

The Use of Synchrotron Radiation as an Absolute Source of VUV Radiation

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Synchrotron radiation has been used as a standard source to calibrate spectrographic instruments at the National Bureau of Standards (NBS). Conceptually it is straightforward to apply the calculable continuum distribution of synchrotron radiation to problems requiring a source of known irradiance if the electron energy, the radius of the electron orbit, and the beam current are known. In practice many factors affect the accuracy of such a calibration, such as temporal and spatial variations in the electron beam, uncertainties in the orbital radius and maximum energy of the orbiting electron beam. These sources of error are discussed and the method of calibration on SURF-I is specified. A storage ring synchrotron radiation facility (SURF-II) is now operational at NBS. The calibration techniques developed for SURF-I are applied to SURF-II with anticipated improvements in calibration accuracy. For SURF-I the incident flux was determined with an accuracy of 15 percent while for SURF-II we anticipate accuracies of about 7 percent.

Key words: Irradiance; radiometry; spectrometer calibration; standard source; synchrotron radiation; vacuum ultraviolet.

1. Introduction

The need for vacuum ultraviolet (vuv) source and detector standards has been growing steadily during the past decade with the requirements of space physics, aeronomy, and plasma physics setting the pace. Reliable detector transfer standards have been developed [1, 2]¹ for use over a wavelength range from 200 to 2500 Å. While detector-transfer-standard systems cover a broad spectral range in the vuv, source standards are not as well developed.

The simplest calibration method is the substitution of a calibrated standard for the unknown in an existing system. This makes source standards the standards of choice in calibrating other sources. The use of detector standards for this purpose requires independent knowledge of the monochromator optical system efficiency. On the other hand, detector standards are the standards of choice for calibrating other detectors.

Several sources have been devised [3–15] for use as standards in the vuv, however the 1000 to 3000 Å spectral range is where the most intense development has taken place. Among the various proposed sources synchrotron radiation [3–6] has appeared especially attractive. In addition, the radiation from wall-stabilized arcs [7, 8], transition radiation [9, 10], and discharge

lamps [11, 12] have also been demonstrated as feasible sources which can be characterized sufficiently well to be used as standards. Branching ratio techniques [13–15] have also proven useful in certain situations.

The characteristics of these different sources are given in table 1 for comparison. It is clear that the features pertaining to each source serve to specialize its use. The best choice must be made with a given experiment in mind. For example, while both the synchrotron and wall-stabilized arc are possible standard sources, one would be drawn to the use of a synchrotron at wavelengths less than 1200 Å, the lithium fluoride cutoff, simply because an expensive differential pumping system is unnecessary. On the other hand if a filled optical system is a more important criterion than high intensity, one would use a transition radiation source which in addition to its greater divergence is also more portable than either a synchrotron or a wall-stabilized arc. While for the 1600 to 2600 Å spectral range a deuterium lamp [12] is the simplest to use. All the sources mentioned except the synchrotron have cutoffs above 500 Å. At wavelengths less than 500 Å the synchrotron remains the only effective candidate for a continuum calibration source.

Wall-stabilized arcs and sources of synchrotron radiation are considered absolute sources since their radiation is a known function of their operating parameters. Both, unfortunately, are rather immobile and require some means of transferring the calibration to

¹ Figures in brackets indicate the literature references at the end of this paper.

TABLE 1. *Characteristics of vuv standard sources*

Source	Synchrotron radiation	Wall-stabilized arc	Transition radiation	Cerenkov radiation	Branching ratio technique	Discharge and deuterium lamps
Relative (<i>R</i>) or absolute (<i>A</i>) standard	<i>A</i>	<i>A</i> ^b , <i>R</i>	<i>A</i>	<i>A</i>	<i>A</i>	<i>R</i>
Line (<i>L</i>) or continuous (<i>C</i>) source	<i>C</i> ^a	<i>C</i>	<i>C</i>	<i>C</i>	<i>L</i>	<i>L</i> , <i>C</i>
Wavelength range (Å)	> 0.1	1300–3600	> 500	> 1200	900–3000 ^c	> 304 ^d
Maximum intensity	Bright ^f	Bright	Dim ^g	Dim	Intermediate	Intermediate
Scalable in intensity?	Yes	Limited ^e	Yes	Yes	Limited	Limited
<i>f</i> Number	Small (<i>f</i> /500)	Small	Large (<i>f</i> /10)	Large	Large	Large
Polarized?	Yes	No	Yes	Yes	No	No
Vacuum in source	High	Poor	High	High	Poor	Poor
Physical size	Massive	Large	Small	Small	Small	Small

NOTES:

^aAdjustable wavelength distribution; storage ring very stable.^bOnly hydrogen arc is absolute.^cUsable only at selected wavelengths; subject to absorption effects; portable.^dUsable only at selected wavelengths; good as transfer standard; portable.^eOver factor of ten.^fAbout 10¹⁶ photons s⁻¹ Å⁻¹ · Sr.^gAbout 10¹⁰ photons s⁻¹ Å⁻¹ · Sr.

the unknown source. Transition radiation sources and the deuterium lamp have been suggested [9, 10, 12] for this purpose in the vuv.

Transferring a calibration from a standard source in one laboratory to an unknown source in a second laboratory effectively involves the calibration of two spectrometers, one at the laboratory housing absolute-transfer standards and the other in the field where the transfer standard is compared with the unknown source. There are significant advantages in an alternate approach; namely to directly calibrate the spectrometer that is to be used for determining the radiance of the unknown source. If the calibration is made on a before-after basis, any changes in sensitivity can be interpolated, and errors resulting from a double transfer are eliminated. This method requires direct illumination (no auxiliary mirrors) of the spectrometer by both standard and unknown sources. When NASA encouraged us to establish a source calibration facility at the National Bureau of Standards "Synchrotron Ultraviolet Radiation Facility" (NBS-SURF) for the Skylab program we took the approach outlined above, namely, calibrate a spectrometer to be used as a transfer standard. We used synchrotron radiation as the absolute standard source because the required calibration range, 200 to 1200 Å, was beyond the range of all other sources. The use of synchrotron radiation to calibrate a spectrometer above 500 Å has recently been reported [16].

The basic assumption of our calibration method is that the intensity distribution of synchrotron radiation is a calculable quantity. Once this assumption is granted, it is straightforward conceptually to apply the

calculable continuum distribution of synchrotron radiation to problems requiring a source of known irradiance provided the electron energy, the radius of the electron orbit, and the beam current are known. In practice many factors affect the accuracy of such a calibration and this paper will discuss the steps taken at NBS to attain a successful calibration. In the following sections the measurements required to determine the parameters necessary for the calibration will be presented. Systematic errors, their sources and cure, will be a topic of discussion, as will some special problems that arise due to the peculiar characteristics of the radiation source. While this paper will deal primarily with synchrotron radiation that arises from the periodic acceleration of electrons in a synchrotron, some time will be devoted to the application of synchrotron radiation from a storage ring to spectrometer calibrations because the NBS synchrotron (SURF-I) has now been converted into an electron storage ring (SURF-II).

2. The Synchrotron as a Primary Radiation Standard

We must first discuss the validity of the fundamental assumption involved in using synchrotron radiation as an absolute source standard: that the photon flux distribution in both wavelength and angle is an exactly calculable quantity. In the following paragraphs ample evidence has been given to justify this basic assumption. The reader is referred to several excellent reviews [17–19] of the historic development of the use of synchrotron radiation for a more detailed account of

the characteristics of the radiation and for other applications of it.

In their classic paper Tomboulion and Hartman [3] suggested that synchrotron radiation could be used as an absolute radiation standard because of the calculability of the radiant energy wavelength distribution. This suggestion arose as a result of their experiments that compared measured synchrotron radiation intensity with the calculated intensity distribution. Their experiments covered different wavelength regions, from the quartz ultraviolet to the vacuum ultraviolet, as well as both radiation from monoenergetic electrons and electrons accelerated over a full machine cycle. They measured the angular distribution of the radiation at several wavelengths and electron energies. The result of this extensive study demonstrated the classical theory was appropriate to the description of synchrotron radiation.

Nine years later Codling and Madden [4] reported measurements of the polarization properties of the radiation in the visible and also used radiometric techniques to measure the beam current. A year later a group [5] at DESY (Deutsches Elektronen-Synchrotron) compared the relative intensity distribution as a function of photon energy and azimuthal angle relative to the orbital plane. In this case the electron energy varied between 4 GeV and 6 GeV and the photon energy extended between 20 keV and 300 keV. Their results substantially confirmed the measurements of Tomboulion and Hartman [3] at lower electron and photon energies, namely, that the measurements were in agreement with calculations to within the experimental error of order 10 percent.

