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Interrelations Between Cement & Concrete Properties PART 5

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Interrelations Between Cement and Concrete Properties, Part 5

Freezing-and-Thawing Durability, Saturation, Water Loss and Absorption, Dynamic Modulus

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This publication is dedicated to the memory of Mr. Raymond L. Blaine, who passed away during its preparation. The death of Mr. Blaine brings deep regret to all those associated with him on this project, as well as throughout his career at the National Bureau of Standards. Mr. Blaine was the guilding light and motivating force of this tremendous undertaking for almost twenty years. His inspiration and leadership spanned the period from the project's inception, acquisition of the cements, testing of the cements and concretes, analysis of the data, and publication of most of the results. For this and for his many other accomplishments and contributions in the field of cement and concrete research, including development of the Blaine Air Permeability Fineness Meter, he will long be remembered by colleagues throughout the world.

Abstract

The concretes described in earlier parts of this series were subjected to laboratory freezing and thawing tests, and measurements were made of the weight loss, dynamic modulus, durability factor, and number of cycles required to reach 40 percent reduction in dynamic modulus. Companion specimens were subjected to drying and subsequent soaking in the laboratory and to dynamic modulus tests at various ages and moisture conditions. The effect on these properties of a large number of variables connected with chemical and physical properties of the cements and with properties of the concretes was studied by multivariable regression techniques. Air content of the concretes and degree of saturation generally had the greatest effect on the measurements. In general, minor constituents and trace elements did not show significant relationships with the measured properties, but there was evidence that some of the variables, such as alkali content, water cement ratio, slump, and possibly setting time might have influenced durability through an effect on the air-void system. Specimens stored in the fog room after the freezing-and-thawing tests generally regained most or all of their original dynamic modulus. There were significant differences between cements with respect to regain of dynamic modulus (autogenous healing), with the non-air-entraining cements gaining more than the air-entraining cements, on the average.

Key words: Absorption; autogenous healing; durability factor; dynamic modulus of elasticity; saturation coefficient.

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Section 11. Freezing and Thawing Durability of Concrete R. L. Blaine and H. T. Arni*

The concretes described in earlier parts of this series were subjected to laboratory freezing and thawing tests, and measurements were made of the weight loss, dynamic modulus, durability factor, and number of cycles required to reach 40 percent reduction in dynamic modulus. The degree of saturation achieved during soaking before freezing and thawing was also measured. The results were analyzed to determine which of several variables connected with chemical and physical properties of the cements plus variables connected with the concretes were significant as independent variables in multivariable regression analyses of these measurements. The air content of the concrete was the significant independent variable. Higher percentages of dicalcium silicate (C_2S), K_2O , and MgO were associated with a lower durability factor. An increase in tricalcium aluminate (C_3A) and tetracalcium aluminoferrite (C_4AF) were associated with greater weight loss at 40 percent reduction in dynamic modulus. There was evidence that some of the variables, such as alkali content, water-cement ratio, slump, and possibly setting time, might have influenced durability through an effect on the air-void system. Specimens stored in the fog room after the freezing-and-thawing tests generally regained most or all of their original dynamic modulus, with the non-air-entrained concretes generally gaining more than the air-entrained concretes. There were also significant differences between cements in the amount of autogenous healing.

Key words: Autogenous healing; durability factor; freezing-and-thawing tests; modulus regain; portland cement; saturation ratio; trace elements; weight loss in freezing-and-thawing tests.

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1. Introduction

It has been well established in both laboratory and field tests that concrete made with air-entraining cements, or with hydraulic cements with airentraining agents added at the time of mixing have, among other properties, greater resistance to damage by freezing and thawing than concretes made without air-entraining agents. Bogue [1]¹ reported that "no consistent relation was found between the composition and fineness of the cements and the behavior of concrete exposed to freezing and thawing." This statement was based on reports on the Portland Cement Association Long-Time Study on Cement Performance in Concrete [2].

Concrete [2].

Grieb and Werner [3] in their further study of concretes made of the cements used in the Long-

^{*}Present address: Federal Highway Administration, Washington, D.C. 20590.

¹ Figures in brackets refer to literature references at the end of this section (p. 38).

Time Study concluded that "concrete prepared with cements having tricalcium aluminate (C_3A) content of more than 10 percent had poorer durability than concrete made with cements having C_3A contents of less than 10 percent." Mather [4] reported on freeze-thaw tests on concretes made of the same cements but with an air-entraining agent added and found all highly resistant to damage by freezing and thawing. Oleson and Verbeck [5] found "no evidence of a significant effect of cement composition or fineness, per se, on concrete performance" (when concrete specimens made of these cements were stored outdoors at the Illinois Test Plot for more than 25 years).

Laboratory tests for evaluation of resistance to freezing and thawing are normally made with specimens which have not been permitted to dry [6], whereas concretes in structures usually (but not always) have a period when some of the water evaporates before being subjected to freezing. In concretes that have not been permitted to dry, the size and spacing of small bubbles of entrained air have been shown to be of paramount importance [7.] Concrete specimens that have been allowed to air-dry take some time to become saturated to the extent that they are damaged by the freezing of the water in the concrete.

Various criteria have been used to evaluate the effects of freezing and thawing on concrete. Among these are loss of compressive or flexural strength,

loss of weight, and expansion of the concrete resulting from repeated freezing and thawing.

Hornibrook [8] found that when specimens were left in the thawing water for several days after a freezing-and-thawing cycle, an increase in resonant frequency occurred which was attributed to autogenous healing. Such autogenous healing of concrete partially damaged by freezing has not been fully explored. Present test methods [6] require that concrete specimens be kept in a frozen condition when the sequence of freezing and thawing cycles is interrupted.

The present investigation was undertaken to determine whether the chemical composition of the cements was associated directly or indirectly with the durability factor calculated from freezingand-thawing tests or with weight loss of concrete which had been partially air dried and then resoaked prior to freezing. In view of the fact that the degree of saturation of the concrete plays such and important role in the results of freezing-andthawing tests, studies were made of the factors associated with a calculated saturation ratio of the concretes. Studies were also made to determine the extent of recovery of the dynamic modulus of concretes (autogenous healing) after the freezingand-thawing tests had been completed. Because of the limited quantities of the various cements available it was not possible to make additional tests with air-entraining agents added.

2. Materials

2.1. Cements

The cements used in this investigation have previously been described. The frequency distributions of the results of chemical analyses as well as spectrochemical analyses were reported in part 1, sections 2 and 3, of this series of articles [9], and other tests with these cements have been reported in parts 2, 3, and 4 [10, 11, 12]. Most of the 199 commercial portland cements were obtained from different areas of the United States, but a few came from other countries. The cements were classified as to type on the basis of chemical and physical properties.²

2.2. Aggregates

The coarse and fine aggregates are described in part 1, section 1 [9] of this series of papers. A high quality, 1-in maximum size, rounded, quartzite, coarse aggregate (White Marsh) and a sand from the same source were used for making the concretes. The fineness modulus of the sand was 2.82, of the coarse aggregates 6.82, and of the combined aggregates 4.82.

3. Methods of Test

3.1. Preparation of Concretes

The details of the proportioning and mixing of the concretes were described in part 1, section 1, of this series of articles [9].

Two series of concretes were made with these cements. One series (Series O) was made with a constant water/cement ratio of 0.635. A second series (Series A) was made in which the water content was changed, if necessary, to obtain a concrete with a 5 ± 1 -in slump. In the two series,

the cement-to-aggregate ratio was the same. The cement factor varied to some extent from the nominal $5\frac{1}{2}$ bags of cement per cubic yard, primarily because of variations of the entrained and entrapped air.

3.2. Test Specimens

Eight $3- \times 4- \times 16$ -in specimens were made from each of the cements, four in each of the two series of concretes. These were made from the same batches of concrete as those used for the $6- \times 8- \times 16$ -in specimens used for shrinkage and

 $^{^2}$ On the basis of this classification, there were 82 Type I, 8 Type IA, 68 Type II, 3 Type IIA, 20 Type III, 3 Type IV, and 12 Type V cements.

expansion tests [12]. The specimens were cast in steel molds in accordance with ASTM Designation C 192–52T procedures [13] except that the molds were lined with sheet plastic and no oil or grease was used. Two of the 3- by 4- by 16-in specimens were subjected to laboratory freezing-and-thawing tests, and the other two were placed in the field for natural weathering tests.

3.3. Storage of Specimens

The 3- \times 4- \times 16-in concrete specimens were covered with moist burlap for the first 20 to 24 hours, then removed from the molds and placed in a fog room at 100-percent relative humidity (RH). At the age of 14 days, the specimens were removed from the fog room and stored on end in laboratory air at 73 °F and 50-percent relative humidity for 4 weeks. After this drying period, the two specimens from each batch which were to be subjected to laboratory freezing-and-thawing tests were placed in water at 40 °F. After 24 hours soaking the freezing-and-thawing tests were started. The weight, fundamental resonant frequencies, and dynamic Young's modulus of elasticity (dynamic E) were determined at 1 and 14 days, at the time just prior to placing in the 40 °F water, at the start of the freezing cycle, and at periodic intervals during the freezing-and-thawing tests. The fundamental transverse resonant frequencies were determined in accordance with ASTM Designation C 215 [14]. After completion of the freezing-and-thawing tests the specimens were placed in the fog room at 100-percent RH, and resonant frequency measurements were again made after storage periods ranging from approximately one to five years.

3.4. Freezing-and-Thawing Cycles

The two duplicate concrete specimens from each concrete batch were frozen in water at 0 °F and thawed in water at 40 °F with each cycle completed in two hours in accordance with ASTM Designation C 290 [15]. The freezing and thawing tests were continued until there was a 40 percent

reduction in dynamic modulus.

The calculations of dynamic Young's modulus of elasticity took into account the weights of the specimens and the fundamental resonant frequencies, but no corrections were made for possible variations of Poisson's ratio nor for dimensional changes caused by sloughing of the specimens. In other words, instead of the ratio of the squares of the resonant frequencies being used as suggested in C 290, the following formula was used for relative dynamic modulus:

$$P_c = \frac{W_1 n_1^2}{W n^2} \times 100$$

where P_c = relative dynamic modulus of elasticity, percent, after c cycles of freezing and thawing

W = weight at 0 cycles of freezing and thawing

 W_1 = weight after c cycles of freezing and thawing

n = resonant frequency at 0 cycles of freezing and thawing, and

 n_1 = resonant frequency after c cycles of freezing and thawing.

3.5. Durability Factor

Durability factors (DF) were calculated using the formula given in ASTM Designation C 290 based on a termination of the tests at 300 cycles of freezing and thawing or 60 percent relative dynamic modulus. In many instances, with the concretes made with air-entraining cements, the freezing-and-thawing tests were continued past 300 cycles in order to obtain the 40 percent reduction in dynamic modulus. The values for the two duplicate specimens from each series were averaged.

3.6. Saturation Ratio

The saturation ratio was calculated from the weight lost during 28 days drying in laboratory air, the weight gained during 24 hours soaking at 40 °F (prior to freezing and thawing), and the volume of air measured in the plastic concrete. The weight lost during drying and the weight gained during soaking, in grams, were taken as the water gained and lost in ml. The percentage of air, determined gravimetrically in the plastic concrete, multiplied by the volume of the specimens in ml was taken as the volume of air in the plastic concrete. The measured volume of air plus the volume of water lost during drying was taken as the total volume of air voids in the hardened concrete available to take up water. The ratio of the volume of water gained during soaking to the total volume of air voids is the saturation ratio. These values were considered as the degree of saturation at the start of the freezing-and-thawing tests. The ratios ranged from about 0.4 to 0.8 for non-air-entrained concrete and 0.2 to 0.4 for airentrained concretes.

3.7. Recovery of Dynamic Modulus After Freezing-and-Thawing Tests

Autogenous healing of the concrete specimens after freezing-and-thawing tests was evaluated by studying the ratio of dynamic modulus after various periods of moist storage following the freezing-and-thawing tests.

4. Abbreviations

The abbreviations, notations, etc., used in this section for chemical and physical properties of the cements are the same as those used in previous

sections of this series of articles.3

In this section, the prefix "O" of the four-letter titles for the various dependent variables refers to the concretes of Series O in which a water/cement ratio (w/c) of 0.635 was used. The prefix "A" refers to the second series of concretes in which the water was readjusted, if necessary, to give a 5 ± 1 -in slump. The abbreviations for the dependent variables used in this section are as follows:

For Series O concretes made with a w/c of 0.635 ODUR = durability factor of concrete specimens which had been air-dried then subjected to rapid freezing and thawing in water.

OWTL = weight loss of concrete specimens at the time of 40 percent loss of dynamic modulus expressed as percent of weight at 0 cycles of freezing and thawing.

OSAT = ratio of volume of water absorbed in 24 hours (prior to start of freezing test) to possible absorption.

OAIR = air content in percent by volume OCYS = number of freezing-and-thawing cycles required to cause a 40 percent reduction in dynamic modulus.

For Series A concretes having a 5 \pm 1-in slump, the letter "A" is used instead of "O" as ADUR, AWTL, ASAT, AAIR, and ACYS for the different variables.

5. Statistical Analyses

The statistical techniques used to find and evaluate the independent variables associated with the durability factor, weight loss, saturation, and dynamic modulus ratios have been described in a previous section of this series entitled "Materials and Techniques" [9]. The statistical treatment was the same as that used in all previous sections of this series of articles. Multiple regression equations were calculated by the method of least squares using various independent variables. As in previous sections, equations were calculated for both AE + NAE cements and NAE cements. Comparisons were made using only commonly determined variables and also using these together with minor and trace elements.

Ratios of reduction in variance to original variance ("F" ratios) obtained by fitting equations were calculated for two kinds of cases: (1) for equations including one or a few main independent variables as compared to the original data on the dependent variable, or (2) for equations in which additional independent variables were included as compared to a previous equation with fewer variables⁴. The "F" ratios and critical "F" values which, when equalled or exceeded, indicate sig-

nificance at the $\alpha = 0.05$ and $\alpha = 0.01$ levels are summarized in table 11–27.

After it had been determined which independent variables were significantly associated with the dependent variable when used in an equation, the residuals of the equation were fitted by the method of least squares to other single independent variables and the reduction in variance calculated. If any of the additional independent variables indicated a significant reduction in variance, they were tried in the equation and retained if the coef./s.d. ratio was greater than 1.0.

Equations were also computed for the "odds" and "evens" in the array of cements. Comparisons were made of the coefficients of the variables in the two groups of cements, and these were compared to the coefficients and coef./s.d. ratios

computed for all the cements.

Although freezing-and-thawing tests were made on all 199 cements, the calculations of the equations presented in this article were limited to those for which trace elements had been determined.

Equations presented in this article were selected from a large number of trial equations indicating the calculated relationship of various independent variables to durability and degree of saturation. These equations were selected primarily to indicate the association with dependent variables of commonly determined variables having coef./s.d. ratios greater than 1.0 when used in multivariable equations, and also to indicate which of the minor and trace elements might have had an effect.

Some of the limitations on interpretations of multivariable regression equations have been discussed in part 1, section 1, subsections 4.2, 4.3, and 5 [9]. Other limitations and problems of interpretation have also been discussed in other sec-

tions of this series of articles.

³ These abbreviations include the use of C₃A, C₃S, C₂S and C₄AF for the calculated potential compounds, tricalcium aluminate, tricalcium silicate, dicalcium silicate, and tetracalcium aluminoferrite, respectively. Insol for insoluble residue, Loss for loss on ignition, APF for air permeability fineness, and Wagn for Wagner turbidimeter fineness are also used. AE + NAE refers to airtentraining plus non-air-entraining cements, and NAE to the non-air-entraining cements.

⁴Statistical terms and notations employed in this section are the same as those used in previous sections of this series of articles. For example, S.D. refers to the estimated standard deviation calculated from the residuals of a fitted equation, or the estimated standard deviation about the average. Also, as in previous sections, s.d. refers to the estimated standard deviation of a coefficient of an independent variable used in a fitted equation. The term coef./s.d. is the ratio of the estimated coefficient (of an independent variable used in an equation) to its estimated standard deviation. "DF" designates degrees of freedom. As indicated in previous sections, a coef./s.d. ratio greater than 1.0 was considered to be of sufficient significance to warrant further investigation.

Table 11-1. Frequency distribution of cements with respect to durability factor of concretes having a nominal 5 ½ bags cement per cubic yard and a water-cement ratio of 0.635 (ODUR)

					D	urability fa	ctor				
Type cement	0 to 10	10 to 20	20 to 30	30 to 40	40 to 50	50 to 60	60 to 70	70 to 80	80 to 90	90 to 100	Total
					Nu	mber of cer	nents				
	10	23	28	16	3	2			2		82
II II IIA	12	22	25	5	2	2		4	3		8 68 3
III IIIA	4	5	4	3	2	2			3	·	20
IV, V	4	8	3								15
Total	30	58	60	24	7	6	1	4	8	1	199

6. Results of Tests

6.1. Durability Factor

6.1.1. Durability Factor of Series O Concretes

The frequency distribution of the durability factors of concretes made with a water-cement ratio of 0.635 (ODUR) is presented in table 11–1. The concretes made with air-entraining cements Types IA, IIA, and IIIA all had higher durability-factor values than did those made with the non-air-entraining cements. There was a fairly broad distribution of values and there was an overlapping of the values of the concretes made with different types of NAE cements. Eighty percent of the non-air-entrained concretes had durability factors below 30, while all of the air-entrained concretes had durability factors greater than 60.

Equations selected from those computed to determine the various independent variables associated with the durability factor are presented in table 11-2. The use of the air content in eq 1, or the saturation coefficient at the start of the freezing-and-thawing tests (OSAT) in eq 2, as independent variables each resulted in a highly significant reduction in variance. (See table 11–27). With the use of the air content and the additional use in equation 3 of C₃S, C₂S, Na₂O, K₂O, MgO and fineness, all commonly determined independent variables, there was a significant reduction in variance. Of the trace elements, Ba, Rb, Pb, Ti, and Cu had coef./s.d. ratios greater than 1.0 when used with commonly determined independent variables in the multivariable regression equation as indicated in eq 4. Use of the trace elements in the equation resulted in a highly significant reduction in variance. (See table 11-27). In eqs 4A and 4B, calculated for the "odds" and "evens" in the array of cements, Pb and Cu, as well as C₃S and fineness had coef./s.d. ratios less than 1.0 in one or the other of the smaller groups of cements⁵.

Equations 5 and 6, calculated using SiO₂ instead of C₃S and C₂S, also resulted in a reduction in variance significant at the 1.0 percent level. The use of the trace elements in addition to the commonly determined variables in eq 6 resulted in a significant reduction in variance. (See table 11–27). In the equations for the "odds" and "evens" (eqs 6A and 6B) fineness, Ba, and Pb had coef./s.d. ratios less than 1.0 in one or the other of the smaller groups of cements.

Equations calculated for the NAE cements are presented in table 11–3. The coefficients for the air content and saturation coefficient in eqs 1 and 2 respectively were highly significant, but the coef./s.d. ratios were lower than when the AE cements were included as in table 11-2. The coefficients for the other independent variables in eqs 3, 4, 5, and 6 of table 11–3 are in reasonable agreement with those of the previous table. Using commonly determined variables in eqs 3 and 5 resulted in highly significant reductions in variance, and the use of trace elements in eqs 4 and 6 each resulted in highly significant reductions in variance as a result of the added independent variables. It may noted, however, that in equations for the "odds" and "evens" eqs 4A, 4B, 6A, and 6B, C₃S, Na₂O, fineness, Ba, and Pb had coef./s.d. ratios less than 1.0 in one or the other of the equations for the smaller groups of cements.

The estimated contributions and ranges of contributions to the durability factor of the various independent variables calculated from the coefficients of eq 4 table 11–3 are presented in table 11–4. The ranges of the independent variables were assumed to be the same as for all 199 cements previously described in sections 2 and 3 of this series [9]. An increase in air content of the NAE cements resulted in an increase in the durability factor. Increase in C₃S, K₂O, MgO, fineness, Rb, Ti, and Cu was associated with a decrease in the durability factor. The coefficients of C₃S, Na₂O, Ba and Pb were of doubtful significance as the coef./s.d. ratios were less than 2.0.

⁶ As has been indicated in previous sections, chance occurrence of two or more extreme values in one of the two groups may cause such anomalous results. Another possible contributing factor was the assignment of zero to values for trace elements having less than the lowest reported value.

Table 11-2. Coefficients for equations for AE + NAE cements relating the freeze-thaw durability factor for concretes of nominal 5½ bags of cement per cubic yard and a water-cement ratio of 0.635 to various independent variables (ODUR)

S.D.	11.18	13.24	9.72	9.14	9.46	9.05	9.73	9.12	9.56	9.01
OSAT	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	-127.6 (10.4)	 				1 1	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1		
Cu	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1			-209.5 (83.5)	* -111.9 (118.6)	-290.2 (133.1)		-216.1 (82.5)	$\frac{-159.8}{(116.1)}$	-289.5 (132.5)
T				-14.05 (6.01)	-13.71 (7.68)	-10.95 (10.56)		-14.44 (5.97)	-15.82 (7.66)	$-11.04 \ (10.51)$
Pb	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1			-208.3 (116.6)	-240.2 (134.0)	$^* - 136.6$ (309.3)		-204.3 (116.2)	-227.5 (135.2)	*-148.3 (306.7)
Rb	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1		1 1	1068 (416)	-892 (557)	-1492 (698)	1 1	-1095 (413)	$-952 \\ (561)$	-1428 (683)
Ba				-40.24 (21.59)	-38.79 (36.07)	-44.98 (29.80)		-39.31 (21.50)	* -34.83 (36.37)	-45.61 (29.61)
C_3S C_2S SiO_2 Na_2O K_2O MgO APF Ba	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1		-0.00207 (0.00156)	-0.00306 (0.00149)	*-0.00082	-0.00469 (0.00226)	-0.00162 (0.00152)	-0.00285 (0.00145)	*-0.00052 (0.00227)	-0.00520 (0.00201)
MgO	1 1		$\frac{-1.932}{(0.707)}$	-2.750 (0.690)	$\frac{-2.758}{(1.057)}$	-2.911 (0.986)	$\frac{-2.176}{(0.677)}$	-2.886 (0.655)	$\frac{-3.111}{(1.045)}$	-2.703 (0.895)
K20		1 1	-22.84 (4.08)	-20.29 (4.24)	-13.48 (6.51)	-26.98 (6.18)	-24.05 (3.97)	-20.85 (4.15)	$\frac{-16.72}{(6.27)}$	$\begin{vmatrix} -27.01 \\ (6.15) \end{vmatrix}$
Na20			-7.211 (4.562)	-8.258 (4.329)	-7.159 (5.921)	-11.135 (6.891)	-8.246 (4.492)	-8.758 (4.260)	-8.381 (5.938)	-10.370 (6.661)
SiO ₂						1 1	-3.108 (0.690)	-2.589 (0.661)	-2.093 (0.961)	(0.984)
C ₂ S	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1		-0.9197 (0.2735)	-0.8174 (0.2626)	-0.4100 (0.3828)	-1.1383 (0.3934)				
C3S	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1		-0.5263 (0.2968)	-0.5301 (0.2847)	*-0.0299 (0.4017)	-0.9782 (0.4629)				1
Air	+8.241 (0.490)		+8.901 (0.448)	+8.887 (0.426)	+8.785	$^{+9.126}_{(0.601)}$	+8.929	+8.899 - (0.425)	+8.788	+9.121 (0.598)
Const.	= +8.577 = (1.306)	= +101.4 = (6.3)	= +80.01 = (23.93)	= +88.58 = (22.92)	d) = +42.69 = (33.81)	en) = +127.59 = (33.75)	= +98.20 = (18.97)	= +98.20 = (17.88)	d) = +78.54 = (26.29)	ODUR (even) = $+117.06$ s.d. = (25.96)
	ODUR s.d.	ODUR s.d.	ODUR s.d.	ODUR s.d.	ODUR (odd) s.d.	ODUR (even) s.d.	ODUR s.d.	ODUR s.d.	ODUR (odd) s.d.	ODUR (ev.
Note	1	1	1	-	67	8	-	-	67	ಣ
Eq.	1	2	es	4	4A	4B	5	9	6A	6B

Note 1, 179 cements, Avg. = 25.44, S.D. = 17.97 Note 2, 90 cements Note 3, 88 cements *Coef./s.d. ratio less than 1.0.

TABLE 11—3. Coefficients for equations for NAE cements relating the freeze-thaw durability factor of concretes of nominal 5 ½ bags cement per cubic yard and a water-cement remains independent variables (ODUR)

						areo of o.	na 00 cco	rrous me	namuada	n var eau	rated of 0.035 to various independent variables (OD OIL)	(1)						
Eq.	Note		Const.	Air	CaS	C ₂ S	SiO ₂	Na ₂ O	K20	MgO	APF	Ba	Rb	Pb	Ë	Cu	OSAT	S.D.
1	1	ODUR s.d.	= +15.25 = (2.02)	+3.957 (1.113)														10.85
2	-	ODUR s.d.	= +58.93 = (6.16)						1 1			1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	1 1		1 1	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	-60.88 (10.02)	10.18
3	1	ODUR s.d.	= +82.38 = (24.29)	+5.436 (1.057)	-0.4817 (0.3024)	-0.8846 (0.2775)	1 1	-4.690 (4.617)	-19.75 (4.21)	-2.089 (0.712)	-0.00253 (0.00158)					1 1	1 1 1 1 1 1 1 1 1 1 1 1	9.55
4	1	ODUR s.d.	= +93.54 = (23.82)	+6.830 (1.062)	-0.5456 (0.2964)	-0.8319 (0.2712)	1 1	-7.094 (4.480)	-19.34 (4.42)	-2.866 (0.713)	-0.00346 (0.00154)	$\begin{bmatrix} -37.03\\ (21.87) \end{bmatrix}$	-883 (427)	-190.6 (116.9)	-14.72 (6.26)	-176.9 (85.8)	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	9.13
4A	67	ODUR (odd) s.d.	= +81.12 = (32.82)	+7.513 (1.540)	*-0.3122 (0.4153)	-0.5951 (0.3769)		-8.208 (5.693)	-14.80 (6.57)	-2.839 (1.058)	-0.00541 (0.00205)	-46.87 (25.38)	-895 (622)	* -351.1 (444.2)	$-13.95 \ (10.51)$	-185.9 (113.9)		90.6
4B	67	ODUR (even) s.d.	= +93.15 = (37.84)	+6.863	-0.5990 (0.4569)	(0.4263)	1 1 1 1 1 1 1 1 1 1	*-4.199	-24.34 (6.86)	-2.996 (1.126)	*-0.00130 (0.00255)	*-48.32 (52.76)	-890 (677)	-137.2 (134.0)	-11.83 (8.57)	-183.3 (143.9)		9.56
	1	ODUR s.d.	= +102.92 = (19.04)	+5.596 (1.053)			-3.074 (0.693)	-5.923 (4.541)	-21.25 (4.08)	-2.359 (0.682)	-0.00207 (0.00155)		1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1			9.57
9	1	ODUR s.d.	= +102.86 = (18.26)	+6.933 (1.046)	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	1 1	-2.623 (0.676)	-7.643 (4.387)	-19.96 (4.29)	-3.000 (0.672)	-0.00330 (0.00150)	-36.56 (21.81)	-917 (422)	-187.3 (116.5)	-15.24 (6.19)	-185.0 (84.3)	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	9.12
6A	ç1	ODUR (odd) s.d.	= +97.47 = (24.35)	+7.602 (1.529)	1 1 1 1 1 1 1 1 1 1	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	-2.139 (0.913)	-9.112 (5.547)	$-16.25 \ (6.26)$	-3.057 (1.009)	(0.00198)	-45.71 (25.24)	-972 (610)	* -320.5 (440.3)	-14.32 (10.46)	-202.3 (1111.0)	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	9.03
6B	¢1	ODUR (even) s.d.	= +106.71 = (31.02)) +7.102	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	-3.126 (1.114)	*-5.527 (8.087)	-24.64 (6.81)	-3.174 (1.080)	*-0.00105 (0.00251)	* -47.03 (52.51)	-937 (671)	-135.4 (133.4)	-13.19 (8.27)	-189.3 (142.8)		9.52

Note 1, 168 cements, Avg. = 21.80, S.D. = 11.22 Note 2, 84 cements *Coef./s.d. ratio less than 1.0.

Table 11-4. Calculated contributions of independent variables to the durability factor of concretes having a nominal 51/2 bags cement per cubic yard and a water cement ratio of 0.635 (ODUR)

Independent variables	Ranges of variables, (percent)	Coefficients from eq 4 table 11-4	Calculated contributions to ODUR	Calculated range of contribu- tions to ODUR
Air content NAE cements CaS CaS Na ₂ O** K ₂ O MgO APF. Ba** Rb Pb** Ti Cu	0 to 4.5 20 to 65 5 to 50 0 to 0.7 0 to 1.1 0 to 5 *2500 to 5500 0 to 0.01 0 to 0.05 0 to 1.0 0 to 0.05	+6.830 -0.5456 -0.8319 -7.094 -19.34 -2.866 -0.00346 -37.03 -883 -190.6 -14.72 -176.9	$\begin{array}{c} \text{Const.} = \ +94 \\ 0 \ \text{to} \ +31 \\ -11 \ \text{to} \ -35 \\ -4 \ \text{to} \ -42 \\ 0 \ \text{to} \ -5 \\ 0 \ \text{to} \ -5 \\ 0 \ \text{to} \ -14 \\ -9 \ \text{to} \ -14 \\ -9 \ \text{to} \ -7 \\ 0 \ \text{to} \ -8 \\ 0 \ \text{to} \ -10 \\ 0 \ \text{to} \ -15 \\ 0 \ \text{to} \ -8 \end{array}$	31 24 38 5 21 14 10 7 8 10 15

* cm²/g.

** Coefficient of doubtful significance as coef./s.d. ratio was less than 2.0.

Somewhat different values may be obtained by use of other equations presented in table 11-3 for NAE cements and also by use of equations in table 11-2 for AE + NAE cements. Other tables of the estimated contributions are, for the sake of consistency, presented for the NAE cements. In all instances, an equation having potential compounds and all other independent variables having coef./s.d. ratios greater than 1.0 will be used. In subsection 7, a summary table is also presented of equations for the AE + NAEcements.

6.1.2. Durability Factor of Series A Concretes

The frequency distribution of the durability factors of concretes made with sufficient water for a 5 \pm 1-in slump (ADUR) is presented in table 11-5. All but two of the 14 concretes made with the air-entraining cements had durability factors higher than those for concretes made with any of the non-air-entrained cements and 78 percent of the non-air-entrained concretes had durability factors below 30. There was an overlapping of the durability values of the NAE concretes made with the different types and a broad distribution of results.

The equations relating the durability factor of AE + NAE cements to the independent variables are presented in table 11-6. Equations 1 and 2 indicate the relationships of the air content and the saturation ratio (ASAT) respectively to the durability factor. The coefficients of both independent variables were highly significant, and in both equations there were highly significant reductions in variance. (See table 11–27).

The use of air content together with other commonly determined variables C₃S, K₂O, MgO, and APF in eq 3 resulted in a further significant reduction in variance, and the additional use of the trace elements Ba, Rb, Pb, Ti, and Cu in eq 4 resulted in a further reduction in variance, sig-

nificant at the 1.0 percent level. (See table 11-27, p. 00.) C₃S and Na₂O had coef./s.d. ratios less than 1.0 when included with the other variables with the 5 ± 1 -in slump concretes but greater than 1.0 in the equations in table 11-2 for the 0.635 w/c concretes.

The use of the oxides CaO and SiO₂ as independent variables (eq 5) together with other commonly determined variables, K₂O, MgO, and fineness, resulted in an S.D. value comparable with that of eq 3 where C₂S was used, and a highly significant reduction in variance was obtained. (See table 11–27.) The fineness of the cements had a coef./s.d. ratio less than 1.0 when included with the other variables in eq 5 but between 1.0 and 2.0 in eq 6. When fineness was used as an independent variable together with the trace elements and other commonly determined variables (eq 6), there was a reduction in variance significant at the 1.0-percent level although the coefficients of none of the added independent variables were, individually, highly significant.

In equations for the "odds" and "evens," eqs 4A, 4B, 6A, and 6B, there were instances where CaO, MgO, fineness, Ba, Pb, Ti, and Cu had

coef./s.d. ratios less than 1.0.

The equations presented in table 11–7 indicate the independent variables associated with the durability factor for concretes having a 5 ± 1 -in slump and made from NAE cements. The same independent variables had coef./s.d. ratios greater than 1.0 as in table 11–6 where the AE cements were included. The use of commonly determined variables (eqs 3 and 5) resulted in highly significant reductions in variance, and with the use of the trace elements and fineness in eqs 4 and 6, a further reduction in variance was obtained (See table 11-27.) In equations for the "odds" and "evens," eqs 4A, 4B, 6A, and 6B, there were instances where CaO, fineness, and all of the trace elements had coef./s.d. ratios less than 1.0 in one or the other of the smaller groups of cements.

The estimated contributions and ranges of the contributions to the durability factor of concretes having a 5 \pm 1-in slump calculated from the coefficients of eq 4, table 11-7 are presented in table 11-8. Increased air content was associated with increased durability. Increases in C₂S, K₂O, MgO, and possibly fineness, Ti, and Cu were associated

with lower durability factor values.

6.2. Weight Loss at 40 Percent Reduction of Dynamic Modulus

6.2.1. Weight Loss of Series O Concretes

The frequency distribution of weight loss of the Series O concrete specimens (OWTL) at the time of 40 percent reduction of dynamic modulus in the freezing-and-thawing test is presented in table 11–9. These concrete specimens were made using a water-cement ratio of 0.635. There was actually a slight weight gain with 11 of the concretes and

Table 11-5. Frequency distribution of cements with respect to durability factor of concretes having a nominal 5 ½ bags cement per cubic yard and a slump of 5 ± 1 inches (ADUR)

					Durabili	ty factor				
Type cement	0 to 10	10 to 20	20 to 30	30 to 40	40 to 50	50 to 60	60 to 70	70 to 80	80 to 90	Total
				1	Number	of cements	I			
I	8	27	22	15	4	2 2	1	3	3	79
II.	12	19	26	7	1	ī	1		2	67 3
III	3	4	6	2	3	1	1		3	20 3
IV, V	4	7	2	2						15
Total	27	57	56	26	8	6	3	4	8	195

a loss of up to 20 to 22 percent with other concretes.

The specimens which showed a weight gain were all specimens which failed very rapidly in the freezing-and-thawing test. One-day soaking in water at 40 °F is not sufficient to saturate the specimens, as is shown below by the saturation ratios. Thus all the specimens showed weight gain in the first few cycles of freezing and thawing as the process of freezing in water forced water into unfilled pores of the concrete. Then weight losses occurred as the surface sloughed off with continued freezing-and-thawing cycles. The only specimens which showed a weight gain, consequently, were those that failed in the first few cycles while they were still taking up water and before sloughing had started.

The concretes made with the AE cements had weight-loss values above the mean for all cements. There was an overlapping of the values of the

different types of cements.

The equations for AE and NAE cements relating weight loss of the concrete specimens at the time of 40 percent reduction of dynamic modulus to various independent variables are presented in table 11–10. Equation 1 indicates that increased air content was associated with increased weight loss. The use of other commonly determined variables C₃A, C₄AF, Na₂O, and K₂O (in addition to the air content) (eq 2) resulted in a significant reduction in variance. With the additional use of the trace elements Rb, Pb, Ti, and Zr (eq 3) a further reduction in variance significant at the 1.0 percent level was attained. (See table 11–27.) In equations 3A and 3B calculated for the "odds" and "evens" in the array of cements, Rb, Ti, and Zr had coef./s.d. ratios less than 1.0 in one or the other of the smaller groups.

The use of Al₂O₃, Fe₂O₃, SO₃ and Al₂O₃/SO₃ (eq 4) instead of C₃A and C₄AF as in eq 2, together with Na₂O and K₂O, the other commonly determined independent variables, also resulted in a significant reduction in S.D. value. (See table 11–27.) By using the trace elements Rb, Pb, Ti, Zr, and Cr in eq 5, a further significant reduction in variance was obtained. Each of these trace

elements, as well as Al_2O_3 , SO_3 , and the Al_2O_3/SO ratio had coef./s.d. ratios less than 1.0 in one or the other of the equations for the "odds" and "evens" (eqs 5A and 5B).

Table 11–11 shows a series of equations for the weight loss at the time of 40 percent reduction of dynamic modulus of NAE cements. As indicated in eq 1, the coef./s.d. ratio of the air content was less than 1.0. When used with other commonly determined independent variables (eqs 2 and 4) the coef./s.d. ratio was greater than 3.0. The use of the commonly determined variables (eqs 2 and 4) resulted in highly significant reductions in variance. The additional use of trace elements Rb, Pb, Ti, and Zr (eq 3), or these together with Cr (eq 5) resulted in reductions in variance significant at the 1.0 percent level (See table 11–27). In eqs 3A, 3B, 5A, and 5B calculated for the "odds" and "evens," Rb, Zr, and Cr as well as Al₂O₃, SO₃, and Al₂O₃/SO₃ had coef./s.d. ratios less than 1.0 in one or the other or both of the equations calculated for the smaller groups.

Estimated contributions and ranges of contributions to the percentage weight loss of concretes made with NAE cements at the time of 40 percent reduction of dynamic modulus as calculated from the coefficients of eq 3, table 11–11, are presented in table 11–12. Increases in air content, C₃A, and C₄AF were associated with an increase in the weight loss. Increases in K₂O and possibly Na₂O, Rb, Pb, and Ti were associated with a decrease in

the weight loss.

6.2.2. Weight Loss of Series A Concretes

The frequency distribution of the weight loss of Series A concrete specimens (AWTL) at the time of 40 percent reduction of dynamic modulus in the freezing-and-thawing tests is presented in table 11–13. These concretes were made with sufficient water to produce a 5 ± 1 -in slump. The specimens made with the air-entraining cements all had weight-loss values above the average for all specimens, but there was some overlapping with the concretes made with NAE cements. There was an overlapping of the groups of values

Table 11-6. Coefficients for equations for AE + NAE cements relating the freeze-thaw durability factor for concretes of nominal 5 ½ bags cement per cubic yard and a slump of 5 \pm 1 inch to various independent variables

	S.D.	11.87	12.86	10.57	10.08	10.47	9.63	10.55	10.09	10.44	9.61
	ASAT		(9.1)								
	Cu		1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1		(92.2)	(130.0)	*-125.5	1 1	(93.6)	(136.1)	*-122.8 (139.61)
	F		1 1		-12.55 (6.77)	-17.41 (8.44)	$\frac{-16.03}{(13.79)}$		-13.18 (6.77)	-17.48 (8.33)	*-13.74 (13.78)
	Pb		1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1		-204.1 (128.0)	$\frac{-215.6}{(189.5)}$	*-165.2 (180.3)	1 1	-184.9 (128.7)	$\frac{-208.7}{(189.2)}$	*-121.2 (181.7)
	Rb		1 1		-895.2 (461.1)	-861.1 (664.5)	-763.4 (657.0)	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	-988.6 (462.3)	-844.5 (672.2)	-815.6 (654.4)
	Ba				(23.53)	-112.37 (36.40)	* -1.71 (33.47)		-40.55 (23.77)	-112.55 (39.00)	*-5.304
	APF		1 5 1 1 1 1 1 1 1 1 1	(0.00170)	-0.00297 (0.00164)	* -0.00136 (0.00254)	-0.00390 (0.00236)		-0.00230 (0.00159)	*+0.00019 (0.00265)	-0.00292 (0.00208)
and and	MgO	1 1		-1.528 (0.739)	-2.378 (0.735)	-2.971 (1.106)	-1.935 (1.016)	(0.977)	-2.160 (0.981)	*-1.493	(1.378)
	K20	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	3 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	-17.35 (4.02)	-15.93 (4.37)	-23.79 (6.02)	-10.95 (7.05)	-18.29 (4.33)	-17.51 (4.75)	-22.03 (6.56)	-12.86 (7.36)
200000	SiO_{z}	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1		1 1			1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	-3.040 (0.700)	-2.727 (0.732)	-1.616 (1.231)	(0.968
S	CaO	1 1	1 1	1 1	1 1 1 1 1 1	1 1	1 1	+1.945 (0.973)	+1.284 (0.956)	+3.026 (1.540)	*+0.504 (1.302)
	CSS	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	1 1	-0.5768 (0.1215)	-0.4679 (0.1185)	-0.4051 (0.1745)	-0.4749 (0.1752)	1 1			1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1
	Air	+7.217 (0.473)	1 1	+7.760 (0.437)	+7.820 (0.424)	+8.582 (0.686)	+7.519 (0.545)	+7.735	+7.809	+8.597	+7.427 (0.542)
	Const.	= +12.18 = (1.29)	= +98.06	= +44.21 = (8.44)	= +52.38 = (8.40)	= +52.68 = (12.69)	= +51.24 = (12.19)	= -36.07 = (67.29)	= +16.01 = (66.84)	= -125.3 = (113.7)	= +66.65 = (87.75)
		ADUR s.d.	ADUR s.d.	ADUR s.d.	ADUR s.d.	ADUR (odd) s.d.	ADUR (even) s.d.	ADUR s.d.	ADUR s.d.	ADUR (odd) s.d.	ADUR (even) s.d.
	Note	1	=	-	H	2	၈	1	-	67	8
	Eq.	1	2	3	4	4A	4B	5	9	6A	6В

Note 1, 175 cements, Avg. = 26.33, S.D. = 18.14 Note 2, 88 cements Note 3, 87 cements *Coef./s.d. ratio less than 1.0.

Table 11-7. Coefficients for equations for NAE cements relating the freeze-thaw durability factor for concretes of nominal $5 \frac{1}{2}$ bags cement per cubic yard and a slump of 5 ± 1 inch to various independent variables (ADUR)

	S.D.	11.17	10.47	10.03	9.65	10.78	8.62	86.6	9.61	10.64	8.60
	ASAT	1 1	-60.56 (9.61)								
	Cu				-281.1 (90.2)	-250.7 (139.7)	-139.8 (121.1)		-218.4 (91.5)	-300.5 (144.9)	*-115.3 (122.2)
	ij			1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	-13.56 (6.77)	*-10.25 (12.21)	-16.82 (8.34)		-14.38 (6.73)	*-10.43	-16.80 (8.29)
	Pb			1 1	-184.4 (123.5)	* -194.5 (195.1)	* -152.8 (163.5)	1 1	-165.3 (123.4)	*-161.2 (192.7)	-165.8 (162.4)
	Rb	1 1			-675.9 (451.1)	-812.1 (689.4)	*595.4 (624.4)	1 1 1 1 1 1 1 1 1 1 1	-769.6 (451.5)	-924.4 (683.5)	-631.5 (624.9)
(110	Ba				-43.60 (23.05)	*-15.69 (50.94)	-59.12 (25.49)	-	-37.00 (23.11)	* -11.31 (51.53)	-55.00 (25.56)
(110 AR) santung markentent antunies (110 AR)	APF			-0.00245 (0.00167)	-0.00337 (0.00163)	-0.00520 (0.00255)	*-0.00130 (0.00221)	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	-0.00298 (0.00158)	-0.00521 (0.00244)	*+0.00013 (0.00218)
ina agama	MgO			-1.689 (0.717)	-2.470 (0.723)	-1.555 (1.187)	-3.332 (0.933)	(0.952)	-2.322 (0.976)	-2.216 (1.548)	(1.335)
ad annu en	K20			-15.32 (3.98)	-16.03 (4.35)	-21.03 (6.61)	-10.12 (6.25)	-15.65 (4.29)	-17.94 (4.72)	-25.12 (7.02)	(6.69)
מינים מינים	SiO2						1 1	-2.614 (0.686)	-2.589 (0.717)	-2.822 (1.169)	(0.951)
T 7 (10C)	CaO	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1		1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1		1 1		+1.897 (0.942)	+1.120 (0.941)	* -0.056 (1.505)	+2.830 (1.320)
3	C3S			-0.5048 (0.1171)	-0.4106 (0.1153)	-0.3187 (0.1870)	-0.4826 (0.1643)				
	Air	+3.886 (0.996)		+5.208 (0.935)	+6.539 (0.957)	+6.593 (1.448)	+6.382 (1.321)	+5.190 (0.935)	+6.606 (0.962)	+7.023 (1.463)	+6.203 (1.323)
	Const.	= +16.73 = (1.76)	= +60.02	= +46.77	= +53.97 = (8.19)	= +57.17 = (14.04)	= +48.72 = (10.44)	= -39.75 = (65.55)	= +27.67 = (66.39)	= +117.33 = (103.26)	= -108.34
		ADUR s.d.	ADUR s.d.	ADUR s.d.	ADUR s.d.	ADUR (odd) s.d.	ADUR (even) s.d.	ADUR s.d.	ADUR s.d.	ADUR (odd) s.d.	ADUR (even)
	Note	-	П	-	-	61	63	-	-	63	23
	Ka.	1	2	3-	4	4A	4B	2	9	6A	6B

Note 1, 164 cements, Avg. = 22.70, S.D. = 11.64 Note 2, 82 cements *Coef./s.d. ratio less than 1.0.

Table 11-8. Calculated contributions of independent variables to the durability factor of concretes having a nominal 51/2 bags cement per cubic yard and a slump of 5 ± 1 inch (ADUR)

Independent variables	Range of variable (percent)	Coefficients from eq 4 table 11-7	Calculated Contributions to ADUR	Calculated range of contribu- tion to ADUR
Air content NAE cements C ₂ S K ₂ O MgO APF Ba** Rb** Pb** Ti Cu	0 to 5.0 5 to 50 0 to 1.1 0 to 5.0 *2500 to 5500 0 to 0.2 0 to 0.01 0 to 0.05 0 to 1.0 0 to 0.05	$\begin{array}{c} +6.539 \\ -0.4106 \\ -16.03 \\ -2.47 \\ -0.00337 \\ -43.6 \\ -675.9 \\ -184.4 \\ -13.56 \\ -218.1 \end{array}$	$\begin{array}{c} \text{Const.} = +54 \\ 0 \text{ to } +33 \\ -2 \text{ to } -21 \\ 0 \text{ to } -18 \\ 0 \text{ to } -18 \\ 0 \text{ to } -19 \\ 0 \text{ to } -9 \\ 0 \text{ to } -9 \\ 0 \text{ to } -9 \\ 0 \text{ to } -14 \\ 0 \text{ to } -11 \\ \end{array}$	33 19 18 12 11 9 7 9 14

for the different types of NAE cements. As indicated in table 11-13, a few cements showed the slight weight gain characteristic of specimens which failed in the first few cycles.

The series of equations presented in table 11–14 indicates the association of various independent variables to the percentage weight loss (AWTL) at the time of 40 percent reduction in dynamic modulus of specimens made of Series A concretes. Equation 1 indicates that an increase in the water/cement ratio is associated at the 5.0 percent significance level with a decrease in the weight loss. (See table 11-27.) Equation 2 indicates the relationship of the air content of the concrete to the weight loss. The reduction in variance is greater than for eq 1. The additional use of other commonly determined variables C₃A, C₄AF, Na₂O, and K₂O in eq 3, or Al₂O₃, Fe₂O₃, Na₂O, and K₂O in eq 5, caused a reduction in variance, significant at the 1.0 percent level. The additional use of the

Table 11-9. Frequency distribution of cements with respect to percentage weight loss of concrete specimens at the time of 40 percent loss of dynamic modulus in the freeze-thaw test. The specimens were made of concretes having a nominal 5 1/2 bags cement per cubic yard and a water-cement ratio of 0.635 (OWTL)

						Perce	ntage weig	th loss					
Type cement	-2 to 0	0 to 2	2 to 4	4 to 6	6 to 8	8 to 10	10 to 12	12 to 14	14 to 16	16 to 18	18 to 20	20 to 22	Tota
						Nun	ber of ce	ments					
	5	17	12	16	8	12	6	4 3	3	2			82 8
A	2	13	5	14	9	12	7	5				1	68
I I A	3	3	3	3	2	3	1 2	1			1		20
, V	1	4	1	2	3	3	1						15
Total	11	37	21	35	22	31	17	13	6	4	1	1	199

 $^{^{*}}$ Cm²/g. ** Coefficient of doubtful significance as coef./s.d. ratio was less than 2.0.

TABLE 11–10. Coefficients for equations for AE + NAE cements relating the percentage weight loss in the freeze-thaw durability test at the time of 40 percent reduction of dynamic modulus of concretes of nominal 5 ½ bags cement per cubic yard and a water cement ratio of 0.635 to various independent variables (OWTL)

	Air	C3A	C4AF	Al ₂ O ₃	\mathbf{F} e $_2$ O $_3$	Na ₂ O	K20	SO3	SO3	Rb	Pb	Ţ	Zr	Ç
	+1.042													
+0.4044 +0.6991	+0.4044 (0.1066)	+0.6991 (0.1372)		1 1		-3.079 (1.545)	-9.739 (1.265)	1 1			1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1			
+0.4112	+0.4112 (0.1025)	+0.7526 (0.1314)		1 1		$\frac{-3.709}{(1.490)}$	-8.435 (1.336)	1 1		-315.5 (143.6)	-85.95 (40.34)	-6.349 (2.059)	+11.22 (6.15)	
+0.4278 +1.0863		+1.0863 (0.1727)				-3.109 (1.692)	-8.511 (1.768)	1 1 1 1 1 1 1 1 1 1		$^*-163.1$ (194.7)	$-366.2 \\ (100.6)$	*+2.306 (3.119)	+11.08 (6.03)	
+0.4277 +0.5552		+0.5552 (0.2096)		- 1 1		-4.933 (2.724)	-9.522 (2.024)			-284.7 (216.4)	-57.45 (47.60)	-7.370 (3.051)	*+13.28 (17.71)	
+2.745 (1.084)				70	+1.475 (0.347)	-3.516 (1.567)	-9.829 (1.283)	-4.498 (2.815)	-3.013 (1.906)				1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	
+2.548 (1.031)				70	$^{+1.607}_{(0.331)}$	-4.109 (1.509)	-8.646 (1.375)	-4.419 (2.681)	-2.584 (1.817)	-286.7 (146.0)	-77.89 (40.84)	-6.131 (2.122)	+10.44 (6.15)	-63.04 (58.49)
*-0.646				70	+2.632 (0.438)	$\frac{-2.887}{(1.708)}$	-8.675 (1.804)	*+0.636 (4.848)	*+0.868 (3.318)	* -94.08 (201.58)	-374.5 (101.4)	*-2.217 (3.374)	+10.05 (6.10)	-109.44 (71.94)
+3.555 (1.384)				7º	+1.000 (0.524)	-6.613 (2.819)	-10.043 (2.150)	-6.839 (3.437)	-4.156 (2.333)	*-204.0 (220.6)	*-45.08 (48.65)	-7.161 (3.124)	*+11.28 (17.62)	* -81.83 (96.80)

Table 11–11. Coefficients for equations for NAE cements relating the percentage weight loss in the freeze-thaw durability test at the time of 40 percent reduction of dynamic modulus of concretes of nominal 5 ½ bags cement per cubic yard and a water cement ratio of 0.635 to various independent variables (OWTL)

	S.D.	4.041	3.426	3.216	3.199	3,292	3.419	3.203	3.217	3.221
	Cr							-68.12 (61.36)	*-72.46 (87.17)	* -61.60 (91.61)
	Zr	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1		+12.34 (6.29)	+14.35 (6.51)	*-18.38 (40.16)		+11.75 (6.28)	+13.07 (6.65)	-42.41 (41.35)
	Ti	1 6 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1		-7.28 (2.16)	(3.60)	(3.59)		-7.02 (2.22)	(3.77)	(3.70)
	Pb			-88.71 (41.03)	-253.2 (152.2)	-66.58 (45.43)		-81.15 (41.44)	-275.72 (155.01)	-59.84 (45.84)
	Rb	1 1		-344.4 (149.0)	*-136.4 (210.4)	-471.6 (237.2)		-314.5 (151.7)	*-76.7 (215.8)	-373.2 (246.6)
	Al ₂ O ₃			1 1	1 6 1 1 1 1 1 1 1 8 1 6		-3.214 (1.993)	$\frac{-3.089}{(1.879)}$	+4.224 (4.189)	-5.506 (2.332)
	SO3	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1			1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	-4.718 (2.964)	$\frac{-5.117}{(2.795)}$	$^*+5.501$ (6.220)	-8.506 (3.435)
	K20		-10.03 (1.35)	$\frac{-8.96}{(1.40)}$	-7.33 (1.96)	-10.48 (2.14)	-10.21 (1.37)	-9.33 (1.45)	$\frac{-7.20}{(2.012)}$	-10.92 (2.30)
	Na ₂ O	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	$\frac{-3.185}{(1.621)}$	-4.168 (1.556)	$\frac{-3.705}{(1.982)}$	-4.477 (2.749)	+3.701 (1.653)	$\frac{-4.768}{(1.582)}$	-3.341 (2.017)	$-6.601 \ (2.822)$
	Fe_2O_3	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1			1 1	1 1	$^{+1.482}_{(0.363)}$	+1.696 (0.344)	+1.701 (0.453)	+1.930 (0.580)
,	Al ₂ O ₃						+2.919 (1.140)	+2.914 (0.072)	*-1.455 (2.294)	+4.641 (1.360)
6 7	C4AF		+0.7113 (0.1433)	+0.8014 (0.1368)	+0.7513 (0.1765)	+0.9155 (0.2307)				
	C3A		+0.4285 (0.1118)	+0.4462 (0.1066)	+0.3147 (0.1476)	+0.5752 (0.1625)				1 1
	Air	*+0.394 (0.415)	+1.470 (0.383)	+1.881 (0.369)	+2.109 (0.504)	+1.791	+1.541 (0.385)	+1.968 (0.370)	+2.140	+1.994 (0.572)
	Const.	= +5.202 = (0.755)	= -1.870 $= (2.078)$	= -2.112	= -2.018 $=$ (2.641)	= -3.486 = (3.350)	= +6.744 = (5.756)	= +7.724 = (5.549)	= -11.901 $= (12.213)$	= +12.24 = (7.05)
Company of company		OWTL s.d.	OWTL =	OWTL s.d.	OWTL (odd) =	OWTL (even) =	OWTL =	OWTL =	OWTL (odd) = s.d.	OWTL (even) = +12.24 s.d. = (7.05)
	Note	-	-	-	61	61	1	1	61	61
	No.	1	2	3	3A	3B	4	5	5A	5B

*Coef./s.d. ratio less than 1.0.

Table 11-12. Calculated contributions of independent variables to the percentage weight loss in the freeze-thaw durability test at the time of 40 percent reduction of dynamic modulus of concretes of nominal 5½ bags cement per cubic yard and a water cement ratio of 0.635 (OWTL)

Independent variables	Range of variable (percent)	Coefficients from eq. 3 table 11–11	Calculated contributions to OWTL	Calculated range of contribu- tion to OWTL
Air content NAE cements C ₃ A C ₄ AF Na ₂ O K ₂ O R _b Pb Ti Zr**	0 to 4.5 1 to 15 1 to 16 0 to 0.7 0 to 1.1 0 to 0.01 0 to 0.05 0 to 1.0 0 to 0.5	$\begin{array}{c} +1.881 \\ +0.4462 \\ +0.8041 \\ -4.168 \\ -8.96 \\ -344.4 \\ -88.71 \\ -7.28 \\ +12.34 \end{array}$	$\begin{array}{c} \text{Const.} = -2.1 \\ 0 \text{ to } +8.5 \\ +0.4 \text{ to } 6.7 \\ +0.8 \text{ to } +12.9 \\ 0 \text{ to } -2.9 \\ 0 \text{ to } -9.9 \\ 0 \text{ to } -9.9 \\ 0 \text{ to } -3.4 \\ 0 \text{ to } -4.5 \\ 0 \text{ to } -7.3 \\ 0 \text{ to } +6.2 \end{array}$	8.5 6.3 12.1 2.9 9.9 3.4 4.5 7.3 6.2

^{**} Coefficient of doubtful significance as coef./s.d. ratio was less than 2.0.

trace elements, Mn, Rb, Pb, and Ti (eqs 4 and 6) resulted in a further reduction in variance (see table 11–27) although the coefficients for the individual trace elements were not highly significant. In equations calculated for the "odds" and "evens," eqs 4A, 4B, 6A, and 6B, the coef./s.d. ratios for Fe₂O₃, Na₂O, Pb, and Ti were less than 1.0 in one or the other of the equations calculated for the smaller groups of cements.

An analogous series of equations for the NAE cements is presented in table 11–15. The coef./s.d. ratios of w/c and air content (eqs 1 and 2) were both less than 1.0. When these were used with other commonly determined variables (eqs 3 and 5), the coefficient for air content was probably significant, and the reduction in variance as a result of the added variables was highly significant. The additional use of four trace elements (eqs 4 and 6) caused a further reduction in vari-

Table 11-13. Frequency distribution of cements with respect to percentage weight loss of concrete specimens at the time of 40 percent loss of dynamic modulus in the freeze-thaw test. The specimens were made of concretes having a nominal 5½ bags cement per cubic yard and a slump of 5 ± 1 inches (AWTL)

		Percentage weight loss													
Type cement	-2 to 0	0 to 2	2 to 4	4 to 6	6 to 8	8 to 10	10 to 12	12 to 14	14 to 16	16 to 18	18 to 20	20 or more	Tota		
		Number of cements													
	4	16	11	9	11	14	9	2 3	2 3			1	79 8		
	3	10	9	10	11	11	5	6 2	i			1	67		
A	2	1	5	2	3	2	$\frac{1}{3}$	1			1		20 3 15		
, V	1	5	1	2	2	2	i	1					15		
Total	10	32	26	23	27	30	21	16	6	1	1	2	195		

TABLE 11–14. Coefficients for equations for AE + NAE cements relating the percentage weight-loss in the freeze-thaw durability test at the time of 40 percent reduction of duramic modulus of concretes of nominal 5 ½ bags cement per cubic yard and a slump of 5 ± 1 inch to various independent variables (AWTL)

	S.D.	4.104	3.982	3.418	3.287	3.387	3.101	3.417	3.285	3,380	3,101
(2)	w/c	-30.69 (12.66)	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1				1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1			# 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1
es (AWI	Ĩ.		1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1		-4.379 (2.145)	*+0.469	-6.988 (2.823)	1 1 1	-4.395 (2.144)	$^{*}_{(3.324)}$	-6.986 (2.823)
בונו המבנמסו	Pb		1 1		-52.45 (41.80)	* _46.87 (62.38)	_60.77 (55.10)		-52.76 (41.76)	*-46.84 (62.23)	_61.07 (55.09)
muadanua	Rb				$-329.2 \\ (150.1)$	-279.1 (225.0)	-434.8 (199.1)		329.7 (150.0)	-279.6 (224.5)	-435.8 (199.2)
en orar roas	Mn				-4.903 (2.119)	-3.976 (2.713)	-7.518 (3.479)		-4.900 (2.117)	-3.995 (2.706)	-7.507 (3.478)
T then	K ₂ O			-10.27 (1.30)	-9.70 (1.39)	-10.84 (2.10)	-7.55 (1.87)	-10.28 (1.30)	-9.70 (1.39)	-10.89 (2.10)	-7.53 (1.87)
o fo dum	Na ₂ O	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1		-1.966 (1.584)	-2.527 (1.538)	-2.652 (2.386)	*-1.865	-1.975 (1.583)	-2.537 (1.537)	-2.665 (2.381)	*-1.863
מות חוות מיני	Fe ₂ O ₃						1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	+0.7496 (0.3571)	+0.9630 (0.3483)	+1.9236 (0.5286)	*+0.2155 (0.4634)
er caoac y	Al ₂ O ₃							+1.264 (0.289)	+1.403 (0.286)	+1.545 (0.448)	+1.202 (0.362)
o cement b	C,AF			+0.5074 (0.1415)	+0.6059 (0.1396)	+0.9466 (0.2112)	+0.3227 (0.1846)		1 1 1 1 1 1 1 1 1 1 1		1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1
re 5 72 oug	C3A			+0.4751 (0.1092)	+0.5275 (0.1081)	+0.5772 (0.1691)	+0.4539 (0.1368)	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1		1 1	1
of nomen	Air		+0.5980 (0.1447)	+0.8991 (0.1321)	+0.9020 (0.1297)	+0.9092 (0.1677)	+0.8862 (0.2136)	+0.8984 (0.1320)	+0.9012 (0.1295)	+0.9077 (0.1673)	+0.8859
l concrete	Const.	= +26.13 = (8.07)	= +5.366 = (0.420)	= +0.997	= +1.157 = (1.956)	= -2.940 $=$ (3.045)	= +4.110 $= (2.513)$	= +0.948 $= (1.972)$	= +1.102 = (1.957)	= -3.046 = (3.039)	+4.101
agnation movements of concretes of notice of 52 ords centerin per caster guid and a stain p of 1 inch to tai tods independent validates (AW 1L)		AWTL =	AWTL =	AWTL =	AWTL =	AWTL (odd) = s.d.	AWTL (even) = s.d.	AWTL =	AWTL =	AWTL (odd) = s.d. =	AWTL (even) = s.d.
ugn	Note	1	1	-	-	2	63	-	-	61	2
	No.	1	2	3	4	4A	4B	5	9	6A	6B

Note 1, 176 cements, Avg. = 6.582, S.D. = 4.161 Note 2, 88 cements *Coef./s.d. ratio less than 1.0.

TABLE 11-15. Coefficients for equations for NAE cements relating the percentage weight loss in the freeze-thaw durability test at the time of 40 percent reduction of dynamic

33400	S.D.	4.045	4.049	3,489	3.317	3.462	3.149	3.487	3.315	3.454	3.150
o for any or	w/c	* +10.69	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	1 1 1 1 1 1 1 1 1 3 1 1 1 1	1 1 1 1 1 1 1 1 1 1	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	1 1		1 1	
WTL)	Ti			1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	-5.534 (2.254)	-4.690 (3.661)	-5.511 (2.878)		-5.552 (2.253)	-4.716 (3.652)	-5.526 (2.881)
ariables (A	Pb	1 1 2 2 3 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	1 1	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	-54.97 (42.58)	* -48.78 (63.29)	-67.14 (58.64)		-55.31 (42.54)	*-48.78 (63.15)	(58.65)
ependent v	Rb	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1		-340.8 (154.7)	-362.9 (223.2)	$-244.9 \\ (221.1)$		$-341.2 \ (154.6)$	-363.6 (227.7)	-245.5 (221.2)
arious ind	Mn		1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1		-6.012 (2.238)	-3.510 (2.955)	$-13.784 \atop (3.871)$		-6.009 (2.236)	-3.532 (2.947)	-13.788 (3.873)
inch to	K20			-10.52 (1.40)	-10.51 (1.47)	-12.13 (2.15)	-8.08 (2.08)	-10.53 (1.40)	-10.52 (1.47)	-12.17 (2.15)	-8.07 (2.08)
p of 5 ±	Na ₂ O	1 1	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	-2.018 (1.658)	$-2.931 \ (1.597)$	-4.943 (2.556)	* -1.299 (2.051)	-2.028 (1.658)	-2.944 (1.596)	-4.987 (2.552)	* -1.230 (2.052)
ind a slum	$\mathrm{Fe}_2\mathrm{O}_3$	1 3 1 1 1 2 1 1 1 1 1 1 1 1 1 1 1 1 1 1						+0.7356 (0.3703)	+1.0238 (0.3583)	+1.0858 (0.5104)	+0.8255 (0.5255)
ubic yard	Al ₂ O ₃	1 1 1 1 1 1 1 1 1 1 1 1			1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1		1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	+1.327 (0.305)	+1.562 (0.300)	+1.560 (0.481)	+1.461 (0.387)
nent per c	C,AF	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	+0.5161 (0.1475)	+0.6593 (0.1449)	+0.6751 (0.2126)	+0.5766 (0.2078)	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1		1 3 1 7 1 3 1 1 1 1 1 1 1 1 1 1	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1
½ bags cer	C_3A	5 1 5 1 2 1 6 1 1 1 1 1		+0.4990 (0.1150)	+0.5875 (0.1134)	+0.5822 (0.1817)	+0.5521 (0.1461)) 	; I I I I I I I I I I I I I I I	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	
nominal 5	Air	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	*+0.0954 (0.3616)	+0.9435 (0.3355)	+1.2442 (0.3298)	+1.541 (0.4797)	+0.8012 (0.4638)	+0.9419 (0.3352)	+1.2430 (0.3294)	+1.5404 (0.4783)	+0.8009 (0.4639)
ncretes of	Const.	= -0.651 $= (10.723)$	= +6.054 $= (0.641)$	= +0.740 = (2.123)	= +0.409 $= (2.081)$	= +0.678 = (3.146)	= +1.284 $= (2.881)$	= +0.692 $= (2.125)$	= +0.355 = (2.081)	= +0.570 $= (3.135)$	= +1.278 = (2.891)
modulus of concretes of nominal 5 ½ bags cement per cubic yard and a slump of 5 ± 1 inch to various independent variables (AWTL)		ATWL s.d.	AWTL s.d.	AWTL s.d.	AWTL s.d.	AWTL (odd) s.d.	AWTL (even) s.d.	AWTL s.d.	AWTL s.d.	AWTL (odd) s.d.	AWTL (even) s.d.
	Note	1	Ħ	П	П	61	67	П	П	61	67
	Eq.	1	2	3	4	4A	4B	5	9	6A	6B

Note 1, 164 cements, Avg. = 6.201, S.D. = 4.038 Note 2, 82 cements *Coef./s.d. ratio less than 1.0.

