# INTERFEROMETER MEASUREMENTS OF WAVE LENGTHS IN THE VACUUM ARC SPECTRA OF TITA-NIUM AND OTHER ELEMENTS

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#### ABSTRACT

Wave-length determinations by means of the Fabry-Perot interferometer have been made for the vacuum are spectrum of titanium. More than 300 lines have been measured between 6743 A in the red and 2941 A in the ultra-violet. For many of the lines the accuracy of measurement exceeds 1 part in 6,000,000; for the majority it exceeds 1 part in 4,500,000. Using only the wave numbers of lines of wave lengths longer than 4700 A, and constant wave-number differences as determined in various parts of the spectrum, a set of terms has been derived, which have been used to calculate the wave lengths of the blue and violet lines. The comparison of calculated with observed wave lengths indicates that no difference in scale exists between the red and violet regions. In addition to titanium some wave lengths were measured for iron, copper, calcium, barium, and other elements.

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### I. INTRODUCTION

In the summer of 1923 the Allegheny Observatory and the spectroscopy section of the Bureau of Standards entered upon a cooperative program for the determination of standard solar wave lengths by interference methods. The results of that work, wave lengths of more than 700 Fraunhofer lines included between 3592 and 7148 A, have now been published.<sup>1</sup> From the earlier results of the solar work it became apparent that a comparison of solar with laboratory wave lengths would have significance only if the latter were obtained from sources unaffected by conditions not present in the sun. It was,

<sup>1</sup> Publ. Allegheny Observatory, 6, p. 105; 1926; pp. 125 and 141; 1927.

therefore, decided to enlarge the scope of the program to include the determination of the vacuum arc wave lengths of the more prominent elements appearing in the solar spectrum.

In the present paper are given the results which have been obtained for the element titanium from 6743 A in the red to 2941 A in the ultra-violet. Some wave lengths of other elements were also measured during the course of the work, and these are presented at this time because of their significance for the solar problem.

# **II. METHOD OF OBSERVATION**

Light rays from the vacuum arc and from the neon tube, which served as the source of standards, were delivered simultaneously to the Fabry-Perot interferometer. The vacuum arc was identical with that designed and described by Curtis.<sup>2</sup> The beam from the arc, perpendicular to the line joining the Ne tube and the slit of the spectrograph, was collimated with the beam from the Ne lamp by means of a thinly silvered diagonal mirror placed about 20 cm in front of the interferometer. The arrangement of the sources was in all respects similar to that used previously in the redetermination of secondary standards from the iron arc.<sup>3</sup>

The material used in the arc was powdered titanium carbide which was packed into a cored graphite rod that served as the lower and positive electrode. The upper, negative electrode was usually a copper rod, but for a few exposures, an upper graphite electrode was employed. The arc operated at 240 volts, d. c. and 8 amperes, and was struck when the bell surrounding it was partially exhausted. When the chamber was reduced to about 10 mm Hg pressure, as indicated by a vacuum gauge, the arc burned steadily for periods approximating an hour without renewal or readjustment of the electrodes. When exposures were in progress the electrodes were separated by 1 cm, and the image projected onto the diaphragm of the interferometer was enlarged about 2.5 times.

Three series of observations were made in all. The first two were obtained with glass interferometer plates with Ag films cathodically deposited. For these two series a glass achromat was used to project the light from the interferometer onto the slit of the spectrograph. Invar etalons of 5, 7.5, 12, 15, 20, and 25 mm thickness were used to separate the plates. In the first series of observations the small camera which takes a flat plate 6 by 20 cm was used. The region covered was from 5500 to 7500 A. In the second and third series of observations the large camera was used. This takes a thin plate 6 by 40 cm, which can be bent over a template to fit the

<sup>&</sup>lt;sup>2</sup> J. Opt. Soc. Am. and Rev. Sci. Inst., 8, p. 697; 1924.

<sup>&</sup>lt;sup>3</sup> B. S. Sci. Papers, No. 478, **19**, p. 263; 1924.

focal curve of the grating. The second set of observations extended from 3650 to 6550 A, and the third from 2820 to 6550 A. The interferometer plates used for the third set were of crystalline quartz and were thinly sputtered with Pt films, and for projecting the rings it was necessary to use the quartz-fluorite achromat. Etalons of 3, 5, 6, 7.5, 8, 12, 15, and 20 mm were used as separators for the quartz plates.

The spectrograph used for all the work was the one carrying the 7,500-lines per inch Anderson concave grating. It has been described elsewhere.<sup>4</sup> The first series of observations was obtained on Eastman 33 plates sensitized with pinacyanol. For the second and third series either experimental plates prepared in the bureau's emulsion laboratory or Schleussner ultrarapid plates were used. Half of each long plate was panchromatized by bathing in a mixture of pantochrome and pinacyanol for recording the green, yellow, and red rays.

For the first series of plates the method of reduction employed in previous work was followed.<sup>5</sup> For the second and third series, however, a slight modification of that described by Robertson<sup>6</sup> or by Childs<sup>7</sup> was adopted. A similar procedure was adopted for the reduction of some of the solar observations mentioned above.<sup>8</sup>

# III. RESULTS FOR TITANIUM

### 1. DESCRIPTION OF BUREAU OF STANDARDS WAVE LENGTHS

Table 1 contains the wave lengths which have been measured in the vacuum arc spectrum of titanium in terms of the neon standards. The values of the Ne lines used for finding the interferometer thicknesses are those of Burns, Meggers, and Merrill.<sup>9</sup> The justification for using these lines as standards instead of the primary standard, the red ray of cadmium, lies not only in the ease and economy with which they may be produced, but also in the fact that in the determination of secondary standards in spectra where exceedingly high orders of interference are not possible, they lead to results of the same precision as is obtained with the use of the Cd standard. This is demonstrated by the recent work of Babcock <sup>10</sup> on the iron spectrum.

The wave lengths entered in the first column of Table 1 are the means of the individual results derived from all the plates. These values are for air at  $15^{\circ}$  C. and 760 mm Hg pressure. The results

<sup>4</sup> B. S. Sci. Papers, Nos. 312, 441, and 499.

<sup>&</sup>lt;sup>5</sup> B. S. Sci. Papers, Nos. 251, 274, 302, 327, 329, 441, 478, and 479.

<sup>&</sup>lt;sup>6</sup> J. Opt. Soc. Am. and Rev. Sci. Inst., 9, p. 611; 1924.

<sup>7</sup> J. Sci. Inst., 3, pp. 97 and 129; 1926.

<sup>&</sup>lt;sup>8</sup> Publ. Allegheny Observatory, 6, p. 126; 1927.

<sup>&</sup>lt;sup>9</sup> B. S. Sci. Paper No. 329, **14**, p. 765; 1918.

<sup>&</sup>lt;sup>10</sup> Astrophys. J., **66**, p. 256; 1927.

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from the Ag films required correction for dispersion of phase change which was determined by the method of short and long etalons as described by Meggers.<sup>11</sup> The phase change curve is illustrated in Figure 1. No phase change correction was apparent for the results obtained with the Pt films in the region under investigation. However, when the means of the wave lengths obtained with the Pt films were compared with the means of all the observations, it was found that they were systematically higher by 0.001 A from 5150 to 4850 A by 0.002 A from 4850 to 4070 A; and by 0.003 A from 4070 to 3650 A. Accordingly, the wave lengths in Table 1 which were derived only from the Pt films have been corrected by the above amounts, the



FIG. 1.—Dispersion of phase change at reflection from silver films

correction 0.003 A being extrapolated to apply to all the lines shorter than 3650 A. The justification for this procedure is given below in the discussion on the calculation of wave lengths from spectral terms.

In columns 2 and 3 of Table 1 are entered the number of observations from which the mean values of the wave lengths were derived, and letters indicating the probable errors of the determinations. The probable errors are expressed in parts per million; thus the letter A denotes a p. e. of 1 part in 6,000,000; B, 1 part in 4,500,000; C, 1 part in 3,000,000; and D, probable errors greater than 1 in 3,000,000. The fourth column of the table contains the intensities and temperature classes of the lines as determined by King.<sup>12</sup> Lines emitted

12 Astrophys. J., 39, p. 139; 1914; 59, p. 155; 1924.

<sup>&</sup>lt;sup>11</sup> B. S. Sci. Papers No. 251, **12**, p. 199; 1915.

by the ionized Ti atom are designated in this column by the symbol Ti II. The remaining three columns of the table contain data the significance of which is discussed below.

