# Heat Capacity of Gaseous Carbon Dioxide<sup>1</sup>

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The heat capacity  $(C_p)$  of gaseous carbon dioxide has been measured at  $-30^\circ$ ,  $0^\circ$ ,  $+50^\circ$ , and  $+90^\circ$  C and at 0.5-, 1.0-, and 1.5-atmosphere pressure, with an accuracy of 0.1 percent. The flow calorimeter used was a modification of the one previously described by Scott and Mellors [1]<sup>2</sup> and Wacker, Cheney, and Scott [2]. In order to test the accuracy of the calorimeter, the heat capacity of oxygen was measured at 1 atmosphere at  $-30^\circ$ ,  $0^\circ$ , and  $+50^\circ$ C. The measured values of  $C_p$  for oxygen were combined with an equation of state to give  $C_p^\circ$ ; these differed from the statistically calculated values by +0.03, -0.06 and -0.01 percent at the three temperatures.

The experimental values of  $C_p$  for carbon dioxide have been used to calculate new values of  $C_p^{\circ}$  and values of the pressure coefficient of heat capacity at the four temperatures of measurement. The theoretical values of  $C_p^{\circ}$  calculated in 1949 [8] were found to be too low by 0.2 to 0.3 percent; the results of a new calculation are in substantial agreement with the experiments. The pressure coefficients are in agreement with those obtained from the recent pressure-volume-temperature work of MacCormack and Schneider [7].

# 1. Introduction

The large number of experimental values of the specific heat of carbon dioxide reported in the literature are in serious disagreement with each other. Leduc, for the International Critical Tables [3], attempted to evaluate and correlate all of the work, both experimental and theoretical, up to 1929. It is now thought that these ICT values are in considerable error. There have been two calorimetric measurements of the heat capacity since that time [4, 5]. There have also been at least two good sets of pressure-volume-temperature measurements [6, 7] and two calculations of the ideal gas heat capacity from spectroscopic data [8, 9]. There have been several compilations, based almost entirely on the combination of equations of state with spectroscopic values of  $C_p^{\circ}$  [10 to 13]. Values from several sources of the heat capacity in dimensionless units,  $C_p/R$ , at 1 atmosphere and 0° C, are given here.

| Partington and Schilling, 1924 [14]  | 4. 40  |
|--------------------------------------|--------|
| Leduc, ICT 1929 [3]                  | 4.37   |
| Eucken and v. Lude, 1929 [4]         | 4.348  |
| Sweigert, Weber and Allen, 1946 [10] | 4. 487 |
| NBS-NACA Table 13.24, 1949 [12]      | 4.396  |
| MacCormack and Schneider, 1950 [13]  | 4.363  |

The present investigation was undertaken because of the impossibility of deciding which values to choose and because of the reluctance, on the part of some users of thermodynamic tables, to accept statistically calculated values without supporting experimental evidence.

Oxygen was chosen as a substance to test the accuracy of the apparatus, because its heat capacity is well known and because a pure sample is rather easily prepared.

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# 2. Materials

The oxygen was prepared by heating potassium permanganate as described by Scott [15] and by Hoge [16]. This is a method that has been shown to produce very pure oxygen. The vapor pressure of the sample at the temperature of boiling nitrogen was found to agree with the value calculated from Hoge's data [16]. During the course of the last series of measurements (those at  $-30^{\circ}$  C), a small air leak in the apparatus was suspected. As soon as the measurements were completed, a portion of the sample was dissolved in alkaline pyrogallol to determine the purity; the amount of residual gas was 0.2 percent, and it was assumed to be nitrogen from air that had leaked in.

Carbon dioxide was purified from commercial gas that had been made from limestone. A large cylinder containing 20 lb of carbon dioxide was opened and the gas allowed to escape until less than half of the contents remained. Several hundred grams were then transferred to a small evacuated cylinder, which was then attached to a purification train. The sample was slowly sublimed from the cylinder and condensed in a glass trap at liquid  $N_2$ temperature, while a high vacuum was maintained by pumping on the trap. Transfer to the final receiver was also accomplished by sublimation and condensation. About 600 g were prepared in this way. The sample was tested several times for permanent gases by dissolving portions in concentrated potassium hydroxide and observing the volumes of residual gas. These were always less than 0.01 percent of the volume of the sample. A test performed by E. R. Weaver showed less than 0.001 percent of moisture.

#### 3. Apparatus

The adiabatic flow calorimeter used in this work was a modification of one that was shown by Wacker, Cheney, and Scott [2] to give heat capacities reliable to better than 0.1 percent. The principal modifi-

<sup>&</sup>lt;sup>1</sup> This work was financed in part by the National Advisory Committee for Aeronautics. <sup>2</sup> Figures in brackets indicate the literature references at the end of this paper.

cation was the substitution of two resistance thermometers of nickel wire for the thermocouple previously used for measuring the rise in temperature of the heated gas. The main advantage of this substitution was that the thermometers could be calibrated in place at any time. A further advantage was that it could be demonstrated by the readings of the lower thermometer that the gas entering the calorimeter always reached the temperature of the bath, and that there was negligible heat leak "upstream" from the hot calorimeter to the incoming cold gas.

The flow calorimeter, as it was used, is shown in figure 1. Most of the essential features are as described by Scott, et al. [1, 2], but so many changes have been introduced that a brief description of the entire apparatus appears desirable.



FIGURE 1. Scale drawing of flow calorimeter.

A, Liquid nitrogen; B, constant-temperature bath; C, protecting cylinder; CR, copper rod; F<sub>1</sub> and F<sub>2</sub>, flanges; Fl, felt insulation; H<sub>b</sub>, bath heater; H<sub>s</sub>, calorimeter heater; H<sub>s</sub>, shield heater; H<sub>t</sub>, tube heater; I, inlet; J, bellows seal; M, mica spacer; MAN, manometer tubes; N<sub>1</sub> and N<sub>2</sub>, nickel thermometers; O, outlet; P, propeller; R, bath-control thermometer; S, radiation shield; T<sub>1</sub>, stirrer tube; T<sub>2</sub>, heilca tube; TC, tube thermel; TC, shield thermel; Th, metal thimble; V, throttle valve; VAC, vacuum line; W, wax seal; X, vanes.

#### 3.1. Constant-Temperature Bath

The calorimeter is immersed in the bath, B, the temperature of which was controlled by supplying electric power to the heater,  $H_b$ . The stirring propeller, P, forced liquid down the brass tube,  $T_1$ , and over the copper resistance thermometer, R, which consisted of about 140 ohms of No. 37 AWG wire and which formed one arm of a Wheatstone bridge. An unbalance in the bridge circuit of 1 µv corresponded approximately to 0.001 deg K. The circuit was ordinarily attached to the galvanometer in a Rubicon phototube amplifier, the output of which was fed to a proportionating heat-control amplifier developed by the Electronic Instrumentation Section of the Bureau. This arrangement gave automatic control of the bath temperature within 0.002 deg, provided there were no large disturbances. The copper thermometer bridge could be switched from the controlling galvanometer to a sensitive wall galvanometer for manual control, or the two galvanometers could be placed in series for momentary observation of the efficiency of control.

When controlling the bath below room temperature, refrigeration was required, and this was provided by the apparatus shown at the left of figure 1. A solid copper rod, CR, with copper vanes, X, at one end and a copper cylinder at the other was immersed in liquid nitrogen, A. The metal tube, C, closed at the bottom end made the rate of heat transfer almost independent of the depth of the nitrogen in the dewar.

The bath liquid was a special light machine oil for temperatures above that of the room and an equivolume mixture of chloroform and carbon tetrachloride for temperatures below that of the room.

#### 3.2 Flow Control

The source of gas flowing into the calorimeter is not shown in figure 1. For oxygen, this was a cylindrical brass boiler with heavy-copper vanes, wound with a heater and immersed in a cold dewar. The rate of flow was controlled by the power supplied to the heater on the boiler for evaporating the liquid oxygen. For carbon dioxide the boiler was replaced by a high-pressure system in which the carbon dioxide was contained in a steel cylinder immersed in melting ice. The pressure (34.38 atm) remained sufficiently constant for good flow control. The gas was admitted to the calorimeter, and its flow rate was controlled, by a very sensitive diaphragm valve. This valve was previously used by Osborne, Stimson, and Ginnings [17] for control of flow of highpressure water. A silver seat moving down against a stainless steel crater-rim cone with a very small opening provided the closing action.