Table 11–16. Calculated contributions of independent variables to the percentage weight loss in the freeze-thaw durability test at the time of 40 percent reduction of dynamic modulus of concretes of nominal $5\frac{1}{2}$ bags cement per cubic yard and a slump of 5 ± 1 inch. (AWTL)

Independent variables	Range of variable (percent)	Coefficients from eq 4 table 11–15	Calculated contributions to AWTL	Calculated ranges of contribu- tion to AWTL
Air content NAE cements C3A C4AF Nac0** K2O Mn Rb Pb** Ti	0 to 5.0 1 to 15 1 to 16 0 to 0.7 0 to 1.1 0 to 1.0 0 to 0.01 0 to 0.05 0 to 1.0	$\begin{array}{c} +1.244 \\ +0.5875 \\ +0.6593 \\ -2.931 \\ -10.51 \\ -6.012 \\ -340.8 \\ -54.97 \\ -5.534 \end{array}$	Const. = +0.4 0 to +6.2 +0.6 to +8.8 0 to +4.6 0 to -3.2 0 to -10.5 0 to -6.0 0 to -3.4 0 to -2.7 0 to -5.5	6.2 8.2 4.6 3.2 10.5 6.0 3.4 2.7 5.5

^{**} Coefficient of doubtful significance as coef./s.d. ratio was less than 2.0

ance, significant at the 1.0-percent level. (See table 11–27.) The coef./s.d. ratio of air content in eqs 4 and 6 was greater than 3.0 indicating that when used with other independent variables in an equation, the coefficient for air content of concretes made of NAE cements may be highly significant. In eqs 4A, 4B, 6A, and 6B, there were instances where Na₂O and Pb had coef./s.d. ratios less than 1.0 in one or the other of the equations for the smaller groups of cement.

The estimated contributions and range of contributions to the percentage weight loss (AWTL) in the freezing-and-thawing tests at the time of 40 percent reduction of dynamic modulus of the concretes of 5 ± 1 -in slump, as calculated from the coefficients of eq 4, table 11-15, are presented in table 11-16. Tables 11-15 and 11-16 show that increases in air content, C_3A , and C_4AF were associated with increase in AWTL. Increases in K_2O , and probably Mn, Rb, and Ti were associated with decrease in AWTL. The coefficients for Na_2O and Pb were of doubtful significance.

6.3. Saturation Ratio

6.3.1. Saturation Ratio of Series O Concretes

As previously indicated in subsection 3.3, the concrete specimens, moist-cured for 14 days, then dried in laboratory air for 4 weeks, were placed in water at 40 °F for 24 hours prior to the start of the freezing-and-thawing tests. Determinations were made of the air content of the freshly-mixed concrete, the loss of weight as a result of drying, and the weight gain after the 24 hours in water. The ratio of this weight gain to the possible weight gain if completely saturated, i.e., the volume of water lost in drying plus the volume of air, was calculated and is here termed the saturation ratio.

The frequency distribution of the saturation ratios is presented in table 11–17 for Series O concretes. The values for the ratio (OSAT) ranged from less than 0.3 to more than 0.8. All of the concretes made with the AE cements (Types IA, IIA, and IIIA) had very low ratios, and the values for the concretes made with the different

types of NAE cements overlapped.

Selected equations presented in table 11–18 indicate the relationship of various independent variables to the saturation ratio (OSAT) for the AE + NAE cements. As indicated in eqs 1 and 2, the ratio is significantly related to the air content (OAIR) of the concretes. A smaller S.D. value was obtained in eq 2 which used the square root of the air content as an independent variable in place of the air content as in eq 1. The additional use of C₂S and C₄AF in eq 3 resulted in a significant reduction in variance. (See table 11-27.) The reduction in variance resulting from also using MgO and Loss in eq 4 was significant at the 1.0 percent level. Comparing eqs 2 and 4 indicated an overall reduction in variance significant at the 1.0 percent level. With the added trace elements Cu, Mn, P, and Rb in addition to commonly determined variables in eq 5 there was a reduction in variance significant at the 1.0 percent level. (See table $11-\overline{27}$.)

Table 11-17. Frequency distribution of cements with respect to the ratio of the volume water absorbed when placed in water for 24 hours divided by the volume water lost after 28 days drying in laboratory air, plus the volume of air in the concrete. The concretes were made with a water-cement ratio of 0.635 (OSAT)

	Saturation ratio													
Type cement	0.25 to 0.30	0.30 to 0.35	0.35 to 0.40	0.40 to 0.45	0.45 to 0.50	0.50 to 0.55	0.55 to 0.60	0.60 to 0.65	0.65 to 0.70	0.70 to 0.75	0.75 to 0.80	0.80 and over	Tota	
		Number of cements												
		4	1	1 3	11	11	29	17	11	1		1	82	
A				3		3	8	18	21	11	2	2	68	
[[A	1	1	1		2	7	4	6	4	1	3		20 3 15	
Total	1	5	2	10	13	21	43	44	36	16	5	3	199	

Table 11–18. Coefficients for equations for AE+NAE cements relating the saturation cubic yard and a water-cement ratio of 0.635

Eq. No.	Note		Const.	OAIR	(OAIR)0-5	C ₂ S	C ₄ AF	CaO
1	1	OSAT s.d.	= +0.6745 = (0.0073)	-0.0396 (0.0026)				
2	1	OSAT s.d.	= +0.7987 = (0.0133)		-0.1522 (0.0092)			
3	1	OSAT s.d.	= +0.6288 = (0.0243)		-0.1406 (0.0079)	+0.00409 (0.00054)	+0.00538 (0.00173)	
4	1	OSAT s.d.	= +0.5879 = (0.0285)		-0.1430 (0.0079)	+0.00440 (0.00055)	+0.00574 (0.00171)	
5	1	OSAT s.d.	= +0.5858 = (0.0283)		-0.1447 (0.0077)	+0.00441 (0.00055)	+0.00537 (0.00176)	
5A	2	OSAT (odd) s.d.	= +0.6197 = (0.0447)		-0.1376 (0.0115)	+0.00416 (0.00078)	+0.00480 (0.00283)	
5B	2	OSAT (even) s.d.	= +0.5628 = (0.0381)		-0.1524 (0.0104)	+0.00455 (0.00082)	+0.00524 (0.00232)	
6	1	OSAT s.d.	=+1.486 (0.223)		-0.1434 (0.0079)			-0.01932 (0.00347)
7	1	OSAT s.d.	= +1.734 = (0.234)		-0.1465 (0.0078)			-0.02246 (0.00355)
7A	2	OSAT (odd) s.d.	= +1.363 = (0.365)		-0.1394 (0.0114)			-0.01797 (0.00563)
7B	2	OSAT (even)	= +2.126 = (0.318)		-0.1553 (0.0109)			-0.02711 (0.00471)

Note $\overline{1, 178}$ cements, Avg. = 0.5911, S.D. = 0.0963 Note 2, 89 cements

*Coef./s.d. ratio less than 1.0.

Table 11–19. Coefficients for equations for NAE cements relating the saturation ratio and a water-cement ratio of 0.635 to

Eq. No.	Note		Const.	OAIR	(OAIR)0.5	C ₂ S	C ₄ AF	CaO
1	1	OSAT s.d.	= +0.7122 = (0.0115)	-0.0633 (0.0063)				
2	1	OSAT s.d.	= +0.8175 = (0.0209)		$-0.1676 \\ (0.0162)$			
3	1	OSAT s.d.	= +0.6400 = (0.0296)		-0.1475 (0.0140)	+0.00396 (0.00056)	+0.00541 (0.00180)	
4	1	OSAT s.d.	= +0.5983 = (0.0342)		$-0.1464 \\ (0.0139)$	+0.00426 (0.00058)	+0.00572 (0.00178)	
5	1	OSAT s.d.	= +0.6023 = (0.0338)		$-0.1526 \\ (0.0144)$	+0.00426 (0.00058)	+0.00523 (0.00184)	
5A	2	OSAT (odd) s.d.	= +0.6247 = (0.0567)		$-0.1485 \\ (0.0255)$	+0.00462 (0.00081)	+0.00415 (0.00302)	
5B	2	OSAT (even) s.d.	= +0.5777 = (0.0428)		-0.1567 (0.0174)	+0.00354 (0.00085)	+0.00723 (0.00235)	
6	1	OSAT s.d.	= +1.411 = (0.231)		-0.1475 (0.0138)			-0.01801 (0.00359)
7	1	OSAT s.d.	= +1.674 = (0.241)		-0.1552 (0.0144)			-0.02124 (0.00365)
7A	2	OSAT (odd) s.d.	= +1.482 = (0.336)		$-0.1550 \\ (0.0243)$			-0.02040 (0.00523)
7B	2	OSAT (even) s.d.	= +1.937 = (0.347)		-0.1605 (0.0178)			-0.02262 (0.00514)

Note 1, 166 cements, Avg. = 0.6070, S.D. = 0.07757 Note 2, 88 cements

*Coef./s.d. ratio less than 1.0.

SiO ₂	Fe ₂ O ₃	MgO	Loss	Cu	Mn	Ni	P	Rb	S.D.
									0.06376
									0.06023
									0.05011
		+0.00612 (0.00319)	+0.01483 (0.00715)						0.04932
		+0.00936 (0.00324)	+0.01660 (0.00707)	+0.9163 (0.4522)	-0.0631 (0.0452)		+0.0442 (0.0341)	-3.653 (1.952)	0.04792
		*+0.00489 (0.00512)	*+0.00334 (0.01113)	+0.7838 (0.6849)	*-0.0419 (0.0440)		*+0.0205 (0.0526)	-5.557 (2.657)	0.05070
		+0.01238 (0.00435)	+0.02943 (0.00948)	$^{+1.3715}_{(0.6409)}$	-0.0885 (0.0459)		$^{+0.0599}_{(0.0465)}$	*-1.195 (3.061)	0.04561
+0.02271 (0.00309)	+0.01239 (0.00547)								0.04912
+0.02134 (0.00316)	+0.00946 (0.00575)			+0.9583 (0.4524)	-0.0529 (0.0315)	$-1.354 \ (1.151)$	+0.0453 (0.0343)	-3.163 (2.014)	0.04787
$^{+0.02472}_{(0.00470)}$	+0.01008 (0.00898)			+1.0170 (0.6775)	*-0.0268 (0.0436)	*-0.616 (1.624)	*+0.0290 (0.0526)	-4.345 (2.776)	0.04997
*+0.01798 (0.00468)	*+0.00507 (0.00777)			+1.2872 (0.6753)	-0.0799 (0.0479)	-1.997 (1.818)	*+0.0361 (0.0477)	*-1.251 (3.175)	0.04659

at the start of freeze-thaw tests of concretes of nominal 5 $\frac{1}{2}$ bags cement per cubic yard various independent variables (OSAT)

SiO ₂	Fe ₂ O ₃	MgO	Loss	Cu	Mn	Ni	P	Rb	S.D.
									0.06124
									0.06055
									0.05077
		+0.00550 (0.00330)	+0.01397 (0.00752)						0.05016
		+0.00885 (0.00332)	+0.01601 (0.00737)	+0.982 (0.473)	-0.0726 (0.0327)		+0.0488 (0.0348)	-3.35 (2.05)	0.04847
		+0.00550 (0.00496)	*+0.01043 (0.01231)	*+0.670 (0.757)	$-0.0624 \\ (0.0438)$		*+0.0123 (0.0555)	-4.79 (2.96)	0.05123
		+0.02111 (0.00456)	+0.02489 (0.00938)	$^{+1.297}_{(0.601)}$	$-0.1012 \\ (0.0512)$		$^{+0.0768}_{(0.0456)}$	*-1.70 (3.07)	0.04556
$^{+0.02242}_{(0.00322)}$	+0.01307 (0.00567)								0.04978
+0.02092 (0.00328)	+0.00962 (0.00599)			$^{+1.019}_{(0.471)}$	-0.0599 (0.0329)	* -1.162 (1.175)	$^{+0.0502}_{(0.0350)}$	-2.78 (2.11)	0.04833
+0.02807 (0.00467)	*+0.00592 (0.00922)			$^{*}_{(0.724)}^{+0.643}$	$-0.0458 \ (0.0423)$	*+0.036 (1.792)	*+0.0244 (0.0535)	-2.85 (3.03)	0.04926
+0.01255 (0.00462)	+0.01228 (0.00782)			+1.522 (0.613)	-0.0796 (0.0532)	-2.170 (1.578)	+0.0598 (0.0470)	* -2.72 (3.12)	0.0463

Table 11-20. Calculated contributions of independent variables to the saturation ratio at the start of the freeze-thaw tests of concretes of nominal 5½ bags cement per cubic yard and a water-cement ratio of 0.635 (OSAT)

Independent variables	Range of variables (percent)	Coefficients from eq 5 table 11–19	Calculated contributions to OSAT	Calculated range of contribu- tion to OSAT
(OAIR) ^{0.5} NAE cements C ₂ S C ₄ AF MgO Loss Cu Mn P** Rb**	0 to 2.12 5 to 50 1 to 16 0 to 5.0 0.3 to 3.3 0 to 0.05 0 to 1 0 to 0.5 0 to 0.5	$\begin{array}{c} -0.1526 \\ +0.00426 \\ +0.00523 \\ +0.00885 \\ +0.01601 \\ +0.982 \\ -0.0726 \\ +0.0488 \\ -3.35 \end{array}$	$\begin{array}{c} \text{Const.} = +0.60 \\ 0 \text{ to } -0.32 \\ +0.02 \text{ to } +0.21 \\ +0.01 \text{ to } +0.08 \\ 0 \text{ to } +0.04 \\ 0 \text{ to } +0.05 \\ 0 \text{ to } +0.05 \\ 0 \text{ to } -0.07 \\ 0 \text{ to } +0.03 \\ 0 \text{ to } -0.03 \\ \end{array}$	0.32 0.19 0.07 0.04 0.05 0.05 0.07 0.02 0.03

^{**} Coefficient of doubtful significance as coef./s.d. ratio less than 2.0.

Equation 6 was calculated using the oxides, CaO, SiO₂, and Fe₂O₃ as independent variables instead of the potential compounds. MgO and Loss had coef./s.d. ratios of less than 1.0 and were not included. The reduction in variance was highly significant. With the added trace elements Cu, Mn, Ni, P, and Rb (eq 7), the reduction in variance was significant at the 5.0 percent level. (See table 11–27.)

In equations calculated for the "odds" and "evens" in the array of cements, (eqs 5A, 5B, 7A, and 7B), the coef./s.d. ratios for Fe₂O₃, MgO, Loss, Mn, Ni, P, and Rb were less than 1.0 in one or the other of the pairs of equations for the smaller

groups of cement.

The equations presented in table 11–19 for the relation of the various independent variables to the saturation ratio of NAE cements are very similar to, and the coefficients and coef./s.d. ratios reasonably consistent with those presented in table 11–18 where the AE cements were included. The coefficients for the air content or square root of the air content (eqs 1 and 2) were highly significant even with the NAE cements. (See table 11–27.) The additional use of C₂S and C₄AF in eq 3 resulted in a highly significant reduction in variance, but with the addition of MgO and Loss in eq 4 the reduction in variance was not significant at the 5.0 percent level. The use of trace

elements Cu, Mn, P, and Rb (eq 5) caused a reduction in variance significant at the 1.0 percent level, but when these plus Ni were used with the oxides (eq 7), the added reduction in variance was significant only at the 5.0 percent level. In the equations for the "odds" and "evens" (eqs 5A, 5B, 7A, and 7B) there were instances where Fe₂O₃, Loss, Cu, Ni, P, and Rb had coef./s.d. ratios less than 1.0 in one or more of the equations for the smaller groups.

The estimated contributions and range of contributions to saturation ratio of the constant w/c concretes, as calculated from the coefficients of eq 5, table 11–19, are presented in table 11–20. Increase in air content and probably Mn were associated with a decrease in the saturation ratio, Increases in C₂S and probably C₄AF, MgO, Loss, and Cu were associated with increases of the

saturation ratio.

6.3.2. Saturation Ratio of Series A Concretes

The frequency distribution of the saturation ratios of the Series A concretes is presented in table 11–21. The AE cements (Types IA, IIA, and IIIA) had low saturation ratios (0.20 to 0.45) whereas the NAE cements had ratios of 0.4 to more than 0.8. There was a broad overlapping of the ratios for the different types of NAE cements.

Equations indicating the various independent variables associated with the saturation ratio of AE + NAE cements are presented in table 11–22. The use of the square root of the air content (eq 2) resulted in a slightly lower S.D. value than when using the air content (eq 1). When the w/crequired to produce the 5 ± 1 -in slump concrete was included as a single additional variable in eq 3, the coefficient for w/c was not significant. In eq 4 where C₂S and C₄AF were added as independent variables, the coefficient for w/c was positive and significant at the 5.0 percent level. The use of the commonly determined variables C_2S , C_4AF , C_3A/SO_3 , MgO, and Loss (eq 5) resulted in a highly significant reduction in variance. (See table 11–27.) The use of Co, Ni, P, Rb, and Zr together with commonly determined variables

Table 11-21. Frequency distribution of cements with respect to the ratio of the volume water absorbed when placed in water for 24 hours divided by the volume water lost by drying for 28 days in laboratory air plus the volume of air in the concrete. The concretes were made with a slump of 5 ± 1 inches (ASAT)

							Saturat	ion ratio						
Type cement	0.20 to 0.25	0.25 to 0.30	0.30 to 0.35	0.35 to 0.40	0.40 to 0.45	0.45 to 0.50	0.50 to 0.55	0.55 to 0.60	0.60 to 0.65	0.65 to 0.70	0.70 to 0.75	0.75 to 0.80	0.80 and Over	Total
	Number of cements													
I	1		<u>4</u>		2 2	8	17	17	15	10	7	2	1	79 8
II.			1		2	3	5	5	16	15	15	4	2	67
III IIIA		1		1		2	4	7	5	1		1		67 3 20 3
IV, V								2	5	4	2	2		15
Total	1	1	6	3	7	13	26	31	41	30	24	9	3	195

(eq 6) resulted in a highly significant reduction in variance. (See table 11–27.) The use of the oxides (eq 7), or the oxides with trace elements (eq 8) resulted in S.D. values and reduction of variance comparable with those obtained using the poten-

tial compounds in eqs 5 and 6.
In equations for the "odds" and "evens" (eqs 6A, 6B, 7A, and 7B) there were instances where C₃A/SO₃, Fe₂O₃, K₂O, MgO, Co, Rb, and Zr had coef./s.d. ratios less than 1.0 in one or the other of the pairs of equations with the smaller groups of cements.

The corresponding series of equations for NAE cements is presented in table 11-23. The results are in reasonable agreement with those presented in the previous table 11–22, where the AE cements

were included.

In eq 4A and 4B the coef./s.d. ratios of Al_2O_3 , Fe₂O₃, Cr, and V had coef./s.d. ratios less than 1.0 in one or the other of the equations for the smaller groups of cements, the "odds" and "evens."

The estimated contributions and range of contributions to saturation ratio of the constant slump concretes, as calculated from the coefficients of eq 6, table 11-23, are presented in table 11-24. Increases in air content, and probably C₃A/SO₃, Ni, and Rb were associated with decreases in the saturation ratio. Increases in C₂S, MgO, and probably C₄AF, Loss, and P were associated with increases of the saturation ratio.

6.4. Cycles of Freezing and Thawing

Frequency distributions of the number of cycles required to cause a 40-percent reduction of dynamic modulus of Series O and Series A concretes are given in tables 11–25 and 11–26, respectively. No analyses of these data were made because of the fact that the distribution curves for these data and those for durability factor are identical except for the air-entraining cements, and, therefore, equations, especially with NAE cements, would have shown the same relationships. For specimens which fail in 300 cycles or less, the durability factor is exactly one-fifth the number of cycles at which the 40-percent reduction in dynamic E is reached. All of the non-air-entrained specimens failed in 300 cycles or less, and thus the distribution curves are the same for dynamic E and number of cycles up to this point. (There are some discrepancies in the distributions given in tables 11-25 and 11-26 as compared to tables 11-1 and 11-5 due to the fact that the durability factors were rounded to the nearest unit and the numbers of cycles were taken to the nearest cycle. The three non-air-entrained cements shown in the 300–500 cell in table 11–26 were ones which failed at 300 cycles). Although the two distributions are different for specimens which do not fail in 300 cycles, the small number of air-entraining cements did not warrant further analysis using the number of cycles instead of the durability factor.

6.5. Autogenous Healing

After completion of the freezing-and-thawing tests, the deteriorated specimens were placed in the fog room. At various periods ranging from approximately one to approximately five years, the specimens were removed from the fog room and retested for dynamic modulus.

The periods during which the specimens were stored in the fog room after freezing-and-thawing tests were nominally 1, 2, 3, 4, and 5 years. However, due to the fact that large groups of specimens which had been removed from freezing and thawing at different times were retested for dynamic modulus at the same time, the actual amount of time in storage varied within each nominal age

The ranges of actual elapsed times in months are given in table 11-28. All of the specimens in the 4-year category were specimens which had been retested at 2 or 3 years, then were placed in the fog room and retested a second time at 4 years. A small number of these were retested a third time and are included with the 5-year group.

Since it appears, as is shown below, that practically all of the autogenous healing that occurred took place in the first year, and no statistical intercomparisons of data are made between years, it seems the variations in time within the nominal

age groups do not affect the results.

Table 11–29 shows the averages and standard deviations of the ratios of dynamic modulus after autogenous healing to dynamic modulus at the end of the freezing-and-thawing test. Most of the specimens achieved calculated dynamic modulus values equal to or higher than the original dynamic modulus, but the moduli for these two periods could not be compared directly, because of the sloughing and consequent changes in dimensions that many of the specimens underwent during freezing-and-thawing. For the period of autogenous healing, however, the dimensions did not change. Also changes in weight during the healing period were negligible.

For the NAE cements alone, the average ratio for all five age groups was 2.32, while the average for the 42 specimens measured at one year was 2.38. Thus all the autogenous healing evidently occurred before 16 months. It seems probable that the length of time required for recovery was actually less than one year, but how much less is not

known.

The ratios for the air-entrained specimens were significantly lower than those for the non-airentrained specimens, an average of 1.34 for both 2- and 3-year storage compared to 2.32 for the non-air-entrained concretes. The air-entrained specimens had lower dynamic modulus values at the start of the freezing-and-thawing tests. However, the air-entrained specimens generally appeared to regain a smaller percentage of their original dynamic modulus during storage. The ratios of calculated dynamic modulus after storage

Table 11–22. Coefficients for equations for AE+NAE cements relating the saturation cubic yard and a slump of 5 \pm 1 inch to

Eq. No.	Note		Const.	AAIR	(AAIR)0.5	w/c	C ₂ S	C ₄ AF	C ₃ A/SO ₃
1	1	ASAT s.d.	= +0.6827 = (0.0067)	$-0.0429 \ (0.0023)$					
2	1	ASAT s.d.	= +0.8119 = (0.0105)		$-0.1657 \ (0.0074)$				
3	1	ASAT s.d.	= +1.0550 = (0.1814)		$^{-0.1774}_{(0.0114)}$	-0.3576 (0.2664)			
4	1	ASAT s.d.	1 0.200		-0.1415 (0.0103)	+0.5867 (0.2391)	$^{+0.00443}_{(0.00049)}$	$^{+0.00464}_{(0.00164)}$	
5	1	ASAT s.d.	= +0.2258 = (0.1647)		$^{-0.1441}_{(0.0100)}$	+0.6212 (0.2317)	$^{+0.00448}_{(0.00050)}$	$^{+0.00358}_{(0.00174)}$	$ \begin{array}{c c} -0.00515 \\ (0.00254) \end{array} $
6	1	ASAT s.d.	= +0.2441 = (0.1583)		$^{-0.1456}_{(0.0096)}$	+0.5880 (0.2229)	$^{+0.00468}_{(0.00048)}$	$^{+0.00408}_{(0.00169)}$	$ \begin{array}{c c} -0.00461 \\ (0.00247) \end{array} $
6A	2	ASAT (odd) s.d.			$-0.1510 \\ (0.0173)$	$^{+0.4931}_{(0.3880)}$	+0.00435 (0.00066)	$^{+0.00440}_{(0.00251)}$	-0.00591 (0.00391)
6B	3	ASAT (even) s.d.	= +0.1735 = (0.1913)		$^{-0.1429}_{(0.0116)}$	+0.6140 (0.2676)	$^{+0.00495}_{(0.00074)}$	$^{+0.00419}_{(0.00249)}$	*-0.00216 (0.00329)
7	1	ASAT s.d.	= +1.419 = (0.302)		$-0.1387 \ (0.0103)$	$^{+0.6888}_{(0.2377)}$			
8	1	ASAT s.d.	=+1.474 = (0.293)		$-0.1413 \ (0.0100)$	$^{+0.6508}_{(0.2303)}$			
8A	2	ASAT (odd) s.d.	= +1.285 = (0.504)		$^{-0.1502}_{(0.0184)}$	$^{+0.4515}_{(0.4103)}$			
8B	3	ASAT (even) s.d.	= +1.844 = (0.389)		$^{-0.1416}_{\ (0.0126)}$	$^{+0.6703}_{(0.2845)}$			

Note 1, 177 cements, Avg. = 0.5961, S.D. = 0.1097 Note 2, 89 cements Note 3, 88 cements

*Coef./s.d. ratio less than 1.0.

Table 11–23. Coefficients for equations for NAE cements relating the saturation ratio and a slump of 5 \pm 1 inch to vari

Eq. No.	Note		Const.	AAIR	(AAIR)0.5	w/c	C ₂ S	C ₄ AF	C ₃ A/SO ₃
	1	ASAT s.d.	= +0.7286 = (0.0086)	-0.0740 (0.0049)					
2	1	ASAT s.d.	= +0.8288 = (0.0147)		$^{-0.1804}_{(0.0119)}$				
3	1	ASAT s.d.	= +1.1607 = (0.1819)		$-0.1945 \\ (0.0141)$	$ \begin{array}{c c} -0.4915 \\ (0.2685) \end{array} $			
4	1	ASAT s.d.			$^{-0.1626}_{(0.0122)}$	$^{+0.4887}_{(0.2439)}$	+0.00428 (0.00050)	$^{+0.00449}_{(0.00162)}$	
5	1	ASAT s.d.	= +0.3201 = (0.1664)		$-0.1628 \ (0.0116)$	$^{+0.5422}_{(0.2349)}$	$^{+0.00419}_{(0.00051)}$	$^{+0.00302}_{(0.00172)}$	-0.00633 (0.00253)
3	1	ASAT s.d.			$-0.1607 \\ (0.0115)$	$^{+0.4814}_{(0.2271)}$	$^{+0.00436}_{(0.00049)}$	$^{+0.00353}_{(0.00168)}$	$-0.00585 \ (0.00249)$
5A	2	ASAT (odd) s.d.	= +0.4760 = (0.2919)		$-0.1712 \ (0.0191)$	*+0.3351 (0.4160)	$^{+0.00421}_{(0.00070)}$	$^{+0.00351}_{(0.00273)}$	$-0.00793 \\ (0.00395)$
SB	3	ASAT (even) s.d.	= +0.2080 = (0.2032)		$-0.1489 \ (0.0152)$	$^{+0.6246}_{(0.2820)}$	+0.00460 (0.00007)	$^{+0.00426}_{(0.00237)}$	*-0.00229 (0.00344)
7	1	ASAT s.d.	= +1.380 = (0.307)		$-0.1567 \\ (0.0118)$	$^{+0.6202}_{(0.2436)}$			
3	1	ASAT s.d.	= +1.469 = (0.298)		$-0.1571 \\ (0.0116)$	$^{+0.5556}_{(0.2367)}$			
BA	2	ASAT (odd)	= +1.980 = (0.486)		$-0.1651 \\ (0.0184)$	$^{*}_{\substack{+0.1914 \ (0.4083)}}$			
BB	3	ASAT (even) s.d.	= +1.287 = (0.405)		-0.1488 (0.0153)	$^{+0.7876}_{(0.2991)}$			

Note 1, 165 cements, Avg. = 0.6152, S.D. = 0.0851 Note 2, 83 cements Note 3, 82 cements

ratio at the start of the freeze-thaw tests of concretes of nominal 5 $\frac{1}{2}$ bags cement per various independent variables (ASAT)

CaO	SiO ₂	Fe ₂ O ₃	K ₂ O	MgO	Loss	Со	Ni	Р	Rb	Zr	S,D.
											0.06400
											0.05596
											0.05583
											0.04483
				+0.00926 (0.00291)	+0.01335 (0.00689)						0.04273
				+0.00868 (0.00276)	$^{+0.01651}_{(0.00625)}$	+4.76 (2.27)	-2.653 (0.991)	$^{+0.0540}_{(0.0293)}$	-4.64 (1.69)	-0.0880 (0.0780)	0.04062
				*-0.00025 (0.00428)	+0.01539 (0.00885)	*+0.44 (5.55)	-3.627 (1.507)	$^{+0.0640}_{(0.0516)}$	-3.19 (2.48)	-0.1360 (0.0858)	0.04238
				+0.01675 (0.00366)	+0.02155 (0.00962)	+5.96 (2.52)	-1.678 (1.384)	$^{+0.0476}_{(0.0360)}$	-6.38 (2.48)	*+0.4208 (0.6572)	0.03846
$-0.0251 \\ (0.0032)$	+0.0235 (0.0030)	+0.00825 (0.00505)	$-0.0424 \\ (0.0176)$								0.04171
$-0.0256 \\ (0.0031)$	$^{+0.0241}_{(0.0030)}$	+0.00930 (0.00500)	-0.0398 (0.0186)			+4.18 (2.22)	-2.847 (0.968)	$^{+0.0520}_{(0.0286)}$	-3.15 (1.82)	-0.1167 (0.0759)	0.03988
-0.0205 (0.0047)	$^{+0.0238}_{(0.0041)}$	$^{+0.01403}_{(0.00801)}$	$-0.0558 \\ (0.0281)$			*-0.86 (5.39)	-3.867 (1.477)	$^{+0.0737}_{(0.0502)}$	* -1.39 (2.59)	-0.1576 (0.0830)	0.04144
-0.0313 (0.0044)	$^{+0.0236}_{(0.0045)}$	*+0.00272 (0.00713)	* -0.0201 (0.0269)			+5.48 (2.47)	-1.877 (1.355)	$^{+0.0452}_{(0.0353)}$	-5.99 (2.77)	*+0.3715 (0.6440)	0.03848

at the start of freeze-thaw tests of concretes of nominal 5 1/2 bags cement per cubic yard ous independent variables (ASAT)

CaO	SiO ₂	Fe ₂ O ₃	K ₂ O	MgO	Loss	Со	Ni	P	Rb	Zr	S.D.
											0.05509
											0.05488
											0.05449
											0.04395
				+0.00881 (0.00279)	-0.01064 (0.00648)						0.04175
				+0.00827 (0.00276)	+0.01452 (0.00636)	+4.46 (2.30)	-2.244 (0.993)	+0.0625 (0.0290)	-4.10 (1.70)	$-0.0980 \ (0.0772)$	0.03993
				$^{+0.00668}_{(0.00412)}$	+0.01351 (0.00951)	*+3.22 (4.24)	* -1.573 (1.827)	+0.0968 (0.0535)	-5.08 (2.67)	-0.0906 (0.0901)	0.04268
				$^{+0.01036}_{(0.00418)}$	+0.01518 (0.00953)	+4.76 (2.91)	$-2.390 \ (1.212)$	$^{+0.0400}_{(0.0365)}$	-2.69 (2.33)	-0.2232 (0.2066)	0.03901
-0.0235 (0.0032)	+0.0235 (0.0031)	+0.00837 (0.00504)	-0.0344 (0.0180)								0.04085
-0.0242 (0.0031)	+0.0237 (0.0031)	+0.00918 (0.00500)	-0.0353 (0.0190)			+3.97 (2.26)	$-2.390 \\ (0.968)$	+0.0596 (0.0283)	-2.80 (1.83)	-0.1310 (0.0749)	0.03919
$-0.0267 \\ (0.0044)$	+0.0203 (0.0043)	*+0.00658 (0.00817)	-0.0942 (0.0304)			*+3.71 (4.02)	-2.413 (1.717)	+0.1085 (0.0501)	* -2.36 (2.65)	-0.1495 (0.0835)	0.04003
-0.0248 (0.0048)	+0.0259 (0.0047)	+0.00765 (0.00669)	*+0.0077 (0.0251)			+3.97 (2.80)	-2.169 (1.179)	$^{+0.0465}_{(0.0354)}$	-3.17 (2.57)	-0.2426 (0.2003)	0.03818

to that at the beginning of freezing and thawing ranged from approximately 0.95 to less than 0.70, while those for the non-air-entrained specimens ranged from approximately 0.9 to 1.9. For the

Table 11–24. Calculated contributions of independent variables to the saturation ratio at the start of the freeze-thaw tests of concretes of nominal 5 $\frac{1}{2}$ bags cement per cubic yard and a slump of 5 \pm 1 inch. (ASAT)

Independent variables	Range of variable (percent)	Coefficients from eq 6 table 11–23	Calculated contributions to ASAT	Calculated range of contribu- tions to ASAT
(AAIR) ^{0.5} NAE cements_w/c C ₂ S_C ₄ AF_C ₂ A/SO ₃ _MgO_Loss_C ₀ ** Ni_P_Rb	0 to 2.23 0.6 to 0.7 5 to 50 1 to 16 0.4 to 10.1 0 to 5.0 0.3 to 3.3 0 to 0.01 0 to 0.02 0 to 0.5 0 to 0.01	$\begin{array}{c} -0.1607 \\ +0.4814 \\ +0.00436 \\ +0.00353 \\ -0.00585 \\ +0.00827 \\ +0.01452 \\ +4.46 \\ -2.244 \\ +0.0625 \\ -4.10 \end{array}$	Const. = +0.35 0 to -0.36 +0.29 to +0.34 +0.02 to +0.02 0 to +0.06 -0.02 to -0.06 0 to +0.04 0 to +0.05 0 to +0.04 0 to -0.04 0 to -0.04 0 to -0.03 0 to -0.03	0.36 0.05 0.20 0.06 0.04 0.04 0.05 0.04 0.04 0.03

^{**} Coefficient of doubtful significance as coef./s.d. rati o was less than 2.0.

non-air-entrained concretes alone the ones that regained the greatest amounts in dynamic modulus were generally those that had lower original dynamic modulus values.

The evaluation of autogenous healing was further complicated by the fact that the specimens were seldom removed from freezing and thawing at exactly 60 percent of original E. A few were removed at 60 to 65 percent E_0 while others which were deteriorating rapidly were below 20 percent E_0 when removed. The latter were specimens which failed during the first freezing-and-thawing period and were first checked at 10 cycles. They were also specimens which showed a weight gain during freezing and thawing due to early failure. However, even these specimens reached higher dynamic modulus values after storage than they had before freezing and thawing.

No multivariable equations are given relating independent variables to regain of dynamic modulus. However, the data were subjected to analysis of variance to determine if there were significant differences in the ratios between cements. The results are shown in table 11–30 for the different

Table 11-25. Frequency distribution of cements with respect to OCYS, the number of cycles of freezing and thawing required to cause a 40-percent reduction in dynamic modulus of Series O concretes

						Numbe	r of cycles					
Type cement	0 to 20	20 to 40	40 to 60	60 to 80	80 to 100	100 to 150	150 to 200	200 to 300	300 to 500	500 to 700	700 to 1000	Total
		Number of cements										
A	. 1	7	7	7	14	28	13	5	5	3		82 8
I	1	8	5	9	12	24	5	4				68 3
IAII		3	2	2	2	4	3	4	1	2	- 	20
IIA		2								1	2	3
V, V	1	Z	4	1	4	3						15
Total	3	20	18	19	32	59	21	13	6	6	2	199

Table 11-26. Frequency distribution of cements with respect to ACYS, the number of cycles of freezing and thawing required to cause a 40-percent reduction in dynamic modulus of Series A concretes

						Number	of cycles					
Type cement	0 to 20	20 to 40	40 to 60	60 to 80	80 to 100	100 to 150	150 to 200	200 to 300	300 to 500	500 to 700	700 to 1000	Total
						Number o	of cements					
I	2	5	2	13	15	21	14	6	1 3	A		79 8
II	1	8	4	7	13	25	6	2	1 2	1		67
III	1	1	2	1	2	6	2	4	ĩ	1	2	20
IV, V	1	1	3	3	4	1	2					15
Total	5	15	11	24	34	53	· 24	13	8	6	2	195

Table 11-27. "F" values for significance of reduction of variance due to added variables.

Table	Equations*	"F"	D.F.	Critical "	F" ratios
Table	Equations	ratio	D.I.	$\alpha = 0.01$	$\alpha = 0.05$
11-2	0,1	118	2:177	4.70	3.04
	0,2	76.4	2:177	4.70	3.04
	1,3	15.1	6:171	2.91	2.15
	3,4	5.48	5:166	3.13	2.27
	1,5	17.8	5:172	3.12	2.27
	5,6	5.76	5:167	3.13	2.27
11-3	0,1	6.83	2:166	4.72	3.04
	0,2	19.0	2:166	4.72	3.04
	1,3	9.04	6:160	2.92	2.15
	3,4	4.01	5:155	3.14	2.27
	1,5	10.5	5:161	3.12	2.27
	5,6	4.25	5:156	3.14	2.27
11-6	0,1	118	2:173	4.71	3.04
	0,2	87.6	2:173	4.71	3.04
	1,3	21.8	4:169	3.42	2.43
	3,4	4.37	5:164	3.13	2.27
	1,5	12.5	4:169	3.42	2.43
	5,6	3.63	6:163	2.92	2.15
11-7	0,1	8.05	2:162	4.72	3.04
	0,2	20.4	2:162	4.72	3.04
	1,3	10.7	4:158	3.43	2.43
	3,4	3.53	5:153	3.14	2.27
	1,5	11.2	4:158	3.43	2.43
	5,6	3.07	6:152	2.92	2.15
11-10	0,1	21.0	2:178	4.70	3.04
	1,2	18.9	4:174	3.14	2.43
	2,3	5.9	4:170	3.14	2.43
	1,4	13.1	6:172	2.91	2.15
	4,5	4.95	5:167	3.13	2.27
11-11	0,1	0.92	2:166	4.72	3.04
	1,2	17.2	4:162	3.14	2.43
	2,3	6.46	4:158	3.14	2.43
	1,4	12.0	6:160	2.92	2.15
	4,5	5.46	5:155	3.14	2.27
11-14	0,1	3.46	2:174	4.71	3.04
	0,2	9.09	2:174	4.71	3.04
	2,3	16.5	4:170	3.14	2.43
	3,4	4.46	4:166	3.14	2.43
	2,5	16.6	4:170	3.14	2.43
	5,6	4.48	4:166	3.14	2.43
11-15	0,3	10.3	6:158	2.92	2.15
	3,4	5.20	4:154	3.14	2.43
	0,5	10.3	6:158	2.92	2.15
	5,6	5.21	4:154	3.14	2.43
11-18	0,1 0,2 2,3 3,4 2,4 4,5 2,6 6,7	115 140 40.1 3.81 22.6 3.55 30.5 2.83	2:176 2:176 2:174 2:172 4:172 4:168 3:173 5:168	4.71 4.71 4.71 4.71 3.14 3.14 3.88 3.13	3.04 3.04 3.04 3.04 2.43 2.67 2.27
11-19	0,1 0,2 2,3 3,4 2,4 4,5 2,6 6,7	51.1 54.2 35.6 2.98 19.7 3.84 27.4 2.58	2:164 2:164 2:162 2:160 4:160 4:156 3:161 5:156	4.71 4.71 4.71 4.71 3.42 3.42 3.88 3.13	3.04 3.04 3.04 2.43 2.43 2.67 2.43
11-22	0,1	173	2:175	4.70	3.04
	0,2	253	2:175	4.70	3.04
	2,4	33.6	3:172	3.88	2.67
	4,5	6.77	3:169	3.88	2.67
	5,6	4.60	5:164	3.13	2.27
	3,7	35.4	4:170	3.42	2.43
	7,8	4.18	5:159	3.17	2.27
11-23	0,1 0,2 2,4 4,5 5,6 3,7 7,8	115 117 31.4 6.77 3.93 32.6 3.73	2:163 2:163 3:160 3:157 5:152 4:158 5:153	4.72 4.72 3.88 3.88 3.14 3.43 3.14	3.04 3.04 2.67 2.67 2.43 2.43

 $^{^{\}ast}\,0$ in the equation column refers to the D.D. value of the corresponding dependent variable as given in footnotes in the tables of equations.

Table 11-28. Autogenous healing—actual elapsed time

Nominal time, years	Actual elapsed time, months
	16.1 to 16.4
	20.1 to 24.8
	33.2 to 38.2
	48.9 to 51.2
	57.5 to 60.4

Table 11-29. Autogenous healing—average ratios of dynamic modulus after storage to that after freezing and thawing

Time, years	Cement type	n	Average	S.D.
	NAE NAE	42 477	2.38 2.34	0.60 1.46
	NAE NAE	302 59	2.34 2.20 2.81	0.82 1.81
	NAE AE	24 31	2.15 1.34	1.78 0.14
	AE	14	1.32	0.14

Table 11-30. Autogenous healing—ANOVA for differences between cements—ratio of dynamic modulus

Time, years	Cement type		n	S.S.	M.S.	F	F crit
1	NAE	Between cements_	8	8.7578	1.0947	6.92	2.30
		Within cements Total	$\frac{27}{35}$	4.2729 13.0307	0.1583		
2	NAE	Between cements_	109	480.643	4.4096	10.32	1.30
		Within cements Total	$\frac{330}{439}$	140.984 621.627	0.4272		
3	NAE	Between cements_	69	108.240	1.5687	3.64	1.37
-		Within cements Total	$\frac{210}{279}$	90.559 198.799	0.4312		
5	NAE	Between cements	4	29.0017	7.2504	2.37	
		Within cements Total	15 19	45.9077 74.9094	3.0605		
2	AE	Between cements.	5	0.0869	0.0174	1.19	2.77
		Within cements Total	18 23	0.2637 0.3506	0.0146		
3	AE	Between cements.	3	0.2485	0.0828	15.33	3.71
		Within cements Total	10 13	0.0540 0.3025	0.0054		

nominal ages for air-entrained and non-air-entrained cements.

There were no significant differences between the O-series and A-series concretes within cements. Therefore the data for the four specimens for each cement were combined in determining the within-cement variance. The critical values in column 8 headed F crit. are those which must be equalled or exceeded by the F ratios in column 7 to indicate a significant difference between cements at the 5.0 percent significance level.

For the non-air-entrained cements, there were significant differences at the nominal 1-, 2-, and 3-year periods of storage, but not at 5 years. The data for 4 years could not be subjected to this analysis because they did not include groups from the same cement, but were mainly individual values.

For the air-entrained cements a significant difference was indicated at 3 years but not at 2.

7. Discussion

7.1. Durability

Tables 11–31 amd 11–32 show selected equations for the various independent variables for the

Table 11–31. Coefficients, coef./s.d. ratios and calculated contributions of independent variables associated with durability, weight loss, and saturation ratio (Series O concretes made of AE + NAE cements)

Column	1	2	3	
Eq. No.	4	3	5	
Table No.	11-3	11-12	11-20	
Dependent variable	ODUR	OWTL	OSAT	
Constant	+88.6	-1.15	+0.586	
Air content, coef	+8.89 20.8 89	+1.42 10.0 14.2	1 -0.145 18.7 0.46	
CaA, coef coef./s.d Calculated range		$\begin{array}{c} +0.411 \\ 4.0 \\ 5.8 \end{array}$		
CaS, coef coef./s.d Calculated range	-0.53 1.9 24			
C2S, coef coef./s.d Calculated range	-0.817 3.1 37		+0.0044 8.0 0.20	
			$^{+0.0054}_{\stackrel{3.1}{0.08}}$	
Na ₂ O, coef coef./s.d Calculated range	-8.26 1.9 6	$ \begin{array}{r} -3.71 \\ 2.5 \\ 2.6 \end{array} $		
K ₂ O, coef coef./s.d Calculated range	$-20.3 \\ 4.8 \\ 22$	$ \begin{array}{c c} -8.44 \\ 6.3 \\ 9.3 \end{array} $		
MgO, coef coef./s.d Calculated range	$-2.75 \\ 3.9 \\ 14$		+0.0094 2.9 0.05	
APF, coef coef./s.d Calculated range	-0.0031 2.1 9			
			+0.0166 2.3 0.05	
Ba, coef coef./s.d Calculated range	-40.2 1.9 8			
Cu, coef coef./s.d Calculated range	-210		+0.916 2.0 0.05	
Mn, coef coef./s.d Calculated range			-0.063 1.4 0.06	
P, coef coef./s.d Calculated range			$^{+0.044}_{1.3}_{0.02}$	
Pb, coef coef./s.d Calculated range	$-208 \\ 1.8 \\ 10$	-86 2.1 4.3		
Rb, coef coef./s.d Calculated range	$-1068 \\ 2.5 \\ 11$	-315 2.6 3.2	+3.65 1.9 0.04	
Fi, coef coef./s.d Calculated range	$-14.0 \\ 2.3 \\ 1.4$	$-6.35 \\ 3.1 \\ 6.4$		
Zr, coef coef./s.d Calculated range		+11.2 1.8 5.6		

^{1 (}OAIR)0.5.

Table 11–32. Coefficients, coef./s.d. ratios, and calculated contributions of independent variables associated with durability, weight loss, and saturation ratio (Series A concretes made of AE + NAE cements)

Column	1	2	3	
Eq. No.	4	4	5	
Table No.	11-8	11–16	11-24	
Dependent variable	ADUR	AWTL	ASAT	
Constant	+52.38	+1,157	+0.2441	
Air content, coef coef./s.d Calculated range	+7.82 18.4 78	+0.902 7.0 9.0	-0.1456 ¹ 15.1 0.46	
			+0.588 2.6 0.10	
C ₃ A, coef coef./s.d Calculated range		+0.5275 4.9 7.4		
C ₂ S, coef coef./s.d Calculated range	$-0.4679 \\ 3.9 \\ 21$		+0.00468 9.7 0.21	
C ₄ AF, coef coef./s.d Calculated range		+0.6059 4.3 9.1	+0.00408 2.4 0.06	
Calculated range		+2.527 1.6 1.8		
K ₂ O, coef coef./s.d Calculated range	-15.93 3.6 18	-9.70 7.0 1.1		
MgO, coefcoef./s.dCalculated range	-2.378 3.2 12		+0.00868 3.1 0.04	
APF, coefcoef./s.dCalculated range	-0.00297 1.8 9			
C ₃ A/SO ₃ , coefcoef./s.dCalculated range			-0.00461 1.9 0.45	
Loss. coef			+0.1651 2.6 0.50	
Ba, coef coef./s.d Calculated range	-47.94 2.0 10			
Co, coef coef./s.d Calculated range			+4.76 2.1 0.05	
Cu, coef coef./s.d Calculated range	-232.0 2.5 12			
Calculated range		-4.903 2.3 4.9		
Calculated range			-2.653 2.7 0.04	
P, coef			+0.054 1.8 0.03	
Pb, coef coef./s.d Calculated range	-204.1 1.6 10	-52.54 1.3 2.6		
Rb, coefcoef./s.dCalculated range	-895.2 1.9 9	-329.2 2.2 3.3	-4.64 2.7 0.05	
Ti, coef coef./s.d Calculated range	-12.55 1.4 13	-4.379 2.0 4.4		
coef./s.d			-0.088 1.1 0.04	

^{1 (}AAIR)0.5.

Series O and Series A concretes respectively with both air-entraining and non-air-entraining cements included. The equations are presented vertically instead of horizontally as in the previous tables. Coef./s.d. ratios to indicate the probable significance of the coefficients, and the calculated ranges of the contributions of the different inde-

pendent variables are also given.

Comparison of the coefficients in the three columns of table 11-31 shows that higher air content was associated with all three of the dependent variables: durability factor, weight loss, and saturation ratio. In each case the coef./s.d. ratio was 10.0 or greater. Durability factor and weight loss are related effects, since specimens which remain in the freezing-and-thawing test longer, thus having higher durability factors, also lose more weight by sloughing. Thus, all the independent variables that appear in both columns 1 and 2 have the same sign in both. The degree of saturation at the time freezing-and-thawing tests start has a significant effect on length of time in the freezing-and-thawing test, and thus on both durability factor and weight loss. Note that all of the coefficients for independent variables that appear in column 3 as well as in either 1 or 2, with one exception, have opposite signs in column 3 to the ones in columns 1 and 2, indicating that factors that are associated with a higher degree of saturation are associated with lower durability and weight loss. Part of the correlation between saturation and air content is due to the fact that the percentage of air is included in the calculation of the saturation ratio.

The independent variables, other than air content, that showed a significant association with two or more of the dependent variables in columns 1, 2, and 3, were C₂S, C₄AF, K₂O, MgO, Cu, Rb, and Ti, with possibly Na₂O and Pb added.

Cements with high C₂S, MgO, and Cu were associated with concretes having high saturation ratios and low durability factors. However, high C₄AF, which was associated with high saturation ratio, was also associated with high weight loss but showed no significant association with durability factor. This suggests that, if these associations result from real cause and effect relationships, the mechanism by which C₄AF affects the saturation ratio differs from that by which the other independent variables affect it. Increasing loss on ignition was also significantly associated with increasing saturation ratio, but showed no significant association with either durability factor or weight loss. Increases in both the two alkalis showed significant associations with decrease in weight loss, but neither had a significant relationship to saturation ratio, and only K₂O had a significant negative association with durability factor. The coefficient for Na₂O was negative, but the coef./s.d. ratio was only 1.9. It is possible that the apparent difference between the two alkalis is due to the wider range of values that existed for K_2O as compared to Na_2O (1.1 percent compared to 0.7 percent, respectively).

Experience in the laboratory and in the field has demonstrated repeatedly and conclusively that if the objective is to produce concrete which will resist damage from freezing and thawing, so far as the paste is concerned, the easiest, cheapest, and surest way to accomplish that end, assuming the concrete is well-designed in other respects. made with good materials, and properly cured, is by the incorporation in the concrete of an adequate system of entrained air voids [2, 5]. Previous studies have indicated that, although changes in composition, fineness, or other properties of the cement may cause significant changes in durability of non-air-entrained concretes, the increase in durability produced by entrained air is so dramatic that the effects of properties of the cement are overshadowed. There is nothing in the results of the present study that changes this picture in any essential manner, although the data do serve to round out some details, thanks mainly to the large number of cements tested. One result from this study is that indications are given of what independent variables may be related to durability of non-air-entrained concretes and to what degree. No indications, unfortunately, are given as to possible relationships in air-entrained concretes directly, because of the small number of air-entraining cements tested.

The above conclusions are based on the following features of the results with the Series O concretes, with a nominal 5½ bags of cement per cubic yard and a water-cement ratio of 0.635. (Results with the A series with constant slump

are similar.)

Table 11–1 shows that all concretes made with non-air-entraining cements had durability factors less than 60, which means that they all suffered a 40-percent reduction in dynamic modulus in less than 300 cycles of freezing and thawing. All of the concretes made with air-entraining cements, however, had durability factors greater than 60, and required from about 300 to almost 1000 cycles of freezing and thawing to produce a 40-percent

reduction in dynamic E.

In table 11–3, for non-air-entrained cements only, eq 1 relates only one independent variable, air content of the concretes, to the durability factor in the laboratory freezing-and-thawing test. The coefficient for air content is highly significant, being about $3\frac{1}{2}$ times its estimated standard deviation, and a significant reduction in the overall S.D. occurs, from 11.22 to 10.85. When six more independent variables are included in the analysis (eq 3) a further significant decrease in S.D. occurs, and all of the added coefficients are greater in magnitude than their s.d.'s, although only three of them have coef./s.d. ratios greater than or equal to 2. In eq 4 with five of the trace elements included as independent variables, a further significant reduction in S.D. occurs; all of the added variables have coefficients greater in

magnitude than their s.d.'s with three being greater than two times the s.d.; and coef./s.d. ratios for the previously included independent variables are as great as or greater than the corresponding ones in eq 3. Also, in going from eq 1 to eq 3 and then to eq 4, there is a progressive increase in both coefficient and coef./s.d. ratio for the air content. To summarize, although there was a significant relationship between the durability factor and air content for the non-air-entraining cements, there was an additional significant correlation with seven out of eleven additional independent variables, after the correlation with air content was accounted for.

Turning to table 11-2 where data for 12 airentrained cements are included with the 168 nonair-entrained cements represented in table 11-4, remarks similar to those given above apply to comparisons between eq 1, 3, and 4. However, there are interesting differences between corresponding equations in the two tables. In the first place, the coefficients for air content in table 11–2 are larger than those in the corresponding equations in table 11-3, and their s.d.'s are smaller, thus causing a large increase in coef./s.d. ratio. These ratios are 3.6, 5.2, and 6.4 for eq 1, 3, and 4, respectively, in table 11-3; and 17., 20., and 21. for the corresponding equations in table 11–2. This, of course, shows the large effect of entrained air on durability. In general, however, the coefficients and coef./s.d. ratios for the other independent variables in eq 3 and 4, table 11-2 are about the same as the corresponding ones in table 11-3, with the same ones being significant in both cases. This may be explained by the fact that the added data for the independent variables other than air content were generally in the same range for the twelve air-entraining cements as for the non-air-entraining cements, while the values for air content were much higher. However, it is of interest that, even with the increase in average durability and in significance of the air content, the other independent variables still show significant correlations. It is, of course, impossible from the evidence given here to predict what would happen if a much larger number of air-entraining cements had been included, or if air-entraining cements alone had been subjected to the same type of analysis.

Statistically significant relationships, of course, do not in themselves constitute evidence of cause-and-effect relationships between variables. It is well known from experimental evidence that entrained air is a cause of increased durability, and much research has gone into investigation of the physical reasons for the effect. So far as the statistical correlations between durability and the other independent variables discussed here are concerned, however, there is no such body of knowledge available. Whether or not any of the relationships indicated are direct effects, or whether they have an indirect effect on durability through their effect on some other variable, or

whether the indicated correlation is gratuitous, can not be determined positively. Two hypotheses that appear plausible, however, and are capable of some investigation on the basis of the data obtained in this study, are that some of the independent variables other than air content may affect durability indirectly through their effect on the system of entrained air voids or through their effect on the degree to which the concretes took up water during the soaking period that preceded freezing.

The equations shown in tables 11–33 through 11–36 were calculated to investigate these hypotheses further. These tables give results for the O- and A-series concretes, with and without the air-entraining cements. The seven equations in each of the four tables all include the same set of independent variables as those in eq 4, tables 11–2 and 11–3. Also the same 177 cements are included in tables 11–33 and 11–34 and the same 165 cements in tables 11–35 and 11–36. Thus comparisons may easily be made of the effects of using different dependent variables or of adding air content, saturation ratio, or both as inde-

pendent variables.

Equation 4 in all four tables shows the relationship of the basic set of eleven independent variables to durability factor of the concretes with no other independent variables included. In the equations with all cements (tables 11-33 and 11-34) the only independent variables which had coef./s.d. ratios greater than 1.0 were C₂S, Rb, and Cu; and Rb was the only one whose ratio was greater than 2.0. For the non-air-entraining cements only, there was a difference between the series O concretes (table 11–35) and the series A concretes (table 11–36). In the former, three of the coef./s.d. ratios, C₂S, K₂O, and MgO, were greater than 2.0, and four others were greater than 1.0. In table 11–36 six coef./s.d. ratios were greater than 1.0, but none was greater than 2.0. All of the coef./s.d. ratios that were greater than 1.0 in eq 4, table 11-35, decreased in table 11-36. This indicates an effect of water-cement ratio which will be discussed further below. Note that all of the coefficients whose coef./s.d. ratios were greater than 1.0 in each of the eqs 4 were negative, indicating that increases in these variables were related to decreases in durability factor.

7.2. Effect of Alkalis on Durability

Equations 1 and 2 in all four of the tables (11–33 through 11–36) show relationships between the same set of independent variables as those in eq 4 and air content and saturation ratio of the concretes, respectively. In eqs 1 for air content, the coef./s.d. ratios for both Na₂O and K₂O are greater than 2.0 in all cases. In fact, the coef./s.d. ratios for K₂O in all four cases and for Na₂O with the non-air-entraining cements were greater than 3.0. The coefficients are all positive also, indicating that increases in the alkalis were significantly related to increased air content.

Table 11-33. Relationship of durability factor, air content, and saturation ratio to various independent variables; O series concretes, air-entraining and non-air-entraining cements

Column	1	2	3	4	5	6	7
Dependent Variable	OAIR	OSAT	OAIR	ODUR	ODUR	ODUR	ODUR
Constant	-0.890	0.637	9.20	80.8	88.4	176.	111.
s.d					8.52 0.422 20.2		7.02 0.667 10.5
Saturation ratio coef s.d coef./s.d			$-15.8 \\ 0.974 \\ 16.3$			-150. 10.75 13.9	-38.4 13.5 2.86
C ₃ S coef s.d coef./s.d	0.00236 0.0546 0.043	$\begin{array}{c} -0.000954 \\ 0.00271 \\ 0.35 \end{array}$	-0.0128 0.0339 0.38	$\begin{array}{c c} -0.502 \\ 0.551 \\ 0.91 \end{array}$	-0.522 0.296 1.77	0.645 0.374 1.72	$-0.556 \\ 0.290 \\ 1.92$
C ₂ S coef s.d coef./s.d	-0.00461 0.0502 0.092	$0.00425 \\ 0.00249 \\ 1.71$	0.0627 0.0314 2.00	-0.915 0.506 1.81	$-0.876 \\ 0.272 \\ 3.22$	$ \begin{array}{c c} -0.279 \\ 0.347 \\ 0.80 \end{array} $	$-0.719 \\ 0.272 \\ 2.65$
Na ₂ O coef s.d coef./s.d	1.779 0.823 2.16	$ \begin{array}{r} -0.0746 \\ 0.0408 \\ 1.83 \end{array} $	0.600 0.516 1.16	6.81 8.30 0.82	-8.34 4.52 1.85	-4.35 5.69 0.76	-8.54 4.42 1.93
K ₂ O coef s.d coef./s.d	2.51 0.787 3.19	$ \begin{array}{c} -0.1070 \\ 0.0390 \\ 2.74 \end{array} $	0.818 0.499 1.64	1.31 7.94 0.17	$ \begin{array}{r} -20.1 \\ 4.39 \\ 4.58 \end{array} $	-14.7 5.51 2.67	$-20.4 \\ 4.30 \\ 4.75$
MgO coef s.d coef./s.d	$0.176 \\ 0.133 \\ 1.33$	-0.000798 0.00658 0.12	$0.164 \\ 0.0824 \\ 1.99$	-0.807 1.34 0.60	$ \begin{array}{c c} -2.31 \\ 0.723 \\ 3.20 \end{array} $	$ \begin{array}{c} -0.927 \\ 0.909 \\ 1.02 \end{array} $	-2.08 0.712 2.92
APF coef s.d coef./s.d.	0.000265 0.000286 0.93	-0.00000909 0.0000143 0.64	$\begin{array}{c} 0.000121 \\ 0.000178 \\ 0.68 \end{array}$	-0.000702 0.00289 0.24	$\begin{array}{c} -0.00296 \\ 0.00155 \\ 1.90 \end{array}$	$\begin{array}{c} -0.00206 \\ 0.00196 \\ 1.05 \end{array}$	-0.00291 0.00152 1.91
3a coef s.d coef./s.d	1.038 4.15 0.25	-0.0363 0.206 0.18	$0.463 \\ 2.58 \\ 0.18$	-28.2 41.8 0.67	-37.0 22.5 1.64	$-33.6 \\ 28.4 \\ 1.18$	-36.8 22.0 1.67
Rb coef s.d coef./s.d.	-168, 79,2 2,12	1.063 3.93 0.27	-151. 49.2 3.08	-2416. 799. 3.02	-984. 435. 2.26	$ \begin{array}{c c} -2257. \\ 543. \\ 4.16 \end{array} $	-1195. 432. 2.77
coef s.d coef./s.d	5.07 22.4 0.23	-0.387 1.109 0.35	-1.063 13.9 0.077	-171. 225. 0.76	-214. 121. 1.77	-229. 153. 1.49	-221. 119. 1.87
coef s.d coef./s.d	1.46 1.17 1.25	-0.0711 0.0580 1.23	0.335 0.729 0.46	0.936 11.79 0.079	-11.50 6.36 1.81	-9.70 8.05 1.21	-12.0 6.23 1.93
coef s.d coef./s.d	-4.10 16.1 0.26	1.135 0.796 1.43	13.9 10.02 1.38	-229. 162. 1.41	-194. 87.0 2.23	-58.7 111. 0.53	-156. 86.1 1.81

The question arises, if increased alkali content was associated with increased air content, why was it not also associated with a higher durability factor? Looking at the coefficients for the two alkalis in eq 2 in all four tables, we find that all eight of the coef./s.d. ratios were greater than 1.0, and all but three of these were greater than 2.0. The coefficients, however, are all negative, indicating that a decrease in saturation ratio was associated with increases in alkali content. This again might be expected to indicate that increases in alkali content should be associated with increased durability.

In eq 3 with air content as the dependent variable and saturation ratio included as an independent variable, the coef./s.d. ratios for the

alkalis are consistently reduced and remain significant only for the non-air-entrained cements.

Comparing eq 4, in which durability factor is related only to the basic set of 11 independent variables, with eq 5, 6, and 7, in which air content alone, saturation ratio alone, and both together are included as independent variables, shows that whatever relationship existed between the basic independent variables in these equations and durability was influenced by their relationship with air content and saturation ratio. Of the 148 coefficients for independent variables (not counting the constant terms) in eqs 5, 6, and 7, only six had coef./s.d. ratios less than 1.0, but 66, or about 45 percent had coef./s.d. ratios greater than 2.0.

For the alkalis specifically, note that in eq 4

Table 11-34. Relationship of durability factor, air content and saturation ratio to various independent variables; A series concretes, air-entraining and non-air-entraining cements

Column	1	2	3	4	5	6	7
Dependent variable	AAIR	ASAT	AAIR	ADUR	ADUR	ADUR	ADUR
Constant	-3.91	-0.845	10.59	60.1	88.2	180.	135.
Air content coef s.d coef./s.d					7.17 0.431 16.6		- 4.25 - 0.778 - 5.47
saturation ratio coefs.d coef./s.d			-17.2 0.827 20.8			-142. 8.93 15.9	-69.1 15.7 4.40
coef s.d coef./s.d	$\begin{array}{c} 0.0249 \\ 0.0618 \\ 0.40 \end{array}$	$-0.00254 \\ 0.00306 \\ 0.83$	-0.0188 0.326 0.58	$ \begin{array}{r} -0.249 \\ 0.559 \\ 0.45 \end{array} $	$ \begin{array}{r} -0.427 \\ 0.342 \\ 1.25 \end{array} $	$\begin{array}{c} -0.610 \\ 0.352 \\ 1.73 \end{array}$	-0.530 0.325 1.63
C ₂ S coefs.d coef./s.d	0.0298 0.0568 0.53	$0.00224 \\ 0.00282 \\ 0.80$	0.0683 0.0300 2.28	-0.682 0.514 1.33	$-0.896 \\ 0.314 \\ 2.85$	-0.364 0.324 1.12	-0.654 0.303 2.16
Na ₂ O coef s.d coef./s.d	1.87 0.930 2.01	$-0.130 \\ 0.0461 \\ 2.79$	$-0.344 \\ 0.501 \\ 0.69$	5.77 8.41 0.69	-7.62 5.21 1.46	-12.5 5.42 2.32	-11.08 5.00 2.22
	2.98 0.890 3.35	$\begin{array}{c} -0.162 \\ 0.0441 \\ 3.68 \end{array}$	$0.196 \\ 0.487 \\ 0.40$	1.90 8.05 0.24	-19.5 5.09 3.83	$-21.1\\ 5.26\\ 4.02$	-22.0 4.86 4.53
MgO coef s.d coef./s.d	$0.262 \\ 0.150 \\ 1.74$	$\begin{array}{c} -0.00318 \\ 0.00744 \\ 0.43 \end{array}$	0.207 0.0791 2.62	-0.306 1.36 0.23	-2.18 0.838 2.61	-0.758 0.854 0.89	$\begin{array}{c} -1.64 \\ 0.804 \\ 2.04 \end{array}$
APF coefs.dcoef./s.d	$\begin{array}{c} 0.000377 \\ 0.000324 \\ 1.17 \end{array}$	$\begin{array}{c} -0.0000133 \\ 0.0000160 \\ 0.83 \end{array}$	$\begin{array}{c} 0.000149 \\ 0.000171 \\ 0.88 \end{array}$	$\begin{array}{c} -0.000381 \\ 0.00293 \\ 0.13 \end{array}$	$\begin{array}{c} -0.00309 \\ 0.00180 \\ 1.72 \end{array}$	$\begin{array}{c} -0.00227 \\ 0.00184 \\ 1.23 \end{array}$	$\begin{array}{c} -0.00290 \\ 0.00170 \\ 1.70 \end{array}$
Ba coefs.d coef./s.d	2.88 4.69 0.61	-0.288 0.233 1.24	-2.06 2.48 0.83	$-20.4 \\ 42.4 \\ 0.48$	$-41.1 \\ 26.0 \\ 1.58$	-61.3 26.8 2.29	-52.5 24.8 2.12
Rb coef s.d coef./s.d	-184. 89.6 2.05	$0.915 \\ 4.44 \\ 0.21$	-168. 47.2 3.56	-2241. 810. 2.77	-925. 502. 1.84	-2111. 510. 4.14	-1397. 488. 2.86
Pb coef s.d coef./s.d	11.7 25.3 0.46	-1.153 1.25 0.92	-8.09 13.3 0.61	-106.2 229. 0.46	$-190. \\ 140. \\ 1.36$	-270. 144. 1.87	-236. 133. 1.77
Гі coef s.d coef./s.d	2.09 1.32 1.58	$\begin{array}{c} -0.1172 \\ 0.0656 \\ 1.79 \end{array}$	0.0825 0.703 0.12	3.88 11.96 0.32	$^{-11.13}_{\begin{array}{c} 7.37\\ 1.15 \end{array}}$	$-12.8 \\ 7.59 \\ 1.68$	-13.1 7.00 1.87
Cu coef s.d coef./s.d	-7.08 18.2 0.39	$0.768 \\ 0.900 \\ 0.85$	6.10 9.58 0.64	-275. 164. 1.68	$-225. \\ 100.4 \\ 2.24$	$-166. \\ 103.5 \\ 1.16$	-192. 95.5 2.01

only one of the eight coef./s.d. ratios is greater than 2.0, and only two others greater than 1.0. However, in eqs 5, 6, and 7 in the four tables, 22 of the 24 coefficients for the two alkalis are greater than 1.0 and 14 of these are greater than 2.0.