λΙ.Α.	Num- ber of obser- va- tions	Weight	Intensity and temperature class	ν (Vac)	Term combi- nation	(0-C) λ
$\begin{array}{c} 6743.\ 124\\ 6556.\ 066\\ 6554.\ 226\\ 6546.\ 276\\ 6366.\ 354\end{array}$		A A A C	$\begin{array}{c} 10 \ \mathrm{III}\mathcal{A} \\ 25 \ \mathrm{III} \\ 30 \ \mathrm{III} \\ 20 \ \mathrm{III} \\ 8 \ \mathrm{III} \end{array}$	$\begin{array}{c} 14825.\ 836\\ 15248.\ 847\\ 15253.\ 126\\ 15271.\ 650\\ 15703.\ 246 \end{array}$	$a{ m D}'-a{ m D}\ b^3{ m F}_4-d^3{ m F}'_4\ b^3{ m F}_3-d^3{ m F}'_3\ b^3{ m F}_2-d^3{ m F}'_2\ b^3{ m F}_4-c^3{ m D}_3$	$000 \\ 000 \\ 000 \\ +004$
$\begin{array}{c} 6336.\ 104\\ 6312.\ 240\\ 6303.\ 754\\ 6261.\ 101\\ 6258.\ 706\end{array}$	$2 \\ 6 \\ 6 \\ 26 \\ 23$	D C C A A	8 III 10 III 10 III 35 II 50 II	$\begin{array}{c} 15778,216\\ 15837,866\\ 15859,188\\ 15967,225\\ 15973,336 \end{array}$	$b^3 F_3 - c^3 D_2$ $b^3 F_4 - b^3 G_4$ $b^3 F_3 - b^3 G_3$ $b^3 F_2 - b^3 G_3$ $b^3 F_4 - b^3 G_5$	$\begin{array}{c} 000 \\ +003 \\ +010 \\ -001 \\ 000 \end{array}$
$\begin{array}{c} 6258.\ 103\\ 6126.\ 217\\ 6091.\ 175\\ 6085.\ 228\\ 6064.\ 631 \end{array}$	$24 \\ 16 \\ 16 \\ 16 \\ 3$	A B A B	40 II 20 II 20 III 20 III 9 II A	$\begin{array}{c} 15974.\ 875\\ 16318.\ 780\\ 16412.\ 662\\ 16428.\ 700\\ 16484.\ 496 \end{array}$	$b_{3}F_{3}-b_{3}G_{4}$ $a_{3}P_{2}-a_{3}S_{1}$ bG'-bG $a_{3}P_{1}-a_{3}S_{1}$ $a_{3}P_{0}-a_{3}S_{1}$	000
5999. 668 5978. 543 5965. 828 5953. 162 5941. 755	$     \begin{array}{c}       1 \\       20 \\       24 \\       22 \\       7     \end{array} $	D A A B	8 III 25 II 30 II 30 II 12 II A	$\begin{array}{c} 16662,984\\ 16721,863\\ 16757,501\\ 16793,155\\ 16825,395 \end{array}$	$a^{3}H_{4}-bG$ $a^{3}G'_{3}-a^{3}H'_{4}$ $a^{3}G'_{4}-a^{3}H'_{5}$ $a^{3}G'_{5}-a^{3}H'_{6}$ $a^{3}P_{1}-b^{3}D_{1}$	$000 \\ 000 \\ 000 \\ +005$
$\begin{array}{c} 5937,806\\ 5922,112\\ 5918,548\\ 5903,317\\ 5899,295\\ \end{array}$	$\begin{array}{c}1\\7\\2\\1\\22\end{array}$	D C D D A	6 II A 18 II 10 II 5 III A 25 II	$\begin{array}{c} 16836.\ 584\\ 16881.\ 201\\ 16891.\ 367\\ 16934.\ 947\\ 16946.\ 493 \end{array}$	$a^3 P_2 - b^3 D_2$ $a^3 P_0 - b^3 D_1$ $a^3 P_2 - a^3 P'_2$ $a^3 P_2 - a^3 P'_1$ $a^3 P_1 - b^3 D_2$	-002 +004
$\begin{array}{c} 5866.\ 453\\ 5804.\ 265\\ 5785.\ 979\\ 5774.\ 037\\ 5766.\ 330 \end{array}$	$     \begin{array}{c}       31 \\       8 \\       3 \\       6 \\       3     \end{array}   $	A C B C D	35 II 5n IV 5n IV 5n IV 4n IV	$\begin{array}{c} 17041,364\\ 17223,947\\ 17278,379\\ 17314,116\\ 17337,257\end{array}$	$a^3 P_2 - b^3 D_3$ $b^5 G_6 - c^5 H_7$ $b^5 G_5 - c^5 H_6$ $b^5 G_4 - c^5 H_5$ $b^5 G_3 - c^5 H_4$	+004
5739.464 5715.123 5689.465 5675.413 5662.154	5 3 7 10 10	B D B A	9 III 9 III 10 III 9 III <i>A</i> 12 III	$\begin{array}{c} 17418.\ 410\\ 17492.\ 594\\ 17571.\ 481\\ 17614.\ 987\\ 17656.\ 237\end{array}$	$a^{3}\mathrm{H}_{5}-b^{3}\mathrm{H}'_{5}\ a^{3}\mathrm{H}_{6}-b^{3}\mathrm{H}'_{6}\ a^{5}\mathrm{D}_{2}-b^{5}\mathrm{F}_{3}\ a^{5}\mathrm{D}_{3}-b^{5}\mathrm{F}_{4}\ a^{5}\mathrm{D}_{4}-b^{5}\mathrm{F}_{5}$	000 000
$\begin{array}{c} 5648.\ 570\\ 5644.\ 137\\ 5565.\ 476\\ 5512.\ 529\\ 5503.\ 897\end{array}$	$     \begin{array}{c}       4 \\       13 \\       11 \\       17 \\       8     \end{array} $	D A A B	5 IV 18 III 9 III 25 II 8 III	$\begin{array}{c} 17698.\ 695\\ 17712.\ 595\\ 17962.\ 941\\ 18135.\ 471\\ 18163.\ 912 \end{array}$	$a^{3}D_{3}-c^{3}F_{4}$ bG'-cG $a^{3}H_{4}-cG$ $b^{3}F_{4}-e^{3}D_{3}$ aH-dG	+003 +001
$\begin{array}{c} 5490.\ 151\\ 5488.\ 210\\ 5481.\ 426\\ 5477.\ 695\\ 5429.\ 139\end{array}$	$     \begin{array}{c c}       10 \\       2 \\       3 \\       11 \\       5     \end{array} $	B D B D	12 II 5 III 6 III 8 III 6 III	$\begin{array}{c} 18209.\ 391\\ 18215.\ 829\\ 18238.\ 374\\ 18250.\ 796\\ 18414.\ 022 \end{array}$	$b^{3}F_{4}-b^{5}D_{3}$ $a^{3}F'_{2}-c^{3}F_{2}$ $a^{3}F'_{2}-c^{3}F_{3}$ $a^{3}F'_{4}-c^{3}F_{4}$ $c^{3}P_{2}-d^{3}P'_{2}$	000 000 000
$\begin{array}{c} 5409.\ 609\\ 5397.\ 093\\ 5389.\ 996\\ 5369.\ 635\\ 5298.\ 429\end{array}$	8 5 2 3 2	C D D D D D D	6 II 4 III 3 III 4 III 4 III	$\begin{array}{c} 18480,500\\ 18523,359\\ 18547,745\\ 18618,077\\ 18868,284 \end{array}$	$a^{3}G'_{5}-e^{3}F'_{4}$ $a^{3}G'_{4}-e^{3}F'_{3}$ $a^{3}G'_{3}-e^{3}F'_{2}$ bD'-cP'	-001 000 000
$\begin{array}{c} 5297.\ 236\\ 5295.\ 781\\ 5283.\ 441\\ 5265.\ 967\\ 5224.\ 928\\ \end{array}$	$\begin{vmatrix} 3\\2\\4\\6\\3 \end{vmatrix}$	D D D C D	6 III 4 III 8 III 10 III 8 III	18872. 532 18877. 720 18921. 809 18984. 597 19133. 706	$\begin{array}{c} a^3{\rm G}'_3-\!\!\!\!\!\!\!\!\!\!\!\!\!\!\!\!\!\!\!\!\!\!\!\!\!\!\!\!\!\!\!\!\!\!\!\!$	$000 + 002 \\ 000 + 602 + 602$

TABLE 1.—Vacuum arc wave lengths of titanium

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# TABLE 1.-Vacuum arc wave lengths of titanium-Continued

