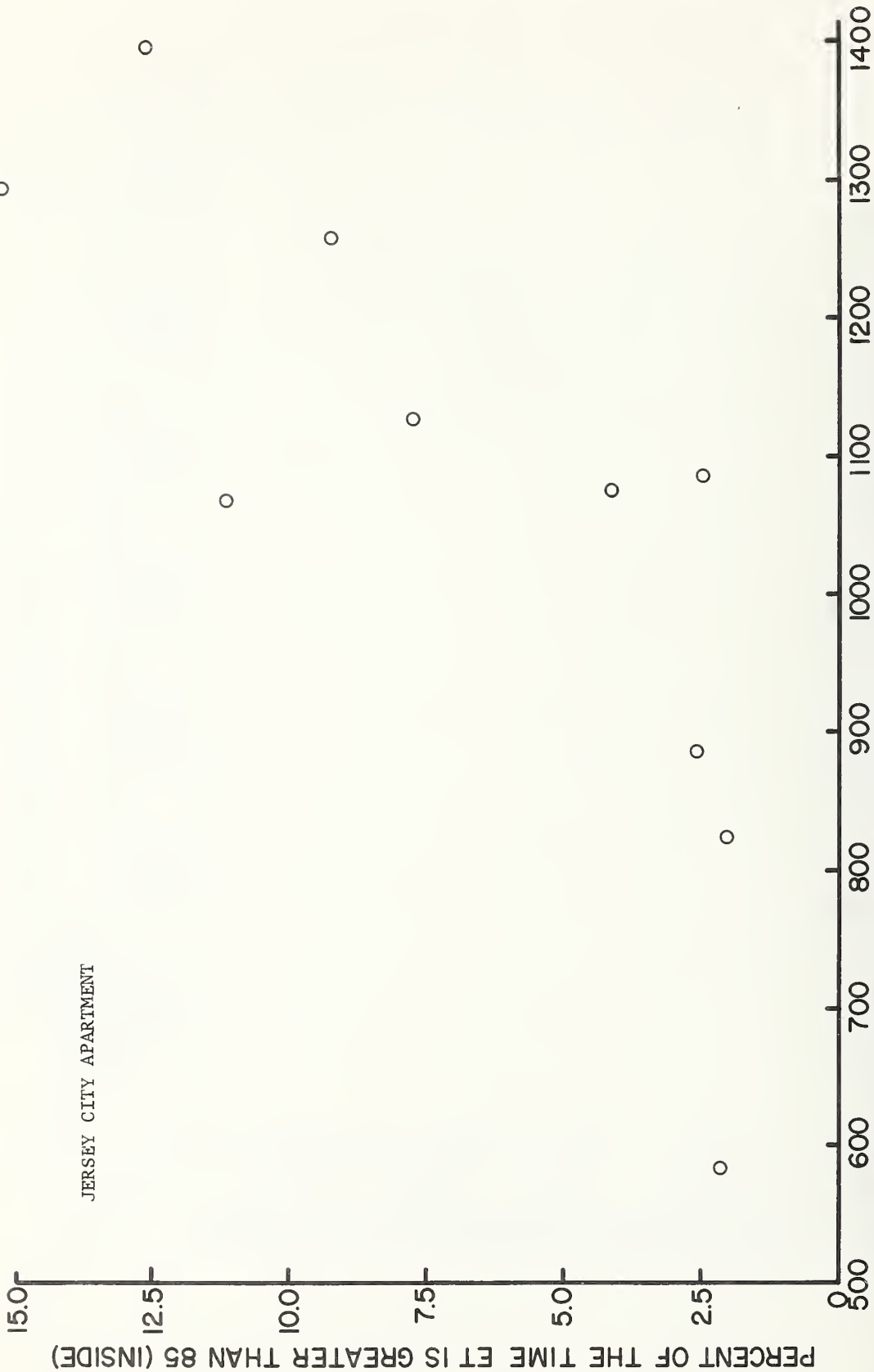
**NUMBER OF HOURS T WET-BULB (OUTSIDE) IS GREATER THAN 67°F (19.4°C)  
IN 4 MONTHS**

Figure 30 Percent Time ET\* (Inside) Greater Than 81 vs Number of Hours Each Year for 10 Years T<sub>wet-bulb</sub> (Outside) Greater Than 67 °F (19.4 °C) for a Heavyweight Apartment in 4 Months, Jersey City, N.J.



NUMBER OF HOURS T DRY-BULB (OUTSIDE) IS GREATER THAN 80°F (26.7°C) IN 4 MONTHS

Figure 31 Percent Time ET\* (Inside) Greater Than 85 vs Number of Hours Each Year for 10 Years T<sub>dry bulb</sub> (Outside) Greater Than 80 °F (26.7 °C) for a Heavyweight Apartment in 4 Months, Jersey City, N.J.



**NUMBER OF HOURS T WET-BULB (OUTSIDE) IS GREATER THAN 67°F (19.4°C) IN 4 MONTHS**

Figure 32 Percent Time ET\* (Inside) Greater Than 85 vs Number of Hours Each Year for 10 Years T<sub>wet-bulb</sub> (Outside) Greater Than 67 °F (19.4 °C) for a Heavyweight Apartment in 4 Months, Jersey City, N.J.

# AUGUST 1954 - JERSEY CITY

$$^{\circ}\text{C} = (^{\circ}\text{F} - 32) \cdot \frac{5}{9}$$

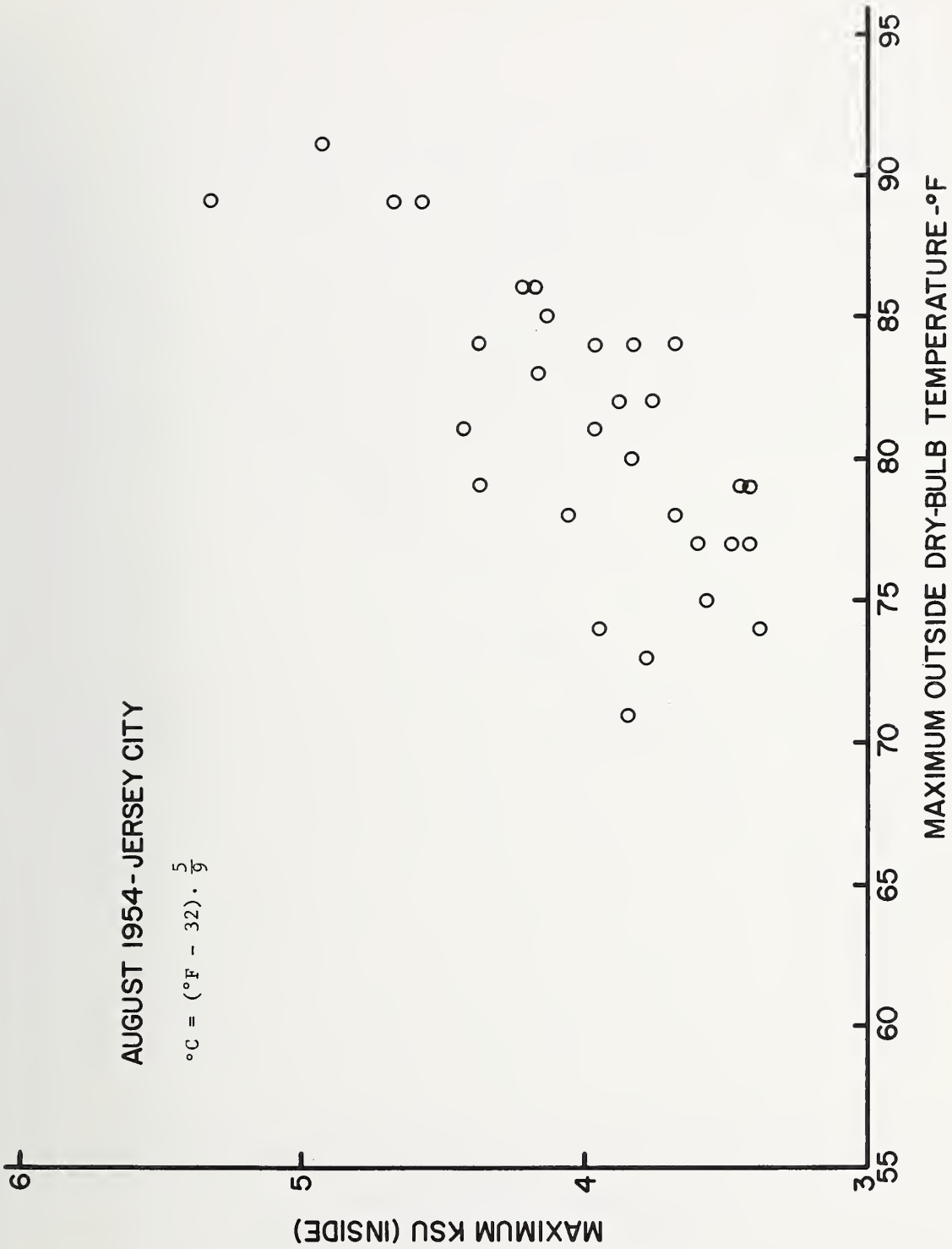


Figure 33 Daily Maximum KSU (Inside) vs Daily Maximum T<sub>dry-bulb</sub> (Outside) for a Heavyweight Apartment, August, 1954, Jersey City, N.J.

# AUGUST 1954 - JERSEY CITY

$$^{\circ}\text{C} = (^{\circ}\text{F} - 32) \cdot \frac{5}{9}$$

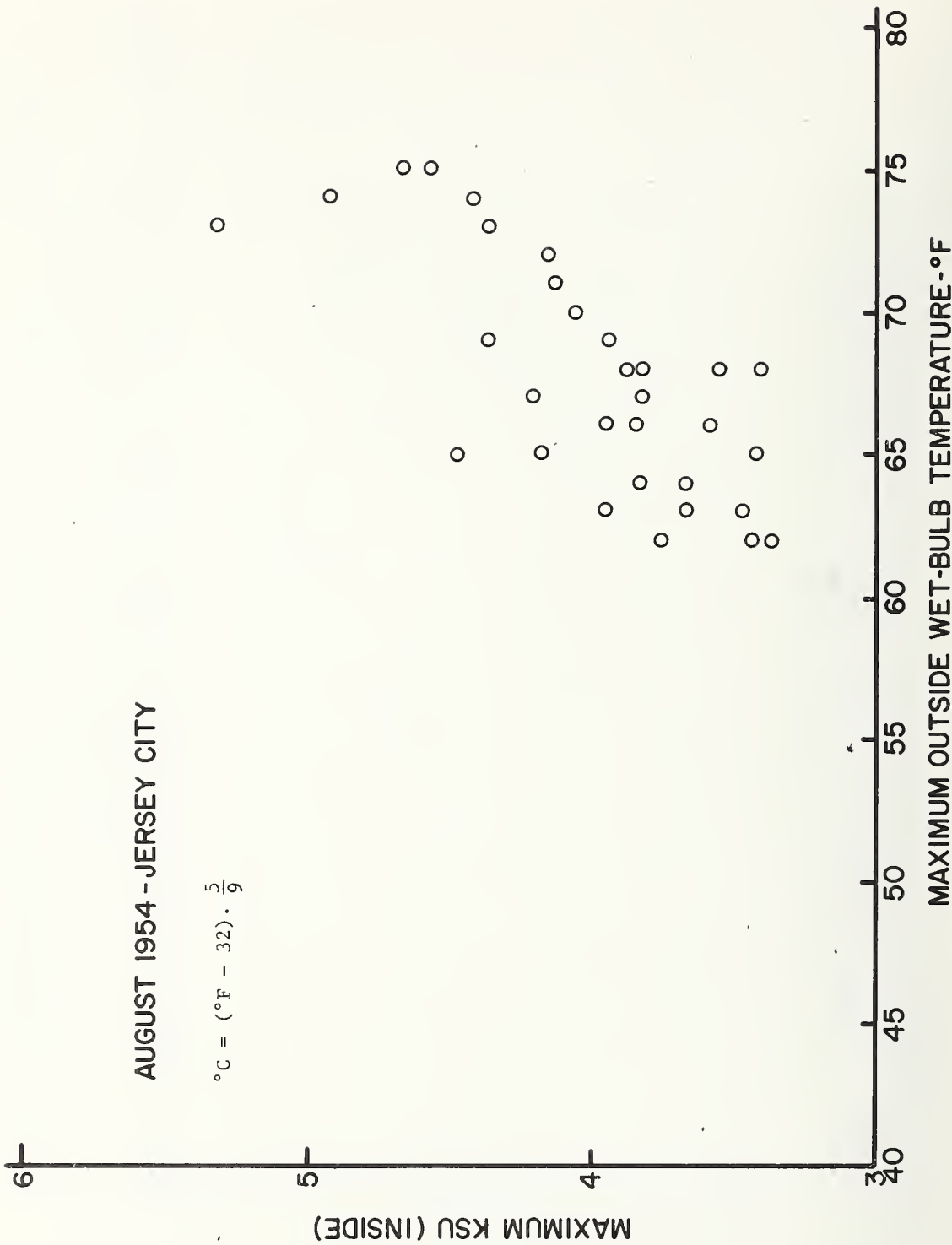
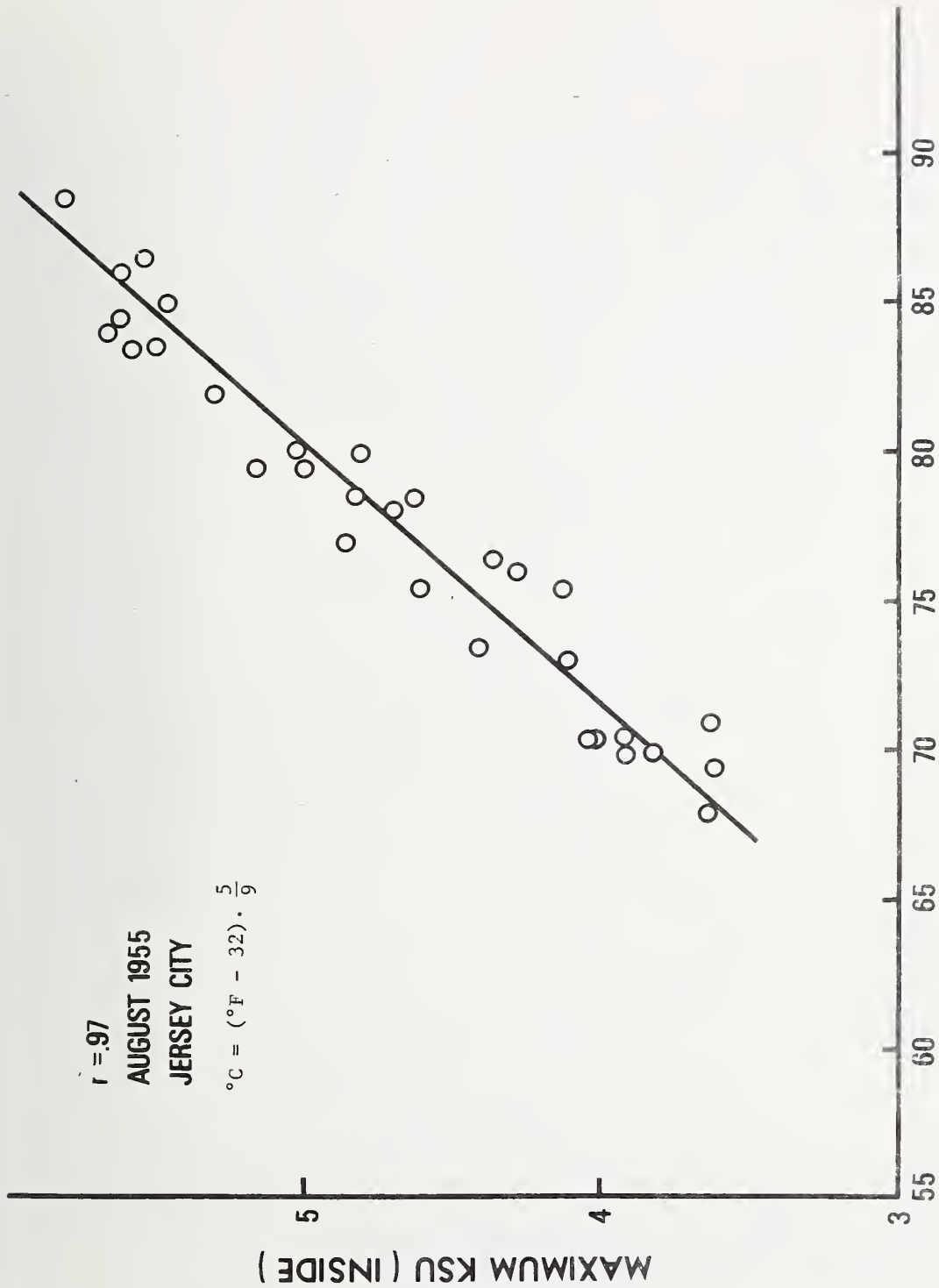


Figure 34 Daily Maximum KSU (Inside) vs Daily Maximum T<sub>wet-bulb</sub> (Outside) for a Heavyweight Apartment, August, 1954, Jersey City, N.J.





**AVERAGE OUTSIDE DRY-BULB TEMPERATURE-°F**

Figure 35 Daily Maximum KSU (Inside) vs Daily Average  $T_{\text{dry-bulb}}$  (Outside) for a Heavyweight Apartment, August, 1955, Jersey City, N.J.

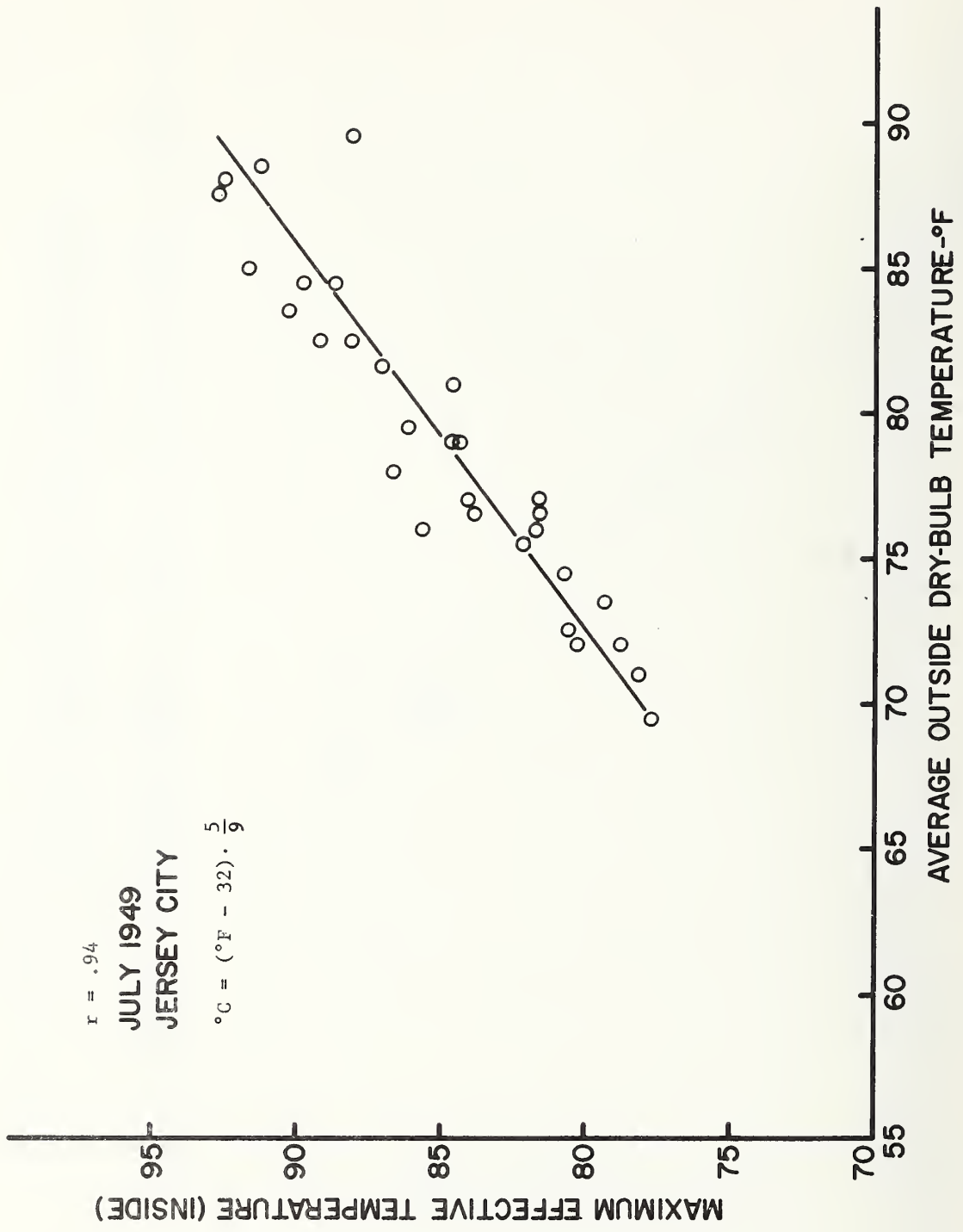


Figure 36 Daily Maximum ET\* (Inside) vs Daily Average T<sub>dry-bulb</sub> (Outside) for a Heavyweight Apartment, July, 1949, Jersey City, N.J.

JULY 1949 JERSEY CITY

$$^{\circ}\text{C} = (^{\circ}\text{F} - 32) \cdot \frac{5}{9}$$

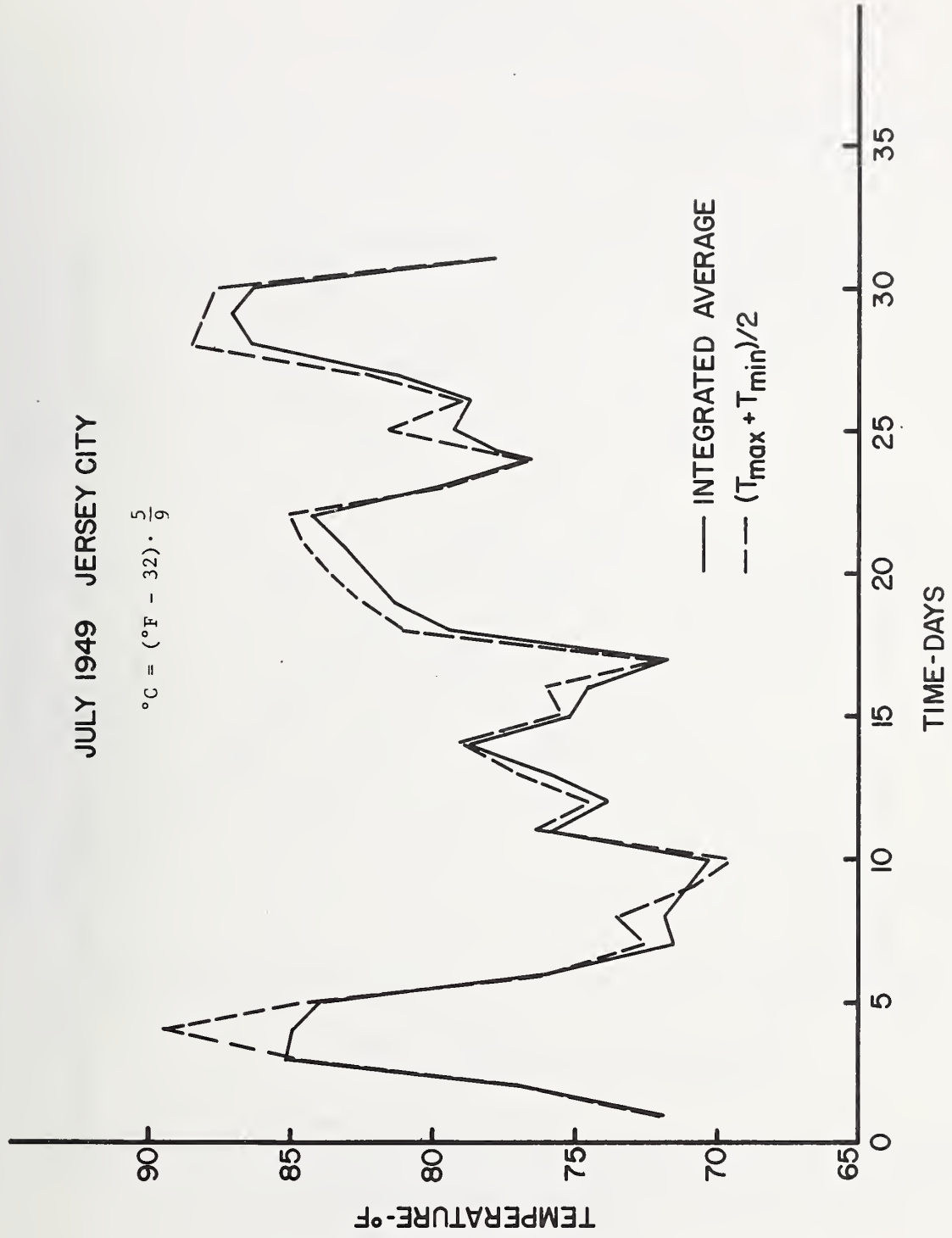


Figure 37 Comparison of Daily Average Temperatures

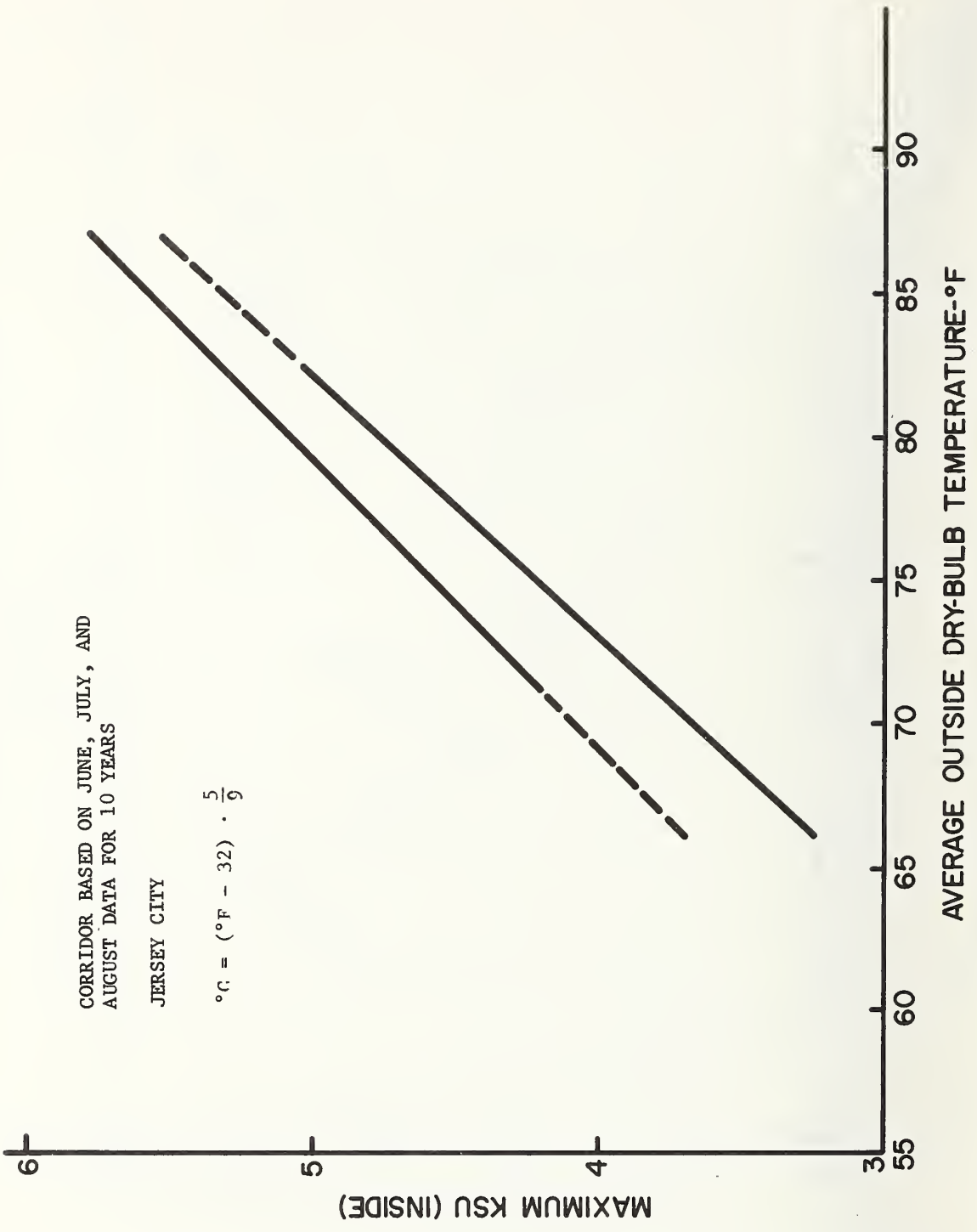


Figure 38 10 Year (June, July, August) Corridor, Jersey City, N.J.

Heavyweight Apartment  
 Jersey City; June 28, 1949  
 1 Air Change Per Hour, Constant

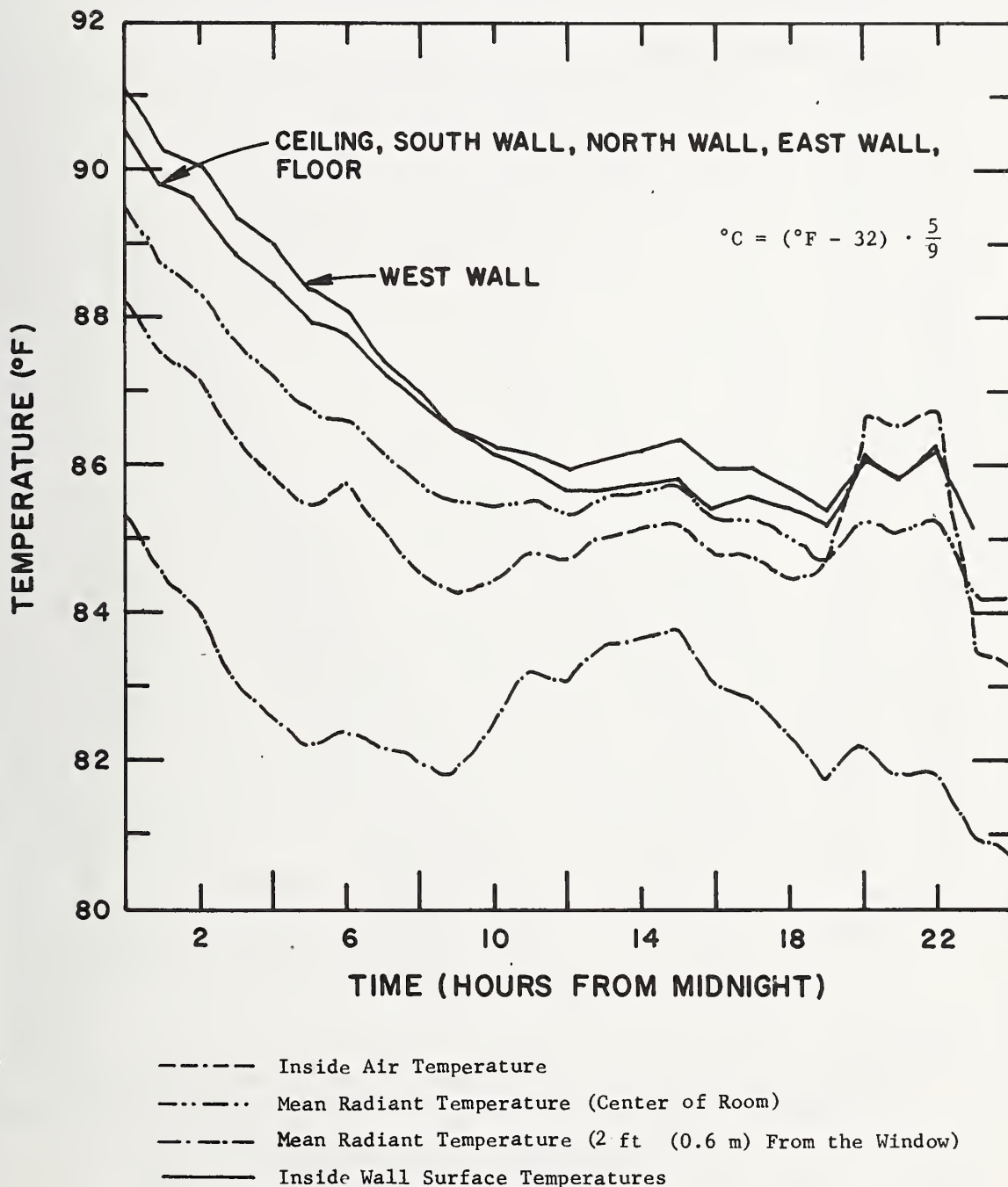


Figure 39A. Comparison of Mean Radiant Temperature Calculation Results for a Heavyweight Apartment, June 28, 1949, Jersey City, N.J.