It has been established by research over a number of years that the beneficial effect of entrained air on the durability of concrete depends not only on the amount of air present, but also on the character of the distribution of that air throughout the paste matrix [16, 17, 18, 19]. For the air to be effective in preventing the build-up of pressures which can cause disruption of the paste during freezing, a significantly large proportion of the total volume of air needs to be present

in the form of small discrete bubbles, evenly distributed throughout the paste. Two parameters of the air void system in the hardened concrete which are of importance in relation to the efficacy of that system in providing protection from frost damage are: (1) the specific surface, α , which is a measure of the ratio of total surface area of the voids to their total volume, and (2) spacing factor, \overline{L} , which is a measure of the average distance between adjacent bubbles in the paste, and thus of the average distance water has to travel in the paste to a bubble where it can freeze without causing trouble. Large α and small \overline{L} are related to better frost resistance of the concrete.

The results of studies by Mielenz and others

Table 11-35. Relationship of durability factor, air content, and saturation ratio to various independent variables; O series concretes, non-air-entraining cements.

				1			
Column	1	2	3	4	5	6	7
Dependent variable	OAIR	OSAT	OAIR	ODUR	ODUR	ODUR	ODUR
Constant	-1.59	0.638	2.62	80.2	91.4	129.	119.
s.d					7.00 1.10 6.36		3.74 1.39 2.69
Saturation ratio coef s.d coef./s.d			$-6.61 \\ 0.634 \\ 10.4$			-76.4 11.07 -6.91	-51.8 14.2 3.65
Cos coef s.d coef./s.d	$0.0267 \\ 0.0224 \\ 1.20$	$\begin{array}{c} -0.00153 \\ 0.00219 \\ 0.70 \end{array}$	0.0166 0.0172 0.97	-0.343 0.342 1.004	-0.530 0.306 1.73	$-0.461 \\ 0.300 \\ 1.54$	$ \begin{array}{c c} -0.523 \\ 0.295 \\ 1.77 \end{array} $
C ₂ S coef s.d coef./s.d	0.01104 0.021 0.54	0.00391 0.00201 1.95	$0.0368 \\ 0.0159 \\ 2.31$	$ \begin{array}{c c} -0.777 \\ 0.314 \\ 2.48 \end{array} $	-0.854 0.280 3.05	-0.478 0.278 1.72	$\begin{array}{c} -0.616 \\ 0.277 \\ 2.22 \end{array}$
Va ₂ O coef s.d coef./s.d	1.056 0.331 3.19	-0.0495 0.0323 1.53	0.729 0.255 2.85	0.412 5.06 0.082	-6.98 4.66 1.50	-3.37 4.46 0.76	-6.10 4.48 1.36
K ₂ O coef s.d coef./s.d	1.114 0.324 3.44	$-0.0614 \\ 0.0317 \\ 1.94$	$0.708 \\ 0.251 \\ 2.82$	-10.44 4.95 2.11	-18.2 4.58 3.98	-15.1 4.39 3.45	-17.8 4.41 4.03
MgO coef s.d coef./s.d	0.0478 0.0544 0.88	0.00357 0.00532 0.67	0.0714 0.0418 1.71	$-2.13 \\ 0.832 \\ 2.55$	$ \begin{array}{r} -2.46 \\ 0.744 \\ 3.31 \end{array} $	-1.85 0.729 2.54	$\begin{array}{c} -2.12 \\ 0.721 \\ 2.94 \end{array}$
APF coef s.d coef./s.d	0.000115 0.000117 0.99	$\begin{array}{c} -0.00000169 \\ 0.0000114 \\ 0.15 \end{array}$	0.000104 0.0000895 1.16	-0.00265 0.00179 1.48	$\begin{array}{c} -0.00346 \\ 0.00160 \\ 2.16 \end{array}$	-0.00278 0.00156 1.78	-0.00317 0.00154 2.06
Ba coef s.d coef./s.d	2.78 1.65 1.69	-0.109 0.161 0.68	2.06 1.26 1.63	-16.6 25,2 0.66	-36.0 22.7 1.59	-24.9 22.1 1.13	-32.6 21.8 1.50
Rb coef s.d coef./s.d	45.7 32.4 1.41	$ \begin{array}{r} -6.01 \\ 3.16 \\ 1.90 \end{array} $	$\substack{6.01\\25.1\\0.24}$	-590. 494. 1.19	-910. 444. 2.05	-1050. 438. 2.40	-1072. 429. 2.50
Pb coef s.d coef./s.d	7.21 8.85 0.81	$-0.469 \\ 0.864 \\ 0.54$	4.11 6.79 0.61	-149. 135. 1.10	-199. 121. 1.65	-184. 118. 1.56	-200. 116. 1.72
Ti coef s.d coef./s.d	0.915 0.479 1.91	-0.0553 0.0468 1.18	$0.550 \\ 0.369 \\ 1.49$	-5.89 7.32 0.81	-12.3 6.60 1.86	-10.1 6.43 1.57	-12.2 6.35 1.92
Cu coef s.d coef./s.d	15.4 6.40 2.41	0.440 0.625 0.70	18.3 4.92 3.72	-62.1 97.9 0.63	-170. 88.9 1.91	-28.5 85.8 0.33	-96.9 87.8 1.10

[20] on the mechanisms by which air-entraining agents facilitate the production of an efficacious air void system in hardened concrete, provide possible explanations for some of the trends shown by these data. In plastic concrete, the air in smaller voids, which are those mainly responsible for the increased durability of air-entrained concrete, is under greater pressure than that in larger voids. The tendency is for air in the smaller voids to dissolve in the water in the mix until the latter becomes saturated and then for air to be released from the solution into larger voids which are under lower pressure [21]. Thus, while the concrete is still plastic, larger air bubbles tend to grow at the expense of smaller bubbles producing an increase

in total air content (providing too many of the large bubbles do not escape from the surface), a decrease in specific surface α of the air void system, and an increase in the spacing factor \bar{L} . The effect of a good air-entraining agent is to change conditions at the air-water interface in such a way as to decrease the rate of transfer of air from smaller bubbles to larger ones, and thus to preserve the system of smaller bubbles which is effective in producing increased frost resistance.

Mielenz, et al, [20] show that certain constituents that may be introduced by the cement and certain characteristics of the concrete mixes or their handling prior to hardening, have an effect on the operation of air-entraining agents. Their

Table 11-36. Relationship of durability factor, air content, and saturation ratio to various independent variables; A series concretes, non-air-entraining cements

Column	1	2	3	4	5	6	7
Dependent variable	AAIR	ASAT	AAIR	ADUR	ADUR	ADUR	ADUR
Constant	-3.94	0.825	3,28	68.7	97.1	142.	136.
Air content coef s.d coef./s.d					7.19 1.04 6.92		
coef s.d			-8.75 0.533 16.4				-72.7 18.1 4.03
coef s.d	$0.0444 \\ 0.0255 \\ 1.74$	-0.00301 0.00233 1.29	$0.0181 \\ 0.0154 \\ 1.17$	-0.213 0.374 0.57	-0.532 0.331 1.61	-0.481 0.314 1.53	-0.515 0.315 1.63
C ₂ S coef	$0.0348 \\ 0.0234 \\ 1.49$	0.00211 0.00213 0.99	$0.0533 \\ 0.0141 \\ 3.77$	-0.631 0.343 1.84	$\begin{array}{c} -0.881 \\ 0.302 \\ 2.91 \end{array}$	-0.443 0.287 1.54	-0.543 0.300 1.81
Va2O coef s.d coef./s.d	$1.170 \\ 0.376 \\ 3.11$	$\begin{array}{c} -0.103 \\ 0.0344 \\ 2.99 \end{array}$	0.270 0.233 1.16	0.439 5.53 0.79	-7.97 4.99 1.60	-8.73 4.75 1.84	-9.23 4.77 1.94
C2O coef	$1.42 \\ 0.369 \\ 3.84$	-0.105 0.0337 3.10	$0.500 \\ 0.229 \\ 2.18$	-9.03 5.42 1.67	-19.2 4.96 3.87	-18.4 4.66 3.93	-19.3 4.73 4.08
MgO coef s.d coef./s.d	$0.0992 \\ 0.0619 \\ 1.60$	0.00282 0.00566 0.50	$0.124 \\ 0.0373 \\ 3.32$	$^{-1.81}_{\substack{0.910\\1.99}}$	-2.52 0.803 3.14	$\begin{array}{c} -1.56 \\ 0.761 \\ 2.05 \end{array}$	-1.79 0.787 2.28
coef s.d	$\begin{array}{c} 0.000211 \\ 0.000133 \\ 1.59 \end{array}$	$\begin{array}{c} -0.00000460 \\ 0.0000121 \\ 0.38 \end{array}$	$\begin{array}{c} 0.000171 \\ 0.0000801 \\ 2.14 \end{array}$	$\begin{array}{c} -0.00243 \\ 0.00195 \\ 1.25 \end{array}$	$\begin{array}{c} -0.00395 \\ 0.00172 \\ 2.29 \end{array}$	-0.00284 0.00163 1.74	$\begin{array}{c} -0.00316 \\ 0.00165 \\ 1.91 \end{array}$
coef s.d coef./s.d	4.88 1.87 2.60	$\begin{array}{c} -0.374 \\ 0.171 \\ 2.18 \end{array}$	1.61 1.15 1.40	$ \begin{array}{r} -9.40 \\ 27.5 \\ 0.34 \end{array} $	-44.5 24.6 1.81	-42.7 23.3 1.83	-45.7 23.5 1.95
coef s.d coef./s.d	49.7 36.8 1.35	-7.70 3.36 2.29	-17.7 22.6 0.78	-560. 541. 1.04	-918. 476. 1.93	-1247. 459. 2.71	-1214. 460. 2.65
coef s.d coef./s.d	15.0 10.07 1.49	$ \begin{array}{c c} -1.28 \\ 0.920 \\ 1.39 \end{array} $	3.78 6.10 0.62	-75.4 148. 0.51	-183. 130. 1.41	-190. 124. 1.53	-197. 124. 1.58
coef s.d coef./s.d	1.35 0.545 2.48	-0.0921 0.0498 1.85	$0.547 \\ 0.332 \\ 1.65$	-4.38 8.00 0.55	-14.1 7.14 1.98	-12.6 6.76 1.86	-13.6 6.81 2.00
coef s.d coef./s.d	15.3 7.29 2.10	-0.0561 0.666 0.084	14.8 4.39 3.37	-123. 107. 1.15	-232. 95.0 2.45	-128. 89.4 1.43	-155. 92.6 1.68

work was done mainly on neat cement slurries and pastes to which air-entraining agents had been added, while the work reported here was done on concretes most of which were made with non-air-entraining cements. However, the fact that many of the effects detected with our data are compatible with the explanations given by Mielenz, et al., and these comparisons tend to be reinforced when the twelve air-entraining cements are included in the analysis appears to be worthy of consideration. There are substances which may accidentally or purposefully (such as grinding aids) become incorporated in a non-air-entraining cement which may act to some extent as air-entraining agents, and if such substances are

present, then the effects shown in Mielenz work might explain some of our indicated relationships. Unfortunately measurements on the air-void systems in the hardened concretes are not available at the present time to provide a further check on possible conclusions, but the indicated trends are explored here.

In the Bureau of Reclamation work [22] some mixtures were prepared with NaOH added. It was known that Na+ and K+ ions had a depressing effect on calcium in solution, and it was therefore postulated that sodium would have an adverse effect on the action of air-entraining agents which produced a film composed of the calcium salt of the surface active constituent of the agent. The

result of the addition was that \bar{L} increased and α decreased compared to those obtained with similar mixes with the same w/c ratio and without the added alkali. In Mielenz' slurries the total air content measured by the air meter remained constant when the alkali was added, while in our data, air content consistently increased with increased alkali. This could be explained by the hypothesis that in the neat cement mixture the large voids present and produced by coalescence of smaller ones could escape more easily, while in concrete mixtures, the large voids tend more to be retained by adhesion to or entrapment in the aggregate particles. Thus the negative association between durability factor and alkalis shown in our concrete data in spite of the positive association between air content and alkali, could be explained by the hypothesis that dissolution of small bubbles and growth of the large ones took place.

7.3. Saturation Ratio

Explanations of the negative associations of saturation ratios with the alkalis are more doubtful. It seems reasonable to assume that if alkalis have some effect on the size, closeness together, and possible interconnections of the air voids in the concrete, they would also have some effect on the rate at and extent to which the concrete could soak up water. However, the fact that coefficients for the alkalis are negative in equations in which the saturation ratio is the independent variable while they are positive in relation to air content could be largely due to the circumstance that air content is a factor in the denominator of the formula for calculating saturation ratio.

7.4. Water-Cement Ratio

Water-cement ratio is another factor which is shown by Mielenz to have an effect on the rate of dissolution of small voids and thus on spacing factor, specific surface, and durability [23, 24]. Increased water/cement ratio tends to increase the fluidity of the mixture, thus aiding the dissolution of small bubbles and decreasing frost resistance. Comparisons between equations in table 11-33 and 11-35 for constant w/c concretes with corresponding ones in tables 11-34 and 11-36 where w/c varied, are somewhat inconclusive, but there are some differences which may be of interest. For instance, comparing eqs 4 in tables 11-35 and 11-36, shows that for all of the independent variables except one, the coef./s.d. ratios in table 11–35 are larger than those in table 11–36. This would indicate that permitting the w/c to vary increased the variation in durability factor and thus reduced the significance of the other

variables in the equation when this extra variation was not accounted for. In order to check this further, some additional equations, not presented here, were calculated using w/c ratio of the Aseries concretes as a dependent variable with the following results: Water-cement ratio (at constant slump)

a. had a negative relationship to air content;

b. had a positive relationship to saturation ratio:

c. had a negative relationship with durability factor when all cements were included, but was not significant when the air-entraining cements were excluded.

As Dr. Mielenz observed in a private communication, item c above "is extremely important since it shows the significance of w/c even when concrete is purposefully air-entrained. One explanation is the decreasing value of alpha as w/c increases."

7.5. Slump

According to Mielenz [25] decreased slump decreases average void size. Additional equations calculated from our data using the slump of the constant w/c ratio concretes indicated the following:

Slump (at constant w/c ratio):

a. had a positive relationship with air content;

 b. had a negative relationship with saturation ratio when all cements were included, but was not significant when air-entraining cements were included;

c. had a positive relationship with durability

The picture here is somewhat confused. Mielenz' tests showed that the effect of slump on durability factor was different with different types of airentraining agents [26]. With our data, there is no information as to what kind of substance, if any, was acting as an air-entraining agent in the nonair-entraining cements, nor even what types were present in the air-entraining cements. As Mielenz pointed out in the private communication mentioned above, "the correlations that are forthcoming from my tests (Series II in ref. [23]) are not subject to the same interpretation as are your data because my tests compare the effect of slump on given cement-AEA combinations whereas yours evaluate the effect of slump on concretes containing diverse cements, the variation in slump occurring at constant w/c. In other words, the concretes developing high slump in your tests contain cements of proportionately lower water requirement, in part because they are air entraining.

In spite of the complications, in view of all the evidence, it seems reasonable to suspect that whatever effect slump has on air content and durability may be largely due to an effect of some kind on the character of the air void system.

7.6. Setting Time

The last variable for which there is any basis for comparing our findings with those of Mielenz is setting time. He points out that anything that prolongs the time of setting increases the time available for dissolution of smaller bubbles before hardening takes place, and therefore results in lower specific surface and higher spacing factor [27]. Mielenz' work was done on neat cement mixtures with retarders added to prolong setting time, whereas in our tests on concretes, only the results of normal variation in setting time of the cements were available. No tests of setting time of the concretes were made. However, additional equations calculated with setting time of the cements as an independent variable produced the following results:

a. both initial and final set had a significant positive relationship with air content when all cements were included, but not when the air-

entraining cements were excluded;

b. both initial and final set had a significant positive relationship to saturation ratio with only non-air-entraining cements; and final set had a significant positive relationship when all air-entraining cements were included;

c. both initial and final set had significant positive relationships with durability factor when

saturation ratio was also included as an independent variable, both with all cements and with air-entraining cements excluded.

Mielenz had the following to say on these results, "The correlation involving setting time of the cements indicates that this property influences the various qualities of the concrete directly or indirectly. A time-of-setting test on the matrix of concrete would be more meaningful. Your correlation of set with air content (a, above) suggests that air content of AE concrete increases with setting time of air-entraining cement, but possibly the relationship is due to a tendency of the AE addition to increase setting time of the cement, rather than through any direct action of setting time on the air content of concrete."

So far as the remaining independent variables in the equations in tables 11–33, 11–34, 11–35, and 11–36 are concerned, we are not aware of any other work with which our results might be compared. Air permeability fineness appears to have a negative association with durability factor for the non-air-entraining cements only when air content is also included as an independent variable. MgO also shows significant negative association with durability factor when air content is included, both with and without the air-entraining cements. Of the trace elements the only one which

shows a consistent significant relationship with

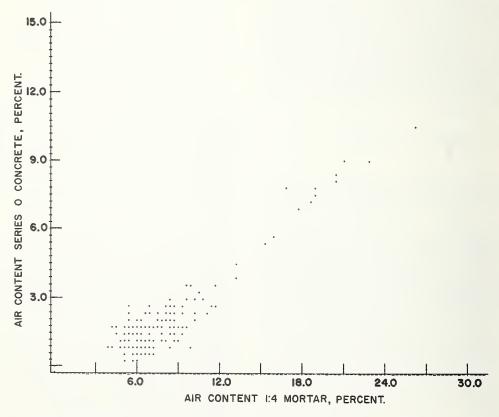


FIGURE 1. Results of plotting the air content of Series O concretes made with AE + NAE cements versus the air content of 1:4 (cement to 20-30 Ottawa sand) mortars.

durability factor is rubidium. This association is most consistent when saturation ratio is included

as an independent variable.

When one considers the small amounts in which rubidium and other trace elements are present in the cement, it seems unreasonable that they should have an effect on such a gross property of the concretes in which the cements are incorporated as the number of cycles of freezing-and-thawing the concrete specimens can withstand. If Rb, for instance, does have a real effect, it seems that it would probably come about by means of some such mechanism as an effect on the most finely divided portion of air void system such as those shown by Mielenz and his colleagues. Effects of some of the trace elements should be investigated directly with neat cement mixtures using similar techniques.

It is interesting to note that for all the independent variables except air content in eqs 4, 5, 6, and 7 in tables 11–33 through 11–36 that have coef./s.d. ratios greater than 1.0, the coefficients are negative. This tends to indicate that, if the hypothesis that the effect on durability is due to an effect on the films protecting the small air voids is valid, most of the minor ingredients that have an effect have an adverse effect on the air

void system.

7.7. Air Content of Test Mortars Versus Air Content of Concretes

The relationship between the air in the Series O concrete (made with a w/c of 0.635) and the air in the standard 1:4 (cement to 20–30 Ottawa sand) mortar is presented in figure 1. This graph is a plot of the values of both the AE and the NAE cements. Some of the plotted points represent more than one value because of the limitations of the computer printer when used as a plotter. A corresponding plot of the air contents of Series A concretes (5 \pm 1-in slump) versus the air content of the 1:4 mortars, both made of AE + NAEcements, is presented in figure 2. In both figures 1 and 2, the cements having high air content in the 1:4 mortar also had high air content in the concrete. The Series O concretes appeared to have a smaller dispersion of values.

Using different scales, plots were also made of the relationships of air in concrete and air in mortar made of the NAE cements. These plots are presented in figures 3 and 4 for the Series O and A concretes respectively.

The equations calculated for the relationships between the air content of the 1:4 (cement to 20–30 Ottawa sand) mortars (SAIR) and the air

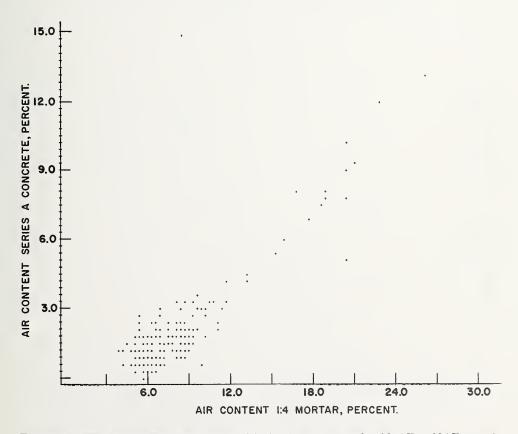


Figure 2. Results of plotting the air content of Series A concretes made with AE + NAE cements versus the air content of 1:4 (cement to 20–30 Ottawa sand) mortars.

content of the Series O and A concretes made of AE + NAE, and the NAE cements are presented in table 11–37. The reduction of variance ("F" values) was, in each equation, highly significant.

However, when the AE cements were included as in eqs 1 and 2 the "F" values were about 10 times those of eqs 3 and 4 where only the NAE cements were included.

Table 11-37. Relationship of air-contents of concretes OAIR and AAIR, and the air-contents of 1:4 (cement to 20-30 Ottawa sand) mortars, SAIR

Equation No.	Figure No.	Cement type	<u> </u>		"F"	D.F.	Critical F
1	1	AE+NAE	OAIR = $-1.604 + 0.455$ s.d. $(0.114) (0.013)$	SAIR	638	2:189	3.05
2	2	AE+NAE	$\begin{array}{ll} AAIR &=& -2.103 + 0.560 \\ s.d. &=& (0.145) & (0.016) \end{array}$	SAIR	488	2:189	3.05
3	3	NAE	OAIR = $-0.388 + 0.274$ s.d. = (0.178) (0.024)	SAIR	66	2:175	3.05
4	4	NAE	AAIR = -0.703 + 0.307 s.d. = (0.214) (0.029)	SAIR	57	2:175	3.05

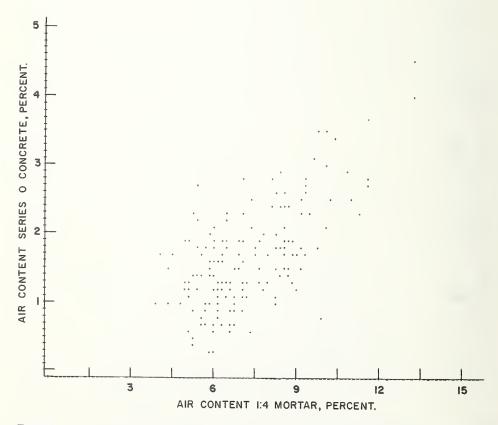


Figure 3. Results of plotting the air content of Series O concretes made with NAE cements versus the air content of 1:4 (cement to 20-30 Ottawa sand) mortars.

8. Summary and Conclusions

Laboratory freezing-and-thawing tests were conducted on concretes made of 199 portland cements of different types and from different sources. One series of concretes was made using a water/cement ratio of 0.635 and the other series with the quantity of water adjusted to give a 5 ± 1 -in slump. A nominal quantity of 5.5 bags of cement per cubic yard was used. The 3- \times 4-× 16-in specimens were moist cured for 14 days then air dried for 28 days after which the rapid (2 hr) cycles of freezing and thawing in water were started. The durability factor was calculated from the relative dynamic Youngs' modulus of elasticity, on the basis of 40-percent reduction or 300 cycles depending on which occurred first. The freezing-and-thawing cycles were continued until a 40-percent reduction in modulus was attained with all specimens. The specimens were then placed in a fog room for different periods and determinations made of the increase in fundamental resonant frequency in order to determine the extent of autogenous healing.

8.2. The saturation ratio or amount of water absorbed in 24 hours divided by the possible absorption ranged from 0.20 to more than 0.80.

8.3. The durability factor for the concretes which had been dried in laboratory air for 28 days

following moist air curing for 14 days ranged from about 5 to 95 when frozen and thawed in water.

8.4. The concretes made with non-air-entraining cements withstood from 10 to about 300 cycles of freezing and thawing before the dynamic modulus was reduced to 60 percent of that at the start of the tests. The average number of cycles was about 100. The concretes made of the air-entraining cements required about 300 to 900 cycles of freezing and thawing for a reduction of 40 percent in dynamic modulus.

8.5. At the time the concrete specimens had attained a 40-percent reduction in dynamic modulus there was a weight loss ranging up to 22 percent. A few specimens which failed very early

had a slight weight gain.

8.6. After the freezing-and-thawing tests had been continued until there was a 40-percent loss of dynamic modulus the concrete specimens were stored in a fog room and retested after 1, 2, 3, 4, or 5 years. The non-air-entrained concretes generally regained their original dynamic modulus or more, but the air-entrained specimens did not gain as much. All of the regain of dynamic modulus took place in 16 months or less. There were significant differences between cements in amount of autogenous healing.

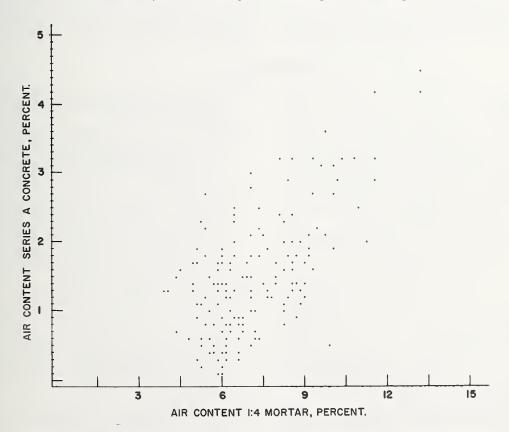


Figure 4. Results of plotting the air content of Series A concretes made with NAE cements versus the air content of 1:4 (cement to 20-30 Ottawa sand) mortars.

8.7. Computations of multivariable equations by a least-squares method were used to determine the chemical and physical properties associated with the durability factor, weight-loss at 40-percent reduction of dynamic modulus, and saturation ratio. The equations were computed for concretes made from all cements for which minor constituents and trace elements had been determined. The equations were computed using as independent variables either the major potential compounds or the major oxides, each with other commonly determined variables, and these with trace elements found to be significant.

The following observations relate to equations as summarized in tables 11–31 and 11–32 for concretes made of AE + NAE cements using a water/cement ratio of 0.635 and concretes made

having a slump of 5 ± 1 in.

8.7.1. The durability factor was primarily dependent on the air content of the concretes. Increases in C₂S, K₂O, MgO and possibly Cu, Rb, Ti and fineness were associated with decreases

of the durability factor.

8.7.2. An increase of the air content was associated with an increase of the weight-loss at the time of 40-percent reduction of dynamic modulus. Increases of C₃A and C₄AF were also associated with increases of the weight-loss. Increases in K₂O and possibly Na₂O, Pb, Rb, and Ti were associated with decreases of the weight-loss.

8.7.3. An increase of the air-content was associated with a decrease of the saturation ratio. An increase of the C₂S, C₄AF and possibly MgO, loss on ignition, Rb, Ni, Co, and Cu were associated with an increase of the saturation ratio.

8.8. Computations of multivariable equations for the concretes made with non-air-entraining cements were in general agreement with those calculated with all the cements. The coefficients for the air content of the concretes were generally not so highly significant as when the air-entraining cements were included but they were generally significant.

Computations made using the principal oxides together with other commonly determined variables, or these with minor constituents and trace elements resulted in equations with nearly the same estimated standard deviation values as when the calculated major potential compounds

were used as independent variables.

The coefficients for the individual trace elements were generally not highly significant when used in multivariable equations for some of the dependent variables and their use did not always result in a significantly better fit, i.e., a significantly lower estimated standard deviation.

8.11. There was a good correlation between the air entrained in the concrete and that entrained in the standard 1:4 (cement to 20-30

Ottawa sand) mortar.

There was evidence that some of the variables such as alkali, water/cement ratio, slump, and possibly setting time, might have influenced durability through an effect on the air-void system, particularly the small air voids, as reported by Mielenz and others.

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Section 12. Water-Loss and Absorption of Concrete

R. L. Blaine and H. T. Arni

The relationships between portland cement characteristics and the loss of weight on drying in air for 56 days and the absorption with subsequent 28 days storage in water of concretes were studied by computing multivariable regression equations with the aid of a digital computer. The percentage absorption on rewetting was significantly related to the weight loss of concretes when air dried. The composition of the cement and the air-content of the concretes were also found to be related to the weight-loss and absorption as well as to ratios of weight-gain/weight-loss. The effects of trace elements in the cements were generally of doubtful significance in the drying and absorption tests.

Key words: Absorption; cement composition; concrete; loss on drying; portland cement; trace elements.

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1. Introduction

The resistance of concrete to attack by salts and other chemical reagents is dependent to some extent on the quality of the concrete. Thus, a concrete made with a high water/cement ratio is more subject to attack than one made of the same cement with a low water/cement ratio. Also, a concrete made with an adequate cement content is more resistant than a leaner concrete. The degree of hydration at the time of exposure to destructive reagents can also be a factor. The porosity and permeability of concrete may be associated with all of these variables.

The amount of an aggressive solution which can

be absorbed is dependent to some extent on the amount of water that is removed on drying.

Lea and Desch [1]¹ have indicated that the weight loss as a result of drying and the weight gain with subsequent rewetting are dependent on conditions of testing, such as temperature and time of drying and rewetting. In this study the specimens were dried under standard laboratory conditions, and the effects of different temperatures, humidities, and drying times were not investigated.

 $^{^1\,\}mathrm{Figures}$ in brackets refer to literature references at the end of this section (p. 68).

2. Materials

2.1. Cements

The portland cements used in this study have previously been described [2,3,4]. They consisted of 199 commercially manufactured cements of different types, and were obtained from different areas of the USA, plus a few from other countries. These cements were classified primarily on the basis of their chemical analyses and physical tests.² The chemical analyses and other tests indicated a fairly broad range of properties.

2.2. Aggregates

The aggregates were, as indicated previously, [2] a high quality rounded quartzite coarse aggregate (White Marsh) and a sand from the same

source. The fineness modulus for the sand was 2.82, for the coarse aggregate, 6.82, and for the combined aggregates 4.82.

2.3. Concrete

The procedures used in mixing and preparing the 6- \times 8- \times 16-in concrete specimens have previously been described in part 1, section 1 [2] as well as in part 4, section 10 [5]. Two series of concretes both with a nominal cement content of 5½ bags per cubic yard, were prepared. In one series a constant water/cement ratio (w/c) of 0.635 was used. These concretes are referred to as the Series O concretes. In the other series the w/c was adjusted, if necessary, to obtain a 5 \pm 1-in slump. These concretes are referred to as Series A concretes.

3. Tests and Nomenclature

The 6- \times 8- \times 16-in (approximately 15- \times 20-× 40-cm) concrete specimens used for drying and absorption tests were the same as those used for the volume change measurements reported in part 4 section 10 [5]. After casting, the specimens were: (1) cured under wet burlap for the first 20 to 24 hours, (2) stored in the fog room at 100percent relative humidity until they were 14 days old, (3) placed in laboratory air at 73 \pm 1 °F, and 50 ± 5 -percent relative humidity for 56 days, and (4) immersed in water at 73 °F for an additional 28 days. Measurements were made of the weights of the specimens at 24 hours, at 14 days, after air-drying for 28 and 56 days, and after storage in water for 28 days. Companion 3- \times 4- \times 16-in beams made from the same concretes were given the same treatment.

The percentage weight-loss of the specimens as a result of drying in laboratory air was calculated from the ratio of the weight after the period of air drying to the weight after removal from the fog room at 14 days. This percentage is referred to as ODRY and ADRY for the Series O and A concretes, respectively. The percentage gain of

weight when the air-dried specimens were placed in water was calculated from the ratio of the weight after water storage to the weight after air storage. This percentage is referred to as OWET and AWET for the Series O and A concretes respectively.

Various other notations are used for the various ratios and differences of the percentage weight-loss and percentage absorption. These are as follows:

ORWT and ARWT are used to designate the ratios of OWET/ODRY and AWET/ADRY. OWTR and AWTR are used to designate the ratios (ODRY-OWET)/ODRY and (ADRY-AWET)/ADRY respectively.

The air contents of the concretes are sometimes referred to as such and at times by OAIR and AAIR for the two series. The values were based on the percentage air by volume determined gravimetrically according to ASTM Designation C 138, on the plastic concrete, as indicated in part 1 section 1 [2].

Other abbreviations and symbols are the same as those used in previous parts and sections of this series of articles.³

4. Statistical Studies

The statistical techniques used to determine and evaluate the independent variables associated with the percentage-loss of weight on drying, or percentage weight-gain with subsequent storage in water, or the various ratios and differences were the same as those described and used in previous parts and sections of this series of articles. Multivariable regression equations were calcu-

lated by the method of least-squares to evaluate the significance of the various independent variables associated with the dependent variables. Residuals of multivariable equations were fitted by a least-squares method to other independent variables and the reduction in variance calculated.

² Included were 82 Type I, 68 Type II, 20 Type III, 3 Type IV, and 12 Type V cements. Also included were 8 Type IA, 3 Type IIA, and 3 Type IIIA cements.

 $^{^3}$ Among the abbreviations or symbols used are C₃A, C₅S, C₅S, and C₄AF for the calculated potential compounds, tricalcium aluminate, tricalcium silicate, dicalcium silicate, and tetracalcium aluminoferrite, respectively. Also, used are AE + NAE for air-entraining plus non-air-entraining cements, NAE for non-air-entraining cements, APF for air permeability fineness, WaGN for Wagner turbidimeter fineness, Loss for loss on ignition, and Insol for insoluble residue.

If any of the additional independent variables indicated a significant reduction in variance, they were tried in the equation and retained if the

coef./s.d. ratio was greater than 1.0.4

As in previous sections, comparisons were made of the degree of fit of equations using commonly determined variables as independent variables and these together with minor and trace elements. The level of significance of any reduction in the S.D. values resulting from the use in the equation of the additional independent variables was calculated for various pairs of equations or for an equation and the S.D. values of the property of the concrete (as presented in footnotes in the tables). The reduction in variance for the different pairs of equations and critical "F" values which must be equalled or exceeded for significance at the 5.0- and 1.0-percent significance levels are presented in a table summarizing these calculations.

Equations were calculated using both the calculated potential compounds as well as the major oxides, each together with other independent variables. Equations were calculated for both the AE + NAE cements and the NAE cements for all the dependent variables.

Equations were also computed for the "odds" and "evens" in the array of cements. If the coefficients and coef./s.d. ratios of these equations were

in close agreement with those for the equation computed for all cements, confidence in the relationship was enhanced.

Although the drying and absorption tests were made on concretes made with each of the cements, the calculations of the equations presented in this section were limited to those for which trace elements had been determined. The concretes made with the three white cements and the one having a high autoclave expansion were excluded, as were a few others that had large deviations from the calculated relationship for no apparent reason. The frequency distributions of the various properties as well as calculated contributions to the various independent variables included all the concretes for which values were available.

Equations presented in this article were selected from a large number of trial equations indicating the relationship of various independent variables to percentage weight loss or gain, or the differences and ratios. The differences and trends indicated by these series of equations will be treated in subsection 6. Some of the limitations on interpretations of multivariable regression equations, as well as the other statistical techniques used, have been discussed in part 1 section 1, subsections 4.2, 4.3, and 5 [2] as well as in most of the preceding sections of this series of articles.

Table 12-1. Frequency distribution of cements with respect to ODRY, the percentage weight loss of Series O concretes when airdried for 56 days

						Pe	rcentage	e weight l	oss					
Type cement	1.8 to 2.0	2.0 to 2.2	2.2 to 2.4	2.4 to 2.6	2.6 to 2.8	2.8 to 3.0	3.0 to 3.2	3.2 to 3.4	3.4 to 3.6	3.6 to 3.8	3.8 to 4.0	4.0 to 4.2	4.2 to 4.4	Total
		Number of cements												
[1	8	16	19	23	7 3	6 3	2						82
II IIA		2	10	17	15	8	8	1	5	2				8 68 3 20
III IIIA	4	6	5 3	3	2									20
iv, v			ĭ	1	1	3	3		4		1		1	15
Total	5	16	35	41	44	21	20	3	10	2	1	0	1	199

5. Results of Tests

5.1. Loss of Weight as a Result of Drying

5.1.1. Weight-Loss of Series O Concretes

The frequency distribution of percentage weightloss during drying of the Series O concretes is presented in table 12–1. The values ranged from less than 2.0 percent to more than 4.2 percent and

'Statistical terms and notations employed in this section are the same as those in previous sections. For example, S.D. refers to the estimated standard deviation calculated from the residuals of a fitted equation, or the estimated standard deviation about the average. Also, s.d. refers to the estimated standard deviation of a coefficient of an independent variable used in a fitted equation, coef./s.d. the ratio of the magnitude of an estimated coefficient (of an independent variable used in an equation) to its estimated standard deviation, and "F" equals Fisher's ratio of variances.

there was an overlapping of the values for the

different types of cement.

Equations relating the variables associated with the loss of weight of Series O concretes made with AE + NAE cements are presented in table 12–2. As indicated in eq 1, an increase in C₃S was associated with a decrease of the weight-loss and an increase in C₄AF with an increase of the weightloss. The reduction in variance was highly significant.⁵

 $^{^5}$ The reduction in variance or ''F'' ratios of comparable S.D. values are presented in table 12–33 together with the critical "F" ratios which must be equaled or exceeded for significance at the $\alpha=0.01$ and $\alpha=0.05$ probability levels. Eq 0 as used in table 12–33 refers to the S.D. value of the corresponding dependent variable as given in footnotes in the tables of equations

TABLE 12-2. Coefficients for equations for AE + NAE cements relating the percentage loss of weight when dried for 56 days in laboratory air after 14 days of moist curing of concretes of nominal 5½ bags cement per cubic yard and a water-cement ratio of 0.635 to various independent variables (ODRY)

S.D.	0.3440	0.2678	0.2649	0.2687	0.2534		0.3240	0.2674	0.2622	0.2696	0.2520
Zr		1 1 1 1 1 1 1 1 1 1	-0.5733 (0.5150)	-3.1321 (1.3896)	*-0.2441 (0.5540)						
Rb		1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	$^{\mathbf{-16.13}}_{(11.91)}$	$^{*}_{(16.13)}$	$-44.20 \\ (18.25)$				$-19.37 \ (11.85)$	* -2.95 (16.22)	-49.61 (18.38)
Cu			+2.702 (2.491)	$^{+5.566}_{(3.672)}$	$^*+0.540$ (3.574)				+3.385 (2.482)	+5.019 (3.713)	$^*+1.534$ (3.652)
Ва		1 1	$^{+1.012}_{(0.604)}$	$^* + 0.763$ (1.156)	$^{+1.159}_{(0.749)}$			1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	$^{+1.426}_{(0.620)}$	*+0.725 (1.161)	+1.488 (0.822)
Air		+0.0681 (0.0119)	$\begin{array}{c} +0.0647 \\ (0.0119) \end{array}$	$^{+0.0728}_{(0.0172)}$	+0.0519 (0.0165)			$^{+0.0680}_{(0.0119)}$	+0.0637 (0.0118)	+0.0743 (0.0175)	+0.0491 (0.0165)
Loss		-0.0692 (0.0403)	-0.0654 (0.0406)	-0.0857 (0.0638)	*-0.0357			-0.0765 (0.0444)	-0.0889 (0.0438)	-0.1163 (0.0650)	*-0.0360 (0.0616)
SO_3		-0.2418 (0.0653)	-0.2490 (0.0653)	-0.3590 (0.0950)	-0.1636 (0.0926)			-0.2111 (0.0728)	-0.2309 (0.0719)	-0.3691 (0.1099)	*-0.0996 (0.1047)
K_2O		-0.6832 (0.0978)	-0.5940 (0.1121)	-0.5920 (0.1672)	$\begin{bmatrix} -0.5782\\ (0.1709) \end{bmatrix}$			-0.7604 (0.1143)	-0.6818 (0.1226)	-0.6597 (0.1818)	-0.6145 (0.1772)
Na ₂ O	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	-0.5737 (0.1245)	-0.5326 (0.1259)	-0.5368 (0.1664)	-0.4597 (0.2243)			-0.6087 (0.1263)	-0.6032 (0.1246)	-0.6142 (0.1657)	-0.5280 (0.2171)
Fe_2O_3	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1				1		+0.1763 (0.0355)	+0.1408 (0.0325)	+0.1211 (0.0338)	+0.0750 (0.0510)	+0.1839 (0.0462)
Al ₂ O ₃	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1		1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1				+0.1747 (0.0435)	+0.1778 (0.0402)	+0.1840 (0.0398)	+0.1794 (0.0539)	+0.2352 (0.0637)
C,AF	+0.04204 (0.01168)	+0.03600 (0.00941)	+0.03219 (0.00973)	+0.01549 (0.01478)	+0.04592 (0.01340)	SiO2	+0.2320 (0.0337)	+0.1615 (0.0354)	+0.1497 (0.0354)	+0.1124 (0.0495)	+0.2114 (0.0573)
CaS	-0.02023 (0.00397)	-0.02259 (0.00327)	-0.02268 (0.00324)	-0.02019 (0.00442)	-0.02620 (0.00505)	Ca0	-0.0342 (0.0224)	-0.1003 (0.0217)	-0.1090 (0.0215)	-0.1013 (0.0336)	-0.1109 (0.0292)
Const.	= +3.249 = (0.253)	= +4.256 = (0.237)	= +4.242 = (0.237)	= +4.479 = (0.340)	= +4.135 = (0.345)	1	= -1.671 = (1.696)	= +4.994 = (1.933)	= +5.815 = (1.935)	= +6.547 = (2.986)	= +3851 $= (2.670)$
	ODRY s.d.	ODRY s.d.	ODRY s.d.	ODRY (odd) s.d.	ODRY (even) s.d.		ODRY s.d.	ODRY s.d.	ODRY s.d.	ODRY (odd) s.d.	ODRY (even) s.d.
Note	1	1	1	63	23		1	1	-	23	63
Eq.	1	2	3	3A	3B		4	5	9	6A	6B

Note 1, 180 cements, Avg. = 2.657, S.D. = 0.3908 Note 2, 90 cements *Coef./s.d. ratio less than 1.0

Table 12-3. Coefficients for equations for NAE cements relating the percentage loss of weight when dried for 56 days in laboratory air after 14 days moist curing of concretes of a nominal 5½ bags cement per cubic yard and a water-cement ratio of 0.635, to various independent variables (ODRY)

		3 6	icometicae o	of a continua 5 /2 ougs centerin per each gain and a auter-centerin ratio of 0.000, to various that perfuent variables (ODRI)	nein per c	ane san	a numa a	aner-reme	ווו ו מונים מ	0.000, 10	our tous t	unebenne	n variant	es (ODu	()		
Kq.	Note		Const.	C3S	CAF	Al ₂ O ₃	Fe ₃ O ₃	Na ₂ O	K20	SO3	Loss	Air	Ba	Cu	Rb	Zr	S.D.
1	1	ODRY s.d.	= +3.093 = (0.266)	-0.01847 (0.00412)	+0.04758 (0.01204)												0.3437
2	-	ODRY s.d.	= +4.234 = (0.255)	-0.02247 (0.00346)	+0.03530			-0.5931 (0.1309)	(0.1040)	-0.2425 (0.0678)	-0.0606 (0.0422)	+0.0886					0.2724
3	-	ODRY s.d.	= +4.233 = (0.254)	-0.02265 (0.00343)	+0.03474 (0.00977)	1 1		-0.5362 (0.1328)	-0.6471 (0.1154)	-0.2549 (0.0678)	-0.0573 (0.0426)	+0.0846 (0.0310)	+0.923 (0.625)		-16.49 (12.46)	-0.657	0.2697
3A	23	ODRY (odd) s.d.	= +4.193 = (0.360)	-0.02259 (0.00504)	+0.04342 (0.01568)	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1		-0.4595 (0.1758)	-0.8450 (0.1841)	-0.2356 (0.0995)	*-0.0480 (0.0793)	+0.0887	+1.265 (1.234)		*-9.07	-3.868	0.2842
3B	73	ODRY (even) s.d.	= +4.246 = (0.395)	-0.02278 (0.00539)	+0.03085 (0.01357)			-0.8014 (0.2319)	-0.4687 (0.1675)	-0.2629 (0.1003)	-0.0810 (0.0548)	+0.0987	+0.981		*-18.00 (18.62)	*-0.124 (0.572)	0.2634
				CaO	SiO_2												
4	-	ODRY s.d.	= -2.941 = (1.724)	*-0.0165 (0.0228)	+0.2336 (0.0344)	+0.1744 (0.0441)	+0.2016 (0.0361)										0.3179
5	П	ODRY s.d.	= +5.290 = (2.012)	-0.1032 (0.0228)	+0.1576 (0.0371)	+0.1736 (0.0423)	+0.1350 (0.0340)	-0.6300 (0.1330)	-0.8013 (0.1222)	-0.2148 (0.0756)	-0.0698 (0.0464)	+0.0895					0.2721
9	1	ODRY s.d.	= +5.841 = (2.032)	-0.1089 (0.0227)	+0.1496 (0.0375)	+0.1819 (0.0421)	+0.1184 (0.0358)	-0.5881 (0.1338)	-0.7230 (0.1309)	-0.2404 (0.0752)	-0.0729 (0.0468)	$^{+0.0756}_{(0.0316)}$	+1.298 (0.646)	+3.014 (2.623)	-18.27 (12.46)	-0.554 (0.528)	0.2674
6A	67	ODRY (odd) s.d.	= +8.432 = (2.738)	-0.1290 (0.0324)	+0.1000 (0.0497)	+0.1688 (0.0555)	+0.1136 (0.0543)	-0.4617 (0.1698)	-0.9274 (0.1925)	-0.3016 (0.1093)	*-0.0547 (0.0781)	+0.0825 (0.0515)	*+1.087	+8.770 (4.010)	*-16.66 (18.23)	*-3.204	0.2698
6B	57	ODRY (even) s.d.	= +1.628 = (3.286)	-0.0771 (0.0340)	+0.2207 (0.0664)	+0.2358 (0.0710)	+0.1515 (0.0519)	-0.8346 (0.2497)	-0.4699 (0.1910)	-0.1697 (0.1182)	*-0.0531 (0.0665)	+0.0973 (0.0422)	+1.002 (0.950)	*-0.109	-20.33 (18.85)	*-0.148	0.2651
toN	168	Note 1 169 compared A 115	- 0 CAE O D	0606 0 =					_				-				

Note 1, 168 cements, Avg. = 2.645, S.D. = 0.3920 Note 2, 84 cements *Coef./s.d. ratio less than 1.0.

Other commonly determined variables, Na₂O, K₂O, SO₃, Loss, and air content of the concrete, also had coef./s.d. ratios greater than 1.0 (eq 2) and, resulted in a further highly significant reduction of variance. (See table 12–33, p 63).

The additional use of the trace elements Ba, Cu, Rb, and Zr in eq 3 resulted in a slightly lower S.D. value, but the reduction in variance was not significant at the $\alpha=0.05$ level. (See table 12–33.) The coefficients for the four trace elements as well as loss on ignition were not highly significant, and when equations 3A and 3B were calculated for the "odds" and "evens" in the array of cements, the coef./s.d. ratio was less than 1.0 for each of these variables.⁶

Equation 4 was calculated using the major oxides instead of the potential compounds as in eq 1. There was a highly significant reduction in the S.D. value, and with the use of other commonly determined variables in eq 5 a further significant reduction in variance was attained. (See table 12–33) The additional use of the trace elements Ba, Cu, and Rb in eq 6 resulted in a slightly lower S.D. value with a reduction of variance significant at the $\alpha=0.05$ level.

In eqs 6A and 6B calculated for the "odds" and "evens," SO₃, Loss, and the trace elements had coef./s.d. ratios of less than 1.0 in one or the other

of the smaller groups of cements.

A similar series of equations calculated for the Series O concretes made with the NAE cements is presented in table 12–3. The use of the variables C₃S and C₄AF in eq 1, or these together with Na₂O, K₂O, SO₃, Loss, and air content in eq 2, each resulted in a highly significant reduction in variance. (See table 12–33.) The additional use of the trace elements Ba, Rb, and Zr in eq 3 did not result in a significant reduction of variance.

In eqs 3A and 3B calculated for the "odds" and "evens" in the array of cements, the coef./s.d. ratios for Loss, Rb, and Zr were less than 1.0 in one or both of the smaller groups.

The coef./s.d. ratio for CaO was less than 1.0 in eq 4 which was calculated using the major oxides. The coefficient for this variable was, however, highly significant in eqs 5 and 6 where other variables were also included. The use of the variables in eq 4 or these together with the additional variables in eq 5 resulted in a highly significant reduction in variance. (See table 12–33.)

The use of the trace elements Ba, Cu, Rb, and Zr in eq 6 did not result in a reduction of the S.D. value significant at the $\alpha=0.05$ level. Also, the coef./s.d. ratios of the trace elements were less than 1.0 in one or both of the equations 6A and 6B calculated for the "odds" and "evens" in the array of cements. The loss on ignition of the cements also had a coef./s.d. ratio less than 1.0 with the smaller groups.

The calculated contributions of the independent variables to the percentage weight loss resulting from drying are presented in table 12-4 together

Table 12-4. Calculated contributions of independent variables to ODRY, the percentage loss of weight resulting from airdrying of Series O concretes made of AE + NAE cements

Independent variables	Ranges of variables (percent)	Coefficients from eq 3 table 12-2	Calculated contributions to ODRY	Calculated range of contribu- tions to ODRY
CaS	20 to 65 1 to 16 0 to 0.7 0 to 1.1 1.2 to 3.0 0.3 to 3.3 0 to 11 0 to 0.2 0 to 0.05 0 to 0.01 0 to 0.5	$\begin{array}{c} -0.02268 \\ +0.03219 \\ -0.5326 \\ -0.594 \\ -0.249 \\ -0.0654 \\ +0.0647 \\ +1.012 \\ +2.702 \\ -16.13 \\ -0.573 \end{array}$	Const. = +4.24 -0.45 to -1.47 +0.03 to +0.51 0 to -0.37 0 to -0.65 -0.30 to -0.75 -0.02 to -0.22 0 to +0.71 0 to +0.20 0 to +0.14 0 to -0.16 0 to -0.29	1.02 0.48 0.37 0.65 0.45 0.20 0.71 0.20 0.14 0.16

^{*}Coefficient of doubtful significance as coef./s.d. ratio was less than 2.0.

with the calculated ranges of these contributions. These contributions and ranges were calculated from the coefficients of the independent variables in an equation and the approximate ranges of these variables in the cements of this investigation. These calculated values are estimates based

Table 12-5. Frequency distribution of cements with respect to ADRY, the percentage weight loss of Series A concretes when airdried for 56 days

						Pe	ercentage	weight l	loss					
Type cement	1.8 to 2.0	2.0 to 2.2	2.2 to 2.4	2.4 to 2.6	2.6 to 2.8	2.8 to 3.0	3.0 to 3.2	3.2 to 3.4	3.4 to 3.6	3.6 to 3.8	3.8 to 4.0	4.0 to 4.2	4.2 to 4.4	Tota
		Number of cements												
A	2	6	6 2	22 5	19	12	5	5	2					79
[A	1		8	21	11	9	8	3		6				79 8 67 3 20 3 15
II IIA	2	3 2	$\bar{7}$	6	î		1							20
v, v			1	1	1	5	1	4	1				1	15
Total	6	11	25	55	34	27	15	12	3	6	0	0	1	195

⁸ If a number of cements having higher than normal values for an independent variable are included in one of the two groups (the "odds" or "evens") by the arbitrary division of the cements, this distribution may result in spurious coefficients for the variable. The estimated standard deviations of the coefficients for the smaller groups were usually larger than when a combination of the "odds" and "evens" in the array of cements was used in calculating the equation. If the coefficients of both "odds" and "evens" of an independent variable are significant, a greater confidence can be placed in the equation, and in the association of that independent variable with the dependent variable. If the coefficient for a variable in either the "odds" or "evens" is not greater than its s.d., some consideration may still be given to the larger groups of cements as indicating a possible relationship.

TABLE 12-6. Coefficients for equations for AE + NAE cements relating the percentage loss in weight when dried for 56 days in laboratory air after 14 days moist curing of concretes of a nominal 5 ½ bags cement per cubic yard and a 5 \pm 1 inch slump, to various independent variables (ADRY)

	w/c content Ba Cu Rb Zr S.D.
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	0.3479
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	0.2755
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	(1.463) (0.01708) (2.569
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	$\begin{array}{cccccccccccccccccccccccccccccccccccc$
-0.0927 (0.0225) +0.1505 (0.0374) +0.2263 (0.0424) +0.1259 (0.0382) +0.1259 (0.1364) +0.1259 (0.1364) +0.1259 (0.1364) -0.6342 (0.1364) -0.6374 (0.1375) -0.1014 (0.0724) -0.1014 (0.1375) -0.1014 (0.1376) -0.1684 (0.0724) -0.1684 (0.1245) -0.1684 (0.1235) -0.1684 (0.1376) -0.1684 (0.0724)	
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	0.2764
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	(1.470) (0.0172)
	$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$

Note 1, 176 cements, Avg. = 2.675, S.D. = 0.3863

*Coef./s.d. ratio less than 1.0.

TABLE 12-7. Coefficients for equations for NAE cements relating the percentage loss of weight when dried for 56 days in laboratory air after 14 days of moist curing of concretes of nominal $5\frac{1}{2}$ bags cement per cubic yard and a slump of 5 ± 1 inch, to various independent variables (ADRY)

	S.D.	0.3506	0.2796	0.2618	953 0.2578 987)		0.2805	0.2627	51) 0.2602
	Zr				(0.5087)				(0.5151)
	Rb				-12.31 (12.11)				-12.89 (12.22)
	Cu				+3.748 (2.504)				+3.684 (2.542)
	Ba		- 1 1		+1.043 (0.625)				
	Air			+0.0797 (0.0329)	+0.0646 (0.0333)			+0.0793 (0.0330)	+0.0689 (0.0335)
	w/c	,		+7.874 (1.634)	+7.864 (1.625)			+7.873 (1.641)	+7.566 (1.632)
	Loss		-0.0870 (0.0441)	-0.0887 (0.0414)	-0.0824 (0.0416)		(0.0482)	-0.0940 (0.0454)	(0.0460)
(SO3	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	-0.1347 (0.0734)	-0.2350 (0.0723)	-0.2511 (0.0721)		(0.0800)	-0.1785 (0.07777)	-0.1824 (0.0772)
	K2O		-0.8764 (0.1111)	-0.7723 (0.1097)	-0.6948 (0.1192)		-0.9019 (0.1234)	-0.7869 (0.1211)	(0.1293)
	Na ₂ O	1 1 1 1 1 1 1 1 1 1 1 1	-0.6204 (0.1339)	-0.6325	-0.5857 (0.1287)		-0.6286 (0.1352)	-0.6373 (0.1289)	-0.6111 (0.1304)
	Fe ₂ O ₃						+0.1178 (0.0350)	+0.1586 (0.0343)	+0.1442 (0.0361)
	C4AF	+0.03969 (0.01492)	+0.05180 (0.01202)	+0.05362 (0.01146)	+0.05101 (0.01170)	Al ₂ O ₃	+0.2213 (0.0446)	+0.1902 (0.0423)	+0.1970 (0.0424)
	C3S	-0.01529 (0.00422)	-0.02071 (0.00356)	-0.02215 (0.00335)	-0.02216 (0.00331)	SiO_2	+0.1445	+0.1611 (0.0368)	+0.1624 (0.0369)
	CaA	*-0.00568 (0.01049)	+0.03583 (0.00955)	+0.01841 (0.00964)	+0.02282 (0.00967)	CaO	-0.0935 (0.0236)	-0.0956 (0.0221)	-0.0953 (0.0220)
	Const.	= +3.109 = (0.323)	= +3.795 = (0.276)	= -1.033 = (1.043)	= -1.069 $=$ (1.041)		= +4.808 = (2.118)	= -0.443 = (2.267)	= -0.310 = (2.270)
		ADRY s.d.	ADRY s.d.	ADRY s.d.	ADRY s.d.		ADRY s.d.	ADRY s.d.	ADRY s.d.
	Note	-	1	-	-		1	п	1
	No.	11	2	3	4		5	9	7

Note 1, 164 cements, Avg. = 2.695, S.D. = 0.3861 *Coef./s.d. ratio less than 1.0.

on a single equation, and somewhat different values would be obtained by use of other equations. Similar computations for calculated contributions to dependent variables have also been made from corresponding equations in order that the trends may be followed more easily.⁷

5.1.2. Weight-Loss of Series A Concretes

The frequency distribution of the weight loss during drying of the Series A concretes is presented in table 12–5. There was an overlapping of the values for the concretes made of the different types of cement and a broad distribution of values.

Equations relating the variables associated with the loss of weight of Series A concretes made with AE + NAE cements are presented in table 12–6. In eq 1 the coef./s.d. ratio for C₃A was less than 1.0 but in eq 2, where other commonly determined variables were included, the coefficient was highly significant. With water/cement ratio and air content included with the independent variables in eq 3, the coef./s.d. ratio for C₃A was lowered. The relationship of C₃A, SO₃, and K₂O to water requirements of Series A concretes was previously reported in eq 5, table 2–20 [2].

The use of C₃A, C₃S, and C₄AF as independent variables in eq 1; these plus Na₂O, K₂O, SO₃, and Loss in eq 2; and the further addition of w/c and air content in eq 3 resulted for each of the equations in a highly significant reduction in variance. (See table 12–33.) The additional use of the trace elements Ba, Cu, Rb, and Zr as independent variables in eq 4 resulted in a slightly lower S.D. value, and the reduction in variance was significant at

the $\alpha = 0.05$ level.

Using the major oxides in eq 5 instead of the calculated potential compounds also resulted in a highly significant reduction in variance. The additional use of w/c and air content as independent variables in eq 6 resulted in a further reduction in the S.D. value. However, addition of the trace

elements Cu, Rb, and Zr in eq 7 did not result in a significant reduction in variance. (See table 12–33.)

A similar series of equations for the Series A concretes made of NAE cements is presented in table 12–7. The coefficients and coef./s.d. ratios of the independent variables are in reasonable agreement with those of table 12–6 where the AE cements were included. One exception may be noted; the coef./s.d. ratio for the air content was lower when only the NAE cements were included as in table 12–7. The use of trace elements together with commonly determined variables did not result in a significant reduction in variance. (See table 12–33.)

Using the coefficients of the independent variables of eq 4, table 12–6, and their ranges of values, computations were made of the calculated contributions to the ADRY values as well as the calculated ranges of these contributions. These calculated values are presented in table 12–8.

Table 12–8. Calculated contributions of independent variables to ADRY, the percentage loss of weight resulting from airdrying of Series A concretes made of AE + NAE cement

Independent variables	Range of variables (percent)	Coefficients from eq 4 table 12-6	Calculated contributions to ADRY	Calculated range of contribu- tions to ADRY
C ₃ A C ₃ S C ₄ AF N ₂ O K ₂ O SO ₃ Loss w/c Air-content Ba* Cu* Rb* Zr*	1 to 15 20 to 65 1 to 16 0 to 0.7 0 to 1.1 1.2 to 3.0 0.55 to 0.72 0 to 13 0 to 0.2 0 to 0.05 0 to 0.05 0 to 0.01	$\begin{array}{c} +0.0232\\ -0.0221\\ +0.0524\\ -0.6528\\ -0.6528\\ -0.2455\\ -0.0898\\ +7.654\\ +0.0594\\ +1.119\\ +3.92\\ -14.56\\ -0.62\end{array}$	$\begin{array}{c} \text{Const.} = -0.97 \\ +0.02 \text{ to } +0.34 \\ -0.44 \text{ to } -1.43 \\ +0.05 \text{ to } +0.83 \\ 0 \text{ to } -0.40 \\ 0 \text{ to } -0.74 \\ -0.29 \text{ to } -0.74 \\ -0.03 \text{ to } -0.30 \\ +4.21 \text{ to } +5.51 \\ 0 \text{ to } +0.22 \\ 0 \text{ to } +0.22 \\ 0 \text{ to } -0.20 \\ 0 \text{ to } -0.31 \\ 0 \text{ to } -0.31 \\ \end{array}$	0.32 0.99 0.78 0.40 0.78 0.45 0.27 1.30 0.77 0.22 0.20 0.15

^{*}Coefficient of doubtful significance as coef./s.d. ratio was less than 2.0.

Increases in C₃A, C₄AF, w/c, and air content were associated with increases in values for weight-loss. Increases in C₃S, Na₂O, K₂O, SO₃, and loss were associated with decreases in the values for weight-loss. Variations of w/c, C₃S, C₄AF, K₂O, and air content had the highest values for the calculated range of contributions to the values for weight-loss.

Table 12-9. Frequency distribution of cements with respect to OWET, the percentage weight gain of Series O concretes when airdried specimens were placed in water for 28 days

]	Percentage	e weight g	ain				
Type cement	1.8 to 2.0	2.0 to 2.2	2.2 to 2.4	2.4 to 2.6	2.6 to 2.8	2.8 to 3.0	3.0 to 3.2	3.2 to 3.4	3.4 to 3.6	3.6 to 3.8	3.8 to 4.0	Total
						Number	of cement	s		-		
IIA	2	13	24	26	9	4 2	4 5					82 8
II IIA	1	7	11	19	12	6	6	4	1	1		68
IIIIIIA	3	7	4	3 2	3							68 3 20 3 15
iV, V			1	ĩ	3	3	1	3	1	1	1	15
Total	6	27	40	51	28	17	16	7	3	2	1	199

 $^{^7}$ Corresponding tables for equations calculated for AE + NAE cements, using the calculated potential compounds, other commonly determined variables, and trace elements having a coef./s.d. ratio greater than 1.0 will be presented for other dependent variables. Summary tables (tables $12{\text -}34$ and $12{\text -}35$) are also presented for greater ease in comparing similar equations for the NAE cements.

