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The Crystal Structure of BaCa(CO₃)₂ (barytocalcite)

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The barytocalcite phase of BaCa(CO₃)₂ crystallizes in the monoclinic unit cell $a = 8.092(1)$ Å, $b = 5.2344(6)$ $\rm \AA$, $c = 6.544(1)$ $\rm \AA$, $\rm \beta = 106.05(1)^{\circ}$ at 25° C with cell contents of 2[BaCa(CO₃)₂]. The structure previously reported by Alm is correct in its coarse details but has been redetermined here and refined to R_w = 0.028, $R = 0.023$ in space-group P_{11}/m using 1652 observed reflections. Corrections were made for absorption, isotropic extinction, and anomalous dispersion.

The structure of barytocalcite has an ... ABCABC ... stacking of cation layers and repeat every 3 layers. The calcite phase of CaCO₃ has an ABC cation layer sequence and repeats every 6 layers. The orientations of the $CO₃$ groups in barytocalcite are like the $CO₃$ group orientation in the aragonite phase of $CaCO₃$, and are rotated about 30[°] from the $CO₃$ group orientation in calcite. The cation layer sequence in aragonite is . . . ABAB . . . and the structure repeats every 2 layers.

The Ca ion in barytocalcite is coordinated to seven oxygens, including an edge of a CO₃ group, with Ca... O distances in the range 2.305(2) Å to 2.518(2) Å. The Ba ion is coordinated to five edges and one apex of the CO₃ groups with Ba... O distances ranging from 2.729(3) \AA to 3.140(2) \AA . The distances of the C atoms in the CO₃ groups from the planes of the O atoms are 0.025(5) Å and 0.022(4) Å for $C(1)$ and $C(2)$, respectively.

Key words: Aragonite: barium calcium carbonate: calcium carbonate: crystal structure: single crystal x-ray diffraction.

Introduction 1.

The crystal structure of the barytocalcite phase of $BaCa(CO₃)₂$ has been redetermined in our program of structural investigations $[1]$ ¹ on calcium carbonates, calcium phosphates, associated hydrates, and related compounds. The structural features in these compounds have important applications in understanding possible epitaxy, syntaxy, and substitutional solid solution in biological minerals such as hydroxyapatite $(Ca₅(PO₄)₃OH)$ and calcite, aragonite and vaterite, the three phase of anhydrous $CaCO₃$.

From a consideration of the morphologies, d -spacings and possible space-groups of barytocalcite and calcite, Gossner and Mussgnug [2] gave a structure for barytocalcite which is a rearrangement of the calcite structure. They assumed the space-group to be $P2_1$. Alm [3] used a relatively large (0.3 mm) single crystal of barytocalcite and unfiltered Cu radiation to collect photographic data from the $h0l$, $h1l$, $hk0$ and hkh levels. He also assumed the space-group to be $P2_1$, rather than $P2_1/m$, on steric considerations which are invalled. The structure he gave for barytocalcite differs from that given by Gossner and Mussgnug in the orientations of the $CO₃$ groups. However, Alm made no corrections for what must have been considerable absorption, gave no

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Data Collection and Structure Refinement $2.$

The crystal used in the data collection is an approximate sphere, radius 0.094(3) mm, ground from a crystal from mineral sample R13868 (from Cumberland, England) obtained from the National Museum of Natural History, Smithsonian Institution, Washington, D.C., and supplied by J. S. White, Jr. It was mounted in our usual way [4].

formula (ideal): $BaCa(CO₃)₂$ (barytocalcite phase). cell: monoclinic $a = 8.092(1)$ Å at 25 °C $b = 5.2344(6)$ Å $c = 6.544(1)$ Å β = 106.05 (1)^o volume = $266.4\AA$ ³ space-group $P2_1/m$; cell contents $2[BaCa(CO_3)_2]$ reciprocal lattice extinctions, $0k0$: $k = 2n + 1$ calculated density 3.72 $g\text{-}cm^{-3}$; observed density $3.71 \text{ g} \cdot \text{cm}^{-3} [5]$.