Heavyweight Apartment  
Jersey City; June 28, 1949  
1 Air Change Per Hour, Constant

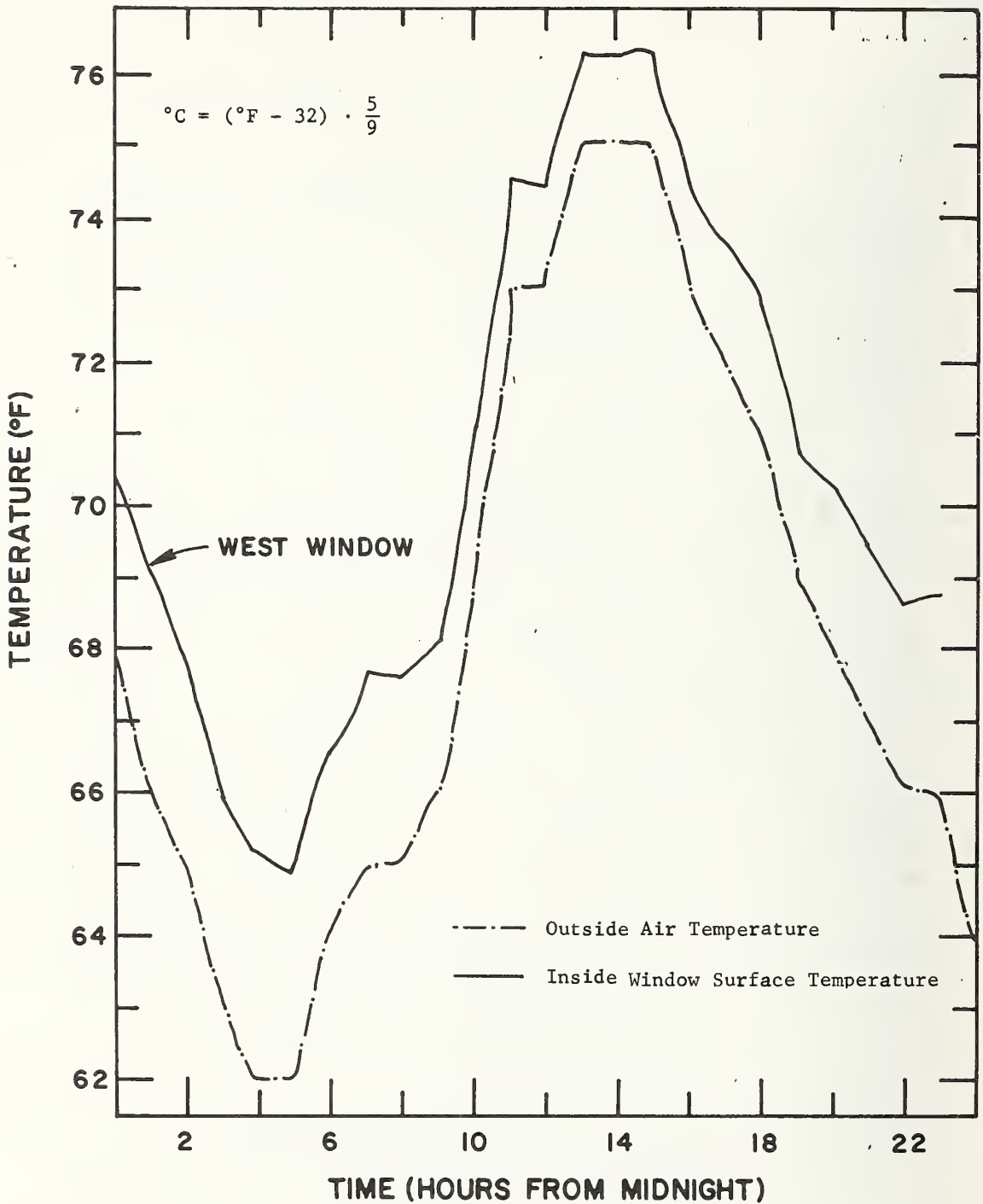


Figure 39B Comparison of Mean Radiant Temperature Calculation Results for a Heavyweight Apartment, June 28, 1949, Jersey City, N.J.:

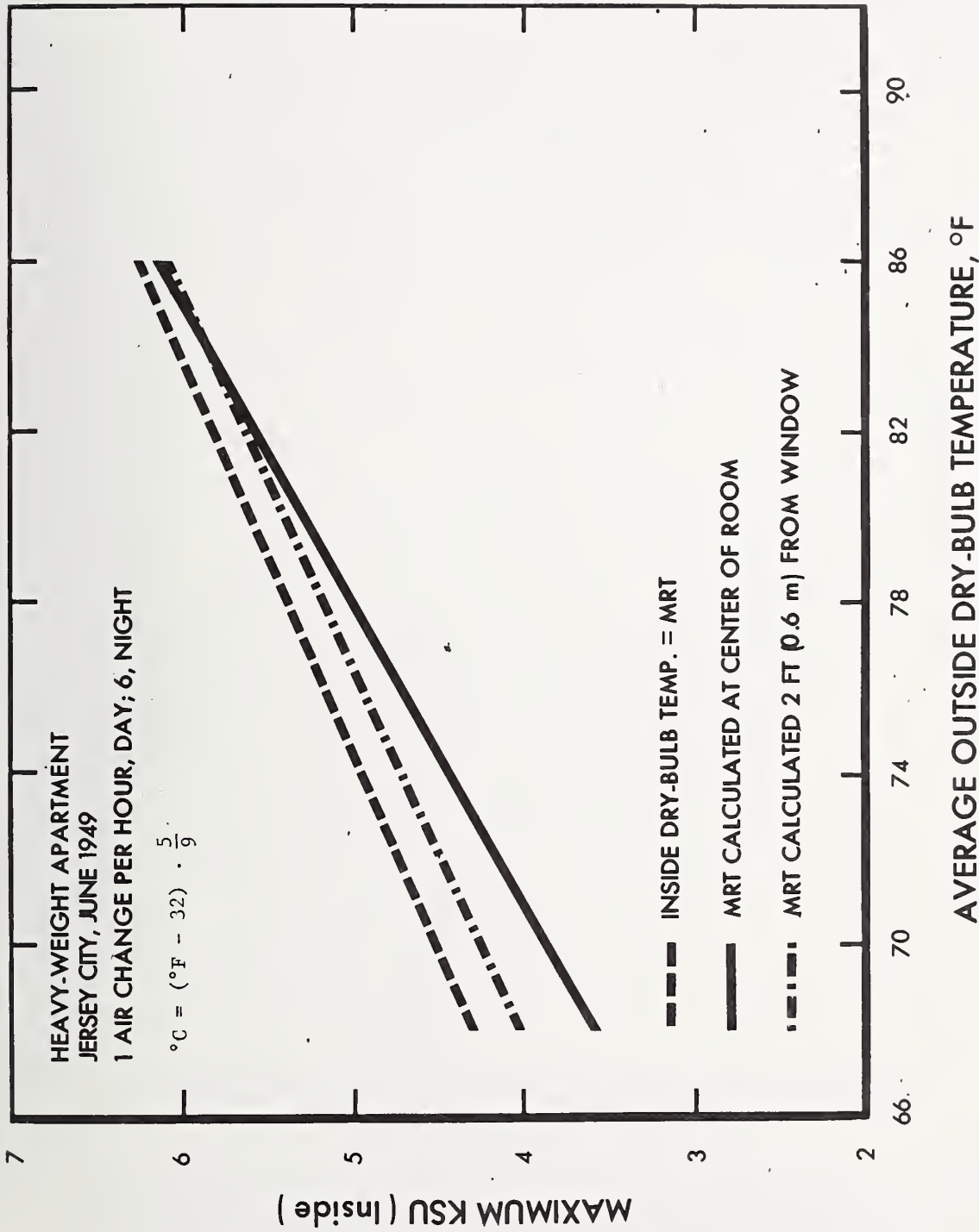


Figure 40 Comparison of Correlation Lines With Different Calculations of Mean Radiant Temperature for a Heavyweight Apartment, Jersey City, N.J.

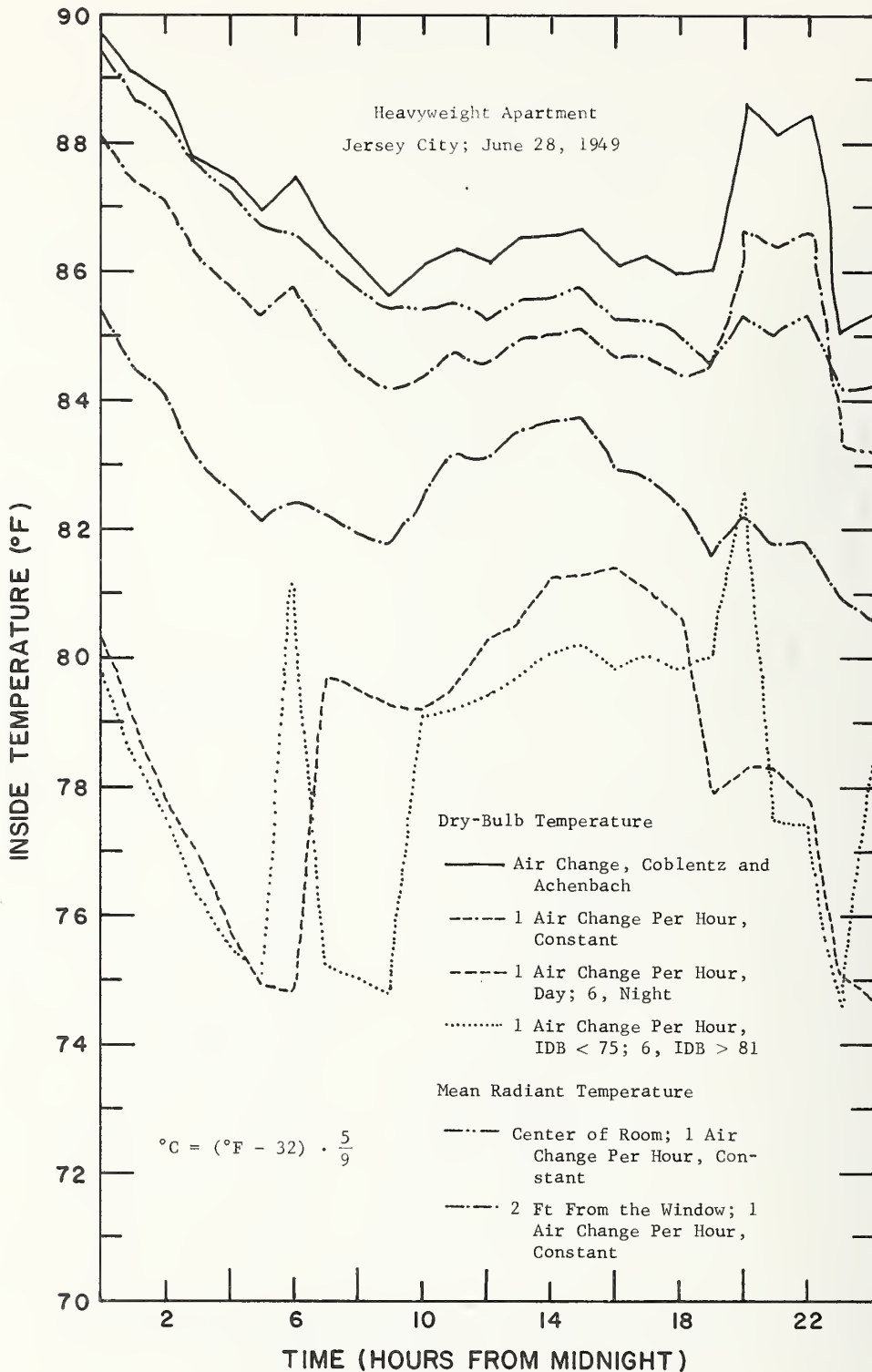


Figure 41 Comparison of Indoor Dry-bulb Temperature Profiles With Different Air Infiltration Assumptions for a Heavyweight Apartment, June 28, 1949, Jersey City, N.J.

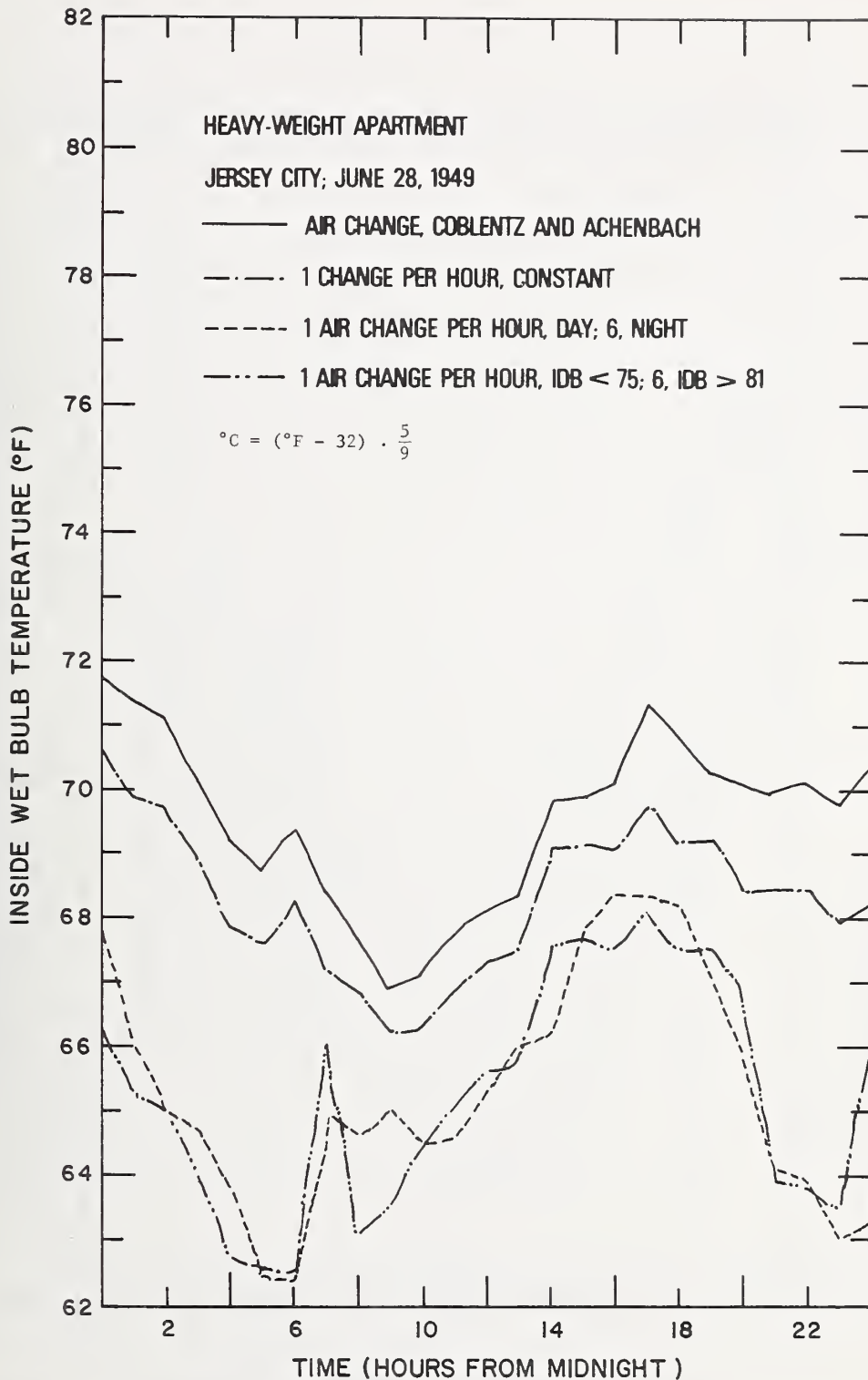


Figure 42 Comparison of Indoor Wet-Bulb Temperature Profiles With Different Air Infiltration Assumptions for a Heavyweight Apartment, June 28, 1949, Jersey City, N.J.

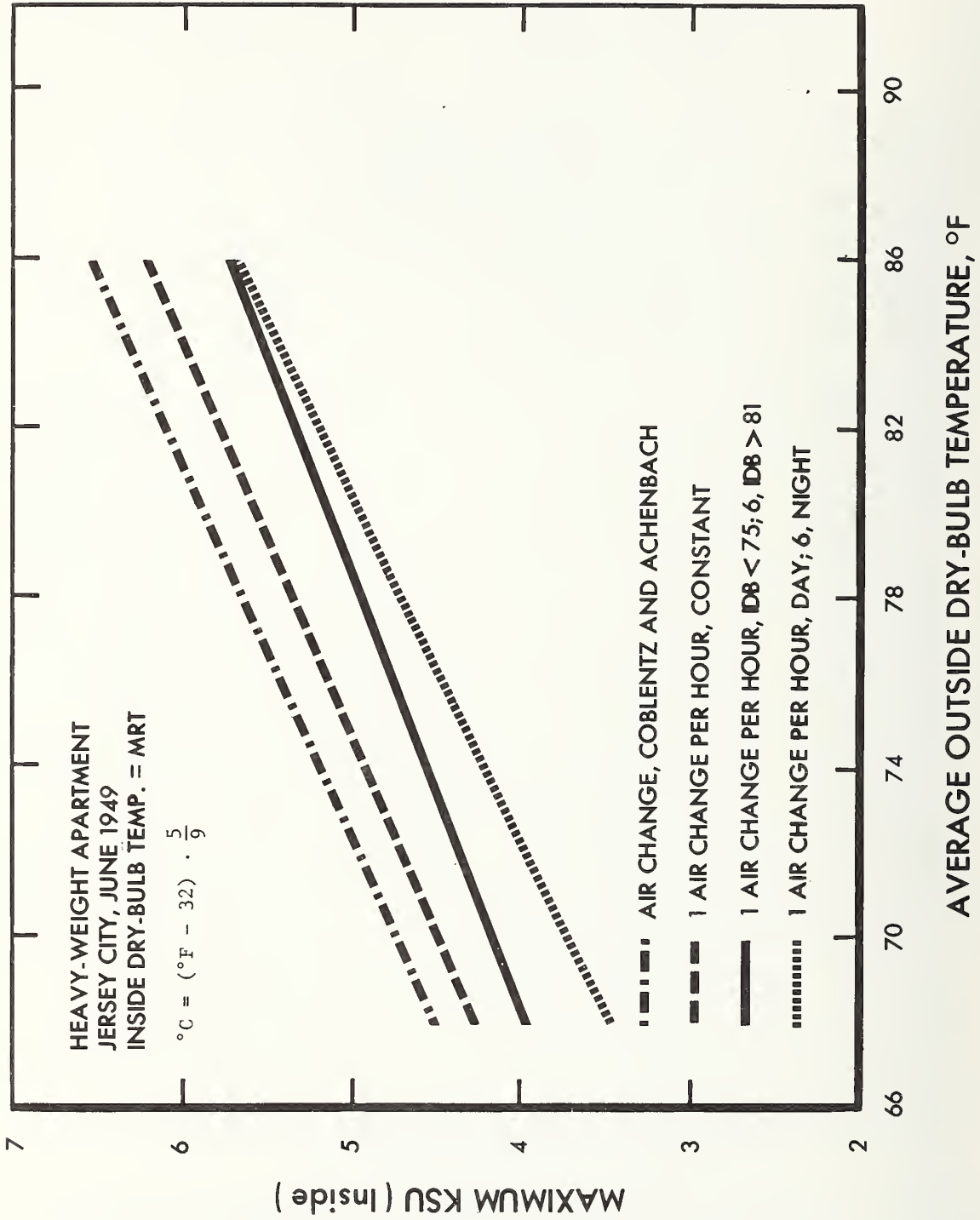


Figure 43 Comparison of Correlation Lines With Different Air Infiltration Assumptions for a Heavyweight Apartment, Jersey City, N.J.



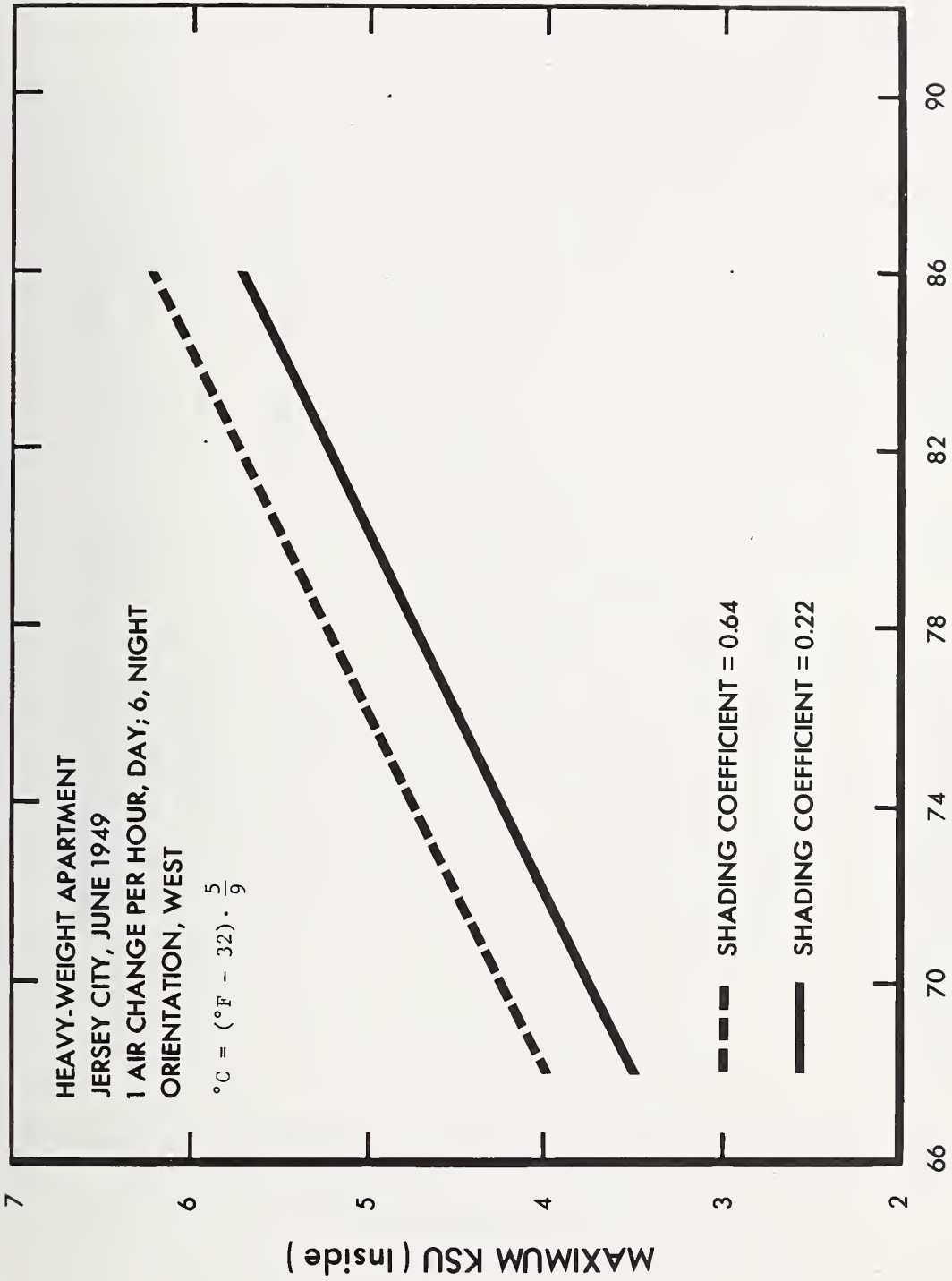


Figure 44 Comparison of Correlation Lines With Different Window Characteristics for a Heavyweight Apartment, Jersey City, N.J.

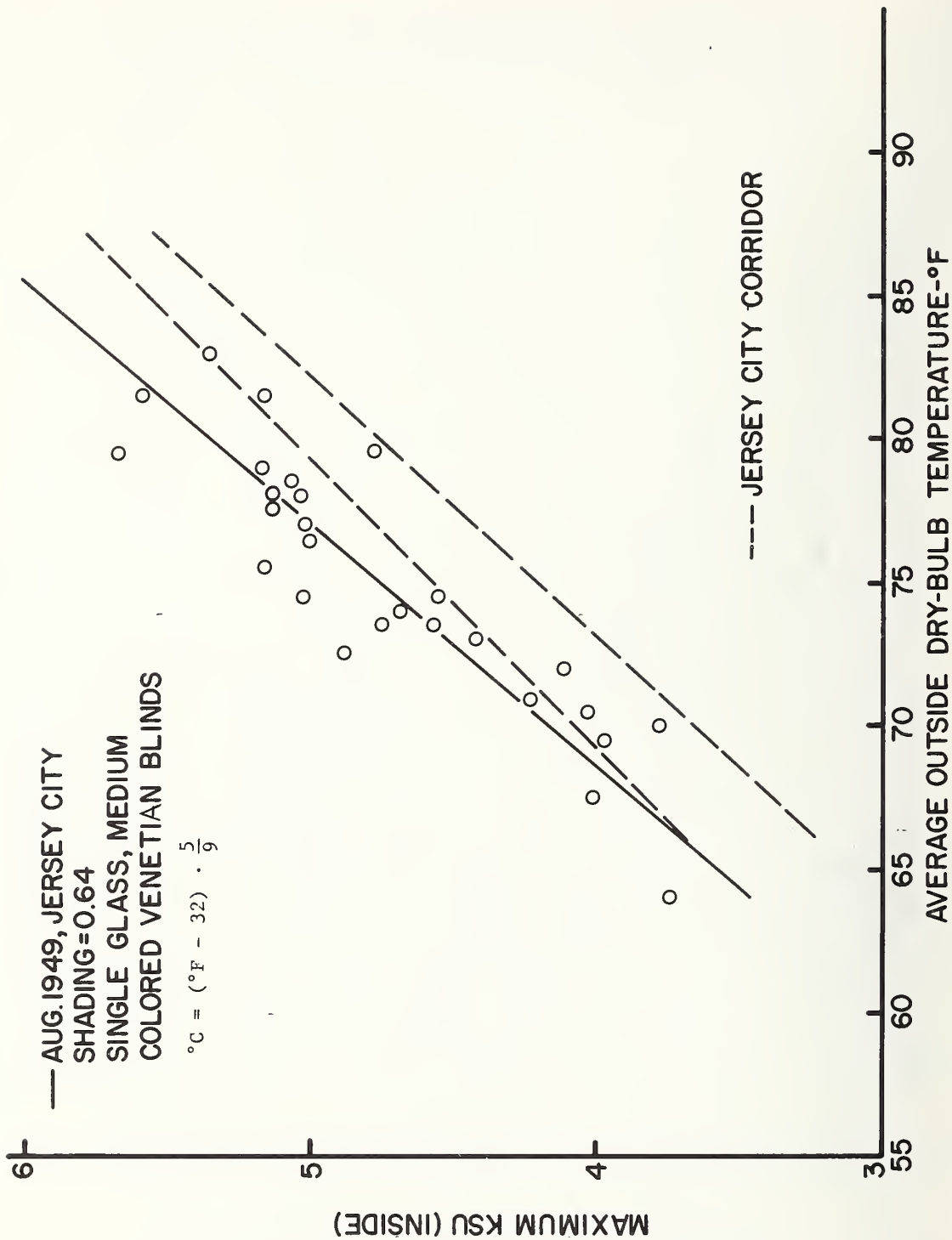


Figure 45 Comparison of Correlation Line and 10 Year Corridor for a Heavyweight Apartment with Different Window Characteristics, Jersey City, N.J.

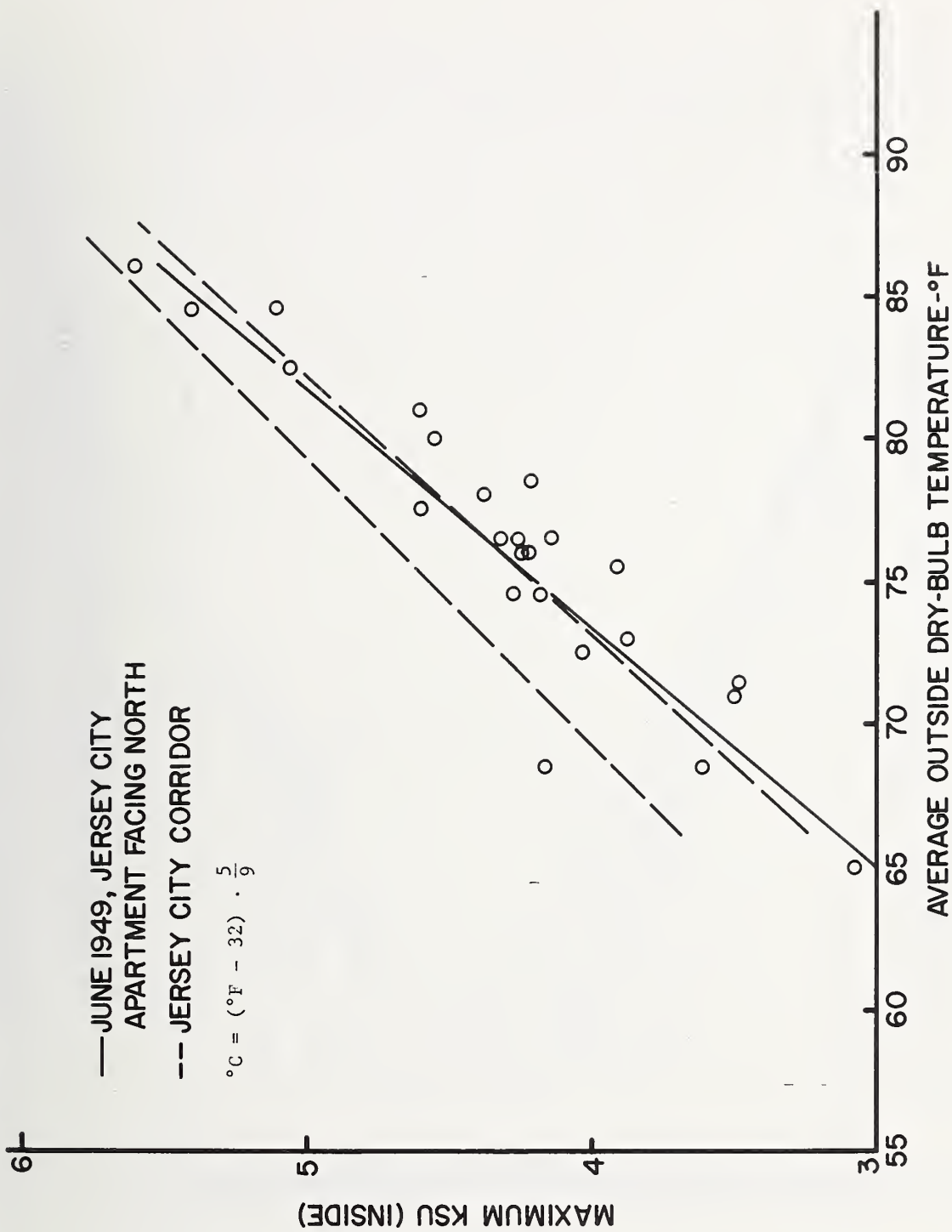


Figure 46 Comparison of Correlation Line and 10 Year Corridor for a Heavyweight Apartment with a Different Orientation, Jersey City, N.J.

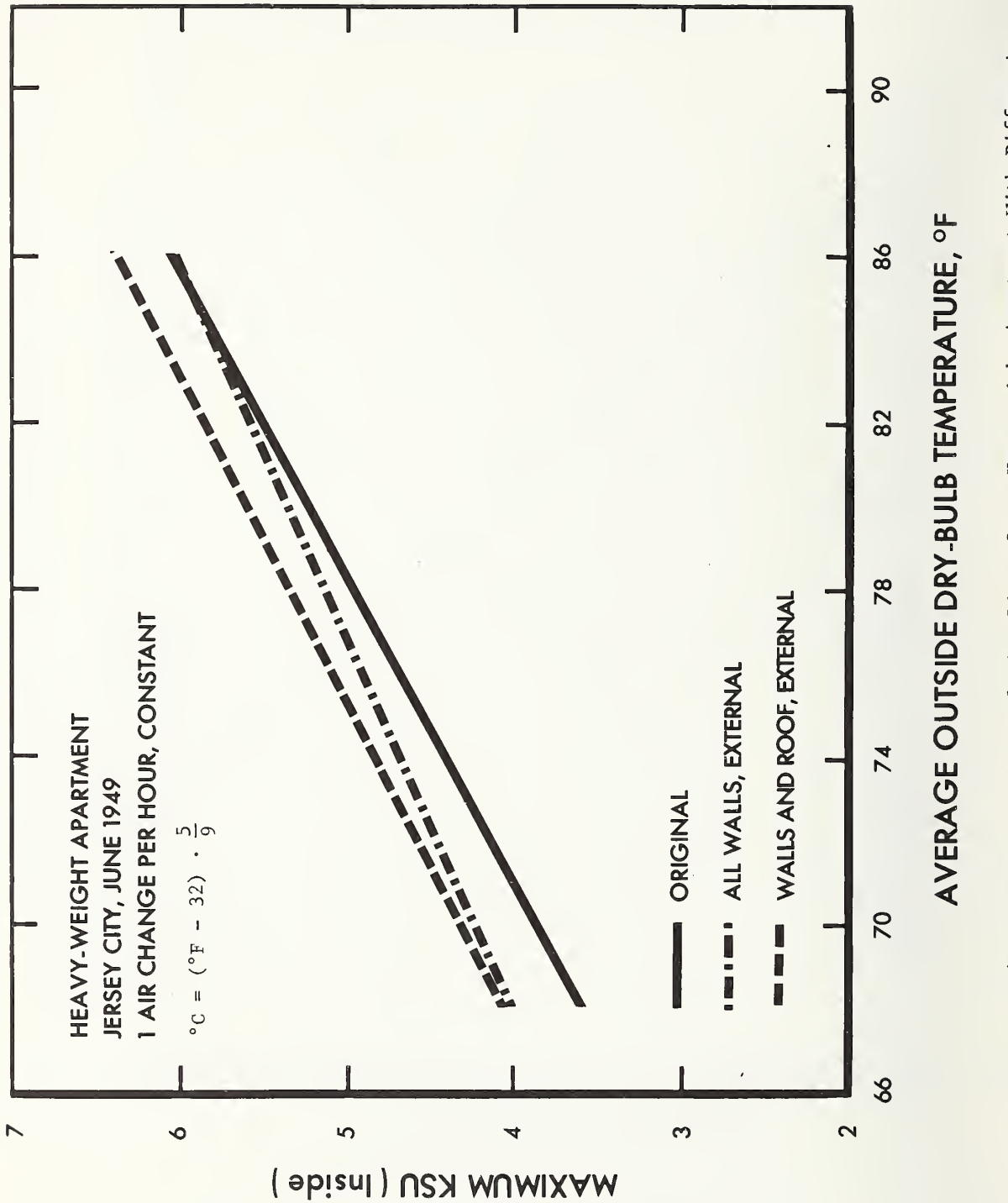


Figure 47 Comparison of Correlation Lines for a Heavyweight Apartment With Different Degrees of Adiabaticity, Jersey City, N.J.

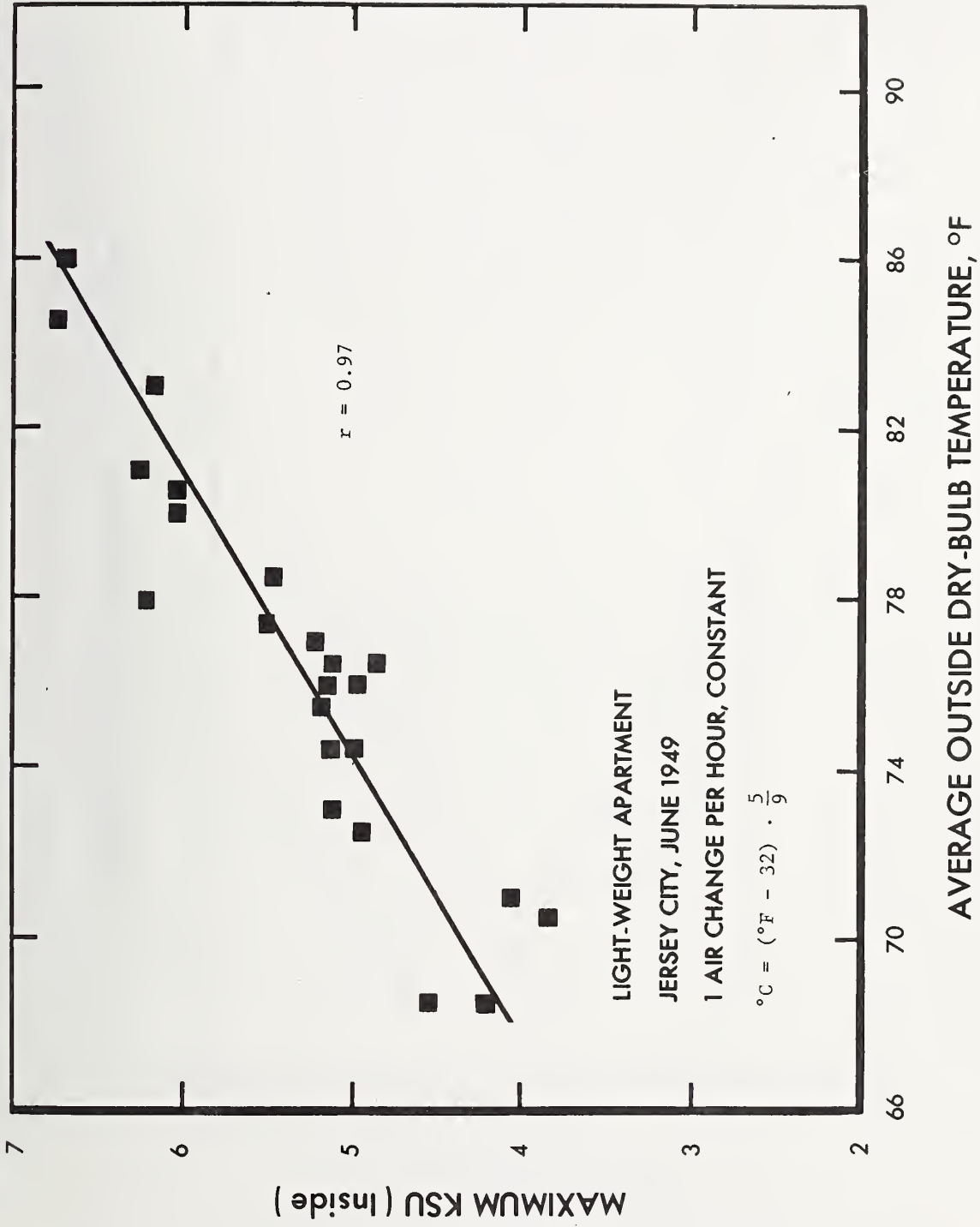


Figure 48 Daily Maximum KSU (Inside) vs Daily Average T<sub>dry-bulb</sub> (Outside) for a Lightweight Apartment, June, 1949, Jersey City, N.J.