Table 12-10. Coefficients for equations for AE + NAE cements relating the percentage gain in weight when moist stored for 28 days following 56 days drying in laboratory air of concretes of a nominal 5 1/8 bass cement ner cubic ward and a mater-cement ratio of 0.635, to anxious independent mariables (OWET)

		arr of concretes of a nominal 5 ½ bags cement per cubic yard and a water-cement ratio of 0.635, to various independent variables (OWET)	retes oy a	nomin	al 5 ½ bag.	s cement 1	per cubic	yard and	a water-	cement ra	tio of 0.63	5, to vario	ns indep	sendent v	ariables (C	WET')		
NEG.	Note	Const.		Air	C3S	C,AF	Al ₂ O ₃	${ m Fe}_2{ m O}_3$	Na2O	K20	SO.	Loss	Cu	Rb	Zr	Ba	ODRY	S.D.
1	-	OWET = $+0$.	+0.140	1 1	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	1 1 1										+0.9082 (0.0241)	0.1264
2	-	OWET = $+2$.	$\begin{vmatrix} +2.440 \\ (0.042) \end{vmatrix} \begin{vmatrix} +0.0 \\ (0.042) \end{vmatrix}$	+0.05301 (0.01503)														0.3660
3	1	OWET = $+2$.	$\begin{vmatrix} +2.742 \\ (0.246) \end{vmatrix} +0.0$	+0.06488 (0.01368)	-0.01592 (0.00372)	+0.04757												0.3243
4	-	OWET = $+3$.	$\begin{array}{c c} +3.868 \\ (0.214) \end{array} +0.$	+0.10186 (0.01083)	-0.01980 (0.00296)	+0.03599			-0.7136 (0.1138)	-0.7094 (0.0895)	-0.1776 (0.0594)	(0.0367)						0.2451
5	-	OWET = +3.	$\begin{array}{c c} +3.843 \\ (0.210) \\ \end{array} \begin{array}{c} +0.0 \\ (0.1) \\ \end{array}$	+0.09755 (0.01066)	-0.01967 (0.00287)	+0.02997			-0.6705 (0.1128)	-0.5972 (0.1002)	-0.1830 (0.0583)	(0.0363)	+4.890 (2.230)	-18.50 (10.53)	-0.8074 (0.4618)	+0.891	1 1	0.2375
5A	81	$\begin{array}{rcl} \text{OWET (odd)} &= +3. \\ \text{s.d.} &= & (0. \end{array}$	$\begin{vmatrix} +3.828 \\ (0.291) \end{vmatrix} \begin{vmatrix} +0.\\ (0.691) \end{vmatrix}$	$^{+0.10766}_{(0.01490)}$	-0.01688 (0.00365)	+0.02126 (0.01227)			-0.7603 (0.1502)	-0.7861 (0.1406)	-0.1649 (0.0915)	-0.1006 (0.0506)	+7.659 (3.219)	*+5.66 (14.12)	-2.5905 (1.1056)	+2.407		0.2329
5В	ಣ	OWET (even) = $+3$.	$\begin{vmatrix} +3.931 \\ (0.308) \end{vmatrix} \begin{vmatrix} +0.0 \\ (0.0) \end{vmatrix}$	+0.09227 (0.01476)	-0.02516 (0.00460)	+0.04072 (0.01213)			-0.7181 (0.1780)	-0.4260 (0.1488)	-0.1831 (0.0736)	*-0.0259	+4.881 (3.168)	-47.88 (15.93)	*-0.3411 (0.5026)	*-0.151		0.2272
					Ca0	SiO2												
9	1	OWET = -2 . s.d. = (1.2)	$\begin{array}{c c} -2.037 & +0.0 \\ (1.608) & (0.0) \end{array}$	$+0.08143$ $\times (0.01296)$	*-0.01505	+0.1940 (0.0308)	+0.1084 (0.0399)	+0.1883										0.2985
7	-	OWET = +5. s.d. = (1.	$ \begin{array}{c c} +5.713 & +0.\\ (1.773) & (0.6) \end{array} $	+0.10070 (0.01092)	-0.09772 (0.01994)	+0.1268 (0.0322)	$^{+0.1167}_{(0.0367)}$	+0.1225 (0.0299)	-0.7317 (0.1160)	-0.7647 (0.1049)	-0.1484 (0.0668)	(0.0406)				1 1		0.2457
8	-	OWET = +6.	$\begin{array}{c c} +6.365 \\ \hline (1.753) \end{array} +0.9$	+0.09597 (0.01068)	-0.10391 (0.01953)	+0.1160 (0.0317)	+0.1228 (0.0357)	+0.0978 (0.0306)	-0.7063 (0.1142)	-0.6823 (0.1106)	-0.1725 (0.0650)	-0.0926 (0.0402)	+5.427 (2.244)	-19.18 (10.57)	-0.7098 (0.4640)	+1.156 (0.562)	1 1	0.2367
8A	67	OWET (odd) = +4. s.d. = (2.	+4.537 +0. (2.800) (0.	+0.10713 (0.01518)	-0.07507 (0.03084)	+0.1201 (0.0423)	+0.0973 (0.0516)	+0.0822 (0.0455)	-0.7521 (0.1568)	-0.7954 (0.1647)	-0.1231 (0.1076)	-0.1047 (0.0543)	+7.684) (3.260)	*+6.26 (14.39)	-2.6118 (1.1275)	+2.399 (0.764)		0.2356
8B	ಣ	OWET (even) = $+6$ s.d. = (2.5)	$\begin{array}{c} +6.749 \\ (2.290) \\ \end{array} \begin{array}{c} +0.749 \\ (0.00) \\ \end{array}$	+0.09142 (0.01465)	-0.12600 (0.02617)	+0.1416 (0.0495)	+0.1688 (0.0507)	+0.1459 (0.0414)	-0.7502 (0.1782)	-0.5194 (0.1543)	$-0.1732 \\ (0.0821)$	0.0598 (0.0590)	+6.582 (3.241)	-51.08 (15.90)	* -0.2381 (0.5052)	*+0.377	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	0.2245
1			1	- 6	1								-		-			

Note 1, 181 cements, Avg. = 2.551, S.D. = 0.3775 Note 2, 91 cements Note 3, 90 cements *Coef./s.d. ratio less than 1.0

Table 12–11. Coefficients for equations for NAE cements relating the percentage gain in weight when moist stored for 28 days following 56 days drying in laboratory air of concretes of a nominal 5 % bas cement per cubic vard and a water-cement ratio of 0.635 to various independent variables (OWET)

	S.D.	0.1128	0.3287	0.2494	0.2421	0.2258	0.2330		0.3027	0.2500	0.2416	0.2251	0.2348
	ODRY	+0.8918 (0.0221)	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1							1 4	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1		
(11)	Ba				+0.8131 (0.5611)	+2.4526 ,(0.7364)	*-0.5402 (0.8275)			1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	+1.062 (0.584)	+2.539 (0.742)	*-0.228 (0.910)
nes (OWE	Zr				-0.8397 (0.4747)	*-1.9810 (2.0753)	*-0.3660 (0.5087)		1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1		-0.7477 (0.4774)	*-1.6909 (2.0928)	*-0.3430 (0.5225)
rent varia	Rb				-19.28 (11.01)	*-7.38 (14.51)	-20.25 (16.14)		1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1		-19.63 (11.06)	* -5.93 (14.90)	-20.38 (16.31)
naepena	Cu				+4.606 (2.354)	+6.409 (3.356)	+4.961		1 1 1 1 1 1 1 1 1	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	+5.128 (2.370)	+6.793 (3.374)	+5.113 (3.219)
o various	Loss		1 1	-0.0726 (0.0385)	-0.0682 (0.0382)	*-0.0520 (0.0555)	-0.1008 (0.0527)			-0.0921 (0.0424)	-0.0939 (0.0421)	-0.0797 (0.0581)	-0.1025 (0.0621)
cement per cuouc yara and a water-cement rawo of 0.035 to varoous inaepenaem variantes (OWEL)	SO3			-0.1772 (0.0617)	-0.1836 (0.0606)	*-0.0252 (0.0903)	$\frac{-0.2720}{(0.0767)}$			-0.1497 (0.0694)	-0.1733 (0.0679)	*-0.0243 (0.1010)	-0.2368 (0.0889)
tent ratio	K20		1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	-0.7404 (0.0952)	$-0.6138 \\ (0.1067)$	-0.9451 (0.1503)	-0.3723 (0.1509)			-0.7971 (0.1122)	-0.6967 (0.1178)	-1.0430 (0.1680)	-0.4074 (0.1617)
water-cen	Na ₂ O		1 1	-0.7359 (0.1196)	-0.6766 (0.1191)	-0.5104 (0.1487)	-0.9581 (0.1853)		1 1	-0.7550 (0.1220)	-0.7107 (0.1207)	-0.5440 (0.1532)	-0.9658 (0.1878)
ra ana a	${ m Fe}_2{ m O}_3$	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1		1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1			+0.1896 (0.0350)	+0.1210 (0.0312)	+0.0972 (0.0324)	+0.1022 (0.0457)	+0.1248 (0.0464)
caose ya	Al ₂ O ₃	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1		1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1			+0.1026 (0.0419)	+0.1093 (0.0386)	+0.1158 (0.0377)	+0.0725 (0.0499)	+0.1581 (0.0559)
ement per	CAF		+0.04795 (0.01177)	+0.03649 (0.00900)	+0.03057 (0.00921)	+0.03754 (0.01297)	+0.03116 (0.01320)	SiO_2	+0.1882 (0.0324)	+0.1228 (0.0336)	+0.1129 (0.0334)	+0.0933 (0.0400)	+0.1482 (0.0553)
o ½ oags o	C ₃ S		-0.01500 (0.00390)	-0.01958 (0.00313)	-0.01931 (0.00305)	-0.01819 (0.00365)	-0.02031 (0.00483)	CaO	*-0.01062 (0.02174)	-0.09868 (0.02091)	-0.10327 (0.02051)	-0.10921 (0.02734)	-0.08643 (0.03003)
a nominai	Air		*+0.0333 (0.0345)	+0.1301 (0.0280)	+0.1128 (0.0285)	+0.1034 (0.0435)	+0.1211 (0.0357)	1	+0.0583 (0.0321)	+0.1306 (0.0280)	$^{+0.1111}_{(0.0284)}$	+0.1111 (0.0438)	+0.1179 (0.0369)
concretes of a nominal 5 ½ oays	Const.	= +0.167 = (0.059)	= +2.742 = (0.267)	= +3.826 = (0.231)	= +3.813 = (0.226)	(i) = +3.478 = (0.285)	OWET (even) = $+3.987$ s.d. = (0.341)		= -2.133 $=$ (1.651)	= +5.883 = (1.846)	= +6.423 = (1.832)	$\begin{array}{ccc} 1) & = & +7.232 \\ & = & (2.423) \end{array}$	OWET (even) = $+4.305$ s.d. = (2.745)
		OWET s.d.	OWET s.d.	OWET s.d.	OWET s.d.	OWET (odd)	OWET (eve		OWET s.d.	OWET s.d.	OWET s.d.	OWET (odd) s.d.	OWET (eve
	Note	1	1	7	1	23	ಣ		н	-	-	61	ಣ
	Eq.	1	2	3	4	4A	4B		5	9	7	7A	7B

Note 1, 169 cements, Avg. = 2.523, S.D. = 0.3680 Note 2, 85 cements Note 3, 84 cements *Coef./s.d. ratio less than 1.0

5.2. Gain of Weight as a Result of Immersion of Air-Dried Specimens in Water

5.2.1. Weight-Gain of Series O Concretes

The frequency distribution of the cements with respect to the weight gain of Series O concretes, moist cured for 14 days then air dried for 56 days, and then placed in water for 28 days, is presented in table 12–9. There was a broad distribution of values and an overlapping of values obtained with concretes made of the different types of cement.

Equations relating the variables associated with the percentage gain of weight on resoaking for the Series O concretes made of AE + NAE cements are presented in table 12-10. Equation 1 indicates a significant relationship between weight-gain and weight-loss during the period of drying in air. The S.D. value obtained for eq 1 was much smaller than was obtained in other equations where air content and other independent variables were used. As indicated in eq 2, an increase in the air content was associated with an increase in the gain of weight of the concrete when rewetted. The additional use of C₃S and C₄AF in eq 3 caused a significant reduction in the S.D. value, and in eq 4, where the variables Na₂O, K₂O, SO₃, and Loss were included, a further significant reduction was obtained. (See table 12-33.) The trace elements Cu, Rb, Zr, and Ba all had coef./s.d. ratios greater than 1.0 in eq 5 where all cements were included, but the coef./s.d. ratios for Rb, Zr, and Ba were less than 1.0 in eqs 5A or 5B, the "odds" or "evens" in the array of cements.

Equations 6, 7, and 8 were calculated using the major oxides instead of the calculated potential compounds as in eqs 3, 4, and 5. There was a significant reduction in variance in the successive eqs 6, 7, and 8 (See table 12–33.), but the S.D. values were about twice as large as that for eq 1 where the weight loss was used as an independent variable. The coef./s.d. ratio of CaO was less than 1.0 in eq 6 but highly significant in eqs 7 and 8.

Equations calculated to indicate the independent variables associated with the weight-gain of Series O concretes made with NAE cements are presented in table 12–11. The independent vari-

ables, their coefficients, and the coef./s.d. ratios were in reasonable agreement with those presented in table 12–10 where the AE cements were included. It may be noted that SO₃ had a coef./s.d. ratio less than one in eqs 4A and 7A calculated for one of the smaller groups of cements.

Using the coefficients of the independent variables of eq 5, table 12–10, and their ranges of values, computations were made of the calculated contributions to the OWET values, as well as the calculated ranges of such contributions. The calculated values are presented in table 12–12. Increases

Table 12–12. Calculated contributions of independent variables to OWET, the percentage gain of weight with resoaking of air-dried Series O concretes made of AE + NAE cements

Independent variables	Ranges of variables (percent)	Coefficients from eq 5 table 12–10	Calculated contributions to OWET	Calculated range of contribu- tions to OWET
Air-content	0 to 11 20 to 65 1 to 16 0 to 0.7 0 to 1.1 1.2 to 3.0 0.3 to 3.3 0 to 0.05 0 to 0.5 0 to 0.5 0 to 0.2	$\begin{array}{c} +0.09755 \\ -0.01967 \\ +0.02997 \\ -0.6705 \\ -0.5972 \\ -0.183 \\ -0.0669 \\ +4.89 \\ -18.5 \\ -0.8074 \\ +0.891 \end{array}$	$\begin{array}{c} \text{Const.} = +3.84 \\ 0 \text{ to } +1.07 \\ -0.39 \text{ to } -1.28 \\ +0.03 \text{ to } +0.48 \\ 0 \text{ to } -0.47 \\ 0 \text{ to } -0.65 \\ -0.22 \text{ to } -0.55 \\ -0.02 \text{ to } -0.22 \\ 0 \text{ to } +0.24 \\ 0 \text{ to } -0.18 \\ 0 \text{ to } -0.41 \\ 0 \text{ to } -0.18 \end{array}$	1.07 0.89 0.45 0.47 0.65 0.33 0.20 0.24 0.18

*Coefficient of doubtful significance as coef./s.d. ratio was less than 2.0.

in the air content of the concretes, C_4AF , and possibly Cu were associated with increases in the values for weight-gain. Increases in C_3S , Na_2O , K_2O , and SO_3 were associated with decreases in the values for weight-gain.

5.2.2. Weight-Gain of Series A Concretes

The frequency distribution of the percentage gain of weight when resoaking air-dried concretes made of AE + NAE cements is presented in table 12–13. There was a broad distribution of values and an overlapping of the values of the different types of cement.

Equations relating the variables associated with the weight-gain of the Series A concretes made with AE + NAE cements are presented in table 12–14. No significant relationship was found in

Table 12-13. Frequency distribution of cements with respect to AWET, the percentage weight gain of Series A concretes when airdried specimens were placed in water for 28 days

					I	ercentage	e weight g	ain				
Type cement	1.8 to 2.0	2.0 to 2.2	2.2 to 2.4	2.4 to 2.6	2.6 to 2.8	2.8 to 3.0	3.0 to 3.2	3.2 to 3.4	3.4 to 3.6	3.6 to 3.8	3.8 to 4.0	Total
						Numbe	er of ceme	nts				
II	2	8	16 2	27	13 2	6	2	4	1			79 8
II.	1	4	16	15	13	7	3	3	3	2		67
III	3	4	4	4	4	i						20
IV, V			î		5	4		3	1		1	15
Total	7	16	41	51	38	19	5	10	5	2	1	195

TABLE 12-14. Coefficients for equations for AE + NAE cements relating the percentage gain in weight after 28 days moist storage following 56 days of drying of concretes of a nominal 5% bags cement per cubic yard and a 5 ± 1 inch slump to various independent variables (AWET)

-															-			
No.	Note		Const.	C3A	CaS	CAF		NazO	K20	SO3	Loss	Cu	Mn	Ba	Co	Zr	w/c	S.D.
1	-	AWET =	+1.100	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1			0 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1		1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	1 1	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1		1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1		+2.293 (1.115)	0.3613
2	-	AWET =	+3.043 (0.300)	-0.01097 (0.00991)	-0.01353 (0.00395)	+0.02905 (0.01401)						1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1			1 1	1 1	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	0.3386
3	-	AWET =	+3.690 (0.252)	+0.02902 (0.00901)	-0.01946 (0.00330)	+0.04135 (0.01123)	1 1	-0.7665 (0.1258)	-0.8079 (0.1034)	(0.0686)	(0.0409)	1 1	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1		1 1	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	0.2681
4	-	AWET =	+3.594 (0.249)	+0.03149 (0.00906)	-0.01846 (0.00325)	+0.03174 (0.01135)	1 1	-0.7300 (0.1247)	-0.7508 (0.1054)	-0.1112 (0.0671)	-0.0643 (0.0404)	+6.210 (2.604)	+0.2703 (0.1712)	+0.8975 (0.6117)	+23.40 (14.87)	(0.5049)		0.2588
4A -	61	AWET (odd) = s.d. =	+3.089 (0.350)	+0.03090 (0.01372)	-0.00953 (0.00442)	+0.03686 (0.01490)	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	-0.7448 (0.1928)	-0.5714 (0.1509)	-0.1567 (0.1128)	* -0.0524 (0.0568)	+5.712 (3.355)	*+0.0380 (0.2633)	+1.3755 (0.8599)	* -1.71 (29.86)	-0.6046 (0.5500)		0.2527
4B -	က	AWET (even) = s.d.	+3.949 (0.389)	+0.03601 (0.01252)	-0.02672 (0.00508)	+0.03122 (0.01796)	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	-0.6031 (0.1722)	-0.7735 (0.1575)	-0.1597 (0.0883)	* -0.0085 (0.0620)	+8.951 (4.180)	+0.4539 (0.2265)	*+0.8569 (0.9437)	+28.89 (18.73)	* +2.0102 (2.4695)		0.2568
5	-	AWET =	$^{+2.555}_{(0.567)}$	+0.02662 (0.00929)	-0.01910 (0.00323)	+0.02925 (0.01131)		-0.7043 (0.1242)	-0.6914 (0.1084)	-0.1201 (0.0666)	-0.0666 (0.0401)	+6.253 (2.579)	+0.2649 (0.1696)	+1.0081 (0.6083)	+21.79 (14.75)	-0.6762 (0.5000)	+1.756 (0.865)	0.2564
				CaO	SiO ₂	Al ₂ O ₃	Fe ₂ O ₃				•							
99	-	AWET =	+6.057 (1.971)	-0.1004 (0.0219)	+0.1166 (0.0363)	+0.1771 (0.0415)	+0.0845 (0.0325)	-0.7843 (0.1265)	-0.8678 (0.1145)	*-0.0703	(0.0448)	1 1	1 1	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	1 1	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1		0.2678
7	-	AWET =	+6.858 (1.952)	-0.1075 (0.0215)	+0.1035 (0.0360)	+0.1784 (0.0405)	+0.0473 (0.0334)	-0.7803 (0.1249)	-0.8591 (0.1124)	-0.0937 (0.0730)	-0.0898 (0.0445)	+6.137 (2.595)		+1.0641 (0.621)	+22.99 (14.88)	-0.6137 (0.5080)	1 1	0.2588
7A -	23	AWET (odd) = s.d. =	+3.471 (2.930)	-0.0425 (0.0307)	+0.0681 (0.0534)	+0.1430 (0.0568)	+0.0706 (0.0464)	-0.7506 (0.1923)	-0.5821 (0.1605)	-0.1374 (0.1274)	*-0.0546 (0.0627)	+5.669		+1.4088 (0.9129)	* -1.32 (29.85)	-0.6047 (0.5556)		0.2529
7B -	က	AWET (even) = s.d. =	+9.991 (2.672)	-0.1694	+0.1357 (0.0526)	+0.2148 (0.0582)	+0.0316 (0.0506)	-0.7126 (0.1715)	-1.0169 (0.1688)	-0.1087 (0.0923)	*-0.0511 (0.0649)	+8.749		*+0.9336 (0.9397)	$^{+25.07}_{(18.67)}$	*+2.3195 (2.4695)	1 1	0.2553
×	-	AWET =	+6.034 (1.965)	-0.1128 (0.0214)	+0.1044 (0.0356)	+0.1650 (0.0405)	+0.0461 (0.0330)	-0.7544 (0.1240)	-0.8010 (0.1142)	-0.1054 (0.0723)	-0.0954 (0.0440)	+6.255 (2.566)		$+1.2012 \\ (0.6170)$	+21.13 (14.73)	-0.6025 (0.5022)	+1.903 (0.865)	0.2558
- 2	1040	Note 1 125 content Acc	- 0	5	- 0										-			

Note 1, 175 cements, Avg. = 2.560, S.D. = 0.3647 Note 2, 88 cements Note 3, 87 cements *Coef./s.d. ratio less than 1.0

Table 12-15. Coefficients for equations for NAE cements relating the percentage gain in weight after 28 days moist storage following 56 days of drying of concretes of nominal 5 % bags cement per cubic yard and a 5 ± 1 inch slump to various independent variables (AWET)

$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$					-				-								
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	Const. CaA CaS CaAF	C ₃ A C ₃ S	C ₃ S		C,AF			Na ₂ O	K20	SO ₃	Loss	Cu	Mn	Ва	Co	Zr	w/c
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	= +0.840	= +0.840 = (0.972)					; ;										+2.694 (1.516)
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	$ \begin{array}{llllllllllllllllllllllllllllllllllll$	$\begin{array}{cccccc} +2.976 & -0.01158 & -0.01218 \\ (0.316) & (0.01038) & (0.00417) \end{array}$	$\begin{array}{c c} -0.01158 & -0.01218 \\ (0.01038) & (0.00417) \end{array}$	1	+0.03015		- 1 1		1 1					1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1			
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	$= +3.674 + 0.02831 -0.01877 + 0.04134 - \dots \\ = (0.265) (0.00931) (0.00345) (0.01160) - \dots \\$	$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	+0.04134				(0.1294)	-0.8543 (0.1075)	(0.0708)	(0.0425)		1 1 1 1 1 1 1 1 1 1				
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	= +3.579 + 0.03172 -0.01797 + 0.03326	$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	+0.03326			Ĩ	(0.1288)	-0.8106 (0.1110)	-0.1064 (0.0692)	-0.0641 (0.0420)	+5.900 (2.648)	+0.1831 (0.1820)	+0.8259 (0.6200)	+27.61 (15.54)	-0.7568 (0.5124)	
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	AWET (odd) = $+3.187$ $+0.02440$ -0.01449 $+0.04201$ $-0.01736) (0.01736)$	$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	+0.04201 (0.01736)		9)	79	-0.5370 (0.2151)	-0.7969 (0.1878)	*-0.0390 (0.1307)	*-0.0553	+7.125 (4.413)	*+0.2167 (0.3058)	*+0.6678 (0.9121)	$+42.16 \ (28.23)$	-0.6448 (0.6174)	
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	AWET (even) = $+3.992$ $+0.03775$ -0.02274 * $+0.01763$ -0.02616) (0.01968) -0.0168 (0.01968) (0.01968) (0.01968)	= +3.992 +0.03775 -0.02274 *+0.01763 = (0.376) (0.01307) (0.00516) (0.01968)	+0.03775 -0.02274 *+0.01763	*+0.01763		0)	90	-0.8590 (0.1737)	-0.7598 (0.1615)	-0.1227 (0.0871)	-0.0867 (0.0631)	+6.447 (4.137)	*+0.1786 (0.2488)	*+0.7026 (0.9461)	*+7.80 (20.49)	$\frac{-1.6910}{(1.2639)}$	
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	= +0.560 + 0.01921 -0.01900 +0.03078 0.0.786)	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	+0.03078 (0.01115)			<u>,0</u>	-0.7028 (0.1230)	-0.6713 (0.1111)	-0.1648 (0.0675)	-0.0743 (0.0401)	+6.973 (2.536)	* +0.1655 $_{(0.1734)}$	+1.287 (0.601)	+19.71 (14.92)	(0.4880)	+5.047 (1.245)
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	CaO SiO ₂ Al ₂ O ₃ Fe ₂ O ₃	SiO ₂ Al ₂ O ₃	SiO ₂ Al ₂ O ₃	Al ₂ O ₃		Fe ₂ O ₃											
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	$ \begin{array}{c} = +5.700 \\ = (2.051) \\ \hline \end{array} \begin{array}{c} -0.0946 \\ (0.0229) \\ \end{array} \begin{array}{c} +0.1162 \\ (0.0378) \\ \end{array} \begin{array}{c} +0.1752 \\ (0.0435) \\ \end{array} \begin{array}{c} +0.0867 \\ (0.0340) \\ \end{array} \begin{array}{c} -0 \\ \end{array}$	$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	$\begin{array}{c ccccc} +0.1752 & +0.0867 \\ \hline (0.0435) & (0.0340) \end{array}$	+0.0867	1	90	-0.7939 (0.1304)	-0.9048 (0.1189)	*-0.0628 (0.0771)	(0.0463)						
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	$ \begin{array}{c} = +6.421 \\ = (2.022) \\ \end{array} \begin{array}{c} -0.1010 \\ (0.0223) \\ \end{array} \begin{array}{c} +0.1040 \\ (0.0373) \\ \end{array} \begin{array}{c} +0.1785 \\ (0.0423) \\ \end{array} \begin{array}{c} +0.0510 \\ (0.0347) \\ \end{array} \begin{array}{c} -0. \\ \end{array}$	$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	$\begin{array}{ccc} +0.1785 & +0.0510 \\ (0.0423) & (0.0347) \end{array}$	+0.0510 (0.0347)		99	-0.7857 (0.1284)	-0.9036 (0.1163)	(0.0752)	(0.0458)	+5.905 (2.625)	1 1	+0.9574 (0.6287)	+27.57 (15.50)	-0.7023 (0.5142)	
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	AWET (odd) = $+9.282$ -0.1123 $*+0.0249$ $+0.1046$ $*+0.0444$ -0.843 (0.0563) (0.0603) (0.0520) (0.0620)	$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	$ \begin{array}{c c} +0.1046 & *+0.0444 \\ \hline (0.0603) & (0.0520) \end{array} $	*+0.0444 (0.0520)		99	-0.6569 (0.2152)	-0.9446 (0.1954)	* -0.0952 (0.1352)	-0.1154 (0.0715)	+7.474 (4.277)	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	+1.3804 (0.9539)	+51.92 (27.80)		
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	A WET (even) = $+2.570$ -0.0836 $+0.1993$ $+0.2855$ $*+0.0457$ -0.8 8.d. (0.0550) (0.0550) (0.0560) (0.0543) (0.0650) (0.0543) (0.0560) $(0.056$	$ \begin{array}{c ccccc} -0.0836 & +0.1993 & +0.2855 & *+0.0457 \\ \hline (0.0347) & (0.0550) & (0.0650) & (0.0543) \\ \end{array} $	$ \begin{array}{c ccccc} -0.0836 & +0.1993 & +0.2855 & *+0.0457 \\ \hline (0.0347) & (0.0550) & (0.0650) & (0.0543) \\ \end{array} $	$\begin{array}{ccc} +0.2855 & *+0.0457 \\ (0.0650) & (0.0543) \end{array}$	*+0.0457		9.0	-0.8818 (0.1705)	-0.7762 (0.1626)	*-0.0287		+5.471 (4.002)	1 1	*+0.6161 (0.9480)	*+10.14 (20.76)	-1.8812 (1.2610)	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1
	= +3.427 - 0.1055 + 0.1105 + 0.1503 + 0.0654 - 0.5 $= (2.055) (0.0213) (0.0355) (0.0408) (0.0498) (0.0332) (0.0654)$	$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	$ \begin{array}{c ccccc} -0.1055 & +0.1105 & +0.1503 & +0.0654 \\ (0.0213) & (0.0355) & (0.0408) & (0.0332) \end{array} $	$\begin{array}{c} +0.1503 \\ (0.0408) \\ \end{array} \begin{array}{c} +0.0654 \\ (0.0332) \end{array}$	+0.0654 (0.0332)		00	-0.7432 (0.1225)	-0.7612 (0.1158)	-0.1442 (0.0728)	(0.0437)	+7.050	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	+1.4295 (0.6085)	+19.48 (14.87)	-0.6987 (0.4888)	

Note 1, 163 cements, Avg. = 2.568, S.D. = 0.3694 Note 2, 82 cements Note 3, 81 cements *Coef./s.d. ratio less than 1.0

eq 1 where the water/cement ratio was used as an independent variable. (See table 12–33.) The use of the potential compounds C₃A, C₃S, and C_4AF in eq 2 resulted in a significant lowering of the S.D. value. The sign of the coefficient for C₃A was negative and not highly significant in eq 2, but in eq 3 where Na₂O, K₂O, SO₃, and Loss were included as variables, the sign was positive, and the coefficient was highly significant. Including the trace elements Cu, Mn, Ba, Co, and Zr with the other independent variables in eq 4 resulted in a significant reduction in variance. (See table 12-33.) With the use of water/cement ratio in addition to all of these independent variables as in eq 5, the reduction in variance due to the one added variable was significant at the $\alpha = 0.05$ level.

A corresponding series of equations, (eqs 6, 7, and 8) calculated with the major oxides, resulted in S.D. values and "F" ratios comparable to those obtained in eqs 3, 4, and 5 where the potential compounds were used. The coef./s.d. ratio for Mn was less than 1.0 when used with these variables, and therefore was not included in eqs 6, 7, and 8.

In equations 4A, 4B, 7A, and 7B calculated for the "odds" and "evens" in the array of cements, Loss, Fe₂O₃, Mn, Ba, Co, and Zr had coef./s.d. ratios less than 1.0 in one or both of the pairs of equations calculated for the smaller groups of cements.

A similar series of equations indicating the independent variables associated with the absorption of Series A concretes made of NAE cements is presented in table 12–15. The coefficients, the coef./s.d. values and the S.D. values of the equations are in reasonable agreement with those presented in the previous table where the AE cements were included. The coefficients for water/cement ratio were somewhat greater in table 12–15, eqs 5 and 8, than they were in corresponding equations in table 12–14.

Using the coefficients of the independent variables of eq 4, table 12–14, and their ranges of values, computations were made of the calculated contributions to the AWET values, as well as the calculated ranges of such contributions. The calculated values are presented in table 12–16. Increases

Table 12–16. Calculated contributions of independent variables to AWET, the percentage gain of weight with resoaking of air-dried Series A concretes made of AE + NAE cement

Independent variables	Range of variables (percent)	Coefficients from eq 4 table 12–14	Calculated contributions to AWET	Calculated range of contribu- tions to AWET
C ₃ A	1 to 15 20 to 65 1 to 16 0 to 0.7 0 to 1.1 1.2 to 3.0 0.3 to 3.3 0 to 0.05 0 to 1.0 0 to 0.2 0 to 0.5	$\begin{array}{c} +0.03149 \\ -0.01846 \\ +0.03174 \\ -0.73 \\ -0.7508 \\ -0.1112 \\ -0.0643 \\ +6.21 \\ +0.2703 \\ +0.8975 \\ +23.4 \\ -0.6765 \end{array}$	Const. = +3.59 +0.03 to +0.47 -0.37 to -1.20 +0.03 to +0.51 0 to -0.83 -0.13 to -0.33 -0.02 to -0.21 0 to +0.31 0 to +0.27 0 to +0.18 0 to +0.23 0 to -0.34	0.44 0.83 0.48 0.51 0.83 0.20 0.19 0.31 0.27 0.18 0.23 0.34

*Coefficient of doubtful significance as coef./s.d. ratio was less than 2.0.

in C_3A , C_4AF , and possibly Cu were associated with increases in absorption. Increases in C_3S , Na_2O , and K_2O were associated with decreases in absorption. Indications of the effects of SO_3 , Loss, Mn, Ba, Co, and Zr were of doubtful significance. Variations in C_3S and K_2O had the highest values for the calculated range of contribution to gain of weight when the air-dried concrete specimens were placed in water.

5.3. Ratio of Weight-Gain to Weight-Loss5.3.1. Weight-Gain/Weight-Loss Ratio of Series O

The frequency distribution of the weight-gain/weight-loss ratio of the Series O concretes is presented in table 12–17. There was a broad distribution of values and an overlapping of the values obtained for the different types of cement. About 70 percent of the concrete specimens absorbed less water in 28 days of soaking than they had lost in 56 days of drying. The other specimens including most of those made of the air-entraining cements had a gain/loss ratio greater than one.

Equations relating the variables associated with the gain/loss ratio for the Series O concretes made of AE + NAE cements are presented in table 12–18. Equation 1 indicates that the gain/loss ratios are significantly related to the air contents of the concretes. With the additional use of com-

Table 12-17. Frequency distribution of cements with respect to ORWT, the ratio of percentage weight gain divided by the percentage weight loss of Series O concretes. ORWT = OWET/ODRY

							Absorpt	ion ratio						
Type cement	0.82 to 0.85	0.85 to 0.88	0.88 to 0.91	0.91 to 0.94	0.94 to 0.97	0.97 to 1.00	1.00 to 1.03	1.03 to 1.06	1.06 to 1.09	1.09 to 1.12	1.12 to 1.15	1.15 to 1.18	1.18 to 1.21	Total
						:	Number	of cemen	ts					
I		2	10	28	21	6	12 3	2	2 2		1			82
II.		3	2	18	24	7	9	4	1 2					8 68 3 20
III IIIA	1			1	4	3	4	2	ĩ	3	1		1	20
IV, V				3	8	1	3							3 15
Total	1	5	12	50	57	18	32	9	8	3	3	0	1	199

Table 12–18. Coefficients for equations for AE + NAE cements relating ORWT, the ratio of the percentage weight-gain with 28 day water storage divided by the percentage weight loss with 56 days air storage of Series O concretes to various independent variables (ORWT = OWET/ODRY)

Eq.	Note		Const.	Air	C ₃ A	CAF	Al ₂ O ₃	Fe ₂ O ₃	NacO	MgO	APF	Loss	Cu	Mn	S.D.
1	-	ORWT s.d.	= +0.936 = (0.005)	+0.0122 (0.0018)								4 I 1 I 1 I 1 I 1 I 1 I 1 I			0.04457
2	-	ORWT s.d.	= +0.847 = (0.031)	+0.0121 (0.0016)	-0.00210 (0.00111)	-0.00288 (0.00152)	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1		-0.0563 (0.0174)	+0.00464 (0.00247)	+0.0000431 (0.0000062)	-0.0111 (0.0059)		1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	0.03752
3	-	ORWT s.d.	= +0.839 = (0.031)	+0.0120 (0.0016)	-0.00160 (0.00110)	(0.00154)			-0.0632 (0.0172)	+0.00655 (0.00252)	+0.0000431 (0.0000061)	-0.0094 (0.0059)	+0.697 (0.347)	-0.0450 (0.0242)	0.03685
3A	23	ORWT (odd) s.d.	= +0.879 = (0.042)	+0.0124 (0.0022)	-0.00278 (0.00141)	(0.00201)		1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	-0.0522 (0.0203)	+0.00555 (0.00313)	+0.00000325 (0.00000082)	*+0.0011 (0.0082)	*-0.010 (0.485)	-0.0800 (0.0376)	0.03454
3B	m	ORWT (even) s.d.	= +0.823 = (0.047)	+0.0122 (0.0024)	*-0.00092 (0.00179)	(0.00242)	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1		-0.1015 (0.0324)	+0.00708 (0.00418)	+0.0000519 (0.0000001)	-0.0184 (0.0086)	+1.557 (0.538)	*-0.0313	0.03878
4	1	ORWT s.d.	= +0.847 = (0.031)	+0.0121 (0.0016)		1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	-0.00554 (0.00294)	-0.00526 (0.00394)	-0.0564 (0.0174)	+0.00463 (0.00247)	+0.0000431 (0.0000062)	-0.0111 (0.0059)			0.03753
20	1	ORWT s.d.	= +0.839 = (0.031)	+0.0120 (0.0016)		1 1	-0.00422 (0.00292)	-0.00650 (0.00410)	-0.0632 (0.0172)	+0.00653 (0.00252)	+0.0000431 (0.0000061)	-0.0094 (0.0059)	+0.699 (0.347)	-0.0451 (0.0242)	0.03685
5A	61	ORWT (odd) s.d.	= +0.879 = (0.042)	+0.0124 (0.0022)			-0.00737 (0.00374)	* -0.00507 (0.00543)	(0.0203)	+0.00553 (0.00313)	+0.0000324 (0.0000082)	*+0.0011 (0.0082)	*-0.008	(0.0376)	0.03454
5B	က	ORWT (even) s.d.	= +0.823 = (0.047)	+0.0123 (0.0024)			*-0.00242 (0.00475)	-0.01036 (0.00624)	-0.1016 (0.0324)	+0.00707 (0.00418)	+0.0000519 (0.0000091)	-0.0184 (0.0086)	+1.560 (0.538)	* -0.0313 (0.0333)	0.03878
*Coef./s.d. ratio less than 1.0.	atio less t		Note 1, 177 cements,		Avg. = 0.9621, S.D. = 0.04971	D. = 0.0497	71 Note 2,	2, 89 cements		Note 3, 88 ce	88 cements				

Table 12-19. Coefficients for equations for NAE cements relating the ratio of the percentage weight-gain with 28 days water storage divided by the percentage weight loss with 56 days of air storage of Series O concretes to various independent variables (ORWT = OWET/ODRY)

N. O.	Note		Const.	Air	CaA	CAAF	Al ₂ O ₃	Fe ₂ O ₃	Na ₂ O	MgO	APF	Loss	Cu	Mn	S.D.
1	1	ORWT s.d.	= +0.936	+0.0124 (0.0046)				1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1							0.04458
2	H	ORWT s.d.	= +0.854 = (0.033)	+0.0145 (0.0041)	-0.00255 (0.00113)	(0.00155)			-0.0596 (0.0177)	+0.00436 (0.00251)	+0.0000428 (0.0000064)	-0.0139 (0.0061)	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	0.03748
3	-	ORWT s.d.	= +0.849 = (0.032)	+0.0124 (0.0041)	-0.00200 (0.00114)	-0.00319 (0.00158)			-0.0653	+0.00611 (0.00255)	+0.0000429	-0.0125 (0.0060)	+0.665	(0.0251)	0.03689
3A	63	ORWT (odd) s.d.	= +0.857 = (0.045)	+0.0150 (0.0068)	-0.00310 (0.00156)	-0.00235	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1		-0.0558 (0.0226)	+0.00607	+0.00000370	*-0.0055 (0.0091)	+0.681	-0.0665 (0.0473)	0.03762
3B	89	ORWT (even) s.d.	= +0.848 = (0.051)	+0.0114 (0.0059)	*-0.00068	-0.00381 (0.00246)			-0.0892 (0.0324)	+0.00587	+0.0000467 (0.0000093)	-0.0188 (0.0090)	*+0.329 (0.559)	(0.0317)	0.03736
4	1	ORWT s.d.	= +0.854 = (0.033)	+0.0145			(0.00301)	-0.00482 (0.00402)	-0.0596 (0.0177)	+0.00434 (0.00251)	+0.0000428 (0.0000064)	-0.0139 (0.0061)	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	0,03749
5	1	ORWT s.d.	= +0.849 = (0.032)	+0.0124 (0.0041)			-0.00526 (0.00301)	-0.00636 (0.00422)	-0.0653 (0.0176)	+0.00610 (0.00255)	+0.0000429	-0.0125 (0.0060)	+0.667	(0.0251)	0.03689
5A	23	ORWT (odd) s.d.	= +0.858 $= (0.045)$	+0.0149			-0.00820 (0.00413)	*-0.00200 (0.00618)	-0.0558 (0.0226)	+0.00607	+0.00000370 (0.0000006)	*-0.0056	+0.686 (0.517)	-0.0663 (0.0473)	0.03762
5B	တ	ORWT (even) = $+0.847$ s.d. = (0.051)	= +0.847 = (0.051)	+0.0114 (0.0059)			* -0.00171 (0.00463)	-0.01043 (0.00633)	-0.0893 (0.0324)	+0.00586 (0.00400)	+0.0000468 (0.00000093)	-0.0188	* +0.329 (0.559)	-0.0431 (0.0317)	0.03736

monly determined variables in eq 2 a further highly significant reduction of variance was achieved. (See also table 12–33.) The use of Cu and Mn as independent variables together with the other independent variables in eq 3 resulted in a slightly lower S.D. value, but, as indicated in table 12–33 this was significant at the $\alpha = 0.05$ level.

Equations 3A and 3B, calculated for the "odds" and "evens" in the array of cements, indicated that C₃A, Loss, Cu, and Mn had coef./s.d. ratios less than 1.0 in one or the other of the equations

for the smaller groups of cements.

In eqs 4 and 5, the oxides were used as independent variables instead of the potential compounds. A highly significant reduction of variance resulted from use of the commonly determined variables in eq 4, but with the additional use of the trace elements in eq 5 the reduction of variance was significant at the $\alpha = 0.05$ probability level.

A corresponding series of equations for the gain/loss ratio of Series O concretes is presented in table 12–19. The coef./s.d. ratio for the air content in eq 1, table 12–19, was smaller than the corresponding one in table 12–18 where the AE cements were included. The use of commonly determined variables C_3A , C_4AF , Na_2O , MgO, APF, and Loss in eq 2 resulted in a highly significant reduction in variance. The additional use of Cu and Mn in eq 3 resulted in a reduction of variance significant at the $\alpha=0.05$ level. (See table 12–33.)

The use in eqs 4 and 5 of the oxides Al₂O₃ and Fe₂O₃ instead of the calculated potential compounds resulted in an equivalent reduction of the

S.D. values.

Equations calculated for the "odds" and "evens" in the array of cements (eqs 3A, 3B, 5A, and 5B) had instances where the coef./s.d. ratio was less than 1.0 for C₃A, Al₂O₃, Fe₂O₃, Loss, and Cu.

Using the coefficients of the independent variables of eq 3 of table 12–18 and their ranges, computations were made of the calculated contributions to the OWTR ratio, as well as the calculated ranges of such contributions. The calculated values

Table 12-20. Calculated contributions of independent variables to ORWT, the ratio of percentage absorption to percentage weight loss on drying of Series O concretes made of AE + NAE cements

Inde- pendent variables	Range of variables (percent)	Coefficients from eq 3 table 12–18	Calculated contributions to ORWT	Calculated range of contribu- tions to ORWT
Air- content C3A** C4AF** Na ₂ O MgO APF Loss** Cu Mn**	0 to 11 1 to 15 1 to 16 0 to 0.7 0 to 5.0 *2500 to 5500 0.3 to 3.3 0 to 0.05 0 to 1.0	$\begin{array}{c} +0.012 \\ -0.0016 \\ -0.00301 \\ -0.0632 \\ +0.00655 \\ +0.000431 \\ -0.0094 \\ +0.697 \\ -0.0450 \end{array}$	Const. = +0.839 0 to +0.132 -0.002 to -0.024 -0.003 to -0.048 0 to -0.044 0 to +0.033 +0.107 to +0.237 -0.03 to -0.031 0 to +0.034 0 to -0.045	0.132 0.022 0.045 0.044 0.033 0.130 0.028 0.034 0.045

*cm²/g.

**Coefficient of doubtful significance as coef./s.d. ratio was less than 2.0.

are presented in table 12-20. Increases of the air content, fineness, and possibly MgO and Cu were associated with an increase of the ORWT ratio. Increase in Na₂O was associated with a decrease of the ORWT ratio.

5.3.2. Weight-Gain/Weight-Loss Ratio for Series A Concretes

The frequency distribution of the ratio of percentage absorption to the percentage weight loss of Series A concretes is presented in table 12–21. There was a broad distribution of values and an overlapping of the values for the different types of cement. About one-fourth of the specimens had a slightly greater absorption than loss on drying, and these included concretes made with 11 of the 14 air-entraining cements.

Equations indicating the variables associated with ARWT are presented in table 12–22. The use of the commonly determined variables, air content, Na₂O, MgO, and APF in eq 1 resulted in a significant reduction in variance. The additional use in eq 2 of C₄AF, Ba, Cu, SrO, and V resulted in a reduction of variance significant at the 5.0-

percent level. (See table 12–33.)

In equations 2A and 2B calculated for the "odds" and "evens" in the array of cements, the coef./s.d. ratios for C₄AF, MgO, Ba, SrO, and V

Table 12–21. Frequency distribution of cements with respect to ARWT, the ratio of percentage weight gain divided by the percentage weight loss of Series A concretes, ARWT = AWET/ADRY

Type cement	0.82 to 0.85	0.85 to 0.88	0.88 to 0.91	0.91 to 0.94	0.94 to 0.97	0.97 to 1.00	1.00 to 1.03	1.03 to 1.06	1.06 to 1.09	1.09 to 1.12	1.12 to 1.15	Total		
		Number of cements												
IIA		3	12	20	23	8	7 2	2 2	3	1		79 8		
II.	1	2	3	22	17	7	10	3	2			67		
IIIA			1	2	6	2	3	2	4		2	20		
IV, V			1	2	6	4		2				15		
Total	1	5	17	46	55	21	24	12	11	1	2	195		

Table 12–22. Coefficients for equations for $AE + NAE$ cements relating $ARWT$, the ratio of the percentage weight-gain with 28 days water-storage divided by the percentag weight loss with 56 days of air storage of Series A concretes to various independent variables ($ARWT = AWET/ADRY$) Eq. (A.1)	e e	11
vients for equations for $AE + NAE$ cements relating $ARWT$, the ratio of the percentage weight-gain with 28 days water-st weight loss with 56 days of air storage of Series A concretes to various independent variables $(ARWT = AWET/A)$. Air	tag	
vients for equations for $AE + NAE$ cements relating $ARWT$, the ratio of the percentage weight-gain with 28 days water-st weight loss with 56 days of air storage of Series A concretes to various independent variables $(ARWT = AWET/A)$. Air	cen	
vients for equations for $AE + NAE$ cements relating $ARWT$, the ratio of the percentage weight-gain with 28 days water-st weight loss with 56 days of air storage of Series A concretes to various independent variables $(ARWT = AWET/A)$. Air	per	ŀ
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vients for equations for $AE + NAE$ cements relating $ARWT$, the ratio of the percentage weight-gain with 28 days water-st weight loss with 56 days of air storage of Series A concretes to various independent variables $(ARWT = AWET/A)$. Air	n t	
vients for equations for $AE + NAE$ cements relating $ARWT$, the ratio of the percentage weight-gain with 28 days water-st weight loss with 56 days of air storage of Series A concretes to various independent variables $(ARWT = AWET/A)$. Air	g f	
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S.D.	0.04436	0.04321	0.04353	0.04387	0.04235	0.04439	0.04320	0.04353	0.04386	0.04234
Δ		(0.204)	* -0.232 (0.325)	(0.276)	** -0.251		(0.204)	* -0.233	(0.276)	** -0.250 (0.201)
Sro		-0.0596 (0.0380)	* -0.0428	(0.0567)	** -0.0556 (0.0373)		-0.0596 (0.0380)	* -0.0428 (0.0544)	-0.0999 (0.0567)	**-0.0556 (0.0373)
Cu		+0.985	+0.996 (0.615)	+0.786 (0.594)	+1.222 (0.408)		+0.987 (0.407)	+0.996 (0.615)	+0.789 (0.594)	+1.226 (0.408)
Ba		+0.195	*+0.212 (0.318)	+0.171 (0.133)	**+0.191 (0.108)		+0.195 (0.110)	*+0.211 (0.317)	+0.171 (0.133)	**+0.192 (0.108)
APF	+0.0000213 (0.0000066)	+0.0000195	+0.0000181 (0.0000095)	+0.0000220 (0.0000097)	+0.0000161	+0.0000209	+0.0000195	+0.0000181 (0.0000095)	+0.0000220 (0.00000097)	+0.0000161
MgO	+0.00414 (0.00294)	+0.00559 (0.00303)	+0.00837 (0.00436)	*+0.00198 (0.00452)	**+0.00553 (0.00297)	+0.00389 (0.00297)	+0.00558 (0.00303)	+0.00835 (0.00436)	$^* + 0.00198$ (0.00452)	**+0.00552 (0.00297)
Na ₂ O	-0.0706 (0.0205)	-0.0634 (0.0213)	-0.0643 (0.0334)	-0.0665 (0.0301)	-0.0761 (0.0213)	-0.0713 (0.0205)	-0.0634 (0.0213)	-0.0642 (0.0334)	-0.0664 (0.0301)	-0.0761 (0.0213)
Fe ₂ O ₃						* -0.00399 (0.02053)	-0.00849 (0.00479)	-0.01173 (0.00741)	* -0.00428 (0.00682)	** -0.00562 (0.00481)
CAF		-0.00276 (0.00157)	-0.00382 (0.00243)	* -0.00138 (0.00223)	**-0.00180 (0.00158)	; i i i i i i i i i i i i i i i i i i i				
Air	+0.00731	+0.00730 (0.00166)	+0.00556 (0.00203)	+0.01196 (0.00310)	+0.00663 (0.00164)	+0.00708 (0.00465)	+0.00730 (0.00166)	+0.00557 (0.00202)	+0.01196 (0.00310)	+0.00663 (0.00164)
ADRY					(0.0093)					(0.0093)
Const.	= +0.877 = (0.025)	= +0.904 = (0.032)	= +0.909 = (0.047)	= +0.896 = (0.046)	= +0.977 = (0.041)	= +0.892 = (0.031)	= +0.905 = (0.032)	= +0.909 = (0.047)	= +0.896 = (0.046)	= +0.978 = (0.041)
	ARWT s.d.	ARWT s.d.	ARWT (odd) s.d.	ARWT (even) = +0.896 s.d. = (0.046)	ARWT s.d.	ARWT s.d.	ARWT s.d.	ARWT (odd) s.d.	ARWT (even) = $+0.896$ s.d. = (0.046)	ARWT s.d.
Note	1	П	61	ဇာ	-	1		61	ဇာ	1
NE So.	1	2	2A	2B	3	4	5	5A	5B	9

*Coef./s.d. ratio less than 1.0.

**Coef./s.d. ratio less than 1.0 in "odds" or "evens."

Note 1, 173 cements, Avg. = 0.9605, S.D. = 0.04956

Note 2, 87 cements

Note 3, 86 cements

Table 12-23. Coefficients for equations for NAE cements relating the ratio of the percentage weight-gain with 28 days water-storage divided by the percentage weight loss with 56 days air storage of Series A concretes to various independent variables (ARWT = AWET/ADRY)

	S.D.	0.04383	0.04233	0.04413	0.04222	0.04153	0.04389	0.04232	0.04413	0.04221	0.04153
	^	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	-0.306 (0.205)	-0.672 (0.334)	*-0.080	** -0.224 (0.203)		(0.205)	-0.670 (0.334)	*-0.080	** -0.223
	SrO	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	(0.0393)	-0.0778 (0.0630)	-0.0852 (0.0531)	-0.0806	-	-0.0865 (0.0393)	-0.0779 (0.0630)	-0.0851 (0.0531)	(0.0386)
	Cu	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	+0.958	*+0.538 (0.686)	+1.111 (0.578)	+1.215 (0.410)		+0.960 (0.406)	*+0.546 (0.686)	+1.109 (0.577)	+1.218 (0.410)
	Ba	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	+0.190 (0.109)	$^*+0.193$ (0.334)	+0.133 (0.133)	**+0.192 (0.107)		$^{+0.190}_{(0.109)}$	$^*_{(0.334)}$	+0.134 (0.132)	** +0.192 (0.107)
	APF	+0.0000183	+0.0000159	+0.0000106 (0.0000100)	+0.0000198	**+0.0000135 (0.0000067)	+0.0000178 (0.0000068)	+0.0000159	+0.0000106 (0.0000100)	+0.0000198 (0.0000098)	** +0.0000135 (0.0000067)
	MgO	+0.00324 (0.00296)	+0.00509 (0.00304)	+0.00721 (0.00481)	*+0.00380 (0.00410)	+0.00511 (0.00298)	+0.00304 (0.00298)	+0.00508 (0.00304)	+0.00721 (0.00481)	*+0.00377 (0.00409)	+0.00510 (0.00298)
,	Na ₂ O	-0.0763 (0.0207)	-0.0653 (0.0213)	-0.0653 (0.0363)	-0.0693 (0.0289)	-0.0755 (0.0213)	-0.0769	-0.0653 (0.0213)	-0.0653 (0.0363)	-0.0693 (0.0288)	(0.0213)
	Fe ₂ O ₃					0 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	* -0.00352 (0.00467)	-0.00839 (0.00481)	* -0.00087 (0.00839)	-0.01244 (0.00662)	** -0.00584 (0.00482)
	CAAF		$\begin{array}{c} -0.00273 \\ (0.00158) \end{array}$	* -0.00023 (0.00028)	-0.00407 (0.00217)	** -0.00188 (0.00158)	1 1				
	Air	+0.00900 (0.00400)	+0.00769 (0.00419)	+0.00957 (0.00597)	*+0.00548 (0.00628)	**+0.00513 (0.00415)	+0.00357 (0.00405)	+0.00770 (0.00411)	+0.00955 (0.00596)	*+0.00549 (0.00628)	** +0.00513 (0.00415)
-	ADRY	1 1 1 1 1 1 1 1	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	1 1 1 1 1 1 1 1 1 1 1 1 1	-0.0247 (0.0095)	1 1 1 1 1 1 1 1 1 1 1 1 1 1	1 1 1 1 1 1 1 1 1 1 1 1 1	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	-0.0247 (0.0094)
	Const.	= +0.887 = (0.026)	= +0.921 = (0.033)	= +0.913 = (0.049)	= +0.924 = (0.047)	= +0.990 = $= (0.042)$	= +0.902 = (0.032)	= +0.921 = (0.033)	= +0.914 = (0.049)	= +0.924 = (0.047)	= +0.990 = (0.041)
		ARWT s.d.	ARWT s.d.	ARWT (odd) s.d.	ARWT (even) s.d.	ARWT s.d.	ARWT s.d.	ARWT s.d.	ARWT (odd) s.d.	ARWT (even) = $+0.924$ s.d. = (0.047)	ARWT s.d.
	Note	1	1	61	es	-	-	-	61	ဧာ	1
	NE o	1	2	2A	2B	89	4	20	5A	5B	9

*Coef./s.d. ratio less than 1.0.

**Coef./s.d. ratio less than 1.0 in "odds" or "evens."

Note 1, 161 cements, Avg. = 0.9563, S.D. = 0.04696

Note 3, 80 cements
Note 3, 80 cements

were less than 1.0 in one or the other of the

smaller groups.

The use in eq 3 of ADRY, the percentage loss on drying as an independent variable, together with those previously mentioned, resulted in a further significant reduction of variance. In eqs 3A and 3B, calculated for the "odds" and "evens" (not presented in the table), there were instances where the same independent variables had coef./s.d. ratios less than 1.0 as was indicated in eqs 2A and 2B. Equations 4, 5, and 6 were calculated using Fe₂O₃ instead of C₄AF as an independent variable. The coef./s.d. ratio for Fe₂O₃ was less than 1.0 in eq 4 and of doubtful significance in eqs 5 and 6. The use of the trace elements in eq 5 resulted in a reduction of variance significant at the 5.0-percent level. (See table 12–33.)

A corresponding series of equations for the NAE cements is presented in table 12–23. The coefficients, the s.d. values for the coefficients, and the S.D. values are in reasonable agreement with those of the previous table where the AE cements were

included.

Using the coefficients of the independent variables of eq 2 table 12–22 and the ranges of these variables, calculations were made of the estimated contributions to ARWT. The results of these calculations are presented in table 12–24 together with the calculated range of these contributions.

Table 12–24. Calculated contributions of independent variables to ARWT, the ratio of absorption to weight loss on drying of Series A concretes made of AE + NAE cements

Inde- pendent variables	Range of variables (percent)	Coefficients from eq 2 table 12-22	Calculated contributions to ARWT	Calculated range of contribu- tions to ARWT
Air- content C4AF** Na ₂ O MgO** APF. Ba** Cu_ SrO** V**	0 to 13 1 to 16 0 to 0.7 0 to 5 *2500 to 5500 0 to 0.2 0 to 0.05 0 to 0.4 0 to 0.1	+0.0073 -0.00276 -0.0634 +0.00559 +0.0000195 +0.195 +0.985 -0.0596 -0.315	Const. = +0.904 0 to +0.095 -0.003 to -0.044 0 to -0.024 +0.049 to +0.107 0 to +0.039 0 to +0.049 0 to -0.024 0 to -0.032	0.095 0.041 0.044 0.028 0.058 0.039 0.049 0.024 0.032

*cm²/g. **Coefficient of doubtful significance as coef./s.d. ratio was less than 2.0. Increases of the air-content, fineness, and possibly Cu were associated with an increase of the ARWT ratio. Increase of Na₂O was associated with decrease of the ARWT ratio.

5.4. Ratio of Weight-Gain Minus Weight-Loss to Weight-Loss

5.4.1. Absorption Ratio for Series O Concretes

The frequency distribution of the cements with respect to OWTR, the ratio (ODRY-OWET)/ODRY, is presented in table 12–25. There was a fairly broad distribution of values and an overlapping of the values obtained with the different

types of cement.

Equations are presented in table 12–26 indicating the independent variables associated with OWTR. The use of the commonly determined independent variables C₃A, C₃S, C₄AF, Na₂O, SO₃, APF, Loss, MgO, and air content in eq 1 resulted in a significant reduction of variance. The additional use of Cu and SrO in eq 2 resulted in a further reduction of variance significant at the 5.0-percent level.

In eq 2B the coef./s.d. ratios of C₄AF, Na₂O, and Cu were less than 1.0 for this group of results.

Equations 3 and 4 were calculated using the major oxides instead of the calculated potential compounds. The coef./s.d. ratios for SO₃, Loss, and MgO were less than 1.0 when included with these variables and were not retained in these equations.

The corresponding series of equations for the NAE cements is presented in table 12–27. The coefficients, their s.d. values, and the S.D. values of the equations are in reasonable agreement with those of the previous table where the AE cements

were included.

Using the coefficients of the independent variables of eq 2, table 12–26, together with the ranges of these variables, calculations were made of the estimated contributions to OWTR and the ranges of such contributions. These calculated values are presented in table 12–28. Increases of air content, fineness, and possibly C₃S, Cu, and MgO were

Table 12-25. Frequency distribution of cements with respect to OWTR, the ratio of the difference between weight loss and weightgain to the weight loss of Series O concretes. OWTR = (ODRY - OWET)/ODRY

		Absorption ratio												
Type cement	-0.21 to -0.18	-0.18 to -0.15	-0.15 to -0.12	-0.12 to -0.09	-0.09 to -0.06	-0.06 to -0.03	-0.03 to 0	0 to +0.03	+0.03 to 0.06	0.06 to 0.09	0.09 to 0.12	0.12 to 0.15	0.15 to 0.18	Total
Number of cements														
IIA					2	1 3	2 2	14	21	29	10	3		82 8
II					$\frac{1}{2}$	4	0	15	25	18	2	3		68
III IIIA				4	· 1	2	î	5	5	1			1	8 68 3 20 3 15
IV, V							1	3	7	4				15
Total	1	0	1	4	7	11	7	38	59	52	12	6	1	199

Eq. No.	Note		Const.	C ₃ A	C ₃ S	C ₄ AF	SiO ₂	Al ₂ O ₃
1	1	OWTR s.d.	= +0.181 = (0.035)	+0.00299 (0.00114)	-0.00087 (0.00046)	+0.00220 (0.00146)		
2	1	OWTR s.d.	= +0.193 = (0.035)	+0.00199 (0.00122)	-0.00094 (0.00045)	+0.00257 (0.00147)		
2A	2	OWTR (odd) s.d.	= +0.184 = (0.049)	+0.00300 (0.00182)	$-0.00061 \\ (0.00058)$	+0.00476 (0.00215)		
2B	2	OWTR (even) s.d.	= +0.221 = (0.060)	+0.00183 (0.00172)	$^{-0.00164}_{(0.00074)}$	*+0.00140 (0.00217)		
3	1	OWTR s.d.	= -0.168 = (0.138)				+0.0095 (0.0044)	+0.0162 (0.0056)
4	1	OWTR s.d.	= -0.217 = (0.138)				+0.0113 (0.0044)	+0.0155 (0.0057)
4A	2	OWTR (odd) s.d.	= -0.234 = (0.189)				+0.0115 (0.0060)	$^{+0.0168}_{(0.0083)}$
4B	2	OWTR (even) s.d.	= -0.231 = (0.208)				+0.0121 (0.0067)	+0.0157 (0.0082)

Note 1, 176 cements, Avg. = 0.0395, S.D. = 0.04671

Note 2, 88 cements *Coef./s.d. ratio less than 1.0.

Table 12-27. Coefficients for equations for NAE cements relating the ratio of differences water storage divided by the percentage weight-loss of Series O concretes

Eq. No.	Note		Const.	C ₃ A	C ₃ S	C ₄ AF	SiO ₂	Al ₂ O ₃
1	1	OWTR	= +0.178 = (0.037)	+0.00347 (0.00114)	+0.00093 (0.00047)	+0.00215 (0.00147)		
2	1	OWTR s.d.	= +0.189 = (0.036)	+0.00223 (0.00121)	$^{-0.00101}_{(0.00046)}$	$^{+0.00241}_{(0.00148)}$		
2A	2	OWTR (odd) s.d.	= +0.153 = (0.048)	+0.00279 (0.00167)	$-0.00079 \\ (0.00056)$	+0.00579) (0.00203)		
2B	2	OWTR (even) s.d.	= +0.226 = (0.058)	*+0.00176 (0.00182)	-0.00141 (0.00078)	*+0.00042 (0.00227)	,	
3	1	OWTR s.d.	= -0.150 = (0.141)				+0.00885 (0.00451)	+0.0167 (0.0057)
4	1	OWTR s.d.	= -0.204 = (0.141)				+0.01070 (0.00452)	$^{+0.0156}_{(0.0058)}$
4A	2	OWTR (odd) s.d.	= -0.325 = (0.176)				+0.01329 (0.00546)	$^{+0.0189}_{(0.0075)}$
4B	2	OWTR (even) s.d.	= -0.141 = (0.231)				+0.00974 (0.00758)	$^{+0.0135}_{(0.0091)}$

Note 1, 164 cements, Avg. = 0.0454, S.D. = 0.04165 Note 2. 82 cements

*Coef./s.d. ratio less than 1.0.

Table 12-28. Calculated contributions of independent variables to OWTR, the ratio (QDRY-OWET)/ODRY for Series O concretes made of AE + NAE cements

Inde- pendent variables	Range of variables (percent)	Coefficients from eq 2 table 12–26	Calculated contributions to OWTR	Calculated range of contribu- tions to OWTR
C ₃ A**	1 to 15 20 to 65 1 to 16 0 to 0.7 1.2 to 3.3 *2500 to 5500 0.3 to 3.3 0 to 5 0 to 11 0 to 0.05 0 to 0.4	$\begin{array}{c} +0.00199 \\ -0.00094 \\ +0.00257 \\ +0.0421 \\ -0.0187 \\ -0.000027 \\ +0.0102 \\ -0.0070 \\ -0.0122 \\ -0.795 \\ +0.0516 \end{array}$	$\begin{array}{c} \text{Const.} = +0.193 \\ +0.002 \text{ to } +0.030 \\ -0.018 \text{ to } -0.061 \\ +0.003 \text{ to } +0.041 \\ 0 \text{ to } +0.029 \\ -0.022 \text{ to } -0.062 \\ -0.068 \text{ to } -0.148 \\ +0.003 \text{ to } +0.034 \\ 0 \text{ to } -0.035 \\ \end{array}$	0.028 0.043 0.038 0.029 0.040 0.080 0.031 0.035 0.134 0.040

*cm 2 /g. **Coefficient of doubtful significance as coef./s.d. ratio was less than 2.0.

associated with decreases of the OWTR ratio. Increases of Na₂O were possibly associated with increases of the OWTR ratio. The coefficients for C₃A, C₄AF, Loss, and SrO were of doubtful significance.

5.4.2. Absorption Ratio for Series A Concretes

The frequency distribution of AWTR, the ratio of (ADRY-AWET)/AWET, is presented in table 12–29. There was a broad distribution of values and an overlapping of the values obtained with the different types of cement.