Lemke and Labs [6], working at DESY, explored the possibility of using synchrotron radiation as a fundamental radiometric standard in the wavelength region 2200 to 5500 Å. They compared the spectral radiance from the synchrotron with that of a standard lamp. From this comparison they were able to measure the relative spectral distribution for their geometry as well as independently determining the circulating electron current. Applying the appropriate polarization correction (synchrotron radiation is highly polarized in the orbital plane) they obtained a relative spectral distribution that agreed with the computed flux within 2 percent. Their optical measurement of the circulating current was consistent with an independent direct measurement of the beam current to within the 15 percent limit of experimental error of this direct technique. These experiments have shown the measurements to be consistent with the calculations of the flux over a broad spectra range for accelerated electrons over a wide energy range. At the Glasgow University synchrotron, Key [20] made a very careful relative flux determination between 3500 Å and 6000 Å by comparing the radiance from the electron beam with the radiance from a standard lamp. This comparison yielded coincidence to $\pm 1/2$ percent between the relative measured spectral distribution and the predicted spectral distribution.

In 1969 Pitz [11] used synchrotron radiation as a

primary standard to calibrate mercury, xenon, and deuterium transfer standard lamps in the wavelength range 1500 to 2700 Å. Later a mercury lamp and a deuterium lamp traceable to one calibrated by Pitz was compared to a wall-stabilized hydrogen arc [21]. Discrepancies were found to be about 10 percent between 1650 Å and 2550 Å. Between 2550 Å and 2700 Å, the long wavelength limit of the calibration, the deviations were as great as 25 percent. Whether these discrepancies were due to aging of the lamp or some other source is not clear, however evidence points to a lamp change rather than something faulty with the synchrotron radiation flux determination. More recently a comparison [22] between a wall-stabilized arc and synchrotron radiation has been made through the use of deuterium lamp and xenon lamp transfer standards at a wavelength near 1650 Å. The resulting calibrations agreed to ± 20 percent at low arc currents and ± 5 percent at the higher currents. The authors concluded that the discrepancies were consistent with errors expected from the synchrotron calibration and the wall-stabilized arc calibration.

From these measurements the validity of the fundamental assumption underlying the use of synchrotron radiation as an absolute standard seems to be well founded. Not only have direct measurements of the spectral distribution confirmed the calculable nature of synchrotron radiation but independent calibrations of transfer standards with synchrotron radiation and with the wall-stabilized arc have also been found consistent.

3. Method

It is conceptually straightforward to apply the calculable continuum distribution of synchrotron radiation to spectrometer calibration since the efficiency, $\epsilon(\lambda)$, of the spectrometer at wavelength λ , is given by:

$$\epsilon(\lambda) = \frac{F(\lambda, \Delta\Omega)}{R(\lambda, \Delta\Omega)}, \quad (1)$$

where $F(\lambda, \Delta\Omega)$ is the flux incident on the entrance aperture of the spectrometer which subtends a solid angle $\Delta\Omega$ located at some angle θ with respect to the orbital plane, and $R(\lambda, \Delta\Omega)$ is the response of the instrument to the incident flux. In order to understand the problems involved in the use of synchrotron radiation and to compute the quantity $F(\lambda, \Delta\Omega)$ it is necessary to delve into the properties of the radiant flux emitted by this source.

3.1. Properties of Synchrotron Radiation

The radiation emanating from centripetally accelerated electrons is confined along the direction of motion due to relativistic effects. The average divergence angle of the radiation is m_0c^2/E where m_0 is the electron rest mass and E is the instantaneous energy of the electrons. Since $E \gg m_0c^2$, the radiation from most

machines is confined to an angle of a few milliradians above and below the orbital plane. Because of the electron orbital motion the radiation is uniform in the orbital plane and at a given energy and radius is a function only of the azimuthal angle. A schematic view of the radiation pattern is shown in figure 1.

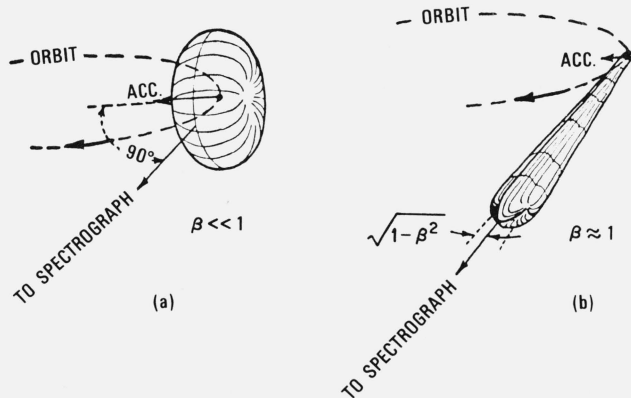


FIGURE 1. Angular radiation patterns for orbiting electrons of greatly different energies.

(a) Nonrelativistic energy, showing the typical dipole pattern; (b) Very relativistic energies, showing that the dipole pattern has been greatly warped around to the forward direction of the electron (from ref. [3]).

This rather narrow distribution presents the first problem for spectrometer calibration since most other sources, whose radiance is to be determined through the use of the calibrated spectrometer, have a much different angular distribution. In addition the radiation from the synchrotron source will often not fill the entrance solid angle of the instrument.

The power radiated by monoenergetic, accelerated electrons is a continuum which has the form [23, 3]

$$P(E, R, \theta, \lambda) = \frac{4e^2 c R}{3\lambda^4} \gamma^{-4} (1 + X^2)^2 \left[K_{2/3}^2(\xi) + \frac{X^2}{1 + X^2} K_{1/3}^2(\xi) \right] \quad (2)$$

where $P(E, R, \theta, \lambda)$ is the power in ergs per second per radian per electron per angstrom, $\gamma = E/m_0 c^2$, and $\xi = (2\pi R/3\lambda) \gamma^{-3} (1 + X^2)^{3/2}$ with $X = \gamma\theta$. The quantity R is the orbital radius and θ is the azimuthal angle with respect to the orbital plane while e and c are the electron's charge and the speed of light respectively. The quantities $K_{2/3}(\xi)$ and $K_{1/3}(\xi)$ are modified Bessel functions of the second kind. This is the fundamental equation that is used to compute the flux incident upon the entrance aperture of a spectrometer. For a storage ring where the instantaneous energy E is a constant it is only necessary to integrate eq (2) over the entrance aperture solid angle to obtain the flux per electron at wavelength λ . However, for many accelerators (of which SURF-I, the old NBS-180 MeV synchrotron was an example) the energy of the electrons varies as they are periodically accelerated from zero to maximum energy. In this case

eq (2) must be integrated over the time variation of the electron energy as well. Figure 2 shows the angular

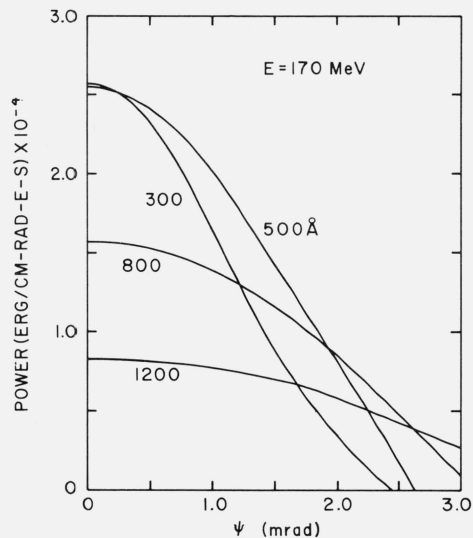


FIGURE 2. Angular distribution of synchrotron radiation at several wavelengths for accelerated electrons with a maximum energy of 170 MeV.

variation of the flux for accelerated electrons at several wavelengths. Equation (2) was integrated numerically for a time variation of the electron energy given by $E(t) = E_{\max} \sin \omega t$. Typical operating conditions for the NBS synchrotron were chosen, namely $E_{\max} = 170$ MeV, $R = 83.4$ cm, and $\omega = 2\pi/T = 2\pi 60$ s⁻¹. The ordinate defines the power $P(E_{\max}, \theta, \lambda)$ in ergs per second per centimeter per radian of azimuthal angle per electron. The quantity $P(E_{\max}, \theta, \lambda)$ is given by

$$P(E_{\max}, \theta, \lambda) = \frac{1}{T} \int_{E(t_1)}^{E(t_2)} P(E, R, \theta, \lambda) dE(t). \quad (3)$$

The limits of integration $E(t_1)$ and $E(t_2)$ are the instantaneous electron energies at t_1 (chosen to be zero, the beginning of the acceleration cycle) and $t_2 = 5.57$ ms the time when the radio frequency accelerating voltage was turned off. It may be seen from figure 2 that in the wavelength region between 100 Å and 2000 Å the angle at which the flux is smaller by a factor of two is typically a few milliradians.