λΙ.Α.	Num- ber of obser- va- tions	Weight	Intensity and temperature class	ν (Vac)	Term combi- nation	(0-C) λ
$\begin{array}{c} 5224,301\\ 5210,386\\ 5192,971\\ 5173,742\\ 5147,483\end{array}$	$3 \\ 29 \\ 26 \\ 27 \\ 12$	D A A A A	15 III 40 I 35 I 30 I 10 IA	$\begin{array}{c} 19136.\ 006\\ 19187.\ 107\\ 19251.\ 453\\ 19323.\ 003\\ 19421.\ 575\end{array}$	$a^5 F'_5 - b^5 F_5$ $a^3 F_4 - a^3 F'_4$ $a^3 F_3 - a^3 F'_3$ $a^3 F_2 - a^3 F'_2$ $a^3 F_2 - a^3 F'_3$	$\begin{array}{c} 000 \\ -001 \\ 000 \\ +001 \end{array}$
$\begin{array}{c} 5145.\ 465\\ 5120.\ 420\\ 5113.\ 448\\ 5087.\ 055\\ 5064.\ 654 \end{array}$	$     \begin{array}{c}       13 \\       10 \\       8 \\       3 \\       26     \end{array} $	A A C D A	12 II 12 III 10 III 8 III 25 I	$\begin{array}{c} 19429,\ 194\\ 19524,\ 222\\ 19550,\ 843\\ 19652,\ 277\\ 19739,\ 198 \end{array}$	$b^{3}F_{4}-f^{3}D_{3}$ $b^{3}F_{3}-f^{3}D_{2}$ $b^{3}F_{2}-f^{3}D_{1}$ $a^{3}F_{4}-a^{3}D_{3}$	000 000 000 000
$\begin{array}{c} 5062.\ 112\\ 5052.\ 879\\ 5039.\ 959\\ 5038.\ 400\\ 5036.\ 468 \end{array}$	$2 \\ 2 \\ 22 \\ 15 \\ 10$	D D A B	7 III 8 IV 22 I 25 II 25 II	$\begin{array}{c} 19749.\ 111\\ 19785.\ 196\\ 19835.\ 917\\ 19842.\ 053\\ 19849.\ 667 \end{array}$	$\begin{array}{c} a^{3}D'_{2} - d^{3}P'_{1} \\ a^{3}D'_{3} - d^{3}P'_{2} \\ a^{3}F_{3} - a^{3}D_{2} \\ b^{3}F_{2} - d^{3}G_{3} \\ b^{3}F_{3} - d^{3}G_{4} \end{array}$	$\begin{array}{c} 000\\ 000\\ 000\\ -001\\ 000 \end{array}$
$\begin{array}{c} 5035.\ 908\\ 5025.\ 570\\ 5024.\ 842\\ 5022.\ 871\\ 5020.\ 028 \end{array}$	$ \begin{array}{c} 11 \\ 9 \\ 12 \\ 22 \\ 22 \\ 22 \end{array} $	B C C A A	25 II 18 III 20 II 25 II 25 II	$\begin{array}{c} 19851.\ 873\\ 19892.\ 711\\ 19895.\ 592\\ 19903.\ 397\\ 19914.\ 670\\ \end{array}$	$\begin{vmatrix} b^3 F_4 - d^3 G_5 \\ a^5 G_6 - b^5 F_5 \\ a^5 F_2 - b^5 G_2 \\ a^5 F_3 - b^5 G_3 \\ a^5 F_4 - b^5 G_4 \end{vmatrix}$	+001
$\begin{array}{c} 5016.\ 162\\ 5014.\ 277\\ 5014.\ 185\\ 5009.\ 652\\ 5007.\ 209 \end{array}$	19 28 3 1 28	A A D A	$\begin{array}{c} 20 \ \text{II} \\ 25 \ \text{I} \\ 25 \ \text{I} \\ 7 \ \text{I} \\ 40 \ \text{II} \end{array}$	$\begin{array}{c} 19930.\ 026\\ 19937.\ 512\\ 19937.\ 878\\ 19955.\ 917\\ 19965.\ 651 \end{array}$	$\begin{array}{c} a^5 {\rm F}_5 {-} b^5 {\rm G}_5 \\ a^5 {\rm F}_1 {-} b^5 {\rm G}_2 \\ a^3 {\rm F}_2 {-} a^3 {\rm D}_1 \\ a^3 {\rm F}_3 {-} a^3 {\rm D}_3 \\ a^5 {\rm F}_2 {-} b^5 {\rm G}_3 \end{array}$	+000 +006
4999. 504 4997. 099 4991. 067 4981. 732 4978. 191	30 2 30 30 8	A D A C	45 II 8 I 4 50 II 60 II 10 III	$\begin{array}{c} 19996.\ 425\\ 20006.\ 046\\ 20030.\ 226\\ 20067.\ 757\\ 20082.\ 031 \end{array}$	$a^5 F_3 - b^5 G_4$ $a^3 F_2 - a^3 D_2$ $a^5 F_4 - b^5 G_5$ $a^5 F_5 - b^5 G_6$ $a^5 G_2 - b^5 F_1$	+001
4975. 344 4938. 283 4928. 342 4921. 768 4919. 867	$     \begin{array}{c}       10 \\       9 \\       13 \\       13 \\       11     \end{array} $	C D A B B	10 III 8 IV 12 III 12 III 10 III	$\begin{array}{c} 20093.\ 523\\ 20244.\ 321\\ 20285.\ 152\\ 20312.\ 248\\ 20320.\ 098 \end{array}$	$\begin{array}{c} bD'-dF'\\ aH-fG\\ a^{3}D'_{1}-g^{3}F'_{2}\\ a^{3}D'_{3}-g^{3}F'_{4}\\ a^{3}D'_{2}-g^{3}F'_{3} \end{array}$	000 000 000
4913. 616 4899. 910 4885. 082 4870. 129 4868. 264	$20 \\ 24 \\ 25 \\ 15 \\ 15 \\ 15$	A A A A A	20 III 20 III 20 II 20 II 18 III	$\begin{array}{c} 20345.\ 946\\ 20402.\ 859\\ 20464.\ 788\\ 20527.\ 621\\ 20535.\ 483 \end{array}$	$\begin{array}{c} a^3{\rm G}'_3 {-} b^3{\rm H}'_4 \\ a^3{\rm G}'_4 {-} b^3{\rm H}'_5 \\ a^3{\rm G}'_5 {-} b^3{\rm H}'_6 \\ a^3{\rm H}_5 {-} a^3{\rm I}_6 \\ a^3{\rm H}_4 {-} a^3{\rm I}_5 \end{array}$	000 000 000
4856. 012 4840. 874 4820. 410 4805. 416 4799. 797	19 25 14 13 14	A A B B	20 III 25 I 20 II 12 III 12 III	$\begin{array}{c} 20587,\ 298\\ 20651,\ 676\\ 20739,\ 345\\ 20804,\ 051\\ 20828,\ 412 \end{array}$	$a^{3}H_{6}-a^{3}I_{7}\ aD'-bD\ aG'-bF'\ c^{3}P_{2}-i^{3}D_{3}\ bG'-c^{3}H'_{4}$	
4792. 482 4778. 259 4759. 272 4758. 120 4742. 791	13 9 21 18 18	A B A A A	10 III 10 III 25 III 25 III 20 III	$\begin{array}{c} 20860,\ 203\\ 20922,\ 292\\ 21005,\ 760\\ 21010,\ 849\\ 21078,\ 756 \end{array}$	$c^{3}P_{1}-i^{3}D_{2}$ $a^{3}H_{4}-dG$ $a^{3}H_{6}-c^{3}H'_{6}$ $a^{3}H_{5}-c^{3}H'_{5}$ $a^{3}H_{4}-c^{3}H'_{4}$	
4731. 172 4715. 295 4710. 186 4698. 766	7 4 15 21	A D A A	9 III 4 II <i>A</i> 18 III 20 II	$\begin{array}{c} 21130.\ 521\\ 21201.\ 668\\ 21224.\ 663\\ 21276.\ 247\\ \end{array}$	$\begin{cases} a^{3}D'_{3}-h^{3}F'_{4}\\ a^{3}F_{4}-a^{3}G_{4}\\ \{a^{3}P_{0}-e^{3}D_{1}\\ a^{3}D'_{3}-h^{3}D_{3}\\ a^{3}P_{1}-e^{3}D_{2} \end{cases}$	$\left. \begin{array}{c} \cdot & \\ -005 \\ 000 \end{array} \right\}$
$\begin{array}{r} 4691.\ 336\\ 4681.\ 908\\ 4675.\ 118\\ 4667.\ 585\\ 4656.\ 468 \end{array}$	$24 \\ 30 \\ 9 \\ 30 \\ 30 \\ 30$	A C A A	20 II 30 I 10 III 25 I 25 I	$\begin{array}{c} 21309,944\\ 21352,857\\ 21383,870\\ 21418,381\\ 21469,515 \end{array}$	$\begin{array}{c} a^{3}\mathrm{P}_{2}-e^{3}\mathrm{D}_{3}\\ a^{3}\mathrm{F}_{4}-a^{3}\mathrm{G}_{5}\\ a^{3}\mathrm{P}_{2}-b^{5}\mathrm{D}_{3}\\ a^{3}\mathrm{F}_{3}-a^{3}\mathrm{G}_{4}\\ a^{3}\mathrm{F}_{2}-a^{3}\mathrm{G}_{3} \end{array}$	-001 +003 +002 +005
$\begin{array}{c} 4645.\ 193\\ 4629.\ 336\\ 4623.\ 098\\ 4617.\ 269\\ 4599.\ 226 \end{array}$	$     \begin{array}{c}       12 \\       24 \\       26 \\       29 \\       9 \\       9     \end{array} $	C A A A A	12 III 15 III 25 III 30 II 5 IV	$\begin{array}{c} 21521.\ 626\\ 21595.\ 343\\ 21624.\ 478\\ 21651.\ 780\\ 21736.\ 720 \end{array}$	$a^5 P_1 - c^5 D_0$ $a^5 P_1 - c^5 D_2$ $a^5 P_2 - c^5 D_3$ $a^5 P_3 - c^5 D_4$	