In the determination of the unit cell and in the collection and processing of data, the general procedure

standard deviations on any parameters and used limited film data. The structure of barytocalcite was, therefore, poorly known by modern standards, and has been redetermined here.

in reference [4] was followed. In the present case, 3379 reflections were collected from the *±h+k+l* and *±h-k+l* quadrants and merged into a unique set of 1772, of which 1652 are "observed" and 120 are "unobserved." The *R* factor

$$
\sum_{hkl}|\,F_{hkl}^{\,i}\!-\!F_{hkl}^{\,j}\,|/\sum F_{hkl}^{\,i}\,
$$

with $i < j$ between pairs F_{hkl}^i and F_{hkl}^j of observed equivalent reflections *F hkl* was 0.018 calculated over 1189 pairs. *i* and j are the sequence numbers in the list of equivalent reflections. Absorption corrections for a sphere with μ =85.6 cm⁻¹ were applied. The maximum and minimum transmission factors were 0.347 and 0.317, respectively.

The $\theta - 2\theta$ scans were carried out on an automated Picker² diffractometer at $2^{\circ}/$ min for 2θ ; backgrounds were counted for 20 s each. Because the least significant digit in all counts was dropped by the Picker hardware, standard deviations, σ_{hkl} , of the structure factors, F_{hkl} , were estimated from $\sigma_{hkl} = F_{hkl}/5.7$ for F_{hkl} < 5.7; σ_{hkl} = 1 for 5.7 < F_{hkl} < 30; and σ_{hkl} = F_{hkl} /30 for F_{hkl} > 30 where F_{max} on this arbitrary scale is 113. The scattering factors used were those for the neutral atoms in reference 6 for the x·ray 67 refinements and those in references 7 and 8 for the extinction and anomalous dispersion refinements.

The quasi·normalized structure factor statistics on our barytocalcite data indicate that the structure is acentric, since $\langle |E| \rangle = 0.885, \langle E^2 \rangle = 1.00$ (fixed), $<$ $|E^2-1|$ > = 0.709; the corresponding theoretical values are 0.886, 1.000, 0.736 for the acentric case and 0.798, 1.000, 0.968 for the centric case. *E* is the quasinormalized structure factor [9]. The fraction of *E* values greater than 1.0,2.0 and 3.0, respectively, was found to be 0.405 , 0.0027 and 0.0000; the corresponding theoretical values are 0.368 , 0.0183 , 0.0001 for the acentric case and 0.317 , 0.0455 , 0.0027 for the centric case. The statistical procedure suggested an average temperature factor, \overline{B} , of about 2.5 \overline{A}^2 and an exponent of 1.00 for $\sin \theta / \lambda$. Our experience has been that the quasi-normalized structure factor statistics are normally much closer to the theoretical values and the exponent of $\sin \theta / \lambda$ is closer to 2.00 than was calculated here for barytocalcite.

Because of the presence of the strongly scattering Ba ions, this indication that the space-group is the acentric $P2_1$ was not considered to be reliable. The structure of barytocalcite was redetermined by us from a sharpened Patterson function calculated with (E^2-1) coefficients and an F_0 Fourier electron density synthesis phased from the positions of the Ba and Ca ions. The γ coordinate of Ba was set equal to zero to define the origin along b. The structure was refined isotropically in space-group $P2_1$ to $R_w = 0.65$, $R = 0.057$ and then anisotropically in P_{2₁} to $R_w = 0.036$, $R = 0.028$ using the x-ray 67 system of computing programs [10]. The least-squares refinements used the full matrix, minimized $\Sigma w(|F_0|-|F_c|)^2$, and included those unobserved reflections for which F_{hkl} calculated more than $2\sigma(F_{hkl})$.

The highest peak in an electron density difference synthesis calculated after anisotropic refinement was equivalent to about 1/3 of an electron and was 0.49 A from Ba. When the space-group is assumed to be $P2_1$ the largest correlation coefficients are 0.90 to 0.95 between (i) x of $O(1)$ and x of $O(2)$, (ii) z of $O(1)$ and z of 0(2), (iii) *x* of 0(4) and *x* of 0(5) and (iv) *z* of 0(4) and *z* of O(5); 0.80 to 0.90 between (i) B_{11} of O(1) and B_{11} of 0(2), (ii) B_{13} of O(4) and B_{13} of O(5), and (iii) B_{23} of O(4) and B_{23} of O(5). There are 48 correlation coefficients greater than 0.50.