The power $P(E_{\max}, \theta, \lambda)$ given by equation (3) was numerically integrated over a round spectrometer aperture (0.836 cm² area) located 13.26 m from the tangent point of the orbiting electrons. This was the size of the aperture used for the calibration of a Wadsworth spectrometer. The flux $P(E_{\max}, \lambda)$ in photons/sec-Å-e passing through this aperture for two values of the maximum electron energy, E_{\max} , is shown in figure 3. Notice that the flux is almost constant between 400 Å and 1000 Å for E_{\max} equal to 170 MeV (curve A) while the magnitude of the flux at these wavelengths is greatly reduced for 140 MeV

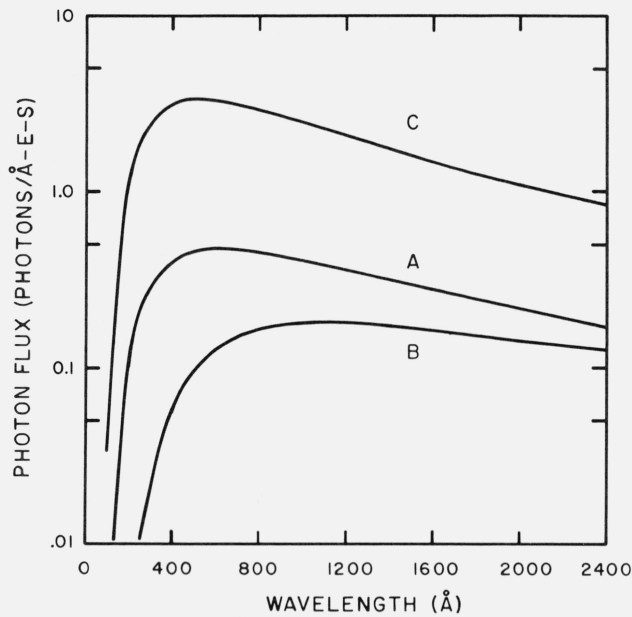


FIGURE 3. Flux passing through a round aperture of solid angle equal to 4.8×10^{-7} strad as a function of wavelength.

Curve A: Accelerated electron whose energy equals 170 MeV. Curve B: Accelerated electrons whose maximum energy is 140 MeV. Curve C: Monoenergetic electrons of energy 170 MeV.

electrons (curve B). In fact, this great variation in the flux can be used to determine the instrument's response to second order radiation [24]. Curve C in figure 3 is the flux for monoenergetic electrons of 170 MeV energy obtained by just integrating equation (2) over the aperture. Notice that for the monoenergetic electrons the peak intensity in the spectral distribution is shifted to shorter wavelengths and the flux per electron is significantly greater than for accelerated electrons of the same peak energy averaged over the acceleration cycle. This difference is due both to the duty cycle of the cyclic accelerator and to the fact that the electrons, emit most of their radiation when their instantaneous energy $E(t)$ is nearly equal to E_{\max} . The contrast between the two curves A and C emphasizes one of the advantages of using a storage ring for a calibration, namely, for the same number of electrons in the beam, the ring will emit about seven times more radiation than the synchrotron.

In figure 4 we show a comparison between accelerated 170 MeV electrons at an instantaneous current of 5 mA (typical of SURF-I operation) and 240 MeV monoenergetic electrons at a current of 10 mA (expected for initial SURF-II operation). Higher flux and the availability of shorter wavelengths make SURF-II a superior calibration source. In addition temporal variation in the radiation from the storage ring is a slowly varying monotonically decreasing function, due to the fact the electron beam lifetime is of the order of an hour, rather than the few milliseconds obtained in a sinusoidally run synchrotron. The fluctuations in the radiation due to variations in the injected current occurs on the order of hours, rather than every few

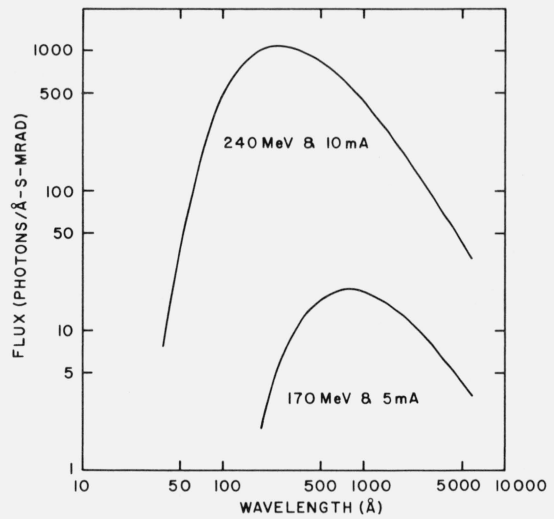


FIGURE 4. Photon flux versus wavelength for (A) a monoenergetic 240 MeV, 10 ma beam of electrons—typical performance expected for SURF-II and (B) an accelerated 5 ma beam of 170 MeV maximum energy electrons—typical performance of SURF-I.

Multiply ordinate by 1.1×10^8 .

milliseconds. These are powerful arguments for the use of a storage ring in spectrometer calibration. Other arguments favoring storage rings will be discussed later.

If the entrance aperture is large enough to accept the full vertical angular distribution of the radiation, eq (2) can be integrated over the azimuthal angle θ to yield the flux distribution for monoenergetic electrons:

$$P(E, \lambda) = \frac{3^{5/2}}{16\pi^2} \frac{e^2 c}{R^3} \gamma^7 G(y). \quad (4)$$

Similarly for electrons whose energy is given by $E(t) = E_{\max} \sin(\omega t)$ eq (2) can be integrated over angle and averaged over one fourth the energy cycle to yield [3]:

$$P(E_{\max}, \lambda) = \frac{3^{5/2}}{8\pi^3} \frac{e^2 c}{R^3} \gamma^7 L(y). \quad (5)$$

In eq (4) and eq (5) the quantities $G(y)$ and $L(y)$ are universal scaling functions independent of the electron energy and orbital radius. The quantity $y = \lambda_c/\lambda$. The critical wavelength λ_c is given in the following equation:

$$\lambda_c = \frac{4}{3} \pi R \gamma^{-3}.$$

These two functions are plotted in figure 5. The simple functional form of eq (4) and eq (5) are conveniently used with the figure 4 to estimate (since the vertical acceptance angle of the experiment is initially unknown) the flux available to an experimental ap-

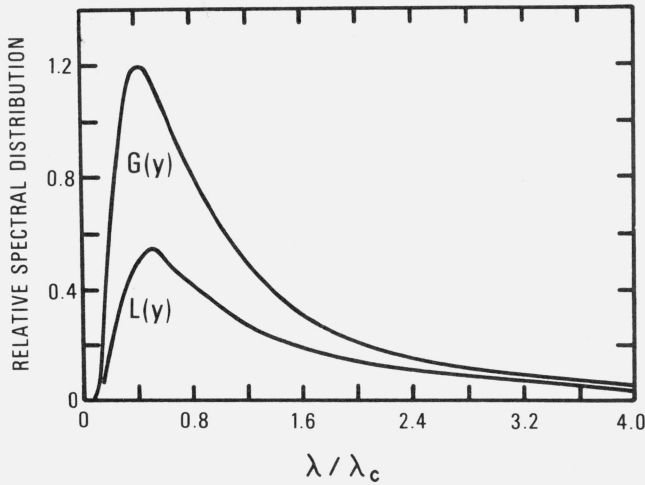


FIGURE 5. Universal photon distribution functions for the total angular flux distribution.

$G(y)$, the distribution function for monoenergetic electrons, and $L(y)$, the distribution function for accelerated electrons. The dimensionless quantity y defining the abscissa scale is equal to λ/λ_c , where λ_c is defined in the text.

paratus from a specific machine. A rather tedious computation and integration is thus reduced to a "back of the envelope" calculation.

