INTERFEROMETER MEASUREMENTS OF WAVE LENGTHS IN THE VACUUM ARC SPECTRA OF TITA. NIUM AND OTHER ELEMENTS

By C. C. Kiess

ABSTRACT

Wave-length determinations by means of the Fabry-Perot interferometer have been made for the vacuum arc spectrum of titanium. More than 300 lines have been measured between 6743 A in the red and 2941 A in the ultra-violet. For many of the lines the accuracy of measurement exceeds 1 part in $6,000,000$; for the majority it exceeds 1 part in 4,500,000. Using only the wave numbers of lines of wave lengths longer than 4700 A, and constant wave-number differences as determined in various parts of the spectrum, a set of terms has been derived, which have been used to calculate the wave lengths of the blue and violet lines. The comparison of calculated with observed wave lengths indicates that no difference in scale exists between the red and violet regions. In addition to titanium some wave lengths were measured for iron, copper, calcium, barium, and other elements.

CONTENTS

1. INTRODUCTION

In the summer of 1923 the Allegheny Observatory and the spectroscopy section of the Bureau of Standards entered upon a cooperative program for the determination of standard solar wave lengths by interference methods. The results of that work, wave lengths of more than 700 Fraunhofer lines included between 3592 and 7148 A, have now been published.¹ From the earlier results of the solar work it became apparent that a comparison of solar with laboratory wave lengths would have significance only if the latter were obtained from sources unaffected by conditions not present in the sun. It was,

1 Pub!. Allegheny Observatory, 6, p. 105; 1926; pp. 125 and 141; 1927.

therefore, decided to enlarge the seope of the program to include the determination of the vacuum arc wave lengths of the more prominent elements appearing in the solar spectrum.

In the present paper are given the results which have been obtained for the element titanium from 6743 A in the red to 2941 A in the ultra-violet. Some wave lengths of other elements were also measured during the course of the work, and these are presented at this time because of their significance for the solar problem.

II. METHOD OF OBSERVATION

Light rays from the vacuum arc and from the neon tube, which served as the source of standards, were delivered simultaneously to the Fabry-Perot interferometer. The vacuum arc was identical with that designed and described by Curtis.² The beam from the arc, perpendicular to the line joining the Ne tube and the slit of the spectrograph, was collimated with the beam from the Ne lamp by means of a thinly silvered diagonal mirror placed about 20 cm in front of the interferometer. The arrangement of the sources was in all respects similar to that used previously in the redetermination of secondary standards from the iron arc.³

The material used in the arc was powdered titanium carbide which was packed into a cored graphite rod that served as the lower and positive electrode. The upper, negative electrode was usually a copper rod, but for a few exposures, an upper graphite electrode was emplayed. The arc operated at 240 volts, d. c. and 8 amperes, and was struck when the bell surrounding it was partially exhausted. When the chamber was reduced to about 10 mm Hg pressure, as indicated by a vacuum gauge, the arc burned steadily for periods approximating an hour without renewal or readjustment of the electrodes. When exposures were in progress the electrodes were separated by 1 cm, and the image projected onto the diaphragm of the interferometer was enlarged about 2.5 times.

Three series of observations were made in all. The first two were obtained with glass interferometer plates with Ag films cathodically deposited. For these two series a glass achromat was used to project the light from the interferometer onto the slit of the spectrograph. Invar etalons of 5, 7.5, 12, 15, 20, and 25 mm thickness were used to separate the plates. In the first series of observations the small camera which takes a flat plate 6 by 20 em was used. The region covered was from 5500 to 7500 A. In the second and third series of observations the large camera was used. This takes a thin plate 6 by 40 cm, which can be bent over a template to fit the

^{&#}x27;J. Opt. Soc. Am. and Rev. Sci. Inst., 8, p. 697; 1924.

³ B. S. Sci. Papers, No. 478, 19, p. 263; 1924.

Kiess] Wave Lengths oj Titanium and Other Elements 77

focal curve of the grating. The second set of observations extended from 3650 to 6550 A, and the third from 2820 to 6550 A. The interferometer plates used for the third set were of crystalline quartz and were thinly sputtered with Pt films, and for projecting the rings it was necessary to use the quartz-fluorite achromat. Etalons of 3, 5,6,7.5,8,12,15, and 20 mm were used as separators for the quartz plates.