Both the rate of flow and the mean pressure during an experiment were adjusted, controlled, and measured by following the readings of a three-column manometer, two columns of which were connected to the calorimeter as shown in figure 1, whereas the third was open to the atmosphere.

#### 3.3 Calorimeter and Shield

The gas being investigated entered at I and passed through the helical tube,  $T_2$ , where it was brought to the temperature of the bath. This tube passes into the vacuum jacket through the bellows joint, J, which was intended to prevent stresses caused by differential expansion.

The calorimeter, considered as the vertical tube between points J and O through which the gas flowed. was constructed of thin-walled seamless Monel tubing. The various pieces were soldered together as nearly coaxially as possible, and the whole length was supported only at the two ends, and at M by a mica spacer. The copper thimble, Th, was used to provide a surface of higher temperature to protect the incoming cold gas from radiation; it was thermally a part of the calorimeter. The latter, with the exception of the necessary lead wires, was completely isolated from contact with surroundings from points *M* to *O*. The thimble was gold-plated and polished; the Monel tubing was covered with thin aluminum foil, except for a short length that was highly polished The copper radiation shield, S, was gold-plated and polished on the inside, and covered with aluminum foil on the outside. It was supported and centered by string spacers.

The temperature of the gas entering the calorimeter was measured by the nickel resistance thermometer,  $N_1$ ; the gas passed over a system of baffles and went twice past the glass-silicone-insulated No.  $36 \,\mathrm{AWG}\,\mathrm{constantan}\,\mathrm{heater}, H_c.$  The direction of flow was again reversed, and another system of baffles was encountered in the region where the exit temperature was measured with the nickel resistance thermometer.  $N_2$ . Heat leak to the upper tube was opposed by supplying heat to a tube heater,  $H_t$ , so that zero temperature gradient was maintained as indicated by a null reading of the copper-constant n thermocouple,  $TC_1$ . Radiation to or from the outer surface of the calorimeter was reduced almost to zero by heating the shield with the heaters,  $H_s$ , which were so arranged that any desired proportion of the heat could be supplied to the top half of the shield. The three junctions of the chromel-constant an thermocouple,  $TC_2$ , could be read in summation or individually, and the attempt was made to keep all of the readings near zero. Heat transfer from the bath by gas conduction was eliminated by evacuating the brass jacket.

Leads were brought in through the wax seal, W, and were tempered nearly to bath temperature on the brass cylinder,  $F_1$ . Leads from the thermometer,  $N_1$ , were taken directly to the brass ring,  $F_2$ , and further tempered; all other leads were wound twice around the shield. All leads were of AWG No. 34 copper wire, silk-and-enamel insulated. All wires, whether heaters, thermometers, thermal junctions, or leads, were cemented to the metal surfaces with glyptal lacquer and afterward baked.

Each nickel thermometer consists of about 55 ohms of AWG No. 40 enameled nickel wire with four copper leads. The thermometers were calibrated by comparing with one or more platinum resistance thermometers suspended in the bath when helium was in the calorimeter jacket. It was found that the resistance of the nickel thermometers in use fluctuated slowly over a range corresponding to 3 or 4 mdeg during a period of 3 months. Consequently, spot checks of the calibration were made each day of heat-capacity measurements.

After leaving the calorimeter through the throttle valve, V, the gas went to one or the other of two receivers through a snap-throw valve, capable of changing the flow from one receiver to the other in less than 0.1 second. This valve in one of the two positions closed the clutch circuit of an interval timer that was driven by a special constant-frequency 60-cycle current, accurate to 0.02 second. This valve was the same one described by Wacker, Cheney, and Scott [2]. The receivers were kept at the temperature of liquid nitrogen.

A Leeds & Northrup G-2 Mueller bridge was used to measure resistances. The potential and current in the calorimeter heater were measured with a precision potentiometer, in conjunction with a calibrated standard resistor and a calibrated volt box. The circuits were essentially the same as those described by Scott, Meyers, Rands, Brickwedde, and Bekkedahl [18].

# 4. Method

The selection of the temperatures and pressures at which to measure the heat capacity of carbon dioxide was made to cover the working range of the calorimeter and obtain as many points as necessary. The usual assumption was made, that the error in an apparent heat capacity caused by heat leak would be inversely proportional to the flow rate. Consequently, at each temperature and pressure, a number of determinations were made over as wide a range of flow rates as was consistent with a reasonable time for measurement, with the size of sample, or with the capacity of the calorimeter.

The determinations of the heat capacity included the measurements necessary to obtain the three fundamental quantities: the mass rate of flow, F, of the gas through the calorimeter; the electric power, W, to the calorimeter heater; and the rise in temperature of the gas,  $\Delta T$ .

A heat-capacity experiment was begun by adjusting both the value, V, and the flow of gas to the calorimeter until the selected values for the mean pressure and pressure drop were obtained. Meanwhile, power was supplied to the heater and adjusted. Neither valve V nor the power supply were changed after the initial adjustment, all control being at the source of gas. Heat was also supplied to the shields. After a length of time that was inversely proportional to the rate of flow, a steady state was reached in which the heated portion of the calorimeter and the shield were at a constant temperature that was approximately 10 deg higher than the constant bath temperature. At this time the gas was directed by means of the snap-throw valve to the other (weighed) receiver, thus starting the measurement. Continuous measurements of the exit temperature  $(N_2)$  of the gas were made, and slight adjustments of the flow were made to keep that temperature constant within 0.03 deg. In addition to the measurements of the resistance of the thermometer,  $N_2$ , readings of current and potential of the heater, resistance of  $N_1$ and the bath thermometer, and heights of the three mercury columns were recorded as often as possible in connection with each run. When about the desired weight of sample had been collected and the temperature was nearly constant and the same as that at the start of the run, the experiment was terminated and the gas was redirected to the other container. The barometric pressure was also recorded, as well as the reading of the interval timer. The receiver was weighed on a large analytical balance, and the weight of sample was corrected for buoyancy.

"Blank" experiments were required in which the temperature drop,  $\delta T$ , in the calorimeter was measured when no heat was applied. This temperature drop is chiefly due to Joule-Thomson cooling, but heat leaks and responsiveness of the nickel thermometers to the gas temperature usually contribute. The blank experiments were made with the bath temperature approximately at the mean temperature of the corresponding heat-capacity measurements, and they were made at the same mean pressures and over the same range of pressure drops as the heat-capacity experiments. The values of  $\delta T/\Delta p$ were plotted as a function of  $\Delta p$  for each pressure vestigation are given in table 1. The experiments

and temperature for each gas. These graphs were used to obtain the quantity  $\delta T$  for each heat-capacity experiment. The value of  $\delta T$  varied from  $0.005^{\circ}$ to  $0.4^{\circ}$  in the extreme cases.

The apparent specific heat of the gas. C. at the mean temperature and pressure of the experiment was computed by the relation

$$C = \frac{WF^{-1}}{(\Delta T + \delta T)}.$$
 (1)

The mean temperature,  $T_m$ , of the experiment was calculated as the bath temperature plus  $\Delta T/2$ . The average pressure,  $p_m$ , in the region of the calorimeter between the thermometers  $N_1$  and  $N_2$  was calculated, from the corrected manometer and barometer readings, as equal to the pressure at the entrance to the calorimeter minus three-eighths of the measured pressure drop,  $\Delta p$ . A consideration of the geometry of the calorimeter had led the authors to the opinion that the factor three-eighths is near the truth and that any uncertainty in this factor will not affect the result by a significant amount.