3.2. Determination of the vuv Irradiance

The vuv irradiance $F(\lambda, \Delta\Omega)$ incident on the spectrometer is given by:

$$F(\lambda, \Delta\Omega) = n_e \int_{\Delta\Omega} P(E_{\max}, \theta, \lambda) d\Omega \quad (6)$$

where $F(\lambda, \Delta\Omega)$ is the number of photons per Å-s passing through the spectrometer aperture subtending a solid angle $\Delta\Omega$ measured from the tangent point. The quantity $P(E_{\max}, R, \theta, \lambda)$ was described in the preceding paragraphs for both monoenergetic and periodically accelerated electrons. $P(E, \theta, \lambda)$ depends on the experimentally determined quantities R , the radius of the electron orbit and, E_{\max} , the maximum electron energy, in a straightforward way. The quantity n_e may be measured by using an induction technique [6] or it can be determined from the synchrotron radiation [4] itself. A particularly elegant technique [25] may be used in the case of photomultiplier calibrations using a storage ring. A reasonably small number of electrons (about 100) is allowed to circulate in the ring. As the electrons are lost from orbit one by one, the decrease in visible emission due to the loss of one electron is noted and from this the exact total number of electrons may be readily obtained. Note with this method the absolute amount of radiation need not be measured. This technique will be available for use at SURF-II. In another method, the radiation is allowed to fall on a suitable calibrated detector. The number of electrons is determined by dividing the measured flux by the flux of synchrotron radiation a single electron

radiates to the detector. At SURF-I the spectral interval used for absolute measurement of the synchrotron flux was a 100 Å wavelength band around 5150 Å because an irradiance standard could be used to calibrate a silicon photodiode-filter combination in this band. The visible region of the spectrum was also chosen because for $\lambda \gg \lambda_c$ (for 170 MeV electrons accelerated at SURF-I $\lambda_c = 940$ Å) the radiated power is approximately independent of the electron energy and proportional to $\lambda^{-7/3}$. Thus small fluctuations in the energy have a negligibly small effect on the determination of the number of electrons in orbit. Thus the number of electrons is given simply by

$$n_e = \frac{F(\lambda_0, \Delta\Omega)}{P(E, \lambda_0)} \quad (7)$$

Explicitly writing the integrations over the variation of the detector sensitivity $R(\lambda)$, the filter transmission $T(\lambda - \lambda_0)$ and the radiated power from the synchrotron we have

$$F(\lambda_0, \Delta\Omega) = \frac{n_e}{2\pi} \int_{\Delta\Omega} \int_{\lambda_1}^{\lambda_2} \int_{E(t_1)}^{E(t_2)} P(E, R, \theta, \lambda) T(\lambda - \lambda_0) R(\lambda) dt d\lambda d\Omega \quad (8)$$

which reduces to

$$F(\lambda_0, \Delta\Omega) = n_e P(E_{\max}, \lambda_0) \frac{\Delta\Omega}{2\pi} A = KV_F \quad (9)$$

under the following simplifying assumptions: (a) that $P(E, R, \theta, \lambda) \approx P(E, R, \lambda)$ (the variation of $P(E, R, \theta, \lambda)$ over the aperture is about 0.1 percent over a 1 cm diameter aperture 13.26 meters from the tangent point); (b) the gate time used for determining $F(\lambda_0, \Delta\Omega)$ is short enough so that $P(E, R, \theta, \lambda) \approx P(E_{\max}, R, \theta, \lambda)$ and (c) the filter is sharp enough so that $P(E_{\max}, \lambda) = P(E_{\max}, \lambda_0) (1 + a(\lambda - \lambda_0))$. Under these assumptions the quantity A is a simple calculable factor while K is the detector sensitivity where F watts input to the detector-filter amplifier combination produces a response of V_F volts. The quantity K is determined by the detector system response to an irradiance standard. Thus

$$KV_S = \int_{\lambda_1}^{\lambda_2} \int_{\Delta\Omega'} S(\lambda, \theta) T(\lambda - \lambda_0) d\Omega d\lambda \quad (10)$$

which reduces to

$$KV_S = S(\lambda_0) \Delta\Omega' B \quad (11)$$

if the standard spectral irradiance $S(\lambda, \theta)$ is constant over the solid angle $\Delta\Omega'$ and if the filter has a narrow enough bandpass so that $S(\lambda, \theta) = S(\lambda_0) (1 + b(\lambda - \lambda_0))$. The quantity B is eq (11) a calculable factor like A in eq (9). Substituting eq (11) into eq (9) we have

$$n_e = C \frac{S(\lambda_0)}{P(E_{\max}, \lambda_0)} \frac{V_F}{V_S} \quad (12)$$

with $C = 2\pi B \Delta \Omega' / (A \Delta \Omega)$ a calculable quantity containing the solid angle factors and the results of integrating eq (8) and eq (10) under the assumptions listed in the preceding paragraphs.

This approach is valid for both accelerated and monoenergetic electrons. Although the case of an accelerated beam was used as an example, the form of eq (12) is the same for monoenergetic electrons. (The most important difference is that for accelerated electrons one must measure the instantaneous number of electrons since the power averaged over one acceleration cycle is used to compute the flux incident on the spectrometer.) The determination of the number of circulating electrons by this method is essentially reduced to a problem of measuring a voltage ratio. The sources of error intrinsic to this method will be discussed in later paragraphs.

The vuv irradiance incident on the spectrometer can be given in terms of eq (6) and eq (12):

$$F(\lambda, \Delta \Omega) = C \frac{S(\lambda_0)}{V_S} \frac{V_F}{P(E_{\max}, \lambda_0)} P(E_{\max}, \lambda). \quad (13)$$

The spectral irradiance incident on the spectrometer is known in terms of calculated quantities and a measured voltage ratio.

Calculations evaluating $P(E_{\max}, \lambda)$ were carried out to a accuracy of better than 1 percent. For monoenergetic electrons, because the integration over the time variation of the electron energy is eliminated, the accuracy of the calculation is an order of magnitude greater than the uncertainty in the flux due to uncertainties in the electron energy. Determining the response of the instrument, $R(\lambda, \Delta \Omega)$, is the next task.

3.3. Positioning of Spectrometer

To determine the flux on the spectrometer, the spectrometer must be aligned at a known angle with respect to the orbital plane of the radiating electrons. In addition, any temporal variation of the inclination of the orbit must be determined since the irradiance is a strong function of the azimuthal angle θ .

Two types of spectrometers have been calibrated at SURF-I: A grazing incidence monochromator [26] and a Wadsworth [27] spectrometer using photographic detection. The instrument to be calibrated, S , (see fig. 6) was installed behind the calibrated detector, C , aperture assemble, A , and an alignment procedure was undertaken with the aid of the visible radiation from the orbiting electrons. The visible radiation was also used to check the effectiveness of the baffling system in eliminating reflections. Since the light beam is almost parallel (average divergence is 3 mrad) and about 1 cm in diameter it is impossible

to fill the grating of many spectrometers. Therefore, provisions were made to scan the beam over the grating by moving the instrument. It is not necessary to make absolute flux measurements during these scans but only measurements relative to the point of calibration on the grating. For this procedure synchrotron radiation was used for convenience rather than out of necessity. At the storage ring radiation facility, SURF-II, two ports with a direct view of the beam will be provided for instrument calibration. However, at the present time the user must supply his own test chamber to house the instrument to be calibrated.

Synchrotron radiation is highly polarized with the most intense component of polarization lying in the orbital plane. To test the instrument response to this polarization, provisions were made to rotate each instrument about the grating pole. For the grazing incidence monochromator the axis of rotation was coincident with a line drawn from the grating pole to the center of the entrance slit. For the Wadsworth mounting the instrument rotated about an axis passing through the grating pole perpendicular to the rulings. To preserve the geometry of illumination under rotation it was important to align the axis of rotation with the axis of symmetry of the beam. By using the visible radiation from the synchrotron it was possible to make these adjustments without evacuating the instrument chamber. Therefore the alignment procedure could be carried out in a straightforward convenient manner.