The spectrograph used for all the work was the one carrying the 7,500-lines per inch Anderson concave grating. It has been described elsewhere. 4 The first series of observations was obtained on Eastman 33 plates sensitized with pinacyanol. For the second and third series either experimental plates prepared in the bureau's emulsion laboratory or Schleussner ultrarapid plates were used. Half of each long plate was panchromatized by bathing in a mixture of pantochrome and pinacyanol for recording the green, yellow, and red rays.

For the first series of plates the method of reduction employed in previous work was followed.⁵ For the second and third series, however, a slight modification of that described by Robertson⁶ or by Childs 7 was adopted. A similar procedure was adopted for the reduction of some of the solar observations mentioned above.⁸

III. RESULTS FOR TITANIUM

1. DESCRIPTION OF BUREAU OF STANDARDS WAVE LENGTHS

Table 1 contains the wave lengths which have been measured in the vacuum arc spectrum of titanium in terms of the neon standards. The values of the Ne lines used for finding the interferometer thicknesses are those of Burns, Meggers, and Merrill.⁹ The justification for using these lines as standards instead of the primary standard, the red ray of cadmium, lies not only in the ease and economy with which they may be produced, but also in the fact that in the determination of secondary standards in spectra where exceedingly high orders of interference are not possible, they lead to results of the same precision as is obtained with the use of the Cd standard. This is demonstrated by the recent work of Babcock¹⁰ on the iron spectrum.

The wave lengths entered in the first column of Table 1 are the means of the individual results derived from all the plates. These values are for air at 15° C. and 760 mm Hg pressure. The results

⁴ B. S. Sci. Papers, Nos. 312, 441, and 499.

[•] n. s. Sci. Papers, Nos. 251, 274, 302, 327, 329, 441, 478, and 479.

⁶ J. Opt. Soc. Am. and Rcv. Sci. Inst., 9, p. 611; 1924.

⁷ J. Sci. Inst., 3, pp. 97 and 129; 1926.

⁸ Pub!. Allegheny Observatory, 6, p. 126; 1927.

⁹ B. S. Sci. Paper No. 329, 14, p. 765; 1918.

¹⁰ Astropbys. J., 66, p. 250; 1927.

78 *Bureau oj Standards Journal oj Research* [Vol. I

from the Ag films required correction for dispersion of phase change which was determined by the method of short and long etalons as described by Meggers.¹¹ The phase change curve is illustrated in Figure 1. No phase change correction was apparent for the results obtained with the Pt films in the region under investigation. However, when the means of the wave lengths obtained with the Pt films were compared with the means of all the observations, it was found that they were systematically higher by 0.001 A from 5150 to 4850 A by 0.002 A from 4850 to 4070 A; and by 0.003 A from 4070 to 3650 A. Accordingly, the wave lengths in Table 1 which were derived only from the Pt films have been corrected by the above amounts, the

FIC. *I.- Dispersion of phase change at reflection from silver films*

correction 0.003 A being extrapolated to apply to all the lines shorter than 3650 A. The justification for this procedure is given below in the discussion on the calculation of wave lengths from spectral terms.

In columns 2 and 3 of Table 1 are entered the number of observations from which the mean values of the wave lengths were derived, and letters indicating the probable errors of the determinations. The probable errors are expressed in parts per million ; thus the letter A denotes a p. e. of 1 part in 6,000,000; B, 1 part in 4,500,000; C, 1 part in 3,000,000; and D, probable errors greater than 1 in 3,000,000. The fourth column of the table contains the intensities and temperature classes of the lines as determined by King.¹² Lines emitted

12 Astrophys. J., 39, p. 139; 1914; 59, p. 155; 1924.

¹¹ B. S. Sci. Papers No. 251, 12, p. 190; 1915.

by the ionized Ti atom are designated in this column by the symbol Ti II. The remaining three columns of the table contain data the significance of which is discussed below.