# 5. Results

#### 5.1 Tests with Oxygen

All the heat-capacity data on oxygen from this in-

Blank correc-Correction for Reciprocal of rate, F-1 Pressure drop, Temperature Heat capacity,  $C^{a}$ Heat capacity,  $C_p$  (observed) Mass of Power, W tion,  $\delta T$ rise,  $\Delta T$  $T_m$  and  $p_m, \delta C$ sample. m  $\Delta p$ -30.00° C=243.16° K: 1.00 atm mm Hg  $jg^{-1} deg^{-1}$ 0.91489 .91487  $jg^{-1} deg^{-1} -0.00012$  $jg^{-1} deg^{-1}$  $\begin{array}{c} sec. \ g^{-1} \\ 11. \ 9673 \\ 20. \ 1028 \end{array}$ Watt  $^{\circ}K$  $^{\circ}K$  $\begin{array}{c} g \\ 70.\ 7703 \\ 49.\ 0120 \end{array}$ 9. 8817 10. 0141 0.0965 0. 91477 . 91481  $\begin{array}{c} 0.\ 762865 \\ .\ 457512 \end{array}$ 270.7 97.5 . 0382 -. 00006 24.256937.9589  $\begin{array}{c} 41.\ 3857\\ 26.\ 9976\end{array}$ 67.427.820.2381375 10.0837 0271 91488 -0000491484 9. 9815 . 0141 . 91435 . 91433 240804 -.0000244.7503 26.0441203395 9 9454 . 0096 91419 -.00004. 91415 0.91519 Extrapolated value.  $0.00^{\circ} \text{ C} = 273.16^{\circ} \text{ K}$ : 1.00 atm 9.59789.738110.17180.12220.91624 -0.00008 0.91616 11.1876 50.7721 0.796101357.4 . 1157 . 1117 . 1115 11.544011.825799. 1040 79. 9193 . 781965 . 796649 -. 00009 -. 00011 334.4 91606 . 91597 320. 9 91608 91597 62.858127.8317 11.8486 796698 320 0 10 1910 91632 -0001091622 . 420780 125.0 8,7491 . 0501 . 91646 -.00013 . 91633 19.1670  $114.\ 2\\73.\ 2\\36.\ 5\\33.\ 2$ 9.0000 0462 . 91639 -. 00004 91635 19.7966 68.4814 . 418768 24.988735.071533, 1234 344989 9 3736 0311 91655 +.0000291657 8.8815 9.4208 26. 4032 . 232535 . 91629 . 00000 91629 0177 28.423530.2936+.00002+.0000137.2491 232170 0173 91619 91621 192647 22. 2 9. 6852 . 91571 . 0155 . 91572 46.1153 0.91625Extrapolated value. 50.00° C=323.16° K: 1.00 atm  $297.8 \\ 284.7 \\ 78.1 \\ 43.3 \\ 6$ 0.0887 0.92317  $11.\,9923\\12,1609$  $\begin{array}{c} 111.\ 6318\\ 46.\ 5598 \end{array}$ 0.867217 11.1740 0 92337 -0.00020 . 866257 . 92282 . 0848 92305 -.0002311.3270 23.609131.992224.135223.467611.3069 -000180233 92272 . 279146 . 0129 92191 -.00002. 92189 9.6740 10.2656 41.8940 23.4888 226012 26.0 .0077 92152 -.00007. 92145 Extrapolated value ..... 0.92366

TABLE 1. Data on oxygen

a The values of C are corrected for 0.0035 g of oxygen left in the delivery tubes because of the vapor pressure of oxygen at the temperature of boiling nitrogen.

are listed in the order of decreasing flow rate at each temperature. The values of C, given in column 7, are calculated by means of eq 1. These are adjusted by the amounts given in column 8, to correct for the difference between  $T_m$  and the nominal temperature and between  $p_m$  and 1-atm pressure, and there are obtained the values of  $C_p$  (observed) in column 9. The values of  $C_p$  (observed) are plotted as a function of  $F^{-1}$ . The straight line drawn through the points was determined by the method of least squares, and the value of  $C_p$  is obtained as the intercept. One of these plots is shown in figure 2, to illustrate the precision obtained. The values of  $C_p$  obtained by this process are labeled "Extrapolated value" in column 9 of table 1. These values, converted to dimensionless form,  $C_p/R$ , are listed again in table 3 (a). There are also given the corrections to ideality calculated by the Beattie-Bridgeman equation [19], and the resulting values of  $C_p^o/R$ . These values are then compared with the values calculated by Woolley [20, 21] from the spectroscopic and molecular data.

#### 5.2 Heat Capacity of Carbon Dioxide

All of the heat-capacity data on carbon dioxide in this research are given in table 2. In addition, plots of all the experimental results at  $-30^{\circ}$  and  $+50^{\circ}$  C are furnished in figures 3 and 4 to show the typical appearance of these plots and to indicate the precision. The value of  $C_p$  (observed) for each point (col. 9), after adjusting for the differences between  $T_m$  and  $p_m$  and the nominal temperature and pressure (col. 8), is plotted against the reciprocal of flow rate (col. 1). The slopes and intercepts of the lines were first obtained by the method of least squares. As the heat leak, of which the slopes of these lines is a measure, would be expected to be independent of pressure, the three lines at each of the temperatures except 90° C were adjusted slightly to a constant average slope. A small but regular change of slope with pressure was noted at  $90^{\circ}$  C, and these lines were therefore unchanged from the least-square values. The intercepts of these lines are the desired values of  $C_p$  and are listed in column 9 of table 2 as the "Extrapolated value." In order to furnish an estimate of the precision of these values of  $C_{p}$ , they are followed in table 2 by values of  $\sigma$ , where  $\sigma$ 

is defined as  $\sqrt{\sum d^2/(n-1)}$ , and d is the deviation from

the extrapolated value of  $C_p$ , of each  $C_p$  (observed), after correcting for heat leak by use of the slope of the straight line previously found.

The values of  $C_p$  have been converted to dimensionless form and are given as  $C_p/R$  in table 3 (b). Although there are a number of experimental measurements at atmospheric pressure recorded in the literature, there is no interest other than historical in making comparisons with the very old work. Partington and Shilling [14], Leduc [3], and Quinn and Jones [22] have made studies that may be referred to. The most recent thermal measurements are those made by Kistiakowsky and Rice [5] by the isentropic expansion method. The values



FIGURE 2. Heat capacity of oxygen at  $-30^{\circ}$  C and 1 atmosphere.



FIGURE 3. Heat capacity of carbon dioxiae at  $-30^{\circ}$  C and three pressures.



FIGURE 4. Heat capacity of carbon dioxide at  $50^{\circ}$  C and three pressures.