At SURF-I the position of the orbital plane could be determined and instruments could be aligned with the plane so that the beam and the optic axis are coincident. The position of the orbital plane was determined by scanning in the vertical direction a grazing incidence monochromator set at a short wavelength (about 200 Å) and oriented so that its entrance slit was horizontal. The position where the maximum output from the monochromator occurs defines the position of the orbital plane. The monochromator was left in this position and the movable aperture, A , was scanned vertically to determine the upper and lower slit occultation positions. Setting the aperture at the average of the upper and lower slit occultation positions aligns its center with the center of the entrance slit. The aperture is set on the orbital plane, the entrance slit of the instrument for calibration is then aligned with the aperture and the optic axis can be aligned with the synchrotron radiation beam by centering the radiation transmitted through the entrance slit on the grating.

Unfortunately, during the course of a day's operation at SURF-I thermal gradients in the magnet produced beam motions of up to one milliradian. Such a motion can produce a large variation in the flux illuminating the optical elements of an instrument. As an example, in figure 7 the variation in output flux from a special toroidal grating monochromator at a wavelength of 188 Å correlates very closely with the temporal variation of the position of the beam illuminating the toroidal grating. Notice that a motion of 0.26 mrad produces a flux variation of 7 percent. A beam motion monitor described in the next section was devised to

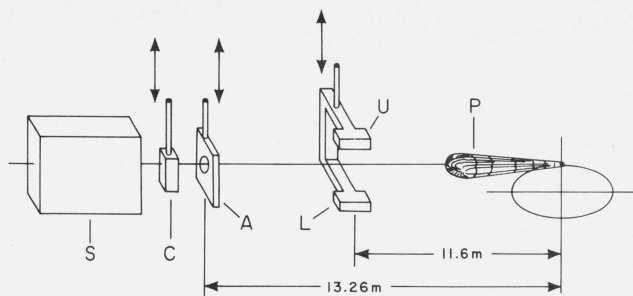


FIGURE 6. Schematic diagram of spectrometer calibration apparatus.

Synchrotron radiation P , illuminates detectors U and L in the beam motion monitor and the calibrated aperture A . Radiation passing through A illuminates either the spectrometer S or the calibrated detector-filter (C).

track this beam motion in addition to providing intensity monitoring during calibration. By monitoring the beam motion it was possible to determine that the beam always moved in one direction, that the greatest motion occurred during the first hour or so of operation, and finally that the daily motion of the beam was regular. A calibration could be carried out when the beam was positioned within acceptable limits.

Beam motion was a potential source of systematic error and a needless complication to the calibration procedure. The conversion of the NBS synchrotron into a storage ring will virtually eliminate beam motion because (a) there will be no eddy current heating in the magnet and (b) the only other important source of heat, the power dissipated in the magnet excitation coils, has been eliminated by water cooling the coils. Consequently, spectrometer calibration at SURF-II will be much more accurate and straightforward.

4. Parameter Measurement and Their Uncertainties

4.1. Measurement of the Electron Current and Beam Position

This basic monitoring system consisted of a detector-filter combination which was calibrated periodically with an irradiance standard and a pair of detectors used both as a beam motion monitor and as an intensity monitor during the spectrometer calibration when the calibrated detector-filter was removed from the beam. The geometrical layout is shown schematically in figure 6. The beam motion monitor was located in front of the calibration aperture 11.6 meters from the tangent point. The central portion of the beam of radiation passed between the monitor diodes to reach the calibration aperture (A). The beam was then allowed to enter either the calibrated detector-filter (C) or the spectrometer (S). The two diodes serving as the beam motion monitor (U, L) were separated by an angle of 3.3 mrad. Nicol prism polarizers placed in front of these detectors were adjusted to view the component of the beam polarized perpendicular to the orbital plane.

Each detector was displaced symmetrically about the orbital plane and viewed radiation for which the

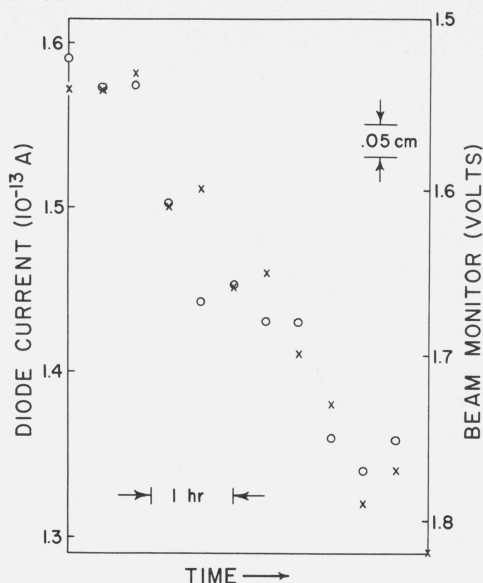


FIGURE 7. Output from the beam motion monitor (BMM) shown as 0 and the output of a diode shown as x versus time.

The diode measures the vuv flux diffracted by a grating illuminated directly by the synchrotron radiation beam.

intensity varied linearly with angle. This is illustrated in fig. 8. Thus if the beam moved upward slightly the signal in the upper detector (U) would decrease an amount proportional to the beam motion and the signal in the lower detector (L) would increase by about the same amount (assuming the sensitivity of the detectors

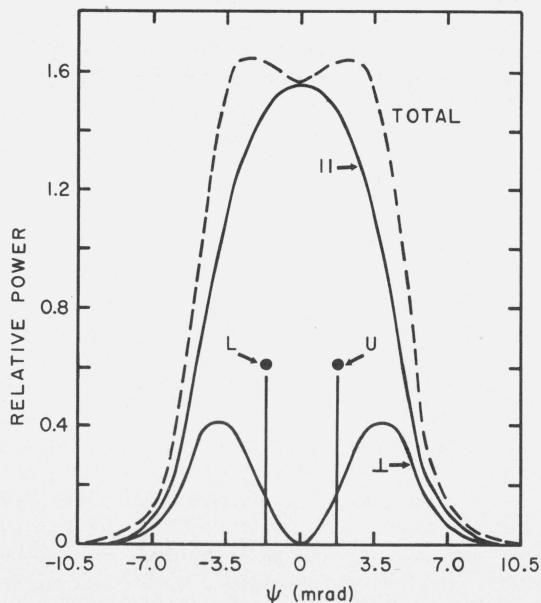


FIGURE 8. Angular distribution of the synchrotron radiation showing the total angular distribution of the flux as well as the component of the flux polarized parallel (\parallel) and perpendicular (\perp) to the orbital plane.

The angular position of the upper (U) and lower (L) beam motion monitors is shown.

are the same). Thus the beam motion, $\Delta\phi$, is proportional to the fractional change of the signal level in the detectors. To first order the beam displacement $\Delta\phi = K(U-L)/(U+L)$, assuming that the sensitivity of the detectors is adjusted equal. The output from the upper detector (U) and the lower detector (L) were amplified and manipulated so that the sum ($L+U$) and difference ($L-U$) were obtained. Using the ($L-U$) signal as the numerator input and the ($L+U$) signal as the denominator input to a quarter-square analogue dividing circuit, the output ratio $R = \frac{L-U}{L+U}$

was proportional to the beam position. A block diagram of the electronic circuitry of the beam motion is shown in fig. 9a. The monitor was calibrated by moving the

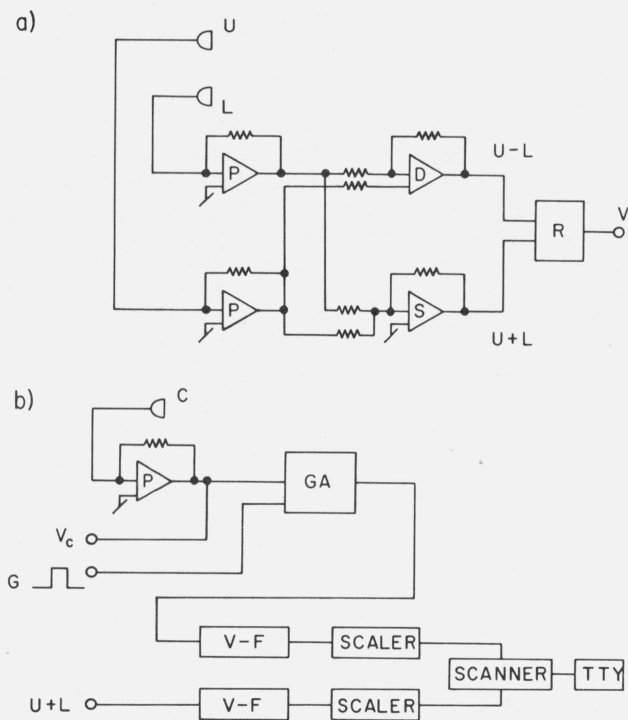


FIGURE 9. (a) Schematic of the electronic circuitry of the beam motion monitor.