λ Ι. Α.	Num- ber of obser- va- tions	Weight	Intensity and temperature class	ν (Vac)	Term combi- nation	$(O-C)$ λ
6743.124 6556.066 6554.226 6546.276 6366.354	6 17 16 12 $\boldsymbol{6}$	\mathbf{A} Λ Λ $_{\rm C}^{\rm A}$	10 $IIIA$ 25 III 30 III 20 III 8 III	14825.836 15248.847 15253.126 15271.650 15703.246	aD' - aD $b^3F_4 - d^3F'_4$ $\substack{b^3\mathrm{F}_3-d^3\mathrm{F'}_3\,\\b^3\mathrm{F}_2-d^3\mathrm{F'}_2}$ $b^3F_4-c^3D_3$	000 000 000 $+004$
6336.104 6312.240 6303.754 6261.101 6258.706	$\overline{2}$ 66 66 26 23	$\mathbf D$ \mathcal{C} \mathcal{C} \mathbf{A} Λ	8 III 10 III 10 III 35 II 50 II	15778.216 15837.866 15859.188 15967.225 15973.336	$b^3F_3-c^3D_2$ $b^3F_4 - b^3G_4$ $b^3F_3 - b^3G_3$ $b^3F_2 - b^3G_3$ $b^3F_4 - b^3G_5$	000 $+003$ $+010$ -001 000
6258.103 6126.217 6091.175 6085.228 6064.631	24 16 16 16 3	Α A B A B	40 II 20 II 20 III 20 II 9 _{II} A	15974.875 16318.780 16412.662 16428.700 16484.496	$b^3F_3 - b^3G_4$ $\overset{a^3\mathrm{P}_2-a^3\mathrm{S}_1}{b\mathrm{G}'-b\mathrm{G}}$ $a^3P_1 - a^3S_1$ $a^3P_0 - a^3S_1$	000
5999.668 5978.543 5965.828 5953.162 5941.755	1 20 24 22 $\overline{7}$	D \mathbf{A} Λ A $\mathbf B$	8 III 25 Π 30 II 30 II 12 IIA	16662.984 16721.863 16757.501 16793.155 16825.395	a^3H_4-bG $a^3G'_{3}-a^3H'_{4}\ a^3G'_{4}-a^3H'_{5}\ a^3G'_{5}-a^3H'_{6}\ a^3P_{1}-b^3D_{1}$	000 000 000 $+005$
5937.806 5922.112 5918.548 5903.317 5899.295	1 $\overline{7}$ $\overline{2}$ \mathbf{I} 22	$\mathbf D$ \mathcal{C} D D Λ	6 _{II} A 18 II 10 II 5 _{IIIA} 25 II	16836.584 16881.201 16891.367 16934.947 16946.493	$a^3P_2 - b^3D_2$ $a^3P_0 - b^3D_1$ $a^3P_2-a^3P'_2$ $a^3P_2-a^3P'_1$ $a^3P_1-b^3D_2$	-002 $+004$ 000
5866.453 5804.265 5785.979 5774.037 5766.330	31 8 $\overline{3}$ 66 $\sqrt{3}$	Λ \overline{C} B \mathcal{C} D	35 Π $5n$ IV $5n$ IV $5n$ IV 4n IV	17041.364 17223.947 17278.379 17314.116 17337.257	$a^3P_2 - b^3D_3$ $\frac{b^5G_6-c^5H_7}{b^5G_5-c^5H_6} \ \frac{b^5G_4-c^5H_5}{b^5G_3-c^5H_4}$	$+004$
5739.464 5715.123 5689.465 5675.413 5662.154	$\overline{5}$ 3 $\overline{7}$ 10 10	$\bf B$ D \bf{B} \bf{B} \bf{A}	9 _{III} 9 III 10 III 9 _{IIIA} 12 III	17418.410 17492.594 17571.481 17614.987 17656.237	$a^3H_5 - b^3H'_{5}$ $a^3H_6-b^3H'_6$ $a^5D_2-b^5F_3$ $a^5D_3-b^5F_4$ $a^5D_4 - b^5F_5$	000 000
5648.570 5644.137 5565.476 5512.529 5503.897	$\overline{4}$ 13 11 17 8	$\mathbf D$ \mathbf{A} \mathbf{A} \rm{A} \bf{B}	5 _{IV} 18 III 9 _{III} 25 II 8 III	17698.695 17712.595 17962.941 18135.471 18163.912	$a^3D_3 - c^3F_4$ $bG' - cG$ $a^3H_4 - cG$ $\overset{b^3\mathrm{F}_4-e^3\mathrm{D}_3}{a\mathrm{H}-d\mathrm{G}}$	$+003$ $+001$
5490.151 5488.210 5481.426 5477.695 5429.139	10 $\boldsymbol{2}$ 3 11 $\overline{5}$	в D D $\bf B$ D	12 II 5 _{III} 6 III 8III 6 III	18209.391 18215.829 18238.374 18250.796 18414.022	$b^3F_4 - b^5D_3$ $a^3F'_{2}-c^3F_{2}\ a^3F'_{2}-c^3F_{3}\ a^3F'_{4}-c^3F_{4}\ c^3P_{2}-d^3P'_{2}$	000 000 000
5409.609 5397.093 5389.996 5369.635 5298.429	8 $\overline{5}$ $\overline{2}$ $\overline{\mathbf{3}}$ $\overline{2}$	\mathcal{C} D D D D	$6\,\mathrm{II}$ 4 III 3 III 4 III 4 III	18480.500 18523.359 18547.745 18868.284	$a^3G'_{5}-e^3F'_{4}$ $a^3\bar{\rm G'}_4-e^3\bar{\rm F'}_3\\ a^3\bar{\rm G'}_3-e^3\bar{\rm F'}_2$ bD' -c P'	-001 000 000
5297.236 5295.781 5283.441 5265.967 5224.928	3 $\bar{2}$ $\overline{4}$ $\boldsymbol{6}$ 3	D D D $\mathbf C$ D	6 III 4 III 8 III 10 III 8 III	18872.532 18877.720 18921.809 18984.597 19133.706	$a^3G'_{3}-f^3F'_{2}$ $\begin{array}{l} a^3\mathrm{P}_2\!-\!c^3\mathrm{D}_3\\ a^3\mathrm{G'}_4\!-\!f)\mathrm{F'}_3\\ a^3\mathrm{G'}_7\!-\!f^3\mathrm{F'}_4\\ a^5\mathrm{F'}_7\!-\!b^5\mathrm{F}_4\\ \end{array}$	000 $+002$ 000 $+002$