# TABLE 1.-Vacuum arc wave lengths of titanium-Continued

λΙ.Α.	Num- ber of obser- va- tions	Weight	Intensity and temperature class	ν (Vac)	Term combi- nation	(0-C) λ
$\begin{array}{c} 4571.\ 971\\ 4563.\ 761\\ 4559.\ 920\\ 4555.\ 486\\ 4552.\ 453\end{array}$	$23 \\ 16 \\ 7 \\ 30 \\ 30 \\ 30$	A A B A A	$\begin{array}{c} 15 \ {\rm V}  E, \ {\rm Ti} \ {\rm II} \\ 15 \ {\rm V}  E, \ {\rm Ti} \ {\rm II} \\ 6 \ {\rm III} \\ 30 \ {\rm II} \\ 35 \ {\rm II} \end{array}$	$\begin{array}{c} 21866,297\\ 21905,632\\ 21924,083\\ 21945,422\\ 21960,044 \end{array}$	$a^{2}\mathrm{H}_{5}-a^{2}\mathrm{G}_{4}$ $a^{2}\mathrm{P}_{1}-a^{2}\mathrm{D}_{2}$ $b^{3}\mathrm{F}_{4}-e^{3}\mathrm{F}'_{4}$ $a^{5}\mathrm{F}_{5}-b^{5}\mathrm{F}'_{4}$ $a^{5}\mathrm{F}_{4}-b^{5}\mathrm{F}'_{3}$	-001
$\begin{array}{c} 4549.\ 622\\ 4548.\ 764\\ 4544.\ 688\\ 4533.\ 238\\ 4527.\ 305 \end{array}$	$     \begin{array}{r}       10 \\       29 \\       29 \\       21 \\       30     \end{array} $	C A B A	25 V <i>E</i> , Ti II 35 II 30 II 80 II 35 II	$\begin{array}{c} -21973.\ 709\\ 21977.\ 853\\ 21997.\ 564\\ 22053.\ 109\\ 22082.\ 026\end{array}$	$\begin{array}{c} a^2 {\rm H}_6 - a^2 {\rm G}_5 \\ a^5 {\rm F}_3 - b^5 {\rm F}'_2 \\ a^5 {\rm F}_2 - b^5 {\rm F}'_1 \\ a^5 {\rm F}_5 - b^5 {\rm F}'_5 \\ a^5 {\rm F}_1 - b^5 {\rm F}'_2 \end{array}$	
$\begin{array}{c} 4522.\ 798\\ 4518.\ 022\\ 4512.\ 734\\ 4503.\ 762\\ 4501.\ 270\\ \end{array}$	$30 \\ 30 \\ 30 \\ 2 \\ 23$	A A D A	40 II 50 II 40 II 4 <i>n</i> IV 25 V <i>E</i> , Ti II	$\begin{array}{c} 22104.\ 030\\ 22127.\ 394\\ 22153.\ 325\\ 22197.\ 454\\ 22209.\ 745 \end{array}$	$a^{5}F_{2}-b^{5}F'_{3}$ $a^{5}F_{3}-b^{5}F'_{4}$ $a^{5}F_{4}-b^{5}F'_{5}$ $a^{2}G'_{4}-a^{2}F'_{3}$	
$\begin{array}{c} 4496.\ 146\\ 4489.\ 089\\ 4482.\ 688\\ 4481.\ 261\\ 4474.\ 852 \end{array}$	$25 \\ 25 \\ 2 \\ 26 \\ 11$	A A D A A	20 III 20 III 10 III 30 III 8 III	$\begin{array}{c} 22235.\ 054\\ 22270.\ 009\\ 22301.\ 809\\ 22308.\ 910\\ 22340.\ 862 \end{array}$	$\substack{a^5\mathrm{P}_3-a^5\mathrm{P'}_2\\a^5\mathrm{P}_2-a^5\mathrm{P'}_1\\b^3\mathrm{F}_4-f^3\mathrm{F'}_3\\a^5\mathrm{P}_3-a^5\mathrm{P'}_3\\b^3\mathrm{F}_3-f^3\mathrm{F'}_2}$	-003 +001
$\begin{array}{c} 4471.\ 238\\ 4468.\ 493\\ 4465.\ 807\\ 4457.\ 428\\ 4455.\ 321 \end{array}$	25 25 25 29 28	B A A A A	20 III 25 V <i>E</i> , Ti II 20 III 40 II 30 II	22358. 920 22372. 651 22386. 108 22428. 187 22438. 796	$a^5 P_1 - a^5 P'_2 \\ a^2 G'_5 - a^2 F'_4 \\ a^5 P_2 - a^5 P'_3 \\ b^3 F_4 - f^3 F'_4 \\ b^3 F_3 - f^3 F'_3$	$-002 \\ -001$
$\begin{array}{r} 4453.\ 708\\ 4453.\ 312\\ 4450.\ 896\\ 4449.\ 143\\ 4443.\ 802 \end{array}$	$2 \\ 17 \\ 29 \\ 30 \\ 21$	D C C A A	20 III 30 II 25 III 30 III 25 V <i>E</i> , Ti II	$\begin{array}{c} 22446.\ 921\\ 22448.\ 916\\ 22461.\ 104\\ 22469.\ 951\\ 22496.\ 960\\ \end{array}$	$a^{3}G'_{3}-e^{3}G_{3}$ $b^{3}F_{2}-f^{3}F'_{2}$ $a^{3}G'_{4}-e^{3}G_{4}$ $a^{3}G'_{5}-e^{3}G_{5}$ $a^{2}D'_{2}-a^{2}F'_{3}$	009
4440. 345 4436. 586 4434. 003 4430. 366	$20 \\ 5 \\ 14 \\ 12$	A C C C	10 III 4 III 15 III A 7 III A	$\begin{array}{c} 22514.\ 475\\ 22533.\ 551\\ 22546.\ 674\\ 22565.\ 183\end{array}$	$\begin{cases} a^{3}G'_{3}-cF'\\ a^{3}G'_{4}-e^{3}G_{5}\\ b^{3}F_{2}-f^{3}F'_{3}\\ a^{3}G'_{3}-g^{3}F'_{2}\\ b^{3}F_{3}-f^{3}F'_{4} \end{cases}$	} 1
$\begin{array}{c} 4427.\ 098\\ 4426.\ 054\\ 4422.\ 823\\ 4421.\ 754\\ 4417.\ 274 \end{array}$	$30 \\ 11 \\ 17 \\ 9 \\ 13$	A C A C B	40 III 10 II 10 II 6 III 15 III	$\begin{array}{c} 22581.\ 841\\ 22587.\ 166\\ 22603.\ 667\\ 22609.\ 135\\ 22632.\ 064 \end{array}$	$a{ m G}'-b{ m G}$ $a^3{ m G}'_4-g^3{ m F}'_3$ $a^3{ m P}_2-f^3{ m D}_3$ $b^3{ m P}_1-j^3{ m D}_2$ $a^3{ m G}'_5-g^3{ m F}'_4$	-001
$\begin{array}{c} 4399.\ 767\\ 4395.\ 031\\ 4393.\ 925\\ 4372.\ 383\\ 4369.\ 682 \end{array}$		B A B D C	6 V <i>E</i> , Ti II 25 V <i>E</i> , Ti II 8 III 3 IV 5 <i>n</i> IV	$\begin{array}{c} 22722,119\\ 22746,602\\ 22752,326\\ 22864,423\\ 22878,552\\ \end{array}$	$\begin{array}{c} a^{2}P_{2}-a^{4}D_{3}\\ a^{2}D'_{3}-a^{2}F'_{4}\\ bG'-fG\\ aH-gG \end{array}$	
$\begin{array}{c} 4360.\ 487\\ 4346.\ 104\\ 4337.\ 916\\ 4325.\ 134\\ 4321.\ 655\end{array}$	$     \begin{array}{c}             11 \\             11 \\         $	B A A A A	$\begin{array}{c} 4 \\ 5 \\ 10 \\ 10 \\ 9n \\ 11 \\ 8n \\ 111 \\ 8n \\ 111 \end{array}$	$\begin{array}{c} 22926,798\\ 23002,667\\ 23046,089\\ 23114,194\\ 23132,801 \end{array}$	$\begin{array}{c} a^{3}D'_{3}-e^{3}P'_{2}\\ a^{3}H_{4}-fG\\ a^{2}D'_{2}-a^{2}D_{2}\\ a^{3}H^{5}-f^{3}G_{4}\\ a^{3}H_{4}-f^{3}G_{3} \end{array}$	
4318. 631 4314. 801 4312. 861 4307. 900	25 30 7 21	A A C B	10n III 25 II 7 V <i>E</i> , Ti II 12 V <i>E</i> , Ti II	23149.000 23169.542 23179.966 23206.664	$\begin{cases} a^{3}H_{6}-f^{3}G_{5} \\ a^{5}F_{4}-e^{3}D_{3} \\ a^{5}F_{2}-e^{3}D_{2} \\ a^{4}P_{3}-a^{4}D_{3} \\ a^{4}P_{2}-a^{4}D_{2} \end{cases}$	}
$\begin{array}{r} 4305.\ 910\\ 4298.\ 664\\ 4295.\ 751\\ 4294.\ 101\\ 4289.\ 068\end{array}$	26 29 29 11 27	A A C A	60 II 40 II 22 II 8 V <i>E</i> , Ti II 25 II	$\begin{array}{c} 23217,386\\ 23256,522\\ 23272,294\\ 23281,234\\ 23308,551\end{array}$	$a^5 F_5 - b^5 D_4$ $a^5 F_2 - b^5 D_1$ $a^5 F_1 - b^5 D_0$ $a^2 D'_3 - a^2 D_3$ $a^5 F_2 - b^5 D_2$	
$\begin{array}{c} 4287.\ 405\\ 4286.\ 006\\ 4282.\ 702\\ 4281.\ 371\\ 4274.\ 584 \end{array}$	$     \begin{array}{r}       26 \\       30 \\       23 \\       11 \\       13     \end{array}   $	A A C B	22 II 25 II 12 III 10 III 15 III	23317. 595 23325. 204 23343. 199 23350. 459 23387. 529	$a^5 F_4 - b^5 D_4$ $a^5 F_3 - b^5 D_3$ $a^3 G'_3 - h^3 F'_2$ $a^3 F_1 - b^5 D_2$ $\{ a^3 G'_4 - h^3 F'_3$ $a^5 F_2 - b^5 D_3$	}