TABLE 2. Data on carbon dioxide

|                                                                                                                                                                                         |                                                                                                                                                                                                                                           |                                                                                                                                                                                              |                                                                                                                                                                                 | a title data and a set of the set |                                                                                                                                  |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       |                                                                                                                                                                                                                                     |                                                                                                                                                                                            |
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| Reciprocal of rate, $F^{-1}$                                                                                                                                                            | Mass of sample, $m$                                                                                                                                                                                                                       | Power, W                                                                                                                                                                                     | Pressure drop, $\Delta p$                                                                                                                                                       | Temperature rise, $\Delta T$                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   | Blank correction, $\delta T$                                                                                                     | $\left \begin{array}{c} \text{Heat capacity,} \\ C \end{array}\right $                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                | Correction for $T_m$ and $p_m$ , $\delta C$                                                                                                                                                                                         | Heat capacity, $C_p$ (observed)                                                                                                                                                            |
|                                                                                                                                                                                         | 1 1                                                                                                                                                                                                                                       |                                                                                                                                                                                              | -30.0                                                                                                                                                                           | $0^{\circ}C = 243.16^{\circ}K; 1.$                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             | 50 atm                                                                                                                           | 1                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     | 1 1                                                                                                                                                                                                                                 | · · · · · · · · · · · · · · · · · · ·                                                                                                                                                      |
| $\begin{array}{c} sec \; g^{-1} \\ 8.\; 8629 \\ 18.\; 5247 \\ 19.\; 5828 \\ 35,\; 2678 \\ 45.\; 6761 \end{array}$                                                                       | $\begin{array}{c} g \\ 41, 3700 \\ 28, 5792 \\ 40, 5411 \\ 27, 3805 \\ 37, 3852 \end{array}$                                                                                                                                              | Watt<br>0.883700<br>.483207<br>.470045<br>.238232<br>.171032                                                                                                                                 | $\begin{array}{c} mm \ \mathrm{Hg} \\ 232. \ 0 \\ 54. \ 0 \\ 48. \ 5 \\ 15. \ 2 \\ 9. \ 0 \end{array}$                                                                          | $^{\circ} K$<br>9. 4287<br>11. 0151<br>11. 3377<br>10. 3897<br>9. 6685                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         | $^{\circ} K$<br>0. 2680<br>. 0740<br>. 0674<br>. 0230<br>. 0181                                                                  | $\begin{array}{c} jg^{-1} \ deg^{-1} \\ 0.\ 80772 \\ .\ 80721 \\ .\ 80708 \\ .\ 80689 \\ .\ 80648 \end{array}$                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        | $\begin{array}{c} jg^{-1} \ deg^{-1} \\ -0. \ 00044 \\ \ 00068 \\ \ 00080 \\ \ 00036 \\ \ 00006 \end{array}$                                                                                                                        | $jg^{-1} deg^{-1}$<br>0.80728<br>.80653<br>.80628<br>.80653<br>.80653<br>.80642                                                                                                            |
|                                                                                                                                                                                         |                                                                                                                                                                                                                                           |                                                                                                                                                                                              |                                                                                                                                                                                 |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                |                                                                                                                                  | Extrapo                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               | plated value                                                                                                                                                                                                                        | $0.80743 \pm 0.00040$                                                                                                                                                                      |
|                                                                                                                                                                                         | 1                                                                                                                                                                                                                                         |                                                                                                                                                                                              | 1                                                                                                                                                                               | 1.00 atm                                                                                                                                                                                                        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| $\begin{array}{c} 8.\ 7392\\ 8.\ 9149\\ 17.\ 9871\\ 33.\ 1864\\ 44.\ 9014 \end{array}$                                                                                                  | $\begin{array}{c} 90.\ 5234\\ 66.\ 0436\\ 34.\ 4809\\ 30.\ 2534\\ 27.\ 7185\end{array}$                                                                                                                                                   | $\begin{array}{c} 0.884995\\ .873842\\ .472673\\ .237875\\ .179918 \end{array}$                                                                                                              | 360.7<br>343.2<br>85.3<br>25.9<br>14.1                                                                                                                                          | $\begin{array}{c} 9.\ 2665\\ 9.\ 3580\\ 10.\ 5263\\ 9.\ 8478\\ 10.\ 0914 \end{array}$                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          | $\begin{array}{c} 0.\ 4018\\ .\ 3843\\ .\ 1148\\ .\ 0393\\ .\ 0353\end{array}$                                                   | $\begin{array}{c} 0.\ 79995\\ .\ 79963\\ .\ 79898\\ .\ 79844\\ .\ 79775 \end{array}$                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  | $\begin{array}{c} -0.\ 00056\\\ 00067\\\ 00064\\\ 00007\\\ 00025\end{array}$                                                                                                                                                        | $\begin{array}{c} 0.\ 79939\\ .\ 79836\\ .\ 79834\\ .\ 79837\\ .\ 79750 \end{array}$                                                                                                       |
| Extrapolated value $\sigma_{\sigma}$                                                                                                                                                    |                                                                                                                                                                                                                                           |                                                                                                                                                                                              |                                                                                                                                                                                 |                                                                                                                                                                                                                 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|                                                                                                                                                                                         |                                                                                                                                                                                                                                           |                                                                                                                                                                                              |                                                                                                                                                                                 | $0.50 \mathrm{~atm}$                                                                                                                                                                                            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| $\begin{array}{c} 17,2954\\ 17,4880\\ 30,0616\\ 45,2457 \end{array}$                                                                                                                    | $\begin{array}{c} 32.\ 0664\\ 33.\ 8616\\ 13.\ 5575\\ 26.\ 3510 \end{array}$                                                                                                                                                              | $\begin{array}{c} 0.\ 471766 \\ .\ 468653 \\ .\ 268526 \\ .\ 169161 \end{array}$                                                                                                             | $     191.2 \\     186.4 \\     63.9 \\     28.9   $                                                                                                                            | $\begin{array}{c} 10.\ 0748 \\ 10.\ 1265 \\ 10.\ 1155 \\ 9.\ 6347 \end{array}$                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 | $\begin{array}{c} 0.\ 2390 \\ .\ 2340 \\ .\ 0928 \\ .\ 0469 \end{array}$                                                         | 0. 79111<br>. 79107<br>. 79076<br>. 79055                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             | $\begin{array}{r} -0.\ 00044 \\\ 00049 \\\ 00014 \\ +.\ 00019 \end{array}$                                                                                                                                                          | 0. 79067<br>. 79058<br>. 79062<br>. 79074                                                                                                                                                  |
|                                                                                                                                                                                         |                                                                                                                                                                                                                                           |                                                                                                                                                                                              |                                                                                                                                                                                 |                                                                                                                                                                                                                 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                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               | plated value $\sigma_{}$                                                                                                                                                                                                            | $0.79162 \\ \pm 0.00049$                                                                                                                                                                   |