Photocurrents from U and L are converted to voltages by P . The sum and difference of these voltages are generated in the amplifiers S and D respectively. The output of S and D is the input for a quarter square divider R , which provides the ratio $(U-L)/(U+L)$.

(b) Schematic of the electronic circuitry used to transfer calibration from calibrated detector to $U+L$.

Photocurrent from calibrated detector-filter combination C is converted to a voltage by P . The output of P or a calibration V_c is the input of a gated amplifier GA whose output is digitized along with $U+L$, the sum signal from the beam motion monitor. The signals $U+L$ and GA are counted on scalars, scanned and printed on a teletype.

detectors some distance and noting the signal change in R . The calibration curve is shown in fig. 10. The sum signal ($L+U$) to first order is independent of beam position and was used as an intensity monitor during actual spectrometer calibrations to determine the temporal variation in n_e while R monitored the change

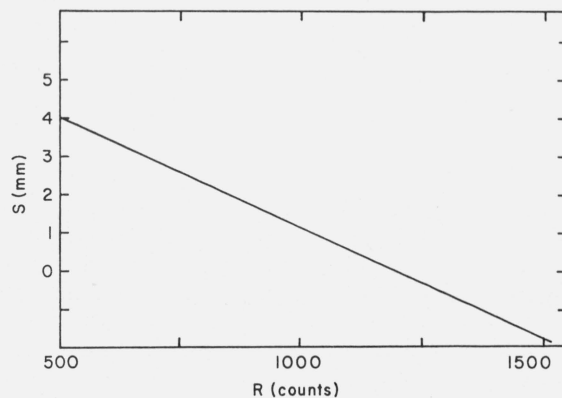


FIGURE 10. The position (S) of the beam motion monitor (BMM) versus the output of ratio R of the BMM.

in beam position. The calibrated detector-filter system provided the absolute measurement of n_e .

An improved system for locating the orbital plane will be used at SURF-II. A pair of open xuv diodes covered with thin carbon foil filters (transmitting between 40 and 250 Å) will be placed above and below the orbital plane. The short wavelength is used to minimize the divergence of the synchrotron radiation beam (see fig. 2) so as to obtain maximum sensitivity. The two diodes will be mounted on a rotatable plate allowing their positions to be interchanged. Thus the position of the orbital plane can be determined as the height at which an interchange of the diodes produces no change in the ratio of the signals from the diodes. This system is expected to be a big improvement over that used on SURF-I.

The temporal stability of the sensitivity of the calibrated detector-filter system and the monitor detectors was sufficient so that it was adequate to calibrate the detector-filter system with an irradiance standard just before and just after the actual spectrometer calibration took place. In a similar manner the calibration was transferred to the monitor diodes sometime during the calibration. Figure 9b shows schematically the measuring system used with the calibrated detector-filter system. The instantaneous voltage is measured by putting the output of the photodiode amplifier (which is fast enough to track the time variation of the light during the acceleration cycles) into a linear gate that is synchronized to the repetition frequency of the accelerator. A peak-reading voltmeter is used to measure and suitably average the voltage pulses that are proportional to n_e . The width and position of the gate input to the gated linear amplifier is suitably chosen so that the light output in the visible is approximately constant over that portion of the acceleration interval. For the accelerated electrons the complicated integral over the time variation of the electron energy is replaced by a small correction factor amounting to a few percent of the value of flux obtained for monoenergetic electrons of energy E_{\max} . This numeric simplification is offset to some extent by more complicated electronics. For stored monoenergetic electrons it is unnecessary to use a gated amplifier, an ordinary

digital voltmeter or other suitable recording device can be used to measure the voltage, and, moreover, no correction is necessary because the electron energy is constant. Because of these factors, n_e can be determined much more accurately for stored electrons than for accelerated electrons.

Two types of spectrometers have been calibrated at SURF-I a grazing-incidence monochromator [26] and a Wadsworth [27] spectrometer using photographic detection. For the monochromator it was easy to use the same visible detector gate for gating the output of the monochromator. For the spectrograph, n_e was assumed constant over the acceleration cycle. This assumption was tested and will be discussed in the section 4.3.

The NBS irradiance standard used to calibrate the filter-detector system was too intense to be used at the calibration distance (1 meter). To achieve the signal level appropriate to the synchrotron (nW/nm), the calibration was carried out with the lamp located at distances between 25 m and 40 m. Thus the validity of the inverse square law was assumed in order to scale the intensity from the lamp calibration distance (1 m) to the detector calibration distance (25 m–40 m). We determined that the measurements over the 25 m–40 m path were consistent with the inverse square law to ± 1.0 percent, the uncertainty level of the measurements. Reproducibility of the measurements with respect to the realignment, lamp current adjustment, detector orientation, etc. was ± 2 percent. Lamp calibration was tested by comparing the working irradiance standard with another standard. The intensity of the working standard derived from the comparison deviated less than 2 percent from its specified value. Combining these sources of errors in quadrature, the quantity $S(\lambda_0)$ in eq 12 could be determined with a probable error of 3 percent. In table 2 we have listed the sources of the errors that contribute to the uncertainty of n_e . Combining all these errors in quadrature we find that n_e can be determined with a probable error of 6 percent.

Possible sources of systematic errors that pertain

TABLE 2. Sources of errors contributing to the uncertainty in the determination of the number of electrons, n_e , in SURF-I.

Source of Error	Magnitude of error
Transfer of calibration to beam motion monitor	3 %
Determination of change in detector efficiency	3 %
Correction factor for accelerated electrons	1 %
$S(\lambda_0)$	3 %
C	1 %
$P(E_{\max}, \lambda_0)$	1 %
V_F	1 %
V_S	1 %
Probable error of $n_e = 6\%$	

to the determination of n_e were investigated such as the assumption that the standard lamp was a point source (implying the validity of the inverse square law), the possibility that the detector interference filter was not properly blocked, or the presence of reflected radiation sources either at the synchrotron or the lamp calibration hall. From an analysis of these possible sources of errors and other tests, we estimate that sources of systematic errors might contribute a 5 percent uncertainty to the measurement of n_e .

A storage ring (SURF-II) is now the source of synchrotron radiation at NBS. Using improved techniques and fewer transfers with SURF-II, the uncertainty in the measurement of n_e should be reduced by at least a factor of two to a probable error of 3 percent. By further testing and cross checking we expect to reduce the systematic error by the same amount. It is very clear that the increased stability both in time and in space achieved at SURF-II will result in an excellent calibration facility for wavelengths in the vuv. Furthermore with the low intensity electron counting method mentioned section 3.2 the error is zero since the total number of electrons is known exactly.

The method of positioning the spectrometer at SURF-I was described in the early paragraphs of this section. The estimated uncertainty in positioning the instrument on the orbital plane according to that method is ± 3 mm at a distance 13.26 m from the tangent point or ± 0.2 mrad. Beam motion monitor drift and other uncertainties associated with the monitor system would increase the positioning uncertainty to ± 4 mm or ± 0.3 mrad. To estimate the error caused by misaligning a spectrometer with respect to the orbital plane, the flux that passed through a circular aperture 1 cm in diameter, located a specified angle off the orbital plane, was calculated. The fractional error in the flux determination for such a misalignment is shown as a function of wavelength in fig. 11. As expected the greater the misalignment the greater the error. However, for displacements of up to 0.4 mrad the error is less than 10 percent for wavelengths greater than 200 Å. For misalignments of 0.8 mrad the error exceeds 10 percent only for wavelengths less than 600 Å. This strong dependence of the error on wavelength is due, of course, to the highly collimated nature of synchrotron radiation, particularly the fact that short wavelength radiation is more tightly collimated than longer wavelength radiation (see fig. 2). Therefore, as the aperture is displaced with respect to the orbital plane, the shorter wavelength radiation becomes occulted first while the longer wavelength radiation, due to its broader angular distribution, is relatively unimpeded. By confining the alignment error to ± 4 mm, (0.3 mrad) at SURF-I the fractional error in intensity is limited to something less than 5 percent at 200 Å decreasing to about 0.5 percent at 1200 Å.

At the SURF-II calibration facility the position of orbital plane will be known to high precision by means of the orbital plane locator described in section 4.1. Therefore errors introduced because of uncertainties in the beam position will be negligibly small.