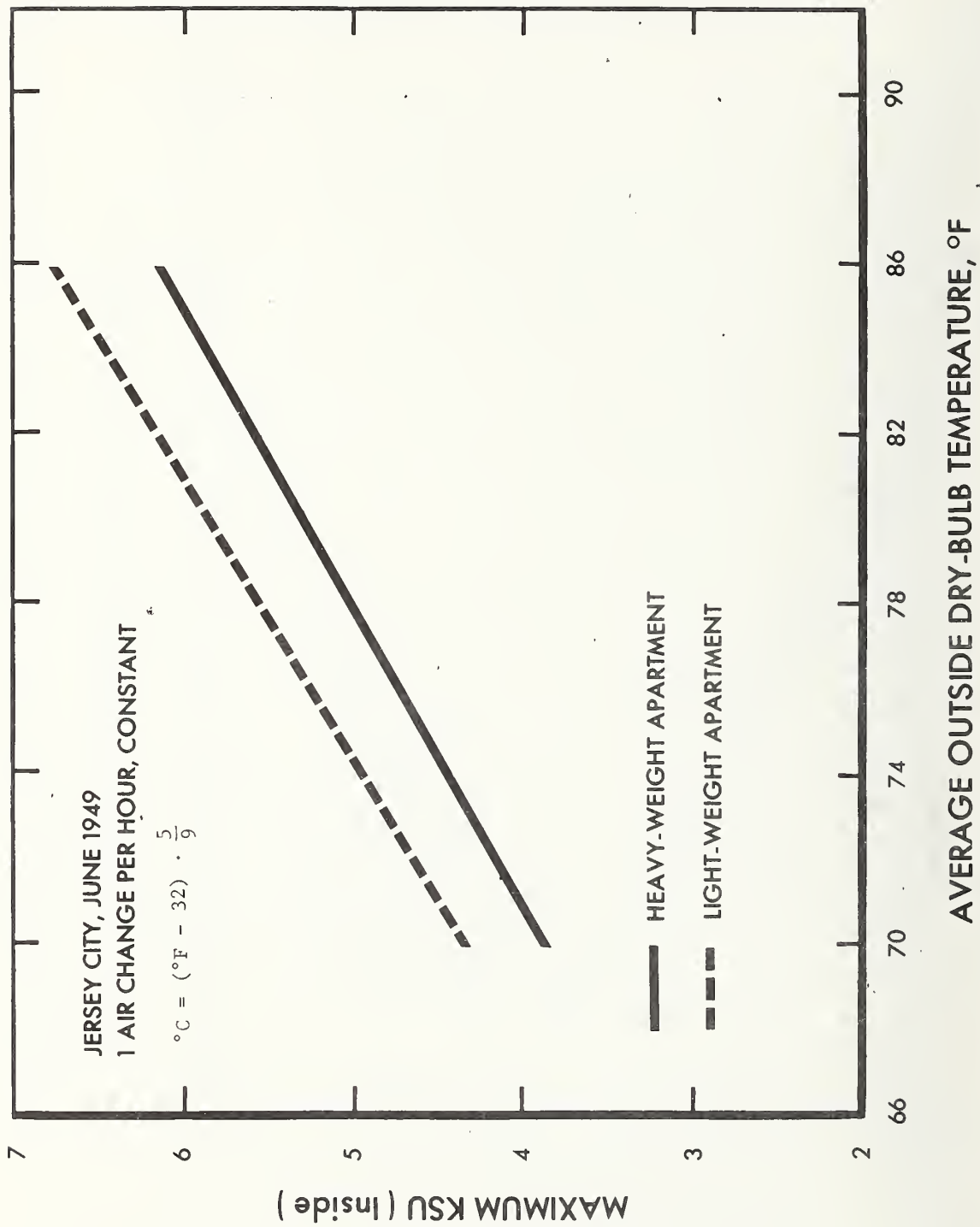


Figure 49 Comparison of Correlation Lines for a Lightweight and Heavyweight Apartment, Jersey City, N.J.

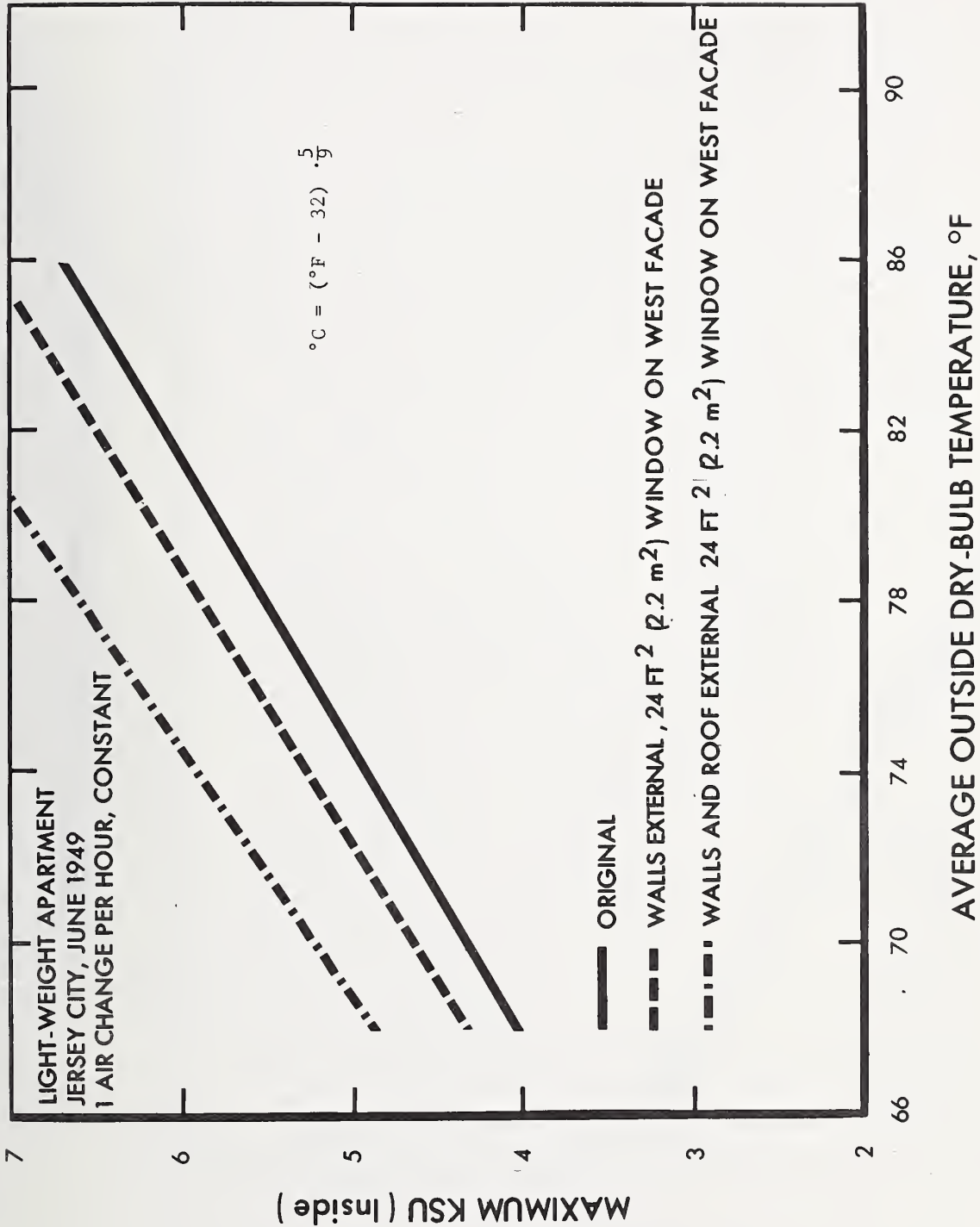


Figure 50 Comparison of Correlation Lines for a Lightweight Apartment With Different Degrees of Adiabaticity, Jersey City, N.J.

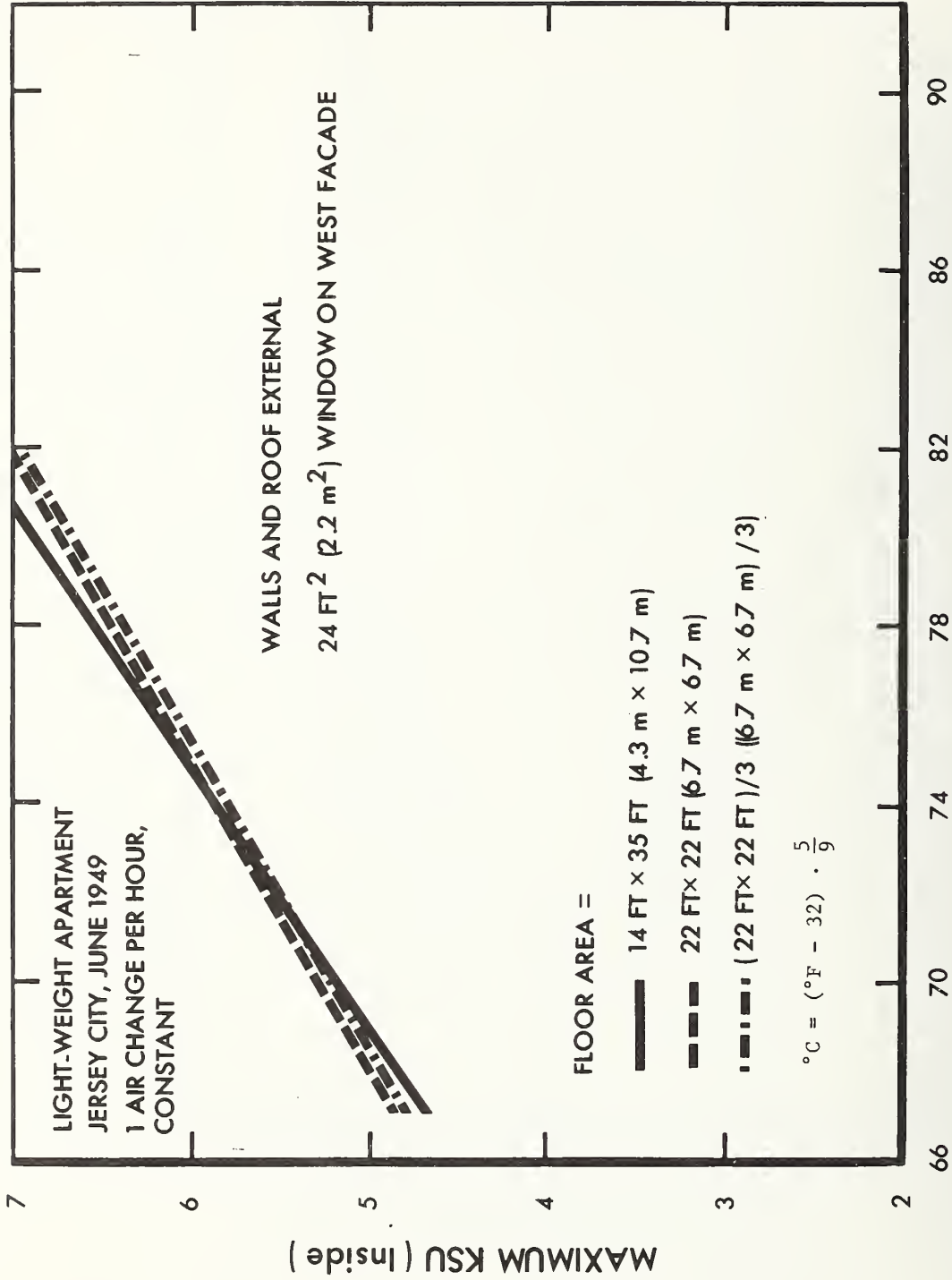


Figure 51 Comparison of Correlation Lines for a Lightweight Apartment With Different Shapes and Floor Area, Jersey City, N.J.

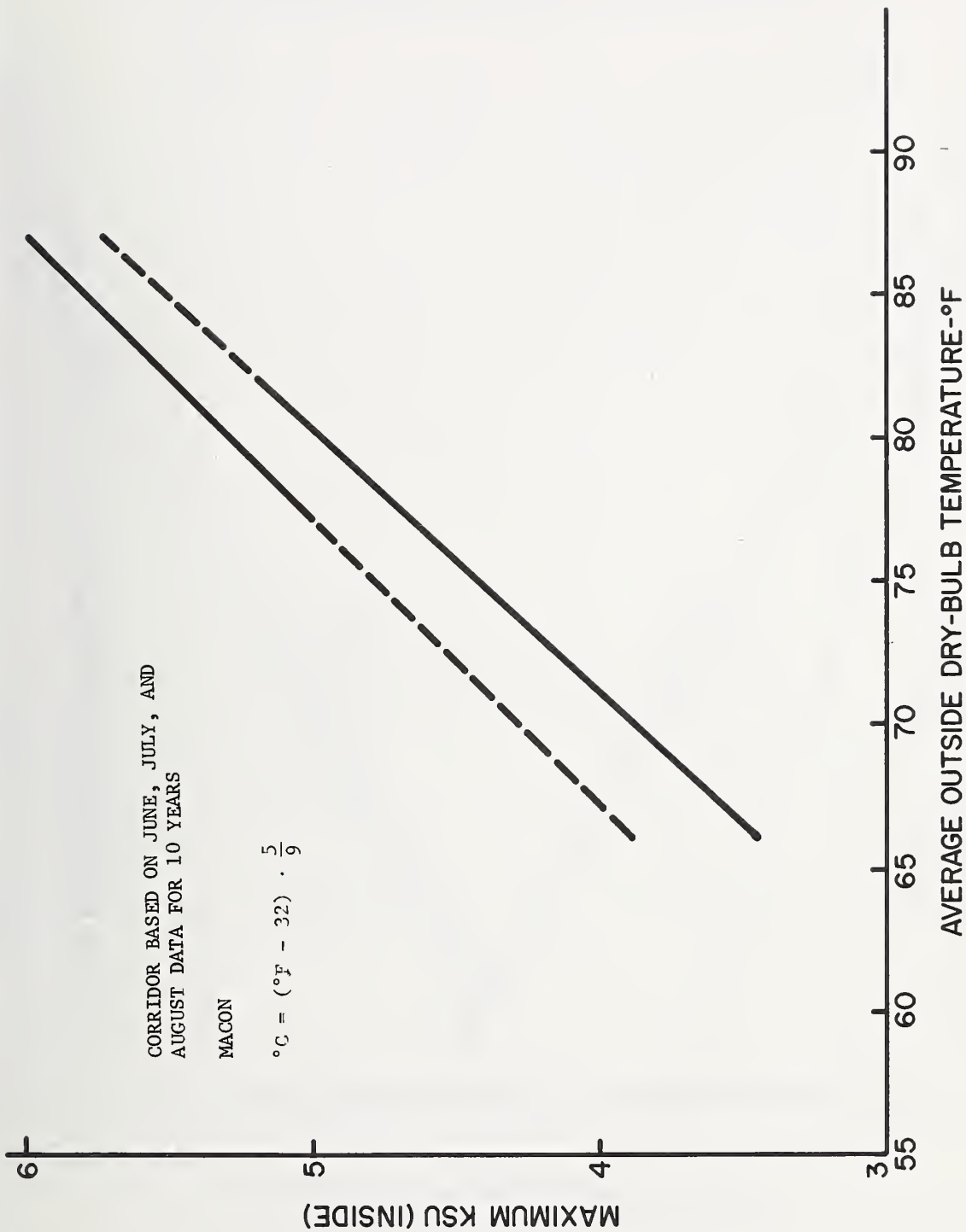


Figure 52 10 Year (June, July, August) Corridor, Macon, Georgia

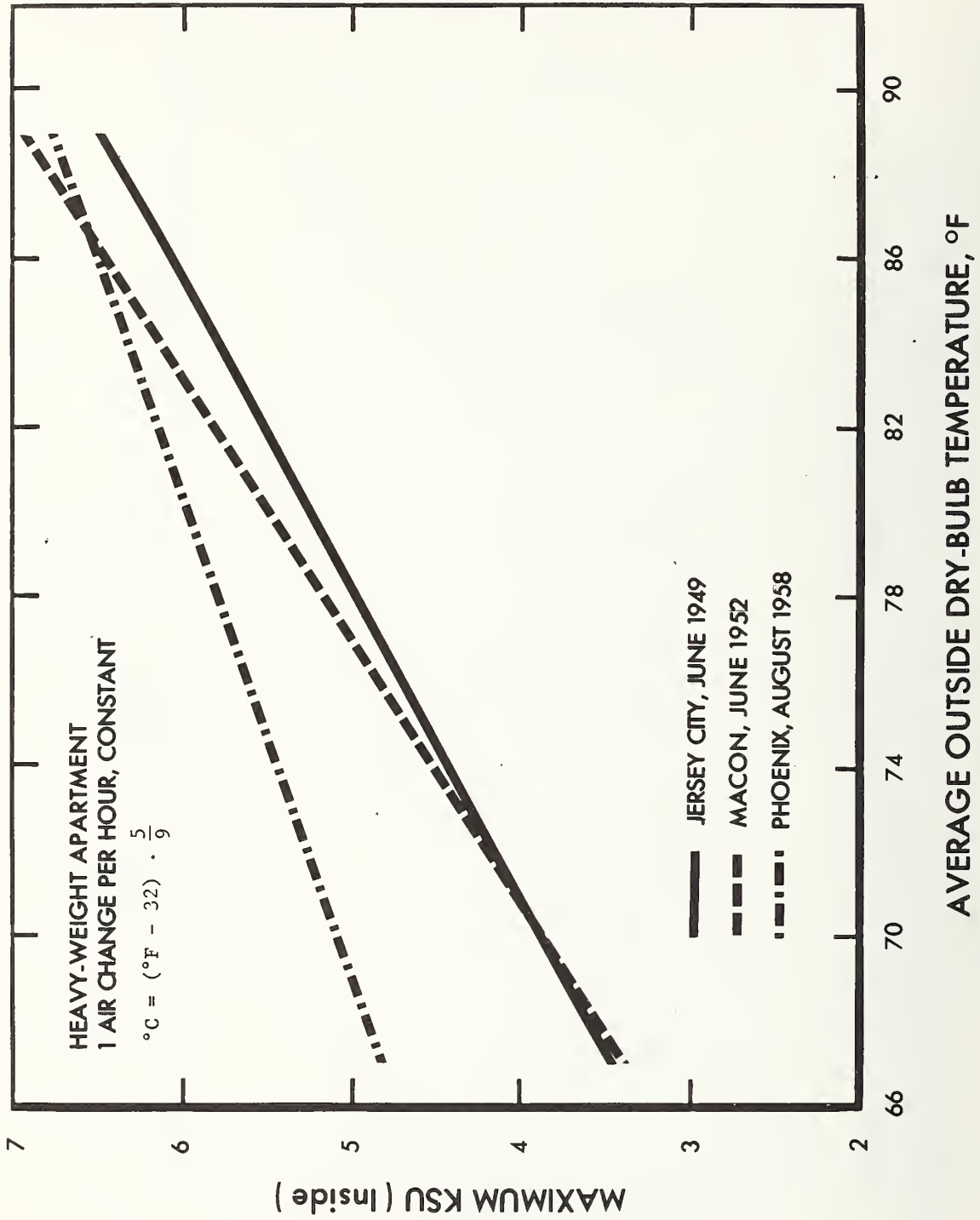


Figure 53 Comparison of Correlation Lines for a Heavyweight Apartment in Three Different Geographical Locations



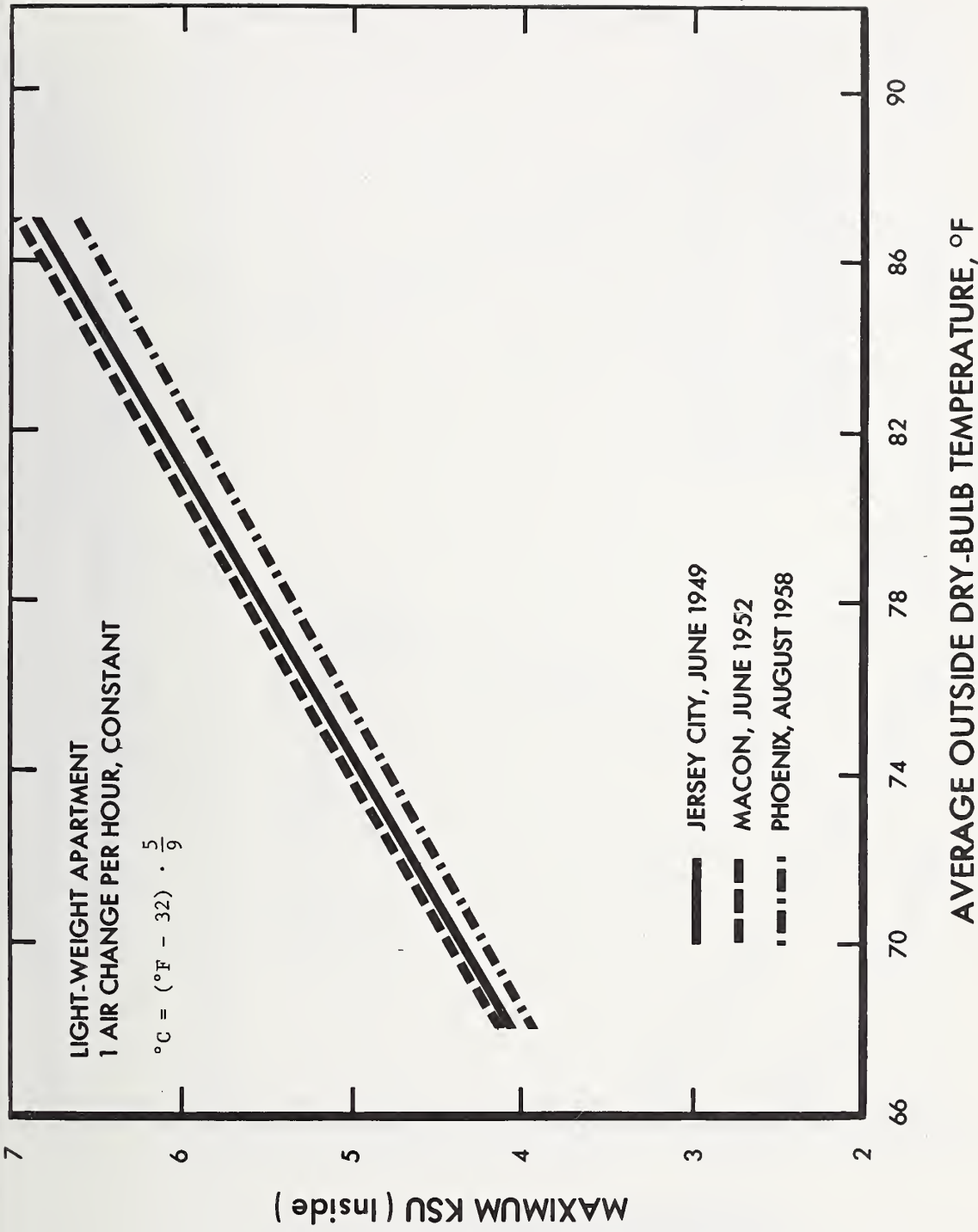


Figure 54 Comparison of Correlation Lines for a Lightweight Apartment in Three Different Geographical Locations

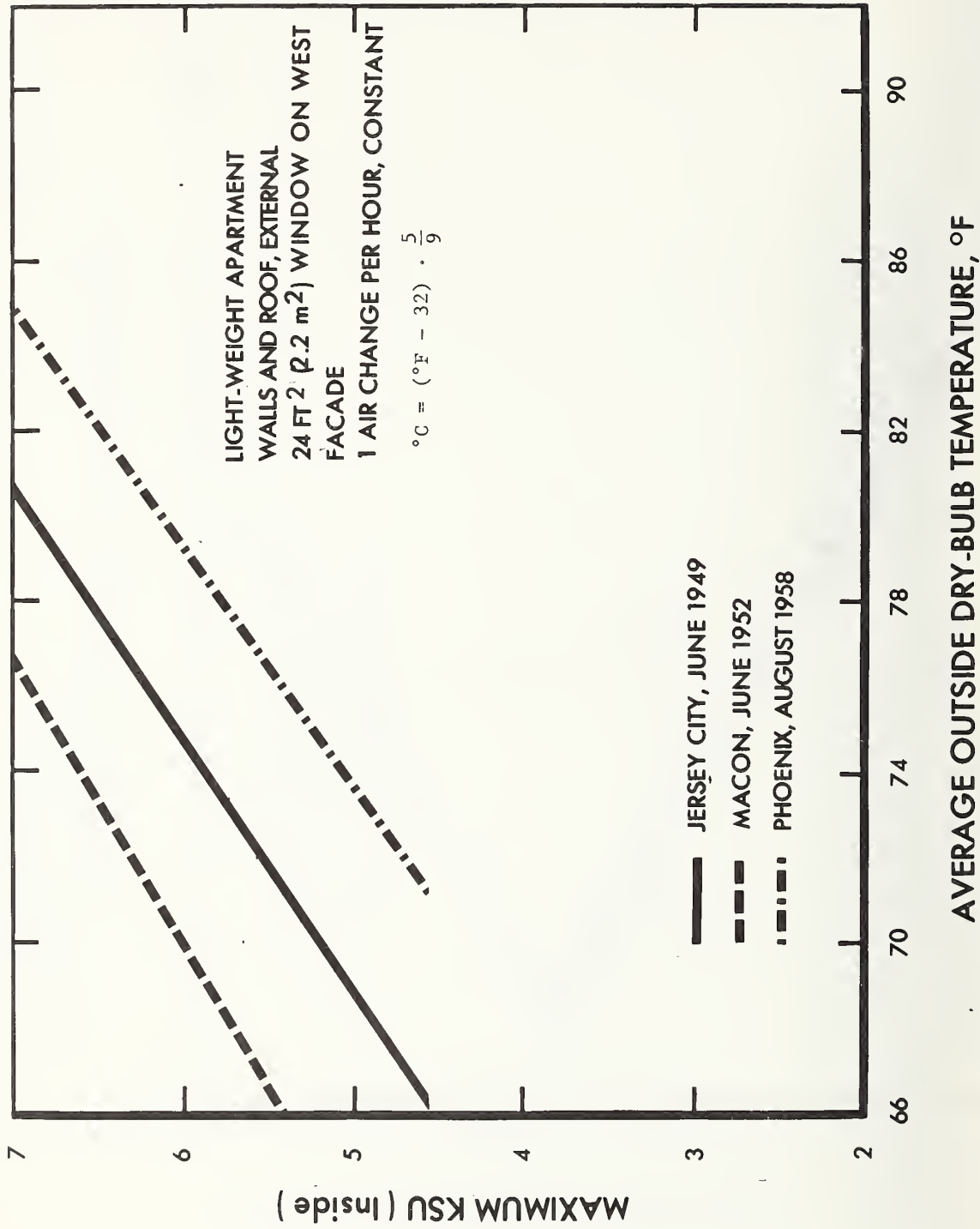


Figure 55 Comparison of Correlation Lines for a Lightweight Apartment with All Walls and Roof Exposed in Three Different Geographical Locations

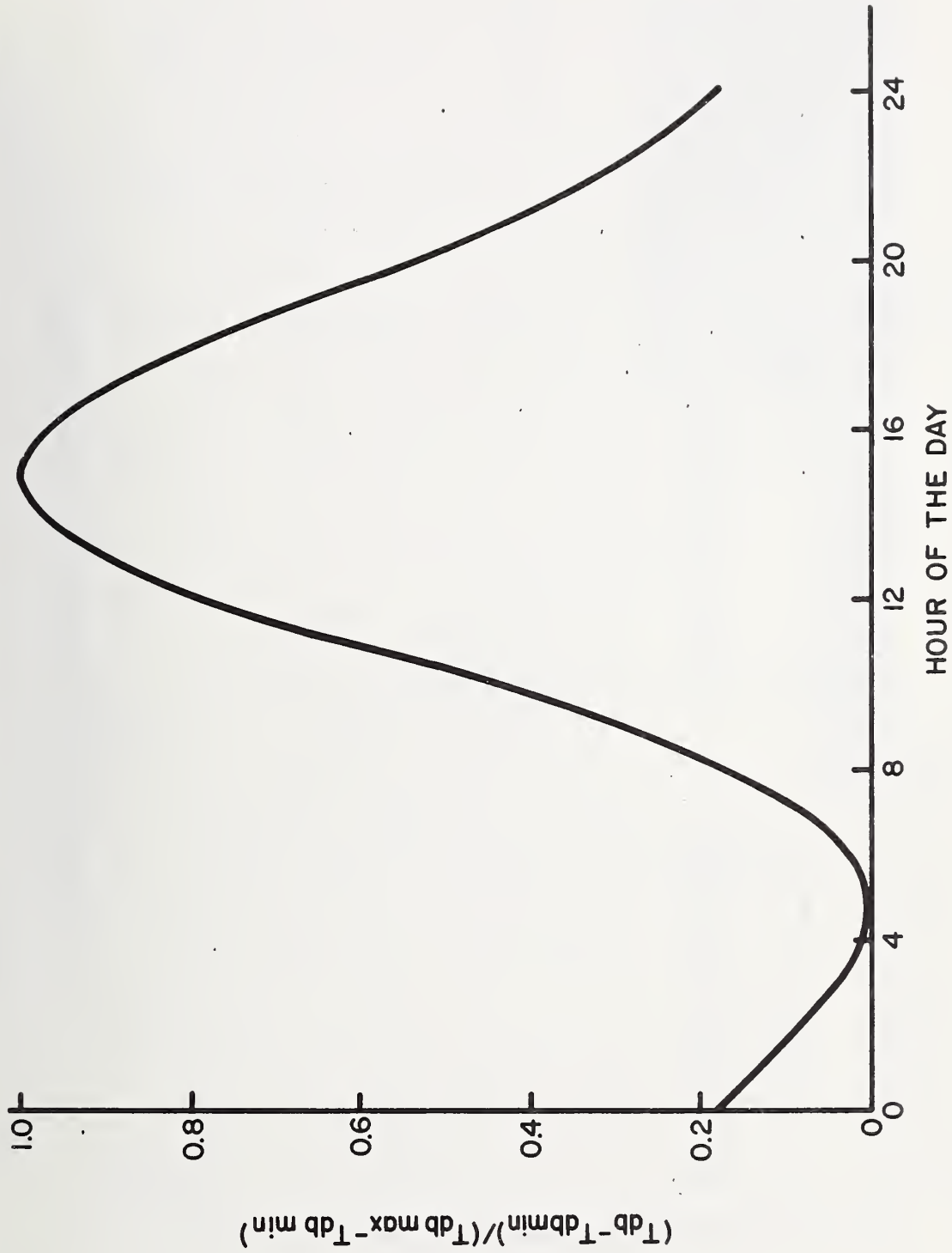


Figure 56 Dimensionless Profile of Daily Dry-bulb Temperature

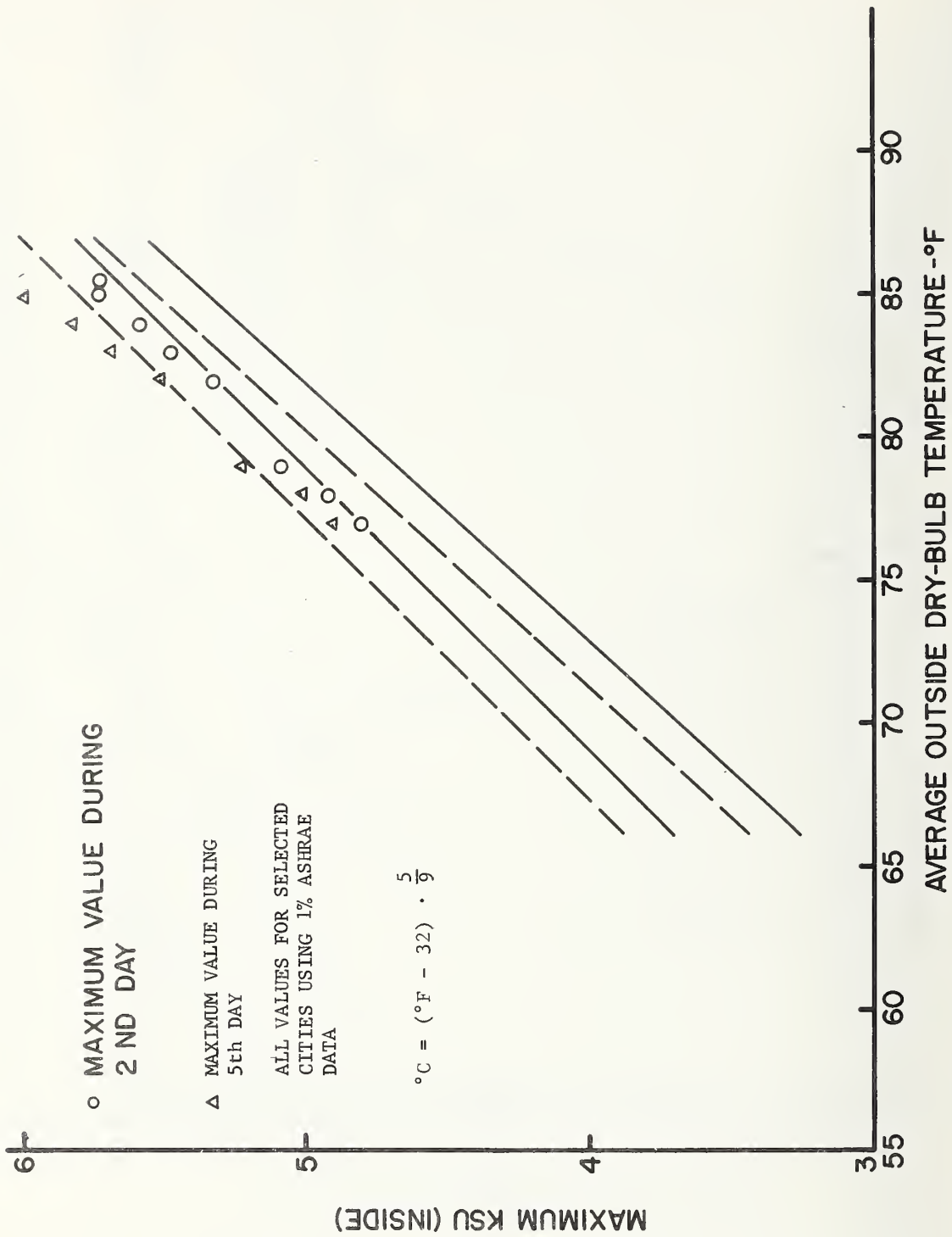


Figure 57 Comparison of Design-Day Calculations with 10 Year Corridors for a Heavyweight Apartment

Table 1

## Maximum Acceptable Values of the Solar Factor

Rooms with Moderate Density of Occupation, Occupied in July and (or) August

Climatic Zone	Thermal Inertia of Construction	Window Orientation	Adequately Ventilated			Badly Ventilated		
			Small Windows	Medium Windows	Large Windows	Small Windows	Medium Windows	Large Windows
M	Moderate	East South West	p.r.	p.r.	70*	p.r.	70*	50*
	Low	East South West	80	50*	35*	55*	35*	25*
			p.r. 50*	55*	40*	60*	35*	25*
N	Moderate	East South West	p.r.	70*	50*	70	45*	30*
	Low	East South West	55	35	25	30	20	15
			50 25	30 20	20 10	20 10	15 10	10
O	Moderate	East South West	70	45*	30*	25	15	10
	Low	East South West	30	20	15			
			20 10	15	10			
P	Moderate	East South West	25	15	10			
	Low	East South West						

Legend: p.r.: no solar-factor requirement

\*: an interior protection device is acceptable if the window is completely openable

 : unsatisfactory conditions whatever sun-control is used.