|                                                                                                                                                                                         |                                                                                                                                                                                                                                           |                                                                                                                                                                                              | 0.00°                                                                                                                                                                           | $C = 273.16^{\circ} \text{ K}; 1.5$                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      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                                                                                                                                                                                                                                      |                                                                                                                                                                                                                                     |                                                                                                                                                                                            |
| $\begin{array}{c} 9,3013\\ 9,3372\\ 9,3329\\ 9,5304\\ 18,0472\\ 18,4196\\ 18,5104\\ 18,5104\\ 19,0150\\ 27,9321\\ 33,2801\\ 33,2990\\ 36,3004\\ 36,9328\\ 44,0597\\ 52,5659\end{array}$ | $\begin{array}{c} 57.\ 1123\\ 55.\ 0724\\ 62.\ 0585\\ 53.\ 53.53\\ 31.\ 1528\\ 31.\ 9291\\ 70.\ 0752\\ 39.\ 8565\\ 52.\ 8550\\ 48.\ 1789\\ 35.\ 3785\\ 28.\ 2507\\ 20.\ 1507\\ 20.\ 1507\\ 26.\ 7567\\ 23.\ 7691\\ 29.\ 4592 \end{array}$ | $\begin{array}{c} 0.866418\\ .881983\\ .881983\\ .81506\\ .866533\\ .470372\\ .461507\\ .470610\\ .400423\\ .279317\\ .231057\\ .231259\\ .197887\\ .197941\\ .170483\\ .142725 \end{array}$ | $\begin{array}{c} 201.\ 4\\ 233.\ 6\\ 233.\ 4\\ 191.\ 6\\ 54.\ 1\\ 60.\ 9\\ 51.\ 5\\ 600.\ 6\\ 49.\ 4\\ 23.\ 0\\ 19.\ 3\\ 19.\ 4\\ 13.\ 9\\ 13.\ 6\\ 11.\ 0\\ 7.\ 0\end{array}$ | $\begin{array}{c} 9.\ 5445\\ 9.\ 6941\\ 9.\ 7189\\ 9.\ 7887\\ 9.\ 9729\\ 10.\ 3594\\ 10.\ 2334\\ 10.\ 4168\\ 9.\ 3786\\ 10.\ 4888\\ 9.\ 3786\\ 9.\ 2371\\ 9.\ 2458\\ 8.\ 6471\\ 8.\ 7985\\ 9.\ 0283\\ 9.\ 0379\end{array}$                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     | $\begin{array}{c ccccccccccccccccccccccccccccccccccc$                                                                            | $\begin{array}{c} 0.\ 83167\\ .\ 83207\\ .\ 83184\\ .\ 83191\\ .\ 83115\\ .\ 83145\\ .\ 83125\\ .\ 83155\\ .\ 83157\\ .\ 83009\\ .\ 83060\\ .\ 83060\\ .\ 83060\\ .\ 83060\\ .\ 83060\\ .\ 83060\\ .\ 83060\\ .\ 83060\\ .\ 83060\\ .\ 83060\\ .\ 83060\\ .\ 83060\\ .\ 83060\\ .\ 83060\\ .\ 83060\\ .\ 83060\\ .\ 83060\\ .\ 83060\\ .\ 83060\\ .\ 83060\\ .\ 83060\\ .\ 83060\\ .\ 83060\\ .\ 83060\\ .\ 83060\\ .\ 83060\\ .\ 83060\\ .\ 83060\\ .\ 83060\\ .\ 83060\\ .\ 83060\\ .\ 83060\\ .\ 83060\\ .\ 83060\\ .\ 83060\\ .\ 83060\\ .\ 83060\\ .\ 83060\\ .\ 83060\\ .\ 83060\\ .\ 83060\\ .\ 83060\\ .\ 83060\\ .\ 83060\\ .\ 83060\\ .\ 83060\\ .\ 83060\\ .\ 83060\\ .\ 83060\\ .\ 83060\\ .\ 83060\\ .\ 83060\\ .\ 83060\\ .\ 83060\\ .\ 83060\\ .\ 83060\\ .\ 83060\\ .\ 83060\\ .\ 83060\\ .\ 83060\\ .\ 83060\\ .\ 83060\\ .\ 83060\\ .\ 83060\\ .\ 83060\\ .\ 83060\\ .\ 83060\\ .\ 83060\\ .\ 83060\\ .\ 83060\\ .\ 83060\\ .\ 83060\\ .\ 83060\\ .\ 83060\\ .\ 83060\\ .\ 83060\\ .\ 83060\\ .\ 83060\\ .\ 83060\\ .\ 83060\\ .\ 83060\\ .\ 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83060\\ .\ 83060\\ .\ 83060\\ .\ 83060\\ .\ 83060\\ .\ 83060\\ .\ 83060\\ .\ 83060\\ .\ 83060\\ .\ 83060\\ .\ 83060\\ .\ 83060\\ .\ 83060\\ .\ 83060\\ .\ 83060\\ .\ 83060\\ .\ 83060\\ .\ 83060\\ .\ 83060\\ .\ 83060\\ .\ 83060\\ .\ 83060$ | $\begin{array}{c} -0.\ 00016\\\ 00035\\\ 00035\\\ 00022\\\ 00049\\\ 00049\\\ 00041\\\ 00032\\ +.\ 000032\\ +.\ 00014\\ +.\ 00013\\ +.\ 00014\\ +.\ 00014\\ +.\ 00014\\ +.\ 00014\\ +.\ 00047\\ +.\ 00047\\ +.\ 00043\\ \end{array}$ | $\begin{array}{c} 0.\ 83151\\ 83167\\ 83156\\ 83093\\ 83096\\ 83096\\ 83089\\ 83114\\ 83105\\ 83004\\ 83074\\ 83074\\ 83114\\ 83967\\ 82987\\ 82987\\ 82987\\ 83099\\ 82986\\ \end{array}$ |
|                                                                                                                                                                                         |                                                                                                                                                                                                                                           |                                                                                                                                                                                              |                                                                                                                                                                                 |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                |                                                                                                                                  | Extrapo                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               | lated value $\sigma_{}$                                                                                                                                                                                                             | $0.83178 \pm 0.00042$                                                                                                                                                                      |
|                                                                                                                                                                                         | 1                                                                                                                                                                                                                                         |                                                                                                                                                                                              |                                                                                                                                                                                 | 1.00 atm                                                                                                                                                                                                        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                                                                                                                                                                                                                                      |                                                                                                                                                                                                                                     |                                                                                                                                                                                            |
| $\begin{array}{c} 9.\ 7661\\ 19.\ 1194\\ 19.\ 4948\\ 19.\ 6730\\ 26.\ 8229\\ 27.\ 3293\\ 28.\ 7456\\ 29.\ 5021\\ 38.\ 6285\\ 49.\ 6069 \end{array}$                                     | $\begin{array}{c} 76.8902\\ 30.6709\\ 29.6885\\ 31.9056\\ 40.7983\\ 21.1385\\ 33.6643\\ 23.1136\\ 21.0078\\ 29.4923\\ \end{array}$                                                                                                        | $\begin{array}{c} 0.864573 \\ .438435 \\ .439721 \\ .440429 \\ .279254 \\ .280370 \\ .278591 \\ .279038 \\ .220050 \\ .154452 \end{array}$                                                   | $\begin{array}{c} 288.1\\ 72.7\\ 69.7\\ 68.2\\ 37.6\\ 35.7\\ 32.2\\ 31.0\\ 18.3\\ 11.0 \end{array}$                                                                             | $\begin{array}{c} 10.\ 0045\\ 10.\ 0863\\ 10.\ 3133\\ 10.\ 4224\\ 9.\ 0375\\ 9.\ 2462\\ 9.\ 6719\\ 9.\ 9955\\ 10.\ 2730\\ 9.\ 2763 \end{array}$                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                | $\begin{array}{c} 0.\ 2132\\ .\ 0640\\ .\ 0637\\ .\ 0594\\ .\ 0398\\ .\ 0392\\ .\ 0339\\ .\ 0334\\ .\ 0256\\ .\ 0187\end{array}$ | $\begin{array}{c} 0.82636\\ .82585\\ .82608\\ .82663\\ .82518\\ .82510\\ .82510\\ .82546\\ .82537\\ .82537\\ .82430 \end{array}$                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      | $\begin{array}{c} -0.\ 00016\\\ 00031\\\ 00026\\\ 00057\\ +.\ 00039\\ +.\ 00027\\\ 00017\\\ 00002\\\ 00040\\ +.\ 00030\\ \end{array}$                                                                                               | $\begin{array}{c} 0.82620\\ .82554\\ .82582\\ .82606\\ .82557\\ .82547\\ .82493\\ .82544\\ .82497\\ .82497\\ .82460 \end{array}$                                                           |
|                                                                                                                                                                                         |                                                                                                                                                                                                                                           |                                                                                                                                                                                              |                                                                                                                                                                                 |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                |                                                                                                                                  | Extrapo                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               | lated value<br>$\sigma$                                                                                                                                                                                                             | $0.82657 \pm 0.00029$                                                                                                                                                                      |
|                                                                                                                                                                                         | 1                                                                                                                                                                                                                                         |                                                                                                                                                                                              |                                                                                                                                                                                 | $0.50 \mathrm{~atm}$                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     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                                                                                                                                                                                                                                      | 1                                                                                                                                                                                                                                   |                                                                                                                                                                                            |
| $\begin{array}{c} 16.\ 0773\\ 20.\ 7110\\ 20.\ 8485\\ 26.\ 7300\\ 27.\ 0941\\ 38.\ 8621\\ 39.\ 4649\\ 51.\ 4968 \end{array}$                                                            | $\begin{array}{c} 55.\ 3158\\ 39.\ 0001\\ 27.\ 4840\\ 36.\ 5463\\ 19.\ 9896\\ 26.\ 1406\\ 24.\ 1511\\ 27.\ 4060 \end{array}$                                                                                                              | $\begin{array}{c} 0.\ 524271\\ .\ 410999\\ .\ 408322\\ .\ 279879\\ .\ 321382\\ .\ 218921\\ .\ 219418\\ .\ 142761\end{array}$                                                                 | $\begin{array}{c} 226.5\\ 129.2\\ 128.3\\ 77.6\\ 73.8\\ 36.3\\ 35.3\\ 21.2 \end{array}$                                                                                         | $\begin{array}{c} 10.\ 0779\\ 10.\ 2405\\ 10.\ 2415\\ 9.\ 0390\\ 10.\ 5239\\ 10.\ 3228\\ 10.\ 5001\\ 8.\ 9446 \end{array}$                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     | $\begin{array}{c} 0.\ 1857\\ .\ 1163\\ .\ 1155\\ .\ 0776\\ .\ 0778\\ .\ 0389\\ .\ 0378\\ .\ 0233 \end{array}$                    | $\begin{array}{c} 0.82124\\ .82189\\ .82195\\ .82061\\ .82165\\ .82165\\ .82173\\ .81978\\ \end{array}$                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               | $\begin{array}{c} -0.\ 00019 \\\ 00037 \\\ 00030 \\ +.\ 00030 \\\ 00059 \\\ 00047 \\\ 00054 \\ +.\ 00028 \end{array}$                                                                                                               | $\begin{array}{c} 0. \ 82105 \\ . \ 82152 \\ . \ 82162 \\ . \ 82091 \\ . \ 82106 \\ . \ 82060 \\ . \ 82119 \\ . \ 82006 \end{array}$                                                       |
|                                                                                                                                                                                         |                                                                                                                                                                                                                                           |                                                                                                                                                                                              |                                                                                                                                                                                 |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                |                                                                                                                                  | Extrapo                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               | plated value                                                                                                                                                                                                                        | $0.82198 \pm 0.00029$                                                                                                                                                                      |