TABLE 1.-Vacuum arc wave lengths of titanium

 $2284^{\circ}-28$ -6

 $Kiesz$

 \triangle

Bureau of Standards Journal of Research

TABLE 1.-Vacuum arc wave lengths of titanium-Continued

TABLE 1.-Vacuum arc wave lengths of titanium-Continued

82

Wave Lengths of Titanium and Other Elements

2. COMPARISON WITH OTHER OBSERVATIONS

Two other observers have measured wave lengths in the vacuum arc spectrum of titanium. In 1922 Brown 13 published a list of more than 100 wave lengths between 4253 and 6261 A determined by interference methods in terms of the primary standard-the red ray of cadmium. This was followed two years later by a more extensive list by Crew.¹⁴ who observed the region from 3653 to 6366 \AA with a plane grating giving high dispersion. There is most excellent agreement between the Bureau of Standards wave lengths and those of Brown in the interval from 4262 to 5200 A. Most of the differences, Bureau of Standards *minus* Brown, are less than 0.003 A and exhibit no systematic shift between the two sets of results, the mean of the differences being $+0.0001$ A. Between 5200 and 5800 A Brown's list contains 13 Ti lines, of which 11 may be compared with the Bureau of Standards determinations. Of these, there are two positive differences, three zeros, and six negative differences, the mean value of Bureau of Standards *minus* Brown being - 0.001 A. From 5800 to the end of Brown's list, his wave lengths are systematically longer than the Bureau of Standards values, the difference increasing from -0.001 A at 5800 A to -0.004 A at 5260 A.

The comparison of the Bureau of Standards wave lengths with Crew's is'limited to the region 3653 to 4263 A, his wave lengths longer than 4263 A being based on those of Brown described above. The differences, Bureau of Standards *minus* Crew, change linearly from -0.005 A at 3653 to +0.002 A at 3800 A, being zero at 3750 A. From 3800 to 4000 A the difference is practically constant, amounting to $+0.002$ A. At 4000 A there is an abrupt increase in the difference to $+0.010$ A from which it decreases linearly to -0.010 A at 4263 A, being zero in the vicinity of 4130 A.