Table 2

Required Building Data for the "NBSLD" Calculations

- Individual room length, width, and height
- Occupant: number and hourly schedule
- Summer and winter design air infiltration rates
- For each exposure:
  - (1) type (roof, wall, etc.)
  - (2) type or response factor to be used  
or specified U-value
  - (3) area
  - (4) orientation
  - (5) absorptivity to solar radiation (if  
opaque surface)
  - (6) shading coefficient (if transparent  
surface)
- Properties of all building materials



The abbreviations used in Tables 3 - 6, besides those that are clearly defined, are:

E. Wall : Exterior wall

I. Wall : Interior wall or partition

P. Wall : Party wall

B. Floor: Basement floor

B. Wall : Basement wall

I. Door : Interior door

E. Door : Exterior door

Table 3  
Sample of Typical Construction and Thermal Property Data of Building Enclosures

DWELLING TYPE -- MULTI-FAMILY LOW RISE

UNIT TYPE ----- 4 BEDROOM UNITS

CONSTRUCTION --- WOOD FRAME

\*\*\*\*\*THERMAL PROPERTY TABLE FOR BUILDING ENCLOSURES\*\*\*\*\*

LAYER	MATERIAL DESCRIPTION	THICKNESS IN.	DENSITY LB./CU.FT.	SP.HEAT BTU/LB-F	Th.CONDUCTIVITY .8TU-IN/HR-SW.FT-F	Th.RESISTANCE HR-SW.FT-F/8TU
<b>EXTERIOR WALL, FIRST TYPE</b>						
1	AIR FILM (7.5 MPH WIND)					.250
2	GYP SUM SHEATHING	.500	50.0	.259	1.125	.450
3	AIR SPACE	4.000				.970
4	GYP SUM WALL	.500	50.0	.259	1.125	.450
5	AIR FILM (STILL AIR)					.680
<b>INTERIOR WALL</b>						
1	AIR FILM (STILL AIR)					.680
2	GYP SUM WALL	.500	50.0	.259	1.125	.450
3	AIR SPACE	3.000				.970
4	GYP SUM WALL	.500	50.0	.259	1.125	.450
5	AIR FILM (STILL AIR)					.680
<b>PARTY WALL (4-BR.)</b>						
1	AIR FILM (STILL AIR)					.680
2	GYP SUM BOARD	.500	50.0	.259	1.125	.450
3	AIR SPACE	4.000				.970
4	PLYWOOD	.375	34.0	.550	.800	.469
5	PLYWOOD	.375	34.0	.550	.800	.469
6	AIR SPACE	4.000				.970
7	GYP SUM BOARD	.500	50.0	.259	1.125	.450
8	AIR FILM (STILL AIR)					.680
<b>FLOOR/CEILING</b>						
1	AIR FILM (STILL AIR)					.920
2	CARPET					1.230
3	PLYWOOD	.625	34.0	.550	.800	.780
4	AIR SPACE	8.000				1.100
5	PLYWOOD	.375	34.0	.550	.800	.470
6	AIR SPACE	6.000				1.100
7	GYP SUM CEILING	.500	50.0	.259	1.125	.450
8	AIR FILM (STILL AIR)					.920

Table 3 (continued)

TOP FLOOR CEILING							
1	AIR FILM (STILL AIR)					.920	
2	CARPET					1.230	
3	PLYWOOD	.625	34.0	.550	.800	1.100	
4	AIR SPACE (18 GA. ST. DECK)					.111	
5	CONCRETE BEARING CHANNEL	1.330	140.0	.210	12.000	.470	
6	PLYWOOD	.375	34.0	.550	.800	1.100	
7	AIR SPACE	6.000				.450	
8	GYP SUM CEILING	.500	50.0	.259	1.125	.920	
9	AIR FILM (STILL AIR)	.300					
FIRST FLOOR							
1	AIR FILM (STILL AIR)					.920	
2	CARPET					1.230	
3	PLYWOOD	.625	34.0	.550	.800	.780	
4	AIR SPACE	8.000				1.100	
5	GYP SUM SHEATHING	.500	50.0	.259	1.125	.450	
6	AIR SPACE	3.000				.970	
7	CONCRETE BEARING CHANNEL	1.330	140.0	.210	12.000	.111	
BASEMENT WALL							
1	NONE						
BASEMENT FLOOR							
1	NONE						
EXTERIOR WALL, SECOND TYPE							
1	NONE						
WINDOW							
1	SINGLE PANE GLASS	.125				.945	

\*NOTE --- 1. RESISTANCE VALUES FOR SURFACE AIR FILM ARE FOR SUMMER CONDITION

$1 \text{ in.} = 0.0254 \text{ m}$   
 $1 \text{ lb/cu. ft.} = 16 \text{ kg/m}^3$   
 $1 \text{ Btu/(lb} \cdot \text{ }^\circ\text{F)} = 4184 \text{ J/(kg} \cdot \text{ }^\circ\text{C)}$   
 $1 \text{ (Btu} \cdot \text{ in.)}/(\text{hr} \cdot \text{ sq. ft} \cdot \text{ }^\circ\text{F)} = 0.144 \text{ W/(m} \cdot \text{ }^\circ\text{C)}$   
 $1 \text{ (hr} \cdot \text{ sq. ft} \cdot \text{ }^\circ\text{F)}/\text{Btu} = 0.176 \text{ (m}^2 \cdot \text{ }^\circ\text{C)}/\text{W}$

Table 4

Sample of Pertinent Thermal Performance Parameters of Building Enclosures

DWELLING TYPE -- MULTI-FAMILY LOW RISE

UNIT TYPE ----- 1 AND 2 BEDROOM UNITS

CONSTRUCTION --- WOOD FRAME

\*\*\*\*\*VALUES OF PERTINENT THERMAL PERFORMANCE PARAMETERS OF BUILDING ENCLOSURES\*\*\*\*\*

	F. WALL	I. WALL	P. WALL	FL./CEIL.	ROOF	1ST FL.	B. FLOOR	R. WALL	2ND F. WALL
VT./UNIT AREA(LB./SQ.FT.)	6.929	4.167	10.417	4.375	17.521	20.433	*****	*****	*****
U-VALUE(BTU/HR-SQ.FT.-F)	.145	.310	.216	.182	.067	.141	*****	*****	*****
TH.MASS(BTU/SQ.FT.-F)	1.638	1.079	2.698	1.648	3.735	5.356	*****	*****	*****
TH.TIME CONST.(HR.)	6.794	1.743	6.232	5.377	11.424	21.547	*****	*****	*****

DWELLING TYPE -- MULTI-FAMILY LOW RISE

UNIT TYPE ----- 4 BEDROOM UNITS

CONSTRUCTION --- WOOD FRAME

\*\*\*\*\*VALUES OF PERTINENT THERMAL PERFORMANCE PARAMETERS OF BUILDING ENCLOSURES\*\*\*\*\*

	E. WALL	I. WALL	P. WALL	FL./CEIL.	ROOF	1ST FL.	B. FLOOR	R. WALL	2ND F. WALL
VT./UNIT AREA(LB./SQ.FT.)	4.167	4.167	6.292	4.917	20.433	19.371	*****	*****	*****
U-VALUE(BTU/HR-SQ.FT.-F)	.357	.310	.195	.143	.141	.180	*****	*****	*****
TH.MASS(BTU/SQ.FT.-F)	1.079	1.079	2.248	2.096	5.356	4.772	*****	*****	*****
TH.TIME CONST.(HR.)	1.274	1.743	5.775	8.109	21.547	22.709	*****	*****	*****

1 lb/sq. ft = 4.88 kg/m<sup>2</sup>

1 Btu/(hr · sq. ft · °F) = 5.67 W/(m<sup>2</sup> · °C)

1 Btu/(sq. ft · °F) = 2.04 x 10<sup>4</sup> J/(m<sup>2</sup> · °C)

1 hr. = 3600 s

## Sample of Typical Geometric Data Room-by-Room, of a Dwelling Unit

DwELLING TYPE -- MULTI-FAMILY LOW RISE

UNIT TYPE ----- 4 BEDROOM UNITS

CONSTRUCTION --- WOOD FRAME

FLOOR LEVEL -- 3

TYPE OF ROOM - BEDROOM NO. 3 (LENGTH=14.0 FT. WIDTH=13.2 FT. HEIGHT= 8.0 FT.)

	E. WALL SQ.FT.	I. WALL SQ.FT.	P. WALL SQ.FT.	OPENING SQ.FT.	WINDOW/ DIMENSION SQ.FT. FT.	SH.FAC. SQ.FT.	E.DOOR SQ.FT.	I.DOOR SQ.FT.	FLOOR/CEILING SQ.FT.
S 1	112.		95.					17.	
S 2	106.		106.						
S 3	112.	48.			64.	9.00X7.33	.55		
S 4	106.		106.						
TOTAL		48.	95.		64.			17.	185.

TOTAL INTERIOR DOOR CRACK= 18.0 FT.

TOTAL EXTERIOR DOOR CRACK= .0 FT.

TOTAL WINDOW CRACK= 47.0 FT.

ROOF AREA- ROOF NOT ON THIS LEVEL

LIGHTING=

FURNITURE=

FLOOR LEVEL -- 3

TYPE OF ROOM - BEDROOM NO. 4 (LENGTH=14.0 FT. WIDTH=13.2 FT. HEIGHT= 8.0 FT.)

	E. WALL SQ.FT.	I. WALL SQ.FT.	P. WALL SQ.FT.	OPENING SQ.FT.	WINDOW/ DIMENSION SQ.FT. FT.	SH.FAC. SQ.FT.	E.DOOR SQ.FT.	I.DOOR SQ.FT.	FLOOR/CEILING SQ.FT.
S 1	112.		95.					17.	
S 2	106.		106.						
S 3	112.	48.			63.	9.00X7.00	.55		
S 4	106.		106.						
TOTAL		48.	95.		63.			17.	185.

TOTAL INTERIOR DOOR CRACK= 18.0 FT.

TOTAL EXTERIOR DOOR CRACK= .0 FT.

TOTAL WINDOW CRACK= 32.0 FT.

ROOF AREA- ROOF NOT ON THIS LEVEL

LIGHTING=

FURNITURE=

FLOOR LEVEL -- 3

TYPE OF ROOM - BATHROOM		(LENGTH= 5.0 FT. WIDTH= 8.0 FT. HEIGHT= 8.0 FT.)		FLOOR/CEILING			
	E.WALL SQ.FT.	I.WALL SQ.FT.	P.WALL SQ.FT.	OPENING WINDOW/DIMENSION SQ.FT.	SH.FAC. SQ.FT.	E.DOOR SQ.FT.	I.DOOR SQ.FT.
S 1	40.		40.				
S 2	64.		64.				
S 3	40.		40.				
S 4	64.		51.				13.
TOTAL			131.				13.
TOTAL INTERIOR DOOR CRACK=		17.0 FT.					
TOTAL EXTERIOR DOOR CRACK=		.0 FT.					
TOTAL WINDOW CRACK=		.0 FT.					
ROOF AREA- ROOF NOT ON THIS LEVEL							
LIGHTING= 180.0 WATTS							
FURNITURE=							

FLOOR LEVEL -- 3

TYPE OF ROOM - HALL AND STAIRWAYS		(LENGTH= 6.0 FT. WIDTH=12.0 FT. HEIGHT= 8.0 FT.)		FLOOR/CEILING			
	E.WALL SQ.FT.	I.WALL SQ.FT.	P.WALL SQ.FT.	OPENING WINDOW/DIMENSION SQ.FT.	SH.FAC. SQ.FT.	E.DOOR SQ.FT.	I.DOOR SQ.FT.
S 1	48.		31.				17.
S 2	96.		83.				13.
S 3	48.		31.				17.
S 4	96.		96.				
TOTAL			145.				47.
TOTAL INTERIOR DOOR CRACK=		53.0 FT.					
TOTAL EXTERIOR DOOR CRACK=		.0 FT.					
TOTAL WINDOW CRACK=		.0 FT.					
ROOF AREA- ROOF NOT ON THIS LEVEL							
LIGHTING= 100.0 WATTS							
FURNITURE=							

FLOOR LEVEL -- 2

TYPE OF ROOM - BEDROOM NO. 1		(LENGTH=14.0 FT. WIDTH=13.2 FT. HEIGHT= 8.0 FT.)		FLOOR/CEILING			
	E.WALL SQ.FT.	I.WALL SQ.FT.	P.WALL SQ.FT.	OPENING WINDOW/DIMENSION SQ.FT.	SH.FAC. SQ.FT.	E.DOOR SQ.FT.	I.DOOR SQ.FT.
S 1	112.		95.				17.



S 2	106.								
S 3	112.	75.							
S 4	106.								
TOTAL		75.	95.					17.	185.

TOTAL INTERIOR DOOR CRACK= 18.0 FT.  
 TOTAL EXTERIOR DOOR CRACK= .0 FT.  
 TOTAL WINDOW CRACK= 37.0 FT.  
 ROOF AREA- ROOF NOT ON THIS LEVEL  
 LIGHTING=  
 FURNITURE=

FLOOR LEVEL -- 2

TYPE OF ROOM - BEDROOM NO. 2									
(LENGTH=14.0 FT. WIDTH=13.2 FT. HEIGHT= 8.0 FT.)									
TOTAL	E.WALL	I.WALL	P.WALL	OPENING	WINDOW/DIMENSION	SH.FAC.	E.DOOR	I.DOOR	FLOOR/CEILING
SQ.FT.	SQ.FT.	SQ.FT.	SQ.FT.	SQ.FT.	FT.	SQ.FT.	SQ.FT.	SQ.FT.	SQ.FT.
S 1	112.	49.			63.	9.00X7.00	.55		
S 2	106.								
S 3	112.	95.							17.
S 4	106.								
TOTAL	155.	95.	106.		63.				17.

TOTAL INTERIOR DOOR CRACK= 18.0 FT.  
 TOTAL EXTERIOR DOOR CRACK= .0 FT.  
 TOTAL WINDOW CRACK= 32.0 FT.  
 ROOF AREA- ROOF NOT ON THIS LEVEL  
 LIGHTING=  
 FURNITURE=

FLOOR LEVEL -- 2

TYPE OF ROOM - BATHROOM									
(LENGTH= 5.0 FT. WIDTH= 8.0 FT. HEIGHT= 8.0 FT.)									
TOTAL	E.WALL	I.WALL	P.WALL	OPENING	WINDOW/DIMENSION	SH.FAC.	E.DOOR	I.DOOR	FLOOR/CEILING
SQ.FT.	SQ.FT.	SQ.FT.	SQ.FT.	SQ.FT.	FT.	SQ.FT.	SQ.FT.	SQ.FT.	SQ.FT.
S 1	40.								
S 2	64.								
S 3	40.								
S 4	64.								
TOTAL	131.	40.	64.						40.

TOTAL INTERIOR DOOR CRACK= 18.0 FT.  
 TOTAL EXTERIOR DOOR CRACK= .0 FT.  
 TOTAL WINDOW CRACK= .0 FT.  
 ROOF AREA- ROOF NOT ON THIS LEVEL  
 LIGHTING= 180.0 WATTS  
 FURNITURE=

FLOOR LEVEL -- 2

TYPE OF ROOM - HALL AND STAIRWAYS		(LENGTH= 6.0 FT. WIDTH=12.0 FT. HEIGHT= 8.0 FT.)							
TOTAL	E.WALL	I.WALL	P.WALL	OPENING	WINDOW/DIMENSION	SH.FAC.	E.DOOR	I.DOOR	FLOOR/CEILING
SQ.FT.	SQ.FT.	SQ.FT.	SQ.FT.	SQ.FT.	FT.	SQ.FT.	SQ.FT.	SQ.FT.	SQ.FT.
S 1	48.		31.					17.	
S 2	96.		83.					13.	
S 3	48.		31.					17.	
S 4	96.			96.					
TOTAL			145.					47.	72.

TOTAL INTERIOR DOOR CRACK= 53.0 FT.  
 TOTAL EXTERIOR DOOR CRACK= .0 FT.  
 TOTAL WINDOW CRACK= .0 FT.  
 ROOF AREA- ROOF NOT ON THIS LEVEL  
 LIGHTING= 100.0 WATTS  
 FURNITURE=

FLOOR LEVEL -- 1

TYPE OF ROOM - LIVING AND DINNING ROOM		(LENGTH=14.2 FT. WIDTH=22.5 FT. HEIGHT= 8.0 FT.)							
TOTAL	E.WALL	I.WALL	P.WALL	OPENING	WINDOW/DIMENSION	SH.FAC.	E.DOOR	I.DOOR	FLOOR/CEILING
SQ.FT.	SQ.FT.	SQ.FT.	SQ.FT.	SQ.FT.	FT.	SQ.FT.	SQ.FT.	SQ.FT.	SQ.FT.
S 1	111.	48.			63.	9.00X7.00		.55	
S 2	180.		180.						
S 3	114.		33.	81.					
S 4	180.	90.	90.						
TOTAL		138.	123.	180.	81.	63.			320.

TOTAL INTERIOR DOOR CRACK= .0 FT.  
 TOTAL EXTERIOR DOOR CRACK= .0 FT.  
 TOTAL WINDOW CRACK= 33.0 FT.  
 ROOF AREA- ROOF NOT ON THIS LEVEL  
 LIGHTING= 360.0 WATTS  
 FURNITURE=

FLOOR LEVEL -- 1

TYPE OF ROOM - KITCHEN		(LENGTH= 8.0 FT. WIDTH=11.2 FT. HEIGHT= 8.0 FT.)							
TOTAL	E.WALL	I.WALL	P.WALL	OPENING	WINDOW/DIMENSION	SH.FAC.	E.DOOR	I.DOOR	FLOOR/CEILING
SQ.FT.	SQ.FT.	SQ.FT.	SQ.FT.	SQ.FT.	FT.	SQ.FT.	SQ.FT.	SQ.FT.	SQ.FT.
S 1	64.								
S 2	90.								
TOTAL									

Table 5 - Page 5

S 3	64.	42.		22.	3.00X7.33	.55	
S 4	90.		66.	24.			
TOTAL		42.	66.	88.	22.		90.

TOTAL INTERIOR DOOR CRACK- .0 FT.  
 TOTAL EXTERIOR DOOR CRACK- .0 FT.  
 TOTAL WINDOW CRACK- 21.0 FT.  
 ROOF AREA- ROOF NOT ON THIS LEVEL  
 LIGHTING= 180.0 WATTS  
 FURNITURE=

FLOOR LEVEL -- 1

TYPE OF ROOM - ENTRANCE HALL		(LENGTH= 5.7 FT. WIDTH=15.0 FT. HEIGHT= 8.0 FT.)							
TOTAL	E. WALL	I. WALL	P. WALL	OPENING	WINDOW/DIMENSION	SH.FAC.	E.DOOR	I.DOOR	FLOOR/CEILING
SQ.FT.	SQ.FT.	SQ.FT.	SQ.FT.	SQ.FT.	FT.	SQ.FT.	SQ.FT.	SQ.FT.	SQ.FT.
S 1	46.		26.	20.					
S 2	120.		74.	24.				22.	
S 3	46.	35.			11.	1.50X7.00	.55		
S 4	120.								
TOTAL	35.	100.	120.	44.	11.			22.	86.

TOTAL INTERIOR DOOR CRACK- .0 FT.  
 TOTAL EXTERIOR DOOR CRACK- 22.0 FT.  
 TOTAL WINDOW CRACK- .0 FT.  
 ROOF AREA- ROOF NOT ON THIS LEVEL  
 LIGHTING= 100.0 WATTS  
 FURNITURE=

1 sq. ft = 0.0929 m<sup>2</sup>  
 1 ft = 0.3048 m

Table 6

Sample of Pertinent Thermal Performance Parameters and Geometric Data Associated with a Dwelling Unit

DWELLING TYPE -- MULTI-FAMILY LOW RISE

UNIT TYPE ----- 2 BEDROOM UNITS

CONSTRUCTION --- STEEL JOIST (GYPSUM FRAME)

	E.WALL	I.WALL	P.WALL	FL./CEIL.	ROOF	1ST FL.	B.FLOOR	B.WALL	I.DOOR	WINDOW	E.DOOR
TOTAL AREA/UNIT (SQ.FT.)	441.	608.	1008.	1025.	512.	512.	0.	0.	94.	204.	22.
WT./UNIT AREA (LB./SQ.FT.)	6.929	4.167	10.417	4.375	17.521	20.433					
U-VALUE (BTU/HR-SQ.FT.-F)	.145	.310	.216	.182	.067	.141			.441	1.058	.481
TH.MASS (BTU/SQ.FT.-F)	1.638	1.079	2.698	1.648	3.735	5.356					
TH.TIME CONST. (HR.)	6.794	1.743	6.232	5.377	11.424	21.547					
SOLAR ABSORPTIVITY	.350	.....	.....	.....	.350	.....	.....	.....	.....	.....	.350
SOLAR TRANSMITTANCE	.....	.....	.....	.....	.....	.....	.....	.....	.....	.870	.....

TOTAL FLOOR AREA PER UNIT = 1025. SQ.FT.

AREA RATIO, EXT.WALL/FLOOR = .430

AREA RATIO, WINDOW/EXT.WALL = .463

DWELLING TYPE -- MULTI-FAMILY LOW RISE

UNIT TYPE ----- 4 BEDROOM UNITS

CONSTRUCTION --- STEEL JOIST (GYPSUM FRAME)

	F.WALL	I.WALL	P.WALL	FL./CEIL.	ROOF	1ST FL.	B.FLOOR	B.WALL	I.DOOR	WINDOW	E.DOOR
TOTAL AREA/UNIT (SQ.FT.)	648.	1221.	1346.	1460.	487.	487.	0.	0.	188.	323.	22.
WT./UNIT AREA (LB./SQ.FT.)	4.167	4.167	6.292	4.917	20.433	19.371					
U-VALUE (BTU/HR-SQ.FT.-F)	.357	.310	.195	.143	.141	.180			.441	1.058	.481
TH.MASS (BTU/SQ.FT.-F)	1.079	1.079	2.248	2.098	5.356	4.772					
TH.TIME CONST. (HR.)	1.279	1.743	5.775	8.109	21.547	22.709					
SOLAR ABSORPTIVITY	.350	.....	.....	.....	.000	.....	.....	.....	.....	.....	.350
SOLAR TRANSMITTANCE	.....	.....	.....	.....	.....	.....	.....	.....	.....	.870	.....

TOTAL FLOOR AREA PER UNIT = 1460. SQ.FT.

AREA RATIO, EXT.WALL/FLOOR = .444

AREA RATIO, WINDOW/EXT.WALL = .494

1 sq. ft = 0.0929 m<sup>2</sup>

1 lb/sq. ft = 4.88 kg/m<sup>2</sup>

1 Btu/(hr · sq. ft · °F) = 5.67 W/(m<sup>2</sup> · °C)

1 Btu/(sq. ft · °F) = 2.04 x 10<sup>4</sup> J/(m<sup>2</sup> · °C)

1 hr = 3600 s

Table 7

Summary of Simulation Results for a Heavyweight Apartment in Jersey City, New Jersey

Month and Year	Outdoor Conditions		Indoor Conditions				
	Total No. of Hours in 4 Months T <sub>dry-bulb</sub> ≥ 80 °F (26.7°C)	Total No. of Hours in 4 Months T <sub>wet-bulb</sub> ≥ 67 °F (19.4°C)	Percent of Time New ET ≥ 81	Percent of Time New ET ≥ 85	Percent of Time KSU ≥ 5	Percent of Time PMV ≥ 1 (0.25 clo)	Percent of Time HSI ≥ 40
1949	613	1397	-	-	-	-	-
June	-	-	-	11.0	8.1	7.9	0.0
July	-	-	-	27.6	22.4	20.6	0.5
August	-	-	-	11.7	8.7	8.2	0.0
September	-	-	-	0.0	0.0	0.0	0.0
1950	431	822	-	-	-	-	-
June	-	-	11.7	0.8	0.6	0.7	0.0
July	-	-	20.3	3.2	2.0	1.9	0.0
August	-	-	9.9	3.1	1.5	0.7	0.0
September	-	-	5.8	1.1	0.4	0.1	0.0
1951	435	1086	-	-	-	-	-
June	-	-	9.2	1.0	0.6	0.3	0.0
July	-	-	30.6	5.5	2.0	1.6	0.0
August	-	-	22.6	3.5	0.5	0.4	0.0
September	-	-	0.8	0.0	0.0	0.0	0.0
1952	615	1258	-	-	-	-	-
June	-	-	18.9	8.7	6.1	6.0	1.1
July	-	-	60.8	27.0	21.1	19.4	0.3
August	-	-	20.6	1.1	0.4	0.1	0.0
September	-	-	3.3	0.1	0.0	0.0	0.0
1953	612	1069	-	-	-	-	-
June	-	-	24.3	5.7	4.0	3.6	0.0
July	-	-	42.5	16.5	11.7	10.8	0.0
August	-	-	20.8	8.5	7.5	7.1	0.0
September	-	-	17.9	13.9	12.2	11.1	0.0
1954	493	583	-	-	-	-	-
June	-	-	8.7	1.0	1.0	1.1	0.0
July	-	-	22.8	4.7	4.2	4.3	0.0
August	-	-	8.1	3.1	2.4	2.6	0.0
September	-	-	3.1	0.0	0.0	0.0	0.0
1955	616	1292	-	-	-	-	-
June	-	-	4.7	0.0	0.0	0.0	0.0
July	-	-	70.8	35.9	26.1	25.5	0.0
August	-	-	51.2	24.9	17.3	15.9	0.0
September	-	-	0.0	0.0	0.0	0.0	0.0
1956	390	887	-	-	-	-	-
June	-	-	17.9	5.1	3.9	3.9	0.0
July	-	-	10.5	1.7	0.8	0.7	0.0
August	-	-	21.5	3.4	1.9	1.3	0.0
September	-	-	2.4	0.0	0.0	0.0	0.0
1957	617	1123	-	-	-	-	-
June	-	-	36.2	13.3	9.4	8.5	0.0
July	-	-	34.9	12.4	10.5	10.9	0.0
August	-	-	17.5	4.6	3.2	3.5	0.0
September	-	-	11.9	0.7	0.4	0.4	0.0
1958	463	1074	-	-	-	-	-
June	-	-	1.0	0.0	0.0	0.0	0.0
July	-	-	43.3	13.2	7.0	6.5	0.0
August	-	-	28.1	3.5	1.2	0.9	0.0
September	-	-	3.7	0.0	0.0	0.0	0.0

Table 8

Correlation Coefficients for the Maximum KSU (Inside)  
and Daily Average  $T_{\text{dry-bulb}}$  (Outside) for a Heavyweight  
Apartment, Jersey City

Month-Year	Correlation Coefficient
June 1949	0.96
July 1949	0.94
August 1949	0.95
September 1949	0.92
June 1953	0.96
July 1953	0.94
August 1953	0.95
September 1953	0.97
June 1954	0.95
July 1954	0.96
August 1954	0.88
September 1954	0.97
June 1955	0.96
July 1955	0.93
August 1955	0.97
September 1955	0.95
June 1956	0.95
July 1956	0.91
August 1956	0.94
September 1956	0.96



Table 9

Frequency Distribution of Average Outside  
Dry-bulb Temperature, Jersey City, 1949

JERSEY CITY, 1949

TEMPERATURE FREQUENCY TABLE

TEMP, F	FREQ	TEMP, F	FREQ	TEMP, F	FREQ	TEMP, F	FREQ
0.	365	25.	362	50.	228	75.	62
1.	365	26.	361	51.	220	76.	55
2.	365	27.	360	52.	214	77.	45
3.	365	28.	356	53.	214	78.	38
4.	365	29.	350	54.	204	79.	32
5.	365	30.	346	55.	197	80.	25
6.	365	31.	340	56.	191	81.	23
7.	365	32.	337	57.	185	82.	18
8.	365	33.	329	58.	180	83.	16
9.	365	34.	320	59.	169	84.	13
10.	365	35.	314	60.	163	85.	9
11.	365	36.	308	61.	153	86.	7
12.	365	37.	301	62.	143	87.	6
13.	365	38.	298	63.	133	88.	3
14.	365	39.	293	64.	129	89.	1
15.	365	40.	287	65.	122	90.	0
16.	365	41.	283	66.	116	91.	0
17.	365	42.	276	67.	113	92.	0
18.	365	43.	272	68.	109	93.	0
19.	365	44.	267	69.	101	94.	0
20.	365	45.	264	70.	97	95.	0
21.	365	46.	255	71.	90	96.	0
22.	365	47.	247	72.	86	97.	0
23.	365	48.	238	73.	79	98.	0
24.	364	49.	231	74.	70	99.	0

$$^{\circ}\text{C} = (^{\circ}\text{F} - 32) \cdot \frac{5}{9}$$

Table 10

Correlation Coefficients for the Maximum KSU (Inside) and Daily Average  
 T<sub>dry-bulb</sub> (Outside) for a Heavyweight Apartment with Configuration Changes, Jersey City

	Apartment Facing North Shading Coefficient = 0.22		Apartment Facing West Shading Coefficient = 0.64		Apartment Facing North Shading Coefficient = 0.64	
June 1949	0.96	0.94	0.96	0.96	0.96	0.96
July 1949	0.93	0.92	0.92	0.94	0.95	0.94
August 1949	0.95	0.94	0.94	0.95	0.95	0.95
September 1949	0.93	0.91	0.91	0.92	0.92	0.92
June 1954	0.95	0.93	0.93	0.95	0.95	0.95
July 1954	0.96	0.93	0.93	0.96	0.96	0.96
August 1954	0.88	0.85	0.85	0.88	0.88	0.88
September 1954	0.96	0.96	0.96	0.96	0.96	0.96

Table 11

## Thermal Performance Parameters for the Simulated Apartments

U-Value at Summer Design Conditions	Heavyweight Apartment			
	Exterior Wall	Interior Wall	Floor	Ceiling
Btu/(h·ft <sup>2</sup> ·°F)	0.082	0.27	0.18	0.18
W/(m <sup>2</sup> ·°C)	0.47	1.5	1.02	1.02
Thermal Mass				
Btu/(ft <sup>2</sup> ·°F)	16.5	10.7	9.8	9.8
J/(m <sup>2</sup> ·°C)	3.37 X 10 <sup>4</sup>	2.19 X 10 <sup>4</sup>	2.0 X 10 <sup>4</sup>	2.0 X 10 <sup>4</sup>
Weight per Unit Surface Area				
lb/ft <sup>2</sup>	78.3	51.0	46.8	46.8
kg/m <sup>2</sup>	382	249	228	228
Thermal Time Constant				
h	116.6	20.1	35.0	35.0

Table 11 - continued

		Lightweight Apartment			
U-Value at Summer Design		Exterior Wall	Interior Wall	Floor	Ceiling
Conditions					
Btu/(h ft <sup>2</sup> .°F)		0.36	0.20	0.14	0.14
W/(m <sup>2</sup> . °C)		2.03	1.1	0.81	0.81
Thermal Mass					
Btu/(ft <sup>2</sup> .°F)		1.8	2.2	2.1	2.1
J/(m <sup>2</sup> . °C)		2.2 x 10 <sup>3</sup>	4.6 x 10 <sup>3</sup>	4.3 x 10 <sup>3</sup>	4.3 x 10 <sup>3</sup>
Weight per Unit Surface Area					
lb/ft <sup>2</sup>		4.17	6.29	4.92	4.92
kg/m <sup>2</sup>		20.3	30.7	24.0	24.0
Thermal Time Constant					
h		1.28	5.78	8.11	8.11

Table 12

Correlation Coefficients for the Maximum KSU (Inside)  
and Daily Average  $T_{\text{dry-bulb}}$  (Outside)  
for a Heavyweight Apartment, Macon, Georgia

Month-Year	Correlation Coefficients
June 1951	0.92
July 1951	0.96
August 1951	0.86
September 1951	0.95
June 1952	0.91
July 1952	0.94
August 1952	0.93
September 1952	0.91
June 1953	0.82
July 1953	0.93
August 1953	0.96
September 1953	0.95
June 1954	0.93
July 1954	0.94
August 1954	0.84
September 1954	0.91
June 1955	0.93
July 1955	0.70
August 1955	0.88
September 1955	0.89
June 1956	0.94
July 1956	0.77
August 1956	0.89
September 1956	0.95
June 1957	0.93
July 1957	0.91
August 1957	0.92
September 1957	0.98
June 1958	0.86
July 1958	0.84
August 1958	0.92
September 1958	0.96

Table 13

Correlation Coefficients for the Maximum KSU (Inside) and Various  
Other Parameters (Outside) for the Simulated Apartments in Three Geographical Locations<sup>a</sup>

	Maximum Outside T dry-bulb	Average Outside T dry-bulb	Maximum Outside T wet-bulb	Average Outside T wet-bulb	Maximum Outside KSU	Average Outside KSU
<b>Heavyweight Apartment</b>						
Jersey City (June 1949)	0.79	0.89	0.84	0.85	0.82	<u>0.90</u>
Macon (June 1952)	0.70	0.89	0.90	<u>0.94</u>	0.80	0.90
Phoenix (August 1958)	0.47	0.54	0.11	0.038	0.49	<u>0.56</u>
<b>Heavyweight Apartment,</b>						
<b>Walls and Roof External</b>						
Jersey City (June 1949)	0.88	0.95	0.89	0.89	0.91	<u>0.96</u>
<b>Lightweight Apartment</b>						
Jersey City (June 1949)	0.96	0.97	0.91	0.88	<u>0.98</u>	0.97
Macon (June 1952)	0.94	0.92	0.64	0.73	<u>0.96</u>	0.97
Phoenix (August 1958)	0.92	0.92	0.03	-0.11	<u>0.93</u>	0.93
<b>Lightweight Apartment,</b>						
<b>Walls and Roof External</b>						
Jersey City (June 1949)	0.94	0.92	0.86	0.82	<u>0.95</u>	0.92
Macon (June 1952)	<u>0.82</u>	0.60	0.20	0.31	<u>0.77</u>	0.60
Phoenix (August 1958)	0.77	<u>0.78</u>	0.10	-0.10	0.77	<u>0.76</u>

<sup>a</sup> The data are for simulations where the mean radiant temperature was being calculated and air infiltration rate was taken to be 1 air change per hour, constant.



Table 14

## ASHRAE 1% Design Weather Conditions for Selected Cities

<u>Location</u>	<u>T<sub>db</sub>, °F</u>	<u>Range, °F</u>	Average Outside Dry Bulb Temperature, °F
			<u>T<sub>db</sub> - <math>\frac{\text{Range}}{2}</math></u>
Portland, Maine	88.0	22.0	77.0
Concord, N. H.	91.0	26.0	78.0
Hartford, Conn.	90.0	22.0	79.0
West Chester, Pa.	92.0	20.0	82.0
New York, N. Y. (Kennedy)	91.0	16.0	83.0
Jersey City, N. J.	94.0	20.0	84.0
Washington, D. C.	94.0	18.0	85.0
New York, N. Y. (Central Park)	94.0	17.0	85.5

$$^{\circ}\text{C} = (^{\circ}\text{F} - 32) \cdot \frac{5}{9}$$



Appendix A

Derivation of the Equations to Calculate  
the Mean Radiant Temperature Within NBSLD,

In analyzing radiation heat transfer processes where completely diffuse exchange is taking place between two or more gray bodies, the governing equations can be put in a form similar to those governing the behavior of electrical networks. Consequently, the electric analogue is quite often used in solving the problems. Such is the case in this Appendix.