Equations are presented in table 12-30 indicating the independent variables associated with AWTR. Equation 1 indicates that an increase of the air content was associated with a decrease of the absorption ratio. (See also table 12-33.) The differences between the percentage weight-loss on air drying and the percentage weight-cretes to various independent variables OWTR = (ODRY - OWET)/ODRY

Fe ₂ O ₃	Na ₂ O	SO ₃	APF	Loss	MgO	Air content	Cu	SrO	S.D.
	+0.0453 (0.0163)	-0.0148 (0.0097)	$-0.000029 \\ (0.000007)$	+0.0098 (0.0055)	-0.0060 (0.0023)	-0.0122 (0.0015)			0.03473
	+0.0421 (0.0167)	-0.0187 (0.0097)	$-0.000027 \\ (0.000007)$	+0.0102 (0.0054)	$-0.0070 \\ (0.0023)$	-0.0122 (0.0015)	-0.795 (0.322)	+0.0516 (0.0340)	0.03402
	$^{+0.0773}_{(0.0227)}$	-0.0313 (0.0156)	$\substack{-0.000032 \\ (0.000010)}$	+0.0095 (0.0082)	-0.0089 (0.0036)	-0.0113 (0.0021)	-1.416 (0.476)	+0.0588 (0.0500)	0.03417
	*-0.0099 (0.0270)	-0.0137 (0.0130)	$\substack{-0.000022 \\ (0.000010)}$	+0.0109 (0.0076)	-0.0047 (0.0033)	$-0.0139 \ (0.0022)$	*-0.477 (0.480)	+0.0527 (0.0476)	0.03338
+0.00607 (0.00382)	$^{+0.0471}_{(0.0164)}$		$-0.000025 \\ (0.000006)$			-0.0127 (0.0015)			0.03529
+0.00928 (0.00399)	$^{+0.0456}_{(0.0170)}$		$\substack{-0.000024 \\ (0.000006)}$			$-0.0128 \ (0.0015)$	$-0.740 \\ (0.327)$	+0.0386 (0.0343)	0.03480
+0.01415 (0.00579)	+0.0857 (0.0234)		$-0.000028 \\ (0.000009)$			$-0.0126 \ (0.0022)$	-1.284 (0.493)	*+0.0250 (0.0494)	0.03555
+0.00744 (0.00569)	*-0.0042 (0.0265)		-0.000020 (0.000008)			$-0.0138 \ (0.0021)$	-0.571 (0.477)	+0.0552 (0.0481)	0.03380

between the percentage weight-loss on air drying and the percentage weight-gain with to various independent variables OWTR = (ODRY - OWET)/ODRY

Fe ₂ O ₃	Na ₂ O	SO ₃	APF	Loss	MgO	Air content	Cu	SrO	S.D.
	$^{+0.0480}_{(0.0165)}$	-0.0152 (0.0098)	$-0.000028 \\ (0.000007)$	+0.0127 (0.0056)	-0.0057 (0.0024)	-0.0150 (0.0038)			0.034
	+0.0408 (0.0168)	-0.0199 (0.0097)	$-0.000026 \\ (0.000007)$	+0.0141 (0.0055)	$-0.0068 \\ (0.0023)$	$-0.0136 \ (0.0037)$	-0.728 (0.326)	+0.0727 (0.0348)	0.033
	$^{+0.0792}_{(0.0205)}$	-0.0240 (0.0144)	-0.000025 (0.000009)	*+0.0061 (0.0086)	$-0.0086 \ (0.0031)$	$-0.0156 \\ (0.0055)$	*-0.403 (0.457)	+0.0590 (0.0524)	0.030
	*+0.0043 (0.0285)	*-0.0134 (0.0141)	$\substack{-0.000029 \\ (0.000011)}$	+0.0184 (0.0079)	-0.0058 (0.0037)	$-0.0122 \\ (0.0056)$	-0.927 (0.477)	+0.0885 (0.0526)	0.035
+0.00489 (0.00389)	+0.0500 (0.0167)		-0.000024 (0.000006)			-0.0162 (0.0038)			0.035
+0.00810 (0.00410)	$^{+0.0452}_{(0.0173)}$		-0.000022 (0.000006)			$-0.0151 \\ (0.0038)$	-0.661 (0.335)	+0.0538 (0.0355)	0.034
+0.01923 (0.00561)	+0.0836 (0.0205)		+0.000021 (0.000008)			-0.0147 (0.0055)	*-0.344 (0.457)	*+0.0328 (0.0483)	0.031
*+0.00079 (0.00592)	*-0.0052 (0.0295)		-0.000023 (0.000009)			-0.0151 (0.0056)	-0.729 (0.488)	+0.0894 (0.0541)	0.036

Table 12–29. Frequency distribution of cements with respect to AWTR, the ratio of the difference between weight-loss and weight-loss. AWTR = (ADRY - AWET)/ADRY

	Absorption ratio												
Type cement	-0.15 to -0.12	-0.12 to -0.09	-0.09 to -0.06	-0.06 to -0.03	-0.03 to 0	0 to 0.03	+0.03 to 0.06	0.06 to 0.09	0.09 to 0.12	0.12 to 0.15	0.15 to 0.18	Total	
	Number of cements												
[1	3	2 2	6	7	24 3	21	11	4		79 8	
II.			1	3	3	13	17	24	3	1	1	66	
II IIA	2		4	î	1	3	8	2	1			66 3 20 3 15	
v, v				2		4	5	3	1			15	
Total	2	1	10	11	11	30	57	50	16	5	1	194	

Table 12-30. Coefficients for equations for AE + NAE cements relating the ratio of the difference between the percentage weight-loss on air drying and the percentage weight gain with water storage divided by the percentage weight-loss of Series A concretes to various independent variables (AWTR = (ADRY - AWET)/ADRY)

$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	SrO S.D.	0.04732	0.04455	+0.0857 0.04324 (0.0380)	(0.0565) 0.04264	(0.0515) 0.04349	0.04468	+0.0857 0.04324 (0.0380)	*+0.0516 0.04264 (0.0565)	
Note	Cu		1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1		*					
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	MgO	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	(0.00296)	-0.00597 (0.00290)	*-0.00364 (0.00416)	-0.00843 (0.00412)	0.00403	-0.00596 (0.00291)	*-0.00364 (0.00416)	
Note Note Const. content C ₃ A C ₄ AF Fe ₂ O ₃ 1 AWTR = $+0.0514$ -0.00527 -0.00531 $+0.00184$ $+0.00258$ -0.00583 -0.00531 $+0.00184$ -0.00258 -0.00560 -0.00660	APF		$\begin{array}{c} -0.0000161 \\ (0.0000065) \end{array}$	-0.0000160 (0.0000063)	-0.0000132 (0.0000095)	-0.0000152 (0.0000086)	-0.0000165 (0.0000065)	$\begin{array}{c} -0.0000160 \\ (0.0000063) \end{array}$	(0.00000133	
Note Const. content CoAA C.AF S.d. = +0.0514	Na ₂ O		+0.0716 (0.0207)	+0.0651 (0.0211)	+0.0564 (0.0311)	+0.0890 (0.0296)	+0.0749 (0.0206)	+0.0651 (0.0211)	+0.0564 (0.0311)	
Note Const. content C ₃ A AWTR = +0.0514	Fe2O3				\$ 1 	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	* +0.00370 (0.00467)	+0.00894 (0.00478)	* +0.00041 (0.00686)	
Note Note	CAAF	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	+0.00258 (0.00182)	+0.00291 (0.00157)	* +0.00011 (0.00224)	+0.00581 (0.00230)	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1			
Note AWTR = +0.0514 S.d. = (0.0050) AWTR = +0.0627 S.d. = (0.0369) AWTR (odd) = +0.0952 S.d. AWTR (even) = +0.0446 S.d. AWTR (even) = +0.0446 S.d. AWTR (even) = +0.0909 S.d. AWTR (even) = +0.0910	C3A	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	+0.00184 (0.00131)				1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1			
Note AWTR S.d. AWTR S.d. AWTR S.d. AWTR S.d. AWTR (odd) S.d. AWTR (even) S.d. AWTR S.d. AWTR	Air	-0.00527 (0.00172)	-0.00531 (0.00170)	-0.00560 (0.00164)	-0.00940 (0.00304)	-0.00432 (0.00199)	-0.00524 (0.00170)	-0.00560 (0.00165)	-0.00939 (0.00303)	
Note	Const.				R (odd) = $+0.0952$ = (0.0416)	R (even) = $+0.0446$ = (0.0457)			R (odd) = $+0.0950$ = (0.0417)	
	ite	AWT s.d.	AWT s.d.	AWT s.d.			AWT s.d.	AWT s.d.		
38A 5A		1	1	1	2	6	1	1	2	

Table 12–31. Coefficients for equations for NAE cements relating the ratio of the difference between the percentage weight-loss on air drying and the percentage weight-gain with water storage divided by the percentage weight-loss of Series A concretes to various independent variables (AWTR = (AWET)/ADRY)

S.D.	0.04688	0.04357	0.04239	0.04252	0.04323	0.04372	0.04238	0.04252	0.04322	
SrO	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1		+0.0800 (0.0392)	*+0.0286 (0.0540)	+0.1395 (0.0590)		+0.0800 (0.0392)	*+0.0287 (0.0540)	+0.1394 (0.0589)	
Cu			-1.007 (0.406)	$\frac{-1.248}{(0.570)}$	-0.809 (0.623)		-1.009 (0.406)	-1.248 (0.570)	-0.814 (0.623)	
MgO		-0.00379 (0.00294)	-0.00527 (0.00290)	* -0.00273 (0.00399)	-0.00795 (0.00442)	-0.00325 (0.00292)	-0.00526 (0.00290)	* -0.00271 (0.00399)	-0.00794 (0.00443)	
APF		-0.0000197 (0.0000066)	-0.0000191 (0.0000064)	-0.0000201 (0.0000100)	-0.0000196 (0.00000089)	-0.0000201 (0.0000066)	-0.0000191 (0.0000064)	-0.0000201 (0.0000100)	-0.0000195 (0.0000089)	, 81 cements
Na ₂ O	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	+0.0731 (0.0207)	+0.0673 (0.0210)	+0.0552 (0.0313)	+0.0690 (0.0306)	+0.0759 (0.0207)	+0.0673 (0.0210)	+0.0551 (0.0313)	+0.0691 (0.0306)	Note 3,
Fe2O3					; 1 ; 1 ; 3 ; 3 ; 1 ; 1 ; 1 ; 1 ; 1 ; 1 ; 1 ; 1 ; 1 ; 1	*+0.00325 (0.00463)	+0.00844 (0.00478)	+0.00727 (0.00696)	+0.00827 (0.00715)	2, 82 cements
CAF		+0.00249 (0.00182)	+0.00274 (0.00157)	+0.00237 (0.00228)	+0.00267 (0.00235)					.6 Note 2,
C3A	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	+0.00190 (0.00131)					1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1			S.D. = 0.0471
Air	-0.00718 (0.00419)	-0.00885 (0.00401)	-0.00787 (0.00394)	-0.01111 (0.00613)	*-0.00443 (0.00538)	-0.00891 (0.00402)	-0.00788 (0.00394)	-0.01111 (0.00614)	*-0.00444 (0.00537)	'g. = 0.04329,
Const.	= +0.0544 $= (0.0074)$	= +0.0788 = (0.0378)	= +0.0904 $= (0.0315)$	$ \begin{array}{rcl} 1) & = +0.1075 \\ & = & (0.0446) \end{array} $	AWTR (even) = $+0.0838$ s.d. = (0.0472)	= +0.1082 = (0.0318)	= +0.0900 = (0.0315)	AWTR (odd) = $+0.1074$ s.d. = (0.0447)	AWTR (even) = $+0.0833$ s.d. = (0.0473)	Note 1, 163 cements, Avg. = 0.04329, S.D. = 0.04716
	AWTR s.d.	AWTR s.d.	AWTR s.d.	AWTR (odd) s.d.	AWTR (eve s.d.	AWTR s.d.	AWTR s.d.	AWTR (ode s.d.	AWTR (eve s.d.	Note 1,
Note	1	-	1	61	60	-	-	61	es	than 1.0.
Eq. No.	1	2	38	3A	3B	4	70	5A	5B	*Coef./s.d. ratio less than 1.0.

Table 12–32. Calculated contributions of independent variables to AWTR, the ratio of (ADRY - AWET)/ADRY for Series A concretes made of AE + NAE cements.

Inde- pendent variable	Range of variables (percent)	Coefficients from eq 3 table 12–30	Calculated contributions to AWTR	Calculated range of contribu- tions to AWTR
Air- content C4AF** Na ₂ O APF MgO Cu SrO	0 to 13 1 to 16 0 to 0.7 *2500 to 5500 0 to 5 0 to 0.05 0 to 0.4	$\begin{array}{c} -0.0056 \\ +0.00291 \\ +0.0651 \\ -0.000016 \\ -0.00597 \\ -1.032 \\ +0.0857 \end{array}$	Const. = +0.0758 0 to -0.073 +0.003 to +0.047 0 to +0.046 -0.040 to -0.088 0 to -0.030 0 to -0.051 0 to +0.034	0.073 0.044 0.046 0.048 0.030 0.051

^{*}cm²/g.
**Coefficient of doubtful significance as coef./s.d. ratio was less than 2.0.

Table 12-33. "F" values for significance of reduction of variance due to added variables

Table	Equations*	"F"	D.F.	Critical "F" ratios		
		ratio		$\alpha = 0.01$	$\alpha = 0.05$	
12-2	0,1 1,2 2,3 0,4 4,5 5,6	18.4 24.0 1.95 17.4 17.4 3.27	3:177 5:172 4:168 5:175 5:170 3:167	3.88 3.13 3.42 3.13 3.13 3.88	2.67 2.28 2.42 2.28 2.28 2.28 2.67	
12–3	0,1	17.8	3:165	3.88	2.67	
	1,2	20.5	5:160	3.13	2.28	
	2,3	2.07	3:157	3.90	2.67	
	0,4	18.5	5:163	3.13	2.28	
	4,5	12.9	5:158	3.13	2.28	
	5,6	2.40	4:154	3.43	2.42	
12-6	0,1	11.2	4:172	3.42	2.42	
	1,2	26.6	4:168	3.42	2.42	
	2,3	13.6	2:166	4.71	3.05	
	3,4	2.56	4:162	3.43	2.42	
	0,5	19.6	9:167	2.52	1.93	
	5,6	13.5	2:165	4.73	3.05	
	6,7	2.21	3:162	3.90	2.67	
12-7	0,1	9.7	4:160	3.43	2.42	
	1,2	23.9	4:156	3.43	2.42	
	2,3	12.0	2:154	4.74	3.05	
	3,4	2.20	4:150	3.44	2.42	
	0,5	17.3	9:155	2.52	1.93	
	5,6	11.9	2:153	4.74	3.05	
	6,7	1.98	3:150	3.90	2.67	
12-10	0,1	718	2:179	4.70	3.05	
	0,2	6.77	2:179	4.70	3.05	
	2,3	25.5	2:177	4.70	3.05	
	3,4	34.2	4:173	3.42	2.42	
	4,5	3.81	4:169	3.42	2.42	
	0,6	19.1	6:175	2.92	2.15	
	6,7	21.8	4:171	3.42	2.42	
	7,8	4.31	4:167	3.42	2.42	
12-11	0,1	816	2:167	4.72	3.05	
	0,2	11.7	4:165	3.43	2.42	
	2,3	31.4	4:161	3.43	2.42	
	3,4	3.46	4:157	3.43	2.42	
	0,5	14.5	6:163	2.92	2.15	
	5,6	20.0	4:159	3.43	2.42	
	6,7	3.81	4:155	3.44	2.42	
12-14	0,1	2.65	2:173	4.73	3.05	
	0,2	8.00	4:171	3.42	2.42	
	2,3	26.4	4:167	3.43	2.42	
	3,4	3.44	5:162	3.13	2.28	
	4,5	4.05	1:161	6.77	3.90	
	0,6	17.6	9:166	2.52	1.93	
	6,7	3.94	4:162	3.44	2.42	
	7,8	4.82	1:161	6.77	3.90	
12-15	0,1 0,2 2,3 3,4 4,5 0,6 6,7 7,8	2.07 7.16 25.8 3.27 16.3 16.7 4.08 16.9	2:161 4:159 4:155 5:150 1:149 9:154 4:150 1:149	4.73 3.44 3.14 6.78 2.52 3.44 6.78	3.05 2.42 2.42 2.28 3.90 1.93 2.42 3.90	

Table 12-33. "F" values for significance of reduction of variance due to added variables—Continued

Table	Equations*		D.F.	Critical "	F" ratios
		ratio		$\alpha = 0.01$	$\alpha = 0.05$
12–18	0,1	22.6	2:175	4.72	3.05
	1,2	13.0	6:169	2.92	2.15
	2,3	4.10	2:167	4.72	3.05
	0,4	17.7	8:169	2.62	2.00
	4,5	4.15	2:167	4.72	3.05
12–19	0,1	4.18	2:163	4.73	3.05
	1,2	12.3	6:157	2.92	2.15
	2,3	3.53	2:155	4.74	3.05
	0,4	10.7	8:157	2.62	2.00
	4,5	3.57	2:155	4.74	3.05
12–22	0,1	9.59	5:168	3.13	2.28
	1,2	2.81	5:163	3.13	2.28
	2,3	7.69	1:162	6.77	3.90
	0,4	8.11	6:167	2.92	2.15
	4,5	3.33	4:163	3.43	2.42
	5,6	7.69	1:162	6.77	3.90
12-23	0,1	5.76	5:156	3.14	2.28
	1,2	3.25	5:151	3.14	2.28
	2,3	6.87	1:150	6.78	3.90
	0,4	4.89	6:155	2.92	2.15
	4,5	3.93	4:151	3.44	2.42
	5,6	6.80	1:150	6.78	3.90
12-26	0,1	15.2	10:166	2.93	1.90
	1,2	4.50	2:164	4.72	3.05
	0,3	19.9	7:169	2.75	2.07
	3,4	3.40	2:167	4.72	3.05
12-27	0,1 1,2 0,3 3,4	$\begin{array}{c} 8.70 \\ 5.15 \\ 10.4 \\ 3.37 \end{array}$	10:154 2:152 7:157 2:155	2.93 4.74 2.75 4.74	1.90 3.05 2.07 3.05
12-30	0,1	5.19	2:173	4.72	3.05
	1,2	5.44	5:168	3.13	2.28
	0,3	6.58	8:167	2.62	2.00
	0,4	6.12	6:169	2.92	2.15
	4,5	6.72	2:167	4.72	3.05
12-31	0,1	1.98	2:161	4.73	3.05
	1,2	6.08	5:156	3.13	2.28
	0,3	5.84	8:155	2.62	2.00
	0,4	5.44	6:157	2.92	2.15
	4,5	6.04	2:155	4.74	3.05

^{*0} in the equation column refers to the S.D. value of the corresponding dependent variable as given in footnotes in the tables of equations.

use of other commonly determined variables, C₃A, C₄AF, Na₂O, APF, and MgO, in eq 2 resulted in a further significant reduction in the S.D. value. The S.D. values of eqs 2 and 3 cannot be compared because of the absence of C₃A in eq 3, but, judging from eqs 4 and 5, it appears likely that the inclusions of Cu and SrO with the commonly determined variables caused a significant reduction of variance. (See table 12–33.)

The coef./s.d. for Fe₂O₃ in eq 4 was less than 1.0, but in eq 5 the ratio was greater than 1.0. In eqs 3A and 5A the coef./s.d. ratios for C₄AF, Fe₂O₃, MgO, and SrO were less than 1.0 with the smaller lot of cements.

A corresponding series of equations for the NAE cements is presented in table 12–31. The use of the air content in eq 1 did not result in a significant reduction of the S.D. value. (See table 12–33.) In eqs 3B and 5B the coef./s.d. ratio for the aircontent of the NAE cements was less than 1.0 with the smaller groups of cement. The coefficients of the other independent variables were consistent with those of the previous table where the AE cements were included.

Using the coefficients of the independent variables of eq 3, table 12–30, and the ranges of these variables, computations were made of the calculated contributions to AWTR. These estimated contributions and the calculated ranges of the

contributions are presented in table 12–32. Increases in air content and possibly fineness, MgO, and Cu were associated with decreases of the AWTR ratio. Increases of Na $_2$ O and possibly SrO were associated with increases of the AWTR ratio.

Table 12-34. Coefficients, coef./s.d. ratios, and calculated ranges of contributions to percentage loss of weight on drying, percentage gain of weight on resoaking, and ratios for Series O concretes made of NAE cements

Column	1	2	3	4
Eq. No.	3	4	3	2
Table No.	12-3	12-11	12-19	12-27
Dependent variables	ODRY	OWET	ORWT	OWTR
Constant	+4.233	+3.813	+0.849	+0.189
Air content, coef	+0.0846 2.7 0.38	+0.1128 3.9 0.51	+0.0124 3.0 0.056 -0.0020	-0.0136 3.7 0.061 +0.00223
Goet./s.d			1.7 0.028	1.8 0.031
C _s S, coef. Coef./s.d	-0.02265 6.6 1.02	-0.01931 6.3 0.87		-0.00101 2.2 0.045
C4AF, coef Coef./s.d Calculated range	+0.03474 3.6 0.49	+0.03057 3.3 0.43	-0.00319 2.0 0.045	+0.00241 1.6 0.034
Va2O, coef. Coef./s.d. Calculated range	-0.5362 4.0 0.38	-0.6766 5.7 0.47	-0.0653 3.7 0.046	+0.0408 2.4 0.029
K ₂ O, coef. Coef./s.d	-0.6471 5.6 0.71	-0.6138 5.8 0.68		
O3, coef	-0.2549 3.8 0.51	-0.1836 3.0 0.36		-0.0199 2.1 0.040
MgO, coef. Joef./s.d. Jalculated range			+0.00611 2.3 0.030	-0.0068 3.0 0.034
.oss, coef	-0.0573 1.3 0.17	-0.0682 1.8 0.20	-0.0125 2.1 0.038	+0.0141 2.6 0.042
APF, coef			+0.0000429 6.8 0.120	-0.000026 3.7 0.078
Ba, coef. Coef./s.d Calculated range	$^{+0.923}_{1.5}_{0.18}$	$^{+0.8131}_{\begin{subarray}{c} 1.4 \\ 0.16 \end{subarray}}$		
Cu, coef. Coef./s.d		$\begin{array}{cccccccccccccccccccccccccccccccccccc$	+0.665 1.8 0.33	-0.728 2.3 0.036
Mn, coef. Coef./s.d. Calculated range			0.0441 1.8 0.044	
Rb, coef. Coef./s.d	-16.49 1.3 0.16	-19.28 1.8 0.19		
SrO, coef. Coef./s.d. Calculated range				-0.0727 2.1 0.029
Zr, coef Coef./s.d. Calculated range	-0.657 1.2 0.33	-0.8397 1.8 0.42		

6. Discussion

6.1. Variables Associated With Weight-Loss, Absorption, and Their Ratios

A series of equations selected from those previously given in tables for concretes made with NAE cements is presented in tables 12–34 and

12–35 in order that the variables, their coefficients, and the possible range of contributions to the dependent variables may be compared more readily. The equations are presented vertically instead of horizontally as in previous tables of this section. Reference is also made to the equations for the

Table 12-35. Coefficients, coef./s.d. ratios, and calculated ranges of contributions to the percentage loss of weight on drying, the percentage gain of weight on resoaking, and ratios for Series A concretes made of NAE cements

Column	1	2	3	4
Eq. No.	4	5	2	3
Table No.	12-7	12-15	12-23	12-31
Dependent variable	ADRY	AWET	ARWT	AWTR
Constant	-1.069	+0.560	+0.921	+0.0904
r content, coef	+0.0646 1.9 0.29 +7.864	+5.047	+0.00769 1.8 0.035	-0.00787 2.0 0.035
c, coef. ef./s.d. lculated range	4.8 1.18	4.1 0.76		
A, coefef./s.del.	+0.02282 2.4 0.32	+0.01921 2.0 0.27		
S, coef. oef./s.d. alculated range	$ \begin{array}{r} -0.02216 \\ 6.7 \\ 1.00 \end{array} $	-0.0190 5.8 0.86		
AF, coef	$^{+0.05101}_{\stackrel{4.4}{0.71}}$	+0.03078 2.8 0.43	-0.00273 1.7 0.038	+0.00274 1.7 0.038
a ₂ O, coef. oef./s.d. alculated range	-0.5857 4.6 0.41	-0.7028 5.7 0.49	-0.0653 3.1 0.046	+0.0673 3.2 0.047
20, coef. oef./s.d. alculated range	$ \begin{array}{r} -0.6948 \\ 5.8 \\ 0.76 \end{array} $	-0.6713 6.0 0.74		
O3, coefoef./s.dalculated range	-0.2511 3.5 0.50	-0.1648 2.4 0.33		
igO, coef oef./s.d alculated range			$\begin{array}{c} +0.00509 \\ 1.7 \\ 0.025 \end{array}$	$ \begin{array}{r} -0.00527 \\ 1.8 \\ 0.026 \end{array} $
PF, coefoef./s.d. oef./s.d. alculated range			+0.0000159 2.3 0.048	-0.0000191 3.0 0.057
oss, coefoef./s.dalculated range	-0.0824 2.0 0.25	-0.0743 1.9 0.22		-
a, coef. oef./a.d. alculated range	$^{+1.043}_{1.7}_{0.20}$	+1.287 2.1 0.25	+0.190 1.7 0.004	
o, coef. pef./s.d. alculated range		$\begin{array}{c c} +19.71 \\ 1.3 \\ 0.19 \end{array}$		
ı, coef. nef./s.d. ılculated range	+3.748 1.5 0.19	+6.973 2.7 0.40	+0.958 2.4 0.048	-1.007 2.5 0.050
o, coef. ef./s.d. clculated range	-12.31 1.0 0.12			_
			-0.0865 2.2 0.035 -0.306	+0.0800 2.0 0.032
ef./s.dlculated range				
r, coef oef./s.d	-0.6953 1.3 0.35	-0.7586 1.6 0.38		

concretes made of AE + NAE cements which

have previously been presented.

The variables associated with the percentage loss of weight when the specimens were dried in air for 56 days (col 1) were generally, but with a few exceptions, also associated with the percentage weight-gain when the dried specimens were later placed in water for 28 days (col 2).

Higher air contents of the concretes were associated with higher values for weight-loss with air-drying and greater absorption on rewetting for the Series O concretes but not the Series A concretes. When the AE cements were included in the computation, the coef./s.d. ratio of the "air content" was greater. See eq 3 table 12–2 and eq 5 table 12–10.

Concretes made with NAE cements, which required a higher water/cement ratio to achieve the desired slump, also had higher weight-loss and absorption in drying and wetting, as shown by the coefficients for w/c in table 12–35, cols. 1 and 2.

Of the major potential compounds, higher C₃A was probably associated with higher loss on drying and gain on rewetting with the Series A concretes, but not with the Series O concretes. Higher

Table 12–36. Relationships of weight loss and weight gain of concretes to dynamic Young's modulus of elasticity (in psi × 10⁻⁶) of concretes at 14, 70, and 98 days

		es at 14, 70, and 98 days		0.5	
Equation	Type cement			S.D.	"F"
	AE+NAE	$ \begin{array}{rcl} \text{ODRY} &= +6.10 - 0.723 \\ \text{s.d.} &= (0.29) & (0.060) \end{array} $	OD14	0.30	72
		$ \begin{array}{rcl} \text{ODRY} &= +5.42 - 0.624 \\ \text{s.d.} &= (0.27) (0.060) \end{array} $	OD70	0.32	54
		$ \begin{array}{rcl} \text{ODRY} &= +5.25 - 0.510 \\ \text{s.d.} &= (0.48) & (0.095) \end{array} $	OD98	0.37	14.5
		OWET = $+6.26 - 0.775$ s.d. = (0.24) (0.051)	OD14	0.26	114
		OWET = $+5.41 - 0.643$ s.d. = $(0.24) (0.054)$	OD70	0.29	71
		OWET = +5.76 - 0.628 s.d. = (0.43) (0.085)	OD98	0.33	27
		ADRY = $+6.12 - 0.720$ s.d. = (0.37) (0.078)	AD14	0.33	43
		ADRY = +5.27 - 0.583 s.d. = (0.33) (0.075)	AD70	0.34	30
		ADRY = +4.64 - 0.384 s.d. = (0.62) (0.122)	AD98	0.39	5.00
)		$\begin{array}{rcl} \text{AWET} &= +6.07 - 0.731 \\ \text{s.d.} &= (0.34) & (0.071) \end{array}$	AD14	0.30	53
L		AWET = $+5.16 - 0.580$ s.d. = $(0.31) (0.070)$	AD70	0.32	35
2		AWET = $+4.96 - 0.467$ s.d. = $(0.58) (0.131)$	AD98	0.36	8.49
3	NAE	$ \begin{array}{rcl} \text{ODRY} &= +8.20 - 1.151 \\ \text{s.d.} &= (0.33) & (0.067) \end{array} $	OD14	0.25	146
4		$ \begin{array}{rcl} \text{ODRY} &= +6.18 - 0.786 \\ \text{s.d.} &= (0.32) & (0.070) \end{array} $	OD70	0.31	63
5		$ \begin{array}{rcl} \text{ODRY} &= +7.67 - 0.978 \\ \text{s.d.} &= (0.76) & (0.148) \end{array} $	OD98	0.36	22
6		$ \begin{array}{rcl} \text{OWET} &= +7.72 & -1.074 \\ \text{s.d.} &= (0.30) & (0.061) \end{array} $	OD14	0.23	152
7		$ \begin{array}{rcl} \text{OWET} &= +5.76 - 0.719 \\ \text{s.d.} &= (0.30) & (0.065) \end{array} $	OD70	0.29	60
8		$ \begin{array}{rcl} \text{OWET} &= +7.23 - 0.913 \\ \text{s.d.} &= (0.70) & (0.136) \end{array} $	OD98	0.22	22
)		ADRY = +8.01 - 1.103 s.d. = (0.35) (0.973)	AD14	0.26	115
)		ADRY = +6.00 - 0.738 s.d. = (0.34) (0.077)	AD70	0.32	46
L		$\begin{array}{rcl} \text{ADRY} &= +6.79 - 0.798 \\ \text{s.d.} &= (0.74) & (0.144) \end{array}$	AD98	0.37	15
2		$\begin{array}{ll} \text{AWET} &= +7.61 - 1.042 \\ \text{s.d.} &= (0.34) (0.072) \end{array}$	AD14	0,26	106
3		$\begin{array}{rcl} \text{AWET} &= +5.71 - 0.699 \\ \text{s.d.} &= (0.33) (0.075) \end{array}$	AD70	0.32	44
4		$\begin{array}{ll} \text{AWET} &= +6.64 - 0.790 \\ \text{s.d.} &= (0.71) (0.138) \end{array}$	AD98	0.35	16

C₃S was associated with lower loss on drying and lower absorption when rewetted for both series. Higher C₄AF was associated with higher loss on drying and higher absorption for both series.

The coefficients for Na₂O and K₂O were highly significant in both drying and wetting for both series of concretes. Increases of the alkalies were associated with decreases of the loss of weight on drying and gain of weight on rewetting. Of the two alkalies, only Na₂O had a significant effect on the ratios ORWT and OWTR.

An increase of the SO₃ content in both series was associated with a decrease of the weight-loss or weight-gain but not with the ratios. However, an increase of fineness was not associated with the loss of weight or weight-regain when rewetted, but was associated with the ratios ORWT,

OWTR, and AWTR.

Of the various trace elements, Cu had coef./s.d. values of 2.0 or greater with 5 of the 8 equations. SrO had coef./s.d. ratios of 2.0 or slightly over in some of the ratios (see columns 3 and 4 of tables 12–34 and 12–35.) Other trace elements usually had coef./s.d. values less than 2.0 and were, therefore, of doubtful significance.

6.2. Weight-Loss and Absorption Versus Dynamic Modulus of Elasticity

Table 12–36 shows linear equations indicating the relationship between the dynamic modulus of elasticity at 14, 70, and 98 days total age and the percentage loss of mositure during 56 days of drying and the percentage absorption with the subsequent 28 days in water. The independent variables, ODRY, OWET, ADRY, and AWET, as indicated previously are the weight-loss and weight-gain of the $6-\times 8-\times 16$ -in concrete blocks. The independent variables represent dynamic modulus values obtained from measurements of fundamental flexural frequencies of companion $3-\times 4-\times 16$ -in concrete beams made from the same concrete mixes as the blocks. OD14

and AD14 refer to the dynamic modulus after 14 days of moist curing; OD70 and AD70 to dynamic modulus of the same beams after 56 days of drying in laboratory air (total age 70 days); and OD98 and AD98 to dynamic modulus after 28 days soaking in water (total age 98 days). The initial O and A, respectively, refer, as with other symbols, to the Series O concretes with constant w/c ratio and Series A concretes with constant slump.

The reduction of variance was greater when the loss or gain of weight was related to the values for dynamic modulus after 14 days moist curing. This was found for both the Series O and Series A concretes each made of AE + NAE or NAE cements. Higher dynamic modulus was significantly related at all ages and conditions of test to lower loss of weight with drying and lower

absorption when rewetting.

6.3. Air Content Versus Absorption and Weight-Loss

As indicated in subsection 6.1 as well as in the various equations of this section, higher air contents of the concretes were associated with higher weight-loss on drying and higher weight-gain when placed in water. It was previously indicated in section 10, tables 10-1 and 10-2, and in the discussion in subsection 6.1 of section 10 that concretes made with air-entraining cements had lower cement contents than the original design mix and most of the concretes made with nonair-entraining cements. The somewhat leaner and more porous nature of the concretes made with the air-entraining cements may therefore have been responsible for the higher weight-loss and absorption. However, as indicated in section 11 on durability in subsection 6.3, the saturation ratio after 24 hours in water was lower with higher air contents. The longer period (28 days versus 24 hours) in water may also have been responsible for the differences in these two series of tests.

7. Summary and Conclusions

Concrete specimens $6 - \times 8 - \times 16$ -in (approx. $15 - \times 20 - \times 40$ -cm) were made from 199 portland cements of different types, using $5\frac{1}{2}$ bags of cement per cubic yard (approx. 307 kg/m^3). In one series, the water-cement ratio was constant at 0.635, and in the other, the water was adjusted, if necessary, to obtain a slump of 5 ± 1 in (12.7 ± 2.5 cm). Specimens were moist cured for 14 days, dried in laboratory air for 56 days, and then immersed in water for 26 days. Determinations were made of the percentage weight-loss and the percentage absorption, and various ratios were calculated for the weight-loss and weight-gain. The observations and conclusions were as follows:

(7.1) The percentage loss of weight as a result of drying in laboratory air ranged from less than

2.0 to more than 4.0 percent.

(7.2) When the air-dried specimens were later immersed in water for 28 days the absorption ranged from less than 2.0 up to 4.0 percent. There was a highly significant relationship between the loss on drying and the subsequent absorption.

(7.3) The ratio of weight-gain to weight-loss ranged from about 0.8 to 1.2 and the ratio of (ODRY-OWET)/ODRY ranged from about -0.15 to +0.18 with similar values for the A

Series

(7.4) The frequency distributions of the weight-loss, weight-gain, and the two ratios indicated that a range of values was obtained for each of the types of cement, and that there was considerable overlapping of the values obtained for the different types.

(7.5) Computations of equations by a least-

squares method were used to determine the chemical and physical properties of the cements which were associated with the weight-loss, the weight-gain, and the ratios of gain to loss. The equations were computed for all cements for which minor constituents and trace elements had been determined. Equations were computed for the AE + NAE cements and for the NAE cements. The equations were computed using the calculated major potential compounds or the major oxides together with other commonly determined variables, and then with trace elements which appeared to have a significant effect.

The following observations relate to the Series O concretes made of NAE cements as summarized

in table 12–34:

(7.5.1) Increases of C₄AF and possibly air content were associated with increases of ODRY, the percentage loss of weight on drying. Increases of C₃S, Na₂O, K₂O, and SO₃ were associated with

decreases of the loss of weight on drying.

(7.5.2) Increases of the air content, C₄AF, and possibly Cu were associated with increases of OWET, the percentage weight-gain when the airdried specimens were immersed in water for 28 days. Increases of C₃S, Na₂O, K₂O, and SO₃ were associated with decreases of the weight-gain.

(7.5.3) Increases of air content and fineness, and possibly MgO, were associated with increases of ORWT, the ratio OWET/ODRY. Increases of Na₂O, and possibly C₄AF and Loss, were associated with decreases of ORWT. Of these, variations of fineness had the greatest calculated effect.

(7.5.4) Increases of air content, fineness, MgO, and possibly C₃S, Cu, and SrO, were associated with decreases of OWTR, the ratio (ODRY −OWET)/ODRY. Increases of Na₂O and loss on ignition were possibly associated with increases

of the OWTR ratio.

(7.6) The independent variables associated with the dependent variables of the Series A concretes (where the water was adjusted to obtain a selected slump) were in general agreement with those of the constant water/cement ratio concretes.

(7.7) The use of the major oxides instead of the calculated potential compounds as independent variables (together with other commonly determined variables) resulted in equations with similar estimated standard deviation values.

(7.8) Of the various trace elements, the coefficients for Cu and SrO were probably significant in equations for some of the properties. Other trace elements, though appearing in the equations, were of doubtful significance.

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Section 13. Dynamic Young's Modulus of Elasticity of Concrete

R. L. Blaine and H. T. Arni

The relationships between cement characteristics and dynamic Young's modulus of elasticity of concretes at different ages and moisture conditions were studied by computing multivariable regression equations with the aid of a digital computer. An increase of the aircontent and water/cement ratio needed for the desired slump were associated with a decrease of the dynamic E. Increases in C_3S and SO_3 were associated with increases of the dynamic E. Other independent variables, although significant, generally had less effect on the dynamic E. The use of trace elements as independent variables in equations resulted in a significant reduction of variance when the concrete specimens were moist. There was generally a decrease of dynamic modulus when moist specimens were dried in laboratory air for 4 or 8 weeks and an increase when the air-dried specimens were resaturated. Placing the air-dried specimens in water for 24 hours resulted in a slight decrease in dynamic modulus with some concretes and an increase with other concretes.

Key words: Cement composition; compressive strength; concrete; dynamic modulus of elasticity; effect of moisture on dynamic E; modulus of rupture; portland cement; trace elements.

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1. Introduction

Modulus of elasticity determined by resonant frequency methods has been used to study the effects on concrete properties of various treatments, conditions, or changes in conditions [1, 2, 3; 4]. Examples of such use include: (1) deterio-

ration due to freezing and thawing in laboratory tests [5, 6]; (2) deterioration due to natural weathering [7]; (3) effect of chemical attack [8]; (4) effects of incomplete consolidation [9]; (5) effect of curing methods [10]. Also various studies have been made in an attempt to relate dynamic modulus to other properties of the concrete such as static modulus of elasticity, creep, relaxation,

¹ Figures in brackets refer to literature references at the end of this section (p. 125).

shrinkage, and compressive, flexural, and tensile

strength [11, 12, 13, 14].

The object of this paper is to investigate the effect on dynamic modulus under various conditions of curing, drying, and rewetting of variables connected with the cements used. The source and

amount of aggregate was the same throughout the study. The cement content was held constant, except for changes required by the amount of entrained air. Dynamic modulus tests were conducted according to ASTM Designation C 215 [15].

2. Materials

2.1. Cements

The cements used in the present tests were the same as those used in the work reported throughout the series of sections of the Interrelation Between Cement and Concrete Properties. The results of chemical analyses and the semiquantitative spectrochemical analyses were presented in sections 2 and 3 of part 1 of this series of articles [16]. Reports of other properties of these cements, mortars, and concretes have been presented in parts 2, 3, 4 [17, 18, 19], and in the first two sec-

tions of the present part 5. Most of the 199 portland cements were obtained from different areas of the United States, but a few were obtained from other countries.

2.2. Aggregates

A high quality rounded quartzite coarse aggregate was used with a sand from the same source. The sand and coarse aggregate gradation was previously presented in section 1 [16].

3. M. thods of Test

3.1. Preparation of Concretes

The details of the proportioning and mixing of the concretes were described in part 1, section 1 of this series of articles [16]. Two series of concretes were made with these cements; one (Series O) was made using a water/cement (w/c) ratio of 0.635, and the other (Series A) with the water varied, if necessary, to give a concrete with a 5 ± 1 -in slump. The concrete mix was designed to contain 5.5 bags of cement per cubic yard but varied somewhat as indicated in section 11 because of the amount of entrained air.

3.2. Test Specimens

The $3\text{-}\times4\text{-}\times16\text{-}\mathrm{in}$ concrete specimens of the two series were made from the same batches of concrete used for the shrinkage and expansion tests [19], the durability tests, and the weight-loss and weight-gain tests reported in sections 11 and 12 of this publication.

3.3. Storage of Test Specimens

The concrete was cured at 73 ± 1 °F in the molds under damp burlap for the first 20 to 24 hours, then placed in a fog room at 100 percent relative humidity until 14 days old. The specimens were then placed on end and exposed to laboratory air at 73 °F and 50 percent relative humidity for 8 weeks. The specimens were then placed in water for an additional 4 weeks.

3.4. Measurements of Specimens

The fundamental transverse frequencies of the concrete specimens were determined in accordance with ASTM Method C 215 [15]. The measurements were made on two 3- × 4- × 16-in prisms of each of the two series of concretes at 14 days (after moist curing), at 70 days (after 8 weeks of drying in laboratory air), at 71 days (after 24 hours in water), and at 98 days (after 4 weeks in water).

4. Abbreviations

The abbreviations, notations, etc., used in this section for physical and chemical properties of the cements are the same as those used in previous sections of this series of articles.²

In this section, as in the previous three, the prefix "O" of the four-letter titles for the various dependent variables refers to the concretes of Series O in which a water/cement (w/c) ratio of

0.635 was used. The prefix A refers to the Series A concretes which had a 5 \pm 1-in slump. A summary of other titles for the dependent variables used in this section are as follows:

For Series O concretes made with a w/c of 0.635 OD14 = dynamic modulus in psi × 10⁻⁶ at 14 days after moist curing.

OD42 = dynamic modulus in psi × 10⁻⁶ after 14 days moist curing followed by 28 days drying in laboratory air.

OD70 = dynamic modulus in psi × 10⁻⁶ after 14 days moist curing followed by 56 days drying in laboratory air.

² These abbreviations include the use of C₂A, C₃S, C₂S, and C₄AF for the calculated potential compounds, tricalcium aluminate, tricalcium silicate, dicalcium silicate, and tetracalcium aluminoferrite, respectively. Also used are Insol for insoluble residue, Loss for loss on ignition, APF for air permeability fineness, Wagn for Wagner Turbidimeter fineness. AE + NAE refers to air-entraining plus non-air-entraining cements, and NAE to the non-air-entraining cements.

OD71 = dynamic modulus in psi \times 10⁻⁶ after air dried specimens had been placed in water for 24 hours.

OD98 = dynamic modulus in psi \times 10⁻⁶ after air dried specimens had been in water for 28 days.

OE 70/14 = OD70/OD14 OE 98/70 = OD98/OD70 OE 71/70 = OD71/OD70 For Series A concretes having a 5 \pm 1-in slump, the letter "A" is used instead of "O", as AD14, AD42, AD70, AD71, AD98, AE 70/14, AE 98/70, and AE 71/70 for the different independent variables.

The values for dynamic Young's modulus of elasticity will generally be referred to as dynamic modulus, or dynamic E.

5. Statistical Analyses

The statistical techniques used to find and evaluate the independent variables associated with the dynamic modulus at the various ages and test conditions and the ratios of these values have been described in a previous section of this series part 1, section 1, Materials and Techniques [16]. The statistical treatment was the same as that used in all previous sections of this series of articles. Multiple regression equations were calculated by a least-squares method using various independent variables to determine which showed an association with each of the dependent variables. As in previous sections, equations were calculated for both the AE + NAE cements and the NAE cements. Calculations were made using only commonly determined variables and also using these together with minor and trace elements.

After equations had been developed in which independent variables showed significant relationships with the dependent variable, the residuals of these equations were fitted by a least-squares method to other independent variables and the reduction in variance calculated. If any of the additional independent variables indicated a significant reduction in variance, they were tried in the equation and retained if the coef./s.d. ratio was greater than 1.0.3

nificant reduction in variance, they were tried in the equation and retained if the coef./s.d. ratio was greater than 1.0.3

Ratios of reduction in variance to original variance ("F" ratios) obtained by fitting equations were calculated for two kinds of cases: (1) for

3 Statistical terms and notations employed in this section are the same as those used in previous sections of this series of articles. For example, S.D. refers to the estimated standard deviation calculated from the residuals of a fitted equation, or the estimated standard deviation of a coefficient of an independent variable used in a fitted equation. The term coef./s.d. is the ratio of the estimated coefficient (of an independent variable used in an equation) to its estimated deviation. "F" designates Fisher's ratio of variances and D.F. is used to designate the number of degrees of freedom. As indicated in previous sections, a coef./s.d. ratio greater than 1.0 was considered to be of sufficient significance to warrant further investigation.

Equations were also calculated for the "odds" and "evens" in the array of cements. Comparisons were made of the coefficients of the variables in the two groups of data and these were compared to the coefficients and coef./s.d. ratios computed for all the cements.

Although dynamic modulus of elasticity was determined for both series of concretes made of all of the 199 cements, the calculations of equations presented in this section were limited to those cements for which trace-element determinations had been made.

Equations presented in this section were selected from a large number of trial equations indicating the calculated relationship of various variables to the dynamic modulus values or their ratios.⁴ A summary of the relationships indicated by the equations for both series of concretes is given in the discussion in subsection 7.

Some of the limitations on interpretation of multivariable regression equations as well as other statistical techniques used in this series of articles have been discussed in section 1, subsections 4.2, 4.3, and 5 [16]. Other limitations and problems of interpretation have also been discussed in other sections of this series of articles.

6. Results of Tests

6.1. Dynamic Modulus After 14 Days Moist Curing

6.1.1. Dynamic Modulus of Series O Concretes

The frequency distribution of the dynamic moduli of the Series O concretes after 14 days moist curing is presented in table 13-1. There

was a broad distribution of values and an overlapping of the values for the different types of cement. The air-entraining cements (Types IA, IIA, and IIIA) generally had values in the lower half of the distribution curve.

Equations are presented in table 13–2 indicating the variables associated with the dynamic modulus of Series O concretes made of AE + NAE

equations including a few main independent variables as compared to the original data on the dependent variable, or (2) for equations in which additional independent variables were included as compared to a previous equation with fewer variables. The calculated "F" ratios and the critical "F" values which must be equaled or exceeded for significance at the $\alpha=0.05$ and $\alpha=0.01$ levels are summarized in a table (table 13–57).

⁴ These equations were selected primarily to indicate the association with commonly determined independent variables having coef./s.d. ratios greater than 1.0 when used in multivariable equations, and also to indicate which of minor and trace elements may show a significant relationship.

Table 13-1. Frequency distribution of cements with respect to OD14, the dynamic modulus of elasticity of Series O concretes after 14 days moist curing

					Dynamic	modulus	of elastici	ty, 10 ⁶ psi				
Type cement	3.4 to 3.6	3.6 to 3.8	3.8 to 4.0	4.0 to 4.2	4.2 to 4.4	4.4 to 4.6	4.6 to 4.8	4.8 to 5.0	5.0 to 5.2	5.2 to 5.4	5.4 to 5.6	Total
						Number	of cements	3				
I .	2	3	3		1	3	16	34	24	3	1	82
II.			1	1	1	13	17	25	9	1		68 3
III.			<u>1</u>				2	4	10	4		20
iV, V	1		2		4	2	3	2	1			15
Total	3	4	7	1	8	19	39	65	44	8	1	199

Table 13-2. Coefficients for equations relating OD14, the dynamic Young's modulus of NAE cements, to various

Eq. No.	Note	10 ⁶ psi	Const.	Air content	C ₃ A	C ₃ S	C ₄ AF	CaO	SiO ₂
1	1	OD14 s.d.	= +3.767 = (0.173)	-0.1622 (0.0078)	+0.00965 (0.00585)	+0.0194 (0.0022)	-0.0196 (0.0075)		
2	1	OD14 s.d.	= +3.723 = (0.170)	-0.1593 (0.0077)	+0.01007 (0.00584)	+0.0196 (0.0021)	-0.0178 (0.0074)		
2A	2	OD14 (odd) s.d.	= +3.718 = (0.248)	-0.1562 (0.0108)	*+0.00332 (0.00850)	+0.0193 (0.0028)	-0.0236 (0.0106)		
2B	2	OD14 (even) s.d.	= +3.811 = (0.249)	-0.1646 (0.0116)	+0.01558 (0.00852)	+0.0190 (0.0036)	-0.0124 (0.0109)		
3	1	OD14 s.d.	= +1.978 = (2.492)	-0.1621 (0.0078)				+0.0975 (0.0272)	-0.1306 (0.0288)
4	1	OD14 s.d.	= +1.681 = (2.504)	-0.1592 (0.0077)				+0.1009 (0.0274)	-0.1298 (0.0285)
4A	2	OD14 (odd) s.d.	= +1.615 = (3.817)	-0.1562 (0.0109)				+0.1003 (0.0411)	-0.1267 (0.0418)
4B	2	OD14 (even) s.d.	= +0.735 = (3.621)	-0.1643 (0.0116)				+0.1093 (0.0403)	-0.1164 (0.0433)

^{*}Coef./s.d. ratio less than one.

Note 1, 180 cements, Avg. = 4.75 \times 10 6 psi, S.D. = 0.3550 \times 10 6 psi Note 2, $\,$ 90 cements

Table 13-3. Coefficients for equations relating OD14, the dynamic Young's modulus cements, to various

Eq. No.	Note	10 ⁶ psi	Const.	Air content	CaA	C ₈ S	C ₄ AF	CaO	SiO ₂
1	1	OD14 s.d.	= +3.691 = (0.171)	-0.1328 (0.0195)	+0.00947 (0.00590)	+0.0193 (0.0022)	-0.0168 (0.0075)		
2:	1	OD14 s.d.	= +3.618 = (0.176)	-0.1346 (0.0193)	+0.01056 (0.00596)	+0.0197 (0.0022)	-0.0144 (0.00 7 5)		
2A	2	OD14 (odd) s.d.	= +3.634 = (0.262)	-0.1344 (0.0321)	+0.01025 (0.00946)	+0.0197 (0.0030)	*-0.0096 (0.0127)		
2B	2	OD14 (even) s.d.	= +3.603 = (0.258)	-0.1369 (0.0252)	+0.01004 (0.00824)	+0.0193 (0.0036)	-0.0193 (0.0099)		
3	1	OD14 s.d.	= +4.377 = (1.174)	-0.1321 (0.0196)				+0.0721 (0.0141)	-0.155 (0.022)
4	1	OD14 s.d.	= +2.249 = (2.593)	-0.1348 (0.0194)				+0.0947 (0.0284)	-0.137 (0.029)
4A	2	OD14 (odd) s.d.	= +4.213 = (4.480)	-0.1351 (0.0316)				+0.1621 (0.0483)	-0.077 (0.047)
4B	2	OD14 (even) s.d.	= +4.081 = (3.414)	-0.1367 (0.0254)				+0.0737 (0.0386)	-0.151 (0.041)

^{*}Coef./s.d. ratio less than one.

Note i, 168 cements, Avg. = 4.820 \times 10 6 psi, S.D. = 0.2585 \times 10 6 psi Note 2, $\,$ 84 cements

cements. The use of commonly determined variables, air content, C₃A, C₃S, C₄AF, SO₃, Na₂O, K₂O, and MgO in eq 1 resulted in a highly significant reduction in variance. (See table 13–57,⁵ p. 108).

Using these commonly determined variables in eq 2 together with the trace elements Mn, Rb, and Zr which had coef./s.d. ratios greater than 1.0, a further significant reduction in variance was obtained. Equations 2A and 2B, calculated for the "odds" and "evens" in the array of cements

indicated that C₃A, Na₂O, MgO, and Mn had coef./s.d. ratios less than 1.0 in one or the other of the smaller groups of cements.⁶

The major oxides CaO, SiO₂, Al₂O₃, and Fe₂O₃ were used in eq 3 instead of the calculated potential compounds as in eqs 1 and 2. There was a significant reduction in variance, and when the trace elements Mn, Rb, and Zr were used with the commonly determined variables in eq 4 there was a further reduction in variance. (See table 13–57.) In eqs 4A and 4B calculated for the "odds" and

elasticity in 10^6 psi after 14 days moist curing of Series O concretes made of AE+ independent variables

Al ₂ O ₃	Fe ₂ O ₃	SO ₃	Na ₂ O	K ₂ O	MgO	Mn	Rb	Zr	S.D.
		+0.146 (0.042)	+0.302 (0.083)	+0.240 (0.071)	+0.0138 (0.0123)				0.1763
		+0.160 (0.041)	+0.260 (0.082)	+0.148 (0.078)	+0.0240 (0.0125)	-1.188 (0.115)	+18.63 (7.76)	+0.561 (0.331)	0.1718
		+0.237 (0.057)	+0.272 (0.105)	+0.124 (0.110)	*+0.0130 (0.0180)	*-0.052 (0.154)	+14.92 (9.92)	+1.675 (0.853)	0.1678
		+0.079 (0.062)	*+0.116 (0.157)	+0.205 (0.121)	+0.0369 (0.0178)	-0.445 (0.181)	+19.82 (12.90)	+0.488 (0.383)	0.1762
-0.0875 (0.0319)	-0.0867 (0.0299)	+0.117 (0.057)	+0.315 (0.085)	+0.253 (0.073)	+0.0298 (0.0257)				0.1765
-0.0855 (0.0317)	-0.0799 (0.0296)	+0.135 (0.057)	+0.273 (0.084)	+0.166 (0.081)	+0.0422 (0.0257)	-0.176 (0.116)	+18.39 (7.77)	+0.617 (0.339)	0.1720
-0.1022 (0.0433)	-0.0856 (0.0440)	+0.215 (0.085)	+0.284 (0.108)	$^{+0.150}_{(0.120)}$	*+0.0296 (0.0354)	* -0.042 (0.156)	+14.57 (9.97)	+1.795 (0.881)	0.1684
-0.0562 (0.0508)	-0.0618 (0.0434)	*+0.070 (0.085)	*+0.140 (0.160)	$^{+0.217}_{(0.122)}$	+0.0673 (0.0402)	-0.416 (0.185)	+19.91 (12.93)	+0.555 (0.392)	0.1765

of elasticity in $10^{\rm e}$ psi after 14 days moist curing of Series O concretes made of NAE independent variables

Al ₂ O ₃	Fe ₂ O ₃	SO ₃	Na ₂ O	K ₂ O	MgO	Mn	Rb	Zr	S.D.
		+0.165 (0.042)	+0.300 (0.084)	+0.252 (0.071)					0.1738
		+0.177 (0.041)	+0.257 (0.085)	+0.152 (0.081)	+0.0204 (0.0126)	$-0.183 \ (0.119)$	$^{+15.39}_{(7.91)}$	+0.580 (0.332)	0.1704
		+0.178 (0.060)	+0.212 (0.109)	*+0.112 (0.125)	*+0.0132 (0.0180)	$-0.415 \\ (0.164)$	+25.07 (11.53)	*+0.586 (2.245)	0.1727
		+0.203 (0.063)	+0.335 (0.148)	$^{+0.119}_{(0.115)}$	+0.0274 (0.0186)	$^{+0.193}_{(0.191)}$	*+3.98 (12.11)	+0.526 (0.362)	0.1691
$-0.112 \\ (0.025)$	-0.101 (0.021)	+0.097 (0.048)	+0.295 (0.085)	$^{+0.236}_{(0.076)}$					0.1741
$-0.092 \\ (0.033)$	-0.077 (0.030)	+0.141 (0.058)	$^{+0.266}_{(0.087)}$	$^{+0.166}_{(0.085)}$	+0.0326 (0.0266)	-0.179 (0.121)	$^{+15.26}_{(7.92)}$	+0.619 (0.340)	0.1707
*-0.035 (0.050)	*+0.007 (0.055)	+0.236 (0.090)	$^{+0.276}_{(0.113)}$	$^{+0.191}_{(0.131)}$	+0.0835 (0.0439)	$-0.401 \ (0.162)$	+25.10 (11.37)	*-0.380 (2.281)	0.1702
-0.108 (0.048)	-0.108 (0.039)	+0.141 (0.083)	+0.333 (0.149)	$^{+0.118}_{(0.117)}$	*+0.0228 (0.0362)	*+0.187 (0.200)	*+3.85 (12.21)	+0.511 (0.381)	0.1702

⁵ A tabulation of the "F" values for reduction in variance for all equations compared is presented in table 13–57. Presented also are the critical values for "F" which must be equaled or exceeded for significance at the 1- and 5-percent levels for the number of degrees of freedom (D.F.) involved in each comparison.

⁶ As has been indicated in previous sections of this series of articles, this may occur if a number of cements having higher than normal values for an independent variable are included in one of the two groups. If the coefficients of a variable in smaller groups, i.e. the odds and evens, both are significant, a greater confidence can be placed on the significance of the variable of the equation where all cements were included.

"evens" in the array of cements, the variables SO₃, Na₂O, MgO, and Mn had coef./s.d. ratios less than 1.0 in one or the other of the equations

for the smaller groups of cements.

A similar series of equations is presented in table 13–3 for the Series O concretes made with NAE cements. The coefficients for the air content were highly significant even with the concretes made with non-air-entraining cements. The coefficients of the other variables, the coef./s.d. ratios, and S.D. values were in reasonable agreement with those of table 13–2 where the air-entraining cements were included. Including the trace elements in eqs 2 and 4 together with commonly determined variables resulted in a reduction of variance significant at the $\alpha=0.05$ level. In eqs 2A, 2B, 4A, and 4B calculated for the "odds" and "evens" the coef./s.d. ratio of C₄AF, Al₂O₃, Fe₂O₃, K₂O, MgO, Mn, Rb, and Zr was less than 1.0 in one or the other of the equations for the smaller groups of cements.

Using the independent variables of eq 2, table 13–3, and the ranges of these variables, values were calculated for their contributions and ranges of contributions to the dynamic modulus after 14 days moist curing. These calculated values, as presented in table 13–4, are approximations based on a single equation, and somewhat different

Table 13-4. Calculated contributions of independent variables to OD14, the 14-day dynamic modulus of Series O concretes

Inde- pendent variable	Range of variables (percent)	Coefficients from eq 2 table 13-3	Calculated contributions to OD14	Calculated range of contribu- tions to OD14
Air- content,			Const. = $+3.62$	8
NAE cements_ C ₃ A* C ₄ AF* SO ₃	0 to 4.5 1 to 15 20 to 65 1 to 16 1.2 to 3.0	$\begin{array}{c} -0.1346 \\ +0.01056 \\ +0.0197 \\ -0.0144 \\ +0.177 \end{array}$	0 to -0.61 +0.01 to +0.15 +0.39 to +1.28 -0.01 to -0.23 +0.21 to +0.53	0.61 0.14 0.89 0.22 0.32
Na ₂ O K ₂ O* MgO* Mn* Rb*	0 to 0.7 0 to 1.1 0 to 5 0 to 1.0 0 to 0.01	$ \begin{array}{c} +0.177 \\ +0.257 \\ +0.152 \\ +0.0204 \\ -0.183 \\ +15.39 \end{array} $	$\begin{array}{c} 0 \text{ to } +0.17 \\ 0 \text{ to } +0.17 \\ 0 \text{ to } +0.10 \\ 0 \text{ to } -0.18 \end{array}$	0.17 0.17 0.10 0.18 0.15
Zr*	0 to 0.5	+0.580	$\begin{array}{c} 0 \text{ to } +0.15 \\ 0 \text{ to } +0.29 \end{array}$	0.13

^{*}Coefficient of doubtful significance as coef./s.d. ratio was less than 2.

values would be obtained by the use of other equations.

Increases in air content were associated with decreases in the dynamic modulus values. Increases of C₃S, SO₃, and Na₂O were associated with increases of dynamic modulus. Differences in the air content and C₃S had the greatest calculated contribution to the 14-day dynamic modulus as determined from this equation.

6.1.2. Dynamic Modulus of Series A Concretes

The frequency distribution of the dynamic modulus of the Series A concretes is presented in table 13–5. There was a broad distribution of values and an overlapping of the values for the different types of cement. The majority of the concretes made of the air-entraining cements, as with the Series O concretes (table 13–1), had lower values for dynamic modulus than the over-all average.

A series of equations is presented in table 13–6 to indicate the relationship of various independent variables to the dynamic modulus of Series A concretes made of AE + NAE cements. The use of the air content as an independent variable in eq 1, or w/c in eq 2 or both in eq 3 resulted in a significant reduction in variance. (See table 13-57). The additional use of the commonly determined variables C₃S, C₄AF, SO₃, Na₂O, K₂O, and MgO in eq 4 resulted in a highly significant reduction in variance. The coefficient for w/c was greater in magnitude and had a higher coef./s.d. ratio in eq 4 than in eq 3. It was indicated in a previous section [16] that a number of independent variables was related to the water requirement of the cements, and it may be that the differences in these coefficients indicate some interaction between water/cement ratio and other independent variables.

With the use of the commonly determined variables together with the trace elements Rb and Mn in eq 5 there was a reduction in variance

Table 13-5. Frequency distribution of cements with respect to AD14, the dynamic modulus of elasticity of Series A concretes after 14 days moist curing

				D	ynamic m	odulus of	elasticity,	psi × 10	-6				
Type cement	3.6 to 3.8	3.8 to 4.0	4.0 to 4.2	4.2 to 4.4	4.4 to 4.6	4.6 to 4.8	4.8 to 5.0	5.0 to 5.2	5.2 to 5.4	5.4 to 5.6	5.6 to 5.8	Total	
	Number of cements												
I			4	3 3	6	20	32	14	1	2	1	79 8	
II	1		2	4	8	21	23	8	1			67 3	
III					2	1	5	11	2	1		20	
IV, V	1	1	1	2	6	2	1	1				15	
Total	2	2	7	12	23	45	62	34	4	3	1	195	

⁷ Computations for contributions to dynamic modulus at other ages have been made from similar equations, i.e., one selected from the NAE cements containing one or more of the potential major compounds, other commonly determined variables, and trace elements in order that the trends may be followed more easily.

significant at the $\alpha=0.05$ level. (See table 13–57.) The coef./s.d. ratios of Na₂O, Rb, and Mn were less than 1.0 in eqs 5A or 5B calculated for the "odds" and "evens" in the array of cements.

The use of the major oxides in eq 6 together with other commonly determined variables resulted in an S.D. value not significantly different from that of eq 4 where the potential compounds were used as independent variables. The additional use of the independent variables MgO, Rb, and Mn in eq 7 did not result in a reduction of variance significant at the $\alpha=0.05$ level. The eqs 7A and 7B calculated for the "odds" and "evens" in the array of cements indicated that CaO, SO₃, Na₂O, K₂O, MgO, and Rb had coef./s.d. ratios of less than 1.0 in one or the other or both of the equations for the smaller group of cements.

An analogous series of equations calculated for the dynamic modulus after 14 days moist curing of Series A concretes made with NAE cements is presented in table 13-7. As indicated in eqs 1, 2, and 3, the coefficients for air content and w/c were not significant. In eqs 4 through 7 the coefficients for air content and w/c were highly significant when used together with other independent variables. Increases in both air content and w/c were associated with decrease in the dynamic modulus. The use of the commonly determined variables in eqs 4 and 6 resulted in a highly significant reduction in variance. The additional use of the trace elements Rb, Mn, and Cu in eqs 5 and 7 resulted in a reduction in variance significant at the 5.0-percent level in eq 7 but not in eq 5. (See table 13–57.)

In equations calculated for the "odds" and "evens" in the array of cement (eqs 5A, 5B, 7A, and 7B) there were instances where the coef./s.d. ratios of SO₃, Na₂O, K₂O, MgO, Rb, Mn, and Cu were less than 1.0 in one or the other or both of the equations for the smaller groups of cement.

Using the independent variables of eq 5 table 13–7 and the ranges of these variables, values were calculated for their contributions and ranges of contributions to the dynamic modulus after 14 days moist curing. These calculated values are presented in table 13–8. Increases of air content, w/c, C₄AF and Mn were associated with decreases of the dynamic modulus values. Increases of C₃S, SO₃, Na₂O, K₂O were associated with increases of the dynamic modulus. Of these variables, differences of air content, w/c, and C₃S showed the greatest calculated contribution.

6.2. Dynamic Modulus After 28 Days Drying

6.2.1. Dynamic Modulus of Series O Concretes

The frequency distribution of the dynamic modulus after 28 days drying for the Series O concretes is presented in table 13–9. The concrete specimens were moist cured for 14 days and then dried in laboratory air for 28 days. There was a broad distribution of results and an overlapping

of the values for the concretes made of the different types of cement.

Variables associated with the dynamic modulus after 28 days drying of the Series O concrete made of AE + NAE cements are presented in table 13–10. The use of the independent variables, air content, C₃A, C₃S, C₄AF, SO₃, Na₂O, APF, and MgO in eq 1 resulted in a highly significant reduction in variance. (See table 13–57.) As indicated in eq 2, Cu was the only trace element having a coef./s.d. ratio greater than 1.0 when used as an independent variable together with commonly determined variables. The reduction in variance was not significant at the 5.0-percent

Equations 2A and 2B indicate that C₃A, fineness, and Cu had coef./s.d. ratios of less than 1.0 in one of the equations for the smaller groups of cements.

level.

The use of SiO_2 , Al_2O_3 , and Fe_2O_3 together with other commonly determined variables in eq 3 resulted in a significant reduction in variance (See table 13–57) but the additional use of Cu in eq 4 did not result in a reduction of variance significant at the 5.0-percent level. In equations for the "odds" and "evens," 4A and 4B, the coef./s.d. ratios of Na_2O and Cu were less than 1.0 in one or the other of the equations for the smaller groups of cement.

A similar series of equations for the NAE cements is presented in table 13–11. The coefficients of the independent variables, the coef./s.d. ratios, and the S.D. values obtained were in reasonable agreement with the preceding table

where the AE cements were included.

Using the independent variables of eq 2, table 13–11, and the ranges of these variables, calculations were made of the estimated contributions and ranges of contributions to the dynamic modulus after 28 days drying for the Series O concretes. These calculated values are presented in table 13–12. It may be noted that an increase in C₃S and probably Na₂O was associated with an increase in dynamic modulus. Increases in air content, SO₃ and probably C₄AF and fineness were associated with a decrease in dynamic modulus. Of these independent variables, differences in air content, C₃S, and SO₃ showed the greatest calculated ranges of contribution to OD42.

6.2.2. Dynamic Modulus of Series A Concretes

The frequency distribution of the dynamic modulus after 28 days drying of the Series A concretes is presented in table 13–13. There was a broad distribution of values and an overlapping of the values obtained with the different types of cement. The concrete specimens were moist cured 14 days and then dried in laboratory air for 28 days.

Selected equations are presented in table 13–14 to indicate the independent variables associated with the dynamic modulus values. Equation 1 indicates the effect of air content, eq 2 the effect of the w/c, and eq 3 the effect of both of these vari-

Table 13-6. Coefficients for equations relating AD14, the dynamic Young's modulus NAE cements, to various

					,	1	1	
Eq. No.	Note	10 ⁶ psi	Const.	Air content	w/c	C ₃ S	C ₄ AF	CaO
1	1	AD14 s.d.	= +4.893 = (0.027)	-0.0648 (0.0092)				
2	1	AD14 s.d.	= +2.498 = (0.551)		+3.551 (0.864)			
3	1	AD14 s.d.	= +5.928 = (0.798)	$-0.0786 \ (0.0141)$	-1.580 (1.218)			
4	1	AD14 s.d.	= +8.044 = (0.615)	$-0.1451 \ (0.0111)$	-6.703 (0.931)	+0.0189 (0.0021)	-0.0291 (0.0064)	
5	1	AD14 s.d.	= +7.870 = (0.611)	$-0.1406 \ (0.0111)$	-6.435 (0.927)	+0.0190 (0.0021)	-0.0273 (0.0064)	
5A	2	AD14 (odd) s.d.	= +9.259 = (0.962)	$-0.1600 \\ (0.0157)$	-8.114 (1.486)	+0.0190 (0.0029)	-0.0453 (0.0096)	
5B	3	AD14 (even) s.d.	= +6.838 = (0.781)	-0.1248 (0.0162)	-5.275 (1.147)	+0.0212 (0.0030)	-0.0109 (0.0084)	
6	1	AD14 s.d.	= +9.244 = (1.336)	-0.1466 (0.0116)	-6.932 (1.007)			+0.0654 (0.0136)
7	1	AD14 s.d.	= +7.445 = (2.530)	-0.1427 (0.0116)	-6.689 (0.999)			+0.0830 (0.0268)
7A	2	AD14 (odd) s.d.	= +13.057 = (4.015)	-0.1654 (0.0164)	-8.823 (1.600)			*+0.0403 (0.0416)
7B	3	AD14 (even) s.d.	= +7.744 $= (3.583)$	-0.1259 (0.0170)	-5.350 (1.234)			+0.0776 (0.0378)

Note 1, 173 cements, Avg. = 4.762 \times 106 psi, S.D. = 0.2860 \times 106 psi. Note 2, 87 cements Nore 3, 86 cements

*Coef./s.d. ratio less than 1.