3. COMPUTATION OF WAVE LENGTHS FROM SPECTRAL TERMS

Classification of the lines of a spectrum as the difference of two spectral· terms permits a calculation of the wave lengths of the lines if the term values are known. In recent years rapid progress has been made in the extension of our knowledge of the structure of spectra not only of neutral atoms which emit arc spectra, but also of ionized atoms which emit the various stages or orders of spark spectra. Such analyses of the spectrum of titanium have been made by Kiess and Kiess¹⁵ and by Russell.¹⁶ From the work of these

¹³ Astrophys. J., 56, p. 53; 1922.

^HAstrophys. J., 60, p. 108; 1924.

l' J. Opt. Soc. Am. and Rev. Sri. lnst., 8, p. 607; 1924.

¹⁸ Astrophys. J. 66, pp. 283 and 347; 1927.

Kiess] Wave Lengths oj Titanium and Other Elements 85

investigators have been taken the term combinations or series classifications of the lines given in column 6 of Table 1. The numerical values of the term combinations are the wave numbers in vacuum of the lines as entered in column 5.

If the terms involved in the production of the spectrum can be determined solely from lines measured in the yellow and red—that is, in the vicinity of the neon standards—then it is possible to calculate from them the wave lengths of lines in the blue and violet and thereby check the accuracy of observations remote from the standards. Such an ideal procedure, however, is not entirely possible in the case of titanium owing to the low intensities and consequent paucity of the longer Ti lines in the vacuum arc. An alternative procedure for testing the scale of a wave-length interval by means of cyclical term combinations, such as carried out by Meggers 17 for the iron spectrum, was likewise not feasible for Ti because of the small number of cycles which could be formed from the Wave lengths of Table 1. It was, therefore, decided to set up a system of terms based not only on the longer wave lengths of the table, but also on the relative term separations as given by observations throughout the measured wave-length interval. The degree of the constancy of these term separations is exhibited in Table 2, wherein are collected various differences used in calculating the relative values of the low terms.

	$a^3F_4 - a^3F_3$ $a^3F_3 - a^3F_2$	$a^3F_4 - b^3F_4$	$a^3\mathrm{F}_3 - b^3\mathrm{F}_2$	$a^3F_2 - b^3F_2$		$a^3F_4 - a^3P_2$ $a^3F_3 - a^3P_1$	$a^3\text{F}_2-a^3\text{P}_0$
216, 722 .726 .755 .752 .744 .742 .741 .749 .735	170.122 .129 .129 .127 .106 .133 .150 .133 .151 .140	11389.934 .960 .955 .952 .940 .947 .940	11469.688 .672 .686 .701 .693 .688	11531.789 .786 .800	8215.486 .488 .467	8322.307 .310	8436.646 .597
216, 741	170.132	11389.947	11469.688	11531, 792	8215, 480	8322, 308	8436.622

TABLE *2.-Constancy of term differences throughout the spectrum*

The mean values of the term differences of Table 2 were used in deriving the values of the terms a^3F , b^3F , and a^3P of Table 3. From these the remainder of Table 3 was calculated by the joint use of wave numbers shorter than 21,300.000 from Table 1. and relative term separations similar to those of Table 2. Although many of the well-observed lines of Table 1. belong to the singlet and quintet systems of Ti I, yet it was not possible to derive good term values for these systems by adhering to the limitations set for the derivation of the triplet system terms. The wave numbers calculated from

¹⁷ Astrophys. J., 60, p. 60 1924.

these terms were converted into wave lengths which were compared with the observed values of Table 1. The results of the comparison are shown in the last column of Table 1, where the residuals $O-C$ are entered. The algebraic sum of the differences $O-C$ for the interval 4700-2941 A is practically zero, although negative residuals predominate in the region 4700-3700 A, and positive residuals in the region 3700-2941 A. However, since the wave lengths would require, in each of these regions, a mean correction of less than 0.001 A to reduce the sums of the residuals to zero, the representation of the wave lengths by means of the terms of Table 3 is regarded as satisfactory and is interpreted as indicating that the blue and violet lines have been measured to the same scale as those longer than 4700 A. For lines longer than 4700 A the majority of the residuals are necessarily zero, since the lines were used directly in the computation of the terms. With one exception the residuals greater than 0.002 A in this region refer to lines observed only a few times.