	1-5-5-1-1					2 3 1 2 3 0 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4
λΙ.Α.	Num- ber of obser- va- tions	Weight	Intensity and temperature class	ν (Vac)	Term combi- nation	(O-C) λ
4263. 134 4258. 523 4256. 025 4249. 114 4237. 889	$25 \\ 3 \\ 10 \\ 5 \\ 10$	A D B D A	$ \begin{array}{c} 15 \ \text{III} \\ 4n \ \text{IV} \\ 8n \ \text{III} \\ 5n \ \text{III} \\ 7 \ \text{III} \end{array} $	23450. 343 23475. 738 23489. 513 23527. 718 23590. 035	$\begin{array}{c} a^{3}{\rm G'}_{5}-h^{3}{\rm F'}_{4}\\ a^{5}{\rm D}_{1}-b^{5}{\rm D'}_{2}\\ a^{5}{\rm D}_{4}-b^{5}{\rm D'}_{4}\\ a^{5}{\rm D}_{2}-b^{5}{\rm D'}_{3}\\ b{\rm D'}-d{\rm D}\end{array}$	
$\begin{array}{c} 4186.\ 119\\ 4171.\ 897\\ 4163.\ 644\\ 4159.\ 634\\ 4150.\ 963\end{array}$	$     \begin{array}{c}       25 \\       8 \\       8 \\       11 \\       8     \end{array} $	A C C A C	25 III 5 V E, Ti II 8 V E, Ti II 9 III 10 III	$\begin{array}{c} 23881.\ 766\\ 23963.\ 179\\ 24010.\ 682\\ 24033.\ 828\\ 24084.\ 030 \end{array}$	$\begin{vmatrix} aG'-cG\\b^2F_3-c^2D_2\\b^2F_4-c^2D_3\\a^3D'_2-i^3F'_3\\a^3D'_3-i^3F'_4 \end{vmatrix}$	
$\begin{array}{c} 4137.\ 284\\ 4127.\ 531\\ 4122.\ 143\\ 4112.\ 708\\ 4099.\ 166\end{array}$	$     \begin{array}{c}       10 \\       12 \\       7 \\       25 \\       8     \end{array} $	B B C A B	10 <i>n</i> III 15 III 10 III 20 II 8 III	$\begin{array}{c} 24163.\ 654\\ 24220.\ 752\\ 24252.\ 407\\ 24308.\ 047\\ 24388.\ 346 \end{array}$	$\begin{vmatrix} a^5 D_4 - b^5 P_3 \\ a^3 G_5 - b^3 H_4 \\ a^3 G_3 - b^3 H_4 \\ a^3 F_4 - a G \\ a^3 D'_3 - f^3 P'_2 \end{vmatrix}$	
$\begin{array}{c} 4082,456\\ 4078,471\\ 4065,094\\ 4060,263\\ 4058,139 \end{array}$	$     \begin{array}{c}       24 \\       26 \\       8 \\       23 \\       6     \end{array} $	A A B A D	20 III 30 III 15 III 20 III 7 IV	$\begin{array}{c} 24488.\ 173\\ 24512.\ 099\\ 24592.\ 756\\ 24622.\ 015\\ 24634.\ 904 \end{array}$	$\begin{bmatrix} a^{3}P_{2}-c^{3}P'_{1} \\ a^{3}P_{2}-c^{3}P'_{2} \\ a^{3}P_{1}-c^{3}P'_{0} \\ a^{3}P_{1}-c^{3}P'_{2} \end{bmatrix}$	
$\begin{array}{c} 4055.\ 011\\ 4035.\ 828\\ 4030.\ 512\\ 4026.\ 539\\ 4024.\ 573\end{array}$	$\begin{array}{c} 22 \\ 1 \\ 15 \\ 10 \\ 29 \end{array}$	A D A B B	20 III 10 III 25 <i>n</i> III 25 <i>n</i> III 35 II	$\begin{array}{c} 24653.908\\ 24771.090\\ 24803.759\\ 24828.232\\ 24840.363\end{array}$	$\begin{vmatrix} a^{3}P_{0}-c^{3}P'_{1} \\ a^{3}D'_{3}-k^{3}D_{3} \\ a^{5}F'_{5}-b^{5}G'_{6} \\ a^{5}F'_{4}-b^{5}G'_{5} \\ a^{3}F_{4}-b^{3}F'_{3} \end{vmatrix}$	000
$\begin{array}{c} 4017.\ 771\\ 4015.\ 377\\ 4013.\ 587\\ 4008.\ 926\\ 3998.\ 635 \end{array}$	$     \begin{array}{c}       10 \\       8 \\       8 \\       28 \\       25     \end{array} $	B B A A	15 <i>n</i> III 12 <i>n</i> III 12 <i>n</i> III 35 II 100 <i>R</i> II	$\begin{array}{c} 24882.\ 418\\ 24897.\ 249\\ 24908.\ 356\\ 24937.\ 314\\ 25001.\ 494 \end{array}$	$\begin{array}{c} a^5 F'_2 - b^5 G'_3 \\ a^5 F'_1 - b^5 G'_2 \\ a^5 F'_5 - b^5 H_6 \\ a^3 F_3 - b^3 F'_2 \\ a^3 F_4 - b^3 F'_4 \end{array}$	$+001 \\ -003$
$\begin{array}{c} 3989.\ 758\\ 3981.\ 761\\ 3964.\ 269\\ 3962.\ 851\\ 3958.\ 206 \end{array}$	$25 \\ 26 \\ 23 \\ 23 \\ 25 \\ 25$	A A B A B	$\begin{array}{c} 80 R \ \Pi \\ 70 R \ \Pi \\ 35 \ \Pi \\ 35 \ \Pi \\ 80 \ \Pi \end{array}$	$\begin{array}{c} 25057,118\\ 25107,441\\ 25218,220\\ 25227,247\\ 252256,850\\ \end{array}$	$\begin{smallmatrix} a^{3}{\rm F}_{3}-b^{3}{\rm F}'_{3}\\ a^{3}{\rm F}_{2}-b^{3}{\rm F}'_{2}\\ a^{3}{\rm F}_{3}-b^{3}{\rm F}'_{4}\\ a^{3}{\rm F}_{2}-b^{3}{\rm F}'_{3}\\ a^{3}{\rm F}_{4}-b^{3}{\rm D}_{3} \end{smallmatrix}$	$\begin{array}{c} -002 \\ +001 \\ -001 \\ -001 \\ +001 \end{array}$
3956. 336 3948. 670 3947. 770 3929. 875 3924. 527	28 26 25 25 25 28	A B B B A	60 II 60 II 40 II 40 II 50 II	$\begin{array}{c} 25268.\ 790\\ 25317.\ 847\\ 25323.\ 617\\ 25438.\ 923\\ 25473.\ 592 \end{array}$	$ \begin{array}{c} a^{3} F_{3} - b^{3} D_{2} \\ a^{3} F_{2} - b^{3} D_{1} \\ a^{3} F_{3} - a^{3} P'_{2} \\ a^{3} F_{2} - b^{3} D_{2} \\ a^{3} F_{3} - b^{3} D_{3} \end{array} $	$+002 \\ +004 \\ +001 \\ 000$
$\begin{array}{c} 3921.\ 423\\ 3914.\ 334\\ 3913.\ 464\\ 3904.\ 785\\ 3900.\ 546\end{array}$	$     \begin{array}{c}         16 \\         20 \\         11 \\         26 \\         7         7         $	B B A D	$\begin{array}{c} 30 \ \mathrm{II} \\ 35 \ \mathrm{II} \\ 40 \ \mathrm{V}\textit{E}, \ \mathrm{Ti} \ \mathrm{II} \\ 40n \ \mathrm{II} \\ 50 \ \mathrm{V}\textit{E}, \ \mathrm{Ti} \ \mathrm{II} \end{array}$	$\begin{array}{c} 25493.\ 757\\ 25539.\ 920\\ 25545.\ 603\\ 25602.\ 379\\ 25630.\ 202\end{array}$	$\begin{array}{c} a^{3}F_{2}-a^{3}P'_{2}\\ a^{3}F_{4}-c^{3}F'_{4}\\ a^{2}G'_{4}-a^{2}G_{4}\\ aD'-bF'\\ a^{2}G'_{5}-a^{2}G_{5} \end{array}$	
3895. 243 3875. 262 3866. 446 3798. 276	6 14 2 3	C C D D	30 <i>n</i> III 20 <i>n</i> III 15 <i>n</i> IV 6 IV	25665.092 25797.424 25856.242 26320.291	$ \left\{ \begin{array}{l} a^5 {\rm G}_6 - b^5 {\rm H}_6 \\ a^3 {\rm F}_2 - c^3 {\rm F}_3 \\ a^5 {\rm G}_4 - b^5 {\rm G}'_5 \\ a^5 {\rm G}_5 - b^5 {\rm H}_6 \\ b^3 {\rm F}_2 - g^3 {\rm D}_1 \end{array} \right. $	}
$\begin{array}{c} 3786.\ 043\\ 3771.\ 652\\ 3761.\ 320\\ 3759.\ 291\\ 3752.\ 860 \end{array}$	$23 \\ 24 \\ 24 \\ 23 \\ 24 \\ 24$	C A B B B	20 II 25 I 40 IV <i>Er</i> , Ti II 40 IV <i>Er</i> , Ti II 80r I	$\begin{array}{c} 26405,331\\ 26506,075\\ 26578,885\\ 26593,234\\ 26638,799 \end{array}$	$\begin{array}{c} aD'-aP'\\ a^{3}F_{4}-d^{3}F'_{3}\\ a^{2}F_{3}-a^{2}F'_{3}\\ a^{2}F_{4}-a^{2}F'_{4}\\ a^{3}F_{4}-d^{3}F'_{4} \end{array}$	000
$\begin{array}{c} 3741.\ 059\\ 3729.\ 806\\ 3725.\ 155\\ 3724.\ 570\\ 3722.\ 568\end{array}$	$25 \\ 25 \\ 5 \\ 7 \\ 14$	B A C C B	60r I 50r I 20 III 20 III 15 II	$\begin{array}{c} 26722,827\\ 26803,450\\ 26836,920\\ 26841,134\\ 26855,565 \end{array}$	$ \begin{array}{c} a^{3}F_{3} - d^{3}F'_{3} \\ a^{3}F_{2} - d^{3}F'_{2} \\ a^{3}P_{2} - b^{3}S_{1} \\ a & G' - d & G \\ a^{3}F_{3} - d^{3}F'_{4} \end{array} $	-002 + 001 -004
$\begin{array}{c} 3717.\ 393\\ 3694.\ 445\\ 3689.\ 916\\ 3685.\ 192\\ 3671.\ 672 \end{array}$	$     \begin{array}{r}       14 \\       9 \\       14 \\       17 \\       14     \end{array} $	A C A B A	20 I 10 III 15 I 40 IV <i>Er</i> , Ti II 20 I	$\begin{array}{c} 26892,955\\ 27059,989\\ 27093,208\\ 27127,936\\ 27227,821 \end{array}$	$\begin{array}{c} a^{3}F_{2} \begin{tabular}{c} d^{3}F_{3} \begin{tabular}{c} b^{3}F_{3} \begin{tabular}{c} h^{3}D_{2} \end{tabular} \\ a^{3}F_{4} \begin{tabular}{c} c^{3}D_{3} \end{tabular} \\ a^{3}F_{4} \begin{tabular}{c} b^{3}G_{4} \end{tabular} \end{array}$	-001 +001 000