Table 13-7. Coefficients for equations relating AD14, the dynamic Young's modulus cements, to various

Eq. No.	Note	10 ⁶ psi	Const.	Air content	w/c	C ₃ S	C ₄ AF	CaO	SiO ₂
1	1	AD14 s.d.	= +4.786 = (0.0392)	*+0.0087 (0.0221)					
2	1	AD14 s.d.	= +5.218 = (0.657)		*-0.654 (1.024)				
3	1	AD14 s.d.	= +5.196 $= (0.817)$	*+0.0012 (0.0266)	*-0.622 (1.236)				
4	1	AD14 s.d.	= +7.930 = (0.659)	$^{-0.1196}_{\ (0.0213)}$	-6.619 (0.999)	+0.0189 (0.0022)	-0.0280 (0.0066)		
5	1	AD14 s.d.	= +7.784 = (0.652)	$-0.1149 \ (0.0215)$	-6.345 (0.990)	+0.0186 (0.0022)	$^{-0.0240}_{(0.0069)}$		
5A	2	AD14 (odd) s.d.	= +8.409 = (0.964)	-0.0889 (0.0332)	-6.821 (1.449)	+0.0160 (0.0031)	-0.0358 (0.0105)		
5B	2	AD14 (even) s.d.	= +7.375 = (0.828)	$-0.1492 \\ (0.0260)$	-6.169 (1.278)	+0.0229 (0.0030)	$-0.0134 \\ (0.0087)$		
6	1	AD14 s.d.	= +9.385 = (1.375)	$-0.1222 \ (0.0216)$	-6.987 (1.077)			$^{+0.0638}_{(0.0140)}$	-0.155 (0.022)
7	1	AD14 s.d.	= +9.991 = (1.396)	$-0.1173 \ (0.0217)$	-6.750 (1.604)			+0.0545 (0.0145)	-p.159 (0.022)
7A	2	AD14 (odd) s.d.	= +8.560 = (2.003)	-0.0877 (0.0331)	-7.243 (1.516)			+0.0667 (0.0214)	-0.126 (0.032)
7B	2	AD14 (even)	= +13.090 = (2.030)	-0.1416 (0.0273)	-6.034 (1.419)			+0.0318 (0.0195)	-0.226 (0.033)

Note 1, 162 cements, S.D. = 0.2466 x 10^6 psi Note 2, 81 cements

^{*}Coef./s.d. ratio less than one.

of elasticity in 10° psi after 14 days moist curing of Series A concretes made of AE + independent variables $\,$

SiO ₂	Al ₂ O ₃	Fe ₂ O ₃	SO ₃	Na ₂ O	K ₂ O	MgO	Rb	Mn	S.D.
									0.2529
									0.2736
									0.2524
			+0.208 (0.043)	+0.290 (0.080)	+0.303 (0.066)	+0.0159 (0.0121)			0.1698
			$^{+0.211}_{(0.042)}$	+0.270 (0.079)	+0.222 (0.073)	+0.0226 (0.0123)	+14.86 (7.68)	-0.185 (0.111)	0.1675
			$^{+0.114}_{(0.066)}$	*+0.061 (0.131)	+0.455 (0.111)	+0.0244 (0.0177)	*+5.86 (11.93)	*-0.116 (0.139)	0.1722
			$^{+0.255}_{(0.054)}$	+0.271 (0.100)	*-0.001 (0.099)	+0.0320 (0.0166)	+21.34 (9.65)	-0.282 (0.197)	0.1518
-0.153 (0.022)	-0.126 (0.025)	-0.126 (0.021)	$^{+0.134}_{(0.049)}$	+0.273 (0.081)	$^{+0.289}_{(0.074)}$				0.1706
-0.139 (0.028)	-0.111 (0.032)	-0.105 (0.030)	$^{+0.161}_{(0.058)}$	+0.266 (0.083)	+0.210 (0.081)	+0.0277 (0.0249)	+14.16 (7.78)	$-0.193 \\ (0.114)$	0.1683
-0.173 (0.042)	-0.125 (0.048)	-0.201 (0.049)	* -0.011 (0.097)	* ~0.018 (0.144)	$^{+0.394}_{(0.121)}$	*-0.0054 (0.0396)	*+1.42 (12.48)	$-0.152 \\ (0.143)$	0.1721
-0.170 (0.041)	-0.148 (0.044)	-0.070 (0.038)	$^{+0.181}_{(0.073)}$	+0.262 (0.107)	*-0.018 (0.117)	*+0.0252 (0.0327)	+21.71 (9.86)	-0.307 (0.218)	0.1538

of elasticity in 10° psi after 14 days moist curing of Series A concretes made of NAE independent variables

Al ₂ O ₃	Fe ₂ O ₃	SO ₃	Na ₂ O	K₂O	MgO	Rb	Mn	Cu	S.D.
									0.2472
									0.2470
									0.2478
		+0.225 (0.045)	+0.269 (0.082)	+0.273 (0.069)	+0.0151 (0.0124)				0.1701
		+0.227 (0.044)	+0.248 (0.082)	+0.173 (0.078)	+0.0207 (0.0126)	+12.59 (7.83)	-0.239 (0.118)	-2.11 (1.66)	0.1674
		+0.260 (0.065)	*+0.107 (0.134)	+0.124 (0.121)	*+0.0059 (0.0185)	*+6.67 (11.33)	-0.380 (0.157)	-6.56 (2.54)	0.1762
		+0.187 (0.057)	+0.316 (0.095)	*+0.037 (0.100)	+0.0652 (0.0172)	+29.53 (10.32)	*-0.067 (0.167)	*+0.64 (2.02)	0.1422
-0.123 (0.026)	-0.125 (0.022)	+0.148 (0.050)	+0.248 (0.084)	+0.245 (0.078)					0.1704
-0.125 (0.026)	-0.118 (0.022)	+0.140 (0.050)	+0.218 (0.084)	+0.135 (0.086)		+11.41 (7.90)	-0.267 (0.121)	-2.14 (1.66)	0.1676
-0.083 (0.035)	-0.127 (0.035)	+0.201 (0.077)	*+0.089 (0.138)	*+0.085 (0.130)		*+3.93 (11.62)	-0.420 (0.160)	-6.30 (2.55)	0.1762
-0.207 (0.039)	-0.120 (0.028)	*+0.034 (0.069)	+0.272 (0.101)	*+0.019 (0.115)		+27.55 (10.64)	*-0.161 (0.184)	*-0.01 (2.09)	0.1465

Table 13-8. Calculated contributions of independent variables to AD14, the 14-day dynamic modulus of Series A concretes

Inde- pendent variable	Range of variables (percent)	Coefficients from eq 5 table 13-7	Calculated contributions to AD14	Calculated range of contribu- tions to AD14
Air- content, NAE cements_w/c. C ₃ S. C ₄ AF. SO ₃ . Na ₂ O. K ₃ O. MgO* Rb* Mn. Cu*	0 to 4.5 0.6 to 0.7 20 to 65 1 to 16 1.2 to 3.0 0 to 0.7 0 to 1.1 0 to 5 0 to 0.01 0 to 1.0 0 to 0.05	$\begin{array}{c} -0.1149 \\ -6.345 \\ +0.0186 \\ -0.0240 \\ +0.227 \\ +0.248 \\ +0.173 \\ +0.0207 \\ +12.59 \\ -0.239 \\ -0.211 \end{array}$	$\begin{array}{c} \text{Const.} = +7.78 \\ \hline & 0 \text{ to } -0.52 \\ -3.81 \text{ to } -4.44 \\ +0.37 \text{ to } +1.20 \\ -0.02 \text{ to } -0.38 \\ +0.27 \text{ to } +0.68 \\ 0.57 \text{ to } +0.19 \\ 0 \text{ to } +0.19 \\ 0 \text{ to } +0.10 \\ 0 \text{ to } +0.13 \\ 0 \text{ to } -0.24 \\ 0 \text{ to } -0.04 \end{array}$	0.52 0.63 0.83 0.36 0.41 0.17 0.19 0.10 0.13 0.24

^{*}Coefficient of doubtful significance as coef./s.d. ratio was less than 2.

ables. The sign of the coefficient for w/c was positive in eq 2 and negative in eq 3 and not highly significant. In eq 4, where other commonly determined variables were included, the coefficients for both air content and w/c were negative and highly significant. The use of the independent variables in eqs 1, 2, or 3 resulted in a significant reduction in the S.D. value. (See table 13–57.) With the additional use of the trace elements Cu, Li, and Zr in eq 4, the reduction in variance was significant at the 5.0-percent level.

Equations 5A and 5B calculated for the "odds" and "evens" in the array of cements indicated that C₃A, C₄AF, fineness, Loss, Cu, Li, and Zr had coef./s.d. valyes less than 1.0 in one or both of the equations calculated for the smaller groups of cement.

The use of SiO₂, Al₂O₃, and Fe₂O₃ in eq 6 instead of the potential compounds but with other commonly determined variables resulted in an S.D. value similar to that of eq 4. The variables Loss and Zr had coef./s.d. ratios less than 1.0 in eq 6. The use of the trace elements Cu and Li in addition to the commonly determined variables resulted in a reduction in variance significant at the 5.0-percent level. (See table 13–57.)

Equations calculated for the dynamic modulus

after 28 days drying of the Series A concretes made with the NAE cements are presented in table 13-15. In eqs 1, 2, and 3 the air content and w/c were not significant when used as independent variables. However, in eqs 4 through 7, where other commonly determined variables were included, the coefficients were highly significant for both air content and w/c. The use of the commonly determined variables in eq 4 resulted in a highly significant reduction in variance, but with the added trace elements Cu, Li, and Zr in eq 6 the reduction in variance was significant at the 5.0-percent level. (See table 13-57.)

Calculations made for the "odds" and "evens" in the array of cements are presented in eqs 5A and 5B. There were instances where the independent variables MgO, fineness, Loss, Cu, Li, and Zr had coef./s.d. ratios of less than 1.0 in one or the other of the equations for the smaller

groups of cement.

With the use of SiO₂, Al₂O₃, and Fe₂O₃ instead of the potential compounds but with the other commonly determined variables, there was a highly significant reduction in variance. The independent variables, Loss and Zr, had coef./s.d. ratios less than 1.0. The use of Cu and Li together with commonly determined variables in eq 7 resulted in a reduction in variance significant at the 5.0-percent level.

Equations calculated for the "odds" and "evens" in the array of cements indicated that MgO, Cu, and Li had coef./s.d. values of less than 1.0 in one or the other of the smaller groups of cement.

Using the independent variables of eq 5, table 13–15, and the ranges of these variables, calculations were made of the estimated contributions to the dynamic-modulus values. These calculated values together with the calculated ranges of values are presented in table 13–16. Increase in C₃S, SO₃ and possibly MgO was associated with higher dynamic-modulus values. Increases in air content, w/c and possibly C₄AF, fineness, and Cu were associated with decreases in the dynamic-modulus values. Differences in air content, w/c, C₃S, and SO₃ showed the greatest calculated range of contributions to AD42.

Table 13-9. Frequency distribution of cements with respect to OD42, the dynamic modulus of elasticity of Series O concretes at 42 days after 14 days moist curing and the storage in air for 28 days

					Dynamic	modulus	of elastici	ty, 10 ⁶ psi				
Type cement	3.2 to 3.4	3.4 to 3.6	3.6 to 3.8	3.8 to 4.0	4.0 to 4.2	4.2 to 4.4	4.4 to 4.6	4.6 to 4.8	4.8 to 5.0	5.0 to 5.2	5.2 to 5.4	Total
						Number o	of cements	3				
<u> </u>					2	7	13	33	20	6	1	82
IAII IIIIA	2	1 1	2	2 1	1 5 1	12	18	14	13	4		68 3
III					2		î	6	5	5	3	20
IV, V		1	1		2	3	6		2			15
Total	2	4	3	3	13	22	39	54	40	15	4	199

Table 13-10. Coefficients for equations relating OD42, the dynamic Young's modulus of elasticity in 10° psi after 14 days moist curing then 28 days drying in laboratory air of Series O concretes made of AE + NAE cements, to various independent variables

Eq.	Note	10¢ psi	Const.	Air	C3A	C3S	C4AF	SiO2	Al ₂ O ₃	Fe2O3	SO3	Na ₂ O	APF	MgO	Cu	S.D.
	1	OD42 s.d.	= +3.634 = (0.181)	-0.1551 (0.0079)	-0.0074 (0.0058)	+0.0171 (0.0023)	-0.0251				+0.515 (0.049)	+0.194 (0.084)	-0.000103 (0.000033)	+0.0287		0.1789
	1	OD42 s.d.	= +3.665 = (0.180)	-0.1549 (0.0078)	(0.0058)	+0.0168 (0.0023)	(0.0076)		1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	+0.507	+0.210 (0.083)	(0.000093)	+0.0246 (0.0121)	-3.284 (1.662)	0.1774
1	61	OD42 (odd) s.d.	= +3.942 = (0.237)	-0.1447 (0.0099)	(0.0086)	+0.0149 (0.0030)	(0.0109)				+0.470 (0.073)	+0.148 (0.111)	-0.000126 (0.000043)	+0.0204 (0.0166)	-5.310 (2.490)	0.1749
1	m	OD42 (even) s.d.	= +3.292 = (0.287)	-0.1715 (0.0125)	* -0.0044 (0.0078)	+0.0196 (0.0038)	-0.0253				+0.499 (0.069)	+0.287 (0.131)	(0.000053)	+0.0348	(2.274)	0.1793
-	1	OD42 s.d.	= +10.51 = (0.80)	(0.0077)	1 1			-0.1969 (0.0254)	-0.2073 (0.0293)	-0.1538 (0.0194)	+0.371 (0.051)	+0.149 (0.892)	-0.000120 (0.000033)	(0.0129)		0.1763
1	1	OD42 s.d.	= +10.42 = (0.80)	(0.0077)	1 1	1 1	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	-0.1933 (0.0253)	-0.2068 (0.0290)	-0.1429 (0.0202)	+0.366 (0.051)	+0.164 (0.082)	-0.000116 (0.000033)	-0.0390 (0.0129)	-3.022	0.1751
1	61	OD42 (odd) s.d.	= +10.04 = (1.09)	-0.1454 (0.0098)	1 1		1 1	-0.1738 (0.0334)	-0.1926 (0.0411)	-0.1307 (0.0304)	+0.324 (0.074)	+0.107	-0.000136 (0.000043)	-0.0373 (0.0183)	-5.104 (2.463)	0.1728
	ಣ	OD42 (even) s.d.	= +10.98 = (1.24)	(0.0123)		1 1		-0.2197 (0.0401)	-0.2228 (0.0428)	-0.1630 (0.0279)	+0.366 (0.072)	+0.225 (0.129)	-0.000071 (0.000054)	(0.0186)	*-0.909	0.1772
			_	_				-	_	_	-					

*Coef./s.d. ratio less than one.

Note 1, 179 cements, Avg. = 4.567 \times 10¢ psi, S.D. = 0.3584 \times 10¢ psi Note 2, 90 cements Note 3, 89 cements

Table 13-11. Coefficients for equations relating OD42, the dynamic Young's modulus of elasticity in 10° psi after 14 days moist curing, then 28 days drying in laboratory air of Series O concretes made of NAE cements, to various independent variables

	S.D.	0.1761	0.1747	0.1848	0.1659	0.1743	0.1731	0.1816	0.1699
	Cu		-3.195	*-2.314 (2.578)	*-1.545	1 0 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	(1.663)	* -2.380 (2.533)	*-1.281
	MgO	+0.0269	+0.0228 (0.0121)	*+0.0045 (0.0192)	+0.0441 (0.0169)	-0.0411 (0.0130)	-0.0436 (0.0130)	(0.0205)	(0.0183)
	APF	-0.000119 (0.000033)	-0.000115 (0.000033)	-0.000145 (0.000047)	-0.000090 (0.000051)	$\begin{array}{c} -0.000133 \\ (0.000034) \end{array}$	(0,000034)	-0.000151 (0.000046)	-0.000117 (0.000054)
san	Na ₂ O	+0.204 (0.085)	+0.214 (0.084)	$^* + 0.120$ (0.121)	+0.359 (0.131)	+0.158 (0.083)	+0.168 (0.083)	$^*+0.101$ (0.119)	+0.269 (0.131)
ent varian	SO3	+0.543	+0.534 (0.049)	+0.553 (0.083)	+0.521 (0.065)	+0.393 (0.051)	+0.387 (0.051)	+0.397 (0.083)	+0.360
nuadanuı	Fe ₂ O ₃					-0.1513 (0.0195)	-0.1395 (0.0205)	-0.1514 (0.0306)	-0.1353 (0.0297)
to various	Al ₂ O ₃			1 1		(0.0296)	-0.2167 (0.0295)	-0.2005 (0.0435)	$\begin{bmatrix} -0.2482\\ (0.0431) \end{bmatrix}$
cements,	SiO_2		1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1			-0.2046 (0.0258)	-0.2008 (0.0257)	-0.1790 (0.0349)	-0.2500 (0.0420)
air of series O concretes made of NAL cements, to various independent variables	CAF	(0.0076)	(0.0077)	(0.0114)	*-0.0072 (0.0115)				
cretes man	C ₃ S	+0.0181 (0.0024)	+0.0178 (0.0024)	+0.0151 (0.0032)	+0.0247 (0.0039)	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1		; 1 ; 1 ; 1 ; 1 ; 1 ; 1 ; 1 ; 1 ; 1
res O con	C3A	-0.0086 (0.0058)	(0.0058)	-0.0116 (0.0092)	* -0.0037			1 1	
arr of De	Air	-0.1597 (0.0192)	-0.1525 (0.0194)	-0.1546 (0.0291)	-0.1570 (0.0236)	(0.0189)	-0.1542 (0.0192)	-0.1562 (0.0286)	-0.1576 (0.0270)
	Const.	= +3.59	= +3.61 = (0.19)	= +3.97 = (0.26)	= +2.94 = (0.30)	= +10.75 = (0.81)	= +10.64 = (0.81)	= +10.19 $= (1.12)$	= +11.84 = (1.29)
	10 ⁶ psi	OD42 s.d.	OD42 s.d.	OD42 (odd) s.d.	OD42 (even) s.d.	OD42 s.d.	OD42 s.d.	OD42 (odd) s.d.	OD42 (even) s.d.
	Note	П	-	61	60	-	-	61	m
	Kg.	1	2	2A	2B	8	4	4A	4B

*Coef./s.d. ratio less than one.

Note 1, 167 cements, Avg. = 4.624×10^6 psi, S.D. = 0.2882×10^6 psi Note 2, 84 cements Note 3, 83 cements

Table 13-12. Calculated contributions of independent variables to OD42, the dynamic modulus after 14 days moist curing followed by 28 days in laboratory air of Series O

Inde- pendent variable	Range of variables (percent)	Coefficients from eq 2 table 13–11	Calculated contributions to OD42	Calculated range of contribu- tions to OD42
Air- content,			Const. = +3.61	
NAE cements_ C ₃ A** C ₃ S	0 to 4.5 1 to 15 20 to 65	$ \begin{array}{r} -0.1525 \\ -0.010 \\ +0.0178 \end{array} $	0 to -0.69 -0.01 to -0.15 +0.35 to +1.16	0.69 0.14 0.81
C ₄ AF	1 to 16 1.2 to 3.0 0 to 0.7 *2500 to 5500	$ \begin{array}{r} -0.0206 \\ -0.534 \\ +0.214 \\ -0.000115 \end{array} $	$ \begin{array}{r} -0.02 \text{ to } -0.32 \\ -0.64 \text{ to } -1.60 \\ 0 \text{ to } +0.15 \\ -0.29 \text{ to } -0.63 \end{array} $	$0.30 \\ 0.96 \\ 0.15 \\ 0.34$
MgO** Cu**	0 to 5.0 0 to 0.05	$^{+0.0228}_{-3.195}$	$\begin{array}{c} 0 \text{ to } +0.11 \\ 0 \text{ to } -0.16 \end{array}$	0.11 0.16

^{*}cm²/g. **Coefficient of doubtful significance as the coef./s.d. ratio was less than 2

6.3. Dynamic Modulus After 56 Days Drying

6.3.1. Dynamic Modulus of Series O Concretes

The frequency distribution of the dynamic modulus of Series O concretes after 56 days drying is presented in table 13-17. The concrete specimens had been moist-cured for 14 days then dried in laboratory air for 8 weeks. There was a broad distribution of values and an overlapping of values obtained with the different types of cements.

Equations are presented in table 13-18 indicating the variables associated with the dynamic modulus of the air-dried Series O concretes made with AE + NAE cements. Commonly determined variables having a coef./s.d. ratio greater than 1.0 when used in the multivariable equation (eq 1) resulted in a highly significant reduction in variance. (See table 13-57.) The only trace element

Table 13-13. Frequency distribution of cements with respect to AD42, the dynamic modulus of elasticity of Series A concretes at 42 days (moist curing 14 days and then drying in laboratory air for 28 days)

					Dynamic	modulus	of elastici	ty, 10 ⁶ psi				
Type cement	3.4 to 3.6	3.6 to 3.8	3.8 to 4.0	4.0 to 4.2	4.2 to 4.4	4.4 to 4.6	4.6 to 4.8	4.8 to 5.0	5.0 to 5.2	5.2 to 5.4	5.4 to 5.6	Total
						Number o	of cements	3				
[1	$\frac{1}{2}$	9	23 3	29	12	1	3		79
I			2	6	13	13	16	12	5			67
IIA	1					2 2	6	5	6		1	79 8 67 3 20 3 15
IIIA [V, V		2		<u>2</u>	5	1 2	$\frac{2}{2}$	2				15
Total	2	2	4	11	28	46	55	31	12	3	1	195

Table 13-14. Coefficients for equations relating AD42, the dynamic Young's modulus ratory air of Series A concretes made of AE +

							-		
Eq. No.	Note	10 ⁶ psi	Const.	Air content	w/c	C ₃ A	C ₃ S	C ₄ AF	SiO ₂
1	1	AD42 s.d.	= +4.675 = (0.030)	-0.0499 (0.0103)					
2	1	AD42 s.d.	= +2.911 = (0.592)		$^{+2.609}_{(0.928)}$				
3	1	AD42 s.d.	= +5.644 = (0.892)	-0.0631 (0.0158)	-1.511 (1.360)				
4	1	AD42 s.d.	= +7.961 = (0.721)	$-0.1281 \ (0.0132)$	-6.879 (1.134)	-0.0118 (0.0067)	+0.0174 (0.0026)	-0.0247 (0.0084)	
5	1	AD42 s.d.	= +7.766 = (0.715)	$-0.1260 \\ (0.0130)$	$ \begin{array}{c} -6.649 \\ (1.121) \end{array} $	-0.0102 (0.0068)	+0.0173 (0.0026)	-0.0193 (0.0085)	
5A	2	AD42 (odd) s.d.	= +9.511 $= (1.166)$	-0.1480 (0.0190)	-8.753 (1.868)	*-0.0088 (0.0104)	+0.0149 (0.0037)	-0.0340 (0.0127)	
5B	3	AD42 (even) s.d.	= +5.855 = (0.957)	$-0.0993 \\ (0.0198)$	-4.415 (1.456)	-0.0113 (0.0098)	+0.0211 (0.0037)	*-0.0075 (0.0130)	
6	1	AD42 s.d.	= +15.23 = (1.15)	-0.1289 (0.0129)	$-6.780 \ (1.114)$				-0.212 (0.028)
7	1	AD42 s.d.	= +14.89 = (1.14)	$-0.1264 \\ (0.0128)$	-6.523 (1.102)				-0.207 (0.028)
7A	2	AD42 (odd) s.d.	= +16.29 = (1.69)	$-0.1498 \\ (0.0185)$	$-8.768 \ (1.821)$				-0.197 (0.040)
7B	3	AD42 (even) s.d.	= +13.89 = (1.61)	$-0.1009 \\ (0.0196)$	-4.212 (1.432)		2		-0.232 (0.041)

Note 1, 173 cements, Avg. = 4.574 \times 106 psi, S.D. = 0.2999 \times 106 psi Note 2, 87 cements Note 3, 86 cements

^{*}Coef./s.d. ratio less than 1.

having a coef./s.d. ratio greater than 1.0 when used with other commonly determined variables was vanadium. The additional use of V in eq 2 did not result in a significant reduction in variance. Equations 2A and 2B calculated for the "odds" and "evens" in the array of cements indicated that K_2O as well as V had coef./s.d. ratios less than 1.0 in one or both of the smaller groups of cement.

Equations 3 and 4, calculated using the major oxides instead of the potential compounds, resulted in approximately the same S.D. values. The coef./s.d. ratio for K_2O was less than 1.0, and that for Loss in eq 4B was less than 1.0. The average value for the dynamic modulus after 8 weeks drying was 4.43×10^6 psi, after 4 weeks drying it was 4.57×10^6 psi, and after 14 days moist curing before the drying cycle, the average value was 4.75×10^6 psi. (See tables 13–18, 13–10, and 13–2.)

A similar set of equations for the Series O concretes made with NAE cements is presented in table 13-19. The use of the commonly determined variables, air content, C₃A, C₃S, C₄AF, SO₃, K₂O, fineness, Loss, and MgO in eq 1 resulted in a highly significant reduction in variance. The use of V in eqs 2 or 4 in addition to other commonly determined variables did not result in a reduction in variance significant at the 0.05 probability level. The coefficient for the air content of the NAE cements was highly significant, but the coef./s.d. ratio was somewhat smaller than when the AE cements were included as in the previous table.

Using the coefficients of the independent variables of eq 2 of table 13-19 as well as their ranges

of values, calculations were made of their estimated contribution to the dynamic modulus after 56 days drying and the calculated ranges of these contributions. These calculated values are presented in table 13–20. Increases of C₃S, SO₃ and possibly loss on ignition and MgO were associated with increases in dynamic modulus values. Higher values for air content, C₃A, C₄AF, and fineness were associated with lower values for dynamic modulus.

6.3.2. Dynamic Modulus of Series A Concretes

The frequency distribution of the dynamic modulus of the air-dried Series A concretes is presented in table 13–21. The use of a 5 \pm 1-in slump rather than a constant water/cement ratio resulted in slightly higher values for the AE cements (types IA, IIA, and IIIA) than was observed in table 13–17. There was a broad distribution of values and an overlapping of the values obtained with the different types of cement.

Equations are presented in table 13–22 indicating the variables associated with the dynamic modulus of the Series A concretes made of AE + NAE cements. Equations 1, 2, 3, and 4 show that using the air content and the water/cement ratio, singly or together, and with other commonly determined variables, resulted in differences in the values for the coefficients as well as in their coef./s.d. ratios. Whereas the coefficient for w/c was positive in eq 2, it was negative in eqs 4 through 7. As indicated in table 13–57, the reduction in vari-

of elasticity in 10⁶ psi after 14 days moist curing followed by 28 days drying in labo-NAE cements, to various independent variables

		independent		1	1				
Al ₂ O ₃	Fe ₂ O ₃	SO ₃	MgO	APF	Loss	Cu	Li	Zr	S.D.
									0.2821
									0.2940
									0.2819
		+0.517 (0.056)	+0.0421 (0.0133)	-0.000120 (0.000038)	+0.0629 (0.0314)				0.1944
		+0.508 (0.056)	$^{+0.0348}_{(0.0138)}$	-0.000104 (0.000038)	+0.0452 (0.0319)	-4.41 (1.89)	+9.11 (4.64)	+0.381 (0.372)	0.1914
		+0.503 (0.086)	+0.0350 (0.0203)	-0.000145 (0.000054)	+0.0751 (0.0491)	-5.33 (2.83)	*+6.92 (7.53)	*+0.313 (0.424)	0.1984
		+0.439 (0.081)	+0.0429 (0.0197)	*-0.000020 (0.000062)	*-0.0180 (0.0465)	* -2.95 (2.99)	*+6.33 (6.78)	*+0.115 (0.982)	0.1834
-0.234 (0.033)	-0.152 (0.022)	+0.379 (0.057)	-0.0277 (0.0143)	-0.000119 (0.000037)					0.1913
-0.227 (0.033)	-0.136 (0.023)	+0.365 (0.056)	-0.0352 (0.0144)	-0.000109 (0.000036)		-4.33 (1.86)	+8.34 (4.50)		0.1885
-0.215 (0.048)	-0.173 (0.035)	+0.388 (0.082)	-0.0334 (0.0202)	-0.000148 (0.000051)		-5.81 (2.73)	*+7.05 (7.12)		0.1935
-0.257 (0.047)	-0.111 (0.032)	+0.283 (0.082)	-0.0322 (0.0203)	*-0.000037 (0.000057)		* -2.85 (2.96)	*+5.85 (6.65)		0.1817

Eq. No.	Note	10 ⁶ psi	Const.	Air content	w/c	C ₈ A	C ₃ S	C ₄ AF	SiO ₂
1	1	AD42 s.d.	= +4.621 = (0.044)	*-0.0153 (0.0249)					
2	1	AD42 s.d.	= +4.742 = (0.741)		*-0.226 (1.155)				
3	1	AD42 s.d.	= +5.212 = (0.919)	*-0.0260 (0.0300)	*-0.895 (1.391)				
4	1	AD42 s.d.	= +7.983 = (0.766)	-0.1270 (0.0239)	-6.905 (1.202)	-0.0127 (0.0068)	+0.0172 (0.0026)	-0.0263 (0.0084)	
5	1	AD42 s.d.	= +7.756 = (0.756)	-0.1231 (0.0240)	-6.645 (1.186)	-0.0111 (0.0069)	+0.0170 (0.0026)	-0.0206 (0.0085)	
5A	2	AD42 (odd) s.d.	= +8.503 = (1.080)	$-0.1195 \ (0.0371)$	-7.462 (1.703)	-0.0164 (0.0116)	+0.0152 (0.0038)	-0.0408 (0.0145)	
5B	2	AD42 (even) s.d.	= +6.899 = (1.084)	-0.1378 (0.0330)	-5.382 (1.688)	-0.0144 (0.0089)	$^{+0.0183}_{(0.0039)}$	-0.0129 (0.0110)	
6	1	AD42 s.d.	= +15.07 = (1.19)	-0.1323 (0.0235)	-6.898 (1.186)				-0.205 (0.029)
7	1	AD42 s.d.	= +14.71 = (1.18)	-0.1286 (0.0236)	-6.624 (1.173)				-0.199 (0.028)
7A	2	AD42 (odd) s.d.	= +15.17 = (1.63)	-0.1263 (0.0359)	-7.542 (1.662)				-0.190 (0.040)
7B	2	AD42 (even) s.d.	= +14.33 = (1.79)	-0.0388 (0.0323)	-5.286 (1.660)				-0.214 (0.044)

Note 1, 162 cements, Avg. = 4.598 \times 10 psi, S.D. = 0.2777 \times 10 psi Note 2, 81 cements

Table 13-16. Calculated contributions of independent variables to AD42, the dynamic modulus after 14 days moist curing followed by 28 days in laboratory air of Series A

Inde- pendent variable	Range of variables (percent)	Coefficients from eq 5 table 13-15	Calculated contributions to AD42	Calculated range of contribu- tions to AD42
Air- content.			Const. = $+7.756$	
NAE cements_w/cC3A**_C3SC4AF_SO3MgO	0 to 4.5 0.6 to 0.7 1 to 15 20 to 65 1 to 17 1.2 to 3.0 0 to 5.0	$\begin{array}{c} -0.1231 \\ -6.645 \\ -0.0111 \\ +0.0170 \\ -0.0206 \\ +0.513 \\ +0.0344 \end{array}$	0 to -0.55 -3.99 to -4.65 -0.01 to -0.16 +0.34 to +1.11 -0.02 to -0.35 +0.62 to +1.54 0 to +0.17	0.55 0.66 0.15 0.77 0.33 0.92 0.17
APF Loss** Cu Li**_ Zr**	*2500 to 5500 0.3 to 3.3 0 to 0.05 0 to 0.02 0 to 0.5	$ \begin{array}{r} -0.000093 \\ +0.0340 \\ -4.41 \\ +9.20 \\ +0.468 \end{array} $	-0.23 to -0.51 +0.01 to +0.11 0 to -0.22 0 to +0.18 0 to +0.23	0.28 0.10 0.22 0.18 0.23

*cm 2 /g. **Coefficient of doubtful significance as coef./s.d. ration was less than 2.

ance was highly significant for each of the first four equations. The use of Li (the only trace element with a coef./s.d. ratio greater than 1.0) in eqs 5 and 7 together with the commonly determined variables did not result in a significant reduction in variance.

In equations calculated for the "odds" and "evens," eqs 5A, 5B, 7A, and 7B, there were instances where the coef./s.d. ratios of K₂O, fineness, and Li were less than 1.0 in one or both of the equations for the smaller groups of cements. The coef./s.d. ratio for Loss was less than 1.0 when included in equations calculated using the oxides (eqs 6 and 7) rather than the potential compounds as in eqs 4 and 5.

A similar series of equations is presented in table 13-23 for the NAE cements. Equations 2 and 3 of this table do not indicate a relationship to the water/cement ratio. However, when w/c was included with other commonly determined variables as in eqs 4 and 6, its coefficient was highly significant. The relationship of various independent variables to the water requirements of pastes, mortars, and concrete was discussed in part 1, section 2 of this series of articles [16]. The use of the commonly determined variables, air content, w/c, C₃A, C₃S, C₄AF, SO₃, K₂O, APF, Loss, and MgO in eq 4 resulted in a highly significant reduction of variance. (See table 13–57.) The only trace element that had a coef./s.d. ratio greater than 1.0 when used with the commonly determined variables was Li. The use of Li in egs 5 and 7 did not result in a reduction of variance significant at the 5.0-percent level.

There were instances in equations calculated for the "odds" and "evens" (eqs 5A, 5B, 7A, and 7B) where the coef./s.d. ratios for fineness, MgO, and Li were less than 1.0 in one or the other of the pairs of equations calculated for the smaller groups of cements.

Using the coefficients of the independent variables of eq 5 of table 13-23 as well as their ranges of values, calculations were made of their estimated contributions to the dynamic modulus after 56 days drying and the calculated ranges of these

^{*}Coef./s.d. ratio less than one.

Al ₂ O ₃	Fe ₂ O ₃	SO_3	MgO	APF	Less	Cu	Li	Zr	S.D.
									0.2783
					^				0.2786
									0.2788
		+0.521 (0.056)	+0.0415 (0.0134)	-0.000110 (0.000039)	+0.0534 (0.0318)				0.1913
		+0.513 (0.056)	+0.0344 (0.0139)	-0.000093 (0.000038)	+0.0340 (0.0322)	-4.41 (1.88)	+9.20 (4.62)	+0.468 (0.367)	0.1877
		+0.526 (0.088)	*+0.0096 (0.0220)	*-0.000061 (0.000066)	+0.0699 (0.0632)	-7.87 (2.86)	* +7.34 (7.78)	*+2.514 (3.030)	0.1984
		$^{+0.490}_{(0.081)}$	+0.0635 (0.0188)	-0.000114 (0.000048)	*+0.0275 (0.0394)	*-1.35 (2.79)	+6.93 (6.72)	+0.478 (0.357)	0.1737
-0.229 (0.033)	-0.153 (0.022)	+0.387 (0.057)	$-0.0262 \\ (0.0143)$	-0.000109 (0.000037)					0.1890
-0.221 (0.033)	-0.137 (0.023)	+0.373 (0.057)	-0.0338 (0.0144)	-0.000100 (0.000037)		-4.27 (1.86)	+8.39 (4.51)		0.1860
-0.222 (0.043)	-0.183 (0.037)	+0.400 (0.087)	-0.0563 (0.0228)	-0.000063 (0.000061)		-8.07 (2.78)	* +6.77 (7.06)		0.1954
-0.247 (0.053)	-0.111 (0.031)	$^{+0.324}_{(0.083)}$	* -0.0110 (0.0191)	-0.000120 (0.000046)		*-1.71 (2.74)	+7.91 (6.63)		0.1717

Table 13-17. Frequency distribution of cements with respect to OD70, the dynamic modulus of elasticity of Series O concretes at 70 days (14 days moist curing and then storage in laboratory air for 8 weeks)

					Dynamic	modulus	of elastici	ty, 10 ⁶ psi				
Type cement	3.2 to 3.4	3.4 to 3.6	3.6 to 3.8	3.8 to 4.0	4.0 to 4.2	4.2 to 4.4	4.4 to 4.6	4.6 to 4.8	4.8 to 5.0	5.0 to 5.2	5.2 to 5.4	Total
						Number o	of cements					
Ä	3	1	3	2	9	15	31	10	12	3		82 8
IA	1 1			6	4	21 1	15	10	10	1		68
II			- 			1	3	4	4	5	3	20 3
V, V		2		î	2	4	4	1	1			15
Total	5	3	3	12	16	42	54	25	27	9	3	199

contributions. These calculated values are presented in table 33–24. Higher values for air content, w/c, C₃A, and C₄AF were associated with lower values for dynamic modulus. Higher values for C₃S, SO₃, and probably K₂O, Loss, and MgO were associated with higher values for dynamic modulus of the air-dried concrete.

6.4. Dynamic Modulus After 28 Days Resoaking

6.4.1. Dynamic Modulus of Series O Concretes

After 14 days moist-air curing, then 8 weeks drying in laboratory air, the concrete specimens were placed in water and the dynamic modulus was again determined after 28 days of soaking.

The frequency distribution of dynamic modulus after 28 days resoaking of the Series O concretes is presented in table 13–25.

There was a fairly broad distribution of values for the concretes made of NAE cements and an overlapping of the values for the cements of the different types.

A series of equations is presented in table 13–26 to indicate the independent variables found to have coef./s.d. ratios greater than 1.0 and their relation to the values for dynamic modulus after 28 days resoaking. The use of the commonly determined variables, air content, C₃A, C₃S, C₄AF, SO₃, APF, and Loss in eq 1 resulted in a highly significant reduction in variance. (See table 13–57.) The additional use of the trace elements Ba, Cu, and Zr in eq 2 resulted in a further significant reduction in variance. In equations calculated for the "odds" and "evens" in the array of cements (eqs 2A and 2B) there were instances where APF, Loss, Cu, and Zr had coef./s.d. ratios of less than 1.0 in one or the other of the equations for the smaller groups of cements.

Table 13-18. Coefficients for equations relating OD70, the dynamic Young's modulus of elasticity in 10° psi after 14 days moist curing, then 56 days drying in laboratory air of Series O concretes made of AE + NAE cements, to various independent variables

					1							-					
Eq. No.	Note	106 psi	Const.	Air	C3A	CaS	CAF	SiO2	Al ₂ O ₃	Fe ₂ O ₃	SO3	K20	APF	Loss	MgO	>	S.D.
1	1	OD70 s.d.	= +3.449 = (0.179)	-0.1569 (0.0079)	-0.0234 (0.0060)	+0.0183 (0.0023)	0.0290 (0.0077)				+0.539	+0.106 (0.076)	$\begin{array}{c} -0.000118 \\ (0.000036) \end{array}$	+0.120 (0.028)	+0.0339	1 1	0.1798
2	1	OD70 s.d.	= +3.523 = (0.190)	-0.1567 (0.0079)	-0.0256 (0.0063)	+0.0181 (0.0023)	(0.0078)	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	+0.551 (0.053)	+0.102 (0.076)	-0.000128 (0.000037)	+0.116 (0.028)	+0.0308 (0.0128)	(0.871)	0.1796
2A	63	OD70 (odd) s.d.	= +3.864 = (0.263)	-0.1469 (0.0104)	-0.0297 (0.0094)	$^{+0.0171}_{(0.0031)}$	(0.0114)		1 1	1 1	+0.438 (0.084)	+0.268 (0.117)	-0.000140 (0.000052)	+0.122 (0.043)	+0.0209 (0.0186)	*-1.061	0.1813
2B	ಣ	OD70 (even).	= +3.121 = (0.280)	-0.1742 (0.0120)	-0.0196 (0.0082)	+0.0202 (0.0036)	(0.0109)	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	1 1	+0.589	* -0.042 (0.099)	-0.000074 (0.000055)	+0.112 (0.040)	+0.0456 (0.0179)	*-0.987	0.1720
3-	1	OD70 s.d.	= +10.89 = (0.87)	(0.0079)			1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	-0.215 (0.028)	-0.260 (0.031)	-0.148 (0.020)	+0.423	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	-0.000122 (0.000035)	+0.0471 (0.0303)	(0.0135)	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	0.1807
4	1	OD70 s.d.	= +10.90 $= (0.87)$	(0.0078)				-0.213 (0.028)	-0.264 (0.031)	-0.147 (0.020)	+0.436	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	-0.000131 (0.000035)	+0.0436 (0.0304)	-0.0354 (0.0137)	(0.875)	0.1805
4A	61	OD70 (odd) s.d.	= +10.68	(0.0105)			1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	-0.196 (0.039)	-0.250 (0.046)	-0.150 (0.032)	+0.375	1 1	-0.000171 (0.000049)	+0.0641 (0.0465)	+0.0334 (0.0205)	*-1.325	0.1875
4B	က	OD70 (even) s.d.	= +11.41 = (1.28)	(0.0118)				(0.042)	(0.044)	-0.152 (0.027)	+0.440 (0.071)		(0.000065)	*+0.0281 (0.0420)	-0.0334 (0.0183)	*-0.804	0.1707

*Coef./s.d. ratio less than one.

S.D. = 0.3819×10^6 psi Note 1, 179 cements, Avg. = 4.425×10^6 psi Note 2, 90 cements Note 3, 89 cements Table 13-19. Coefficients for equations relating OD70, the dynamic Young's modulus of elasticity in 10° psi after 14 days moist curing, then 56 days drying in laboratory air of Series O concretes made of NAE cements. to parious independent variables

	S.D.	0.1795	0.1793	0.1867	0.1724	0.1804	0.1802	0.1889	0.1717
	Λ		-1.035 (0.893)	*-0.933	$\frac{-1.285}{(1.220)}$		-1.062 (0.895)	*-0.060	-1.152 (1.202)
	MgO	+0.0308 (0.0128)	+0.0278 (0.0131)	*+0.0210 (0.0216)	+0.0441 (0.0175)	(0.0138)	-0.0410 (0.0140)	-0.0315 (0.0230)	-0.0487 (0.0184)
	Loss	+0.110 (0.029)	+0.106 (0.029)	+0.141 (0.044)	+0.064 (0.041)	+0.035	+0.032 (0.031)	+0.078 (0.047)	*-0.029 (0.046)
es	APF	-0.000125 (0.000037)	-0.000135 (0.000038)	-0.000170 (0.000052)	-0.000066	-0.000133 (0.000035)	-0.000142 (0.000036)	-0.000178 (0.000049)	(0.000057)
un of peries O concretes made of NAD cements, to various independent variables	K20	+0.132 (0.079)	+0.124 (0.079)	+0.171 (0.114)	*+0.063 (0.115)				
naebenae	SO3	+0.559 (0.053)	+0.571 (0.054)	+0.527 (0.091)	+0.559	+0.442 (0.053)	+0.454 (0.054)	+0.420	+0.403 (0.073)
artous t	Fe ₂ O ₃					-0.149 (0.021)	(0.021)	(0.029)	-0.143 (0.031)
ents, to t	Al ₂ O ₃					$\frac{-0.272}{(0.032)}$	(0.032)	-0.257 (0.047)	-0.314 (0.047)
A L Cemi	SiO2					-0.226 (0.029)	-0.224 (0.029)	-0.199 (0.038)	-0.280 (0.046)
ane of IV.	CAAF	-0.0287	-0.0296 (0.0079)	(0.0106)	-0.0148 (0.0123)				
ncreues m	C ₃ S	+0.0191 (0.0024)	+0.0189 (0.0024)	+0.0172 (0.0032)	+0.0235 (0.0039)				
ries O co	C3A	-0.0244 (0.00 61)	-0.0267 (0.0064)	-0.0291 (0.0097)	-0.0196 (0.0089)				
arr of De	Air	-0.1761 (0.0198)	-0.1716 (0.0202)	-0.1693 (0.0285)	-0.1764 (0.0299)	-0.1767 (0.0194)	-0.1724 (0.0197)	-0.1667 (0.0284)	-0.1862 (0.0284)
	Const.	= +3.44 = (0.19)	= +3.50 = (0.20)	= +3.86 = (0.27)	= +2.92 = (0.31)	= +11.27 = (0.90)	= +11.26 = (0.90)	= +10.77 $= (1.21)$	= +12.63 = (1.41)
	10¢ psi	OD70 s.d.	OD70 s.d.	OD70 (odd) s.d.	OD70 (even) s.d.	OD70 s.d.	OD70 s.d.	OD70 (odd) s.d.	OD70 (even) s.d.
	Note	-	-	67	က	-	-	61	es
	Eq.	1	2	2A	2B	3	4	4A	4B

*Coef./s.d. ratio less than one.

Note 1, 167 cements, Avg. = 4.481×10^6 psi, S.D. = 0.3203×10^6 psi Note 2, 84 cements Note 3, 88 cements

Table 13-20. Calculated contributions of independent variables to OD70, the dynamic modulus after 14 days moist curing followed by 8 weeks in laboratory air of Series O concretes

Inde- pendent variable	Range of variables (percent)	Coefficients from eq 2 table 13–19	Calculated contributions to OD70	Calculated range of contribu- tions to OD70
Air- content, NAE			Const. = +3.50	
cements_	0 to 4.5	-0.1716	0 to -0.77	0.77
C ₃ A C ₃ S	1 to 15 20 to 65	$-0.0267 \\ +0.0189$	$-0.03 \text{ to } -0.40 \\ +0.38 \text{ to } +1.23$	0.37 0.85
C ₄ AF	1 to 17	-0.0296	-0.03 to -0.50	0.47
SO3	1.2 to 3.0	+0.571	+0.69 to +1.71	1.02
K2O**	0 to 1.1	+0.124	0 to +0.14	0.14
APF	*2500 to 5500	-0.000135	-0.34 to -0.74	0.40
Loss	0.3 to 3.3	+0.106	+0.03 to +0.35	0.32
MgO V**	0 to 5.0 0 to 0.1	$^{+0.278}_{-1.035}$	$\begin{array}{c} 0 \text{ to } +1.39 \\ 0 \text{ to } -0.10 \end{array}$	1.39 0.10

*cm²/g.

**Coefficient of doubtful significance as coef./s.d. ratio was less than 2.

Equations 3 and 4 were calculated using the major oxides instead of the potential compounds as in eqs 1 and 2. The S.D. values were about the same in both instances. In eqs 4A and 4B SiO₂ and Fe₂O₃ had coef./s.d. ratios of less than 1.0 in addition to APF, Loss, Cu, and Zr as in eqs 2A and 2B.

A corresponding series of equations for the concretes made—with NAE cements is presented in table 13–27. The independent variables, their coefficients, and the coef./s.d. ratios were generally in good agreement with those in table 13–26 where the AE cements were included. In the equations calculated for the "odds" and "evens" (eqs 2A, 2B, 4A, and 4B) Fe₂O₃ and Loss had coef./s.d. ratios of less than 1.0 with the smaller groups of cements in one or the other of the pairs of equations.

Using the independent variables of eq 2, table 13–27, and the ranges of these variables, calculations were made of the estimated contributions to the dynamic modulus at 98 days and the ranges of these contributions. The calculated values are presented in table 13–28. Higher values for air

content, C₃A and APF, and possibly C₄AF, Ba, and Cu were associated with lower values for dynamic modulus. Higher values for C₃S, SO₃, Loss, and possibly Zr were associated with higher values for dynamic modulus after 28 days resoaking.

6.4.2. Dynamic Modulus of Series A Concretes

The frequency distribution of the dynamic modulus of the Series A concretes (5 \pm 1-in slump) is presented in table 13–29. There was a broad distribution of values and an overlapping of the values obtained with the concretes made of the different types of cement.

A series of equations for concretes made of AE + NAE cements is presented in table 13–30, indicating the independent variables associated with the dynamic modulus of the Series A concretes after the 28-day resoaking period. Equation 1 shows that higher air content and higher w/c were associated with lower dynamic modulus. Other commonly determined variables, C₃A, C₃S, C₄AF, SO₃, and APF were, as indicated in eq 2, also associated with the dynamic modulus after 28 days resoaking. The reduction in variance was highly significant. (See also table 13-57.) The additional use of the trace elements Cu, Zr, Ti, Rb, and Ba together with the commonly determined variables in eq 3 resulted in a further significant reduction in variance.

Equations 3A and 3B calculated for the "odds" and "evens" in the array of cements indicated that the coef./s.d. ratios for fineness, Rb, and Ba were less than 1.0 in one or the other of the equations for the smaller groups of cements.

A corresponding series of equations for the NAE cements is presented in table 13–31. As indicated in eq 1, the dynamic modulus after 28 days resoaking was related to the air content and water/cement ratio of the concrete made of the different cements. The additional use of commonly determined independent variables, C₃A, C₃S, C₄AF, SO₃, and fineness in eq 2 resulted in a significant reduction in variance. (See table 13–57.) Use of

TABLE 13-21. Frequency distribution of cements with respect to AD70, the dynamic modulus of elasticity of Series A concretes at 70 days (11 days moist curing and then storing in laboratory air for 8 weeks)

					Dynamic	modulus	of elastici	ty, 10 ⁶ psi				
Type cement	3.2 to 3.4	3.4 to 3.6	3.6 to 3.8	3.8 to 4.0	4.0 to 4.2	4.2 to 4.4	4.4 to 4.6	4.6 to 4.8	4.8 to 5.0	5.0 to 5.2	5.2 to 5.4	Total
						Number	of cement	s				
I			1	1 3	15	13	25	18	5		1	79 8
II IIA				4	8	19 2	12	14	8	2		67
III IIIA	1					2	2	6 2	3	6	1	20
IV, V		2		1	2	4	4		2			15
Total	1	3	1	9	28	42	43	40	18	8	2	195

Table 13-22. Coefficients for equations relating AD70, the dynamic Young's modulus of elasticity in 10° psi after 14 days moist curing followed by 56 days drying in labotable.

S.D.	0.2993	0.3132	0.2996	0.1861	0.1853	0.1847	0.1887	0.1865	0.1858	0.1864	0.1882	
ធ	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1				+7.07 (4.41)	*+5.88 (7.06)	*+4.97 (6.34)		+6.63	+7.00 (6.92)	+3.80 (6.27)	
MgO	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1			+0.0391 (0.0133)	+0.0349 (0.0136)	+0.0355 (0.0190)	+0.0432 (0.0211)	-0.0315 (0.0143)	-0.0357 (0.0145)	-0.0292 (0.0211)	-0.0369 (0.0213)	
Loss	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1			+0.1016 (0.0300)	+0.0951 (0.0302)	+0.1206 (0.0440)	+0.0658 (0.0480)				1 1	
APF				-0.000097 (0.000038)	(0.000038)	-0.000118 (0.000052)	*-0.000017 (0.000066)	-0.000089 (0.000037)	-0.000081 (0.000038)	-0.000108 (0.000052)	* -0.000023 (0.000061)	
K20	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1			+0.215 (0.081)	+0.249 (0.083)	+0.258 (0.126)	+0.176 (0.125)	+0.154 (0.082)	+0.185 (0.084)	+0.208 (0.126)	*+0.089 (0.127)	
SO ₃				+0.540 (0.057)	+0.532 (0.057)	+0.533 (0.084)	+0.484 (0.086)	+0.420 (0.058)	+0.410 (0.058)	+0.457 (0.085)	+0.327 (0.086)	
Fe ₂ O ₃								-0.135 (0.022)	-0.136 (0.022)	-0.138 (0.033)	-0.132 (0.030)	
Al ₂ O ₃			1 1					-0.300 (0.032)	-0.296 (0.032)	-0.271 (0.048)	(0.048)	
SiO2								$\frac{-0.222}{(0.028)}$	-0.221 (0.028)	-0.198 (0.039)	-0.260 (0.045)	
C4AF		1 1		-0.0304 (0.0081)	-0.0299 (0.0081)	-0.0360 (0.0118)	-0.0216 (0.0124)					
C3S	1 1		1 1	+0.0181 (0.0025)	+0.0183 (0.0025)	+0.0153 (0.0035)	+0.0226 (0.0039)					
C3A	1 1			-0.0349 (0.0068)	-0.0336 (0.0068)	-0.0317 (0.0102)	-0.0327 (0.0098)					0 9009 \ 106
w/c		+3.300	*-1.196	-5.339 (1.101)	-5.356 (1.101)	-6.346 (1.753)	-3.996 (1.520)	-5.412 (1.103)	-5.234 (1.105)	-6.631 (1.766)	-3.935 (1.511)	
Air content	(0.0109)		(0.0168)	-0.1247 (0.0126)	-0.1235 (0.0126)	-0.1366 (0.0177)	-0.1076 (0.0204)	-0.1265 (0.0126)	-0.1252 (0.0126)	-0.1405 (0.0178)	-0.1094 (0.0203)	Of 25: C D
Const.	= +4.551 = (0.032)	= +2.329 = (0.631)	= +5.334 = (0.947)	= +6.783 = (0.700)	= +6.621 = (0.704)	= +7.653 = (1.105)	= +5.453 = (0.997)	= +14.48 = (1.14)	= +14.31 = (1.14)	= +14.57 = (1.62)	= +14.48 = (1.77)	Note 1 179 comparts Ame - 4 499 × 106 mil S D
10° psi	AD70 s.d.	AD70 s.d.	AD70 s.d.	AD70 s.d.	AD70 s.d.	AD70 (odd) s.d.	AD70 (even) s.d.	AD70 s.d.	AD70 s.d.	AD70 (odd) s.d.	AD70 (even) s.d.	A stangardo C'
Note	-	П	-	1	-	61	က	-	-	23	က	1 1 10
No.	1	2	3	4	5	5A	5B	9	7	7A	7B	7

Note 1, 173 cenents, Avg. = 4
Note 2, 87 cenents
Note 3, 86 cenents
*Coef./s.d. ratio less than one.

TABLE 13-23. Coefficients for equations relating AD70, the dynamic Young's modulus of elasticity in 10° psi after 14 days moist curing followed by 56 days drying in laborates. Tatory air of Series A concretes made of NAE cements, to various independent variables

	s.D.	0.2998	0.3016	0.3006	0.1866	0.1848	0.2028	0.1668	0.1870	0.1855	0.2045	0.1653
	Ë				1 1	+9.09 (4.59)	*+4.00 (8.27)	+9.81 (5.91)		+8.56 (4.53)	*+5.36	(5.86)
	MgO			1 1	+0.0382 (0.0137)	+0.0314 (0.0140)	*+0.0167 (0.0225)	+0.0583 (0.0199)	(0.0146)	-0.0381 (0.0148)	-0.0536 (0.0242)	*-0.0161 (0.0193)
	Loss			1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	+0.0891 (0.0310)	+0.0784 (0.0312)	+0.1141 (0.0623)	+0.0814 (0.0363)	1 1	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1		
9990	APF				-0.000088 (0.000039)	-0.000075 (0.000039)	* -0.000051 (0.000070)	-0.000099 (0.000048)	-0.000082 (0.000038)	-0.000071 (0.000038)	* -0.000033	(0.000048)
theory were of the real records the second of the second of the real records the second records the second of the	K2O				+0.228 (0.085)	+0.282 (0.088)	+0.232 (0.141)	+0.220 (0.120)	+0.171 (0.085)	+0.221 (0.089)	$^{+0.186}_{(0.139)}$	+0.160 (0.121)
aradamara	SO3	1 1	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	1 1	+0.547 (0.058)	+0.538 (0.058)	+0.542 (0.094)	+0.520 (0.078)	+0.427 (0.059)	+0.417 (0.059)	+0.445 (0.097)	+0.376 (0.079)
2000	Fe ₂ O ₃		1 1		1 1				-0.138 (0.022)	-0.141 (0.022)	-0.185 (0.038)	(0.027)
no tennos	Al ₂ O ₃		1 1						(0.033)	-0.292 (0.033)	-0.301 (0.046)	(0.051)
117	SiO ₂								-0.218 (0.029)	-0.217 (0.028)	-0.209 (0.041)	(0.043)
To annu	C,AF		1 1 1 1 1 1 1 1 1 1		-0.0319 (0.0083)	(0.0082)	-0.0524 (0.0147)	-0.0191 (0.0100)				
construction	C3S		1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	+0.0181 (0.0025)	+0.0184 (0.0025)	+0.0176 (0.0037)	+0.0194 (0.0038)	1 1 1 1 1 1 1 1 1 1 1 1 1 1	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1		
77 629 12	C3A				-0.0354 (0.0070)	-0.0336 (0.0070)	-0.0403 (0.0119)	-0.0307 (0.0087)		1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1		
d for som for	w/c		*+0.520 (1.250)	*-0.683	-5.610 (1.183)	-5.536 (1.173)	-5.597 (1.745)	-5.501 (1.620)	(1.185)	-5.676	-5.853 (1.752)	(1.603)
ion i	Air	-0.038 (0.027)		(0.032)	-0.1424 (0.0234)	-0.1517 (0.0237)	-0.1287 (0.0397)	-0.1737 (0.0305)	-0.1490 (0.0234)	-0.1570 (0.0236)	(0.0388)	(0.0301)
	Const.	= +4.518 = (0.038)	= +4.126 = (0.802)	= +4.970 = (0.991)	= +6.969	= +6.871 = (0.748)	= +7.112 = (1.115)	= +6.763 = (1.035)	= +14.61 = (1.20)	= +14.47 = (1.19)	= +14.45 = (1.70)	= +15.17 = (1.78)
	10¢ psi	AD70 s.d.	AD70 s.d.	AD70 s.d.	AD70 s.d.	AD70 s.d.	AD70 (odd) s.d.	AD70 (even) = s.d.	AD70 s.d.	AD70 s.d.	AD70 (odd) s.d.	AD70 (even) = +15.17 s.d. = (1.78)
	Note	-	1	-	-	1	61	61	-	1	63	2
	No.	1	2	3	4	5	5A	5B	9	T	7A	7B

Note 1, 162 cements, Avg. = 4.460×10^6 psi, S.D. = 0.3008×10^6 psi Note 2, 81 cements *Coef./s.d. ratio less than one.

Table 13-24. Calculated contributions of independent variables to AD70, the dynamic modulus after 14 days moist curing followed by 8 weeks in laboratory air of Series A concretes

Inde- pendent variable	Range of variables (percent)	Coefficients from eq 5 table 13-23	Calculated contributions to AD70	Calculated range of contribu- tions to AD70
Air- content,			Const. = $+6.87$	
NAE cements_w/cC3AC3SK2OAPF**_Loop_	0 to 4.5 0.6 to 0.7 1 to 15 20 to 65 1 to 16 1.2 to 3.0 0 to 1.1 *2500 to 5500	$\begin{array}{c} -0.1517 \\ -5.536 \\ -0.0336 \\ +0.0184 \\ -0.0318 \\ +0.538 \\ +0.282 \\ -0.000075 \\ \end{array}$	0 to -0.68 -0.33 to -0.39 -0.03 to -0.50 +0.37 to +1.20 -0.03 to -0.51 +0.65 to +1.61 0 to +0.31 -0.19 to -0.45	0.68 0.06 0.47 0.83 0.48 0.96 0.31 0.22
Loss MgO Li**	0.3 to 3.3 0 to 5.0 0 to 0.02	$+0.784 \\ +0.314 \\ +9.09$	+0.24 to +2.59 0 to +1.57 0 to +0.18	2.35 1.57 0.18

*cm²/g.
**Coefficient of doubtful significance as coef./s.d. ratio was less than 2.0.

the trace elements Cu, Zr, Ti, Rb, and Ba as independent variables in eq 3, caused a further significant reduction in variance, although the coefficients of the individual trace elements were not highly significant.

Equations calculated for the "odds" and "evens" in the array of cements, eqs 3A and 3B, indicated instances where fineness, Zr, Rb, and Ba had

coef./s.d. ratios less than 1.0 in eq 3A.

The use of the major oxides in eqs 4, 5, and 6 resulted in S.D. values which were nearly the same as those obtained in eqs 2 and 3. The coef./s.d. ratio for Fe₂O₃ was greater than 1.0 in eq 5 but was less than 1.0 in eq 6. In eqs 5A and 5B calculated for the "odds" and "evens" the coef./s.d. ratios were less than 1.0 with SiO₂, CaO, fineness, Cu, Rb, and Ba in one or the other of the smaller lots of cements.

Using the independent variables of eq 3 of table 13-31, and the ranges of these variables, calculations were made of the estimated contributions to the dynamic modulus of the Series A concretes after 28 days resoaking and the ranges of these contributions. The calculated values are presented in table 13-32.

Higher values for air content, w/c, C₃A, C₄AF, were associated with lower values for dynamic modulus. Higher values for SO3 and possibly C3S and Zr were associated with higher dynamic modulus values. Variations of air content, w/c and SO₃ had the greatest calculated range of contributions to AD98.

6.5. Effect of Drying on Dynamic Modulus

6.5.1. Ratio of OD70 to OD14 for Series O Concretes (OE70/14)

The dynamic modulus was determined at 14 days after moist curing and again after drying in air for an additional 8 weeks. The frequency distribution of the ratios of dynamic modulus after drying to that before drying of the Series O concretes is presented in table 13–33. Concretes made of nine of the cements had higher dynamic modulus after the drying period but the majority of the concretes had lower values after the drying period than after the original 14 days in moist air. There was a broad distribution of results and an overlapping of the ratios for the concretes made of the different types of cement.

A series of equations for concretes made of AE + NAE cements is presented in table 13-34 indicating the independent variables associated with the dynamic modulus ratio. The use of commonly determined variables C₃A, Na₂O, SO₃, APF, Loss, and MgO in eq 1 resulted in a highly significant reduction in variance. (See table 13-57.) The additional use of the trace elements Rb, Zr, and Mn in eq 2 resulted in a reduction of variance, significant at the 5.0-percent level.

Calculations made for the "odds" and "evens" in the array of cements indicated that the coef./ s.d. ratios for MgO, Rb, and Mn were less than

1.0 in eqs 2A or 2B.

Equations 3 and 4 were calculated using CaO and Al₂O₃ instead of C₃A and including also the air content. The use of the commonly determined variables resulted in a highly significant reduction in variance. The additional use of the trace elements as independent variables resulted in a

Table 13-25. Frequency distribution of cements with respect to OD98, the dynamic modulus of elasticity of Series O concretes after storage of air-dried specimens in water for 28 days

				D	ynamic mo	dulus of el	asticity, 10	⁶ psi			
Type cement	3.8 to 4.0	4.0 to 4.2	4.2 to 4.4	4.4 to 4.6	4.6 to 4.8	4.8 to 5.0	5.0 to 5.2	5.2 to 5.4	5.4 to 5.6	5.6 to 5.8	Total
					Nu	mber of cer	nents	-			
<u>I</u>					3	16	35	19	8	1	82
IAII II IIA	1	3	3	1		10	29	22	5	1	8 68
III IIIA			<u>i</u>	-			8	9	3		68 3 20 3 15
IV, V				î		4	6	4			15
Total	1	3	5	5	3	32	78	54	16	2	199

TABLE 13-26. Coefficients for equations relating OD98, the dynamic Young's modulus of elasticity in 10° psi after air-dried specimens of Series O concretes made of AE + NAE cements were stored in water for 28 days, to various independent variables

S.D.	0.1267	0.1214	0.1099	0.1303	0.1270	0.1213	0.1104	0.1299
Zr		$\begin{array}{c c} +0.619 & 0.1214 \\ (0.231) & \end{array}$	*-0.535 0.1099	$\begin{array}{c c} +0.674 & 0.1303 \\ (0.266) & \end{array}$		+0.579 0.1213	* -0.649 0.1104	+0.600 (0.273)
Cu		-2.34 (1.12)	-3.45 (1.58)	*-1.12 (1.61)		-2.56 (1.13)	-3.64 (1.61)	*-1.42 (1.63)
Ba		(0.288)	(0.356)	-0.639 (0.474)		(0.294)	-0.746 (0.359)	$\begin{array}{c c} -0.831 & *-1.42 \\ (0.500) & (1.63) \end{array}$
Loss	+0.0449 (0.0199)	-0.0361 (0.0194)	+0.0443 (0.0274)	* -0.0163 (0.0308)	+0.0497	+0.0455 (0.0212)	+0.0483 (0.0284)	*+0.0346 (0.0346)
APF	-0.000076 (0.000025)	-0.000078 (0.000024)	-0.000097 (0.000029)	$ \begin{array}{c} *-0.000036 \\ (0.000042) \end{array} \begin{array}{c} *-0.0163 \\ (0.0308) \end{array} $	-0.000076 (0.000025)	-0.000080 (0.000024)	-0.000098 (0.000029)	* -0.000039 * $+0.0346$ (0.000042) (0.0346)
SO_3	+0.169	+0.183 (0.034)	+0.152 (0.047)	+0.191 (0.051)	+0.161 (0.038)	$^{+0.181}_{(0.037)}$	+0.144 (0.051)	+0.203 (0.055)
Fe ₂ O ₃		1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1		1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	(0.0152)	-0.0173 (0.0155)	$\begin{array}{c c} -0.0740 & * -0.0133 \\ (0.0247) & (0.0219) \end{array}$	-0.0283 (0.0244)
Al ₂ O ₃		1 1		1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	(0.0199)	-0.0676 (0.0191)	-0.0740 (0.0247)	(0.0306)
SiO2					-0.0378 (0.0170)	-0.0327 (0.0165)	-0.0449 (0.0196)	*-0.0773
CaO		1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1			+0.0286 (0.0096)	+0.0325 (0.0095)	+0.0338 (0.0120)	+0.0306 (0.0157)
CAAF	-0.0155 (0.0053)	-0.0142 (0.0052)	(0.0070)	-0.0214 (0.0083)				
C3S	+0.00593 (0.00161)	+0.00601 (0.00154)	+0.00696 (0.00185)	+0.00421 (0.00262)		1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1		1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1
C ₃ A	-0.0124 (0.0041)	-0.0152 (0.0041)	-0.0135 (0.0055)	-0.0173				
Air	-0.1401 (0.0055)	-0.1400 (0.0052)	-0.1277 (0.0062)	-0.1585 (0.0090)	-0.1394 (0.0056)	(0.0053)	(0.0063)	(0.0091)
Const.	= +5.22 = (0.12)	= +5.25 = (0.12)	= +5.27 = (0.15)	= +5.31	= +4.70 = (0.84)	= +4.32 = (0.83)	= +4.66 = (1.05)	= +3.71 = (1.38)
Note 106 psi	OD98	OD98	OD98 (odd) s.d.	OD98 (even) s.d.	0D98	0D98 s.d.	OD98 (odd) s.d.	OD98 (even) s.d.
Note	-	-	¢1	က	-	-	83	ಣ
NE o	1	2	2A	2B	3	1	1A	4B

Note 1, 179 cements, Avg. 5.077 \times 10¢ psi, S.D. = 0.2841 \times .10¢ psi Note 2, 90 cements Note 3, 89 cements *Coef./s.d. ratio less than one.