The isotropic extinction parameter, r , where $F^2 = F_{\text{unc}}^2 (1 + \beta r F_{\text{unc}}^2)$ and F_{unc} is the structure factor uncorrected for extinction, was then refined together with the structural and scale parameters using the least-squares program RFINE written by L. W. Finger of the Carnegie Institution of Washington; these refinements included only the observed reflections. The resulting *R* values were $R_w=0.027$, $R=0.022$. The structure obtained had essentially the symmetry $P2_1/m$; subsequent anisotropic refinement in $P2_1/m$ gave $R_w = 0.036$, $R = 0.028$ without extinction refinement and $R_w = 0.028$, $R = 0.025$ in refinements in which r refined to 0.000100(4) cm. All unconstrained parameters were varied. Finally, three cycles of refinement including corrections for anomalous dispersion and extinction gave $R_w=0.028$, $R=0.023$; *r* became $0.000100(5)$ cm. The largest change in the other parameters was an increase of ~ 0.1 \AA^2 in all B_{ii} parameters of Ca. In the final cycle, the average shift/error was 0.02, and the standard deviation of an observation of unit weight, $\left[\sum_{w} (F_0 - F_c)^2 / (1652 - 56)\right]^{1/2}$, was 0.43.

The final \overline{R}_w values for the centric and acentric cases are near the limit of the experimental data. The weighting scheme is arbitrary, though reasonable. Further, there are large correlation coefficients in the acentric refinement. From the first two considerations, the authors feel that the ratio test [11] on $\Sigma w (F_0-F_c)^2$, the numerator of the R_w term, is not really applicable in this border-line case, even though it appears from this test that refinement in the acentric $\overline{P2}_1$ is to be preferred at a confidence level greater than 99.5 percent. Because refinement in the centric space-group $P2_1/m$ gives essentially the same result as refinement in P_{21} but has more restraints which remove the high correlation coefficients, the space-group of barytocalcite is assumed here to be $P2₁/m$. This is consistent with the symmetry of 2/m in the observed crystalline forms of the mineral [12]. With refinement in $P2_1/m$, the largest correlation coefficients were removed, and only six were greater than 0.50. The four largest were about 0.60 and were between the scale factor and the extinction parameter, and between the scale factor and B_{11} , B_{22} , and B_{33} of Ba.

Because Sr has been reported [13] in the alstonite phase of $BaCa(CO₃)₂$, a refinement of barytocalcite in which the cation positions were considered to be occupied by Sr^{2+} in solid solution was carried out using Finger's least-squares program. The occupan-

² Certain commercial equipment, instruments, or materials are identified in this paper in order to adequately specify the experimental procedure. In no case does such identifica-
tion imply recommendation or endorsement by the National Bureau of Standards, nor does it imply that the materials or equipment identified is necessarily the best available for the purpose.

TABLE 1. *Atomic parameters for barytocalcite* BaCa(CO₃)₂

Atoms				B_{11} *	B_{22}	B_{33}	B_{12}	B_{13}	B_{23}
Ba	0.14740(3)	0.25	0.28824(3)	0.883(6)	0.646(6)	0.652(6)	.	0.399(4)	.
Ca	.62320(8)	.25	.19855(9)	.64(2)	.50(2)	.58(1)	.	.21(1)	.
C(1)	.8972(5)	.75	.2483(5)	.83(8)	.65(8)	.55(7)	.	.17(8)	.
O(1)	.0057(4)	.75	.1393(4)	1.44(9)	1.31(9)	1.03(8)	.	.77(7)	.
O(2)	0.8457(3)	.9620(4)	.3089(3)	1.45(6)	0.85(6)	1.25(6)	0.50(5)	.45(6)	0.03(5)
C(2)	.6149(4)	.25	.7468(5)	0.68(8)	.74(8)	0.61(7)	.	.27(6)	.
O(3)	.6383(4)	.25	.5644(4)	2.4(1)	1.9(1)	.80(7)	.	.97(8)	.
O(4)	.6066(2)	.4604(4)	.8474(3)	1.29(6)	0.61(5)	1.00(6)	.16(4)	.52(4)	$-.04(4)$

Figures in parentheses are standard errors in the last significant figure quoted, and were computed in the final cycle of full-matrix leastsquares refinements.

*Thermal parameters have the form $\exp\left[-1/4(a^{*2}B_{11}h^2 + b^{*2}B_{22}k^2 + c^{*2}B_{33}l^2 + 2a^{*}b^{*}B_{12}hk + 2a^{*}c^{*}B_{13}hl + 2b^{*}c^{*}B_{23}kl\right]\right]$.

cies, 1.003(13) and 1.004(4), for Ba and Ca respectively, suggest that there *is* no solid solution of Sr ions in this sample of barytocalcite.