The mean radiant temperature in relation to a person in a given body posture and clothing placed at a given point in a room, is defined as that uniform temperature of the surroundings (considered a black body) which will give the same radiant heat transfer to or from a person as the actual case under study.

Figure A1 is the electric analog of the situation in which a person is exchanging radiation with the surfaces of a room in which it is broken down into only four separate isothermal surfaces. All radiation is assumed to be diffuse, the person is assumed not to exchange radiation with himself, and the following definition of terms applies:

- $\sigma$  = Stefan-Boltzmann constant
- $\rho$  = surface reflectivity
- A = surface area
- $\epsilon$  = surface emissivity
- $\alpha$  = surface absorptivity
- T = temperature (absolute)
- J = radiosity (flow rate of radiant energy per unit area)
- $F_{ij}$  = radiation view factor from surface i to surface j
- $Q_{ij}$  = flow rate of energy exchange occurring by radiation from surface i to surface j

Subscripts

- cl = outer layer of the person's clothing
- p = person
- 1, ..., 4 = surface 1, ..., 4
- e = environment
- MRT = mean radiant temperature

Using Ohm's law, the flow through the left-most leg of the electric circuit is given by:

$$Q_e = \sigma (T_{cl}^4 - J_p) \frac{A_p \epsilon_p}{\rho_p}$$

or since

$$\rho_p = 1 - \alpha_p = 1 - \epsilon_p$$

$$Q_e = (\sigma T_{cl}^4 - J_p) \frac{A_p \epsilon_p}{1 - \epsilon_p} \quad (1)$$

Applying Kirchoff's law at node  $J_p$ :

$$\begin{aligned}
 p Q_e = & (J_p - J_1) A_p F_{p1} + (J_p - J_2) A_p F_{p2} \\
 & + (J_p - J_3) A_p F_{p3} + (J_p - J_4) A_p F_{p4}
 \end{aligned} \quad (2)$$

From the definition of the mean radiant temperature:

$$\begin{aligned}
 p Q_e = & \frac{(\sigma T_{cl}^4 - \sigma T_{MRT}^4)}{\frac{A_p \epsilon_p}{p p} + \frac{1}{A_p F_{pe}} + \frac{1 - \epsilon_e}{A_e \epsilon_e}} \\
 p Q_e = & A_p \epsilon_p \sigma (T_{cl}^4 - T_{MRT}^4)
 \end{aligned} \quad (3)$$

Equating equations (1) and (3):

$$J_p = \sigma T_{cl}^4 \epsilon_p (1 - \epsilon_p) \sigma T_{MRT}^4 \quad (4)$$

Equating equations (2) and (3) and utilizing the derived expression for  $J_p$  (equation (4)):

$$T_{MRT}^4 = \frac{1}{\sigma} (J_1 F_{p1} + J_2 F_{p2} + J_3 F_{p3} + J_4 F_{p4}) \quad (5)$$

In order to use equation (5) for calculating mean radiant temperature, the radiosities  $J_1, J_2, J_3, J_4$  must be determined. Most building materials have a high emittance, and for the calculation, it is often an acceptable approximation to disregard the reflections, i.e., to assume that all the surfaces in the room are black. Equation (5) is thus simplified to:

$$T_{MRT}^4 = T_1^4 F_{p1} + T_2^4 F_{p2} + T_3^4 F_{p3} + T_4^4 F_{p4} \quad (6)$$

As the sum of the angle factors is unity, the fourth power of the mean radiant temperature is seen to be equal to the mean value of the surrounding surface temperatures to the fourth power, weighted according to the size of the respective angle factors.

If there are only relatively small temperature differences between the surfaces of the enclosure, equation (6) can be further simplified by linearizing,

$$T_{MRT} = T_1 F_{p1} + T_2 F_{p2} + T_3 F_{p3} + T_4 F_{p4} \quad (7)$$

In other words, the mean radiant temperature is calculated as the mean value of the surrounding temperatures weighted according to the magnitude of the respective angle factors. Fanger [1]<sup>a</sup> has shown that the error in using equation (7) compared to equation (6) is less than 0.2 °C for most realistic building applications.

In calculating the mean radiant temperature using equation (7), it is necessary to know the angle factors between persons and typical surfaces. These are sometimes difficult to calculate and therefore an additional rough approximation has often been used. The mean radiant temperature is calculated as the mean temperature of all the surfaces in the enclosure:

$$T_{MRT} = \frac{T_1 A_1 + T_2 A_2 + T_3 A_3 + T_4 A_4}{A_1 + A_2 + A_3 + A_4} \quad (8)$$

<sup>a</sup>Reference numbers refer to references listed at the end of this Appendix.

This is equivalent to assuming:

$$F_{p1} = \frac{A_1}{A_1 + A_2 + A_3 + A_4}$$

$$F_{p2} = \frac{A_2}{A_1 + A_2 + A_3 + A_4}$$

·  
·  
·  
·

The authors compared the results of calculating  $T_{MRT}$  using equations (7) and (8) for a person located in the center of the masonry building apartment described in section 6. and the results were different by less than 0.1°C.

#### References

1. P. O. Fanger, Thermal Comfort, Danish Technical Press, Copenhagen, 1970.
2. E. M. Sparrow and R. D. Cess, Radiation Heat Transfer, Wadworth Publishing Company, Belmont, California, 1970.



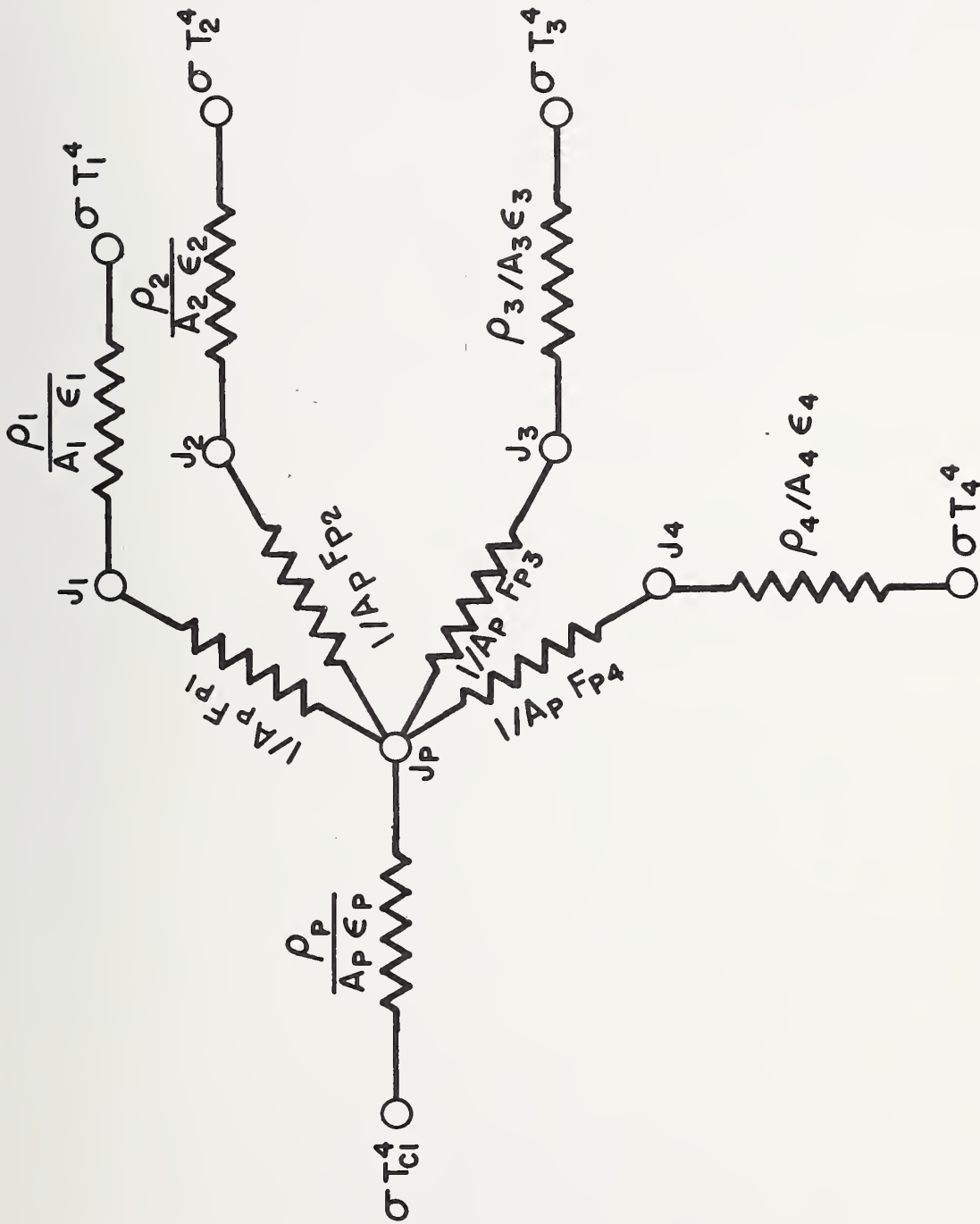


Figure A1 Electric Analog for Radiation Exchange Between a Person and His Enclosure



Appendix B

A Review of Comfort and Physiological Indices

In this Appendix, the methods of computation for several of the analytically determined comfort indices are discussed. The expressions for heat transfer rate between the subject and environment by convection, radiation, etc., are given at the end of each section where appropriate. Unless otherwise specified, the following nomenclature applies to the various relations:

- $A_{DU}$  = body surface area,  $m^2$
- $\alpha$  = coefficient related to the transfer of energy from clothing by convection (approximately 11.6 for 0.6 clo standard clothing)
- $f_{cl}$  = ratio of the surface area of the clothed body to the nude body (= 1.1 for 0.6 clo standard clothing)
- $F_{cl}$  = a factor that measures the efficiency for the passage of dry heat from the skin surface through the clothing to the environment (= .58 for 0.6 clo clothing)
- $f_{eff}$  = the ratio of the effective radiation area of the clothed body to the surface area of the clothed body (0.65 for seated position and 0.75 for standing)
- $F_{pcl}$  = permeation efficiency factor for water vapor evaporated from the skin surface through clothing to the ambient air (= 0.82 for 0.6 clo clothing)
- $h_c$  = convection coefficient,  $kcal/(h \cdot m^2 \cdot ^\circ C)$
- $h_r$  = radiation coefficient,  $W/(m^2 \cdot ^\circ C)$ , = 5.23 in the ET\* model
- $I_{cl}$  = conduction resistance value for clothing, clo
- $M$  = metabolic heat production, kcal/h
- $P$  = clothing coefficient (approximately 13.0 for standard clothing)
- $P_a$  = vapor pressure in ambient air, mm Hg
- $P_{sk}$  = saturated vapor pressure corresponding to skin temperature, mm Hg
- $T_a$  = ambient air temperature,  $^\circ C$
- $T_{cl}$  = clothing surface temperature,  $^\circ C$
- $T_{cr}$  = core or deep body temperature,  $^\circ C$
- $T_{MRT}$  = mean radiant temperature,  $^\circ C$
- $T_{sk}$  = skin surface temperature,  $^\circ C$
- $v$  = air velocity, m/s

#### Old Effective Temperature (ET)

Undoubtedly the most familiar of all comfort indices is the American Society of Heating, Refrigerating and Air Conditioning Engineers' Effective Temperature. The scale was first established in the 1920's by Houghten and Yaglou [1]<sup>a</sup>. Subjects wearing clothing having an unspecified insulation value<sup>b</sup> were passed between test chambers in which the temperature, air

<sup>a</sup>Reference numbers refer to references listed at the end of this Appendix.

<sup>b</sup>At the time this particular index was developed, the analysis of human comfort had not progressed to the point that insulation values for clothing ensembles were being given.

velocity, and humidity were maintained at specified levels and were asked to describe their feeling immediately upon entering the new environment. The results are shown in Figure B1 where lines of constant thermal sensation are shown plotted on a standard psychrometric chart. The experiments were conducted for a large range of air velocities; however, the data shown here is for an air velocity of less than 20 fpm<sup>a</sup> (0.1 m/s). The lines of constant thermal sensation were arbitrarily given numerical values corresponding to the dry-bulb temperature at which the line intersected the saturation curve (100% relative humidity). If the dry-bulb temperature were a sole indicator of thermal comfort according to this scale, the lines would run vertically. The data therefore indicates that as the relative humidity is increased, the temperature has to be decreased to maintain the same feeling. This is natural since cooling by sweat evaporation is restricted somewhat as the relative humidity increases.

This scale originally did not take into account the effect of radiation to or from room walls where the walls' temperature is maintained at values quite different from the room air. However, a correction was proposed later [2] in order to account for this effect. The ET scale continues to be accepted as valid in the very hot region where man's cooling rate depends almost entirely on his sweat evaporation but has been abandoned as inaccurate in the comfort region or the region of most interest to this study.

As a result of the apparent disagreement between field tests and the lines of constant thermal sensation or effective temperature at the moderate temperatures, ASHRAE undertook an additional study at their research laboratory in 1960 and the results are shown in Figure B2. In this study [3], subjects wore light indoor clothing and were seated at rest. Room surfaces were held at the same temperature as the room air in all tests, and the air motion in the space was 20 fpm (0.1 m/s) or less. The thermal sensation votes used in analyzing the test data were those which were cast in the chamber at the end of the three hour occupancy period. These lines show the conditions under which subjects cast votes of 3, 4, 5, or 6, indicating sensations of slightly cool, comfortable, slightly warm, and warm respectively. It is evident from Figures B1 and B2 that the old effective temperature index predicts a considerably greater effect of relative humidity on the thermal sensation feeling than do the lines determined by Koch, Jennings, and Humphreys [3]. In defense of the old effective temperature, it may be explained that the two groups of data apply to different conditions. The effective temperature lines indicate a person's feeling immediately after entering the conditioned space, while the lines of Figure B2 are for people who have been in the conditioned space for approximately three hours and are in equilibrium with their environment.

### Resultant Temperature

In 1948, Missenard [4] proposed an index called the resultant temperature. Its development was motivated by the fact that the effective temperature was not based on experiments where thermal equilibrium was achieved between the human body and the environment. The experiments on which the resultant temperature was based were conducted with about six subjects in a psychrometric chamber with a duration of exposure greater than was used in the experiments for the effective temperature. The resultant temperature is identical in structure with the effective temperature and is shown in Figure B3 for clothed subjects exposed to an air velocity of 0.1 m/s (20 fpm). The resultant temperature shows that thermal sensation is much less dependent on humidity than it was with effective temperature. However, the results still indicate more of a dependence of humidity in the moderate temperature range than do the comfort votes of Koch, et. al.

### Kansas State Index

Perhaps the most definitive experimental study on thermal comfort is one conducted on over 1600 college students at Kansas State University over the past several years [5, 6]. The students were exposed (over a 3 hour period) to a uniformly heated or cooled environment (wall temperatures identical to the air temperature) with moderate air velocities and asked to vote on a scale from 1 to 7 which ranged from cold to hot:

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<sup>a</sup>For purposes of this study, the data for all the indices described will be for very nominal air velocities (i.e., 20 fpm or 0.1 m/s) since higher velocities very rarely occur in residences.

1. cold
2. cool
3. slightly cool
4. comfortable
5. slightly warm
6. warm
7. hot

All subjects, males and females alike, were clothed in cotton twill shirts and trousers. The shirts were worn outside of the trousers. The subjects wore the underwear they had on when reporting for this test, which usually consisted of cotton undershorts or jockey shorts for the men and brassieres and underpants for the women. All other clothing, including T-shirts, girdles, slips, etc., were removed. The subjects wore cotton sweat socks without shoes. The net insulating value for the clothing ensemble, as computed by means of an electrically heated copper manikin [7] has been determined to be 0.6 clo<sup>a</sup> which has been generally accepted as the standard clothing for thermal comfort studies.

Even though the results are available for men and women separately and also for the votes taken at each half an hour for the entire 3 hours of exposure, the data shown in Figure B4 is an average for the votes of men and women taken together at the end of the 3 hours.

Until very recently, the results of comfort studies were represented as lines on a psychrometric chart as done above. As Rohles of Kansas State University pointed out in 1969 [8], "from a purely operational point of view this [type of representation] is totally impractical since there is nothing in the way of a range or plus or minus limit about the line. Moreover, the requirement for limits of this type becomes more apparent when we consider the data used in the construction of the line itself are based on value judgments of unknown reliability". As an alternative, Rohles [9, 10] proposed zones or envelopes of the thermal comfort.

The Modal Comfort Envelope (MCE) was derived purely by trial and error from the distribution of thermal sensations from the above-mentioned study with 1600 subjects. The set of 15 conditions which has been identified as the MCE are: 80 °F (26.7 °C) at 15, 25, 35, and 45% RH; 78 °F (25.6 °C) at 15, 25, 35, 45, 55 and 65% RH; and 76 °F (24.4 °C) at 45, 55, 65, 75 and 85% RH. The distribution of thermal sensations within this envelope after an exposure of 3 hours showed that none of the subjects voted hot or cold; approximately 3% were warm and cool and 94% reported a sensation of slightly cool, comfortable, or slightly warm. The mean sensation was 4.0 or "comfortable" with a standard deviation of 0.72.

Besides defining the thermal environment in which sedentary man is comfortable, the MCE forms a prescribed set of temperature-humidity conditions that can be used for studying the thermal sensation as a function of such factors as age, clothing, activity, radiant temperature, air movement, color of the surroundings, and illumination level. As such, it replaces the traditional approach to studies in this area which arbitrarily select temperatures which are equally spaced physically yet totally unequal from the standpoint of the thermal sensation.

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<sup>a</sup>1 clo represents a measured resistance to heat transfer of the clothing ensemble of 0.18 (m<sup>2</sup> · h · °C) cal (0.88 (ft<sup>2</sup> · h · °F)/Btu or equivalent of an overall heat transfer coefficient = 1.13 Btu/(h · ft<sup>2</sup> · °F)).



The Modal Comfort Envelope has been used in two studies to determine the independence of the environmental constituents that affect the thermal sensation. In the first application, the thermal sensations of elderly subjects were compared to those of college students [11], and in the second study the MCE was used to determine the influence of clothing and temperature on sedentary comfort [12].

The MCE was also used as a reference in defining the KSU-ASHRAE Comfort Envelope in the 1972 ASHRAE Handbook of Fundamentals [13]. This envelope is represented in Figure B5 as the quadrilateral having its points at 80 °F (26.7 °C) 45% RH; 80 °F (26.7 °C) 15% RH; 76 °F (24.4 °C) 85% RH; and 76 °F (24.4 °C) 45% RH.

For purposes of comparison, the shaded envelope on the chart defines the limits of the conditions prescribed in ASHRAE Standard 55-74 [14]. Whereas the KSU-ASHRAE Comfort Envelope applies to subjects wearing clothing whose insulation value is 0.6 clo, the ASHRAE Comfort Standard applies to subjects wearing 0.8 to 1.0 clo. In addition, the KSU-ASHRAE Comfort Envelope applies to sedentary activity whereas the ASHRAE Standard applied to office work which is slightly greater than sedentary. The differences in activity level and clothing account for the differences in the two envelopes. The area where the two envelopes overlap is recommended as the "design conditions for comfort" [15].

#### Predicted Mean Vote and Predicted Percentage of Dissatisfied

One of the most significant attempts to predict analytically the thermal interaction between man and his environment is presented by P. O. Fanger of the Technical University of Denmark in his recent book Thermal Comfort [16]. He begins by pointing out the most important variables which influence the condition of thermal comfort:

1. activity level (heat production in the body)
2. thermal resistance of the clothing (clo-value)
3. air temperature (dry-bulb)
4. mean radiant temperature
5. relative air velocity
6. water vapor pressure in ambient air

The basis of his analysis is the so-called general comfort equation which defines all combinations of the variables which will create thermal comfort. Its specific form is as follows:

$$M - E_{diff} - E_{sw} - E_{res} - D = K = R + C \quad (1)$$

where

M = the internal heat production in the human body

$E_{diff}$  = the energy loss by water vapor diffusion through the skin

$E_{sw}$  = the energy loss by evaporation of sweat from the surface of the skin

$E_{res}$  = the latent respiration heat loss

D = the dry respiration loss

$K$  = the heat transfer from the skin to the outer surface of the clothed body (conduction through the clothing)<sup>a</sup>

$R$  = the heat loss by radiation from the outer surface of the clothed body

$C$  = the heat loss by convection from the outer surface of the clothed body

The double equation expresses that the internal heat production  $M$  minus the heat loss by evaporation from the skin ( $E_{diff} + E_{sw}$ ) and by respiration ( $E_{res} + D$ ) is equal to the heat conducted through the clothing  $K$  and dissipated at the outer surface of the clothing by radiation and convection ( $R + C$ ). It is assumed that the evaporation corresponding to  $E_{sw}$  and  $E_{diff}$  takes place at (or underneath) the skin surface.

After formulating expressions for each component in the above equation (see the end of this section) and substituting them into equation (1), two algebraic equations result in the following 9 unknowns:

$M$  - (defined previously)

$T_s$  - skin surface temperature

$P_w$  - water vapor pressure in the ambient air

$E_{sw}$  - (defined previously)

$T_a$  - ambient air dry-bulb temperature

$T_{cl}$  - clothing surface temperature

$I_{cl}$  - insulation value of the clothing

$T_{MRT}$  - mean radiant temperature of the environment

$v$  - the relative air velocity

Six of the unknowns ( $M$ ,  $P_w$ ,  $T_a$ ,  $I_{cl}$ ,  $V$ , and  $T_{MRT}$ ) can be considered as controllable or specified for any particular subject--environment situation. Two of the remaining unknowns are eliminated by what may be considered Fanger's most questionable assumption. During studies at Kansas State University on college students, data was obtained for mean skin temperature and evaporative heat loss of the subjects while they reported being comfortable conducting various activities (different  $M$ 's).  $E_{sw}$  and  $T_s$  were plotted individually as a function of the metabolic production and even though the data was rather widely scattered, linear equations

$$T_s = f(M) \quad (2)$$

and

$$E_{sw} = f(M) \quad (3)$$

were determined by regression analysis. The procedure then used was to specify 5 of the 6 controllable or specified quantities ( $M$ ,  $P_w$ ,  $T_a$ ,  $I_{cl}$ ,  $v$ , and  $T_{MRT}$ ), and use the 4 equations (1, 2, and 3) to determine the remaining four unknowns, one of which is the sixth of the controllable parameters that would give thermal comfort. The results are presented in the form of comfort charts.

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<sup>a</sup>The resistance value for the clothing is determined in such a way that it accounts for the heat transfer from the nude portion of the body as well.

Having determined the conditions for optimum thermal comfort, Fanger recognized the need for being able to evaluate an existing room climate and quantify its deviation from the comfort condition. A similar scale to the one used in the Kansas State studies were chosen:

- 3 cold
- 2 cool
- 1 slightly cool
- 0 neutral
- +1 slightly warm
- +2 warm
- +3 hot

The numerical values however are lower by 4. A scale is thus obtained which is easier to remember, as it is symmetrical around the zero point, so that a positive value corresponds to the warm side and a negative value to the cold side of neutral. He then proposed that the thermal sensation values, to be called the Predicted Mean Vote (PMV), would be a function of the thermal load of the body, defined as the difference between the internal heat production and the heat loss to the actual environment for a man hypothetically kept at the comfort values of the mean skin temperature and the sweat secretion of the actual activity level.

$$PMV = f (M - E_{diff} - E_{sw} - E_{res} - D - R - C) \quad (4)$$

The nature of equation (4) enabled Fanger to use the same component expressions as in the general comfort equation. The particular form of the function was determined from analyzing the Kansas State studies once again as well as similar experiments conducted at the Technical University of Denmark.

Values of the predicted mean vote (PMV) are shown on the psychrometric chart in Figure B6. The data was calculated assuming a resting metabolic rate ( $M = 50 \text{ kcal/h.m}^2$ ), an air velocity of 0.1 m/s, a mean radiant temperature equal to the ambient air temperature, and a clothing insulation value of 0.6 clo. In Figure B7 the results are compared with the experimentally determined KSU comfort vote. As can be seen the agreement is excellent for the comfort line ( $KSU = 0$ ,  $PMV = 4$ ) but not so good for environmental conditions outside of the comfort range.

An advantage of an analytical model such as this is the capability of observing the effect of one of the six controllable parameters without having to conduct extensive experiments. For example, it may be unrealistic to determine air conditioning criteria using subjects that wear the standard 0.6 clo clothing ensemble. Certainly in hot weather people would be more inclined to wear lighter clothing such as shorts and an open neck shirt with short sleeves. Data for this type of clothing ensemble ( $clo = 0.25$ ) is shown in Figure B8 and compared with the standard Kansas State clothing ensemble in Figure B9. The comparison shows what one might intuitively expect. With lighter clothing, subjects would report comfort at 4 or 5 °F (2.2 or 2.8 °C) warmer temperature. It would be expected that they would vote cool at a somewhat higher temperature also (approximately 6 °F or 3.3 °C). However, both subjects would vote hot at approximately the same temperature and relative humidity.

Instead of just giving the predicted mean vote as an expression for the thermal environment, Fanger felt it might be even more meaningful to state what percent of persons can be expected to be decidedly dissatisfied since this can readily be interpreted by both the engineer and the layman. This same concept has been proposed more recently by Nevins and McNall [17]. After choosing the limits of -2 and +2 for being dissatisfied on the cold and hot side respectively, the American and Danish experiments already mentioned were again analyzed to determine the percent of the subjects voting cool or below and warm or above at each environment condition. The same relationship was assumed to hold between PMV and the new factor, predicted percentage of dissatisfied (PPD). The exact relation is given below.

The relevant mathematical relations used by Fanger in his work were:

Rate of Heat Loss by Convection (C):

$$C = A_{DU} f_{cl} h_c (T_{cl} - T_a) \text{ kcal/h}$$

$$h_c = 2.05 (T_{cl} - T_a)^{0.25} \text{ for } 2.05 (T_{cl} - T_a)^{0.25} > 10.4 \sqrt{v}$$

$$= 10.4 \sqrt{v} \text{ for } 2.05 (T_{cl} - T_a)^{0.25} < 10.4 \sqrt{v}$$

Rate of Heat Loss by Radiation (R):

$$R = 4.8 \times 10^{-8} A_{DU} f_{cl} f_{eff} [(T_{cl} + 273)^4 - (T_{MRT} + 273)^4] \text{ kcal/h}$$

Rate of "Dry" Heat Loss in Respiratory Passages (D):

$$D = .0014 M (34 - T_a) \text{ kcal/h}$$

Rate of Energy Loss Due to Evaporative Cooling in Respiratory Passages ( $E_{res}$ ):

$$E_{res} = .0023 M (44 - P_a) \text{ kcal/h}$$

Rate of Energy Loss Due to Evaporative Cooling, Normal Skin Diffusion ( $E_{diff}$ ):

$$E_{diff} = .35 A_{DU} (43 - 0.061 \frac{M}{A_{DU}} - P_a) \text{ kcal/h}$$

Rate of Energy Loss Due to Evaporative Cooling, Regulatory Sweat Production ( $E_{sw}$ ):

$$E_{sw} = .42 A_{DU} (\frac{M}{A_{DU}} - 50) \text{ kcal/h}$$

Rate of Heat Conduction Through Clothing (K):

$$K = A_{DU} \frac{T_{sk} - T_{cl}}{.18 I_{cl}} \text{ kcal/h}$$

Relation Between PMV and Body Heat Load (L):

$$PMV = [.352 e^{-.942 (M/A_{DU})} + .032] L$$

Relation for PPD:

A second order equation was fit to the tabular data given by Fanger for the Predicted Percentage of Dissatisfied (due to heat only) as a function of PMV:

$$PPD = 1.63 + 10.98 (PMV) + 13.41 (PMV)^2$$

#### New Effective Temperature (ET\*)

The other major analytical contribution to the field of thermal comfort to be mentioned in this paper is a transient heat transfer model presented by Gagge, Stolwijk, and Nishi [18]. The model differs most significantly from Fanger's in the fact that physiological responses have included the effect of vascular restrictions and dilation on the blood flow to the skin and regulatory sweating proportional to a deep body temperature deviation from some predetermined set point. The human body is pictured as composed of two distinct parts; a central core and skin shell. An energy balance is written for each part:



the rate of energy increase of the skin shell = the net rate of energy transfer from the core to the skin + the net rate of energy transfer from the environment to the skin

and

the rate of energy increase of the central core = the rate of energy generation (metabolic production in the core) + the net rate of energy transfer from the skin to the core + the net rate of energy transfer from the environment to the core

or in equation form

$$M_{sk} C_{sk} \frac{dT_{sk}}{d\tau} = Q_{con} + Q_{bl} - E_{diff} - E_{rsw} - R - C \quad (5)$$

and

$$M_{cr} C_{cr} \frac{dT_{cr}}{d\tau} = M - Q_{con} - Q_{bl} - E_{res} \quad (6)$$

where

$M_{sk}$  = mass of the skin shell

$C_{sk}$  = specific heat of the skin shell

$T_{sk}$  = temperature of the skin shell

$M_{cr}$  = mass of the central core

$C_{cr}$  = specific heat of the central core

$T_{cr}$  = temperature of the central core

$\tau$  = time

$Q_{con}$  = heat transferred by conduction from the core to the skin  
(a function of  $T_{cr}$  and  $T_{sk}$ )

$Q_{bl}$  = energy transferred by blood flow from the core to the skin  
(a function of  $T_{cr}$  and  $T_{sk}$ )

$E_{diff}$  = the energy loss by water vapor diffusion through the skin

$E_{rsw}$  = the energy loss by evaporation as a result of regulatory sweat production (a function of  $T_{cr}$  and  $T_{sk}$ )<sup>a</sup>

$R$  = the heat loss by radiation from the skin to the environment

$C$  = heat loss by convection from the skin to the environment

<sup>a</sup>This particular component is extremely important in the performance of the model yet the expression doesn't agree with all physiological observations reported in the literature. A discussion of this discrepancy is given in Appendix C.

M = metabolic heat production in the core

$E_{res}$  = the latent respiration loss from the lungs

The form of the differential equation implies a lumped capacity analysis or in other words; the temperature of the skin and core are assumed uniform throughout at every instant. The model is no doubt unrealistic in this respect, since the temperature can and does often vary widely within the body. Recently another dynamic model [19] has been developed in which 25 nodes (instead of 2 in the present model) are used to represent the thermal characteristics of the body, with four nodes each representing the head, trunk, arms, hands, legs and feet. The twenty-fifth node represents the central blood.

After formulating expressions for the various energy components and choosing appropriate numerical values for the various parameters (see below), the two differential equations are solved simultaneously (numerically on a digital computer) to predict the time variation of the core and skin temperatures when the controllable parameters mentioned previously are specified. The model predicts a response that levels off at the end of approximately one hour. Once  $T_{cr}$  and  $T_{sk}$  have been determined, it is possible to work back through the analysis and calculate the regulatory sweat production (at the end of one hour), associated with the given environmental-human conditions. Mass transfer theory is then used to calculate the maximum possible evaporation cooling for given skin temperature and ambient temperature and vapor pressure. The ratio of calculated regulatory sweat evaporation to the maximum possible is given the notation of skin wettedness. It is then postulated (as a result of experimental observation) that in warm environments, various conditions giving the same skin wettedness will also cause the same thermal sensation or feeling of warmth or coolness. This particular point is debatable and is the subject of discussion in Appendix C.

Lines of constant skin wettedness at the end of one hour's exposure are shown in Figure B10 for a resting subject ( $58.2 \text{ W/m}^2$ ) with the standard clothing (0.6 clo) subjected to a small air velocity. This model has been proposed to ASHRAE and accepted as properly predicting the lines of constant thermal sensation. Consequently the lines in Figure B10 are labelled as lines of New Effective Temperature (ET\*). Actually the model predicts zero regulatory sweating at 77 °F (25 °C) and 50% R.H. or in other words, the 77 ET\* lines correspond to a skin wettedness of 0. Effective temperature lines below this temperature are simply drawn as parallel to the 77 ET\* line. The numerical values associated with the lines were determined by using the dry-bulb temperature at the intersection of the constant skin wettedness line and the 50% relative humidity curve. This in contrast to the original effective temperature where experimentally determine lines of constant thermal sensation were given numerical values corresponding to the dry-bulb temperature where the lines intersected the saturation or 100% relative humidity curve. The labelling of the new effective temperature seems more reasonable since the values will more closely correspond to dry-bulb temperatures experienced in everyday living. However, the confusion that results from the two effective temperature scales can be seen by observing Figure B11. The numerical values of the two scales are very widely separated. Since the old effective temperature was considered standard for almost 50 years, many guidelines and comfort limits will have to be reevaluated in terms of the new scale.

By observing the new scale, one sees that the dependence of thermal sensation on relative humidity at the higher temperatures is approximately the same as with the old effective temperature. This is quite acceptable since the old effective temperature scale was considered accurate at these temperatures. However, at temperatures near the comfort zone, the new model predicts a much less dependence on relative humidity which is in good agreement with the most recent studies. These two factors no doubt contributed significantly to the new scale's acceptance by ASHRAE.

The component expression used by Gagge, et. al. are as follows:

Rate of Heat Loss by Convection (C):

$$C = h_c (T_{sk} - T_a) F_{cl} \text{ W/m}^2$$

$$h_c = 11.6 v^{0.5} \text{ W/(m}^2 \cdot \text{°C)}$$



Rate of Heat Loss by Radiation (R):

$$R = h_r (T_{sk} - T_a) F_{pcl} \text{ W/m}^2$$

Rate of Energy Loss Due to Evaporative Cooling in Respiratory Passage ( $E_{res}$ ):

$$E_{res} = .0023 M (44 - P_a) \text{ W/m}^2$$

M = metabolic heat production,  $\text{W/m}^2$

Rate of Energy Loss Due to Evaporative Cooling, Normal Skin Diffusion ( $E_{diff}$ ):

$$E_{diff} = 0.06 \cdot 2.2 h_c (P_{sk} - P_a) F_{pcl} \text{ W/m}^2$$

$h_c$  = convection coefficient given in the previous section,  $\text{W}/(\text{m}^2 \cdot ^\circ\text{C})$

Rate of Energy Loss Due to Evaporative Cooling, Regulatory Sweat Production ( $E_{rsw}$ ):

$$E_{rsw} = 70 (T_{cr} - 36.6) (T_{sk} - 34.1) \text{ W/m}^2$$

for  $T_{cr} \geq 36.6 \text{ } ^\circ\text{C}$  and  $T_{sk} \geq 34.1 \text{ } ^\circ\text{C}$

$$E_{rsw} = 0.0$$

for  $T_{cr} < 36.6 \text{ } ^\circ\text{C}$  or  $T_{sk} < 34.1 \text{ } ^\circ\text{C}$

Maximum Evaporative Cooling Rate Possible ( $E_{max}$ ):

$$E_{max} = 2.2 h_c (P_{sk} - P_a) F_{pcl} \text{ W/m}^2$$

$h_c$  = convection coefficient given in the previous section,  $\text{W}/(\text{m}^2 \cdot ^\circ\text{C})$

### Heat Stress Index

The heat stress index was developed by Belding and Hatch at the University of Pittsburgh and first published in 1955 [20]. The postulation that forms the basis of their index is as follows: the metabolic production of the body minus the energy that can be given off by radiation and convection to the surroundings equals a quantity of energy that must be given off by sweat evaporation in order to maintain thermal equilibrium with the environment. Consequently the expression for the required evaporative cooling ( $E_{req}$ ) is

$$E_{req} = M - R - C \quad (7)$$

As mentioned previously, for a given skin temperature and ambient air temperature and vapor pressure, mass transfer theory can be used to calculate the maximum evaporative cooling possible. The heat stress index is defined as being equal to the ratio of the two quantities  $E_{req}/E_{max}$  multiplied by 10. Belding and Hatch assumed a constant skin temperature of  $35 \text{ } ^\circ\text{C}$  and used the most up-to-date (at that time) expressions for radiation and convection heat loss from the body to calculate values of the index and present them in nomographs as functions of the metabolic production and environmental conditions. In addition, physiological and hygienic implications of 8 hour exposures to various heat stresses were given and are shown in Table B1.