TABLE 13-27. Coefficients for equations relating OD98, the dynamic Young's modulus of elasticity in 10° psi after air dried specimens of Series O concretes made of NAE cements user stored in water for 28 days, to various independent variables

S.D.	0.1245	0.1186	0.1149	0.1207	0.1247	0.1181	0.1157	0.1205
Zr		+0.608	+1.483 (0.536)	+0.505 (0.258)	1 1	+0.558	+1.475 (0.543)	+0.455
Cu		-2.47 (1.11)	-2.93 (1.58)	-2.41 (1.71)		(1.14)	(1.60)	(1.80)
Ba	1 8 5 1 1 8 0 7 1 1 0 8	-0.702 (0.285)	(0.375)	(0.446)	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	(0.291)	-0.848 (0.381)	-0.704 (0.465)
Loss	+0.0474 (0.0201)	+0.0397 (0.0195)	+0.0875 (0.0263)	* -0.0174 (0.0300)	+0.0563 (0.0216)	+0.0522 (0.0212)	+0.0892 (0.0278)	*-0.0007
APF	-0.000080 (0.000025)	-0.000081 (0.000024)	-0.000095 (0.000030)	-0.000052 (0.000040)	(0.000025)	-0.000084 (0.000024)	-0.000096 (0.000031)	-0.000051 (0.000040)
SO3	+0.184 (0.035)	+0.197 (0.034)	+0.174 (0.052)	+0.199 (0.048)	+0.178 (0.038)	+0.200 (0.037)	+0.166 (0.061)	+0.193
Fe ₂ O ₃				1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	-0.0252 (0.0153)	* -0.0081 (0.0157)	-0.0252 (0.0227)	*-0.0021 (0.0233)
Al ₂ O ₃	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1				-0.0650 (0.0201)	-0.0674 (0.0192)	-0.0692 (0.0266)	-0.0741 (0.0294)
SiO2					-0.0381 (0.0171)	-0.0307 (0.0166)	-0.0391 (0.0213)	-0.0366 (0.0285)
CaO					+0.0311 (0.0096)	+0.0362 (0.0094)	+0.0251 (0.0142)	+0.0414 (0.0138)
C4AF	-0.0142 (0.0054)	(0.0052)	-0.0139 (0.0070)	(0.0083)				
C ₃ S	+0.00626 (0.00162)	+0.00632 (0.00155)	+0.00554 (0.00196)	+0.00777 (0.00257)				
C3A	-0.0124 (0.0041)	-0.0158 (0.0041)	-0.0133 (0.0057)	-0.0154 (0.0061)				
Air	= +5.18 -0.1406 $= (0.13) (0.0133)$	-0.1293 (0.0131)	-0.1241 (0.0178)	= +5.05 -0.1373 $= (0.19) (0.0192)$	-0.1393 (0.0134)	-0.1262 (0.0132)	-0.1237 (0.0180)	(0.0199)
Const.	= +5.18 = (0.13)	= +5.18 = (0.12)	= +5.24 = (0.17)	= +5.05 = (0.19)	= +4.51 = (0.84)	= +3.97 = (0.83)	= +4.98 = (1.27)	= +3.76 = (1.22)
10 ⁶ psi	OD98	OD98 s.d.	OD98 (odd) s.d.	OD98 (even) s.d.	OD98	OD98 s.d.	OD98 (odd) s.d.	OD98 (even) s.d.
Note	1	1	61	es	-	-	63	က
No.	1	2	2A	2B	3	4	4A	4B

Note 1, 167 cements, Avg. = 5.136 \times 106 psi, S.D. = 0.1752 \times 106 psi Note 2, 84 cements Note 3, 83 cements

*Coef./s.d. ratio less than one.

Table 13-28. Calculated contributions of independent variables to OD98, the dynamic modulus of Series O concretes after air dried specimens were stored in water for 28 days

Inde- pendent variable	Range of variables (percent)	Coefficients from eq 2 table 13-27	Calculated contributions to OD98	Calculated range of contribu- tions to OD98
Air- content,			Const. = +5.18	
NAE cements_ C3A C4S C4AF SO3 APF Loss Ba Cu	0 to 4.5 1 to 15 20 to 65 1 to 16 1.2 to 3.0 *2500 to 5500 0.3 to 3.3 0 to 0.05	$\begin{array}{c} -0.1293 \\ -0.0158 \\ +0.00632 \\ -0.0124 \\ +0.197 \\ -0.000081 \\ +0.0397 \\ -0.702 \\ -2.47 \end{array}$	$\begin{array}{c} 0 \text{ to } -0.58 \\ -0.02 \text{ to } -0.24 \\ +0.13 \text{ to } +0.41 \\ -0.01 \text{ to } +0.49 \\ -0.20 \text{ to } -0.45 \\ +0.01 \text{ to } +0.13 \\ 0 \text{ to } -0.14 \\ 0 \text{ to } -0.12 \end{array}$	0.58 0.22 0.28 0.19 0.35 0.25 0.12 0.14

 $*cm_2/g.$

reduction of variance significant at the 5.0-percent level.

A corresponding series of equations calculated for the Series O concretes made of NAE cements is presented in table 13-35. The coefficient and coef./s.d. ratio for air content of concretes made of NAE cements were greater in magnitude and appeared somewhat more significant than in the previous table where the AE cements were included although there were instances (eqs 2A and 4A) where the coef./s.d. ratio was less than 1.0. The coef./s.d. ratios of CaO, fineness, Rb, Zr, and Mn were also less than one in 1.0 or both of the equations calculated for the "odds" or "evens" in the array of cements.

Using the coefficients of the independent variables of eq 2, table 13-35, and the ranges of these variables, computations were made of the esti-

Table 13-29. Frequency distribution of cements with respect to AD98, the dynamic modulus of elasticity of Series A concretes after storage of air-dried specimens in water for 28 days

				D	ynamic mo	odulus of ela	asticity, 10	⁶ psi			
Type cement	4.0 to 4.2	4.2 to 4.4	4.4 to 4.6	4.6 to 4.8	4.8 to 5.0	5.0 to 5.2	5.2 to 5.4	5.4 to 5.6	5.6 to 5.8	5.8 to 6.0	Total
					Nu	mber of cer	nents				
A			3	4	22	35	14	2	1	1	79 8
II IIA		1		$\frac{4}{2}$	10	25	22	8			67
II IIA				1	5 1	3	11 1		1		67 3 20 3 15
IV, V			1		2	9	3				15
Total	1	1	4	11	42	72	51	10	2	1	195

Table 13-30. Coefficients for equations relating AD98, the dynamic Young's modulus NAE cements were stored in water for 28

Eq. No.	Note	$10^6~\mathrm{psi}$	Const.	Air content	w/c	C ₃ A	C ₃ S	C ₄ AF	CaO
1	1	AD98 s.d.	= +8.814 = (0.450)	-0.1134 (0.0080)	-5.499 (0.687)				
2	1	AD98 s.d.	= +9.501 = (0.455)	$-0.1298 \ (0.0083)$	$-6.754 \\ (0.717)$	-0.0146 (0.0043)	+0.00468 (0.00159)	-0.0194 (0.0053)	
3	1	AD98 s.d.	= +9.589 = (0.445)	-0.1285 (0.0080)	$ \begin{array}{r} -6.795 \\ (0.694) \end{array} $	-0.0179 (0.0043)	+0.00475 (0.00153)	-0.0166 (0.0052)	
3A	2	AD98 (odd) s.d.	=+11.170 = (0.728)	$-0.1504 \\ (0.0116)$	-9.106 (1.148)	-0.0192 (0.0079)	+0.00524 ·(0.00221)	-0.0268 (0.0081)	
3B	3	AD98 (even) s.d.	= +8.108 = (0.573)	-0.1033 (0.0119)	-4.633 (0.892)	-0.0190 (0.0056)	+0.00445 (0.00220)	-0.0097 (0.0079)	
4	1	AD98 s.d.	=+10.216 = (0.888)	$-0.1303 \\ (0.0083)$	-6.739 (0.718)				+0.0130 (0.0092)
5	1	AD98 s.d.	= +8.672 = (0.721)	-0.1242 $-(0.0077)$	-6.562 (0.687)				+0.0262 (0.0084)
5A	2	AD98 (odd) s.d.	= +9.822 = (1.180)	-0.1427 (0.0118)	$-8.490 \\ (1.182)$				+0.0276 (0.0131)
5B	3	AD98 (even) s.d.	= +7.181 = (1.018)	$-0.1026 \ (0.0111)$	-4.726 (0.875)				+0.0263 (0.0114)
6	1	AD98 s.d.	= +9.699 = (0.872)	-0.1287 (0.0081)	-6.693 (0.702)				**+0.0181 (0.0091)

Note 1, 173 cements, Avg. = 5.080 \times 106 psi, S.D. = 0.2146 \times 106 psi Note 2, 87 cements

^{*}Coef./s.d. ratio less than 1.
**Coef./s.d. ratio less than 1 in "odds" or "evens".

mated contributions to the dynamic modulus ratio and the calculated range of these contributions. The results of these calculations are presented in table 13–36. Higher C_3A , and possibly Na_2O , fineness, and Zr were associated with lower values for the OE70/14 ratio. Higher values for SO_3 and loss on ignition were associated with higher values for the ratio.

6.5.2. Ratio of OD70 to OD14 for Series A Concretes (OE70/14)

The frequency distribution of the ratio of the dynamic modulus of Series A concretes after drying for 8 weeks to the dynamic modulus after the initial 14-day moist curing is presented in table 13–37. Twelve of the concretes made of the 195 cements had higher dynamic modulus values after drying in laboratory air whereas most had lower values after than before the dry storage. There was a broad distribution of values and an overlapping of values obtained with the different types of cement.

A series of equations for concretes made of AE + NAE cements is presented in table 13–38 to

indicate the variables associated with the dynamic modulus ratio of the Series A concretes. The use of the commonly determined variables, C₃A, C₄AF, SO₃, Na₂O, MgO, APF, and Loss in eq 1 resulted in a highly significant reduction in variance. (See table 13–57.) The additional use in eq 2 of the trace elements Co, Rb, and Mn resulted in a reduction of variance significant at the 5.0-percent level although none of the coefficients for the individual trace elements was highly significant.

The use of CaO, Al₂O₃ and Fe₂O₃ together with the other commonly determined variables in eqs 3 and 4 resulted in S.D. values which were about the same as those obtained in eqs 1 and 2 where the calculated potential compounds were used.

Equations calculated for the "odds" and "evens" in the array of cements indicated that the coef./s.d. ratios were less than 1.0 for C₄AF, CaO, Fe₂O₃, Co, Rb, and Mn in one or the other of the smaller lots of cement. (See eqs 2A, 2B, 4A, and 4B.)

A series of equations calculated for the Series A concretes made of NAE cements is presented in table 13-39. As was the case with the Series O

of elasticity in 10 6 psi after air-dried specimens of Series A concretes made of AE + days, to various independent variables

SiO ₂	Al ₂ O ₃	Fe ₂ O ₃	SO ₃	APF	Cu	Zr	Ti	Rb	Ba	S.D.
										0.1423
			$^{+0.216}_{(0.035)}$	-0.000053 (0.000023)						0.1230
			+0.204 (0.035)	$\begin{array}{c} -0.000051 \\ (0.000022) \end{array}$	-3.02 (1.08)	$^{+0.541}_{(0.222)}$	-0.165 (0.080)	$+\frac{8.60}{(5.04)}$	-0.428 (0.284)	0.1166
			+0.254 (0.053)	$-0.000073 \\ (0.000033)$	-3.89 (1.64)	$^{+0.450}_{(0.250)}$	$-0.161 \\ (0.099)$	*+8.15 (8.16)	$-0.644 \\ (0.428)$	0.1206
			+0.129 (0.049)	*-0.000008 (0.000034)	$-2.42 \\ (1.51)$	`+0.733 (0.571)	-0.183 (0.150)	+11.53 (6.59)	*-0.254 (0.455)	0.1085
-0.0459 (0.0163)	$-0.0815 \ (0.0197)$	-0.0469 (0.0150)	$^{+0.189}_{(0.038)}$	-0.000055 (0.000023)						0.1231
$-0.0280 \ (0.0155)$	-0.0701 (0.0190)		$^{+0.200}_{(0.037)}$	$\substack{-0.000049 \\ (0.000023)}$	-3.69 (1.05)	$^{+0.547}_{(0.224)}$	$-0.189 \ (0.081)$	+8.93 (5.10)	$-0.450 \\ (0.289)$	0.1177
$-0.0288 \ (0.0225)$	$-0.0718 \ (0.0312)$		$^{+0.251}_{(0.060)}$	$-0.000063 \\ (0.000034)$	-4.66 (1.75)	$^{+0.475}_{(0.263)}$	-0.171 (0.105)	+8.70 (8.66)	$-0.601 \\ (0.462)$	0.1266
*-0.0187 (0.0225)	-0.0647 (0.0247)		$^{+0.134}_{(0.052)}$	*-0.000005 (0.000033)	-2.35 (1.33)	$^{+0.706}_{(0.566)}$	-0.194 (0.144)	$^{+11.50}_{(6.55)}$	*-0.219 (0.449)	0.1078
* -0.0405 (0.0159)	-0.0853 (0.0193)	**-0.0314 (0.0153)	+0.197 (0.037)	**-0.000052 (0.000023)	-2.81 (1.11)	$^{+0.479}_{(0.223)}$		**+8.04 (5.11)	**-0.489 (0.289)	0.1182

Eq. No.	Note	10 ⁶ psi	Const.	Air content	w/c	C ₃ A	CsS	C ₄ AF	CaO
1	1	AD98 s.d.	= +8.749 = (0.477)	-0.1075 (0.0156)	-5.412 (0.722)				
2	1	AD98 s.d.	= +9.703 = (0.494)	$-0.1396 \\ (0.0154)$	-7.118 (0.778)	-0.0137 (0.0044)	+0.00463 (0.00164)	-0.0195 (0.0054)	
3	1	AD98 s.d.	= +9.712 $= (0.475)$	$-0.1276 \\ (0.0150)$	$-7.051 \\ (0.743)$	-0.0173 (0.0044)	+0.00468 (0.00157)	-0.0160 (0.0053)	
3A	2	AD98 (odd) s.d.	=+10.001 = (0.609)	$-0.1215 \\ (0.0204)$	$-7.531 \ (0.971)$	-0.0266 (0.0067)	+0.00329 (0.00220)	-0.0294 (0.0084)	
3B	2	AD98 (even) s.d.	= +9.274 = (0.684)	$-0.1391 \ (0.0203)$	$ \begin{array}{r} -6.315 \\ (1.054) \end{array} $	-0.0142 (0.0057)	+0.00410 (0.00237)	-0.0081 (0.0069)	
4	1	AD98 s.d.	= +10.216 = (0.924)	-0.1397 (0.0155)	-7.101 (0.780)				+0.0145 (0.0095)
5	1	AD98 s.d.	= +9.565 $= (0.908)$	-0.1311 (0.0152)	-6.951 (0.755)				+0.0203 (0.0094)
5A	2	AD98 (odd) s.d.	= +8.161 = (1.212)	$-0.1195 \\ (0.0200)$	-7.667 (0.961)				+0.0316 (0.0137)
5B	2	AD98 (even) s.d.	= +10.611 = (1.382)	$-0.1495 \\ (0.0223)$	-5.971 (1.148)	1			*+0.0103 (0.0134)
6	1	AD98 s.d.	= +8.527 = (0.731)	$-0.1196 \\ (0.0141)$	-6.850 (0.727)				+0.0282 (0.0085)

Note 1, 162 cements, Avg. = 5.112×10^6 psi, S.D. = 0.1716×10^6 psi. Note 2, 81 cements

*Coef./s.d. ratio less than one.

Table 13-32. Calculated contributions of independent variables to AD98, the dynamic modulus of Series A concretes after the air-dried specimens were stored in water for 28 days

Inde- pendent variable	Range of variables (percent)	Coefficients from eq 3 table 13–31	Calculated contributions to AD98	Calculated range of contribu- tions to AD98
Air- content,			Const. = +9.712	
NAE cements_ w/c C ₃ A C ₃ S	0 to 4.5 0.6 to 0.7 1 to 15 20 to 65	$ \begin{array}{r} -0.1276 \\ -7.051 \\ -0.0173 \\ +0.00468 \end{array} $	0 to -0.57 -4.23 to -4.94 -0.02 to -0.25 +0.09 to +0.30	0.57 0.71 0.23 0.21
C4AF SO3 APF** Cu Zr	1 to 16 1.2 to 3.0 *2500 to 5500 0 to 0.05 0 to 0.5	$\begin{array}{r} -0.0160 \\ +0.209 \\ -0.000042 \\ -3.09 \\ +0.581 \end{array}$	-0.02 to -0.26 +0.25 to +0.63 -0.10 to -0.23 0 to -0.15 0 to +0.29	0.24 0.38 0.13 0.15 0.29
Ti Rb** Ba**	0 to 1.0 0 to 0.01 0 to 0.02	$ \begin{array}{r} -0.189 \\ +8.10 \\ -0.460 \end{array} $	0 to -0.19 0 to +0.08 0 to -0.01	0.19 0.08 0.01

concretes, the coefficients of the air content of the concretes made with NAE cements are probably significant, which was not evident when the AE cements were included. The use of commonly determined variables in eqs 1 and 3 resulted in a highly significant reduction in variance. (See table 13–57.) The additional use of the trace elements Co, Rb, and Mn in eq 2 resulted in a reduction of variance significant at the 5.0 percent probability level. In eq 3, CaO had a coef./s.d. ratio greater than 1.0 but the ratio was less than 1.0 in eq 4; therefore an evaluation of the reduction of variance was not made.

With the use of the coefficients of the independent variables of eq 2 table 13-39 and the ranges of these variables, computations were made of the estimated contributions to the AE70/14 ratio. These computed values are presented in table 13-40 together with the calculated ranges of the contributions. Higher values for C₃A, Na₂O, and probably air content, and fineness were associated

^{**}Coef./s.d. ratio less than one in "odds" or "evens".

^{*}cm 2 /g. **Coefficient of doubtful significance as coef./s.d. ratio was less than 2.0.

SiO ₂	Al ₂ O ₃	Fe ₂ O ₃	SO ₃	APF	Cu	Zr	Ti	Rb	Ba	S.D.
										0.144
			+0.224 (0.035)	$-0.000045 \\ (0.000024)$						0.124
			$^{+0.209}_{(0.035)}$	$-0.000042 \\ (0.000023)$	-3.09 (1.12)	+0.581 (0.224)	-0.189 (0.083)	+8.10 (5.22)	-0.460 (0.288)	0.116
			+0.267 (0.050)	*-0.000009 (0.000036)	-5.24 (1.61)	*+0.204 (1.884)	+0.169 (0.137)	*+7.02 (7.03)	* -0.169 (0.870)	0.11
			+0.176 (0.050)	-0.000045 (0.000030)	-2.13 (1.49)	$^{+0.639}_{(0.217)}$	-0.459 (0.116)	$^{+10.26}_{(7.31)}$	* -0.058 (0.323)	0.10
-0.0428 (0.0169)	-0.0759 (0.0205)	-0.0469 (0.0156)	$^{+0.201}_{(0.039)}$	$-0.000046 \\ (0.000024)$	· 					0.12
$-0.0367 \\ (0.0164)$	-0.0802 (0.0199)	-0.0293 (0.0160)	+0.209 (0.039)	$-0.000043 \\ (0.000024)$	-2.85 (1.15)	+0.497 (0.225)		+8.05 (5.32)	-0.524 (0.296)	0.11
-0.0006 (0.0212)	-0.0667 (0.0233)	-0.0299 (0.0226)	$^{+0.277}_{(0.052)}$	*-0.000003 (0.000035)	-5.92 (1.62)	*+0.670 (1.669)		+9.29 (7.10)	*-0.461 (0.856)	0.11
-0.0687 (0.0275)	-0.1052 (0.0350)	-0.0333 (0.0228)	$^{+0.129}_{(0.059)}$	$-0.000058 \\ (0.000033)$	*-0.55 (1.60)	$^{+0.465}_{(0.231)}$		+11.48 (8.03)	* -0.210 (0.352)	0.11
-0.0227 (0.0159)	-0.0633 (0.0196)		$^{+0.210}_{(0.038)}$	**-0.000040 (0.000023)	-3.80 (1.06)	**+0.591 (0.225)	**-0.225 (0.084)	+8.11 (5.26)	** -0.517 (0.292)	0.11

Table 13-33. Frequency distribution of cements with respect to OE 70/14, the ratio of dynamic modulus of Series O concretes determined after 8 weeks in laboratory air divided by the values after the original 14 days of moist curing

						Dynami	c E ratio					
Type cement	0.82 to 0.84	0.84 to 0.86	0.86 to 0.88	0.88 to 0.90	0.90 to 0.92	0.92 to 0.94	0.94 to 0.96	0.96 to 0.98	0.98 to 1.00	1.00 to 1.02	1.02 to 1.04	Total
						Number o	of cements	3				
A	2	4	11	10 2	13	12 3	17	7 2	6			82
I IA	2	2	7	5	8	16	9	8	8	1	2	60 3
II. IIA			1	1	2	2	2	5	5	2		20 3
iv, v				2	1	2	4	î	3	2		15
Total	4	6	19	20	25	36	34	24	22	6	3	191

TABLE 13-34. Coefficients for equations relating OE 70/14, the ratio of dynamic Young's modulus of elasticity at 70 days (after drying in cir.) to that at 14 days (after moist curing) of Series O concretes made with AE + NAE cements, to various independent variables

	5 :	2	2	<u> </u>	∞ 1	₅₃ ¦	, ;	
S.D.	0.03232	0.03167	0.03247	0.03191	0.03248	0.03172	0.03251	0.03237
Air				1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	-0.00148 (0.00139)	-0.00170 (0.00137)	*-0.00160 (0.00193)	*-0.00184 (0.00207)
Mn		+0.0324 (0.0203)	+0.0345 (0.0260)	*+0.0295 (0.0356)	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	+0.0345 (0.0208)	+0.0335 (0.0267)	*+0.0318 (0.0372)
Zr		-0.134 (0.063)	-0.140 (0.070)	-0.191 (0.174)	1 1	-0.136 (0.063)	-0.128 (0.070)	-0.258 (0.176)
Rb		-2.14 (1.30)	$\frac{-3.25}{(1.92)}$	*-1.07		-2.27 (1.34)	-3.46 (2.04)	*+1.52 (1.93)
MgO	+0.00354	+0.00225 (0.00210)	*+0.00022 (0.00308)	+0.00477 (0.00304)			1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	
Loss	+0.0252 (0.0051)	+0.0259 (0.0051)	+0.0257 (0.0076)	+0.0277	+0.0214 (0.0052)	+0.0228 (0.0053)	+0.0239	+0.0238
APF	-0.0000147 (0.0000058)	-0.0000170 (0.0000058)	-0.0000197 (0.0000075)	-0.0000133 (0.0000097)	-0.0000132 (0.0000061)	-0.0000162 (0.0000060)	$\begin{array}{c} -0.0000192 \\ (0.0000083) \end{array}$	-0.0000114 (0.0000097)
SO3	+0.0702 (0.0088)	+0.0698	+0.0612 (0.0139)	+0.0732 (0.0122)	+0.0685 (0.0092)	+0.0690 (0.0090)	+0.0582 (0.0149)	+0.0724 (0.0124)
Na ₂ O	-0.0458 (0.0148)	-0.0385 (0.0149)	-0.0425 (0.0202)	-0.0311 (0.0239)	-0.0492 (0.0151)	-0.0403 (0.0153)	-0.0484 (0.0203)	-0.0267 (0.0252)
Al ₂ O ₃		1 1 1 1 1 1 1 1 1 1 1 1			-0.0181 (0.0028)	-0.0177 (0.0028)	-0.0165 (0.0045)	-0.0175 (0.0038)
CaO					-0.00535 (0.00225)	-0.00426 (0.00233)	-0.00481 (0.00337)	-0.00378 (0.00348)
C3A	-0.00605	-0.00587 (0.00085)	-0.00560 (0.00136)	-0.00575 (0.00119)		1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	
Const.	= +0.871 = (0.019)	= +0.880 = (0.019)	OE $70/14 \text{ (odd)} = +0.911$ s.d. = (0.027)	OE $70/14$ (even) = $+0.849$ s.d. = (0.029)	= +1.270 = (0.145)	= +1.206 = (0.150)	OE $70/14$ (odd) = $+1.267$ s.d. = (0.216)	OE $70/14$ (even) = $+1.147$ s.d. = (0.226)
,	OE 70/14 s.d.	OE 70/14 s.d.	OE 70/14 s.d.	OE 70/14 s.d.	OE 70/14 s.d.	OE 70/14 s.d.	OE 70/14 s.d.	OE 70/14 s.d.
Note	T	1	67	တ	1	1	63	တ
Eq. No.	1	2	2A	2B	3	4	4A	4B

Note 1, 179 cements, Avg. = 0.9307, S.D. = 0.04385 Note 2, 90 cements Note 3, 89 cements *Coef./s.d. ratio less than one.

Table 13-35. Coefficients for equations relating OE 70/14, the ratio of dynamic Young's modulus of elasticity at 70 days (after drying in air) to that at 14 days (after moist curin) of Series O concretes made with NAE cements, to various independent variables

	S.D.	0.03152	0.03102	0.03057	0.03126	0.03148	0.03087	0.02975	0.03192
	Air	-0.01061 (0.00340)	-0.01012 (0.00343)	* -0.00195 (0.00465)	(0.00517)	-0.01173 (0.00336)	-0.01140 (0.00339)	$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	(0.00519)
	Mn		+0.0288 (0.0207)	*+0.0177 (0.0273)	+0.0474 (0.0319)		+0.0345 (0.0211)	*+0.0244 (0.0274)	+0.0516 (0.0330)
	Zr		-0.136 (0.062)	-0.119 (0.065)	$ \begin{array}{c cccc} +0.00485 & *+0.27 & *-0.561 \\ (0.00301) & (1.97) & (0.617) \end{array} $		-0.144 (0.062)	-0.128 (0.064)	*+0.74 *-0.530 (0.626)
ean	Rb		-1.37 (1.32)	-2.48 (1.83)	$^{*}_{(1.97)}^{+0.27}$		* -1.15 (1.35)	-2.39 (1.82)	*+0.74 (2.07)
rederies our sa	MgO	+0.00388	+0.00269 (0.00213)	* -0.00093 (0.00323)	+0.00485 (0.00301)	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1			
ad anna sa	Loss	+0.0209 (0.0051)	+0.0223 (0.0051)	+0.0186 (0.0071)	+0.0197 (0.0082)	+0.0175 (0.0052)	+0.0197	+0.0185	+0.0177 (0.0087)
Derves O concretes made win in A.B. cements, to various independent variables	APF	$\begin{array}{c} -0.0000149 \\ (0.0000058) \end{array}$	$\begin{array}{c} -0.0000171\\ (0.0000058) \end{array}$	$\begin{array}{c} -0.0000228 \\ (0.0000074) \end{array}$	* -0.0000081 (0.00000098)	$\begin{array}{c} -0.0000141 \\ (0.0000061) \end{array}$	-0.0000170 (0.0000060)	-0.0000233 (0.00000078)	+0.0700 *-0.0000074 (0.0123) (0.0000101)
MAD CEM	SO3	+0.0724 (0.0088)	+0.0719 (0.0088)	+0.0718 (0.0146)	$^{+0.0701}_{(0.0118)}$	+0.0711 (0.0091)	+0.0710 (0.0090)	+0.0678 (0.0142)	+0.0700 (0.0123)
ae with i	Na ₂ O	-0.0422 (0.0150)	-0.0343 (0.0151)	-0.0517 (0.0198)	-0.0336 (0.0251)	-0.0461 (0.0151)	-0.0361 (0.0153)	-0.0479 (0.0192)	-0.0348 (0.0271)
cretes ma	A12O3					-0.0180 (0.0027)	-0.0182 (0.0028)	-0.0172 (0.0040)	-0.0178 (0.0039)
ertes O con	CaO	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1				-0.00469 (0.00220)	(0.00230)	*-0.00232 (0.00316)	*-0.00354
c fo (furth)	C3A	-0.00581 (0.00086)	-0.00573	-0.00488 (0.00130)	-0.00578 (0.00118)				
3	Const.)/14 = +0.886 = (0.019)	= +0.894 = (0.020)	OE $70/14 \text{ (odd)} = +0.911$ s.d. $= (0.027)$	OE $70/14$ (even) = $+0.879$ s.d. = (0.031)	1/14 = +1.246 = (0.143))/14 = +1.168 = (0.148)	OE $70/14$ (odd) = $+1.115$ s.d. = (0.203)	OE $70/14$ (even) = $+1.163$ s.d. = (0.230)
		OE 70/14 s.d.	OE 70/14 s.d.	OE 70	OE 70	OE 70/14 s.d.	OE 70/14 s.d.	OE 70	OE 70
	Note	н	-	23	ಣ	-	-	61	60
	Eq. No.	1	2	2A	2B	3	4	4A	4B

Note 1, 167 cements, Avg. = 0.9295, S.D. = 0.04400 Note 2, At cements Note 3, B3 cements *Coef./s.d. ratio less than one.

Table 13-36. Calculated contributions of independent variables to OE70/14, the ratio of dynamic modulus of Series O concretes after drying in air for 8 weeks divided by the dynamic modulus after the original 14-day moist curing

Inde- pendent variable	Range of variables (percent)	Coefficients from eq 2 table 13–35	Calculated contributions to OE70/14	Calculated range of contribu- tions to OE70/14
C ₃ A	1 to 15 0 to 0.7 1.2 to 3.0 *2500 to 5500 0.3 to 3.3 0 to 5.0 0 to 0.01 0 to 0.5 0 to 1.0	$\begin{array}{c} -0.00573 \\ -0.0343 \\ +0.0719 \\ -0.0000171 \\ +0.0223 \\ +0.00269 \\ -1.37 \\ -0.136 \\ +0.0288 \end{array}$	Const. = +0.894 -0.006 to -0.086 0 to -0.024 +0.086 to +0.216 -0.043 to -0.094 +0.007 to +0.074 0 to -0.014 0 to -0.014 0 to -0.068 0 to +0.029	0.080 0.024 0.130 0.051 0.067 0.013 0.014 0.068 0.029
NAE cements_	0 to 4.5	-0.01012	0 to -0.046	0.046

*cm²/g.
**Coefficient of doubtful significance as coef./s.d. ratio was less than 2.0.

with lower values for AE70/14. Higher values for SO₃ and loss on ignition were associated with higher values for the AE70/14 ratio.

6.6. Effect of Rewetting on Dynamic Modulus

6.6.1. Ratio of 98-Day (Wet) to 70-Day (Dry) Dynamic Modulus of Series O Concretes

After drying in laboratory air for 8 weeks, the dynamic modulus was determined (total age 70 days). The specimens were then placed in water and the dynamic modulus was again determined after 4 weeks (total age 98 days). The ratio of the dynamic modulus values OE98/70 was calculated and the frequency distribution of this ratio for the Series O concretes is presented in table 13–41. The concretes made with all of the cements showed some increase in dynamic modulus due to the

Table 13-37. Frequency distribution of cements with respect to AE 70/14, the ratio of dynamic modulus of Series A concretes determined after 8 weeks in laboratory air divided by the values after the original 14 days of moist curing

					D	ynamic E r	atio				
Type cement	0.82 to 0.84	0.84 to 0.86	0.86 to 0.88	0.88 to 0.90	0.90 to 0.92	0.92 to 0.94	0.94 to 0.96	0.96 to 0.98	0.98 to 1.00	1.00 to 1.02	Total
					Nu	mber of cen	nents				
I IA	. 1	5	8	12	13 1	19	12 2	5	4	2	79 8
II IIA	. 3		4	8	11	11	11	6	10	3	67
III IIIA			2		3	2	3	3	5	2	20 3
iv, v			1	1	1	1	4	3		4	15
Total	4	5	15	22	30	35	34	18	20	12	195

TABLE 13-38. Coefficients for equations relating AE 70/14, the ratio of dynamic Young's modulus of elasticity at 70 days (after drying in air) to that at 14 days (after moist curing) with Series A concretes made of AE + NAE cements, to various independent variables

			3	fan m	-		6							-			
NE o	Note	Const.		C3A	CAF	CaO	Al ₂ O ₃	Fe_2O_3	SO3	Na ₂ O	MgO	APF	Loss	ပိ	Rb	Mn	S.D.
	-	AE $70/14$ = $+0.905$ s.d. = (0.027)	' '	-0.00768 (0.00106)	-0.00137	1 1 1 4 1 3 1 8 1 8 1 8 1 1 1 1 1 1	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	+0.0702 (0.0091)	-0.0452 (0.0149)	+0.0044 (0.0021)	-0.0000160 (0.0000059)	+0.0216 (0.0052)				0.03210
1	-	AE $70/14$ = $+0.904$ s.d. = (0.027)	$\begin{vmatrix} 904 & -0.\\ 027 & (0.$	-0.00741 (0.00107)	-0.00173				+0.0722 (0.0090)	-0.0434 (0.0147)	+0.0037 (0.0021)	-0.0000166 (0.0000059)	+0.0203 (0.0051)	+2.59 (1.74)	(1.35)	+0.0396 (0.0207)	0.03146
2A	63	AE $70/14$ (odd) = $+0.869$ s.d. = (0.040)	869 -0. 040) (0.	* (0.00165)	*-0.00092				+0.0817 (0.0135)	-0.0264 (0.0222)	+0.0037 (0.0031)	$\begin{array}{c} -0.0000143 \\ (0.0000074) \end{array}$	+0.0203 (0.0074)	+4.38 (2.66)	*-1.93	+0.0483 (0.0248)	0.03130
2В	က	AE $70/14$ (even) = $+0.926$ s.d. = (0.038)	926 038) —0.	-0.00691 (0.00157)	-0.00257 (0.00193)				+0.0687	-0.0515 (0.0212)	+0.0035 (0.0034)	$\begin{array}{c} -0.0000172 \\ (0.0000108) \end{array}$	+0.0168 (0.0085)	*+0.91 (2.65)	-2.41 (1.95)	*+0.0326 (0.0433)	0.03294
	-	AE $70/14$ = $+1.207$ s.d. = (0.167)	207			-0.00435 (0.00246)	-0.0206 (0.0028)	+0.00548 (0.00369)	+0.0678 (0.0094)	-0.0494	1 1	-0.0000140 (0.0000062)	+0.0186 (0.0053)				0.03219
	-	AE 70/14 = +1.190 s.d. = (0.168)	168)			-0.00415 (0.00250)	-0.0198 (0.0029)	+0.00418 (0.00366)	+0.0698 (0.0093)	(0.0150)		-0.0000147 (0.0000061)	+0.0175 (0.0053)	+2.71 (1.36)	(1.36)	+0.0392 (0.0208)	0.03147
4A	67	AE $70/14$ (odd) = $+1.287$ s.d. = (0.236)	287			-0.00617 (0.00351)	-0.0217 (0.0043)	+0.00747 (0.00559)	+0.0766 (0.0140)	(0.0228)		-0.0000108 (0.0000077)	+0.0167 (0.0074)	+4.52 (2.62)	-2.52 (2.11)	+0.0457 (0.0243)	0.03094
4B	က	AE $70/14$ (even) = $+1.084$ s.d. = (0.269)	269)			*-0.00224 (0.00396)	-0.0181 (0.0042)	* +0.00135 (0.00553)	+0.0674 (0.0144)	(0.0213)		-0.0000158 (0.0000110)	+0.0144 (0.0086)	* +1.29 (2.62)	(1.96)	*+0.0333	0.03310
			_											-	-		

Note 1, 171 cements, Avg. = 0.09311, S.D. = 0.04347 (Note 2, 86 cements Note 3, 85 cements *Coef./s.d. ratio less than 1.

soaking. There was, however, a fairly broad distribution of values and an overlapping of the values obtained with the different types of cement.

A series of equations is presented in table 13–42 to indicate the independent variables associated with the 98-day/70-day dynamic modulus ratio of Series O concretes made with AE + NAE cements. The use of air content, C₃A, C₃A/SO₃, C₃S, C₄AF, K₂O, Loss, and MgO as independent variables in eq 1 resulted in a highly significant reduction in variance. With the additional use of the trace elements Co, Li, Zr, and P in eq 2 there was a further significant reduction of the S.D. value. (See table 13–57.)

The use of CaO and SiO₂ together with Al₂O₃/SO₃ instead of the calculated potential compounds in eq 3 also resulted in a significant reduction in variance. In eq 4 the use of the trace elements caused a reduction of variance significant at the

5.0-percent level.

Equations calculated for the "odds" and "evens" in the array of cements (eqs 2A, 2B, 4A, and 4B) show instances where the coef./s.d. ratio was less than 1.0 for C_4AF , K_2O , MgO, Co, and P in one or both of the equations for the smaller lots of cement.

A corresponding series of equations for the ratio of dynamic modulus after to that before resoaking for the Series O concretes made of NAE cements is presented in table 13–43. The coefficients for the independent variables as well as the coef./s.d. ratios were in reasonable agreement with those of the previous table where the AE cements were

included. Using the coefficients of the independent variables in eq 2 table 13-43 as well as the ranges of these variables, calculations were made of the estimated contributions to the ratio of dynamicmodulus values after to that before resoaking and the ranges of these contributions. The calculated values are presented in table 13–44. Higher values for air content and C₃A/SO₃ were associated with higher values for the dynamic-modulus ratio. Higher values for C₃A, C₃S, and possibly K₂O, Loss, MgO, and Li were associated with lower values for the dynamic-modulus ratio. Variations of C₃A, C₃A/SO₃ and C₃S had the greatest effect on the calculated range of contributions to OE98/70.

6.6.2. Ratio of 98-Day (Wet) to 70-Day (Dry) Dynamic Modulus of Series A Concretes

The frequency distribution of the ratio of dynamic modulus after to that before resoaking for Series A concretes is presented in table 13–45. Concretes made of all of the cements increased in dynamic modulus with the increase ranging from less than 5 to more than 40 percent. There was an overlapping of the values obtained with the different types of cement.

A series of equations indicating the independent variables associated with the OE98/70 dynamicmodulus ratio of Series A concretes made with

AE + NAE cements is presented in table 13-46. The use of the air content, C₃A, C₃S, C₄AF, SO₃, K₂O, Loss, and MgO in eq 1 resulted in a highly significant reduction of variance. (See table 13–57.) With the addition of C₃A/SO₃ as an independent variable in eq 2 the sign of the coefficient for C₃A became negative and the coef./s.d. ratio for SO₃ became less than 1.0. Deleting SO₃ as an independent variable in eq 3 resulted in higher coef./ s.d. ratios for both C_3A and C_3A/SO_3 . The interrelation between these independent variables is obvious and has been discussed in previous sections. The use of the trace elements Li, P, and Co in eq 4 together with the commonly determined variables resulted in a significant reduction in variance. (See table 13–57.) Equations 5 and 6 were calculated using CaO and SiO₂ in place of C₃A, C₃S, and C₄AF. There was a significant reduction in variance in both equations.

In equations calculated for the smaller lots of cement, C₄AF, P, and Co had coef./s.d. ratios less than 1.0 in eq 4B, and P and Co had coef./s.d.

ratios less than 1.0 in eq 6B.

With the use of only the NAE cements, equations were calculated to determine the variables associated with the OE98/70 dynamic-modulus ratio. The results are presented in table 13–47. There was a reasonable agreement of the coefficients and coef./s.d. ratios with those of the previous table where the AE cements were included. There were instances in the equations for the "odds" and "evens" where air content, MgO, P, and Co had coef./s.d. ratios less than 1.0 in the smaller lots of cement.

Using the coefficients of the independent variables of eq 4 table 13–47, calculations were made of the estimated contributions to the AE 98/70 dynamic-modulus ratio. These calculated values together with the calculated ranges of contributions to the ratio are presented in table 13–48. Higher values for C₃A/SO₃ and possibly air content, C₄AF, and P were associated with higher ratios. Higher values for C₃A, C₃S, K₂O, and possibly loss-on-ignition, MgO, and Li were associated with lower ratios. Variations of C₃A, C₃A/SO₃ and C₃S had the greatest effect on the calculated range of contributions to AE98/70.

6.7. Effect of 24-Hour Water Storage of Air-Dried Concrete on Dynamic Modulus

6.7.1. Ratio of 71-Day (24-Hour Water Storage) to 70-Day (Air-Dried) Dynamic Modulus of Series O Concretes

The frequency distribution of the ratio of dynamic modulus after one day of soaking to that of air-dried Series O concretes (OE98/70) is presented in table 13–49. The concretes made with more than half of the cements decreased slightly in dynamic modulus when the air-dried specimens were placed in water for 24 hours. Other specimens showed a slight increase in dynamic modulus. As indicated in tables 13–41 and 13–45, storage in

Eq. No.	Note		Const.	Air content	C ₃ A	C ₄ AF	CaO	Al ₂ O ₃	Fe ₂ O ₃
1	1	AE 70/14 s.d,	= +0.930 = (0.027)	-0.00802 (0,00289)	-0.00809 (0.00104)	-0.00198 (0.00132)			
2	1	AE 70/14 s.d.	= +0.928 = (0.027)	-0.00708 (0.00291)	-0.00794 (0.00106)	-0.00234 (0.00134)			
2A	2	AE 70/14 (odd) s.d.	= +0.946 = (0.045)	-0.00772 (0.00491)	-0.00977 (0.00179)	-0.00414 (0.00233)			
2B	2	AE 70/14 (even) s.d.	= +0.917 = (0.038)	-0.00637 (0.00406)	-0.00656 (0.00143)	*-0.00122 (0.00179)			
3	1	AE 70/14 s.d.	= +1.233 = (0.168)	-0.00817 (0.00291)			-0.00437 (0.00246)	-0.0217 (0.0028)	+0.00429 (0.00375)
4	1	AE 70/14 s.d.	= +0.932 = (0.027)	-0.00815 (0.00288)				-0.0199 (0.0029)	+0.00491 (0.00339)
4A	2	AE 70/14 (odd) s.d.	= +0.958 = (0.044)	-0.00986 (0.00468)				-0.0260 (0.0048)	*+0.00298 (0.00589)
4B	2	AE 70/14 (even) s.d.	= +0.917 = (0.037)	$-0.00674 \\ (0.00393)$				-0.0158 (0.0038)	+0.00565 (0.00457)

Note 1, 160 cements, Avg. = 0.9293, S.D. = 0.04321 Note 2, 80 cements

Table 13-40. Calculated contributions of independent variables to AE70/14, the ratio of dynamic modulus of Series A concretes after drying in air for 8 weeks divided by the dynamic modulus after the original 14 days moist curing

Inde- pendent variable	Range of variables (percent)	Coefficients from eq 2 table 13-39	Calculated contributions to AE70/14	Calculated range of contribu- tions to AE70/14
Air- content, NAE			Const. = +0.928	
cements_	0 to 4.5 1 to 15	$-0.00708 \\ -0.00794$	0 to -0.032 -0.008 to -0.119	0.032 0.111
C ₄ AF** SO ₃	1 to 17 1.2 to 3.0	$-0.00234 \\ +0.0732$	-0.002 to $-0.040+0.088$ to $+0.220$	0.038
Na ₂ O	0 to 0.7	-0.0432	0 to -0.030	0.132 0.030
MgO**	0 to 5.0	+0.0038	0 to +0.019	0.019
APF	*2500 to 5500	-0.0000169	-0.042 to -0.093	0.051
Loss Co**	0.3 to 3.3 0 to 0.01	$\begin{array}{c} +0.0161 \\ +2.53 \end{array}$	+0.005 to +0.053 0 to +0.025	0.048 0.025
Rb**	0 to 0.01	+2.55 -1.45	0 to +0.025 0 to -0.014	0.025
Mn**	0 to 1.0	+0.0392	0 to +0.039	0.039

water for 28 days resulted in an increase of the

dynamic modulus with all the concretes.

The inclusion of C₃A, C₃S, K₂O, C₃A/SO₃, Loss, and MgO as independent variables in eq 1 of table 13-50 resulted in a significant reduction of the S.D. value. The use of Co, Ni, Zr, and Mn together with commonly determined variables in eq 2 caused an additional reduction in variance. (See also table 13–57.) The use of SiO_2 and Al_2O_3 / SO₃ in eqs 3 and 4 in place of C₃A and C₃S, MgO and C₃A/SO₃ resulted in similar S.D. values.

In equations calculated for the "odds" and "evens" in the array of cements, the coef./s.d. ratio for C₃S, K₂O, MgO, Co, Ni, and Mn was less than 1.0 in one or the other of the equations for

the smaller lots of cements.

A corresponding series of equations calculated for the NAE cements is presented in table 13-51. The independent variables, their coefficients and coef./s.d. ratios were generally in agreement with

^{*}Coef./s.d. ratio less than one.

^{*}cm²/g. **Coefficient of doubtful significance as coef./s.d. ratio was less than 2.0.

SO ₃	Na ₂ O	MgO	APF	Loss	Со	Li	Rb	Mn	S.D.
+0.0718 (0.0090)	-0.0451 (0.0148)	+0.0045 (0.0021)	-0.0000166 (0.0000058)	$^{+0.0168}_{(0.0051)}$					0.03088
+0.0732 (0.0089)	-0.0432 (0.0147)	+0.0038 (0.0021)	-0.0000169 (0.0000059)	$^{+0.0161}_{(0.0051)}$	+2.53 (1.74)		-1.45 (1.33)	+0.0392 (0.0208)	0.03049
+0.0761 (0.0138)	-0.0334 (0.0269)	+0.0041 (0.0034)	-0.0000156 (0.0000105)	$^{+0.0179}_{(0.0090)}$	+3.15 (2.32)		* -1.21 (2.06)	+0.0483 (0.0283)	0.03212
+0.0686 (0.0140)	-0.0456 (0.0194)	+0.0032 (0.0032)	-0.0000170 (0.0000070)	$^{+0.0148}_{(0.0070)}$	*+1.23 (3.10)		*-1.29 (2.07)	*+0.0333 (0.0360)	0.03077
+0.0695 (0.0093)	-0.0492 (0.0150)		-0.0000147 (0.0000060)	$^{+0.0138}_{(0.0053)}$					0.03100
+0.0731 (0.0088)	-0.0542 (0.0160)		-0.0000154 (0.0000058)	$^{+0.0142}_{(0.0051)}$	+2.87 (1.75)	+1.45 (0.79)		+0.0474 (0.0203)	0.03043
+0.0792 (0.0136)	-0.0341 (0.0288)		$-0.0000160 \\ (0.0000104)$	+0.0157 (0.0096)	+2.77 (2.29)	*+0.85 (1.26)		+0.0544 (0.0275)	0.03209
+0.0673 (0.0136)	-0.0588 (0.0205)		$-0.0000150 \\ (0.0000074)$	+0.0138 (0.0068)	* +2.63 (3.07)	+1.65 (1.07)		+0.0456 (0.0344)	0.03036

		Dynamic E ratio										
Type cement	1.00 to 1.05	1.05 to 1.10	1.10 to 1.15	1.15 to 1.20	1.20 to 1.25	1.25 to 1.30	1.30 to 1.35	1.35 to 1.40	1.40 to 1.45	Total		
					Number	r of cements						
		17	40	16 2	8	1				82		
A		9	3 19	222	$\frac{2}{13}$	3	2			8 68 3		
IA	8	5	- 6	1						20		
, V.		1	4 .	5	2		2		1	15		
Total	8	35	74	46	25	6	4	0	1	199		

Eq. No.	Note	Const.	Air content	C3A	C ₃ S	C4AF	CaO	SiO ₂
1	1	OE 98/70 = +1.35 s.d. = (0.04		-0.0173 (0.0025)	-0.00395 (0.00054)	+0.00245 (0.00190)		
2	1	OE $98/70$ = $+1.37$ s.d. = (0.04)		-0.0178 (0.0024)	-0.00411 (0.00053)	+0.00261 (0.00186)		
2A	2	OE $98/70 \text{ (odd)} = +1.36$ s.d. = (0.05)		-0.0163 (0.0039)	-0.00349 (0.00070)	*+0.00067 (0.00280)		
2B	3	OE $98/70 \text{ (even)} = +1.43$ s.d. = (0.07		-0.0197 (0.0031)	-0.00518 (0.00083)	*+0.00267 (0.00268)		
3	1	OE $98/70 = +1.79$ s.d. $= (0.32)$					-0.0206 (0.0044)	+0.0269 (0.0036)
4	1	OE $98/70 = +1.92$ s.d. $= (0.32)$					-0.0227 (0.0044)	+0.0280 (0.0036)
4A	2	OE $98/70 \text{ (odd)} = +1.67$ s.d. $= (0.51)$					-0.0177 (0.0068)	+0.0251 (0.0053)
4B	3	OE 98/70 (even) = $+2.03$ s.d. = (0.40)					-0.0268 (0.0058)	+0.0340 (0.0049)

Note 1, 179 cements, Avg. = 1.152, S.D. = 0.06653

Note 2, 90 cements

Note 3, 89 cements

*Coef./s.d. ratio less than one.

Table 13-43. Coefficients for equations relating OE 98/70, the ratio of dynamic You days (after drying in air) of Series O concretes made

					1				
Eq. No.	Note		Const.	Air content	CaA	C ₃ S	C ₄ AF	CaO	SiO ₂
1	1	OE 98/70 s.d.	= +1.351 = (0.045)	+0.0144 (0.0049)	-0.0172 (0.0026)	-0.00403 (0.00056)	+0.00261 (0.00196)		
2	1	OE 98/70 s.d.	= +1.366 = (0.044)	+0.0170 (0.0050)	-0.0179 (0.0025)	-0.00423 (0.00055)	+0.00278 (0.00190)		
2A	2	OE 98/70 (odd) s.d.	=+1.285 = (0.054)	+0.0243 (0.0066)	-0.0157 (0.0040)	-0.00336 (0.00067)	+0.00649 (0.00251)		
2B	3	OE 98/70 (even) s.d.	= +1.506 = (0.078)	+0.0094 (0.0079)	-0.0192 (0.0034)	-0.00582 (0.00095)	*-0.00163 (0.00311)		
3	1	OE 98/70 s.d.	= +1.878 = (0.336)	+0.0123 (0.0048)				-0.0219 (0.0046)	+0.0266 (0.0037)
4	1	OE 98/70 s.d.	= +2.006 = (0.330)	+0.0145 (0.0049)				-0.0242 (0.0045)	+0.0282 (0.0037)
4A	2	OE 98/70 (odd) s.d.	= +2.463 = (0.484)	+0.0185 (0.0066)				-0.0279 (0.0062)	+0.0204 (0.0054)
4B	3	OE 98/70 (even	=+1.904 = (0.477)	+0.0095 (0.0079)				-0.0253 (0.0068)	+0.0353 (0.0055)

Note 1, 167 cements, Avg. = 1.151, S.D. = 0.06643 *Coef./s.d. ratio less than one.

Note 2, 84 cements

Note 3, 83 cements

Table 13-44. Calculated contributions of independent variables to OE 98/70, the ratio of the dynamic modulus of Series O concretes after 28 days in water divided by the dynamic modulus after the previous 8 weeks in air

Inde- pendent variable	Range of variables (percent)	Coefficients from eq 2 table 13-43	Calculated contributions to OE98/70	Calculated range of contribu- tions to OE98/70
Air- content, NAE cements CaA CaS C4AF**- K2O	0 to 4.5 1 to 15 20 to 65 1 to 1.7 0 to 1.1	$ \begin{array}{r} +0.0170 \\ -0.0179 \\ -0.00423 \\ +0.00278 \\ -0.0566 \end{array} $	Const. = +1.366 0 to +0.077 -0.018 to -0.268 -0.084 to -0.274 +0.003 to +0.047 0 to -0.062	0.077 0,250 0.190 0.044 0.062
Loss MgO C ₃ A/SO ₃ Co** Li Zr**_ P**	0.3 to 3.3 0 to 5.0 0.4 to 10.1 0 to 0.01 0 to 0.02 0 to 0.5 0 to 0.5	$\begin{array}{c} -0.0191 \\ -0.0065 \\ +0.0340 \\ -3.48 \\ -2.97 \\ +0.149 \\ +0.0422 \end{array}$	-0.006 to -0.063 0 to -0.032 +0.014 to +0.343 0 to -0.035 0 to -0.059 0 to +0.074 0 to +0.021	0.057 0.032 0.329 0.035 0.059 0.074 0.021

**Coefficient of doubtful significance as coef./s.d. ratio was less than 2.0.

those of the previous table where the AE cements were included.

Using the coefficients of the independent variables of eq 2, table 13–51, calculations were made of the estimated contributions to the OE71/70 dynamic modulus values. These calculated contributions are presented in table 13–52 together with the calculated ranges of these contributions. Increases of air content, C₃A/SO₃, and Zr were associated with increases of the ratio (OE71/70). Increases of C₃A, K₂O, Loss, MgO, and possibly Ni were associated with decreases of the OE71/70 values.

6.7.2. Ratio of 71-Day (24-Hour Water Storage) to 70-Day (Air-Dried) Dynamic Modulus of Series A Concretes

The frequency distribution of the ratio of dynamic modulus after 24 hours soaking to that of

K ₂ O	Loss	MgO	<u>CaA</u>	Al ₂ O ₃ SO ₃	Со	Li	Zr	P	S.D.
-0.0427 (0.0178)	-0.0227 (0.0065)	-0.0091 (0.0031)	$^{+0.0351}_{(0.0043)}$						0.04420
-0.0495 (0.0178)	-0.0232 (0.0065)	-0.0069 (0.0031)	+0.0339 (0.0042)		-3.13 (2.35)	-2.53 (1.01)	+0.162 (0.084)	+0.0506 (0.0305)	0.04286
-0.0891 (0.0266)	-0.0141 (0.0097)	*-0.0009 (0.0045)	+0.0286 (0.0068)		* -0.69 (3.54)	-3.06 (1.47)	+0.135 (0.090)	+0.1546 (0.0532)	0.04243
*-0.0161 (0.0245)	-0.0316 (0.0092)	$-0.0104 \\ (0.0043)$	+0.0376 (0.0054)		-4.05 (3.17)	-2.23 (1.40)	$^{+0.329}_{(0.230)}$	*+0.0109 (0.0370)	0.04173
$-0.0483 \\ (0.0184)$	-0.0255 (0.0074)	-0.0137 (0.0043)		+0.0526 (0.0062)					0.04433
-0.0577 (0.0187)	-0.0271 (0.0074)	-0.0127 (0.0043)		+0.0497 (0.0061)	-2.72 (2.35)	-2.51 (1.02)	+0.142 (0.084)	+0.0419 (0.0307)	0.04328
-0.0968 (0.0279)	-0.0157 (0.0116)	*-0.0040 (0.0070)		+0.0385 (0.0096)	*+0.36 (3.46)	-3.22 (1.48)	+0.128 (0.091)	+0.1458 (0.0535)	0.04284
*-0.0220 (0.0251)	-0.0362 (0.0099)	-0.0171 (0.0054)		+0.0584 (0.0077)	-4.56 (3.14)	-2.03 (1.39)	+0.262 (0.227)	*+0.0031 (0.0366)	0.04152

ng's modulus of elasticity at 98 days (after soaking in water for 28 days) to that at 70 with NAE cements, to various independent variables

K ₂ O	Loss	MgO	CaA SO ₃	Al ₂ O ₃ SO ₃	Со	Li	Zr	P	S.D.
-0.0461 (0.0187)	-0.0192 (0.0068)	-0.0091 (0.0032)	+0.0351 (0.0044)						0.04457
-0.0566 (0.0189)	-0.0191 (0.0067)	-0.0065 (0.0032)	+0.0340 (0.0043)		-3.48 (2.44)	-2.97 (1.05)	+0.149 (0.084)	+0.0422 (0.0312)	0.04305
-0.0894 (0.0260)	-0.0169 (0.0088)	*-0.0028 (0.0046)	+0.0292 (0.0073)		-7.88 (4.78)	-4.35 (1.38)	+0.155 (0.084)	+0.1266 (0.0506)	0.04076
*-0.0276 (0.0281)	-0.0223 (0.0107)	$-0.0101 \\ (0.0046)$	+0.0354 (0.0057)		* -2.69 (3.05)	-2.46 (1.63)	*-0.265 (0.863)	*+0.0093 (0.0414)	0.04391
-0.0524 (0.0193)	-0.0223 (0.0076)	-0.0145 (0.0045)		+0.0532 (0.0063)					0.04456
-0.0657 (0.0198)	-0.0233 (0.0076)	$-0.0132 \\ (0.0044)$		+0.0505 (0.0062)	-3.08 (2.43)	-2.88 (1.06)	+0.124 (0.085)	$^{+0.0361}_{(0.0314)}$	0.04336
-0.1127 (0.0284)	-0.0278 (0.0108)	-0.0150 (0.0066)		+0.0411 (0.0104)	*-4.33 (4.73)	-3.96 (1.43)	+0.124 (0.087)	+0.1172 (0.0524)	0.04219
*-0.0257 (0.0292)	-0.0244 (0.0118)	-0.0141 (0.0064)		+0.0547 (0.0083)	*-3.07 (3.09)	-2.61 (1.66)	*-0.324 (0.872)	*-0.0090 (0.0419)	0.04450

Table 13-45. Frequency distribution of cements with respect to AE 98/70, the ratio of dynamic modulus of Series A concretes determined after 4 weeks in water divided by the values after the previous 8 weeks in laboratory air

	Dynamic E ratio									
Type cement	1.00 to 1.05	1.05 to 1.10	1.10 to 1.15	1.15 to 1.20	1.20 to 1.25	1.25 to 1.30	1.30 to 1.35	1.35 to 1.40	1.40 to 1.45	Total
					Numbe	r of cements				
I_		16	34	18 2	10 2	1				79 8
IAII		10	21 2	16	14	4	2			67 3 20 3 15
III	. 8	4 2	7	1						20 3
IV, V.			5	5	2		2		1	15
Total	. 8	33	73	42	28	6	4	0	1	195

Eq. No.	Note		Const.	Air content	C ₃ A	C ₃ S	C ₄ AF	CaO	SiO ₂
1	1	AE 98/70 s.d.	= +1.447 = (0.040)	+0.00455 (0.00158)	+0.00458 (0.00134)	-0.00308 (0.00051)	+0.00334 (0.00177)		
2	1	AE 98/70 s.d.	= +1.332 = (0.059)	$^{+0.00469}_{(0.00155)}$	-0.01209 (0.00656)	$-0.00351 \\ (0.00053)$	$^{+0.00313}_{\ (0.00174)}$		
3	1	AE 98/70 s.d.	=+1.315 = (0.040)	$^{+0.00469}_{(0.00155)}$	-0.01446 (0.00228)	$-0.00358 \ (0.00050)$	$^{+0.00308}_{(0.00173)}$		
4	1	AE 98/70 s.d.	=+1.333 = (0.039)	$^{+0.00491}_{(0.00151)}$	$-0.01555 \ (0.00224)$	$-0.00376 \\ (0.00049)$	$^{+0.00325}_{(0.00169)}$		
4A	2	AE 98/70 (odd) s.d.	= +1.299 = (0.056)	$^{+0.00566}_{(0.00193)}$	$-0.01831 \ (0.00356)$	-0.00299 (0.00070)	$^{+0.00322}_{(0.00252)}$		
4B	2	AE 98/70 (even) s.d.	=+1.390 = (0.056)	$^{+0.00424}_{(0.00256)}$	$-0.01550 \ (0.00294)$	$ \begin{array}{c} -0.00471 \\ (0.00072) \end{array} $	*+0.00229 (0.00237)		
5	1	AE 98/70 s.d.	= +1.795 = (0.291)	$^{+0.00446}_{(0.00152)}$				-0.0187 (0.0040)	+0.0212 (0.0032)
6	1	AE 98/70 s.d.	=+1.918 = (0.285)	$^{+0.00452}_{(0.00148)}$				-0.0211 (0.0039)	+0.0230 (0.0032)
6A	2	AE 98/70 (odd) s.d.	=+1.595 = (0.468)	$^{+0.00499}_{(0.00192)}$				-0.0163 (0.0062)	+0.0233 (0.0050)
6B	2	AE 98/70 (even) s.d.	= +2.022 = (0.368)	$^{+0.00427}_{(0.00251)}$				-0.0238 (0.0052)	+0.0258 (0.0043)

Note 1, 172 cements, Avg. = 1.148, S.D. = 0.06000 Note 2, $\,$ 86 cements

Table 13-47. Coefficients for equations relating AE 98/70, the ratio of dynamic You (after drying in air) of Series A concretes made

						(1910)			
Eq. No.	Note		Const.	Air content	C3A	C ₃ S	C ₄ AF	CaO	SiO ₂
1	1	AE 98/70 s.d.	=+1.435 = (0.042)	+0.00674 (0.00385)	$+0.00493 \\ (0.00138)$	-0.00309 (0.00053)	$^{+0.00375}_{(0.00180)}$		
2	1	AE 98/70 s.d.	= +1.332 = (0.061)	$^{+0.00698}_{(0.00380)}$	$-0.01019 \ (0.00673)$	$-0.00346 \ (0.00055)$	$^{+0.00352}_{(0.00178)}$		
3	1	AE 98/70 s.d.	=+1.304 = (0.041)	$^{+0.00700}_{(0.00380)}$	-0.01411 (0.00237)	-0.00357 (0.00052)	+0.00343 (0.00177)		
4	1	AE 98/70 s.d.	=+1.322 = (0.040)	$^{+0.00854}_{(0.00386)}$	$-0.01528 \ (0.00232)$	$-0.00376 \ (0.00051)$	$^{+0.00358}_{(0.00173)}$		
4A	2	AE 98/70 (odd) s.d.	= +1.282 = (0.059)	*+0.00532 (0.00657)	-0.01652 (0.00364)	$-0.00367 \ (0.00072)$	+0.00597 (0.00288)		
4B	3	AE 98/70 (even) s.d.	= +1.355 = (0.058)	+0.01100 (0.00495)	$-0.01431 \ (0.00317)$	$-0.00408 \\ (0.00076)$	+0.00244 (0.00225)		
5	1	AE 98/70 s.d.	=+1.891 = (0.297)	$^{+0.00609}_{(0.00373)}$				-0.0199 (0.0040)	+0.0202 (0.0033)
6	1	AE 98/70 s.d.	= +2.010 = (0.290)	$^{+0.00751}_{(0.00379)}$				-0.0223 (0.0040)	+0.0222 (0.0033)
6A	2	AE 98/70 (odd) s.d.	= +2.103 = (0.483)	*+0.00297 (0.00654)				-0.0237 (0.0064)	+0.0219 (0.0053)
6B	3	AE 98/70 (even) s.d.	= +1.964 = (0.366)	$^{+0.01103}_{(0.00479)}$				-0.0219 (0.0051)	$^{+0.0231}_{(0.0043)}$

Note 1, 161 cements, Avg. = 1.148, S.D. = 0.05965 Note 2, 81 cements Note 3, 80 cements

^{*}Coef./s.d. ratio less than 1.