IV. RESULTS FOR OTHER ELEMENTS

In Tables 4, 5, and 6 which follow are given the vacuum arc wave lengths of a few lines of elements which appeared as impurities in the titanium or were especially observed to supply additional data for the solar work. The most abundant impurity in the titanium was iron; in lesser amounts were calcium, aluminum, chromium, vana dium, and sodium. The elements especially observed for wave lengths in the yellow and red were calcium, barium, manganese, and nickel, the observations being made at the same time as the first series of titanium. Owing to the fact that a copper rod was used

nearly always for the negative electrode, 26 lines of this element were also measured on the spectrograms of all three series and are given below.

$\lambda I.A$	Num- ber of obser- vations	Weight	Intensity, tem- perature, and pressure classes	Bureau of Stand- ards minus Bab- cock	$\lambda I. A$	Num- ber of obser- vations	Weight	Intensity, tem- perature, and pressure classes	Bureau of Stand- ards minus Bab- cock
5371.488 5328, 044 5269, 539 4415, 123 4383.545	5 10 13 6 25	D Λ Λ Λ \mathbf{A}	IB 50 α IB 50 \boldsymbol{a} IB 60 \boldsymbol{a} $_{\rm II}$ \boldsymbol{b} 20 \mathbf{I} 45r \boldsymbol{b}	-005 $+002$ -002 -002 -003	3799.554 3795.005 3767.193 3763.791 3758.237 3749.488	$\overline{4}$ 6 14 14 $\overline{7}$ 8	\mathcal{C} \mathcal{C} Λ Λ \mathcal{C} \overline{C}	II 50 $\rm II$ 60 \boldsymbol{b} 80r $\scriptstyle\rm II$ \boldsymbol{b} \mathcal{I} 100r \boldsymbol{b} 150R II \boldsymbol{b} II 200R \boldsymbol{b}	$+005$ $+001$ 000 000 $+003$ $+001$
4271, 762 4260, 476 4250.789 4235, 937 4202.030 4143.869	22 12 9 6 10 $\overline{7}$	\mathbf{A} B \mathbf{A} D \mathbf{A} $\bf B$	\prod \boldsymbol{b} 35 III 35 \overline{d} II 25 \boldsymbol{b} II 25 \overline{d} II 30 Ъ III \boldsymbol{b} 15	-002 -004 -001 -005 -002 -002	3748.264 3745.560 3737, 132 3734.865 3733, 320 3727, 621	8 14 13 17 11 10	B Λ \bf{B} B B B	IA 60R \overline{a} 100R Ι 150R I α \mathbf{H} 300R IA 40r \overline{a} 50r II \boldsymbol{b}	000 -002 $+002$ 000
4132.060 4071.740 4045.813 4005.244 3930.294	11 22 27 $\overline{4}$ $\overline{2}$	$\mathbf B$ \mathbf{A} \mathbf{A} \overline{C} \mathcal{C}	II 25 \boldsymbol{b} II \boldsymbol{b} 40 \mathbf{H} 60r \boldsymbol{b} \mathbf{I} 25 \boldsymbol{b} IB 25R α	-001 -001 -001 000 -004	3719, 934 3709.256 3705, 566 3687.454 3679.915	13 8 13 12 14	B \mathcal{C} Λ $\, {\bf B}$ Λ	I 250R α 75r \mathcal{I} \boldsymbol{b} 100r Ι α I 40r \boldsymbol{b} IA 40r \overline{a}	-003 $+008$ -001 -005 000
3927, 919 3922.914 3920.261 3899.712 3886.281	14 $\overline{5}$ $\overline{5}$ 3 24	Λ \mathcal{C} D D B	IB 30R α 25R IB \boldsymbol{a} I B 20r \boldsymbol{a} IB 30R α IB 40R \overline{a}	-002 $+001$ $+002$ $+004$ -003	3647.844 3631.465 3618, 769 3608.861	14 14 14 8	Λ Λ Λ B	\boldsymbol{b} 100R Ι 125R r \boldsymbol{b} Ι \boldsymbol{b} 125R T 100r	$+001$ 000 000 -001
3859, 905 3856, 377 3834, 221 3827.821	8 $\overline{2}$ 12 $\overline{2}$	$\rm C$ \overline{C} Λ \mathcal{C}	300R T. IA 50r $_{\rm II}$ \boldsymbol{b} 100r II \boldsymbol{b} 75r	$+004$ -003 -003	3581, 194 3570.099 3565, 380 3558.517	12 11 12 11	Λ B $\mathbf B$ B	I 250R I 100R II 60r II 30	-002 -001
3825, 881 3824.447 3820, 428 3815, 844 3806.711	$\overline{4}$ 3 20 21 $\overline{2}$	B $\rm C$ Λ \mathbf{A} D	II 200R \boldsymbol{b} IA 50r Π 250R II \boldsymbol{b} 100r III 10	-003 $+002$ 000 $+002$ $+013$	3497.844 3465, 862 3440.990 3020.635	$\overline{4}$ 11 12 6	\mathcal{C} B \mathcal{C} D	I 40 I 60r I 75R I 200R	$+001$ 000