Calculations have been made using the original expressions for radiation and convection losses and maximum evaporative cooling from the body for a resting person subjected to a uniform environment with an air velocity of 20 fpm (0.1 m/s). The results are shown in Figure B12 in the form of lines of constant heat stress index. Notice that using these expressions sweat evaporation to maintain body equilibrium is not required until the environment reaches approximately 82 °F (27.8 °C). This is in definite contrast to Gagge's effective temperature model which shows regulatory sweat production starting at approximately 5 °F (2.2 °C) lower. The expressions were reevaluated and updated in 1966 by McKarns and Brief [21]. ASHRAE recommends in their 1972 Handbook of Fundamentals [13] the calculation of the index using the same expressions for R, C and  $E_{max}$  that were used in the new effective temperature model. In addition, expressions for dry and latent heat losses from the lung passages have been subtracted from the right side of equation (7) and the results of new calculations are shown in Figure B13 and compared with the original lines of constant heat stress in Figure B14. The latest computations seem to be reasonable since the evaporative cooling as a result of sweat production is seen to be necessary at a temperature as low as 74 °F (23.3 °C).

In retrospect, it can be seen that the quantity called skin wettedness in the new effective temperature model is very similar to a heat stress index. Instead of dividing the maximum possible evaporative cooling rate into a required evaporative cooling rate, the maximum value is divided into a sweat cooling rate that is predicted from known physiological responses.

As stated above, the expressions for C, R,  $E_{res}$ ,  $E_{diff}$ , and  $E_{max}$  used in computing the heat stress index according to ASHRAE [13] are identical with those used in computing ET\*. In addition, the expression for D was:

$$D = .0014 M (34 - T_a) W/m^2$$

$M = \text{metabolic heat production, } W/m^2$

The component equations used in calculating HSI (original) are as follows:

Rate of Heat Loss by Convection (C):

$$C = 2 v^{0.5} (95 - T_a) \text{ Btu/h}$$

where

$v = \text{air velocity, fpm}$

$T_a = \text{ambient air temperature, } ^\circ\text{F}$

Rate of Heat Loss by Radiation (R):

$$R = 22 (95 - T_{MRT}) \text{ Btu/h}$$

$T_{MRT} = \text{mean radiant temperature, } ^\circ\text{F}$

Maximum Evaporative Cooling Rate Possible ( $E_{max}$ ):

$$E_{max} = 10 v^{.4} (P_{sk} - P_a) \text{ Btu/h}$$

$v = \text{air velocity, fpm}$

#### Thermal Comfort When Equilibrium is Maintained by Sweating

Before publishing a new effective temperature model, Gagge and his associates published still another model for indicating thermal comfort [22] that is very similar to the heat stress index. The cooling due to evaporation of sweat production necessary to maintain body thermal equilibrium is determined by subtracting the body heat loss by radiation, convection, latent loss from the lung passages and the loss due to evaporation of moisture diffusing

through the skin from the metabolic heat production. The resulting required evaporative cooling is divided by the maximum possible and then multiplied by 100 to give a factor "percentage of wettedness".

The main difference between this model and the two previous ones mentioned is that the skin temperature is not held constant as in the case of heat stress index or predicted from known physiological responses as with the new effective temperature model, but rather assumed to be a polynomial function of the environment temperature (see below). The function was determined by fitting an equation (by regression analysis) to experimental data that was determined at the John B. Pierce Foundation. Computations were made using the model and the results are shown in Figure B15 for a resting person with the standard clothing (0.6 clo) subjected to a uniform environment with an air velocity of 20 fpm (0.1 m/s).

The equations used in computing the values of C, R,  $E_{res}$ , and  $E_{max}$  were identical to those used in computing ET\*. In addition, the following two expressions were used:

Rate of Energy Loss Due to Evaporative Cooling, Normal Skin Diffusion ( $E_{diff}$ ):

$$E_{diff} = .35 (P_{sk} - P_a) F_{pcl} W/m^2$$

Relation for Skin Temperature as a Function of Ambient Air Temperature:

$$T_{sk} = 25.49 + .249 T_a \text{ } ^\circ\text{F}$$

#### Index of Thermal Stress

Givoni [23, 24] has done extensive work over the past few years on measuring and evaluating heat stress. Having compared actual response with the predictions of many models and found much disagreement, he developed his own "index of thermal stress" (ITS) which according to additional extensive experiments conducted by Givoni correctly predicts the physiological strain imposed on resting and working people by metabolic and environmental factors. The index is structured exactly like the heat stress index with two important differences. An expression has been included for the radiant heat load due to solar radiation so that the index can predict responses for people working or resting outdoors. This is not directly applicable to this study but certainly makes a useful addition to the field of heat stress evaluation. The other difference is a factor called cooling efficiency of sweating (f) and is included in the equation as follows:

$$E_{req} = [M - R - C] \frac{1}{f} \quad (8)$$

The concept is that where other indices assume all the sweat produced or required is evaporated and provides cooling for the body, this may not be true. For example, some of the evaporation could occur in the clothing and not result directly in cooling for the body. Calculations using Givoni's expressions have been made and are shown in Figure B16. The data used was for a resting person ( $M = \frac{100 \text{ kcal}}{h}$ ), subjected to a uniform environment with an air velocity of .1 m/s. The clothing ensemble chosen (affects the radiation and convection expression) was very similar to the Kansas State standard clothing. It should be noted that the upper limit for comfort (according to Givoni) is associated with an evaporative loss of 60 g/h and that distinct thermal discomfort is experienced progressively as the sweat rate is elevated above 100 g/h.

Even though Givoni states that the model predicts a sweat rate that is in agreement with experimentally measured rates, the results shown in Figure B16 appear questionable. Sweating is seen necessary at approximately 64 °F (17.8 °C). The index does show small dependence on relative humidity at the lower temperatures and somewhat more dependence at the higher temperature which agrees with the new effective temperature model. However, it should be remembered that what is shown in the figure is sweat rate and not the ratio between the sweat rate and some maximum possible.

The equations used to calculate the values of ITS are as follows:

Rate of Heat Loss by Convection (C):

$$C = \alpha v^{0.3} (35 - T_a) \text{ kcal/h}$$

Rate of Heat Loss by Radiation (R):

accounted for in the convection term by replacing  $T_a$  by  $T_{MRT}$

Maximum Evaporative Cooling Rate Possible ( $E_{max}$ ):

$$E_{max} = P v \cdot^3 (42 - P_a) \text{ kcal/h}$$

Relation for Sweating Efficiency:

$$\frac{1}{f} = e^{0.6} (E_{req}/E_{max} - 0.12)$$

#### Predicted Four Hour Sweat Rate

The P4SR index was developed by McArdle and his colleagues during World War II at the Royal Naval Research Establishment [25]. Sweat rate was measured for fit, young men dressed in shorts only or overall and shorts when subjected to many different combinations of temperature, humidity, and air velocities for four hour periods. The results were presented in the form of nomographs and have been adapted to a psychrometric chart as shown in Figure B17. The particular conditions for this chart are a metabolic production of 54 kcal/(m<sup>2</sup> · h), a uniform radiation environment (mean radiant temperature equal to air temperature), and an air velocity of 10 fpm (0.05 m/s). As was the case with the original heat stress index, sweat production is shown to start only after the temperature has reached approximately 80 °F (26.7 °C). Based on the experiments, a limit of 3.0 was established as the upper tolerable limit for daily exposure.

#### Wet-Dry Index

In 1957 Lind and Hellon [26] proposed the use of the Oxford Index or wet-dry index to assess the severity of hot climates. It is simply a combination of the wet-bulb and dry-bulb temperatures (°F) according to

$$WD = 0.85 T_{wb} + 0.15 T_{db}$$

The extreme dependence on relative humidity is obvious and is shown in Figure B18. Due to its simplicity it has been used quite often in setting limits or correlating data in extremely hot and wet conditions where there is no radiant stress and very low air velocity.

#### Temperature-Humidity Index

Another index very similar to the Oxford Index is one called the temperature-humidity index defined by

$$THI = 0.4 (T_{db} + T_{wb}) + 4.8$$

where all values are in °C. This index like the last, attempts to combine the effect of temperature and humidity in environments where radiant stress and air velocity are not important. Figure B19 shows that the THI index is much less dependent on humidity than the

W-D index was. As an example of its use, Bridger and Helfand [27] correlated death rates during the 1966 heat wave in St. Louis and found that when the 24 hour average of the THI was greater than 81 °F (27 °C), there was an usually large number of deaths due to heat stroke.

Table B2 has been included here as a summary to give the range of application of the various indices that have been discussed.



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EFFECTIVE TEMPERATURE (ET)

$$^{\circ}\text{C} = (^{\circ}\text{F} - 32) \cdot \frac{5}{9}$$

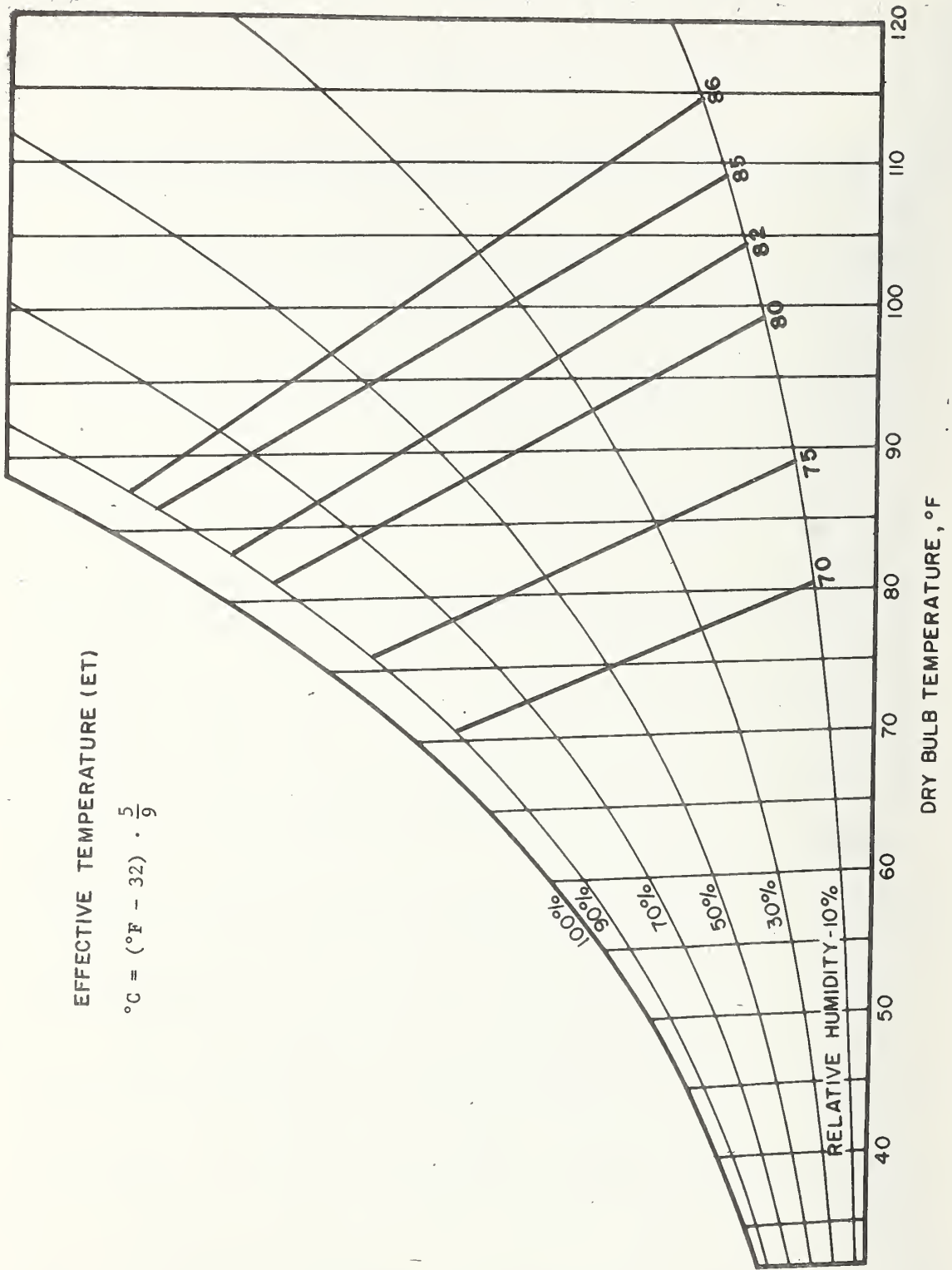


Figure B1 Lines of Constant Effective Temperature (ET) on a Psychrometric Chart

ASHRAE RESULTS, 1960  
(Koch, et. al.)

- 3 SLIGHTLY COOL
- 4 COMFORTABLE
- 5 SLIGHTLY WARM
- 6 WARM

$$^{\circ}\text{C} = (^{\circ}\text{F} - 32) \cdot \frac{5}{9}$$

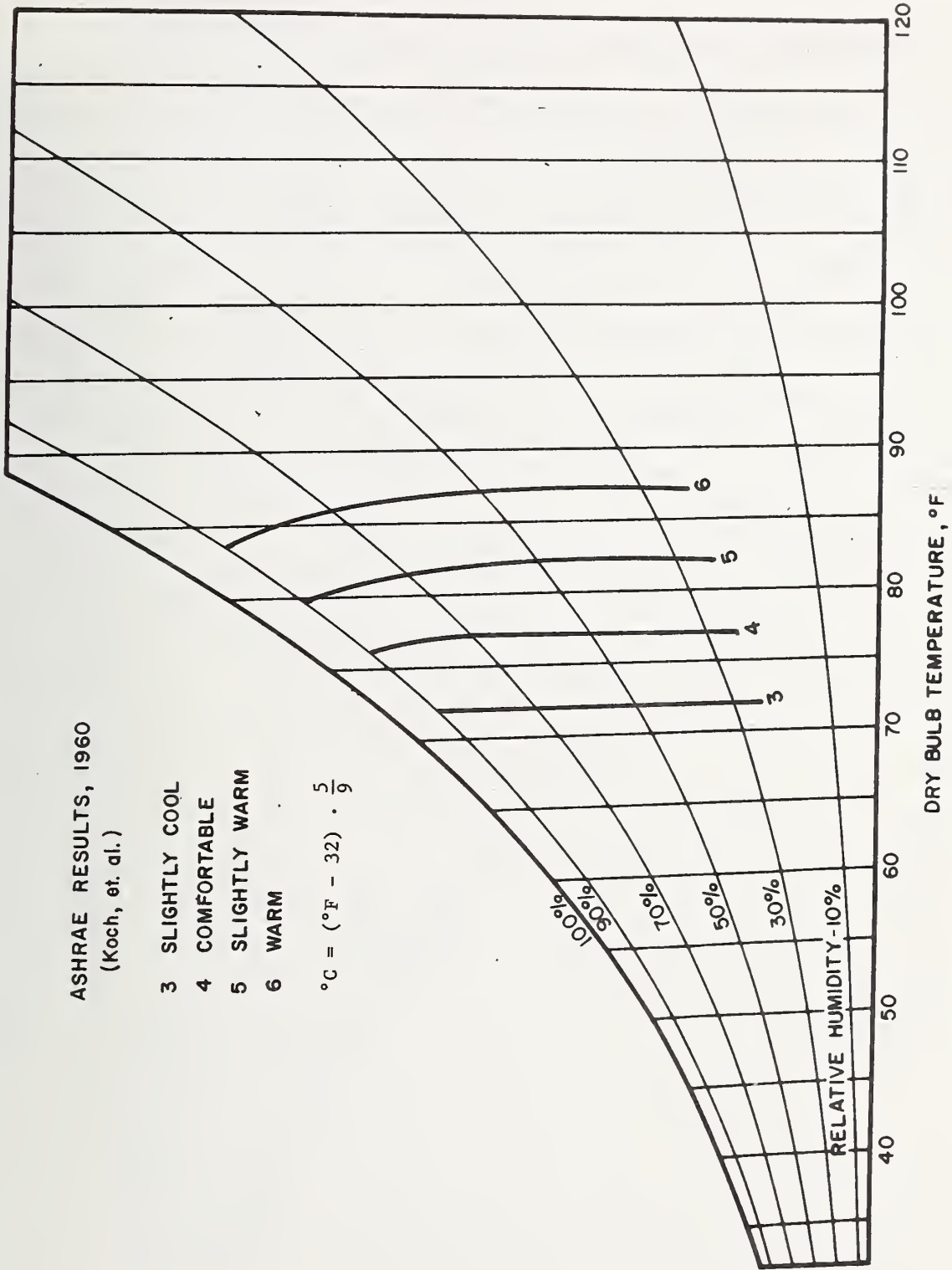


Figure B2 Lines of Constant Thermal Sensation as Determined by Koch, et. al. on a Psychrometric Chart

RESULTANT TEMPERATURE

$$^{\circ}\text{C} = (^{\circ}\text{F} - 32) \cdot \frac{5}{9}$$

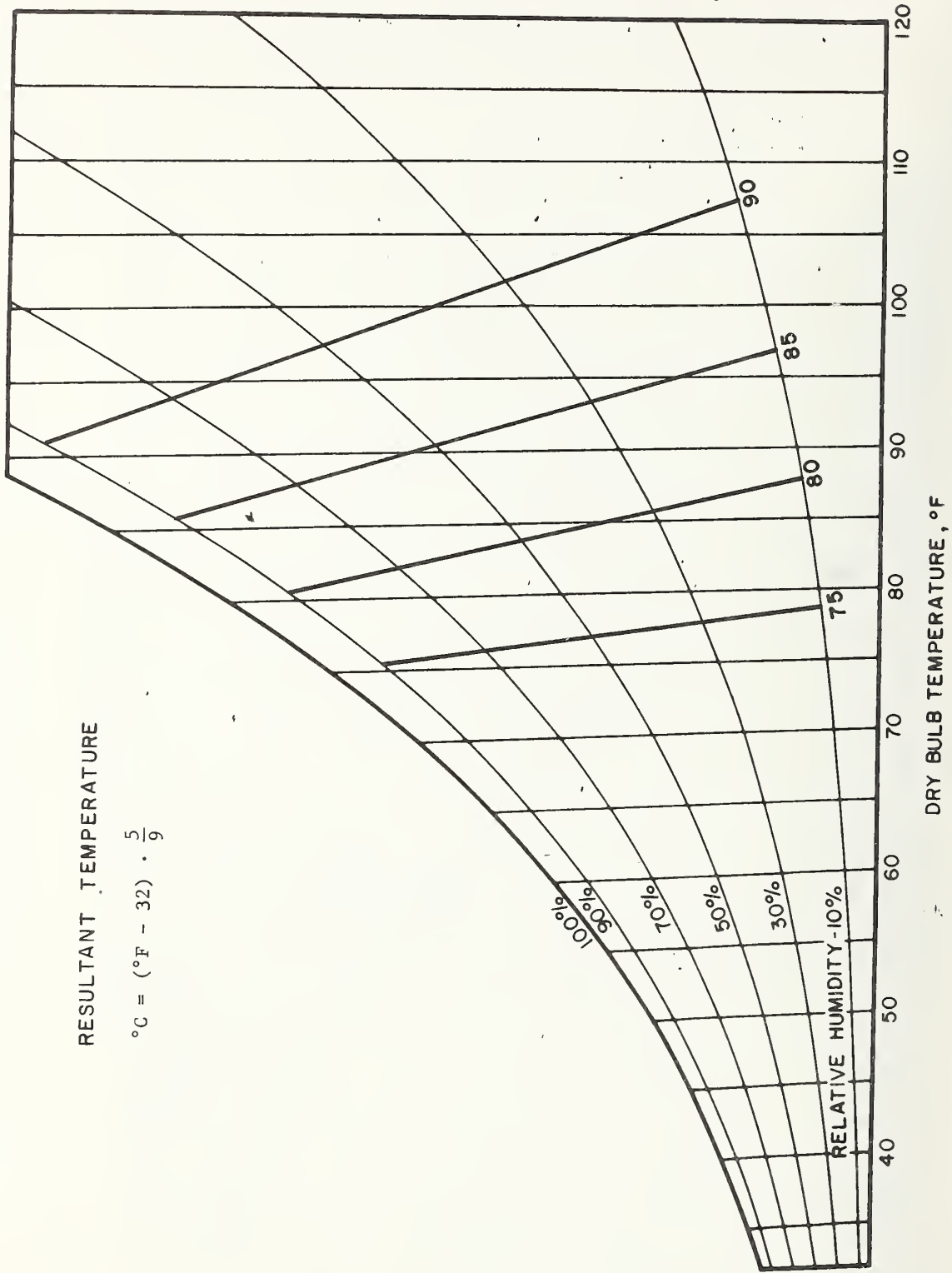


Figure B3 Lines of Constant Resultant Temperature on a Psychrometric Chart

**KANSAS STATE INDEX**

- 2 COOL**
- 3 SLIGHTLY COOL**
- 4 COMFORTABLE**
- 5 SLIGHTLY WARM**
- 6 WARM**

$$^{\circ}\text{C} = (^{\circ}\text{F} - 32) \cdot \frac{5}{9}$$

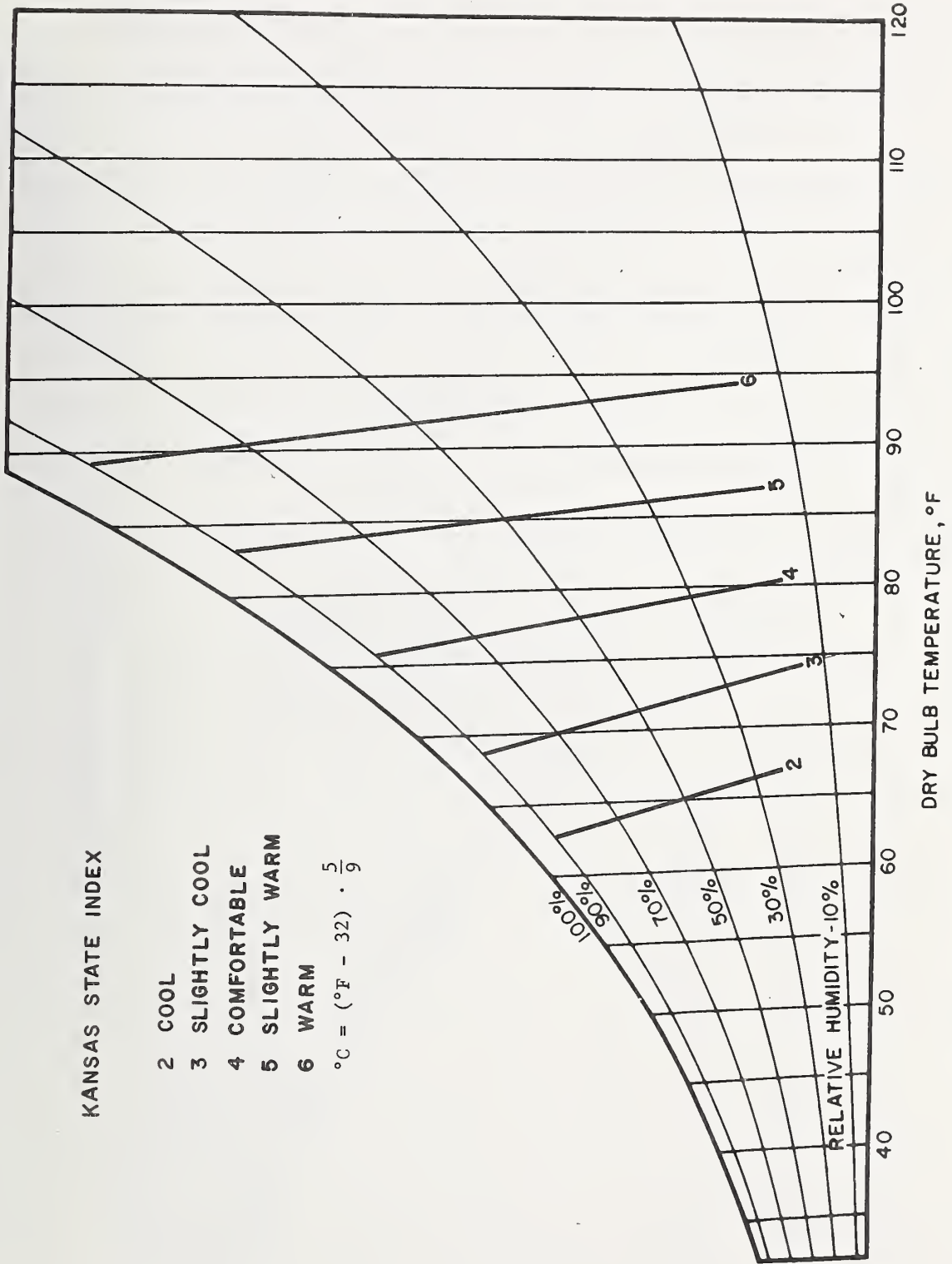


Figure B4 Lines of Constant Kansas State Index on a Psychrometric Chart

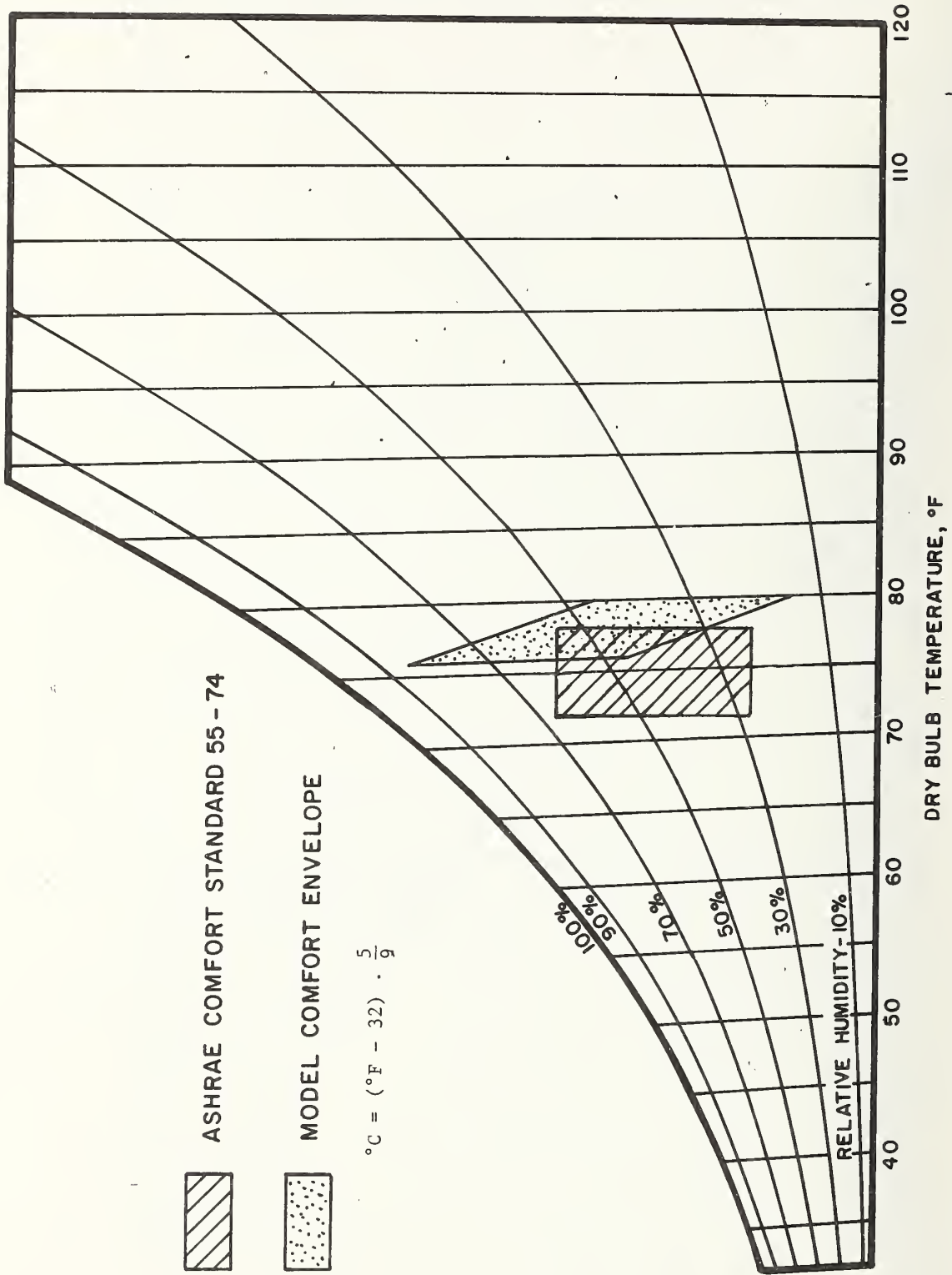


Figure B5 A Comparison of the Model Comfort Envelope and ASHRAE Comfort Standard on a Psychrometric Chart



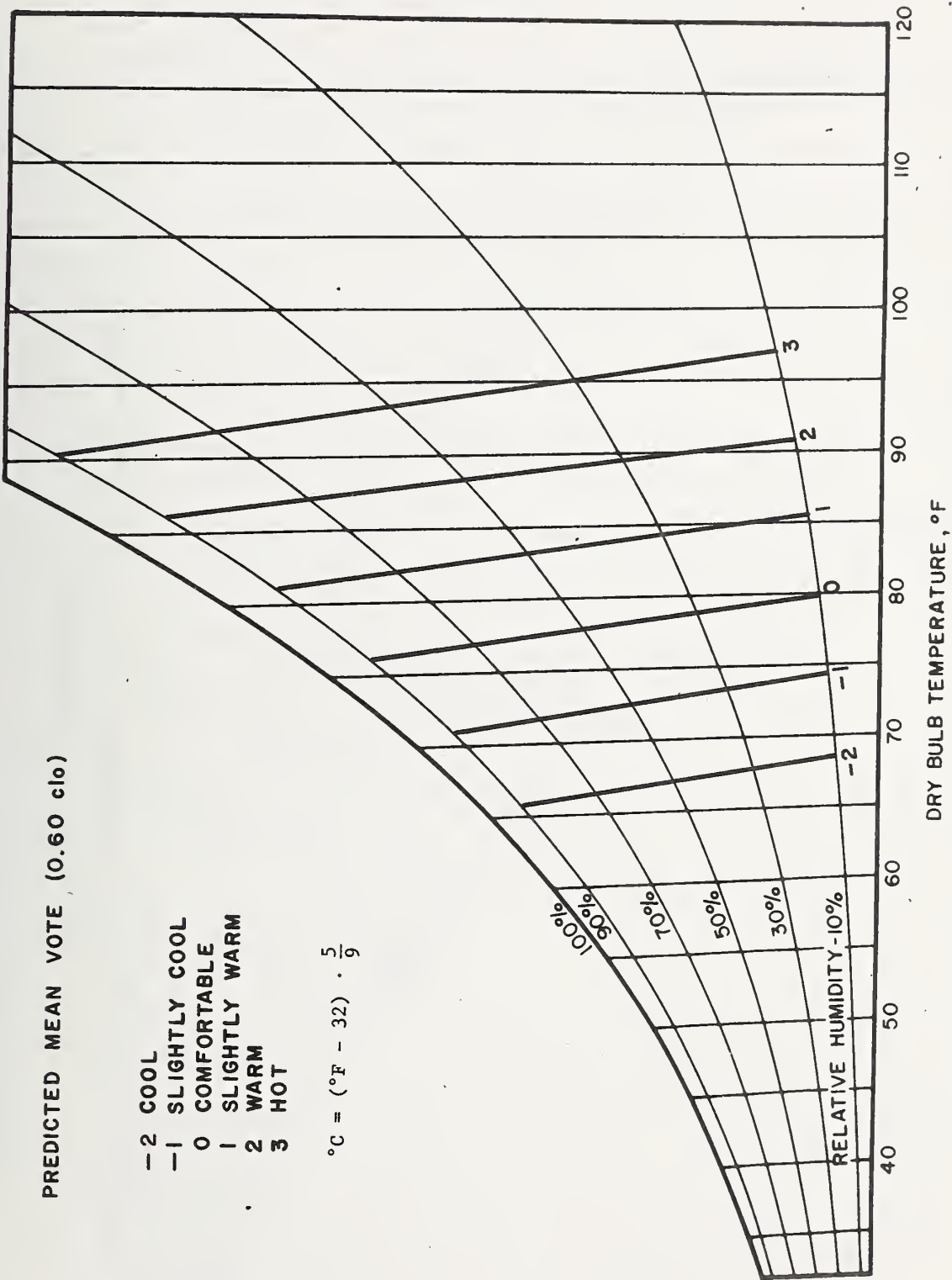


Figure B6 Lines of Constant Predicted Mean Vote (0.60 clo) on a Psychrometric Chart

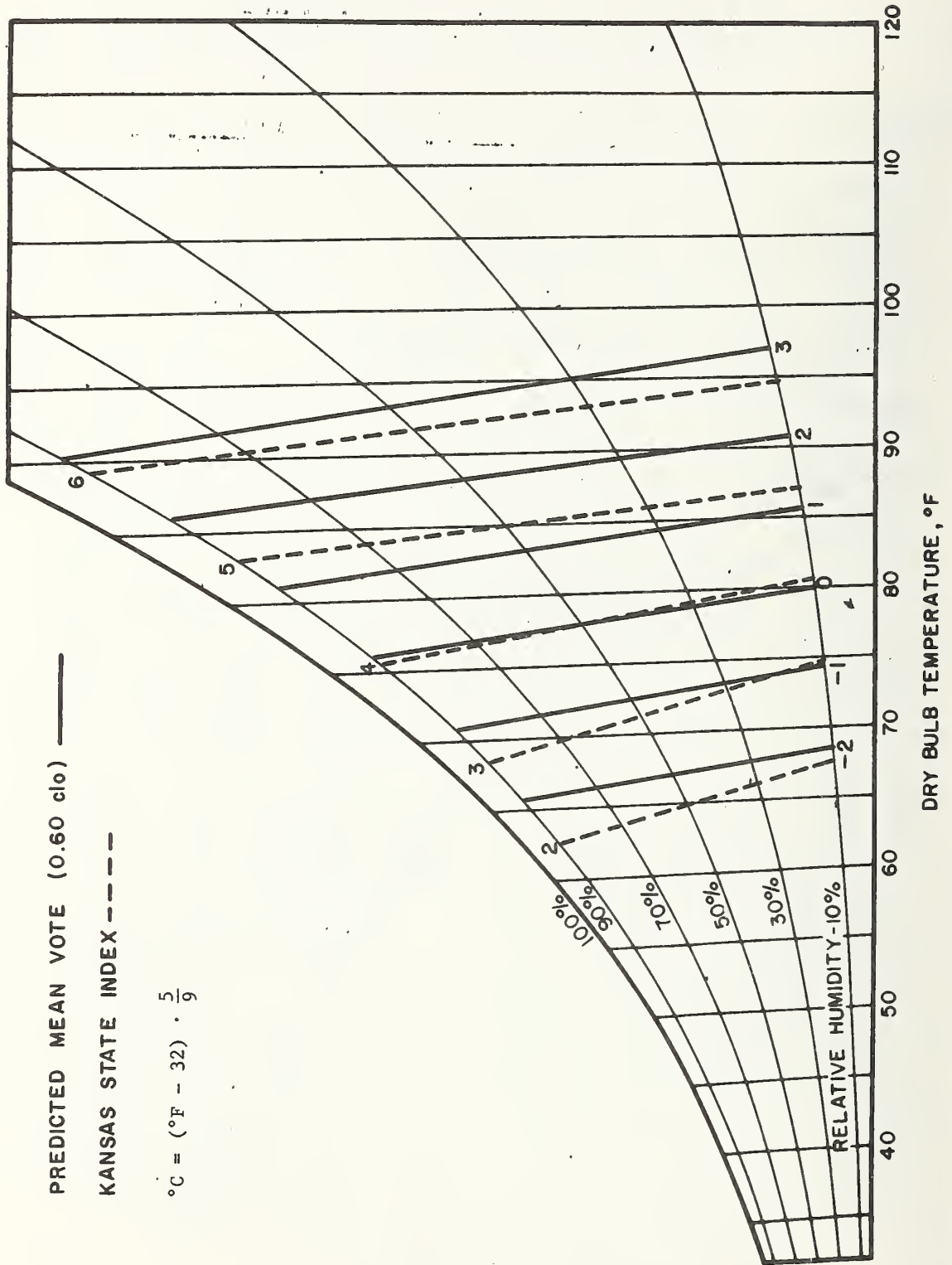


Figure B7 Comparison of Predicted Mean Vote (0.60 clo) and Kansas State Index on a Psychrometric Chart