^{*}Coef./s.d. ratio less than 1.

ng's modulus of elasticity at 98 days (after 28 days soaking in water) to that at 70 days AE+NAE cements, to various independent variables

SO ₃	K ₂ O	Loss	C ₃ A SO ₃	Al ₂ O ₃ SO ₃	MgO	Li	P	Со	S.D.
-0.0856 (0.0106)	-0.0519 (0.0168)	-0.0158 (0.0062)			-0.00929 (0.00290)				0.04053
*-0.0117 (0.0303)	-0.0527 (0.0165)	$-0.0181 \ (0.0062)$	$^{+0.0313}_{(0.0120)}$		$-0.00858 \ (0.00286)$				0.03983
	-0.0532 (0.0164)	-0.0187 (0.0060)	+0.0357 (0.0041)		$-0.00850 \\ (0.00285)$				0.03973
	-0.0632 (0.0164)	$ \begin{array}{r} -0.0172 \\ (0.0059) \end{array} $	+0.0356 (0.0040)		$-0.00716 \ (0.00281)$	-2.19 (0.91)	+0.0667 (0.0291)	-3.22 (2.13)	0.03861
	-0.0611 (0.0241)	-0.0160 (0.0087)	+0.0384 (0.0062)		$-0.00448 \\ (0.00409)$	-2.74 (1.47)	+0.1949 (0.0591)	-6.43 (3.31)	0.03887
	$-0.0590 \\ (0.0241)$	-0.0181 (0.0087)	+0.0372 (0.0054)		$-0.01158 \ (0.00428)$	-1.62 (1.22)	*+0.0317 (0.0341)	*+0.22 (2.95)	0.03792
	-0.0565 (0.0168)	-0.0217 (0.0068)		+0.0566 (0.0058)	$-0.01314 \ (0.00394)$				0.03965
	-0.0698 (0.0169)	$-0.0215 \\ (0.0067)$		+0.0551 (0.0056)	$-0.01288 \ (0.00384)$	-2.28 (0.91)	+0.0605 (0.0289)	-3.28 (2.10)	0.03853
	$-0.0754 \\ (0.0242)$	-0.0157 (0.0107)		+0.0547 (0.0088)	$-0.00729 \\ (0.00648)$	-2.92 (1.49)	+0.1741 (0.0597)	-5.15 (3.23)	0.03936
	$-0.0651 \\ (0.0251)$	$-0.0225 \\ (0.0093)$		+0.0600 (0.0076)	$-0.01699 \ (0.00517)$	-1.74 (1.20)	*+0.0322 (0.0337)	* -0.31 (2.94)	0.03786

ng's modulus of elasticity at 98 days (after 28 days soaking in water) to that at 70 days with NAE cements, to various independent variables

SO ₃	K ₂ O	Loss	C ₃ A SO ₃	$\frac{\text{Al}_2\text{O}_3}{\text{SO}_3}$	MgO	Li	P	Со	S.D.
-0.0857 (0.0107)	-0.0533 (0.0175)	-0.0127 (0.0064)			-0.00939 (0.00296)				0.04050
*-0.0192 (0.0309)	$-0.0535 \\ (0.0173)$	$-0.0151 \\ (0.0064)$	+0.0282 (0.0123)		$-0.00876 \ (0.00294)$				0.03995
	-0.0543 (0.0172)	$-0.0162 \\ (0.0062)$	+0.0354 (0.0042)		$-0.00863 \ (0.00292)$				0.03986
	$-0.0665 \\ (0.0174)$	$-0.0142 \\ (0.0061)$	$^{+0.0354}_{(0.0041)}$		-0.00699 - (0.00290)	-2.46 (0.95)	+0.0604 (0.0295)	-3.39 (2.20)	0.03864
	-0.0536 (0.0270)	$-0.0190 \ (0.0111)$	$^{+0.0394}_{(0.0064)}$		*-0.00420 (0.00440)	-2.21 (1.60)	+0.1687 (0.0504)	*1.92 (2.87)	0.04000
	$-0.0760 \\ (0.0242)$	-0.0137 (0.0078)	$^{+0.0339}_{(0.0056)}$		$-0.00870 \ (0.00421)$	-2.93 (1.28)	*-0.0046 (0.0380)	-6.89 (3.76)	0.03704
	-0.0589 (0.0175)	$-0.0200 \ (0.0070)$		+0.0564 (0.0059)	$-0.01428 \ (0.00405)$				0.03962
	-0.0745 (0.0177)	-0.0191 (0.0068)		+0.0551 (0.0057)	$^{-0.01371}_{(0.00394)}$	-2.52 (0.94)	+0.0552 (0.0292)	-3.48 (2.16)	0.03837
	$-0.0703 \\ (0.0277)$	$-0.0226 \ (0.0131)$		+0.0591 (0.0091)	$-0.01249 \ (0.00649)$	-2.33 (1.60)	+0.1667 (0.0510)	*-1.43 (2.83)	0.04038
	-0.0802 (0.0243)	-0.0180 (0.0082)		+0.0570 (0.0078)	-0.01427 (0.00511)	-3.09 (1.23)	*-0.0106 (0.0363)	-7.92 (3.64)	0.03593

Table 13-48. Calculated contributions of independent variables to AE 98/70, the ratio of the dynamic modulus of Series A concretes after 28 days in water divided by the dynamic modulus after the previous 8 weeks in air

Inde- pendent variable	Range of variables (percent)	Coefficients from eq 4 table 13-47	Calculated contributions to AE98/70	Calculated range of contribu- tions to AE98/70
Air- content, NAE			Const. = +1.322	
cements_ C ₃ A C ₃ S C ₄ AF K ₂ O	0 to 4.5 1 to 15 20 to 65 1 to 17 0 to 1.1	$ \begin{array}{r} +0.00854 \\ -0.01528 \\ -0.00376 \\ +0.00358 \\ -0.0665 \end{array} $	0 to +0.038 -0.015 to -0.229 -0.075 to -0.244 +0.004 to +0.061 0 to -0.073	0.038 0.214 0.169 0.057 0.073
Loss	0.3 to 3.3 0.4 to 10.1 0 to 5.0 0 to 0.02 0 to 0.5 0 to 0.01	$ \begin{array}{r} -0.0142 \\ +0.0354 \\ -0.00699 \\ -2.46 \\ +0.0604 \\ -3.39 \end{array} $	-0.004 to -0.047 +0.014 to +0.358 -0.007 to -0.035 0 to -0.049 0 to +0.030 0 to -0.033	0.043 0.344 0.028 0.049 0.030 0.033

^{**}Coefficient of doubtful significance as coef./s.d. ratio was less than 2.0.

Table 13-49. Frequency distribution of cements with respect to OE 71/70, the ratio of dynamic modulus of Series O concretes determined after 24 hours in water divided by the values after the previous 8 weeks in laboratory air

				D	ynamic	E rati	io		
Type cement	0.92 to 0.94	0.94 to 0.96	0.96 to 0.98	0.98 to 1.00	1.00 to 1.02	1.02 to 1.04	1.04 to 1.06	1.06 to 1.08	Total
			N.	umber	of cem	ents			
I IA II	1	7 2	18 1 18	24 3 17	16 2 19	10 1 3 2	<u>-</u>	i	76 8 64 3
IIA III IIIA IV, V		<u>4</u> 1	7 1 1	7 2 4	$\begin{bmatrix} 1\\2\\\frac{1}{4} \end{bmatrix}$	 1			20 3 13
Total	1	14	46	57	44	17	7	1	187

air-dried Series A concretes (AE71/70) is presented in table 13–53. As was found for the Series O concretes, the Series A concretes made with most of the cements showed a slight reduction of dynamic modulus when the air-dried specimens were placed in water for 24 hours. There was an overlapping of the values for the concretes made with the different types of cement.

Equations are presented in table 13-54 indicating the independent variables associated with the AE71/70 dynamic-modulus ratio of concretes made with AE + NAE cements. The use of the commonly determined independent variables, air content, C₃A, C₃S, K₂O, C₃A/SO₃ and MgO in eq 1 resulted in a highly significant reduction of the S.D. value. The additional use of the trace elements Zr, Co, Li, Rb, and Ni as independent variables in eq 2 resulted in a further significant reduction of variance. In eq 4 the use of the trace elements Zr, Co, Li, Rb, Ni, and Ti, together with the commonly determined variables, also resulted in a significant reduction of variance. (See table 13-57.)

In eqs 2A, 2B, 4A, and 4B calculated for the

"odds" and "evens" in the array of cements the coef./s.d. ratios for C₃S, Loss, MgO, Zr, Rb, Ni, and Ti were less than 1.0 in one or more of the

equations for the smaller lots of cement.

A corresponding series of equations for the NAE cements is presented in table 13-55. The independent variables, their coefficients, and coef./s.d. ratios were generally in agreement with those of the previous table where the AE cements were included. The use of commonly determined independent variables or these with the trace elements resulted in a significant reduction of variance.

Using the coefficients of the independent variables of eq 2 table 13-55 and the ranges of these variables, computations were made of the estimated contributions to the AE71/70 dynamicmodulus values. These calculated contributions are presented in table 13-56 together with the calculated ranges of these contributions. Higher values for air content and C₃A/SO₃ were associated with higher ratios (AE71/70).

Higher values for C₃A, K₂O, and possibly Loss, MgO, and Li were associated with lower values

for the ratio.

Table 13-50. Coefficients for equations relating OE 71/70, the ratio of dynamic Young's modulus of elasticity at 71 days (after soaking in water for 24 hours) to that at 70 days (after drying in air) of Series O concretes made with AE + NAE cements, to various independent variables

S.D.	0.01967	0.01835	0.01789	0.01892	0.01941	0.01821	0.01771	0.01888
Mn		-0.0199 (0.0122)	-0.0478 (0.0208)	*+0.0013 (0.0163)		(0.0116)	-0.0465 (0.0201)	*-0.0028 (0.0155)
Zr	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	+0.130 (0.036)	+0.241 (0.095)	+0.109 (0.041)		+0.131 (0.035)	+0.232 (0.093)	+0.119 (0.040)
ž	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	-0.898	-0.651 (0.633)	-1.081 (0.698)		-0.812 (0.437)	*-0.556	-0.850 (0.671)
Co	1 1 3 1 1 1 1 1 1 1 1 1 1 1	$\frac{-2.07}{(1.05)}$	+2.35 (1.43)	-2.54 (1.63)	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	$\frac{-1.83}{(1.04)}$	-2.10 (1.40)	* -1.53 (1.60)
MgO	-0.00285 (0.00141)	$\begin{array}{c} -0.00215 \\ (0.00138) \end{array}$	* -0.00016 (0.00191)	-0.00541 (0.00219)	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1		1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1
Loss	-0.0148 (0.0030)	-0.0165 (0.0028)	(0.0038)	-0.0160 (0.0047)	-0.0115 (0.0031)	-0.0139 (0.0030)	-0.0153 (0.0040)	(0.0048)
Al ₂ O ₃				1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	$^{+0.0107}_{(0.0027)}$	+0.0087 (0.0026)	+0.0072 (0.0042)	+0.0102 (0.0034)
C ₃ A SO ₃	+0.00819 (0.00193)	+0.00702 (0.00182)	+0.00645	+0.00768 (0.00243)		1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1		
K ₂ O	(0.0080)	-0.0213 (0.0077)	-0.0194 (0.0112)	-0.0140 (0.0118)	-0.0206 (0.0077)	-0.0195 (0.0074)	-0.0204 (0.0098)	* -0.0093
SiO ₂			1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	+0.00737 (0.00147)	+0.00655 (0.00140)	+0.00448 (0.00191)	+0.00938 (0.00220)
C ₃ S	-0.000397 (0.000238)	-0.000413 (0.000226)	-0.000154 (0.000286)	-0.000830 (0.000392)		1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	
C3A	-0.00446 (0.00107)	-0.00412 (0.00100)	-0.00377 (0.00155)	-0.00453 (0.00144)	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1		1 1	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1
Air	+0.00456 -0.00446 (0.00086) (0.00107)	+0.00435 (0.00081)	+0.00510 (0.00122)	+0.00331 (0.00119)	+0.00428	+0.00408	+0.00480 (0.00113)	+0.00305 (0.00119)
Const.	= +1.038 = (0.013)	= +1.046 = (0.013)	OE $71/70 \text{ (odd)} = +1.027$ s.d. = (0.017)	en) = +1.072 = (0.022)	= +0.817 = (0.039)	= +0.847 = (0.037)		en) = $+0.774$ = (0.058)
	OE 71/70 s.d.	OE 71/70 s.d.	OE 71/70 (od s.d.	OE $71/70$ (even) = $+1.072$ s.d. = (0.022)	OE 71/70 s.d.	OE 71/70 s.d.	OE $71/70 \text{ (odd)} = +0.897$ s.d. = (0.051)	OE $71/70$ (even) = $+0.774$ s.d. = (0.058)
Note	-	-	63	ಣ	-	-	61	9
NEG.	1	2	2A	2B	3	4	4A	4B

Note 1, 169 cements, Avg. = 0.9922, S.D. = 0.02501 Note 2, 85 cements Note 3, 84 cements

*Coef./s.d. ratio less than one.

TABLE 13-51. Coefficients for equations relating OE 71/70, the ratio of dynamic Young's modulus of elasticity at 71 days (after soaking in water for 24 hours) to that at 70 days (after drying in air) of Series O concretes made of NAE cements, to various independent variables

S.D.	0.01981	0.01844	0.01954	0.01785	0.01965	0.01841	0.01910	0.01808
Mn		(0.0128)	(0.0207)	*-0.0110 (0.0174)		(0.0123)	0.0228	*-0.0091 (0.0164) -
Zr	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	+0.128 (0.036)	*+0.259 (0.296)	+1.040 (0.038)		+0.131 (0.036)	+0.346	+0.108 (0.038)
ä		-1.12 (0.46)	*-0.61	-1.55 (0.59)		-0.97 (0.45)	*-0.62 (0.78)	(0.57)
Co	1 1	$\frac{-1.63}{(1.10)}$	-1.61 (1.43)	*-1.77 (2.16)		-1.43 (1.09)	-1.59 (1.38)	*-1.35 (2.19)
MgO	-0.00335 (0.00146)	-0.00284 (0.00142)	* -0.00135 (0.00210)	-0.00392 (0.00224)	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1			
Loss	-0.0142 (0.0031)	-0.0156 (0.0030)	-0.0166 (0.0047)	-0.0134 (0.0044)	-0.0109 (0.0032)	-0.0130 (0.0031)	-0.0146 (0.0048)	-0.0104 (0.0044)
Al ₂ O ₃					+0.0104 (0.0028)	+0.0085	*+0.0043 (0.0045)	+0.0105 (0.0034)
C ₃ A SO ₃	+0.00768 (0.00198)	+0.00646 (0.00187)	+0.00403 (0.00338)	+0.00782 (0.00237)		1 1		
K2O	-0.0212 (0.0085)	-0.0200 (0.0082)	-0.0189 (0.0130)	-0.0227 (0.0109)	-0.0209 (0.0081)	-0.0198 (0.0078)	-0.0176 (0.0144)	-0.0207 (0.0110)
SiO ₂			1 7 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1		+0.00709 (0.00153)	+0.00637 (0.00146)	+0.00405 (0.00208)	+0.00883 (0.00215)
CaS	-0.000395 (0.000249)	-0.000420 (0.000236)	*-0.000166 (0.000332)	-0.000745 (0.000375)	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1		1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	
C3A	-0.00427 (0.00111)	-0.00395 (0.00104)	-0.00235 (0.00175)	-0.00511 (0.00141)				
Air	+0.00600 (0.00224)	= +1.045 +0.00634 $= (0.013) (0.00211)$	+0.00526 (0.00371)	+0.00736 (0.00270)	+0.00555 (0.00220)	+0.00570 (0.00208)	+0.00436 (0.00357)	+0.00624 (0.00265)
Const.	= +1.037 = (0.014)	= +1.045 = (0.013)	OE $71/70 \text{ (odd)} = +1.024$ 8.d. = (0.021)	OE $71/70$ (even) = $+1.068$ s.d. = (0.019)	= +0.821 = (0.040)	= +0.848 = (0.039)	OE $71/70 \text{ (odd)} = +0.909$ 8.d. $= (0.056)$	OE $71/70$ (even) = $+0.788$ s.d. = (0.057)
	OE 71/70 8.d.	OE 71/70 s.d.	OE 71/70 (o s.d.	OE 71/70 (e ⁸ .d.	OE 71/70 s.d.	OE 71/70 s.d.	OE 71/70 (o s.d.	OE 71/70 (e s.d.
Note	1	-	21	က		-	23	m
NEG.	1	2	2A	2B	63	4	4A	4B

Note 1, 157 cements, Avg. = 0.9911, S.D. = 0.02460 Note 2, 79 cements Note 3, 78 cements *Coef./s.d. ratio less than one.

Table 13-52. Calculated contributions of independent variables to OE 71/70, the ratio of dynamic modulus of Series O concretes after 24 hours in water divided by the dynamic modulus after the previous 8 weeks in air

Inde- pendent variable	Range of variables (percent)	Coefficients from eq 2 table 13–51	Calculated contributions to OE71/70	Calculated range of contribu- tions to OE71/70
Air- content, NAE cements C ₃ A C ₃ S** K ₂ O. C ₃ S** K ₂ O. C ₃ C ₃ A/SO ₃ Loss MgO Co** Ni Zr Mn**	0 to 4.5 1 to 15 20 to 65 0 to 1.1 0.4 to 10.1 0.3 to 3.3 0 to 5.0 0 to 0.01 0 to 0.02 0 to 0.5 0 to 1.0	+0.00634 -0.00395 -0.00042 -0.020 +0.00646 -0.0156 -0.00284 -1.63 -1.12 +0.128 -0.0152	Const. = +1.045 0 to +0.029 -0.004 to -0.059 -0.008 to -0.027 0 to -0.022 +0.003 to -0.051 0 to -0.014 0 to -0.016 0 to -0.022 0 to +0.064 0 to -0.015	0.029 0.055 0.019 0.022 0.062 0.046 0.014 0.016 0.022 0.064 0.015

^{**}Coefficient of doubtful significance as coef./s.d. ratio was less than 2.0.

Table 13-53. Frequency distribution of cements with respect to AE71/70, the ratio of dynamic modulus of Series A concretes determined after 24 hours in water divided by the values after the previous 8 weeks in laboratory air

Type cement	0.94 to 0.96	0.96 to 0.98	0.98 to 1.00	1.00 to 1.02	1.02 to 1.04	1.04 to 1.06	Total
		N	umber o	of cemer	nts		
[6	23	24	12 4	9		74
I	2	18	2 15	19	9 2 5 1	4	63
IA	3	9	5 2 5	1 3 1	1		20
V, V		<u>i</u>	2 5	1 4	<u>ī</u>	2	74 8 63 3 20 3 13
Total	. 11	51	54	44	18	6	184

Table 13-54. Coefficients for equations relating AE 71/70, the ratio of dynamic Yo days (after drying in air) of Series A concretes made

Eq. No.	Note		Const.	Air content	C ₂ A	C ₃ S	SiO ₂	K ₂ O	Loss
1	1	AE 71/70 s.d.	= +1.030 = (0.012)	+0.00379 (0.00071)	-0.00428 (0.00103)	-0.000394 (0.000223)		-0.0205 (0.0077)	-0.00906 (0.00281)
2	1	AE 71/70 s.d.	= +1.038 = (0.012)	+0.00399 (0.00068)	-0.00454 (0.00099)	-0.000382 (0.000216)		-0.0295 (0.0086)	-0.00882 (0.00279)
2A	2	AE 71/70 (odd) s.d.	= +1.038 = (0.018)	$^{+0.00377}_{(0.00116)}$	-0.00296 (0.00155)	-0.000446 (0.000280)		-0.0245 (0.0118)	-0.01102 (0.00382)
2B	3	AE 71/70 (even) s.d.	= +1.035 = (0.020)	+0.00434 (0.00097)	-0.00537 (0.00141)	* -0.000263 (0.000385)		-0.0370 (0.0148)	-0.00656 (0.00467)
3	1	AE 71/70 s.d.	= +0.841 = (0.039)	$^{+0.00364}_{(0.00070)}$			+0.00612 (0.00145)	-0.0185 (0.0076)	-0.00652 (0.00299)
4	1	AE 71/70 s.d.	= +0.842 = (0.038)	$^{+0.00393}_{(0.00068)}$			+0.00657 (0.00141)	-0.0288 (0.0085)	-0.00682 (0.00299)
4A	2	AE 71/70 (odd) s.d.	=+0.882 = (0.052)	$^{+0.00370}_{(0.00115)}$			+0.00485 (0.00189)	$-0.0256 \\ (0.0113)$	$-0.00994 \\ (0.00411)$
4B	3	AE 71/70 (even) s.d.	= +0.797 = (0.060)	+0.00422 (0.00096)			+0.00833 (0.00228)	-0.0307 (0.0149)	*-0.00243 (0.00492)

Note 1, 163 cements, Avg. = 0.9909, S.D. = 0.02300 *Coef./s.d. ratio less than one.

Note 2, 82 cements

Note 3, 81 cements

Table 13-55. Coefficients for equations relating AE 71/70, the ratio of dynamic Youn days (after drying in air) of Series A concretes made

Eq. No.	Note		Const.	Air content	CaA	CaS	SiO ₂	K ₂ O	Loss
1	1	AE 71/70 s.d.	= +1.026 = (0.013)	+0.00513 (0.00180)	-0.00435 (0.00109)	-0.000352 (0.000237)		-0.0206 (0.0083)	-0.00856 (0.00298)
2	1	AE 71/70 s.d.	= +1.035 = (0.013)	$^{+0.00635}_{(0.00177)}$	-0.00468 (0.00104)	-0.000358 (0.000227)		-0.0305 (0.0091)	-0.00790 (0.00294)
2A	2	AE 71/70 (odd) s.d.	= +1.044 = (0.019)	$^{+0.00761}_{(0.00284)}$	-0.00558 (0.00176)	-0.000451 (0.000339)		-0.0277 (0.0137)	-0.01046 (0.00474)
2B	2	AE 71/70 (even) s.d.	= +1.027 = (0.021)	+0.00589 (0.00260)	-0.00433 (0.00146)	* -0.000341 (0.000354)		$-0.0372 \\ (0.0139)$	$-0.00459 \\ (0.00427)$
3	1	AE 71/70 s.d.	= +0.844 = (0.041)	+0.00481 (0.00179)			+0.00592 (0.00153)	$-0.0195 \\ (0.0081)$	-0.00604 (0.00316)
4	1	AE 71/70 s.d.	= +0.841 = (0.040)	$^{+0.00646}_{(0.00180)}$			+0.00649 (0.00148)	-0.0311 (0.0090)	-0.00599 (0.00314)
4A	2	AE 71/70 (odd) s.d.	= +0.822 = (0.062)	+0.00785 (0.00278)			+0.00766 (0.00224)	-0.0317 (0.0130)	-0.01016 (0.00494)
4B	2	AE 71/70 (even) s.d.	= +0.851 = (0.056)	+0.00515 (0.00267)			+0.00566 (0.00212)	-0.0353 (0.0140)	*-0.00226 (0.00458)

Note 1, 152 cements, Avg. = 0.9899, S.D. = 0.2291

*Coef./s.d. ratio less than 1.

Note 1, 76 cements

Table 13-56. Calculated contributions of independent variables to AE 71/70, the ratio of the dynamic modulus of Series A concretes after 24 hours in water divided by the dynamic modulus after the previous 3 weeks in air

Inde- pendent variable	Range of variables (percent)	Coefficients from eq 2 table 13-55	Calculated contributions to AE71/70	Calculated range of contribu- tions to AE71/70
Air- content,			Const. = +1.035	
NAE cements_	0 to 4.5 1 to 15	+0.00635 -0.00468	0 to +0.029 -0.005 to -0.070	0.029 0.065
C ₃ S** K ₂ O Loss	20 to 65 0 to 1.1 0.3 to 3.3	-0.000358 -0.0305 -0.0079	-0.007 to -0.023 0 to -0.034 -0.002 to -0.026	0.016 0.034 0.024
C3A/SO3 MgO Zr**	0.4 to 10.1 0 to 5.0 0 to 0.5	+0.0081 -0.00307 +0.0567	+0.003 to +0.082 0 to -0.015 0 to +0.028	0.079 0.015 0.028
Co** Li Rb**	0 to 0.01 0 to 0.02 0 to 0.01	$ \begin{array}{r} -1.82 \\ -0.912 \\ +1.68 \end{array} $	0 to -0.018 0 to -0.018 0 to +0.017	$0.018 \\ 0.018 \\ 0.017$
Ni	0 to 0.02	-1.08	0 to -0.022	0.022

^{**}Coefficient of doubtful significance as coef./s.d. ratio was less than 2.0.

ung's modulus of elasticity at 71 days (after soaking in water for 24 hours) to that at 70 of AE+NAE cements, to various independent variables

C ₃ A SO ₃	Al ₂ O ₃ SO ₃	MgO	Zr	Со	Li	Rb	Ni	Ti	S.D.
+0.00855 (0.00190)		-0.00388 (0.00135)							0.01837
+0.00811 (0.00182)		$-0.00328 \ (0.00134)$	+0.0580 (0.0341)	-1.85 (1.01)	$-0.743 \\ (0.430)$	+1.84 (0.87)	-0.978 (0.453)		0.01739
+0.00496 (0.00302)		$-0.00261 \\ (0.00206)$	+0.2239 (0.0887)	-1.81 (1.36)	-0.780 (0.587)	+1.86 (1.08)	-0.813 (0.606)		0.01697
+0.00986 (0.00248)		-0.00382 (0.00206)	*+0.0217 (0.0404)	-1.91 (1.61)	$-0.663 \\ (0.662)$	*+1.59 (1.60)	-1.144 (0.769)		0.01842
	+0.0114 (0.0027)	$-0.00234 \ (0.00137)$							0.01823
	+0.0108 (0.0026)	$-0.00191 \ (0.00137)$	+0.0656 (0.0343)	$-1.65 \\ (0.99)$	-0.813 (0.426)	+1.88 (0.86)	$-0.788 \ (0.455)$	$-0.0190 \ (0.0122)$	0.01726
	+0.00840 (0.00431)	*-0.00115 (0.00212)	+0.2418 (0.0904)	-1.86 (1.34)	-0.804 (0.588)	+2.09 (1.08)	*-0.527 (0.609)	*-0.0202 (0.0220)	0.01686
	+0.01319 (0.00357)	-0.00237 (0.00207)	*+0.0251 (0.0400)	-1.78 (1.57)	-0.848 (0.662)	*+1.35 (1.56)	-1.137 (0.746)	-0.0250 (0.0160)	0.01814

g's modulus of elasticity at 71 days (after soaking in water for 24 hours) to that at 70 of NAE cements, to various independent variables

CaA SOa	Al ₂ O ₃ SO ₃	MgO	Zr	Со	Li	Rb	Ni	Ti	S.D.
+0.00851 (0.00199)		-0.00382 (0.00142)							0.01881
+0.00810 (0.00189)		$-0.00307 \\ (0.00141)$	+0.0567 (0.0349)	-1.82 (1.07)	$ \begin{array}{c c} -0.912 \\ (0.455) \end{array} $	+1.68 (0.90)	$-1.08 \\ (0.47)$		0.01767
+0.00964 (0.00329)		$-0.00392 \\ (0.00230)$	+0.0542 (0.0405)	-3.77 (2.51)	-1.279 (0.706)	*+0.88 (1.29)	-0.72 (0.70)		0.01898
+0.00779 (0.00263)		$ \begin{array}{c} -0.00222 \\ (0.00216) \end{array} $	*+0.1258 (0.4165)	*-1.15 (1.26)	-0.757 (0.668)	+2.57 (1.49)	-1.43 (0.74)		0.01751
	+0.0112 (0.0028)	$-0.00237 \\ (0.00144)$							0.01870
	+0.0108 (0.0027)	-0.00181 (0.00145)	+0.0653 (0.0351)	-1.59 (1.05)	$-0.990 \\ (0.453)$	+1.72 (0.89)	-0.87 (0.47)	-0.0222 (0.0131)	0.01757
	+0.0121 (0.0045)	-0.00259 (0.00223)	+0.0703 (0.0397)	*-2.39 (2.40)	$-1.592 \\ (0.684)$	*+0.90 (1.21)	*-0.43 (0.68)	-0.0426 (0.0172)	0.01826
	$^{+0.0098}_{(0.0038)}$	*-0.00070 (0.00225)	*+0.1160 (0.4206)	*-1.10 (1.27)	-0.685 (0.666)	+2.55 (1.51)	-1.46 (0.74)	*-0.0081 (0.0230)	0.01756

Table 13-57. "F" values for significance of reduction of variance due to added variables—Continued

Table	Equation*	"F" ratio	D.F.**	Critical "F" Ratio		
14510			D.1.	$\alpha = 0.01$	$\alpha = 0.05$	
13-2	0,1	62.1	9:171	2.52	1.93	
	1,2	4.03	3:168	3.88	2.67	
	0,3	55.8	10:170	2.40	1.89	
	3,4	4.0	3:167	3.88	2.67	
13-3	0,1	26.5	8:160	2.62	2.00	
	1,2	2.61	4:156	3.44	2.42	
	0,3	23.5	9:159	2.52	1.93	
	3,4	2.60	4:155	3.43	2.42	
13-6	0,1	25.1	2:171	4.72	3.05	
	0,2	9.0	2:171	4.72	3.05	
	0,3	17.4	3:170	3.88	2.67	
	3,4	35.3	6:164	2.92	2.15	
	4,5	3.27	2:162	4.74	3.05	
	0,6	32.3	10:163	2.40	1.89	
	6,7	2.50	3:160	3.89	2.67	
13-7	0,4 4,5 0,6 6,7	20.8 2.66 18.7 2.71	9:153 3:150 10:152 3:149	2.52 3.90 2.40 3.90	1.93 2.67 1.89 2.67	
13-10	0,1	60.9	9:170	2.52	1.93	
	1,2	3.89	1:169	6.77	3.90	
	0,3	63.3	9:170	2.52	1.93	
	3,4	3.34	1:169	6.77	3.90	
13–11	0,1	32.1	9:158	2.52	1.93	
	1,2	3.54	1:157	6.78	3.90	
	0,3	33.2	9:158	2.52	1.93	
	3,4	3.20	1:157	6.78	3.90	
13–14	0,1	12.3	2:171	4.72	3.05	
	0,2	4.51	2:171	4.72	3.05	
	0,3	8.60	3:170	3.88	2.67	
	3,4	27.8	7:163	2.75	2.07	
	4,5	2.72	3:160	3.89	2.67	
	0,6	29.0	9:164	2.52	1.93	
	6,7	3.45	2:162	4.73	3.05	
13-15	0,4 4,5 0,6 6,7	18.9 2.96 21.9 3.49	10:152 3:149 9:153 2:151	2.40 3.90 2.52 4.75	1.89 2.67 1.93 3.05	
13-18	0,1	63.9	10:169	2.40	1.89	
	1,2	1.38	1:168	6.76	3.90	
	0,3	69.9	9:170	2.52	1.93	
	3,4	1.38	1:169	6.76	3.90	
13–19	0,1 1,2 0,3 3,4	37.5 1.35 40.9 1.35	10:157 1:156 9:158 1:157	2.40 6.78 2.52 6.78	1.89 3.90 1.93 3.90	
13-22	0,1	14.8	2:171	4.72	3.05	
	0,2	6.10	2:171	4.72	3.05	
	0,3	10.1	3:170	3.88	2.67	
	3,4	43.5	8:162	2.62	2.00	
	4,5	2.40	1:161	6.77	3.90	
	0,6	35.4	10:163	2.40	1.89	
	6,7	2.23	1:162	6.77	3.90	
13-23	0,4	24.5	11:151	2.38	1.87	
	4,5	3.96	1:150	6.78	3.90	
	0,6	26.7	10:152	2.40	1.89	
	6,7	3.47	1:151	6.78	3.90	
13–26	0,1	91.1	8:171	2.62	2.00	
	1,2	6.09	3:168	3.88	2.67	
	0,3	80.6	9:170	2.52	1.93	
	3,4	6.45	3:167	3.88	2.67	
13-27	0,1 1,2 0,3 3,4	$21.5 \\ 6.40 \\ 19.1 \\ 7.05$	8:159 3:156 9:158 3:155	2.62 3.89 2.52 3.89	2.00 2.67 1.93 2.67	
13-30	0,1	74.5	3:170	3.88	2.67	
	1,2	12.5	5:165	3.13	2.28	
	2,3	4.72	5:160	3.13	2.28	
	0,4	40.2	9:164	2.52	1.93	
	4,6	4.47	4:160	3.43	2.42	
13-31	0,1	22.8	3:159	3.89	2.67	
	1,2	12.6	5:154	3.14	2.28	
	2,3	4.91	5:149	3.14	2.28	
	0,4	17.3	9:153	2.52	1.93	
	4,5	4.55	4:149	3.44	2.42	

Table	Equation*	ion* "F" ratio	D.F.**	Critical	Critical "F" Ratio		
				$\alpha = 0.01$	$\alpha = 0.05$		
13-34	0,1	22.5	7:172	2.75	2.07		
	1,2	3.38	3:169	3.88	2.67		
	0,3	19.4	8:169	2.62	2.00		
	3,4	3.76	3:168	3.88	2.67		
13-35	0,1 1,2 0,3 3,4	20.8 2.72 20.9 3.12	8:159 3:156 8:159 3:156	2.62 3.89 2.62 3.89	2.00 2.67 2.00 2.67		
13-38	0,1	18.8	8:163	2.62	2.00		
	1,2	3.23	3:160	3.88	2.67		
	0,3	18.6	8:163	2.62	2.00		
	3,5	3.51	3:160	3.88	2.67		
13-39	0,1 1,2 0,3	$18.0 \\ 2.30 \\ 17.8$	9:151 3:148 9:151	2.53 3.90 2.53	1.93 2.67 1.93		
13-42	0,1	26.2	9:170	2.52	1.93		
	1,2	3.70	4:166	3.43	2.42		
	0,3	29.0	8:171	2.62	2.00		
	3,4	3.10	4:167	3.43	2.42		
13-43	0,1	23.7	9:158	2.52	1.93		
	1,2	3.84	4:154	3.44	2.42		
	0,3	26.5	8:159	2.62	2.00		
	3,4	3.23	4:155	3.44	2.42		
13-46	0,1	23.8	9:163	2.52	1.93		
	1,2	6.78	1:162	6.77	3.90		
	0,3	25.5	9:163	2.52	1.93		
	3,4	4.20	3:160	3.88	2.67		
	0,5	28.7	8:164	2.62	2.00		
	5,6	4.22	3:161	3.88	2.67		
13–47	0,1	21.8	9:152	2.53	1.93		
	1,2	5.21	1:151	6.78	3.90		
	0,3	23.2	9:152	2.53	1.93		
	3,4	4.25	3:149	3.90	2.67		
	0,5	26.5	8:153	2.62	2.00		
	5,6	4.38	3:150	3.90	2.67		
13-50	0,1 1,2 0,3 3,4	$\begin{array}{c} 14.0 \\ 7.0 \\ 19.6 \\ 6.55 \end{array}$	8:161 4:157 6:163 4:159	2.62 3.43 2.92 3.43	2.00 2.42 2.15 2.42		
13-51	0,1	11.6	8:149	2.62	2.00		
	1,2	6.74	4:145	3.44	2.42		
	0,3	15.8	6:151	2.92	2.15		
	3,4	6.26	4:147	3.44	2.42		
13-54	0,1 1,2 0,3 3,4	12.6 4.59 14.8 4.00	8:155 5:150 7:156 6:150	2.62 3.14 2.75 2.92	2.00 2.28 2.07 2.15		
13–55	0,1	10.2	8:144	2.62	2.00		
	1,2	4.84	5:139	3.15	2.28		
	0,3	11.9	7:145	2.76	2.07		
	3,4	4.21	6:139	2.93	2.15		

*Equation 0 refers to the variance for the values themselves with no fitted equation.

**D.F. = degrees of freedom. Numbers preceding and following the colon refer to degrees of freedom for the numerator and denominator of the "F" ratio, respectively.

7.1. Independent Variables Associated with the Dynamic Modulus of Elasticity

One equation selected from each of the tables of equations representing Series O concretes made of AE + NAE cements is presented in table 13–58, columns 1, 2, 3, and 4, to facilitate a comparison of the independent variables associated with the dynamic modulus at the different ages and test conditions. The ratios of the dynamic modulus values at the different ages and curing conditions are presented in columns 5, 6, and 7 of this table. The coef./s.d. values of the independent variables and the calculated ranges of contributions to the dynamic modulus and the ratios are also presented in this table.

Higher air contents were associated with lower dynamic modulus values at all ages and conditions (columns 1, 2, 3, and 4). Higher air contents were associated with higher values of both the ratios involving soaking, but there was no evidence of a relationship with the OE70/14 ratio involving drying. It was previously noted in part 3 section 7 table 7-77 that an increase in the air content was associated with a decrease of compressive

strength at all ages [18].

The coefficient for C₃A was significant and negative after the 56-day drying period (col 3) and after the 28 days in water (col 4) as well as for the three ratios (cols 5, 6, and 7). It was noted in section 7 that C₃A was associated with lower compressive strengths at the later ages [18].

The coefficient for C₃S was positive and highly significant at each of the test conditions. This was also true with respect to the compressive strength of mortar cubes at early ages in section 7 [18]. In column 6, the coefficient for C₃S was negative and

highly significant.

The coefficient for C₄AF was negative and significant at each of the test conditions (cols 1, 2, 3, and 4). No evidence was found for a strong correlation with the compressive strength in sec-

tion 7 [18].

The coefficient for SO₃ was positive and highly significant at each of the test conditions (cols 1, 2, 3, and 4) and also for the OE70/14 ratio (col 5). The coefficient for C₃A/SO₃ was positive and highly significant for the OE98/70 and OE71/70 ratios. The SO₃ was also positive in the equations for 1, 3, and possibly 7-day compressive strength of 1:2.75 (cement to sand) mortar cubes in section 7 [18] and also for the equation for the cubes stored in air.

The coefficient for Na₂O was positive and significant at 14 days in the dynamic tests (col 1). This differs from the results of static strength tests (See part 4, section 7) where there was no evidence of a relationship at the early ages, but at 1, 5, and 10 years the coefficient had a negative

sign. The coefficients for K₂O were not highly significant in the dynamic tests but were probably significant at early ages in the compressive strength tests [18].

An increase in fineness was associated with a decrease in dynamic modulus after 28 and 56 days drying and 28 days resoaking. As previously indicated in part 3 section 7, an increase in fineness was associated with an increase of compressive

strength of mortar cubes [18].

The coefficient for loss-on-ignition was positive in the equation for the dynamic modulus after 8 weeks of drying (col 3) and was also significant but with a negative sign in cols 5, 6, and 7 with the ratios for the different conditions. Higher loss-on-ignition was associated with lower compressive strength of mortar cubes at the early ages [18].

In general the coefficients for the trace elements were not highly significant. Of the 19 included in table 13–58, 8 had coef./s.d. ratios of 2.0 or greater, and one of these (Zr in col. 7) was greater

than 3.0.

Equations for the Series A concretes made with a slump of 5 ± 1 -in are presented in table 13–59. An increase of the amount of water required to obtain the desired slump was associated with lower dynamic-modulus values at each of the test conditions. It has previously been indicated in part 1, section 2 [16] that the water/cement ratio is also a function of the properties of the cements. Thus, interaction of this variable with other so-called independent variables of the equations is a possibility. In general, the differences in air content, w/c, C₃S, and SO₃ of the cements of the Series A concretes had the greatest effect on the calculated ranges of contributions after 14 days moist curing and after both 4 and 8 weeks of drying (cols 1, 2, and 3), and an increase of C₃A was associated with lower strengths after the 28 days in water (col 4).

7.2. Effect of Trace Elements

Evidence from many of the previous tables in this section, especially those dealing with the wet specimens, shows that the additional use of the trace elements in an equation generally caused a significant reduction in variance. After 4 or 8 weeks drying there was no evidence that the trace elements had a significant effect. (See tables 13–10, 13–11, 13–14, 13–15, 13–18, 13–19, 13–22, 13–23, and 13–57.) In equations for the ratios, inclusion of the trace elements resulted in a more significant reduction of variance for the AE71/70 and OE71/70 ratios, and somewhat less for the 98/70-day ratio. There were more instances of questionable significance for the 70/14-day ratios of dynamic modulus values.

Table 13-58. Coefficients, coef./s.d. ratios, and calculated ranges of contributions of independent variables associated with the dynamic modulus values of Series O concretes at various ages

		iynamic moauiu 	i	1	1	1	1
Column	1	2	3	4	5	6	7
Eq. No.	2	2	2	2	2	2	2
Table No.	13-2	13-10	13-18	13-26	13-34	13-42	13-50
Dependent variable	OD14	OD42	OD70	OD98	OE70/14	OE98/70	OE71/70
Constant	+3.723	+3.665	+3.523	+5.25	+0.880	+1.374	+1.046
Air content, coef Coef./s.d Calculated range	$ \begin{array}{r} -0.1593 \\ 20.7 \\ 1.59 \end{array} $	-0.1549 19.9 1.55	-0.1567 19.8 1.57	-0.1400 26.9 1.40		+0.0101 5.3 0.101	+0.00435 5.3 0.044
C ₃ A, coef Coef./s.d Calculated range	+0.01007 1.7 0.14	-0.0086 1.5 0.12	-0.0256 4.1 0.36	-0.0152 3.7 0.21	-0.00587 6.9 0.082	-0.0178 7.4 0.249	-0.00412 4.1 0.058
C3S, coef. Coef./s.d. Calculated range	+0.0196 9.3 0.88	+0.0168 7.3 0.76	+0.0181 7.9 0.81	+0.00601 3.9 0.27		-0.00411 7.8 0.185	-0.000413 1.8 0.018
C4AF, coef Coef./s.d. Calculated range	-0.0178 2.4 0.25	-0.0224 2.9 0.31	-0.0302 3.9 0.42	-0.0142 2.7 0.20		+0.00261 1.4 0.036	
SO ₃ , coef Coef./s.d Calculated range		+0.507 10.3 1.01	+0.551 7.9 1.10	+0.183 5.4 0.37	+0.0698 8.0 0.134		
C ₃ A/SO ₃ , coef Coef./s.d Calculated range	l.					+0.0339 8.1 0.829	+0.00702 3.8 0.068
Na ₂ O, coef Coef./s.d Calculated range	+0.260 3.2 0.18	+0.210 2.5 0.15			-0.0385 2.6 0.027		
K ₂ O, coef Coef./s.d Calculated range	1.9		-0.102 1.3 0.11			-0.0495 2.8 0.054	-0.0213 2.8 0.023
MgO, coef Coef./s.d Calculated range	0.12	+0.0246 2.0 0.12	+0.0308 2.4 0.15		+0.00225 1.1 0.011		-0.00215 1.6 0.011
APF, coef Coef./s.d Calculated range		-0.000099 3.0 0.30	-0.000128 3.5 0.38	-0.000078 3.8 0.23	-0.0000170 2.9 0.051		
Loss, coef			+0.116 4.1 0.35	-0.0361 1.9 0.11	-0.0259 5.1 0.078	-0.0232 8.6 0.070	-0.0165 5.9 0.050
Ba, coef Coef./s.d Calculated range				-0.663 2.8 0.13			
Co, coef Coef./s.d Calculated range						-8.18 1.8 0.081	-2.07 2.0 0.021
Cu, coef Coef./s.d Calculated range				-2.84 2.1 0.12			
Li, coef Coef./s.d Calculated range						-2.53 2.5 0.051	
Mn, coef Coef./s.d Calculated range	-0.188 1.6 0.19				+0.0324 1.6 0.032		-0.0199 1.6 0.020
Ni, coef Coef./s.d Calculated range							-0.898 2.0 0.018
P, coef Coef./s.d Calculated range						+0.0506 1.7 0.025	
Rb, coef Coef./s.d Calculated range	+18.63 2.4 0.19				$ \begin{array}{r} -2.14 \\ 1.6 \\ 0.021 \end{array} $		
V, coef Coef./s.d Calculated range			-1.019 1.2 0.10				
Zr, coef Coef./s.d Calculated range	+0.561 1.7 0.28			+0.619 2.7 0.82	-0.134 2.1 0.067	+0.162 1.9 0.081	+0.130 3.6 0.065

Table 13-59. Coefficients, coef./s.d. ratios, and calculated ranges of contributions of independent variables associated with the dynamic modulus values of Series A concretes at various ages

	1	I Module	s tutues by Berte	es A concretes a	i turious ages		1
Column	1	2	3	4	5	6	7
Eq. No.	5	5	5	3	2	4	2
Table No.	13-6	13-14	13-22	13-30	13-38	13-46	13-54
Dependent variable	AD14	AD42	AD70	AD98	AE70/14	AE98/70	AE71/70
Constant	+7.870	+7.766	+6.621	+9.589	+0.905	+1.333	+1.038
Air content, coef Coef./s.d Calculated range	-0.1406 12.7 1.83	$ \begin{array}{c} -0.1260 \\ 9.7 \\ 1.64 \end{array} $	$ \begin{array}{c c} -0.1235 \\ 9.8 \\ 1.61 \end{array} $	-0.1285 16.1 1.67		+0.00491 3.2 0.064	+0.00399 5.9 0.052
w/c, coef Coef./s.d Calculated range	-6.435 6.9 1.09	-6.649 5.9 1.13	$ \begin{array}{r} -5.356 \\ 4.9 \\ 0.91 \end{array} $	-6.795 9.8 1.16			
C ₃ A, coef Coef./s.d Calculated range		$ \begin{array}{r} -0.0102 \\ 1.5 \\ 0.14 \end{array} $	-0.0336 4.9 0.47	-0.0179 4.2 0.25	-0.00714 6.9 0.104	-0.01555 6.9 0.218	-0.00454 4.6 0.063
C ₃ S, coef Coef./s.d Calculated range	+0.0190 9.0 0.86	+0.0173 6.7 0.78	+0.0183 7.3 0.82	+0.00475 3.1 0.21		-0.00376 7.7 0.169	-0.000382 1.8 0.017
C ₄ AF, coef Coef./s.d Calculated range	-0.0273 4.3 0.38	-0.0193 2.9 0.27	-0.0299 3.6 0.42	-0.0166 3.2 0.23	$\begin{array}{c c} -0.00173 \\ 1.3 \\ 0.024 \end{array}$	$^{+0.00325}_{1.9}_{0.045}$	
SO ₃ , coef Coef./s.d Calculated range	+0.211 5.0 0.42	+0.508 2.3 1.02	+0.532 9.3 1.06	+0.204 5.8 0.40	+0.0722 8.0 0.144		
C ₃ A/SO ₃ , coef Coef./s.d Calculated range						+0.0356 8.9 0.345	+0.00811 4.5 0.079
Na ₂ O, coef Coef./s.d Calculated range	+0.270 3.4 0.19				$\begin{array}{c c} -0.0434 \\ 2.95 \\ 0.030 \end{array}$		
K ₂ O, coef Coef./s.d Calculated range	+0.222 3.0 0.24		+0.249 3.0 0.27			-0.0632 3.9 0.070	-0.0295 3.4 0.32
MgO, coef Coef./s.d Calculated range	+0.0226 1.8 0.11	+0.0348 2.5 0.17	+0.0349 2.6 0.17		+0.0037 1.8 0.019	-0.00716 2.5 0.036	-0.00328 2.4 0.016
APF, coef Coef./s.d Calculated range		-0.000104 2.7 0.31	-0.000088 2.3 0.26	-0.000051 2.3 0.15	$ \begin{array}{r} -0.0000166 \\ 2.8 \\ 0.050 \end{array} $		
Loss, coef Coef./s.d Calculated range		+0.0452 1.4 0.14	+0.0951 3.1 0.28		+0.0203 4.0 0.061	-0.0172 2.9 0.052	-0.00882 3.2 0.026
Ba, coef Coef./s.d Calculated range				-0.428 1.5 0.09			
Co, coef Coef./s.d Calculated range					+2.59 1.5 0.026	-3.22 1.5 0.032	-1.85 1.8 0.018
Cu, coef Coef./s.d Calculated range		-4.41 2.3 0.22		-3.02 2.7 0.15			
Li, coef Coef./s.d Calculated range		+9.11 2.0 0.18	+7.07 1.6 0.14			-2.19 2.4 0.043	-0.743 1.7 0.014
Ni, coef Coef./s.d Calculated range							-0.978 2.2 0.020
Mn, coef	-0.185 1.7 0.18				+0.0396 1.9 0.040		
P, coef Coef./s.d Calculated range					+0.0667 2.3 0.033		
Rb, coef	+14.86 1.9 0.15			+8.60 1.7 0.09	-2.45 1.8 0.024		+1.84 2.1 0.018
Ti, coef Coef./s.d Calculated range				-0.165 2.1 0.16			
Zr, coef Coef./s.d Calculated range		+0.381 1.0 0.19		+0.541 2.4 0.27			-0.0580 1.7 0.029

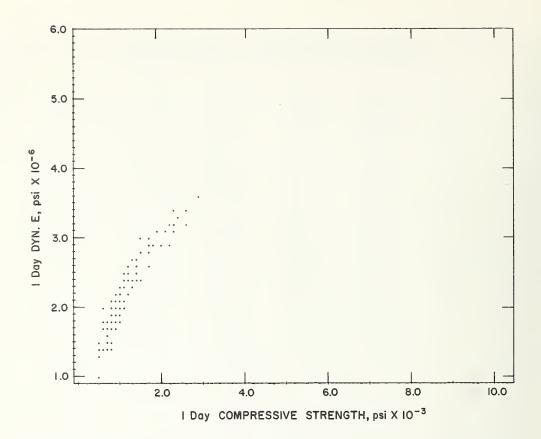


FIGURE 13-1. Dynamic Young's modulus of elasticity at 1 day versus the 1-day compressive strength of 1:2.75 (cement to graded Ottawa sand) mortars.

7.3. Relationships of Dynamic Modulus to Various Characteristics of Mortar Bars

Investigation was made of the relationship between 14-day dynamic modulus of the concretes and the following characteristics of 4- \times 4- \times 16cm mortar bars made with the same cements: (1) 7-day dynamic modulus of the bars, (2) modulus of rupture of the bars, and (3) compressive strengths of modified cubes from the ruptured bars. In none of these cases was a significant relationship found.

Relationships between dynamic modulus, compressive strength, and modulus of rupture of the $4-\times 4-\times 16$ -cm mortar prisms at 1, 3, and 7 days age are presented graphically in figures 13–1 through 13–9. The first three figures show relationships between dynamic modulus and compressive strength at the three ages. Figures 13-4 through 13–6 show dynamic modulus versus modulus of rupture, and figures 13-7 through 13-9 show compressive strength versus modulus of rupture.

Highly significant relationships evidently exist between these three variables when measured on the same specimens. The relationships appear to

be nonlinear, however.

7.4. Compressive and Flexural Tests of Concretes

No compressive or flexural strengths of these concretes were determined at the time the cements were tested. At the age of 7 years, 24 pairs of $3-\times 4-\times 16$ -in specimens were removed from the field exposure and placed in water for 28 days. Then resonant frequency and flexural and compressive strengths were determined on one of the beams. The compressive strengths were determined on 3- \times 3- \times 4-in prisms sawed from the broken beams. No correction was made for the nonstandard shape and height-width ratio of the specimens. The specimens selected were all from concretes which had the same w/c for the Series O and Series A concretes.

The average dynamic modulus of elasticity was 5.58×10^6 psi with a range of values from 4.95 to 5.96×10^6 psi. The average compressive strength was 4350 psi with a range of 3040 to 5660 psi The average modulus of rupture was 624 psi with a range of 490 to 770 psi. The trends of the relationships are indicated by the dashed lines in figures 13-10 and 13-11. No trend line was placed in figure 13-12 showing the relationship of compressive to flexural strengths because of the broad

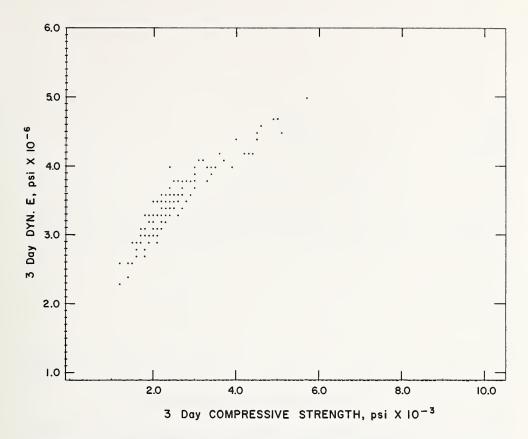


FIGURE 13-2. Dynamic Young's modulus of elasticity at 3 days versus the 3-day compressive strength of 1:2.75 (cement to graded Ottawa sand) mortars.

scatter of results. The ranges of values of the concretes selected for these tests were much less than those of the 1-, 3-, and 7-day mortar tests in Figures 13-1 through 13-9, and this makes it more difficult in the case of concretes to establish overall trends.

7.5. Effect of Drying and Resoaking on Dynamic Modulus of Concretes

The average dynamic-modulus values and averages of the ratios for 70/14-, 98/70-, and 71/70-day dynamic-modulus values have been presented in the tables of equations. There was an average reduction of dynamic modulus of 7 percent when the specimens were dried for 8 weeks, an average increase of dynamic modulus of 15 percent when the dried specimens were placed in water for 28 days. When the air-dried specimens were placed in water for 24 hours the average dynamic modulus for all specimens was about 1 percent less than when measurements were made on the dry specimens.

However, consideration must be given to the broad distribution of values for all of the ratios as it was evident that concretes made of the different

cements behaved quite differently. Drying and wetting can produce tensile and compressive stresses in a concrete specimen and these may be factors affecting the fundamental resonant frequencies of the specimens. Soaking the air-dried specimens in water for 24 hours resulted in as much as 5-percent reduction in dynamic modulus for some specimens and in others, up to a 5percent increase in dynamic modulus. It has previously been noted that the saturation ratio (part 5 section 11) also varied with concretes made of different cements. Whereas some specimens were about 80 percent saturated in 24 hours, others were only about 20 percent saturated. The slight reduction in dynamic modulus with 24 hours of resoaking of the air-dried specimens of some of the cements may have resulted from a relief of possible tensile stresses on the skin of the specimens whereas the slight increase may have resulted from the filling of the voids.

One of the contributing factors to the 70/14-day ratio was undoubtedly the continued hydration which occurred during the 56-day storage in laboratory air. The rate of hydration may have been different for concretes made with different cements. The loss of different quantities of water

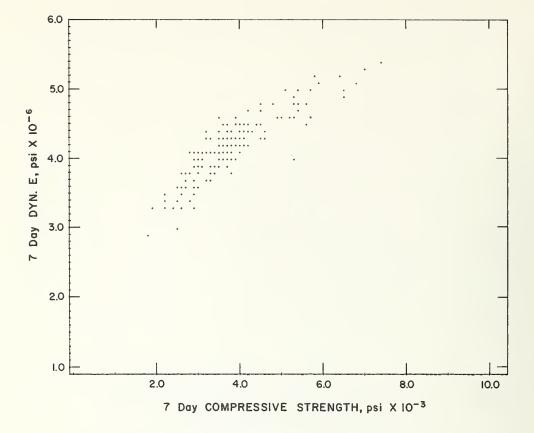


FIGURE 13-3. Dynamic Young's modulus of elasticity at 7 days versus the 7-day compressive strength of 1:2.75 (cement to graded Ottawa sand) mortars.

as indicated in section 12 would result in differences of the voids of the different concretes.

It was noted that the 98/70-day ratios were all greater than 1.0 but there was a broad distribution of values. The extent of filling of the pore structure plus continued hydration could account for the increase in dynamic modulus and for some of these differences.

When concrete specimens are exposed to outdoor weathering, the dynamic modulus of elasticity may be affected by the moisture condition and moisture distribution within the specimens. Unless there are gross differences in dynamic properties there would be the uncertainty of the role of the moisture condition. If specimens are kept moist prior to measurement there is, as indicated in section 11, a possibility of autogenous healing. Measurements made on the specimens stored outdoors indicated a slight (perhaps significant) increase in dynamic modulus in the fall as compared to measurements made in the spring after the winter freezing and thawing exposure. Factors other than normal weathering may have been responsible.

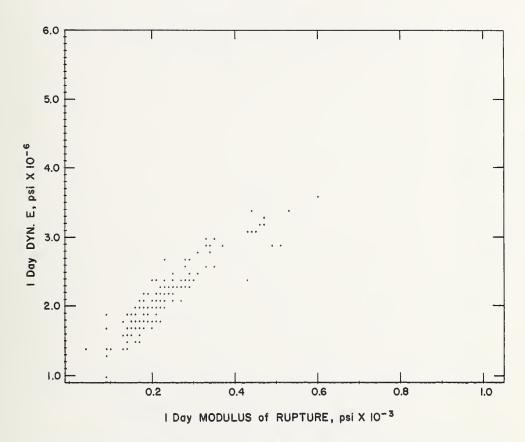


FIGURE 13-4. Dynamic Young's modulus of elasticity at 1 day versus the 1-day modulus of rupture of 1:2.75 (cement to graded Ottawa sand) mortars.

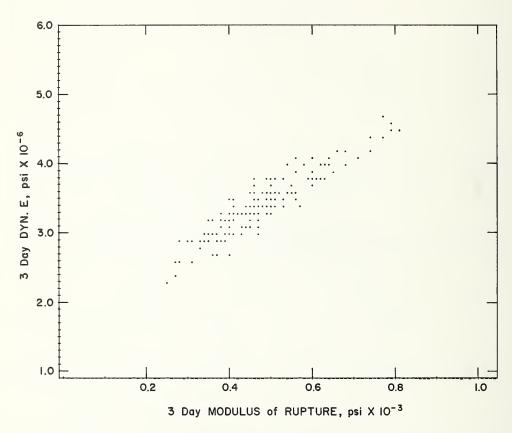


Figure 13-5. Dynamic Young's modulus of elasticity at 3 days versus the 3-day modulus of rupture of 1:2.75 (cement to graded Ottawa sand) mortars.

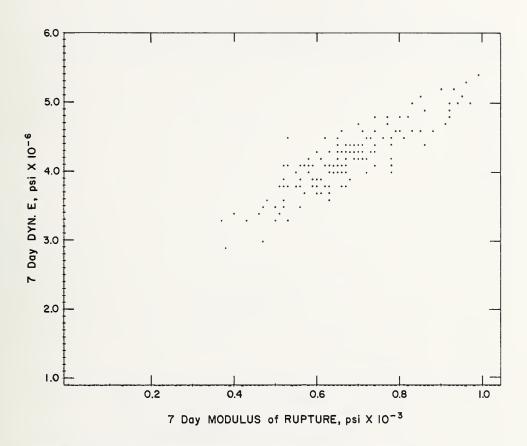


FIGURE 13-6. Dynamic Young's modulus of elasticity at 7 days versus the 7-day modulus of rupture of 1:2.75 (cement to graded Ottawa sand) mortars.

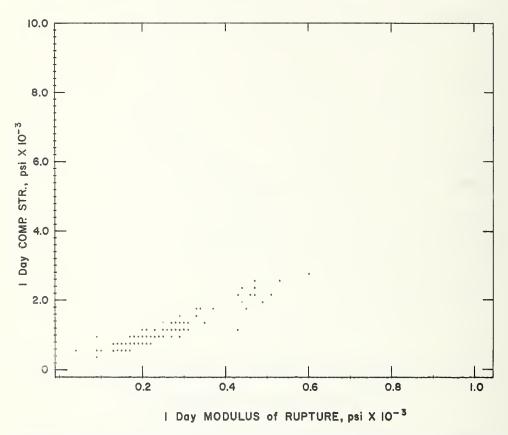


Figure 13-7. Compressive strength at 1 day versus the modulus of rupture at 1 day of 1:2.75 (cement to graded Ottawa sand) mortars.

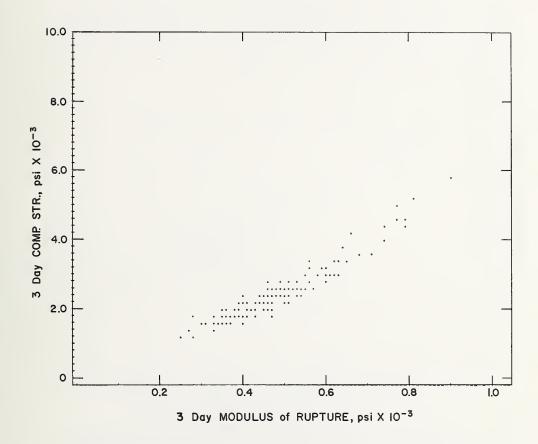


Figure 13-8. Compressive strength at 3 days versus the 3-day modulus of rupture of 1:2.75 (cement to graded Ottawa sand) mortars.

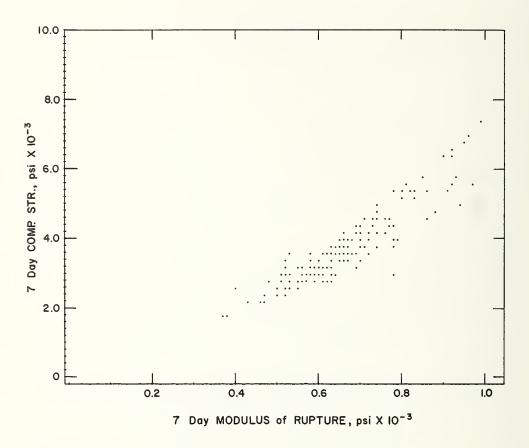


Figure 13–9. Compressive strength at 7 days versus the 7-day modulus of rupture of 1:2.75 (cement to graded Ottawa sand) mortars.

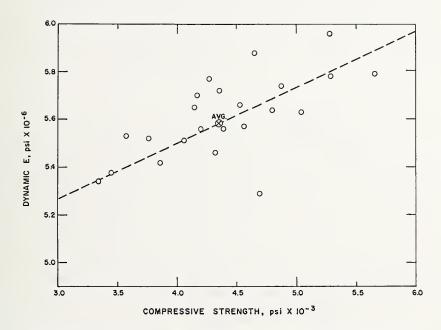


Figure 13–10. Dynamic Young's modulus of elasticity of concretes versus the compressive strength at 7 years after outdoor storage.

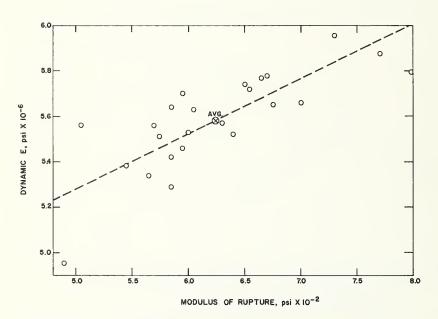


Figure 13–11. Dynamic Young's modulus of elasticity of concretes versus the modulus of rupture at 7 years after outdoor exposure.

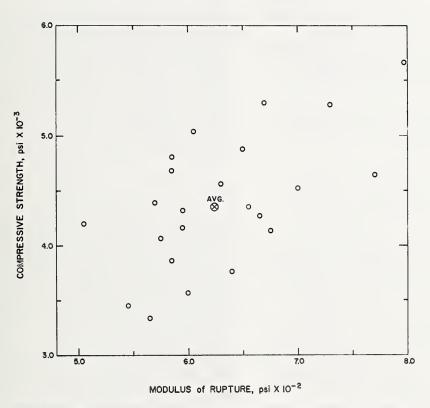


Figure 13–12. Compressive strength of concretes versus the modulus of rupture at 7 years after outdoor exposure.

8. Summary and Conclusions

(1) Measurements were made of the dynamic Young's modulus of elasticity of concretes made with 199 portland cements from different mills. One series of concretes (Series O) was made using a water/cement ratio of 0.635 and the other series (Series A) with the quantity of water adjusted to give a slump of 5 ± 1 in. A nominal quantity of 5.5 bags of cement per cubic yard was used. The $3-\times 4-\times 16$ -in specimens were moist cured for 14 days, dried in laboratory air for 8 weeks, then placed in water for 4 weeks. The fundamental transverse frequency was determined at 14, 42, 70, 71, and 98 days. The ratios of the dynamic modulus values at 70/14, 98/70, and 71/70 days were computed.

(2) The dynamic modulus after 14 days moist curing ranged from 3.4 to 5.8×10^6 psi, with an average of 4.75×10^6 psi for the Series O concretes amd 4.76×10^6 psi for the Series A con-

cretes.

(3) After drying in laboratory air for 4 weeks there was an average reduction of about 4 percent in the dynamic modulus. There was, however, a broad distribution of values.

(4) After drying in laboratory air for 8 weeks there was an average reduction of 7 percent in dynamic modulus. Concretes made with some of the cements showed an increase in dynamic modulus during the drying period, possibly due to continued hydration.

(5) When the concrete specimens which had been air-dried for 8 weeks were placed in water for 24 hours, the dynamic modulus of some decreased up to 5 percent and others increased up

to 5 percent.

(6) When the concrete specimens which had been air-dried for 8 weeks were placed in water for 4 weeks, there was an average of 15 percent increase in dynamic modulus. There was a broad distribution of values. Some concretes increased only about 5 percent, and others had a 40-percent

increase in dynamic modulus.

(7) Computations of multivariable equations by a least-squares method were used to investigate what chemical and physical properties of the cements and concretes were associated with the dynamic modulus of elasticity at the various ages, and with the ratios of the dynamic E at the various ages after the different curing conditions. The equations were computed for all the cements for which minor constituents and trace elements had been determined. The equations were computed using as independent variables, either the major potential compounds, or the major oxides, each with other commonly determined variables and these with trace elements found to be significant.

The following observations relate to equations as summarized in tables 13-58 and 13-59 for concretes made of AE + NAE cements using a

water/cement ratio of 0.635 and concretes having

a slump of 5 ± 1 inches respectively:

(7.1) An increase in the air content for both series of concretes and the water/cement ratio required to produce a concrete of the desired slump for the Series A concretes was associated with a decrease of the dynamic modulus at all conditions. An increase in the air content was associated with an increase of the OE98/70 (28-day soaking) and OE71/70-day (1-day soaking) ratios of dynamic modulus for both series.

(7.2) An increase of C₃A was associated with a decrease of the dynamic modulus after the 8-week drying period and after the subsequent 4 weeks in water. An increase in C₃A was also associated with a decrease of the dynamic modulus ratios,

70/14-day, 98/70-day, and 71/70-day.

(7.3) An increase of C₃S was associated with an increase of the dynamic modulus at all conditions and with a decrease of the 98/70-day ratio.

- (7.4) An increase of C₄AF was generally associated with a decrease of the dynamic modulus at all conditions although there were a number of instances where the coef./s.d. ratio was less than 3.0.
- (7.5) An increase of SO_3 was associated with an increase of the dynamic modulus at all conditions and with the 70/14-day ratio. An increase of C_3A/SO_3 was associated with an increase of the 98/70-day and 71/70-day ratios of dynamic modulus. The C_3A/SO_3 ratio interacts with the coefficients for C_3A and SO_3 and all must be taken into consideration in evaluating the effect.

(7.6) An increase in Na₂O was associated with an increase of the dynamic modulus after 14 days moist curing and possibly with a decrease of the

70/14-day ratio.

(7.7) An increase in K₂O was associated with an increase of the dynamic modulus after 14 days moist curing and after the 8-week drying period for the Series A concretes. The coefficient was of doubtful significance for the Series O concretes.

(7.8) An increase in MgO is probably associated with an increase in dynamic modulus after 4 and

8 weeks of drying.

(7.9) An increase of air-permeability fineness was associated with a decrease of dynamic modulus after 4 and 8 weeks of drying and after the 4 weeks resoaking for the Series O concretes and probably for the Series A concretes.

(7.10) An increase of the loss on ignition of the cements was associated with an increase of the dynamic modulus after the 8-week drying period, and with a decrease in the ratios of dynamic mod-

ulus at all conditions.

(7.11) The use of trace elements having coef./s.d. ratios greater than 1.0 as independent variables, together with other commonly determined independent variables in equations, generally resulted in a significant reduction of variance when

the concrete was moist. After 4 or 8 weeks drying in laboratory air there was no evidence that the trace elements had a significant effect. With a few exceptions, the coefficients of the trace elements

were of doubtful significance.

(8) The use of the major oxides instead of the major compounds, but with other commonly determined independent variables and trace elements, generally resulted in equations with about the same estimated standard deviation.

(9) Equations calculated for concretes made of the NAE cements resulted in coefficients, coef./ s.d. ratios, and S.D. values in reasonable accord with those calculated for the concretes made of the AE + NAE cements.

(10) There was no significant relationship between the dynamic modulus of the concretes at 14 days and the dynamic modulus of 1:2.75 (cement to graded Ottawa sand) mortar prisms

at 7 days.

9. References

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