TABLE 4. - Vacuum arc wave lengths of iron

TABLE 5.-Vacuum arc wave lengths of copper

λ I. A.	Num- ber of obser- vations	Weight	Inten- sities	Bureau of Standards minus Wolf- sohn		λ I. A.	Num- ber of obser-	Weight	Inten- sities	Bureau of Standards minus Wolf- sohn	
				Vac- uum	Air		vations			Vac- uum	Air
5782, 132* 5700.239* 5292, 519 5220, 070*	31 23 Ω 13	$\begin{smallmatrix} \mathbf{A} \ \mathbf{A} \ \mathbf{C} \end{smallmatrix}$	8r 8r 6 $6\overline{6}$	-004 -040	-008	3530.382 3337.845 3279.815 3273.956*	9 10 10 7	\bf{B} $_{\rm B}^{\rm A}$ \mathbf{A}	$\overline{7}$ 8 $\overline{5}$ 10R	-017 -018	-005 -005
5218.202	27	\tilde{A}	10	-031	000	3247.540*	$\,$ 8 $\,$	$\mathbf B$	10R	-016	-002
5153.237* 5105.542 4704.593 4651.124	27 23 $6\overline{6}$ 14	\mathbf{A} $\overset{\text{A}}{\mathbf{D}}\overset{\text{B}}{\mathbf{B}}$	$\frac{8}{7}$ 8	-035 -017 -025	$+004$ -009	3208, 230 3194.096 3063.411	$\frac{8}{8}$ 10	$_{\rm B}^{\rm B}$ Λ	6 8	-020 -018 -015	-010 -008
4530.786*	11		6	-009		3036.101 3010, 838	10 10	B Λ	8	-013 -013	-006 -007
4509.374 4480.360* 4062.639 4022.627	10 6 8 11	$_{\rm C}^{\rm B}$ \mathbf{A}	6 $\overline{7}$ 10 10	-015 -004	-013	2961, 164 2824.369	$\overline{4}$ $\overline{4}$	D B	Ω 10	-015 -013	-009

Kiess]

TABLE 6. - Vacuum arc wave lengths of Na, Al, Ca, V, Cr, Mn, Ni, and Ba

1. IRON

The iron lines whose wave lengths are given in the first column of Table 4 all originate in the lowest or the low metastable states of the iron atom. They are, accordingly, easily excited and appear with great intensity. In arcs in air most of them are reversed. The character of the lines in arcs in air and their behavior in the vacuum furnace are described in columns 4 and 5, the data for which are taken from King.¹⁸ In the vacuum arc, however, these lines become narrow and give sharp interference fringes with high orders, a phenomenon pointed out long ago by Fabry and Buisson.¹⁹ With two exceptions these lines belong to pressure classes a and b which means that they experience the least displacement with increasing pressure. We should, therefore, expect to find very little difference between their wave lengths in vacuum and in air, the amount of the displacement increasing with wave length. Such, indeed, is the case. Quite

¹⁸ Astrophys. J., 37, p. 239; 1913; 56, p. 318; 1922.