PREDICTED MEAN VOTE (0.25 clo)

- 3 COLD
- 2 COOL
- 1 SLIGHTLY COOL
- 0 COMFORTABLE
- 1 SLIGHTLY WARM
- 2 WARM
- 3 HOT

$$^{\circ}\text{C} = (^{\circ}\text{F} - 32) \cdot \frac{5}{9}$$

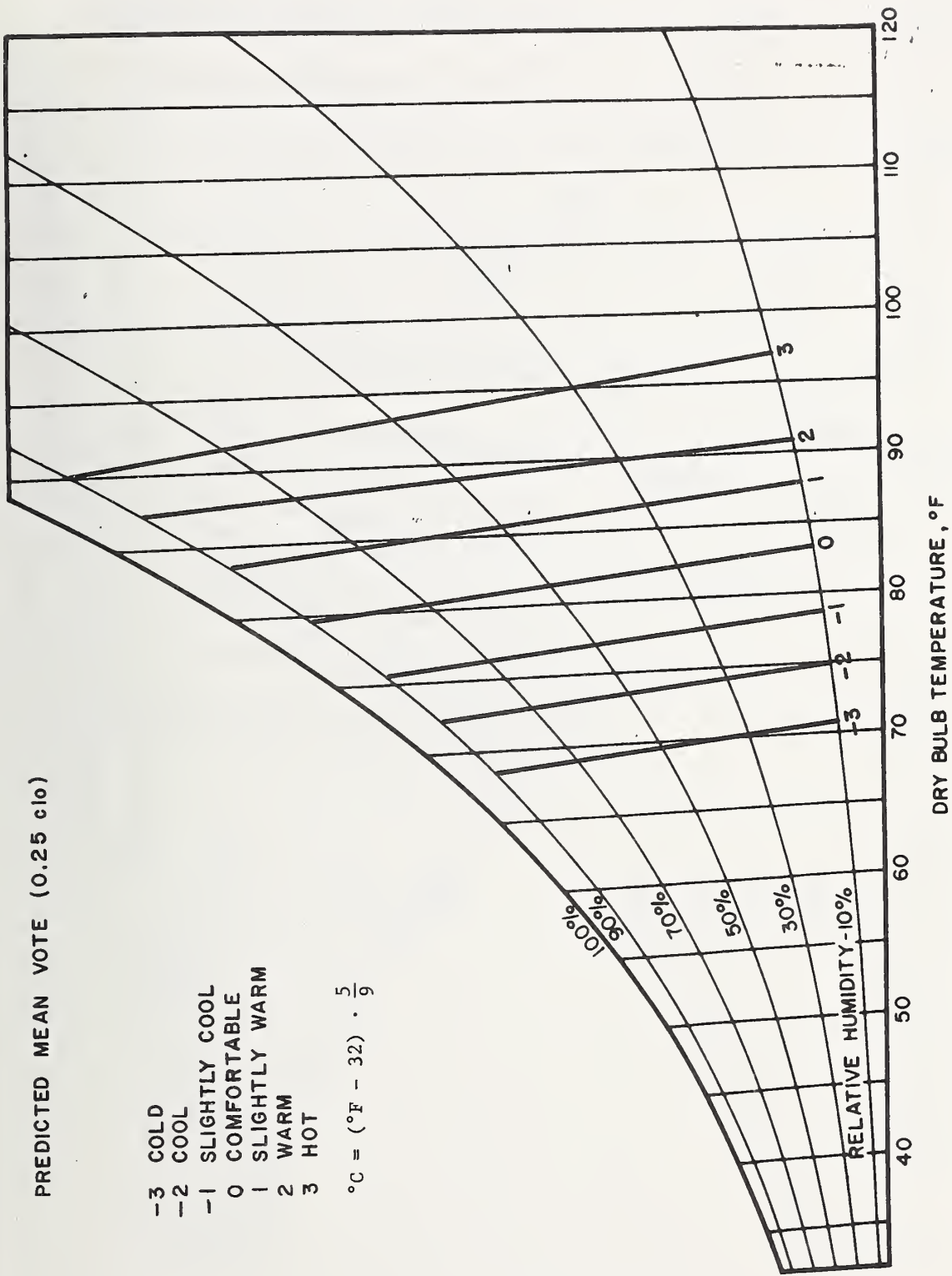


Figure B8 Lines of Constant Predicted Mean Vote (0.25 clo) on a Psychrometric Chart

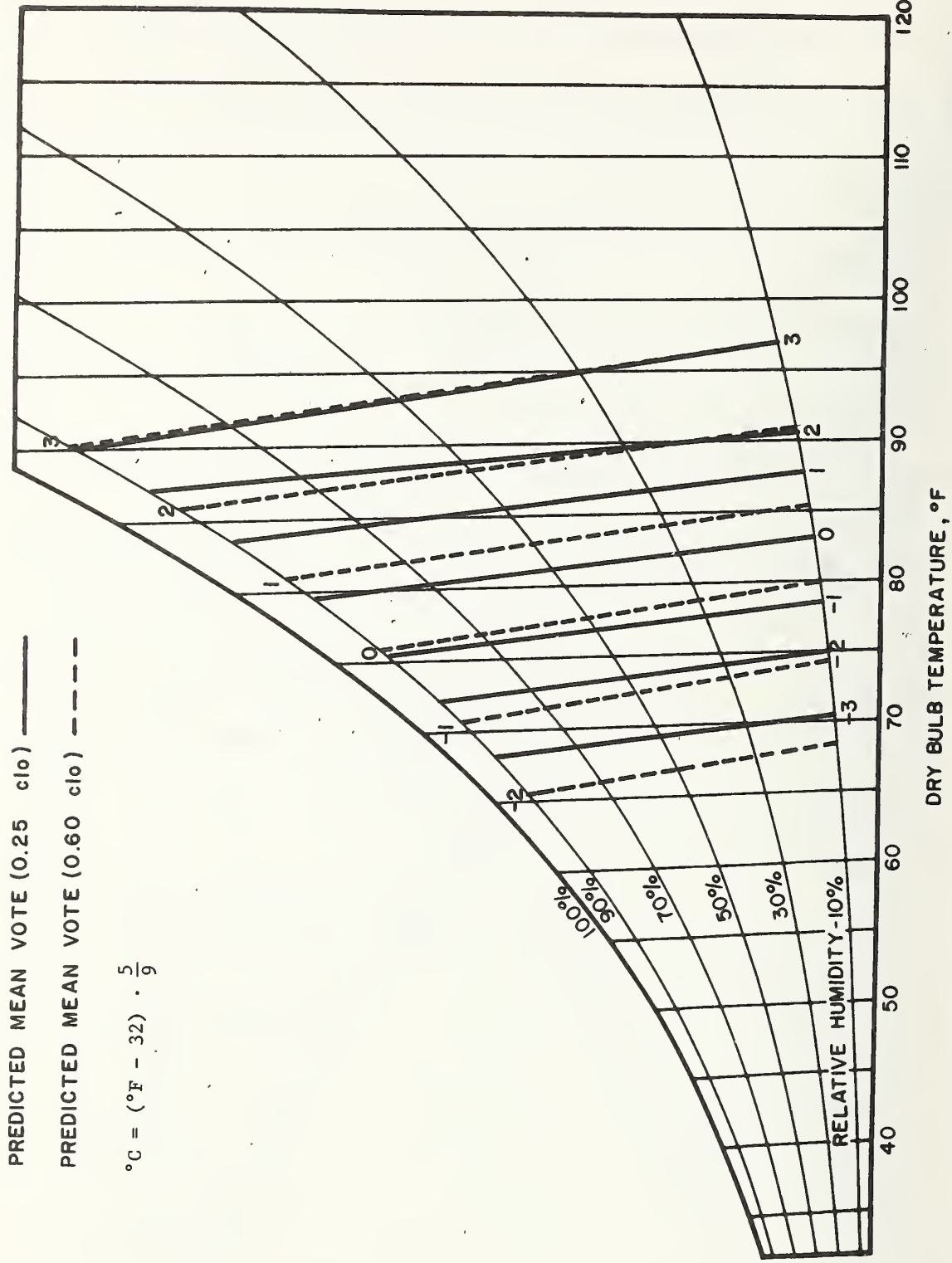


Figure B9 Comparison of 0.25 clo and 0.60 clo Predicted Mean Vote on a Psychrometric Chart

EFFECTIVE TEMPERATURE (ET\*)

$$^{\circ}\text{C} = (^{\circ}\text{F} - 32) \cdot \frac{5}{9}$$

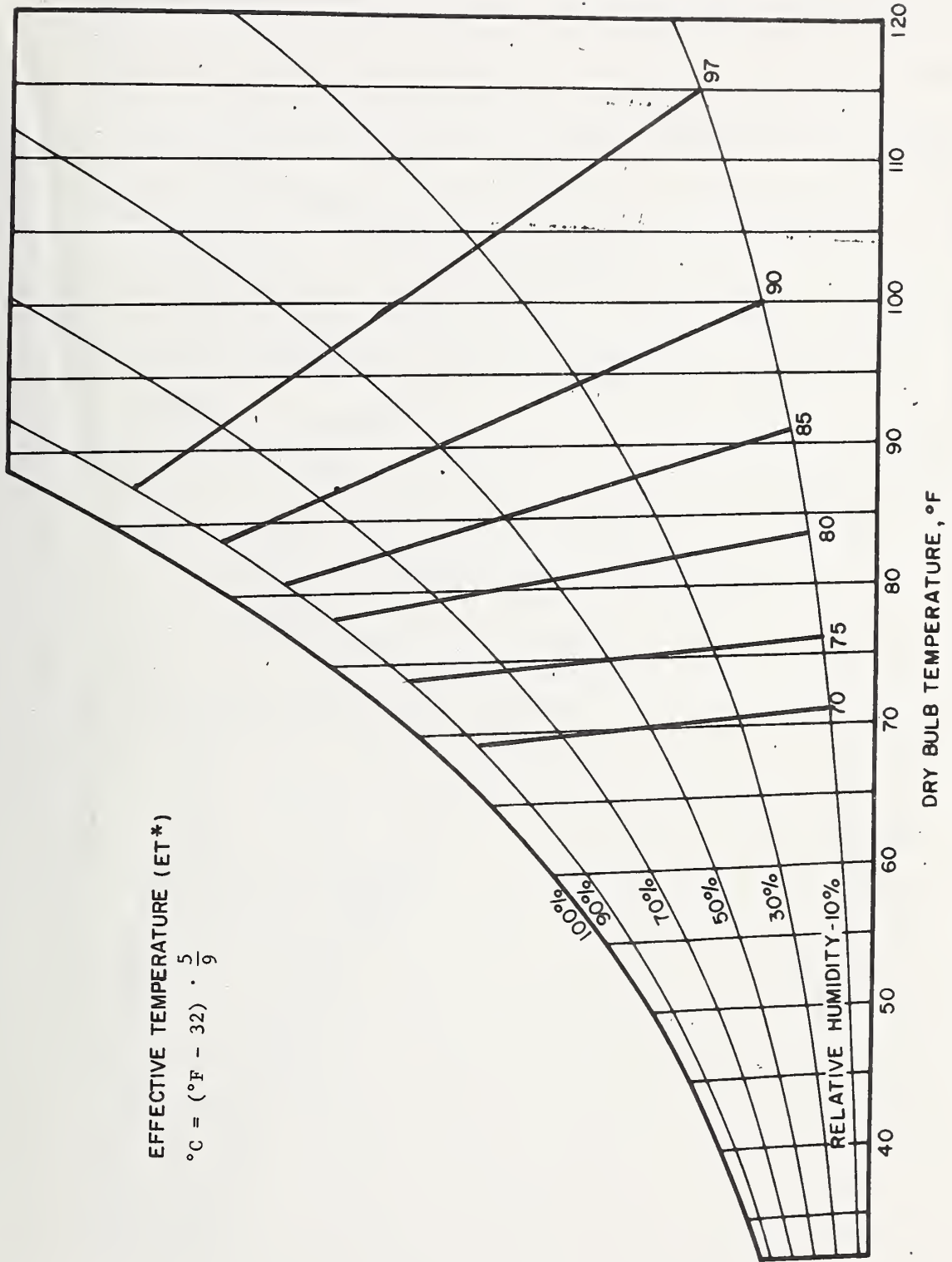


Figure 10 Lines of Constant Effective Temperature (ET\*) on a Psychrometric Chart

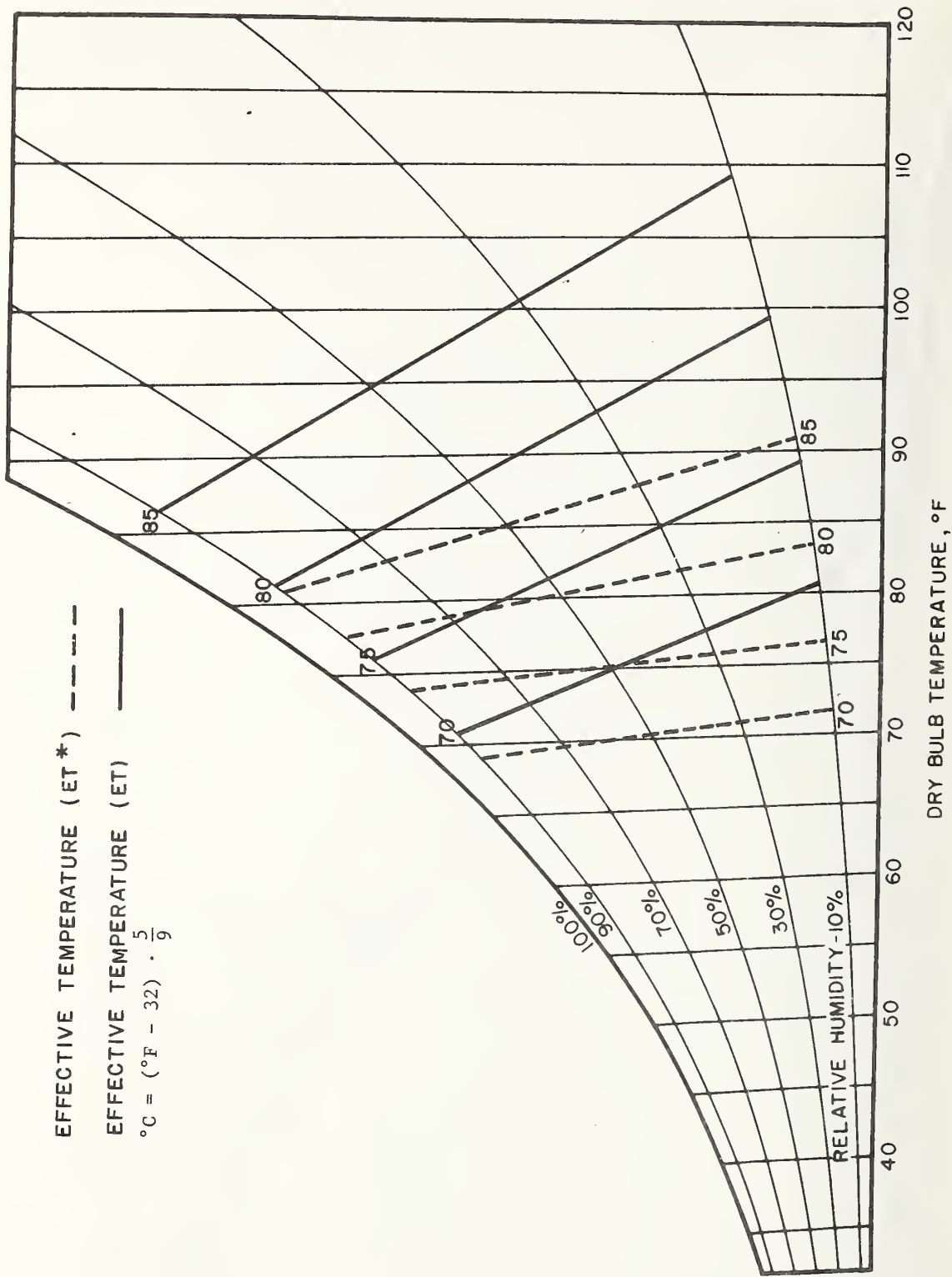


Figure B11. Comparison of ET\* and ET Effective Temperatures on a Psychrometric Chart



HEAT STRESS INDEX  
(ORIGINAL)

- 0 - NO THERMAL STRAIN
- 10 - MILD TO MODERATE HEAT STRAIN
- 40 - SEVERE HEAT STRAIN
- 70 - VERY SEVERE HEAT STRAIN

$$^{\circ}\text{C} = (^{\circ}\text{F} - 32) \cdot \frac{5}{9}$$

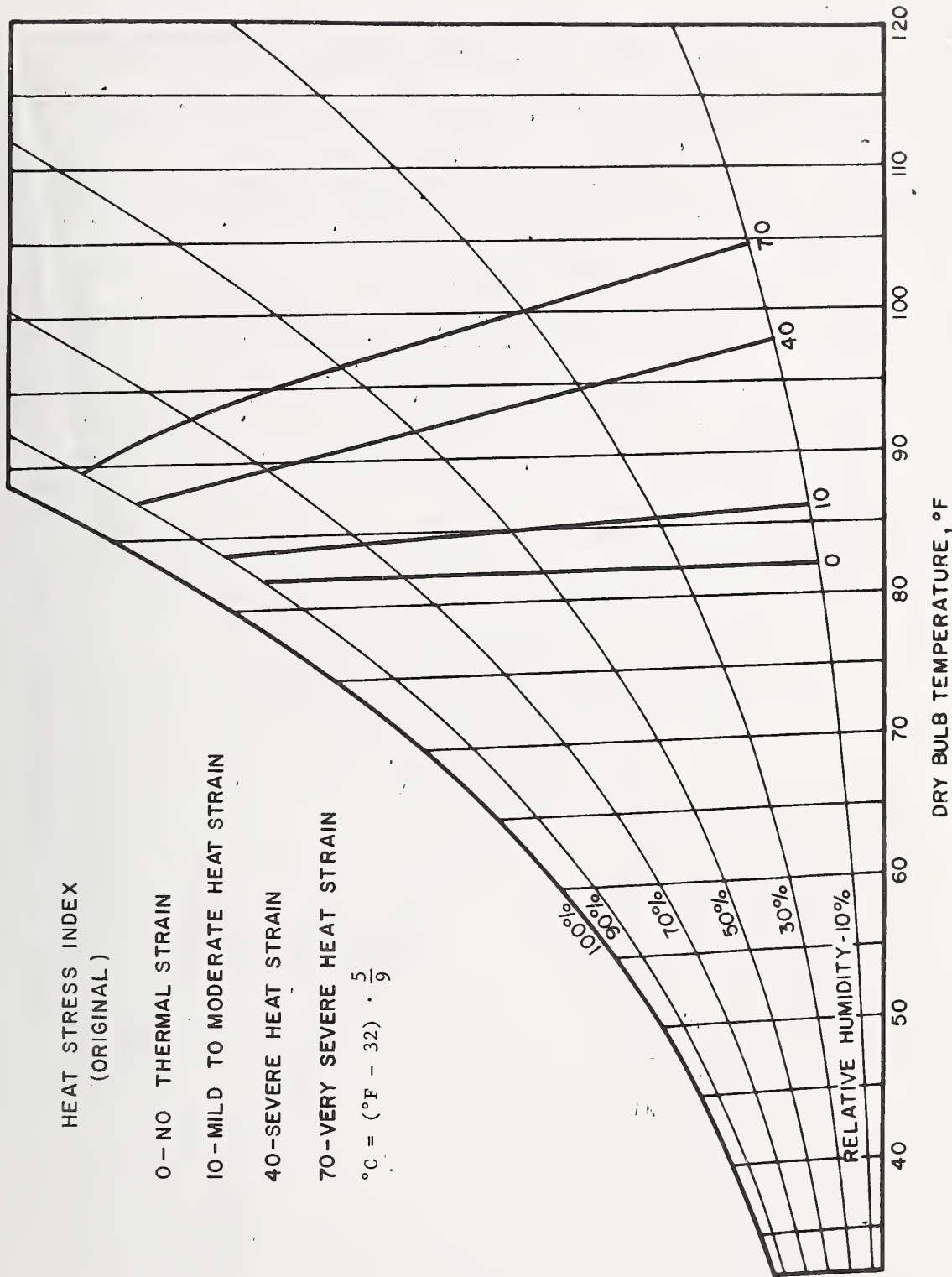


Figure B12 Lines of Constant Heat Stress Index (Original) on a Psychrometric Chart

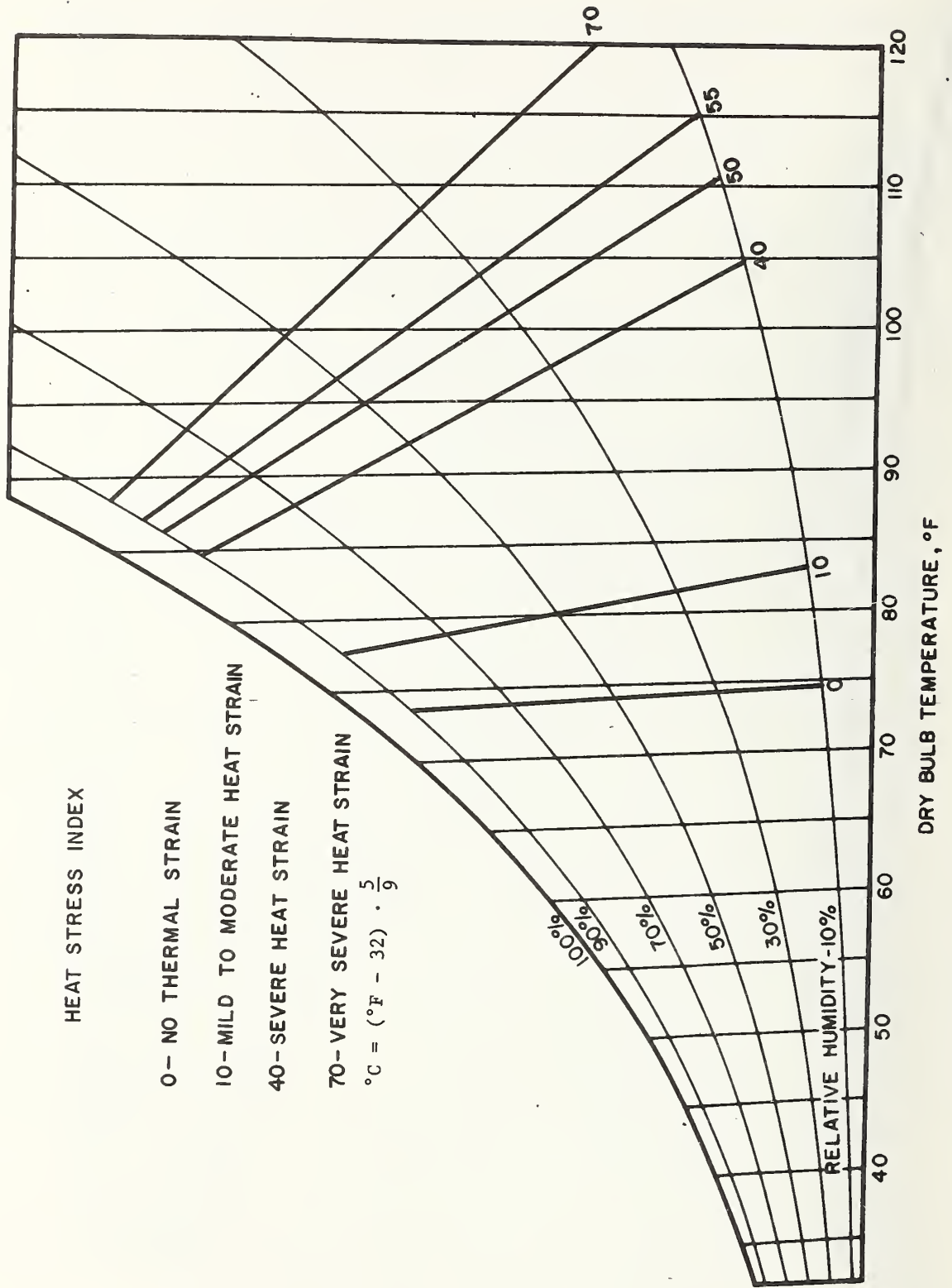


Figure B13 Lines of Constant Heat Stress Index on a Psychrometric Chart

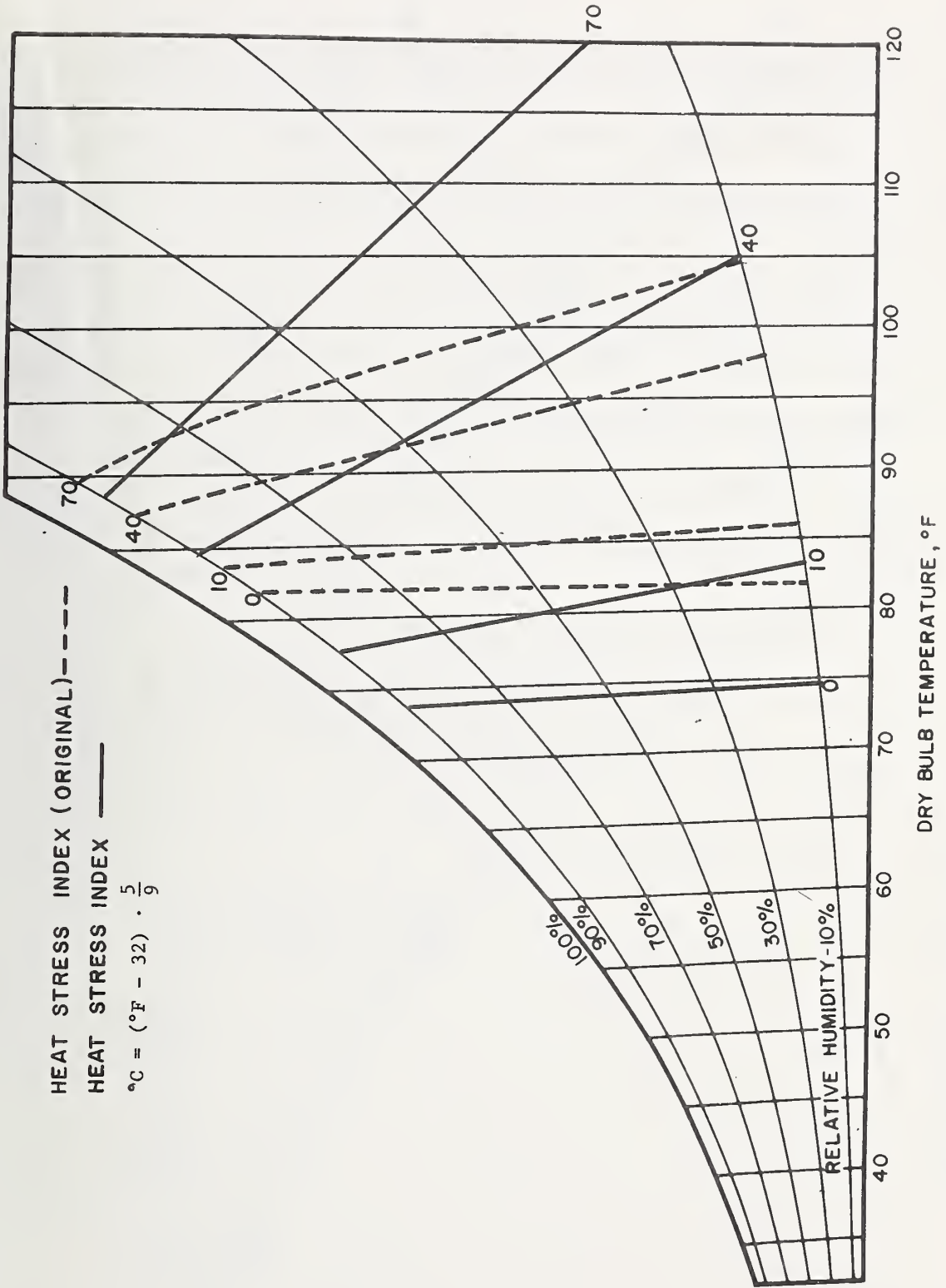


Figure B14 Comparison of Heat Stress Index (Original) and Heat Stress Index on a Psychrometric Chart

**THERMAL COMFORT WHEN EQUILIBRIUM  
IS MAINTAINED BY SWEATING**

$$^{\circ}\text{C} = (^{\circ}\text{F} - 32) \cdot \frac{5}{9}$$

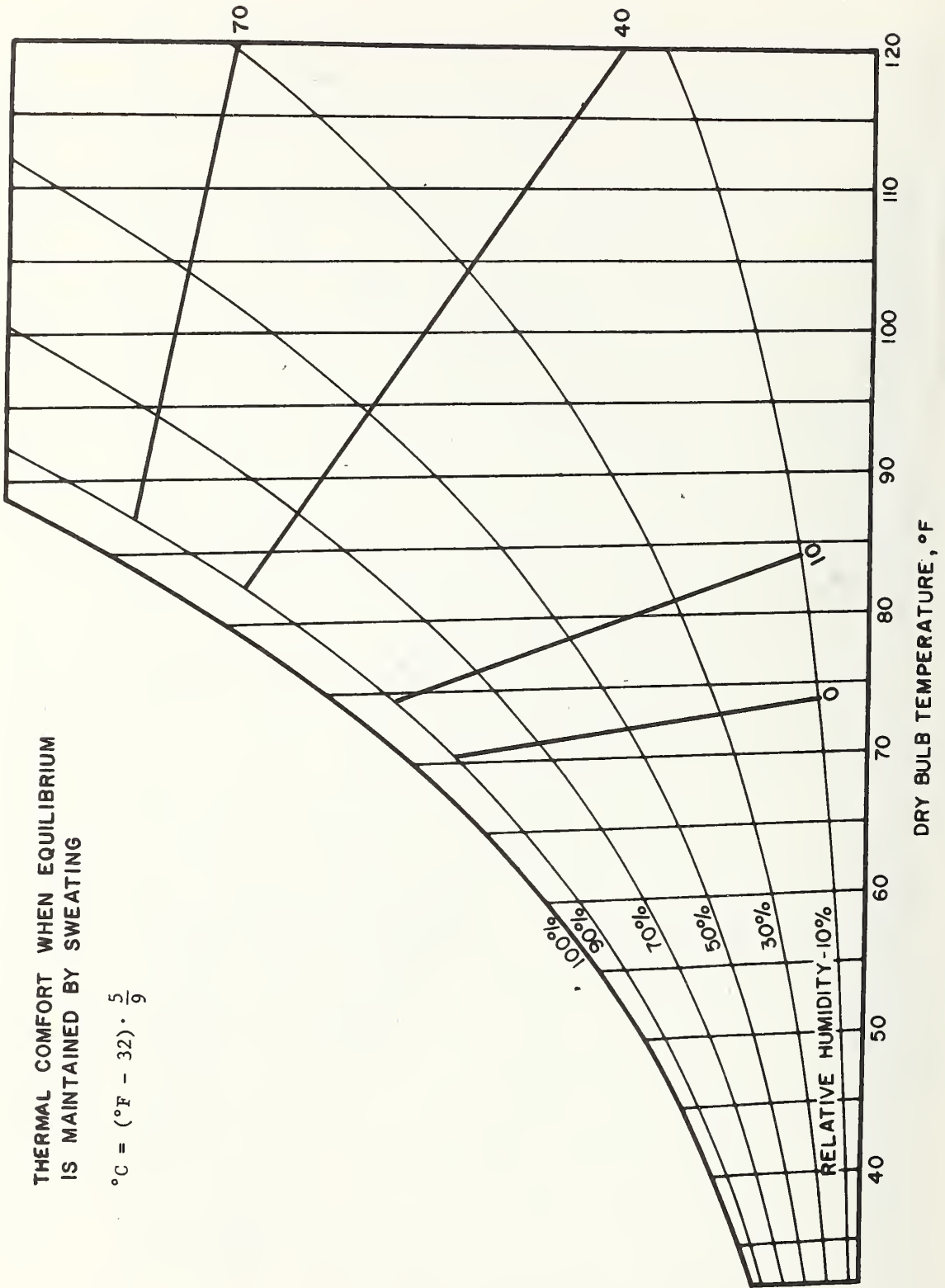


Figure B15 Lines of Constant Percentage of Wettedness for Thermal Comfort When Equilibrium is Maintained by Sweating, on a Psychrometric Chart