ABLE 1. Vacuum arc wave lengins of manuum-Contin	TABLE	1Vacuum	arc wave	lenaths o	f titanium-	Continue	ed
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λΙ.Α.	Num- ber of obser- va- tions	Weight	Intensity and temperature class	ν (Vac)	Term combi- nation	(0-C) λ
$\begin{array}{c} 3668,965\\ 3660,631\\ 3658,097\\ 3654,592\\ 3653,497 \end{array}$	$14 \\ 12 \\ 12 \\ 10 \\ 15$	B A B B C	15 I 12 I 20 I 15 I 1007 I	$\begin{array}{c} 27247.\ 912\\ 27309.\ 943\\ 27328.\ 863\\ 27355.\ 073\\ 27363.\ 270\end{array}$	$\begin{array}{c} a^3 F_3 - c^3 D_2 \\ a^3 F_3 - c^3 D_3 \\ a^3 F_3 - b^3 G_3 \\ a^3 F_2 - c^3 D_1 \\ a^3 F_4 - b^3 G_5 \end{array}$	$\begin{array}{c} -001 \\ 000 \\ +005 \\ -001 \\ +002 \end{array}$
$\begin{array}{c} 3646.\ 198\\ 3642.\ 675\\ 3641.\ 330\\ 3635.\ 462\\ 3624.\ 826 \end{array}$	$9 \\ 14 \\ 6 \\ 12 \\ 10$	A B B B B	$\begin{array}{c} 12 \text{ I} \\ 80r \text{ I} \\ 10 \text{ VE, Ti II} \\ 80r \text{ I} \\ 8 \text{ VE, Ti II} \end{array}$	$\begin{array}{c} 27418.\ 045\\ 27444.\ 563\\ 27454.\ 697\\ 27499.\ 014\\ 27579.\ 694 \end{array}$	$\begin{array}{c} a^{3}F_{2} - c^{3}D_{2} \\ a^{3}F_{3} - b^{3}G_{4} \\ a^{2}P_{2} - a^{2}S_{1} \\ a^{3}F_{2} - b^{3}G_{3} \\ a^{2}P_{1} - a^{2}S_{1} \end{array}$	$-001 \\ 000 \\ +003$
$\begin{array}{c} 3610.\ 154\\ 3598.\ 714\\ 3596.\ 048\\ 3547.\ 029\\ 3535.\ 408 \end{array}$	9 12 9 5 9	B A B B A	12 III 15 III 10 V <i>E</i> , Ti II 15 IV 10 V <i>E</i> , Ti II	$\begin{array}{c} 27691.\ 779\\ 27779.\ 807\\ 27800.\ 404\\ 28184.\ 583\\ 28277.\ 224 \end{array}$	$ \begin{array}{c} a \ D' - b \ P' \\ a \ D' - c \ D \\ a^2 F_4 - a^4 D_3 \\ a \ G' - d \ F' \\ b^2 P_2 - c^2 D_3 \end{array} $	
$\begin{array}{c} 3510.\ 840\\ 3504.\ 890\\ 3491.\ 053\\ 3480.\ 525\\ 3477.\ 181 \end{array}$	$     \begin{array}{c}       12 \\       12 \\       3 \\       5 \\       9     \end{array} $	B A D C	10 V Er, Ti II 8 V Er, Ti II 8 III Eru, Ti II 12 II 15 III Eru, Ti II	$\begin{array}{c} 28475,101\\ 28523,436\\ 28636,491\\ 28723,103\\ 28750,726\end{array}$	$\begin{smallmatrix} b^2{\rm G'}_4 - b^2{\rm G}_4 \\ b^2{\rm G'}_5 - b^2{\rm G}_5 \\ b^4{\rm F}_2 - a^4{\rm G}_3 \\ a^3{\rm P}_2 - d^3{\rm P'}_2 \\ b^4{\rm F}_3 - a^4{\rm G}_4 \end{smallmatrix}$	
$\begin{array}{c} 3461.\ 496\\ 3444.\ 306\\ 3394.\ 574\\ 3387.\ 834\\ 3385.\ 944 \end{array}$	$12 \\ 12 \\ 12 \\ 12 \\ 12 \\ 12 \\ 12 \\ 12 \\$	A C B B B B	20 III Eru, Ti II 15 III Eru, Ti II 15 III Eru, Ti II 15 III Eru, Ti II 15 III Eru, Ti II 40r II	$\begin{array}{c} 28881.\ 000\\ 29025.\ 141\\ 29450.\ 353\\ 29508.\ 944\\ 29525.\ 411 \end{array}$	$\begin{array}{c} b^4 F_4 - a^4 G_5 \\ b^4 F_5 - a^4 G_6 \\ a^4 F_3 - a^4 G_3 \\ a^4 F_4 - a^4 G_4 \\ a^3 F_4 - e^3 D_3 \end{array}$	000
$\begin{array}{c} 3383.\ 761\\ 3380.\ 278\\ 3377.\ 577\\ 3371.\ 447\\ 3370.\ 436 \end{array}$	$     \begin{array}{r}       10 \\       12 \\       9 \\       4 \\       6     \end{array} $	A C D C	40 III Eru, Ti II 15 III Eru, Ti II 30r I 80R II 40r II	$\begin{array}{c} 29544.\ 463\\ 29574.\ 905\\ 29598.\ 557\\ 29652.\ 367\\ 29661.\ 260\\ \end{array}$	$\begin{array}{c} a^{4}F_{2}-a^{4}G_{3}\\ a^{4}F_{5}-a^{4}G_{5}\\ a^{3}F_{3}-e^{3}D_{2}\\ a^{3}F_{4}-c^{3}G_{5}\\ a^{3}F_{2}-e^{3}D_{1} \end{array}$	$^{+001}_{+001}_{+001}$
$\begin{array}{c} 3361.\ 213\\ 3358.\ 271\\ 3354.\ 634\\ 3349.\ 399\\ 3341.\ 875 \end{array}$	$     \begin{array}{c}       11 \\       5 \\       11 \\       11 \\       11 \\       11     \end{array} $	B C B C B	40 III <i>Er</i> , Ti II 10 I 60 <i>r</i> II 40 II <i>Er</i> , Ti II 50 <i>r</i> II	$\begin{array}{c} 29742.\ 652\\ 29768.\ 709\\ 29800.\ 975\\ 29847.\ 557\\ 29914.\ 755\\ \end{array}$	$\begin{array}{c} a^{4}\mathrm{F}_{4} - a^{4}\mathrm{G}_{5} \\ a^{3}\mathrm{F}_{2} - e^{3}\mathrm{D}_{2} \\ a^{3}\mathrm{F}_{3} - c^{3}\mathrm{G}_{4} \\ a^{4}\mathrm{F}_{5} - a^{4}\mathrm{G}_{6} \\ a^{3}\mathrm{F}_{2} - c^{3}\mathrm{G}_{3} \end{array}$	$-002 \\ 000 \\ +003$
$\begin{array}{c} 3340.\ 344\\ 3335.\ 192\\ 3332.\ 111\\ 3329.\ 455\\ 3326.\ 762 \end{array}$	$     \begin{array}{r}       10 \\       12 \\       8 \\       9 \\       2     \end{array} $	C B B D	$\begin{array}{c} 15 \text{ III} \textit{Eru}, \text{ Ti II} \\ 20 \text{ III} \textit{Eru}, \text{ Ti II} \\ 8 \text{ V}\textit{Er}, \text{ Ti II} \\ 20 \text{ III} \textit{Eru}, \text{ Ti II} \\ 5 \text{ III} \textit{Eru}, \text{ Ti II} \end{array}$	$\begin{array}{c} 29928,462\\ 29974,689\\ 30002,406\\ 30026,342\\ 30050,641 \end{array}$	$b^4 F_2 - a^4 F'_2 \\ b^4 F_3 - a^4 F'_3 \\ b^4 P_3 - a^4 S_2 \\ b^4 F_4 - a^4 F'_4 \\ b^4 F_2 - a^4 F'_3$	
$\begin{array}{c} 3322,936\\ 3318,024\\ 3314,422\\ 3292,078\\ 3287,657 \end{array}$	$     \begin{array}{c}       11 \\       7 \\       10 \\       10 \\       10 \\       10     \end{array} $	A B B B	20 III Eru, Ti II 8 III Eru, Ti II 10 I 20 I 10 V Er, Ti II	$\begin{array}{c} 30085.\ 241\\ 30129.\ 784\\ 30162.\ 528\\ 30367.\ 234\\ 30408.\ 067 \end{array}$	$\begin{array}{c} b^{4}{\rm F}_{5}-a^{4}{\rm F}'_{5}\\ b^{4}{\rm F}_{3}-a^{4}{\rm F}'_{4}\\ a^{3}{\rm P}_{2}-h^{3}{\rm D}_{3}\\ a{\rm D}'-c{\rm F}'\\ b^{2}{\rm G}'_{4}-a^{2}{\rm H}'_{5} \end{array}$	
3261, 596 3241, 984 3239, 037 3236, 573	8 10 10 10	B A C B	25 V Er, Ti II 40 III Er, Ti II 40 III Er, Ti II 50 III Er, Ti II	$\begin{array}{c} 30651,031\\ 30836,445\\ 30864,588\\ 30888,089 \end{array}$	$\begin{cases} b^{2}\mathrm{G'}_{5} - a^{2}\mathrm{H'}_{6} \\ b^{4}\mathrm{P}_{2} - b^{4}\mathrm{D}_{3} \\ a^{4}\mathrm{F}_{2} - a^{4}\mathrm{F'}_{2} \\ a^{4}\mathrm{F}_{3} - a^{4}\mathrm{F'}_{3} \\ a^{4}\mathrm{F}_{4} - a^{4}\mathrm{F'}_{4} \end{cases}$	}
$\begin{array}{c} 3234.\ 517\\ 3229.\ 397\\ 3222.\ 843\\ 3217.\ 056\\ 3214.\ 240\\ \end{array}$	$     \begin{array}{r}       10 \\       4 \\       9 \\       9 \\       9 \\       8     \end{array} $	B D A C	60 III <i>Er</i> , Ti II 10 V <i>Eru</i> , Ti II 15 III <i>Er</i> , Ti II 15 III <i>Er</i> , Ti II 12 I	$\begin{array}{c} 30907,726\\ 30956,623\\ 31019,583\\ 31075,376\\ 31102,603 \end{array}$	$\begin{array}{c} a^{4}\mathrm{F}_{5}-a^{4}\mathrm{F}'_{5}\\ a^{2}\mathrm{G}'_{4}-b^{2}\mathrm{F}'_{4}\\ a^{4}\mathrm{F}_{3}-a^{4}\mathrm{F}'_{4}\\ a^{4}\mathrm{F}_{4}-a^{4}\mathrm{F}'_{5}\\ a^{3}\mathrm{F}_{4}-d^{3}\mathrm{G}_{4} \end{array}$	+002
$\begin{array}{c} 3202,\ 535\\ 3199,\ 915\\ 3191,\ 994\\ 3190,\ 801\\ 3186,\ 451 \end{array}$	$9 \\ 10 \\ 9 \\ 4 \\ 10$	A B A D A	12 V Er, Ti II 100R II 80R II 20 IV Er, Ti II 60r II	$\begin{array}{c} 31216,276\\ 31241,828\\ 31319,353\\ 31331,070\\ 31373,839 \end{array}$	$a^{2}D'_{2}-b^{2}F'_{3}$ $a^{3}F_{4}-d^{3}G_{5}$ $a^{3}F_{3}-d^{3}G_{4}$ $a^{2}D'_{3}-b^{2}F'_{4}$ $a^{3}F_{2}-d^{3}G_{3}$	$000 \\ 000 \\ +002$
$\begin{array}{c} 3168.\ 519\\ 3161.\ 755\\ 3148.\ 033\\ 3130.\ 804\\ 3088.\ 027 \end{array}$	$     \begin{array}{c}       10 \\       6 \\       2 \\       3 \\       10     \end{array} $	A D D A	30 III Eru, Ti II 20 III Eru, Ti II 12 IV E, Ti II 15 IV, Ti II 60 III Er, Ti II	$\begin{array}{c} 31551,385\\ 31618,884\\ 31756,698\\ 31931,457\\ 32373,764 \end{array}$	$b^4{ m F}_5-a^4{ m D}_4\ b^4{ m F}^3-a^4{ m D}_2\ a^4{ m F}_2-a^2{ m D}_2\ a^4{ m F}_3-a^2{ m D}_3\ a^4{ m F}_5-a^4{ m D}_4$	
$\begin{array}{c} 3078.\ 645\\ 3075.\ 225\\ 2956.\ 133\\ 2948.\ 255\\ 2941.\ 995 \end{array}$	10 10 7 8 7	A C C A C	45 III <i>Er</i> , Ti II 40 III <i>Er</i> , Ti II 70 <i>R</i> II 607 II 607 II	$\begin{array}{c} 32472,424\\ 32508,527\\ 33818,127\\ 33908,489\\ 33980,630\\ \end{array}$	$\begin{array}{c} a^{4}\mathrm{F}_{4} - a^{4}\mathrm{D}_{3} \\ a^{4}\mathrm{F}_{3} - a^{4}\mathrm{D}_{2} \\ a^{3}\mathrm{F}_{4} - f^{3}\mathrm{F}'_{4} \\ a^{3}\mathrm{F}_{3} - f^{3}\mathrm{F}'_{3} \\ a^{3}\mathrm{F}_{2} - f^{3}\mathrm{F}'_{2} \end{array}$	$000 \\ 000 \\ +004$

# 2. COMPARISON WITH OTHER OBSERVATIONS

Two other observers have measured wave lengths in the vacuum arc spectrum of titanium. In 1922 Brown <sup>13</sup> published a list of more than 100 wave lengths between 4263 and 6261 A determined by interference methods in terms of the primary standard-the red ray of cadmium. This was followed two years later by a more extensive list by Crew.<sup>14</sup> who observed the region from 3653 to 6366 A with a plane grating giving high dispersion. There is most excellent agreement between the Bureau of Standards wave lengths and those of Brown in the interval from 4262 to 5200 A. Most of the differences, Bureau of Standards minus Brown, are less than 0.003 A and exhibit no systematic shift between the two sets of results, the mean of the differences being +0.0001 A. Between 5200 and 5800 A Brown's list contains 13 Ti lines, of which 11 may be compared with the Bureau of Standards determinations. Of these, there are two positive differences, three zeros, and six negative differences. the mean value of Bureau of Standards minus Brown being -0.001 A. From 5800 to the end of Brown's list, his wave lengths are systematically longer than the Bureau of Standards values, the difference increasing from -0.001 A at 5800 A to -0.004 A at 5260 A.

The comparison of the Bureau of Standards wave lengths with Crew's is limited to the region 3653 to 4263 A, his wave lengths longer than 4263 A being based on those of Brown described above. The differences, Bureau of Standards *minus* Crew, change linearly from -0.005 A at 3653 to +0.002 A at 3800 A, being zero at 3750 A. From 3800 to 4000 A the difference is practically constant, amounting to +0.002 A. At 4000 A there is an abrupt increase in the difference to +0.010 A from which it decreases linearly to -0.010 A at 4263 A, being zero in the vicinity of 4130 A.