The atomic parameters from the final extinction refinement in space-group $P2_1/m$ are given in table 1. The observed structure factors are given in table 2.

3. Description of the Structure

The structure of barytocalcite (fig. 1) consists of $Ba \ldots CO_3$ chains and $Ca \ldots CO_3$ chains, both parallel to [001], in which the cations are coordinated to an edge of one neighboring $CO₃$ group in the chain, and to an apex of the other $CO₃$ group. The $C(2)O₃$ group is in the $CaCO₃$ chain with its plane parallel to (100). The $C(1)O_3$ group is in the BaCO₃ chain, with its plane nearly parallel to (101), and is pushed out of the line of the chain because of the large ionic radius of the Ba ion. The chains lie in layers parallel to (210) , a perfect cleavage in $BaCa(CO₃)₂$. The structure may also be considered to consist of layers of $CO₃$ groups coordinated to layers of cations, and is related in this way to the calcite [14] phase of $CaCO₃$, with (201) of barytocalcite corresponding to (001) of calcite.

3.1. The Barium Ion Environment

The Ba ion is coordinated (fig. 1, table 3) to 11 oxygen atoms with Ba... O distances less than 3.2 Å , i.e.,

b

in the normal range. These oxygens consist of 5 edges of $CO₃$ groups, $O(2, 2¹)$, $O(1¹, 2¹¹)$, $O(1¹¹, 2¹¹¹)$, $O(3, 4)$, $O(3¹, 4¹)$ and one apex, $O(1)$. The Ba ion is more extensively coordinated than it is in the witherite phase of $BaCO₃$, where it has a coordination of 9 oxygens. The structure of witherite resembles that of the aragonite phase of $CaCO₃$.

TABLE 3. Ba *environment in barytocalcite,* $BaCa(CO₃)₂$

Atoms	Distance, A				
Ba. O(1) Ba, O(4, 4 ¹) Ba, $O(2, 2^1)$ Ba. $O(2^{11}, 2^{111})$ Ba, $O(1^1, 1^{\text{II}})$ Ba, $O(3, 3^1)$ Ba, C(1) Ba, C(2)	2.729(3) 2.833(2) 2.847(2) 2.904(2) 2.914(1) 3.140(2) 3.152(3) 3.294(2)				

In all tables of interatomic distances and angles, the quantities in parentheses are standard errors in the last significant figure and

FIGURE 1. The crystal structure of barytocalcite, $BaCa(CO₃)₂$, and the environments of the Ba *and* Ca *ions.* The origin of the crystallographic coordinate system is marked by *. The labels refer to atoms in tables 3 and 4.

Table 2. Observed structure factors for barytocalcite, BaCa(CO3)2

reflections are marked by $*_\bullet$

3.2. **The Calcium Ion Environment**

The Ca ion is coordinated (fig. 1, table 4) to seven oxygen atoms, including one edge, $O(4¹¹, 4¹¹¹)$, of a $\overline{CO_3}$ group, with \overline{Ca} ... O distances in the normal range. The five apex oxygen atoms lie in a square pyramid. The center of the coordinated edge of the $CO₃$ group is near the remaining octahedral position. The coordination of Ca in barytocalcite is thus intermediate between the octahedral coordination of six $CO₃$ apexes with no shared edges in the calcite phase of CaCO₃ and the nine-fold coordination of three shared $CO₃$ edges and three apexes in the aragonite phase of $CaCO₃$.

The atomic labels refer to atoms in figure 1.

3.3. **The Carbonate Groups and Their Environments**

There are two crystallographically different $CO₃$ groups in the structure. One (table 5, fig. 2) is in the Ba . . . $CO₃$ chains and the other (table 5, fig. 2) is in the Ca... $CO₃$ chains. The former, the $C(1)$ $CO₃$ group, coordinates with all edges to Ba ions, and coordinates one apex, $O(1)$, to another Ba ion. The two remaining apexes $O(2, 2^l)$ are coordinated to Ca ions.

The $\overline{C(2)}$ $CO₃$ group coordinates the edge containing the $O(4, 4^1)$ atoms to Ca^{II} and the remaining two edges,

The atomic labels refer to atoms in figure 2.