¹⁹ J. de Physique (IV), 9, p. 947; 1910.

Kiess) Wave Lengths oj Titanium and Other Elements 89

recently Babcock 20 has published interferometer measurements of iron wave lengths emitted by arcs in air. The comparison of the Bureau of Standards values with his is shown in the last column of Table 4. In the ultra-violet—that is, the region of wave lengths shorter than 3922 A-the residuals, Bureau of Standards *minus* Babcock, are about equally distributed among positive and negative values, being in the mean $+0.0007$ A. But for all lines longer than 3922 A the residuals, Bureau of Standards *minus* Babcock, are negative, with one exception, the mean being -0.002 A.

2. COPPER

The copper lines which were measured are listed in Table 5. Of these, the pair at 5700 and 5782 A in the yellow, and the *raies ultimes,* 3247 and 3274 A, always appeared reversed. The intensities assigned to the lines are taken from Kayser's *Tabelle der Hauptlinien.* Four pairs of lines in this table, marked with an asterisk (*), involve the term ${}^{2}P_{1,2}$ as may be seen by reference to Shenstone's 21 classification of the Cu arc spectrum. They may, therefore, be used to determine the separation of the components of this term, and thereby check the relative accuracy of the measurements. The four values of ${}^{2}P_{2}-{}^{2}P_{1}$ are: 248.392, 248.377, 248.335, and 248.364. The low value of the third is accounted for by the fact that the wave length 4480.360 A which enters into its determination is affected by the Ti line at 4480.60 . A correction of -0.009 A applied to the tabulated wave length would give a value of ${}^{2}P_{2} - {}^{2}P_{1}$ equal to the mean of the other three determinations.

The vacuum arc spectrum of Cu has been measured recently by Wolfsohn²² who photographed it in juxtaposition with the spectrum of the arc in air, using the high dispersion afforded by the grating spectrograph at Bonn. His vacuum values are systematically larger than his air values which he interprets as a pressure shift toward the violet for lines emitted by the arc in air. A comparison of the Bureau of Standards wave lengths with Wolfsohn's is given in the last two columns of Table 5, which shows that his conclusions concerning the pressure shift toward the violet are not verified. In fact, assuming the correctness of his arc-in-air measurements the residuals, Bureau of Standards *minus* W olfsohn, indicate for copper the same type of pressure shift as has been found for all other spectra which have been investigated.

!l Phys. Rev., 28, p. 449; 1926.

¹⁰ Astrophys. J. 66, p. 256: 1927.

²² Annalen der Physik (IV), 80, p. 415; 1926.

3. Na, AI, Ca, V, Cr, Mn, Ni, Ba

In Table 6 are listed some wave lengths of Na, Al, Ca, V, Cr, Mn, Ni, and Ba. Some of these elements, as stated above, occurred as impurities in the electrodes. Ca, Mn, Ni, and Ba were especially investigated to furnish additional standards in the red for comparison with the solar wave lengths. The intensities and temperature classes given for each line are those assigned by King, except for Na, and Al, for which the estimates given by Kayser²³ are quoted. The impurity lines are in all cases either the *raies ultimes* or persistent lines of the corresponding elements, and all appear among the Fraunhofer lines of the sun's spectrum.

v. ACKNOWLEDGMENTS

The work described in the foregoing pages has been in progress at the Bureau of Standards for several years. Various persons have cooperated with me in carrying it to completion, and it is a pleasure to acknowledge here my appreciation of their assistance. D. D. Laun, formerly of the bureau staff, did a large share of the observing and computations required for the work with the silveron-glass interferometers. Dr. K. Burns, of the Allegheny Observatory, shared in the observing with the platinum-on-quartz interferometers; and B. W. Scribner, jr., of the bureau staff, has assisted in the reductions of the last series of observations. Finally, to Prof. H. N. Russell, of Princeton University, I owe my thanks for placing at my disposal his unpublished results on the classification of the titanium arc and spark spectra.

 $\frac{d}{dt}$

WASHINGTON, December 19, 1927.

²³ Kayser, Tabelle der Hauptlinien. Julius Springer, Berlin, 1926.