# 3. COMPUTATION OF WAVE LENGTHS FROM SPECTRAL TERMS

Classification of the lines of a spectrum as the difference of two spectral terms permits a calculation of the wave lengths of the lines if the term values are known. In recent years rapid progress has been made in the extension of our knowledge of the structure of spectra not only of neutral atoms which emit arc spectra, but also of ionized atoms which emit the various stages or orders of spark spectra. Such analyses of the spectrum of titanium have been made by Kiess and Kiess<sup>15</sup> and by Russell.<sup>16</sup> From the work of these

<sup>13</sup> Astrophys. J., 56, p. 53; 1922.

<sup>14</sup> Astrophys. J., 60, p. 108; 1924.

<sup>15</sup> J. Opt. Soc. Am. and Rev. Sci. Inst., 8, p. 607; 1924.

<sup>16</sup> Astrophys. J. 66, pp. 283 and 347; 1927.

investigators have been taken the term combinations or series classifications of the lines given in column 6 of Table 1. The numerical values of the term combinations are the wave numbers in vacuum of the lines as entered in column 5.

If the terms involved in the production of the spectrum can be determined solely from lines measured in the yellow and red-that is, in the vicinity of the neon standards—then it is possible to calculate from them the wave lengths of lines in the blue and violet and thereby check the accuracy of observations remote from the standards. Such an ideal procedure, however, is not entirely possible in the case of titanium owing to the low intensities and consequent paucity of the longer Ti lines in the vacuum arc. An alternative procedure for testing the scale of a wave-length interval by means of cyclical term combinations, such as carried out by Meggers <sup>17</sup> for the iron spectrum, was likewise not feasible for Ti because of the small number of cycles which could be formed from the wave lengths of Table 1. It was, therefore, decided to set up a system of terms based not only on the longer wave lengths of the table, but also on the relative term separations as given by observations throughout the measured wave-length interval. The degree of the constancy of these term separations is exhibited in Table 2, wherein are collected various differences used in calculating the relative values of the low terms.

$a^{3}\mathrm{F}_{4}-a^{3}\mathrm{F}_{3}$	$\begin{vmatrix} a^3\mathbf{F}_3-a^3\mathbf{F}_2 \end{vmatrix}$	a3F4-b3F4	$a^3\mathrm{F}_3-b^3\mathrm{F}_2$	$a^3\mathrm{F}_2$ - $b^3\mathrm{F}_2$	$a^{3}\mathrm{F}_{4}-a^{3}\mathrm{P}_{2}$	$a^{3}F_{3}-a^{3}P_{1}$	$a^3\mathbf{F}_2-a^3\mathbf{P}_0$
$216.722 \\ .726 \\ .755 \\ .752 \\ .744 \\ .742 \\ .741 \\ .749 \\ .735$	$170.122 \\ .129 \\ .129 \\ .127 \\ .106 \\ .133 \\ .150 \\ .133 \\ .151$	11389.934.960.955.952.940.947.940	11469. 688 672 686 701 693 . 688	11531. 789 . 786 . 800	8215. 486 . 488 . 467	8322. 307 . 310	8436. 646 . 597
216. 741	. 140	11389. 947	11469. 688	11531.792	8215. 480	8322. 308	8436. 622

TABLE 2.—Constancy of term differences throughout the spectrum

The mean values of the term differences of Table 2 were used in deriving the values of the terms  $a^3F$ ,  $b^3F$ , and  $a^3P$  of Table 3. From these the remainder of Table 3 was calculated by the joint use of wave numbers shorter than 21,300.000 from Table 1 and relative term separations similar to those of Table 2. Although many of the well-observed lines of Table 1 belong to the singlet and quintet systems of Ti I, yet it was not possible to derive good term values for these systems by adhering to the limitations set for the derivation of the triplet system terms. The wave numbers calculated from

17 Astrophys. J., 60, p. 60 1924.

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these terms were converted into wave lengths which were compared with the observed values of Table 1. The results of the comparison are shown in the last column of Table 1, where the residuals O-Care entered. The algebraic sum of the differences O-C for the interval 4700-2941 A is practically zero, although negative residuals predominate in the region 4700-3700 A, and positive residuals in the region 3700-2941 A. However, since the wave lengths would require, in each of these regions, a mean correction of less than 0.001 A to reduce the sums of the residuals to zero, the representation of the wave lengths by means of the terms of Table 3 is regarded as satisfactory and is interpreted as indicating that the blue and violet lines have been measured to the same scale as those longer than 4700 A. For lines longer than 4700 A the majority of the residuals are necessarily zero, since the lines were used directly in the computation of the terms. With one exception the residuals greater than 0.002 A in this region refer to lines observed only a few times.

		and the second se		and the second second		and the second second			
a3F.	386 873	a <sup>3</sup> Da	20126 072	a3F'	19573 980	a3G.	91730 743	a3H'a	32013 555
u° 1 4	216.741	u-D3	120.023	U-1 4	152.400	4-45	151.223	u.11 0	99.251
$a^3F_3$	170. 132	$a^{3}D_{2}$	20006.049	a3F'3	19421. 580	a3G4	21588. 520	a3H'5	31914. 304
	170.132		68.171	1	98.011		118.986		84.288
$a^3 F_2$	0.000	$a^3D_1$	19937.878	a <sup>3</sup> F'2	19323.003	a <sup>3</sup> G <sub>3</sub>	21469. 534	a <sup>3</sup> H' <sub>3</sub>	31830.016
<b>b</b> <sup>3</sup> <b>F</b> <sub>4</sub>	11776.820	$b^3D_3$	25643. 724	b3F'4	25388. 345	b3G5	27750.156	b3H'6	35685. 188
	137.000		204.794		161.109		135.463		125.526
3F2	11639, 820	b3D2	25438, 930	b3F'2	25227. 236	1 b3G4	27614, 693	1 3H's	35559, 662
	108.008		121.088		119.783		115,660		105.563
3F2	11531, 812	3D1	25317.842	b3F'2	25107.453	b3Ga	27499, 033	1 3H'4	35454,099
				1.1.1.1.1.1					
$a^{3}P_{2}$	8602.353	$c^{3}D_{3}$	27480.077	d3F'4	27025.667	c3G5	30039. 246	121233	Sec. 2
	109.8 6		62.040		132.721		68.140	1.000	
a3P1	8492. 4: /	$c^{3}D_{2}$	27418.037	d3F'3	26892.946	c3G4	29971.106		
1 San Trais	55.807	1000	62.972	Con take	89.484		56.333	1 States	Carles Carlo
a <sup>3</sup> Po	8436.630	$c^{3}D_{1}$	27355.065	d3F'2	26803. 462	c3G3	29914.773	and the	
		10000		CONTRACTOR OF				1999	
a3G'5	15220.400	$c^{3}D_{3}$	29912.292	e3F4	33700.897	d3G5	31628.698		
	63.597		143.606	1.4.1	20.735		139.212	A States	
$a^3G'_4$	15156.803	e3D2	29768.686	e3F'3	33680.162	$d^3G_4$	31489.486	1.000	
	48.650	1200	107.414	1	24.264	Children and	115.624	1 1 1 1 1 1 1	101101010
a3G'3	15108.153	$e^{3}D_{1}$	29661. 272	e3F'2	33655. 898	d3G3	31373.862	A STATE STATE	
						1. 1. 1. 1. 1. 1. 1. 1. 1. 1. 1. 1. 1. 1		1	
$a^{3}H_{6}$	18192.594	$f^3D_3$	31206.014	f3F4	34205.001			los antes	
	51.342		15.351	1.5.5.50	126.389			1.2.1.2.1.1	
a3H5	18141.252	$f^3D_2$	31190.663	f3F'3	34078.612			1	
			6.574		97.927			1.50.50	Constant and the second
a <sup>3</sup> H <sub>4</sub>	Carl States	$f^3D_1$	31184.089	f3F'2	33980. 685				

TABLE	3.	-T	erms	in	the	triplet	system	of	titanium
								-1	

## IV. RESULTS FOR OTHER ELEMENTS

In Tables 4, 5, and 6 which follow are given the vacuum arc wave lengths of a few lines of elements which appeared as impurities in the titanium or were especially observed to supply additional data for the solar work. The most abundant impurity in the titanium was iron; in lesser amounts were calcium, aluminum, chromium, vanadium, and sodium. The elements especially observed for wave lengths in the yellow and red were calcium, barium, manganese, and nickel, the observations being made at the same time as the first series of titanium. Owing to the fact that a copper rod was used nearly always for the negative electrode, 26 lines of this element were also measured on the spectrograms of all three series and are given below.

λΙ.Α	Num- ber of obser- vations	Weight	Intensity, tem- perature, and pressure classes	Bureau of Stand- ards <i>minus</i> Bab- cock	λΙ.Α	Num- ber of obser- vations	Weight	Intensity, tem- perature, and pressure classes	Bureau of Stand- ards <i>minus</i> Bab- cock
$\begin{array}{c} 5371.\ 488\\ 5328.\ 044\\ 5269.\ 539\\ 4415.\ 123\\ 4383.\ 545\end{array}$	$5 \\ 10 \\ 13 \\ 6 \\ 25$	D A A A A		$ \begin{array}{c c} -005 \\ +002 \\ -002 \\ -002 \\ -003 \end{array} $	3799. 554 3795. 005 3767. 193 3763. 791 3758. 237 3749. 488		C C A C C	$\begin{array}{cccccccc} 50 & \text{II} & & \\ 60 & \text{II} & b \\ 80r & \text{II} & b \\ 100r & \text{II} & b \\ 150R & \text{II} & b \\ 200R & \text{II} & b \end{array}$	+005 +001 000 000 +003 +001
4271. 762 4260. 476 4250. 789 4235. 937 4202. 030 4143. 869	$22 \\ 12 \\ 9 \\ 6 \\ 10 \\ 7$	A B A D A B	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	$ \begin{bmatrix} -002 \\ -004 \\ -001 \\ -005 \\ -002 \\ -002 \end{bmatrix} $	3748. 264 3745. 560 3737. 132 3734. 865 3733. 320 3727. 621	8 14 13 17 11	B A B B B B B	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	000 -002 +002 -000
4132. 060 4071. 740 4045. 813 4005. 244 3930. 294	$     \begin{array}{c}       11 \\       22 \\       27 \\       4 \\       2     \end{array} $	B A C C	$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	$ \begin{array}{c c} -001 \\ -001 \\ -001 \\ 000 \\ -004 \end{array} $	3719. 934 3709. 256 3705. 566 3687. 454 3679. 915	13 8 13 12 14	B C A B A	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	$\begin{array}{c} -003 \\ +008 \\ -001 \\ -005 \\ 000 \end{array}$
3927. 919 3922. 914 3920. 261 3899. 712 3886. 281	$ \begin{array}{c}     14 \\     5 \\     5 \\     3 \\     24 \end{array} $	A C D D B	$\begin{vmatrix} 30R & IB & a \\ 25R & IB & a \\ 20r & IB & a \\ 30R & IB & a \end{vmatrix}$	$ \begin{array}{c c} -002 \\ +001 \\ +002 \\ +004 \\ -003 \end{array} $	$\begin{array}{c} 3647.\ 844\\ 3631.\ 465\\ 3618.\ 769\\ 3608.\ 861 \end{array}$	$\begin{array}{c}14\\14\\14\\8\end{array}$	A A B	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	$+001 \\ 000 \\ 000 \\ -001$
3859. 905 3856. 377 3834. 221 3827. 821	8 2 12 2	C C A C	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	$+004 \\ -003 \\ -003$	3581, 194 3570, 099 3565, 380 3558, 517	$12 \\ 11 \\ 12 \\ 11 \\ 11$	A B B B	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	-002 -001
$\begin{array}{c} 3825.\ 881\\ 3824.\ 447\\ 3820.\ 428\\ 3815.\ 844\\ 3806.\ 711 \end{array}$	$     \begin{array}{c}       4 \\       3 \\       20 \\       21 \\       2     \end{array} $	B C A D	200R         II         b           50r         IA           250R         II           100r         II           10         III	$\begin{array}{c c} -003 \\ +002 \\ 000 \\ +002 \\ +013 \end{array}$	3497.844 3465.862 3440.990 3020.635	$\begin{array}{c} 4\\11\\12\\6\end{array}$	C B C D	$\begin{array}{cccc} 40 & I \\ 60r & I \\ 75R & I \\ 200R & I \end{array}$	$+001 \\ 000$