| Reciprocal of rate, $F^{-1}$                                                                                                                         | Mass of sample, $m$                                                                                                                                  | Power, W                                                                                                                          | Pressure drop, $\Delta p$                                                                           | $\begin{array}{c} \text{Temperature} \\ \text{rise, } \Delta T \end{array}$                                                                    | Blank correction, $\delta T$                                                                                                        | Heat capacity, $C$                                                                                                                        | Correction for $T_m$ and $p_m$ , $\delta C$                                                                                      | Heat capacity,<br>$C_p$ (observed)                                                                                                       |
|------------------------------------------------------------------------------------------------------------------------------------------------------|------------------------------------------------------------------------------------------------------------------------------------------------------|-----------------------------------------------------------------------------------------------------------------------------------|-----------------------------------------------------------------------------------------------------|------------------------------------------------------------------------------------------------------------------------------------------------|-------------------------------------------------------------------------------------------------------------------------------------|-------------------------------------------------------------------------------------------------------------------------------------------|----------------------------------------------------------------------------------------------------------------------------------|------------------------------------------------------------------------------------------------------------------------------------------|
|                                                                                                                                                      |                                                                                                                                                      |                                                                                                                                   | 50.00                                                                                               | $^{\circ}$ C=323.16° K; 1                                                                                                                      | .50 atm                                                                                                                             | 1                                                                                                                                         |                                                                                                                                  |                                                                                                                                          |
| $\begin{array}{c} sec \ g^{-1} \\ 9, 9533 \\ 20, 5446 \\ 30, 0909 \\ 41, 6754 \end{array}$                                                           | $\begin{array}{c} g \\ 62.1153 \\ 32.9410 \\ 25.6955 \\ 22.0562 \end{array}$                                                                         | Watt<br>0. 865713<br>. 440265<br>. 279579<br>. 198506                                                                             | $\begin{array}{ c c c c c c c c c c c c c c c c c c c$                                              | $^{\circ} K$<br>9, 7182<br>10, 2884<br>9, 5905<br>9, 4465                                                                                      | $^{\circ} K$<br>0.1035<br>.0260<br>.0124<br>.0067                                                                                   | $jg^{-1} deg^{-1}$<br>0.87731<br>.87694<br>.87607<br>.87513                                                                               | $\begin{array}{c} jg^{-1} \ deg^{-1} \\ -0.\ 00012 \\\ 00024 \\ +.\ 00010 \\ +.\ 00018 \end{array}$                              | $jg^{-1} deg^{-1} \\ 0.87719 \\ .87670 \\ .87617 \\ .87531$                                                                              |
|                                                                                                                                                      |                                                                                                                                                      |                                                                                                                                   |                                                                                                     |                                                                                                                                                |                                                                                                                                     | Extrapo                                                                                                                                   | plated value<br>$\sigma$                                                                                                         | $0.87779 \pm 0.00010$                                                                                                                    |
|                                                                                                                                                      |                                                                                                                                                      |                                                                                                                                   |                                                                                                     | 1.00 atm                                                                                                                                       |                                                                                                                                     |                                                                                                                                           |                                                                                                                                  |                                                                                                                                          |
| $\begin{array}{c} 10.\ 4374\\ 10.\ 4894\\ 21.\ 0786\\ 21.\ 0995\\ 21.\ 4479\\ 29.\ 2761\\ 29.\ 4729\\ 36.\ 3511\\ 37.\ 0996\\ 38.\ 3836 \end{array}$ | $\begin{array}{c} 88.\ 9567\\ 73.\ 2889\\ 40.\ 0728\\ 25.\ 2669\\ 37.\ 7110\\ 21.\ 0018\\ 22.\ 2099\\ 25.\ 2598\\ 28.\ 1755\\ 27.\ 9002 \end{array}$ | $\begin{array}{c} 0.866111\\ .866896\\ .447243\\ .445427\\ .406496\\ .280525\\ .280078\\ .226390\\ .234775\\ .219624 \end{array}$ | $\begin{array}{c} 281.8\\ 285.0\\ 69.2\\ 69.4\\ 67.0\\ 36.6\\ 36.0\\ 24.0\\ 23.0\\ 21.7\end{array}$ | $\begin{array}{c} 10.\ 1896\\ 10.\ 2484\\ 10.\ 7445\\ 10.\ 7141\\ 9.\ 9321\\ 9.\ 3880\\ 9.\ 4321\\ 9.\ 4134\\ 9.\ 9595\\ 9.\ 6411 \end{array}$ | $\begin{array}{c} 0.\ 1437\\ .\ 1453\\ .\ 0377\\ .\ 0379\\ .\ 0366\\ .\ 0202\\ .\ 0199\\ .\ 0133\\ .\ 0123\\ .\ 0120\\ \end{array}$ | $\begin{array}{c} 0.87484\\ .87488\\ .87434\\ .87434\\ .87410\\ .87459\\ .87293\\ .87303\\ .87300\\ .87300\\ .87347\\ .87329 \end{array}$ | $\begin{array}{c} -0.\ 00037\\\ 00026\\\ 00054\\\ 00018\\ +.\ 00018\\ +.\ 00010\\ +.\ 00001\\ +.\ 000016\\ +.\ 00001\end{array}$ | $\begin{array}{c} 0.87447\\ .87462\\ .87378\\ .87356\\ .87356\\ .87341\\ .87305\\ .87343\\ .87308\\ .87308\\ .87331\\ .87330\end{array}$ |
|                                                                                                                                                      | 1 1                                                                                                                                                  |                                                                                                                                   |                                                                                                     |                                                                                                                                                |                                                                                                                                     | Extrapo                                                                                                                                   | lated value<br>$\sigma_{}$                                                                                                       | $0.87515 \pm 0.00030$                                                                                                                    |
|                                                                                                                                                      |                                                                                                                                                      |                                                                                                                                   |                                                                                                     | 0.50 atm                                                                                                                                       |                                                                                                                                     |                                                                                                                                           |                                                                                                                                  |                                                                                                                                          |
| $\begin{array}{c} 16.\ 9244\\ 22.\ 0871\\ 22.\ 6081\\ 30.\ 2390\\ 44.\ 1108\\ \end{array}$                                                           | $\begin{array}{c} 33.\ 9652\\ 27.\ 3684\\ 34.\ 2599\\ 34.\ 4856\\ 23.\ 2882 \end{array}$                                                             | $\begin{array}{c} 0.\ 523830\\ .\ 402422\\ .\ 440823\\ .\ 279988\\ .\ 216601 \end{array}$                                         | $232. \ 6 \\ 131. \ 4 \\ 125. \ 3 \\ 69. \ 9 \\ 33. \ 7 $                                           | $\begin{array}{c} 10.\ 0336\\ 10.\ 1132\\ 11.\ 3464\\ 9.\ 6780\\ 10.\ 9518 \end{array}$                                                        | $\begin{array}{c} 0.\ 1375 \\ .\ 0846 \\ .\ 0801 \\ .\ 0465 \\ .\ 0230 \end{array}$                                                 | $\begin{array}{c} 0.87164 \\ .87159 \\ .87220 \\ .87064 \\ .87058 \end{array}$                                                            | $\begin{array}{c} -0.\ 00014 \\\ 00023 \\\ 00083 \\\ 00001 \\\ 00060 \end{array}$                                                | $\begin{array}{c} 0.\ 87150\\ .\ 87136\\ .\ 87137\\ .\ 87063\\ .\ 86998 \end{array}$                                                     |
|                                                                                                                                                      | <u>I. F</u>                                                                                                                                          |                                                                                                                                   | 11                                                                                                  |                                                                                                                                                |                                                                                                                                     | Extrapola                                                                                                                                 | ated value $\sigma$                                                                                                              | $0.87251 \pm 0.00012$                                                                                                                    |
|                                                                                                                                                      |                                                                                                                                                      |                                                                                                                                   | 90.00                                                                                               | ° C=363.16° K; 1.                                                                                                                              | 50 atm                                                                                                                              |                                                                                                                                           |                                                                                                                                  |                                                                                                                                          |
| $\begin{array}{c} 10.\ 6379\\ 10.\ 6711\\ 21.\ 8113\\ 22.\ 1309\\ 31.\ 8221\\ 43.\ 3567\end{array}$                                                  | 53. 2143<br>64. 2950<br>31. 5644<br>23. 8029<br>24. 2740<br>22. 2464                                                                                 | $\begin{array}{c} 0.\ 865605\\ .\ 866260\\ .\ 392277\\ .\ 396665\\ .\ 282280\\ .\ 205021 \end{array}$                             | $199.9 \\197.7 \\48.9 \\47.9 \\23.6 \\13.5$                                                         | $\begin{array}{c} 10.\ 0164\\ 10.\ 0538\\ 9.\ 3726\\ 9.\ 6176\\ 9.\ 8573\\ 9.\ 7692 \end{array}$                                               | $\begin{array}{c} 0.\ 0780\\ .\ 0771\\ .\ 0191\\ .\ 0187\\ .\ 0092\\ .\ 0053 \end{array}$                                           | $\begin{array}{c} 0.\ 91\ 221\\ .\ 91\ 245\\ .\ 91\ 102\\ .\ 91\ 099\\ .\ 91\ 043\\ .\ 909\ 41 \end{array}$                               | $\begin{array}{c} -0.\ 00006\\\ 00010\\ +.\ 00028\\ +.\ 00018\\ +.\ 00009\\ +.\ 00012\end{array}$                                | $\begin{array}{c} 0.\ 91215\\ .\ 91235\\ .\ 91130\\ .\ 91117\\ .\ 91052\\ .\ 90953 \end{array}$                                          |
|                                                                                                                                                      |                                                                                                                                                      |                                                                                                                                   |                                                                                                     |                                                                                                                                                |                                                                                                                                     | Extrapo                                                                                                                                   | lated value $\sigma_{}$                                                                                                          | $0.91310 \pm 0.00008$                                                                                                                    |
|                                                                                                                                                      |                                                                                                                                                      |                                                                                                                                   |                                                                                                     | 1.00 atm                                                                                                                                       |                                                                                                                                     |                                                                                                                                           |                                                                                                                                  |                                                                                                                                          |
| $\begin{array}{c} 11.\ 1544\\ 22.\ 3219\\ 22.\ 8647\\ 30.\ 5500\\ 31.\ 6170\\ 38.\ 3123\\ 38.\ 3154\\ 40.\ 0074 \end{array}$                         | $\begin{array}{c} 60.\ 3069\\ 26.\ 4180\\ 23.\ 1588\\ 25.\ 0064\\ 26.\ 8963\\ 25.\ 9995\\ 24.\ 6919\\ 29.\ 5816 \end{array}$                         | $\begin{array}{c} 0.866978\\ .396304\\ .396651\\ .280344\\ .279376\\ .220204\\ .220204\\ .220067\\ .219191 \end{array}$           | $\begin{array}{c} 277.7 \\ 69.8 \\ 66.7 \\ 37.8 \\ 35.5 \\ 24.3 \\ 24.5 \\ 22.4 \end{array}$        | $\begin{array}{c} 10.\ 4979\\ 9.\ 6914\\ 9.\ 9364\\ 9.\ 4027\\ 9.\ 6989\\ 9.\ 2771\\ 9.\ 2728\\ 9.\ 6382 \end{array}$                          | $\begin{array}{c} 0.\ 1222\\ .\ 0307\\ .\ 0294\\ .\ 0166\\ .\ 0156\\ .\ 0107\\ .\ 0108\\ .\ 0099 \end{array}$                       | $\begin{array}{c} 0.\ 91060\\ .\ 90991\\ .\ 91004\\ .\ 90930\\ .\ 90926\\ .\ 90837\\ .\ 90826\\ .\ 90891 \end{array}$                     | $\begin{array}{c} -0.\ 00029\\\ 00022\\\ 00035\\\ 00007\\\ 00020\\ +.\ 00030\\ +.\ 00030\\\ 00017\end{array}$                    | $\begin{array}{c} 0. \ 91031 \\ . \ 90969 \\ . \ 90969 \\ . \ 90923 \\ . \ 90906 \\ . \ 90867 \\ . \ 90856 \\ . \ 90874 \end{array}$     |
|                                                                                                                                                      | ·                                                                                                                                                    |                                                                                                                                   |                                                                                                     |                                                                                                                                                |                                                                                                                                     | Extrapol                                                                                                                                  | lated value                                                                                                                      | $0.91102 \pm 0.00009$                                                                                                                    |
|                                                                                                                                                      |                                                                                                                                                      |                                                                                                                                   |                                                                                                     | $0.50 \mathrm{~atm}$                                                                                                                           |                                                                                                                                     |                                                                                                                                           |                                                                                                                                  |                                                                                                                                          |
| $\begin{array}{c} 17.\ 6983\\ 17.\ 8550\\ 23.\ 6482\\ 31.\ 5103\\ 44.\ 7281\\ 44.\ 8320 \end{array}$                                                 | $\begin{array}{c} 33.\ 4157\\72.\ 7266\\24.\ 4505\\20.\ 4568\\19.\ 6214\\29.\ 8347\end{array}$                                                       | $\begin{array}{c} 0.\ 523971\\ .\ 524275\\ .\ 401379\\ .\ 279808\\ .\ 219747\\ .\ 219444 \end{array}$                             | $\begin{array}{c} 232.3\\ 227.0\\ 125.3\\ 71.4\\ 36.3\\ 36.1 \end{array}$                           | $\begin{array}{c} 10.\ 0869\\ 10.\ 1915\\ 10.\ 3876\\ 9.\ 6812\\ 10.\ 8154\\ 10.\ 8265 \end{array}$                                            | $\begin{array}{c} 0.\ 1171 \\ .\ 1144 \\ .\ 0631 \\ .\ 0360 \\ .\ 0183 \\ .\ 0182 \end{array}$                                      | $\begin{array}{c} 0.\ 90880\\ .\ 90831\\ .\ 90825\\ .\ 90734\\ .\ 90725\\ .\ 90718 \end{array}$                                           | $\begin{array}{c} -0.\ 00006\\\ 00012\\\ 00022\\ +.\ 00011\\\ 00037\\\ 00037\end{array}$                                         | $\begin{array}{c} 0.\ 90874\\ .\ 90819\\ .\ 90803\\ .\ 90745\\ .\ 90688\\ .\ 90681 \end{array}$                                          |
|                                                                                                                                                      | <u> </u>                                                                                                                                             |                                                                                                                                   | ·1                                                                                                  | 1                                                                                                                                              | I                                                                                                                                   | Extrapol                                                                                                                                  | ated value                                                                                                                       | $0.90948 \pm 0.00019$                                                                                                                    |