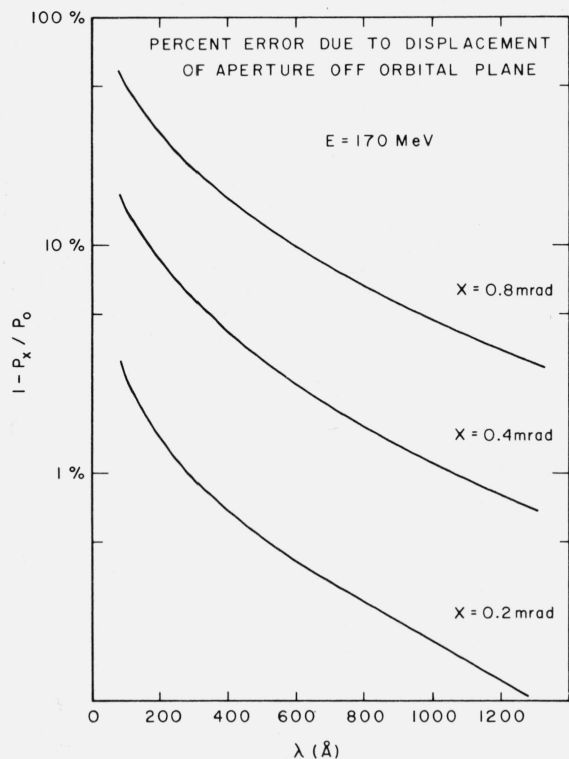


FIGURE 11. The percent error due to the displacement of aperture *A* in figure 7 by the indicated angle *X* from the orbital plane.

The curves were calculated for accelerated electrons whose maximum energy was 170 MeV.

4.2. Uncertainty in the Orbital Radius of the Electrons

The magnet geometry at SURF-I and SURF-II is such that the electrons travel in very nearly circular orbits. Thus *R*, the orbital radius, is simply related to the rf accelerating frequency ν_0 (known to a few parts-per-million). However in practice, since the beam executes small betatron oscillations about the equilibrium orbit, knowledge of the value of *R* is limited by the extent of these horizontal oscillations which typically have a radial amplitude of a few mm. However since the oscillations result in an instantaneous radius that is equally likely to be larger or smaller than the equilibrium radius, errors in flux determinations tend to cancel. The beam also executes betatron oscillations in the vertical plane which smear the angular distribution somewhat. The extent of this smearing has been computed [28] and while the sum of the intensity due to both polarizations changes very little from the distribution of radiation by a point source of electrons, the magnitude of individual polarization components is affected somewhat. The effect is very small in SURF-I because the observations [4] of both polarization components deviated only slightly from distribution expected for a point source. For the spectrometer calibrations achieved on SURF-I a point source was assumed and the flux distribution was computed

accordingly. We estimate that this assumption contributes an error of less than 1 percent to the total flux calculations. Also the beam rather than being 100 percent polarized in the orbital plane is about 95 percent polarized. The response of a spectrometer to both planes of polarization while an important test does not affect the accuracy of the instrument calibration for unpolarized radiation since the average response to both orientations is used. However to properly determine the amount of polarization an instrument introduces to unpolarized radiation the degree of polarization of the radiation on the instrument should be measured.

4.3. Determination of *E*, the Electron Energy

In its early life the synchrotron supplying radiation for SURF-I was used for the production of gamma rays. The maximum energy of the electrons accelerated in this synchrotron was determined, at that time, both from the threshold energy for the production of π^0 mesons and from the kinematics of the reaction $h\nu + \text{C}^{12} \rightarrow p + \text{B}^{11}$. An integrating fluxmeter measured the ac magnetic field at a point away from the electron orbit, to which the energy calibration of the nuclear reaction could be attached (since $E_{\text{max}} \propto B_{\text{max}}$). This fluxmeter was also used to measure the maximum electron energy when the synchrotron became the radiation source for SURF-I. At the time of calibration the maximum energy of the electrons was known to 0.6 percent.

At SURF-I measurements were made to test the assumption made in section 3.1 that (a) the electron energy varied sinusoidally and (b) that the number of electrons captured, n_e , was constant over the acceleration cycle. A grazing incidence monochromator was set at 212 Å. The output pulses from this monochromator were accumulated in a multichannel analyzer (MCA) whose sweep was synchronized with the acceleration cycle of the synchrotron. The analyzer display, shown as open circles in fig. 12, represents the instantaneous intensity (averaged over many machine cycles) as a function of time. The dwell time for each channel is 50 μs . The vertical aperture of the apparatus to the 212 Å radiation was large enough so that all of the radiation entered the monochromator. The solid line represents the flux integrated over all azimuthal angles and normalized to the peak of the time distribution. The flux was calculated for an electron energy variation proportional to $\sin(2\pi 60t)$. The time scale has an arbitrary zero so that the maximum count rate, which corresponded to the maximum electron energy, occurred at $t = 2.2$ ms rather than $t = 4.17$ ms. Note the step at 3.6 ms, about 1.4 ms after the maximum count rate. The rf voltage is turned off at this time because the electrons can no longer be maintained in a stable orbit as the magnetic field decreases. From a comparison of the calculated curve with the observations it is quite plain that the electron energy is proportional to $\sin 2\pi 60t$. If the number of electrons captured per cycle were not constant then the data in fig. 12 would not fit the symmetrical calculated curve. As a by-product of the measurement we may note that

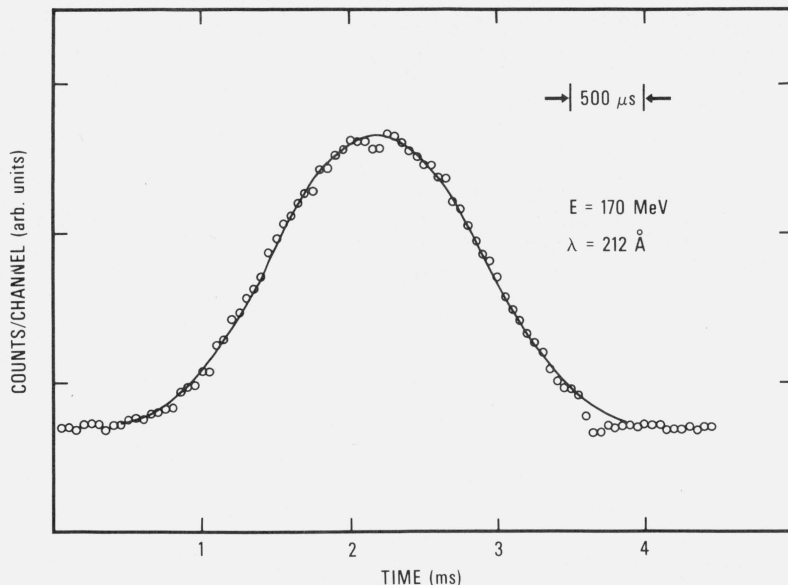


FIGURE 12. Photon flux per 50 μs channel dwell time versus time (zero displaced shown as 0).

The flux was integrated over many cycles at 212 \AA for electrons accelerated to a maximum energy of 170 MeV. The solid line is the calculated photon flux.

if the maximum energy were much greater than 170 MeV, the full width at half maximum of the distribution would be somewhat wider since the electrons would radiate at 212 \AA sooner, broadening the time distribution. However, this is not a very sensitive electron energy indicator because for an electron whose peak energy is 170 MeV a 10-MeV variation in energy produces only a 7 percent variation in the full width at half maximum of the time varying light flux at 200 \AA . Nonetheless, the observations are consistent with a maximum electron energy of 170 MeV with an uncertainty of ± 5 MeV. As a further consistency check the accuracy of maximum electron energy changes was tested by another experiment. As before the output of the monochromator at 212 \AA was recorded by a MCA synchronized to the acceleration cycle of the synchrotron. The maximum electron energy was first set at 170 MeV and the signal was integrated for a time determined by integrating the light flux in the visible to some predetermined level. The maximum energy was then set at 160 MeV and the integration was carried out using the multichannel analyzer until the visible light integration reached the same level as before. Since the visible flux is very nearly independent of energy (the flux at 5150 \AA for 160 MeV electrons is only about 2 percent less than the flux at 5150 \AA for 170 MeV electrons), an equal number of electrons contribute to the time distribution for $E_{\text{max}} = 170$ MeV as for $E_{\text{max}} = 160$ MeV (once the 2 percent correction is made). As these curves are normalized to the same number of electrons, the instantaneous flux radiated by electrons when their energy is E should be the same independent of the eventual maximum energy. If $E_{\text{max}} = 170$ MeV the flux radiated by these electrons at

160 MeV should equal the flux radiated by electrons at their maximum energy when $E_{\text{max}} = 160$ MeV.

In figure 13 the 170 MeV data is shown as dots while the 160 MeV data (normalized to the same total number of electrons) is shown as solid squares. The large tic on the abscissa indicates the time when electrons whose maximum energy is 170 MeV have an instantaneous energy of 160 MeV. A horizontal line indicating the instantaneous flux radiated by 160 MeV electrons guides the eye to the data where the maximum electron energy is 160 MeV. The correspondence between the data is quite clear. Two short horizontal lines, one above and the other below the data for which the maximum electron energy was 160 MeV, indicate the instantaneous flux radiated by electrons of energy 158 MeV and 162 MeV. From figure 13 we see a change of electron energy of 2 MeV produces a rather large change in intensity at this wavelength. From this data we infer that the probable error in the energy change of 10 MeV was about 0.2 MeV.