TABLE 4.—Vacuum arc wave lengths of iron

TABLE 5.—Vacuum arc wave lengths of copper

λ I. A.	Num- ber of	Weight	t Inten- sities	Bureau of Standards minus Wolf- sohn		λ I. A.	Num- ber of obser-	Weight	Inten-	Burea Stand <i>minus</i> sob	au of ards Wolf- in
	vations			Vac- uum	Air	e setterin Lei pur M	vations			Vac- uum	Bureau of Standards tinus Wolf- sohn 7ac- um -017 -005 -018 -005 -016 -002 -018 -005 -016 -002 -013 -006 -013 -006 -013 -006
5782. 132* 5700. 239* 5292. 519 5220. 070*	$31 \\ 23 \\ 9 \\ 13$	A A C A	8r 8r 6 6	-004	-008	3530. 382 3337. 845 3279. 815 3273. 956*	9 10 10 7	B A B A	7 8 5 10 <i>R</i>	-017	005 005
5218. 202	27	Â	10	-031	000	3247 540*	8	B	102	-016	-002
5153. 237* 5105. 542 4704. 593 4651 124	27 23 6	A A D B	8 7 4 8	$-035 \\ -017 \\ -025$	$+004 \\ -009$	$\begin{array}{c} 3208.\ 230\\ 3194.\ 096\\ 3063.\ 411 \end{array}$	8 8 10	B B A	6 8 7	$-020 \\ -018 \\ -015$	-010 -008
4530. 786*	11	A	6	-009		3036.101 3010.838	10 10	BA	87	$-013 \\ -013$	$-006 \\ -007$
4509. 374 4480. 360* 4062. 639 4022. 627	10 6 8 11	B C C A	6 7 10 10	$-015 \\ -004$	-013	2961. 164 2824. 369	4 4	D B	9 10	$-015 \\ -013$	-009

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				and the second second					
λΙ.Α.	Number of observations	Weight	Intensity	Tempera- ture class	λΙ. Λ.	Number of observations	Weight	Intensity	Tempera- ture class
SODIUM					MANGANESE			1.20	
5895. 927 5889. 954 ALUMINUM	5 8	A A	8 <i>R</i> 10 <i>R</i>		$\begin{array}{c} 6021.\ 798\\ 6016.\ 639\\ 6013.\ 490 \end{array}$	$\begin{array}{c} 12\\9\\4 \end{array}$	A A B	50 40 30	III III III
3961, 527 3944, 009 CALCIUM	6 6	B B	10 <i>R</i> 10 <i>R</i>		NICKEL 6767.778 6643.641 6314.666 6956.965	10 10 10	A A A	20 20 15	I I II I
$\begin{array}{c} 6499.\ 651\\ 6493.\ 780\\ 6471.\ 661\\ 6462.\ 565\\ 6449.\ 809 \end{array}$	3 8 4 7 7	C A B A A	$30 \\ 80 \\ 40 \\ 125 \\ 50$	II II II II II	6256, 565 6176, 813 6108, 121 5892, 878	6 6 6	A A A	12 8 12	V II II
$\begin{array}{c} 6439.\ 073\\ 6169.\ 554\\ 6169.\ 048\\ 6162.\ 173\\ 6122.\ 217\end{array}$	7 3 4 7 8	A B C A A	$150 \\ 40 \\ 25 \\ 150 \\ 100$	II III III II II	6595. 328 6527. 314 6498. 762 6496. 901 6482. 912	4 $5$ $6$ $6$ $3$	A A A B	200 250 300r 600r 200	I I III III III
$\begin{array}{c} 6102.\ 720\\ 5857.\ 451\\ 4226.\ 728\\ 3968.\ 469\\ 3933.\ 669 \end{array}$	$     \begin{array}{c}       7 \\       6 \\       3 \\       12 \\       4     \end{array} $	A C A C	80 100 500 <i>R</i> 350 <i>R</i> 400 <i>R</i>	II III II II II	$\begin{array}{c} 6450.\ 854\\ 6341.\ 683\\ 6141.\ 716\\ 6110.\ 785\\ 6063.\ 118 \end{array}$	33553 3553	A A A A	125 150 600r 300r 200	I I III II II
VANADIUM 4379. 234 CHROMIUM	7	в	150r	п	6019. 474 5997. 091 5971. 701 5853. 679	$2 \\ 3 \\ 3 \\ 4$	C A A A	100 100 100 200	II II II III
4254. 337 3593. 488 3578. 687	19 12 11	A B B	$500 R \\ 160 R \\ 200 R$	II II II					

TABLE 6.-Vacuum arc wave lengths of Na, Al, Ca, V, Cr, Mn, Ni, and Ba

### 1. IRON

The iron lines whose wave lengths are given in the first column of Table 4 all originate in the lowest or the low metastable states of the iron atom. They are, accordingly, easily excited and appear with great intensity. In arcs in air most of them are reversed. The character of the lines in arcs in air and their behavior in the vacuum furnace are described in columns 4 and 5, the data for which are taken from King.<sup>18</sup> In the vacuum arc, however, these lines become narrow and give sharp interference fringes with high orders, a phenomenon pointed out long ago by Fabry and Buisson.<sup>19</sup> With two exceptions these lines belong to pressure classes a and b which means that they experience the least displacement with increasing pressure. We should, therefore, expect to find very little difference between their wave lengths in vacuum and in air, the amount of the displacement increasing with wave length. Such, indeed, is the case. Quite

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<sup>&</sup>lt;sup>18</sup> Astrophys. J., 37, p. 239; 1913; 56, p. 318; 1922.

<sup>19</sup> J. de Physique (IV), 9, p. 947; 1910.

recently Babcock <sup>20</sup> has published interferometer measurements of iron wave lengths emitted by arcs in air. The comparison of the Bureau of Standards values with his is shown in the last column of Table 4. In the ultra-violet—that is, the region of wave lengths shorter than 3922 A—the residuals, Bureau of Standards *minus* Babcock, are about equally distributed among positive and negative values, being in the mean +0.0007 A. But for all lines longer than 3922 A the residuals, Bureau of Standards *minus* Babcock, are negative, with one exception, the mean being -0.002 A.

### 2. COPPER

The copper lines which were measured are listed in Table 5. Of these, the pair at 5700 and 5782 A in the yellow, and the raies ultimes, 3247 and 3274 A, always appeared reversed. The intensities assigned to the lines are taken from Kayser's Tabelle der Hauptlinien. Four pairs of lines in this table, marked with an asterisk (\*), involve the term <sup>2</sup>P<sub>1, 2</sub> as may be seen by reference to Shenstone's <sup>21</sup> classification of the Cu arc spectrum. They may, therefore, be used to determine the separation of the components of this term, and thereby check the relative accuracy of the measurements. The four values of <sup>2</sup>P<sub>2</sub>-<sup>2</sup>P<sub>1</sub> are: 248.392, 248.377, 248.335, and 248.364. The low value of the third is accounted for by the fact that the wave length 4480.360 A which enters into its determination is affected by the Ti line at 4480.60. A correction of -0.009 A applied to the tabulated wave length would give a value of  ${}^{2}P_{2} - {}^{2}P_{1}$  equal to the mean of the other three determinations.

The vacuum arc spectrum of Cu has been measured recently by Wolfsohn<sup>22</sup> who photographed it in juxtaposition with the spectrum of the arc in air, using the high dispersion afforded by the grating spectrograph at Bonn. His vacuum values are systematically larger than his air values which he interprets as a pressure shift toward the violet for lines emitted by the arc in air. A comparison of the Bureau of Standards wave lengths with Wolfsohn's is given in the last two columns of Table 5, which shows that his conclusions concerning the pressure shift toward the violet are not verified. In fact, assuming the correctness of his arc-in-air measurements the residuals, Bureau of Standards minus Wolfsohn, indicate for copper the same type of pressure shift as has been found for all other spectra which have been investigated.

- <sup>21</sup> Phys. Rev., 28, p. 449; 1926.
- <sup>22</sup> Annalen der Physik (IV), 80, p. 415; 1926.

<sup>&</sup>lt;sup>20</sup> Astrophys. J. 66, p. 256; 1927.

## 3. Na, Al, Ca, V, Cr, Mn, Ni, Ba

In Table 6 are listed some wave lengths of Na, Al, Ca, V, Cr, Mn, Ni, and Ba. Some of these elements, as stated above, occurred as impurities in the electrodes. Ca, Mn, Ni, and Ba were especially investigated to furnish additional standards in the red for comparison with the solar wave lengths. The intensities and temperature classes given for each line are those assigned by King, except for Na, and Al, for which the estimates given by Kayser<sup>23</sup> are quoted. The impurity lines are in all cases either the *raies ultimes* or persistent lines of the corresponding elements, and all appear among the Fraunhofer lines of the sun's spectrum.

# V. ACKNOWLEDGMENTS

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<sup>23</sup> Kayser, Tabelle der Hauptlinien. Julius Springer, Berlin, 1926.