 $O(3, 4)$ and $O(3, 4^t)$, to ions Ba^V and Ba^W , respectively. The average values of the $C - Q$ bond distance in the $C(1)$ and $C(2)$ $CO₃$ groups, 1.283 Å and 1.283 Å, respectively, compare well with the $C-O$ bond lengths ob-

FIGURE 2. *The* CO₃ environments in barytocalcite, BaCa(CO₃)₂. The labels refer to atoms in table 5.

served in the calcite $(1.283(2)$ Å [14]) and aragonite $(1.288(2)$ and $1.283(1)$ Å $[4]$) phases of CaCO₃.

The two $CO₃$ groups are nonplanar in barytocalcite. The displacements of C from the plane of the oxygen atoms are 0.025(5) \AA for C(1) and 0.022(4) \AA for C(2). Both displacements are toward the two central Ca ions Ca^{III} and Ca^{IV} in figure 2, and probably arise from polarization of the O atoms by these Ca ions. Similarly distorted CO₃ groups have been found in aragonite [15, 4] and $Ca₂Na₂(CO₃)₃$ [1]. (In calcite, the $CO₃$ group point symmetry is constrained to 32 by the choice of R3c as the space-group.)

The different $C - O$ bond lengths in the $CO₃$ groups (table 5) are consistent with the observed features in the structure. $O(1)$ is bonded to three Ba ions. $O(2)$ is bonded to two Ba ions and one Ca ion. Thus $O(2)$ experiences stronger interaction with its cation neighbors, which is compatible with the $C(1)-O(2)$ distance being longer than $C(1)-O(1)$. Similarly, $O(4)$ is coordinated to two Ca ions and one Ba ion, whereas $O(3)$ is coordinated to one Ca ion and two Ba ions. Thus, the $C(2)-O(4)$ bond distance is expected to be longer than the $C(2) - O(3)$ distance. Because the $O(4, 4')$ edge is coordinated to Ca whereas the $O(3, 4)$ and $O(3, 4')$ edges are coordinated to Ba, the $O(4)$, $C(2)$, $O(4')$ angle is expected to be less than 120°. Both these effects are realized.

Although $O(2)$ and $O(3)$ have similar environments, comparison of the lengths of the bonds $C(1)-O(2)$ and $C(2)-O(3)$ is not fruitful. Such a superficial comparison only applies when the oxygen atoms are competing in their bonding to the same central atom or when the other oxygens in the $CO₃$ groups also have similar environments.

4. **Discussion**

AIm [3] showed that the structure given by Gossner and Mussgnug [2] is incorrect. The general features of the structure given by Alm for barytocalcite are correct to within \sim 0.3 Å. The details given here are, however, far more precise. Gossner and Mussgnug and AIm gave the space-group of barytocalcite as $P2₁$ in their limited analyses of the structure. Our more extensive analysis shows, howe ver, that barytocalcite can be refined equally well, within the limits of the data, in the centrosymmetric space-group $P2_1/m$.

Barytocalcite is related to the calcite and aragonite phases of $CaCO₃$. There are pseudo-hexagonal layers of cations parallel to (101) in the barytocalcite structure. If the difference between Ca and Ba is ignored, a pseudo-cell may be defined with $a' \sim 8.7$ A (along $[10\overline{1}])$, $b' = 5.2$ $\rm \AA$ (along $[010]$), $c' \sim 9.2$ $\rm \AA$ (along $[101]$) and $\beta' \sim 95^{\circ}$. In this pseudo-cell, the cation layers repeat every third layer along c' as they do in calcite. The pseudo-cell of barytocalcite compares well with the orthohexagonal cell 8.641, 4.989 , 17.062 A of calcite. The orientations of the $CO₃$ groups in the two compounds calcite and barytocalcite differ by a rotation of \sim 30° (the C(2)O₃ group in barytocalcite further differs in that it makes an angle of $\sim 20^{\circ}$ with the (101) plane), and the cell repeat, 17.062 A, perpendicular to the

layers in calcite encompasses six cation layers whereas barytocalcite repeats every three cation layers. As regards the ... ABCABC ... sequence of cation layers, barytocalcite is like calcite. However, the rotation of the CO_3 groups by $\sim 30^\circ$ relative to the CO_3 positions in calcite relates barytocalcite to the aragonite phase of $CaCO₃$. Thus the detailed coordinations of the $CO₃$ groups are like those in aragonite, which also has $CO₃$ groups rotated by \sim 30° from the CO₃ positions in calcite, because all $CO₃$ edges in both compounds are shared in coordination to neighboring cations and all apexes are further coordinated to cations. The coordinations of the cations in barytocalcite are however different from the coordination of Ca in aragonite, partly because in the former there are two differently sized cations.

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