**INDEX OF THERMAL STRESS,**

$$\frac{\text{kcal/h}}{^\circ\text{C}} = (\text{°F} - 32) \cdot \frac{5}{9}$$

$$^\circ\text{C} = (\text{°F} - 32) \cdot \frac{5}{9}$$

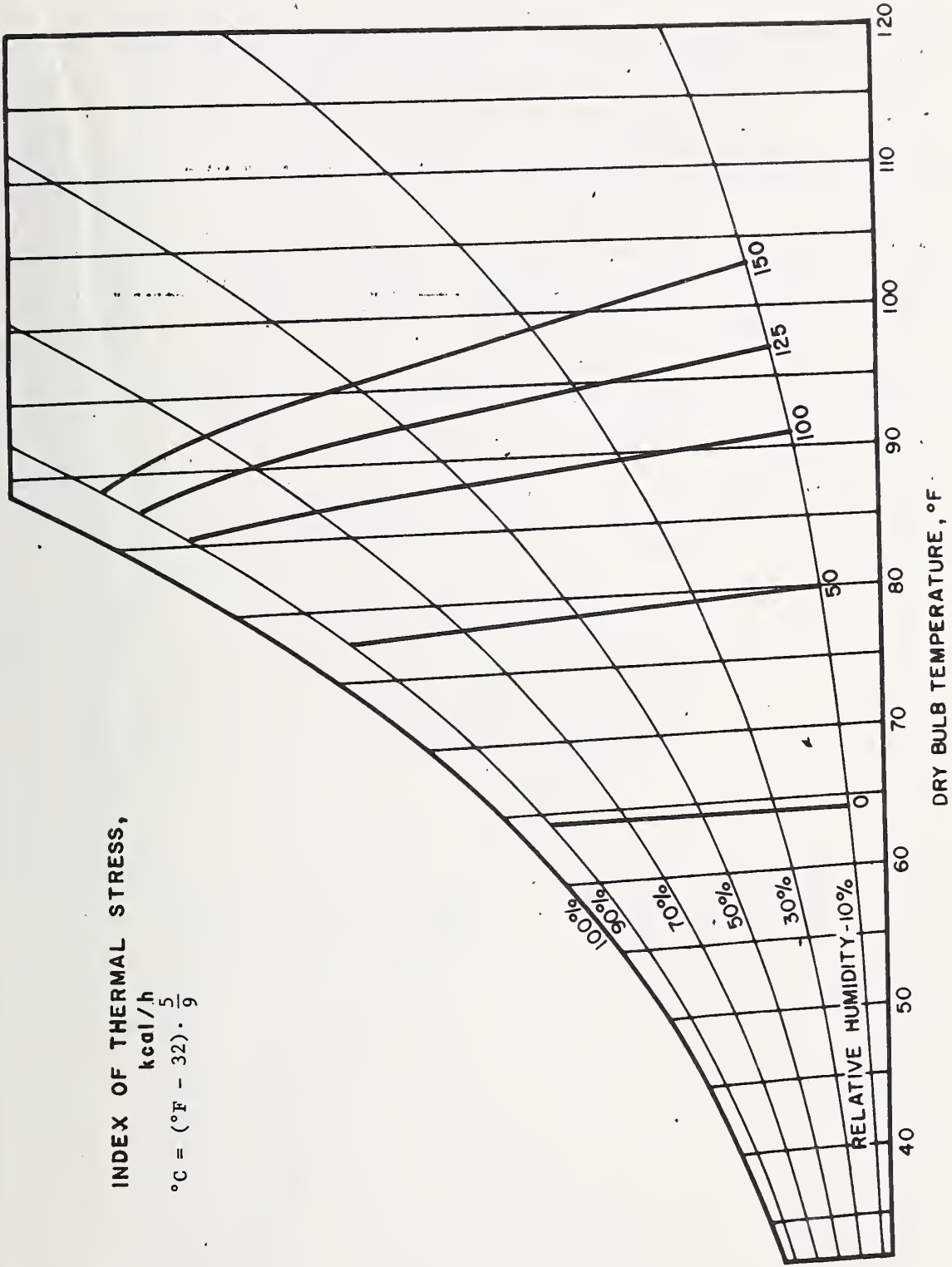


Figure B16 Lines of Constant Index of Thermal Stress on a Psychrometric Chart

PREDICTED FOUR HOUR  
SWEAT RATE

$$^{\circ}\text{C} = (^{\circ}\text{F} - 32) \cdot \frac{5}{9}$$

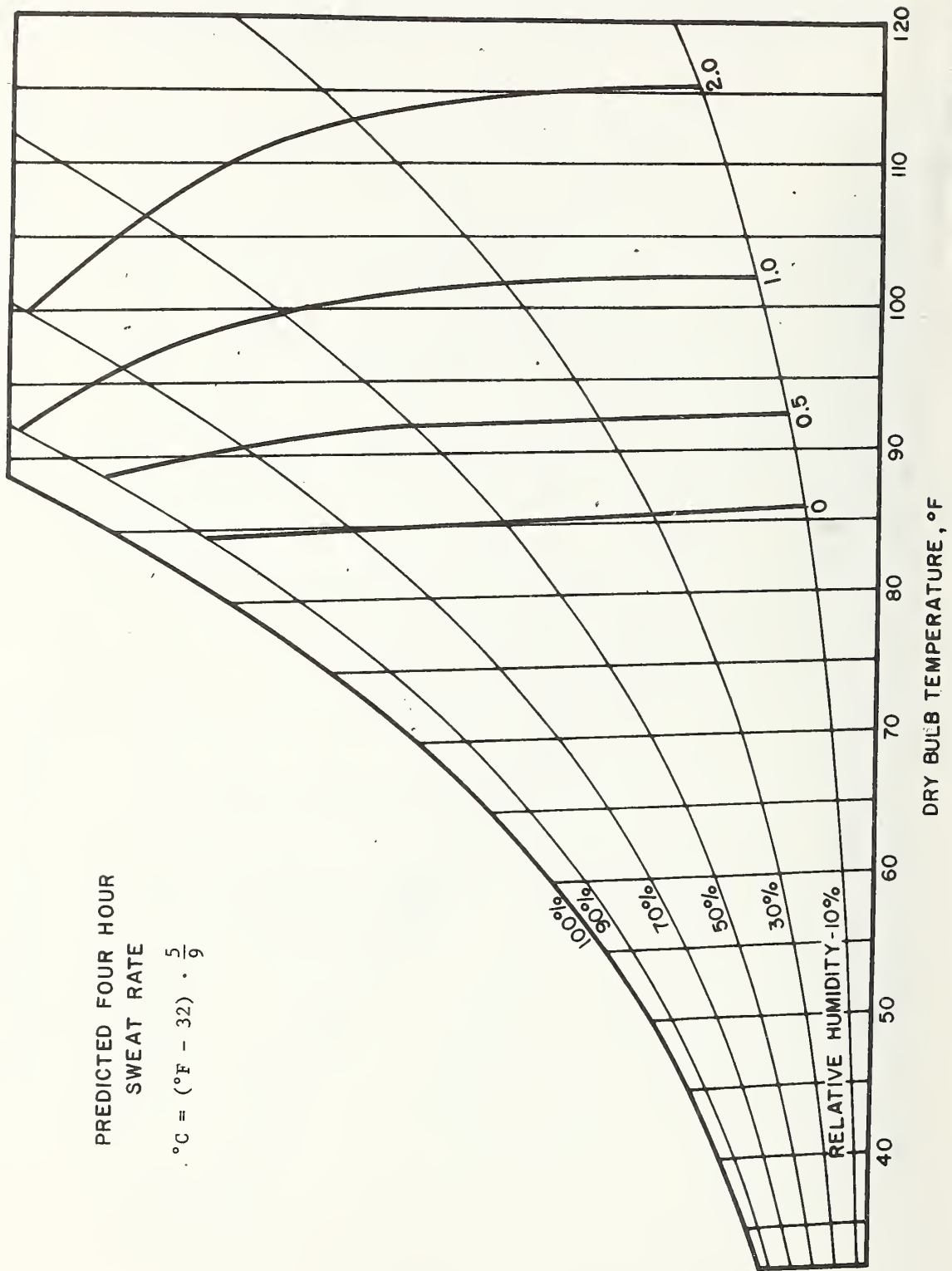


Figure B17 Lines of Constant Predicted Four Hour Sweat Rate on a Psychrometric Chart



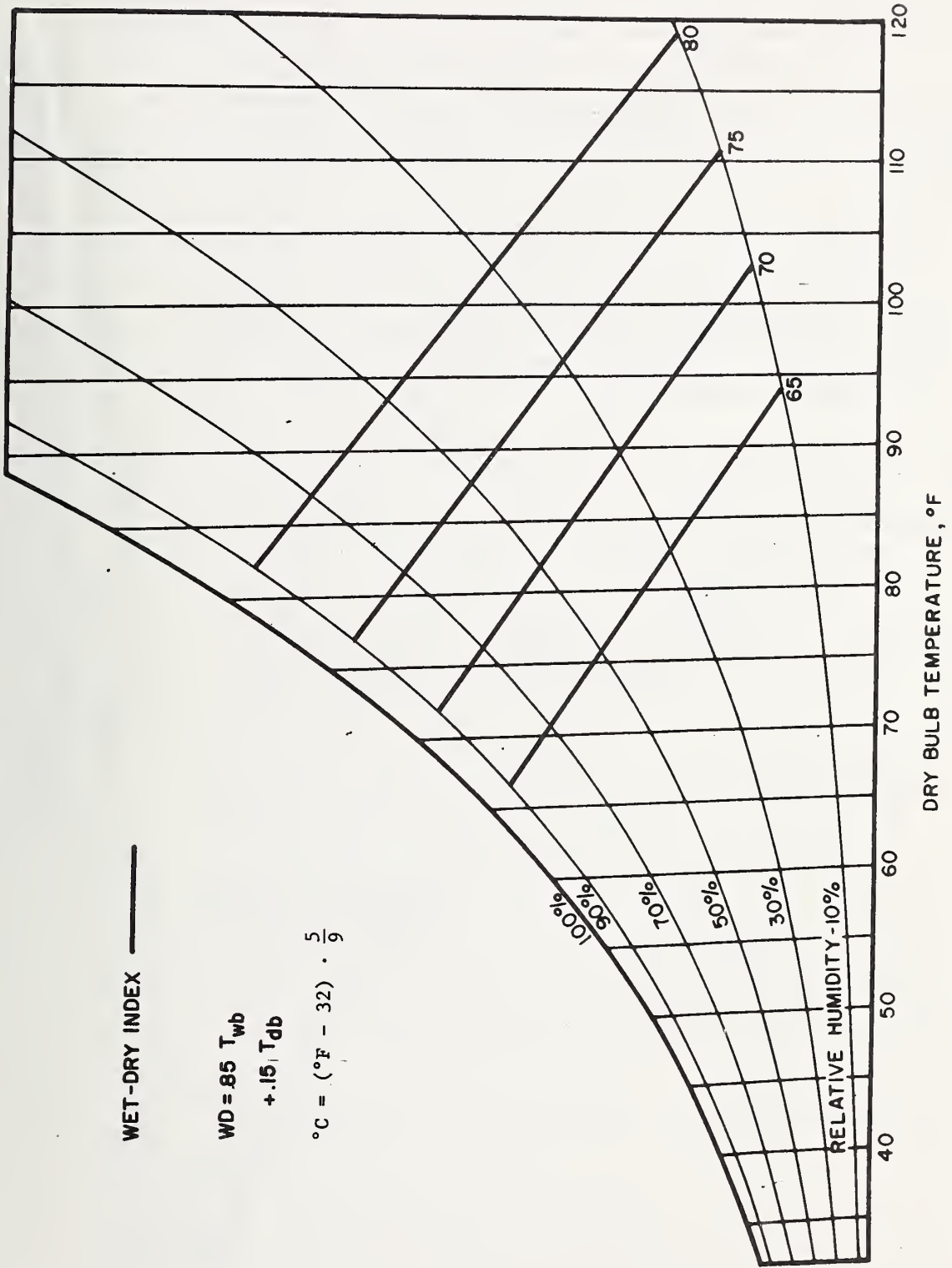


Figure B18 Lines of Constant Wet-Dry Index on a Psychrometric Chart

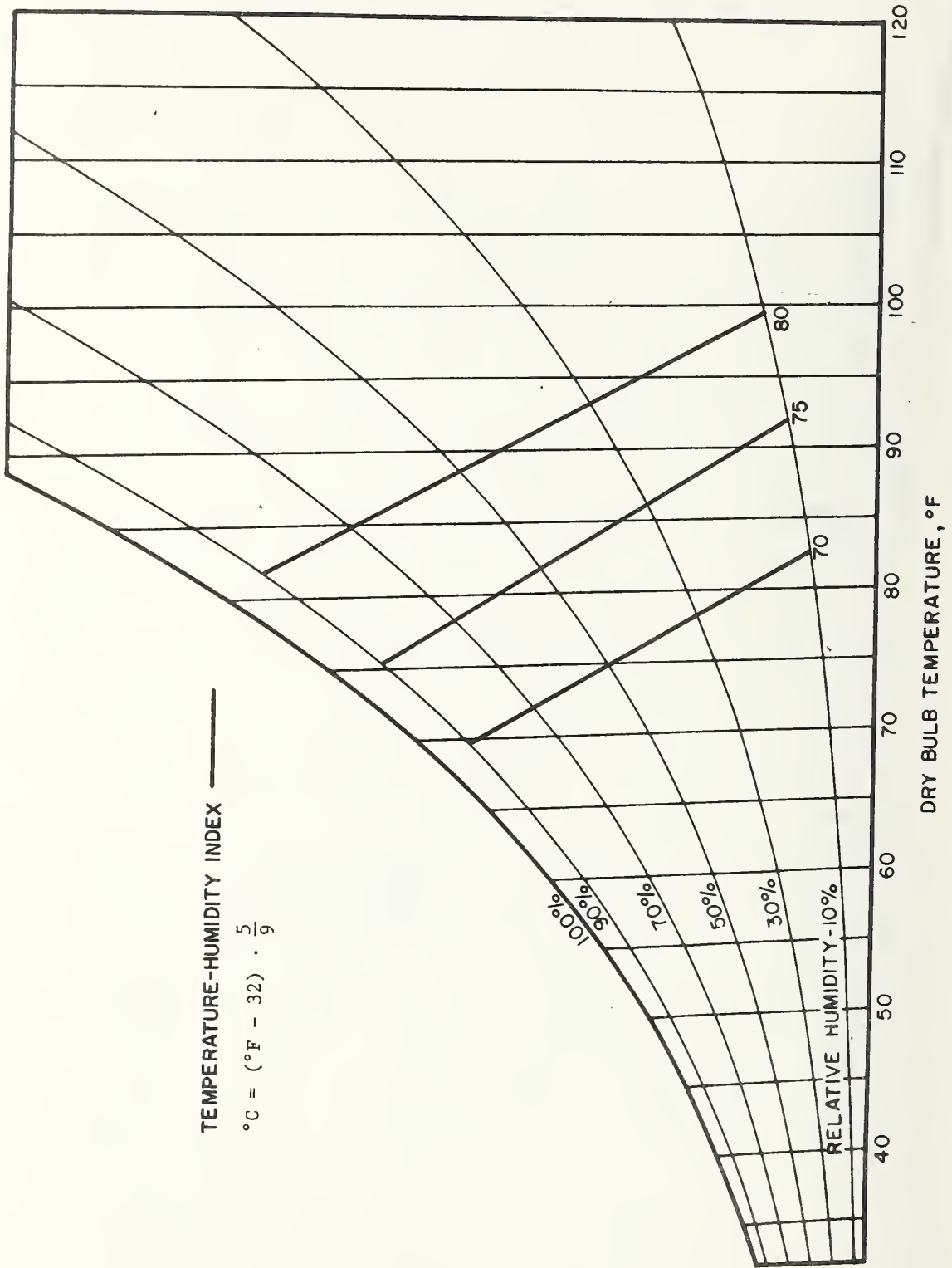


Figure B19 Lines of Constant Temperature-Humidity Index on a Psychrometric Chart

Table B1 Evaluation of Index of Heat Stress

Index of Heat Stress	Physiological and Hygienic Implications of 8-Hr Exposures to Various Heat Stresses
0	No thermal strain
+10	Mild to moderate heat strain. Where a job involves higher intellectual functions, dexterity, or alertness, subtle to substantial decrements in performance may be expected. In performance of heavy physical work, little decrement expected unless ability of individuals to perform such work under no thermal stress is marginal.
40	Severe heat strain, involving a threat to health unless men are physically fit. Break-in period required for men not previously acclimatized. Some decrement in performance of physical work is to be expected. Medical selection of personnel desirable because these conditions are unsuitable for those with cardiovascular or respiratory impairment or with chronic dermatitis. These working conditions are also unsuitable for activities requiring sustained mental effort.
50	
60	
70	Very severe heat strain. Only a small percentage of the population may be expected to qualify for this work. Personnel should be selected (a) by medical examination and (b) by trial on the job (after acclimatization). Special measures are needed to assure adequate water and salt intake. Amelioration of working conditions by any feasible means is highly desirable, and may be expected to decrease the health hazard while increasing efficiency on the job. Slight "indisposition" which in most jobs would be insufficient to affect performance may render workers unfit for this exposure.
80	
90	
100	The maximum strain tolerated daily by fit, acclimatized young men.

Table B2 Range of Application of Various Physiological Indices as Calculated in This Paper

<u>Index</u>	<u>Metabolic Production</u>	<u>Clothing</u>	<u>Dry-bulb Temperature</u>	<u>Wet-bulb Temperature</u>	<u>Air Velocity</u>
ET	rest only	Summer clothing	1 - 43 °C	1 - 43 °C	.1 - 3.5 m/s
RT	rest only	Light clothing	18 - 45 °C	18 - 45 °C	.1 - 3.0 m/s
KSU	rest only	0.6 clo	15.6 - 36.7 °C	5.6 - 34.4 °C	< .23 m/s
PMV	50 $\frac{\text{kcal}}{\text{m}^2 \cdot \text{h}}$	0.25 clo and 0.60 clo	-	-	.1 m/s
ET*	58.2 $\frac{\text{W}}{\text{m}^2}$	0.60 clo	-	-	.1 m/s
HSI (original)	100 - 500 kcal/h	unspecified	27 - 60 °C	15 - 35 °C	.25 - 10.0 m/s
HSI	58.2 $\frac{\text{W}}{\text{m}^2}$	0.60 clo	-	-	.1 m/s
Thermal Comfort when Equil. is Maintained by Sweating	58.2 $\frac{\text{W}}{\text{m}^2}$	0.60 clo	-	-	.1 m/s
ITS	100 - 600 kcal/h	Military overalls over shorts	20 - 55 °C	15 - 35 °C	.1 - 3.5 m/s
P4SR	100 - 350 kcal/h	Wearing only shorts	27 - 55 °C	15 - 36 °C	.05 - 2.5 m/s

Appendix C

Discussion of Regulatory Sweating Models

In Appendix B it was noted that the component expression for regulatory sweating in the new effective temperature model contributed significantly to the response of the model. As given in Appendix B, the component expression is

$$E_{\text{rsw}} = 70 (T_{\text{cr}} - 36.6) (T_{\text{sk}} - 34.1) \text{ W/m}^2$$

for  $T_{\text{cr}} \geq 36.6 \text{ }^\circ\text{C}$  and

$$T_{\text{sk}} \geq 34.1 \text{ }^\circ\text{C}$$

$$E_{\text{rsw}} = 0 \text{ if } T_{\text{cr}} < 36.6 \text{ }^\circ\text{C} \text{ or}$$

$$T_{\text{sk}} < 34.1 \text{ }^\circ\text{C}$$

The interpretation of this expression is that sweat production is caused by signals from both the skin and the deep body. If the temperature in either one of the regions rises above the normal value, then the body secretes sweat for the purpose of evaporative cooling. This sweating model is in definite contrast to the results of experiments conducted by Dr. T. H. Benzinger of the Naval Medical Research Institute [1, 2]<sup>a</sup>. Dr. Benzinger concludes as a result of his studies, that the signal for sweat secretion is a sole function of the temperature in the anterior portion of the hypothalamus region of the brain. When this temperature rises above a sharply determined set point, warm sensitive neurons begin to fire and excite sweating such that the rate of sweat production is directly proportional to deviation beyond the set point.

The skin temperature does play a role in the evaporative cooling process; however, in contrast to the interpretation of Hardy and Stolwijk [3, 4] (which has been adapted for the new effective temperature model), Benzinger concludes that the effect is one of inhibition. Whenever the skin temperature drops below approximately 33 °C the rate of sweat production begins to decrease below its normal value (given a hypothalamus temperature above the set point) and the amount of decrease is proportional to the deviation of skin temperature below 33 °C. A comparison between these two distinctly different interpretations is shown in Figure C1. The rate of evaporative cooling is plotted against the deviation of skin temperature from 33 °C. As can be seen, Gagge's model simulates zero cooling by sweat evaporation as long as the skin temperature is below 34.1 °C and is directly proportional to  $(T_{\text{sk}} - 34.1) \cdot (T_{\text{cr}} - 36.6)$  above this point. Benzinger's data indicates a constant rate of sweat production whenever the skin temperature is above 33 °C (the value of the rate dependent on  $(T_{\text{cr}} - 36.6)$ ) and a progressively decreasing rate as the skin temperature drops below 33 °C.

The importance of the evaporative cooling in the model can be seen in Figure C2 where new effective temperature lines are plotted that have been calculated using Benzinger's results for sweat production. Since his data generally gives larger values of evaporative cooling for specified core and skin temperatures, it would be expected that this modified scale would show more dependence on humidity than the standard new effective temperature lines and this can be seen in Figure C3. It is not recommended that the new data be used in the simulation of the body response since the experiments used to generate them were very special in nature. Men were enclosed in a gradient calorimeter [5] such that all sweat evaporated could be instantly carried away. This may not be true in ordinary environments, particularly where the humidity of the ambient air is high. However, it should be obvious that much more study and refinement is needed before an accurate simulation of human response to an environment can be accomplished.

The interpretation that lines of equivalent thermal comfort are identical with lines of constant sweat ratio could be adjusted in light of Dr. Benzinger's findings. The feeling of thermal comfort is no doubt linked to the necessity for sweat secretion when subjected to warm environments. However, as a result of his studies this is in turn linked directly to the hypothalamus temperature or deep body temperature since this is the sole source of the sweating signal. The reasoning is substantiated by an additional experiment conducted by him.

<sup>a</sup>Reference numbers refer to references listed at the end of this Appendix.



A subject was cooled in a tank of cold water until the hypothalamus temperature was well below the individual's set point. He was then put into a very hot bath where the skin temperature and hypothalamus temperature were monitored with time. Even though the skin temperature went to a relatively high value almost immediately, the subject did not report discomfort until the hypothalamus temperature began to rise above his set point.

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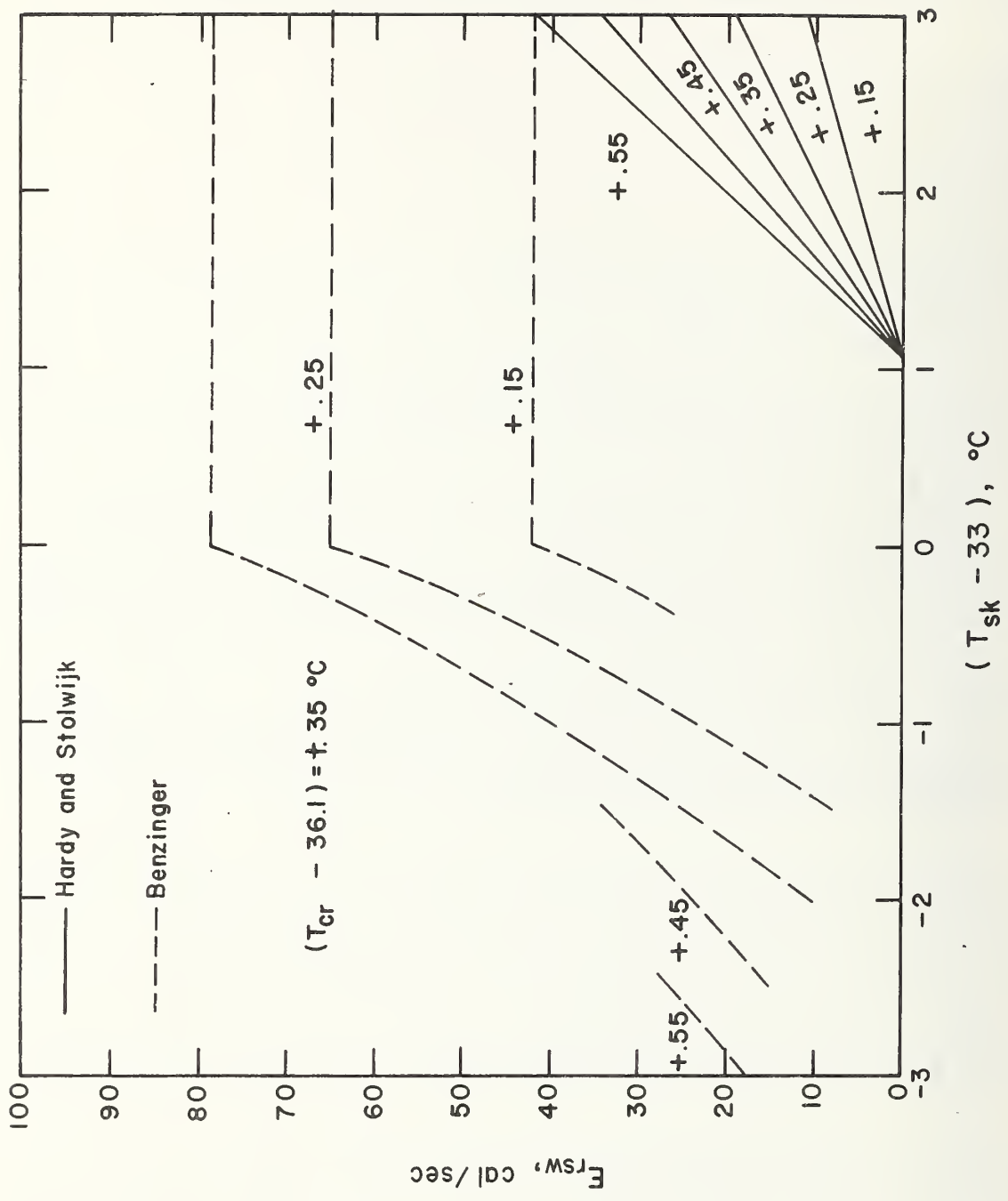


Figure C1 Rate of Evaporative Cooling for Two Different Sweating Models

**ET\* EFFECTIVE TEMPERATURE MODEL  
WITH MODIFIED SWEATING**

$$^{\circ}\text{C} = (^{\circ}\text{F} - 32) \cdot \frac{5}{9}$$

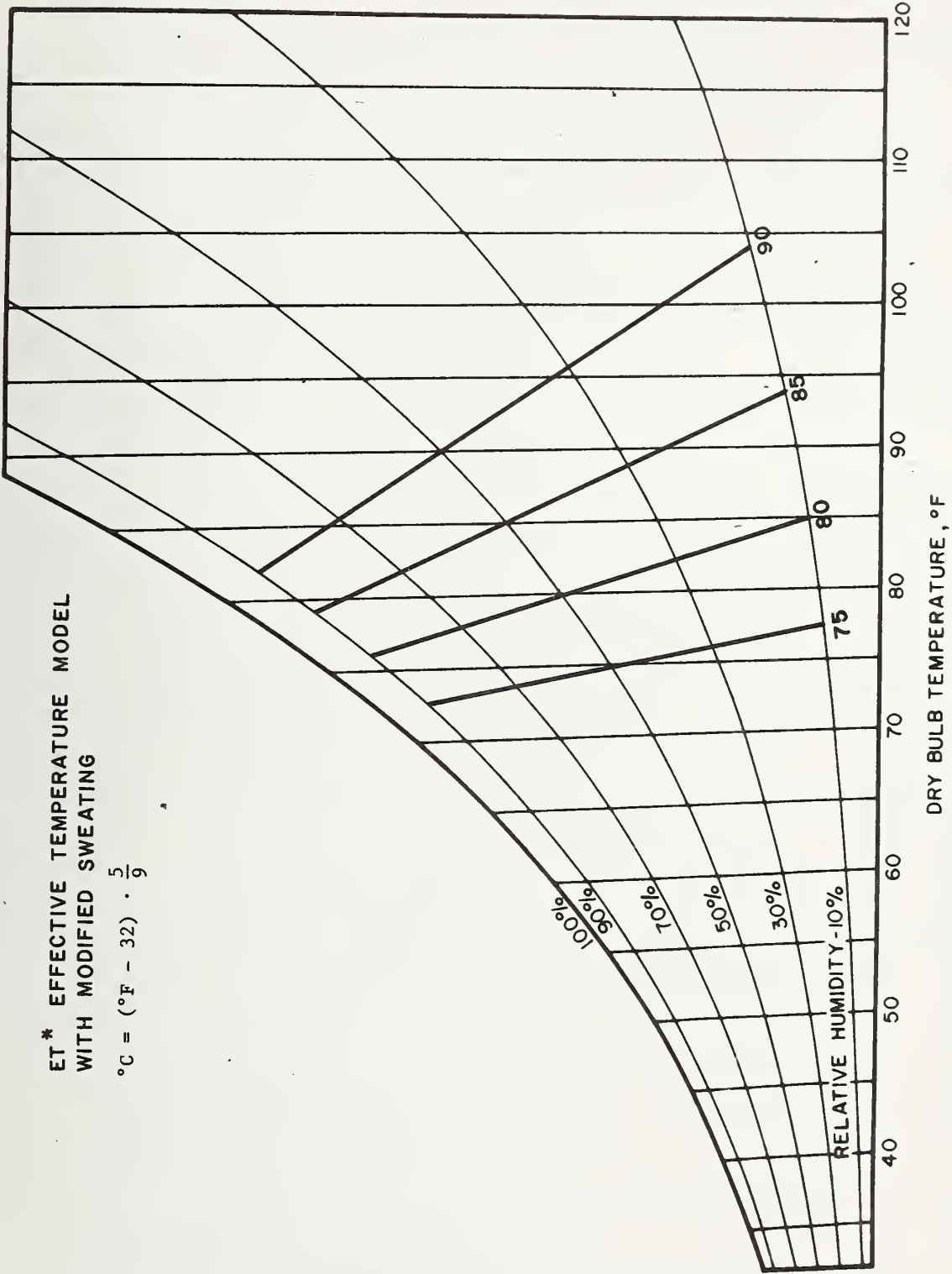


Figure C2 Lines of Constant Effective Temperature (ET\*) With Modified Sweating on a Psychrometric Chart

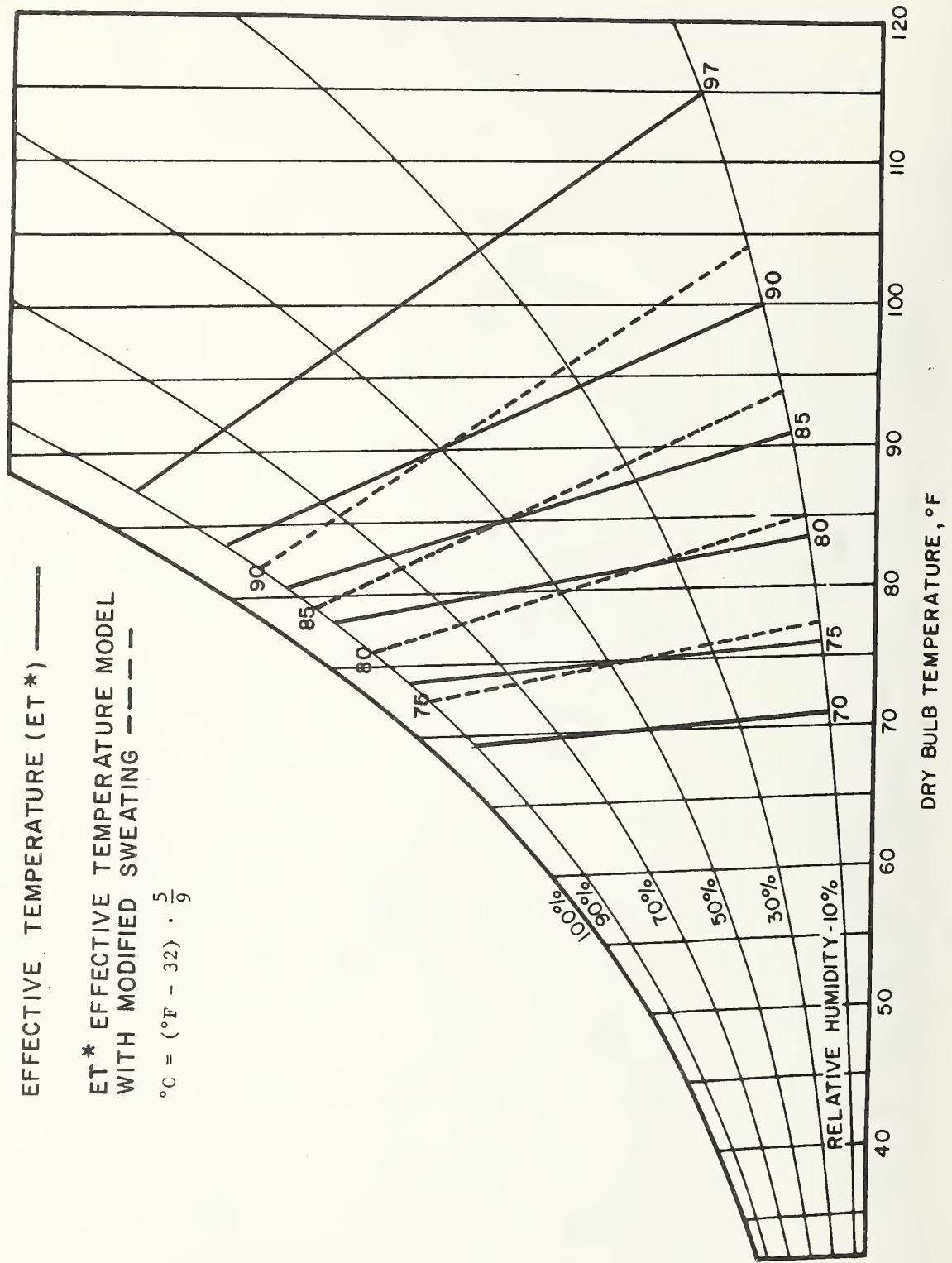


Figure C3 Comparison of the Effective Temperature (ET\*) With the Modified Effective Temperature on a Psychrometric Chart

U.S. DEPT. OF COMM. BIBLIOGRAPHIC DATA SHEET	1. PUBLICATION OR REPORT NO.  NBS BSS 71	2. Gov't Accession No.	3. Recipient's Accession No.
4. TITLE AND SUBTITLE  A Proposed Concept for Determining the Need for Air Conditioning for Buildings Based on Building Thermal Response and Human Comfort		5. Publication Date  August 1975	6. Performing Organization Code
7. AUTHOR(S)  J. E. Hill, T. Kusuda, S. T. Liu, and F. J. Powell		8. Performing Organ. Report No.	
9. PERFORMING ORGANIZATION NAME AND ADDRESS  NATIONAL BUREAU OF STANDARDS DEPARTMENT OF COMMERCE WASHINGTON, D.C. 20234		10. Project/Task/Work Unit No.  4624 141	11. Contract/Grant No.
12. Sponsoring Organization Name and Complete Address (Street, City, State, ZIP)  Department of Housing and Urban Development 451 Seventh Street, S.W. Washington, D. C. 20410		13. Type of Report & Period Covered Final - June 1971 - December 1974	14. Sponsoring Agency Code
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16. ABSTRACT (A 200-word or less factual summary of most significant information. If document includes a significant bibliography or literature survey, mention it here.)  Determining the need for air conditioning can be based on a wide variety of factors. To date, the only criteria that have been written and can be referenced are those of several federal organizations and many are not really criteria in the true sense of the word. They are guidelines to be used in the determination of fund allocation; in other words, provisions are made to air condition federal facilities in specific geographical locations if pertinent weather characteristics of that locality meet certain requirements. This paper presents the concept that a true criteria can be established based both on weather characteristics of the locality as well as characteristics of the building or structure under consideration.  The paper gives the details of a study showing the feasibility of such a scheme. A simulation was made of two proposed residences in several geographical localities. For the simulation, actual hour-by-hour weather data was used in conjunction with a sophisticated computer program. The results revealed for the non air-conditioned spaces, the extent and duration of undesirable indoor conditions based upon generally accepted comfort indices. The concept of a new "comfort" or "discomfort" index called Predicted Indoor Habitability Index (PIHI) is introduced. The authors indicate the way in which a criterion could be established that would be in the form of tables, indicating for a given specified building and geographical locality, whether mechanical cooling should or should not be installed.			
17. KEY WORDS (six to twelve entries; alphabetical order; capitalize only the first letter of the first key word unless a proper name; separated by semicolons)  Air conditioning criteria; building thermal response; comfort indices; human comfort; predicted indoor habitability index			
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