TABLE 2. Data on carbon dioxide—Continued

TABLE 3. Summary of results

|                                                                                                   | Temperature, °C                                                    |                                                                         |                                                                         |                                                                    |  |  |
|---------------------------------------------------------------------------------------------------|--------------------------------------------------------------------|-------------------------------------------------------------------------|-------------------------------------------------------------------------|--------------------------------------------------------------------|--|--|
|                                                                                                   | -30.00                                                             | 0.00                                                                    | +50.00                                                                  | +90.00                                                             |  |  |
|                                                                                                   | (a) Oxygen                                                         |                                                                         |                                                                         |                                                                    |  |  |
| C <sub>p</sub> /R, 1.00 atm                                                                       | 3. 5223                                                            | 3. 5264                                                                 | 3. 5549                                                                 |                                                                    |  |  |
| $C_p = 1 - C_p^\circ)/R_{$                                                                        | 0.0100                                                             | 0.0079                                                                  | 0.0055                                                                  |                                                                    |  |  |
| $C_p^{\circ}/R$ , observed                                                                        | 3. 5123                                                            | 3. 5185                                                                 | 3. 5494                                                                 |                                                                    |  |  |
| $C_p^{\circ}/R$ , spectroscopic                                                                   | a 3. 5112                                                          | 3. 5207                                                                 | 3. 5499                                                                 |                                                                    |  |  |
| Percentage difference, observed-<br>spectroscopic                                                 | +0.03                                                              | -0.06                                                                   | -0.01                                                                   |                                                                    |  |  |
|                                                                                                   | (b) Carbon dioxide                                                 |                                                                         |                                                                         |                                                                    |  |  |
| C <sub>p</sub> /R, 1.50 atm<br>1.00 atm<br>0.50 atm                                               | $\begin{array}{r} 4.2739 \\ 4.2306 \\ 4.1902 \\ 4.148 \end{array}$ | $\begin{array}{r} 4.\ 4028\\ 4.\ 3752\\ 4.\ 3509\\ 4.\ 324 \end{array}$ | $\begin{array}{r} 4.\ 6463\\ 4.\ 6324\\ 4.\ 6184\\ 4.\ 604 \end{array}$ | $\begin{array}{r} 4.8332 \\ 4.8222 \\ 4.8141 \\ 4.804 \end{array}$ |  |  |
| $C_p^{\circ}/R$ , observed                                                                        | 1.110                                                              | 1.021                                                                   | 1,001                                                                   | 1.001                                                              |  |  |
| $C_p^{\circ}/R$ , spectroscopic:                                                                  |                                                                    |                                                                         | 1.1.1                                                                   |                                                                    |  |  |
| Benedict [24]<br>Wagman [25]                                                                      | 4.148                                                              | 4.325                                                                   | 4.600<br>4.600                                                          | $\begin{array}{c} 4.800 \\ 4.799 \end{array}$                      |  |  |
| Percentage difference, observed-<br>spectroscopic<br>$\Delta(C_p/R)/\Delta p,  \mathrm{atm}^{-1}$ | 0.00                                                               | -0.02<br>.0519                                                          | +0.09.0279                                                              | +0.08<br>.0192                                                     |  |  |

<sup>a</sup> Corrected for presence of 0.2% of nitrogen.

of  $C_p/R$  at 1 atm obtained by those authors were 0.13, 0.04, and 0.08 percent higher than values obtained by interpolation in the present experimental results, at the three temperatures of their experiments:  $26.9^{\circ}$ ,  $58.7^{\circ}$ , and  $94.56^{\circ}$  C.