To determine the systematic error introduced by the quoted uncertainty in the maximum energy (0.6%), the percent change in flux for an electron energy change of 1 MeV (0.6%) at 170 MeV is plotted as a function of wavelength in figure 14. Notice as the wavelength increases the photon flux change is much less sensitive to changes in the electron energy. At 200 \AA such an uncertainty in energy results in a 9 percent uncertainty in the photon flux. This uncertainty decreases monotonically to 1 percent at a wavelength of approximately 2000 \AA .

At the SURF-II storage ring a great deal of effort has been expended to measure the (now dc) magnetic field at the orbit to 0.1 percent. A highly accurate

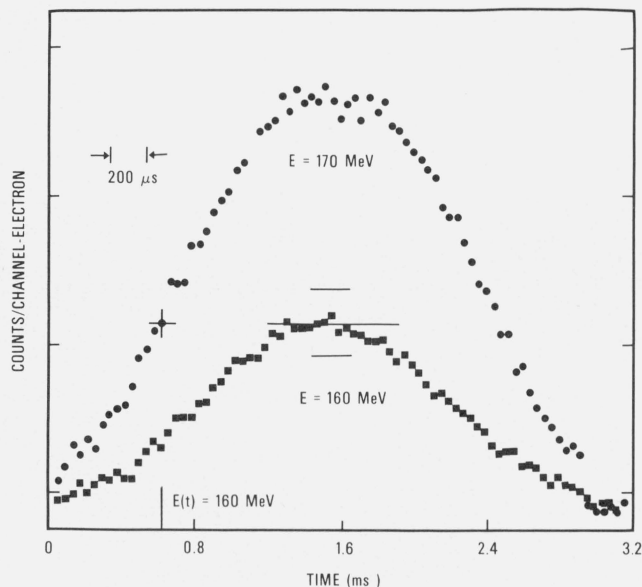


FIGURE 13. Instantaneous photon flux normalized to the same total beam current for two maximum energies: $E_{\max}=170$ MeV and $E_{\max}=160$ MeV.

Vertical line on abscissa denotes time when electrons with $E_{\max}=170$ MeV have an energy of 160 MeV. The horizontal lines indicate the maximum flux expected if $E_{\max}=162$ MeV or if $E_{\max}=158$ MeV.

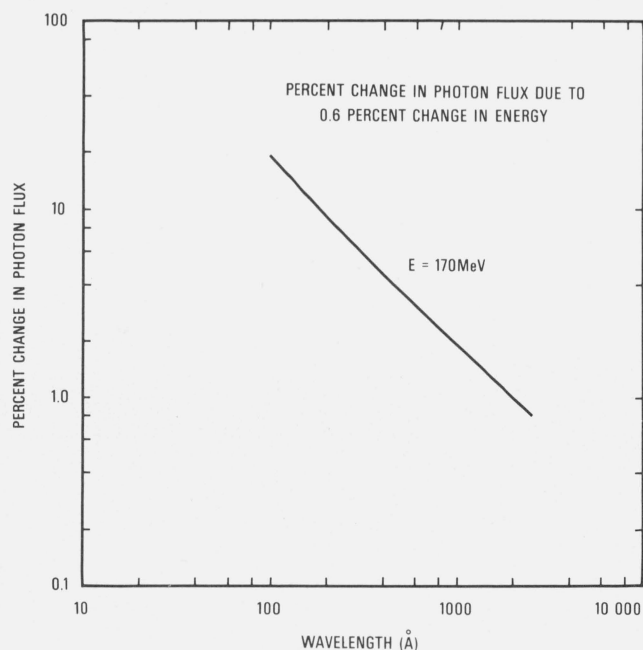


FIGURE 14. Percent change in photon flux emitted by accelerated electrons with $E_{\max}=170$ MeV due to a 0.6 percent change in electron energy.

Hall probe (calibrated by the NBS magnetic field calibration group to 0.1%) is inserted at a point on the electron orbit. Because an active probe would interfere with the electron beam, the orbital field calibration

was transferred to the Hall probe field monitor located away from the electron orbit.

With the magnetic field and hence the electron energy known to this accuracy, radiometric uncertainties will be much less, as is indicated in figure 15. In this figure we show as a function of wavelength the flux change, passing through an aperture subtending an angle 2 mrad centered on the orbital plane and 1 mrad along the orbit, that is due to a change in electron energy of 0.1 percent. The flux change for 200 MeV *monoenergetic* electrons is shown in the top curve while the bottom curve represents the flux change for 240 MeV *monoenergetic* electrons. With the electron energy known to this accuracy, it is possible to keep the uncertainties in photon flux less than 5 percent for all wavelengths greater than 40 Å, the practical short wavelength limit of our storage ring. Now instead of being one of the major sources of systematic error, especially at shorter wavelengths, the uncertainty in the energy introduces one of the smaller errors into the calibration process.

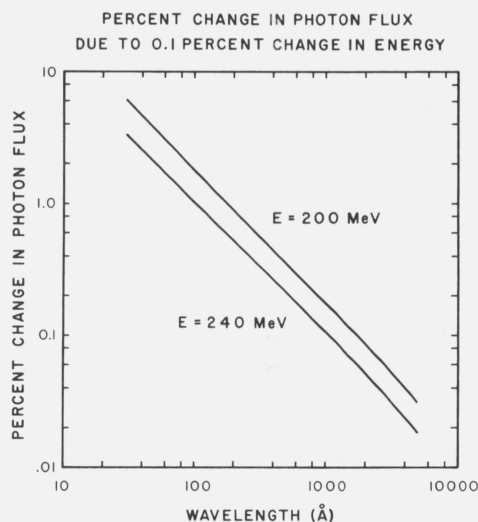


FIGURE 15. Percent change in photon flux emitted by monoenergetic electrons with the energies shown for a 0.1 percent change in the electron energy.

The uncertainty of 0.1 percent is that expected at SURF-II.

5. Summary

In this report we have dealt with the use of synchrotron radiation as an absolute irradiance standard in the vacuum ultraviolet in general. In addition, we detailed the calibration procedures devised at the NBS-SURF-I facility for several spectrometer calibrations. General sources of systematic errors were identified and their importance was studied relative to SURF-I. Improved calibrations are anticipated at the NBS storage ring (SURF-II) based mainly on better energy determination of the monoenergetic electrons, higher spatial and temporal beam stability due to the storage ring operation and finally, a more accurate determina-

tion of the circulating current. Table 3 is a final summary of the sources of errors for SURF-I and SURF-II and the role they play in the overall accuracy of a calibration.

TABLE 3. Sources of errors in the use of synchrotron radiation as an absolute source

Error source	Type ^a	Magnitude of error	
		SURF-I	SURF-II
Determination of n_e	R	6%	3%
	S	6%	3%
Electron energy calibration	S	8%–1% ^b	5%–0.04% ^c
Electron energy variation	R	8%–1% ^b	Negligible ^d
Orbital radius	S	< 2%	< 1%
Uncertainty in beam position	S	5%–0.5% ^b	< 1%
Finite source size	S	< 1%	< 1%
Precision of calculated model	S	< 4%	< 1%
Total	R	11%–6%	3%
	S	< 10%	< 6%

^aR designates random errors and S designates systematic errors.
^bThe first value is the uncertainty at 200 Å and the second value is the uncertainty at 2000 Å.
^cThe first value is the uncertainty at 40 Å and the second value is the uncertainty at 2000 Å.
^dA readout of electron energy will be available.

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