The results at each temperature were extrapolated linearly to zero pressure to obtain the values of  $(C_p^{\circ}/R)$ , observed) listed in table 3 (b). These values were first compared with the most recently published theoretical ones [8, 23] and found to be 0.2 to 0.3 percent higher. Recalculation of the theoretical values was made by W. S. Benedict and independentally checked by H. W. Woolley [24]. The results are shown in table 2 on the line labeled "Benedict". Two values interpolated in the National Bureau of Standards tables of "Selected values of chemical thermodynamic properties" [25], which were recalculated by Wagman from the older calculations of Kassel [9], are also given.

A consideration of the possible errors of the various measurements involved in these heat-capacity determinations, as well as the precision of the results, and the agreement of the observed and calculated heat capacities of oxygen, leads to the conclusion that the error in the final values of  $C_p/R$  at each pressure should not exceed 0.1 percent. The extrapolated values of  $C_p^{\circ}/R$  should therefore be reliable to 0.15 percent.

#### 5.3. Equation of State of Carbon Dioxide

It is assumed here that in the low-pressure region covered by these experiments the equation of state of carbon dioxide is of the form

 $pV = RT + Bp, \tag{2}$ 

where B is a function of the temperature. The thermodynamic relation

$$\left(\frac{\partial \frac{C_p}{R}}{\partial p}\right)_T = -\frac{T}{R} \left(\frac{\partial^2 V}{\partial T^2}\right)_p = -\frac{T}{R} \left(\frac{\partial^2 B}{\partial T^2}\right)_p \qquad (3)$$

must be satisfied by the second derivative of the second virial coefficient, B. The values of the change in heat capacity with pressure, obtained in this research, are given in the last line of table 3 and plotted as circles in figure 5. Also in figure 5 are shown curves representing the right-hand side of eq 3 obtained from (1) the recent pVT isotherms of Mac-Cormack and Schneider [13]; (2) the Berthelot equation, using the critical constants of Meyers and Van Dusen [26]; and (3) the Lennard-Jones potential function [27, 28]. The dashed curve affords a comparison with other experimental work through the equation

$$\left(\frac{\partial \frac{C_p}{R}}{\partial p}\right)_T = -\mu \left(\frac{\partial \frac{C_p}{R}}{\partial T}\right)_p - \frac{C_p}{R} \left(\frac{\partial \mu}{\partial T}\right)_p, \qquad (4)$$

where the values of the Joule-Thomson coefficient  $\mu$ , and its derivative were obtained by interpolation in the tables of Roebuck, Murrell, and Miller [29].

A simple calculation shows that the quantity given by eq 3 is approximately 1 percent of the heat capacity and also 1 percent of the values of the second virial coefficient, in the region covered by this investigation. Therefore, if second virial coefficients could be determined to the same percentage accuracy as the heat capacities, the values of  $\partial(C_p/R)/\partial p$ calculated from the right-hand side of eq 3 would be about half as accurate (because of two differentiations) as those obtained from direct heat-capacity



FIGURE 5. Change of heat capacity of carbon dioxide with pressure as a function of temperature.

O, This research; —, MacCormack and Schneider [13]; —, Joule-Thomson-Roebuck, Murrell and Miller [18]; -----, Berthelot; -----, Lennard-Jones 6-12 potential function. measurements. However, the limit of error generally to be expected from good pVT measurements, and that given by MacCormack and Schneider for their work [7], is about 0.5 percent of the value of B in this region. As the heat-capacity measurements are thought to be good to 0.1 percent, the values of  $\partial(C_p/R)/\partial p$  obtained in this research are about an order of magnitude more accurate than those calculated from second virial coefficients.

The comparisons made in figure 5 show that the Lennard-Jones function cannot be used successfully to calculate the equation of state of carbon dioxide. An attempt was made to fit new Lennard-Jones constants to the results of this research, but unreasonable values ( $b_0 = 25 \text{ cm}^3 \text{ mole}^{-1}$  and  $\epsilon/k = 550^{\circ} \text{K}$ ) were obtained. The difficulties presented by ellipsoidal molecules such as carbon dioxide have been mentioned by others [28].

The data of state of MacCormack and Schneider are evidently adequate to give good second derivatives of the second virial, as shown by figure 5. Other empirical equations, such as van der Waals' and the Beattie-Bridgeman equation, give curves similar to the Berthelot equation.

The authors are grateful for the valuable help and encouragement freely given by Russell B. Scott. For assisting at various times with the experimental work, we wish to thank William L. Cross, Jr., Dino Zei, and Richard J. Sherman.

# 6. References

- [1] R. B. Scott and Jane W. Mellors, J. Research NBS 34, 243 (1945) RP1640.
- [2] P. F. Wacker, Ruth K. Cheney, and R. B. Scott, J. Research NBS 38, 651 (1947) ŘP1804.
- [3] A. Leduc, Int. crit. tables V, 83 (McGraw-Hill Book Co., Inc., New York, N. Y., 1929) [4] A. Eucken and K. v. Lude, Z. physik. Chem. [B] 5, 413
- (1929)
- [5] G. B. Kistiakowsky and W. W. Rice, J. Chem. Phys. 7, 281 (1939).

- [6] A. Michels and C. Michels, Proc. Roy. Soc. London [A] 153, 201 (1935)
- [7] K. E. MacCormack and W. G. Schneider, J. Chem. Phys. 18, 1269 (1950).
- [8] Serge Gratch, Trans. Am. Soc. Mech. Engrs. 71, 897 (1949).
- [9] L. S. Kassel, J. Am. Chem. Soc. 56, 1838 (1934).
  [10] R. L. Swigert, P. Weber, and R. L. Allen, Ind. Eng. Chem. 38, 185 (1946)
- [11] A. Michels and S. De Groot, Applied Scientific Research AI, 94 and 103 (1948)
- [12] NBS-NACA tables of thermal properties of gases. Table 13.24, Carbon dioxide, specific heat (1949). [13] K. E. MacCormack and W. G. Schneider, J. Chem. Phys.
- 18, 1273 (1950).
- [14] J. R. Partington and W. G. Shilling, The specific heats of [11] gases, p. 204 (Ernest Benn, London, 1924).
  [15] R. B. Scott, J. Research NBS 25, 459 (1940) RP1339.
- H. J. Hoge, J. Research NBS 44, 321 (1950) RP2081. 16
- [17] N. S. Osborne, H. F. Stimson, and D. C. Ginnings, J.
- [11] Research NBS 18, 389 (1937) RP983.
  [18] R. B. Scott, C. H. Meyers, R. D. Rands, Jr., F. G. Brickwedde, and N. Bekkedahl, J. Research NBS 35, 39 (1945) RP1661.
- [19] J. A. Beattie and O. C. Bridgeman, J. Am. Chem. Soc. 50, 3133 (1928)
- [20] H. W. Woolley, J. Research NBS 40, 163 (1948) RP1864.
   [21] NBS-NACA tables of thermal properties of gases. Table 1.10-Molecular oxygen (ideal gas state), specific
- heat, enthalpy, entropy.
  [22] E. L. Quinn and C. L. Jones, Carbon dioxide (Reinhold Pub. Co., Inc., New York, N. Y., 1936).
- [23] NBS-NACA tables of thermal properties of gases. Table 13.10-Carbon dioxide (ideal gas state), specific heat, enthalpy, entropy
- [24] W. S. Benedict and H. W. Woolley, Private communications.
- [25] Selected values of chemical thermodynamic properties, NBS Circular 500 (in press)
- [26] C. H. Meyers and M. S. Van Dusen, BS J. Research 10, 381 (1933) RP538.
- [27] NBS-NACA tables of thermal properties of gases. Tables of corrections of thermodynamic properties for gas imperfection, using the Lennard-Jones 6-12 potential (1950).
- B. Bird, Ellen L. Spotz, and J. O. Hirschfelder, J. [28] R. Chem. Phys. 18, 1395 (1950).
- [29] T. R. Roebuck, T. A. Murrell, and E. E. Miller, J. Am. Chem. Soc. 64, 400 (1942).

WASHINGTON, October 15, 1951.